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*Knut and Alice
Wallenberg
Foundation*

The Size of Strangeness

- New Perspectives on Hyperon Structure

EMMI Workshop
on Meson and Hyperon Interactions with Nuclei
September 14-16, 2022

Prof. Dr. Karin Schönning, Uppsala University



Outline

- The Size of Protons and Neutrons
- The Size of Strangeness
 - Electromagnetic Form Factors
 - High q^2 : Recent measurement by BESIII
 - Low q^2 : Ongoing and future measurements at HADES and PANDA.
- Summary



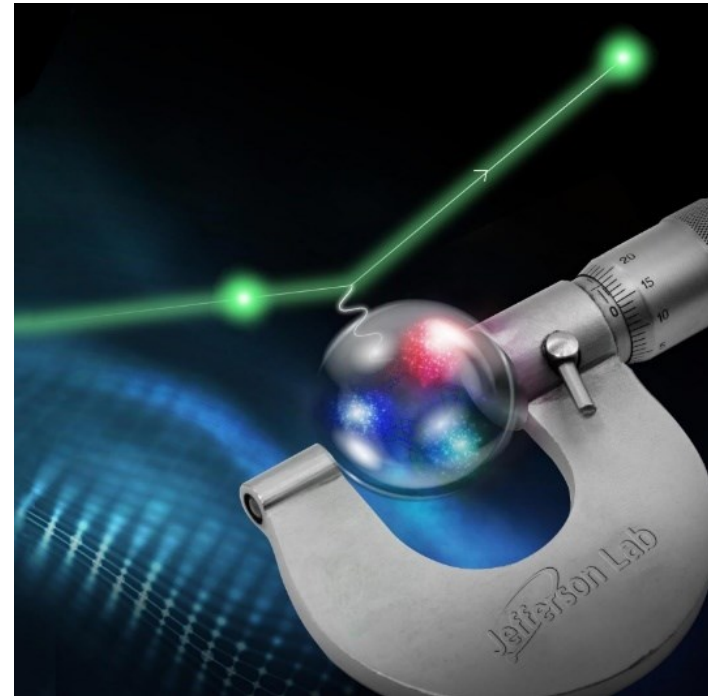
The Size of Protons

Strong interaction dynamics manifest in *e.g.*

- Charge distributions
- Charge radius

Proton radius:

Very rapidly progressing field!





The Size of Protons

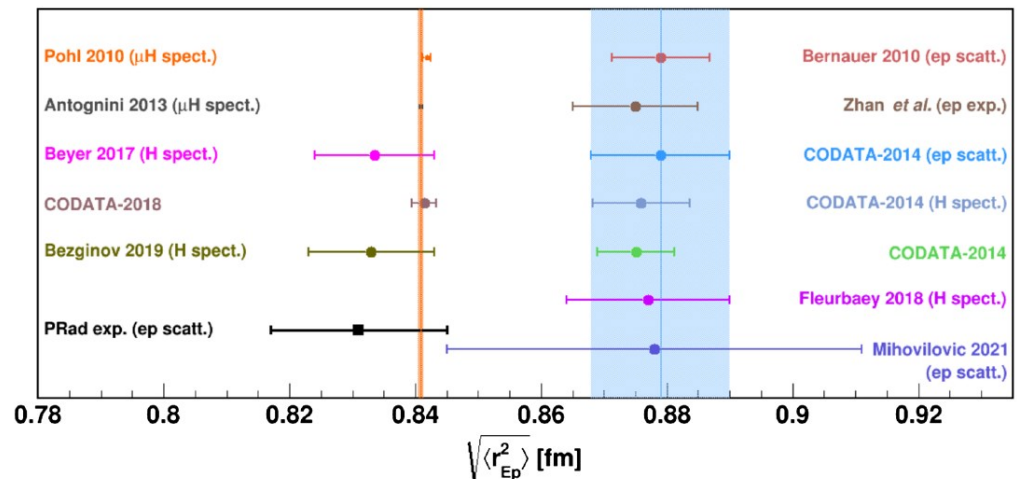
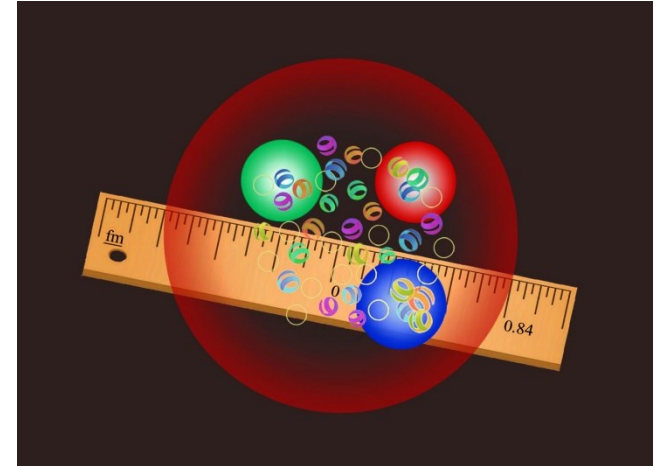
Ways to measure proton size:

- Electron scattering
 - Hydrogen spectroscopy
- } ~0.88 fm



2010 – 2019:
Unexplained discrepancies
= *Proton radius puzzle**

- Muonic hydrogen spectroscopy
- ~0.84 fm



*Gao & Vanderhaegen Rev. Mod. Phys. 94, 015002 (2022)

Pictures from

- Y-H Lin, U. Bonn

- Rev. Mod. Phys. 94, 015002 (2022)



The Size of Protons

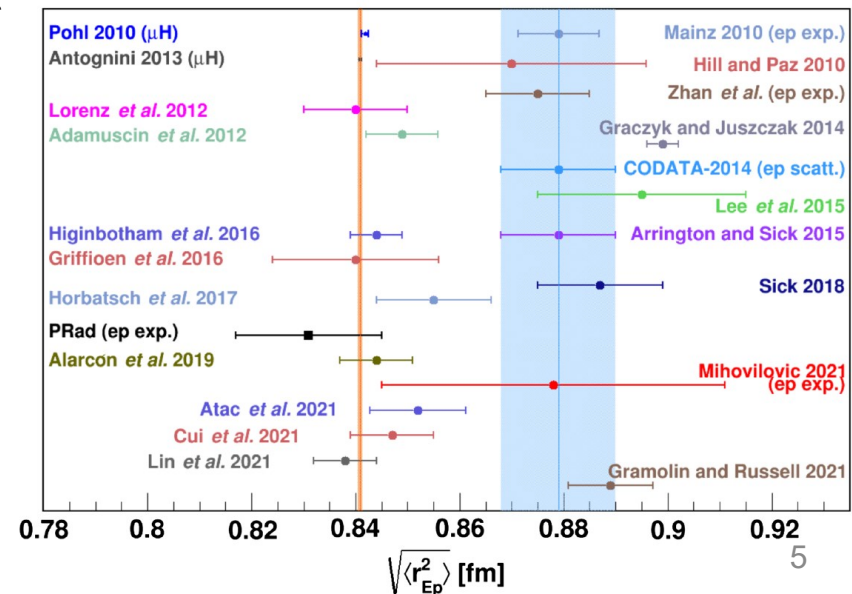
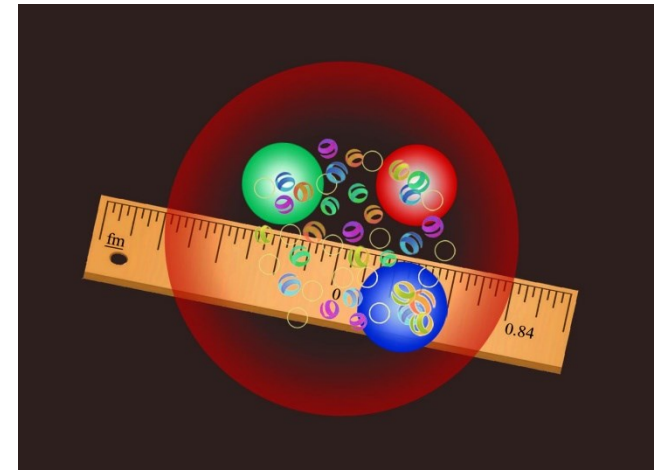
Ways to measure proton size:

- Electron scattering
- Hydrogen spectroscopy



Recently:
Dispersive calculations
Respecting analyticity and
unitarity give consistent results.*

- Muonic hydrogen spectroscopy



*Lin, Hammer & Meissner, Phys. Rev. Lett. 128, 052002 (2022).

Pictures from

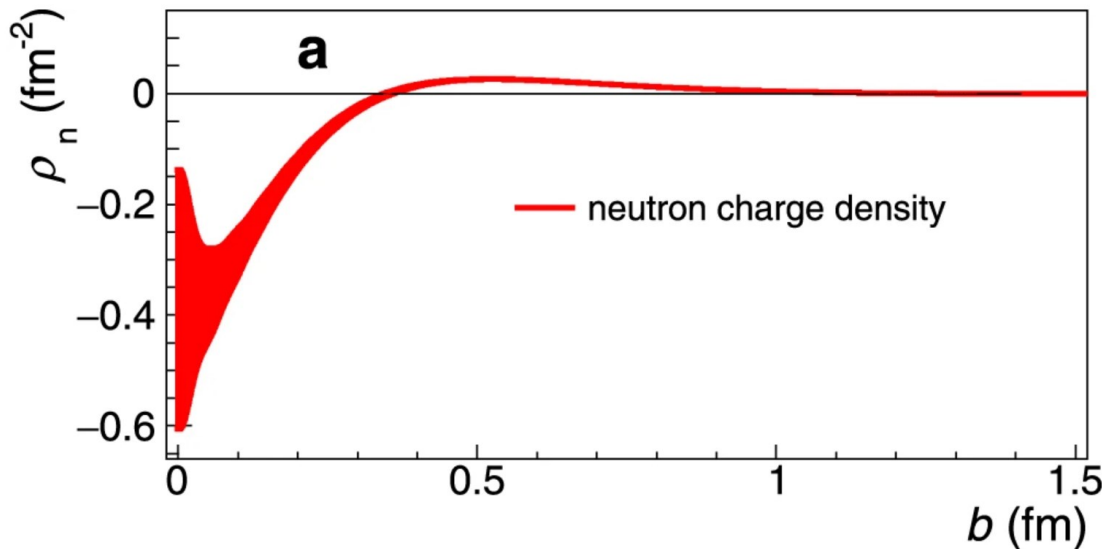
- Y-H Lin, U. Bonn
- Gao & Vanderhaegen, Rev. Mod. Phys. 94, 015002 (2022)



The Size of Neutrons

Neutral and unstable ($\tau \sim 15$ min) when “free”:

- Atomic spectroscopy methods not suitable
- Electron scattering possible but difficult
 - Often based on low-energy scattering of bound neutrons
 - New calculation based on neutron EM form factor*.



$$\langle r_n^2 \rangle = -0.110 \pm 0.008 \text{ fm}^2$$

Negative = asymmetric quark distribution

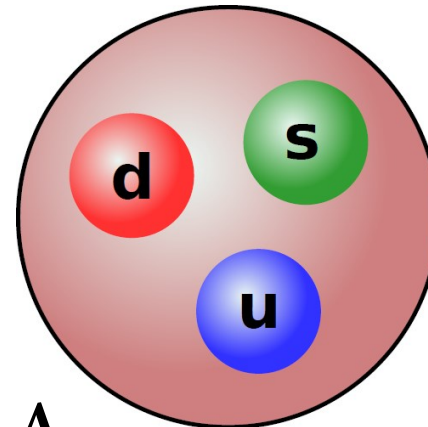
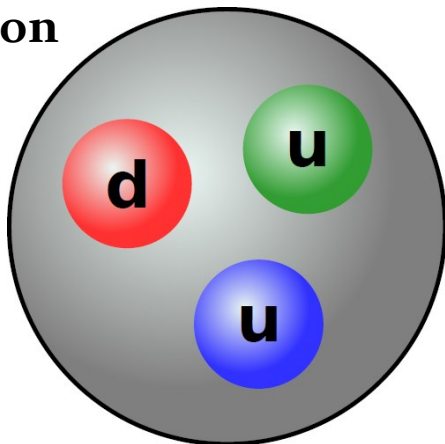
*Atac *et al.*,
Nature Com. 12, 1759 (2021)



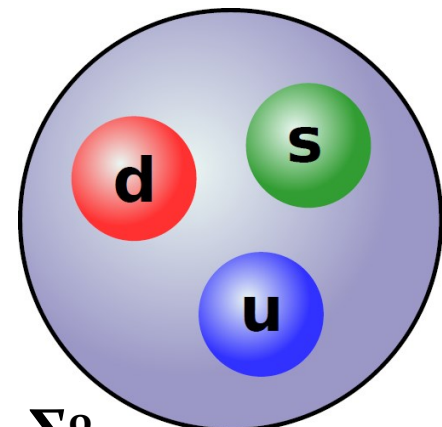
The Size of Strangeness

What happens if we replace one of the light quarks in the proton with one - or many - heavier quark(s)?

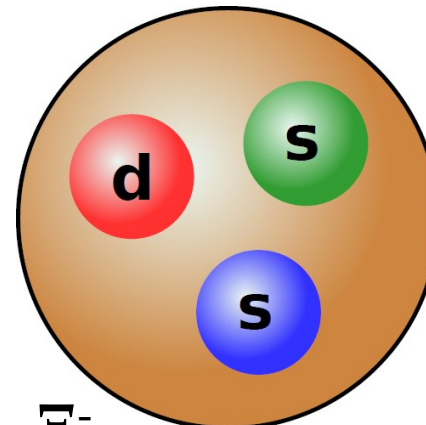
proton



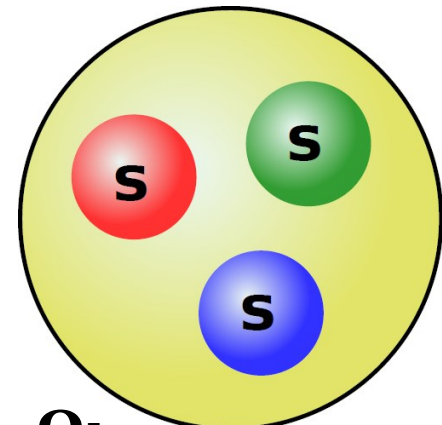
Λ



Σ^0



Ξ^-



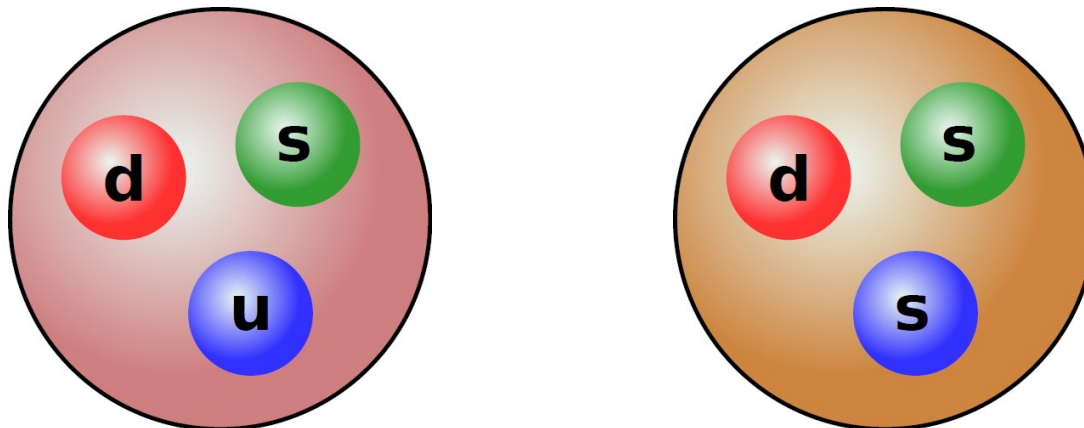
Ω^-



The Size of Strangeness

- Hyperons are even less stable ($\tau \sim 10^{-10}$ s) than neutrons.
- Many of them are neutral or decay into neutrals.

Q: How can we study their size?





The Size of Strangeness

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- Many of them are neutral or decay into neutrals.

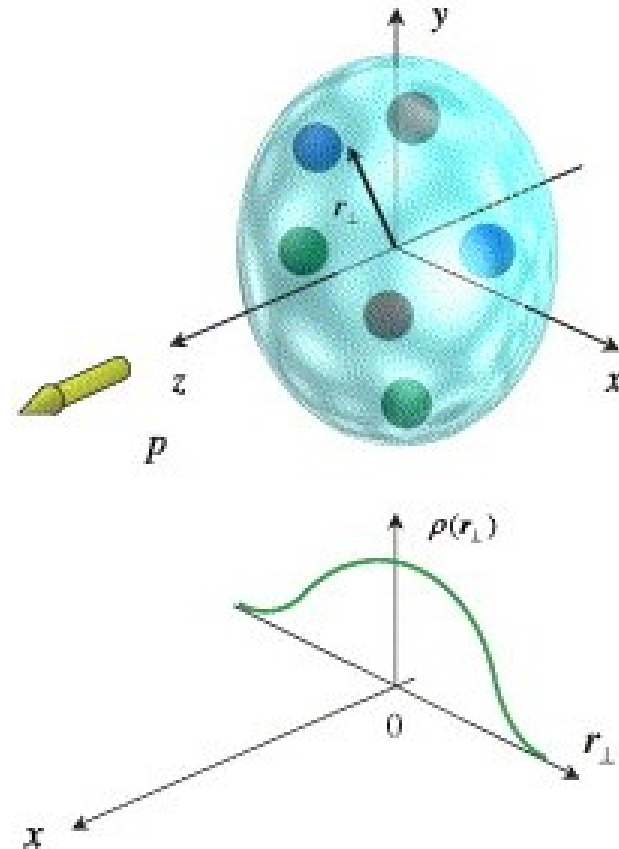
Q: How can we study their size?

A: By electromagnetic form factors!



Electromagnetic Form Factors

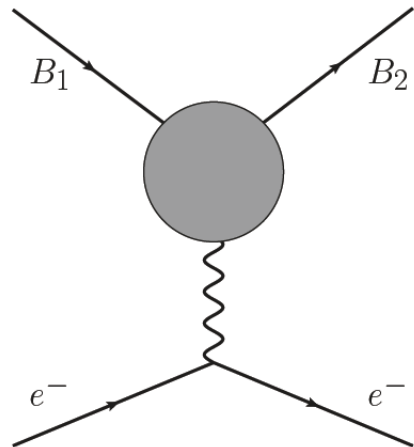
- Probed in hadron – photon interactions
- Functions of momentum transfer q^2
- Quantify the deviation from point-like behaviour.
- Predictions from
 - LatticeQCD
 - ChPT
 - Dyson-Schwinger
 - Vector Meson Dominance





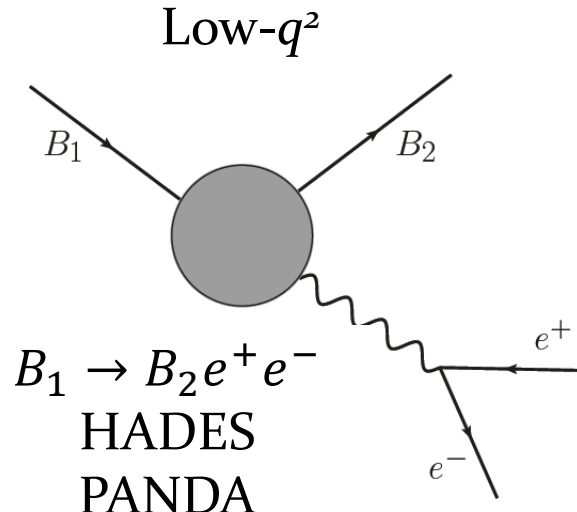
Space-like vs. time-like FF's

Space-like
 $q^2 < 0$

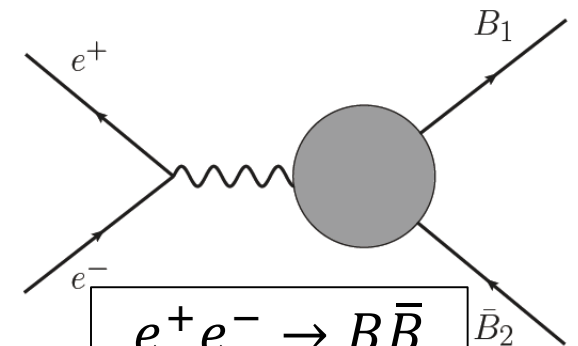


$e^- B \rightarrow e^- B$
e.g. JLAB

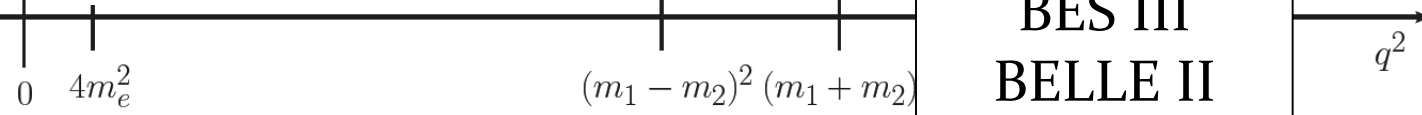
Time-like
 $q^2 > 0$



High- q^2



$e^+ e^- \rightarrow B \bar{B}$
 $\bar{B} B \rightarrow e^+ e^-$
BES III
BELLE II
PANDA





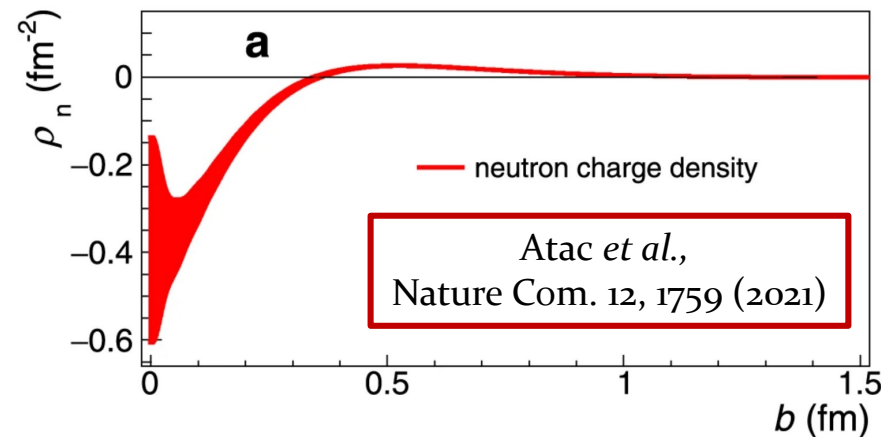
Space-like form factors

- Number of EMFFs = $2J+1 \rightarrow$ spin $\frac{1}{2}$ baryons have 2.
- Dirac and Pauli FFs F_1 (spin non-flip) and F_2 (spin flip).
- Sachs FFs G_E and G_M .

- $G_E(q^2) = F_1(q^2) - \tau F_2(q^2)$

- $G_M(q^2) = F_1(q^2) + F_2(q^2)$

- $\tau = q^2/4M_B^2$



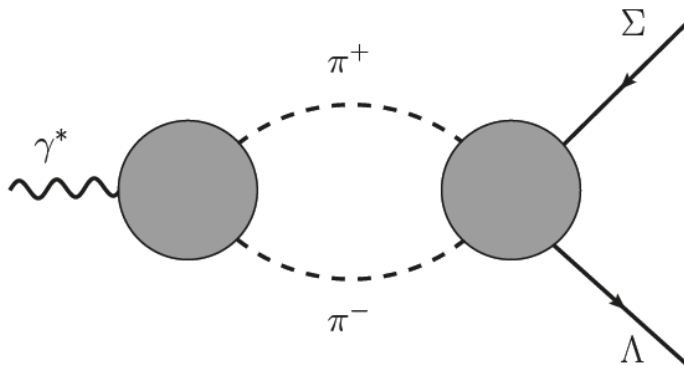
- Charge radius: $\langle r_E^2 \rangle = 6 \frac{dG_E(q^2)}{dq^2} \Big|_{q^2=0}$

- Magnetic radius: $\langle r_M^2 \rangle = \frac{6}{G_M(0)} \frac{dG_M(q^2)}{dq^2} \Big|_{q^2=0}$



Time-like form factors

- Related to space-like EMFFs *via* dispersion relations.
 - Are complex:
 - $G_E(q^2) = |G_E(q^2)| \cdot e^{i\Phi_E}$, $G_M(q^2) = c \cdot e^{i\Phi_M}$
 - Ratio $R = \frac{|G_E(q^2)|}{|G_M(q^2)|}$ accessible from baryon scattering angle.
 - $\Delta\Phi(q^2) = \Phi_M(q^2) - \Phi_E(q^2) =$ phase between G_E and G_M
 - Phase a reflection of intermediate fluctuations of the γ^* into *e.g.* $\pi\pi$.
- **Polarises final state!**

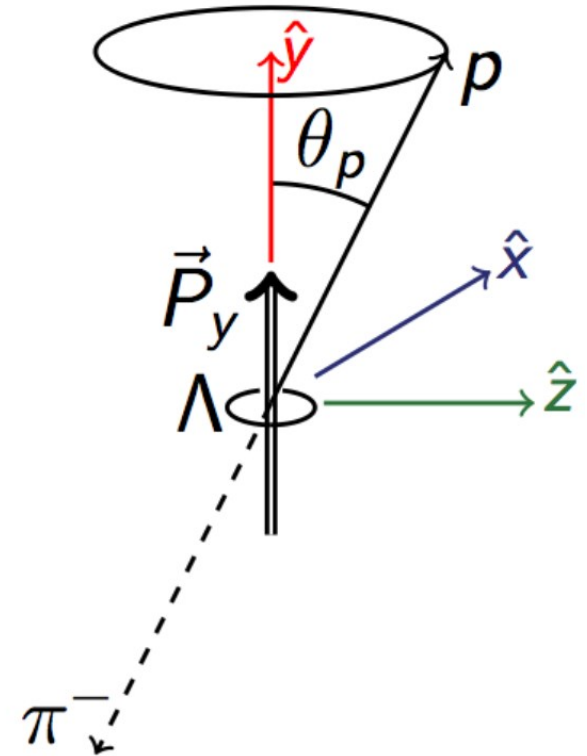
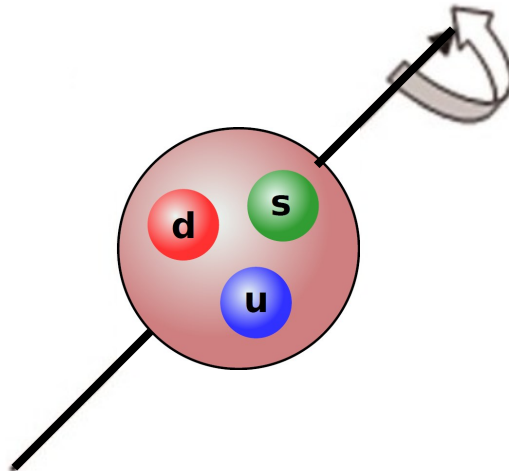


Picture credit:
Elisabetta Perotti, PhD Thesis,
UU (2020)



Advantage of hyperons

Polarisation experimentally accessible
by the weak, parity violating decay:

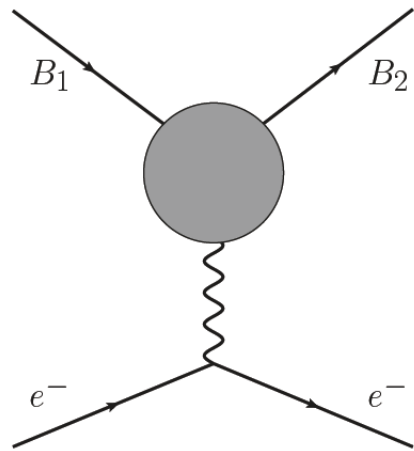


$$I(\cos\theta_p) = N(1 + \alpha_\Lambda P_\Lambda \cos\theta_p)$$



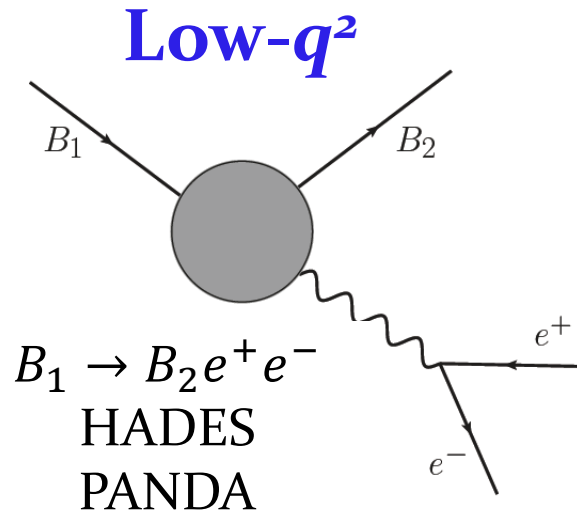
Space-like vs. time-like FF's

Space-like
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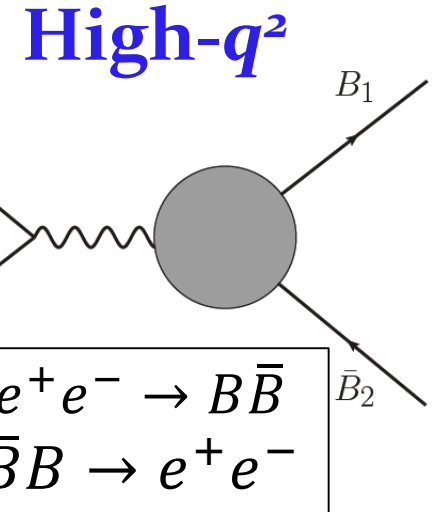


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e.g. JLAB

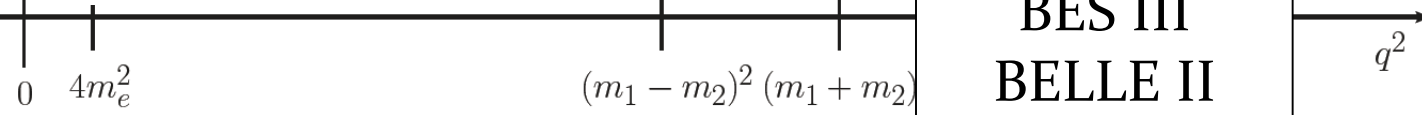
Time-like
 $q^2 > 0$



$B_1 \rightarrow B_2 e^+ e^-$
HADES
PANDA



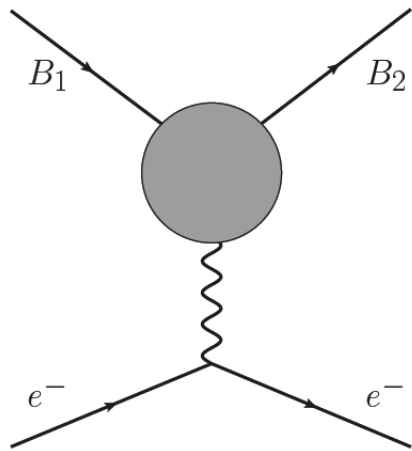
$e^+ e^- \rightarrow B \bar{B}$
 $\bar{B} B \rightarrow e^+ e^-$
BES III
BELLE II
PANDA





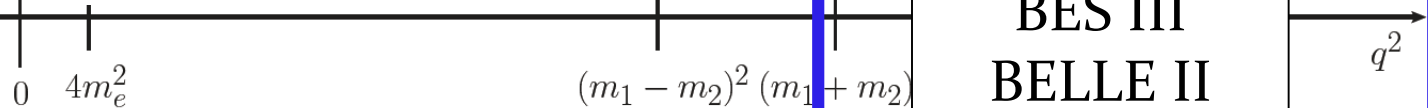
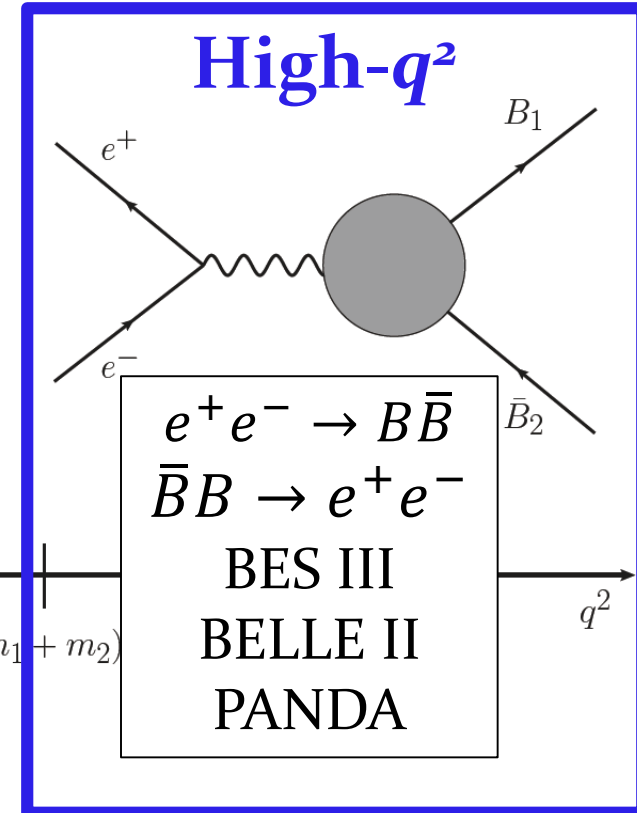
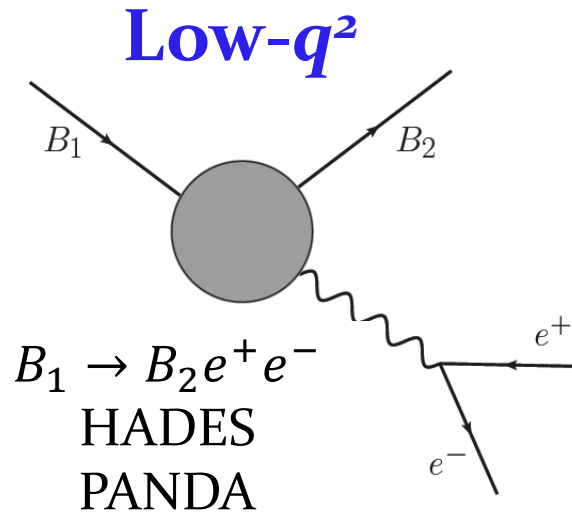
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 $q^2 > 0$





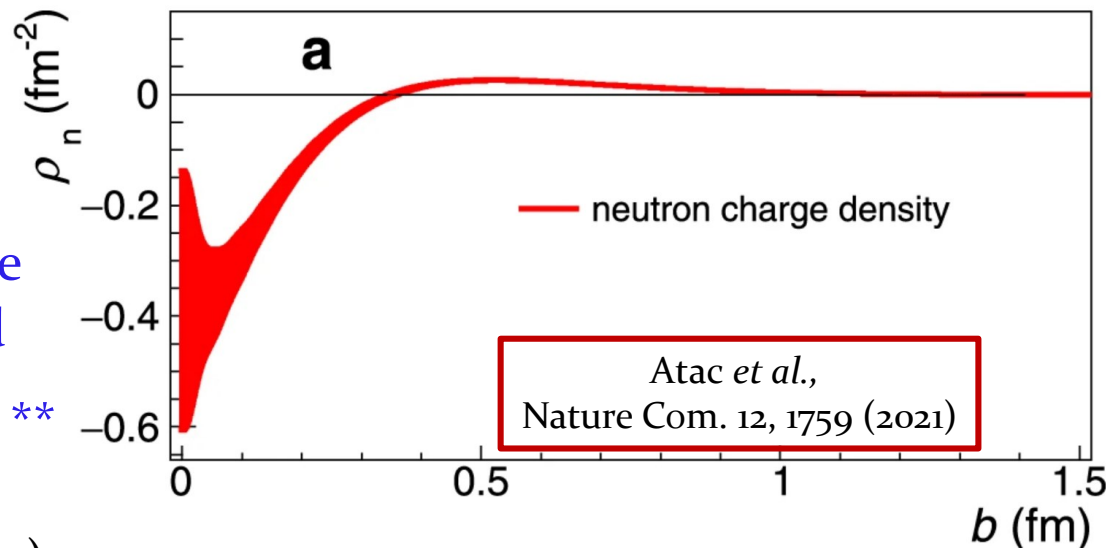
Nucleon *versus* hyperon EMFFs

Asymptotic behaviour as $|q^2| \rightarrow \infty$: SL \sim TL

- Nucleons: SL and TL accessible.
- Hyperons: Only TL accessible, but also phase!
SL = TL $\leftrightarrow \Delta\Phi(q^2) \rightarrow 0$ as $|q^2| \rightarrow \infty$ (or at $> q_{asy}^2$)

Baryon charge radius:

- Neutron: Found to be negative *
- Neutral hyperons: Can be calculated from q_{asy}^2 and
 $Im(R(q^2)) = Im\left(\frac{G_E(q^2)}{G_M(q^2)}\right)$ **



*Atac et al., Nature Com. 12, 1759 (2021)

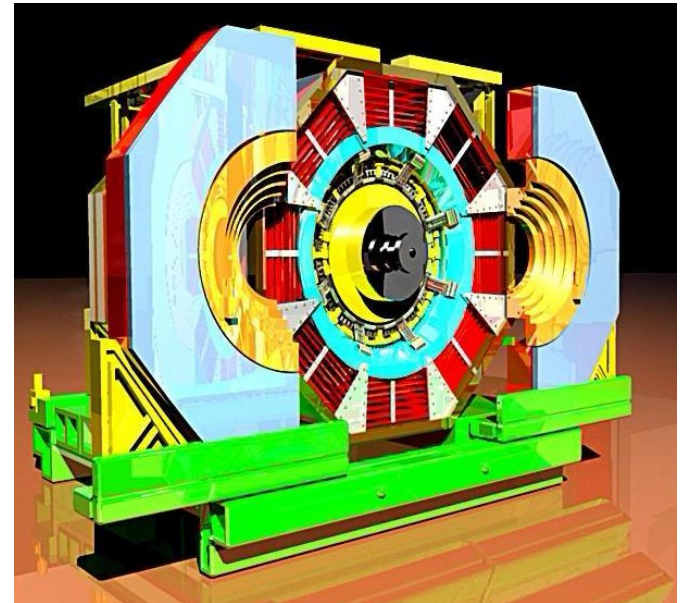
**Mangoni et al., Phys. Rev. D 104, 116016 (2021)



Recent measurements by BESIII

- Study the $e^+e^- \rightarrow B\bar{B}$, where $B = \Lambda, \Sigma, \Xi, \Lambda_c^+$
- Beijing Electron Positron Collider (BEPC II):
 - e^+e^- collider within CMS range 2.0 – 4.95 GeV.
 - Optimised in the τ -charm region.
- Beijing Spectrometer (BES III):
 - Near 4π coverage
 - Tracking, PID, Calorimetry
 - Broad physics scope

BES III

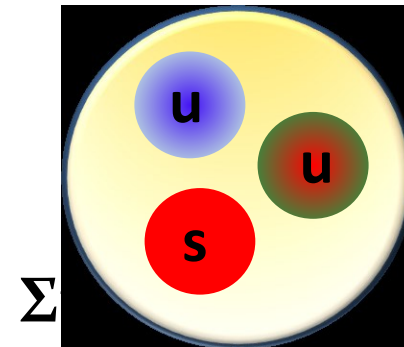
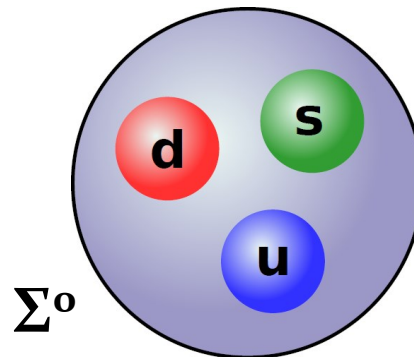
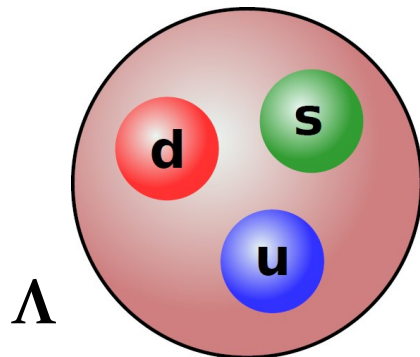




Single-strange hyperons

Diquark correlations in baryons?

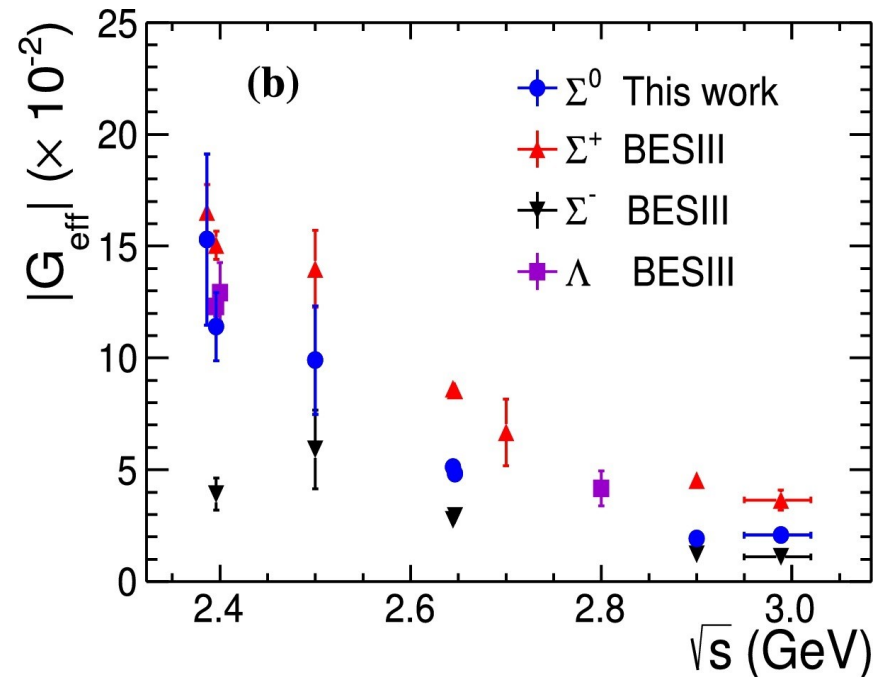
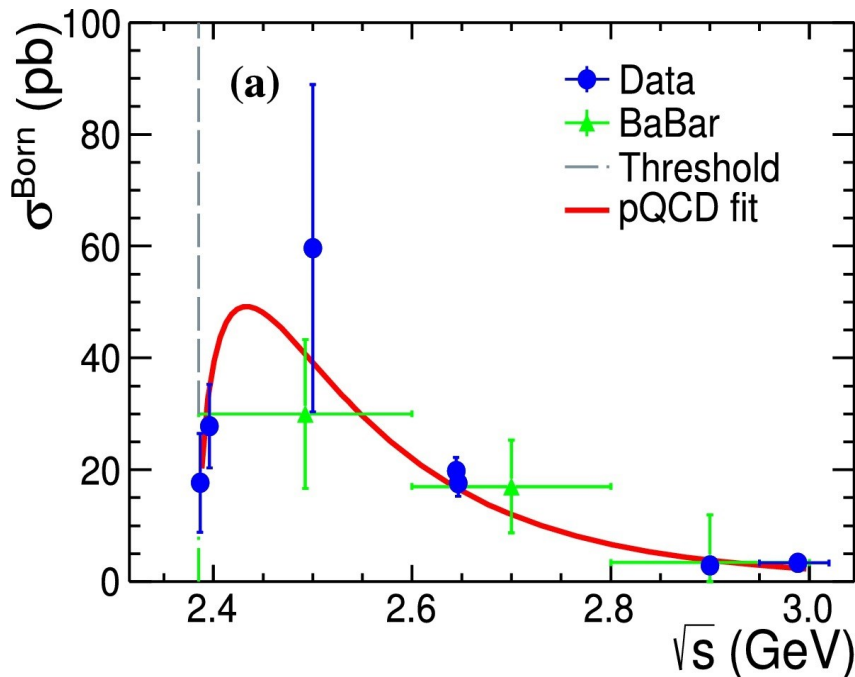
- The Σ^0 has isospin 1 whereas Λ has isospin 0
 - Strange quark has no isospin \rightarrow difference is in the ud diquark.
 - Different isospin structure \rightarrow different spin structure.
 - Difference in cross section and form factors expected.*
- In Σ^+ , the uu should have same spin structure as the ud in Λ .
 - Similar cross sections expected.*





Single-strange hyperons

- Λ/Σ^+ effective FFs similar as expected from diquark correlations.^{*,**,***}
- Σ^+/Σ^- cross section ratio $\sim 9^{**}$, in disagreement with the expected SU(3) symmetry breaking of 10-30%.



* BESIII: Phys. Lett. B 831, 137187 (2022)

** BESIII: Phys. Lett. B 814, 136110 (2021)

*** BESIII: Phys. Rev. D 97, 032013 (2018)

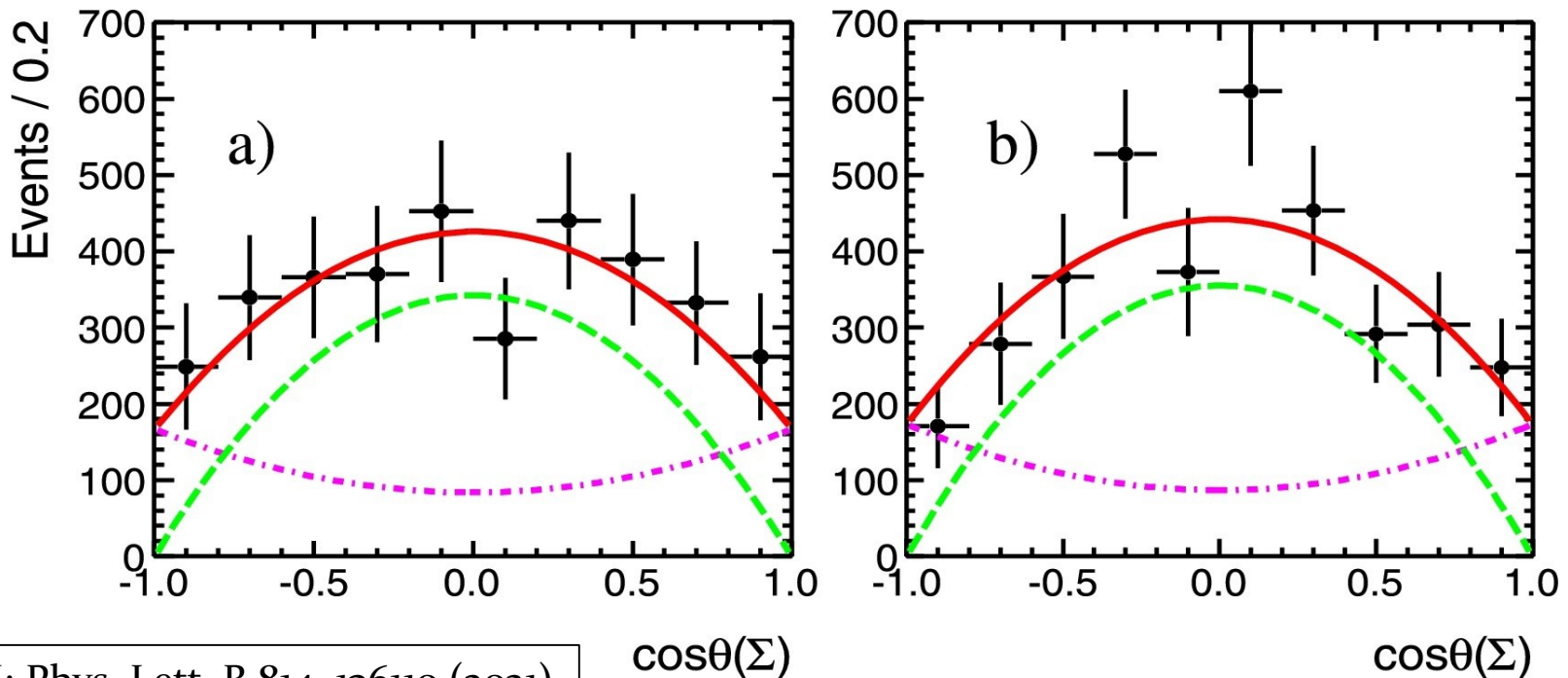


Single-strange hyperons

Σ^+ Form Factor Ratio:

$$R = \frac{|G_E(q^2)|}{|G_M(q^2)|} \text{ measured at } 2.396 \text{ GeV to be } 1.83 \pm 0.26$$

BESIII

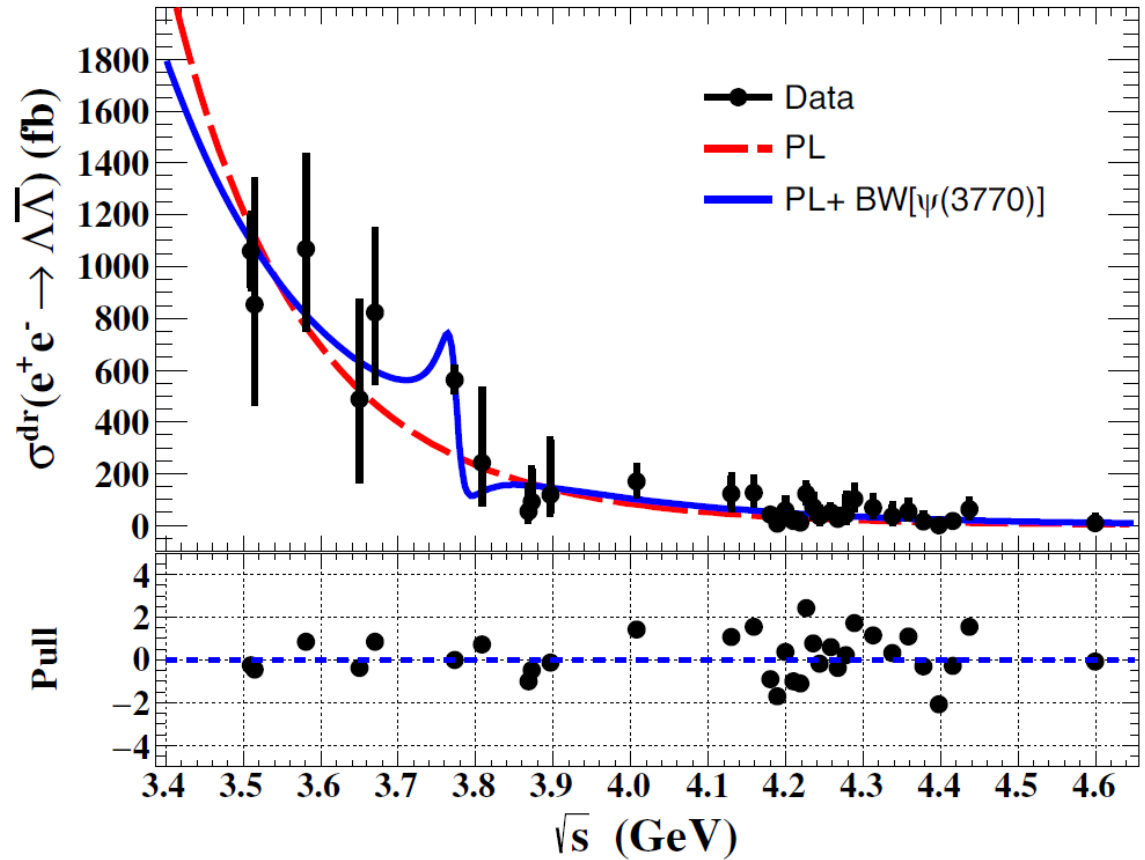




Production of Λ at high q^2

- $\Lambda\bar{\Lambda}$ production near vector charmonia^{*,**}
- $BR(\Psi \rightarrow \Lambda\bar{\Lambda}) > 10$ times larger than assumed in previous studies by CLEO-c^{***}.

BES III



* BESIII: Phys. Rev. D 104, L091104 (2021)

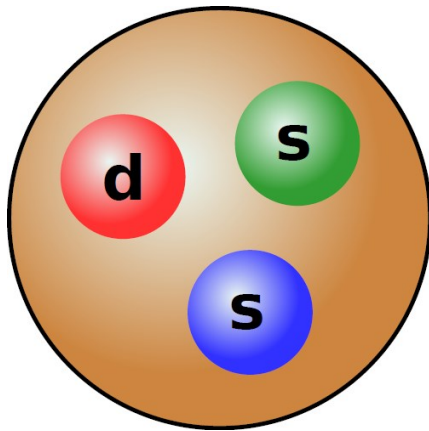
** BESIII: Phys. Rev. D 105, L011101 (2022)

*** CLEO-c: Phys. Rev. D 96, 092004 (2017); Phys. Lett. B 739, 90 (2014)

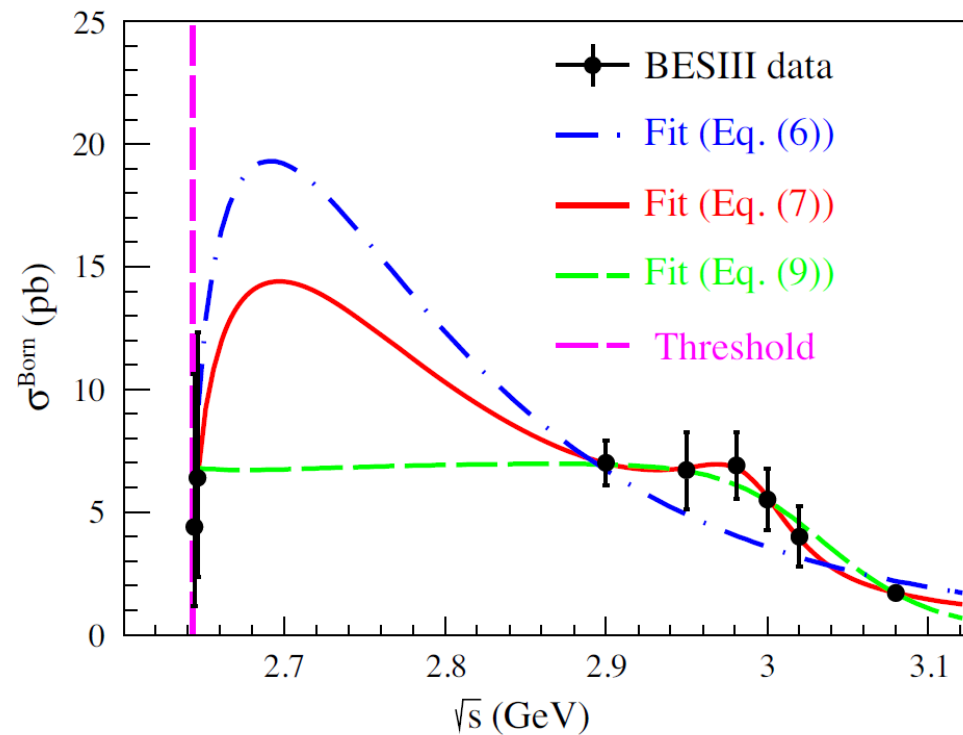


Double-strange hyperons

- $e^+e^- \rightarrow \Xi^- \bar{\Xi}^+$ studied for the first time.
- Possible resonance around 3 GeV.

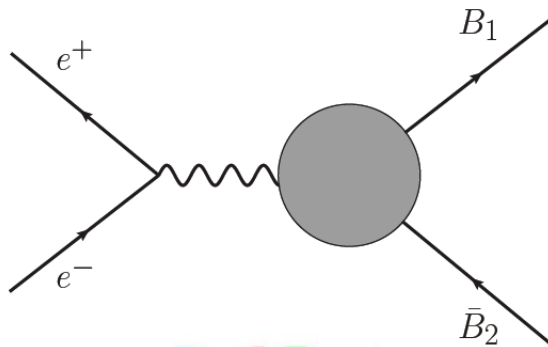


BESIII



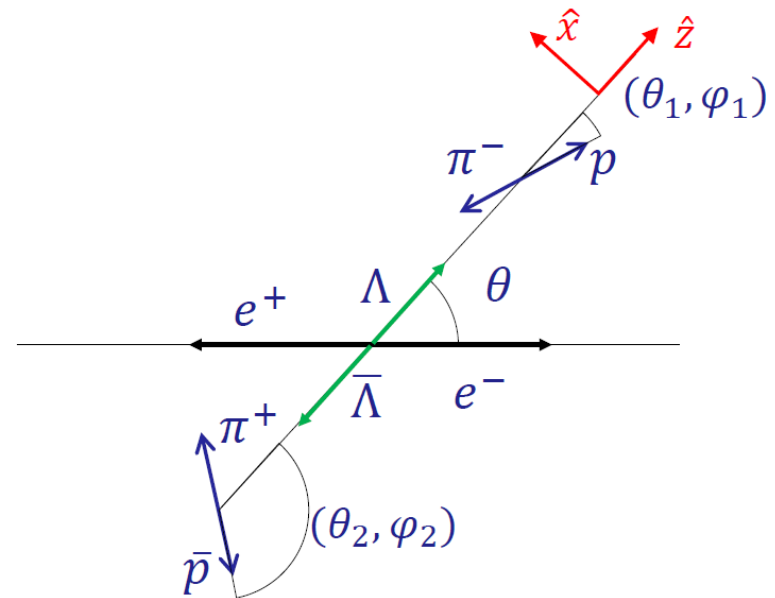
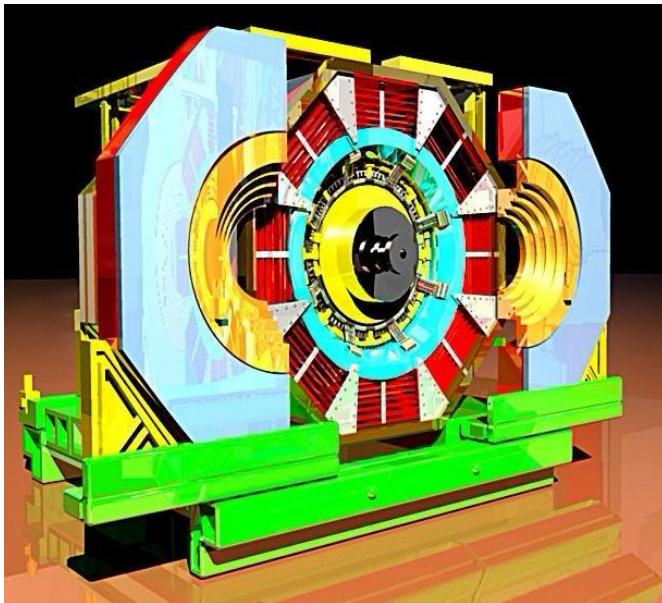


Spin Analysis



BES III

Consider $e^+e^- \rightarrow \bar{Y}Y, Y \rightarrow BM + c.c$



Formalism for $e^+ e^- \rightarrow \bar{Y}Y, Y \rightarrow BM + c.c.$

Production parameters of spin $\frac{1}{2}$ baryons:

- Angular distribution parameter η
- Phase $\Delta\Phi$

Decay parameters for 2-body decays: α_1 and α_2 .

Unpolarized part

Polarised part

Correlated part

$$W(\xi) = F_0(\xi) + \eta F_5(\xi) - \alpha_1 \alpha_2 (F_1(\xi) + \sqrt{1 - \eta^2} \cos(\Delta\Phi) F_2(\xi) + \eta F_6(\xi)) + \sqrt{1 - \eta^2} \sin(\Delta\Phi) (\alpha_1 F_3(\xi) - \alpha_2 F_4(\xi))$$

$$\mathcal{T}_0(\xi) = 1$$

$$\mathcal{T}_1(\xi) = \sin^2 \theta \sin \theta_1 \sin \theta_2 \cos \phi_1 \cos \phi_2 + \cos^2 \theta \cos \theta_1 \cos \theta_2$$

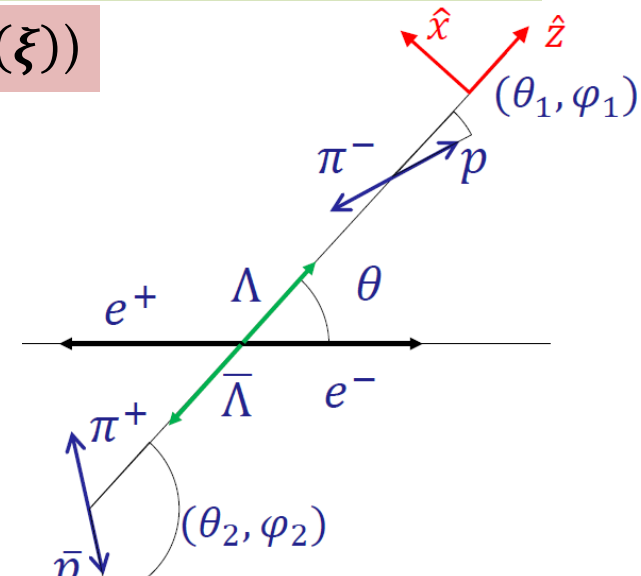
$$\mathcal{T}_2(\xi) = \sin \theta \cos \theta (\sin \theta_1 \cos \theta_2 \cos \phi_1 + \cos \theta_1 \sin \theta_2 \cos \phi_2)$$

$$\mathcal{T}_3(\xi) = \sin \theta \cos \theta \sin \theta_1 \sin \phi_1$$

$$\mathcal{T}_4(\xi) = \sin \theta \cos \theta \sin \theta_2 \sin \phi_2$$

$$\mathcal{T}_5(\xi) = \cos^2 \theta$$

$$\mathcal{T}_6(\xi) = \cos \theta_1 \cos \theta_2 - \sin^2 \theta \sin \theta_1 \sin \theta_2 \sin \phi_1 \sin \phi_2$$





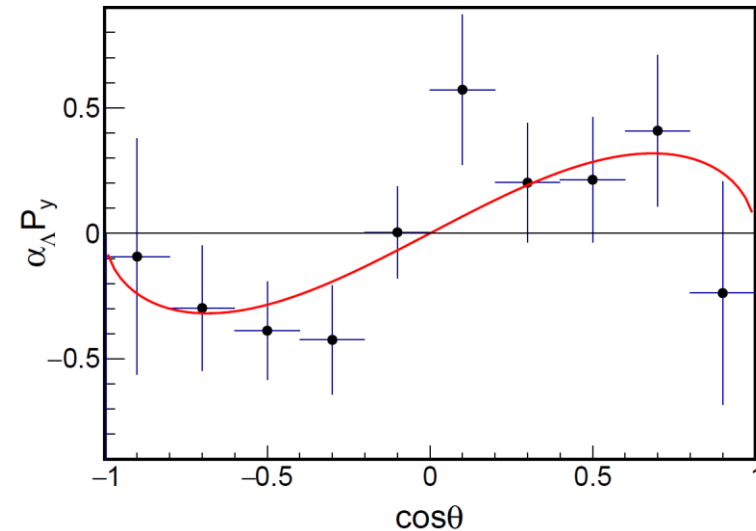
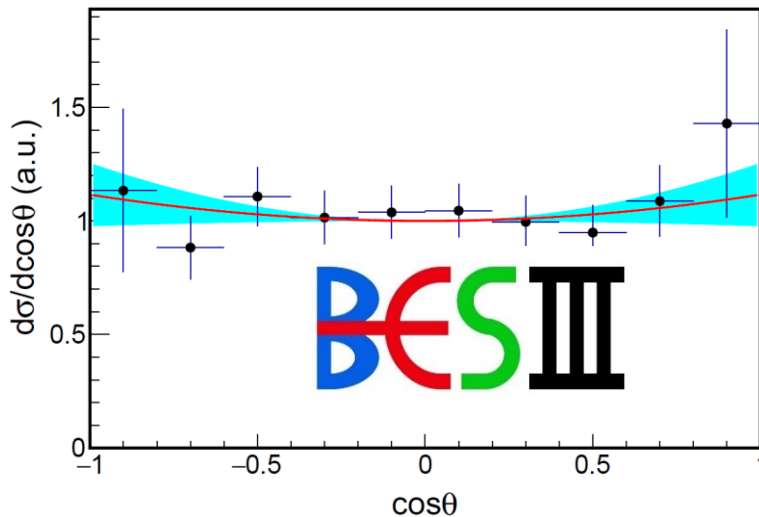
First complete measurement of Λ EMFF

- New BESIII data at 2.396 GeV with 555 exclusive $\bar{\Lambda}\Lambda$ events in sample.

- $R = |G_E/G_M| = 0.96 \pm 0.14 \pm 0.02$
- $\Delta\Phi = 37^\circ \pm 12^\circ \pm 6^\circ$
- $\sigma = 118.7 \pm 5.3 \pm 5.1$ pb

BESIII:
Phys. Rev. Lett. 123, 122003 (2019)

- Most **precise** result on R and σ
- **First** conclusive result on $\Delta\Phi$

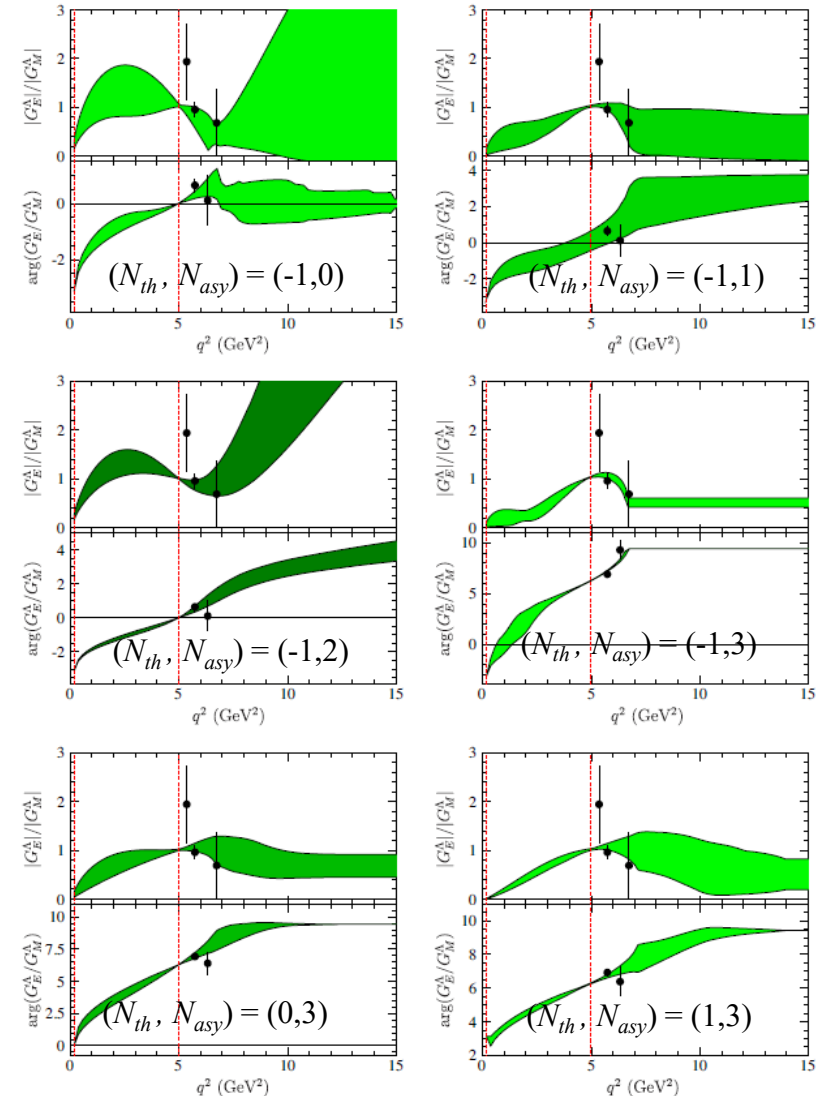




The Λ Charge Radius

Mangoni, Pacetti & Gustafsson*:

- Recall $\langle r_E^2 \rangle = 6 \frac{dG_E(q^2)}{dq^2} \Big|_{q^2=0}$
 - Neutrals: $\left. \frac{dR(q^2)}{dq^2} \right|_{q^2=0} = \frac{1}{\mu} \frac{\langle r_E \rangle^2}{6}$
- Extract $\langle r_\Lambda^2 \rangle$ from
 - $N_{th} = \frac{1}{\pi} \arg\left(\frac{G_E^\Lambda(q_{th}^2)}{G_M^\Lambda(q_{th}^2)}\right)$ and
 - $N_{asy} = \frac{1}{\pi} \arg\left(\frac{G_E^\Lambda(q_{asy}^2)}{G_M^\Lambda(q_{asy}^2)}\right)$



Picture credit and results:

Mangoni, Pacetti & Tomasi Gustafsson,
Phys. Rev. D 104, 116016 (2021)

Data:

BESIII: Phys. Rev. Lett. 123, 122003 (2019)

BaBar: Phys. Rev. D 76, 092006 (2007)

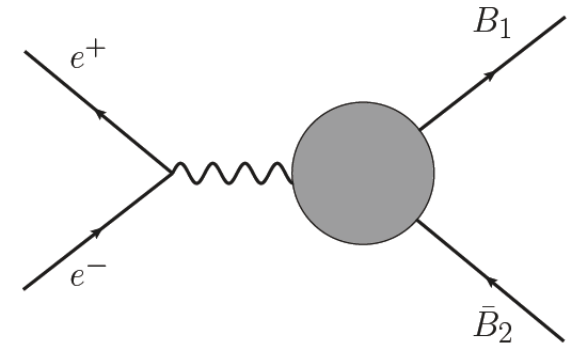
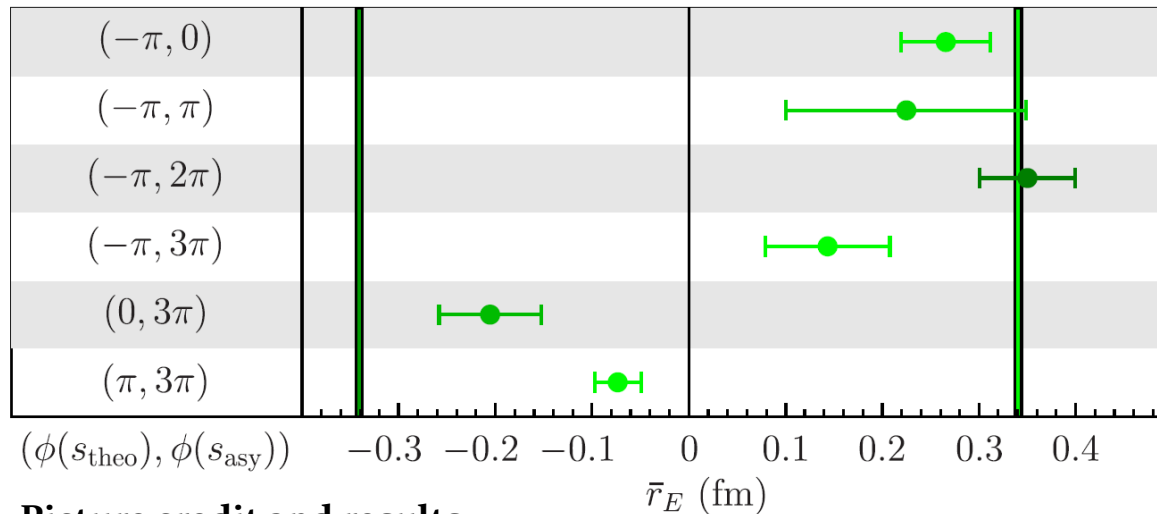


The Λ Charge Radius

Mangoni, Pacetti & Tomasi-Gustafsson*:

- Fit of different data from ** and *** to different scenarios
→ pinpointing the radius requires data at more energies

”Snapshot → Movie”



Picture credit and results:

Mangoni, Pacetti & Tomasi Gustafsson, Phys. Rev. D 104, 116016 (2021)

Data:

BESIII: Phys. Rev. Lett. 123, 122003 (2019)

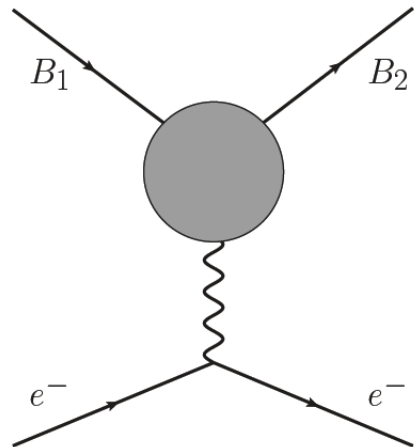
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Space-like

$$q^2 < 0$$



$e^- B \rightarrow e^- B$
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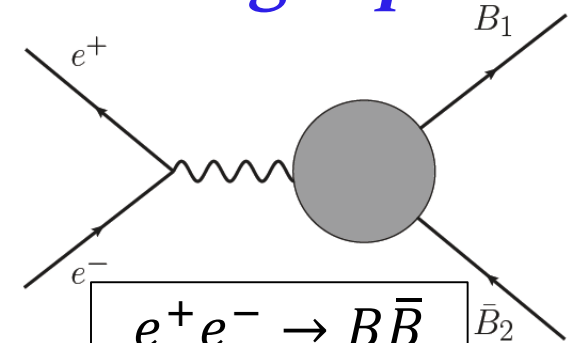
Time-like

$$q^2 > 0$$

Low- q^2

$B_1 \rightarrow B_2 e^+ e^-$
HADES
PANDA

High- q^2



$e^+ e^- \rightarrow B \bar{B}$
 $\bar{B} B \rightarrow e^+ e^-$
BES III
BELLE II
PANDA

$4m_e^2$

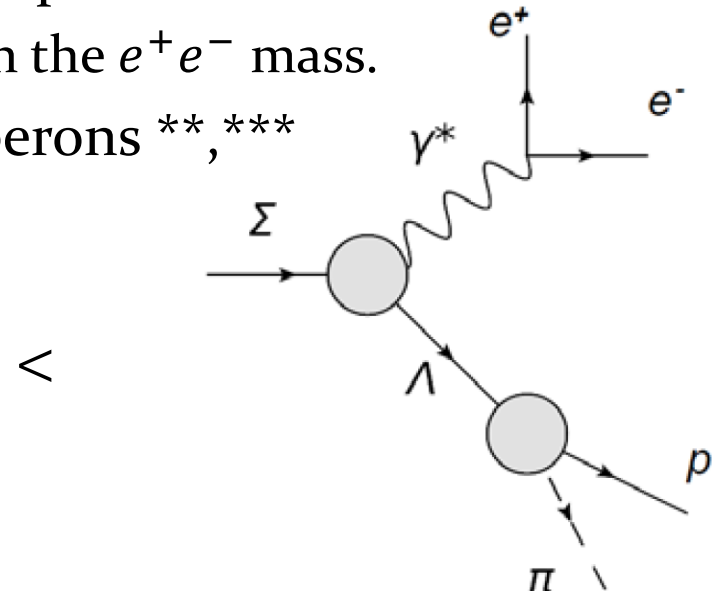
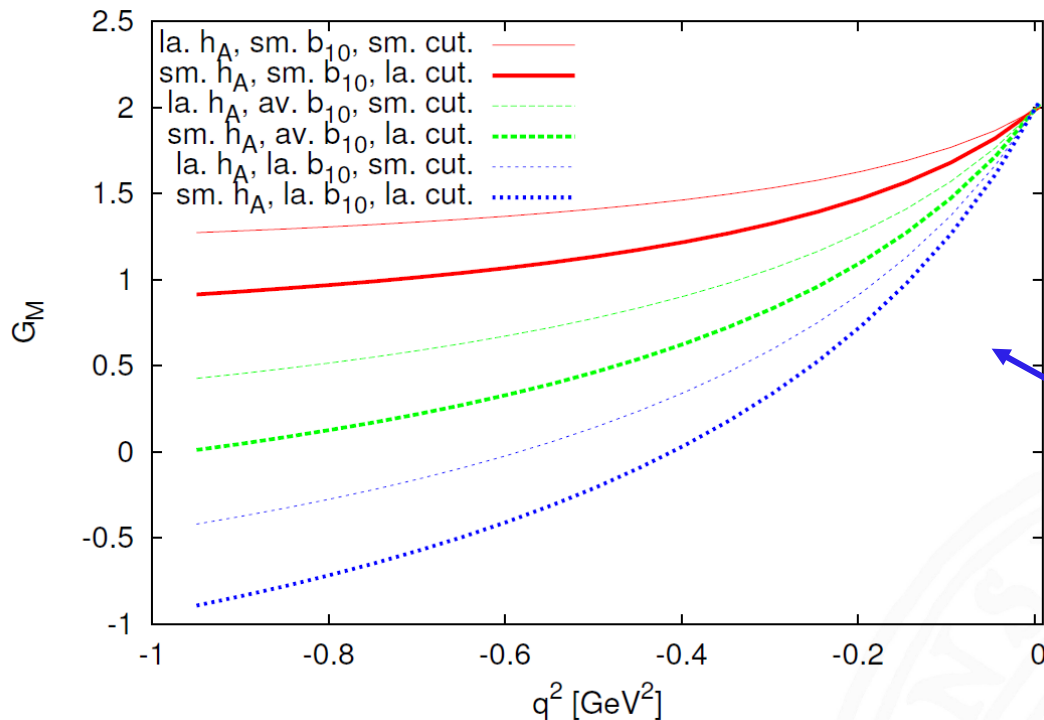
$(m_1 - m_2)^2 (m_1 + m_2)$

q^2



Low- q^2 : Hyperon transition FF

- Can be measured in Dalitz decay with HADES and PANDA.
- Dispersive + ChPT framework* developed for $\Sigma^0 \Lambda$
 $\rightarrow \langle r_M^2 \rangle$ from the G_M dependence on the e^+e^- mass.
- Framework extended to other J^P hyperons **, ***



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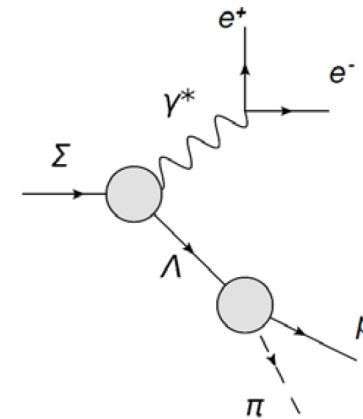
Leupold *et al.*:
 * Eur. Phys. J A 53, 117 (2017)
 ** Phys. Rev. C 101, 015206 (2020)
 *** Eur. Phys. J A 57, 183 (2021)



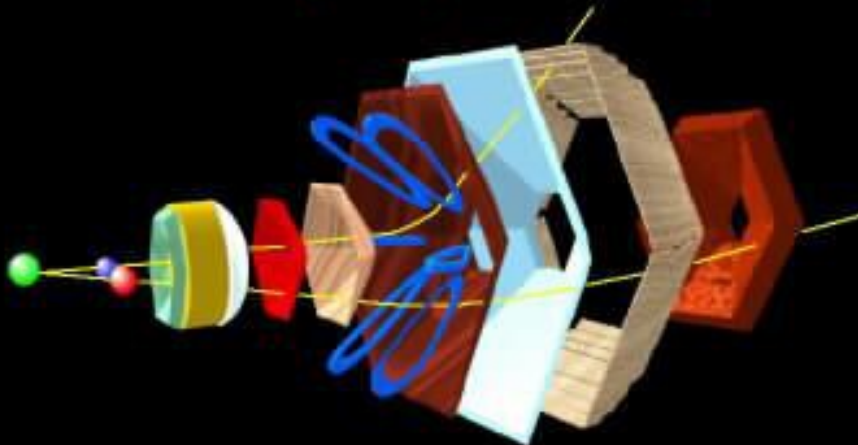
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Low- q^2 Structure with HADES

- * HADES + PANDA: Eur. Phys. J A 57, 138 (2021)
- ** Rafal Lalik, see dedicated EMMI presentation
- *** Jenny Regina, PhD Thesis Uppsala U and EMMI poster (2022)
- **** Jana Rieger, FAIRNESS talk (2022)



HADES High Acceptance BElectron Spectrometer



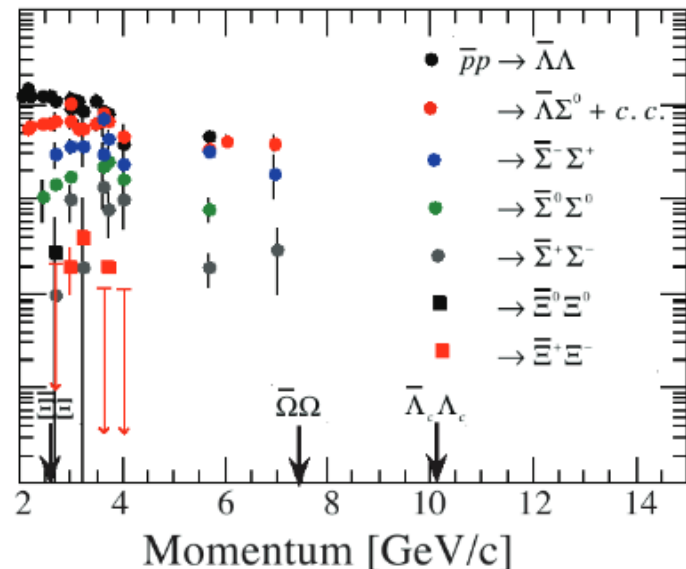
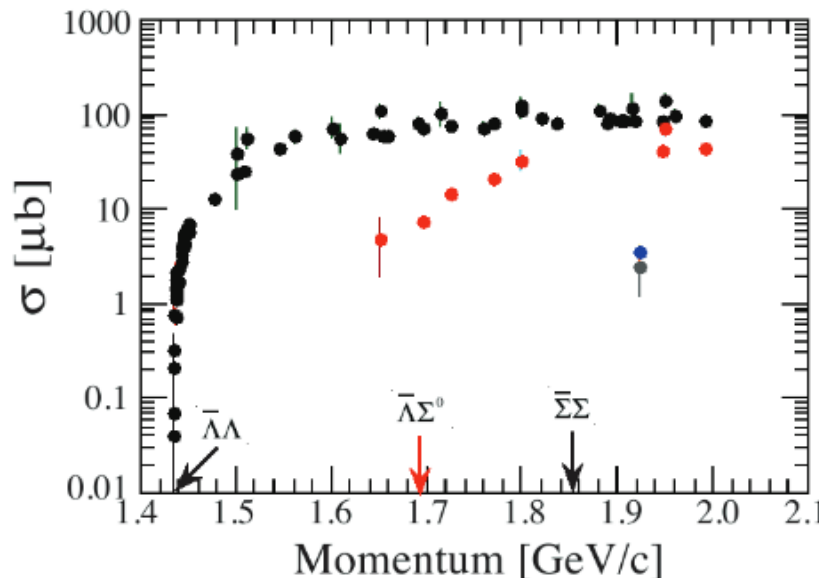
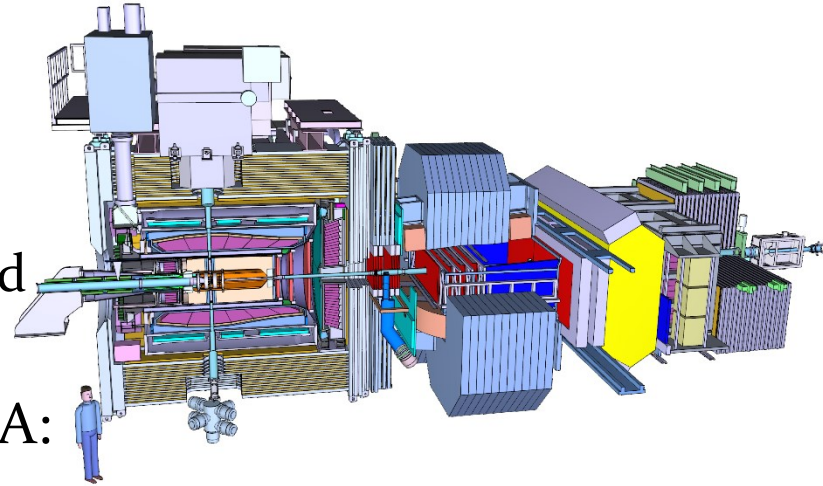
BICH MDC1 MDC2 MAGNET MDC3 MDC4 TOP2 SHOWER

- Hyperons from pp collisions^{*,**}.
- Part of FAIR Phase 0
→ Forward trackers from PANDA
- Excellent for e^+e^- tagging.
- Hyperon reconstruction refined^{***,****}.
- First beam time February 2022.



Low- q^2 Structure with PANDA

- Large expected Σ^0 hyperon yields in $\bar{p}p$ annihilations!
- Beam momenta up to 15 GeV/c
→ e^+e^- from antihyperon decay boosted
→ better chance to be detected?
- Hyperon reconstruction in PANDA:
Poster by A. Akram.



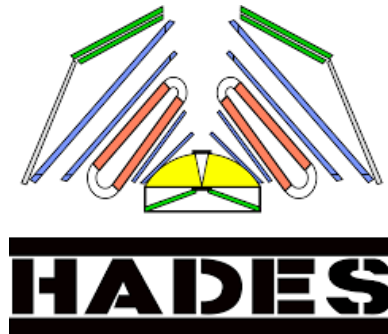


Summary

- The strong interaction manifest in the structure and size of hadrons.
- Hyperon polarisation accessible by their self-analysing decays
 - New angle to structure and size!
- Recent progress from BESIII.
- Pioneering measurements possible at experiments world-wide.

The logo for the BESIII experiment, with 'B' in blue, 'E' in red, 'S' in green, and 'III' in black.

BESIII





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Thanks for your attention!

*Knut and Alice
Wallenberg
Foundation*



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Research
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STINT

The Swedish Foundation for International
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