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Fast Neutrino Flavor Conversions in Densa Neutrino Media: A Machine Learning Approach

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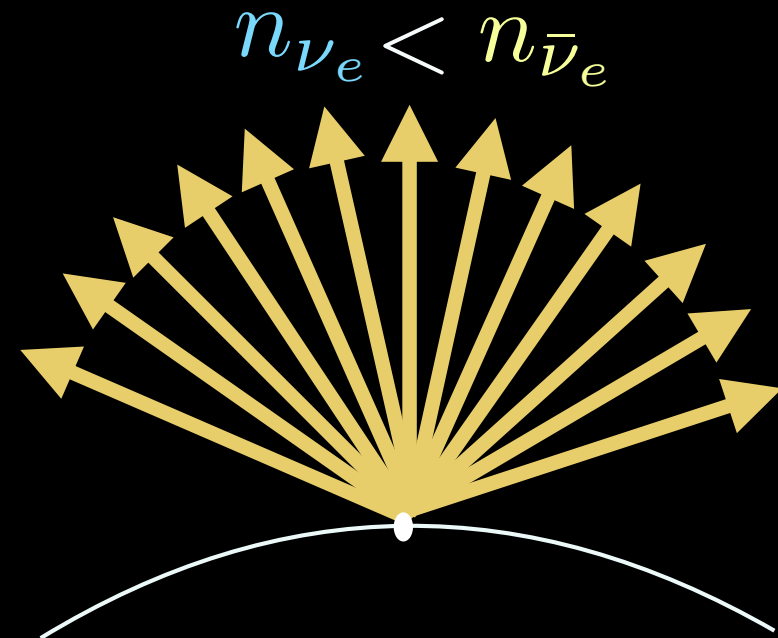
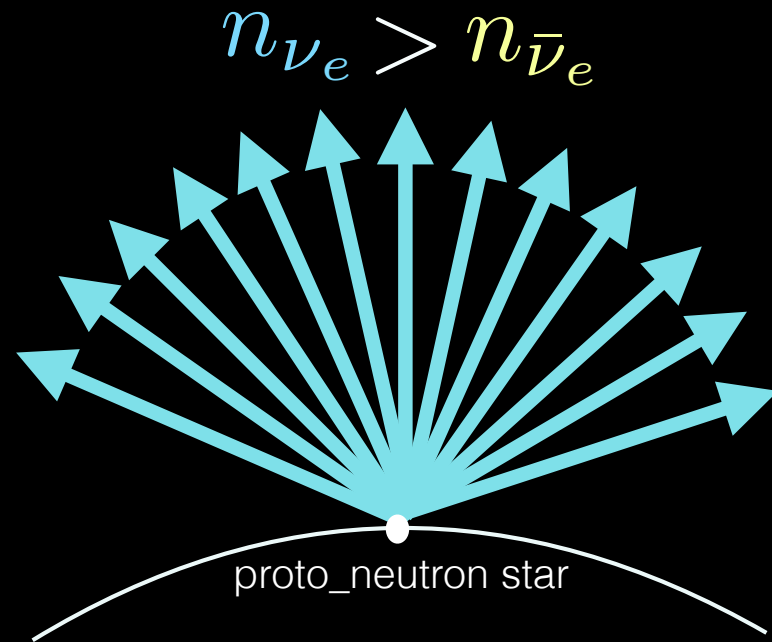
SFB 1258

Neutrinos
Dark Matter
Messengers



Fast Flavor Conversion Modes

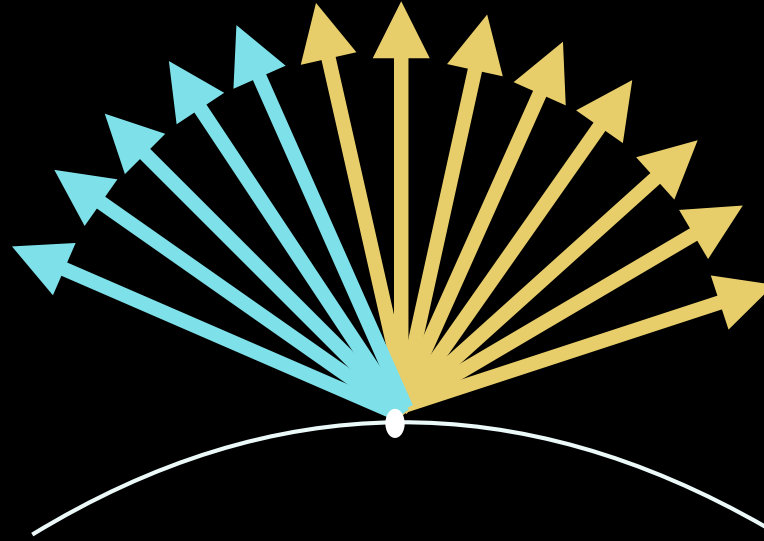
- We assumed that neutrinos and antineutrinos are emitted **isotropically** from the surface of the neutrino source
- $f_{\nu_e}(\theta) - f_{\bar{\nu}_e}(\theta)$ is either always **positive or negative**



- This implies that the **scales** on which flavor conversion could occur are determined by **vacuum frequency** $\Delta m^2 / 2E \sim 1 \text{ km}^{-1}$

Fast Flavor Conversion (FFC)

- **FFC** could occur when there is **crossing** in $f_{\nu_e}(\theta) - f_{\bar{\nu}_e}(\theta)$



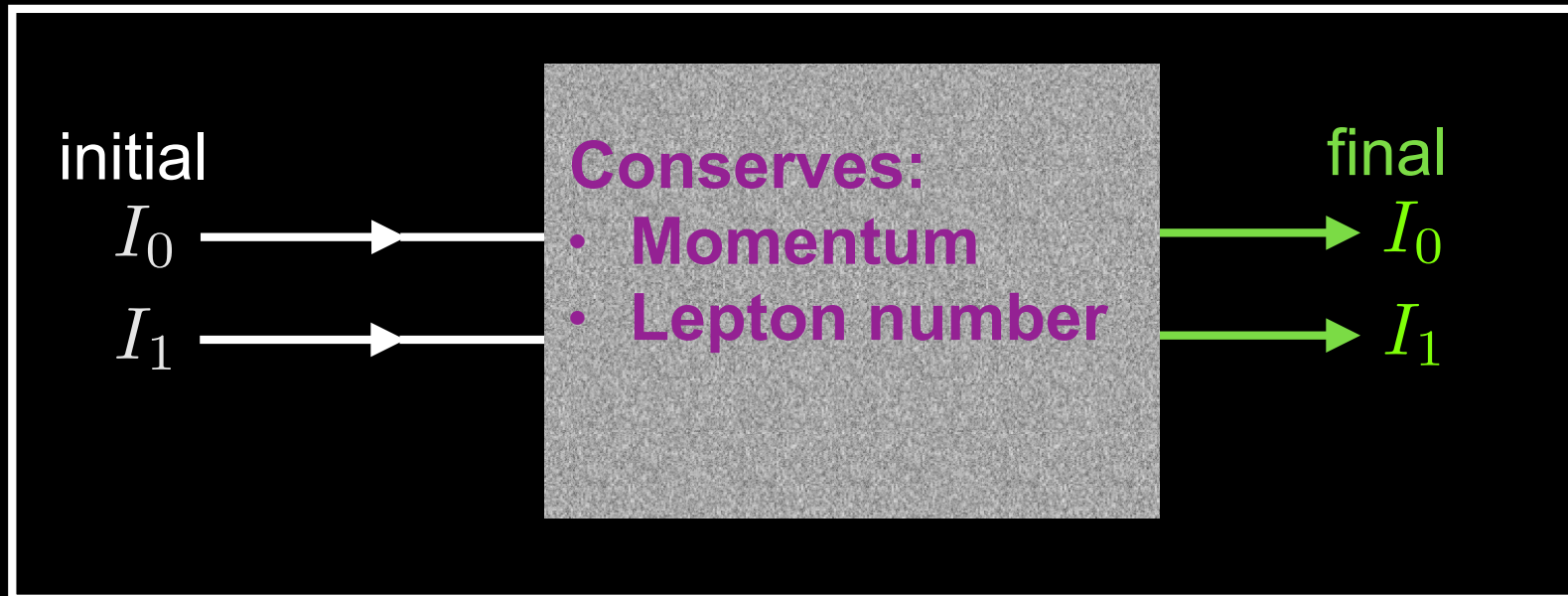
- **Scales** on which flavor conversion can occur is now proportional to n_ν and could be < 10 cm

- Neutrino oscillations **can** now occur at densities that had been long thought to be the realm of collisional and scattering processes

Including FFC in CCSNe

- We assume FFC lead to a sort of flavor **equilibrium**

FFC



Neutron Star Mergers

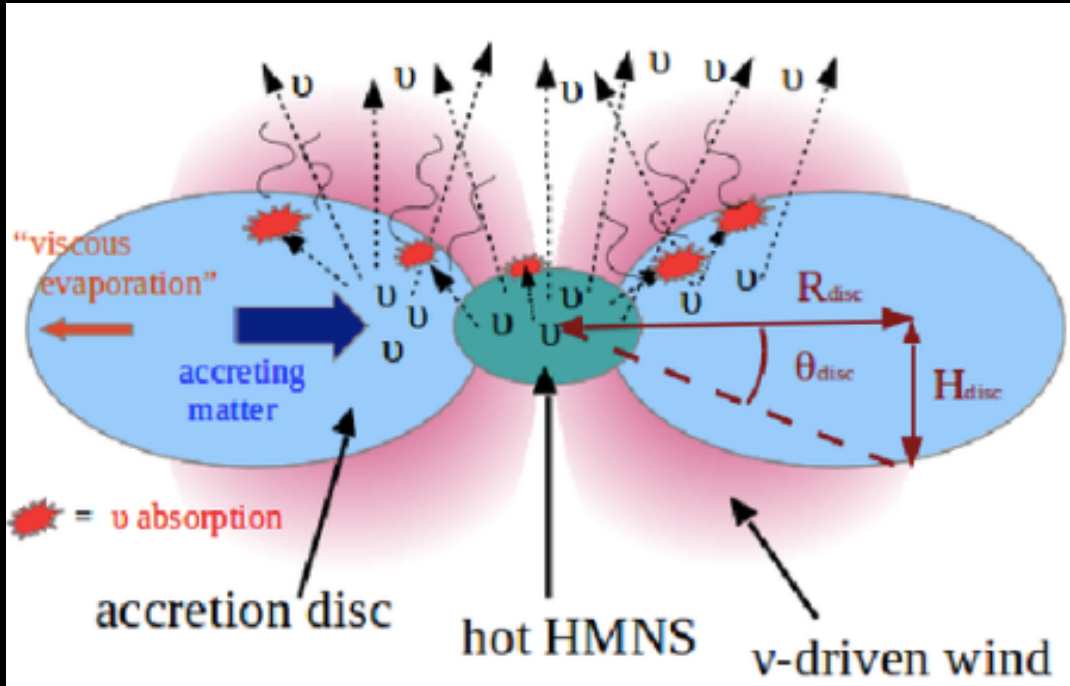


Figure from Perego et. al., arxiv: 1405.6730

- Hot **hyper massive NS** and the **accretion disk** emit a huge number of neutrinos

Neutron Star Mergers

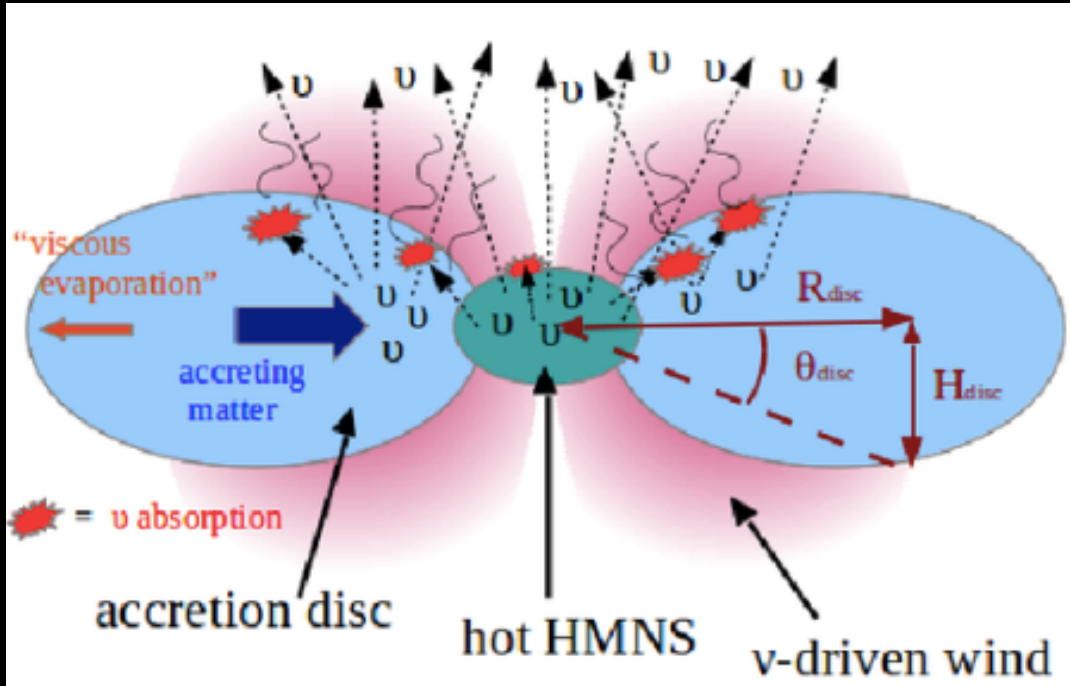
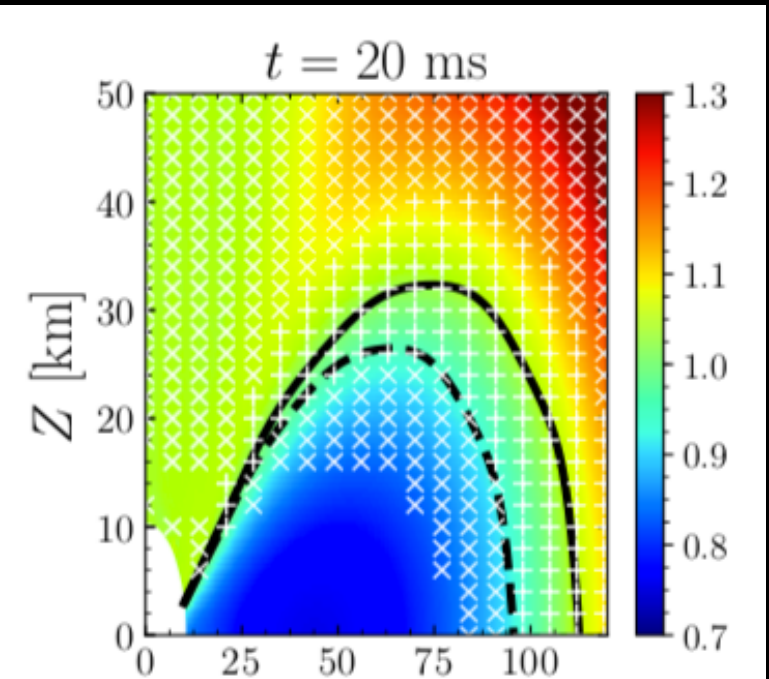


Figure from Perego et. al., arxiv: 1405.6730

- Fast modes can occur in a wide region even **inside** the disk
- Any self-consistent neutrino transport should **implement** fast conversions.

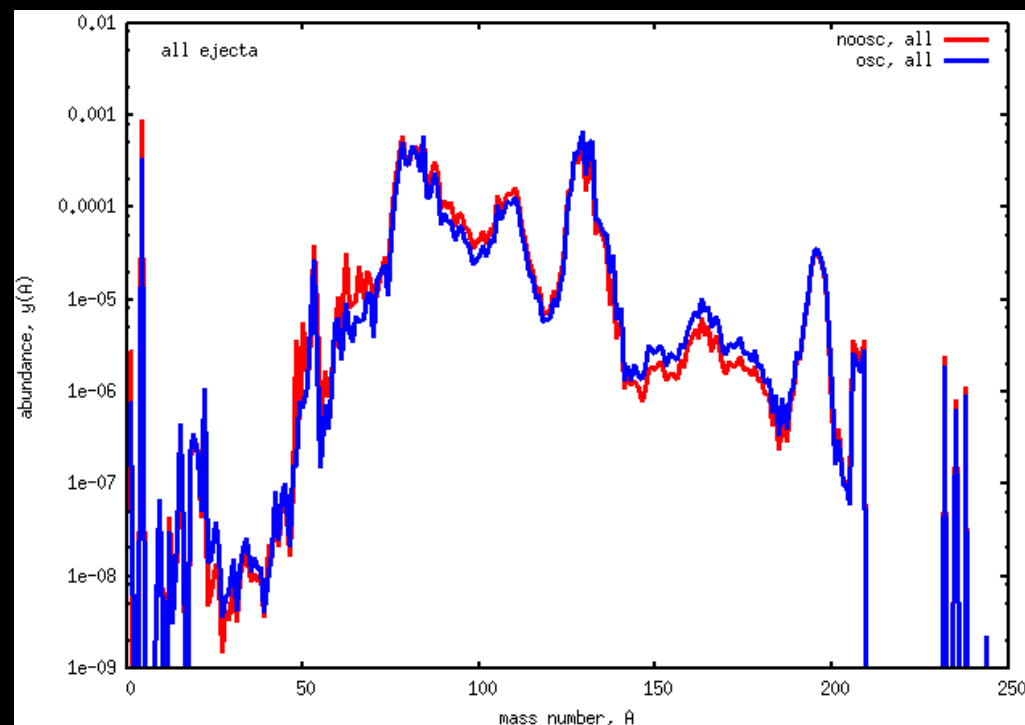
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Just+2022 (also Li+2021, Fernandez+2022, Grohs+2022,)



Neutron Star Mergers

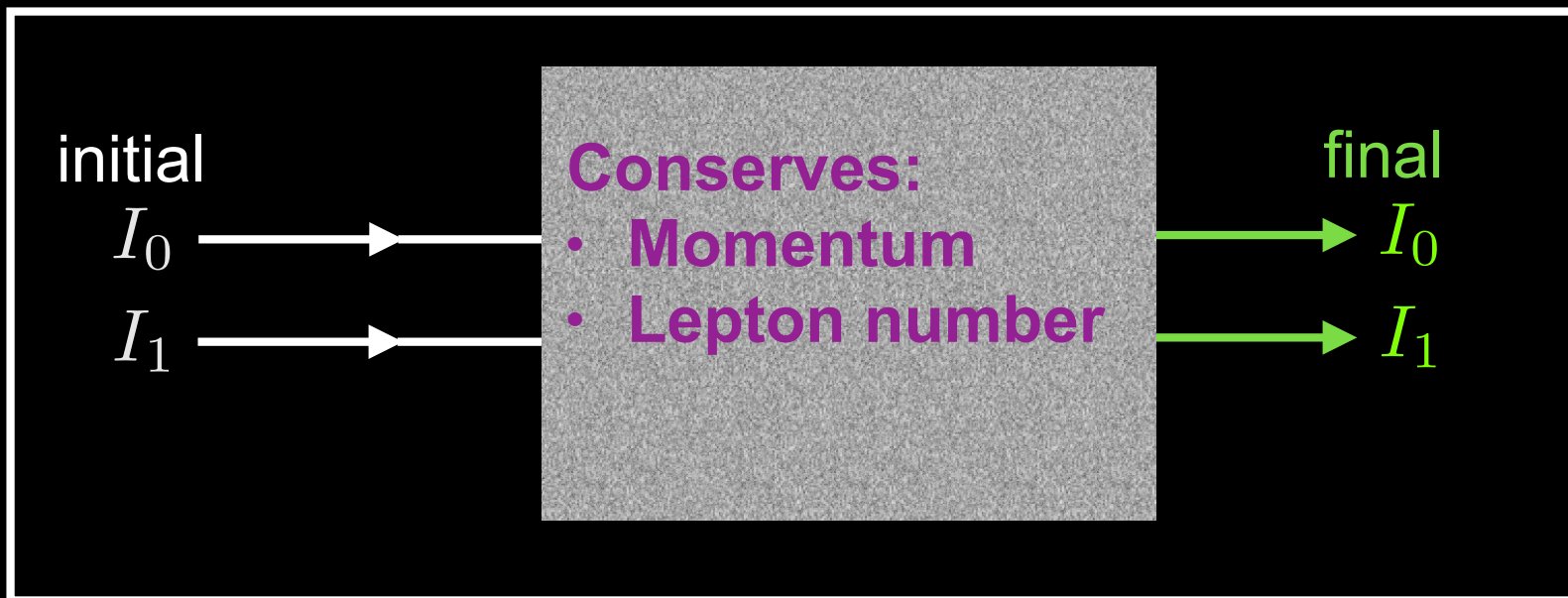
- We perform simulations with **self-consistent neutrino transport**
- The presence of fast conversions inside the torus opens up a new **cooling channel**
- The impact of the fast modes remains **small** on the Y_e due to a sort of **self-regulating** mechanism



Including FFC in CCSNe

- We perform SN simulations including FFC for a **1D** $20M_{\odot}$ model, in a **parametric** way
- We set a density **threshold** ($\rho_c = 10^9 - 10^{14} \text{ g cm}^{-3}$) below which FFC can occur

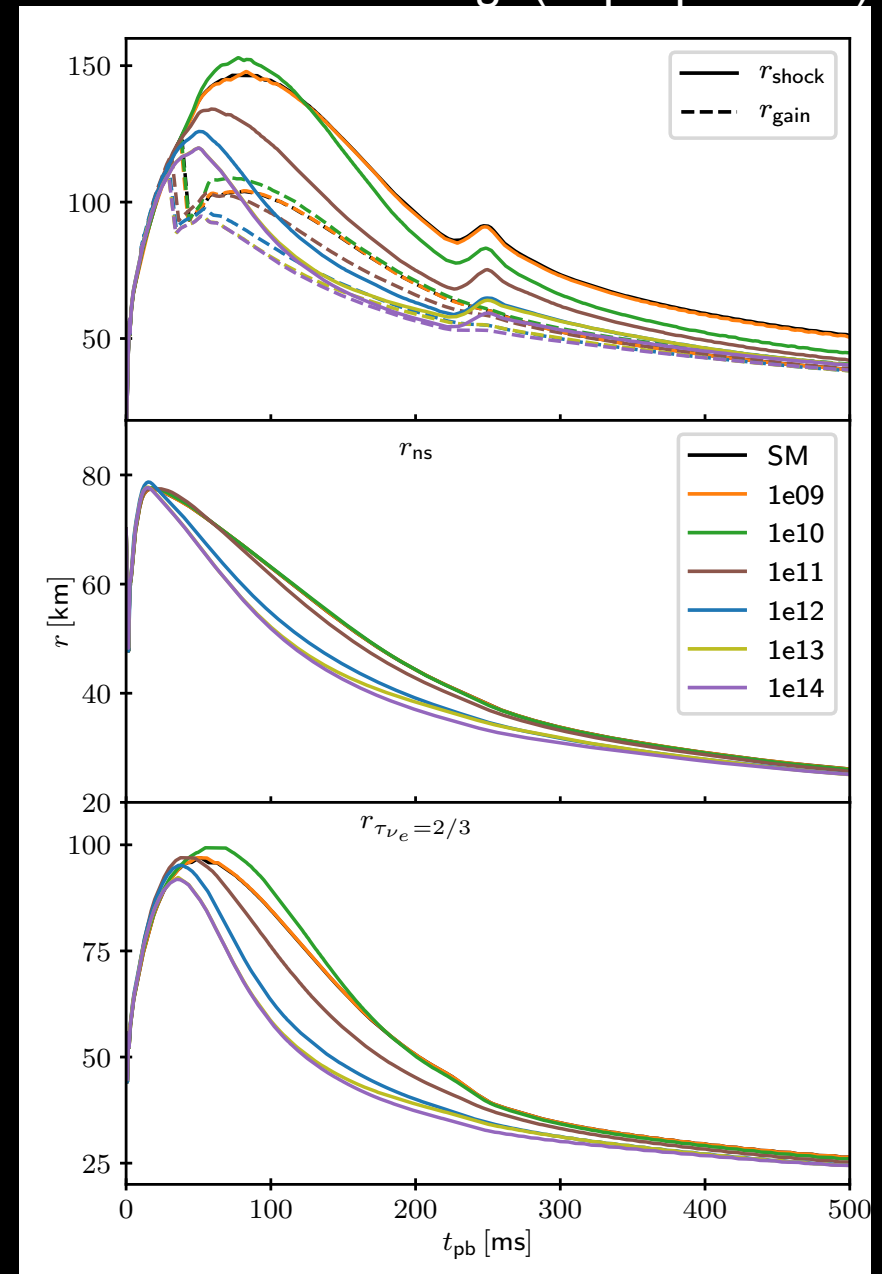
FFC



Including FFC in CCSNe

Ehring+(In preparation)

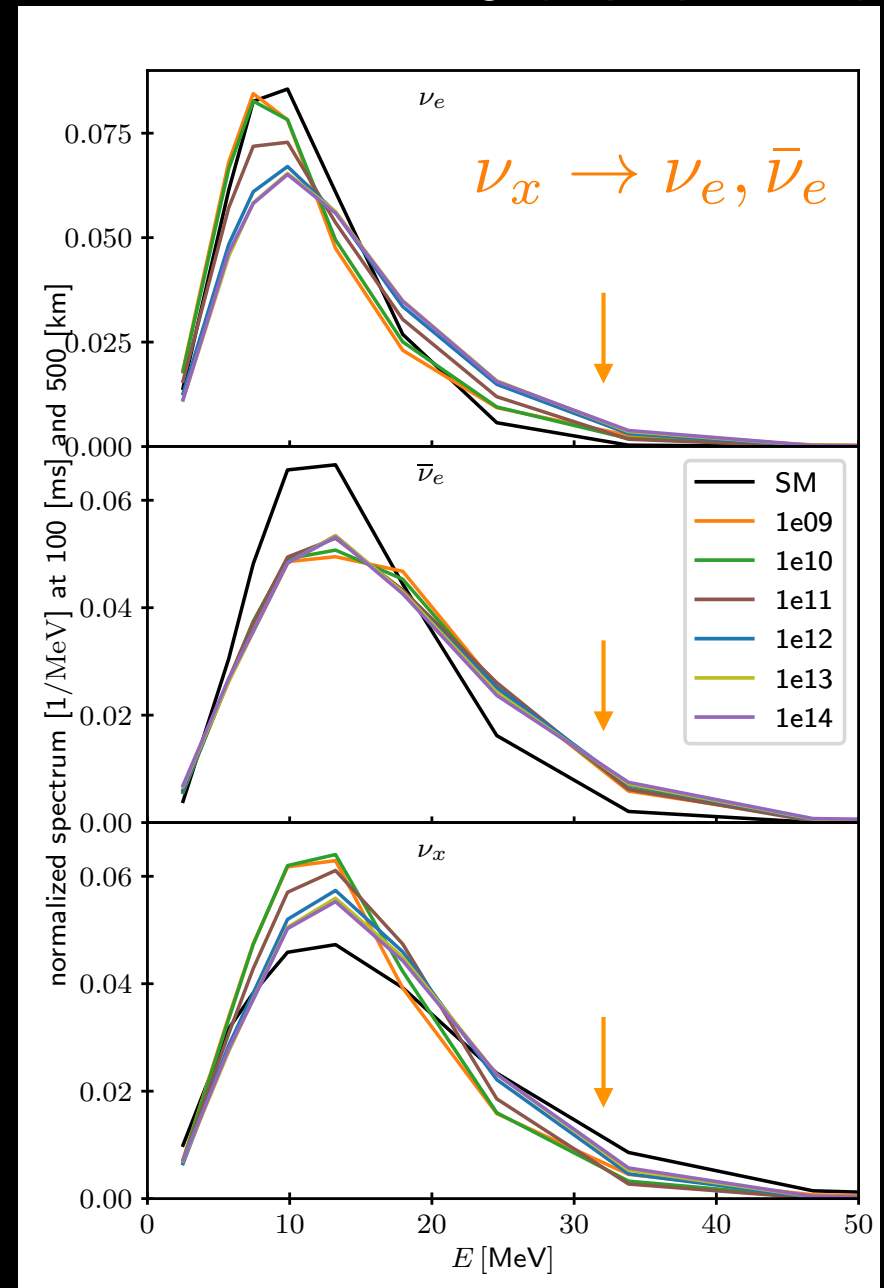
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Including FFC in CCSNe

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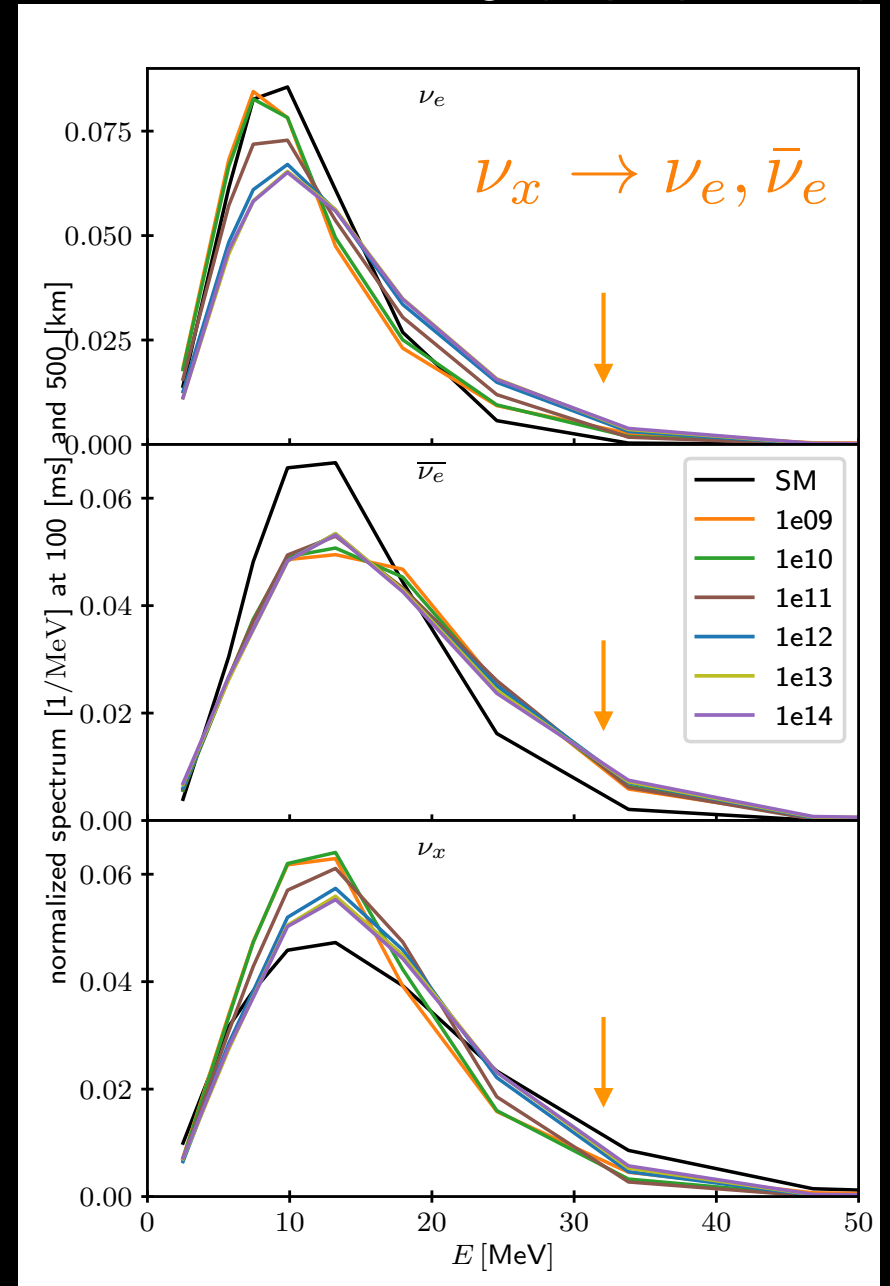
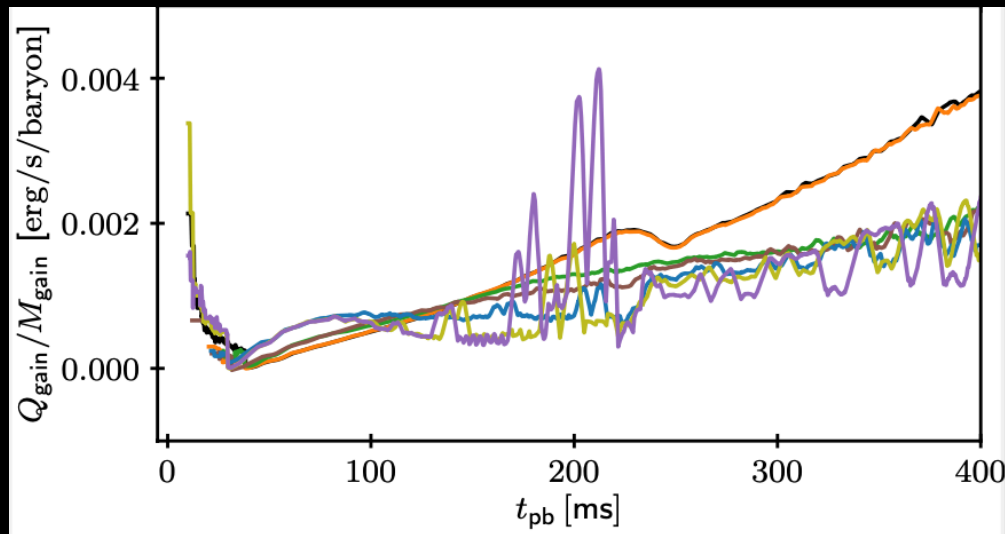
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 - $\nu_x \rightarrow \nu_e, \bar{\nu}_e$ at the tail increases heating



Including FFC in CCSNe

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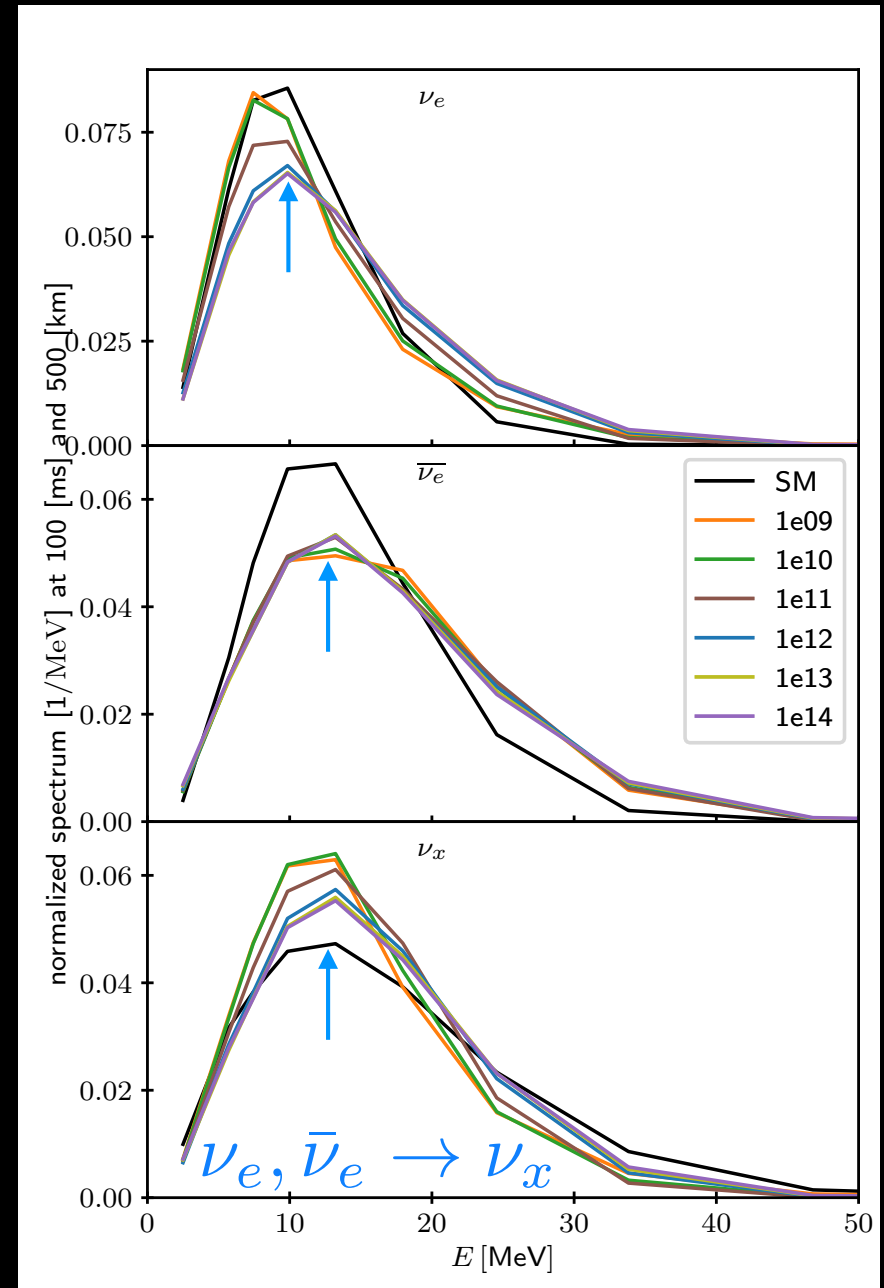
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Including FFC in CCSNe

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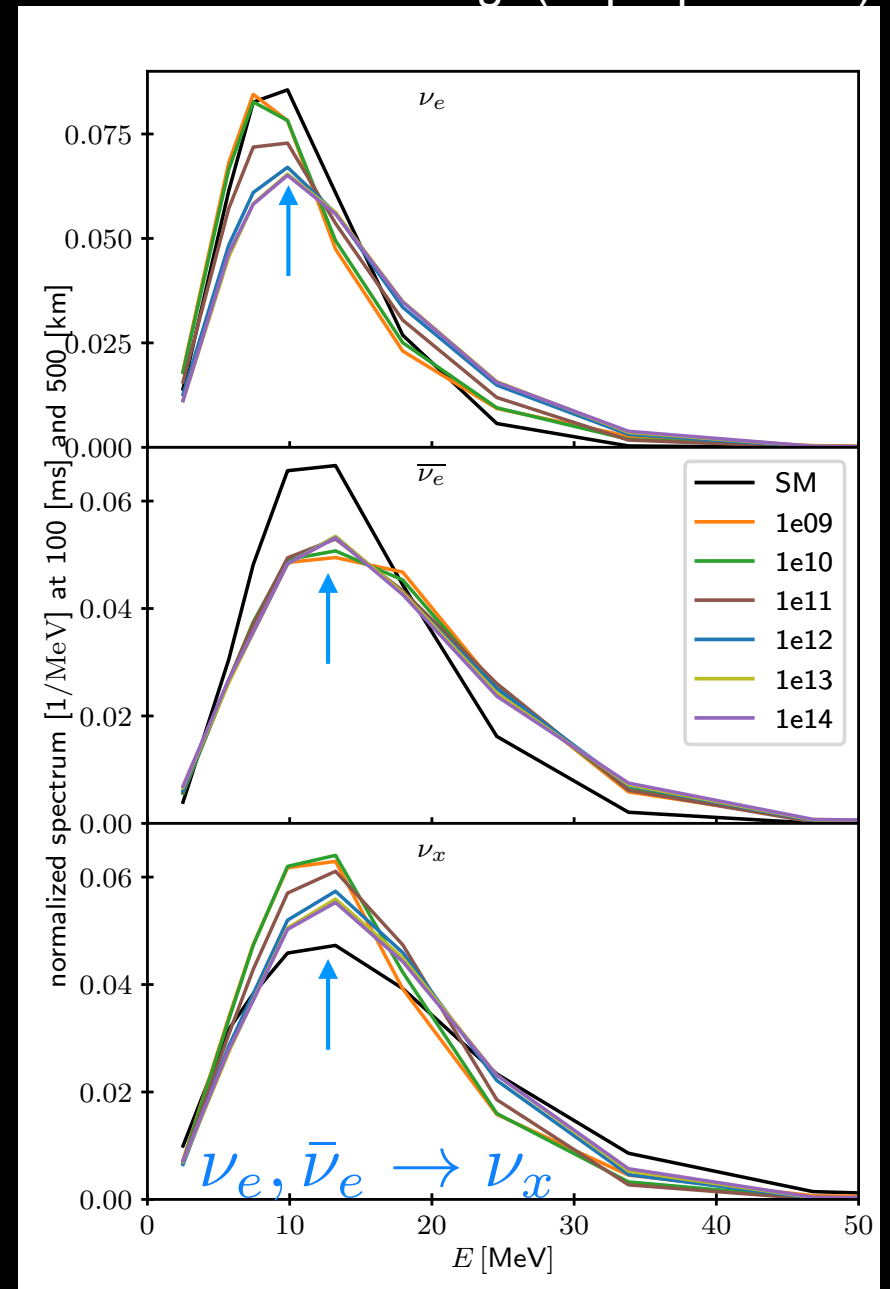
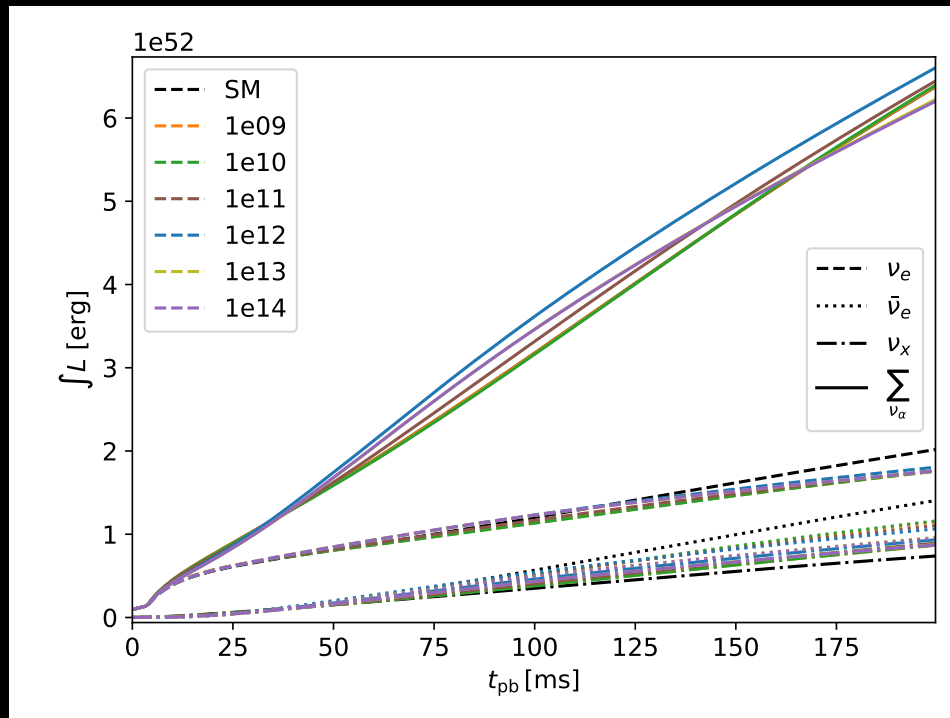
- Two **competing** effects here
 - $\nu_x \rightarrow \nu_e, \bar{\nu}_e$ at the tail **increases** heating
 - $\nu_e, \bar{\nu}_e \rightarrow \nu_x$ at the peak **increases** total neutrino luminosity



Including FFC in CCSNe

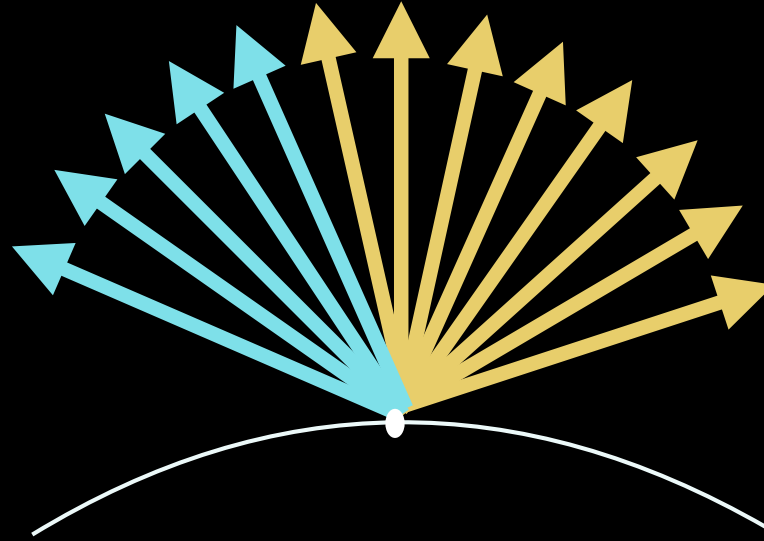
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Fast Flavor Conversion (FFC)

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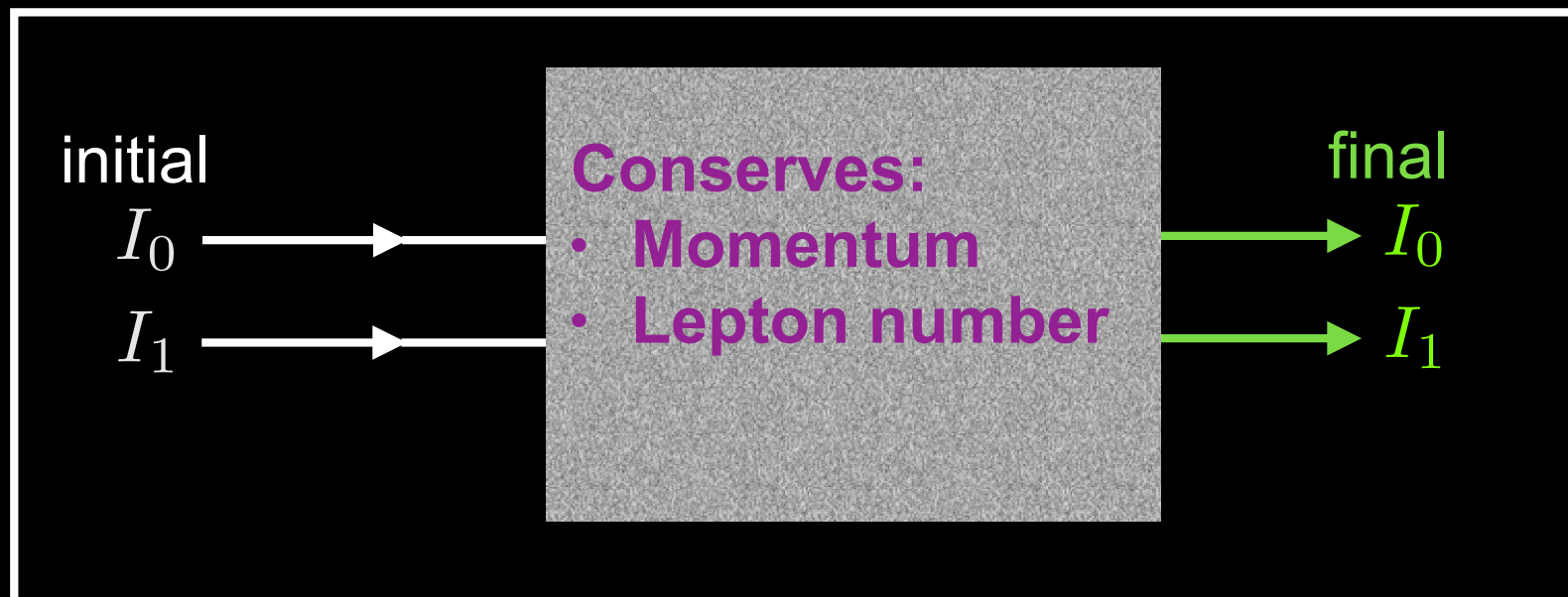


Fast Flavor Conversion (FFC)

- The angular distributions are **not available**, instead we have only access to their moments

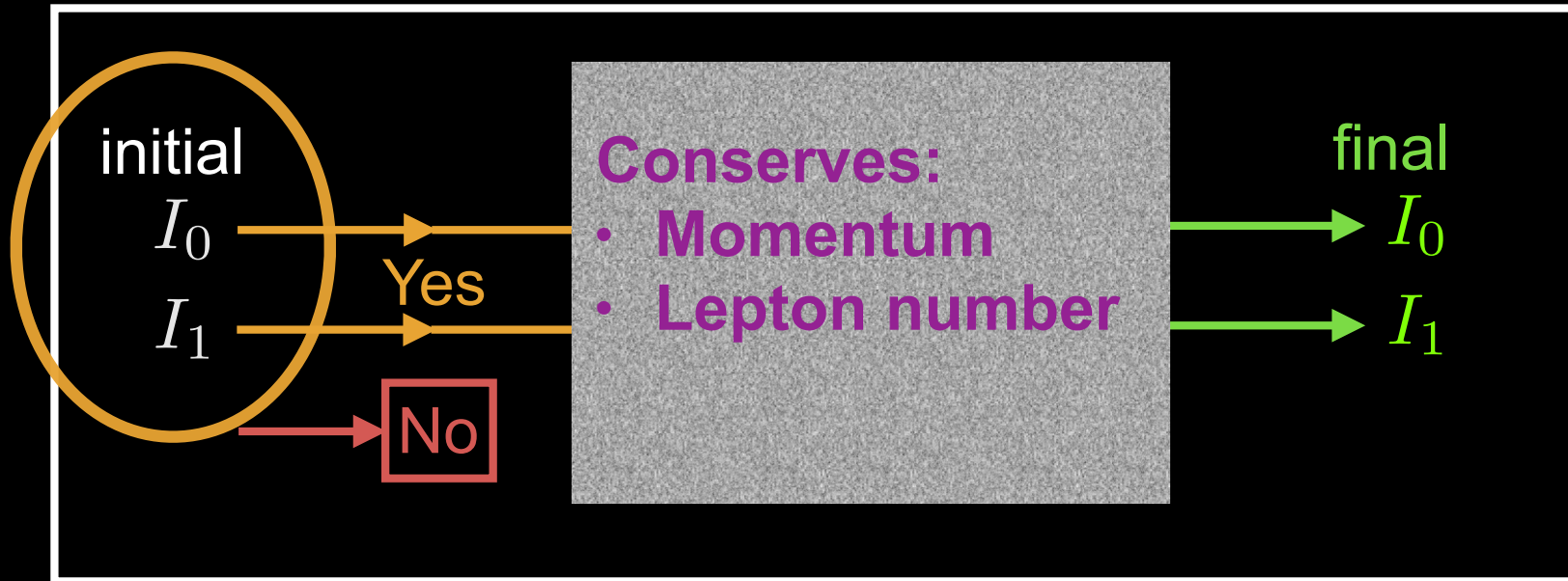
$$I_n = \int d \cos \theta_\nu \cos^n \theta_\nu f_\nu(\cos \theta_\nu)$$

- We can still make progress! Dasgupta+2018; Abbar2020; Johns+2021; Richers2022;
- But these methods are normally **inefficient** and **very slow**
- FFC can not be detected **on the fly**



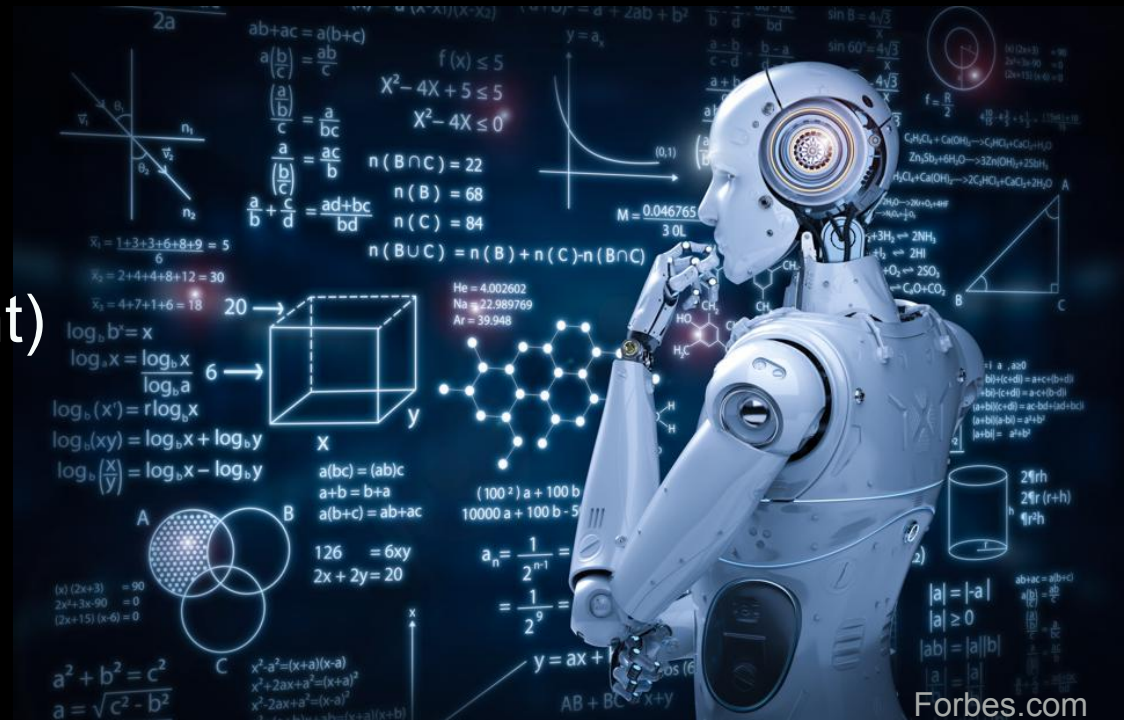
Fast Flavor Conversion (FFC)

- A **classification** problem!



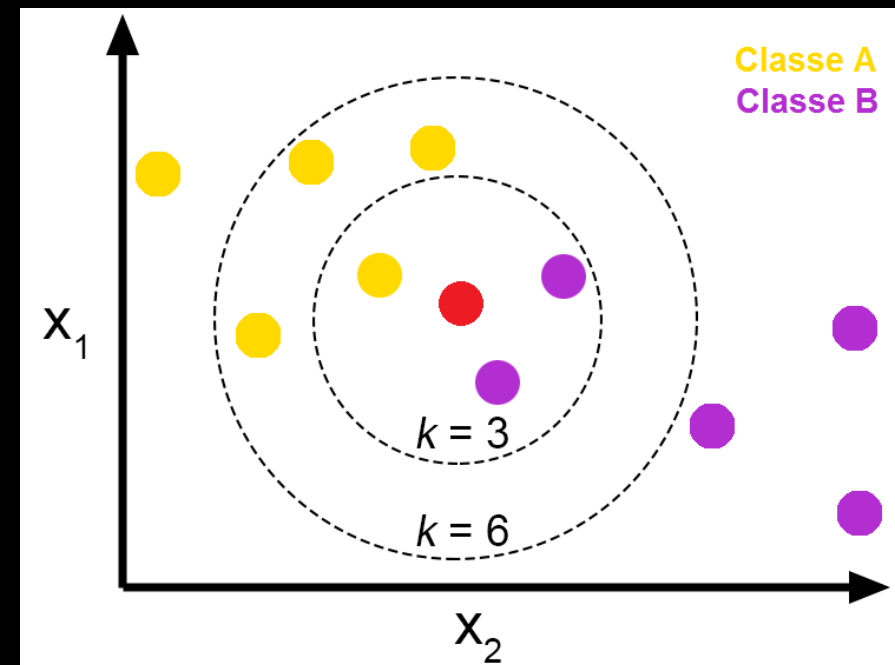
Fast Flavor Conversion (FFC)

- **Machine learning** can help us
- We have **four** feature here: I_0 and I_1 for neutrinos and antineutrinos (one is redundant)
- A number of ML algorithms out there. I here introduce:
 - **KNN**
 - **Decision Tree**
 - **Naive Bayes**
 - **SVM**
 - **Logistic Regression**



Including FFC in CCSNe

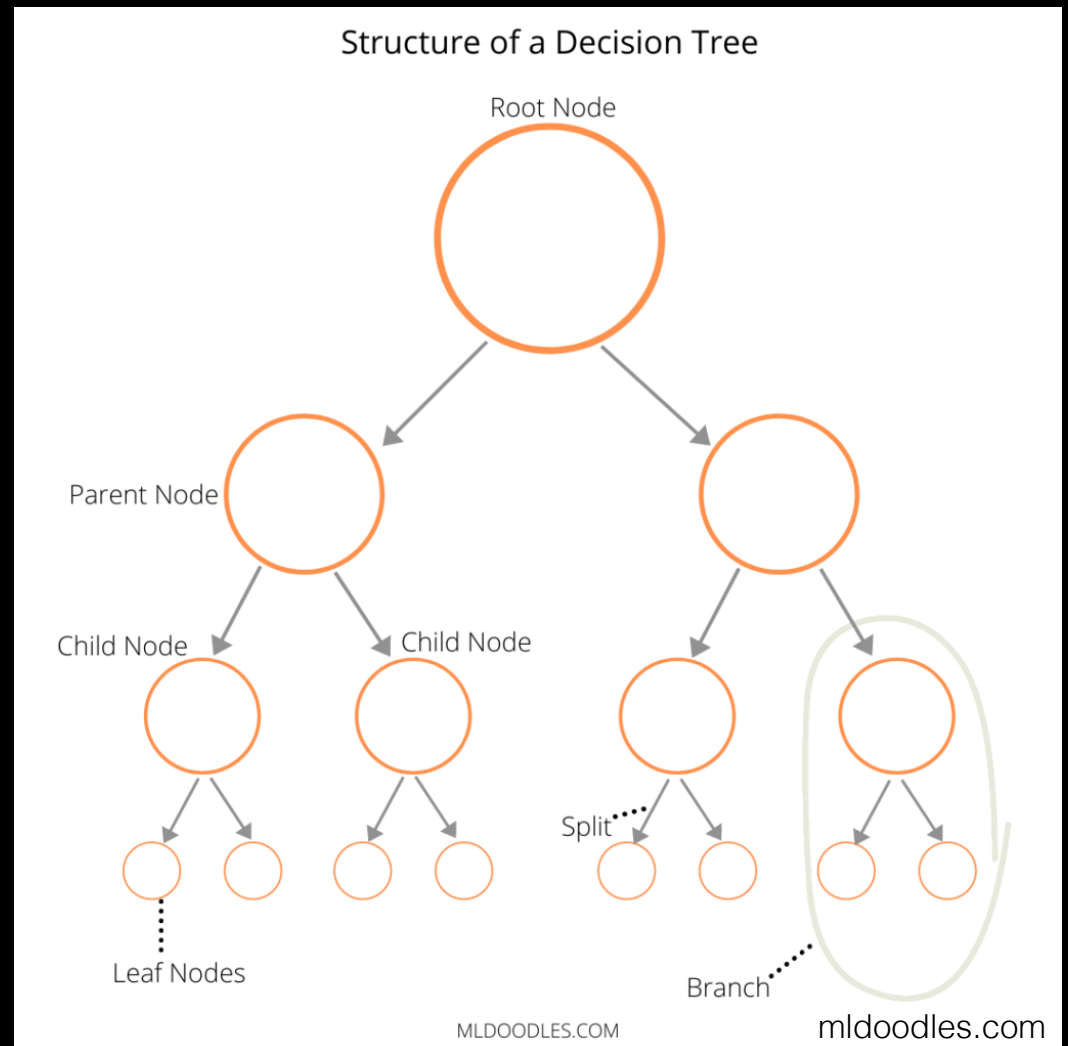
- KNN is one of the simplest forms of machine learning algorithms mostly used for classification. It **classifies the data point on how its neighbor is classified.**



townrdsdatascience.com

Decision Tree

- In decision tree, one makes decision using a tree-like structure. At each node, one of the features is selected and the branching occurs.



Naive Bayes

- Naive Bayes classifier is a probabilistic machine learning model which is based on the Bayes theorem

The diagram illustrates Bayes' Theorem with the following components and labels:

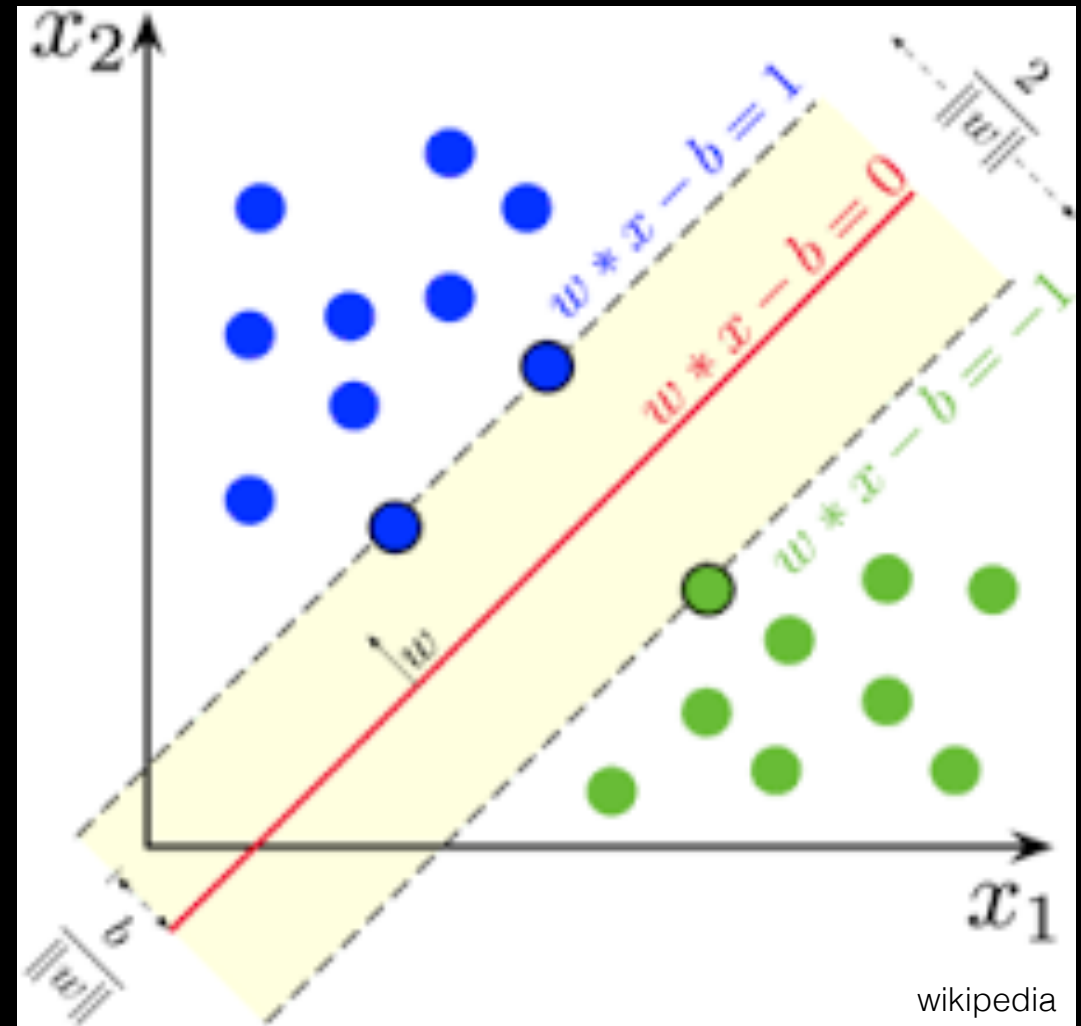
- Likelihood of the Evidence given that the Hypothesis is True**: $P(E|H)$ (indicated by a blue arrow pointing to the numerator's first term)
- Prior Probability of the Hypothesis**: $P(H)$ (indicated by a red arrow pointing to the numerator's second term)
- Posterior Probability of the Hypothesis given that the Evidence is True**: $P(H|E)$ (indicated by a blue arrow pointing to the left side of the equation)
- Prior Probability that the evidence is True**: $P(E)$ (indicated by a green arrow pointing to the denominator)

$$P(H|E) = \frac{P(E|H) * P(H)}{P(E)}$$

medium.com

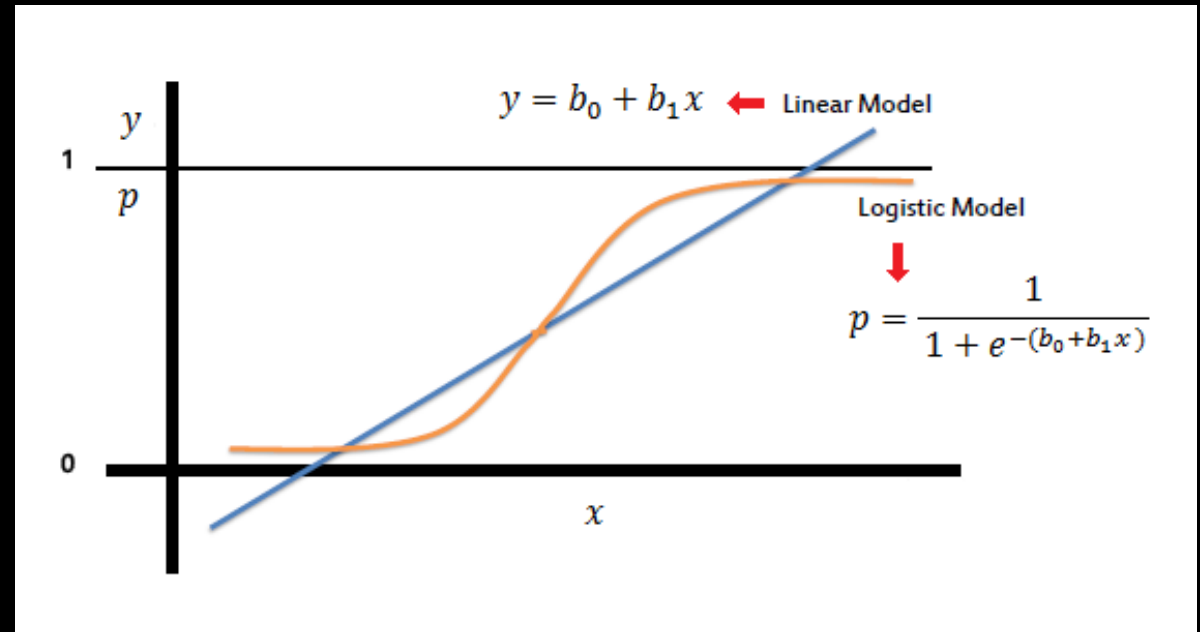
SVM

- **Support Vector Machine** is a classification based on finding a line that classifies the data points, maximises the margins



Logistic Regression

- Based on finding a line that separates the data points, in which a **logistic** function is applied on the top of the linear one so that one can decide on the basis of some final values which are in (0,1)



Fast Flavor Conversion (FFC)

- For training, we use analytical **maximum-entropy** distribution

$$f_\nu(\cos \theta_\nu) = \exp(-\eta + a \cos \theta_\nu)$$

Fast Flavor Conversion (FFC)

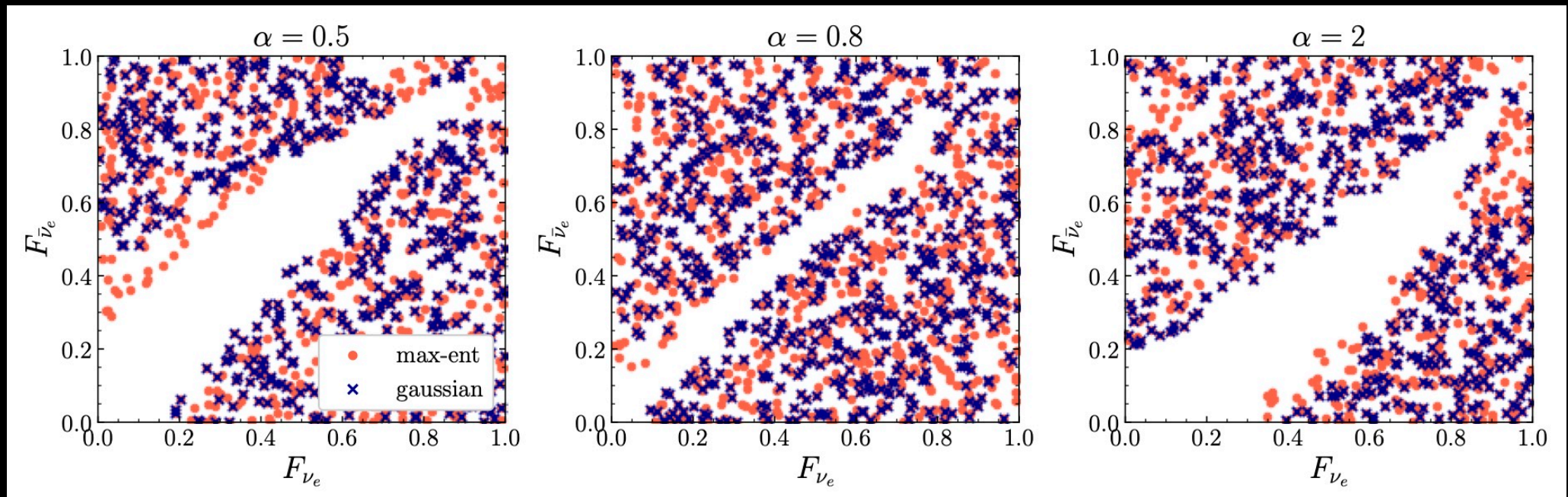
- For training, we use analytical **maximum-entropy** distribution

$$f_\nu(\cos \theta_\nu) = \exp(-\eta + a \cos \theta_\nu)$$

gaussian $f_\nu(\cos \theta_\nu) = \exp[-a(1 - \cos \theta_\nu)^2 + b]$

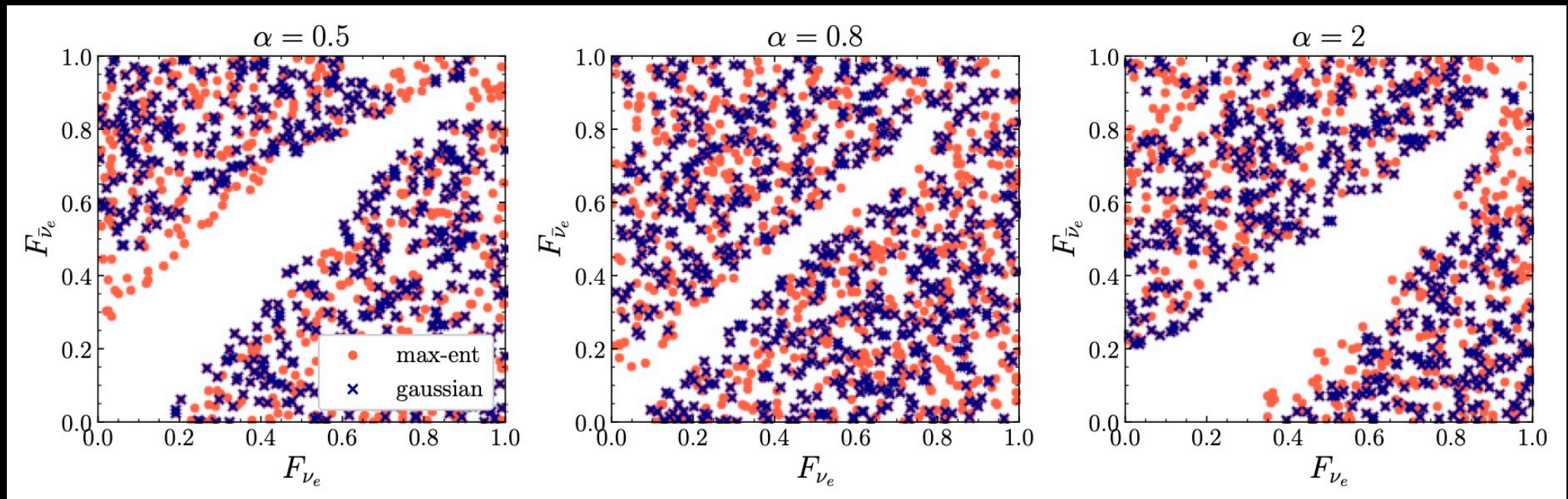
- We have **four** feature here: I_0 and I_1 for neutrinos and antineutrinos (one is **redundant**)

$$\alpha = \frac{I_0^{\bar{\nu}_e}}{I_0^{\nu_e}} \quad F_\nu = \frac{I_1}{I_0}$$



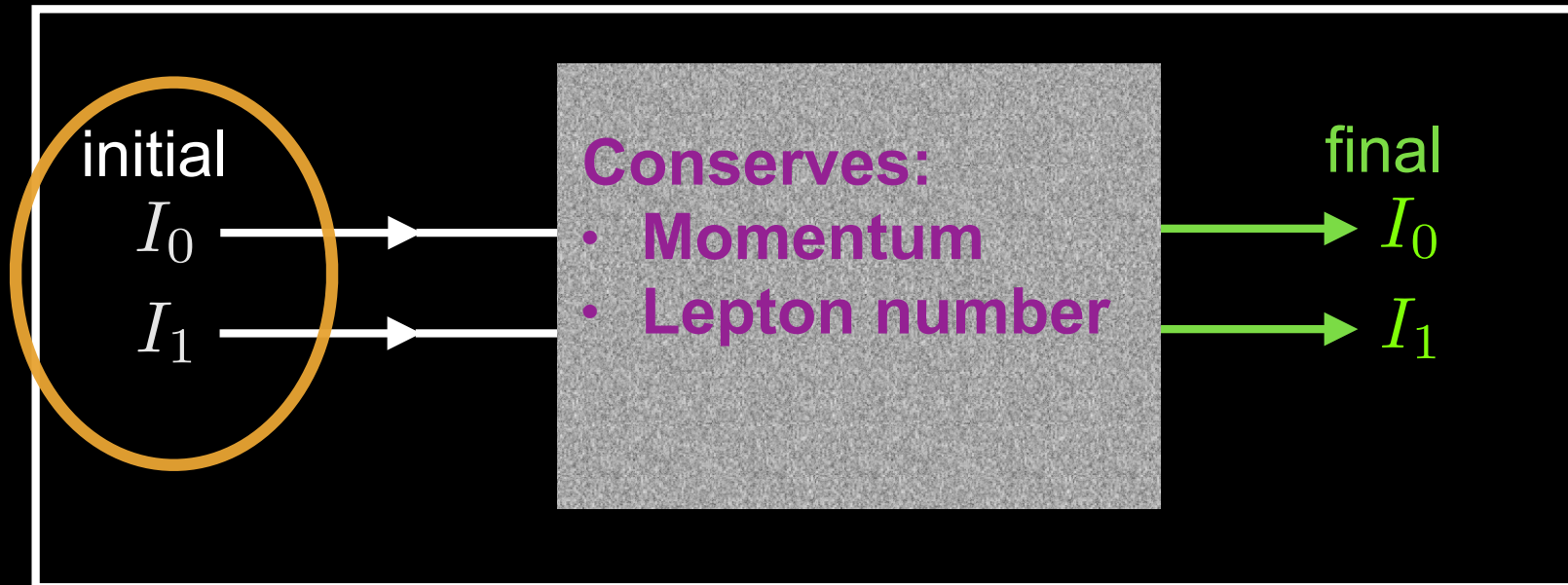
Fast Flavor Conversion (FFC)

- KNN accuracy $\sim 95\%$
- Decision Tree accuracy $\sim 92\%$
- Naive Bayes accuracy $\sim 90\%$
- SVM accuracy $\sim 94\%$
- Logistic Regression accuracy $\sim 94\%$



Machine Learning

- Machine learning methods prove to be very promising regarding the detection of FFI



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