

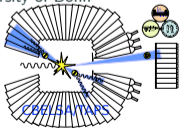
η and η' physics at ELSA

EMMI Workshop "Meson and Hyperon Interactions with Nuclei" 2022

Farah Afzal for the CBELSA/TAPS collaboration

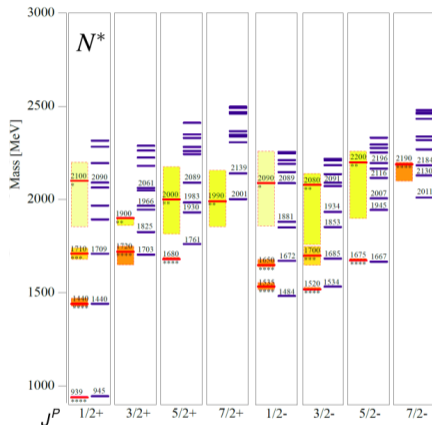
15.09.2022

University of Bonn



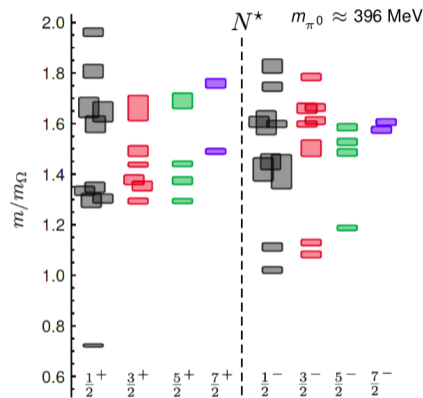
Baryon spectroscopy

Quark model with experimental data



[M. Ronninger and B. Metsch, Eur. Phys. J. A 47 (2011) 162]

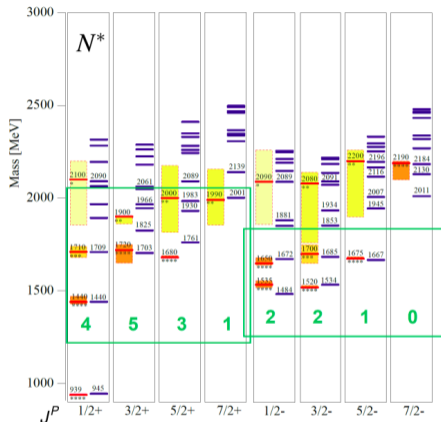
Lattice QCD calculations



[R. G. Edwards et al., Phys. Rev. D 84 (2011) 074508]

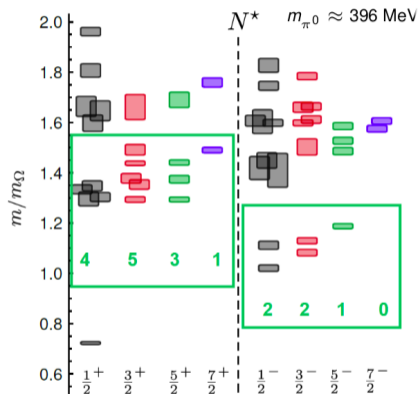
- Discrepancy between theory and experiment: missing resonances, ordering of states

Quark model with experimental data



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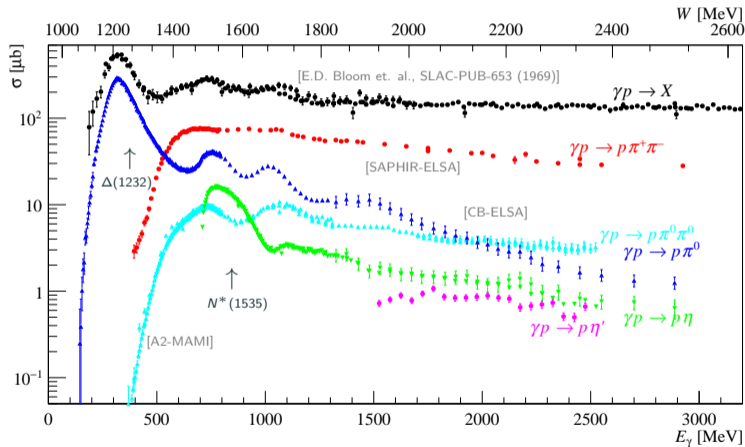
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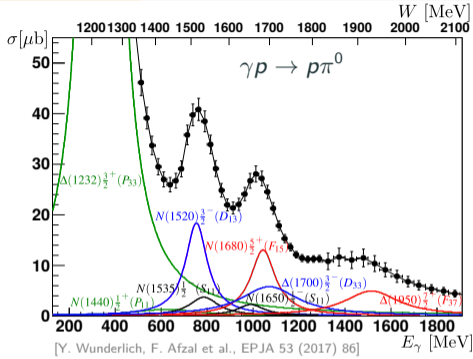
- Discrepancy between theory and experiment: missing resonances, ordering of states
- most resonances observed in πN scattering \rightarrow experimental bias?

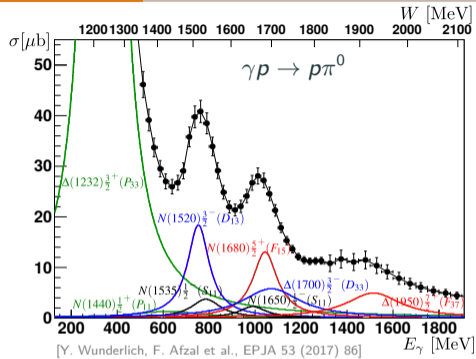
Worldwide effort to get high precision data (ELSA, MAMI, JLab, SPring-8, ...)



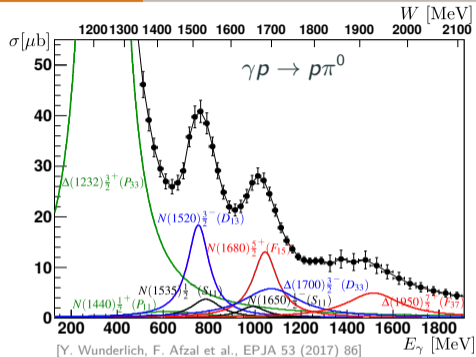
[A. Thiel, F. Afzal, Y. Wunderlich, Prog. Part. Nucl. Phys. 125 (2022) 103949]

- Photoproduction reactions are an excellent tool to probe excitation spectra!
- Resonances contribute with different strength to distinct channels
- How can we disentangle contributing resonances?





$$\frac{d\sigma}{d\Omega_0}(W, \theta) \propto \sum_{\text{spins}} | \langle f | \mathcal{F} | i \rangle |^2$$

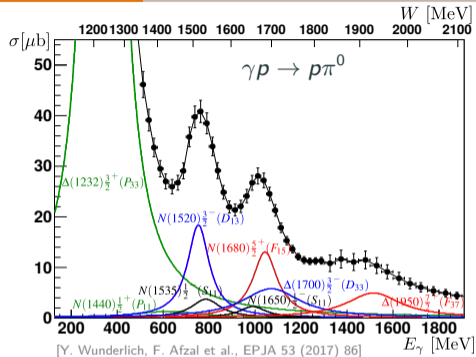


$$\frac{d\sigma}{d\Omega_0}(W, \theta) \propto \sum_{\text{spins}} | \langle f | \mathcal{F} | i \rangle |^2$$

Photoproduction amplitude \mathcal{F}

\leftrightarrow 4 complex amplitudes

e.g. CGLN amplitudes: F_1, F_2, F_3, F_4



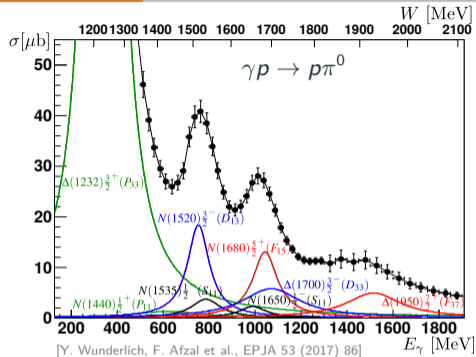
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- PWA: e.g. $F_1 = \sum_{l=0}^{\infty} (lM_{l+} + E_{l+})P'_{l+1} + [(l+1)M_{l-} + E_{l-}]P'_{l-1}$
 - $E_{l\pm}(W), M_{l\pm}(W)$: Multipoles
 - $P'_{l\pm 1}(\cos \theta_{cm})$: Legendre polynomials



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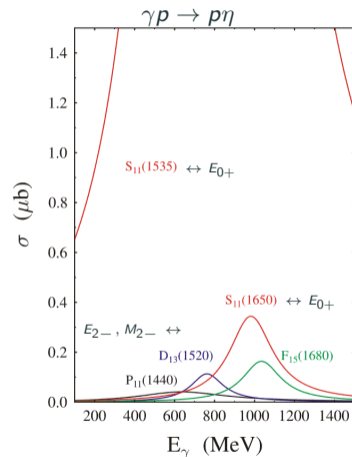
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 - $E_{l\pm}(W), M_{l\pm}(W)$: Multipoles
 - $P'_{l\pm 1}(\cos \theta_{cm})$: Legendre polynomials
- $\sigma \sim |E_{0+}|^2 + |E_{1+}|^2 + |M_{1+}|^2 + |M_{1-}|^2 + \dots$
 - \rightarrow unpolarized cross section is sensitive to dominant contributing resonances

Polarization observables in the 2-body kinematic system for the photoproduction of a pseudoscalar meson

Photon polarization		Target polarization			Recoil nucleon polarization			Target and recoil polarizations			
		X	Y	Z _(beam)	X'	Y'	Z'	X'	X'	Z'	Z'
unpolarized	σ	-	T	-	-	P	-	$T_{x'}$	$L_{x'}$	$T_{z'}$	$L_{z'}$
linear	$-\Sigma$	H	(-P)	-G	$O_{x'}$	(-T)	$O_{z'}$	(-L _z)	(T _z)	(L _x)	(-T _x)
circular	-	F	-	-E	$C_{x'}$	-	$C_{z'}$	-	-	-	-

σ, Σ, T, P + 4 double pol. observables needed for a unique solution

[W. Chiang and F. Tabakin, Phys. Rev., C55 (1997) 2054-2066]



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Photon polarization		Target polarization	Recoil nucleon polarization	Target and recoil polarizations
		X Y Z _(beam)	X' Y' Z'	X' X' Z' Z' X Z X Z
unpolarized	σ	- T -	- P -	$T_{x'}$ $L_{x'}$ $T_{z'}$ $L_{z'}$
linear	$-\Sigma$	H (-P) -G	$O_{x'}$ (-T) $O_{z'}$	(-L _z) (T _z) (L _x) (-T _x)
circular	-	F - -E	$C_{x'}$ - $C_{z'}$	- - - -

$\sigma, \Sigma, T, P + 4$ double pol. observables needed for a unique solution

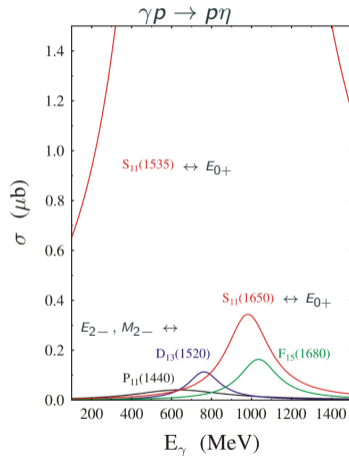
[W. Chiang and F. Tabakin, Phys. Rev., C55 (1997) 2054-2066]

$$\sigma \sim |E_{0+}|^2 + |E_{1+}|^2 + |M_{1+}|^2 + |M_{1-}|^2 + \dots$$

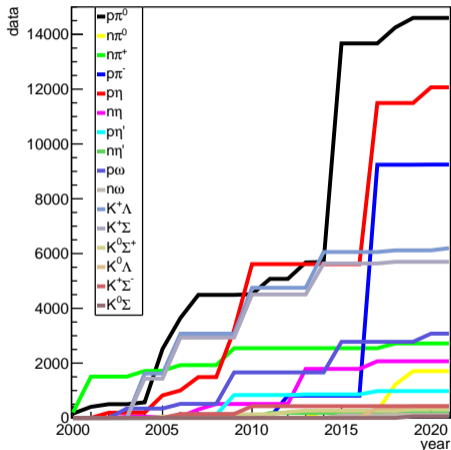
$$\Sigma \sim \underbrace{-2E_{0+}^* E_{2+} + 2E_{0+}^* E_{2-} - 2E_{0+}^* M_{2+} + 2E_{0+}^* M_{2-}}_{\langle S, D \rangle} + \dots$$

→ Polarization observables are sensitive to interference terms!

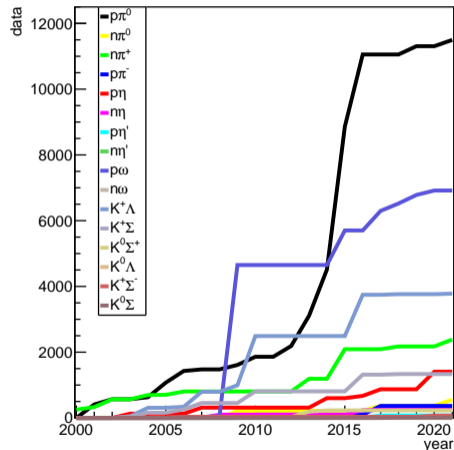
→ Interferences with the dominant S-wave (E_{0+}) important in η photoproduction!



Unpolarized cross section



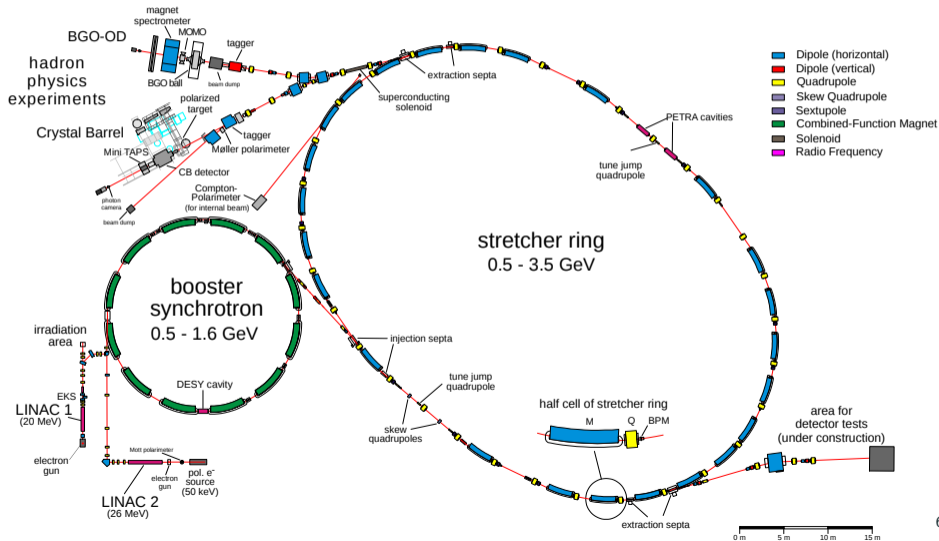
Polarization observables



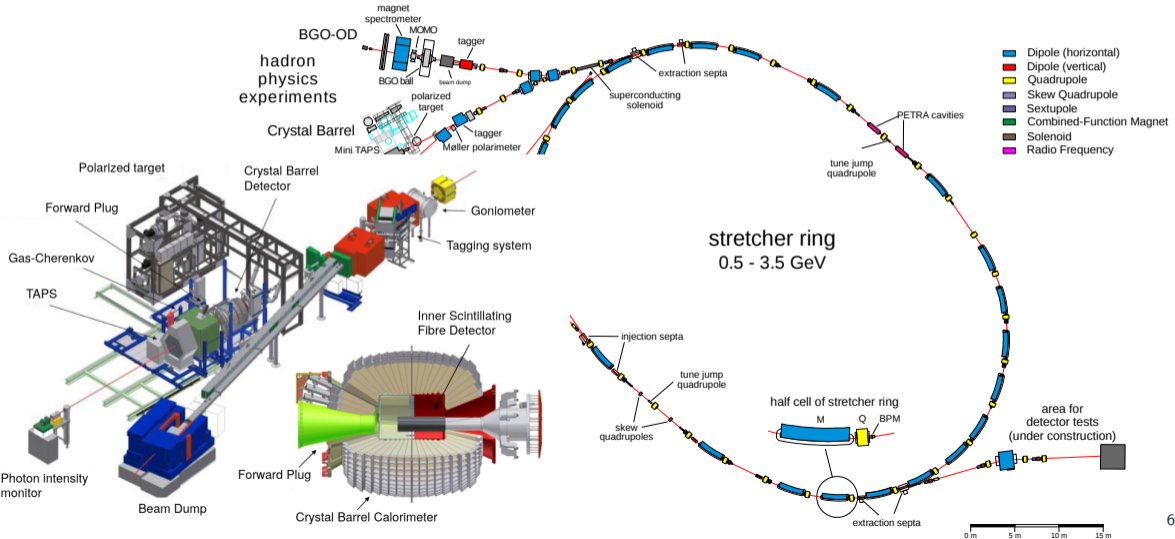
[A. Thiel, F. Afzal, Y. Wunderlich, Prog. Part. Nucl. Phys. 125 (2022) 103949]

Results from ELSA

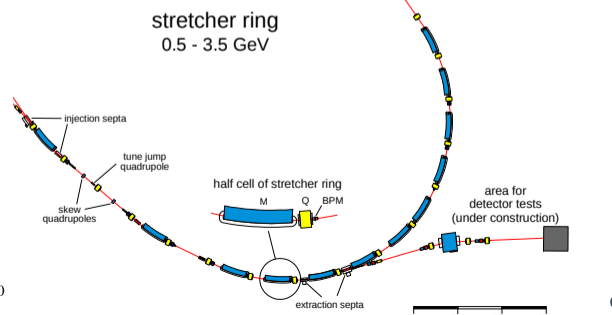
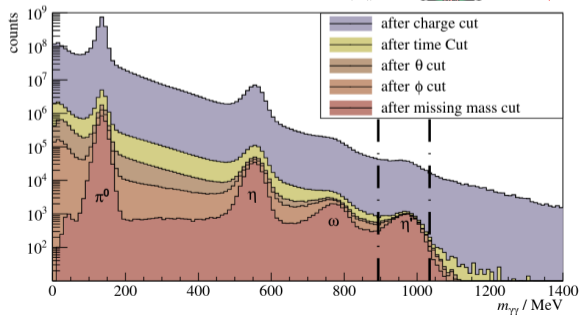
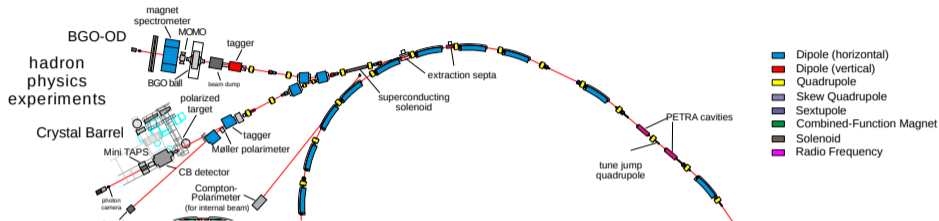
Physics Institute, University of Bonn



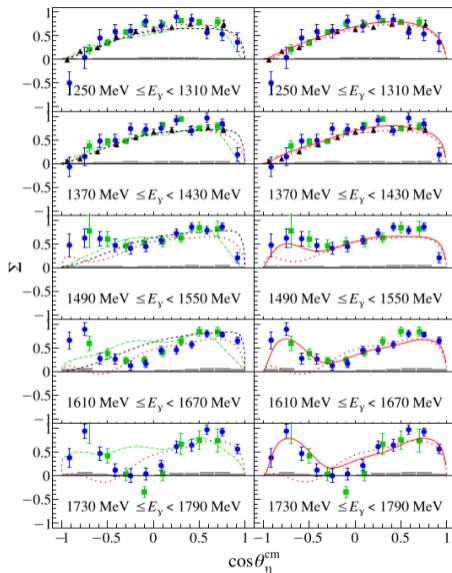
Physics Institute, University of Bonn



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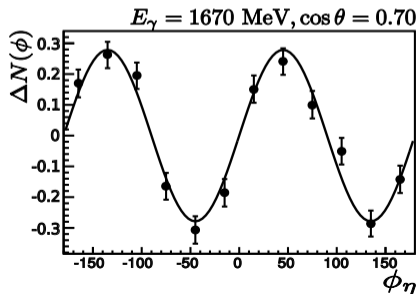
η photoproduction off protons



[F. Afzal et al., Phys. Rev. Lett. 125, 152002 (2020)]

- CBELSA/TAPS data (F. Afzal et al.)
- ▲ GRAAL data (O. Bartalini et al., Eur. Phys. J. A33 (2007) 169)
- CLAS data (P. Collins et al., Phys. Lett. B 771 (2017) 213-221)
- BnGa-2014-02 -.-.-.- JüBo-2015-FitB - - - ηMAID
- BnGa-2019

$$\Delta N = \frac{N_{-45^\circ} - N_{+45^\circ}}{N_{-45^\circ} + N_{+45^\circ}} = p_\gamma^{\text{lin}} \Sigma \sin(2\phi)$$



$$\check{\Sigma}(W, \cos \theta) = \Sigma(W, \cos \theta) \cdot \frac{d\sigma}{d\Omega}(W, \cos \theta) = \sum_{k=2}^{2L_{\max}} (a_{L_{\max}}(W))_k^{\check{\Sigma}} \cdot P_k^2(\cos \theta), \text{ i.e. } L_{\max} = 2;$$

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$(a_{L_{\max}})_k^{\check{\Sigma}}$ defined by matrices with $\langle \ell_1, \ell_2 \rangle$ -interference blocks

$$(\partial_2)_2^{\check{\Sigma}} = \left[\begin{array}{cccc} E_{0+}^* & E_{1+}^* & \dots & M_{2-}^* \end{array} \right] \left[\begin{array}{cccc|cccc} 0 & 0 & 0 & 0 & \frac{1}{2} & \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} \\ 0 & -\frac{3}{2} & \frac{1}{2} & -\frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & -\frac{1}{2} & \frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ \hline \frac{1}{7} & 0 & 0 & 0 & -\frac{36}{7} & -\frac{1}{7} & \frac{9}{7} & -\frac{9}{7} \\ \frac{1}{2} & 0 & 0 & 0 & -\frac{1}{7} & -\frac{1}{2} & -\frac{1}{2} & \frac{1}{7} \\ -\frac{1}{2} & 0 & 0 & 0 & \frac{9}{7} & -\frac{1}{2} & \frac{18}{7} & \frac{9}{14} \\ \frac{1}{2} & 0 & 0 & 0 & -\frac{9}{7} & \frac{1}{2} & \frac{9}{14} & \frac{3}{2} \end{array} \right] \left[\begin{array}{c} E_{0+} \\ E_{1+} \\ M_{1+} \\ M_{1-} \\ E_{2+} \\ E_{2-} \\ M_{2+} \\ M_{2-} \end{array} \right]$$

$$\check{\Sigma}(W, \cos \theta) = \Sigma(W, \cos \theta) \cdot \frac{d\sigma}{d\Omega}(W, \cos \theta) = \sum_{k=2}^{2L_{\max}} (a_{L_{\max}}(W))_k^{\check{\Sigma}} \cdot P_k^2(\cos \theta), \text{ i.e. } L_{\max} = 2;$$

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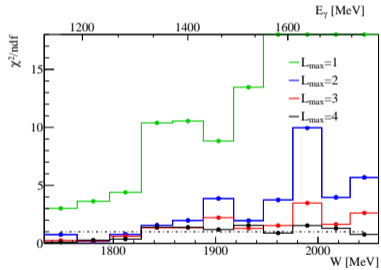
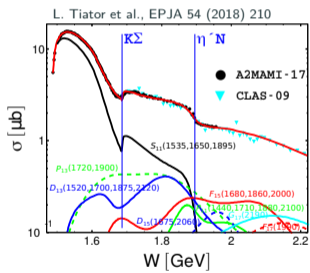
$$\begin{aligned}
 \underline{(\partial_2)}_2^{\check{\Sigma}} &= \begin{bmatrix} E_{0+}^* & E_{1+}^* & \dots & M_{2-}^* \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 0 & \frac{1}{2} & \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} \\ 0 & -\frac{3}{2} & \frac{1}{2} & -\frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & -\frac{1}{2} & \frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ \hline \frac{1}{7} & 0 & 0 & 0 & -\frac{36}{7} & -\frac{1}{7} & \frac{9}{7} & -\frac{9}{7} \\ \frac{1}{2} & 0 & 0 & 0 & -\frac{1}{7} & -\frac{1}{2} & -\frac{1}{2} & \frac{1}{7} \\ -\frac{1}{2} & 0 & 0 & 0 & \frac{9}{7} & -\frac{1}{2} & \frac{18}{7} & \frac{9}{14} \\ \frac{1}{2} & 0 & 0 & 0 & -\frac{9}{7} & \frac{1}{2} & \frac{9}{14} & \frac{3}{2} \end{bmatrix} \begin{bmatrix} E_{0+} \\ E_{1+} \\ M_{1+} \\ M_{1-} \\ E_{2+} \\ E_{2-} \\ M_{2+} \\ M_{2-} \end{bmatrix} \\
 &= \frac{1}{14} \left[E_{2-}^* \left(-7E_{2-} + 7E_{0+} - 2E_{2+} + 7M_{2-} - 7M_{2+} \right) + 7E_{0+}^* \left(E_{2-} + E_{2+} + M_{2-} - M_{2+} \right) \right. \\
 &\quad + E_{2+}^* \left(-2E_{2-} + 7E_{0+} - 18(4E_{2+} + M_{2-} - M_{2+}) \right) + M_{2-}^* \left(7E_{2-} + 7E_{0+} - 18E_{2+} \right. \\
 &\quad \left. + 21M_{2-} + 9M_{2+} \right) + M_{2+}^* \left(-7E_{2-} - 7E_{0+} + 9(2E_{2+} + M_{2-} + 4M_{2+}) \right) \\
 &\quad \left. + 7 \left(E_{1+}^* \left(-3E_{1+} - M_{1-} + M_{1+} \right) + M_{1-}^* \left(M_{1+} - E_{1+} \right) + M_{1+}^* \left(E_{1+} + M_{1-} + M_{1+} \right) \right) \right]
 \end{aligned}$$

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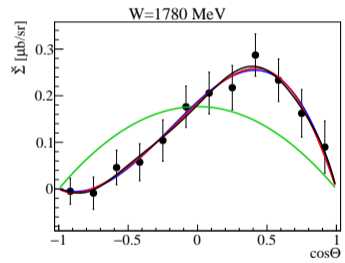
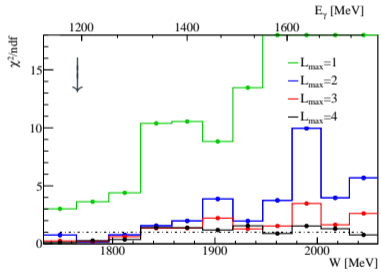
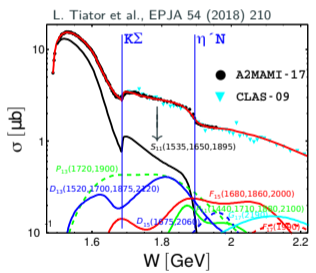
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 &= \langle P, P \rangle + \langle S, D \rangle + \langle D, D \rangle
 \end{aligned}$$

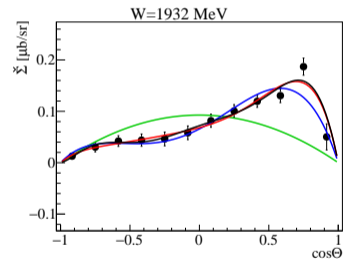
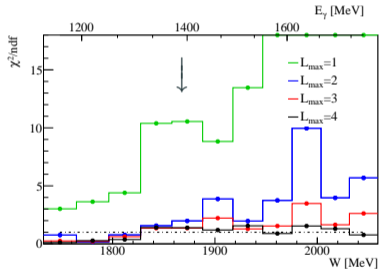
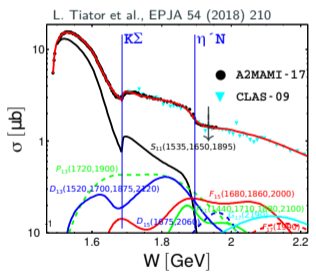
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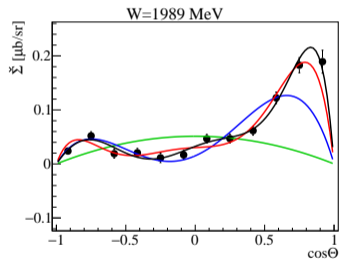
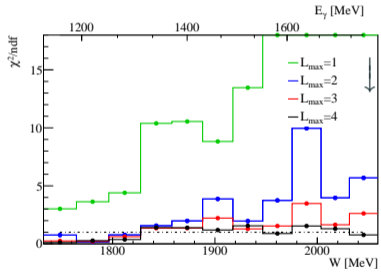
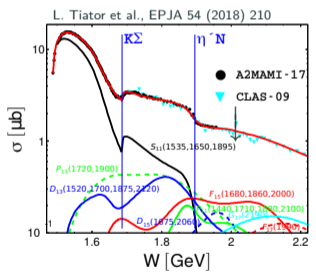
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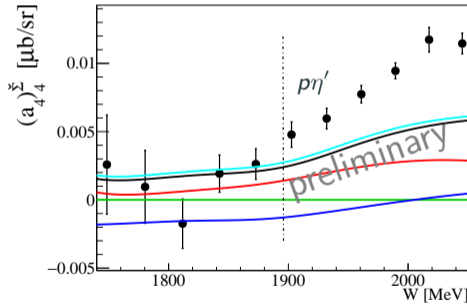


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$N(1895) \frac{1}{2}^- (S_{11})$

$N(2190) \frac{7}{2}^- (G_{17})$

Compare extracted fit coefficient to BnGa-2014-02 prediction

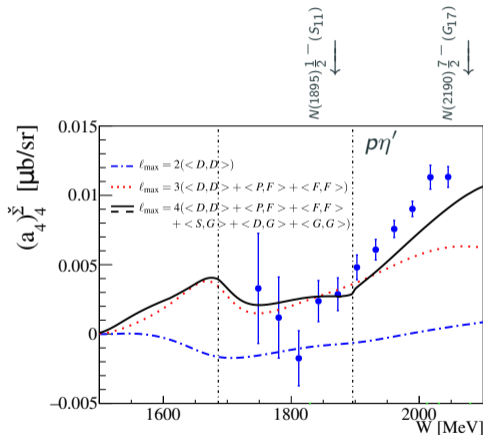


$$(a_5^{\check{\Sigma}})_4 = \langle D, D \rangle$$

- + $\langle P, F \rangle + \langle F, F \rangle$ —
- + $\langle \mathbf{S}, \mathbf{G} \rangle + \langle D, G \rangle + \langle G, G \rangle$ —
- + $\langle P, H \rangle + \langle F, H \rangle + \langle H, H \rangle$ —

$p\eta'$ channel needs to be included in PWA to describe data
 Evidence for $N(1895) \frac{1}{2}^- (S_{11})$ resonance due to strong $p\eta'$ cusp in $p\eta$ S wave

$$\check{\Sigma}(W, \cos \theta) = \Sigma(W, \cos \theta) \cdot \frac{d\Omega}{d\Omega}(W, \cos \theta) = \sum_{k=2}^{2L_{\max}} (a_L(W))_k \cdot P_k^2(\cos \theta)$$



Compare extracted fit coefficient to BnGa-2019 solution

$$(a_5)_{4}^{\check{\Sigma}} = \langle D, D \rangle \quad \text{--- blue ---}$$

$$+ \langle P, F \rangle + \langle F, F \rangle \quad \text{--- red ---}$$

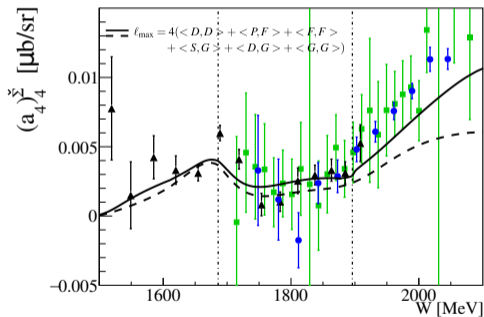
$$+ \langle S, G \rangle + \langle D, G \rangle + \langle G, G \rangle \quad \text{--- black ---}$$

F. Afzal et al., Phys. Rev. Lett. 125, 152002 (2020)

$p\eta'$ channel needs to be included in PWA to describe data

Evidence for $N(1895) \frac{1}{2}^{-} (S_{11})$ resonance due to strong $p\eta'$ cusp in $p\eta$ S wave

$$\check{\Sigma}(W, \cos \theta) = \Sigma(W, \cos \theta) \cdot \frac{d\sigma}{d\Omega}(W, \cos \theta) = \sum_{k=2}^{2L_{\max}} (a_L(W))_k \cdot P_k^2(\cos \theta)$$



▲ GRAAL data (O. Bartalini et al., Eur. Phys. J. A33 (2007) 169)

● P. Collins et al., Phys. Lett. B 771 (2017) 213-221 (CLAS)

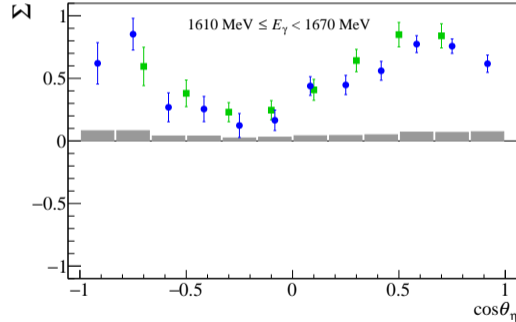
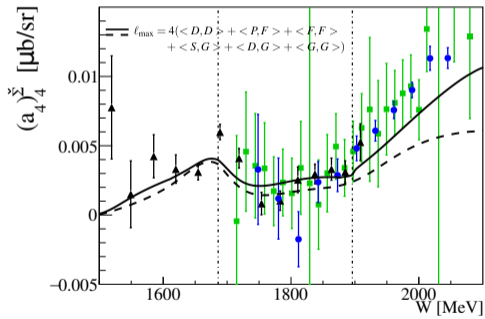
— BnGa-2019

- - - BnGa-2014-02

F. Afzal et al., Phys. Rev. Lett. 125, 152002 (2020)

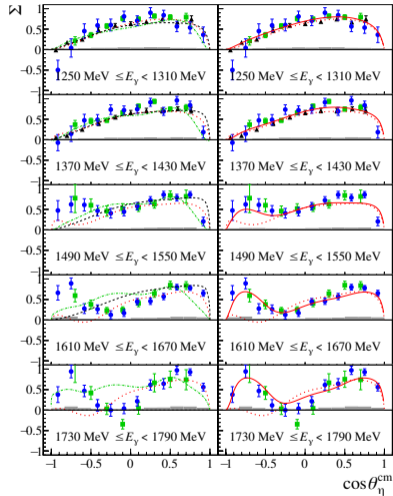
Full angular coverage is very important for $\langle S, G \rangle$ interference

$$\check{\Sigma}(W, \cos \theta) = \Sigma(W, \cos \theta) \cdot \frac{d\sigma}{d\Omega}(W, \cos \theta) = \sum_{k=2}^{2L_{\max}} (a_L(W))_k \cdot P_k^2(\cos \theta)$$

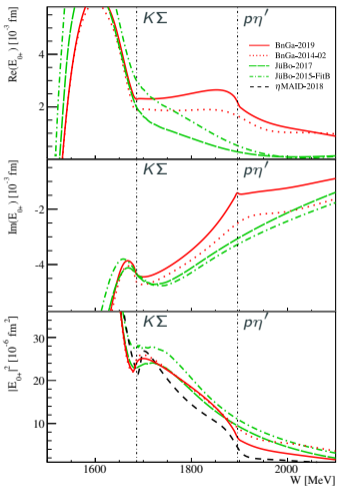
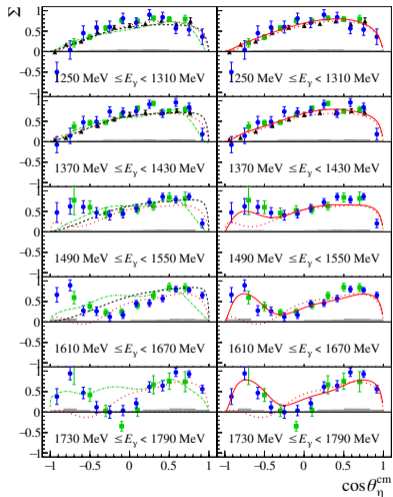


Phys. Rev. Lett. (2007) 169
 CLAS

Full angular coverage is very important for $< S, G >$ interference



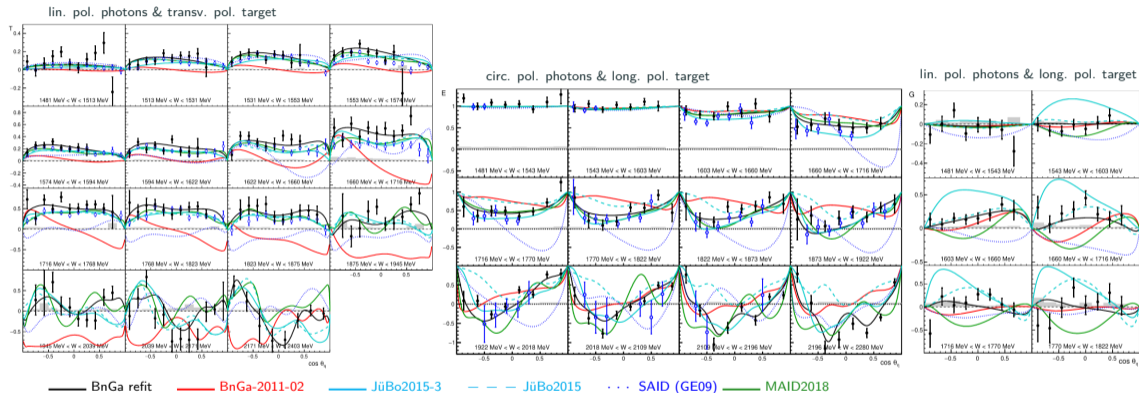
F. Afzal et al., Phys. Rev. Lett. 125, 152002 (2020)



- PWA predictions (BnGa, JüBo, η MAID) can not describe backward peak in data!
- New fits of BnGa and η MAID have included the $p\eta'$ cusp in the S wave
- However, JüBo does not!

F. Afzal et al., Phys. Rev. Lett. 125, 152002 (2020)

Combined analysis of the polarization observables σ, G, E, T, P, H in $\gamma p \rightarrow p\eta$ [J. Mueller et al., Phys. Lett. B 803 (2020), p. 135323]



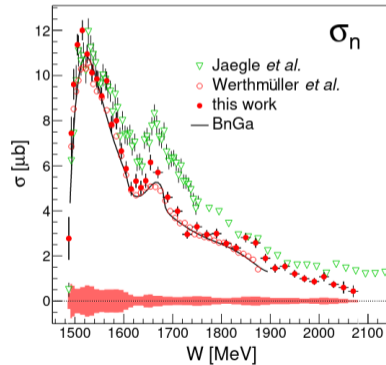
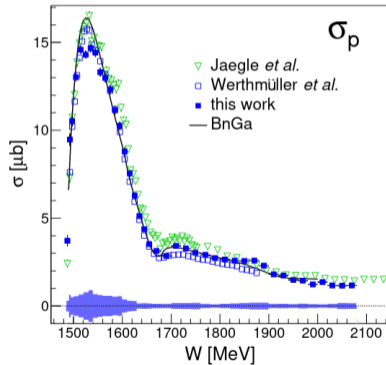
	$N(1535)\frac{1}{2}^-$	$N(1650)\frac{1}{2}^-$
BnGa refit	0.41 ± 0.04	0.33 ± 0.04
PDG 2017	$0.32 - 0.52$	$0.14 - 0.22$

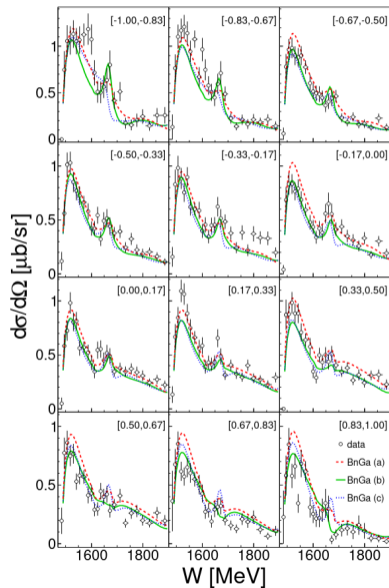
Large and heavily discussed difference in the $p\eta$ -branching ratio of $N(1535)\frac{1}{2}^-$ and $N(1650)\frac{1}{2}^-$ now significantly reduced!

η photoproduction off neutrons

- Complicated to measure due to no free neutrons \rightarrow helium, deuterium, deuterated butanol targets
- Nuclear Fermi motion effects eliminated by a complete kinematic reconstruction of the final state
- FSI estimated through comparison of quasi-free and free proton data

L. Witthauer et al., Eur. Phys. J. A (2017) 53:58

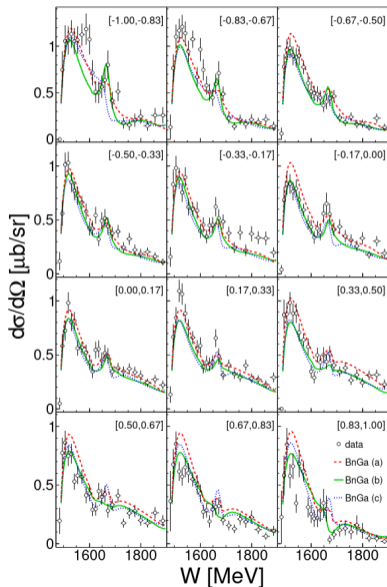




Narrow peak observed in $\gamma n \rightarrow n\eta$

at $W = (1670 \pm 5)$ MeV with $\Gamma = (30 \pm 15)$ MeV

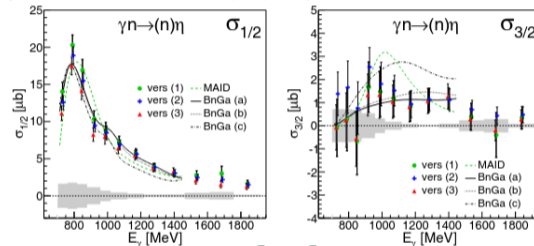
[L. Witthauer et al., Eur. Phys. J. A (2017) 53:58]



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[L. Witthauer et al., Eur. Phys. J. A (2017) 53:58]



Helicity asymmetry: $E = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}}$

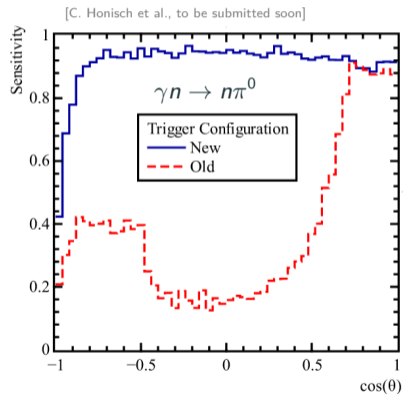
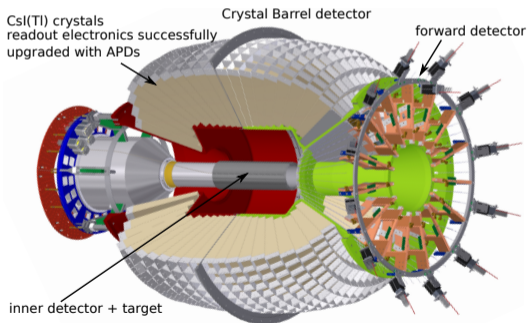
Spin dependent cross sections

$$\sigma_{1/2(3/2)} = \sigma_0 \cdot (1 \pm E)$$

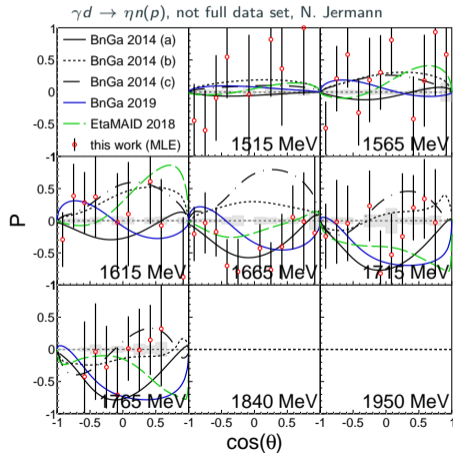
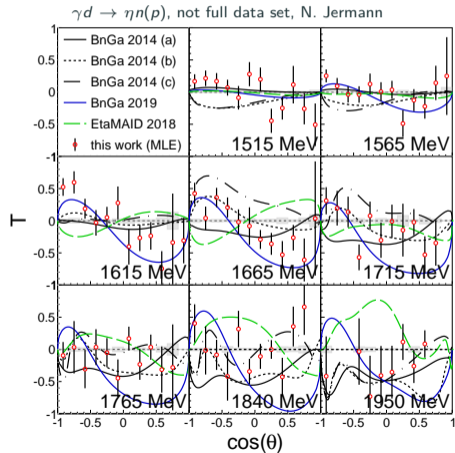
Structure only present in $\sigma_{1/2}^n$!

Intrinsic resonance/ interference effects?

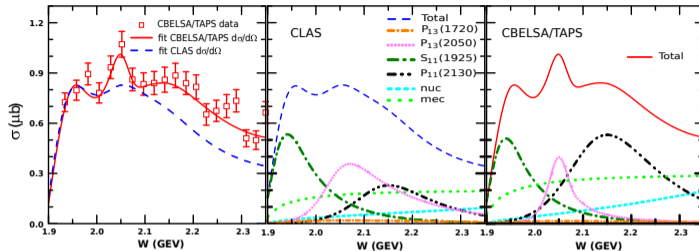
- Each CsI(Tl) crystal readout with 2 APDs instead of PIN photodiodes
- Crystal Barrel $\theta > 12^\circ$ included in first level trigger
- high trigger acceptance for complete neutral final states



- More data taken for T, P, H with coherent edges at 1300 MeV, 1600 MeV
- Selection of exclusive reaction possible now



η' photoproduction off protons



Huang et al., arXiv:1208.2279v1, (2012)

F. Huang, H. Haberzettl, and K. Nakayama Phys. Rev. C 87, 054004, 2013

○ CBELSA/TAPS: V. Crede et al., Phys. Rev. C80 (2009), p. 055202

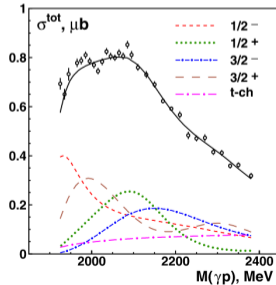
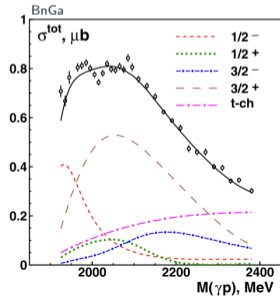
○ CLAS: M. Williams et al., Phys. Rev. C 80 (2009), p. 045213

● A2-MAMI: V.L. Kashevarov et al., Phys.Rev.Lett. 118.21 (2017)

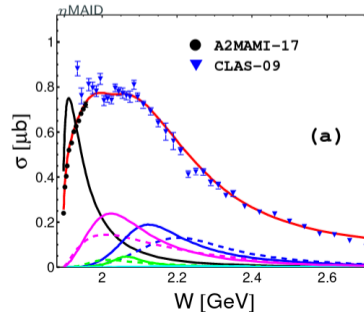
main contributions from (BnGa):

$$N(1895)_{\frac{1}{2}^-}(S_{11}), N(1900)_{\frac{3}{2}^+}(P_{13}),$$

$$N(2100)_{\frac{1}{2}^+}(P_{11}), N(2120)_{\frac{3}{2}^-}(D_{13})$$



BnGa: A.V. Anisovich et al., Phys.Lett. B 772 (2017) 247-252



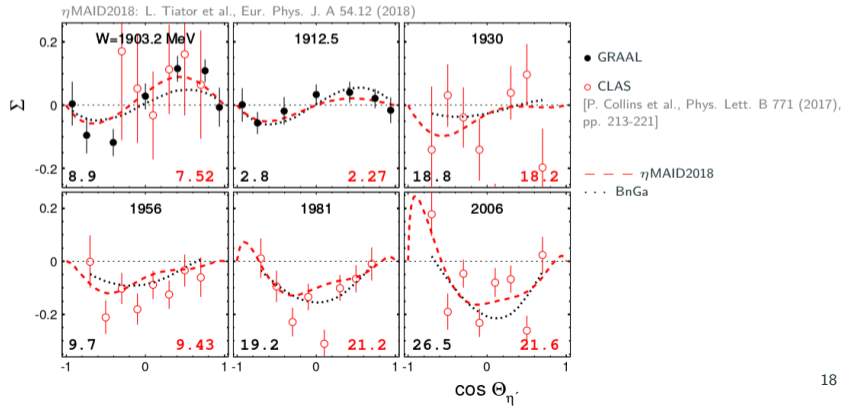
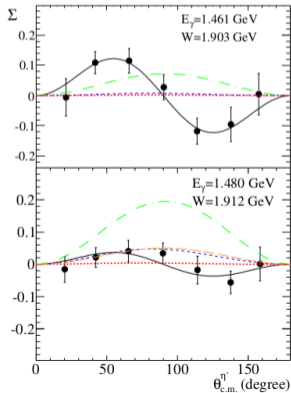
η' MAID2018: L. Tiator et al., Eur. Phys. J. A 54.12 (2018)

- Unexpected strong angular dependence observed near threshold ($W=1896\text{MeV}$) in GRAAL data
- Angular dependence sensitive to $\langle P, D \rangle$, $\langle S, F \rangle$ and $\langle D, F \rangle$ interference terms
- Angular dependence described by introducing a narrow resonance:

BnGa: $N(1900)\frac{3}{2}^-(D_{13})$ or $N(1900)\frac{5}{2}^-(D_{15})$ A.V. Anisovich et al., Phys.Lett.B 785 (2018) 626-630

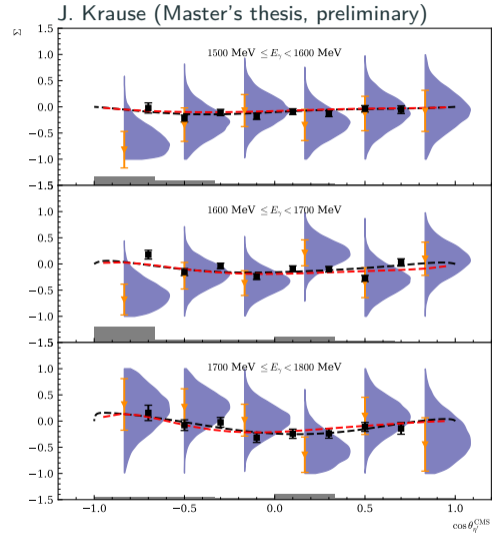
η MAID2018: $N(1902)\frac{1}{2}^-(S_{11})$ L. Tiator et al., Eur. Phys. J. A 54.12 (2018)

GRAAL: P.L. Sandri et al., Eur.Phys. J. A 51.7 (2015), p. 77

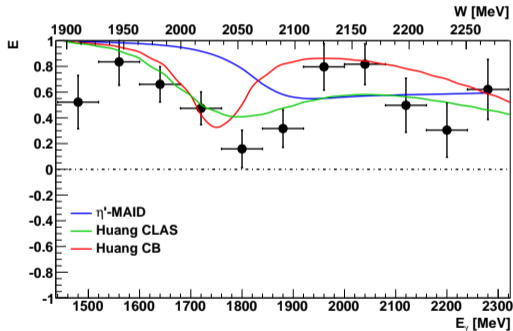


- $\eta' \rightarrow \gamma\gamma$ (BR: 2.2%)
- 8000 selected events
- Unbinned maximum likelihood fit used to get Σ
- comparison between Frequentist and Bayesian approach:

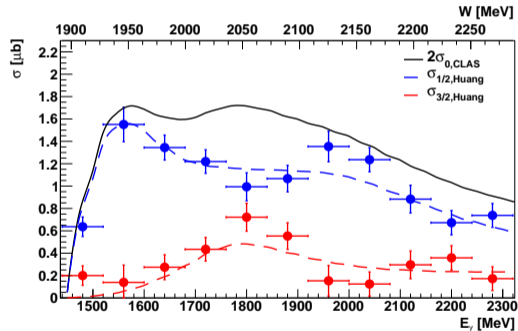
$$p(\Sigma, a, b, \Sigma^{bg}, a^{bg}, b^{bg} | \phi, p_\gamma) \propto \mathcal{L}(\phi, p_\gamma | \Sigma, a, b, \Sigma^{bg}, a^{bg}, b^{bg}) \cdot \pi(\Sigma, a, b, \Sigma^{bg}, a^{bg}, b^{bg})$$
- Good agreement between CBELSA/TAPS (\blacktriangle) and CLAS (\blacksquare)
- BnGa (---) and η MAID2018 (---) can describe data



- Helicity asymmetry obtained with circ. pol. photon beam and long. pol. target
- Strong contribution to $\sigma_{1/2} \rightarrow$ strong contributions from S_{11} and P_{11} waves
- Significant contributions to $\sigma_{3/2}$ at $W=2050$ MeV



F. Afzal, preliminary data



- Outlook: More data for T, P, H will be analyzed!

- Are $\eta'p$ bound states possible?
- Real and imaginary part of the S_{11} amplitude were fit by BnGa using

$$A = \frac{ak}{1 - ika + Rk^2 a/2 + dk^4 a} \quad k = \frac{\sqrt{(s - (M_p + M_{\eta'})^2)(s - (M_p - M_{\eta'})^2)}}{2\sqrt{s}}$$

$a = a_{p\eta'}$: $\rho\eta'$ scattering length

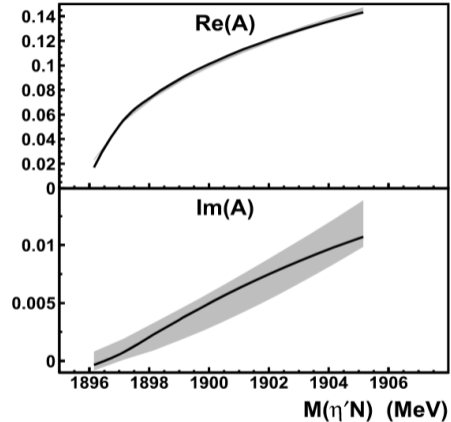
R : range of the $\eta'p$ interaction

d : parameter representing higher-order terms

$\sqrt{s} = M_{\eta'p}$: invariant mass

k : η' momentum in the $\eta'p$ rest frame

- $|a_{p\eta'}| = (0.403 \pm 0.020 \pm 0.060)$ fm
- $\delta_{N\pi} = (87 \pm 2)^\circ$
 → real part of the scattering length is small compared to imaginary part
 → disfavors $\eta'p$ bound states



BnGa: A.V. Anisovich et al., Phys.Lett.B 785 (2018) 626-630

Particle	J^P	overall	N_γ	N_π	$\Delta\pi$	N_σ	N_η	ΛK	ΣK	N_ρ	N_ω	$N_{\eta'}$
N	$1/2^+$	****										
$N(1440)$	$1/2^+$	****	****	****	****	***	-					
$N(1520)$	$3/2^-$	****	****	****	****	**	****			---		
$N(1535)$	$1/2^-$	****	****	****	**	*	****			--		
$N(1650)$	$1/2^-$	****	****	****	**	*	****	*--	--	--		
$N(1675)$	$5/2^-$	****	****	****	****	**	*	*	*	-		
$N(1680)$	$5/2^+$	****	****	****	****	***	*	*	*	---		
$N(1700)$	$3/2^-$	**	**	**	**	*	*	--	-	-		
$N(1710)$	$1/2^+$	****	****	**	*	*	**	**	*	*	*	
$N(1720)$	$3/2^+$	****	****	****	**	*	*	****	*	*	*	
$N(1860)$	$5/2^+$	**	*	**	*	*	*					
$N(1875)$	$3/2^-$	***	**	**	*	**	*	*	*	*	*	
$N(1880)$	$1/2^+$	***	**	*	**	*	*	**	**		**	
$N(1895)$	$1/2^-$	****	****	*	*	*	****	**	**	*	*	****
$N(1900)$	$3/2^+$	****	****	**	**	*	*	**	**	-	*	**
$N(1990)$	$7/2^+$	**	**	**			*	*	*			
$N(2000)$	$5/2^+$	**	**	*	**	*	*	-	-	--	*	
$N(2040)$	$3/2^+$	*	*									
$N(2060)$	$5/2^-$	***	***	**	*	*	*	*	*	*	*	
$N(2100)$	$1/2^+$	***	**	***	**	**	*	*	*	*	*	**
$N(2120)$	$3/2^-$	***	***	**	**	**	*	**	*	*	*	*
$N(2190)$	$7/2^-$	****	****	****	****	**	*	**	*	*	*	
$N(2220)$	$9/2^+$	****	**	****			*	*	*			
$N(2250)$	$9/2^-$	****	**	****			*	*	*			
$N(2300)$	$1/2^+$	**	**	**								
$N(2570)$	$5/2^-$	**	**	**								
$N(2600)$	$11/2^-$	***	***	***								
$N(2700)$	$13/2^+$	**	**	**								

- mostly πN data were used until 2010
- photoproduction data is now used by most PWA groups and new fit values for resonance parameters have entered the PDG
- Still a lot of work to do!
- More information in
A. Thiel, F. Afzal, Y. Wunderlich, Prog. Part. Nucl. Phys. 125 (2022) 103949

Summary and Outlook

Summary:

- High precision polarization data measured at the CBELSA/TAPS experiment for $p\eta$ final state
→ Sensitivity up to G -waves reached! $p\eta'$ cusp observed in the beam asymmetry Σ data!
- Significant contributions to confirming poorly known states like $N(1895)\frac{1}{2}^-$
→ Upgraded to a 4star resonance in PDG
- Improved precision of resonance properties → BR
→ Our knowledge of the spectrum and the properties of baryons is steadily increasing!
- Still a lot of interesting, not understood observations, like narrow structure in $m\eta$
- Beam and helicity asymmetry extracted for the $p\eta'$ final state
- $p\eta'$ scattering length results disfavors $\eta'p$ bound states

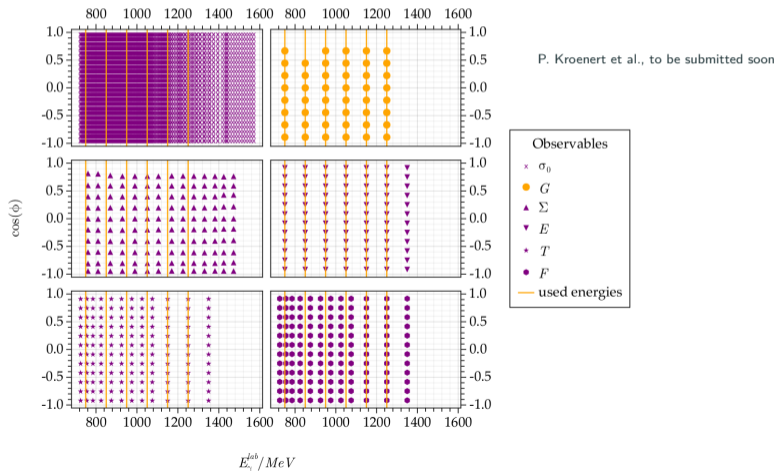
Outlook:

- APD-Upgrade of the Crystal Barrel detector at the CBELSA/TAPS experiment successfully completed
→ Ongoing analysis of different final states ($N\pi^0$, $N\eta$, $N\eta'$, $N\omega$, $N\pi^0\pi^0$, $N\pi^0\eta\dots$) and PWA of the data

Truncated PWA using "complete" data set of polarization observables

Goal: Extract multipoles model independent

- 6 single energy fits from threshold, 750 MeV to 1250 MeV
- Complete data set ($\sigma_0, T_{\text{MAMI}}, F_{\text{MAMI}}, E_{\text{MAMI}}, \Sigma_{\text{GRAAL}}, G_{\text{CBELSA/TAPS}}$)



Truncated PWA using "complete" data set of polarization observables

Method:

- Fit the angular distributions of observables, parametrized

by

$$\check{\Omega}_{\text{theo}}^{\alpha}(W, \theta) = \rho \sum_{k=\beta_{\alpha}}^{2\ell_{\max} + \beta_{\alpha} + \gamma_{\alpha}} \mathcal{A}_k^{\alpha}(W) P_k^{\beta_{\alpha}}(\cos \theta)$$

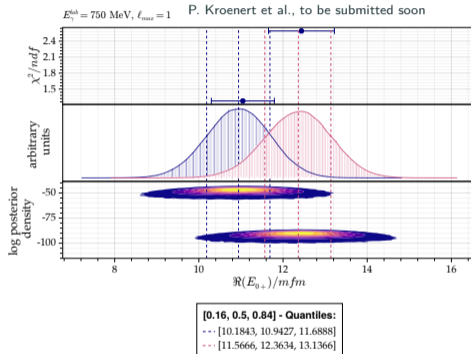
- Frequentist Ansatz: Minimize the function

$$\chi_{\mathcal{M}}^2 = \sum_{i,j} \left[(a_L^{\text{Fit}})_i - \langle \mathcal{M}_\ell | (C_L)_i | \mathcal{M}_\ell \rangle \right] C_{ij}^{-1} \left[(a_L^{\text{Fit}})_j - \langle \mathcal{M}_\ell | (C_L)_j | \mathcal{M}_\ell \rangle \right]$$

- Bayesian Ansatz:

$$\rho(\Theta | \mathbf{y}) = \rho(\mathbf{y} | \Theta) \pi(\Theta)$$

- Conditional likelihood distribution
- Priors $\pi(\Theta)$: broad uniform distributions for multipoles
- Monte Carlo maximum likelihood estimation
- Extract multipoles at single energies



Truncated PWA using "complete" data set of polarization observables

Method:

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$$\check{\Omega}_{\text{theo}}^{\alpha}(W, \theta) = \rho \sum_{k=\beta_{\alpha}}^{2\ell_{\max} + \beta_{\alpha} + \gamma_{\alpha}} \mathcal{A}_k^{\alpha}(W) P_k^{\beta_{\alpha}}(\cos \theta)$$

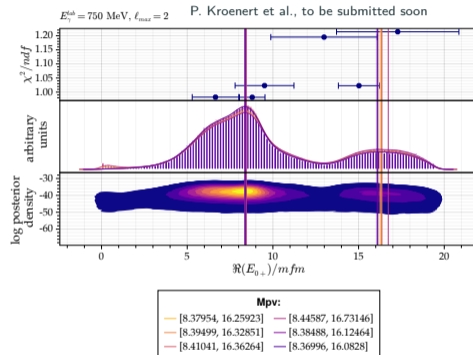
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Truncated PWA using complete data set of polarization observables

Results:

