

Key Uncertainties in Astrophysical r-Process Nucleosynthesis

Kelsey Lund

19 October 2022

In collaboration with G. McLaughlin, Y. Zhu, J. Barnes and many others

Disclaimer

This Document cleared for unlimited release with LA-UR-22-30999

The submitted materials have been authored by an employee or employees of Triad National Security, LLC (Triad) under contract with the U.S. Department of Energy/National Nuclear Security Administration (DOE/NNSA). Accordingly, the U.S. Government retains an irrevocable, nonexclusive, royalty-free license to publish, translate, reproduce, use, or dispose of the published form of the work and to authorize others to do the same for U.S. Government purposes."

Scope

Nucleosynthesis
calculations

probe

Uncertainties from
unknown nuclear
properties of nuclei
far from stability

on

Abundance patterns

Nuclear energy generation

Light curve evolution

Sources of Nuclear Uncertainty

See also, e.g.

Mumpower+ 2016

Vassh+ 2019

Giuliani+ 2020

Nikas+ 2020

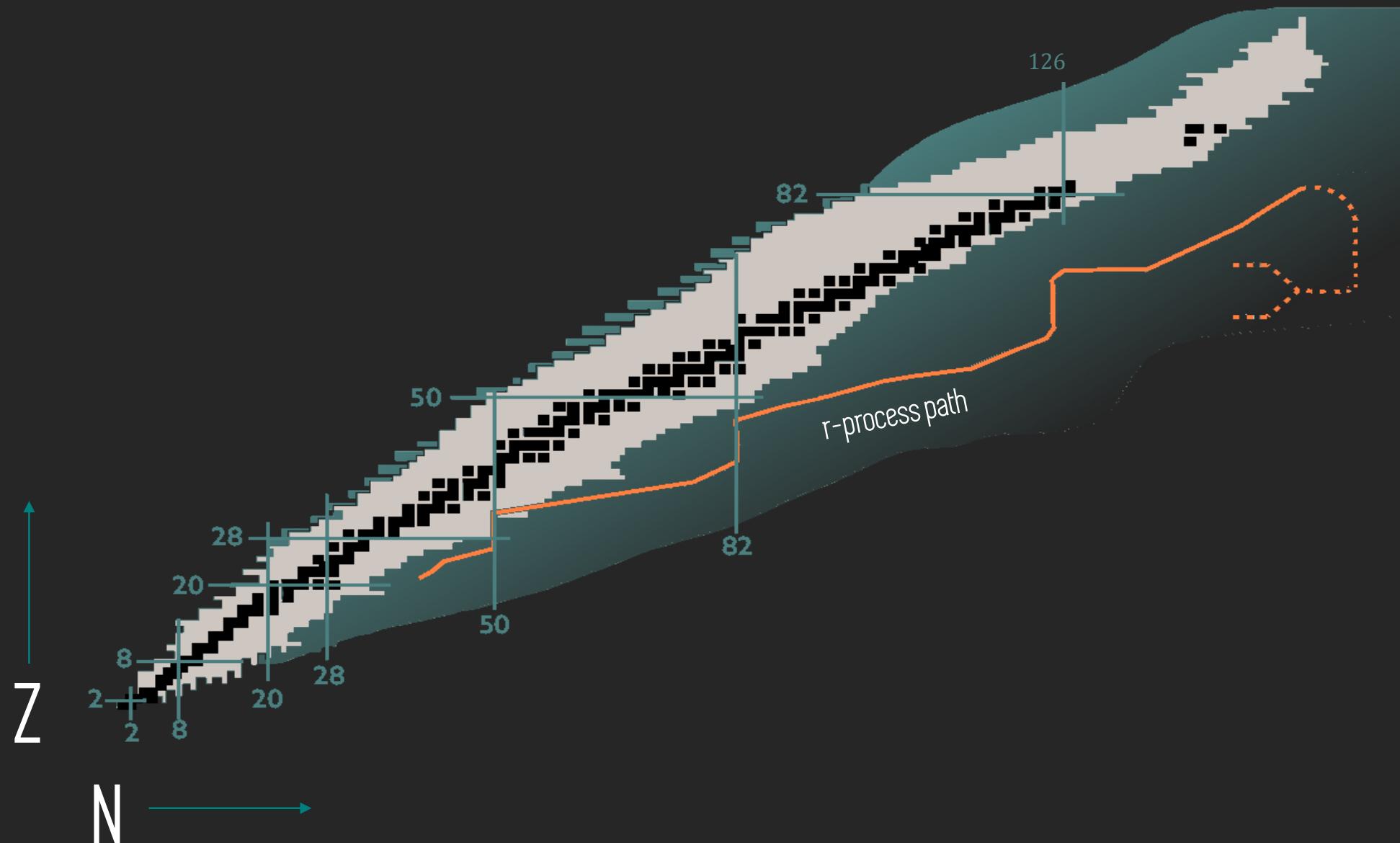
Wang+ 2020

Zhu+ 2021

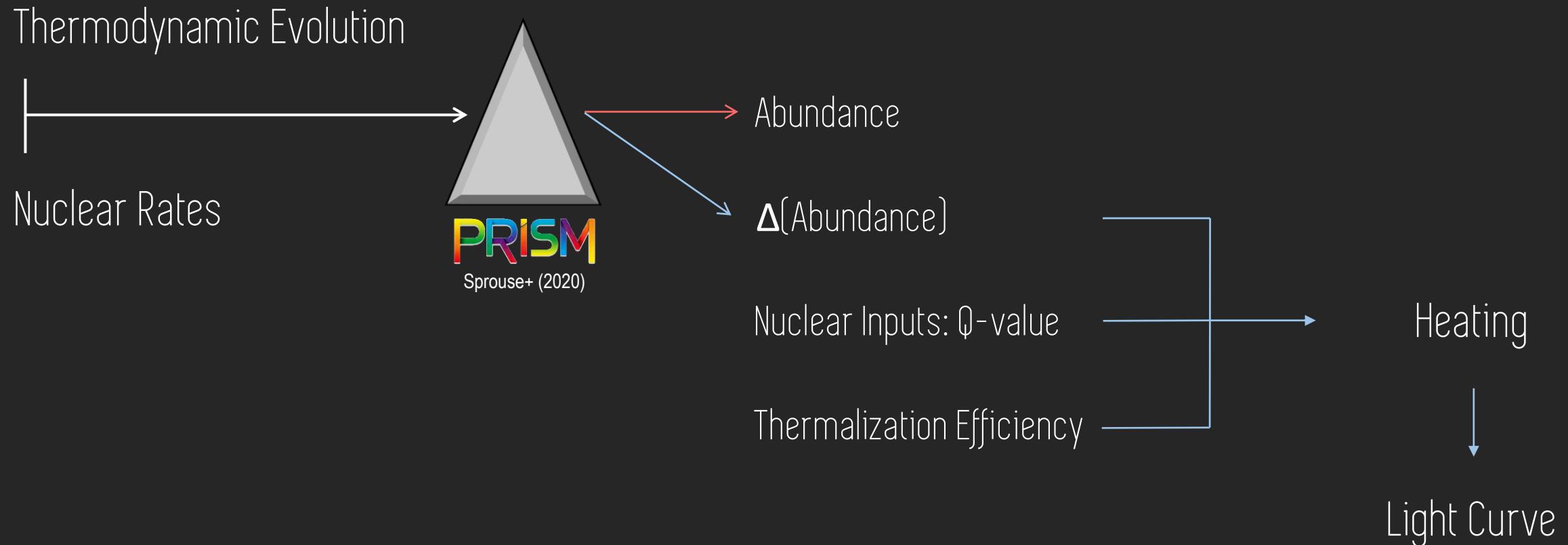
Barnes+ 2021

Kullmann+ 2022

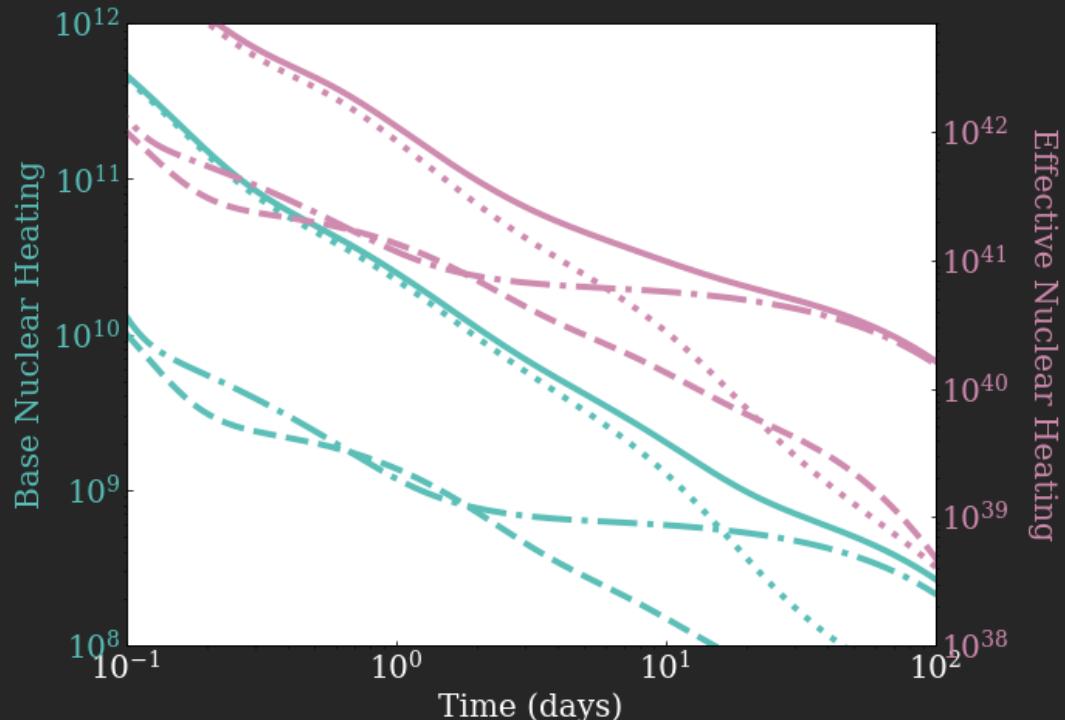
and many others



PRISM: A Sparse Matrix Solver



Nuclear Heating



$$\dot{Q}(t) = \sum_i f_i(M_{ej}, v_{ej}, t) \dot{q}_i(t) M_{ej}$$

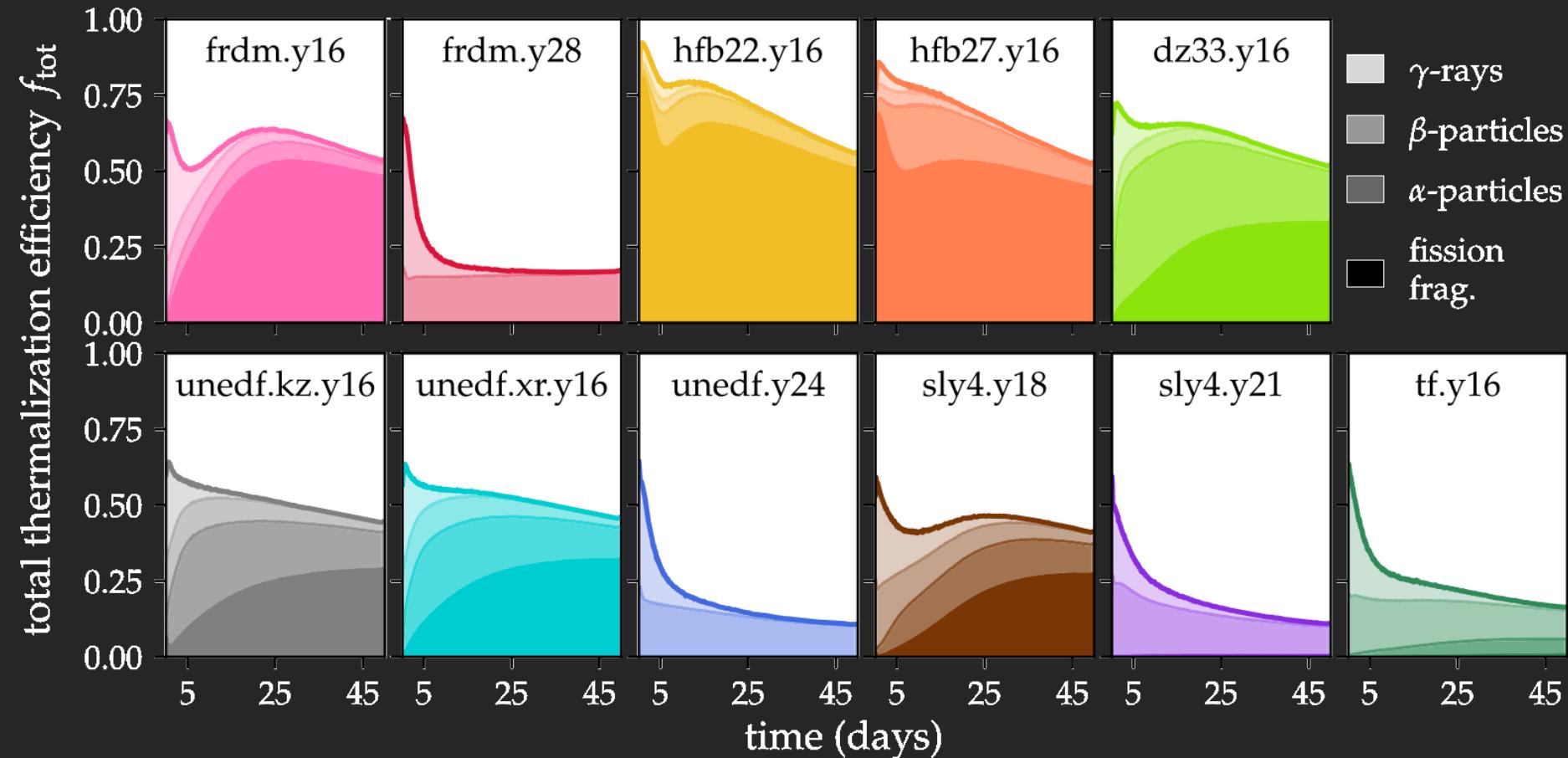
Total effective heating Thermalization efficiency Nuclear Heating Ejecta mass

Thermalization efficiency: how effectively decay products can heat ejecta (function of time, ejecta mass, and characteristic velocity)

Thermalization based on Kasen & Barnes (2019)

Nuclear Heating

See Barnes+ 2021



Light Curve Shell Model

Shell model for ejecta: the mass of each shell, M_v , depends on the velocity, v , of that shell (100 shells evenly distributed between 0.1c and 0.4c)

Time evolution of the energy of a shell:

$$\frac{dE_v}{dt} = \frac{M_v}{M_{ej}} \dot{Q}(t, v) - \frac{E_v}{t} - \frac{E_v}{t_{d,v} + t_{lc,v}}$$

Luminosity

Effective heating

Adiabatic expansion

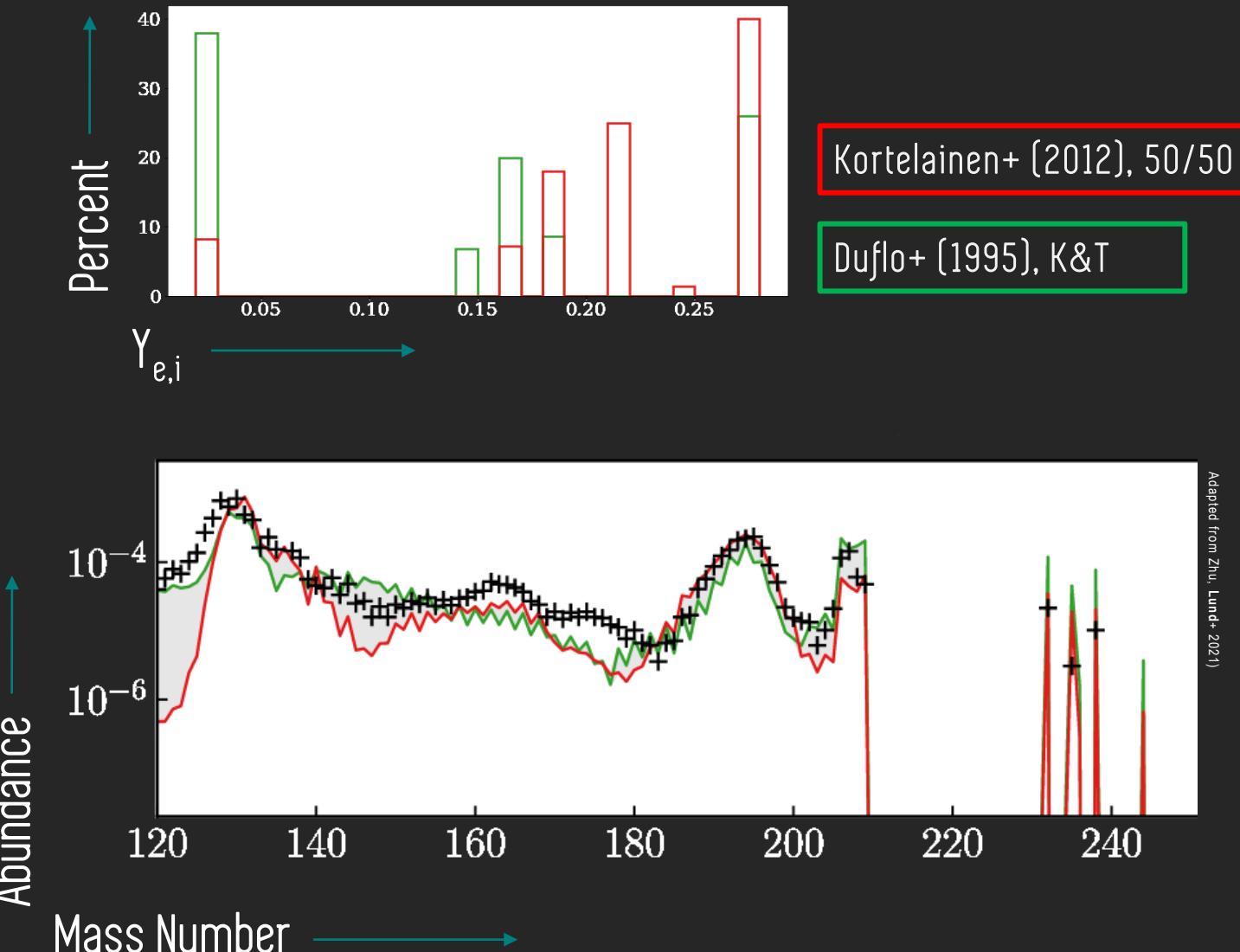
Diffusion timescale
(depends on opacity)

Light-crossing
timescale

Combined Trajectories



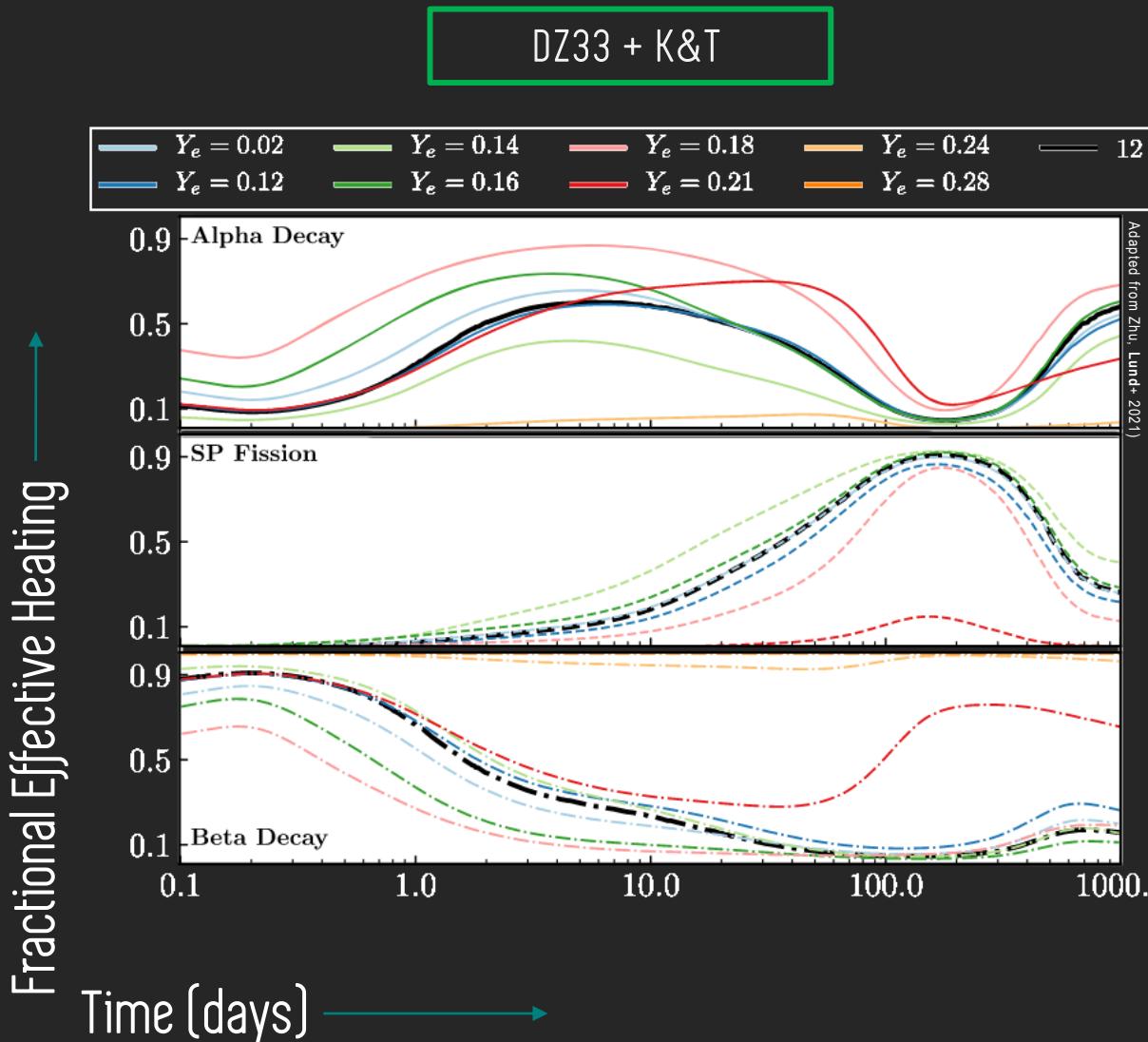
Finding a Linear Combination



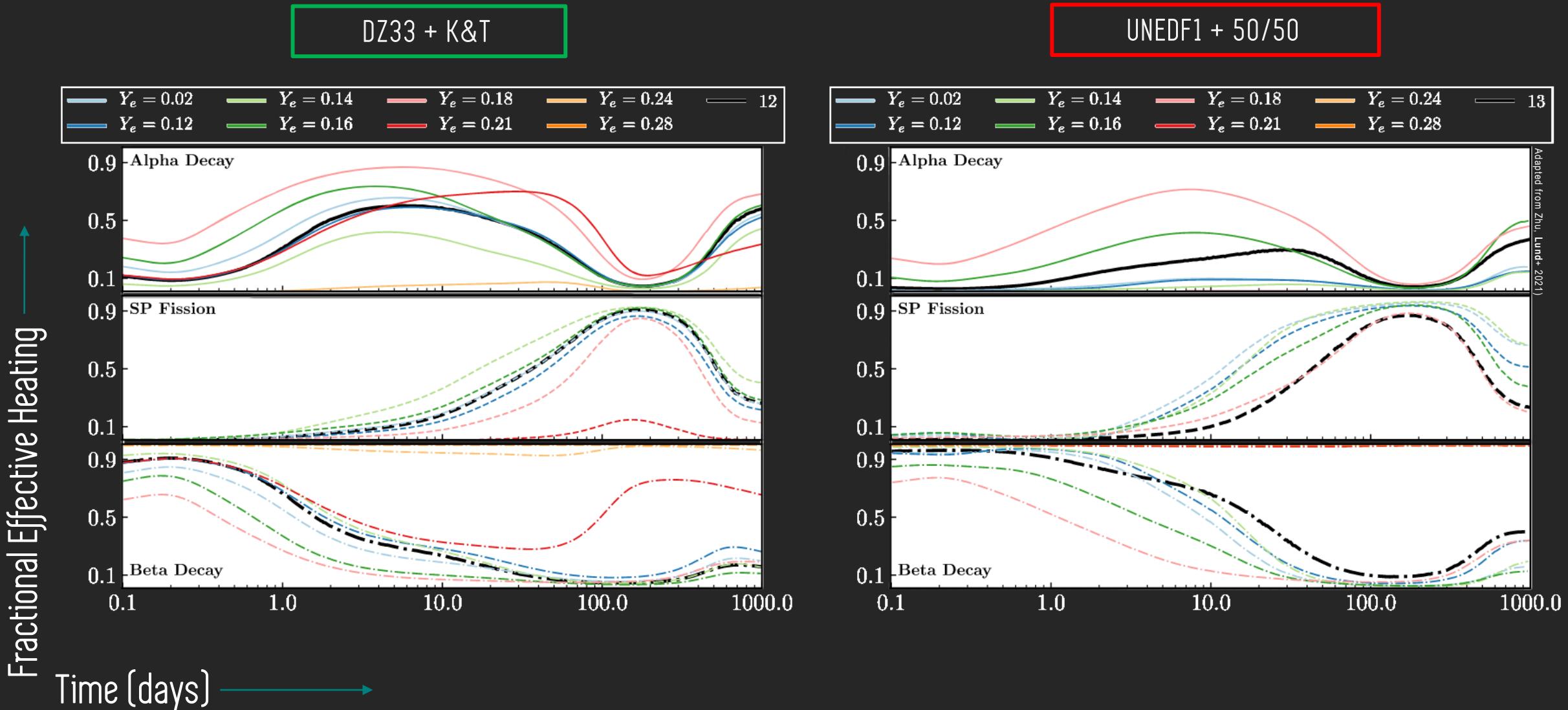
Linear combination to fit to solar abundance pattern.

- Select from single- Y_e trajectories [0.02-0.28]
- Necessary to combine low *and* high Y_e material

Fractional Nuclear Heating



Fractional Nuclear Heating



Single-Ye Trajectories



Astrophysical Uncertainty: Initial Y_e

Single Trajectory:

0.02

Large potential
for fission cycling

0.18

Interesting
reaction
competition

0.21

r-Process but
minimal fission

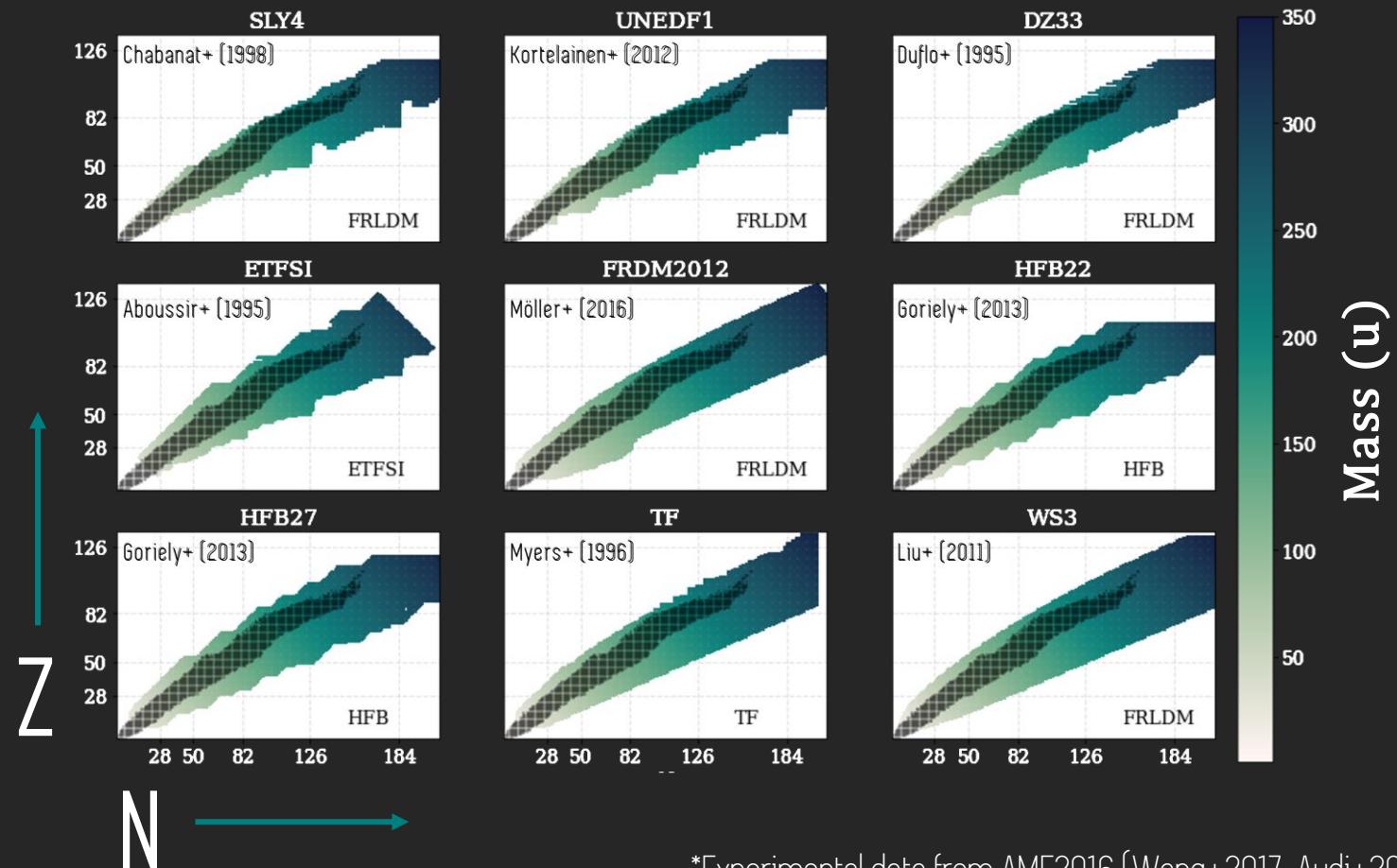
More neutron rich

Less fission

Nuclear Uncertainty: Mass Model

Most basic nuclear property:
 mass

Each mass model associated
 with fission barrier height
 model



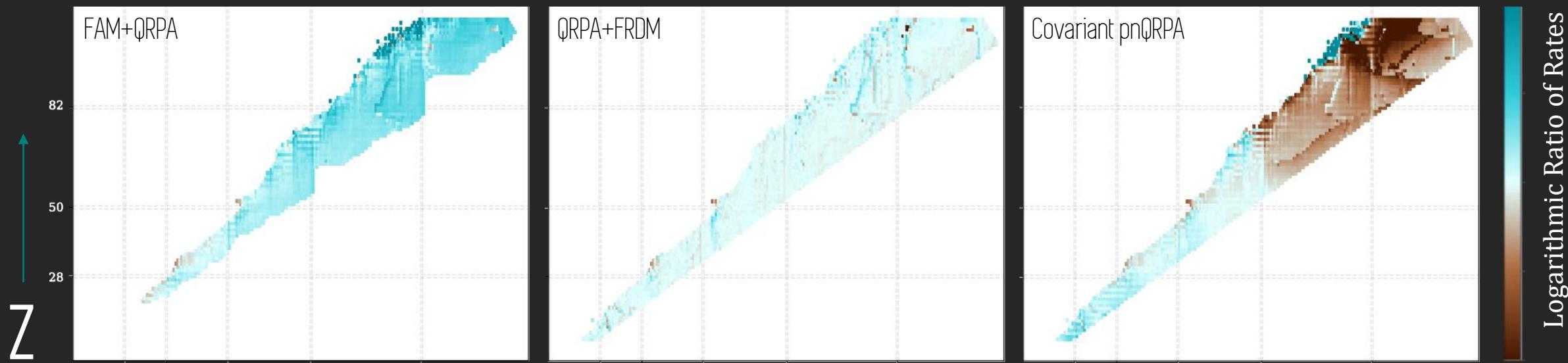
*Experimental data from AME2016 (Wang+2017, Audi+2017)

Effect of nuclear mass: Mendoza-Temis+2015, Mumpower+2015, 2016, Barnes+2016, Wu+2019, Nikas+2020, Zhu+2021, Barnes+2021, Kullmann+2022

Nuclear Uncertainty: Beta Decay Rates

← ~ slower rate*

Logarithmic ratio compared to Möller+ 2003



Z

N

Ney (NES)

Ney+ 2020

Möller (MLR)

Möller+ 2019

Marketin (MKT)

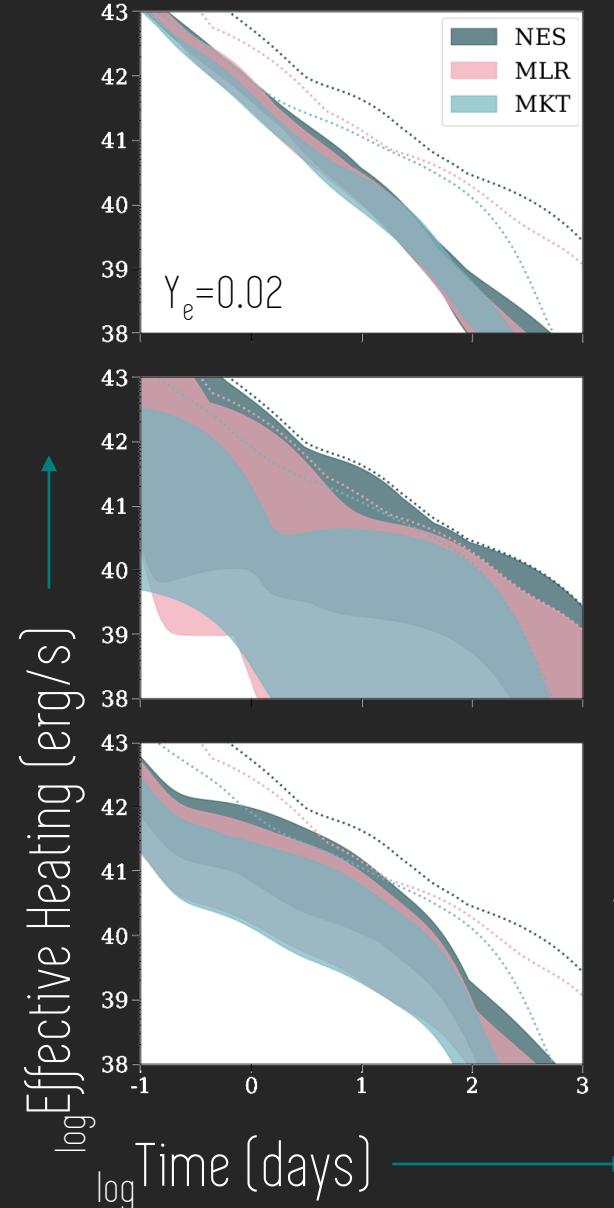
Marketin+ 2016

Effect of beta decay rates: Marketin+ 2016, Nikas+ 2020, Kullmann+ 2022

Nuclear Heating

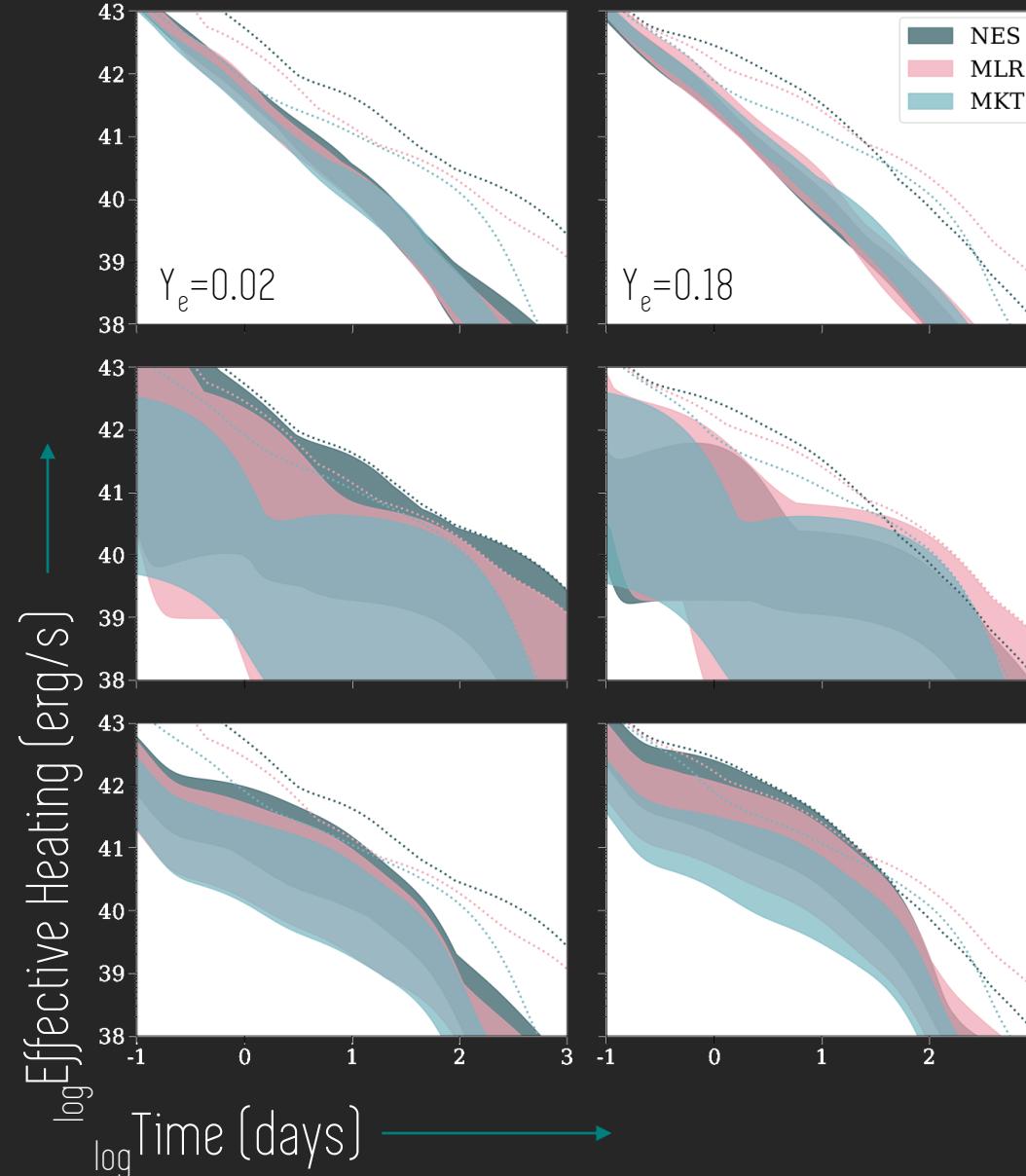


Nuclear Heating by Reaction Type



- Upper limit of heating uncertainty can be set by fission
- Beta models differ in behavior of dominating fission heating

Nuclear Heating by Reaction Type



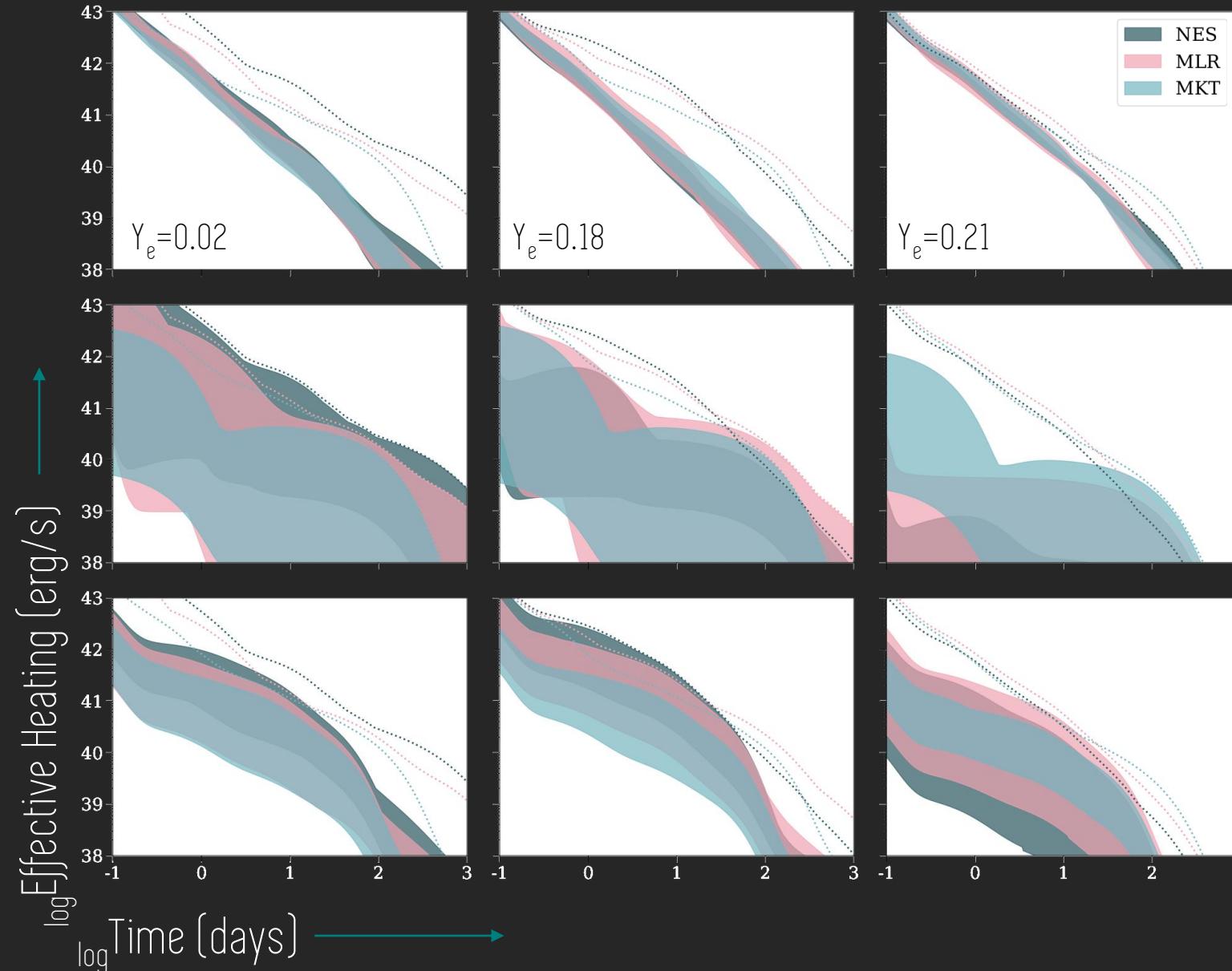
Beta Decay

Spontaneous
Fission

Alpha
Decay

- Alpha heating becomes more important 10-100 days
- Beta models differ in predicting when alpha tends to dominate heating+ late-time tail shape of fission

Nuclear Heating by Reaction Type



Beta Decay

- Much more overlap, total heating tends to be set by beta, then alpha decay

Sp. Fission

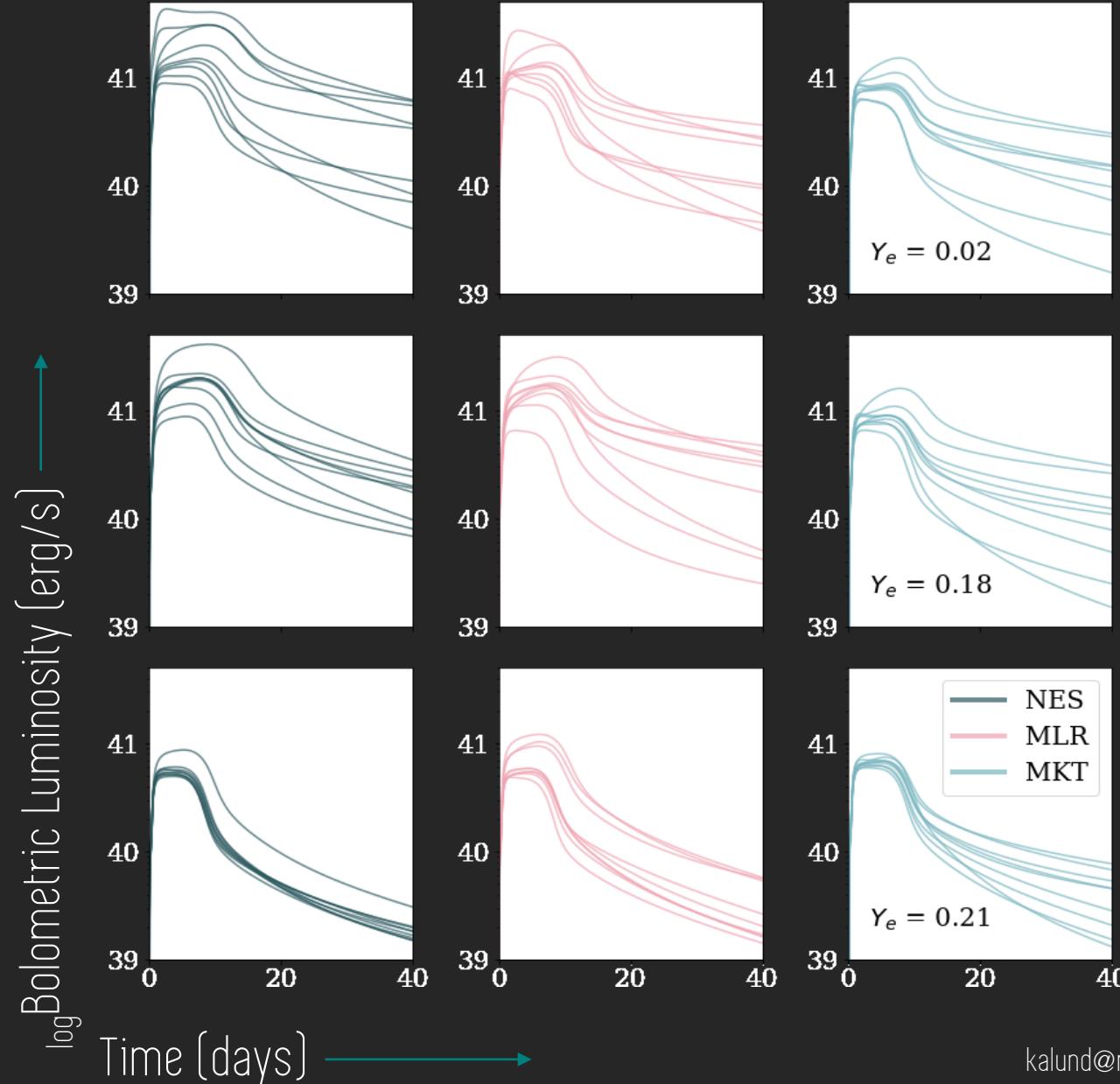
- Overall effect on beta decay heating is small

Alpha Decay

Light Curve



Light Curves



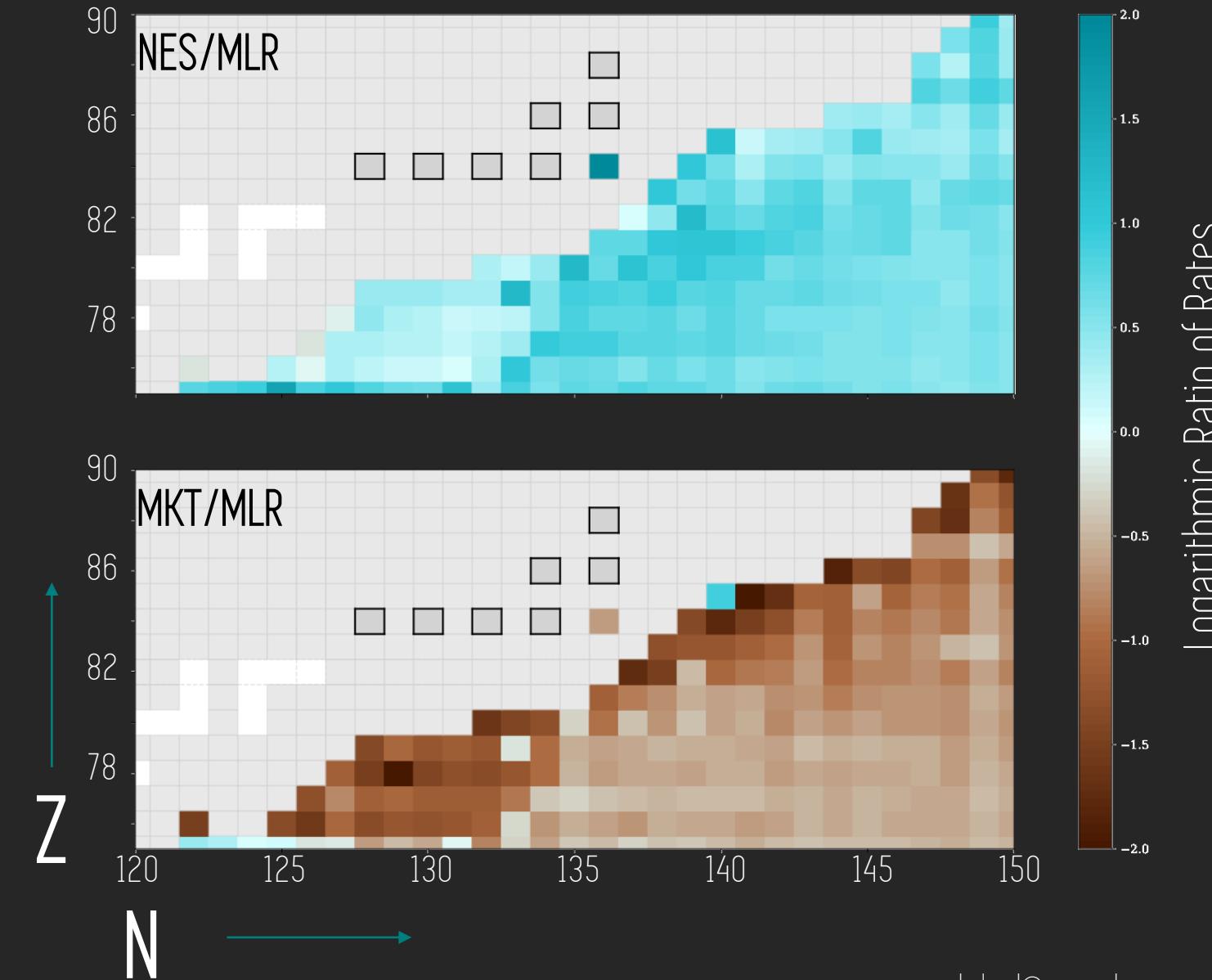
Diversity in heating sources changes shape of light curves

Generally slower rates (NES) yield more heating and brighter light curves

Nuclear Heating (revisited)



Alpha Decay Heating

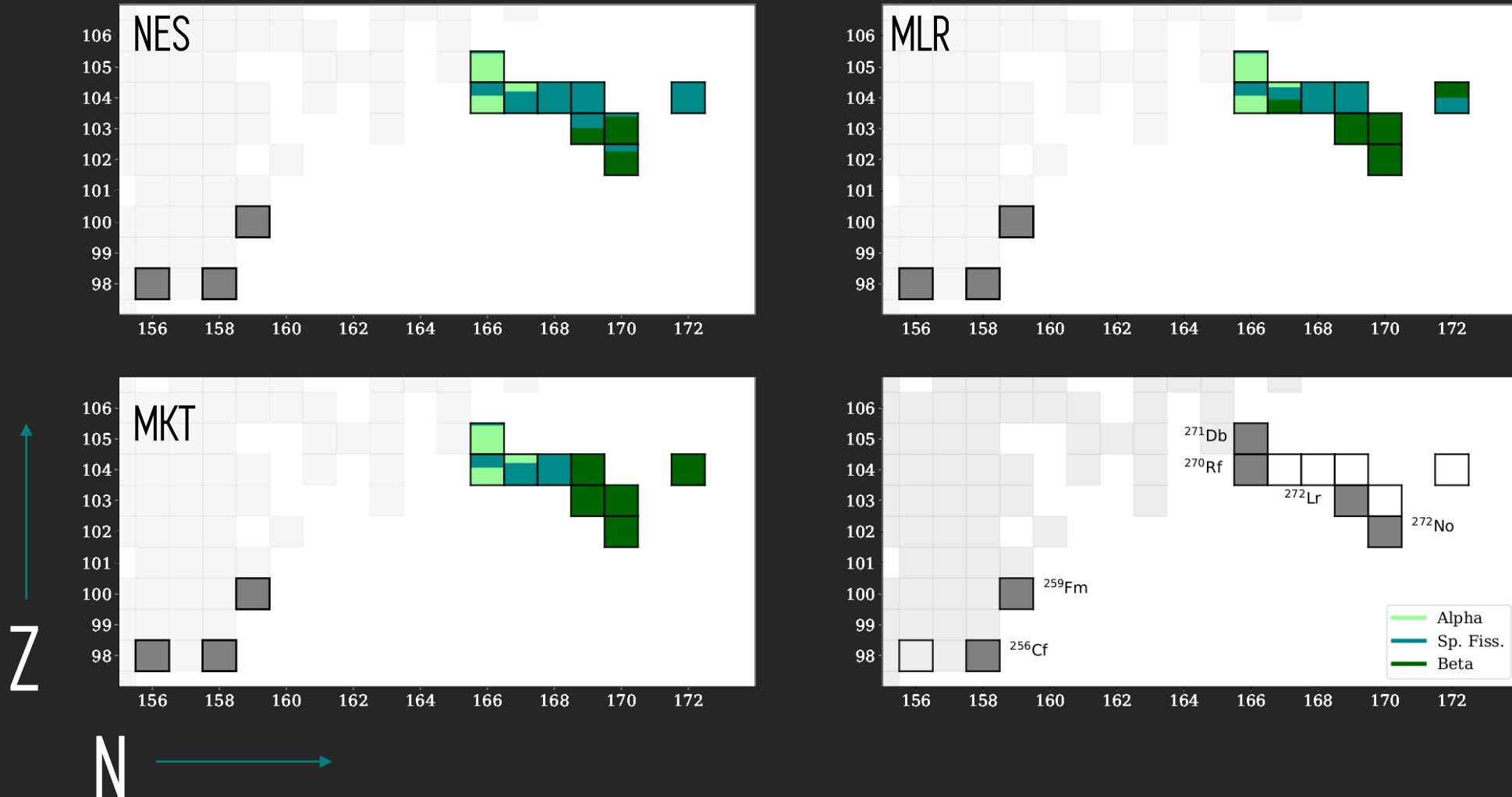


Differences in beta decay rates affect heating from alpha heaters with measured decay times, especially:



Spontaneous Fission (et al.) Heating

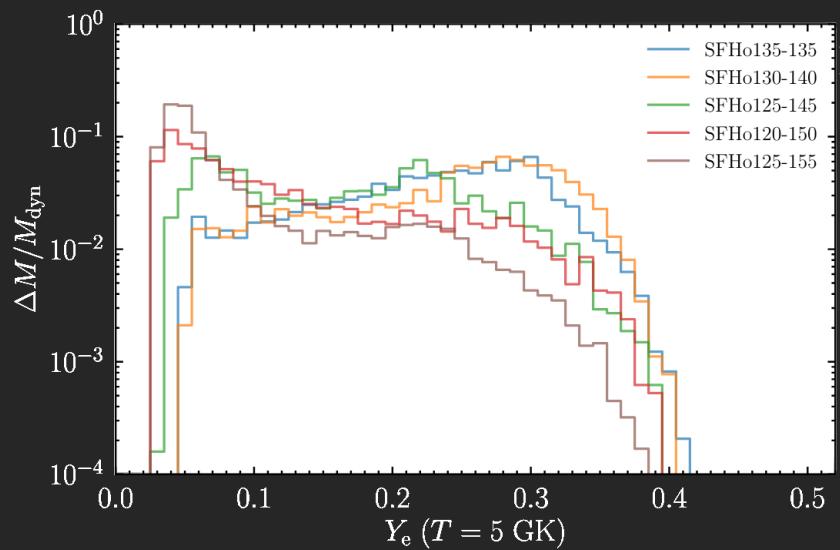
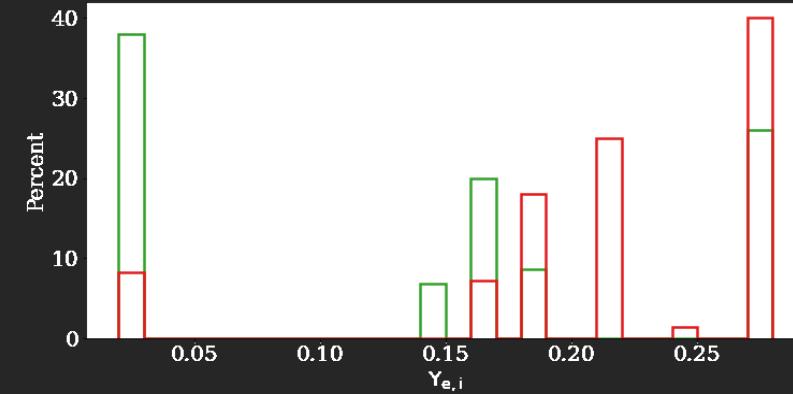
Theoretical
branching ratios
affect
spontaneous
fission heating



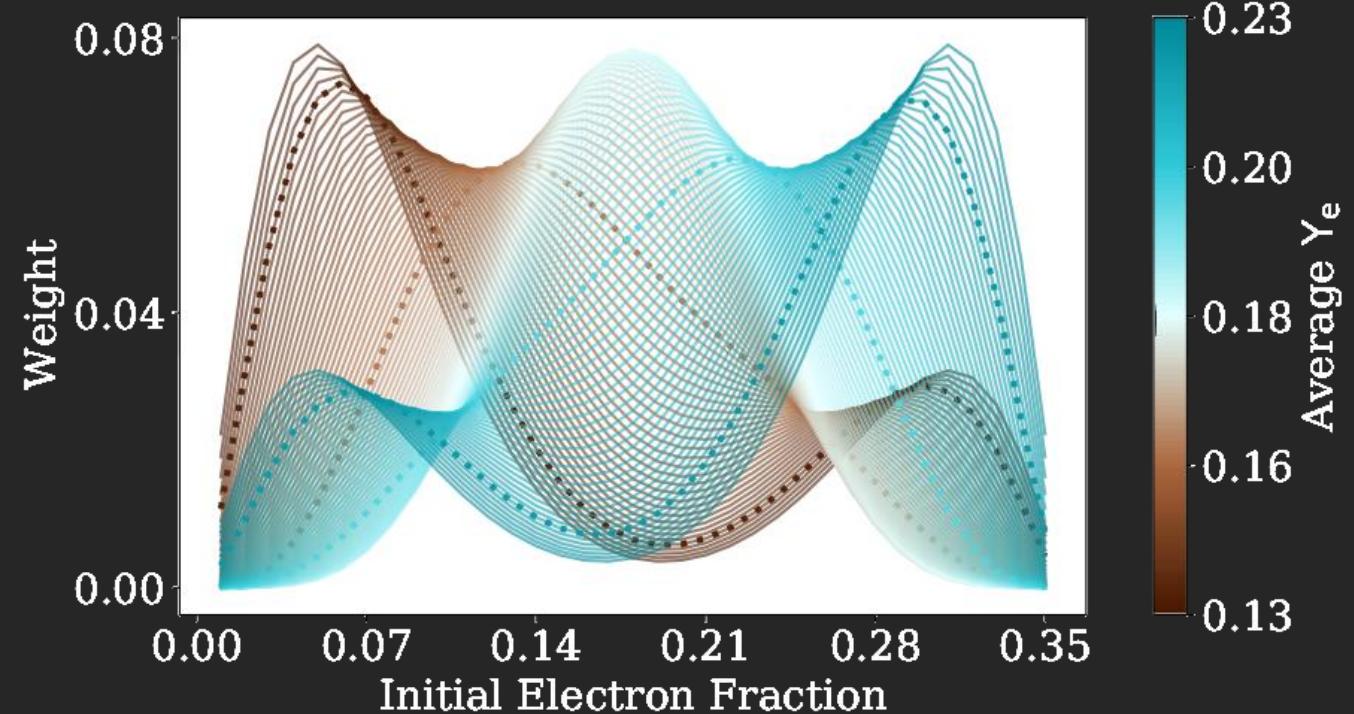
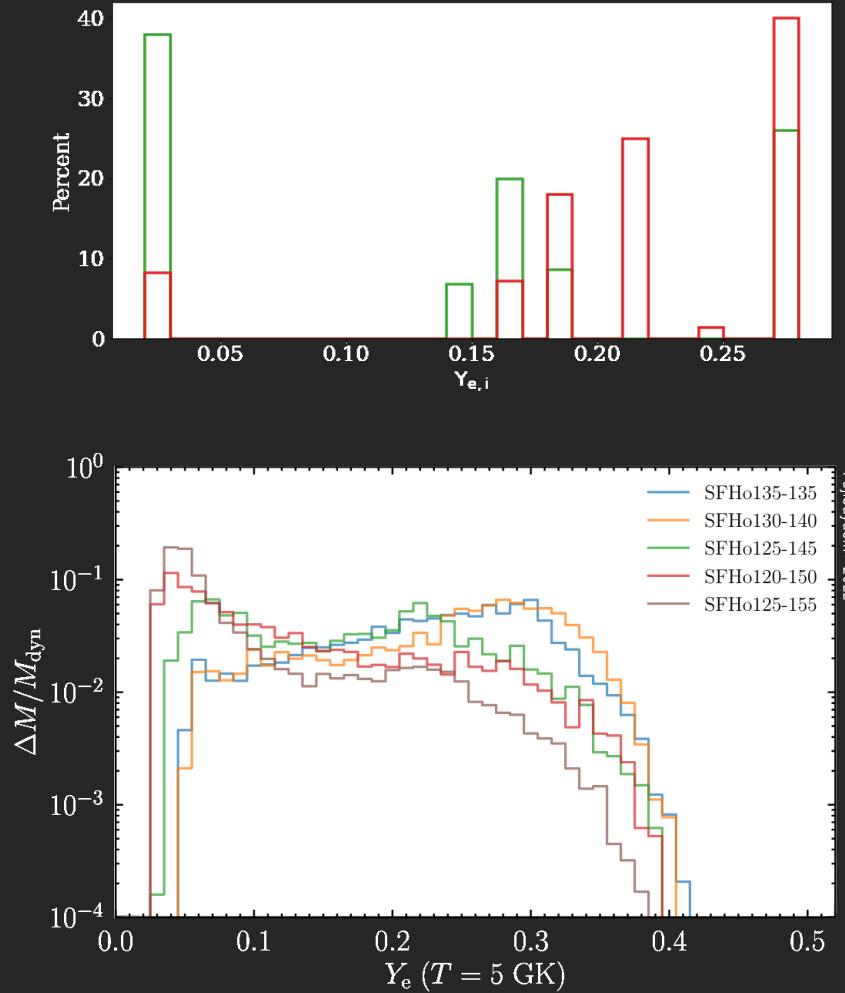
Combined Trajectories (revisited)



Multiple Y_e components



Multiple Y_e components

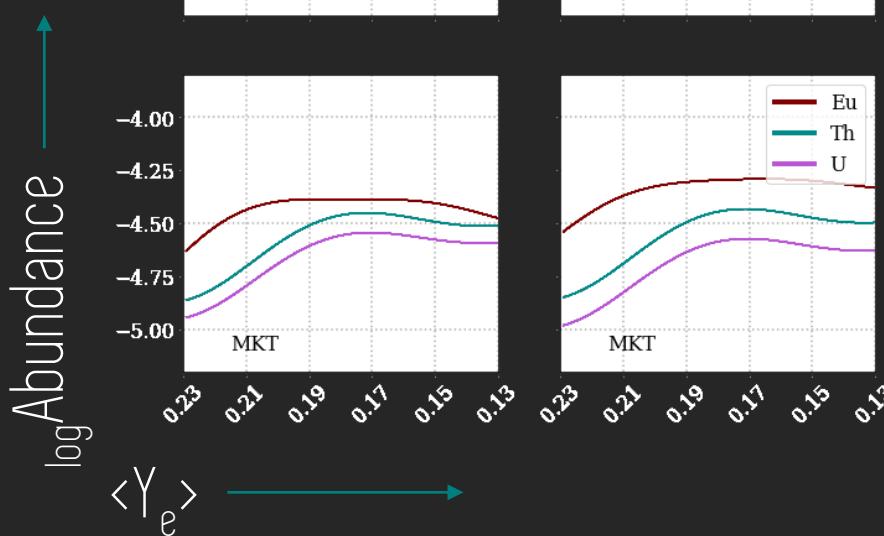


Astronomical Sample

Increasing actinide enhancement ↓

Star Name	$\log_{\epsilon}(\text{Eu})$	$\log_{\epsilon}(\text{Th})$	$\log_{\epsilon}(\text{U})$	Reference
HE1523-0901	-0.62	-1.2	-2.06	Frebel+2007
CS29497-004	-0.66	-1.16	-2.20	Hill+2017
J2038-0023	-0.75	-1.24	-2.14	Placco+2017
CS31082-001	-0.72	-0.98	-1.92	Siquiera Mello+2013
J0954+5246	-1.19	-1.31	-2.13	Holmbeck+2018

Abundances for Cosmochronometry



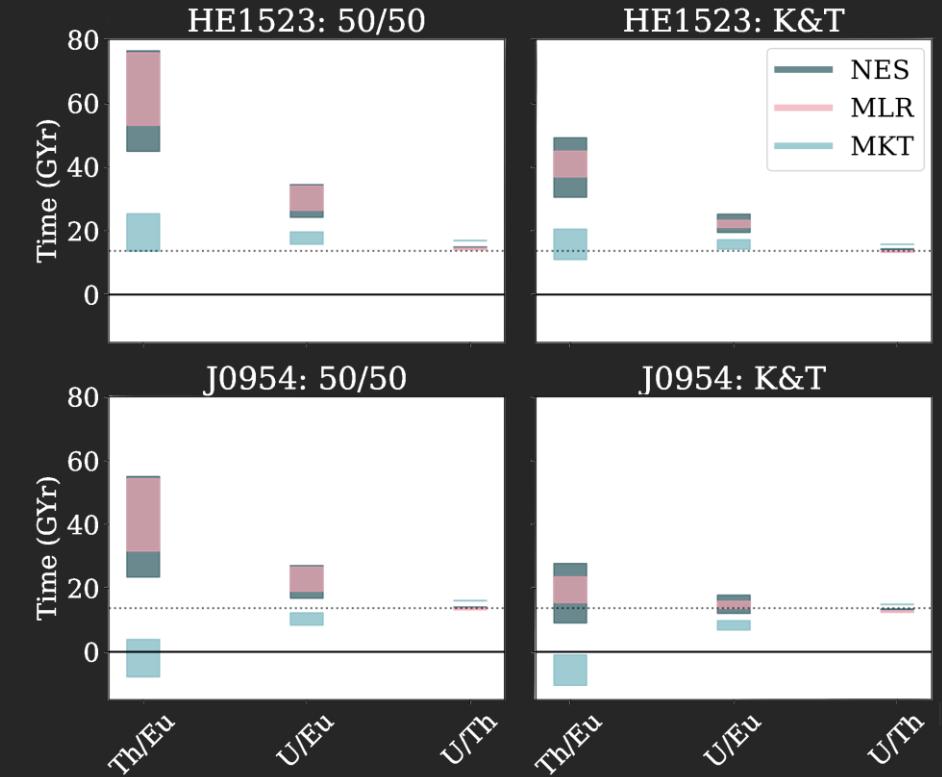
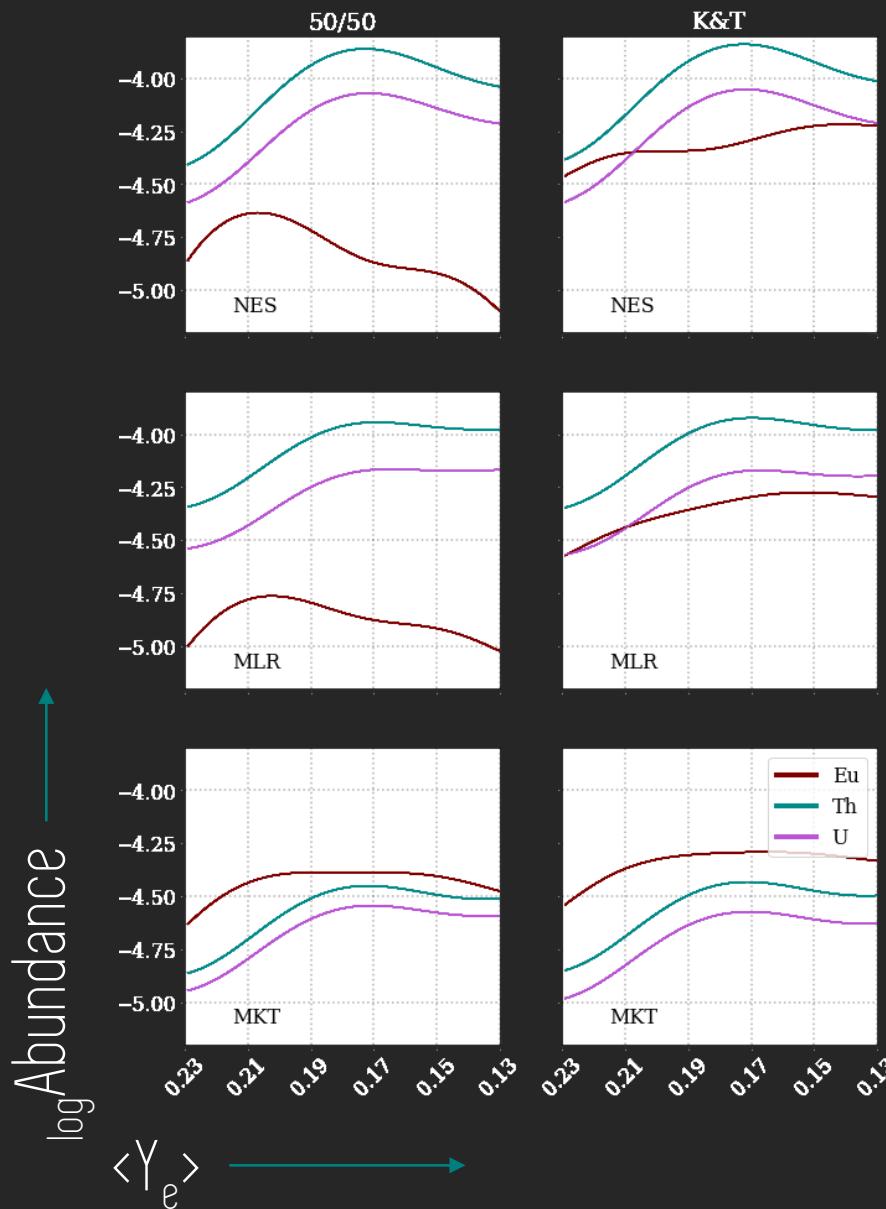
$$t = 46.67 \text{Gyr} \left[-\log_{\epsilon} \left(\frac{\text{Th}}{\text{Eu}} \right)_{\text{obs}} + \log_{\epsilon} \left(\frac{\text{Th}}{\text{Eu}} \right)_0 \right]$$

$$t = 14.84 \text{ Gyr} \left[-\log_{\epsilon} \left(\frac{\text{U}}{\text{Eu}} \right)_{\text{obs}} + \log_{\epsilon} \left(\frac{\text{U}}{\text{Eu}} \right)_0 \right]$$

$$t = 21.80 \text{ Gyr} \left[-\log_{\epsilon} \left(\frac{\text{U}}{\text{Th}} \right)_{\text{obs}} + \log_{\epsilon} \left(\frac{\text{U}}{\text{Th}} \right)_0 \right]$$

^{232}Th & ^{238}U : produced exclusively via r-process ($t_{1/2} = 14$ Gyr, 4.486 Gyr respectively)

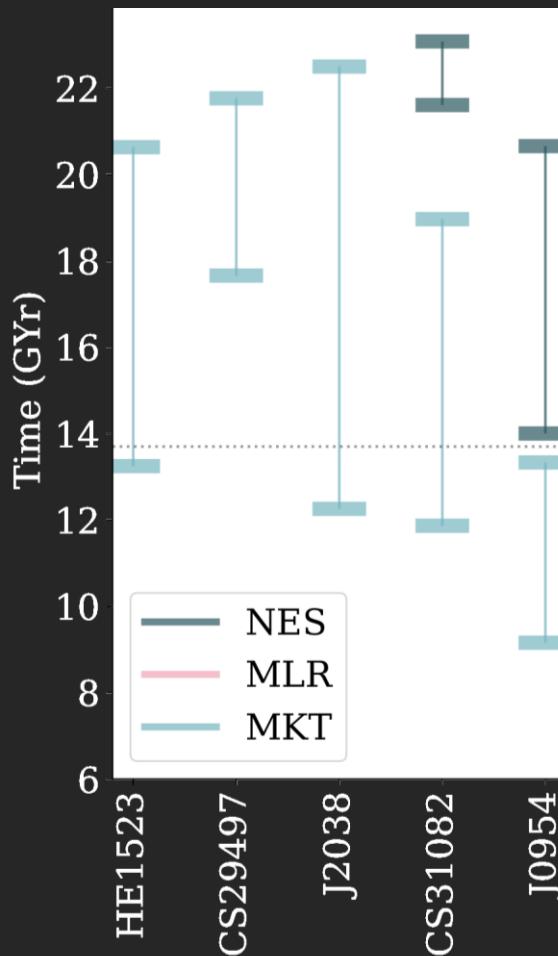
Abundances for Cosmochronometry



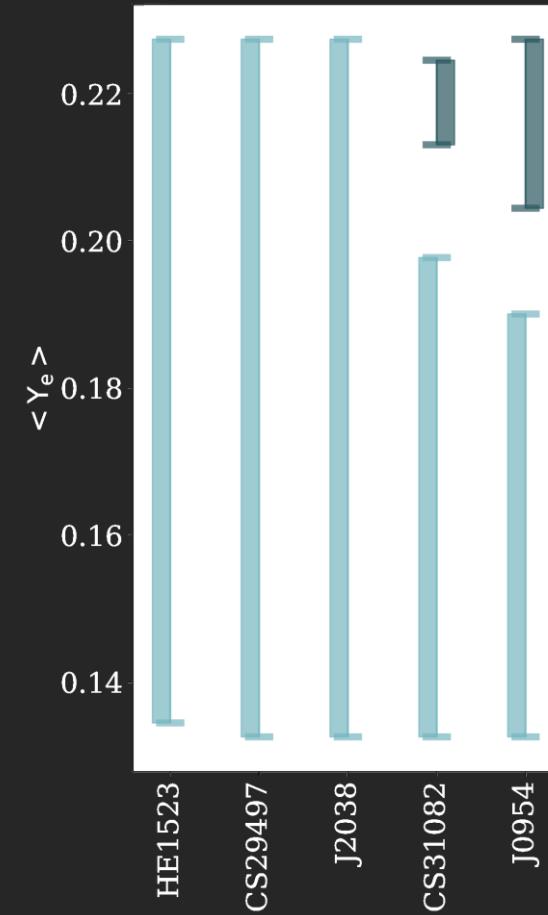
- Europium production highly sensitive to average Ye and fission yield
- Underabundance of actinides can lead to negative age predictions

Error Bars from Observations

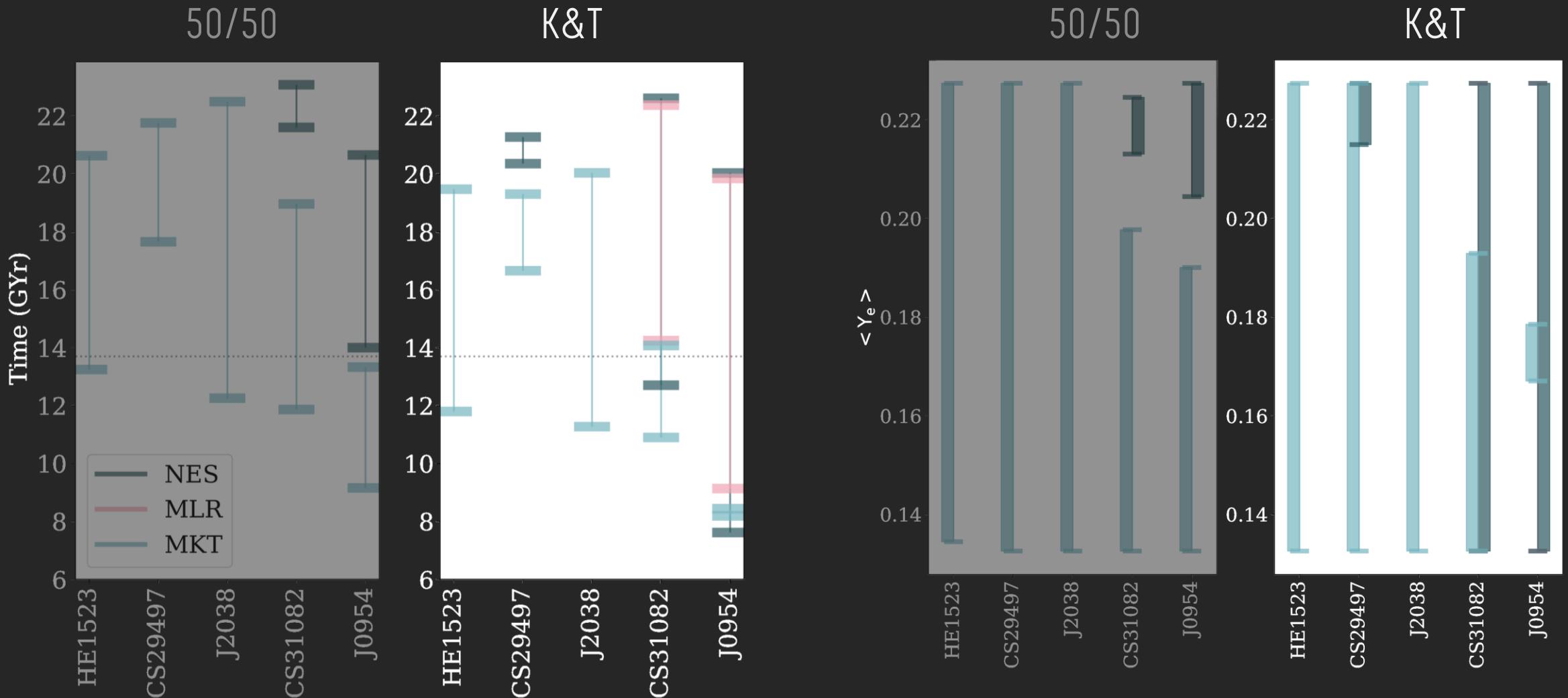
50/50



50/50



Error Bars from Observations



Conclusions

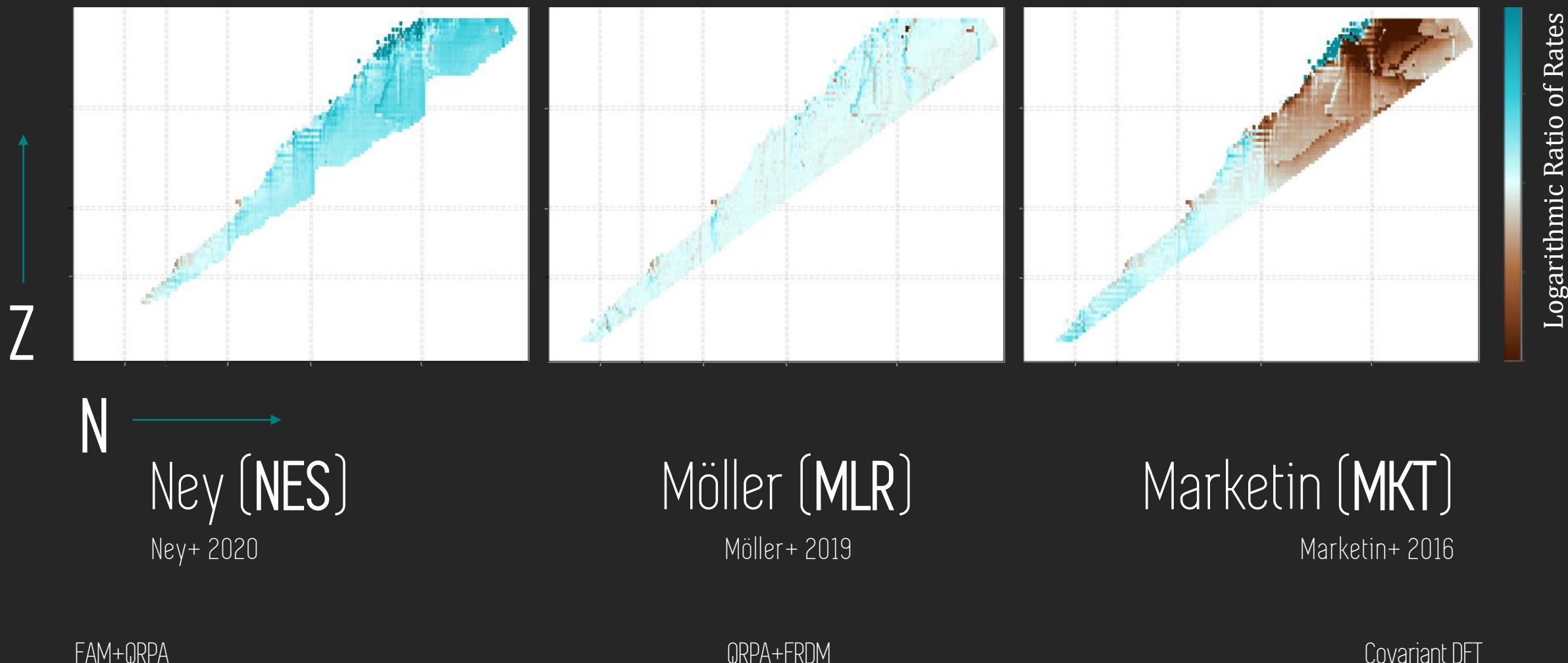
There is a wealth of physics in the unknown properties of nuclei far from stability that can impact key kilonova related quantities

- Identified key measured and unmeasured nuclei important for nuclear heating on light curve-relevant time scales.
- Explored a variety of theoretical nuclear models as a source of uncertainty for nuclear energy generation.
- Probed lanthanide/actinide abundances for cosmic dating of r-process enhanced metal-poor stars.

Nucleosynthesis Appendix

Appendix: Beta Decay Rates

Logarithmic ratio compared to Möller+ 2003



Appendix: Thermalization Efficiency

Kasen & Barnes 2019 ApJ (arXiv: 1807.03319)

Assume thermalization of massive particles: $f = (1 + \tau)^{-n}$

Electrons ($n=1$): $t_{th,\beta} = 12.9 M_{0.01}^{2/3} v_{0.2}^{-2}$ days

γ -rays: $t_\gamma = 0.3 M_{0.01}^{1/2} v_{0.2}^{-1}$ and

$$f_\gamma(t) = 1 - \exp\left[-\frac{t_\gamma^2}{t^2}\right]$$

α -decay: $t_{th,\alpha} = 2t_{th,\beta}$ and

$$f_\alpha(t) = \left(1 + \frac{t}{t_{th,\alpha}}\right)^{-1.5}$$

Fission: $t_{th,f} = 4t_{th,\beta}$ and

$$f_f(t) = \left(1 + \frac{t}{t_{th,f}}\right)^{-1}$$

Appendix: Opacity (i)

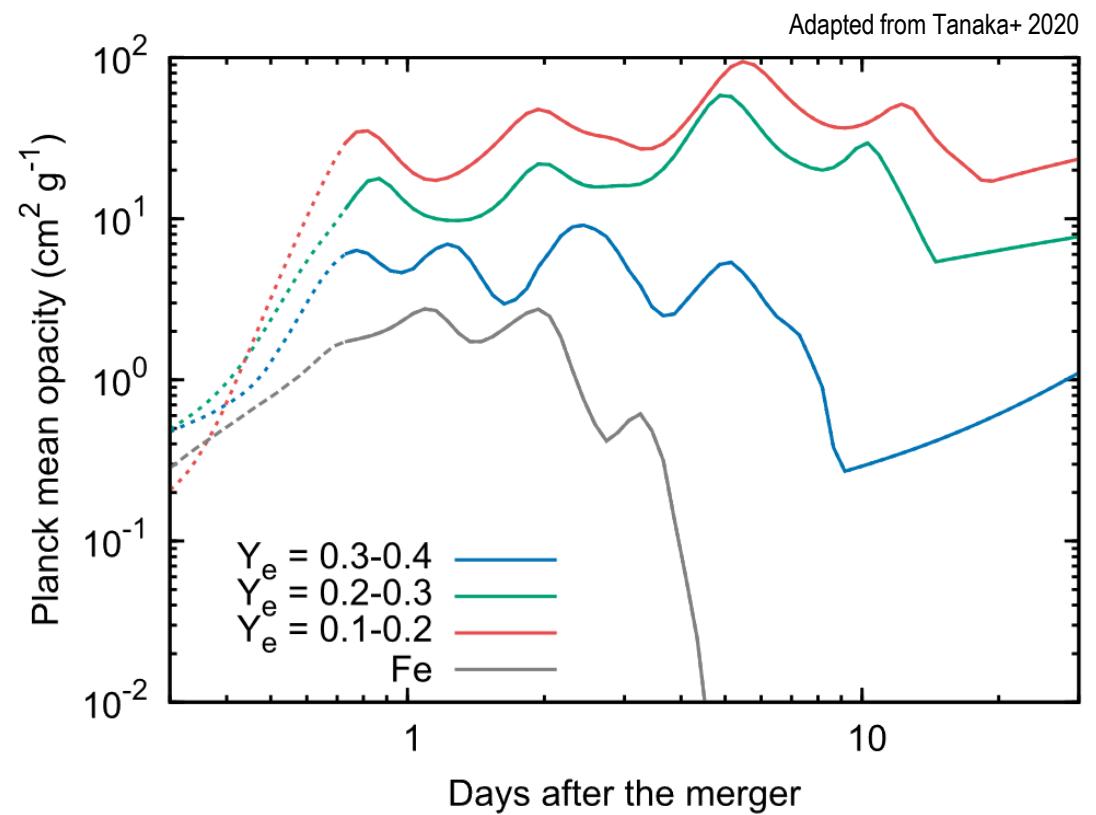
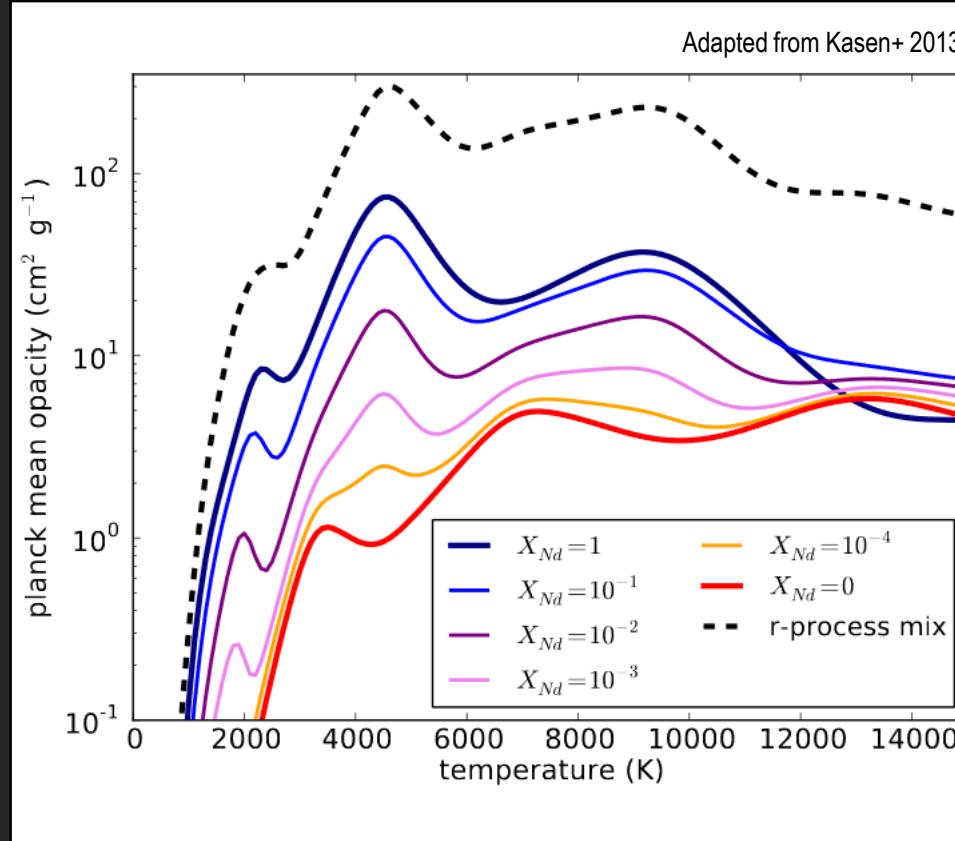
Diffusion timescale is dependent on opacity; in this model, the opacity is temperature dependent.

$$\kappa = \begin{cases} \kappa_{max} \left(\frac{T}{4000K} \right)^{5.5} & T < 4000K \\ \kappa_{max} & \text{otherwise} \end{cases} \quad \text{with } \kappa_{max} = 100 \text{ cm}^2\text{g}^{-1}$$

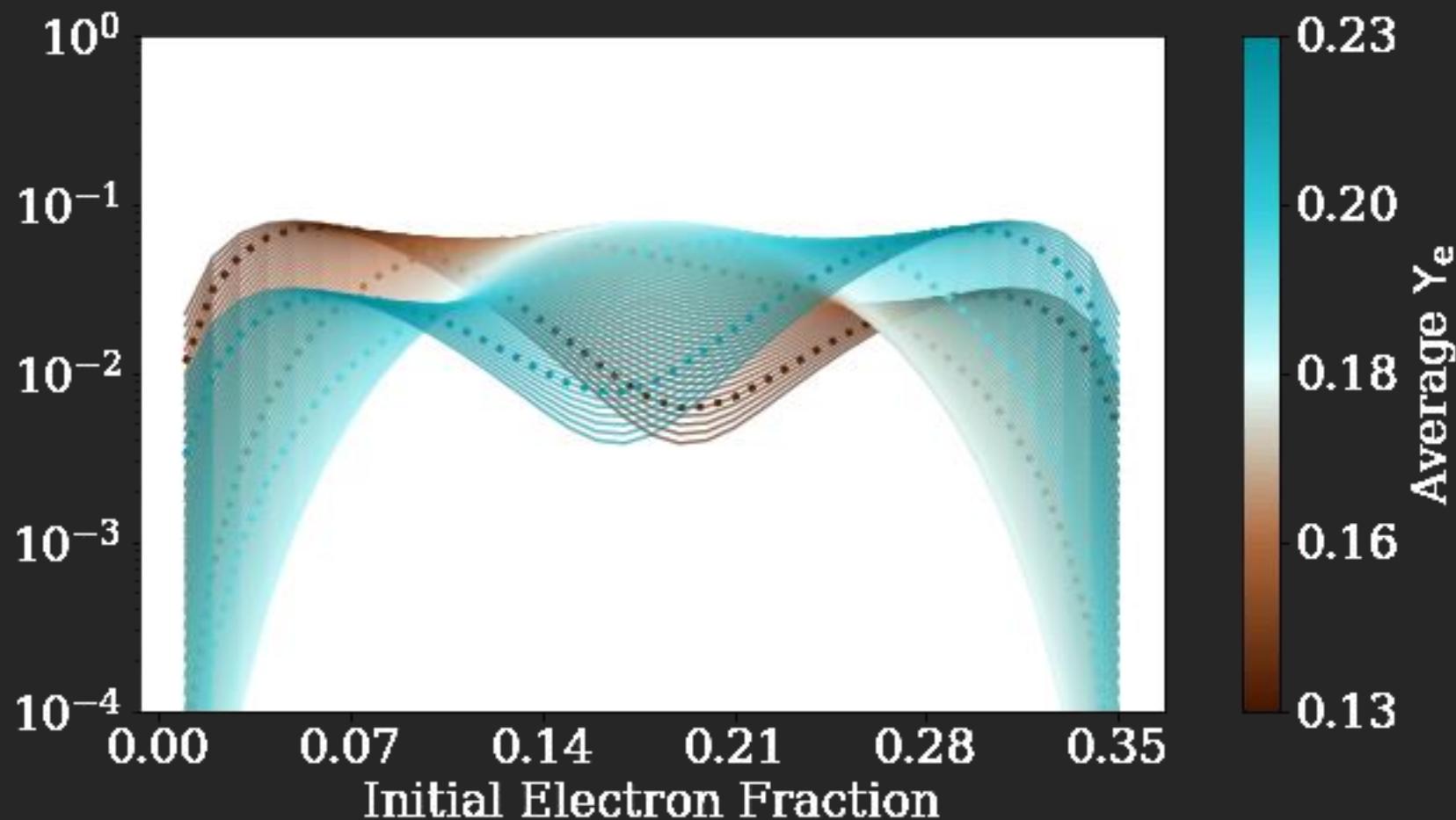
Technically, κ_{max} should be calculated uniquely for each composition. For now, consider mainly that a larger opacity should

- extend the light curve in time, and
- decrease the height of the light curve peak

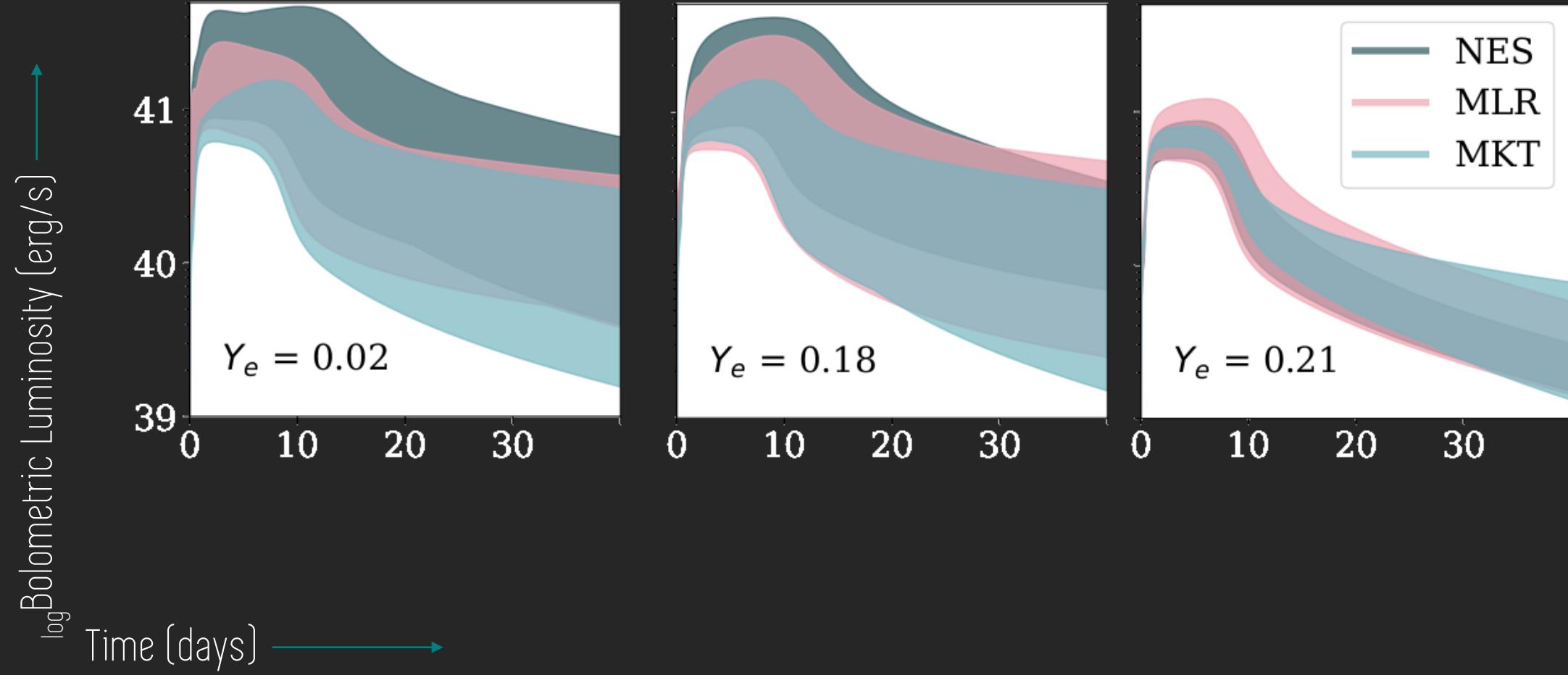
Appendix: Opacity (ii)



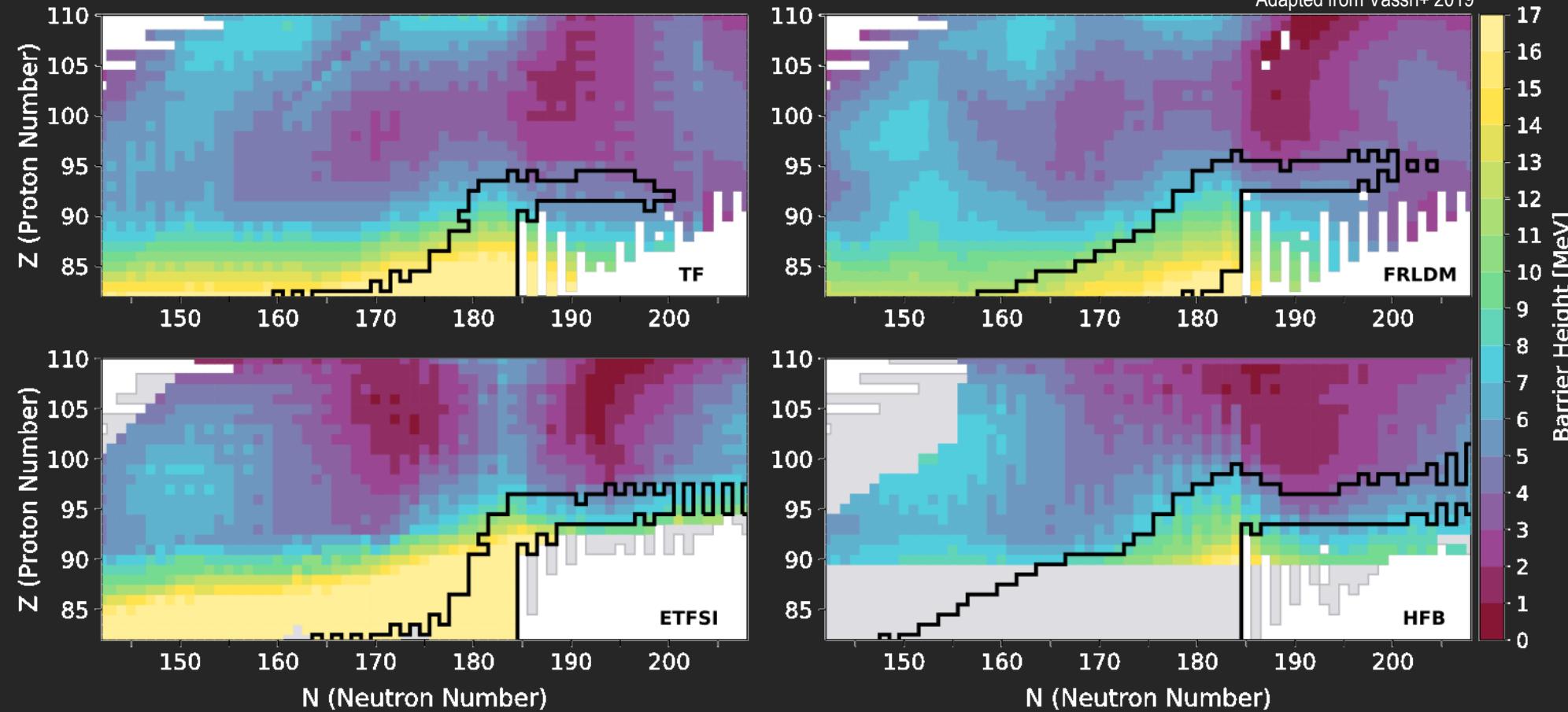
Appendix: Linear Combinations



Backup: Light Curves



Appendix: Fission Barriers



Appendix: Reaction Network

The evolution of the abundance of species i can be described by:

$$\frac{dY_i}{dt} = \sum_j N_j^i \lambda_j Y_j + \sum_{j,k} N_{j,k}^i \rho N_A \langle j, k \rangle Y_j Y_k + \sum_{j,k,l} N_{j,k,l}^i \rho^2 N_A^2 \langle j, k, l \rangle Y_j Y_k Y_l$$

One-body Two-body Three-body

Decay Rate Thermal Cross-Section

The diagram illustrates the decomposition of the reaction network equation into three-body interactions. The first term, involving the decay rate λ_j , is labeled 'One-body'. The second term, involving the thermal cross-section $\rho N_A \langle j, k \rangle$, is labeled 'Two-body'. The third term, involving the triple thermal cross-section $\rho^2 N_A^2 \langle j, k, l \rangle$, is labeled 'Three-body'. Brackets below the terms group them according to their physical interpretation.