

# Experimental status of nuclear shapes and shape coexistence for zirconium and ruthenium isotopes around A = 96

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1. June 2022





European Research Council

Established by the European Commission



**1** Experimental determination of nuclear deformation

- **2** Deformation in the A = 90 100 mass region
- 3 The case of <sup>96</sup>Ru and <sup>96</sup>Zr
- 4 Summary



# Experimental determination of nuclear deformation



# **Observations of deformation**

observations:

- electric quadrupole moments and quadrupole transition rates are orders of magnitude larger than single-particle estimates (quantum transition of a single proton)
  - $\rightarrow$  interpretation as collective excitations
- already deuteron has non-zero quadrupole moment → nuclear force non-spherical
- sequence of low-energy states J(J+1)
  - ightarrow quantum mechanical rotations
  - $\rightarrow$  breaking of spherical symmetry and deformation
- many physical observables can be interpreted as signs of deformation
- usually some degree of model dependence is involved in the analysis
- all nuclei are somewhat deformed, for  $^{208}$ Pb  $\beta_2 = 0.055$





$${\it R}( heta,\phi) = {\it R}_0\left(\sum_{\lambda=0}^\infty\sum_{\mu=-\lambda}^\lambda lpha_{\lambda\mu}\,{\it Y}_{\lambda\mu}( heta,\phi)
ight)$$

- $\blacksquare$  incompresibility of nuclear matter  $\rightarrow$  volume conservation
- dipole term ( $\lambda = 1$ ) just a shift of center of mass  $\rightarrow$  quadrupole term ( $\lambda = 2$ ) first important one



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- triaxial degrees of freedom:

$$\alpha_{02} = \beta \cos \gamma$$
  
$$\alpha_{22} = \alpha_{2-2} = \frac{1}{\sqrt{2}}\beta \sin \gamma$$

•  $\beta$  is the axial elongation,  $\gamma$  asymmetry from an axial shape

$$\beta = \frac{4}{3}\sqrt{\frac{\pi}{5}}\left(\frac{c-a}{R}\right)$$

• oblate eta < 0, prolate eta > 0





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# 🖪 🗲 🗴 🔹 Rotational model

- measuring  $\beta$  or  $\gamma$  is not possible
- need to use nuclear models to estimate the deformation from the data
- rotational model:

$$E(J) = \frac{\hbar^2}{2I} (J(J+1) + K(K+1))$$

8 + ---- 1024.6

6+ \_\_\_\_\_614.4

4<sup>+</sup> ----- 299.4 2<sup>+</sup> ----- 91.4

 with moment of inertia for an ellipsoid (rigid, first order)

$$I_{\text{rigid}} = \frac{2}{5} AMR_0^2 (1 + 0.31\beta)$$
 10<sup>+</sup> 1518.1

- increasing deformation  $\beta$  $\rightarrow$  smaller energy spacing
- assumption: constant I along band
- superposition of vibrational excitations below the pairing gap

9 + 1977.2  
8 + 1744.9  
7 + 1545.1  
6 + 1358.7  
5 + 1197.5  
4 + 1058.5  
3 + 946.3  
2 + 860.2  

$$K = 2 \gamma$$
 band with  
 $\hbar^2/2I = 13.9$  keV

$$6^{+} - 1706.7$$

$$4^{+} - 1469.7$$

$$2^{+} - 1314.6$$

$$0^{+} - 1246.1$$

$$K = 0 \beta \text{ band with}$$

$$\hbar^{2}/2I = 11.0 \text{ keV}$$

K = 0 gs band with  $\hbar^2/2I = 14.4$  keV

# 🖪 🚍 🗴 🔹 Rotational model

- experimental moments of inertia are intermediate between a rigid body and irrotational flow → nuclear superfluidity due to the pairing force
- rigid body with deformation  $\beta$

$$H_{\mathsf{rigid}} = rac{2}{5} \textit{AMR}_0^2 (1+0.31eta)$$

irrotational flow

$$I_{\rm irr}=rac{9}{8\pi}MR_0^2eta^2$$

experimental data approximated by

$$\textit{I}_{exp} = \frac{\hbar^2\beta^2\textit{A}^{7/3}}{400[\text{MeV}]}$$



- spectroscopy of first few excited states
- low  $E(2_1^+)$  indicates collective nature

energy ratio 
$$R_{4/2} = \frac{E(4_1^+)}{E(2_1^+)}$$
, for vibrational  $R_{4/2} = 2$ , for rotational  $R_{4/2} = 3.333$ 



# r 🖬 🖬 🛛 Charge radii

- detailed spectroscopy of the atomic spectrum allows to draw conclusions on the nuclear size
- mean square radius of a deformed nucleus:



smooth increase with mass

$$rac{\delta \langle r^2 
angle_{
m sph}}{\delta A} = rac{2}{5} R_0^2 A^{-1/3} \sim 0.1 \; {
m fm}^2 \; {
m for} \; A \sim 200$$



- $\blacksquare \beta$  is the charge deformation
- experimentally determined from isotope shifts (difference in optical transition frequency of two isotopes)
- for stable isotopes with electron scattering
- matter radii from interaction cross section measurements

electric quadrupole moment

$$eQ_0 = \int \left(3z^2 - r^2\right)\rho(r,\theta,\phi)\mathrm{d}^3r = \sqrt{\frac{16\pi}{5}}\int r^2 Y_{20}(\theta,\phi)\rho(r,\theta,\phi)\mathrm{d}^3r$$

intrinsic quadrupole moment

$$Q_0=ZR_0^2rac{3}{\sqrt{5\pi}}\left(eta_2+rac{2}{7}\sqrt{rac{5}{\pi}}eta_2^2+\cdots
ight)$$

spectroscopic quadrupole moment (observed in the lab)

$$Q_{\rm s} = rac{3K^2 - I(I+1)}{(I+1)(2I+3)}Q_0,$$
 implies  $Q_{\rm s} = 0$ , for  $I = 0$  or  $1/2$ 

hyperfine splitting depends on magnetic dipole and electric quadrupole coupling of electrons to the nuclear moments

$$E(F) = \frac{1}{2}AC + B\frac{3/4C(C+1) - I(I+1)J(J+1)}{2I(2I-1)J(2J-1)}, \text{ with } C = F(F+1) - I(I+1) - J(J+1)$$

*I* nuclear angular momentum, *J* electron angular momentum, *F* total angular momentum  $A = \mu_I B_e(0)/(IJ)$  and  $B = eQ_s V_{zz}(0)$  $B_e(0)$  magnetic field and  $V_{zz}(0)$  electric field gradient of the electron at the nucleus

Failure of the nuclear shell model to give correct quadrupole moments is in contrast to the situation with nuclear magnetic moments, which can all be accounted for by a suitable admixture of states of a single nucleon. In the shell model approximation, these large quadrupole moments must represent a considerable contribution from the protons in the closed shells. The polarization of this core would presumably require a sharing of angular momentum between the protons of the incomplete shell and those of the closed shells. The magnitude of the polarization, however, and the resulting large asymmetry of the nucleon distribution is hardly consistent with the single particle-central field quantization which is the basis of the shell structure model.

C. H. Townes, H. M. Foley, and W. Low, Phys. Rev. 76 (1949) 1415.



reduced transition probability

$$B(\Pi\lambda) = rac{|\langle I_i || \Pi\lambda || I_i 
angle|}{2I_i + 1}$$

■ large B(E2) values indicate similar structure of states

■ is related to the intrinsic quadrupole moment

$$eQ_{0} = \sqrt{\frac{16\pi}{5}} \frac{\langle l_{\rm f} ||E2||l_{\rm f}\rangle}{\sqrt{2l_{\rm f}+1} \langle l_{\rm f}K20|l_{\rm f}0\rangle}$$
$$B(E2; \ l_{\rm f} \rightarrow l_{\rm f}) = \frac{5}{16\pi} \left(eQ_{0}\right)^{2} \langle l_{\rm f}K20|l_{\rm f}0\rangle^{2}$$

in rotational model

$$B(E2; 0_1^+ \to 2_1^+) = \left(rac{3}{4\pi} ZeR^2 eta_2
ight)^2$$

reduced transition probability and lifetime are related:

$$B(E2) = \frac{8.177 \cdot 10^{-10}}{\tau E_{\gamma}^{5}} \frac{1}{1 + \alpha}$$

*E* in keV,  $\tau$  (partial) lifetime in s, *B*(*E*2) in  $e^2$ fm<sup>4</sup>,  $\alpha$  conversion coefficient



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# **IF If Transition strengths over the nuclear chart**

- extraction of the B(E2) values of require some modeling
- energies are a good indicator of nuclear structure

$$B(E2; 0_1^+ \rightarrow 2_1^+) = (124 \pm 41) \frac{Z^2}{E(2_1^+)A}$$

~

L. Grodzins, Phys. Lett. 2 (1962) 88.

energies not sensitive to the details of the wave function



# **IF If Transition strengths over the nuclear chart**

- Weisskopf units, single-particle estimate, how many nucleons participate in the excitation
- **assuming axial symmetry, deformation can be extracted from** B(E2) values

$$eta_2 = rac{4\pi}{3eZR^2}\sqrt{B(E2;\ 0^+_1 o 2^+_1)}$$

- $\beta = 0.3$  for well-deformed rare-earth and super-heavy nuclei
- lacksquare outliers with very large eta
  ightarrow limitations of the approximations made



probe of collective shape degrees of freedom

• excitation of the nucleus in the electromagnetic field of the target V(t)

$$\left(\frac{\mathrm{d}\sigma}{\mathrm{d}\Omega}\right)_{i\to f} = \left(\frac{\mathrm{d}\sigma}{\mathrm{d}\Omega}\right)_{\mathsf{Ruth}} |a_{i\to f}|^2$$

perturbation theory

$$a_{i 
ightarrow f} = rac{1}{i\hbar} \int_{-\infty}^{\infty} \mathrm{d}t \; e^{i\omega t} \; \langle f | V(t) | i 
angle$$

$$\sigma(\pi\lambda)_{i
ightarrow f} \propto B(\pi\lambda; \ I_i 
ightarrow I_f)$$

- other processes contribute to the excitation
- for pure Coulomb excitation, the contribution from nuclear processes has to be eliminated



 $\theta$  scattering angle b impact parameter a distance of closest approach

# **G S** it Coulomb excitation

- at high beam energies, above Coulomb barrier, main uncertainties come from nuclear excitations and reaction modeling, few percent for B(E2)
- excitation is limited to 2<sup>+</sup> states which can feed the state of interest

$$\sigma(\pi\lambda)_{i\to f} \propto B(\pi\lambda; I_i \to I_f)$$

- at Coulomb barrier energies, longer interaction times allow for multi-step processes  $\rightarrow$  excitation of 4<sup>+</sup>, 2<sup>+</sup><sub>2</sub>, 0<sup>+</sup><sub>2</sub>, etc states
- in addition the cross section becomes sensitive to the static quadrupole moment through the re-orientation effect











# Coulomb excitation

- full two-dimensional  $\chi^2$  surface for  $\langle 2_1^+ || E2 || 0_1^+ \rangle$  and  $\langle 2_1^+ || E2 || 2_1^+ \rangle$  shows the correlation of the two values
- combination with other observable, here τ from direct lifetime measurement allows for determination of sign and magnitude of the matrix elements

M. Zielinska et al., Eur. Phys. J. A 52 (2016) 99.

- remember: quadrupole moments from hyperfine studies are only for J > 1/2 and ground or long-lived states
- only way to access the quadrupole moments of excited states
- sensitivity depends on the complexity of the level scheme and statistics
- Coulomb excitation also provides access to E3 moments



# G S u Quadrupole invariants

quadrupole rotationally invariant sum rules provide a more model independent measure of the shape

K. Kumar, Phys. Rev. Lett. 28 (1972) 249, D. Cline, Annu. Rev. Nucl. Part. Sci. 36 (1986) 681.



J. Henderson, Phys. Rev. C 102 (2020) 054306.

• charge distribution  $E(\lambda, \mu)$  in the intrinsic frame:  $E(2,0) = Q\cos(\delta), E(2,\pm 1) = 0, E(2,\pm 2) = \frac{1}{\sqrt{2}}Q\sin(\delta)$ 

#### invariants

$$\langle Q^2 \rangle = \sqrt{\frac{5}{2I_s + 1}} \sum_i \langle s ||E2||i\rangle \langle i||E2||s\rangle \begin{cases} 2 & 2 & 0\\ I_s & I_s & I_i \end{cases}$$

$$egin{aligned} &\langle Q^3 cos(3\delta) 
angle = -\sqrt{rac{35}{2}}rac{1}{2l_s+1} imes \ &\sum_{i,j} \langle s || E2 || i 
angle \langle i || E2 || j 
angle \langle j || E2 || s 
angle egin{cases} 2 & 2 \ l_s & l_j \ l_s \end{bmatrix} \end{aligned}$$

relates to deformation parameter

$$\langle {\cal Q}^2 
angle = \left( {3 \over 4\pi} Z {\cal R}_0^3 
ight)^2 \langle \beta^2 
angle, \qquad \delta = \gamma$$

# 🖬 🖬 👖 🛛 Quadrupole invariants

 $\blacksquare$  higher order products give also access to the fluctuations of Q and  $\delta$ 

$$\sigma(Q^2) = \sqrt{\langle Q^4 
angle - \langle Q^2 
angle^2} \quad ext{ and } \quad \sigma(\cos(3\delta)) = \sqrt{rac{\langle Q^6 \cos^2(3\delta) 
angle}{\langle Q^6 
angle} - \left(rac{\langle Q \cos(3\delta) 
angle}{\langle Q^2 
angle^{3/2}}
ight)^2}$$

experimentally challenging as many matrix elements, with sign, have to be measured



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# Deformation in the $A \sim 100$ region



• two-neutrons separation energy  $S_{2n}$  drops at sub-shell closures N = 56,58, but rises at N = 60 $\rightarrow$  additional binding from deformation

I jump in charge radius at N=60
ightarrow sudden increase in apparent size arises from deformation

similar features observed in neighboring isotopic chains

• but not in Kr or Mo  $\rightarrow$  island of deformation

data on isomeric states suggests shape coexistence

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#### Spectroscopy of excited states



- high energies of  ${}^{96,98}$ Zr  $\rightarrow$  sub-shell closures of the 1 $d_{5/2}$  and  $2s_{1/2}$
- sharp drop at  $N = 60 \rightarrow$  spherical-deformed shape transition
- much smoother decrease for Mo and Kr
- increase in collectivity B(E2) rises from to  $\sim$  100 W.u.
- gradual transition to deformation for Mo and Kr

**R**<sub>4/2</sub> ratio consistent with deformed rotor at and beyond N = 60

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#### Shape coexistence



- similar drop of the energy of the excited 0<sup>+</sup> state
- $B(E2; 0^+_2 \rightarrow 2+_2)$  very small in <sup>98</sup>Sr at N = 60
- shape change of the ground state and inversion of configurations
- most rapid onset of deformation in the nuclear chart
- shape coexistence of two or even three configurations of different deformation



18+ 7522

#### Shape coexistence

8726

7597

• at N = 58 excited strongly deformed band  $R_{4/2} \sim 3$ 

■ large electric monopole transitions (large difference in deformation)



K. Heyde, J. L. Wood, Rev. Mod. Phys. 83 (2011) 1467.



#### Shape coexistence

0726

	0720	at $N = 58$ excited strongly deformed band $R_{4/2} \sim 3$		
<u>18</u> <sup>+</sup> 7522	7597		isitions (large difference	an delormation)
<u>16<sup>+</sup> 6515</u>	<u>16<sup>+</sup> 6540</u> or 15 <sup>-</sup>	■ at <i>N</i> = 60, ground state is deformed	B (E2) W.u. ρ <sup>2</sup> (E0) x 10 <sup>3</sup>	$6^+$ 1856 $8^+$ 1687
14 <sup>+</sup> 5593	<u>14</u> <sup>+</sup> 5590	■ <i>R</i> <sub>4/2</sub> = 3.0 for <sup>98</sup> Sr	<u>8<sup>+</sup> 1432</u>	$4^+$ 1415
		■ large $B(E2)$ values		$2^+$ 1196
12+ 4721	12 4756			$6^+$ 1062
$10^+$ 3886	$10^+$ 3986		$6^+$ 867 $2^+$ 871	$\frac{2^+ 879}{0^+ 829}$
<u>8<sup>+</sup> 3125</u>	<u>8<sup>+</sup> 3216</u>			$\frac{4^+}{564}$
<u>6+ 2466</u>	<u>4+ 2277</u> <u>6<sup>+</sup> 2491</u>		$\frac{4}{127}$ o <sup>+</sup> 215	$2^{+}$ $331$
$\frac{4^{++} 2120}{4^{+} 1793}$ $\frac{4^{+} 1975}{2^{+} 1628}$	$\frac{0^{+}\ 1859}{2^{+}\ 1744}$ $\frac{4^{+}\ 2048}{2^{+}\ 1843}$ $\frac{4^{+}\ 1843}{2^{+}\ 1843}$		$2^+$ 144 515 57	
17 185 185	$2^+$ 1223		$0^+$ $96$ $0$	$0^+$ 0 U
5	0+ 853		<sup>98</sup> 38 <sup>Sr</sup> 60	$^{100}_{40}$ Zr <sub>60</sub>
	<u>0</u> <sup>+</sup> 0			
<sup>96</sup> <sub>38</sub> Sr <sub>58</sub>	$^{98}_{40}$ Zr <sub>58</sub>	K. Heyde, J. L. Wood, Rev. Mod. Phys. 83 (2011) 1467.		

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<u>0+ 1229</u> <u>2+ 815</u>

#### 🖬 🖬 👖 Shape coexistence in Sr nuclei





#### **Federman-Pittel Mechanism**



- $^{90}$ Zr spherical, closed-shell Z = 40, N = 50
- microscopic, shell model description of deformation

P. Federman and S. Pittel, Phys. Lett. B **69** (1977) 385, Phys. Rev. C **20** (1979) 820.

excitations to the neutron  $0g_{7/2}$  orbital  $\rightarrow$  residual p-n interaction lowers proton  $0g_{9/2}$  orbital

- increased occupation of the  $\pi 0g_{9/2}$  orbital  $\rightarrow p-n$  correlations dominate over pairing correlations
- deformed excited configurations at high excitation energy  $E_{def} \gg E_{sph}$
- <sup>100</sup>Zr: drop in excitation energy, deformed ground state



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#### Large-scale shell model calculations







E (MeV)

#### Large-scale shell model calculations



octupole 3<sup>-</sup> state underestimated

651

0.27

# Monte-Carlo shell model calculations

- microscopic description of shapes change as a function of proton or neutron number
- proton-neutron interaction changes the ordering and spacing of levels
- (near-) degeneracy triggers symmetry breaking and deformation

calculations reproduce the abrupt shape change in Zr

talk by Y. Tsunoda tomorrow

T. Togashi et al., Phys. Rev. Lett. 117 (2016) 172502.



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T. Togashi et al., Phys. Rev. Lett. 117 (2016) 172502.





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# The case of <sup>96</sup>Ru and <sup>96</sup>Zr



■ high  $2_1^+$  state, with small  $\beta = 0.062(3)$  from  $B(E2; 0_1^+ \rightarrow 2_1^+) = 2.3(3)$  W.u.

G. Kumbartzki et al., Phys. Lett. B 562 (2003) 193.

# F S S M Properties of <sup>96</sup>Zr

- only one measurement for  $B(E2; 0_1^+ \rightarrow 2_1^+)$  but compilations also cite a publication for 1965 "Coulomb Excitation of the First 2<sup>+</sup> Levels of <sup>90</sup>Zr and <sup>96</sup>Zr" with an almost two times larger B(E2)S. Raman et al., At. Data Nucl. Data Tables **78** (2001) 1, Y. P. Gangrskii, I. K. Lemberg, Yadern. Fiz. **1** (1965) 1025.
- quadrupole moment and branch ratio to  $0^+_2$  unknown
- 2<sup>+</sup><sub>2</sub> state populated using electron scattering
- $B(E2; 0_1^+ \rightarrow 2_2^+)$  can be extracted relative to the  $B(E2; 0_1^+ \rightarrow 2_1^+)$  value
- known decay branching ratios of  $2^+_2$  allow to extract  $B(E2; 2^+_2 \rightarrow 0^+_2) = 36(11)$  W.u.
- collective, similar deformation for 2<sup>+</sup><sub>2</sub> and 0<sup>+</sup><sub>2</sub>, assuming rigid axial rotor β = 0.24
- two decoupled configurations with different deformation
- supported by calculations and two-state mixing modelshape coexistence

C. Kremer et al., Phys. Rev. Lett. 117 (2016) 172503.



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- shape coexistence

C. Kremer et al., Phys. Rev. Lett. 117 (2016) 172503.



# **EG ES I** Octupole deformation of <sup>96</sup>Zr

- octupole correlations are dominant in regions where  $\Delta I = \Delta j = 3$  orbitals are close to the Fermi surface
- proton  $1p_{3/2} 0g_{9/2}$  and  $1d_{5/2} 0h_{11/2}$  excitations across Z = 40 and N = 56
- large  $B(E3; 3^-_1 \rightarrow 0^+_1)$  values from lifetime measurements and proton inelastic scattering



yields  $eta_3 \sim$  0.25

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# **I** = = **i** Structure of <sup>96</sup>Ru

18+----8205.7



H. Klein et al., Phys. Rev. C 65 (2002) 044315.

- $B(E2; 0_1^+ \rightarrow 2_1^+) = 18.2$  W.u.
- c.f. 2.3 W.u. for <sup>96</sup>Zr
- **\beta\_2 = 0.154**
- moderately deformed ground state band
- Q = -0.13(9) prolate, but with very large uncertainty
   S. Landsberger et al., Phys. Rev. C 21 (1980) 588.
- excited 0<sup>+</sup> state known
- many lifetimes known
- transfer reactions (p, d) shows distribution of strength over several levels
  - ightarrow consistent with deformation

**G Summary** 



are two very different nuclei

# Thank you for your attention