

# Anisotropic flow measurements by ALICE

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(EMMI/GSI)

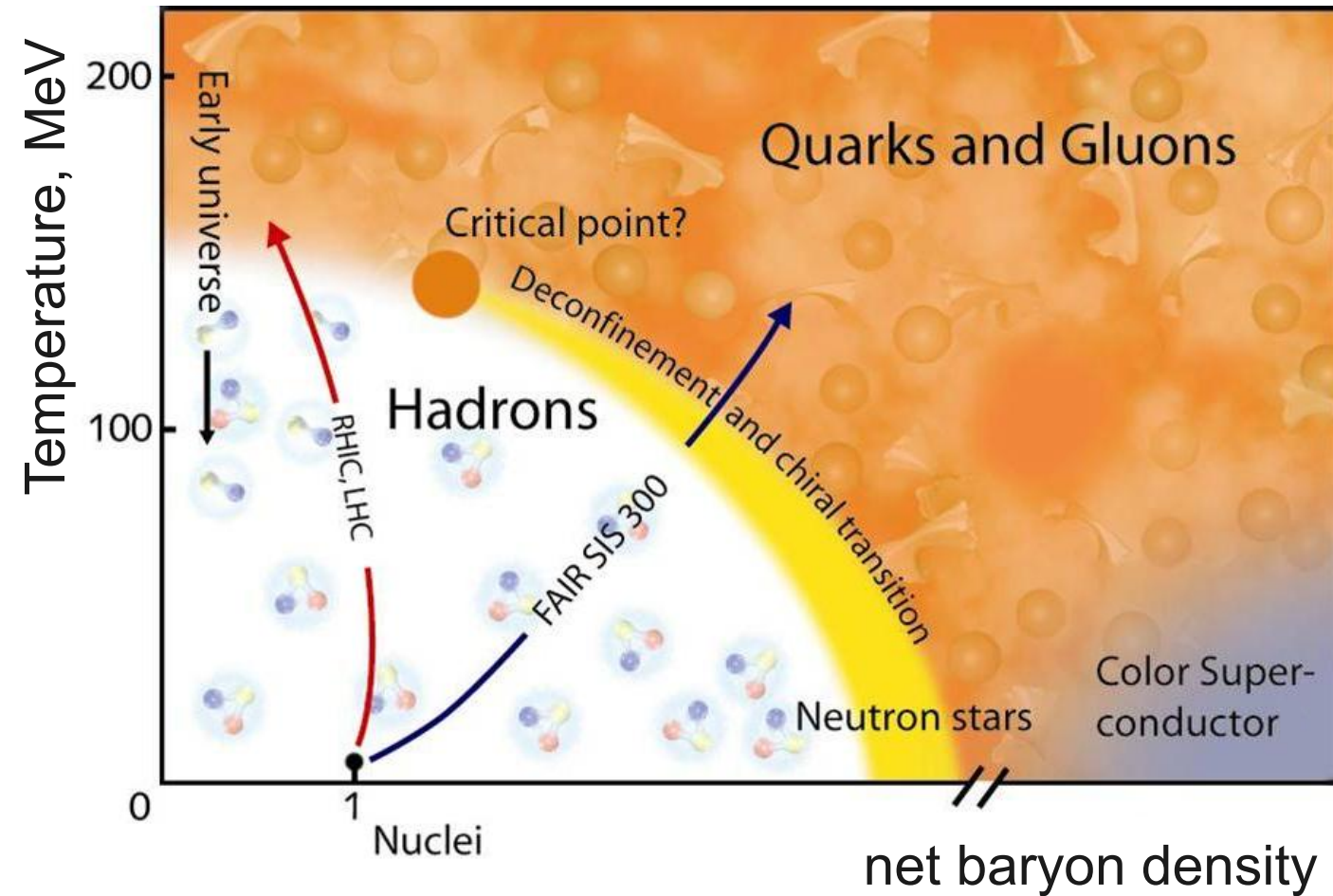
One day workshop on the reaction plane reconstruction and flow

GSI, March 16, 2012

# Outline

- ✓ Why do we measure anisotropic flow?
- ✓ Measurement techniques: correlations and non-flow
- ✓ Elliptic flow at LHC
- ✓ Flow fluctuations and higher harmonics
- ✓ Directed flow
- ✓ Fourier decomposition of the 2-particle azimuthal correlation

# Traveling across the phase diagram by varying the collision energy



AGS/SPS (CERN)

FAIR (GSI/Germany)

NICA (Russia)

$$\sqrt{s_{NN}} \sim 1-10 \text{ GeV}$$

RHIC (BNL/USA)

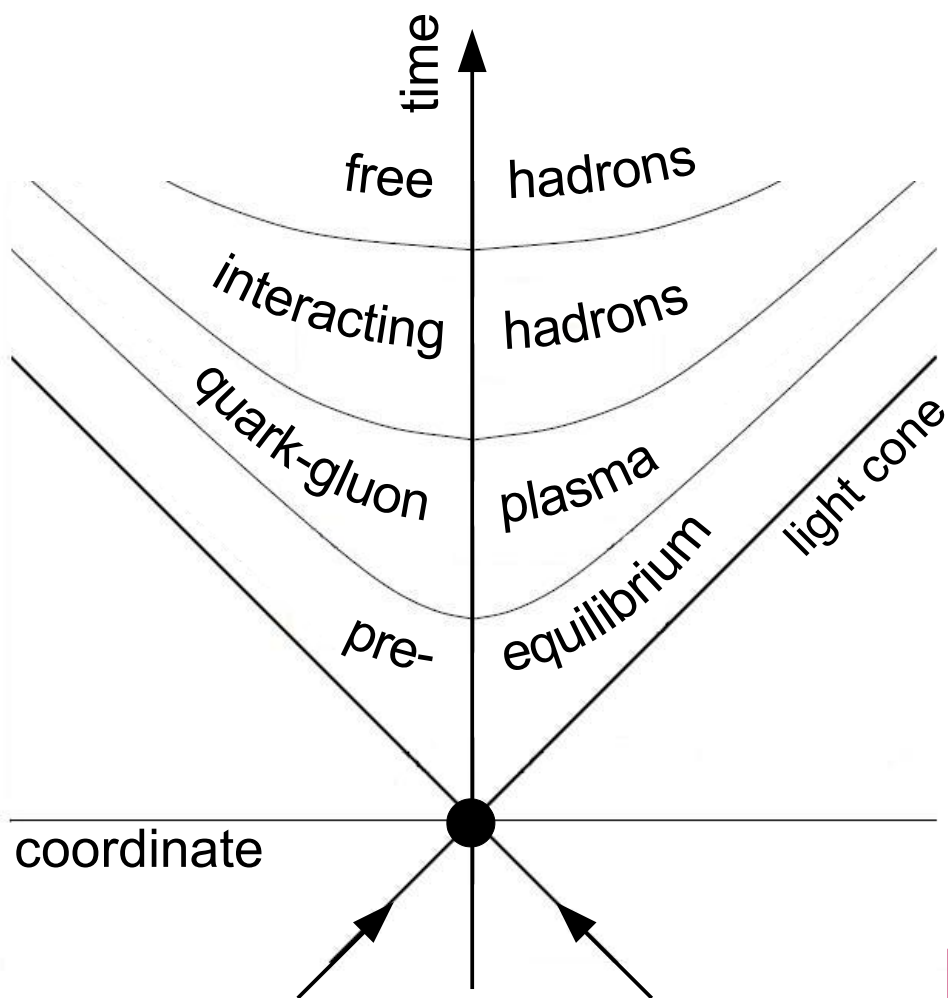
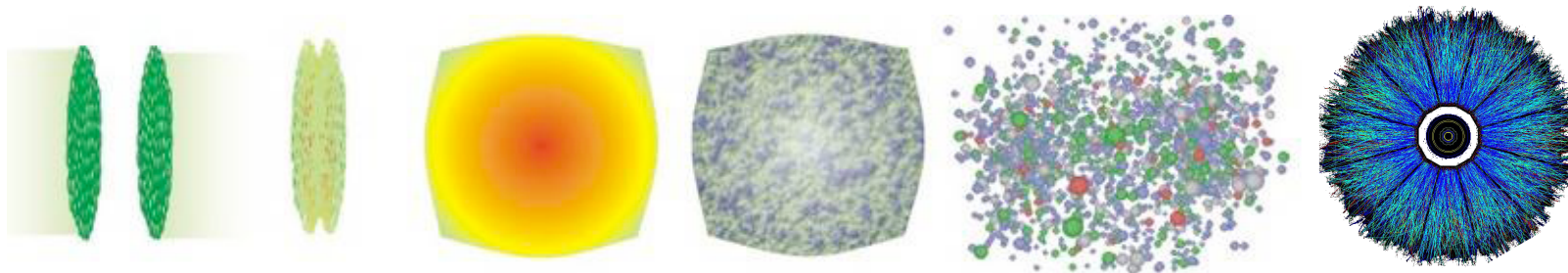
$$\sqrt{s_{NN}} \sim 10-200 \text{ GeV}$$

LHC (CERN)

$$\sqrt{s_{NN}} \sim 2-5 \text{ TeV}$$

By varying the incident collision energy  
(i.e. measurements at different accelerators)  
we can travel across the phase diagram

# Evolution of the system created in HIC



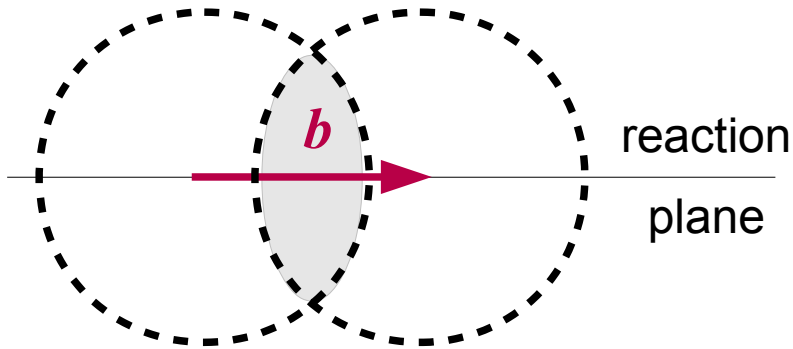
Nuclei just before collision

- Initial pre-equilibrium state
  - hard parton scattering & jet production
  - gluonic fields (Color Glass Condensate)
- Quark-gluon plasma formation
  - thermalization (hydrodynamics)
- QGP expansion and decay
  - phase transition of partons into hadrons
    - Hadronization
    - Rescattering & chemical freeze out
    - Kinetic freeze out (stop interacting)
- Experimentally access only hadronic state

Many observables need to be studied to establish the properties of QGP

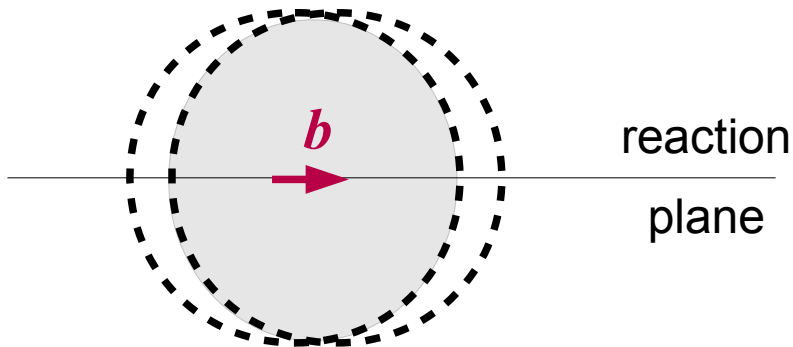
# Colliding nuclei has a finite size

Peripheral collision (large  $b$ )



Overlap region is strongly asymmetric in the transverse plane

Central collision (small  $b$ )



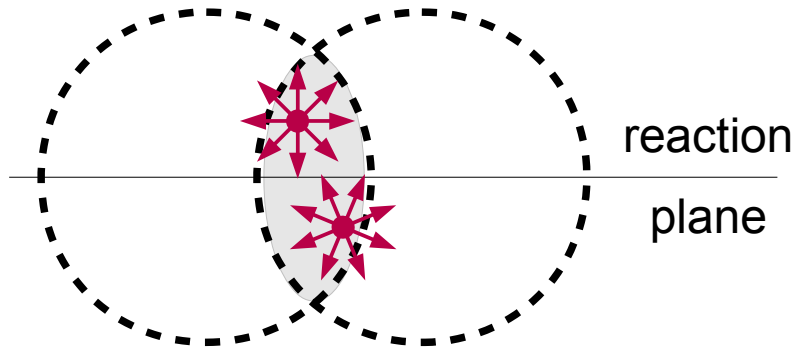
Overlap region is close to be symmetric in the transverse plane

Asymmetry of the overlap region depends on the impact parameter

$b$  - impact parameter

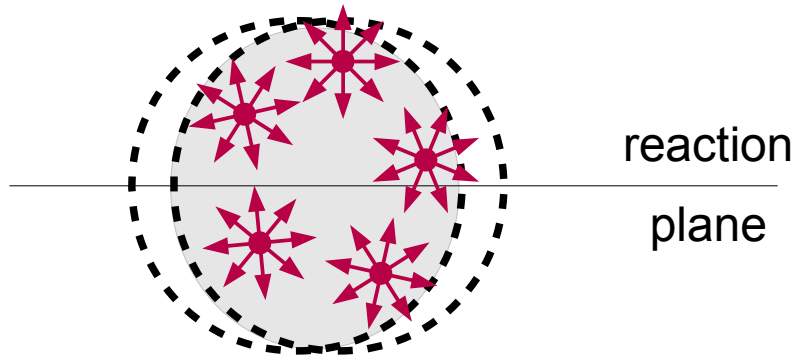
# Nucleon-nucleon collisions in the overlap region

## Peripheral collision



Small number of nucleon-nucleon collisions:  
few particles produced

## Central collision



Large number of NN collisions:  
abundant particle production

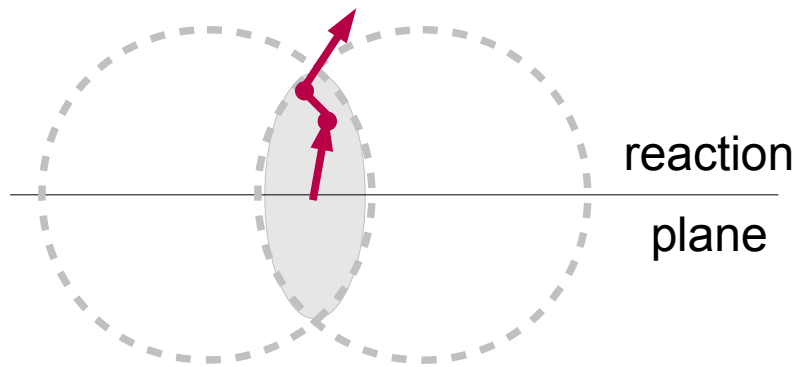
Number of produced particles  
is correlated with the impact parameter



- elementary  
nucleon-nucleon (NN) collision

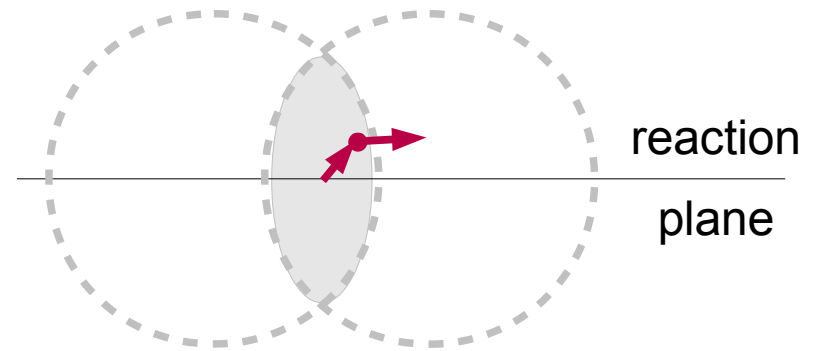
# Produced particles interact with each other

Particle emitted out-of-plane



Multiple interaction with medium

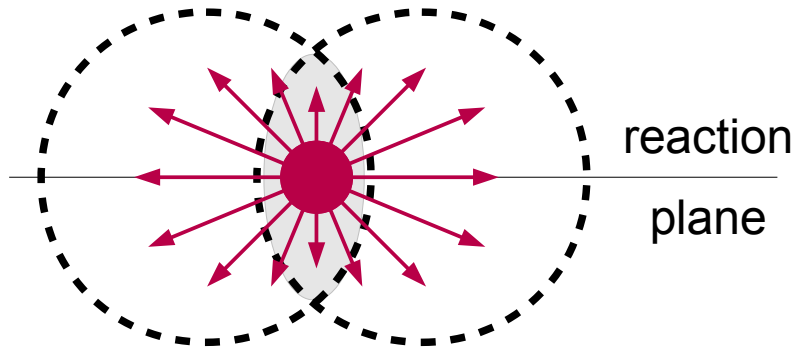
Emitted in-plane



Less interaction - small modification

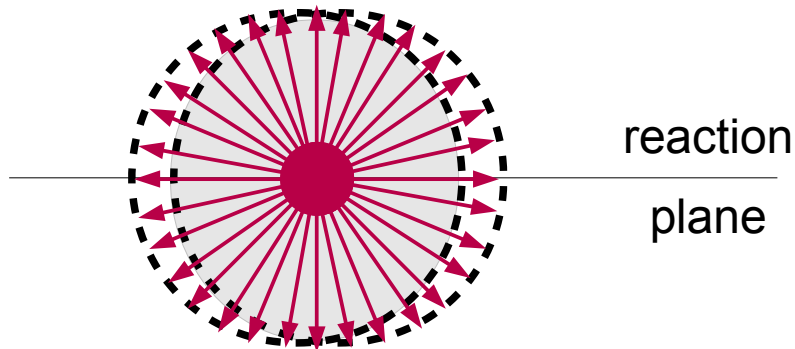
# Particle collectivity

Peripheral collision



Strong coordinate space asymmetry transforms into the azimuthal asymmetry in the momentum space

Central collision



Multiple interaction with medium but small initial spacial asymmetry: small asymmetry in the momentum space

Correlated particle production wrt. the collision plane of symmetry

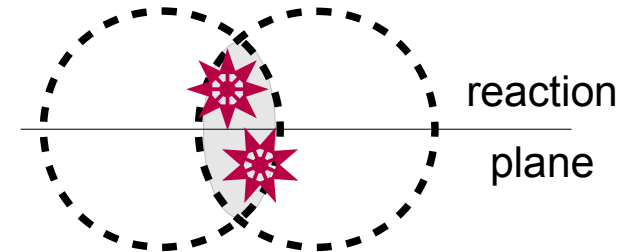


# Quantifying azimuthal asymmetry

Coordinate space asymmetry is  $\sim$  ellipsoidal  
quantified by eccentricity:

$$\epsilon_s = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

$x, y$  - position of each elementary NN interaction

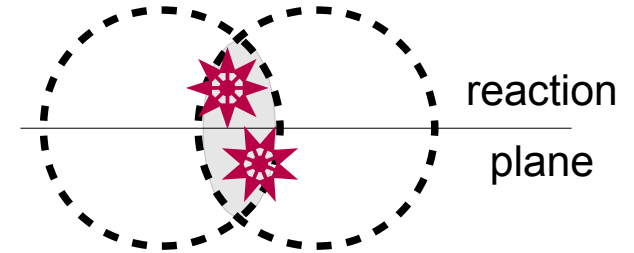


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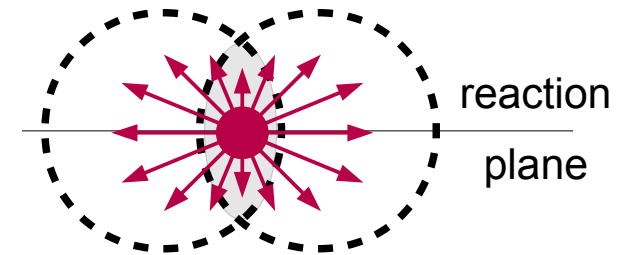
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$x, y$  - position of each elementary NN interaction



Momentum space asymmetry:

$$e_p \sim \frac{\langle p_x^2 - p_y^2 \rangle}{\langle p_y^2 + p_x^2 \rangle} \rightarrow \langle \cos(2 \Delta \phi) \rangle$$

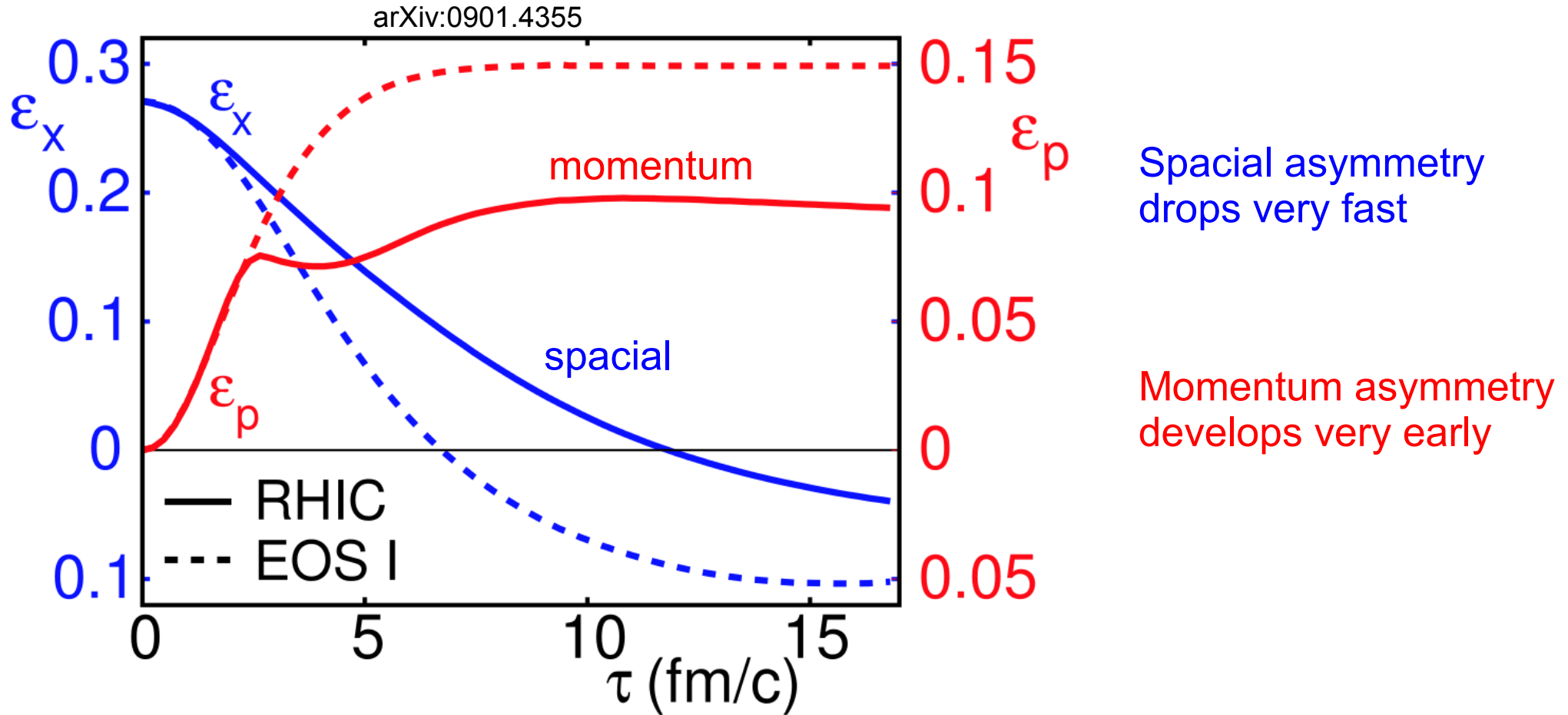


Second Fourier harmonic in momentum space

$p_t$  - particle transverse momentum

$\Delta \phi$  - azimuthal angle relative to the reaction plane

# Time evolution of the spacial and momentum asymmetries



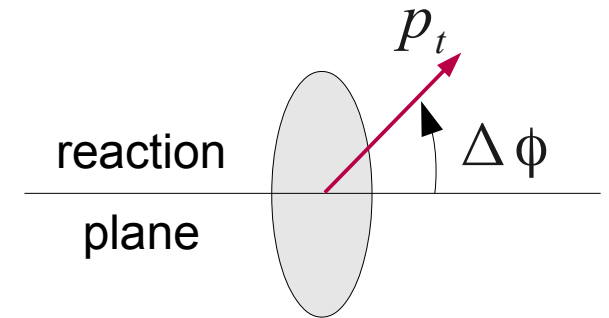
EoS I: massless ideal gas  
 EoS RHIC: matching Lattice QCD

Momentum asymmetry is sensitive to:

- Early times of the system evolution
- Equation of State

# Anisotropic transverse flow: Fourier harmonics

Fourier decomposition of the particle azimuthal distribution wrt. the reaction plane:



$$\frac{dN}{d(\Delta\phi)} \sim 1 + 2 \sum_{n=1} v_n(p_t, \eta) \cos(n \Delta\phi)$$

No “sin” terms because of the collision symmetry

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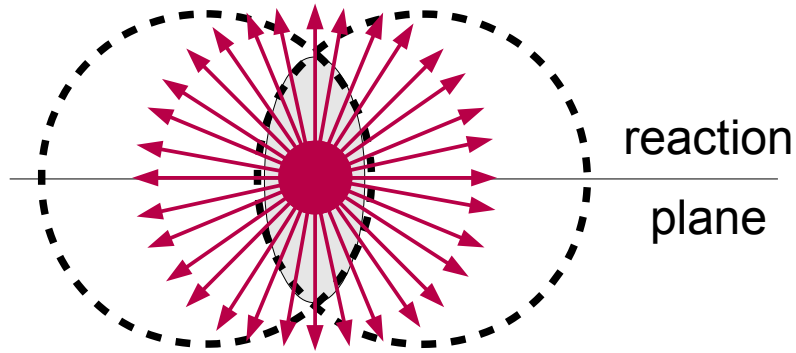
$v_n(p_t, \eta)$  – anisotropic transverse flow coefficients

$v_1$  - directed flow

$v_2$  - elliptic flow

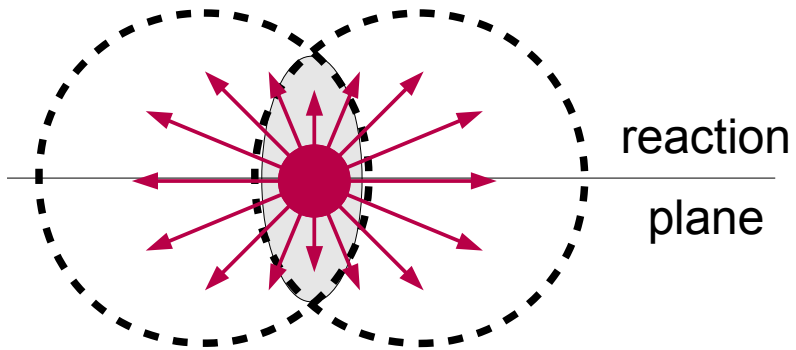
$v_3$  - triangular flow

# Different types of transverse flow



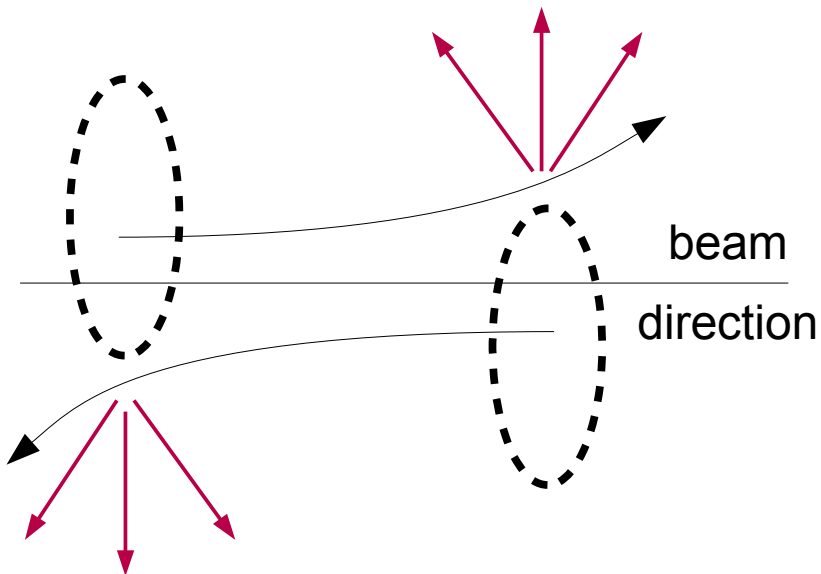
Radial flow (symmetric in azimuth)

Reflects the history of the radial expansion  
Boost particle spectra to higher transverse momenta



Elliptic flow:  $v_2 = \langle \cos 2 \Delta \phi \rangle$

Originate from ellipticity of the overlap region  
Self quenching effect - develops at early time  
(spacial asymmetry decrease with expansion)



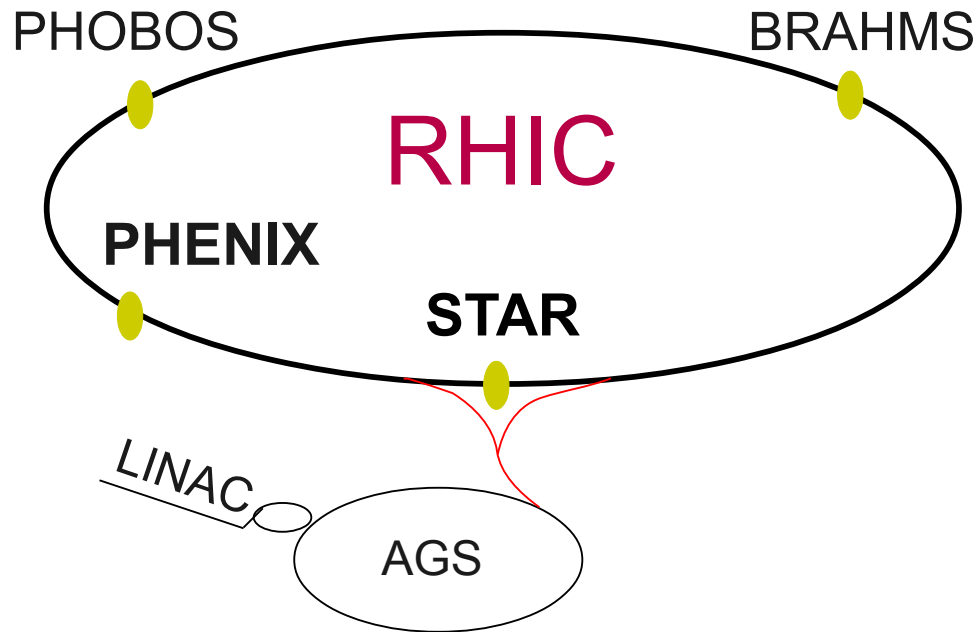
Directed flow:  $v_1 = \langle \cos \Delta \phi \rangle$

Deflection of particles in the beam direction.  
Develops at earliest time.  
At forward (large) rapidity is sensitive to the pre-equilibrium stage

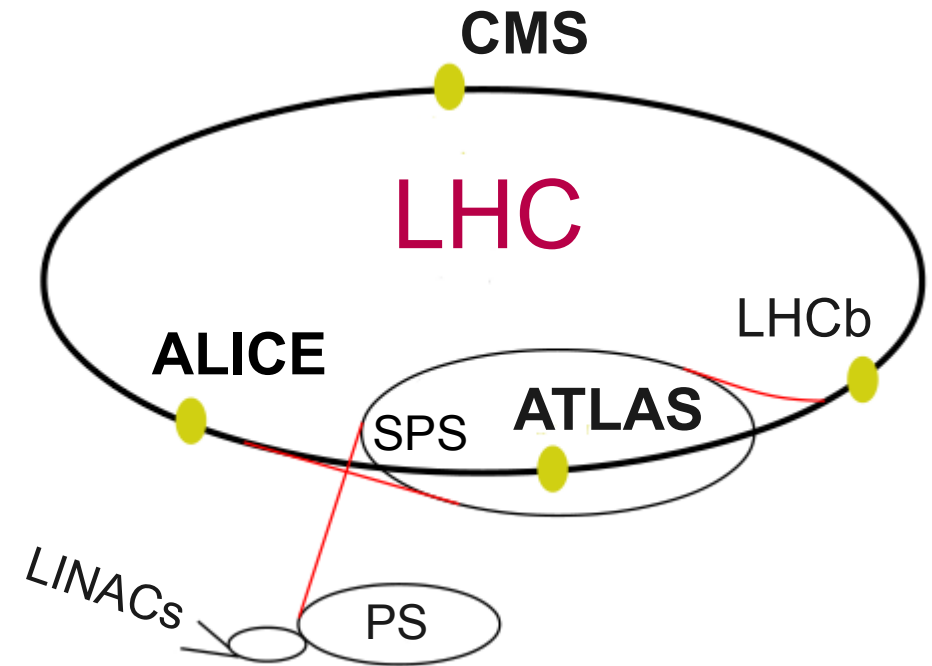
# Experimental measurements of the anisotropic flow

# Modern ultra-relativistic HI colliders

## Relativistic Heavy Ion Collider



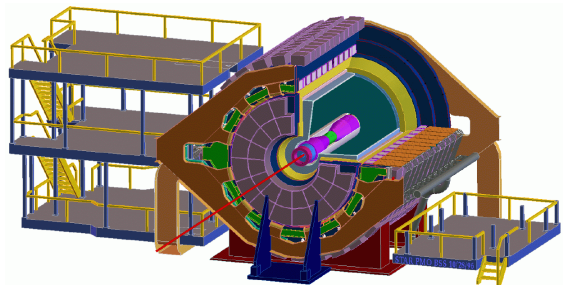
## Large Hadron Collider



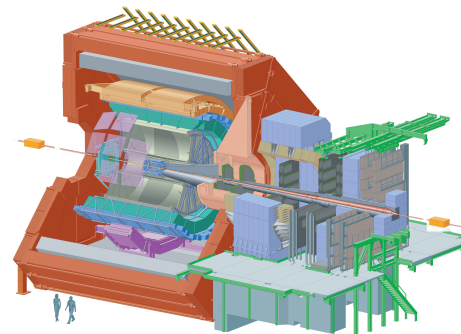
	<b>RHIC</b>	<b>LHC</b>
Location	BNL (USA)	CERN (Europe)
Circumference	3.8 km	27 km
Species	p, d, Cu, Au, U polarized protons	p, Pb
Center of mass energy per nucleon pair	in GeV 7.7-38, 62, 200 500 (pp only)	in TeV 0.9, 2.76, 7 (pp) 2.76 (Pb)

# Current heavy-ion experiments at RHIC and LHC

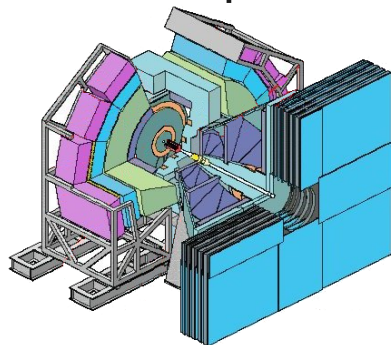
**STAR** (Solenoidal Tracker At RHIC)



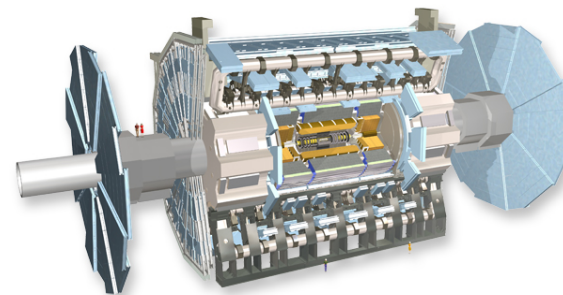
**ALICE** (A Large Ion Collider Experiment)



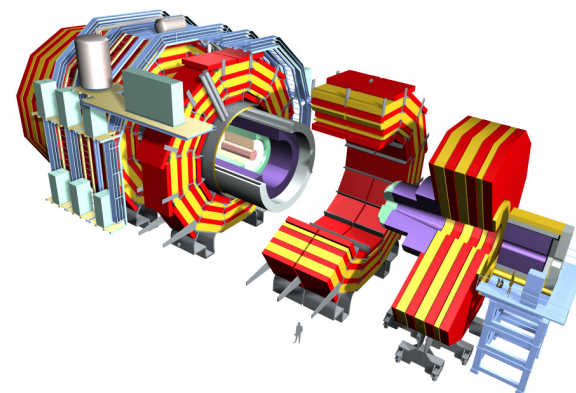
**PHENIX** (Pioneering High Energy Nuclear Ion Experiment)



**ATLAS** (A Toroidal LHC Apparatus)



**CMS** (Compact Muon Solenoid)



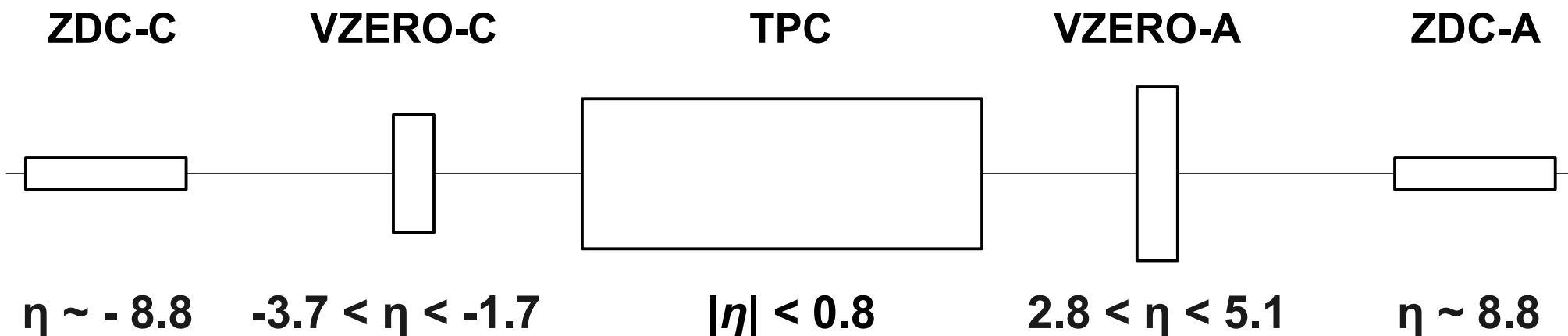
## Main capabilities for heavy-ion studies:

Charge particle tracking and identification:  
full azimuth, large rapidity coverage  
wide  $p_t$  range:  $\sim 100$  MeV/c to  $\sim 100$  GeV/c

Calorimetry and rare probes:  
neutral particles, photons, jets, heavy flavor



# The ALICE subsystems used for the flow measurements



Data from LHC running in November 2010

System	Energy, $\sqrt{s_{NN}}$	Events
Pb-Pb	2.76 TeV	13 M

## TPC:

Time Projection Chamber  
charged tracks at midrapidity

## VZERO:

Forward Scintillator Arrays  
multiplicity counters

## ZDCs:

Zero Degree Calorimeter  
recoil neutrons at beam rapidity

## Charged particle cuts for correlations:

Pseudo-rapidity:  $|\eta| < 0.8$

Transverse momentum  $p_t > 0.15$  GeV/c

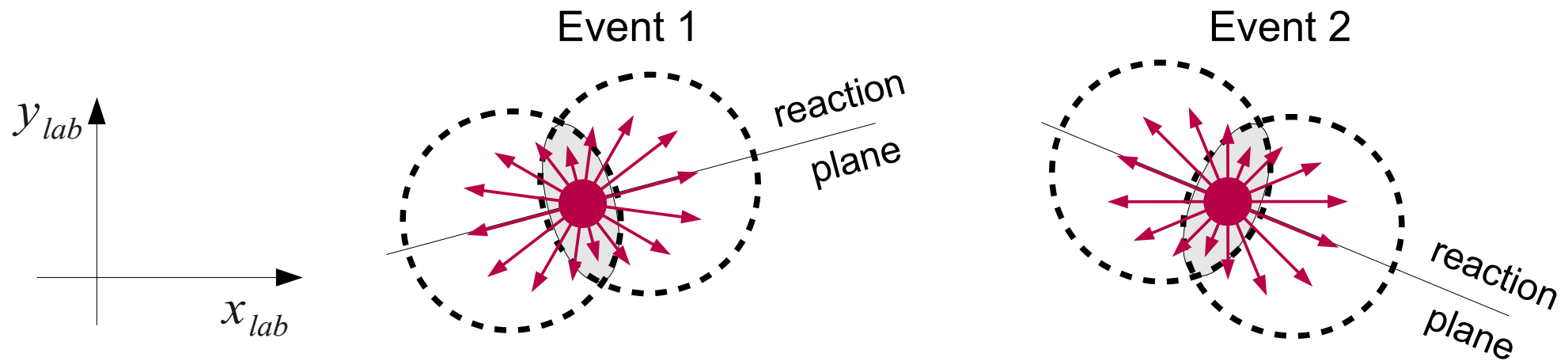
## Reaction plane:

Estimated with TPC, VZERO, and ZDCs

# Anisotropic flow measurement: Using collectivity to study collectivity

Reaction plane is not known experimentally

Orientating wrt. to the laboratory frame changes event-by-event

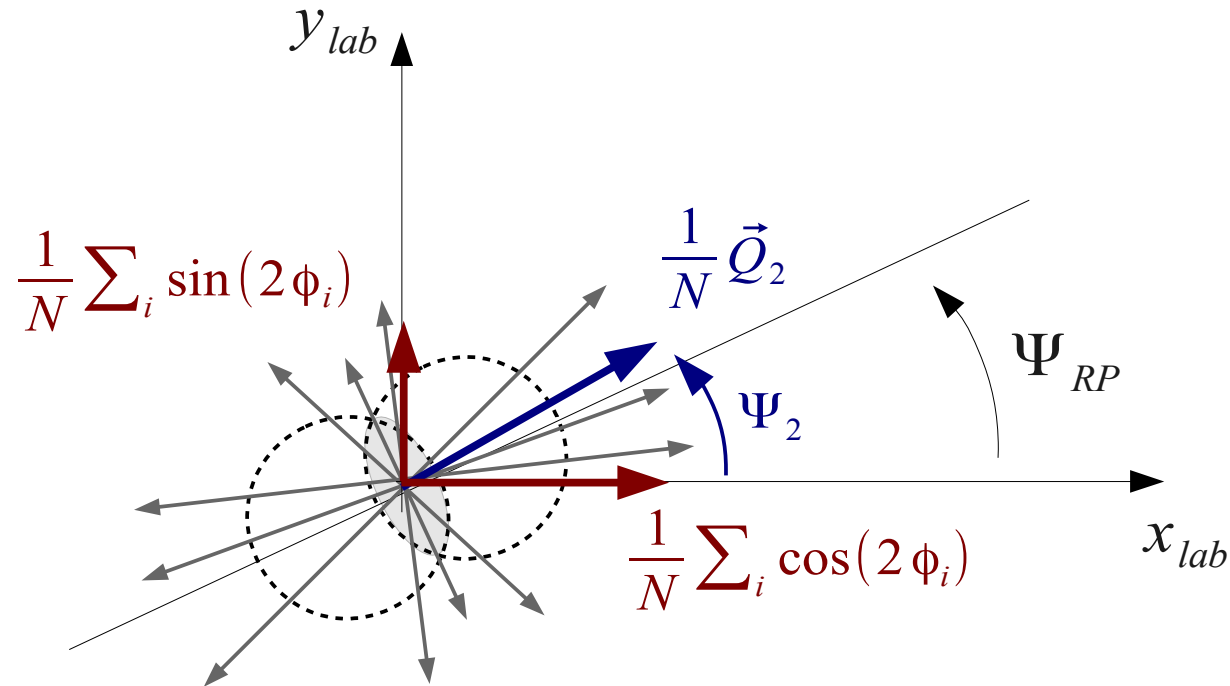


Only measuring particles distribution in the momentum space

If the momentum distribution is azimuthally asymmetric due to flow,  
then this asymmetry should be correlated  
with the impact parameter direction (reaction plane orientation)

Use particle azimuthal distribution in the event  
to estimate the reaction plane angle – event plane vector

# Event plane vector



Vector sum of all particles direction:

$$Q_{n,x} = \sum_i w_i \cos(n\phi_i) \quad Q_{n,y} = \sum_i w_i \sin(n\phi_i)$$

Experimental estimate of the reaction plane:

Event plane vector: 
$$\Psi_{n,EP} = \frac{1}{n} \tan^{-1} \left( \frac{Q_{n,y}}{Q_{n,x}} \right)$$

# Measuring flow with the event plane vector

$$\frac{dN}{d(\phi - \Psi_{RP})} \sim 1 + 2 \sum_{i=1} v_n(p_t, \eta) \cos[n(\phi - \Psi_{RP})]$$

Want to measure:

$$v_n = \langle \cos[n(\phi - \Psi_{RP})] \rangle$$



Measured:

$$v_n^{obs} = \langle \cos[n(\phi - \Psi_{n,EP})] \rangle$$

# Measuring flow with the event plane vector

$$\frac{dN}{d(\phi - \Psi_{RP})} \sim 1 + 2 \sum_{i=1} v_n(p_t, \eta) \cos[n(\phi - \Psi_{RP})]$$

Want to measure:

Measured:

$$v_n = \langle \cos[n(\phi - \Psi_{RP})] \rangle \longrightarrow v_n^{obs} = \langle \cos[n(\phi - \Psi_{n,EP})] \rangle$$

Event plane vector and the reaction plane are correlated with finite resolution:

$$v_n = \frac{\langle \cos[n(\phi - \Psi_{n,EP})] \rangle}{\langle \cos[n(\Psi_{n,EP} - \Psi_{RP})] \rangle} = \frac{v_n^{obs}}{R_n}$$

Resolution can be measured from subevents:

$$R \sim \sqrt{\langle \cos[n(\Psi_{n,EP}^a - \Psi_{n,EP}^b)] \rangle}$$

# Anisotropic flow measurement and correlations

$$\frac{dN}{d(\phi_i - \Psi_{RP})} \sim 1 + 2 \sum_{n=1} v_n \cos[n(\phi_i - \Psi_{RP})]$$

$$v_n = \langle \cos[n(\phi_i - \Psi_{RP})] \rangle \quad - \text{directly calculable only in theory when the reaction plane orientation is known}$$

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$$v_n = \langle \cos[n(\phi_i - \Psi_{RP})] \rangle \quad \text{- directly calculable only in theory when the reaction plane orientation is known}$$

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Event plane angle - experimental estimate of the reaction plane angle based on the measured azimuthal distribution of particles:

$$\Psi_{RP} \rightarrow \Psi_{EP} \left\{ \sum_{\phi_j} g(\phi_j) \right\}$$

$$v_n^{obs} = \langle \cos[n(\phi_i - \Psi_{EP})] \rangle \sim \left\langle \sum_{\phi_j \neq \phi_i} \cos n(\phi_i - \phi_j) \right\rangle$$

$$c_n\{2\} = \langle \cos n(\phi_i - \phi_j) \rangle \quad \text{- two particle correlations}$$

Measure anisotropic flow with azimuthal correlations

# Non-flow correlations

Non-flow: correlations among the particles unrelated to the reaction plane

In case of two particle correlations:  $\langle \cos[n(\phi_i - \phi_j)] \rangle = \langle v_n^2 \rangle + \delta_{2,n}$

Sources of non-flow correlations:

- Resonance decay
- Jet production
- In general - any cluster production



# Non-flow correlations

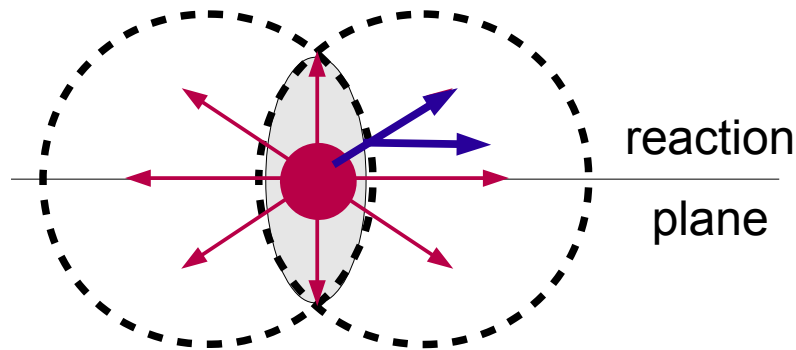
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Sources of non-flow correlations:

- Resonance decay
- Jet production
- In general - any cluster production

Example: 2-particle decay



Probability to be correlated for one particle with another out of  $M$ -particles is  $1/(M-1)$ :

$$\delta_2 \sim \frac{1}{M-1}$$

To measure flow with 2-particle correlations:

$$v_n \gg 1/\sqrt{M}$$

Collective flow:  
correlations between particles through  
the common plane of symmetry

$$M = 200 \rightarrow v_n \gg 0.07$$

For RHIC/LHC:  $v_n \approx 0.04 - 0.07$

# Suppressing non-flow with multi-particle correlations

Two particle correlations:

$$\delta_2 \sim \frac{1}{M}$$

Measurement requirement:

$$v_n \gg \frac{1}{M^{1/2}}$$

$$M = 200 \rightarrow v_n \gg 0.07$$

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Four-particle correlations:

$$\delta_4 \sim \frac{1}{M^3}$$

$$v_n \gg \frac{1}{M^{3/4}}$$

$$M = 200 \rightarrow v_n \gg 0.019$$

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$k$ -particle correlations:

$$\delta_k \sim \frac{1}{M^{k-1}}$$

$$v_n \gg \frac{1}{M^{(k-1)/k}}$$

---

Large  $k$  (  $k \rightarrow \infty$  )

$$v_n \gg \frac{1}{M}$$

$$M = 200 \rightarrow v_n \gg 0.005$$

# Multi-particle cumulants

Cumulants are used to study the genuine  $n$ -particle correlations

$n$ -particle cumulant can be defined as a correlation function which is zero if there are no  $n$ -particle correlations in the system (it is insensitive to other,  $k \neq n$ , correlations)

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## Example:

2-particle correlations

$$\langle \cos[n(\phi_1 - \phi_2)] \rangle = \langle e^{in(\phi_1 - \phi_2)} \rangle \quad \text{Note: imaginary part is zero (no sin terms)}$$

2-particle cumulant:

$$c_n\{2\} = \langle e^{in(\phi_1 - \phi_2)} \rangle - \langle e^{in\phi_1} \rangle \langle e^{in\phi_2} \rangle$$

If there are no correlations in the particle distribution,

but  $\langle e^{in\phi_{1,2}} \rangle \neq 0$  (for example non-uniform detector acceptance)

$$\langle \cos[n(\phi_1 - \phi_2)] \rangle \neq 0 \quad c_n\{2\} = 0$$

# Multi-particle cumulants and relation to flow

2-particle cumulant:

$$c_n\{2\} = \langle e^{in(\phi_1 - \phi_2)} \rangle = v_n^2 + \delta_{2,n} \quad \delta_2 \sim \frac{1}{M}$$

4-particle cumulant:

$$c_n\{4\} = \langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle - 2 \langle e^{in(\phi_1 - \phi_2)} \rangle^2$$

$$c_n\{4\} = \left( v_n^4 + \delta_{4,n} + 4v_n^2 \delta_{2,n} + 2\delta_{2,n}^2 \right) - 2 \left( v_n^2 + \delta_{2,n} \right)^2$$

$$c_n\{4\} = \langle -v_n^4 + \delta_{4,n} \rangle \quad \delta_4 \sim \frac{1}{M^3}$$

No contribution from 2-particle non-flow to the 4-particle cumulant

# Multi-particle cumulants and relation to flow

2-particle cumulant:

$$c_n\{2\} = \langle e^{in(\phi_1 - \phi_2)} \rangle = \langle v_n^2 + \delta_{2,n} \rangle$$

4-particle cumulant:

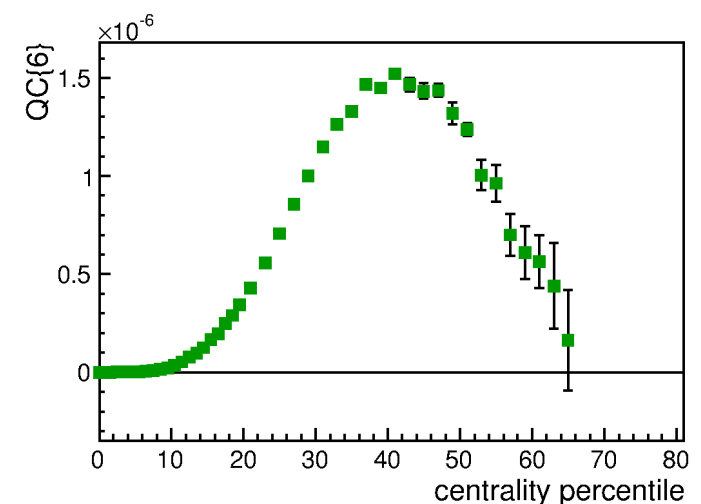
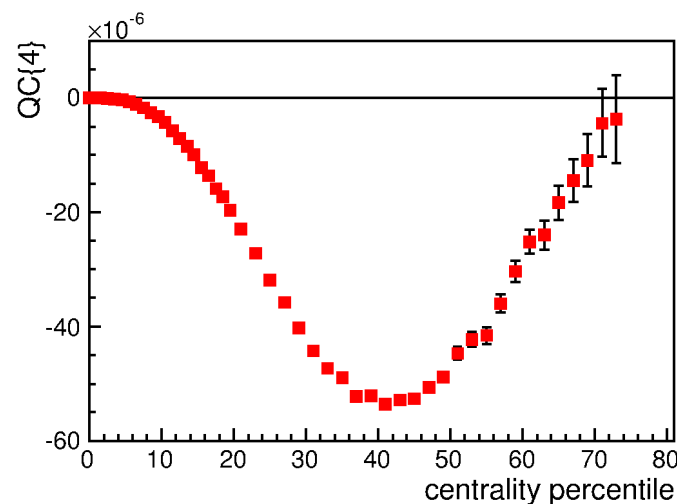
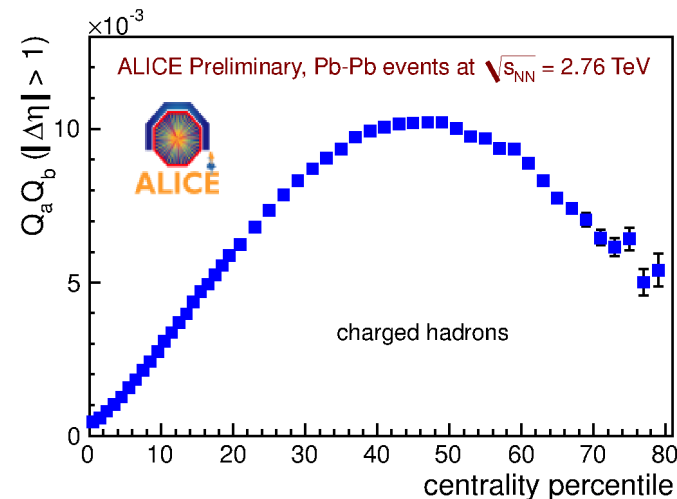
$$c_n\{4\} = \langle -v_n^4 + \delta_{4,n} \rangle$$

Connection of cumulants to the anisotropic flow

$$v_n\{2\}^2 = c_n\{2\}$$

$$v_n\{4\}^2 = -c_n\{4\}$$

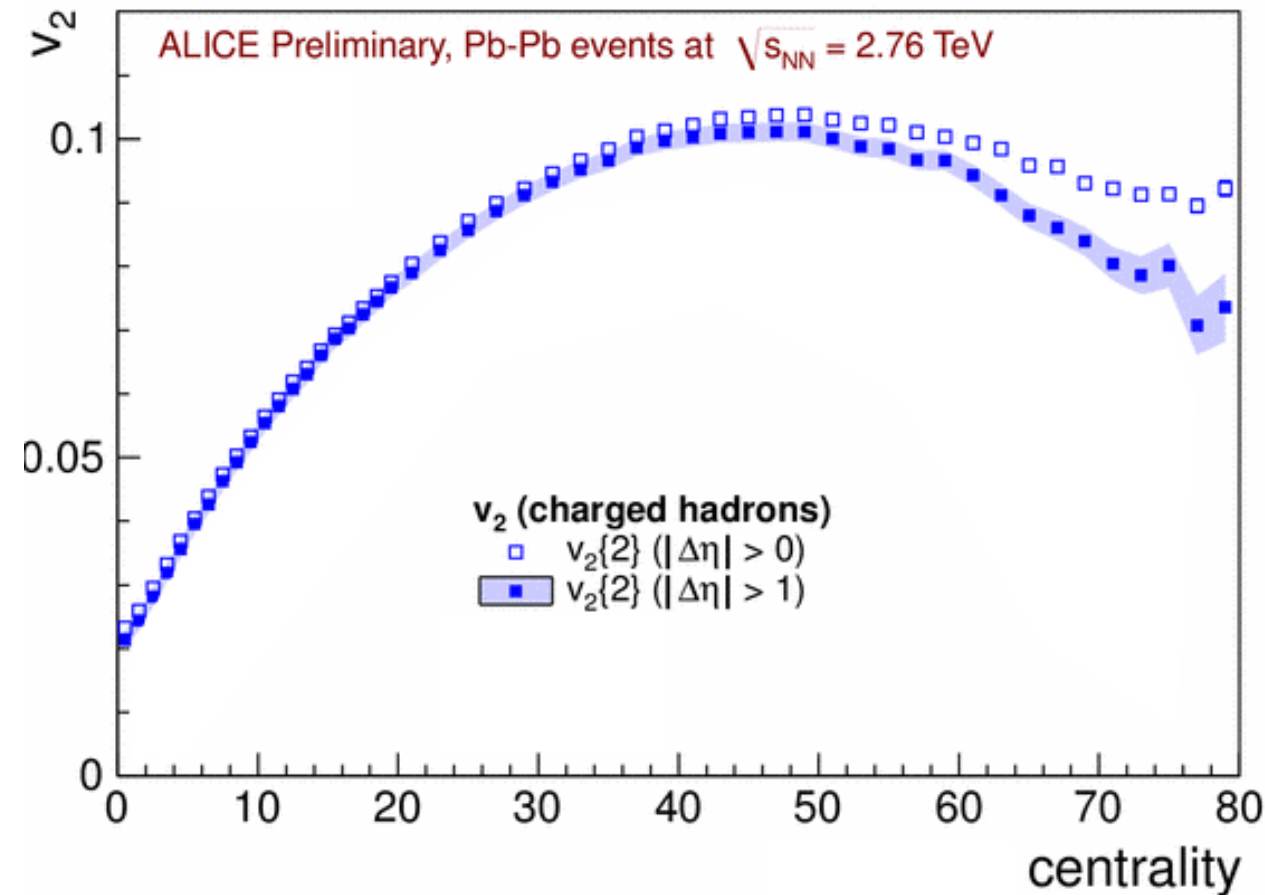
$$v_n\{6\}^6 = \frac{1}{4} c_n\{6\}$$



Characteristic pattern of the cumulants changing sign

# Estimating flow with multi-particle cumulants

## elliptic flow vs. centrality



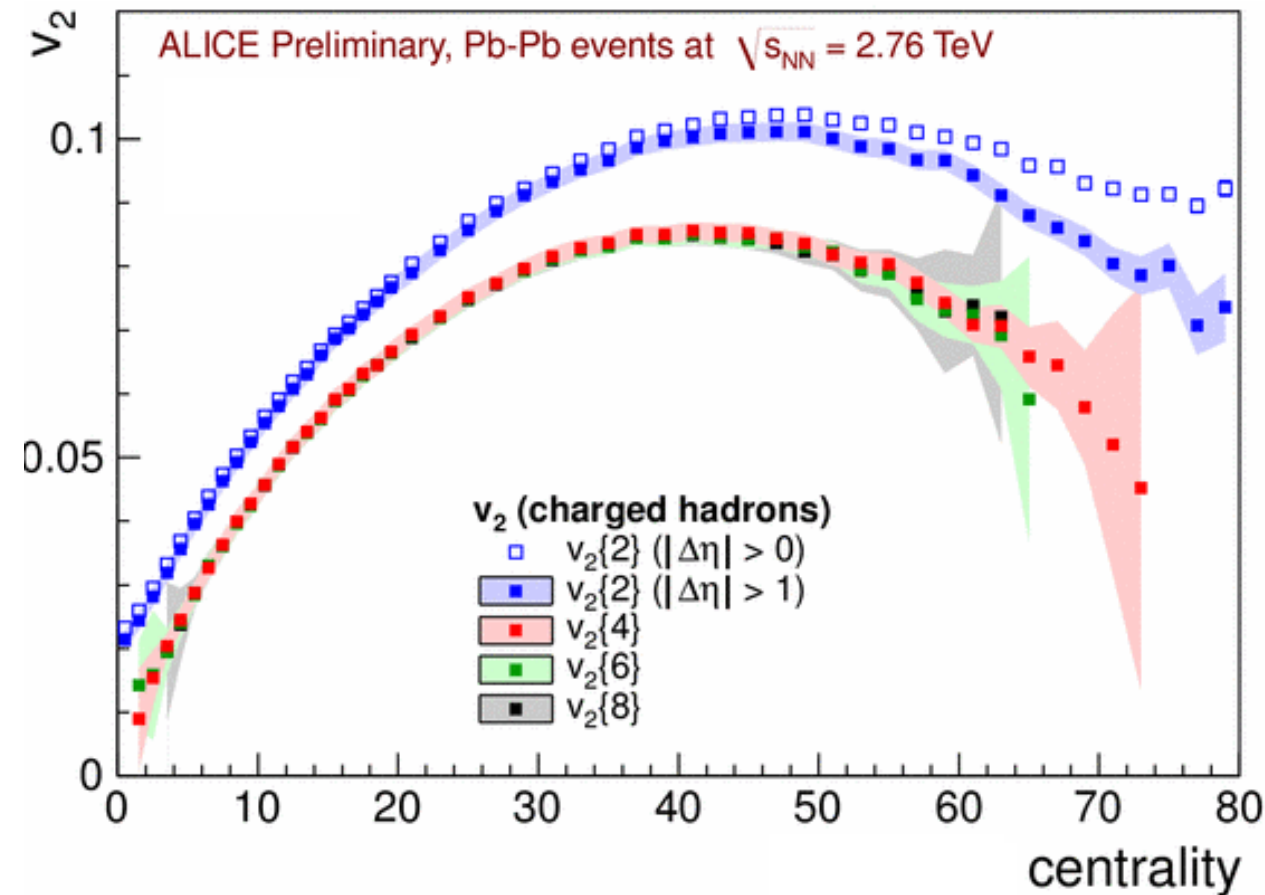
Rapidity separation between correlated particles suppress short-range non-flow:

$$v_2\{2\} > v_2\{2, |\Delta\eta|\}$$

Large non-flow in peripheral collisions

# Estimating flow with multi-particle cumulants

elliptic flow vs. centrality



Rapidity separation between correlated particles suppress short-range non-flow:

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Large non-flow in peripheral collisions

Note:

$v_2\{2\}$  and  $v_2\{4\}$  differ not only because of non-flow, but also due to flow fluctuations (discussed later)

Multi-particle cumulants remove residual non-flow:

$$v_2\{4\} \approx v_2\{6\} \approx v_2\{8\}$$

# Overview of methods to measure anisotropic flow

Based on 2-particle correlations:

$$v_n^{obs} = \left\langle \sum_{\phi \neq \phi_i} \cos n(\phi - \phi_i) \right\rangle \rightarrow c_n\{2\} = \langle \cos n(\phi_i - \phi_j) \rangle$$

Event plane method

Scalar Product

$$v_n(p_T, y) = \frac{\sqrt{\langle M_a M_b \rangle}}{\langle M \rangle - 1} \frac{\langle Q_n u_{n,i}^*(p_T, y) \rangle}{\sqrt{\langle Q_n^a Q_n^{b*} \rangle}}$$



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Based on multi-particle cumulant:

Cumulants from generating function (GF):

GF: function which expanded in series gives multi-particle correlations as expansion coefficients

$$G_n(z) = \prod_{j=1}^M \left( 1 + \frac{z^* e^{in\phi_j} + z e^{-in\phi_j}}{M} \right)$$

Q-cumulants (or direct cumulants)

$$\langle 4 \rangle = \frac{|Q_n|^4 + |Q_{2n}|^2 - 2 \cdot \Re [Q_{2n} Q_n^* Q_n^*]}{M(M-1)(M-2)(M-3)}$$

$$\langle 2 \rangle = \frac{|Q_n|^2 - M}{M(M-1)} - 2 \frac{2(M-2) \cdot |Q_n|^2 - M(M-3)}{M(M-1)(M-2)(M-3)}$$

$$v_n\{2\}^2 = c_n\{2\} \quad v_n\{4\}^4 = -c_n\{4\} \quad v_n\{6\}^6 = \frac{1}{4} c_n\{6\} \quad v_n\{8\}^8 = -\frac{1}{33} c_n\{8\}$$

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Scalar Product

$$v_n(p_T, y) = \frac{\sqrt{\langle M_a M_b \rangle}}{\langle M \rangle - 1} \frac{\langle Q_n u_{n,i}^*(p_T, y) \rangle}{\sqrt{\langle Q_n^a Q_n^{b*} \rangle}}$$

Based on multi-particle cumulant:

Cumulants from generating function (GF)  
Q-cumulants (or direct cumulants)

GF: function which expanded in series  
gives  
$$\exp\{G_n(z)\} = \prod_{j=1}^M \left( 1 + \frac{z^* e^{in\phi_j} + z e^{-in\phi_j}}{M} \right)$$

$$v_n\{2\}^2 = c_n\{2\} \quad v_n\{4\}^4 = -c_n\{4\} \quad v_n\{6\}^6 = \frac{1}{4} c_n\{6\} \quad v_n\{8\}^8 = -\frac{1}{33} c_n\{8\}$$

Method based on the event flow vector:

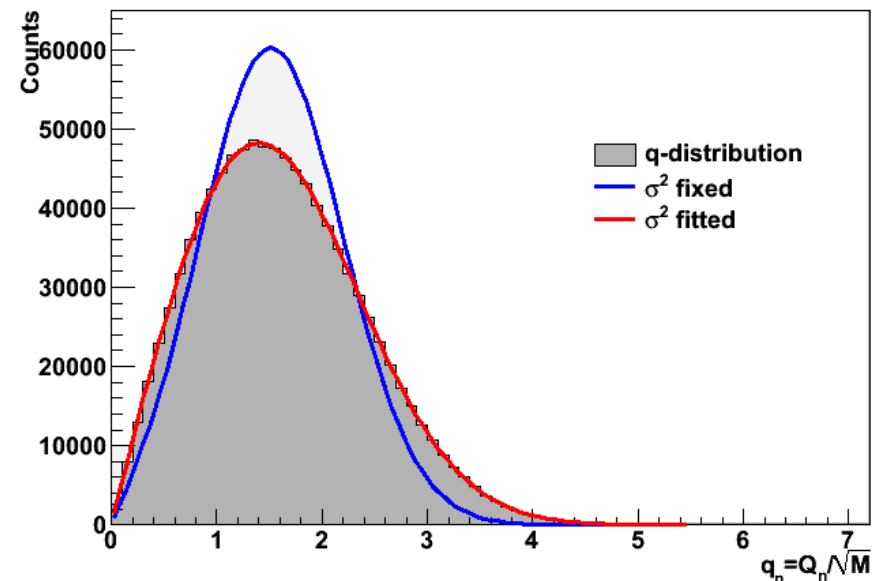
Fitting Q-vector distribution

$$\frac{dN}{dq_n} = \frac{q_n}{\sigma_n^2} e^{-\frac{v_n^2 M + q_n^2}{2\sigma_n^2}} I_0 \left( \frac{q_n v_n \sqrt{M}}{\sigma_n^2} \right) \quad q_n \equiv \frac{Q_n}{\sqrt{M}}$$

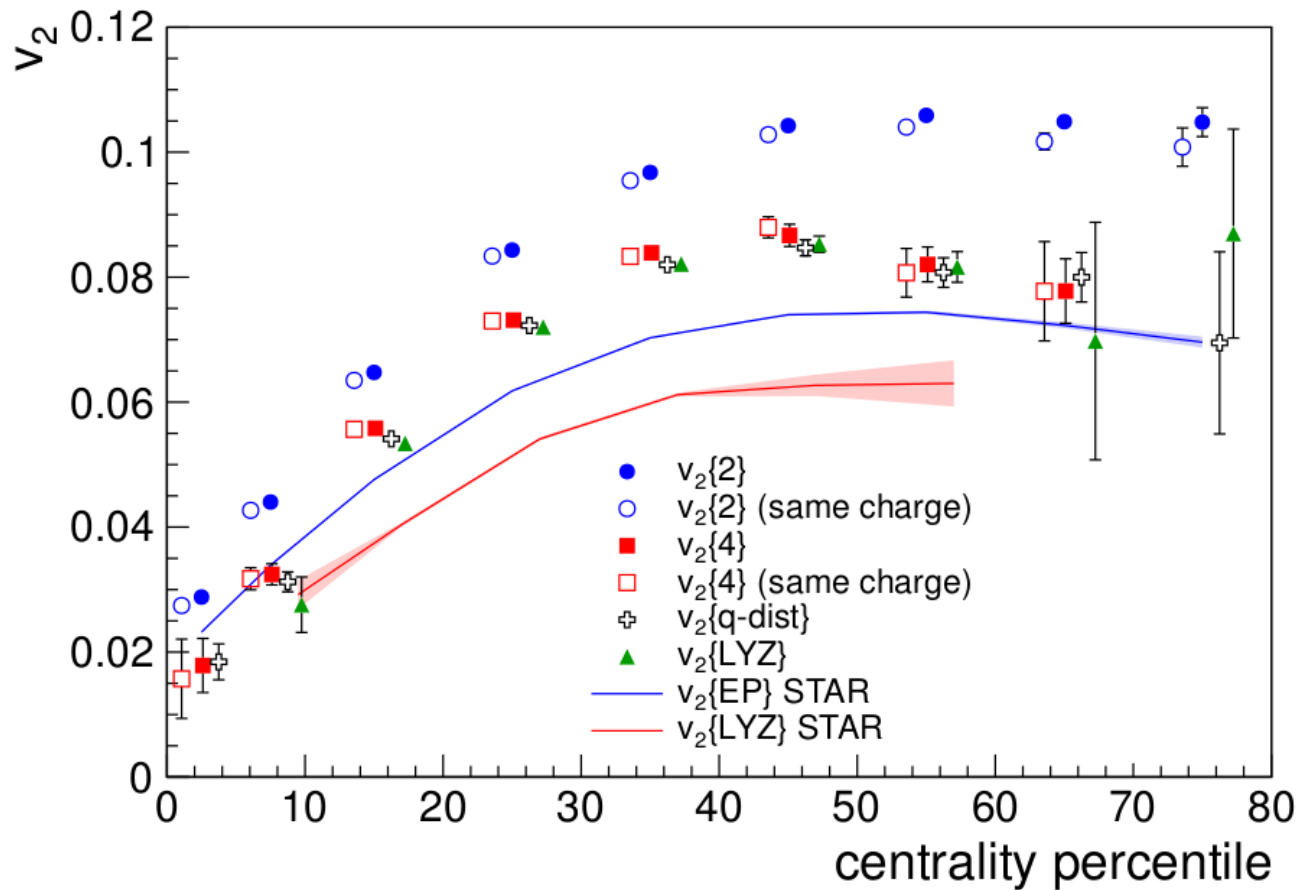
Lee-Yang zeros

(first minimum of the generating function)

$$G_2^\theta(ir) = \left| \left\langle e^{irQ_2^\theta} \right\rangle_{\text{evts}} \right| \quad V_n^\theta\{\text{LYZ}\} = \frac{j_{01}}{r_0^\theta}$$



# ALICE results from different techniques

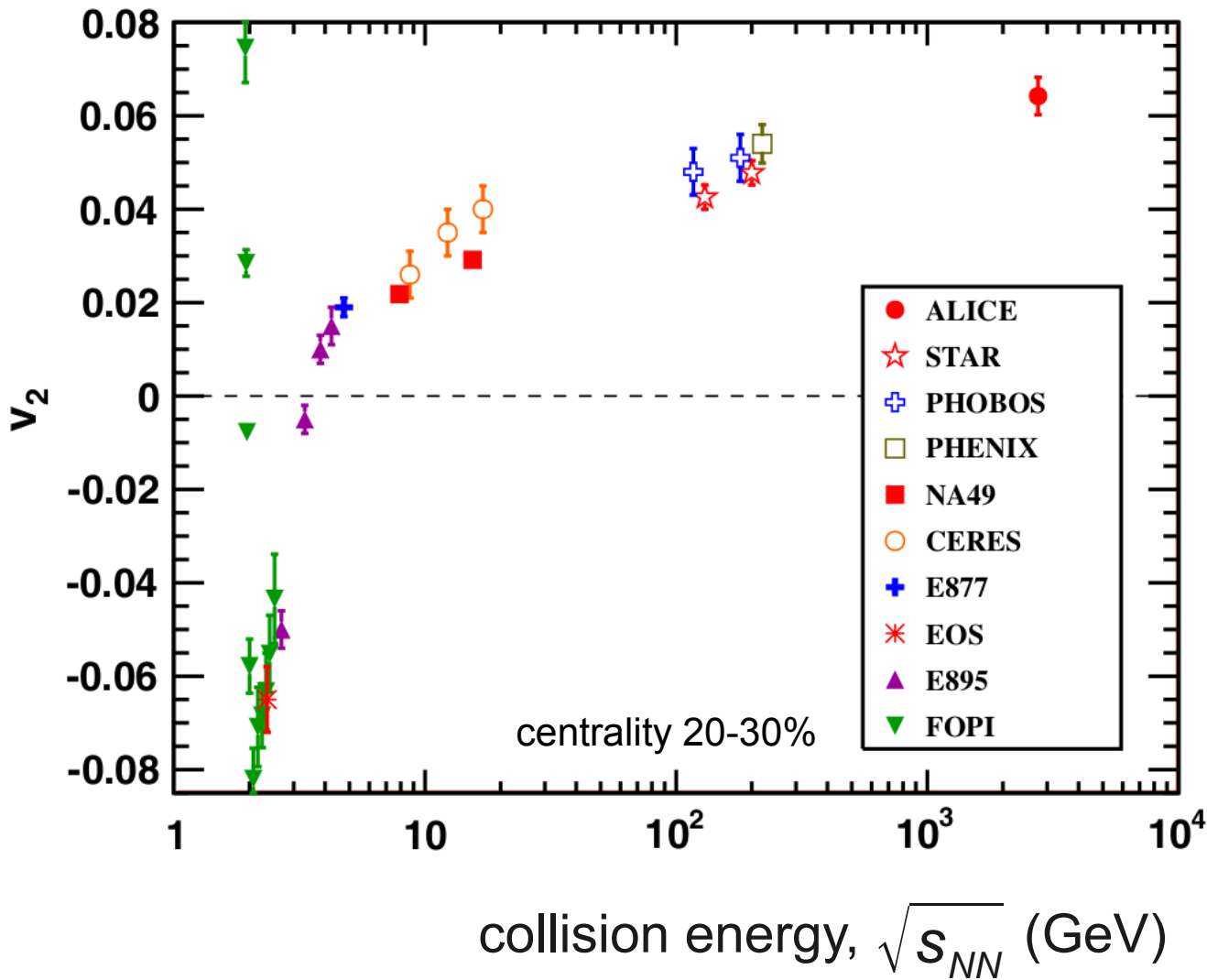


Results separate into two bands: from two and multi-particle correlations

**In-plane elliptic flow:  
the dominant flow component  
at the relativistic energies**

$$\frac{dN}{d(\Delta\phi)} \sim 1 + 2 \mathbf{v}_2 \cos(2\Delta\phi)$$

# Elliptic flow vs. collision energy

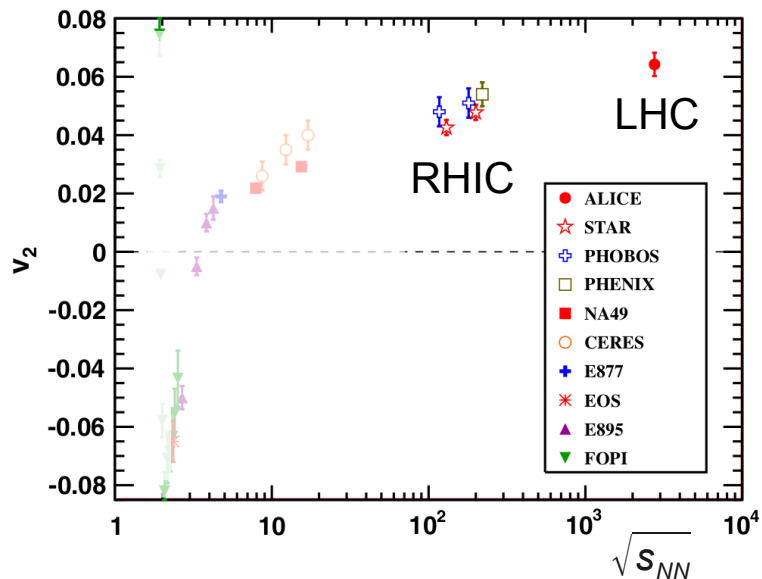
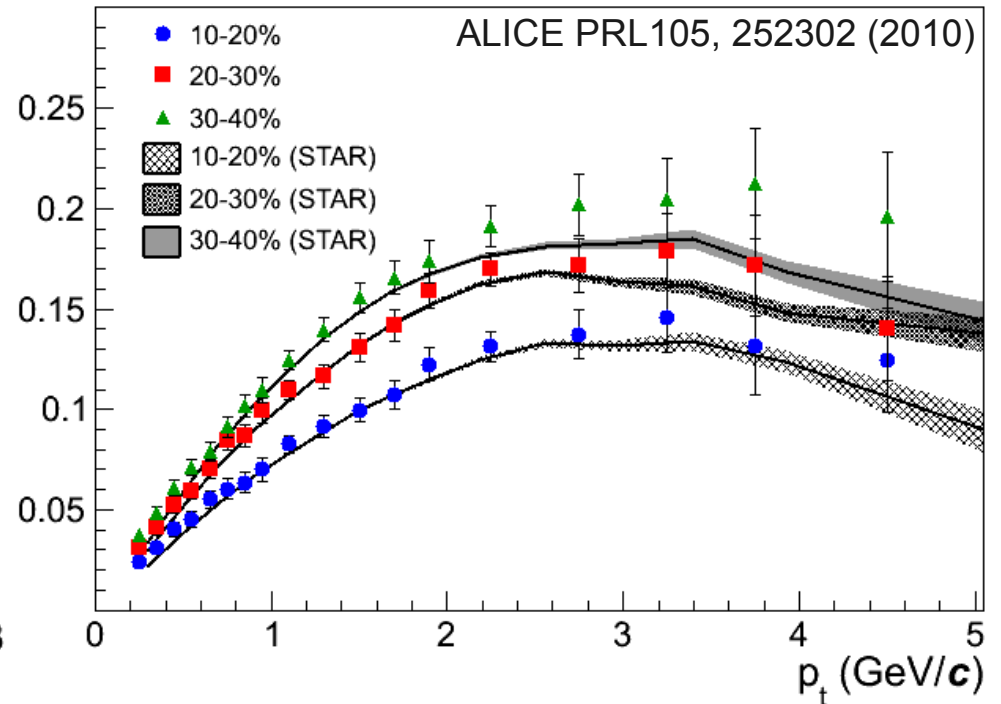
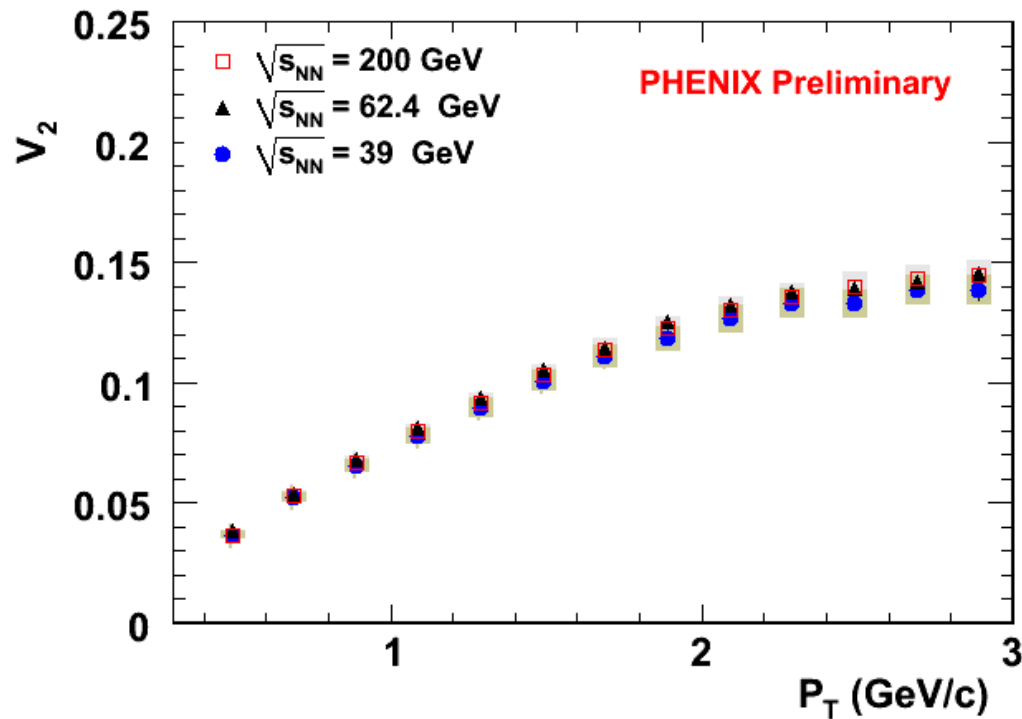


Experimental results covers about 4 decades of the collision energy

Data from GSI, AGS, SPS, RHIC, and LHC experiments

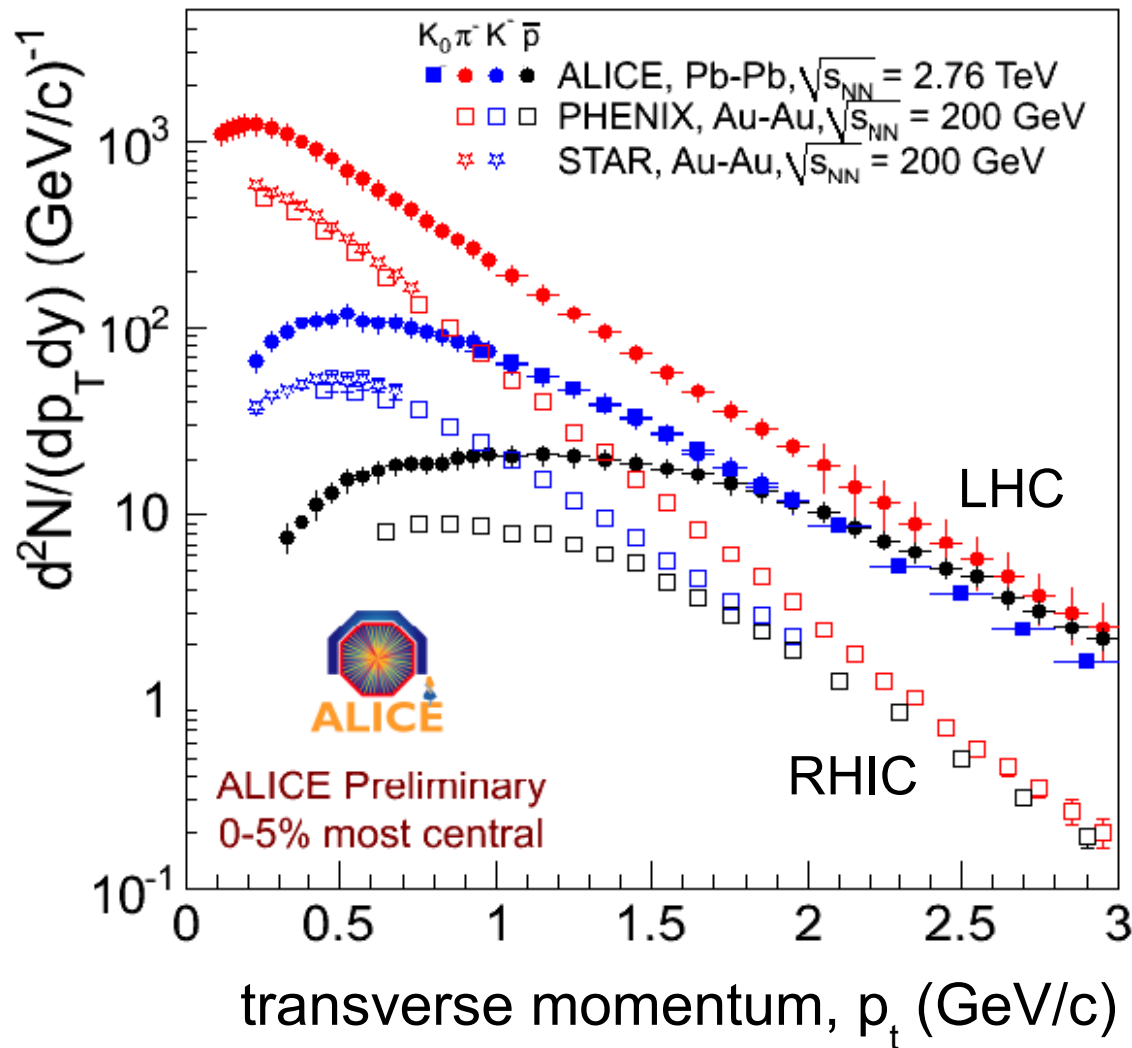


# $p_t$ differential elliptic flow vs. collision energy



$v_2(p_t)$  has similar shape and magnitude:  
 increase of integral  $v_2$  is driven  
 by stronger radial flow (boost to higher  $p_t$ )

# Identified particle spectra: LHC vs. RHIC



Spectra shapes changed significantly from RHIC to LHC

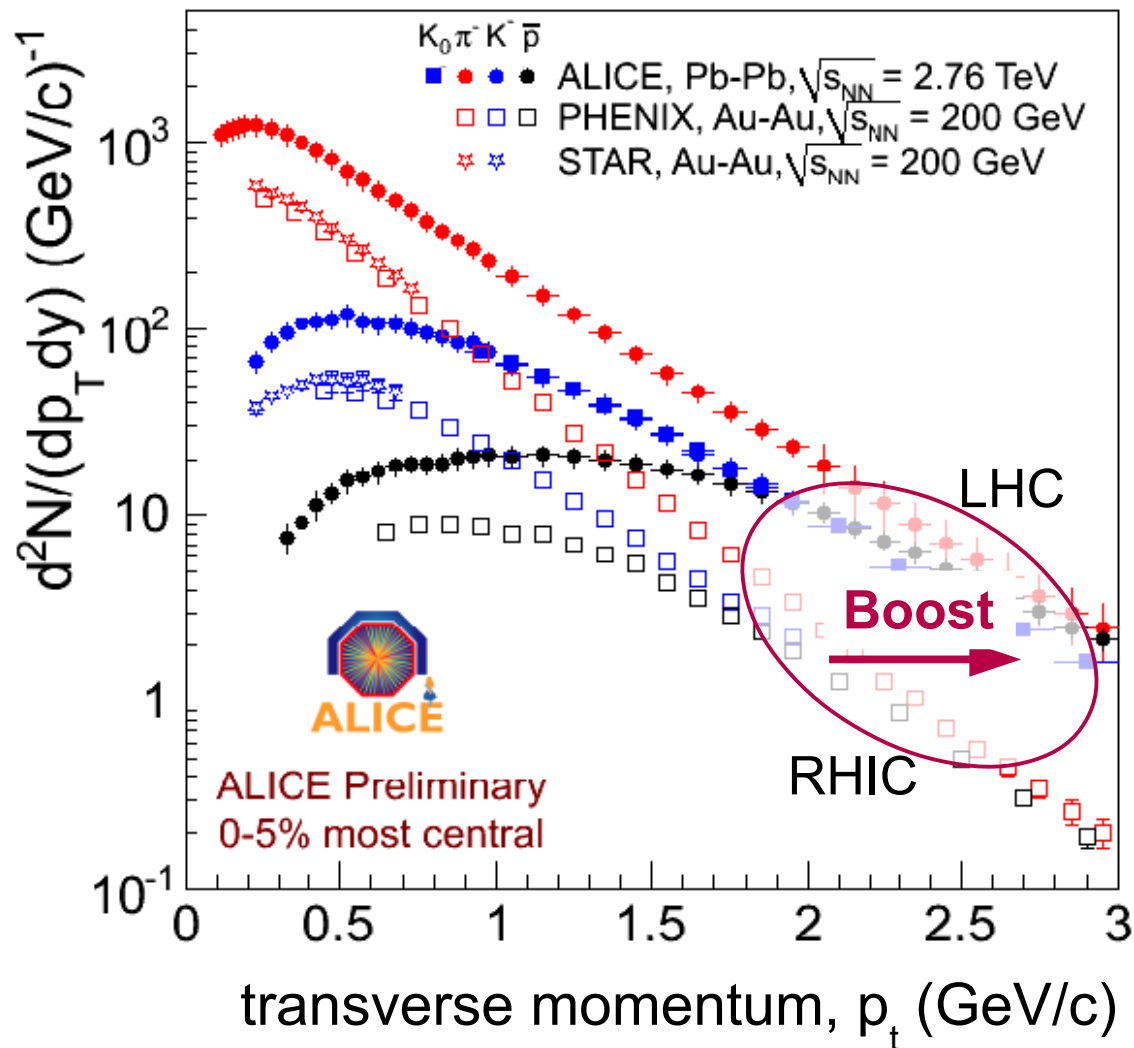
Radial expansion (flow):

Boost particles to higher  $p_t$   
(particles gain extra radial velocity)

From Blast wave spectra fits:  
20% stronger radial flow at LHC  
→ increase of integral  $v_2$



# Identified particle spectra: LHC vs. RHIC

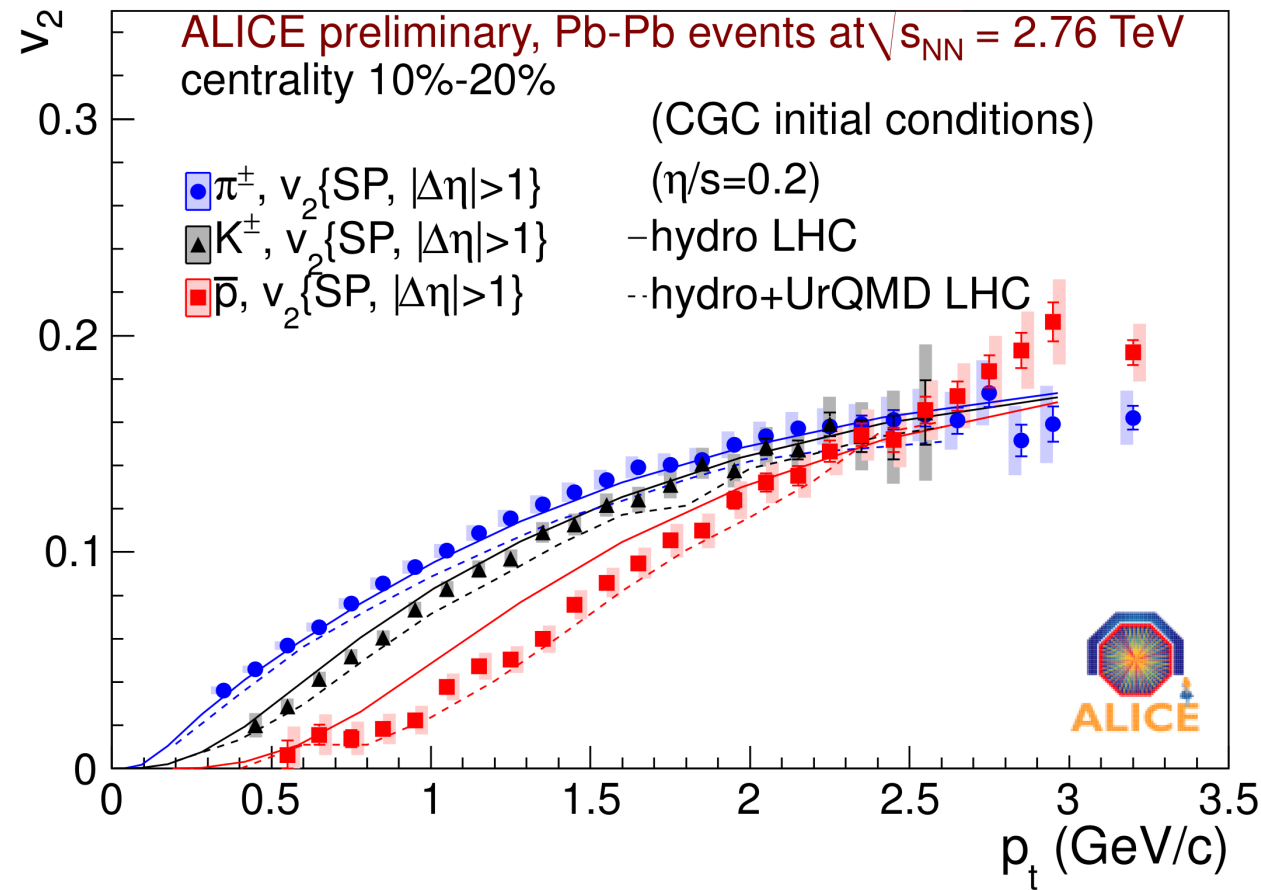


Spectra shapes changed significantly from RHIC to LHC

Radial expansion (flow):  
 Boost particles to higher  $p_t$   
 (particles gain extra radial velocity)

From Blast wave spectra fits:  
 20% stronger radial flow at LHC  
 → increase of integral  $v_2$

# Elliptic flow mass splitting



VISHNU: Heinz et. al, arxiv:1108.5323

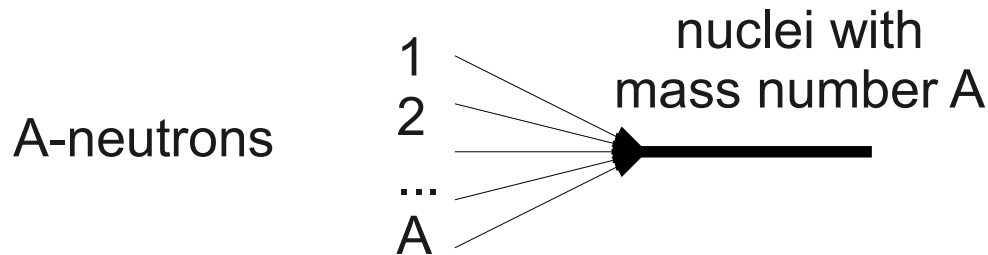
Similar to spectra:  
 $v_2$  of heavier particles  
is pushed to higher  $p_t$

Viscous hydrodynamics  
well describe flow of  $\pi^\pm$  and  $K^\pm$ :  
→ sensitivity to QGP viscosity

Including hadronic rescattering  
with UrQMD model allows  
better reproduce proton  $v_2$ :  
→ sensitivity to the evolution

# Coalescence and $v_2$ number of quarks scaling

Distribution of primordial particles  
reflects the distribution of original particles:



$$\frac{E_A d^3 n_A}{d^3 p_A} = B_A \left( \frac{E_p d^3 n_p}{d^3 p_p} \right)^A$$

$$\frac{dN}{d(\phi - \Psi_{RP})} \sim 1 + 2 \sum_{i=1} v_n(p_t, \eta) \cos[n(\phi - \Psi_{RP})]$$

If distribution is affected by flow,  
it will be amplified by coalescence:

$$v_{n,A}(p_{T,A}) \approx A v_{n,p}(p_{T,A}/A)$$

Mesons:

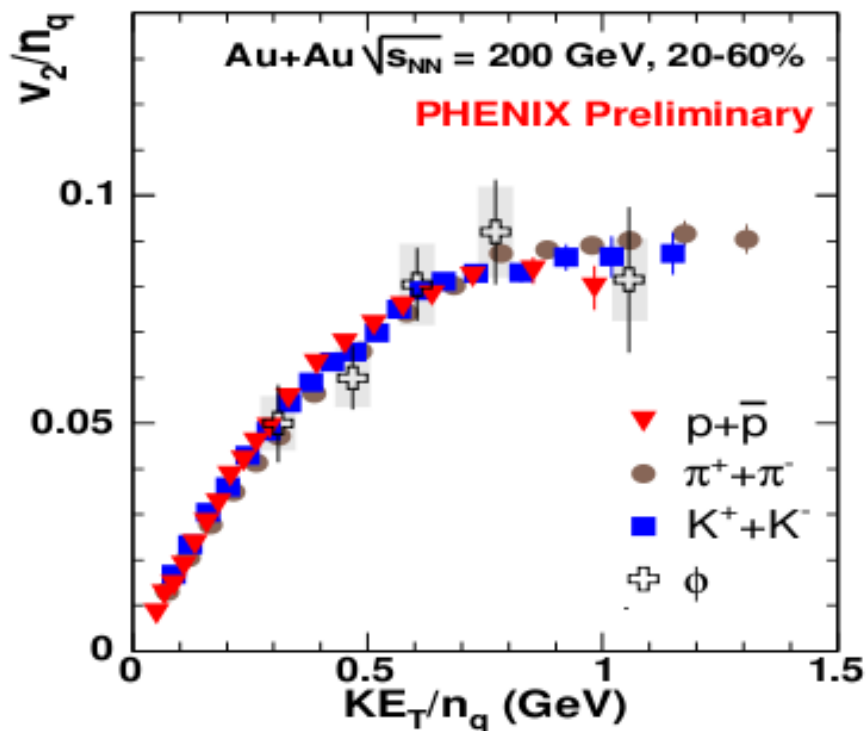
$$\frac{d^3 n_M}{d^3 p_M} \propto \left[ \frac{d^3 n_q}{d^3 p_q} (p_q \approx p_M/2) \right]^2$$

Baryons:

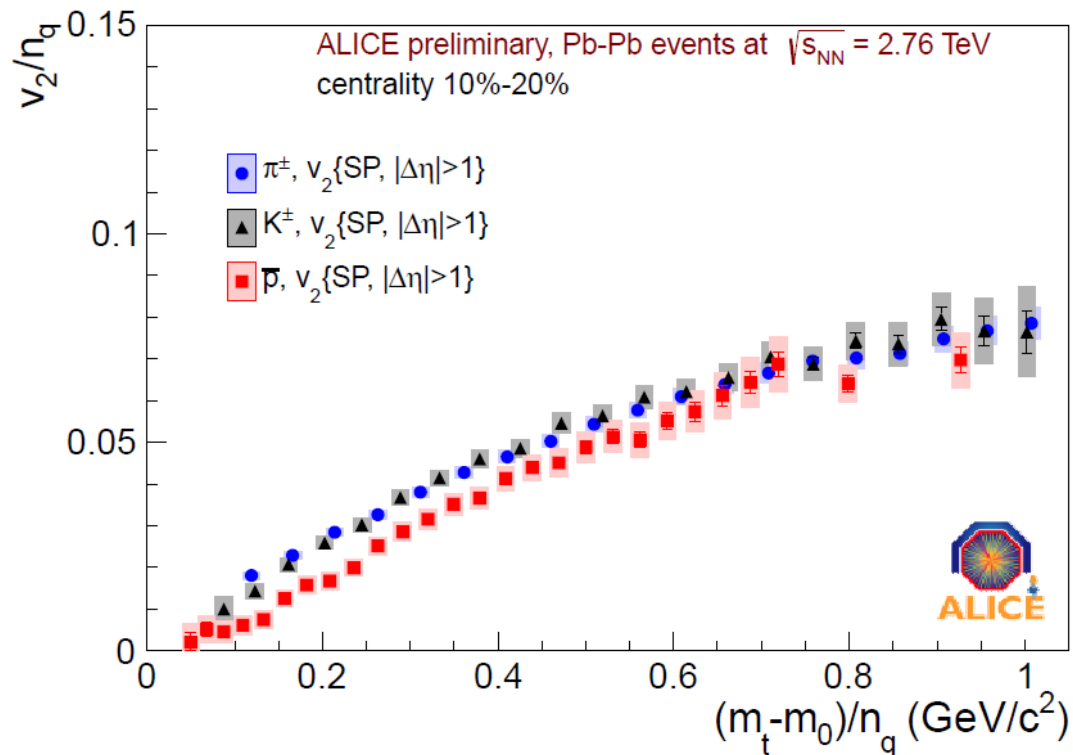
$$\frac{d^3 n_B}{d^3 p_B} \propto \left[ \frac{d^3 n_q}{d^3 p_q} (p_q \approx p_B/3) \right]^3$$

# Constituent number of quarks scaling

RHIC



LHC

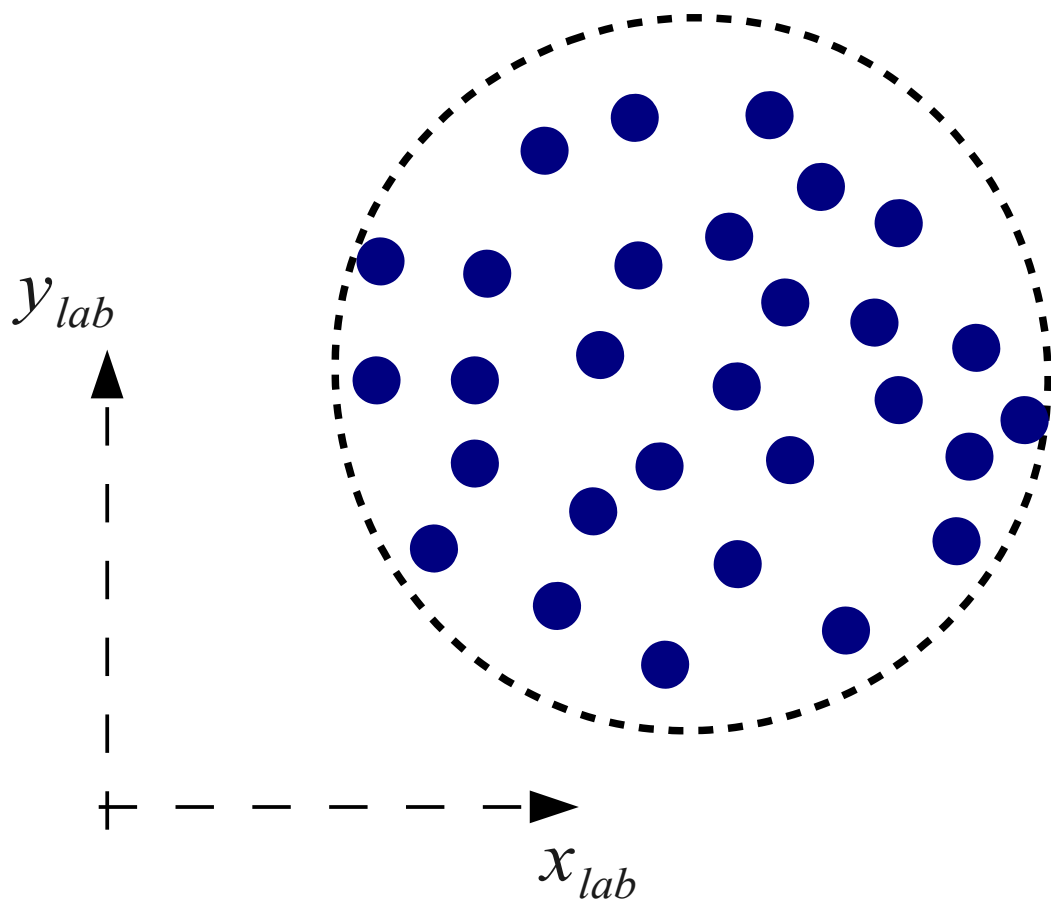


Observe approximate number of quark scaling:  
Strong indication that system evolved  
through deconfined (QGP) phase

# Flow fluctuations

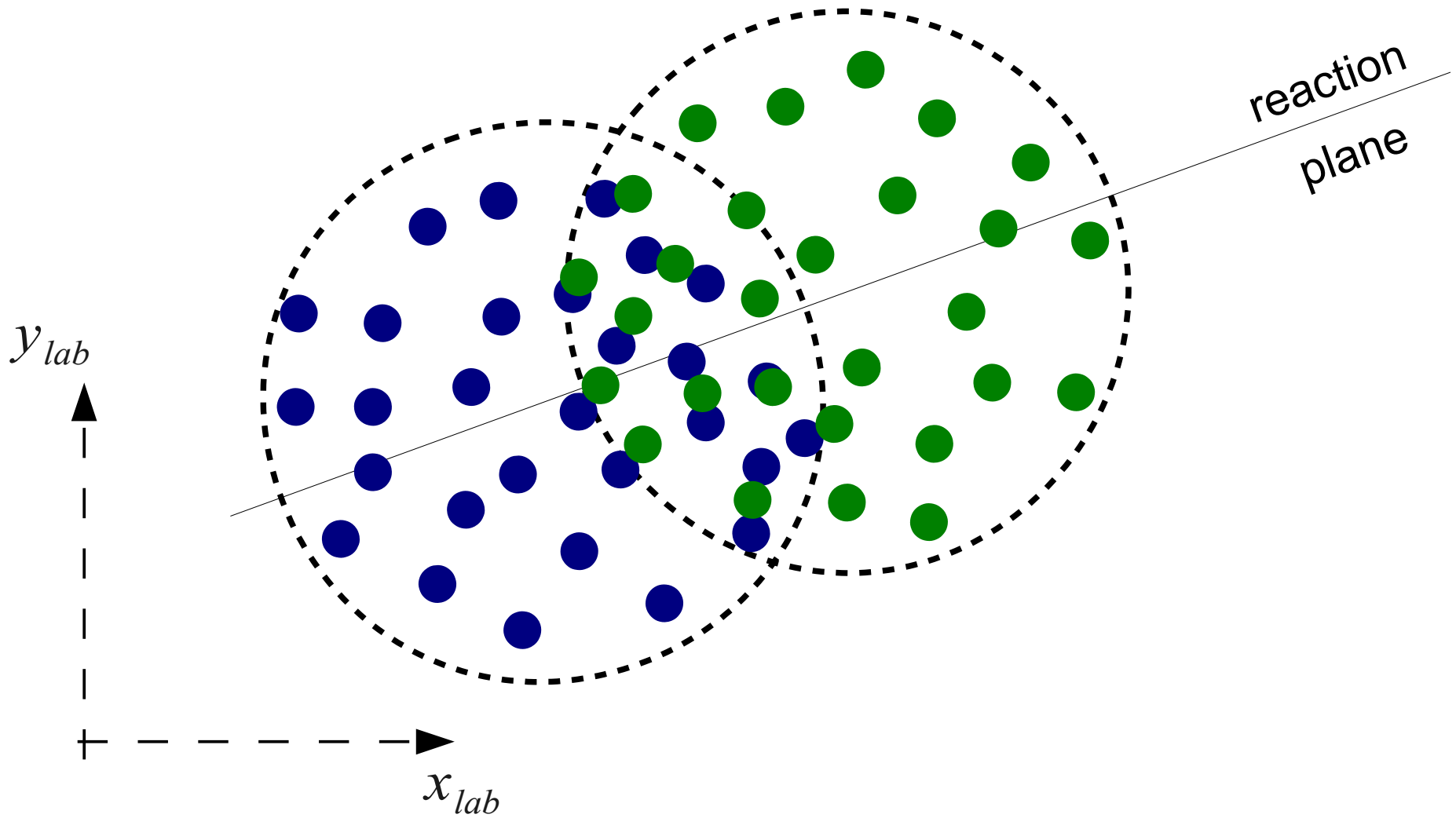
# Flow fluctuations

Transverse distribution of nucleons inside a nuclei  
(e.g. can be simulated with Glauber Monte-Carlo)



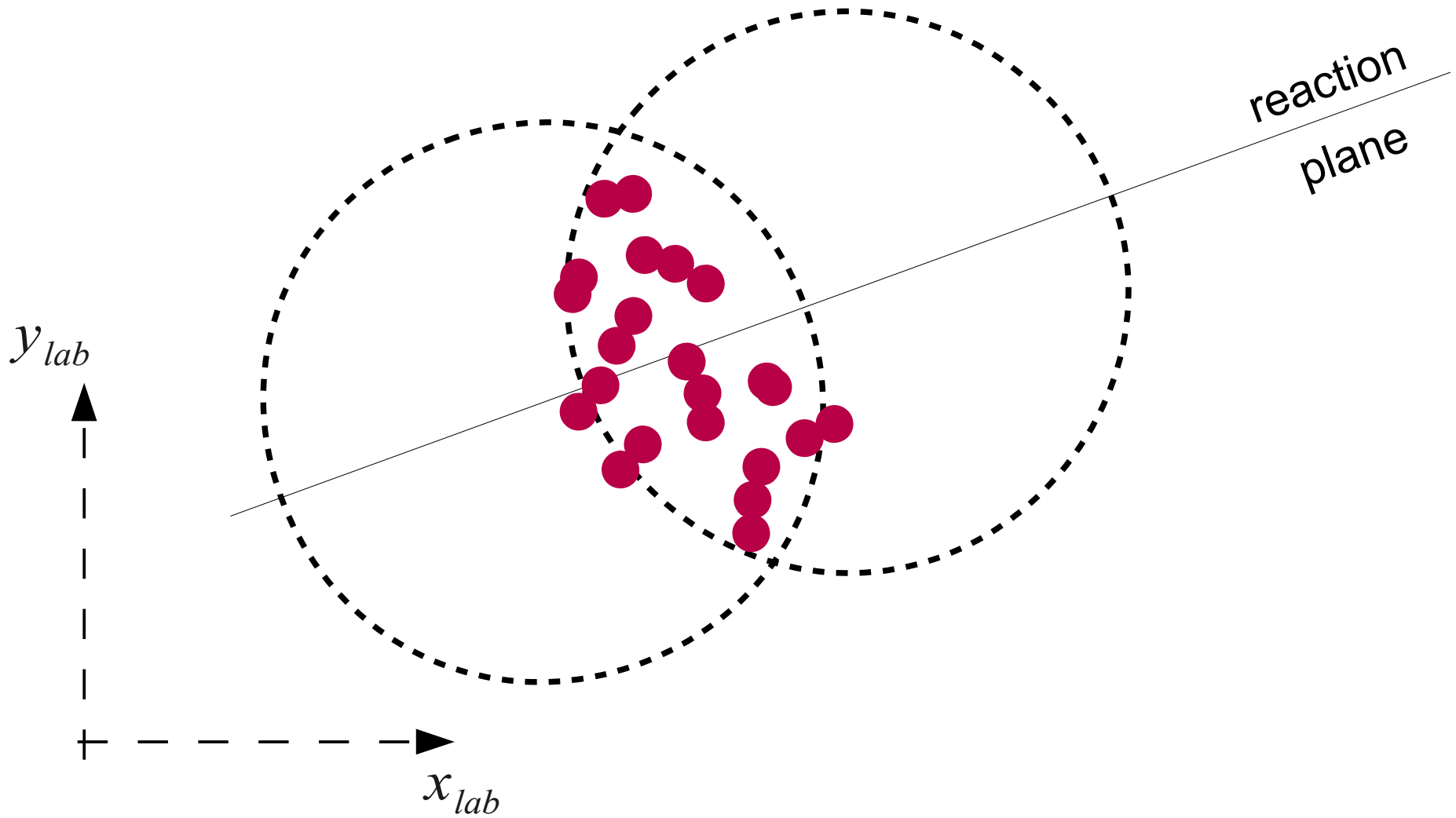
# Flow fluctuations

A moment just before collision:  
overlaid transverse distributions of nucleons inside each nuclei



# Flow fluctuations

Some of the nucleons (participants) interacted; others (spectators) passed by



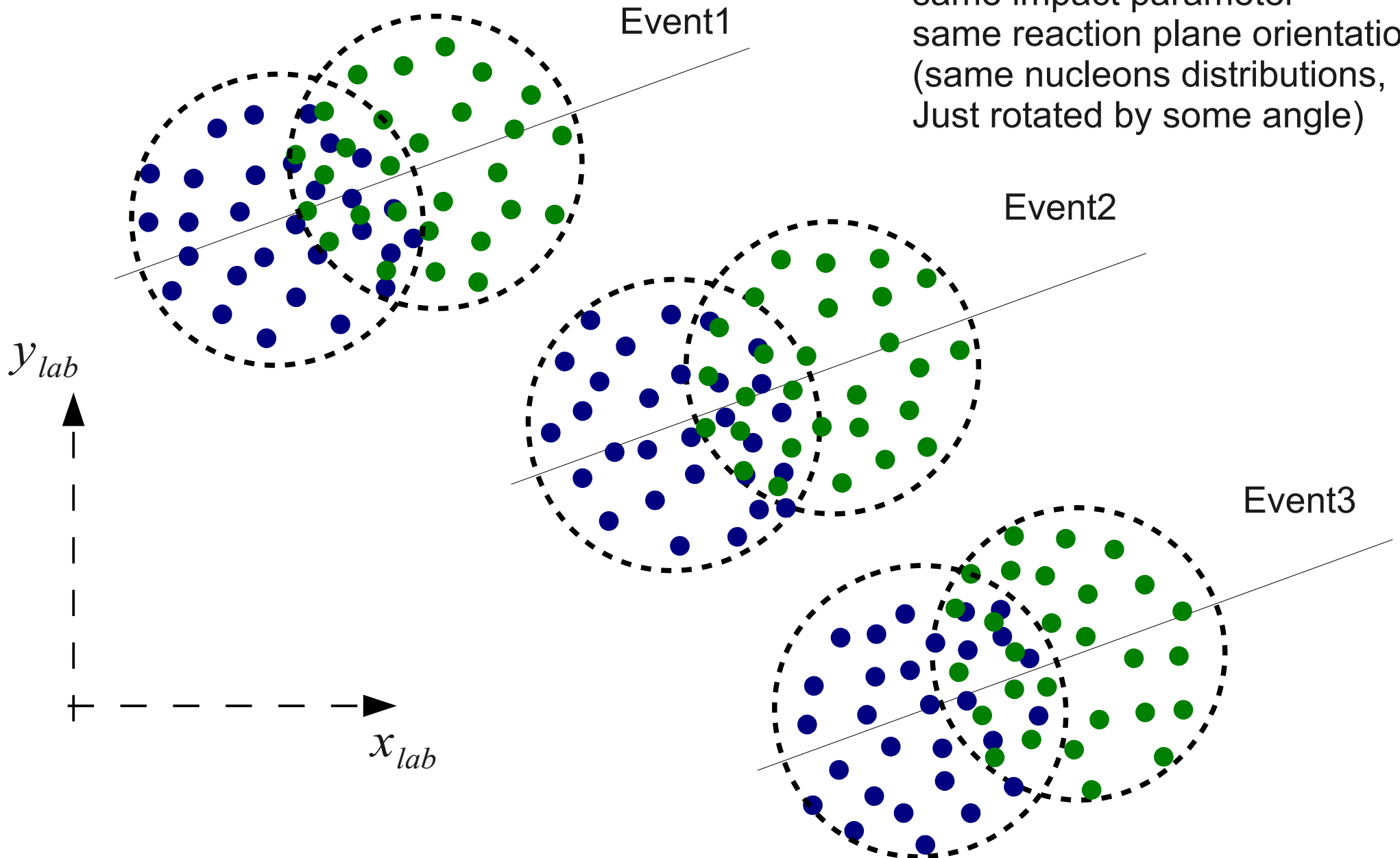


# Flow fluctuations

Event-by-event flow fluctuations

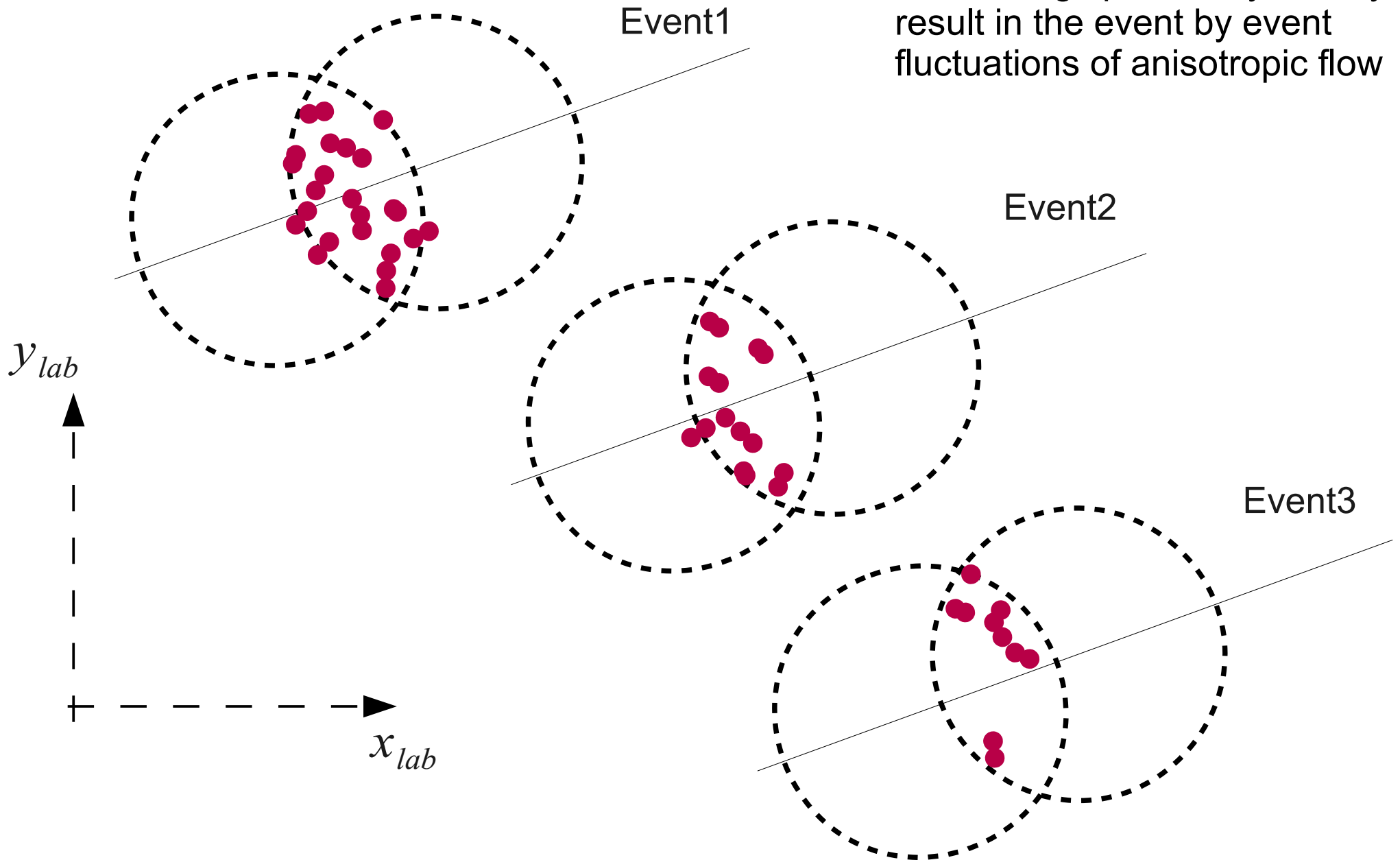
**Example:**

same impact parameter  
same reaction plane orientation  
(same nucleons distributions,  
Just rotated by some angle)

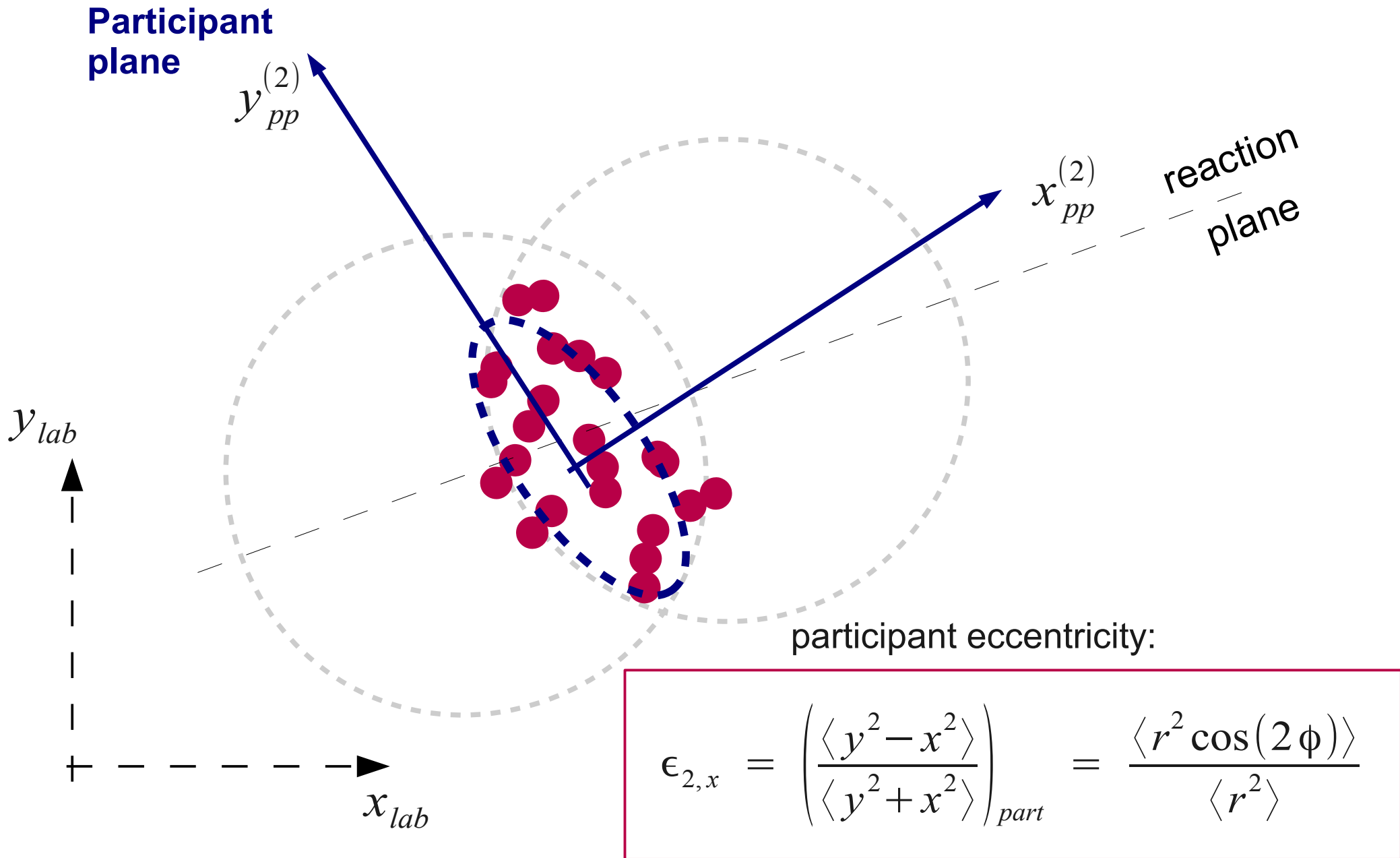


# Flow fluctuations

Fluctuating spatial asymmetry  
result in the event by event  
fluctuations of anisotropic flow



# Flow fluctuations: participant eccentricity



# How fluctuations affect the measured flow?

2-particle azimuthal correlation:

$$c_n\{2\} = \langle \cos[2(\phi_i - \phi_j)] \rangle = \langle v_n^2 \rangle + \delta_{n,2}$$

$$\langle v_n^2 \rangle \neq \langle v_n \rangle^2$$

$$\langle v_n^2 \rangle = \langle v_n \rangle^2 + \sigma_n^2$$

$$\langle \cos[n(\phi_i - \phi_j)] \rangle = \langle v_n \rangle^2 + \sigma_n^2 + \delta_{n,2}$$

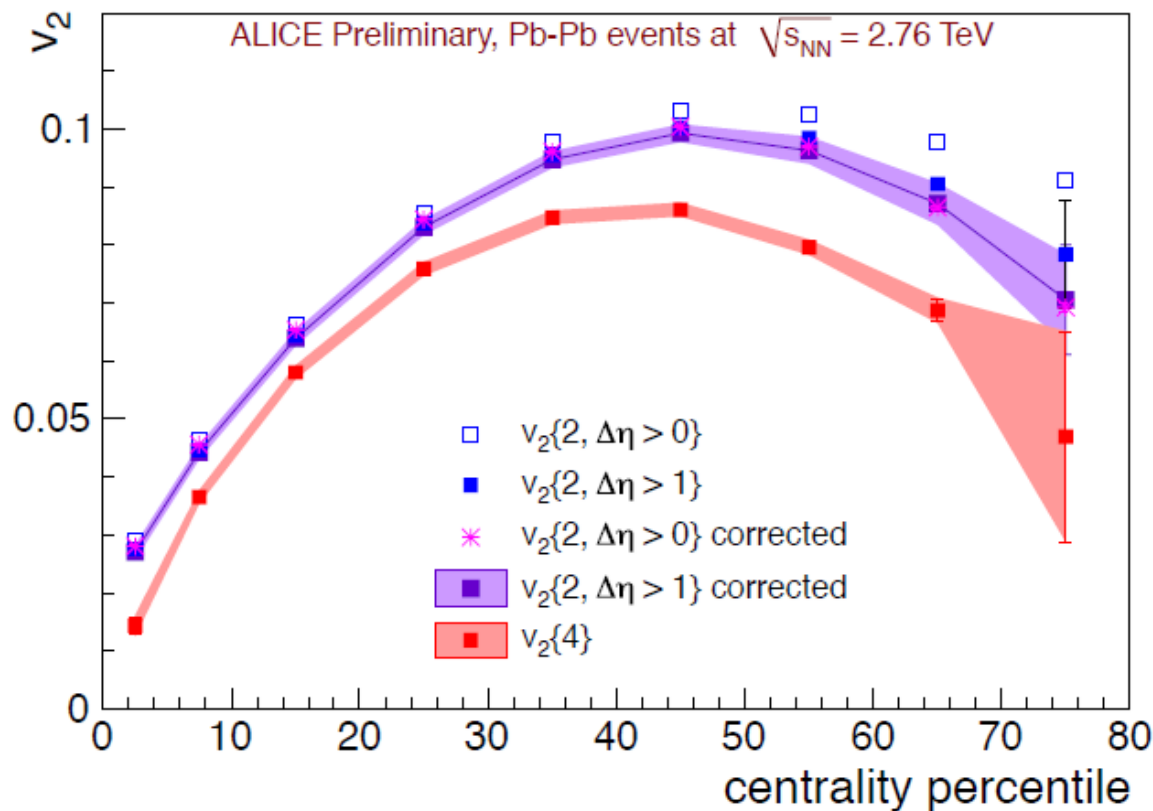
flow

fluctuations

non-flow

# Elliptic flow fluctuations

2-particle correlations affected by 3 effects:  $v_2\{2\} = \sqrt{\langle v_2 \rangle^2 + \sigma_2^2 + \delta_2}$



Residual non-flow subtracted based on HIJING Monte-Carlo:

$$v_2^{corr}\{2\} \approx \langle v_2 \rangle + \frac{\sigma_2^2}{2\langle v_2 \rangle}$$

Many-particle correlations free of non-flow:

$$v_2\{4\} \approx \langle v_2 \rangle - \frac{\sigma_2^2}{2\langle v_2 \rangle}$$

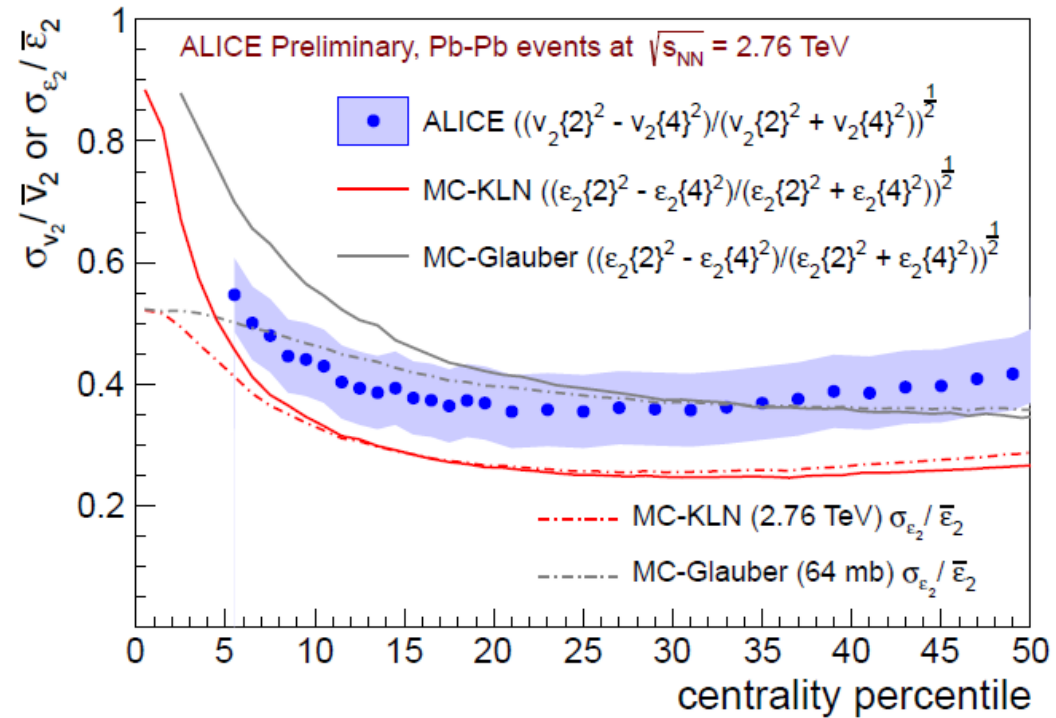
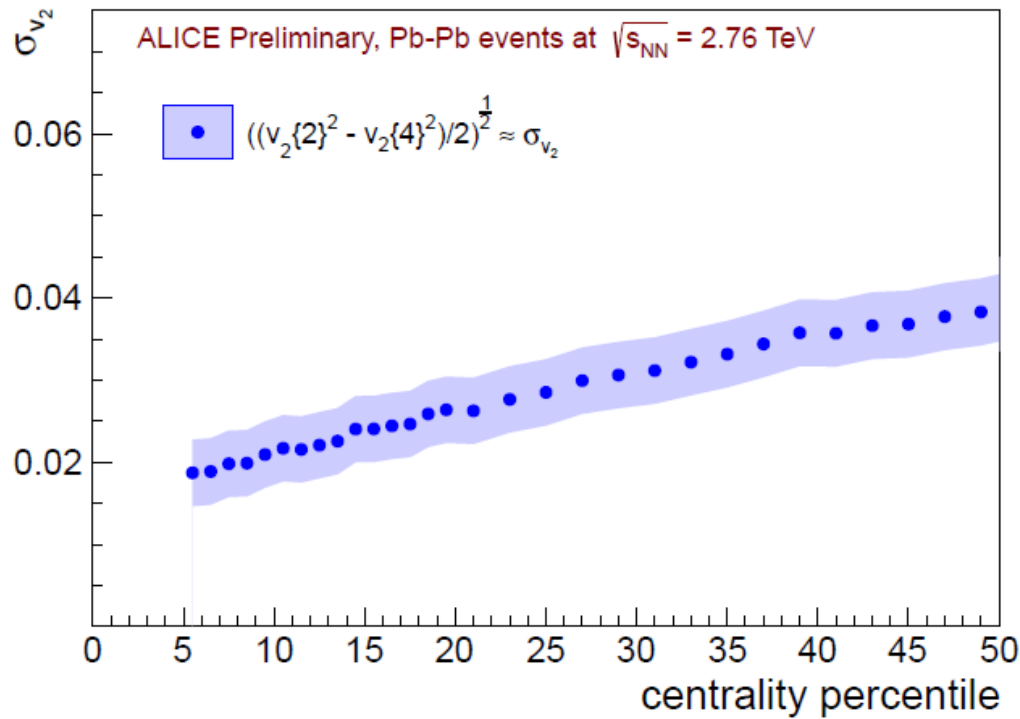
Fluctuations set the difference between  $v_2^{corr}\{2\}$  and  $v_2\{4\}$

Flow fluctuations are significant  
Additional constraint on the initial condition

# Estimating flow fluctuations from data

$\sigma_2$

$\sigma_2 / \langle v_2 \rangle$



Gaussian fluctuations or  $\sigma_n \ll \langle v_n \rangle$

$$\sigma_2 \approx \sqrt{\frac{v_2\{2\} - v_2\{4\}}{2}}$$

$$\langle v_2 \rangle = \sqrt{\frac{v_2\{2\} + v_2\{4\}}{2}}$$

Fluctuations can be significant

Helps to constrain initial condition

# “Odd” harmonic flow and fluctuations

$$\frac{dN_\alpha}{d(\Delta\phi_\alpha)} \sim 1 + 2 \sum_{i=1} v_{n,\alpha} \cos(n \Delta\phi_\alpha)$$

By symmetry of the collision, odd harmonic flow  $v_{2m+1}$  measured wrt. the reaction plane should vanish at mid-rapidity (or in any symmetric rapidity range):

$$v_{2m+1}^{odd}(-\eta) = -v_{2m+1}^{odd}(\eta)$$

Fluctuations does not obey the symmetry rule of the odd harmonic flow wrt. reaction plane.  
For example in case of directed flow:

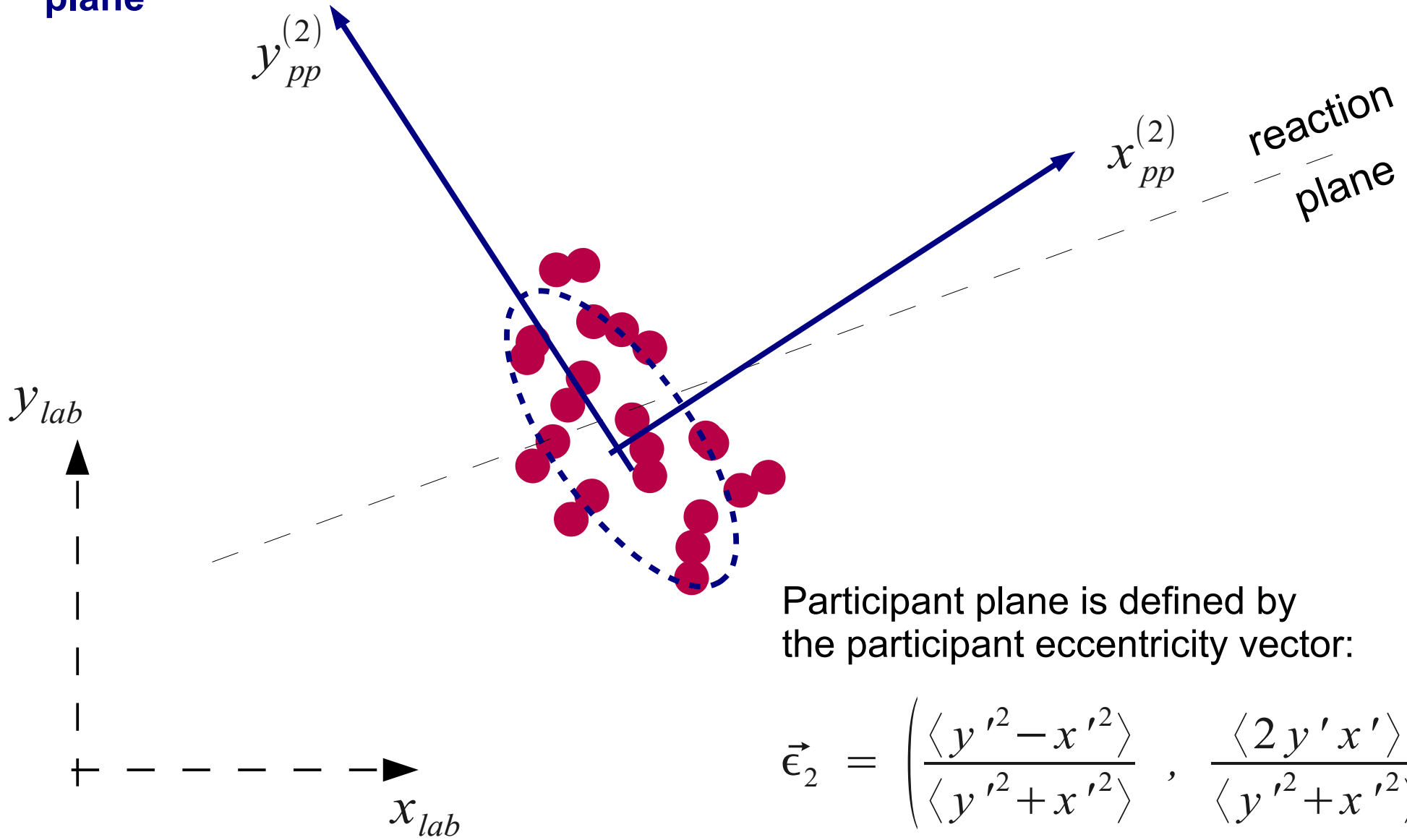
$$v_1\{2\} = \sqrt{\langle v_1^2 \rangle} = \sqrt{\langle v_1 \rangle^2 + \sigma_1^2} = \sigma_1 \neq 0$$

Conclusion: in the symmetric rapidity range all odd harmonics originates from flow fluctuations:

$$v_{2m+1}^{even}(-\eta) = +v_{2m+1}^{even}(\eta) \text{ - rapidity “even” odd harmonic flow}$$

# Flow fluctuations: ellipticity

Participant plane



Participant plane is defined by the participant eccentricity vector:

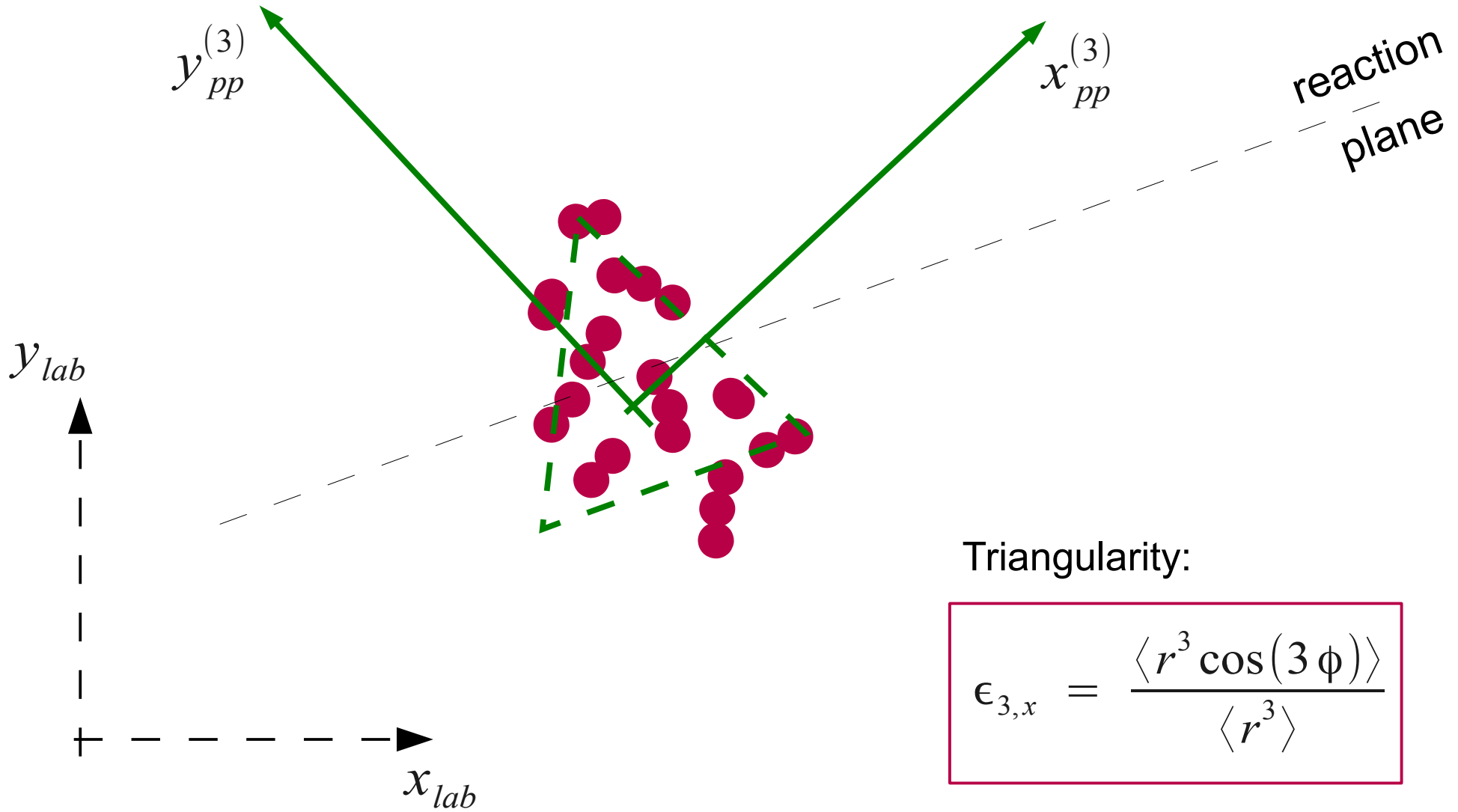
$$\vec{\epsilon}_2 = \left( \frac{\langle y'^2 - x'^2 \rangle}{\langle y'^2 + x'^2 \rangle}, \frac{\langle 2y'x' \rangle}{\langle y'^2 + x'^2 \rangle} \right)_{part}$$

$$x' = x - \langle x \rangle \quad y' = y - \langle y \rangle$$



# Flow fluctuations: triangularity

Triangularity  
plane

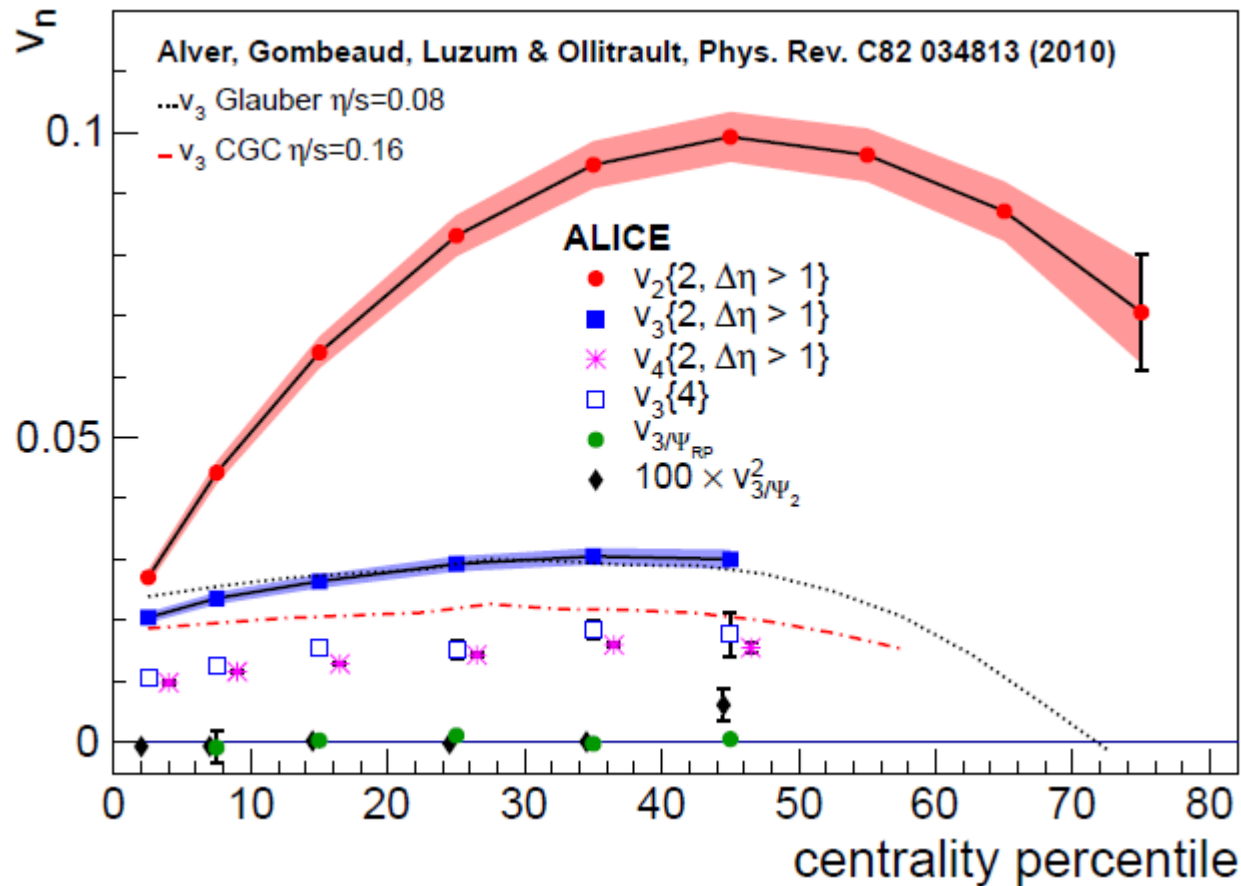


Triangularity:

$$\epsilon_{3,x} = \frac{\langle r^3 \cos(3\phi) \rangle}{\langle r^3 \rangle}$$

# Triangular flow, $v_3$

Measured odd harmonic flow provides clean probe of fluctuations



$$\langle v_3 \rangle = 0 \quad \sigma_3 \neq 0$$

$\sigma_n \ll \langle v_n \rangle$  does not apply

Non-zero  $v_3$  is observed

$v_3$  shows weak centrality dependence - collectivity  
 (non-flow correlations should drop as  $1/\text{multiplicity}$ )

# Triangular flow, $v_3$

Cumulant results consistent with expectations for fluctuations:

$$\frac{v_3\{2\}}{v_3\{4\}} \approx 2$$

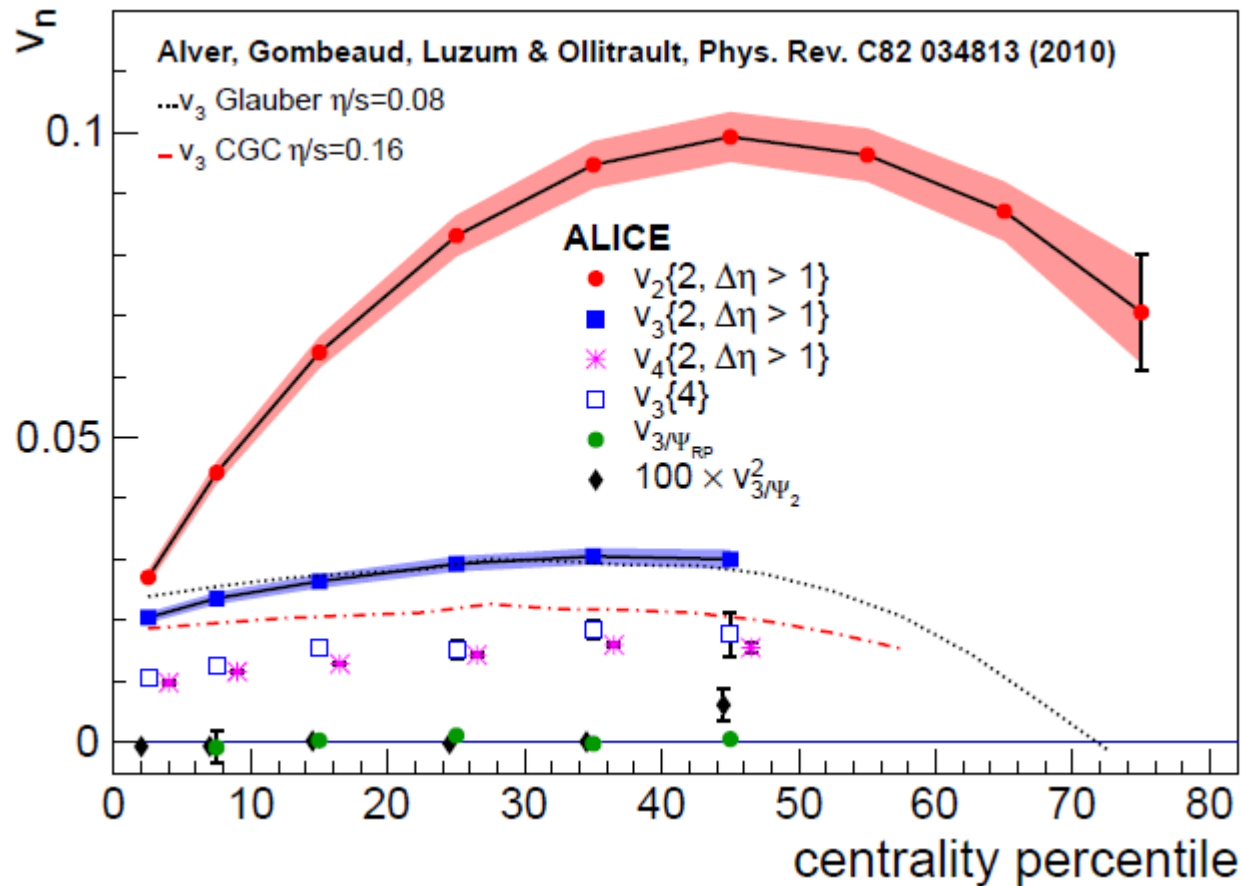
Uncorrelated to reaction plane zero  $v_3$  with spectators:

$$v_3\{\Psi_{RP}\} \equiv v_3\{ZDC\} = 0$$

Mixed harmonics (3<sup>rd</sup> and 2<sup>nd</sup>):

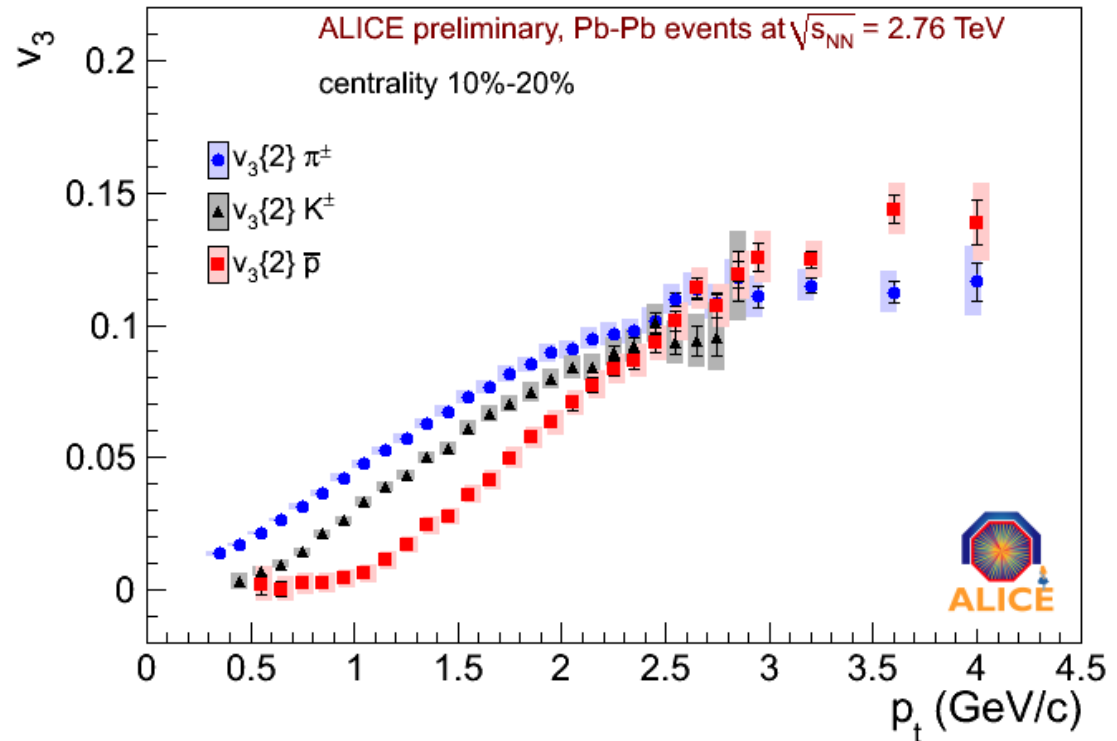
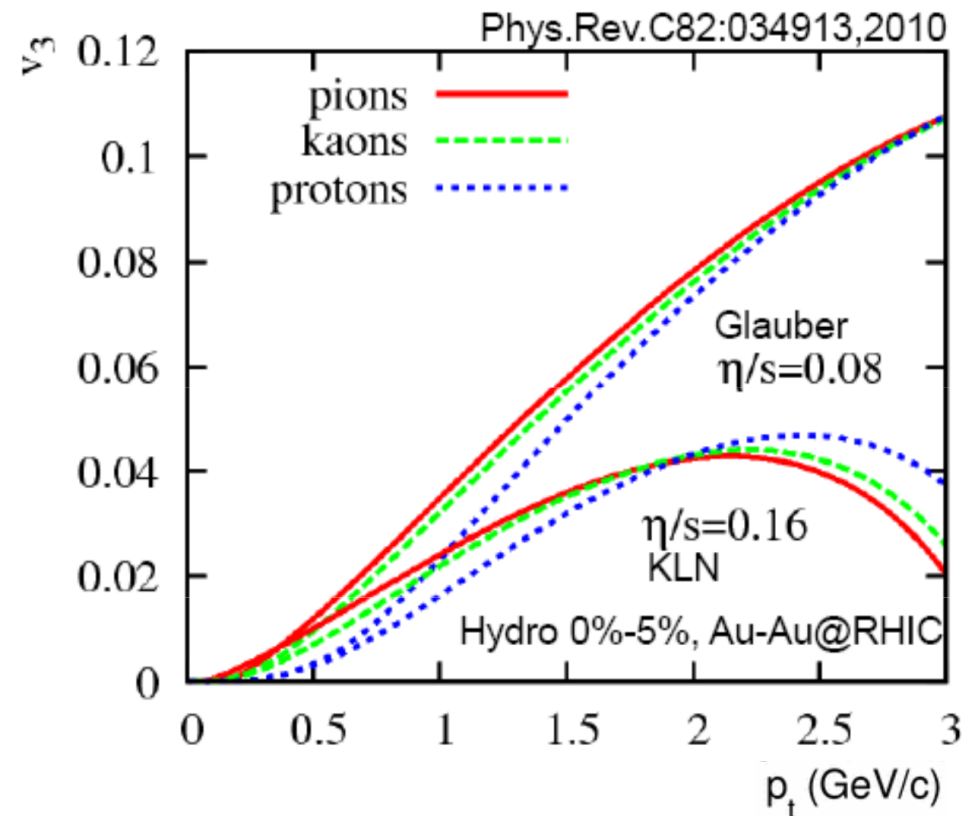
$$v_3\{\Psi_2\} = 0$$

Weak centrality dependence



Strong evidence for the geometrical (due to spacial fluctuations) origin of  $v_3$

# Mass splitting: test of “hydrodynamic” origin of $v_3$

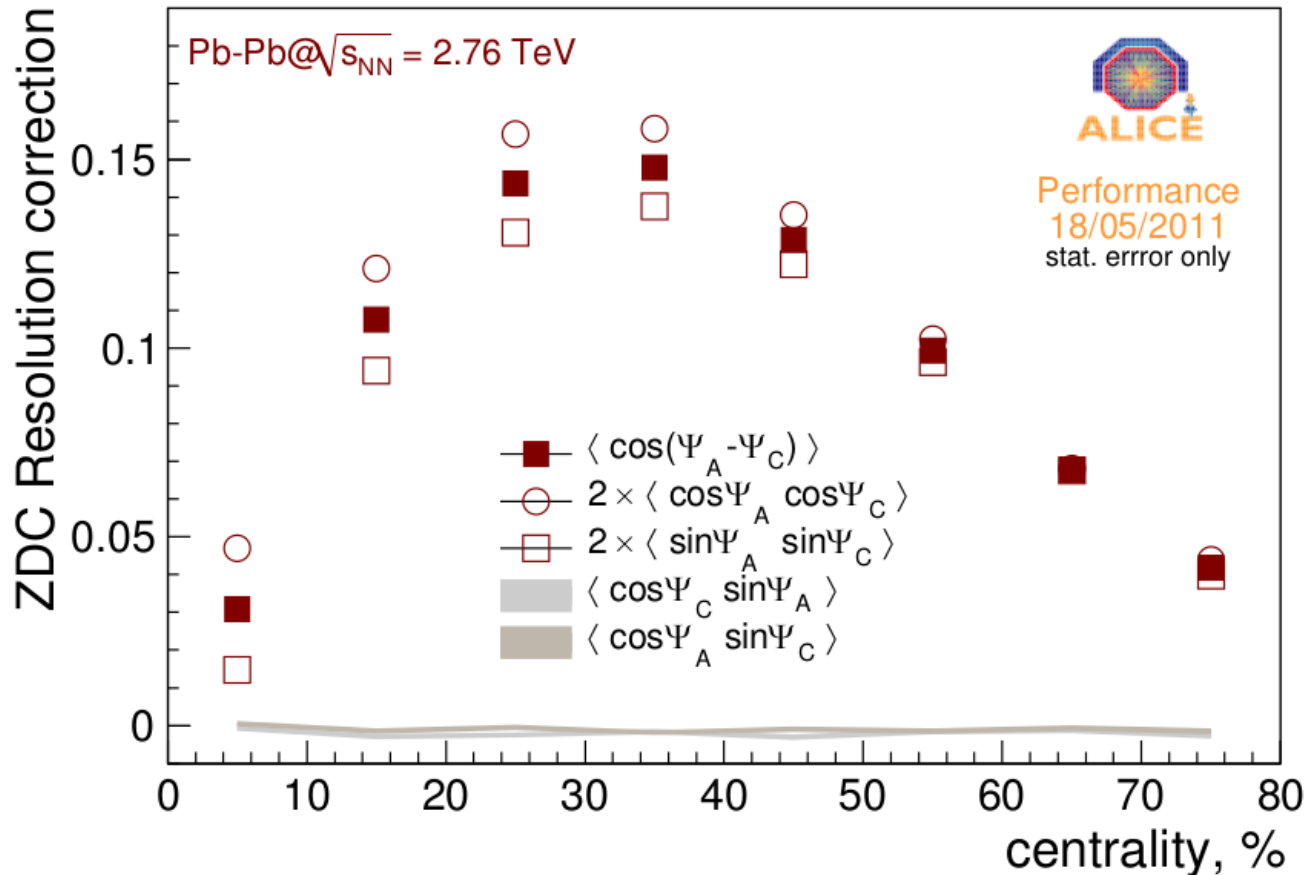


- Observed mass splitting for  $v_3$  supports its hydrodynamic origin
- Additional strong constraint on viscosity and initial condition

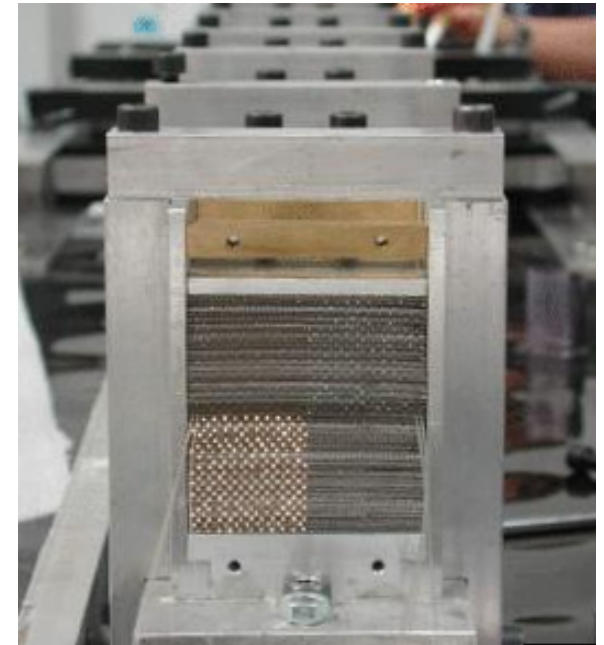
# Directed flow measured with spectators

$$\frac{dN}{d(\Delta\phi)} \sim 1 + 2v_1 \cos \Delta\phi$$

# Sensitivity to spectator's directed flow with ZDC

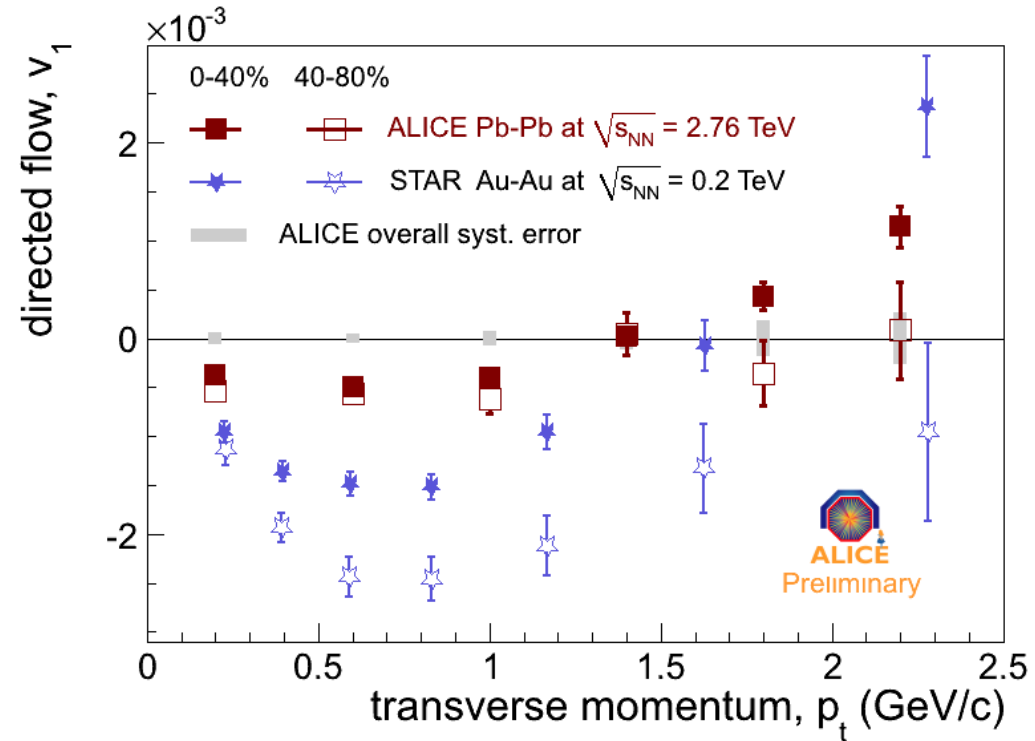
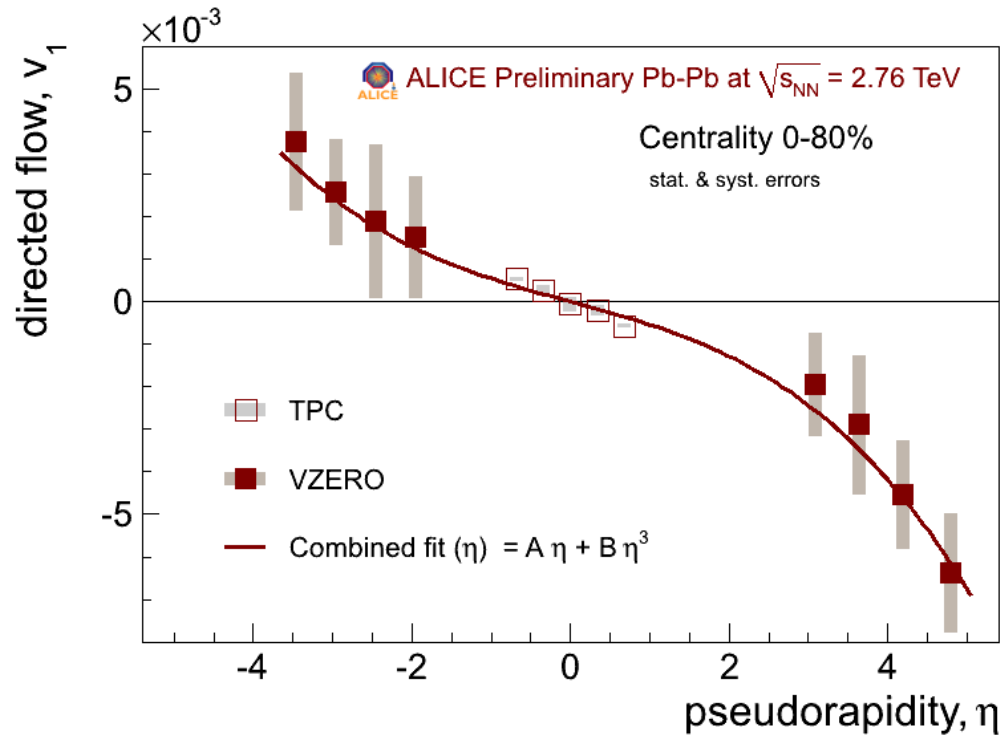


ZDC: 7.2 x 7.2 cm<sup>2</sup>



Observe correlation between spectators' deflection measured with neutron Zero Degree Calorimeters located 114meters on each side from the collision vertex:  
sensitivity to the directed flow of spectator

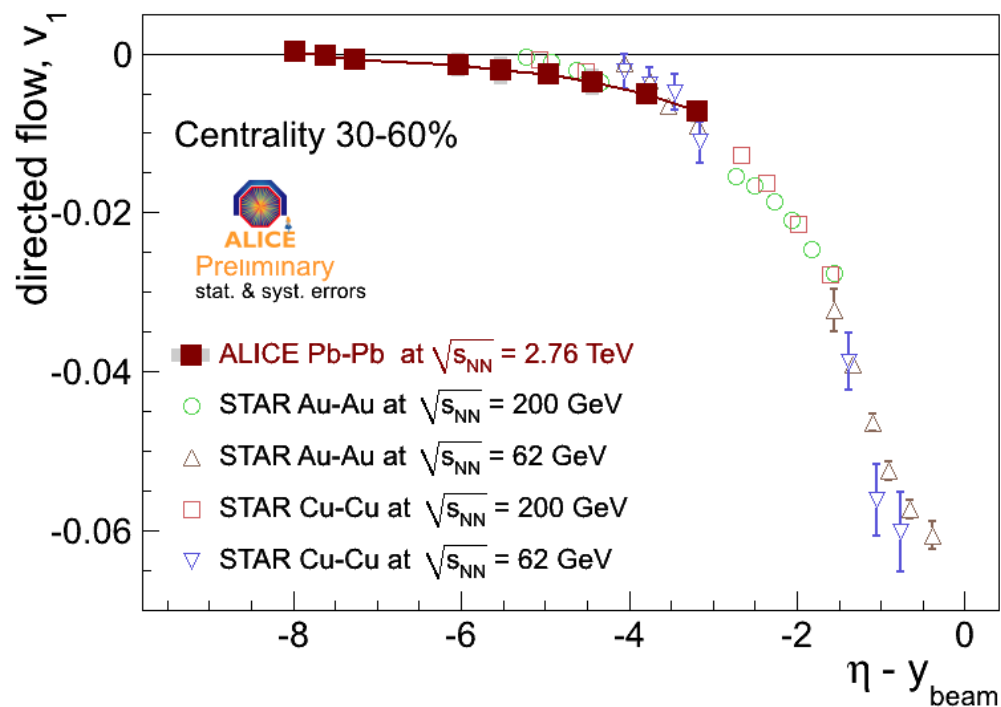
# Directed flow: $\eta$ , $p_t$ and centrality dependence



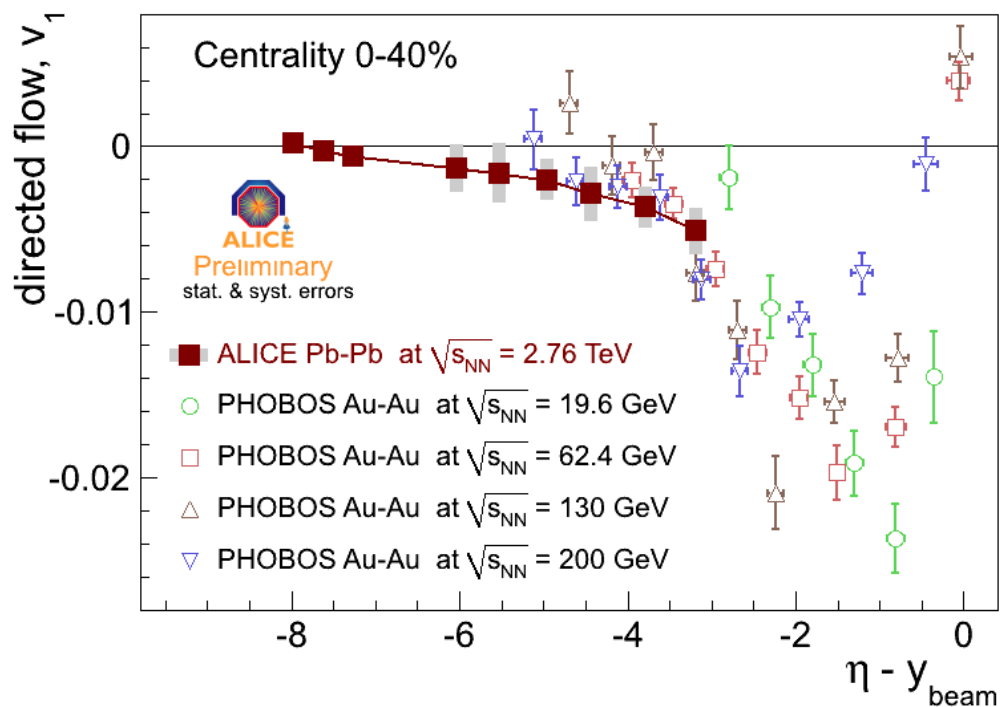
- Negative slope at midrapidity:
  - ✓ Same as at RHIC
  - ✓ In contrast to some of the theoretical predictions
- Zero crossing around  $p_T \sim 1.5$  GeV

# Directed flow: longitudinal scaling

STAR data: PRL 101, 252301 (2008)



PHOBOS data: PRL97, 012301 (2006)



Universal trend when shifted to beam rapidity  
Data follows the longitudinal scaling observed at RHIC



# Two particle azimuthal correlation:

collective flow modulations  
or ridge & mach cone?

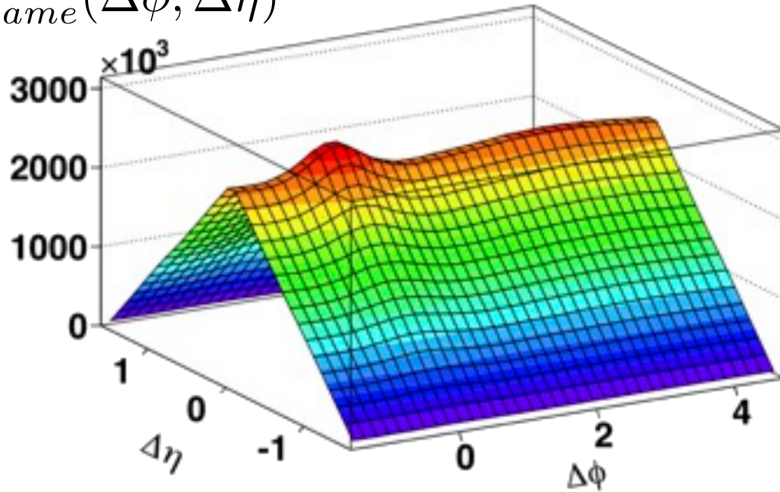
?

$$C(\phi_1 - \phi_2) \sim 1 + 2 \sum_{i=1} v_{n,1} v_{n,2} \cos(n[\phi_1 - \phi_2])$$

# Two particle azimuthal correlations

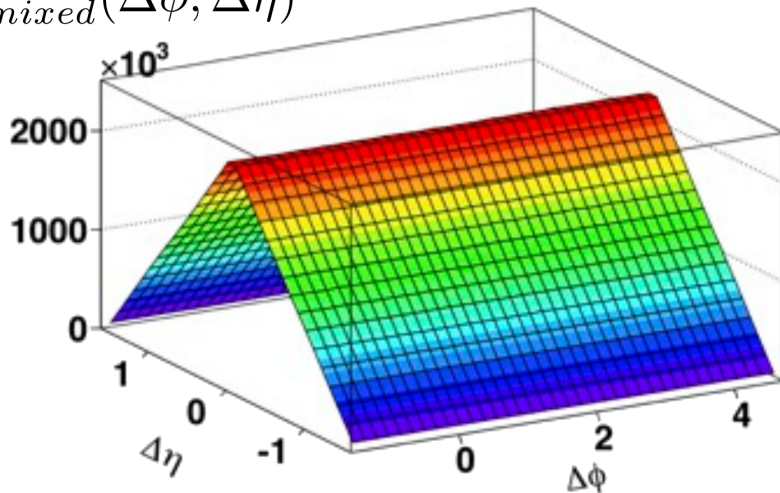
SameEv  $3.0 < p_{T,trig} < 4.0$   $2.0 < p_{T,assoc} < 3.0$  0-20%

$N_{same}^{AB}(\Delta\phi, \Delta\eta)$



MixBkg  $3.0 < p_{T,trig} < 4.0$   $2.0 < p_{T,assoc} < 3.0$  0-20%

$N_{mixed}^{AB}(\Delta\phi, \Delta\eta)$



2D-correlations:

$$\Delta\phi = \phi_A - \phi_B$$

$$\Delta\eta = \eta_A - \eta_B$$

Correlation function:

$$C(\Delta\phi) \equiv \frac{N_{mixed}^{AB}}{N_{same}^{AB}} \cdot \frac{dN_{same}^{AB}/d\Delta\phi}{dN_{mixed}^{AB}/d\Delta\phi}$$

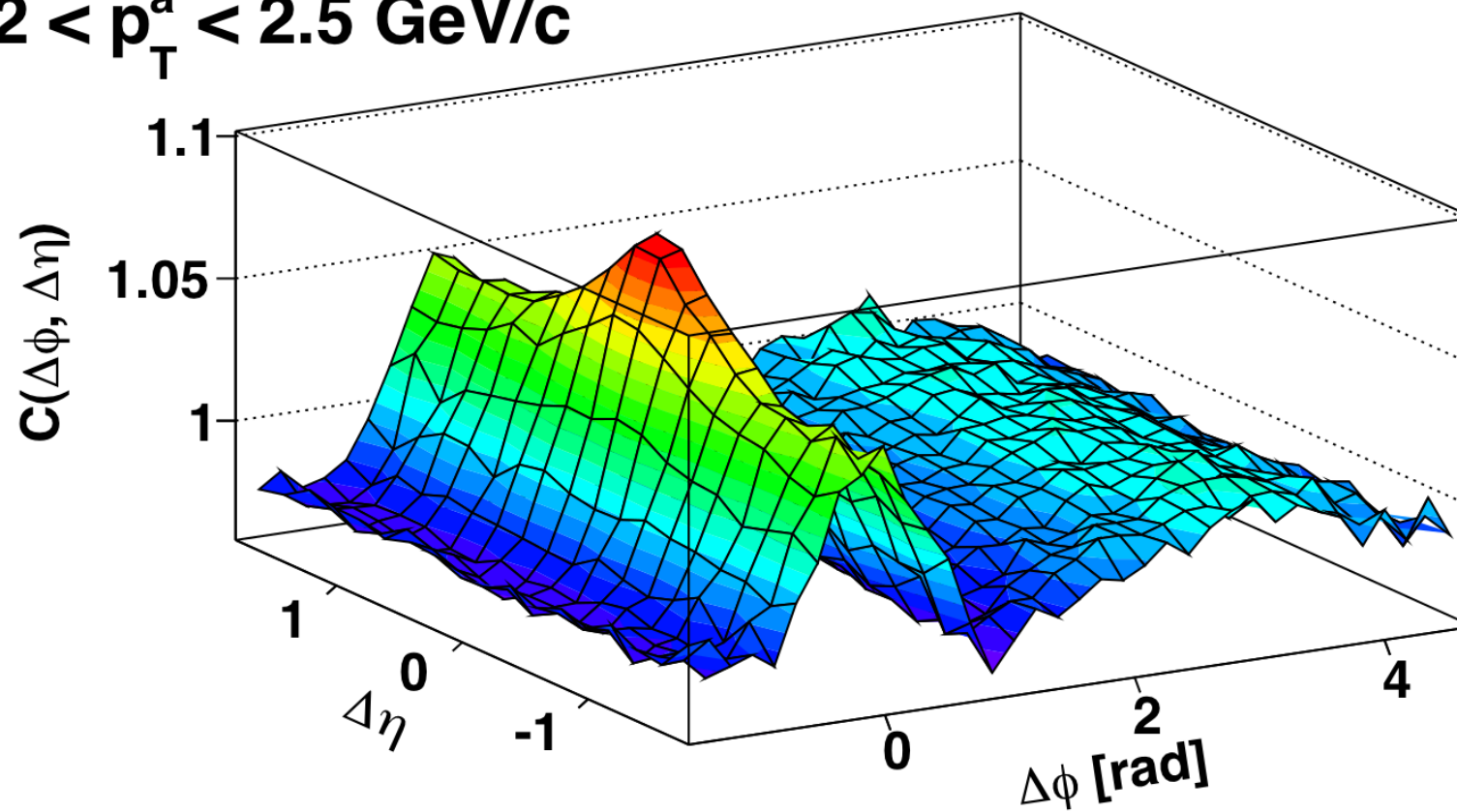
# Two particle azimuthal correlations

Correlations at small  $p_t$  (bulk particles)

$3 < p_T^t < 4 \text{ GeV/c}$

$2 < p_T^a < 2.5 \text{ GeV/c}$

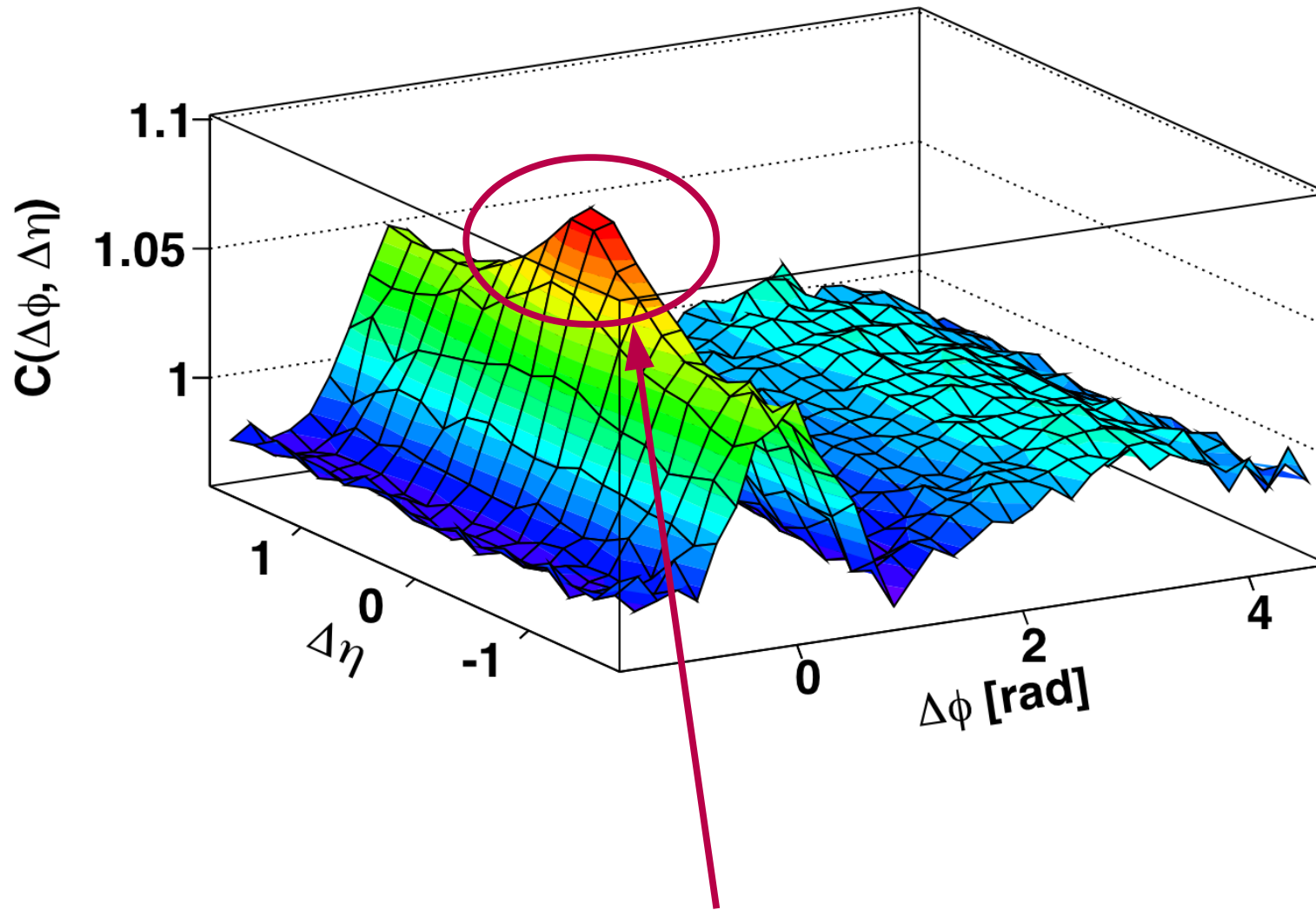
**Pb-Pb 2.76 TeV  
0-10%**



Non-trivial shape of the correlation function

# Anatomy of the two particle correlations

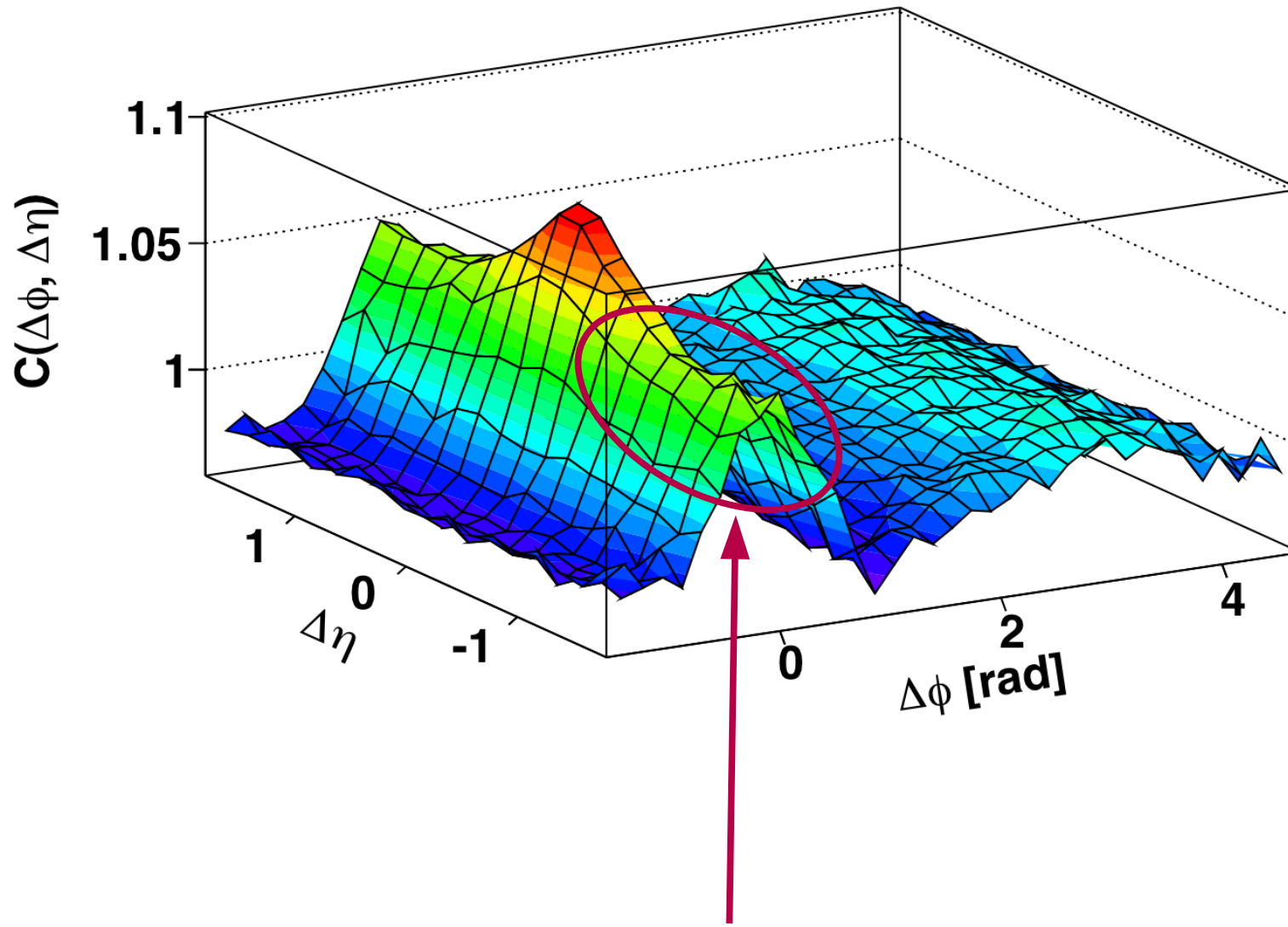
Correlations at small  $p_t$  (bulk particles)



Same side "jet" peak

# Anatomy of the two particle correlations

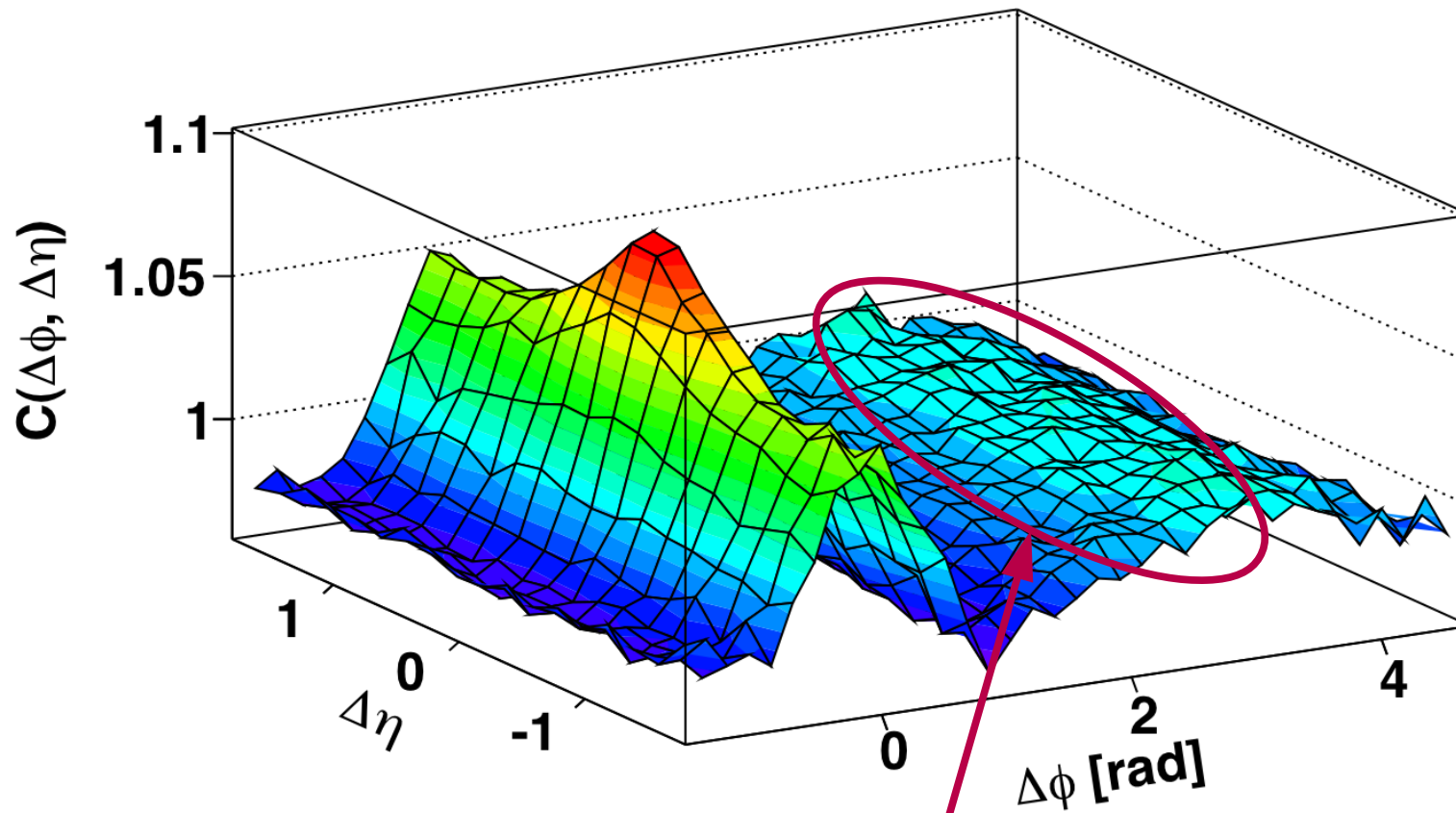
Correlations at small  $p_t$  (bulk particles)



“ridge” (extended in rapidity)

# Anatomy of the two particle correlations

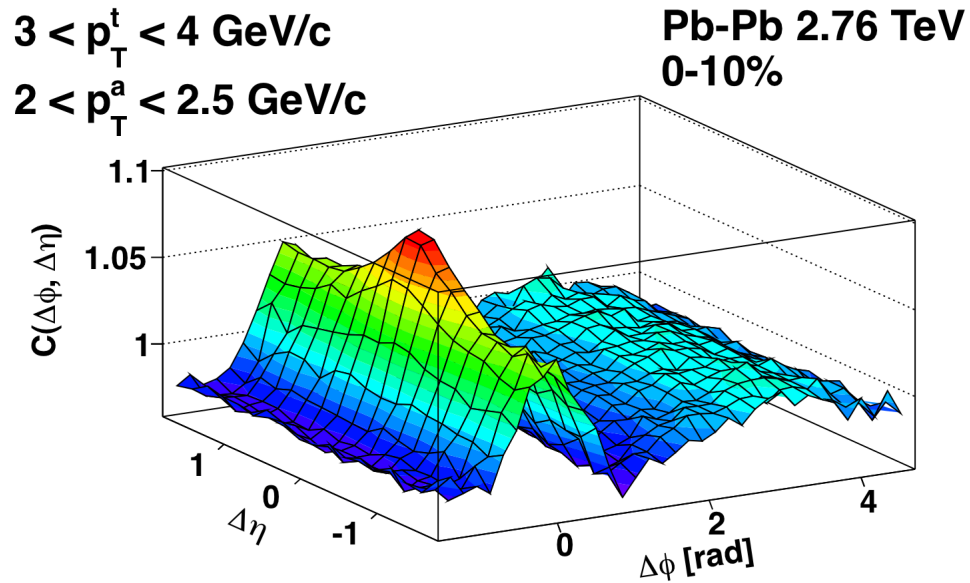
Correlations at small  $p_t$  (bulk particles)



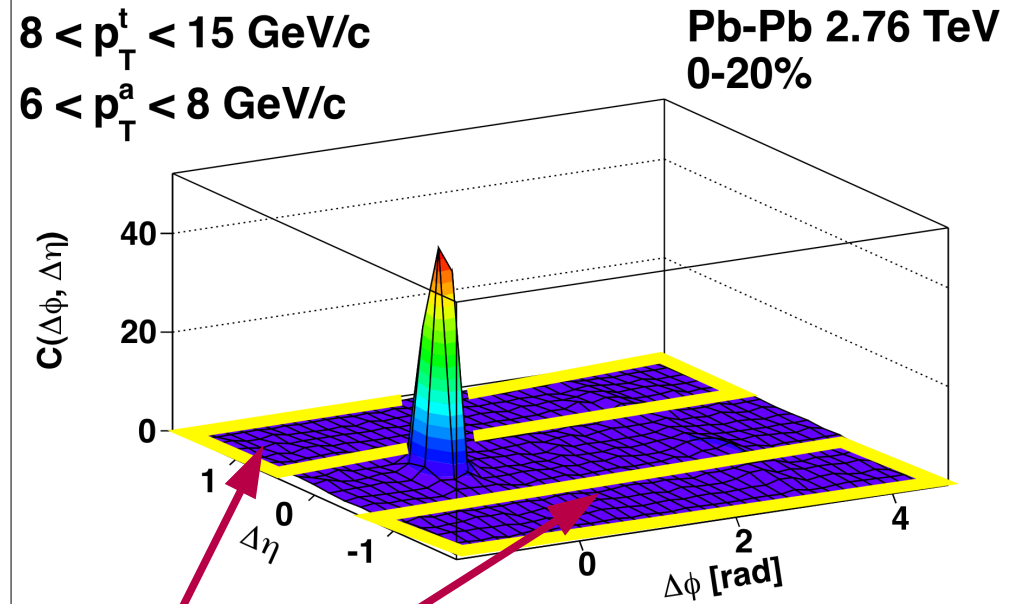
“Mach-cone” region  
(double hump structure on the away side region)

# Two particle azimuthal correlations: small and high $p_t$

## Correlations at small $p_t$ (bulk)

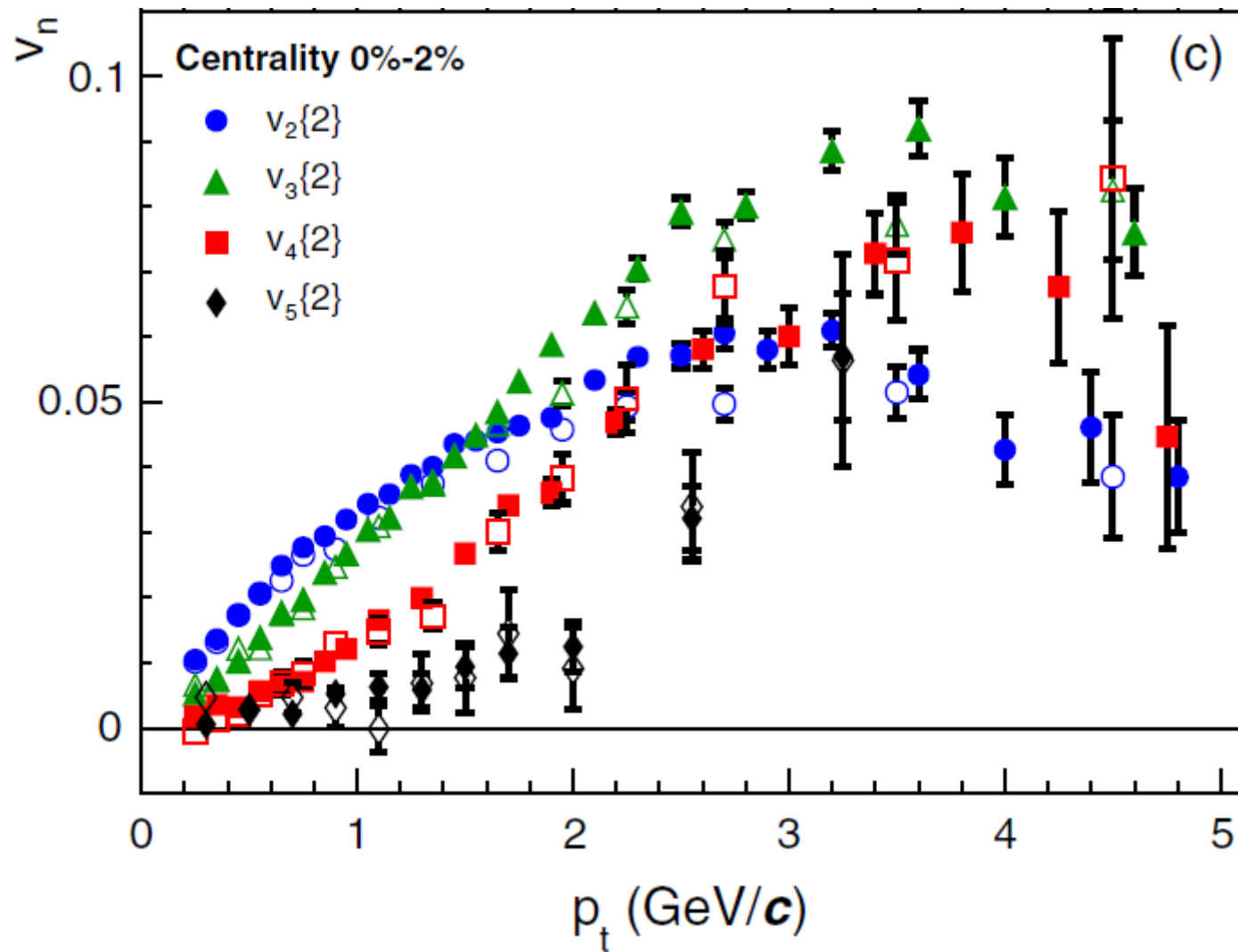


## Correlations at high $p_t$ (away side jet)



Lets study the azimuthal shape of  
the correlations outside of the jet peak  
in terms of collective modulations

# Higher harmonics for very central collisions



At  $p_t \sim 1.5$  GeV  $v_3$  become larger  $v_2$

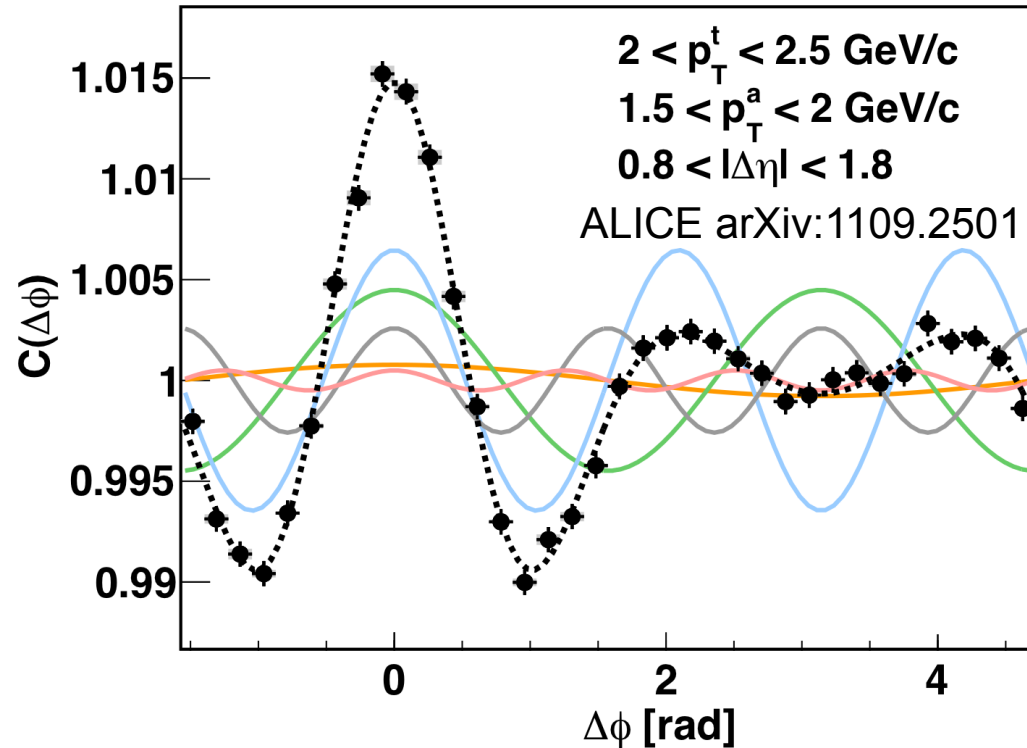


# Two particle correlations and higher harmonic flow

Azimuthal correlations are studied with large rapidity gap:  $0.8 < |\Delta\eta| < 1.8$

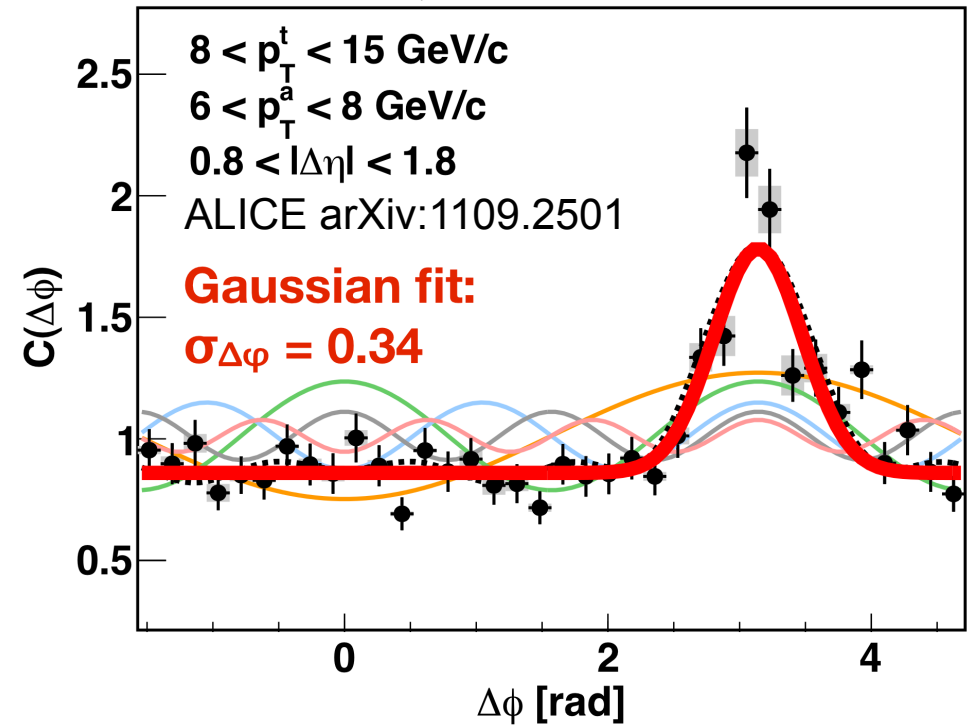
Correlations at small  $p_t$  (bulk)

Pb-Pb 2.76 TeV, 0-2% central



Correlations at high  $p_t$  (away side jet)

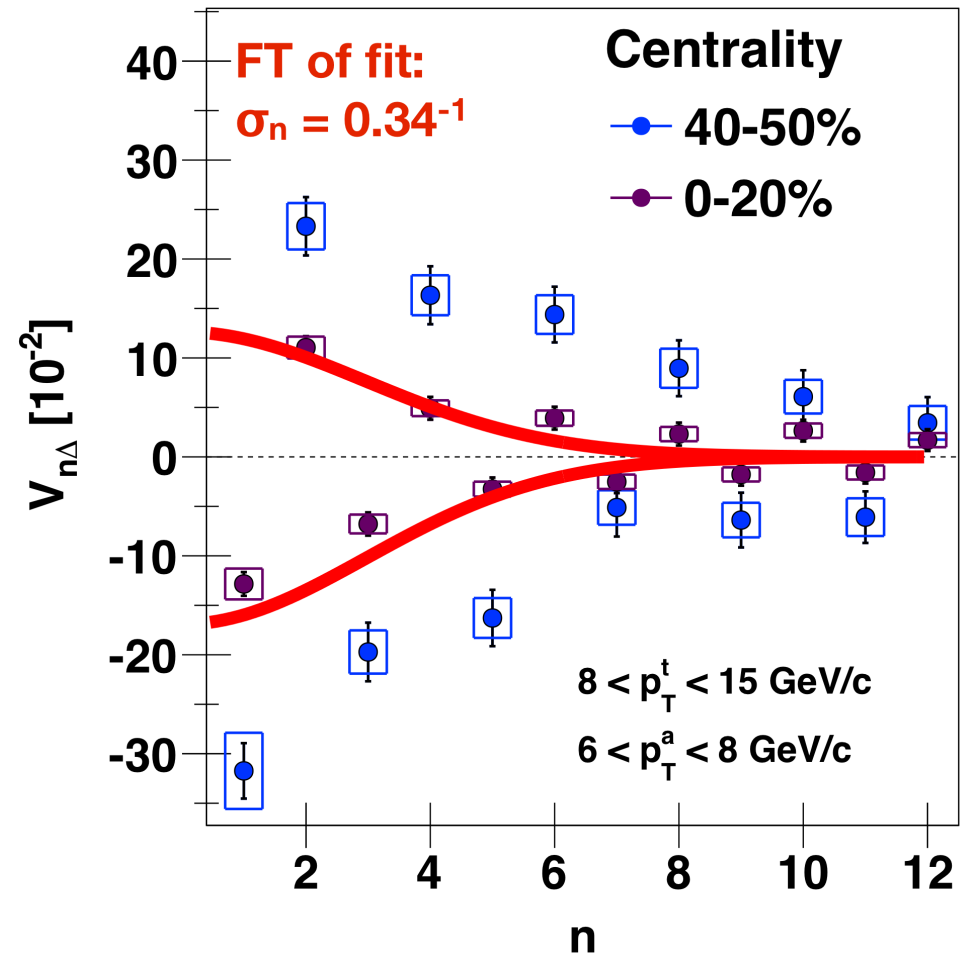
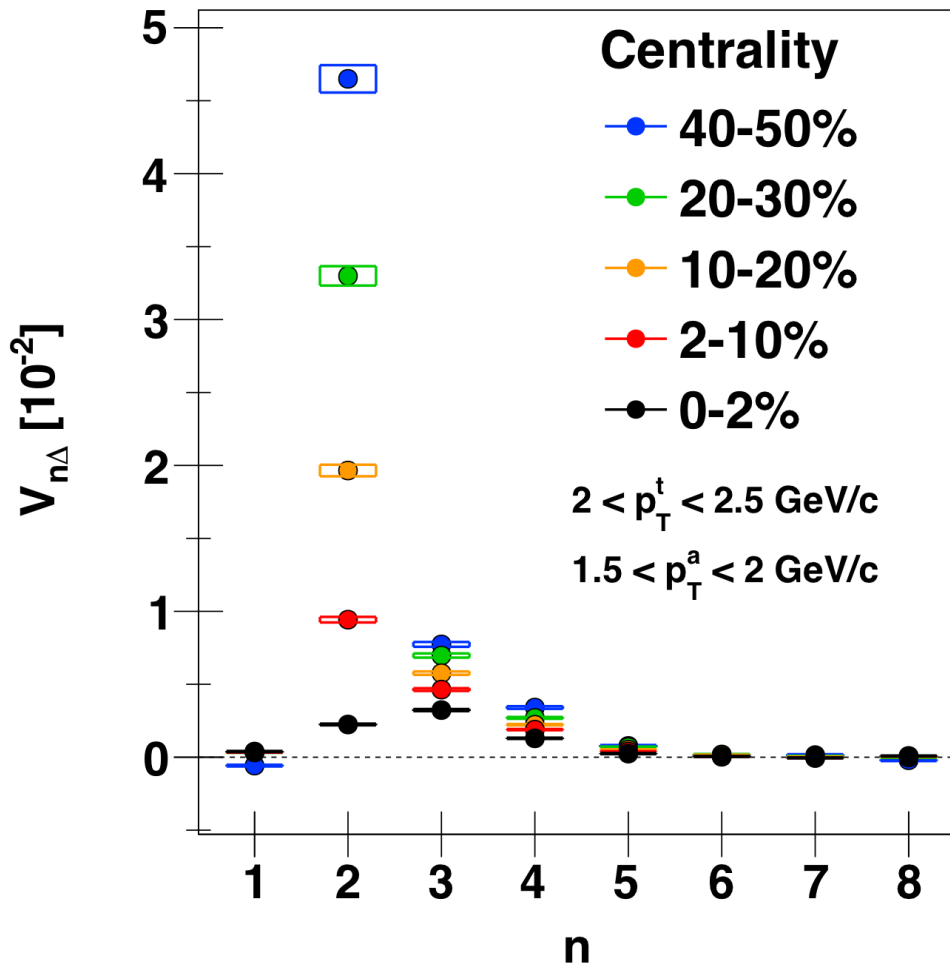
Pb-Pb 2.76 TeV, 0-20% central



“ridge” and “mach-cone” like structures are naturally described by the collective flow effects

# Power spectrum from two particle correlations

$$C(\phi_1 - \phi_2) \sim 1 + 2 \sum_{i=1} V_n \cos(n[\phi_1 - \phi_2])$$



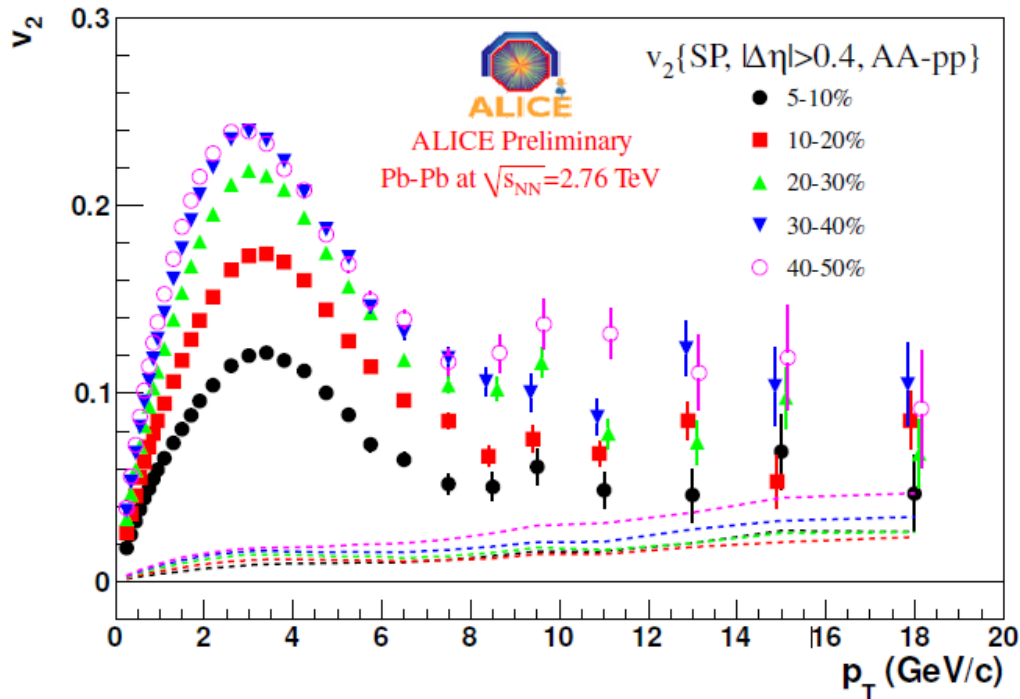
# Anisotropic flow: summary

- Anisotropic transverse flow is an important experimental observable to study the evolution of a heavy-ion collision and understand the properties of the quark-gluon plasma (QGP).
- It provides constraints on:
  - ✓ Equation of state of the created matter
  - ✓ Transport properties (i.e. viscosity) of the QGP matter
  - ✓ Shape of the initial conditions in a heavy-ion collision
- Helps to understand the origin of the correlations between produced particles
- Path length dependence of the parton energy loss (flow at high transverse momenta)

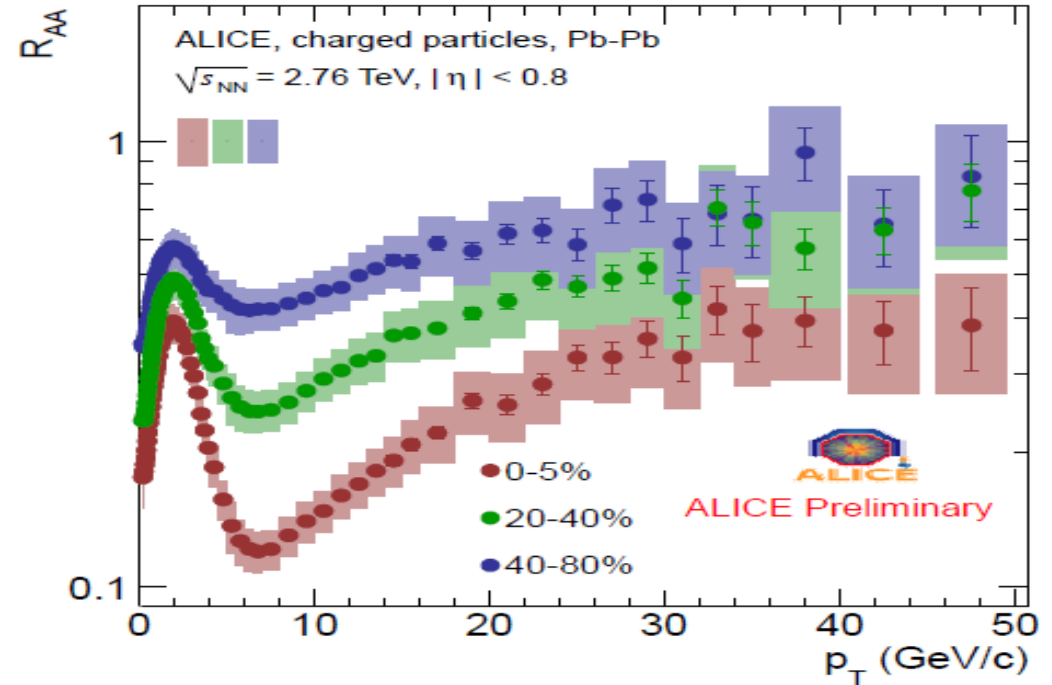
# Backup

# Elliptic flow at high $p_t$

## Elliptic flow, $v_2$

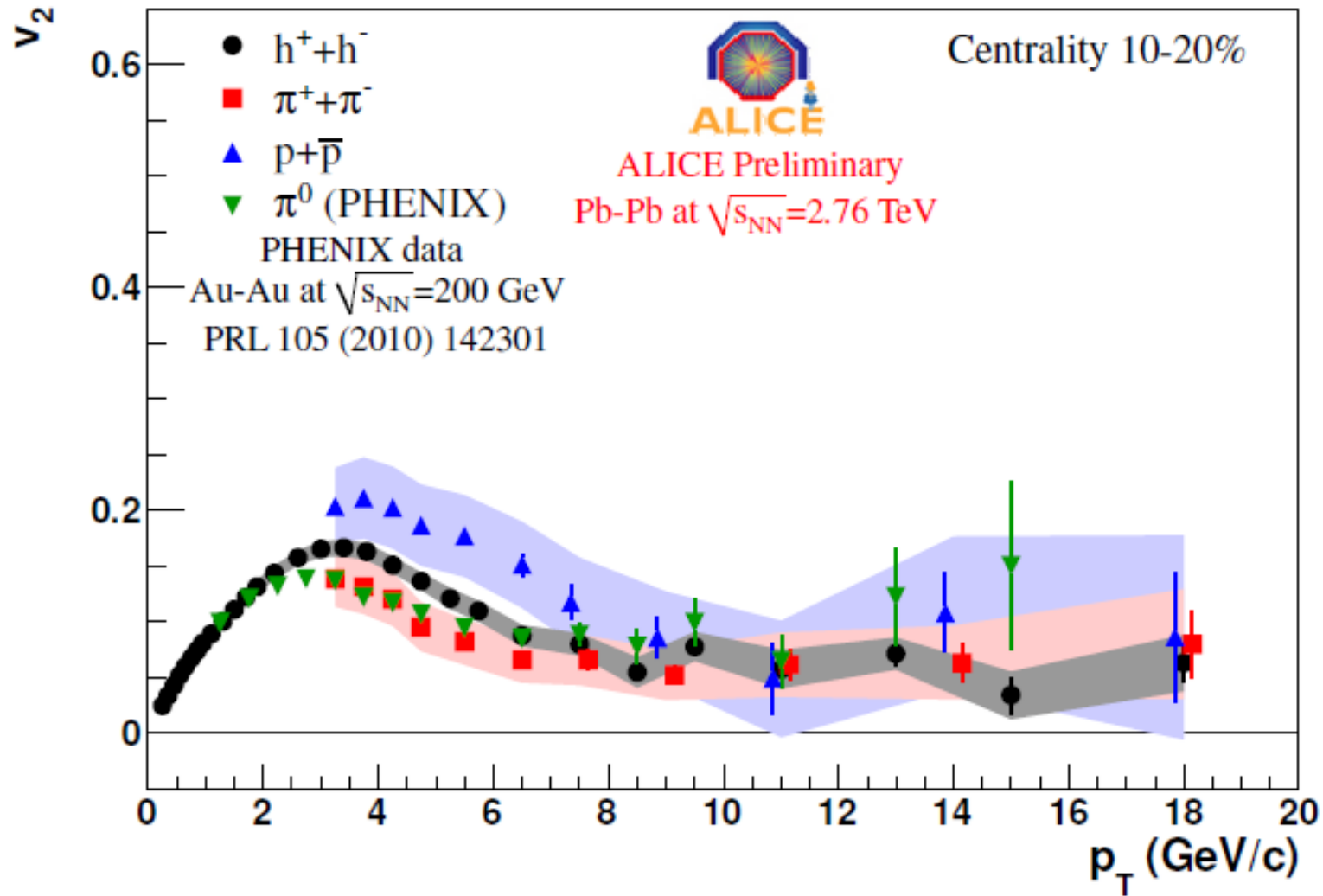


## Nuclear modification factor, $R_{AA}$



- Non-zero elliptic flow at large transverse momenta  $p_t > 8$  GeV
- Centrality dependence is consistent with suppression measure via nuclear modification factor  $R_{AA}$

# Identified particle $v_2$ at high $p_t$

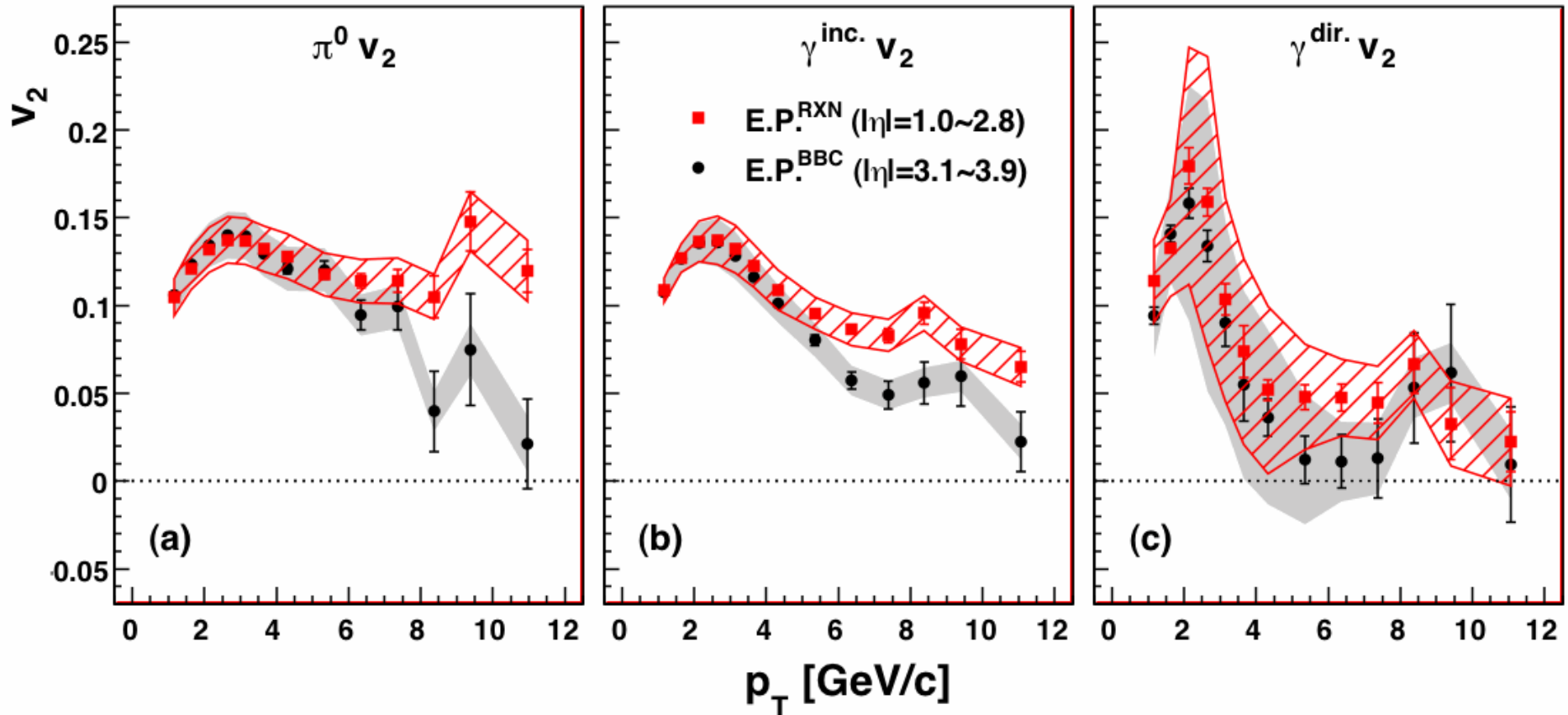


Bulk:  
described by hydro

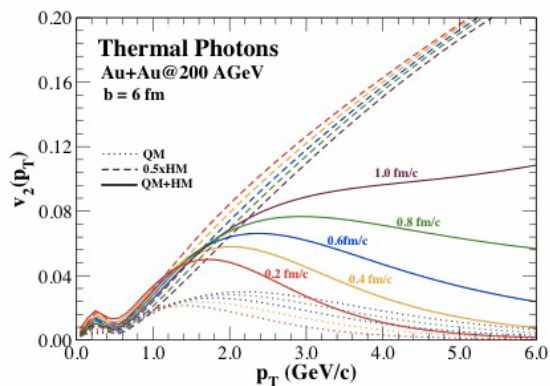
Coalescence:  
breaks at  $p_t \sim 8\text{GeV}$

High  $p_t$ :  
jet quenching

# Direct photon $v_2$



Chatterjee, Srivastava  
PRC79, 021901 (2009)

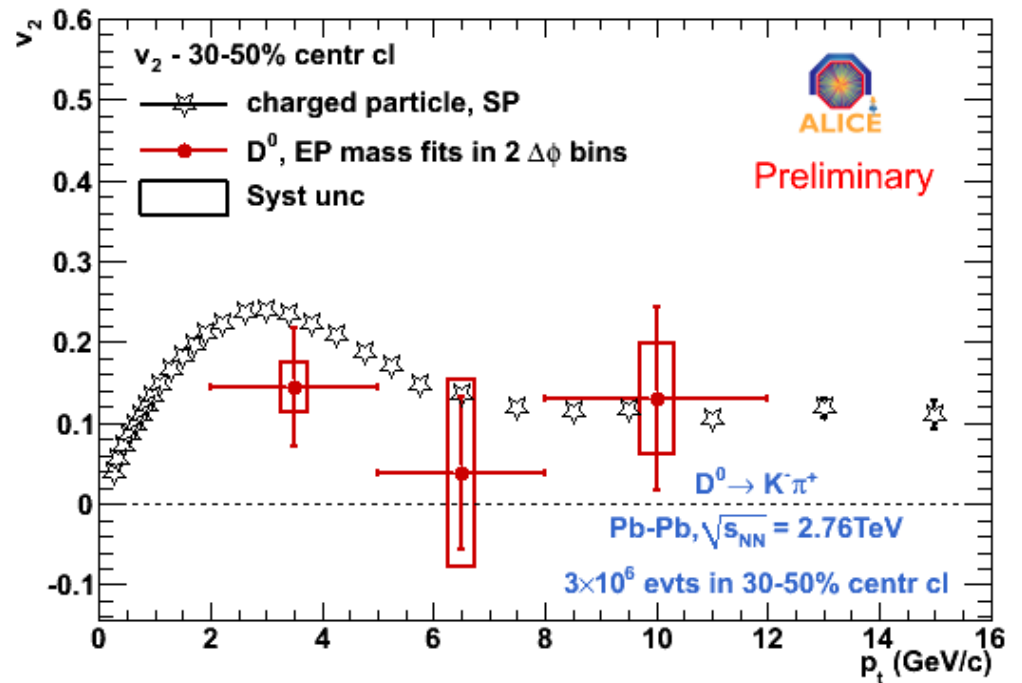
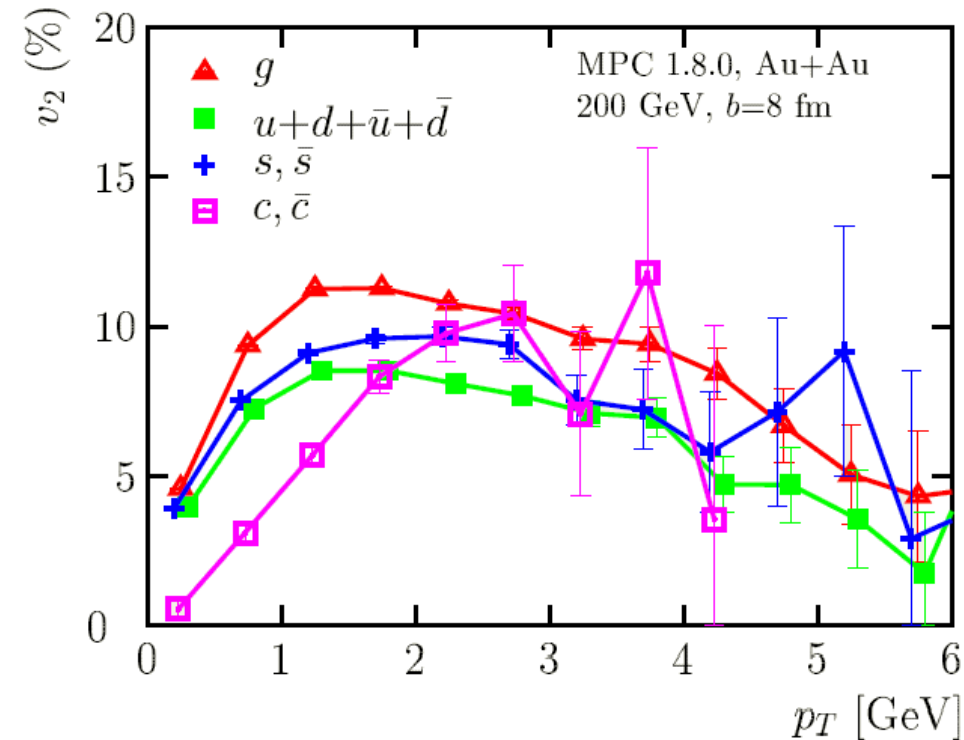


significant difference between  $\pi^0$  and  $\gamma^{\text{inc.}} v_2$  above 5 GeV/c

surprisingly large  $\gamma^{\text{dir.}} v_2$  is seen, similar to hadron  $v_2$  at low  $p_T$

$\gamma^{\text{dir.}} v_2$  is small at high  $p_T$ , consistent with prompt photon

# $v_2$ of heavy quarks (charm from $D^0 \rightarrow K^+\pi^-$ )



- Charm quark  $v_2$  predicted to be smaller than flow of light quarks at small transverse momentum
- No particle type dependence at high  $p_t$

Within large statistical errors, the flow of  $D^0$  is consistent with that of charged particles