

The chiral anomaly and the eta-prime in vacuum and at low temperatures

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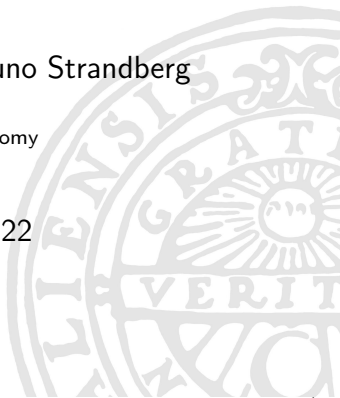


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- $U_A(1)$: would also be spontaneously broken (chiral condensate not invariant w.r.t. $U_A(1)$)
- ↪ would lead to 9th Goldstone boson (flavor singlet with quantum numbers of η , η')

No symmetry of *Quantum* Chromodynamics

- chiral anomaly: $U_A(1)$ is not symmetry of quantized theory



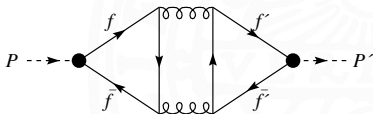
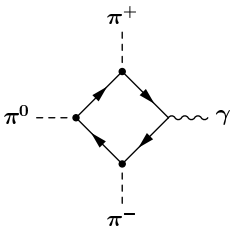
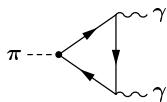
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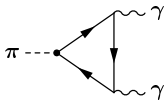


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- ↪ experimental fact: nature seems to prefer Lorentz invariance
- ↪ consequences ...



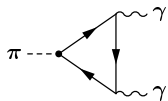
Consequences of $U_A(1)$ anomaly in vacuum



- parameter-free prediction of $\pi^0 \rightarrow 2\gamma$ in terms of pion decay constant f_π

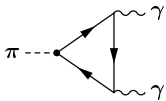


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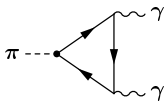
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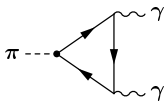
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- ↪ corrections suppressed $\sim m_\pi^2 \varepsilon^{\mu\nu\alpha\beta} \pi^0 F_{\mu\nu} F_{\alpha\beta}$

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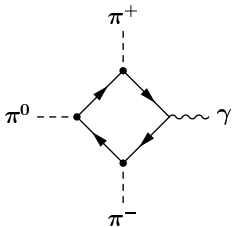


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in power counting of chiral perturbation theory:

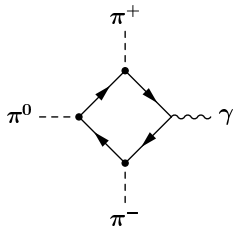
- anomaly $\sim O(q^4)$
- otherwise $\sim O(q^6)$
with generic momentum $q \sim m_\pi$

Consequences of $U_A(1)$ anomaly in vacuum II



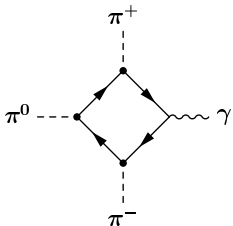
- coupling constant of $\varepsilon^{\mu\nu\alpha\beta} \partial_\mu \pi^0 \partial_\nu \pi^+ \partial_\alpha \pi^- A_\beta \sim O(q^4)$
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- predictive power for reactions $e^+ e^- \rightarrow 3\pi$ and/or $\gamma + \pi \rightarrow 2\pi$
close to threshold? \rightsquigarrow spare slides

Consequences of $U_A(1)$ anomaly in vacuum III

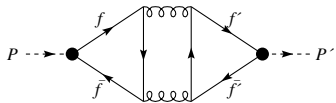


figure from Klabucar/Kekez/Scadron,
hep-ph/0012267

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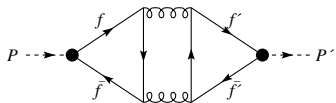


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- Veneziano formula for mass of eta singlet:

$$m_{\eta_1}^2 = \frac{2N_f \tau}{f_\pi^2} \sim \frac{1}{N_c}$$

with topological susceptibility $\tau = -i \int d^4x \langle 0 | \omega(x) \omega(0) | 0 \rangle$

and $\omega \sim G_{\mu\nu}^a \tilde{G}_a^{\mu\nu}$

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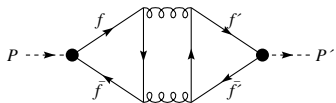


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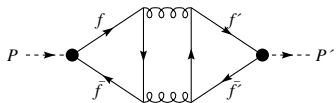


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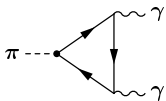
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- ↪ starting point of large- N_c chiral perturbation theory (χ PT)
(Kaiser/Leutwyler, EPJ C 17, 623 (2000))

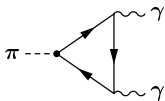
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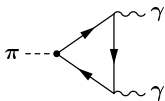
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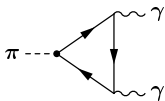
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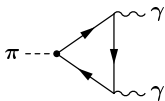
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instead: decay decouples from anomaly,
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- ↪ but maybe at **finite density**
(Goda/Jido, PTEP 2014, 3, 033D03 (2014))
- ↪ contradiction? ↪ should be resolved



Chiral multiplets

at chiral restoration of $SU(3)$ (no statement about $U_A(1)$ needed!):

- chiral multiplets (L, R) instead of just flavor multiplets

thanks to D. Jido for pointing this out to me, Phys.Rev.C85 (2012) 032201

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- ↪ η' should become light at transition

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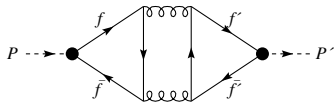
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- caveats: only good argument if not strong first-order transition and **if states survive as quasi-particles**



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task: determine in-medium width of η' meson



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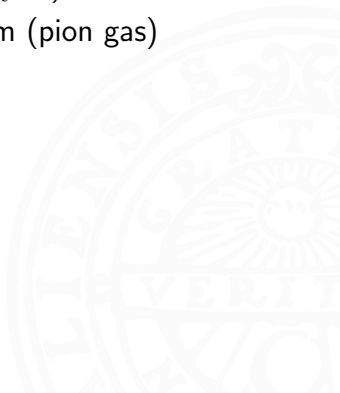
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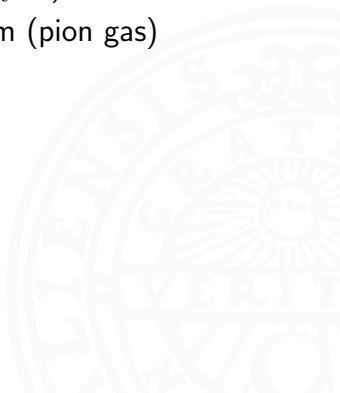
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 - outlook: consequences for finite density



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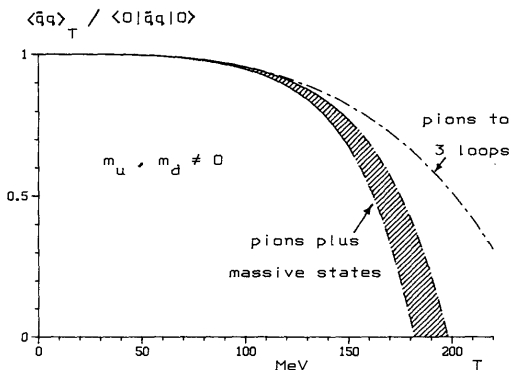
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- ↪ chiral perturbation theory allows for **systematic**, model independent calculations at low temperatures
- provides excellent description of onset of chiral restoration for chiral condensate (and for pion decay constant) \rightsquigarrow next slide
- ↪ chiral perturbation theory has something to say about not too low temperatures

Drop of quark condensate



- uses interacting pions and resonance gas
- produces realistic transition temperature

Gerber/Leutwyler, Nucl.Phys.B 321, 387 (1989)

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- include resonances such that formal low-energy and large- N_c limit fits to chiral perturbation theory

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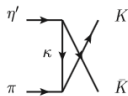
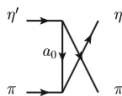
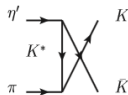
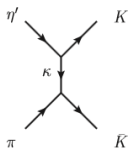
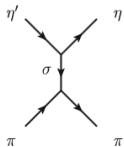
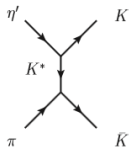
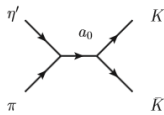
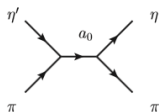
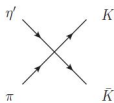
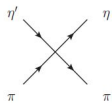
- while for $N_c = 3$:

$$m_{\eta'} \stackrel{!}{\approx} m_R$$

for resonances $R = a_0, f_0, \kappa, K^*$

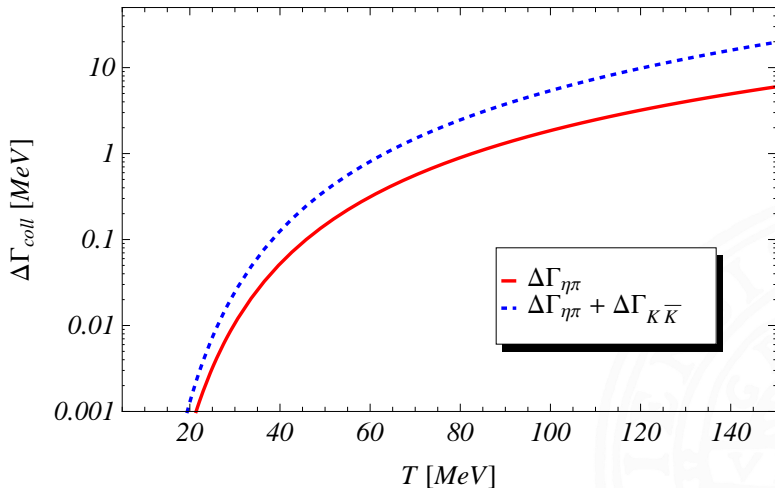
- ↪ include resonances such that formal low-energy and large- N_c limit fits to chiral perturbation theory
- ↪ inclusion of resonances as model independent as possible

Processes/diagrams for $\pi\eta'$ scattering

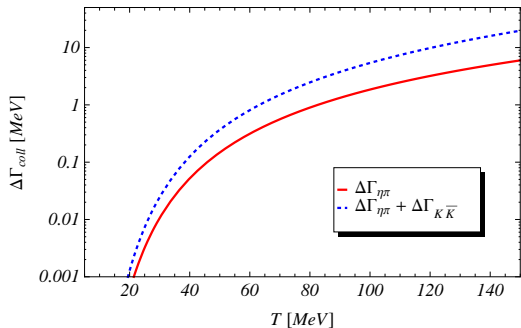


(note: loops are suppressed in the large- N_c limit)

Results: collisional width of η' meson

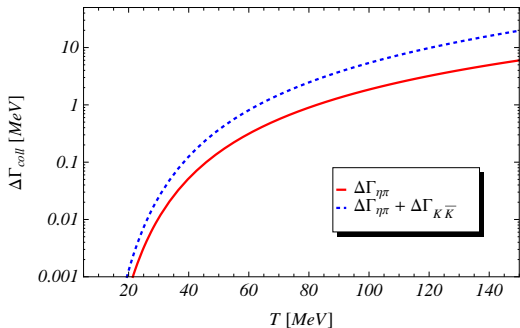


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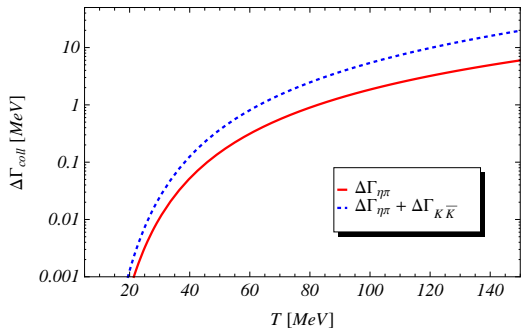
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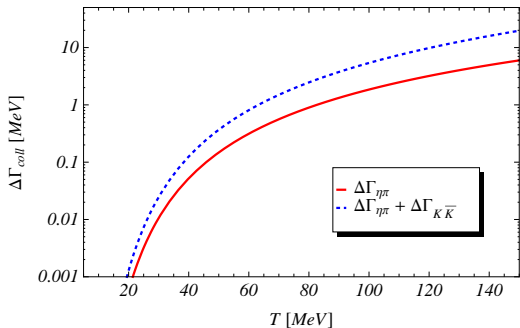
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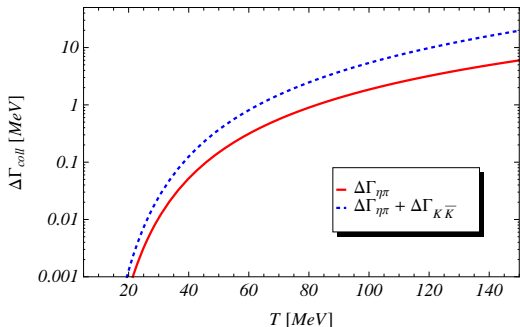
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- maybe via anomaly driven processes $\eta' \rightarrow \gamma\gamma, \gamma\pi^+\pi^-$

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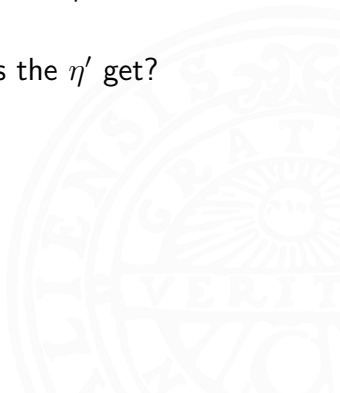
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- ↪ η' survives as a quasi-particle

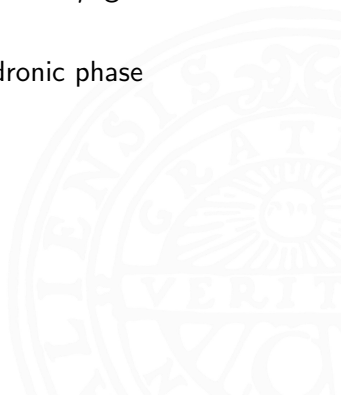
Outlook

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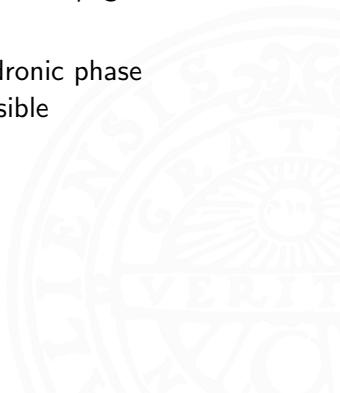
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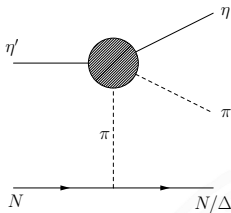
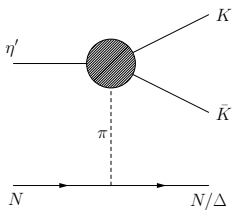
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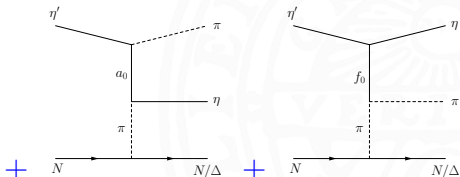
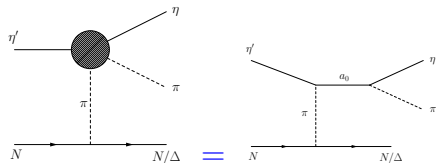
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- ↪ **suggests that three-body final states are important!** (while most calculations implicitly assume dominance of two-body final states)
- in-medium modifications of $\pi^0 \rightarrow \gamma\gamma$, $\eta' \rightarrow \gamma\gamma$, $\eta' \rightarrow \gamma\pi^+\pi^-$
- ↪ still work left to do for theory

Important processes at finite density

three-body final states!



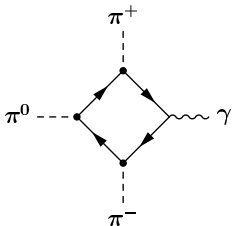
in more detail:



Spare slides

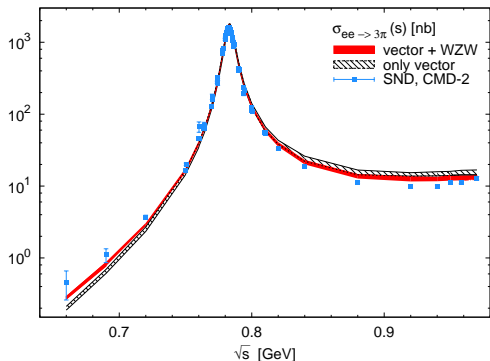


Consequences of $U_A(1)$ anomaly in vacuum II



- coupling constant of $\varepsilon^{\mu\nu\alpha\beta} \partial_\mu \pi^0 \partial_\nu \pi^+ \partial_\alpha \pi^- A_\beta \sim O(q^4)$
fixed by anomaly
- corrections (=dominant in absence of anomaly) $\sim O(q^6)$
- ↪ predictive power for reactions $e^+ e^- \rightarrow 3\pi$ and/or $\gamma + \pi \rightarrow 2\pi$
close to threshold?
- ↪ How far is threshold away from idealized case of chiral limit?

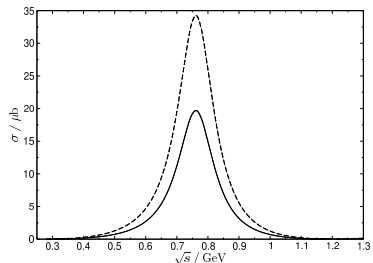
$$e^+ e^- \rightarrow 3\pi$$



C. Terschläsen, B. Strandberg, SL, F. Eichstädt,
Eur.Phys.J.A 49 (2013) 116

- anomaly caused by Wess-Zumino-Witten (WZW) term
- data dominated by ω vector meson peak
- ↪ anomaly has some effect, but does not dominate a region
- ↪ threshold at $3 m_\pi$ already quite sizable \neq chiral limit

$$\gamma + \pi \rightarrow 2\pi$$



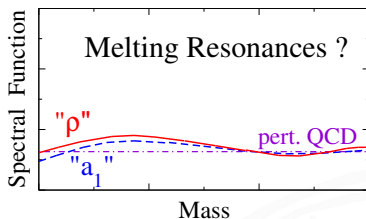
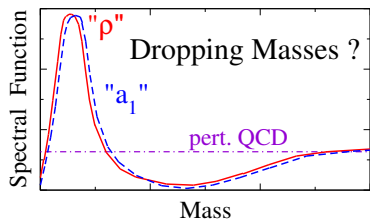
M. Hoferichter, B. Kubis, D. Sakkas,
Phys.Rev.D86, 116009 (2012)

- expect completion of data analysis from COMPASS@CERN
(pion beam, Primakov effect, cf. J.M. Friedrich, EPJ Web Conf. 199, 01016 (2019))
 - calculation includes anomaly and pion-pion rescattering using dispersion theory
 - **solid line:** prediction from anomaly
dashed line: size of anomaly scaled up by about 30%
- ↪ can use whole range to pin down anomaly, not just threshold region

Mass shift?

- systematic calculation of thermal modifications of properties of η' using large- N_c chiral perturbation + resonances is interesting
- ↪ mass shift?
- ↪ check first: does η' survive at all in a thermal medium?
 - personal history in scepticism against mass shifts ;-)
 - hadronic many-body framework often produces broad spectral functions instead of dropping masses
 - deconfinement shines out chiral effects

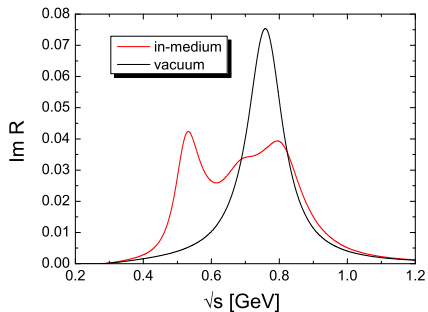
Mass shift vs. broadening



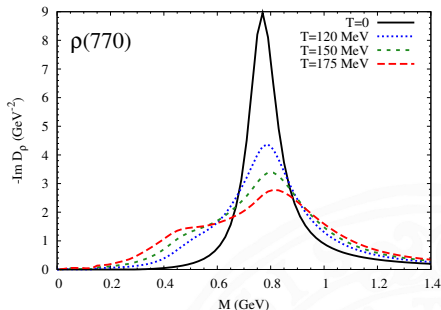
- chiral restoration demands degeneracy of spectra of chiral partners
(btw: for spin 1: 16-plets, not 18-plets)
- melting of resonances might be hadronic precursor to deconfinement

figures from Rapp, Wambach, van Hees, arXiv:0901.3289 [hep-ph]

Much celebrated example: ρ meson



M. Post, SL, U. Mosel,
Nucl.Phys.A 741, 81 (2004)



R. Rapp, J. Wambach, H. van Hees,
arXiv:0901.3289 [hep-ph]

different groups (with different models) obtain
broad ρ meson spectra, essentially no mass shift