

# Searches for Lorentz violation in

W.Heil

## $^3\text{He}/^{129}\text{Xe}$ clock comparison experiments

### Outline:

- Features of frequency standards and clocks
- $^3\text{He}/^{129}\text{Xe}$  „spin“-clock
- $^3\text{He}/^{129}\text{Xe}$  clock-comparison experiments
- Conclusion and outlook

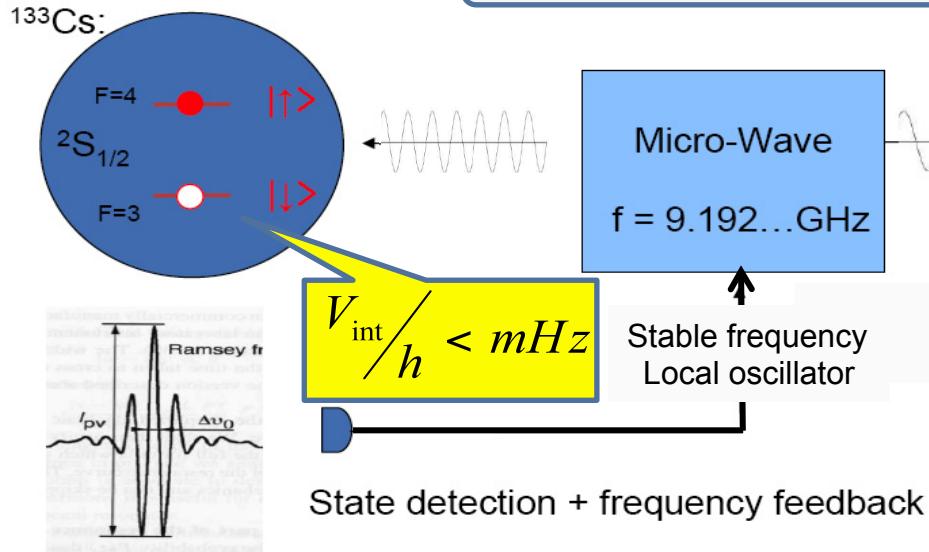
# Atomic Clocks

Oscillator + Frequency divider + Counter

$6S_{1/2}: F=3, m_F=0 \leftrightarrow F=4, m_F=0$   
 @  $\nu = 9.192 \dots \text{GHz}$

1 second = 9,192,631,770 cycles

Current accuracy:  
 Microwave:  $6 \times 10^{-16}$   
 Optical :  $3 \times 10^{-17}$

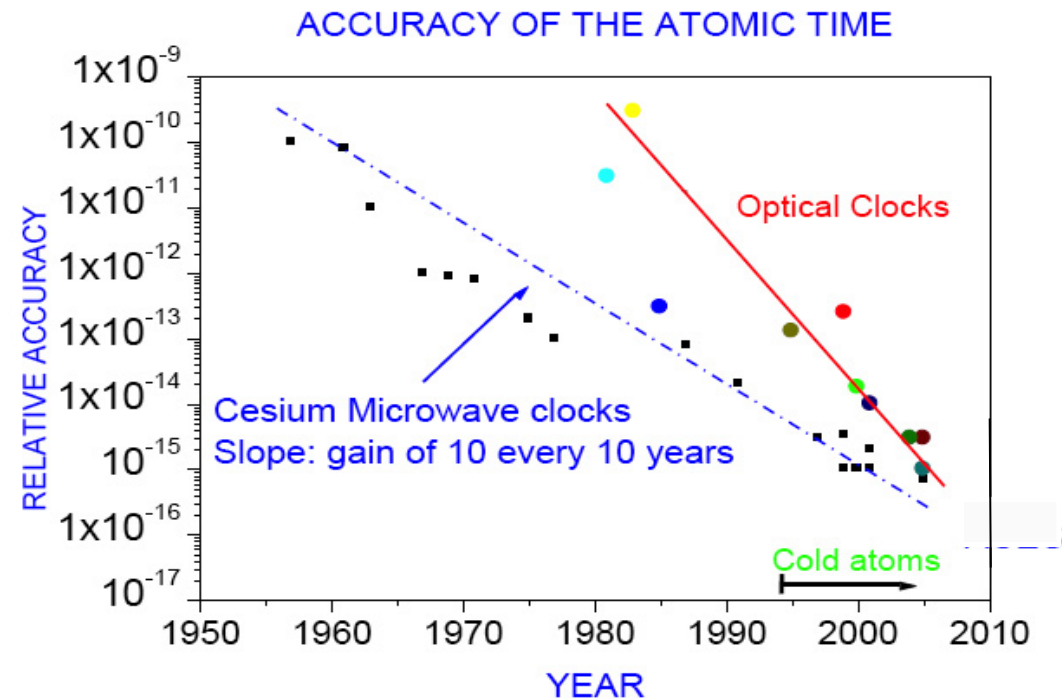


$\approx 1 \text{ ns / day}$

sensitivity (absolute scale):  $\delta\nu \approx \text{mHz}$

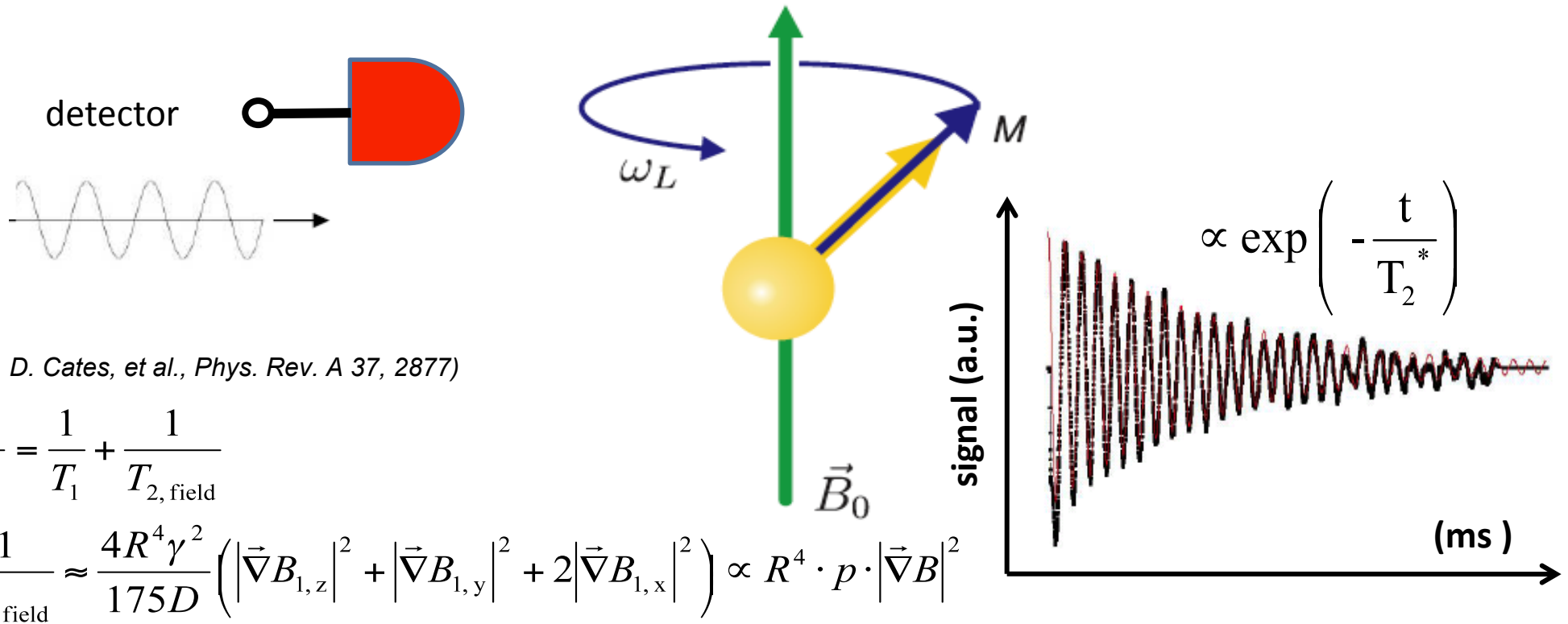
better:  
 reference transition at  $f \approx 1 \text{ Hz}$  with  
 $\delta f / f \approx 10^{-14}$

$\Rightarrow$  „nuclear spin -clock“



# Clock based on nuclear spin precession „ spin-clock“

A magnetic moment  $M$  is associated with the atomic spin.



(G. D. Cates, et al., Phys. Rev. A 37, 2877)

$$\frac{1}{T_2^*} = \frac{1}{T_1} + \frac{1}{T_{2,\text{field}}}$$

$$\frac{1}{T_{2,\text{field}}} \approx \frac{4R^4\gamma^2}{175D} \left( |\vec{\nabla}B_{1,z}|^2 + |\vec{\nabla}B_{1,y}|^2 + 2|\vec{\nabla}B_{1,x}|^2 \right) \propto R^4 \cdot p \cdot |\vec{\nabla}B|^2$$

$$T_1 > 100 \text{ h} \implies$$

This moment precesses in a magnetic field.

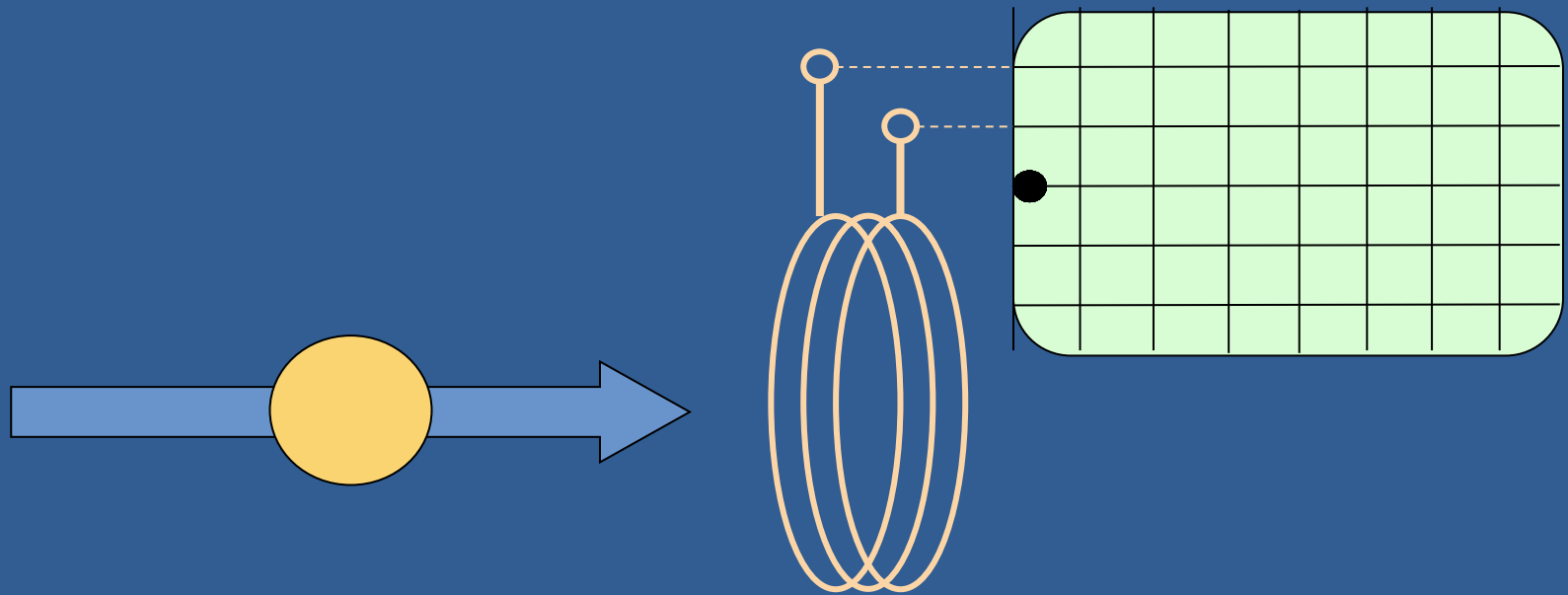
Long  $T_2^*$  :

$$p \sim \text{mbar}, R \sim 3 \text{ cm}, B_1 \sim \mu\text{T}$$

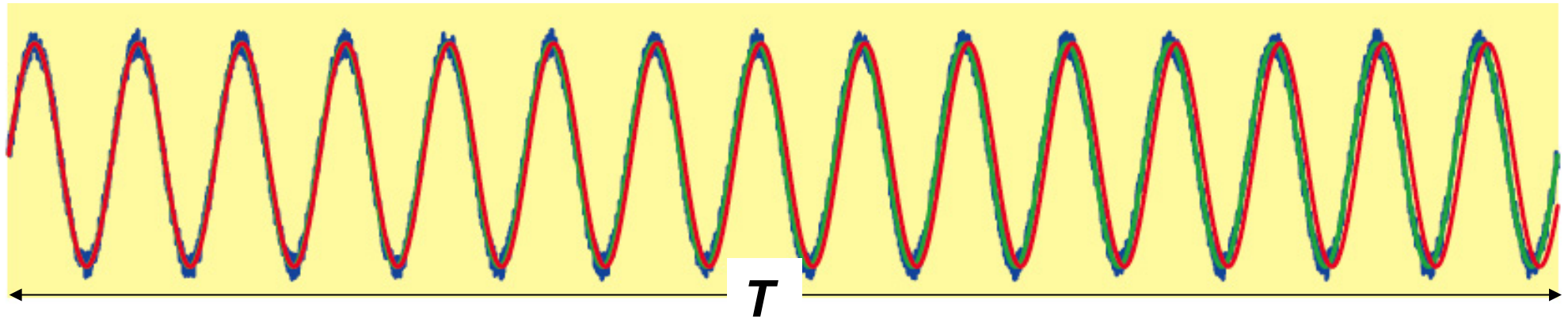
$$\omega_L = 2\pi\nu_L = \gamma |\vec{B}|$$

# Spin-clock: Detection of free spin precession:

- long spin coherence times  $T_2^* > 1$  day @  $\Delta f/f \sim 10^{-14}$
- free spin precession: no induced frequency shifts due to feedback phase error, light shift, etc. (Maser, Cs-M)
- use of  $LT_c$ -SQUIDs to detect the spin precession signal
  - intrinsic noise of SQUID:  $\sim 1$  fT/ $\sqrt{\text{Hz}}$
- no feedback coupling between detector and spin sample



# FREQUENCY ESTIMATION



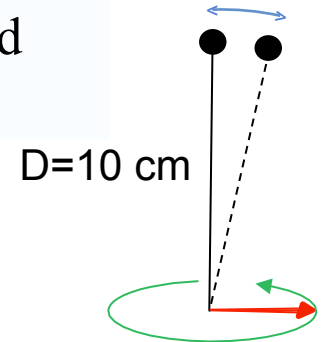
Accuracy of frequency determination:

$$\sigma_f \propto \left[ \text{Fourier width} \frac{1}{T} \right] \times \left[ \frac{1}{\left[ \# \text{ data points } T \right]^{1/2}} \right] \propto \frac{1}{T^{3/2}}$$

If the noise  $w[n]$  is **Gaussian distributed**, the Cramer-Rao Lower Bound (CRLB) sets the lower limit on the variance  $\sigma_f^2$

$$\sigma_f^2 \geq \frac{12}{(2\pi)^2 \cdot (SNR)^2 \cdot f_{BW} \cdot T^3} \times C(T_2^*)$$

$\Delta x \approx 0.1 \mu\text{m} / \text{day}$



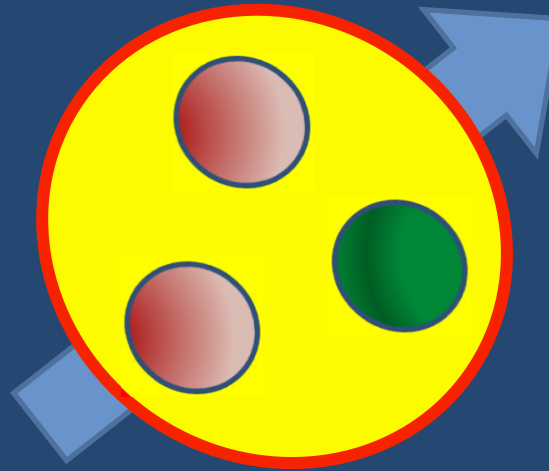
example:  $SNR = 10000:1$ ,  $f_{BW} = 1 \text{ Hz}$ ,  $T = 1 \text{ day} \Rightarrow \sqrt{\sigma_f^2} \approx \text{pHz}$

# ${}^3\text{He}/{}^{129}\text{Xe}$ „spin“-clock

$$\mu_n = -1.913 \mu_K$$

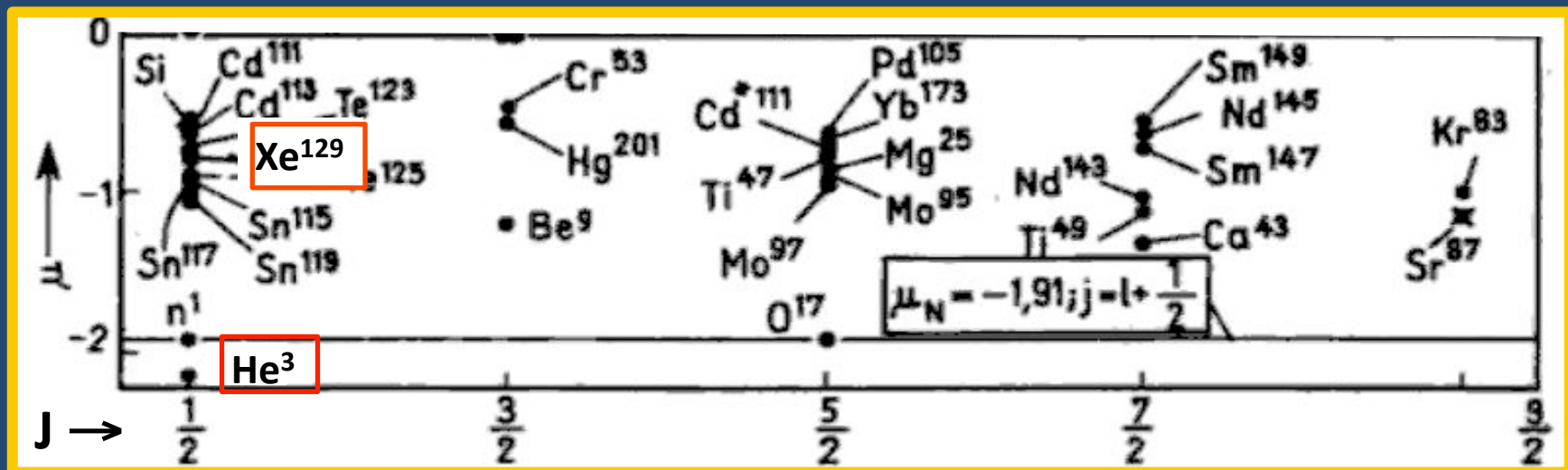
$$\mu_{\text{He}} = -2.1276 \mu_K$$

$$\mu_{\text{Xe}} = -0.7779 \mu_K$$

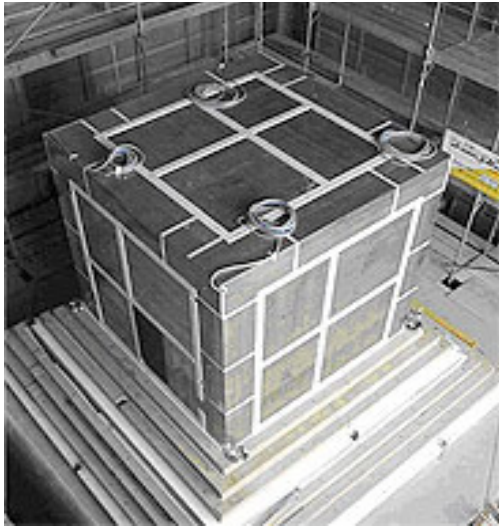


OP-techniques:  
MEOP  
SEOP

Schmidt-model:

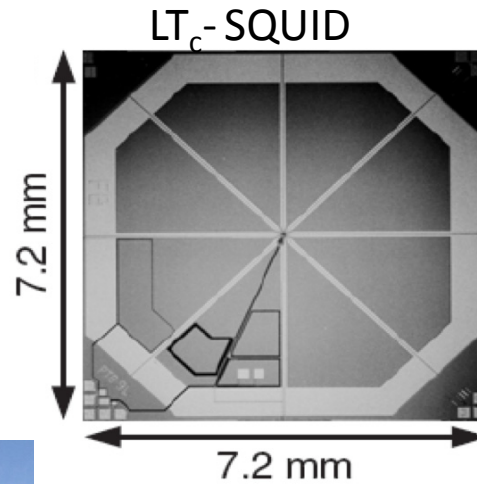


# BMSR 2, PTB Berlin

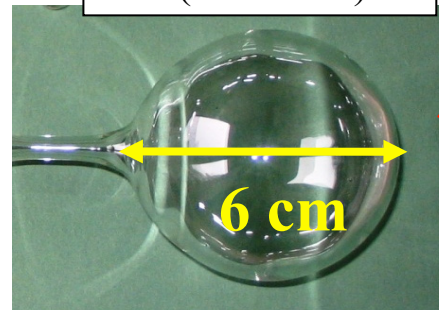


The 7-layered magnetically shielded room  
(residual field < 2 nT)

J. Bork, et al., Proc. Biomag 2000, 970 (2000).



<sup>3</sup>He (4.5 mbar)

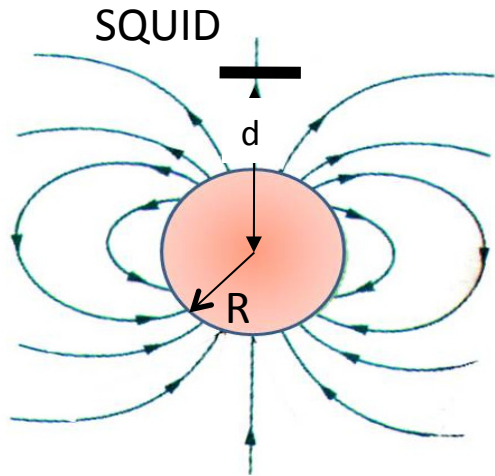


magnetic guiding field  $\approx 0.4 \mu\text{T}$   
(Helmholtz-coils)

$$\left| \vec{\nabla} B_{x,y,z} \right| \approx 20 \text{ pT/cm}$$

# $^3\text{He}$ free spin-precession signal

Eur. Phys. J. D 57, 303–320 (2010)



**Signal:**

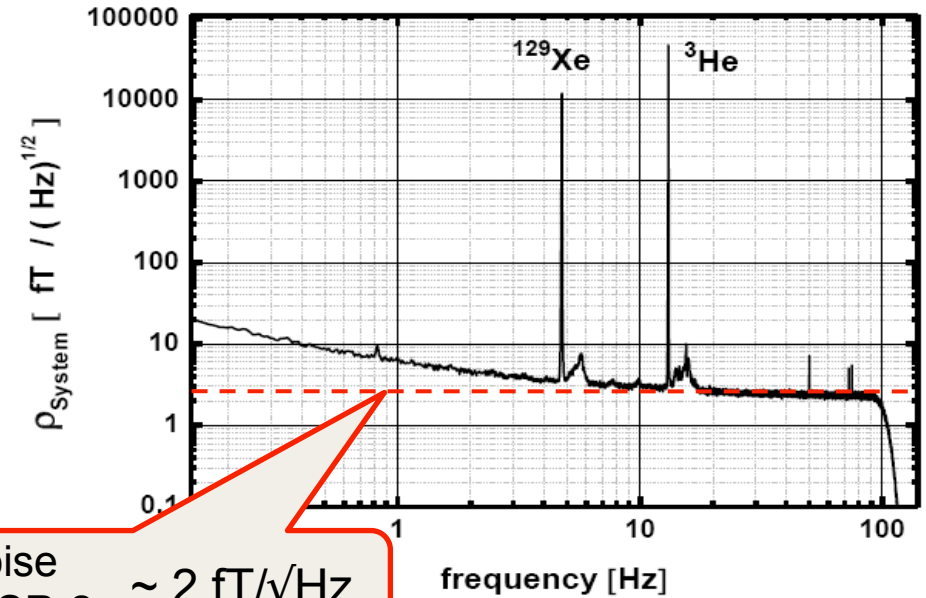
$$\Delta B[\text{pT}] \approx 220 \cdot p[\text{mbar}] \cdot P \cdot \left(\frac{R}{d}\right)^3$$

parameters:

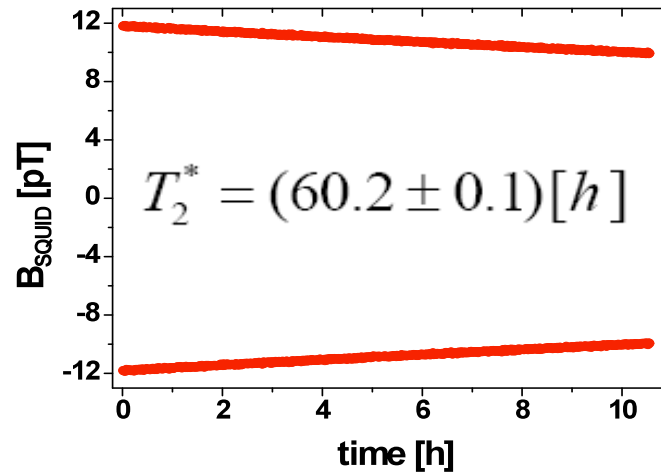
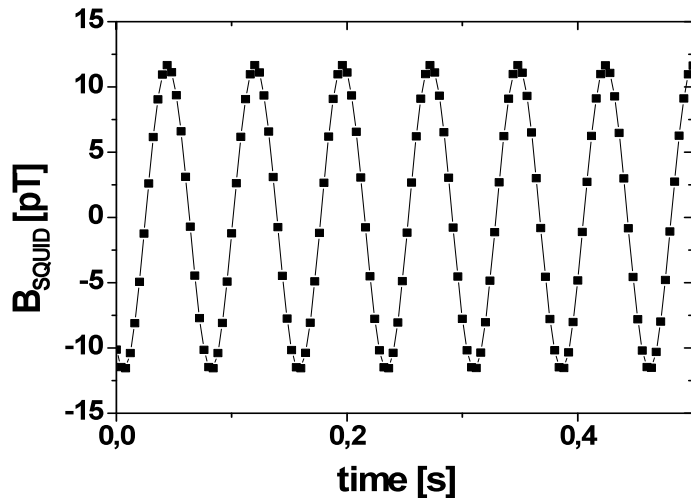
$p_{\text{He}} = 1\text{-}3 \text{ mbar}$  ;  $P = 10\text{-}50\%$

$R = 2.9 \text{ cm}$  ;  $d = 6 \text{ cm}$

$\rightarrow \Delta B = 10\text{-}30 \text{ pT}$



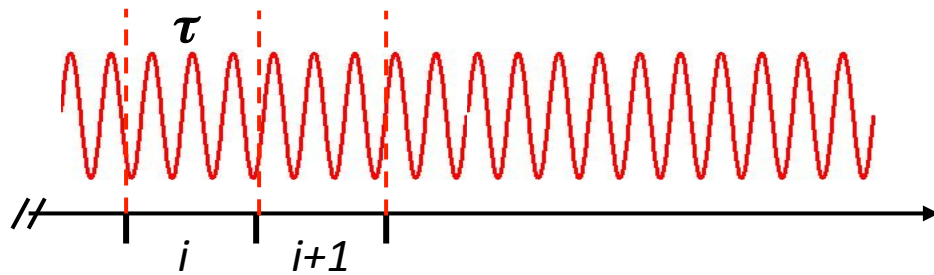
system noise inside BMSR-2  $\sim 2 \text{ fT}/\sqrt{\text{Hz}}$



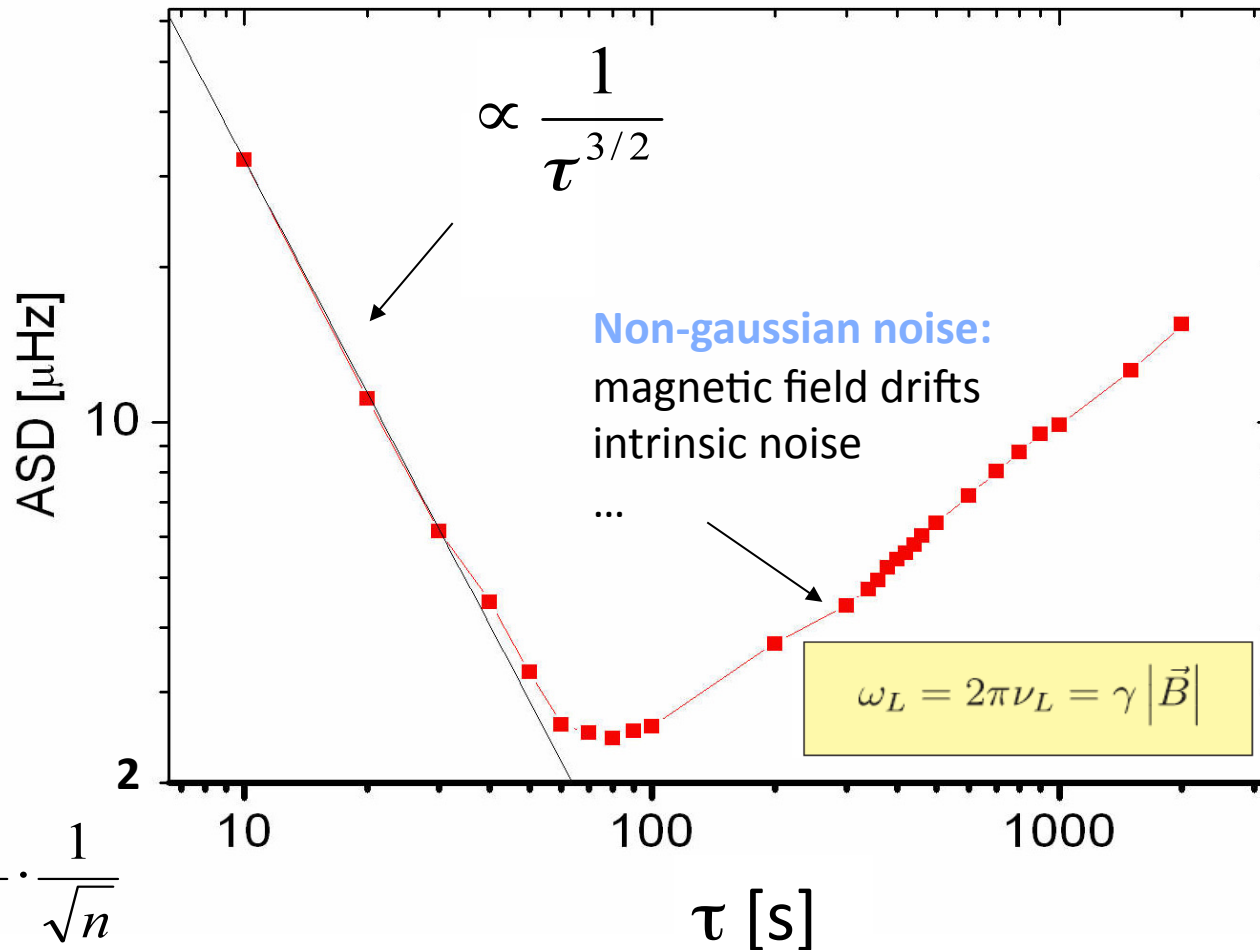
**Note:**  
 At present, the Xe spin coherence time  $T_2^*$  is limited to  
 $3 \text{ h} < T_2^* < 4 \text{ h}$   
 due to wall relaxation



# Test of CRLB via Allan Standard Deviation (ASD)

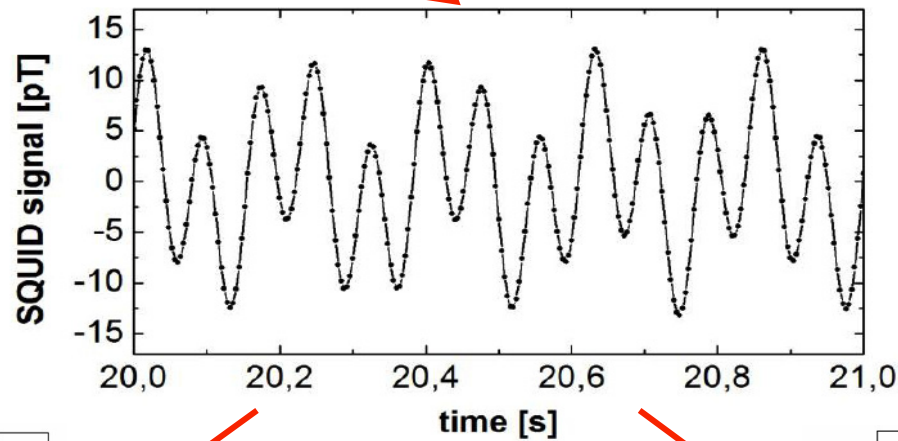
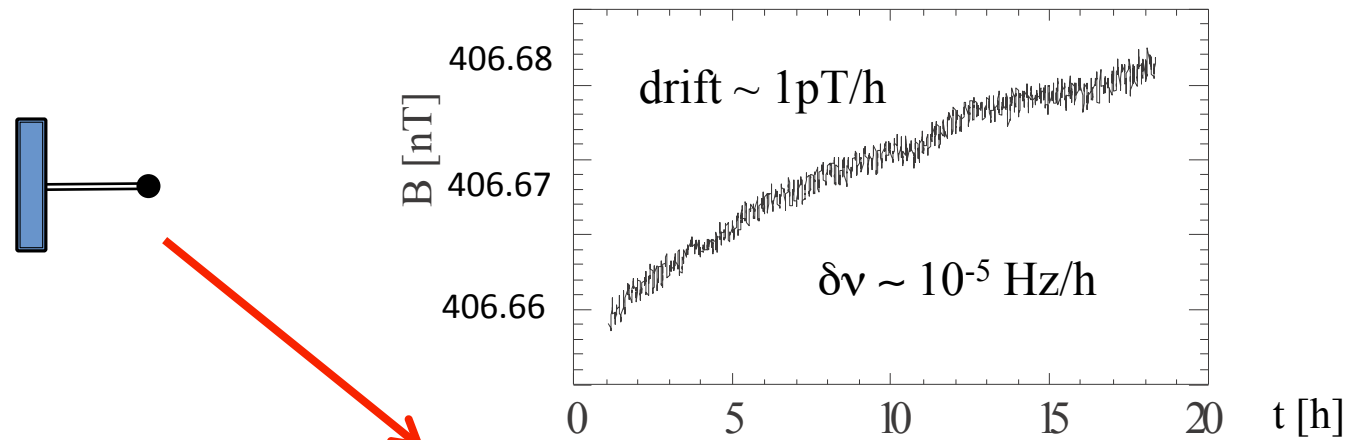
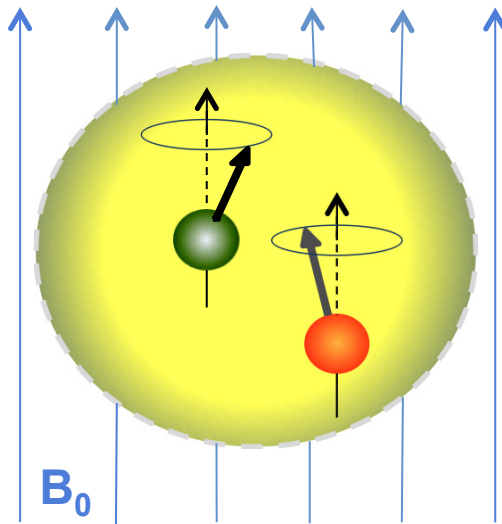


$$\sigma_v(\tau) = \sqrt{\frac{1}{2} \frac{\sum_{i=1}^{N-1} (\bar{v}_{i+1}(\tau) - \bar{v}_i(\tau))^2}{N-1}}$$

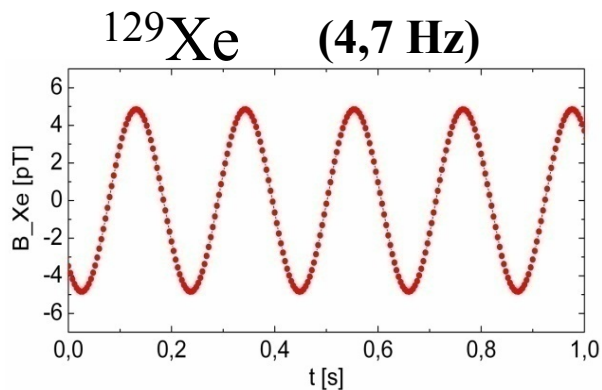


$$\sigma_v \propto \frac{1}{(60s)^{3/2}} \cdot \frac{1}{\sqrt{n}}$$

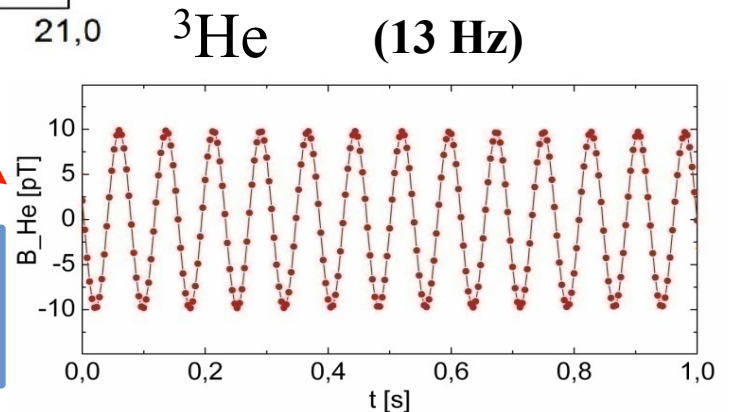
# $^3\text{He}$ / $^{129}\text{Xe}$ clock comparison to get rid of magnetic field drifts



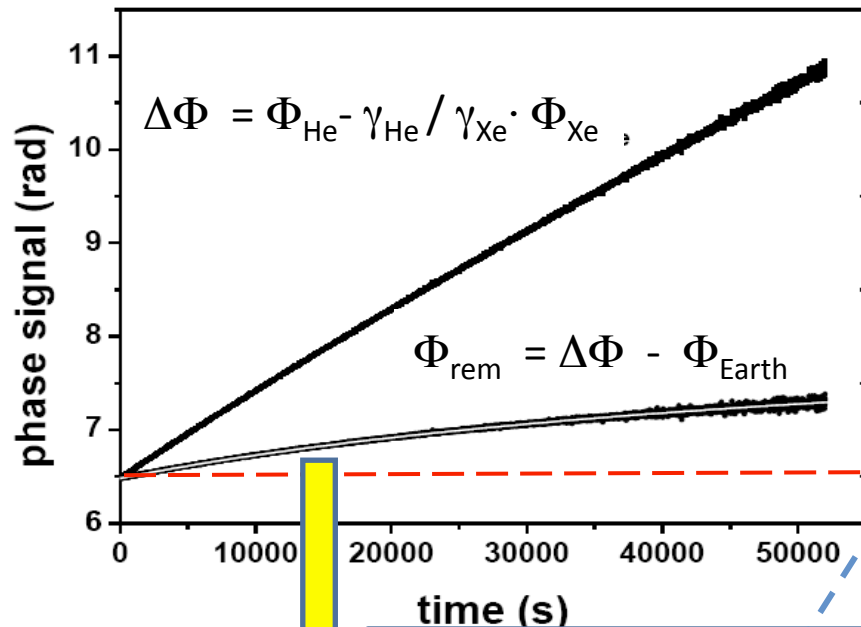
$$\omega_L = 2\pi\nu_L = \gamma |\vec{B}|$$



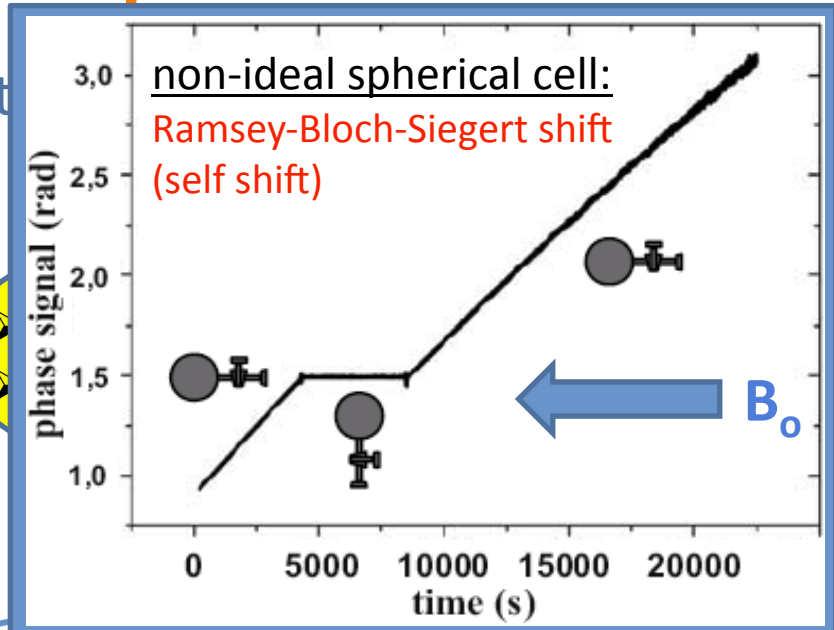
$$\Delta\Phi = \Phi_{\text{He}} - \frac{\gamma_{\text{He}}}{\gamma_{\text{Xe}}} \cdot \Phi_{\text{Xe}} \stackrel{!}{=} \text{const.}$$



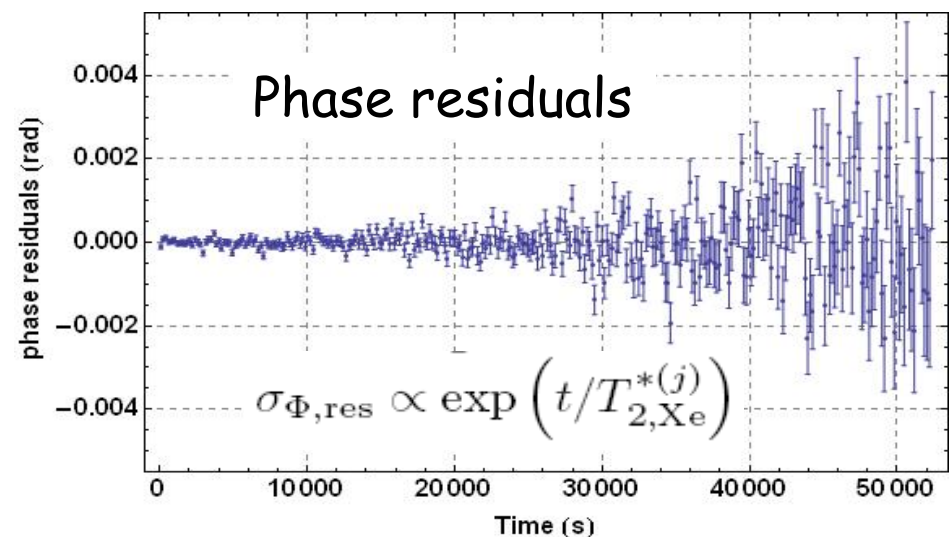
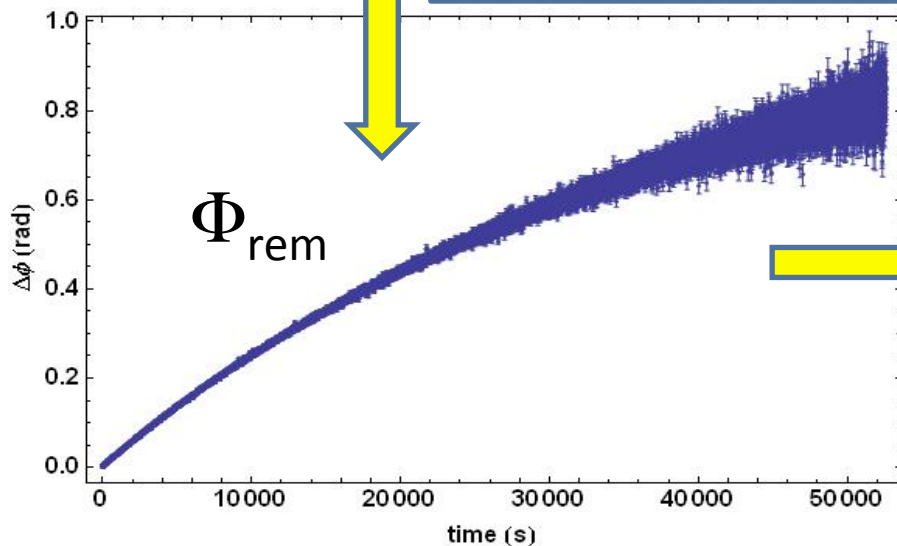
# Subtraction of deterministic phase shifts



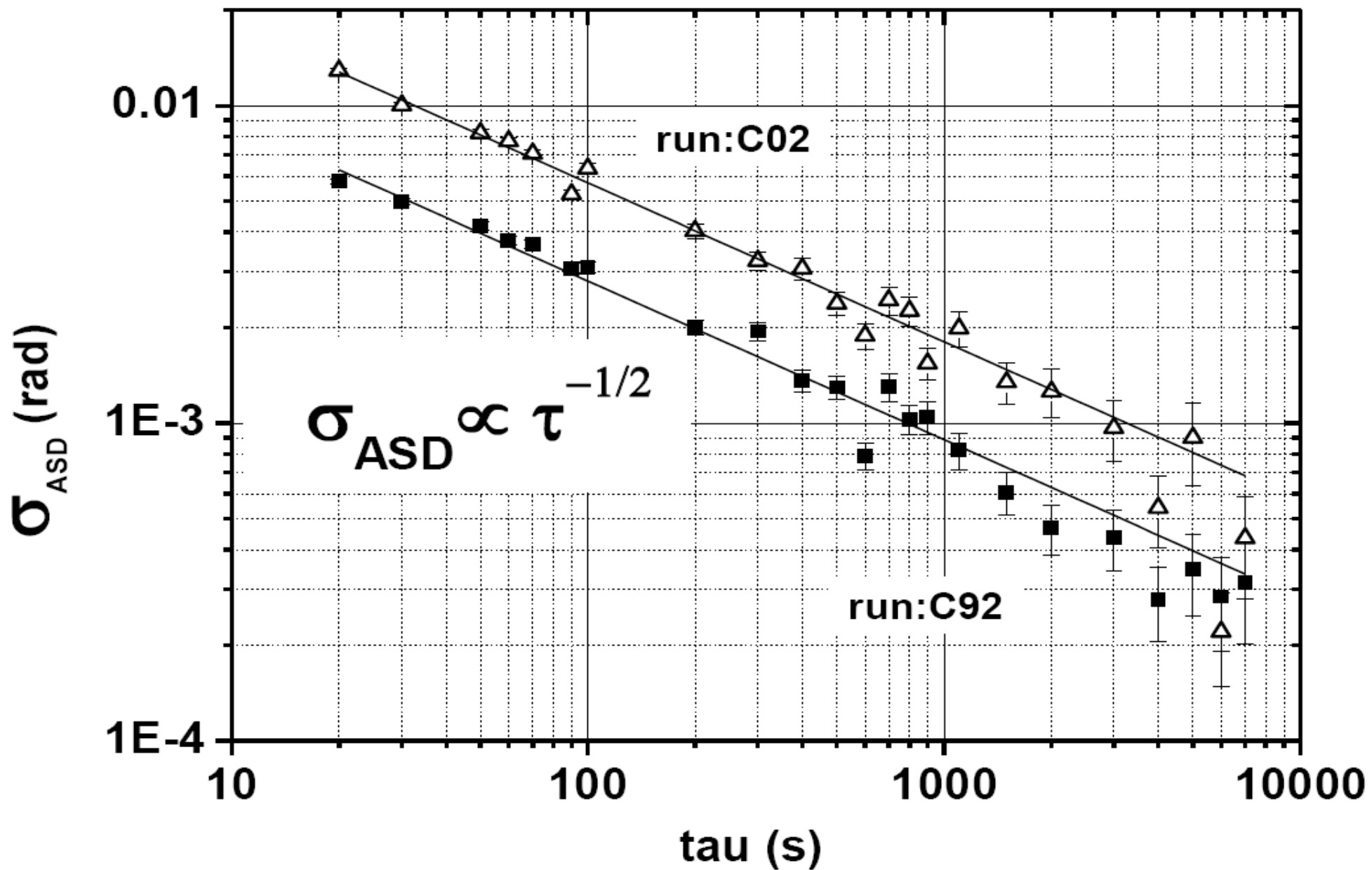
I. Earth



II.  $Fit = c + a_{lin} \cdot t + a_{He} \cdot e^{-t/T_{2,He}^*} + a_{Xe} \cdot e^{-t/T_{2,Xe}^*} + \Phi(t)_{spin-coupling}$



# ASD of phase residuals



The detection of the free precession of co-located  $^3\text{He}/^{129}\text{Xe}$  sample spins can be used as ultra-sensitive probe for

non-magnetic spin interactions of type:

$$V_{non-magn.} = \vec{a} \cdot \vec{\sigma} \equiv -\vec{\mu}_{PM} \cdot \vec{B}_{PM}$$

- Search for a Lorentz violating sidereal modulation of the Larmor frequency

$$V(r)/\hbar = \langle \tilde{\mathbf{b}} \rangle \hat{\varepsilon} \cdot \vec{\sigma} / \hbar$$

- Search for spin-dependent short-range interactions

$$V(r)/\hbar = c \vec{\sigma} \cdot \hat{n} / \hbar$$

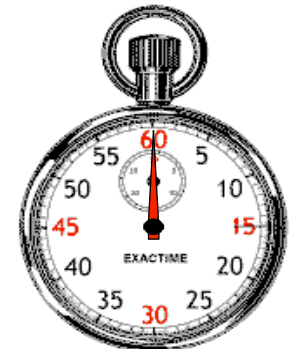
- Search for EDM of Xenon

$$V(r)/\hbar = -|d_n| \vec{\sigma} \cdot \vec{E} / \hbar$$

- ...

Observable:

$$\Delta\omega = \omega_{L,He} - \frac{\gamma_{He}}{\gamma_{Xe}} \cdot \omega_{L,Xe} \neq 0$$



# Search for a Lorentz violating sidereal modulation



preferred direction in space-time

# A closer look...



**General relativity** is a classical theory, i.e., non-quantum



**Standard Model (SM)** of particle physics

SM: relativistic quantum field theory

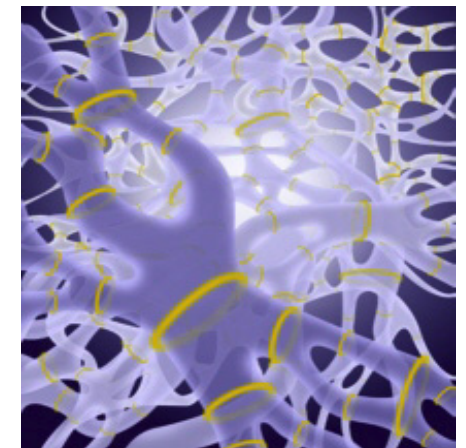
Courtesy of C. Lämmerzahl

## Unification theories:

string theory, loop quantum gravity,...

Planck scale: energy scale where gravity meets quantum physics

$$M_p \sim 10^{19} \text{ GeV}$$

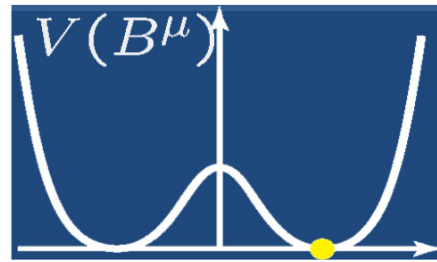


**Fundamental Theory:  
Lorentz & CPT invariant**

**String theory  
M theory**

~ Planck scale  
 $10^{19}$  GeV

Spontaneous Lorentz symmetry  
breaking in string theory  
e.g. Lorentz vector field makes  
non zero vacuum expectation  
value



$$\langle B^\mu \rangle \neq 0$$



Background fields (tensor fields) give preferred direction  
e.g. rest frame of CMB  
→ *talk of Ralf Lehnert*

low-energy  
world

**Effective theory:  
„low-energy“  
Lorentz & CPT violating**

**Standard-Model  
extension (SME)**



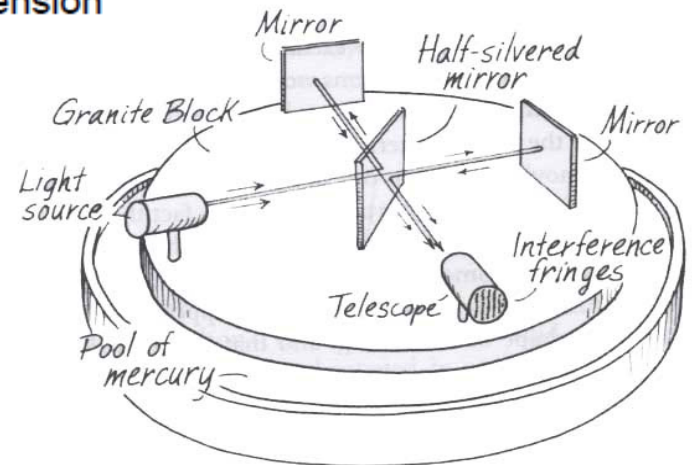
# Traditional tests of Lorentz symmetry & special relativity

photon sector:  $\mathcal{L} = -\underbrace{\frac{1}{4}F^{\mu\nu}F_{\mu\nu}}_{\text{Standard Lagrangian}} - \underbrace{\frac{1}{4}(k_F)_{\kappa\lambda\mu\nu}F^{\kappa\lambda}F^{\mu\nu}}_{\text{Lorentz Invariance violating Extension}} \quad (k_F)_{\kappa\lambda\mu\nu}: 19 \text{ independent parameters}$

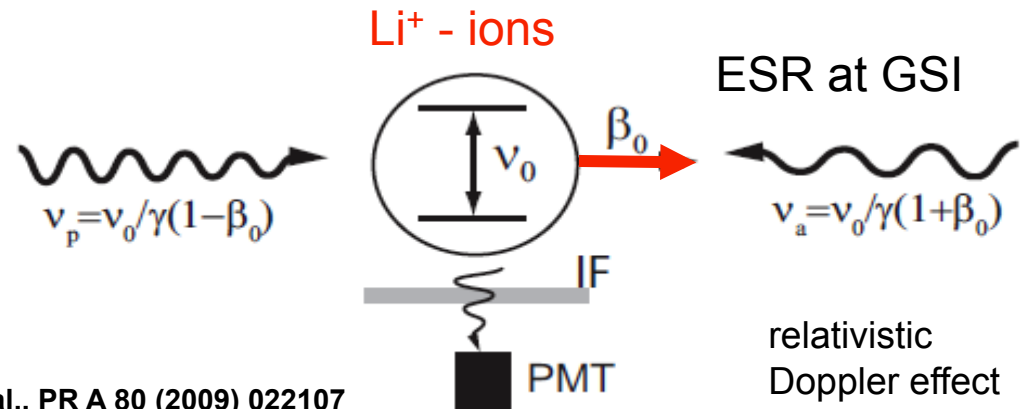
- **Michelson-Morley**  
isotropy of speed of light  $c(\theta) = c$

- **Kennedy-Thorndike**  
boost-independence of speed of light  $c(v) = c$

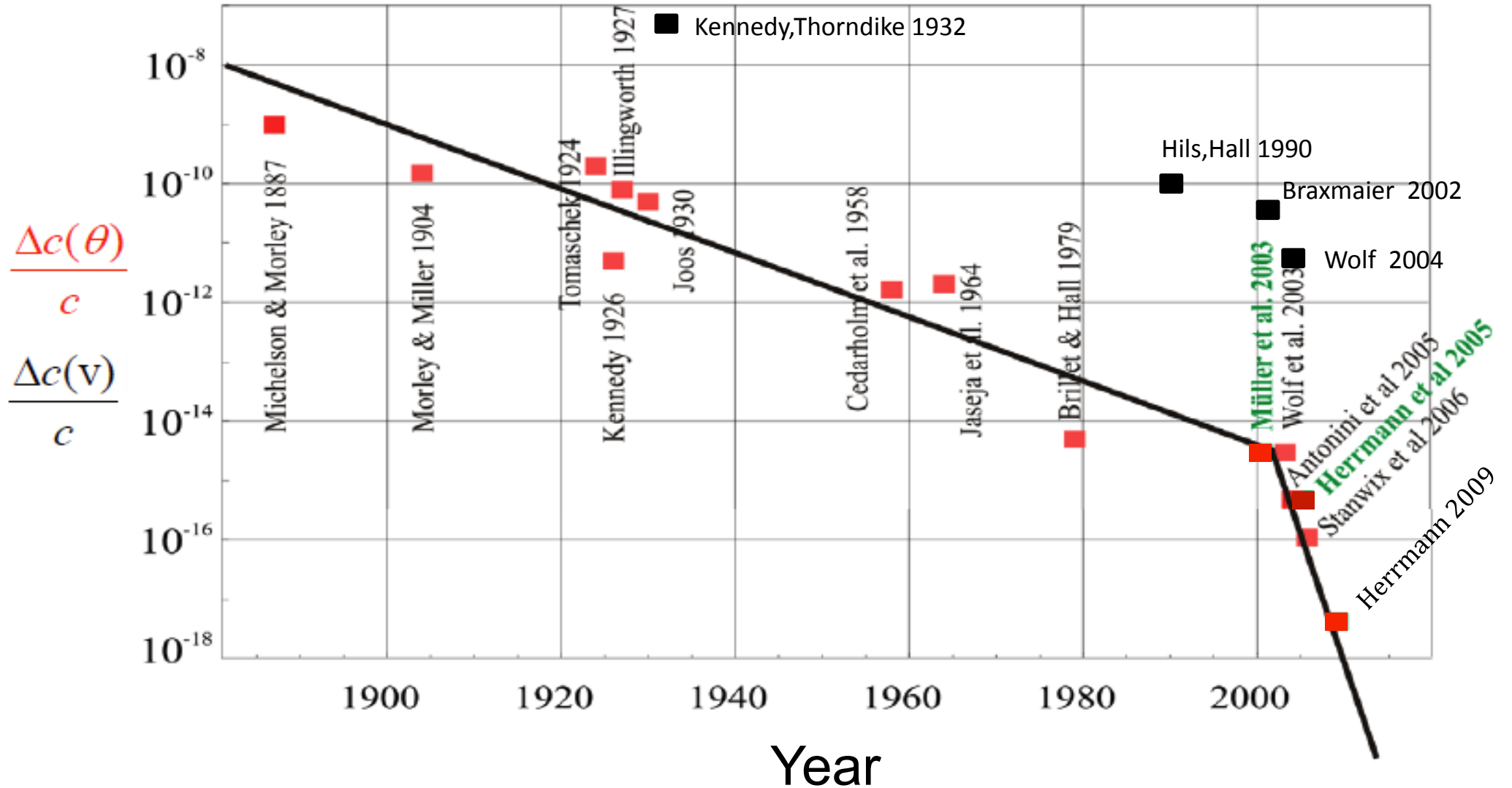
- **Ives-Stillwell**  
special-relativistic time dilation  $\frac{v_p \cdot v_a}{v_0^2} = 1 + \varepsilon(\beta^2)$



Michelson (1881, Potsdam)  
Michelson & Morley (1887, Cleveland)



# Test of constancy of c



# Modern Tests of Lorentz violation

## Topics:

- searches for CPT and Lorentz violations involving

- birefringence and dispersion from cosmological sources
- clock-comparison measurements
- CMB polarization
- collider experiments
- electromagnetic resonant cavities
- equivalence principle
- gauge and Higgs particles
- high-energy astrophysical observations
- laboratory and gravimetric tests of gravity
- matter interferometry
- neutrino oscillations
- oscillations and decays of K, B, D mesons
- particle-antiparticle comparisons
- space-based missions
- spectroscopy of hydrogen and antihydrogen
- spin-polarized matter

*Fifth Meeting on*  
**CPT AND LORENTZ SYMMETRY**  
*June 28-July 2, 2010*

**Indiana University, Bloomington**

- \* Theoretical studies of CPT and Lorentz violation involving

- physical effects at the level of the SM, General Relativity, and beyond
- origins and mechanisms for violations classical and quantum issues in field theory, particle physics, gravity, and strings

# Standard-Model Extension

## - matter sector -

A. Kostelecky and C. Lane: *Phys. Rev. D* **60**, 116010 (1999)

Modified Dirac equation for a free spin 1/2 particle (w=e,p,n)

$$\left( \underbrace{i\gamma^\mu \partial_\mu - m_w}_{\text{standard DE}} - \underbrace{a_\mu^w \gamma^\mu - b_\mu^w \gamma_5 \gamma^\mu}_{\text{CPT violating}} + i e_v^w \partial^v - f_v^w \gamma_5 \partial^v + i \frac{1}{2} g_{\lambda\mu\nu}^w \sigma^{\lambda\mu} \partial^\nu - \frac{1}{2} H_{\mu\nu}^w \sigma^{\mu\nu} + i c_{\mu\nu}^w \gamma^\mu \partial^\nu + i d_{\mu\nu}^w \gamma_5 \gamma^\mu \partial^\nu \right) \Psi = 0$$

CPT preserving terms

Lorentz violating terms

### Experimental access:

$$a_\mu^w, b_\mu^w, \dots \approx \eta_w \cdot \left( \frac{m_w}{M_{Planck}} \right) \cdot m_w$$

coupling strength

**Cs- fountain** Wolf et al., PRL **96**, 060801 (2006)

**Torsion pendulum** B.Heckel et al. PRD 78 (2008) 092006

**Antihydrogen spectroscopy**

**Astrophysics**

**Hg/Cs comparison**

**UCN/Hg comparison**

**He/Xe maser**

**K/He co-magnetometer**

clock  
comparison  
experiments

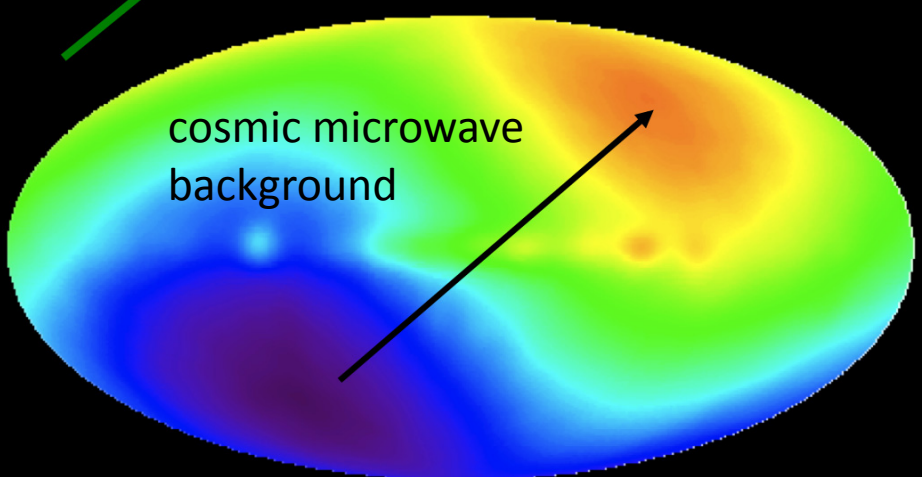
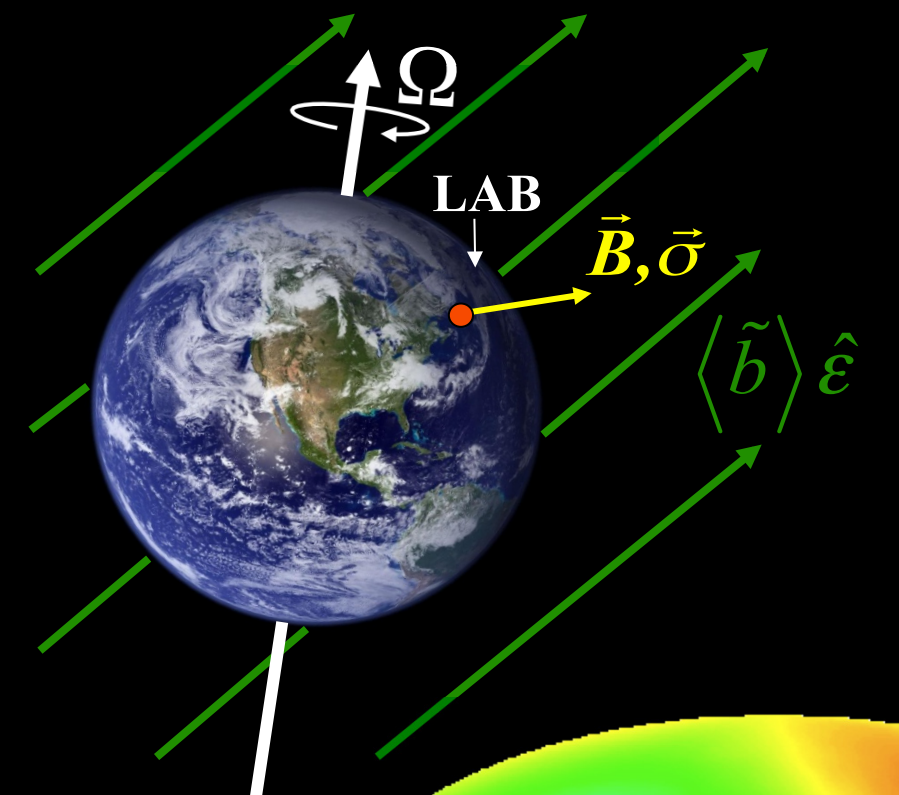
$$b_\mu^n$$



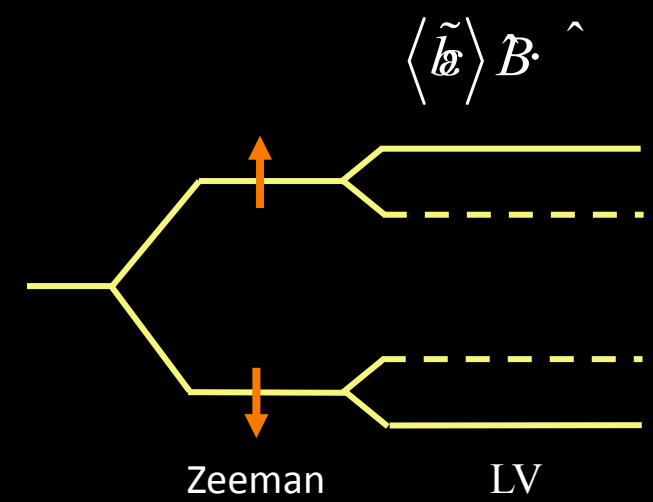
Coupling of spin  $\vec{\sigma}$  to background field:  $V = -\vec{b} \cdot \vec{\sigma}$

$$H = -\vec{\mu} \cdot \vec{B} - \vec{b} \cdot \vec{\sigma}$$

$$\rightarrow \nu = \underbrace{\frac{2}{h} \mu B}_{\nu_{\text{Zeeman}}} + \underbrace{\frac{2}{h} \langle \vec{b} \rangle \cos(\hat{\epsilon}, \hat{B})}_{\nu_{LV}}$$



$v = 368 \text{ km/s}$   
 $\Delta T_{\text{dip}} \approx 3.3 \text{ mK}$

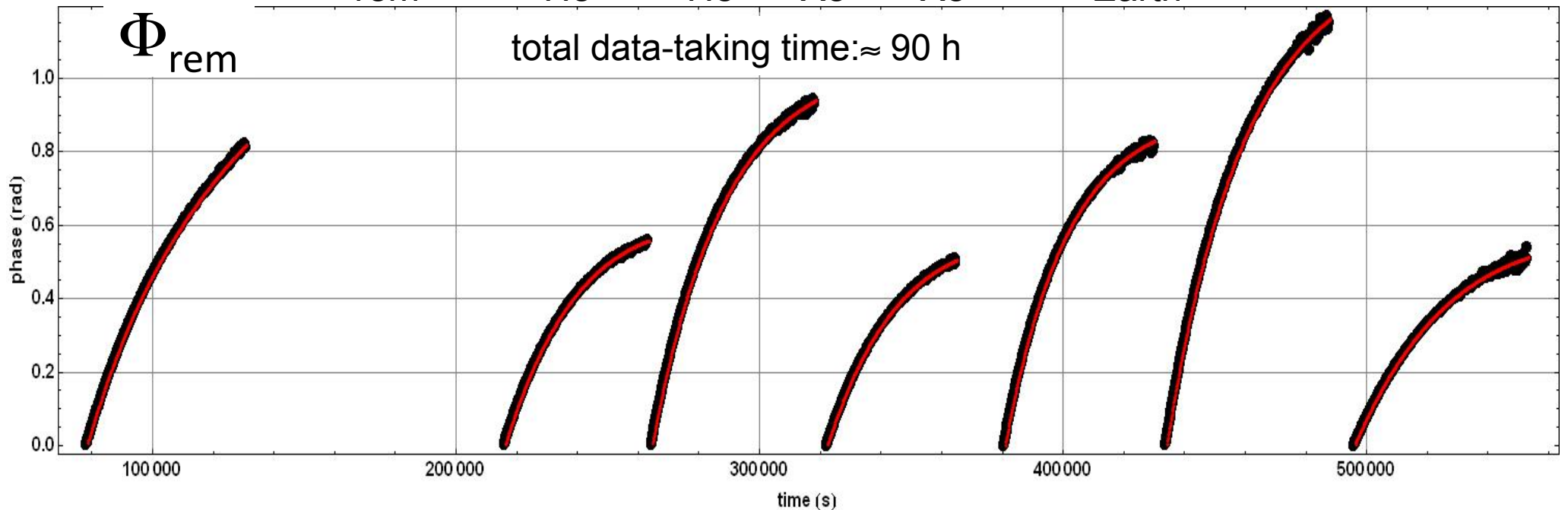


$$\sim a_s \cdot \sin(\Omega_s \cdot t) - a_c \cdot \cos(\Omega_s \cdot t)$$

# Search for a sidereal modulation of the weighted phase difference

March 2009 run:

$$\Phi_{\text{rem}} = \Phi_{\text{He}} - \gamma_{\text{He}} / \gamma_{\text{Xe}} \cdot \Phi_{\text{Xe}} - \Phi_{\text{Earth}}$$



$$Fit = \sum_{n=1}^7 \left\{ c_n + a_{lin,n} \cdot t + a_{He,n} \cdot e^{-t/T_{2,He,n}} + a_{Xe,n} \cdot e^{-t/T_{2,Xe,n}} \right\} + a_s \cdot \sin(\Omega_s \cdot t) - a_c \cdot \cos(\Omega_s \cdot t)$$

expect strong correlated error for

$$T_{SD} > T_2^*$$

$$\Omega_s = 2\pi/T_{SD} = 2\pi/(23^h:56^m:4.091^s).$$

Results of  $\chi^2$ -fit for the sidereal phase amplitudes  $a_c$  and  $a_s$  together with their correlated and uncorrelated  $1\sigma$ -errors .

To demonstrate the strong dependence of the correlated error on  $\Omega_s$ , corresponding fit results are shown for multiples of  $\Omega_s$ :  $\Omega'_s = g \cdot \Omega_s$  .

	$a_c$ mrad	$\sigma_{ac}^{corr}$	$\sigma_{ac}^{uncorr}$	$a_s$ mrad	$\sigma_{as}^{corr}$	$\sigma_{as}^{uncorr}$
$\Omega_s = 2\pi / T_{SD}$	-0.882	0.814	0.015	-2.067	1.057	0.019

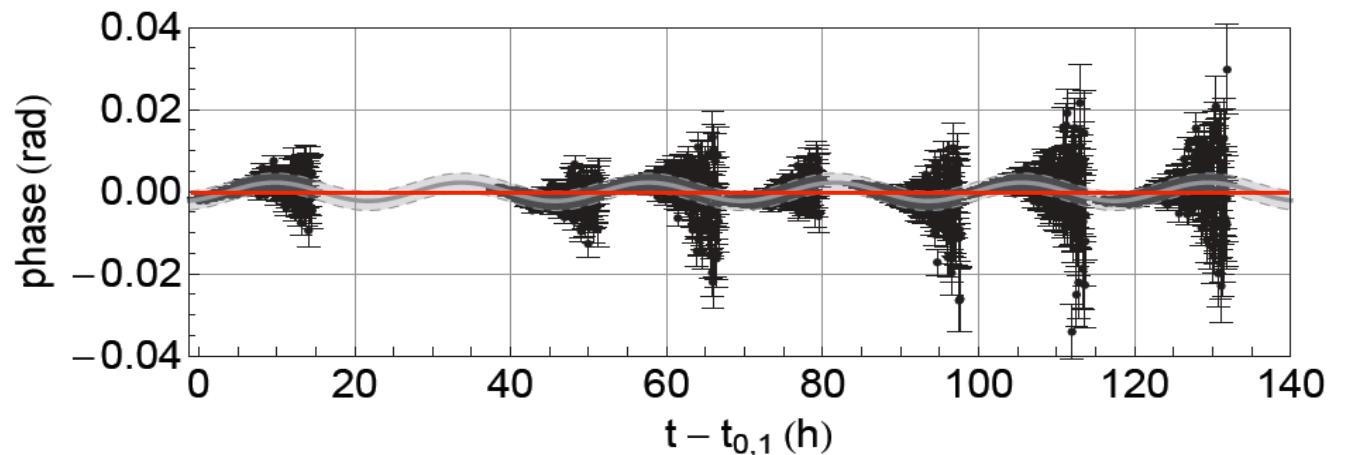
$2 \cdot \Omega_s$	-0.048	0.120	0.016	-0.149	0.112	0.017
$3 \cdot \Omega_s$	-0.184	0.052	0.019	-0.011	0.043	0.016
$4 \cdot \Omega_s$	-0.001	0.034	0.018	0.057	0.030	0.016

**Phaseamplitude of the sidereal modulation:**

$$a_{\max} = \sqrt{a_s^2 + a_c^2} = (2.25 \pm 2.29) \text{ mrad (95\% CL)}$$

Phase residuals with fit-results for

$$a_s \cdot \sin(\Omega_s \cdot t) - a_c \cdot \cos(\Omega_s \cdot t)$$



In terms of frequency:

$$v_{\perp} = a_{\max} \cdot \frac{\Omega_s}{2\pi} = (26.1 \pm 26.6) \text{ nHz} \quad (95\% \text{ C.L.})$$

Kostelecky et al. , Phys. Rev. D 60, 116010 (1999)

free neutron:

$$n : \mu = -1.913 \mu_K$$

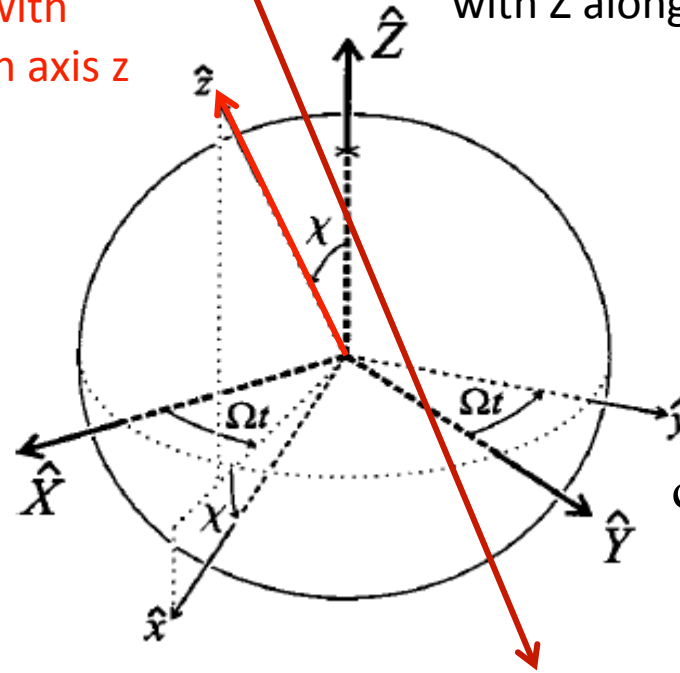
Schmidt-Model

$${}^3\text{He} : \mu = -2.1276 \mu_K$$

$${}^{129}\text{Xe} : \mu = -0.7779 \mu_K$$

Lab-frame with  
quantization axis z

(X,Y,Z) non-rotating frame  
with Z along Earth's rotation axis



PTB Berlin:

$$\Theta = 52,5164^\circ \text{ north}$$

$$\rho = 28^\circ \text{ (north-south)}$$

$$\cos \chi = \cos \theta \cdot \cos \rho = 0.543$$

$$\sin \chi \cdot \left| -3.5 \cdot \tilde{b}_{\perp}^n + 0.012 \cdot \tilde{d}_{\perp}^n + 0.012 \cdot \tilde{g}_{D,\perp}^n \right| \leq 2\pi \cdot \delta v_{\perp} \cdot \hbar$$

$$\tilde{b}_{\perp}^n = \leq 3.72 \cdot 10^{-32} \text{ GeV} \quad (95\% \text{ C.L.})$$



# Tightest constrains on SME parameters on neutron sector:

V. Alan Kostelecký<sup>a</sup> and Neil Russell<sup>b</sup> [arXiv:0801.0287]

Coefficient	Proton	Neutron	Electron
$\tilde{b}_X$ [GeV]	$< 10^{-31}$	$< 10^{-32}$	$< 10^{-31}$
$\tilde{b}_Y$ [GeV]	$< 10^{-31}$	$< 10^{-32}$	$< 10^{-31}$
$ \tilde{b}_\perp $ [GeV]	$< 10^{-31}$	$< 10^{-32}$	$\tilde{b}^n \approx \left(\frac{m_n}{M_P}\right)^k \cdot m_n \quad k=1 \text{ excluded}$ $\Rightarrow \text{exp. upgrade: } k=2!$

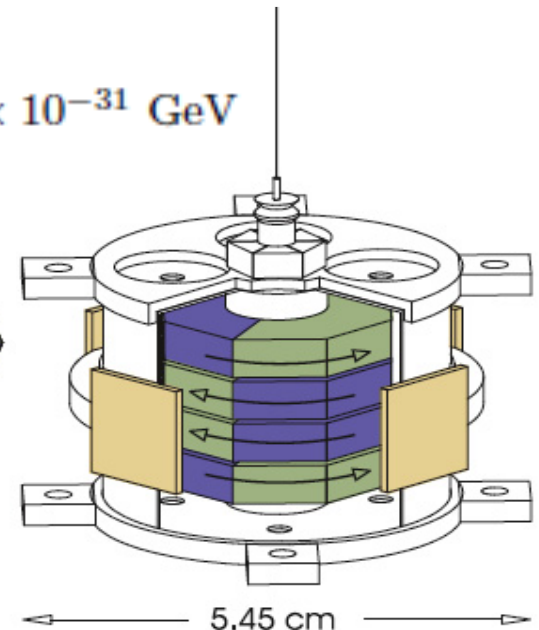
## our result:

$$\tilde{b}_\perp^n = \leq 3.72 \cdot 10^{-32} \text{ GeV (95\% C.L.)}$$

## • Torsion pendulum

B.R.Heckel et al., PRD 78 (2008) 092006

$$\tilde{b}_X^e = (-0.9 \pm 1.4) \times 10^{-31} \text{ GeV}$$



## • K-<sup>3</sup>He co-magnetometer

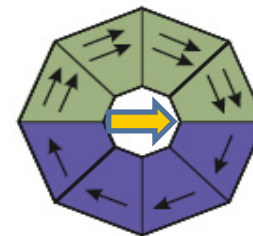
$$\tilde{b}_\perp^n < 3.7 \cdot 10^{-33} \text{ GeV (68\% C.L.)}$$

J. M. Brown et al. Phys. Rev. Lett., 105, 151604 (2010).

## • Spin maser experiments with <sup>3</sup>He and <sup>129</sup>Xe

(D.Bear et al., PRL 85 (2000) 5038)

$$\tilde{b}_\perp^n \equiv \sqrt{(\tilde{b}_X^n)^2 + (\tilde{b}_Y^n)^2} = (4.0 \pm 3.3) \times 10^{-31} \text{ GeV}$$



(95% C.L.)

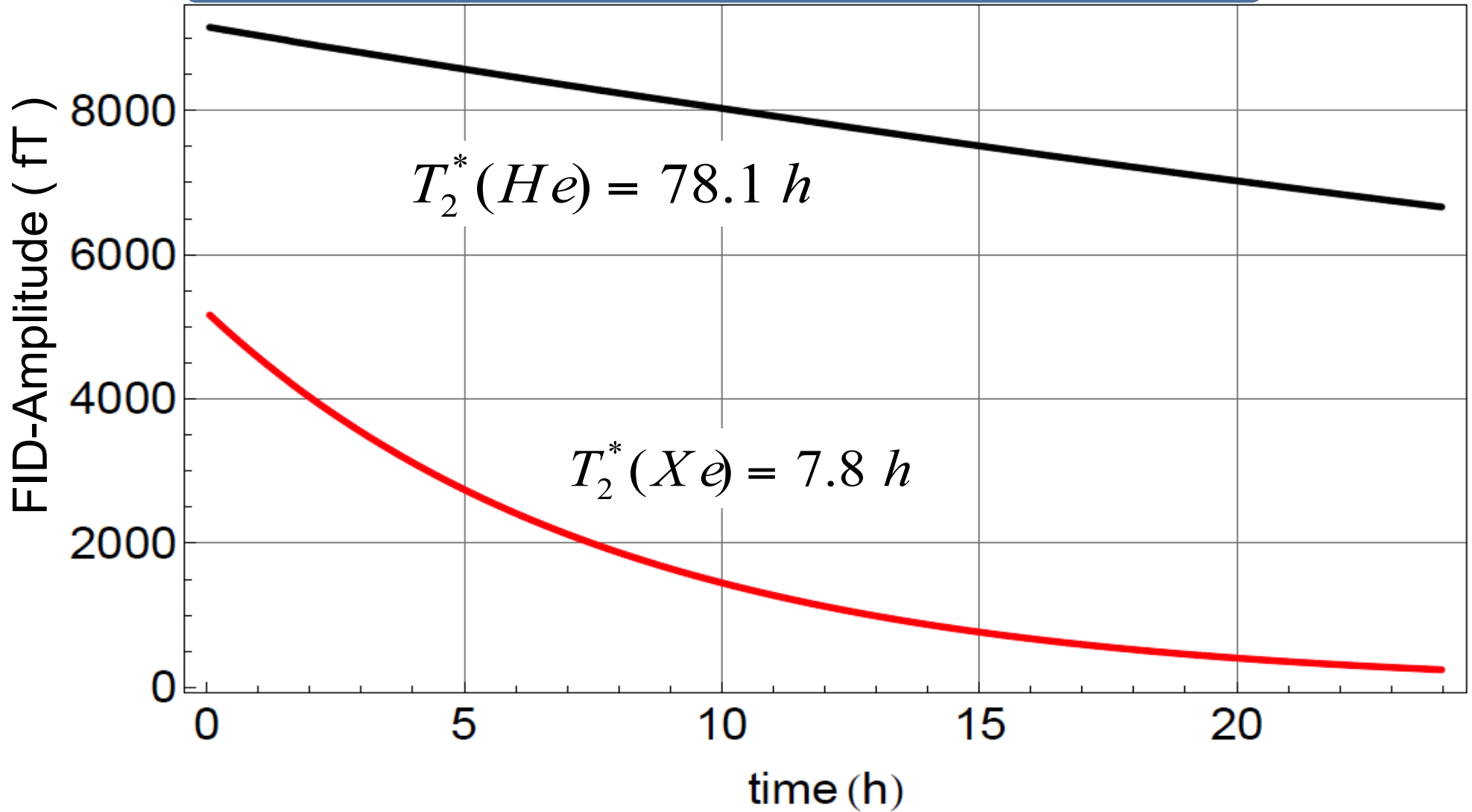
# March 2012 run at PTB

- (1) conventional runs with B-field fixed
- (2) active rotation of B-field (2 h / turn)

# $T_2^*$ - improvements:

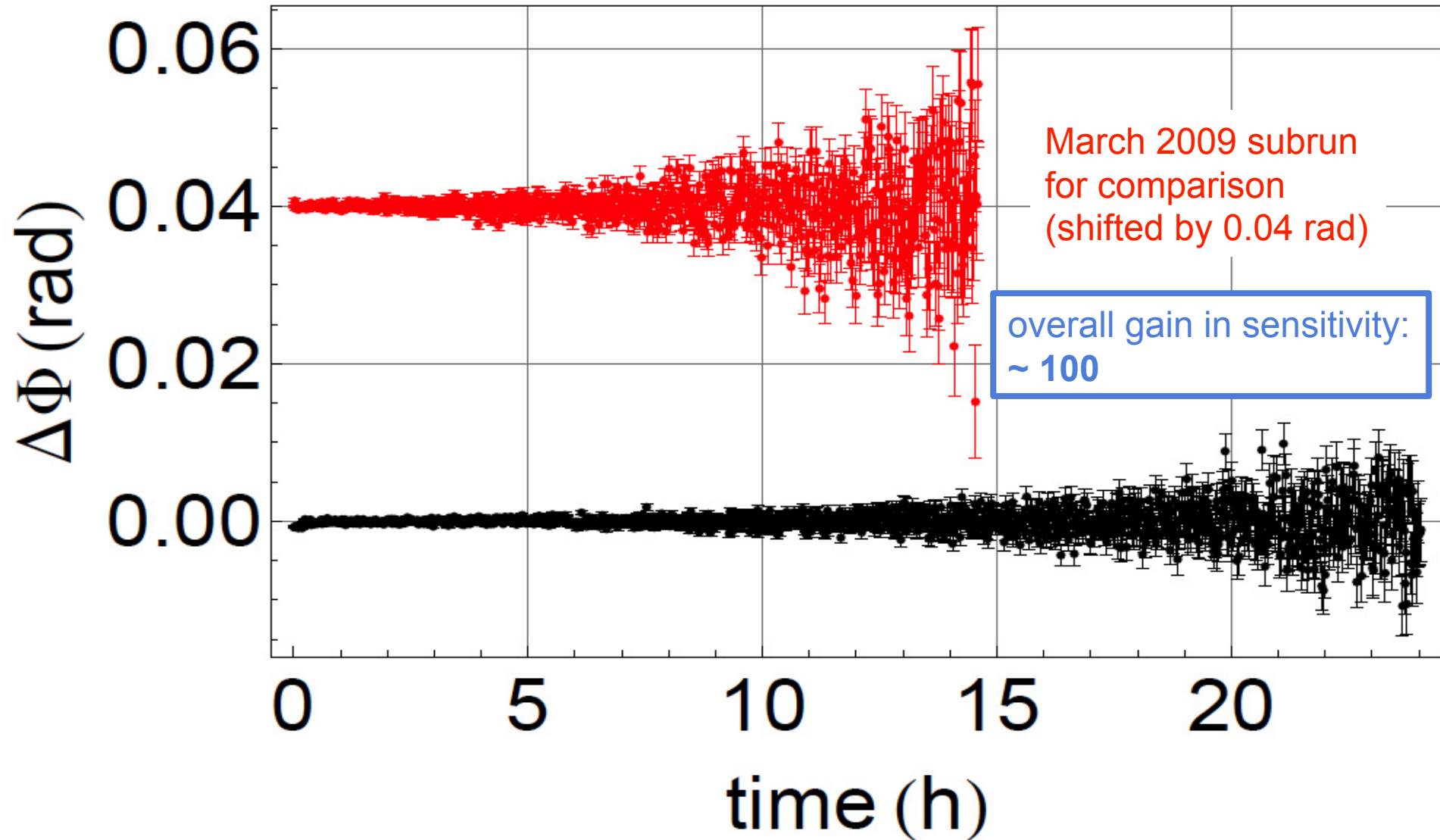
pure  $^3\text{He}$  @  $p=2.5$  mbar :  $T_2^*(\text{He})=124$  h

Gas mixture:  $p_{\text{He}}=2.7$  mbar,  $p_{\text{Xe}}=4.9$  mbar,  $p_{\text{N}_2}=24.8$  mbar



## Phase residuals:

- total data taking time: 165 h (90 h March 2009 ) ~1.8
- gain in SNR: **2-3**
- gain due to CRLB power law ( $\sim 1/T^{3/2}$ ) : **2.8**
- reduction of correlated error: **~ 7**



## (2) rotation of B-field (quantization axis)

5 subruns (~ 14 h each)

Sequence:

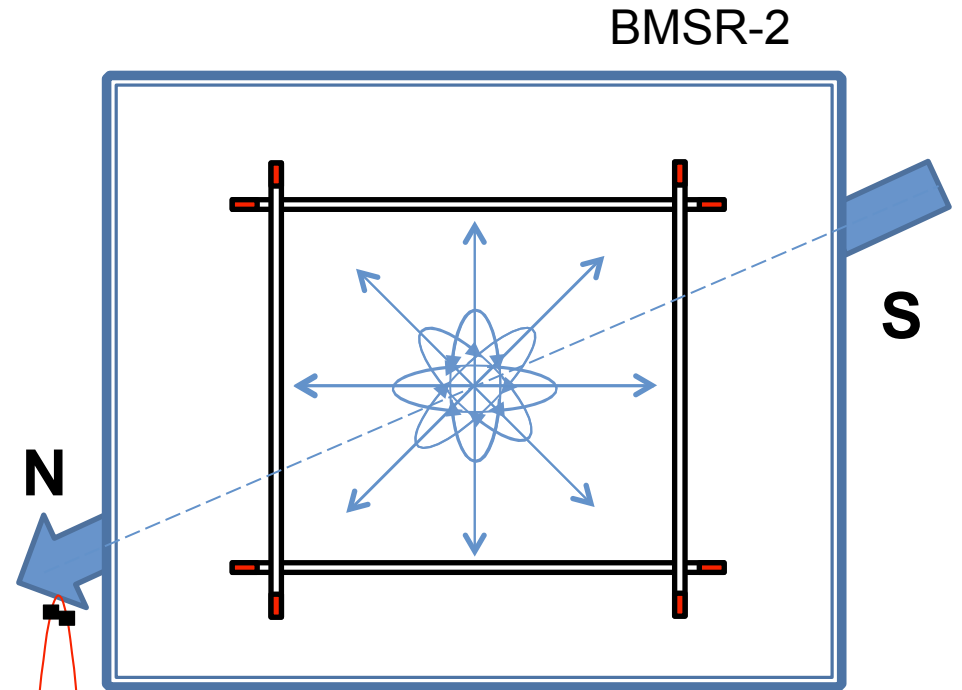
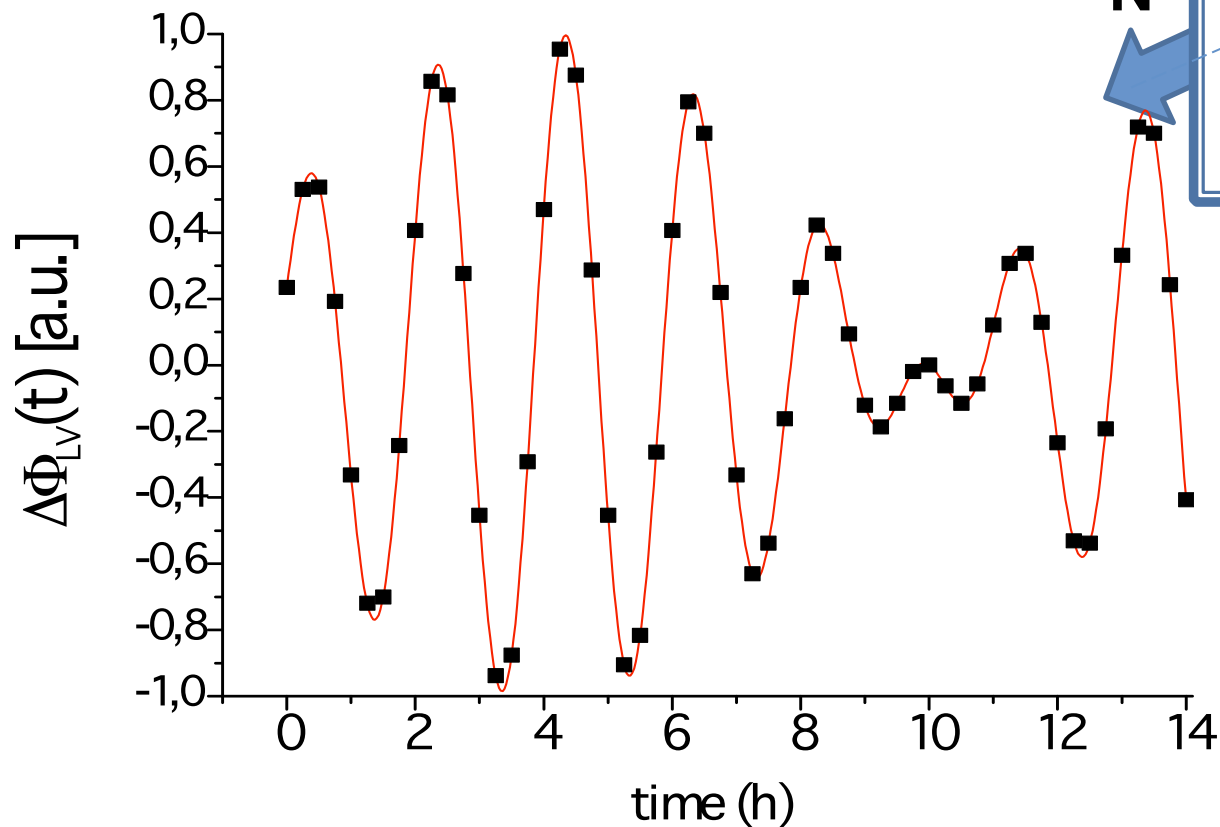
...

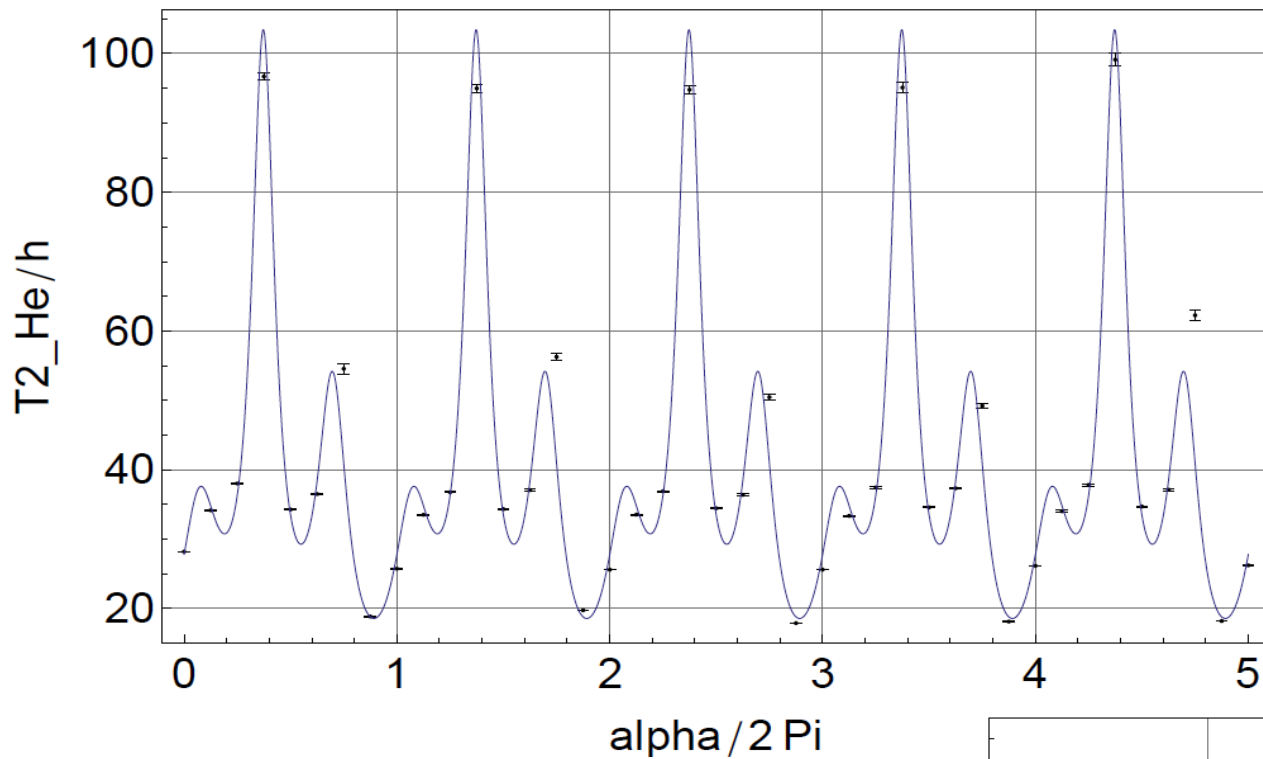
field rotation ( $45^\circ$ ) : 2.5 min

measurement (static): 12.5 min

...

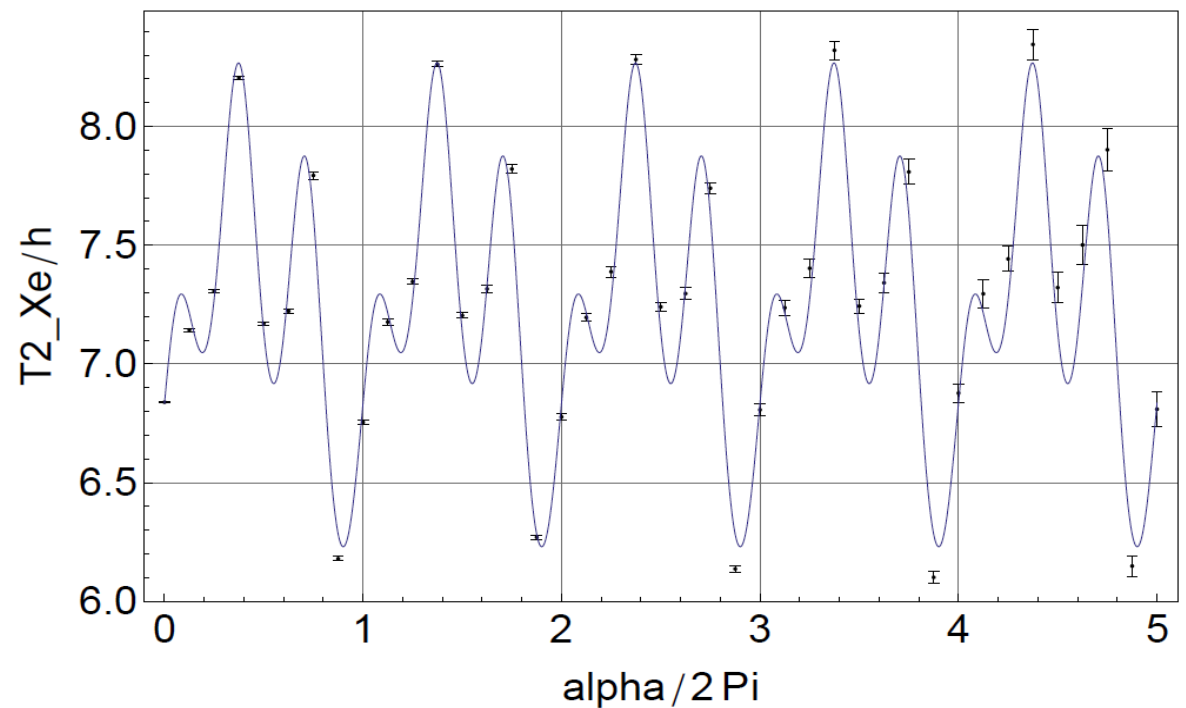
expected LV-signal:  $\sim \sin(\Omega_s \cdot t + \Phi) \cdot \sin \chi(t)$





Change of the absolute field gradient during rotation and its effect on  $T_2^*$

$$\frac{1}{T_2^*} \propto |\nabla B|^2$$



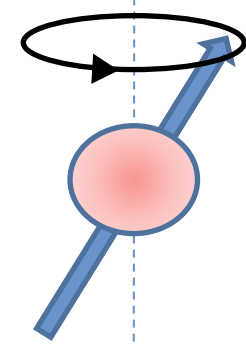
data analysis ongoing

# Conclusion and Outlook

- $^3\text{He}$ ,  $^{129}\text{Xe}$  spin clock based on free spin precession  
→ long spin coherence times

$$T_{2,He}^* \approx 60 \text{ hours} \quad ( T_{2,He}^* = 124 \text{ h, March 2012 run } )$$

$$T_{2,Xe}^* = 3 - 4 \text{ hours} \quad ( T_2^*(Xe) \approx 8 \text{ h @ } T_{1,wall} \sim 11 \text{ h } )$$



Eur. Phys. J. D 57, 303–320 (2010)

- Search for neutron spin coupling to a Lorentz and CPT-violating background field

$$V(r)/\hbar = \langle \tilde{\mathbf{b}} \rangle \hat{\mathbf{e}} \cdot \vec{\sigma} / \hbar$$

K- $^3\text{He}$  and  $^3\text{He}/^{129}\text{Xe}$  co-magnetometer set the tightest limits on SME-parameters

- K- $^3\text{He}$  co-magnetometer :  $\tilde{b}_{\perp}^n < 3.7 \cdot 10^{-33} \text{ GeV (68\% C.L.)}$  PRL 105, 151604 (2010)
- $^3\text{He}$ - $^{129}\text{Xe}$  co-magnetometer :  $\tilde{b}_{\perp}^n \leq 3.72 \cdot 10^{-32} \text{ GeV (95\% C.L.)}$  PRD 82, 111901 (2010)

March 2012 run: expected gain in sensitivity  $\sim 100$  to trace LV interactions

● Short range spin-dependent interaction:

$$V(r) = \frac{g_S g_P}{8\pi} \frac{(\hbar)^2}{m_n} (\sigma_n \cdot \vec{n}) \left[ \frac{1}{r\lambda} + \frac{1}{r^2} \right] e^{-r/\lambda}$$

J.E.Moody, F.Wilczek  
PRD 30 (1984) 130

September 2010 run

●  $^{129}\text{Xe}$  electric dipole moment (Groningen-Heidelberg-Mainz collaboration):

**Proposal:**  $|d_{Xe}| < 10^{-31} \text{ ecm}$

$$|d_{Xe}| = (0.7 \pm 3.3 \pm 0.1) \times 10^{-27} \text{ ecm}$$

Rosenberry and Chupp, PRL 86,22 (2001)

present sensitivity of  $^3\text{He}/^{129}\text{Xe}$ -comagnetometer:  $< 0.1 \text{ nHz per day}$

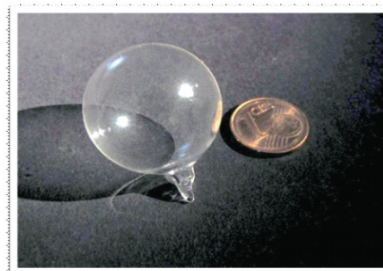
➤ **Magnetometry ( $^3\text{He}$ )**

low field :  $\approx 1\mu \text{ Tesla}$

$\langle \delta B \rangle \approx 1 \text{ f T @ } 200 \text{ s} \longrightarrow$

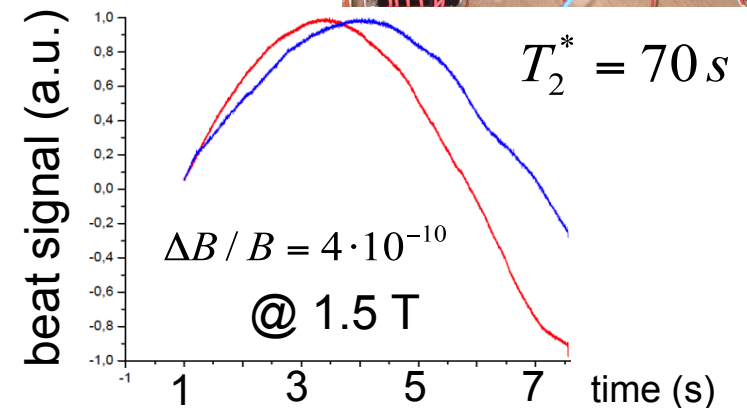
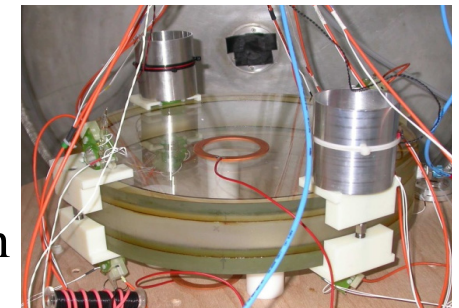
high field :  $> 1 \text{ Tesla}$

ultra-high sensitive magnetometer to monitor relative field changes of  $\approx 10^{-12}$



magnetometer for nEDM experiment at PSI

$T_2^* > 30 \text{ min}$





# $^3\text{He}/^{129}\text{Xe}$ clock comparison

## probing fundamental symmetries



### Institut für Physik, Universität Mainz:

C. Gemmel, W. Heil, H. Hofsetz, S. Karpuk, Y. Sobolev,  
K. Tullney

### Physikalisch-Technische Bundesanstalt, Berlin:

M. Burghoff, W. Kilian, S. Knappe-Grüneberg,  
W. Müller, A. Schnabel, F. Seifert, L. Trahms

### Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg:

F. Allendinger, U. Schmidt

Thank you for your attention



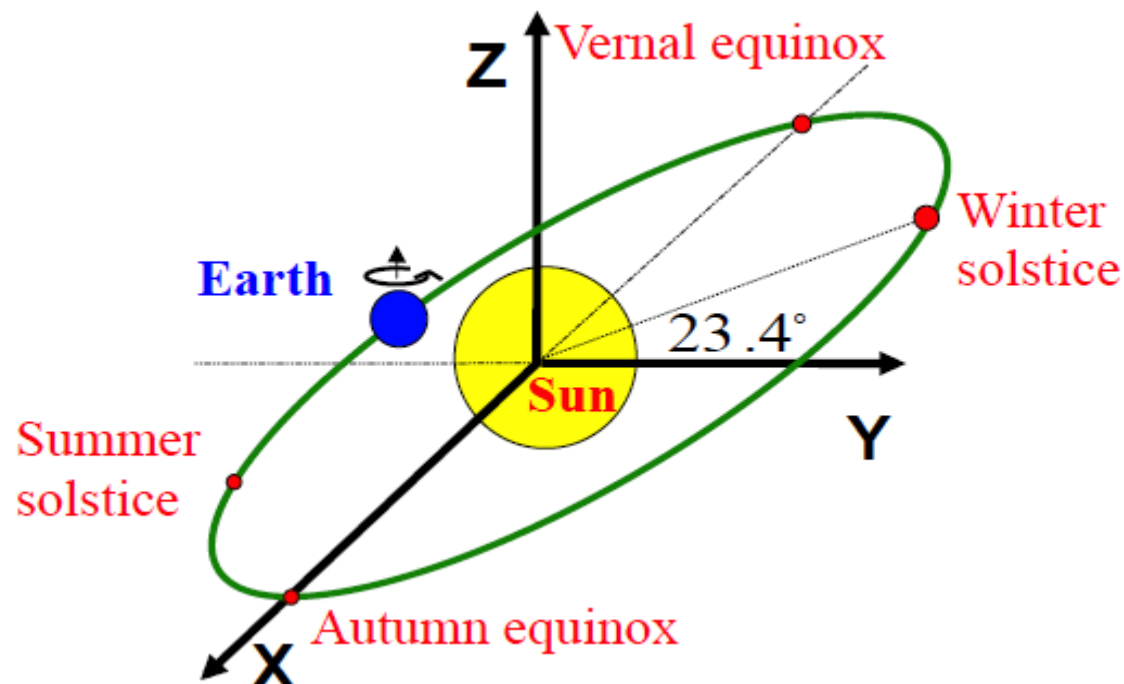
# Standard Model Extension (SME)

## How to detect Lorentz violation?

Lorentz violation is realized as a coupling of particle fields and the background fields, so the basic strategy is to find the Lorentz violation is;

- (1) choose the coordinate system to compare the experimental result
- (2) write down Lagrangian including Lorentz violating terms under the formalism
- (3) write down the observables using this Lagrangian

The standard choice of the coordinate is **Sun-centred coordinates**



# Search for a new pseudoscalar boson (Axion-like particle)

[Gerardus 't Hooft](#),: QCD has a non-trivial vacuum structure that in principle permits CP-violation

$$L_{\bar{\theta}} = \frac{\alpha_s \bar{\theta}}{8\pi} \vec{G}_{\mu\nu} \cdot \vec{G}^{\mu\nu} \quad \text{from neutron EDM we get:} \quad d_n \approx 10^{-16} \cdot \bar{\theta} < 3 \cdot 10^{-26} \text{ e} \cdot \text{cm}$$

**Original proposal for Axion** ( R. Peccei, H.Quinn PRL 38(1977),1440)

as possible solution to the „Strong CP Problem“ that cancels the CP violating term in the QCD Lagrangian

$$L_a = \xi \frac{\alpha_s}{8\pi f_a} a(x) \vec{G}_{\mu\nu} \cdot \vec{G}^{\mu\nu}$$

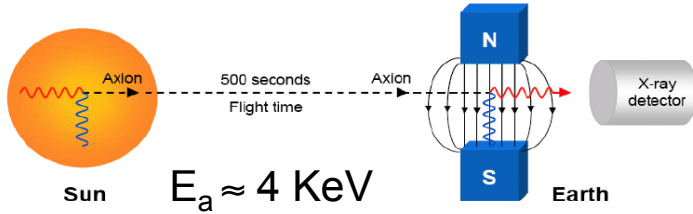
$$\langle \alpha \rangle = -f_a \frac{\bar{\theta}}{\xi}$$

**Modern interest:** Dark Matter candidate. All couplings to matter are weak

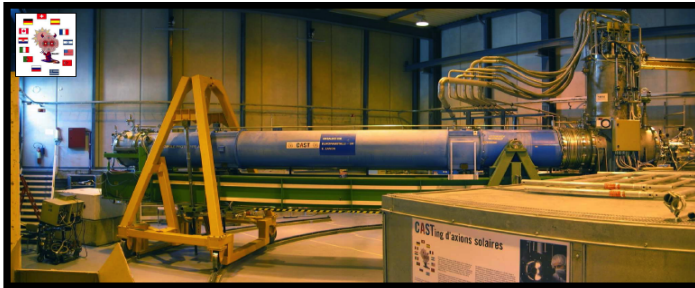
**Axions**, if they exist, will be very light and will mediate a macroscopic CP- ~~force~~

$$m_a \approx \frac{m_\pi \cdot f_\pi}{f_a} \approx 6\mu\text{eV} \cdot \left( \frac{10^{12} \text{ GeV}}{f_a} \right) \quad f_a : \text{ energy scale P.Q.-symmetry is spontaneously broken}$$

## Axions generated in the sun



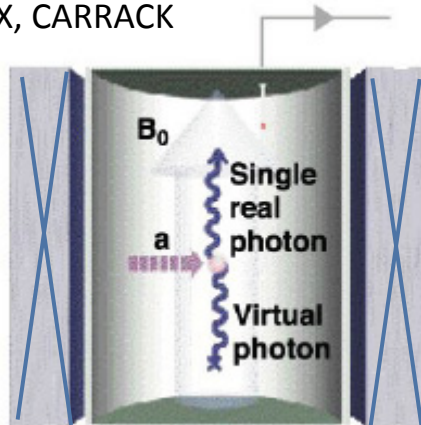
CAST : CERN AXION SOLAR TELESCOPE



## Galactic axions

Tunable resonant cavity in magnetic field coupled to a ultra low noise microwave receiver

ADMX, CARRACK



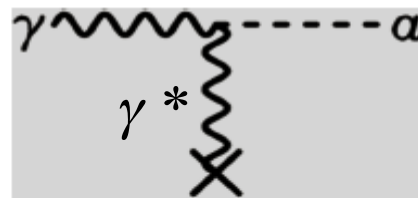
8 Tesla

1GHz:  $4 \mu\text{eV}$

## AXION SEARCHES using the Primakoff Effect

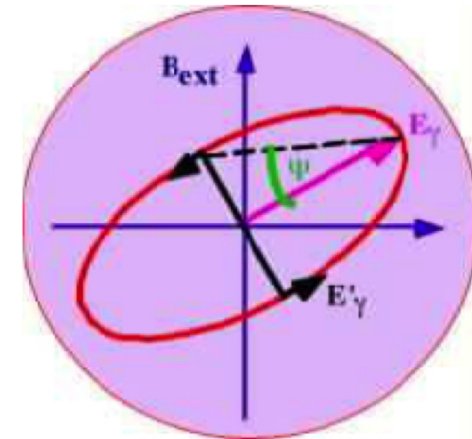
### Primakoff Effect

Axion conversion into photon (or the inverse)



## Laboratory axions

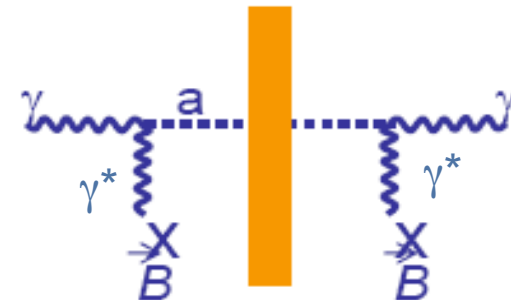
Polarised laser through vacuum in a strong magnetic field (PVLAS)



“Light shines through the wall”

Photonregeneration

(BFRT, OSQAR, ALPS, LIPPS, GammeV)

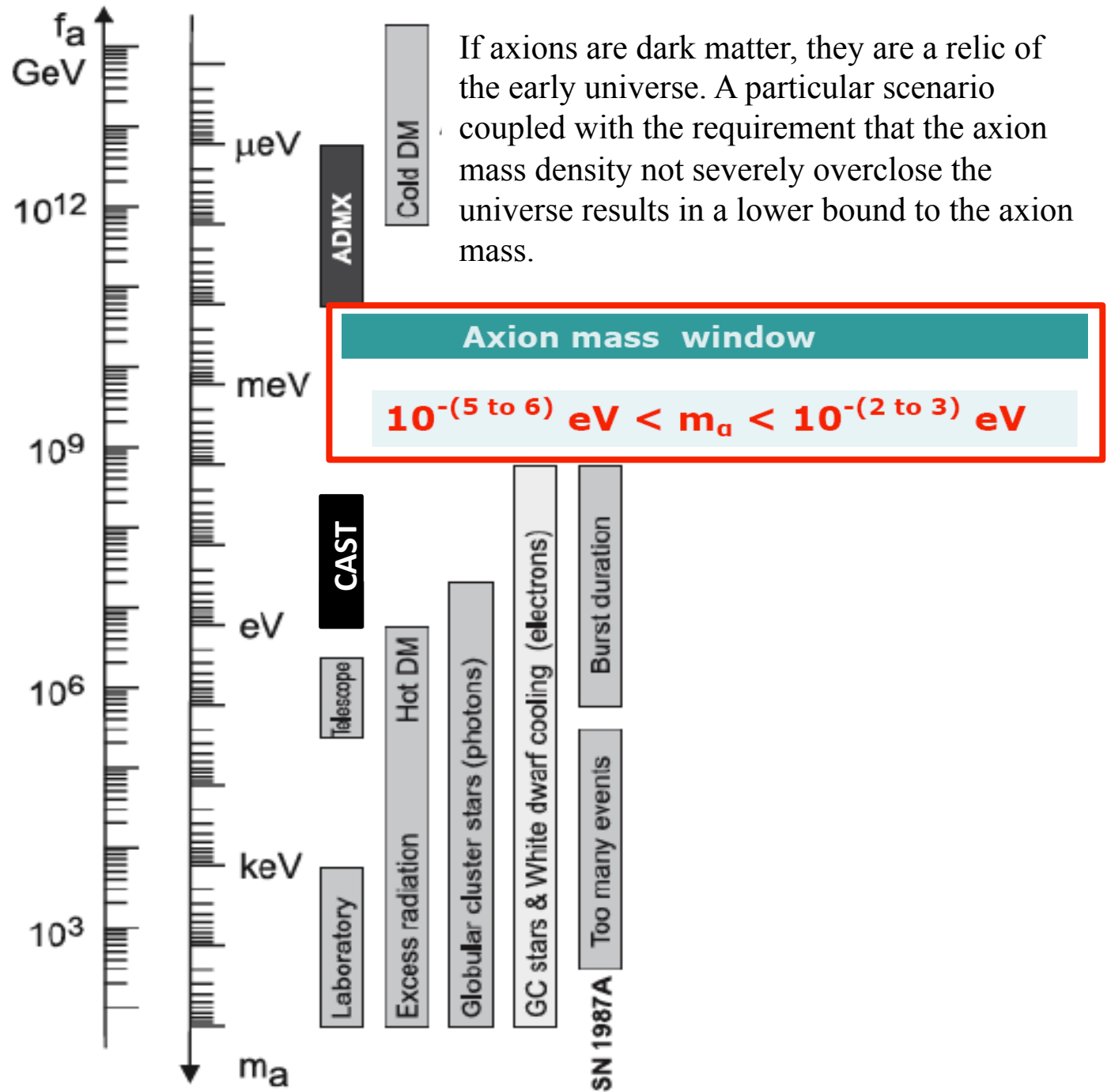


# THE CURRENT BOUNDS

C. Hagmann, H. Murayama, G.G. Raffelt, L.J. Rosenberger, and K. van Bibber  
 2008 Rev. Part. Physics.  
 Phys. Lett. B 667,1 (2008).

## Current Axion Search Experiments

- Solar Axion Telescope – „CAST“
- Dark Matter Axion Search – „ADMX“
- Vacuum Optical Properties –“PVLAS“ etc.
- Photon Disappearance Experiments
- New Force Search – Torsion Pendulums, etc.



If axions are dark matter, they are a relic of the early universe. A particular scenario coupled with the requirement that the axion mass density not severely overclose the universe results in a lower bound to the axion mass.

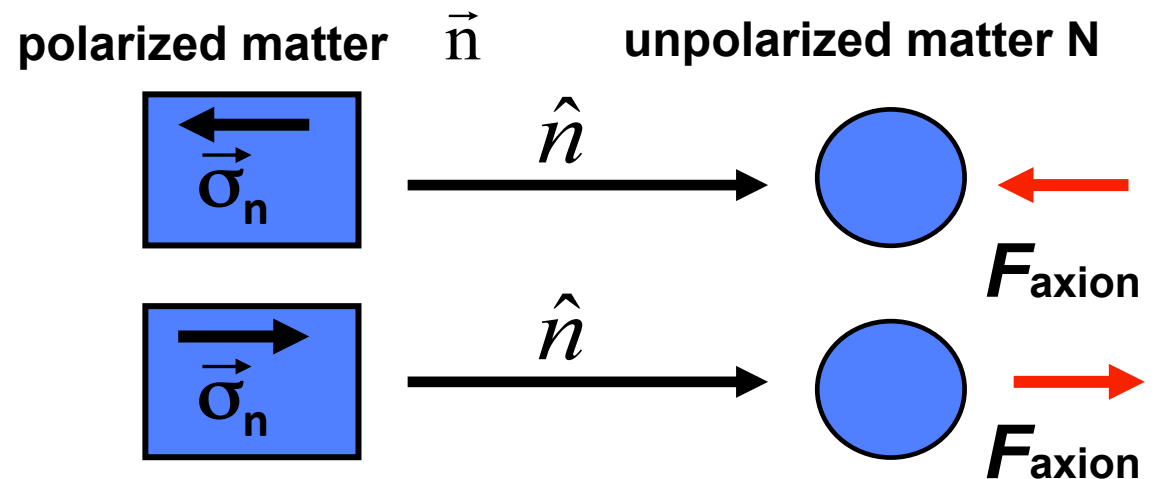
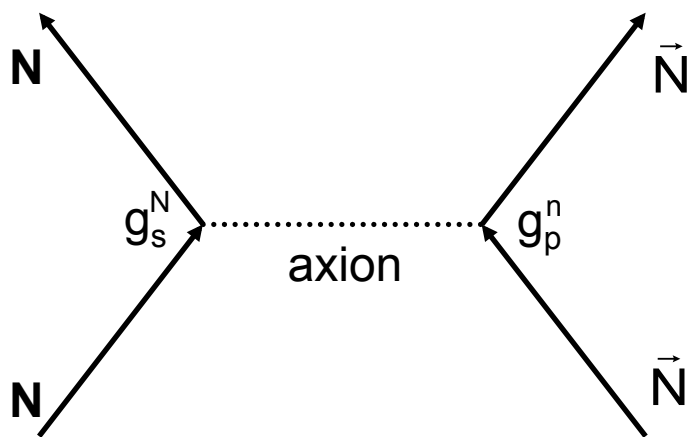
# Short range interaction of the axion

Yukawa-type potential with monopole-dipole coupling:

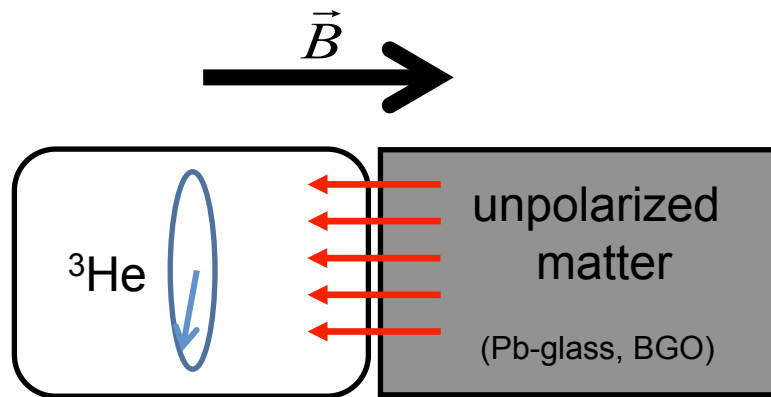
$$V(r) = \kappa \hat{n} \cdot \vec{\sigma} \left( \frac{1}{\lambda r} + \frac{1}{r^2} \right) e^{-r/\lambda}$$

(Moody and Wilczek PRD 30 130 (1984))

with :  $\kappa = \frac{\hbar^2 g_s g_p}{8\pi m_n}$  ,  $\lambda = \frac{\hbar}{m_a c}$   $\left( \begin{array}{l} 10^{-6} \text{ eV} < m_a < 10^{-2} \text{ eV} \\ 10^{-5} \text{ m} < \lambda < 10^{-1} \text{ m} \end{array} \right)$



# How to measure?

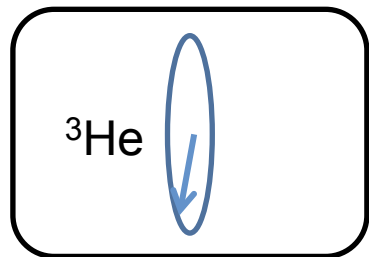


$$\omega_{\text{L,He}}(t) = \gamma_{\text{He}} \cdot B(t)$$

$$\omega_{\text{Close}}(t) = \omega_{\text{L,He}}(t) + \Delta\omega$$

$$\text{(with: } \Delta\omega = 2\pi \cdot \delta\nu = \bar{V} / \hbar \text{)}$$

**Position: Close**



**Position: Far**

$$\omega_{\text{Far}}(t) = \omega_{\text{L,He}}(t)$$

$$\Rightarrow \Delta\omega = \omega_{\text{Close}} - \omega_{\text{Far}}$$

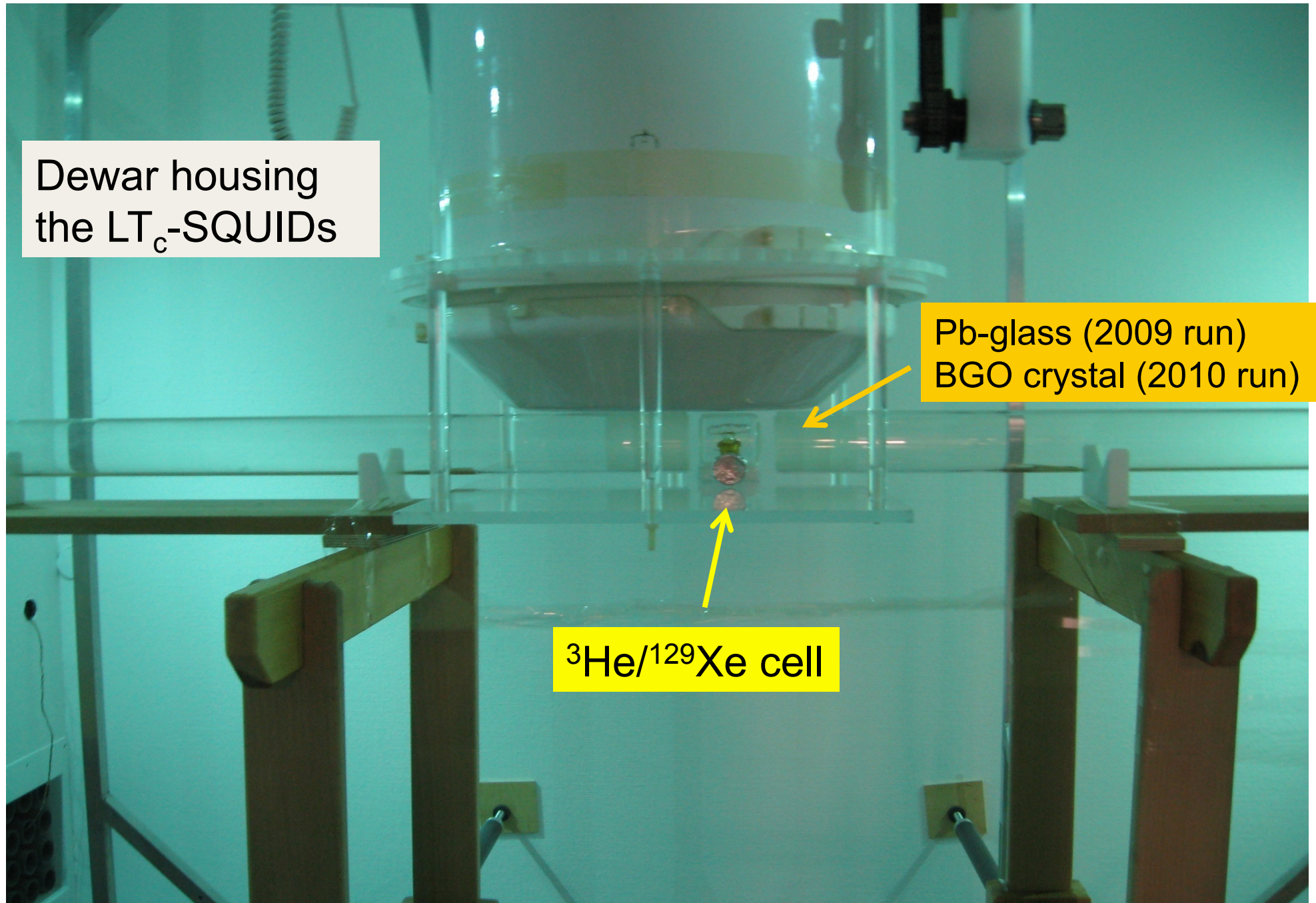
**Requirement:**  $\omega_{\text{L,He}}(t) = \text{const.}$



Dewar housing  
the  $LT_c$ -SQUIDS

Pb-glass (2009 run)  
BGO crystal (2010 run)

$^3\text{He}/^{129}\text{Xe}$  cell



# Data processing for extraction of short-range interaction effect:

1. To cancel magnetic field influence we calculate the weighted phase difference:

$$\Delta\Phi(t) = \Phi_{\text{He}} - \frac{\gamma_{\text{He}}}{\gamma_{\text{Xe}}} \cdot \Phi_{\text{Xe}} \quad \neq \text{const}$$

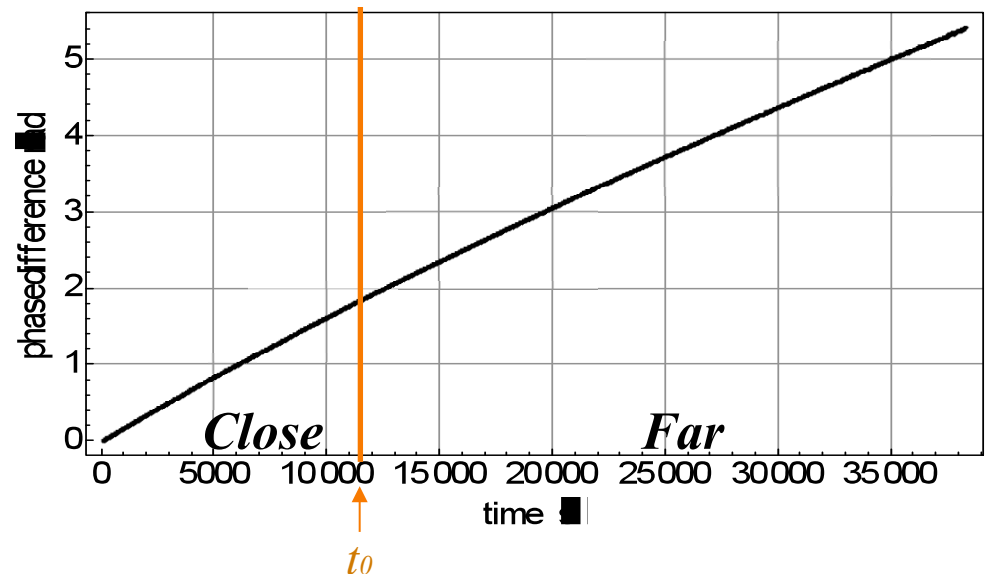
2. Temporal dependence can be described by:

$$f(t) = c + (a_{\text{ER}} + a_{\text{CS}} + a_{\text{SR}}) \cdot t + a_{\text{He}} \cdot e^{-t/T_{2,\text{He}}} + a_{\text{Xe}} \cdot e^{-t/T_{2,\text{Xe}}}$$

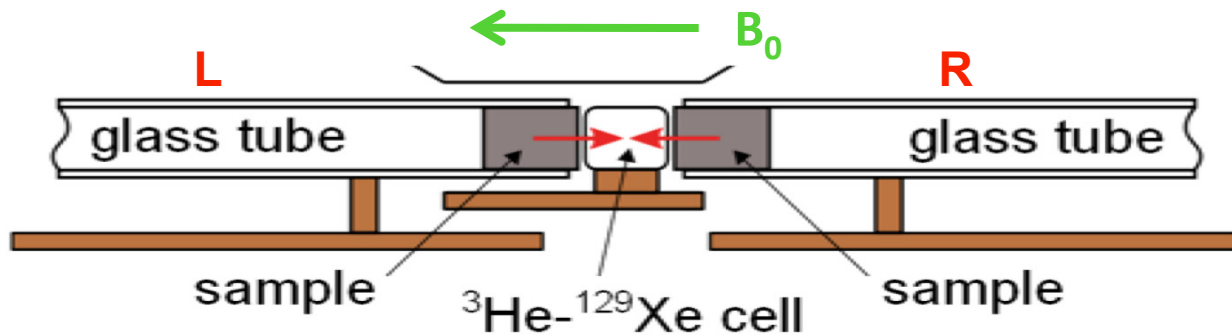
Ramsey-Bloch-Siegert-Shift

- Earth rotation
- chemical shift
- **short range !**

$$\Delta\omega_{\text{SR}} = (a_{\text{SR,close}} - a_{\text{SR,far}}) \cdot \left(1 - \frac{\gamma_{\text{He}}}{\gamma_{\text{Xe}}}\right)^{-1}$$



# Results



## September 2010:

11 measurements (~9 hours)

gap = 2.2 mm

Mass sample: BGO crystal with density  $\rho=7.13 \text{ g/cm}^3$

$\Rightarrow \overline{\Delta v_{SR}} = (-0.78 \pm 1.22 \pm 0.15) \text{ nHz}$

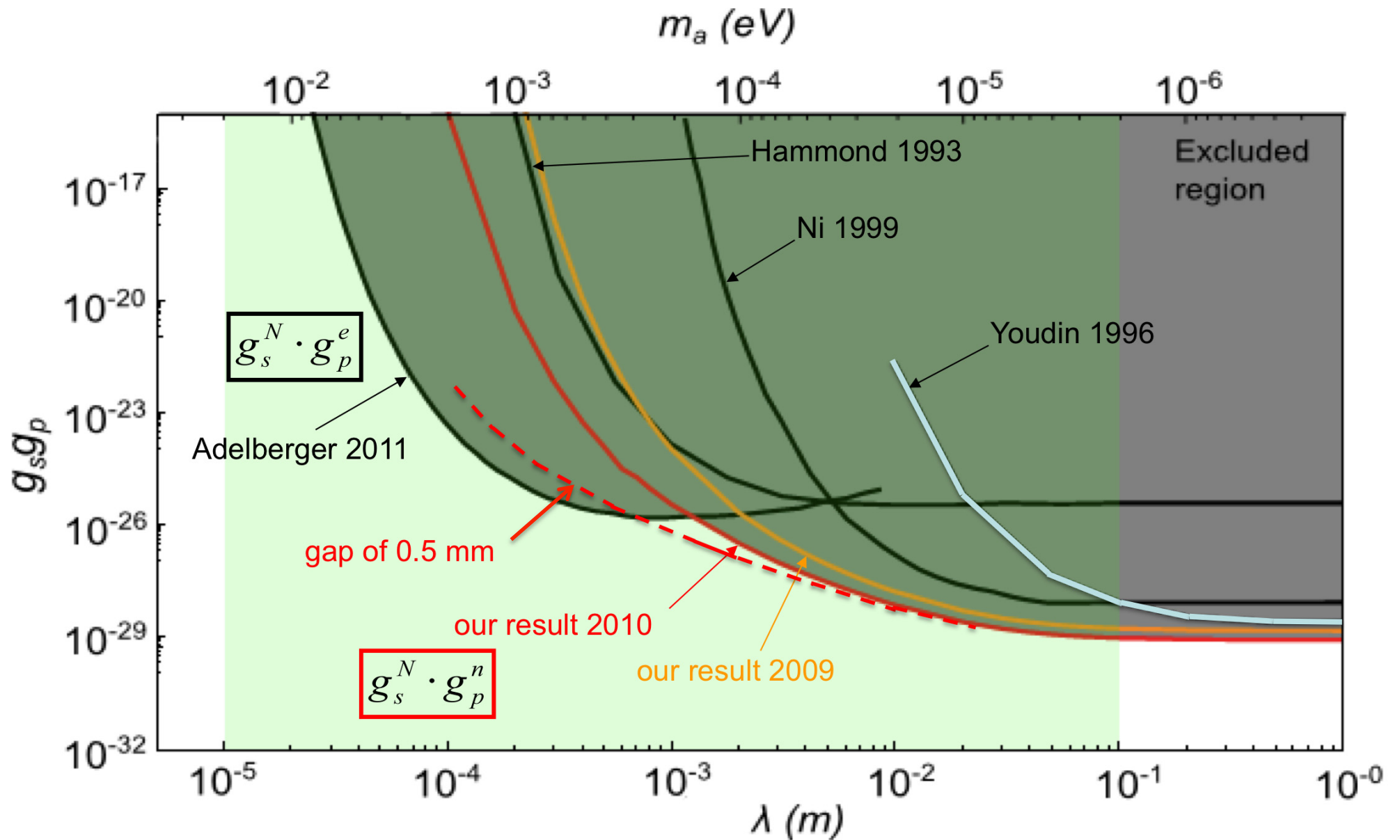
**Analysis:** 
$$V_{SP}(\vec{r}) = \frac{\hbar^2 g_S g_P}{8\pi m} \left( \frac{\vec{r}}{r} \cdot \vec{\sigma} \right) \left( \frac{1}{r\lambda} + \frac{1}{r^2} \right) \cdot e^{-r/\lambda}$$

Average potential  $\langle V^*(\lambda) \rangle$  was calculated numerically for our cells ( $\varnothing = 6 \text{ cm}$ ,  $l = 6 \text{ cm}$ ), a gap of 2.2 mm between cell inner volume and BGO crystal ( $\varnothing = 57 \text{ mm}$ ,  $l = 81 \text{ mm}$ ). Due to the inequation  $\langle V^*(\lambda) \rangle / \hbar < \Delta(\delta v)$  the sensitivity level of  $g_S g_P$  can be determined by:

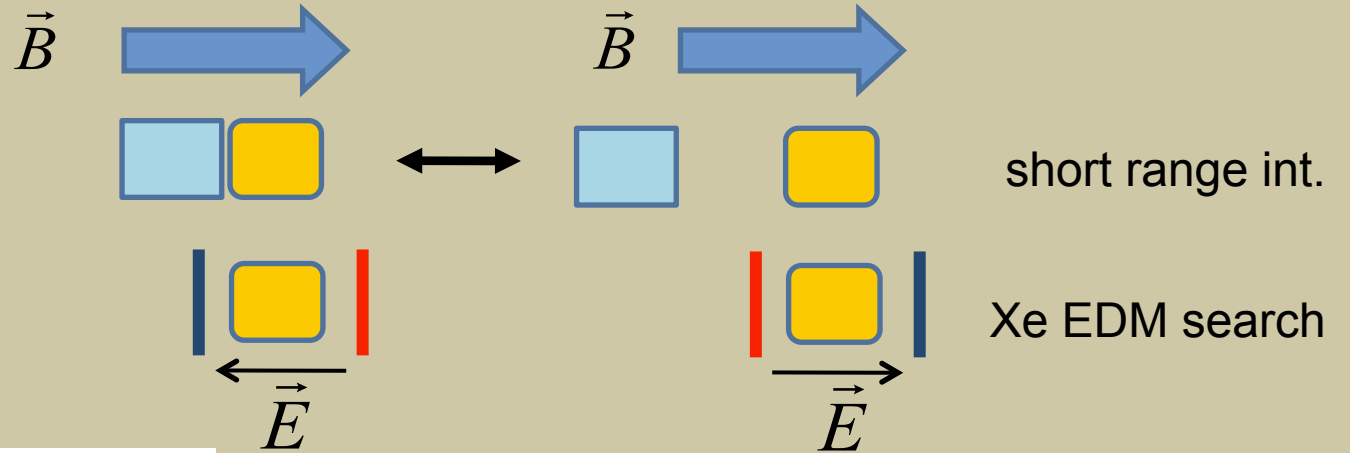
$$g_S g_P < 4 (2\pi)^2 m_n \overline{\delta(\Delta v)_{corr}} / (NV \hbar \langle V^*(\lambda) \rangle)$$

	$\Delta v_{SR}$ [nHz]	$\delta(\Delta v)_{corr.}$ [nHz]	$\delta(\Delta v)_{uncorr.}$ [nHz]
C53-R	25.17	6.19	0.68
C54-R	-7.39	4.28	0.56
C55-L	-1.87	4.63	0.52
C60-L	15.19	5.19	0.57
C63-L	2.34	3.40	0.44
C65-L	1.10	4.26	0.54
C67-R	-3.82	4.09	0.53
C68-R	-7.46	3.39	0.43
C71-R	8.04	3.09	0.40
C80-L	18.35	3.95	0.51
C82-L	-22.00	4.43	0.56

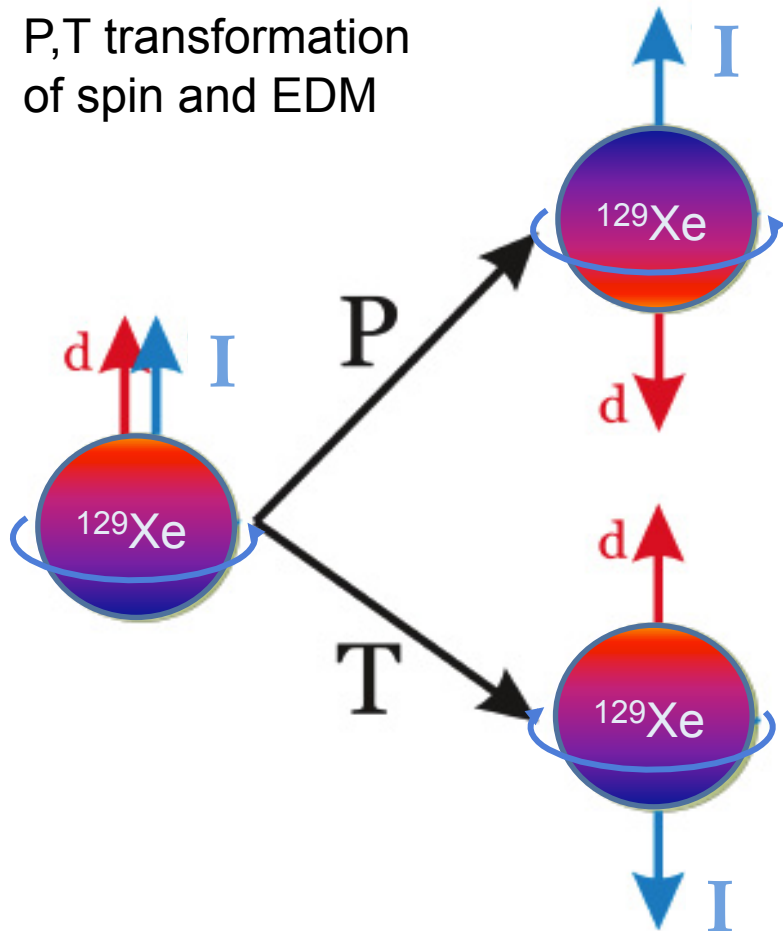
# Exclusion Plot for new spin-dependent forces



# Search for a Xe EDM



P,T transformation  
of spin and EDM

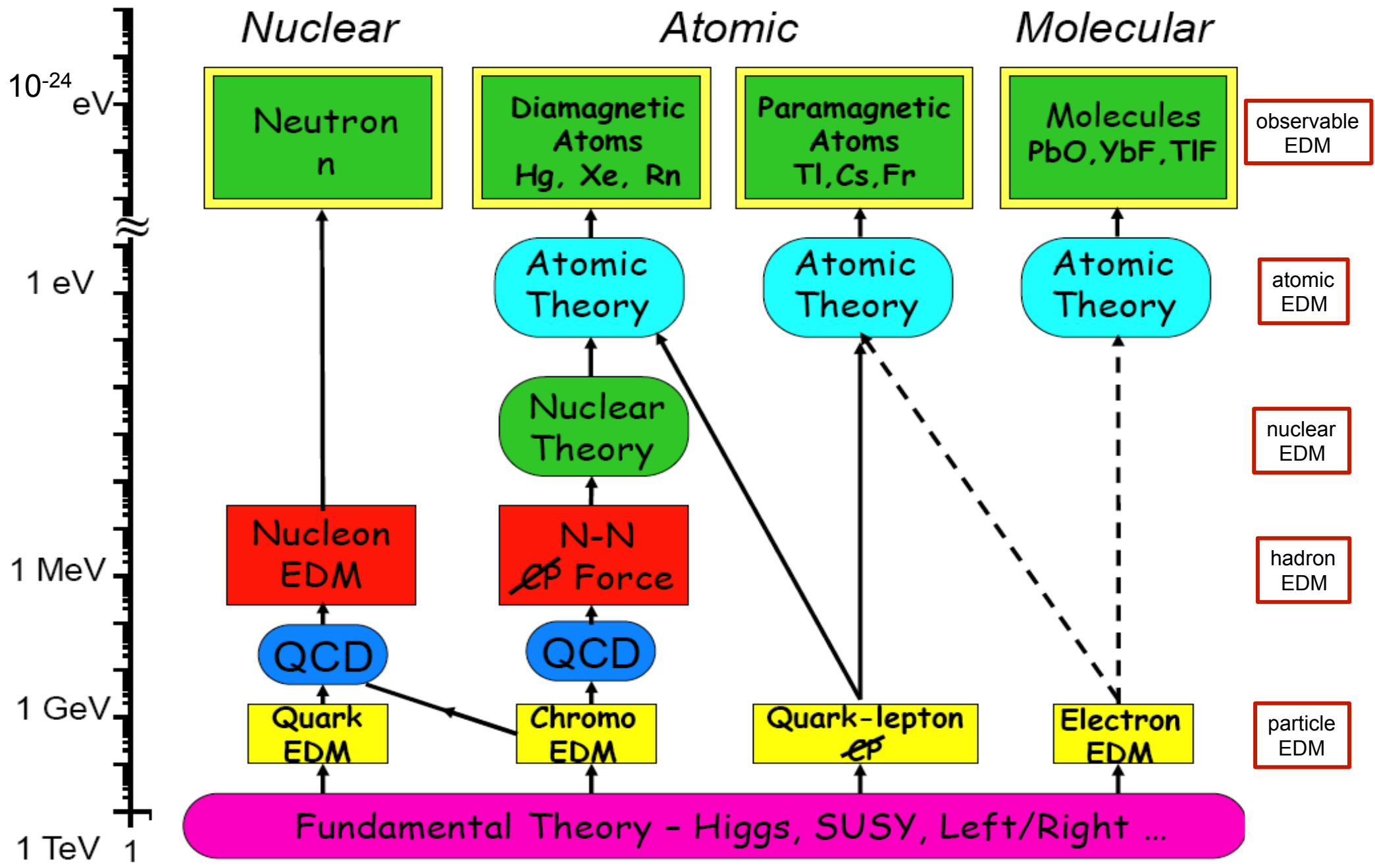


**violate**  
**Parity & Time Reversal**  
**Symmetry**  
**(and also CP)**

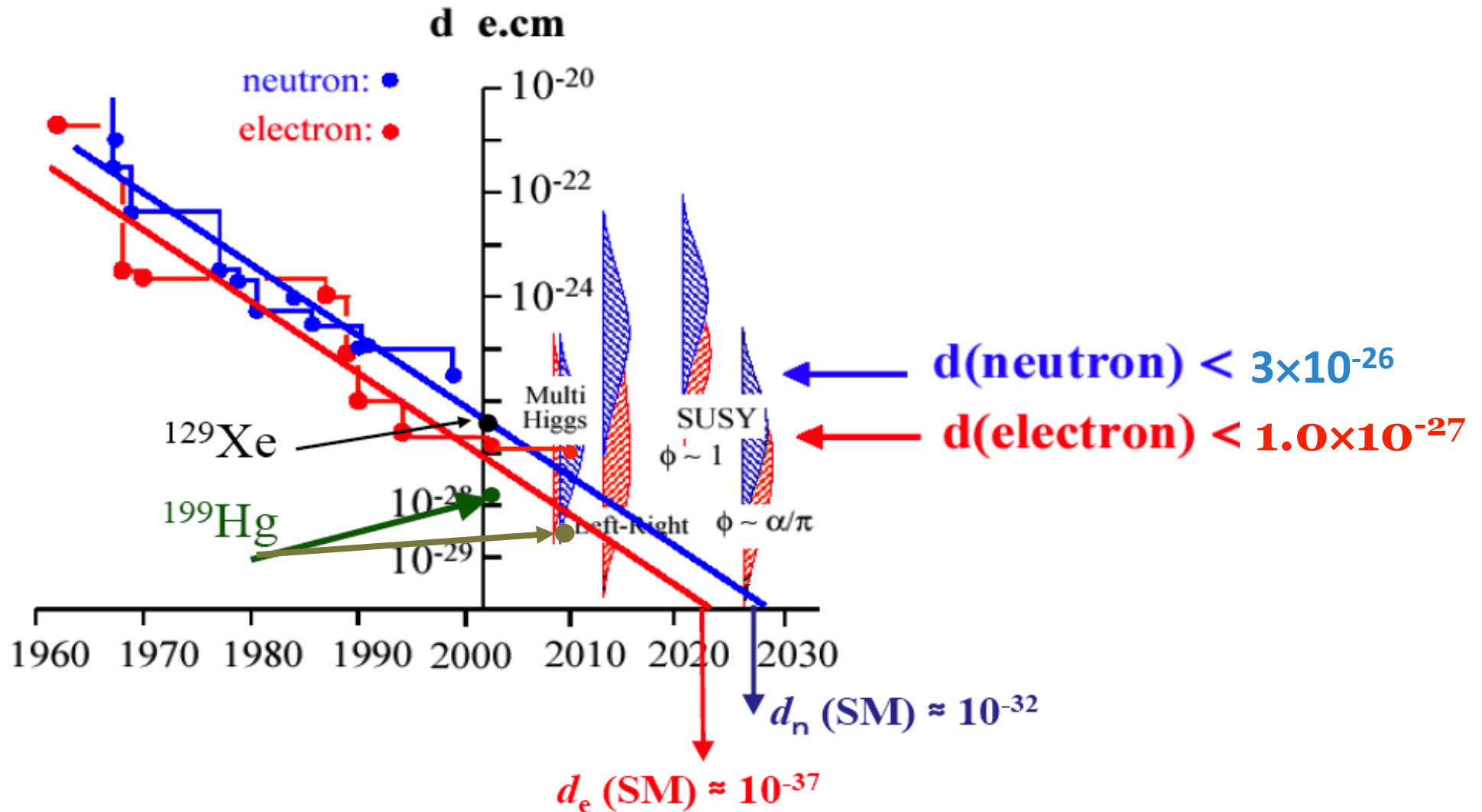
$\rightarrow$  could offer hint to  
**Matter-Anti-matter Puzzle**

Standard-model: CKM-~~CP~~ too small to produce  
observed baryon asymmetry

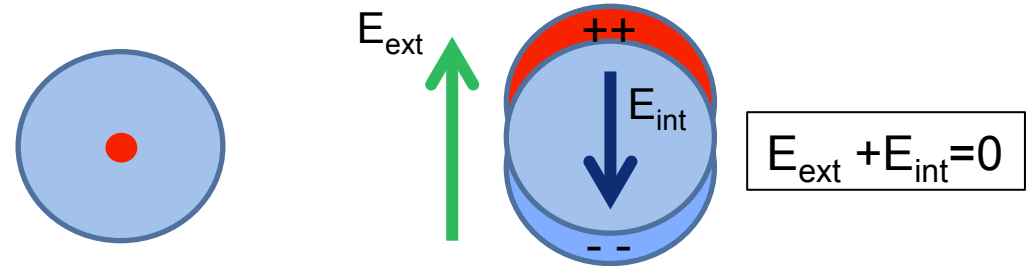
$$\eta_{\text{exp}} = \frac{n_B - n_{\bar{B}}}{n_\gamma} = (6.0 \pm 0.3) \cdot 10^{-10}$$



# Experimental upper limits on EDM



# Atomic EDM's



➤ L.I.Schiff (*PR 132 2194, 1963*):

System of non-relativistic charged point particles that interact electrostatically can not have an EDM

➤ Heavy atoms (relativistic treatment):

-  $d_e \neq 0 \rightarrow d_{\text{atom}} \neq 0$   $\sim Z^3 \alpha^2 d_e$

- P,T-odd eN interaction  
 Tensor-Pseudotensor  $\sim Z^2 G_F C_T$   
 Scalar- Pseudoscalar  $\sim Z^3 G_F C_S$

- Nuclear EDM – finite size  
 Schiff moment induced by P,T-odd N-N interaction  $\sim 10^{-25} \eta$  [ecm]

$|d(^{199}\text{Hg})| < 3.1 \times 10^{-29} e \text{ cm (95\% C.L.)}$   
 PRL 102, 101601 (2009)

Parameter	<sup>199</sup> Hg	Best alternate limit
$d_e$ (e cm)	$3.0 \times 10^{-27}$	YbF: $1.0 \times 10^{-27}$
$d_n$ (e cm)	$5.8 \times 10^{-26}$	n: $2.9 \times 10^{-26}$
$C_S$	$5.2 \times 10^{-8}$	Tl: $2.4 \times 10^{-7}$
$C_T$	$1.5 \times 10^{-9}$	TlF: $4.5 \times 10^{-7}$
$C_{PS}$	$5.1 \times 10^{-7}$	TlF: $3 \times 10^{-4}$
$\eta$	$8.0 \times 10^{-5}$	Xe: $5 \times 10^{-2}$

➤ Diamagnetic atoms:

Ginges & Flambaum, *Phys. Rep.* 397 (04) 63.  
 Dzuba, Flambaum, Ginges, *Phys. Rev. A* 66 (02) 012111.

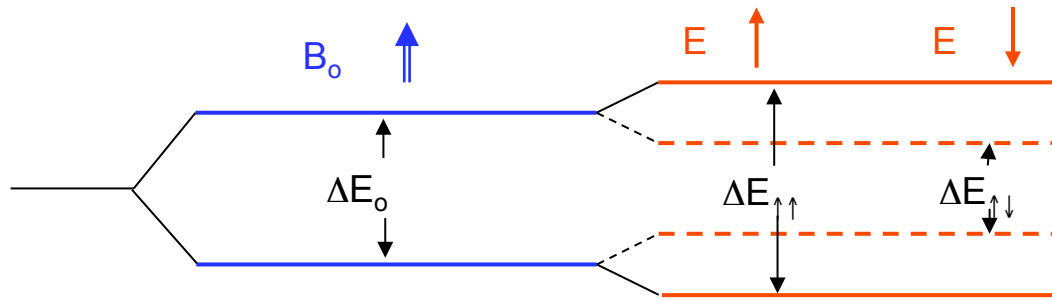
$$d(^{199}\text{Hg}) = 10^{-2} d_e + 2.0 \times 10^{-20} C_T + 5.9 \times 10^{-22} C_S + 6 \times 10^{-23} C_{PS} + 3.9 \times 10^{-25} \eta \text{ [ecm]}$$

$$d(^{129}\text{Xe}) = 10^{-3} d_e + 5.2 \times 10^{-21} C_T + 5.6 \times 10^{-23} C_S + 1.2 \times 10^{-23} C_{PS} + 6.7 \times 10^{-26} \eta$$

6× less sensitive to CP violating interactions



# Measurement sensitivity: $^{129}\text{Xe}$ electric dipole moment



$$h \cdot \Delta\nu = h \cdot (\Delta\nu_{\uparrow\uparrow} - \Delta\nu_{\uparrow\downarrow}) = 4 \cdot E \cdot |d_{Xe}|$$

Rosenberry and Chupp, PRL 86,22 (2001)

$$|d_{Xe}| = (0.7 \pm 3.3 \pm 0.1) \times 10^{-27} \text{ ecm}$$

**Observable:**  
weighted frequency  
difference

$$\Delta\nu_{\uparrow\uparrow} = \Delta\nu_{\uparrow\uparrow}^{He,EDM} - (\gamma_{He}/\gamma_{Xe}) \cdot \Delta\nu_{\uparrow\uparrow}^{Xe,EDM} \approx -(\gamma_{He}/\gamma_{Xe}) \cdot \Delta\nu_{\uparrow\uparrow}^{Xe,EDM}$$

$$\Delta\nu_{\uparrow\downarrow} = \Delta\nu_{\uparrow\downarrow}^{He,EDM} - (\gamma_{He}/\gamma_{Xe}) \cdot \Delta\nu_{\uparrow\downarrow}^{Xe,EDM} \approx -(\gamma_{He}/\gamma_{Xe}) \cdot \Delta\nu_{\uparrow\downarrow}^{Xe,EDM}$$

sensitivity limit:

$$|d_{Xe}| < \frac{\pi \cdot \hbar}{2E \cdot (\gamma_{He}/\gamma_{Xe})} \cdot \delta\nu$$

from 2010 run:  $\delta\nu = 0.2 \text{ nHz @ 1 day}$   
assume :  $E=2 \text{ kV/cm}$



$$|d_{Xe}| < 4 \cdot 10^{-29} \text{ ecm}$$

Then we will reach

... after 100 days of data taking:

$$|d_{Xe}| \approx 4 \cdot 10^{-30} \text{ ecm}$$

# Proposed setup

## Collaboration:

University of Mainz  
 KVI Groningen  
 University of Heidelberg  
 PTB Berlin

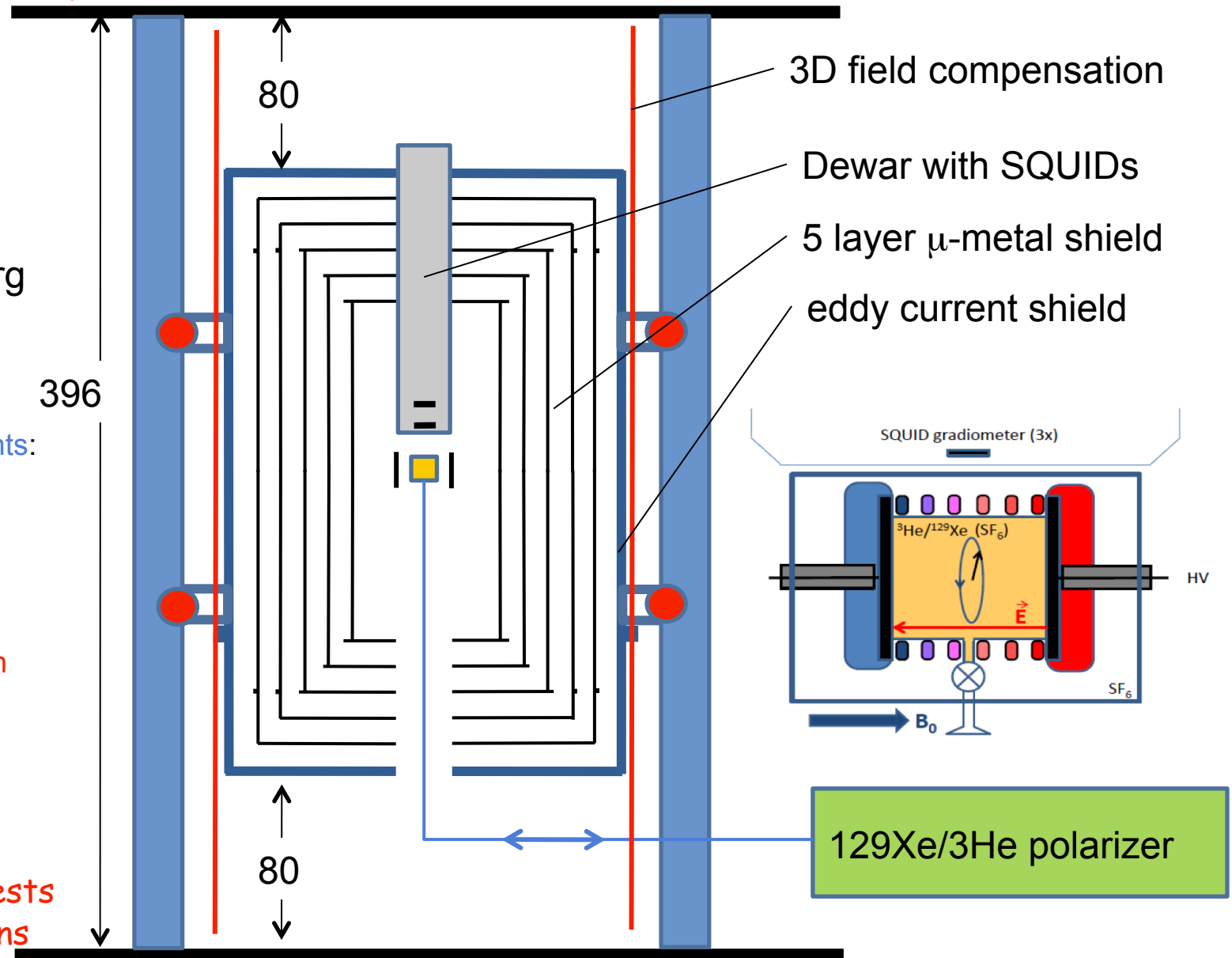
There is room for improvements:

- Increase of SNR of Xe  
 ( $P_{Xe}$ : 10%  $\Rightarrow$  70%)
- Increase of  $T_{2,Xe}$   
 5h (at present)  $\Rightarrow$  10-20 h

$$\triangleright \delta d_{Xe} < 10^{-31} \text{ ecm}$$

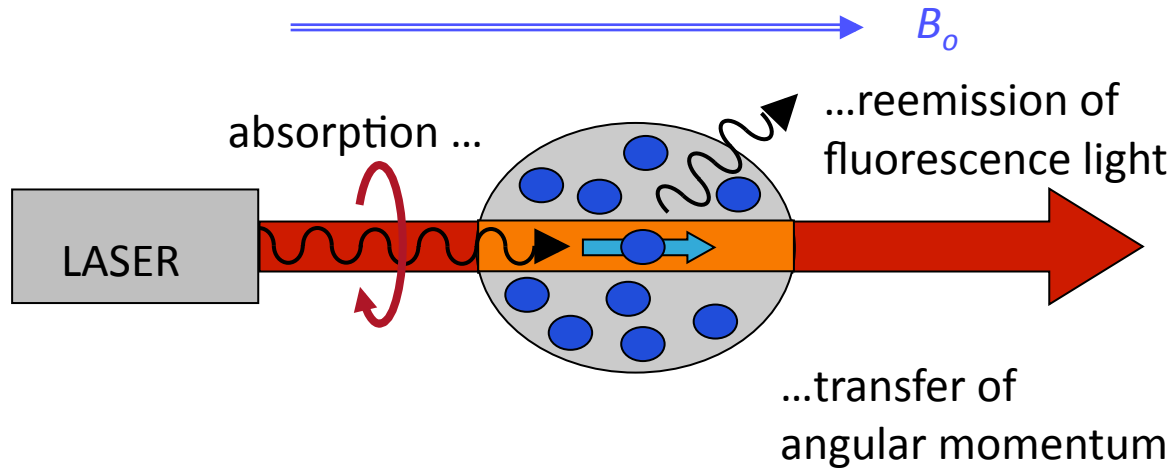
...new sensitivity levels for

- $\triangleright$  Lorentz-invariance tests
- $\triangleright$  short range interactions

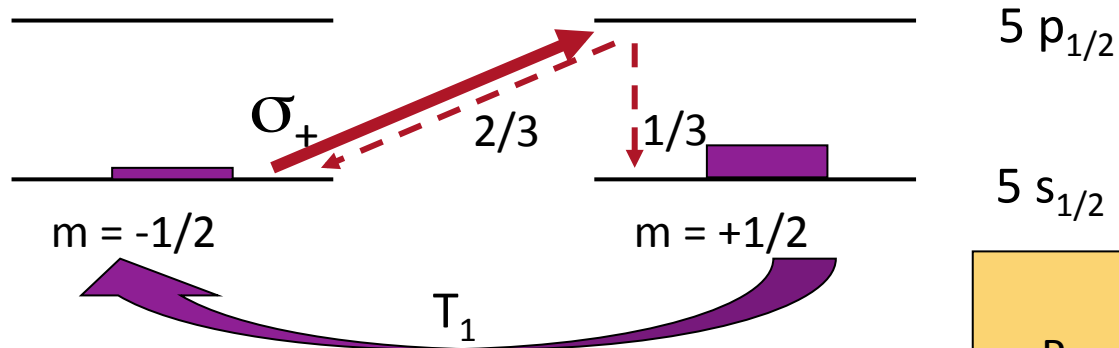




# Optical Pumping



Rb-pumping



rate equation:

$$N \cdot \frac{dP}{dt} = 2 \cdot \eta(P) \cdot \frac{dL}{dt} / \hbar - P \cdot N / T_1$$

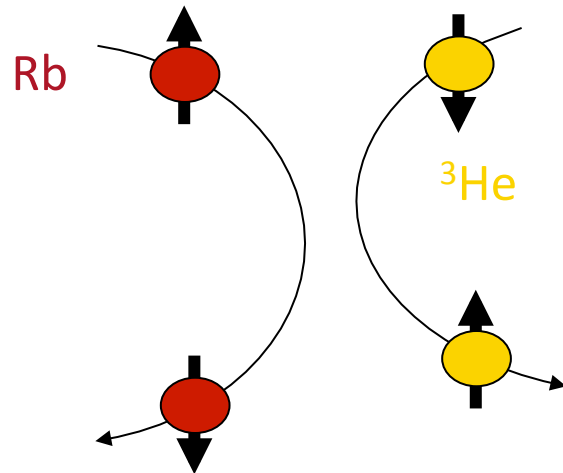
$$P = \frac{N(1/2) - N(-1/2)}{N(1/2) + N(-1/2)}$$

$$= 1 - (2/3)^n$$

# Optical Pumping of $^3\text{He}$

## history :

- Spin exchange with optically pumped Rb-vapour ( SEOP )  
( Bouchiat et al., Phys. Rev. Lett. 5 (1960) 373 )



$$p_{\text{He}} \approx 1\text{-}10 \text{ bar}$$

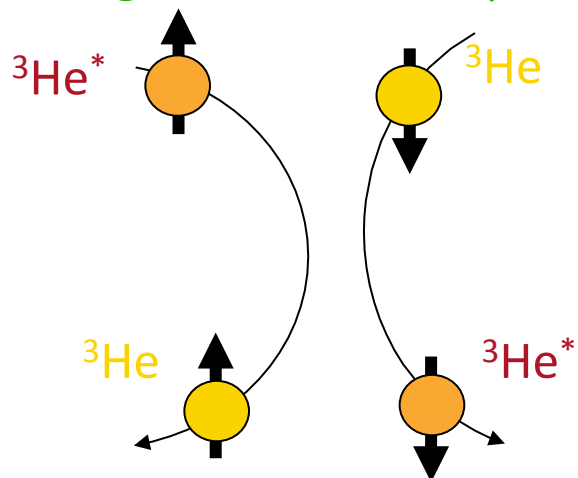
$$H_{\text{HFI}} = \alpha \cdot \vec{S}_{\text{Rb}} \cdot \vec{I}_{\text{He}} \quad (\Delta E / \hbar \approx 10^8 \text{ Hz})$$

$$\text{collision time: } \tau_c \approx 10^{-12} \text{ s}$$

$$\Gamma_{\text{SE}} \approx \langle (\tau_c \cdot \Delta E / \hbar)^2 \cdot \sigma_{\text{SE}} \cdot v_r \rangle \cdot [\text{Rb}]$$

$$\approx 10^{-8} \cdot \langle \sigma_{\text{SE}} \cdot v_r \rangle \cdot [\text{Rb}] \approx \frac{1}{3} [\text{h}^{-1}]$$

- Optical pumping of metastable  $^3\text{He}^*$ -atoms ( MEOP )  
( Colegrove et al., Phys. Rev. 132 (1963) 2561 )



$$p_{\text{He}} \approx 1 \text{ mbar}$$

$$\Gamma_{\text{ME}} \approx \langle \sigma_{\text{ME}} \cdot v_r \rangle \cdot [^3\text{He}]$$

$$\approx 1 [\text{s}^{-1}]$$

# Polarization of He<sup>3</sup> Gas by Optical Pumping

F. D. COLEGROVE, L. D. SCHEARER,\* AND G. K. WALTERS\*

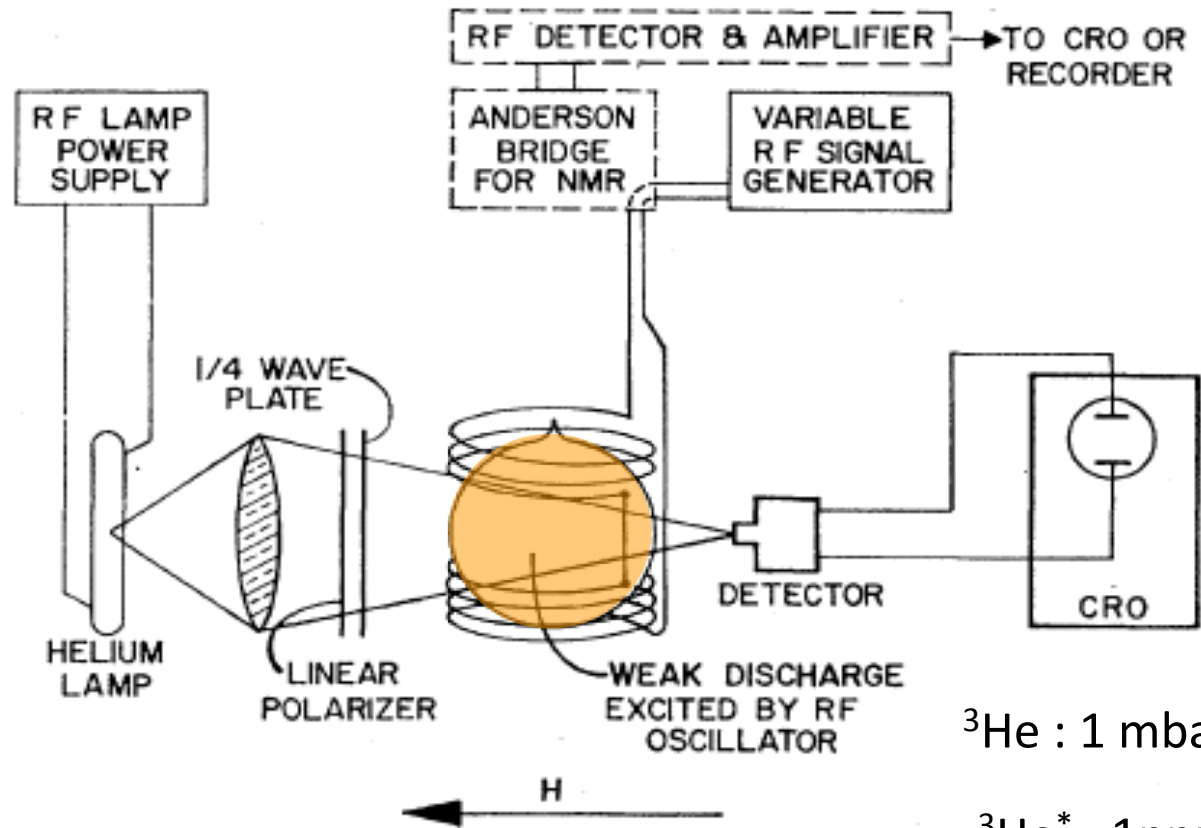
*Texas Instruments Incorporated, Dallas, Texas*

(Received 5 August 1963)

## MEOP: Metastability Exchange Optical Pumping



L.D. Schearer



<sup>3</sup>He : 1 mbar

<sup>3</sup>He\* ≈ 1ppm

In terms of frequency:

$$v_{\perp} = a_{\max} \cdot \frac{\Omega_s}{2\pi} = (26.1 \pm 26.6) \text{ nHz} \quad (95\% \text{ C.L.})$$

**Kostelecky et al. , Phys. Rev. D 60, 116009 (1999)**

free neutron:

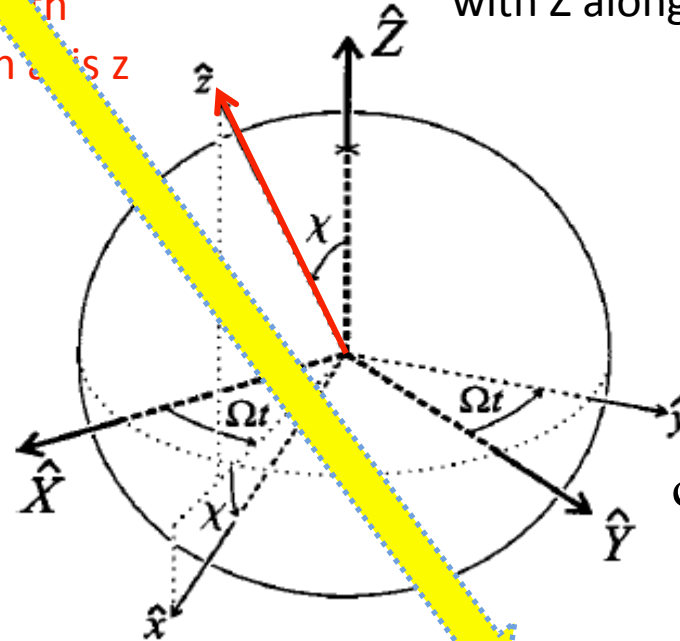
$$n : \mu = -1.913 \mu_K$$

Schmidt-Model

$${}^3\text{He} : \mu = -2.1276 \mu_K$$

$${}^{129}\text{Xe} : \mu = -0.7779 \mu_K$$

Lab-frame with  
quantization axis z



(X,Y,Z) non-rotating frame  
with Z along Earth's rotation axis

PTB Berlin:

$$\Theta = 52,5164^\circ \text{ north}$$

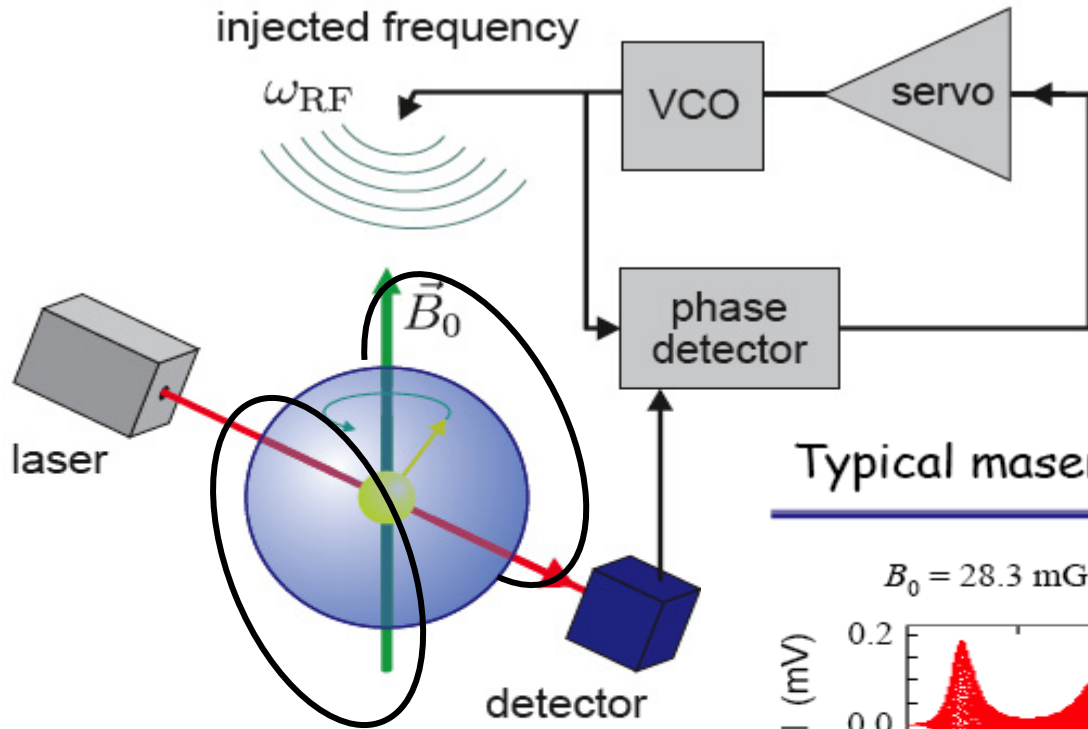
$$\rho = 28^\circ \text{ (north-south)}$$

$$\cos \chi = \cos \theta \cdot \cos \rho = 0.543$$

$$\sin \chi \cdot \left| -3.5 \cdot \tilde{b}_{\perp}^n + 0.012 \cdot \tilde{d}_{\perp}^n + 0.012 \cdot \tilde{g}_{D,\perp}^n \right| \leq 2\pi \cdot \delta v_{\perp} \cdot \hbar$$

$$\tilde{b}_{\perp}^n \leq 3.72 \cdot 10^{-32} \text{ GeV} \quad (95\% \text{ C.L.})$$

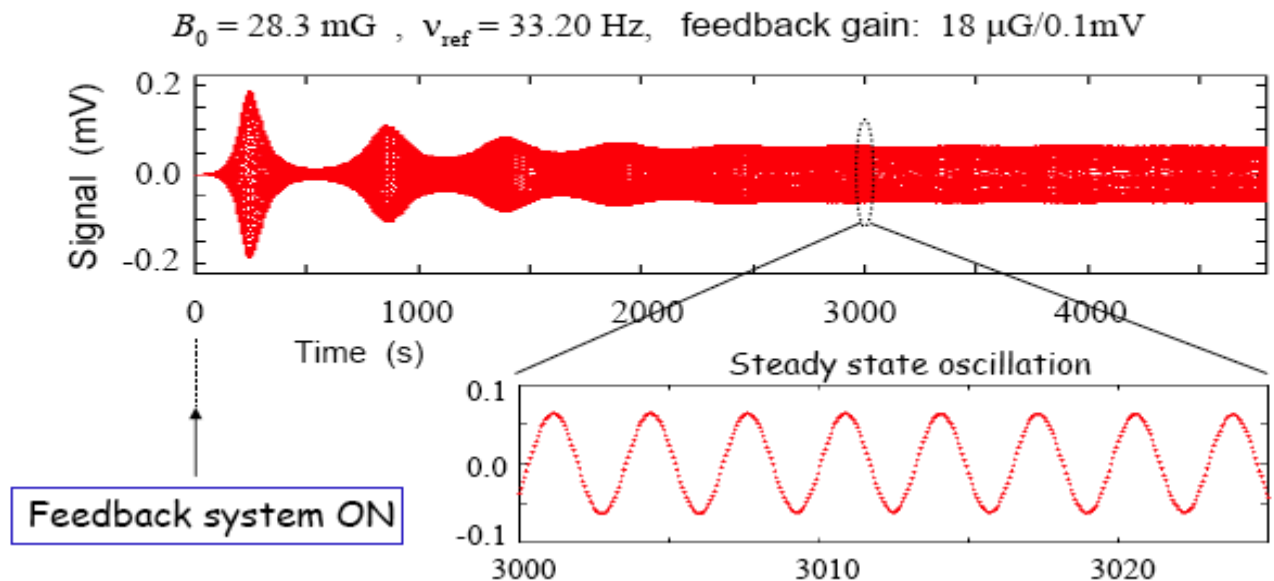
# Feedback loop to get long coherence times ... ( Cs-Magnetometer, Maser, ... )



but ...

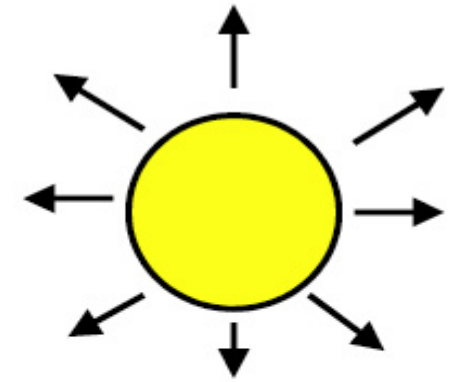
- frequency shifts due to feedback phase error
- light shift
- ...

Typical maser oscillation signal

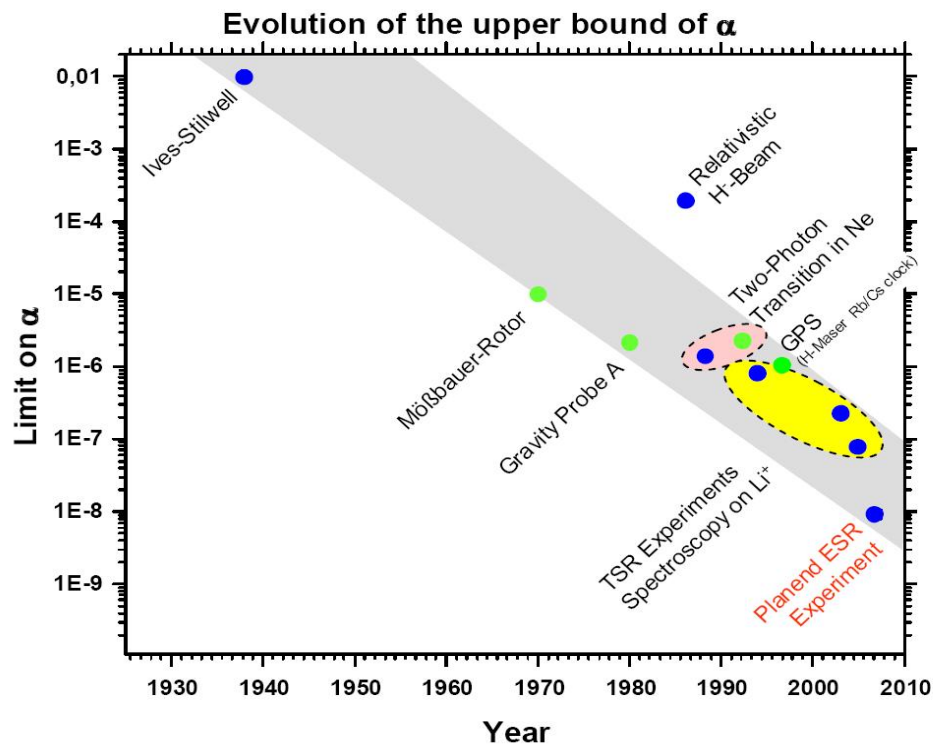
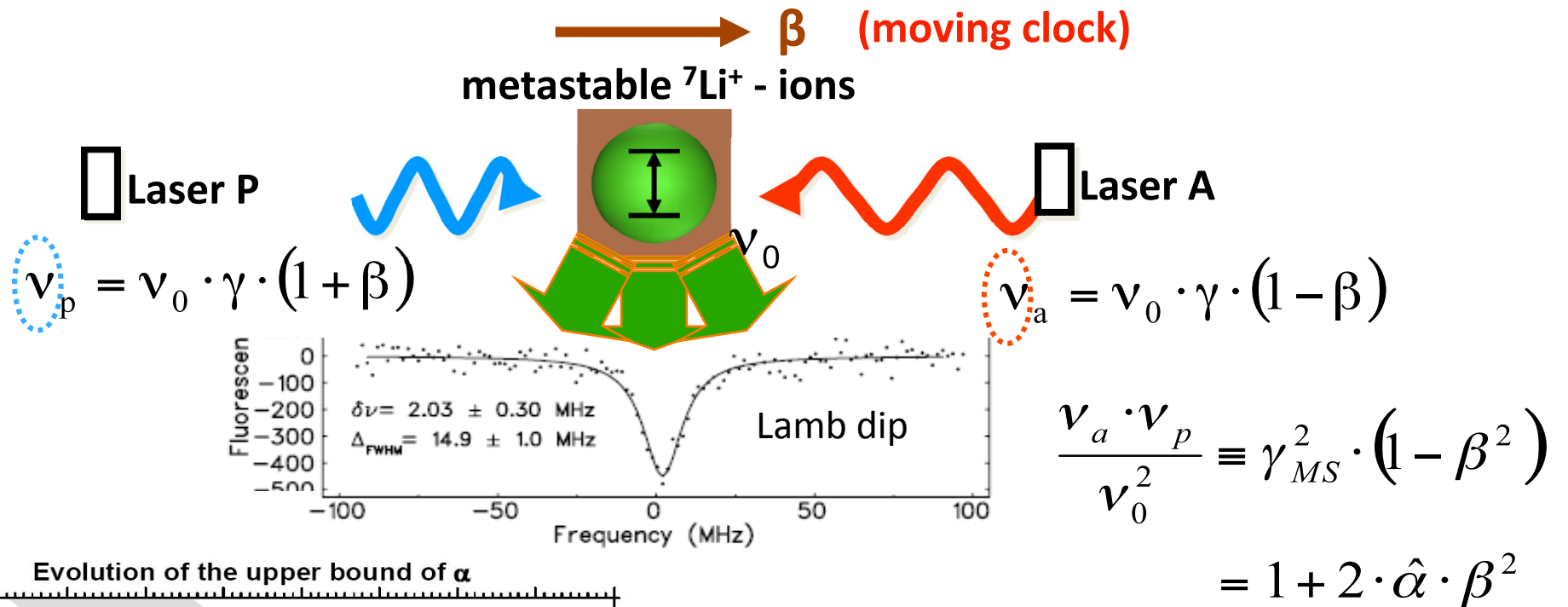




# Astrophysics limits on axion



Observation	Bound on Coupling	Bound on Mass
Solar $^8\text{B}$ Neutrino Flux	$g_{a\gamma\gamma} < 5 \times 10^{-10} \text{ GeV}^{-1}$	$m_a < 1 \text{ eV}$
Lifetime of HB Stars	$g_{a\gamma\gamma} < 1 \times 10^{-10} \text{ GeV}^{-1}$	$m_a < 0.3 \text{ eV}$
Cooling rate of White Dwarf G117-B15A	$\frac{C_e m_e}{f_a} < 1 \times 10^{-13}$	$m_a < 0.005 \text{ eV}$
Cooling rate of SN1987A	$\frac{C_N m_N}{f_a} < 6 \times 10^{-10}$	$m_a < 0.02 \text{ eV}$



$$\hat{\alpha} < 2.2 \times 10^{-7}$$



$$|c_{XX}^p + c_{YY}^p - 2c_{ZZ}^p| \approx 10^{-11},$$

$$|c_{TJ}^p + c_{JT}^p| \approx 10^{-8} \quad (J = X, Y, Z),$$

$$|c_{XX}^e + c_{YY}^e - 2c_{ZZ}^e| \approx 10^{-5},$$

$$\text{and } |c_{TJ}^e + c_{JT}^e| \approx 10^{-2} \quad (J = X, Y, Z).$$

Coefficient	Proton	Neutron	Electron
$\tilde{b}_X$	$10^{-27}$ GeV	$10^{-31}$ GeV	$10^{-31}$ GeV
$\tilde{b}_Y$	$10^{-27}$ GeV	$10^{-31}$ GeV	$10^{-31}$ GeV
$\tilde{b}_Z$	–	–	$10^{-30}$ GeV
$\tilde{b}_T$	–	$10^{-27}$ GeV	$10^{-27}$ GeV
$\tilde{b}_J^* (J = X, Y, Z)$	–	–	–
$\tilde{c}_-$	$10^{-25}$ GeV	$10^{-27}$ GeV	$10^{-19}$ GeV
$\tilde{c}_Q$	$10^{-22}$ GeV	–	$10^{-19}$ GeV
$\tilde{c}_X$	$10^{-25}$ GeV	$10^{-25}$ GeV	$10^{-19}$ GeV
$\tilde{c}_Y$	$10^{-25}$ GeV	$10^{-25}$ GeV	$10^{-19}$ GeV
$\tilde{c}_Z$	$10^{-24}$ GeV	$10^{-27}$ GeV	$10^{-19}$ GeV
$\tilde{c}_{TX}$	$10^{-20}$ GeV	–	$10^{-18}$ GeV
$\tilde{c}_{TY}$	$10^{-20}$ GeV	–	$10^{-18}$ GeV
$\tilde{c}_{TZ}$	$10^{-21}$ GeV	–	$10^{-20}$ GeV
$\tilde{c}_{TT}$	–	–	$10^{-18}$ GeV
$\tilde{d}_+$	–	$10^{-27}$ GeV	$10^{-27}$ GeV
$\tilde{d}_-$	–	$10^{-27}$ GeV	$10^{-27}$ GeV
$\tilde{d}_Q$	–	$10^{-27}$ GeV	$10^{-27}$ GeV
$\tilde{d}_{XY}$	–	$10^{-27}$ GeV	$10^{-27}$ GeV
$\tilde{d}_{YZ}$	–	$10^{-26}$ GeV	$10^{-27}$ GeV
$\tilde{d}_{ZX}$	–	–	$10^{-26}$ GeV
$\tilde{d}_X$	$10^{-25}$ GeV	$10^{-29}$ GeV	$10^{-22}$ GeV
$\tilde{d}_Y$	$10^{-25}$ GeV	$10^{-28}$ GeV	$10^{-22}$ GeV
$\tilde{d}_Z$	–	–	$10^{-19}$ GeV

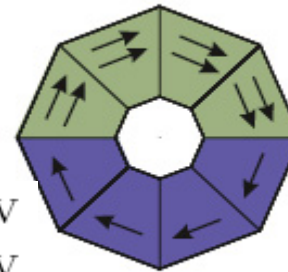
Coefficient	Proton	Neutron	Electron
$\tilde{H}_{XT}$	–	$10^{-26}$ GeV	$10^{-27}$ GeV
$\tilde{H}_{YT}$	–	$10^{-27}$ GeV	$10^{-27}$ GeV
$\tilde{H}_{ZT}$	–	$10^{-27}$ GeV	$10^{-27}$ GeV
$\tilde{g}_T$	–	$10^{-27}$ GeV	$10^{-27}$ GeV
$\tilde{g}_c$	–	$10^{-27}$ GeV	$10^{-27}$ GeV
$\tilde{g}_Q$	–	–	–
$\tilde{g}_-$	–	–	–
$\tilde{g}_{TJ} (J = X, Y, Z)$	–	–	–
$\tilde{g}_{XY}$	–	–	–
$\tilde{g}_{YX}$	–	–	–
$\tilde{g}_{ZX}$	–	–	–
$\tilde{g}_{XZ}$	–	–	–
$\tilde{g}_{YZ}$	–	–	–
$\tilde{g}_{ZY}$	–	–	–
$\tilde{g}_{DX}$	$10^{-25}$ GeV	$10^{-29}$ GeV	$10^{-22}$ GeV
$\tilde{g}_{DY}$	$10^{-25}$ GeV	$10^{-28}$ GeV	$10^{-22}$ GeV
$\tilde{g}_{DZ}$	–	–	–

**Clock-comparison  
experiments**

## Torsion pendulum

B.R.Heckel et al., PRD 78 (2008) 092006

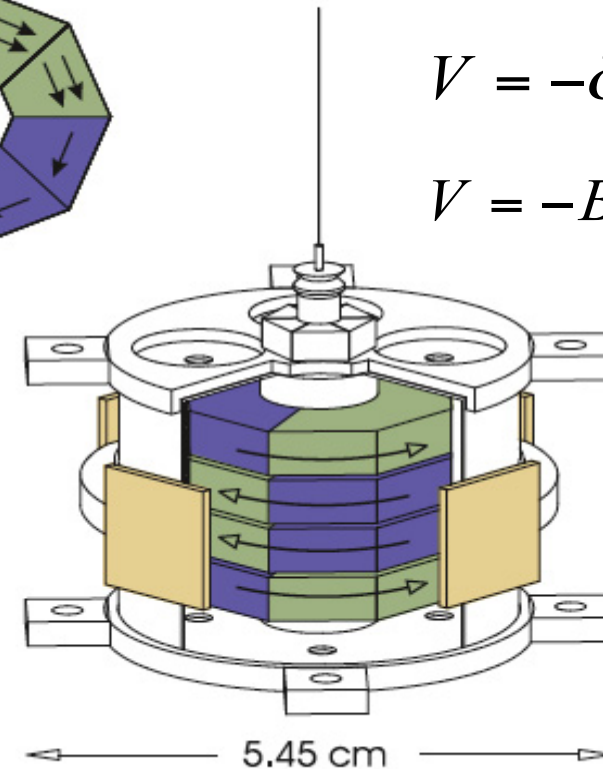
$\tilde{b}_X$	$(-0.9 \pm 1.4) \times 10^{-31}$ GeV
$\tilde{b}_Y$	$(-0.9 \pm 1.4) \times 10^{-31}$ GeV
$\tilde{b}_Z$	$(-0.3 \pm 4.4) \times 10^{-30}$ GeV
$\frac{1}{2}(\tilde{b}_T + \tilde{d}_- - 2\tilde{g}_c - 3\tilde{g}_T + 4\tilde{d}_+ - \tilde{d}_Q)$	$(0.9 \pm 2.2) \times 10^{-27}$ GeV
$\frac{1}{2}(2\tilde{g}_c - \tilde{g}_T - \tilde{b}_T + 4\tilde{d}_+ - \tilde{d}_- - \tilde{d}_Q)$	$(-0.8 \pm 2.0) \times 10^{-27}$ GeV
$+ \tan \eta(\tilde{d}_{YZ} - \tilde{H}_{XT})$	
$\tilde{d}_{XY} - \tilde{H}_{ZT} + \tan \eta \tilde{H}_{YT}$	$(0.1 \pm 1.8) \times 10^{-27}$ GeV
$\tilde{H}_{ZT}$	$(-4.1 \pm 2.4) \times 10^{-27}$ GeV
$\tilde{H}_{YT} - \tilde{d}_{ZX}$	$(-4.9 \pm 8.9) \times 10^{-27}$ GeV
$-\tilde{H}_{XT} + \tan \eta(\tilde{g}_T - 2\tilde{d}_+ + \tilde{d}_Q)$	$(1.1 \pm 9.2) \times 10^{-27}$ GeV



spin-coupled interactions

$$V = -\vec{\sigma} \cdot \vec{A}$$

$$V = -B \cdot \vec{\sigma} \cdot \vec{v} / c$$



## Antihydrogen Spectroscopy ( $\rightarrow$ J. Walz )

1S–2S frequency difference:

$$\Delta^{H-\bar{H}} \nu_{1S-2S} \approx -(b_3^e - b_3^p) / \pi$$

Ground state HFS frequency difference:

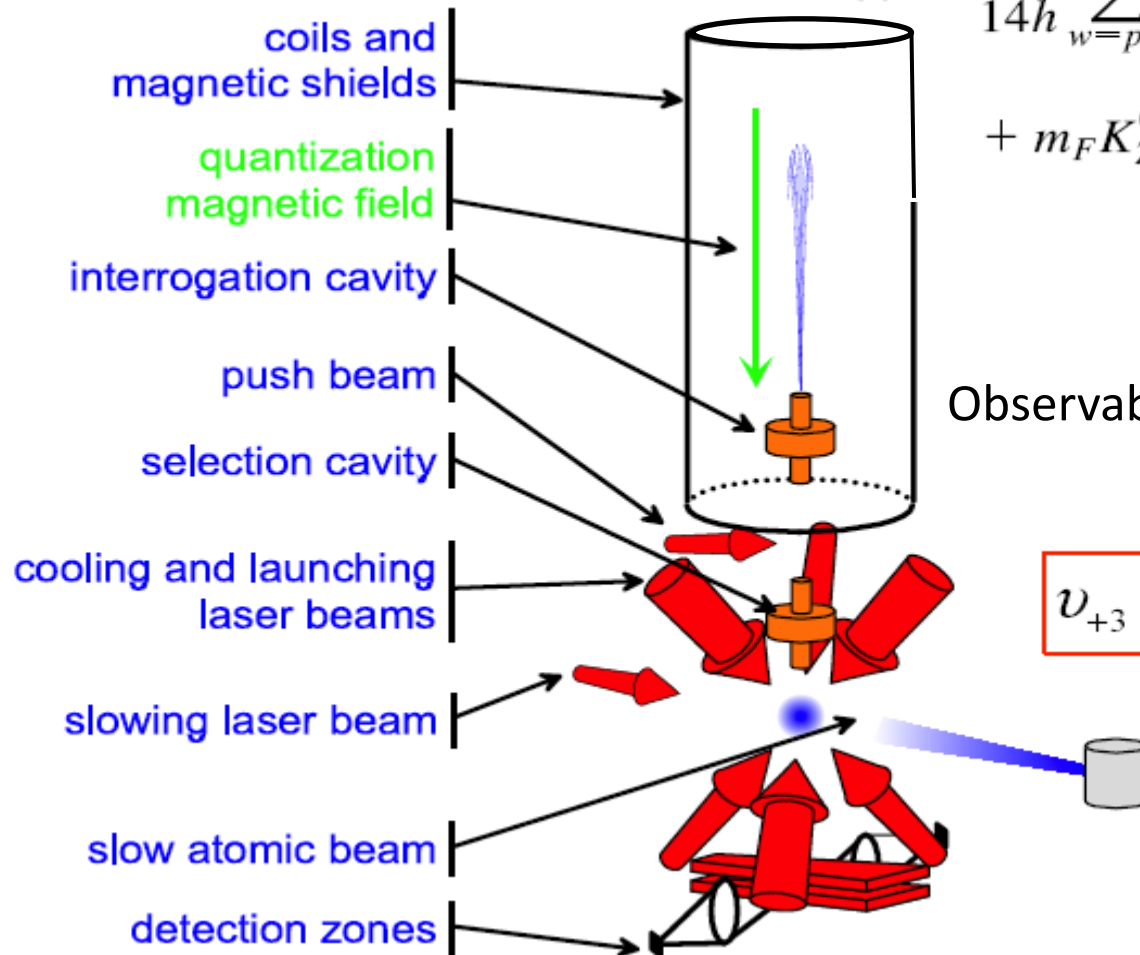
$$\Delta^{H-\bar{H}} \nu_{\text{HFS}} \approx -2b_3^p / \pi$$

# Fundamental physics tests using Rb and Cs fountains

Wolf et al., PRL **96**, 060801 (2006)

Cs  $|3, m_F\rangle \leftrightarrow |4, m_F\rangle$  transition in the SME

$$\delta\nu = \frac{m_F}{14h} \sum_{w=p,e} (\beta_w \tilde{b}_3^w - \delta_w \tilde{d}_3^w + \kappa_w \tilde{g}_d^w) - \frac{m_F^2}{14h} (\gamma_p \tilde{c}_q^p) + m_F K_Z^{(1)} B + \left(1 - \frac{m_F^2}{16}\right) K_Z^{(2)} B^2$$



Observable free of 1st order Zeeman-effect

$$\nu_{+3} + \nu_{-3} - 2\nu_0 = \frac{1}{7h} K_p \tilde{c}_q^p - \frac{9}{8} K_z^{(2)} B^2$$



$$\tilde{c}_q^p = A + C_{\Omega_{\oplus}} \cos(\omega_{\oplus} t) + S_{\Omega_{\oplus}} \sin(\omega_{\oplus} t) + C_{2\Omega_{\oplus}} \cos(2\omega_{\oplus} t) + S_{2\Omega_{\oplus}} \sin(2\omega_{\oplus} t)$$

$\Omega_{\oplus}$  : Earth's orbital motion

$\omega_{\oplus}$  : Earth's rotation frequency

$A, C_i, S_i$ , are functions of the 8 proton components:  $\tilde{c}_Q, \tilde{c}_X, \tilde{c}_Y, \tilde{c}_Z, \tilde{c}_-, \tilde{c}_{TX}, \tilde{c}_{TY}, \tilde{c}_{TZ}$



## RESULTS

(in GeV)

8 proton parameters

$$\tilde{c}_Q = -0.3(2.2) \times 10^{-22}$$

$$\tilde{c}_- = -1.8(2.8) \times 10^{-25}$$

$$\tilde{c}_X = 0.6(1.2) \times 10^{-25}$$

$$\tilde{c}_Y = -1.9(1.2) \times 10^{-25}$$

$$\tilde{c}_Z = -1.4(2.8) \times 10^{-25}$$

$$\tilde{c}_{TX} = -2.7(3.0) \times 10^{-21}$$

$$\tilde{c}_{TY} = -0.2(3.0) \times 10^{-21}$$

$$\tilde{c}_{TZ} = -0.4(2.0) \times 10^{-21}$$

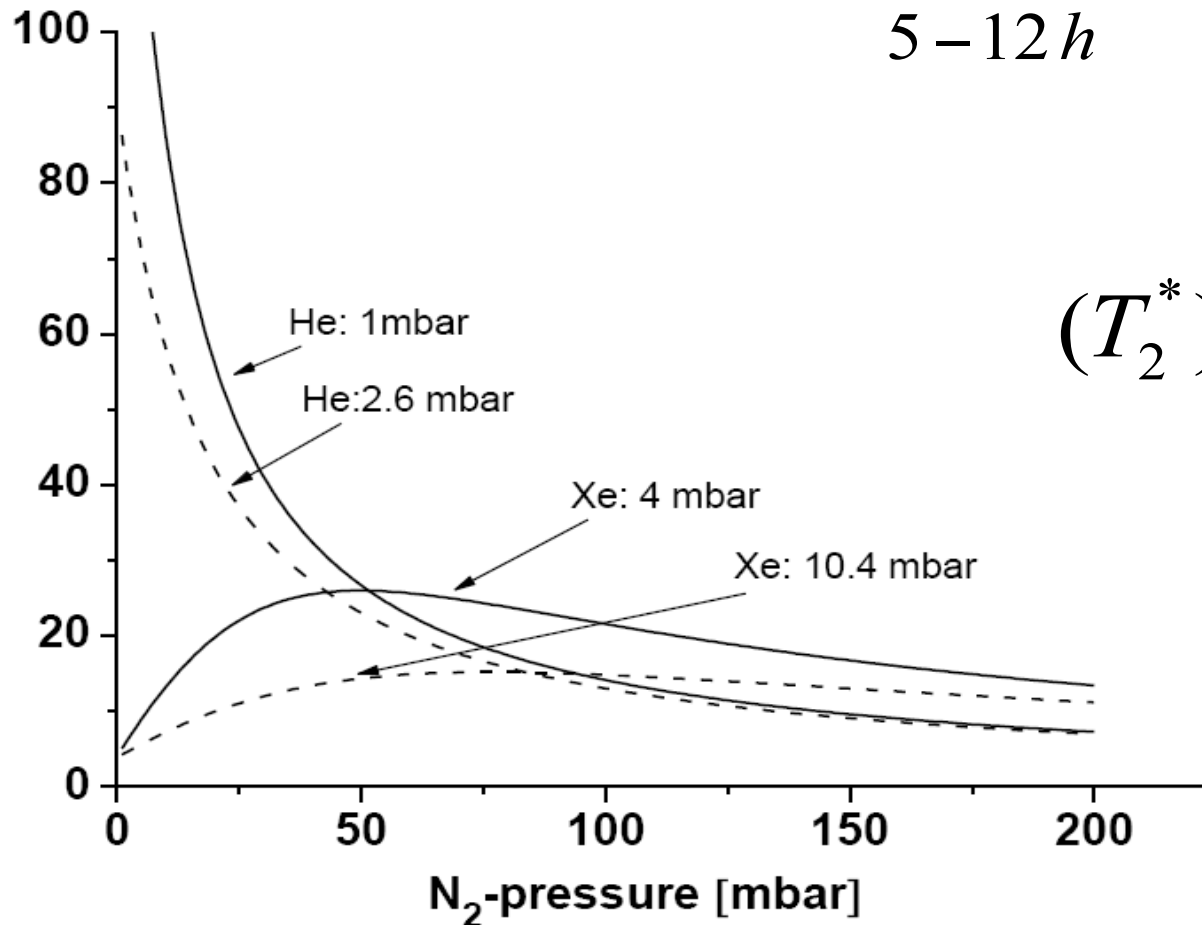
# Relaxation of $^{129}\text{Xe}$

$$\frac{1}{T_2^*} = \frac{1}{T_{1,\text{wall}}} + \frac{1}{T_{1,\text{vdW}}} + \frac{1}{T_{2,\text{field}}}$$

$5 - 12 h$

$$\frac{1}{4.1h} \cdot \frac{1}{(1 + 1.05 \cdot [N_2]/[Xe])}$$

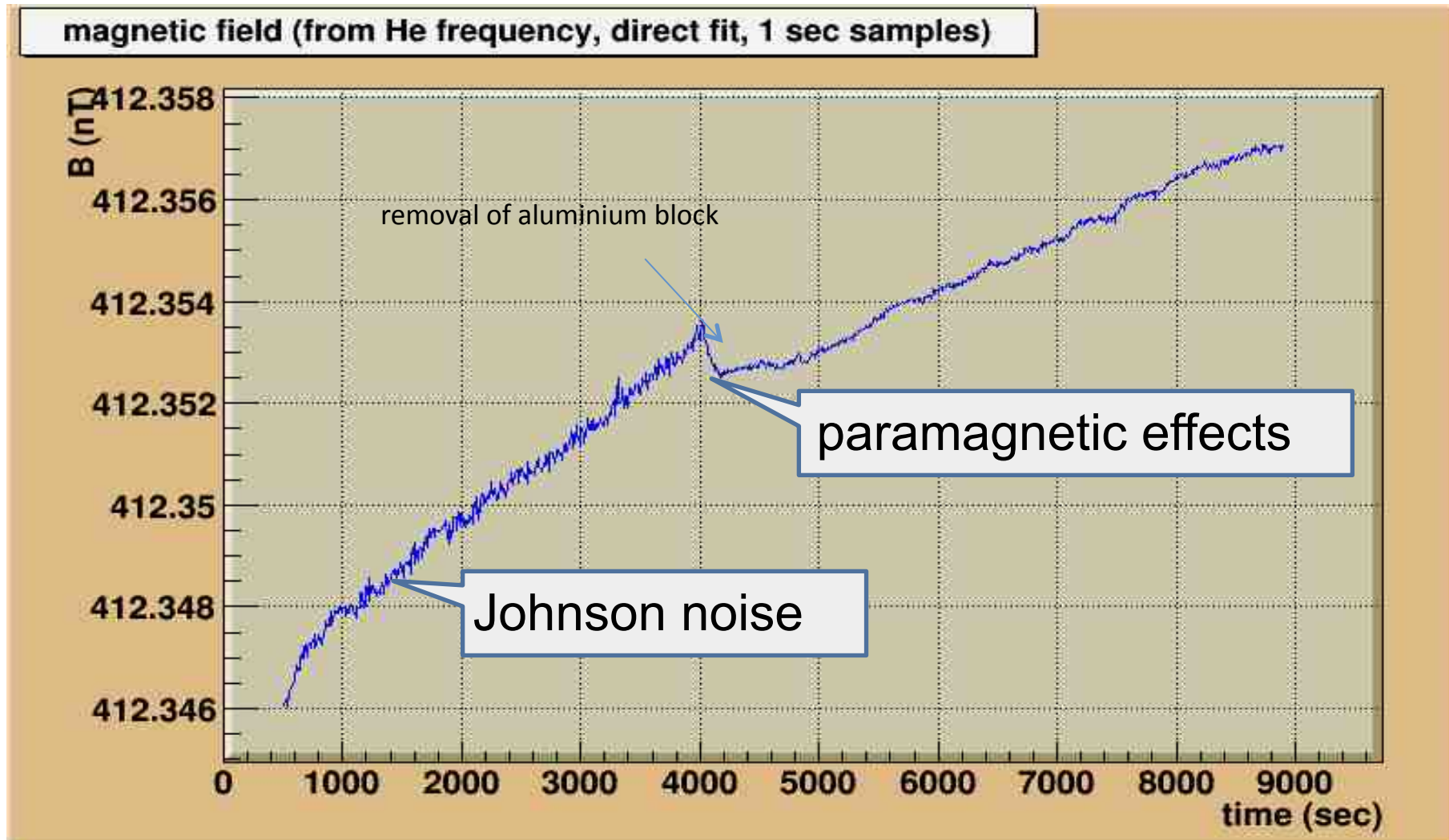
$$\left( \frac{1}{T_{1,\text{vdW}}} + \frac{1}{T_{2,\text{field}}} \right)^{-1} [h]$$



$$(T_2^*)_{Xe} \approx 3 - 6 h$$

*(measured)*

Magnetic field (measured via the He spin precession signal )  
in presence of a conductor  
( aluminium cylinder : diameter 56 mm, length 70 mm)



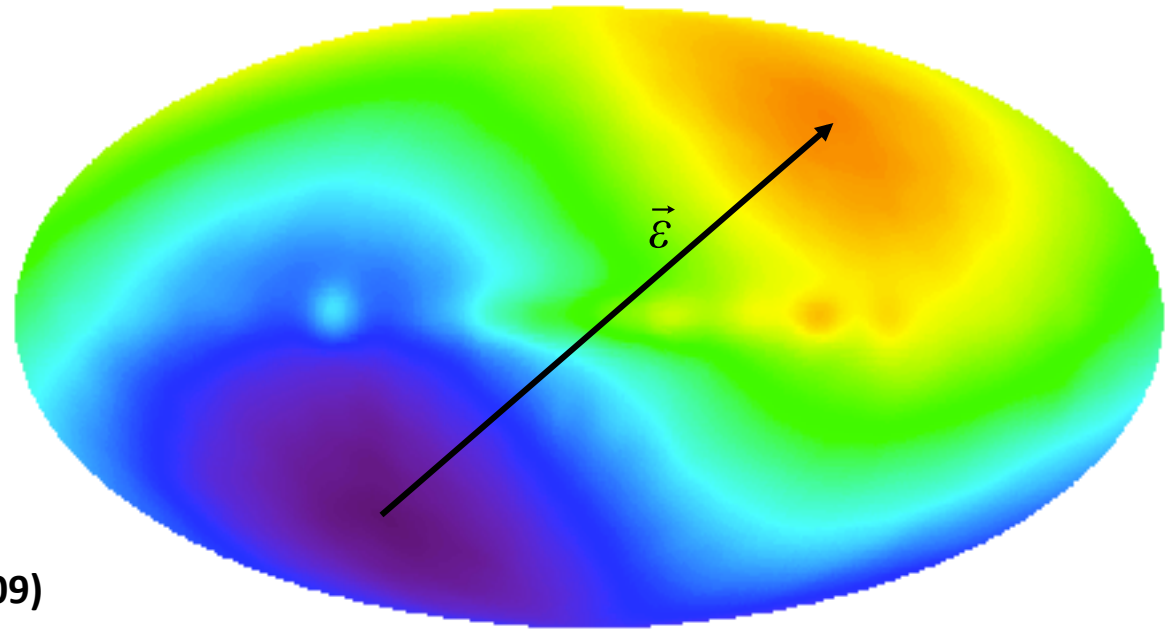


# CMB dipole

$$v = 368 \text{ km/s}$$
$$\Delta T_{\text{dip}} \approx 3.3 \text{ mK}$$

## galactic coordinate system

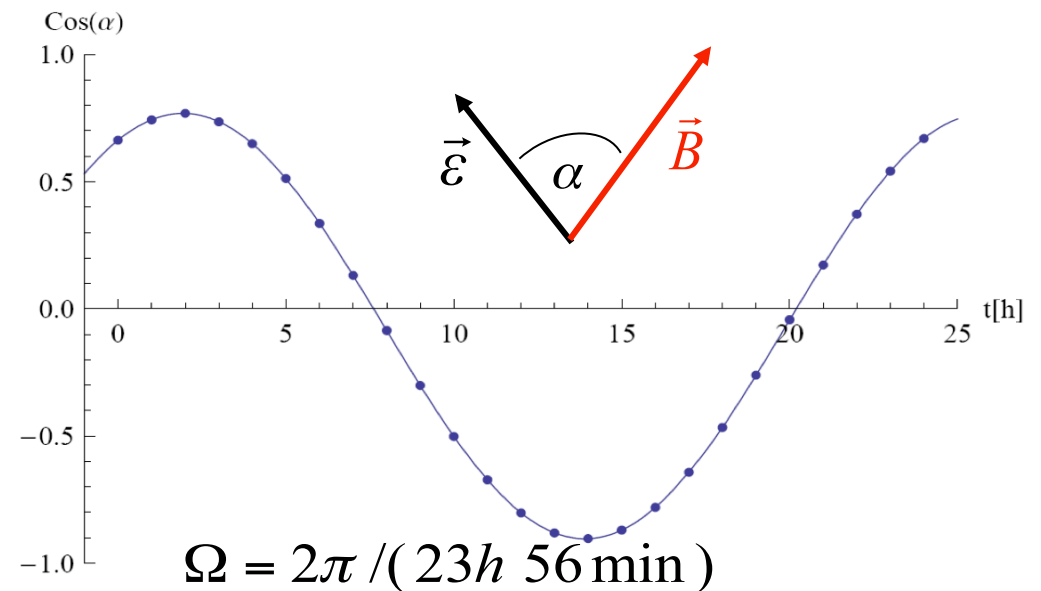
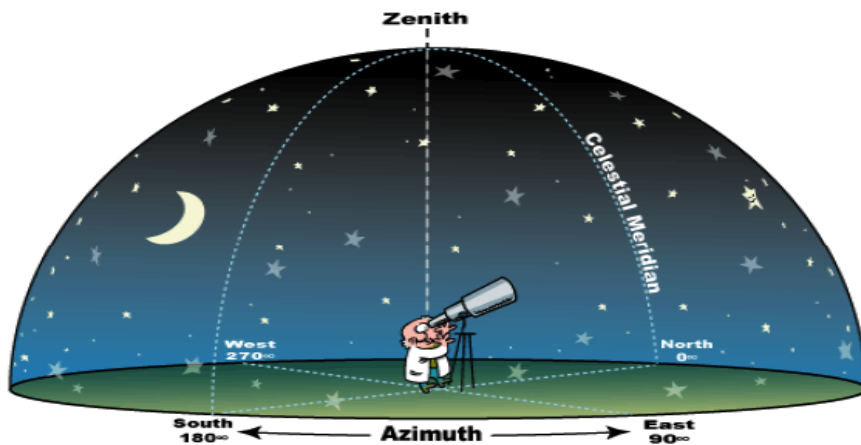
$$(l, b) = (264^{\circ}.31 \pm 0^{\circ}.04 \pm 0^{\circ}.16, +48^{\circ}.05 \pm 0^{\circ}.02 \pm 0^{\circ}.09)$$



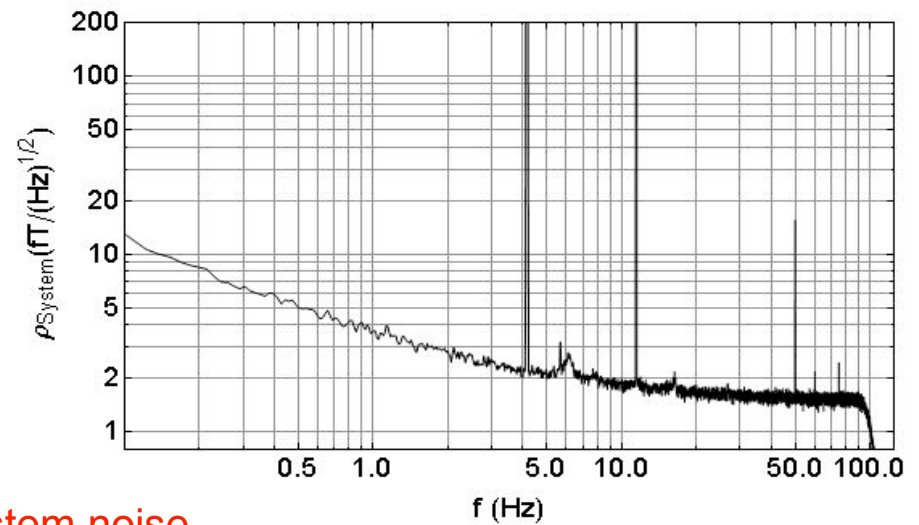
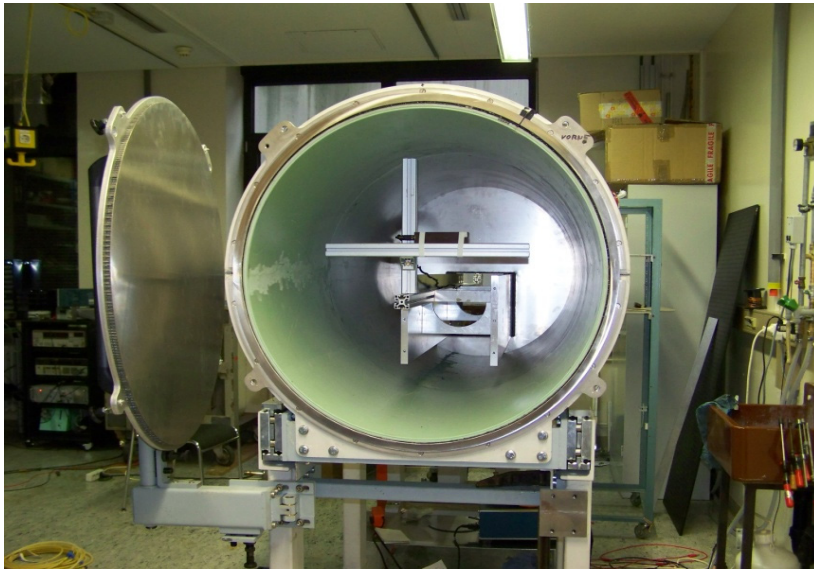
measurement on 01.10.2007 at  
PTB-Berlin ( $52^{\circ} 31'$  north,  $13^{\circ} 25'$  east)

## horizon coordinate system

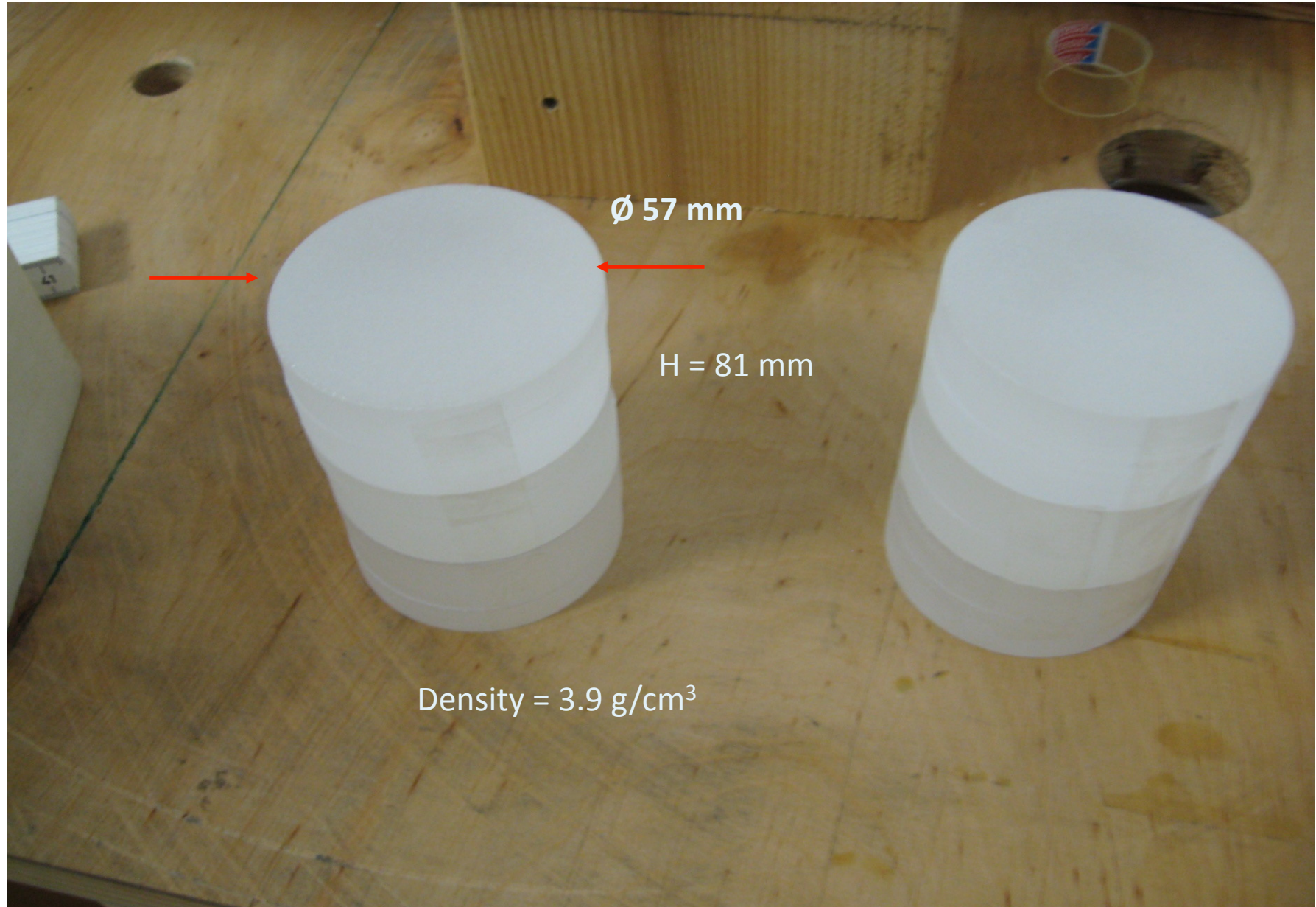
(observer's local horizon)



## Prototype of cylindrical $\mu$ -metal shield

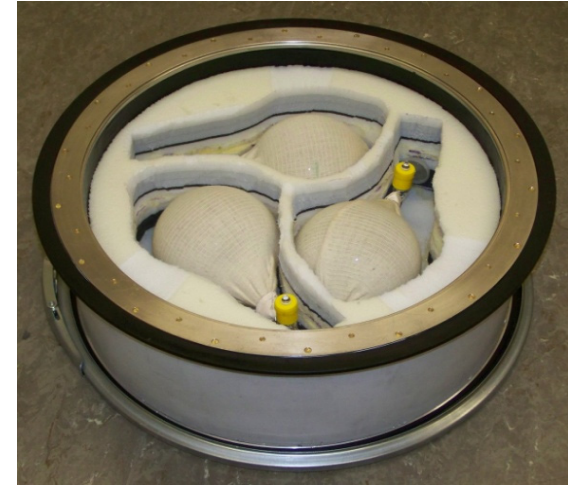
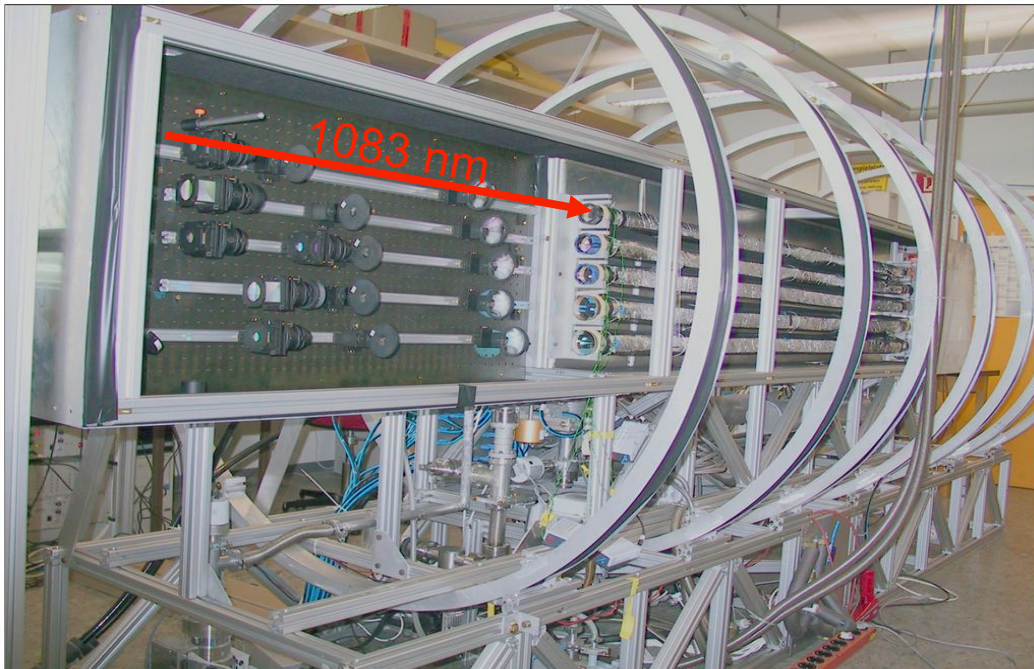


no elevated system noise  
inside inner shield made out  
of metglas (amorphous metal alloy ribbon)

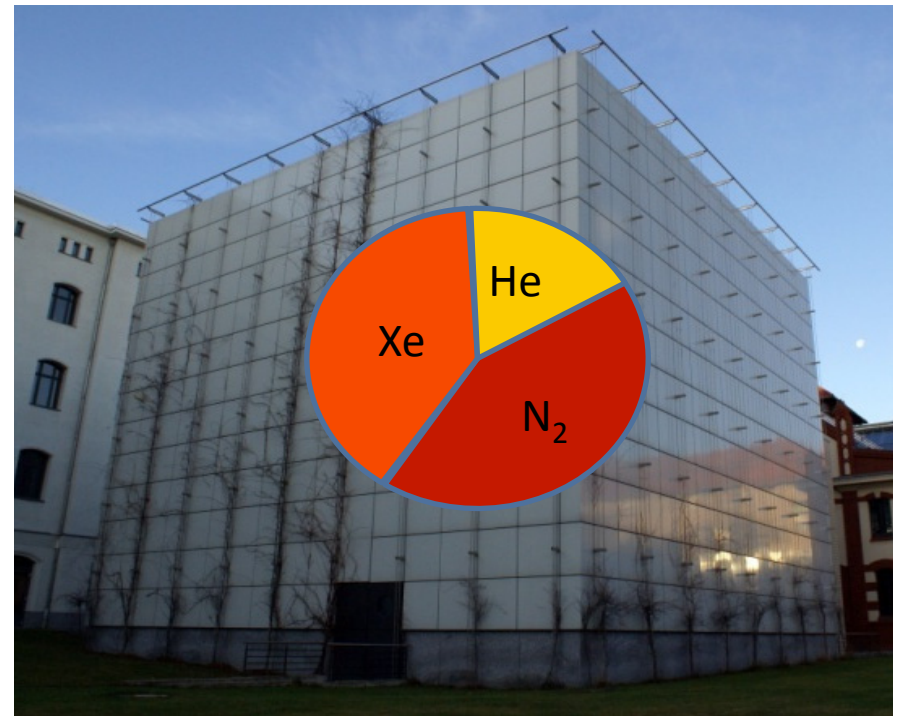
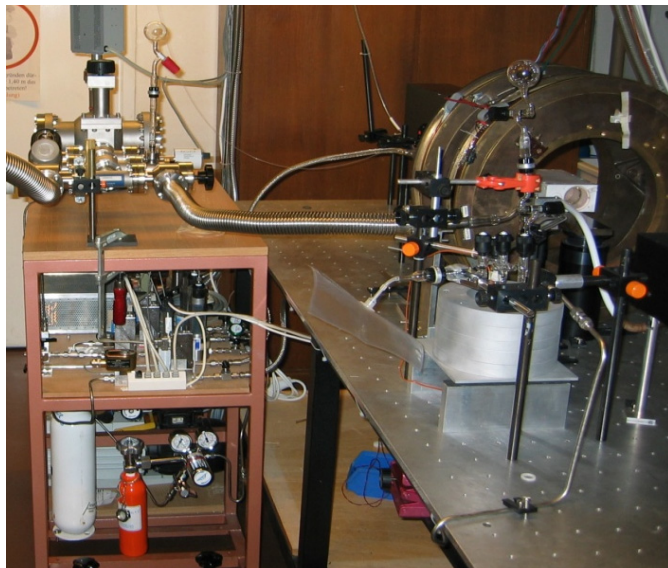


**Lead glass samples**

# MEOP Polarizer Mainz: $^3\text{He}$

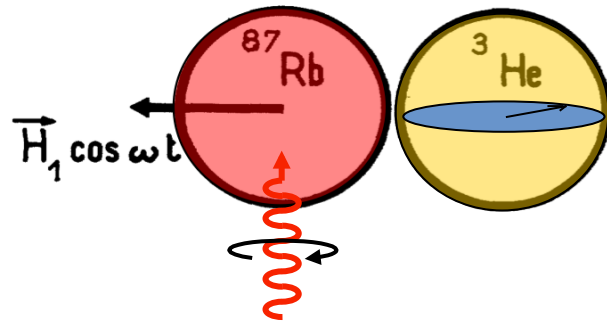


# SEOP Polarizer PTB: Xe



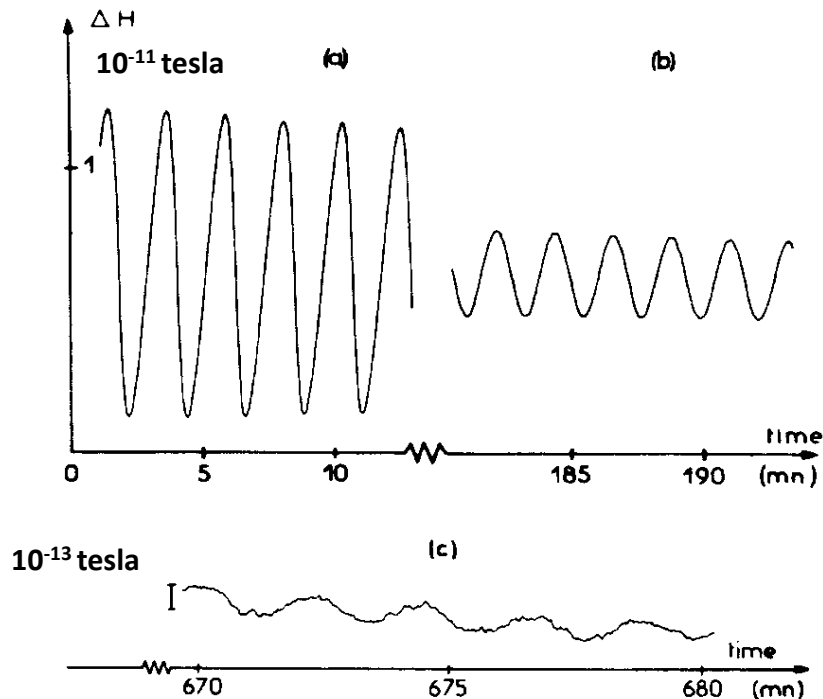
# Detection of magnetic field produced by oriented nuclei

(Cohen-Tannoudji et al., PRL 22 (1969),758)



## Results:

- $^3\text{He}$  spin precession:  $T_2^* = 2\text{h } 20\text{min}$
- sensitivity of Rb-magnetometer:  
100fT@ BW 0.3 Hz
- $P_{\text{He}} \approx 5\% @ 4 \text{ mbar}$

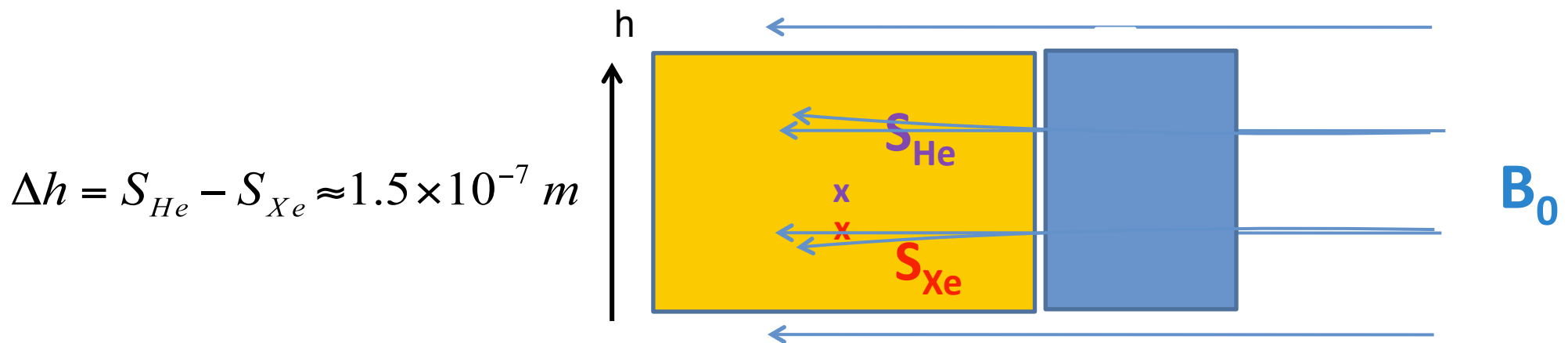


## Improvement of measurement sensitivity:

- SQUID-detectors@2 fT/ $\sqrt{\text{Hz}}$
- laser for OP of  $^3\text{He}$  @  $P > 70\%$
- longer  $T_2^*$ -times (needed !!!)

# False effects :

Barometric formula :  $p(h) = p^0 \exp\left(\frac{-h}{h^0}\right)$ .  $h^0 = \frac{RT}{Mg}$



assume:  $\Delta \left( \frac{\partial B}{\partial h} \right) \approx 20 \frac{pT}{cm}$

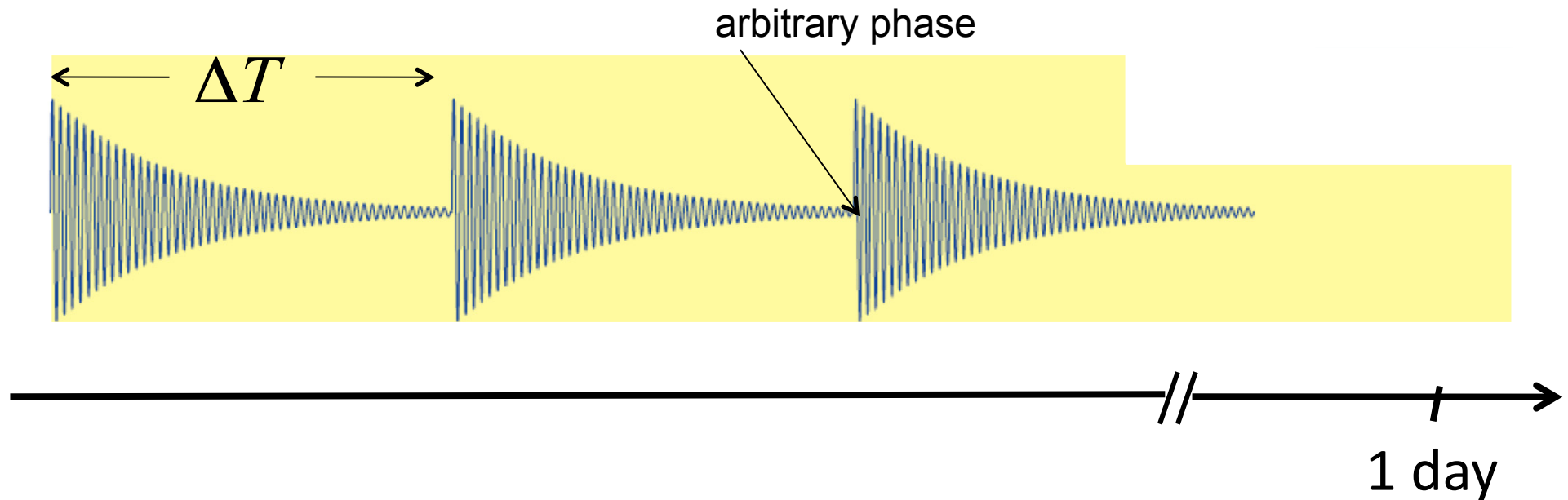
$$\Rightarrow \Delta B \approx 0.3 \text{ f T} \Rightarrow \Delta \nu \approx 10 \text{ nHz}$$

drops out in  $\delta \nu = \frac{1}{2} (\Delta \nu_{\text{right sample}} - \Delta \nu_{\text{left sample}}) = (4.8 \pm 7.0 \pm 0.4) \text{ nHz}$

From the measured value of  $\delta \nu$  we get:

$$g_S g_P < 4 (2\pi)^2 m_{3He} \delta \nu / (NV \hbar \langle V^*(\lambda) \rangle)$$

# Gain in sensitivity compared to measurements with short coherence times:



$$\sigma_v \propto \left( \frac{1}{\Delta T^{3/2}} \right) \sqrt{n} = \left( \frac{1}{T^{3/2}} \right) \frac{T}{\Delta T} \quad \left( \text{with : } n = \frac{T}{\Delta T} \right)$$

Example „short spin coherence time“:

$\Delta T = 5 \text{ min} \rightarrow \approx 300 \times \text{less sensitive !}$