

# Bottomonium results and prospects at Belle II

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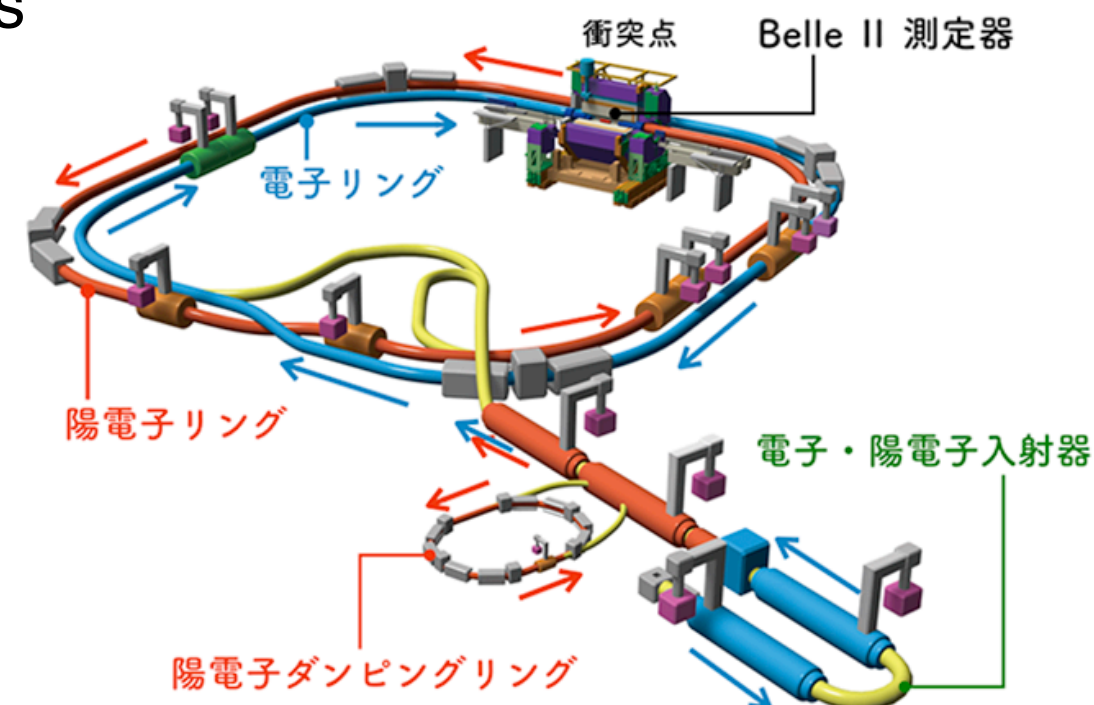
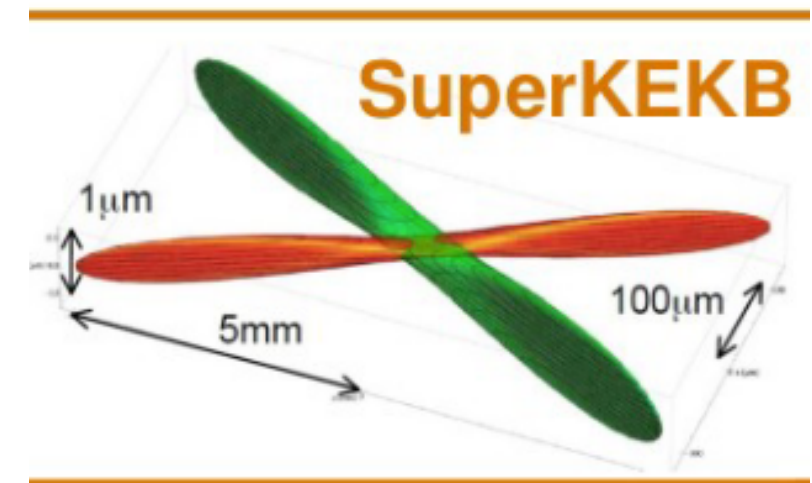
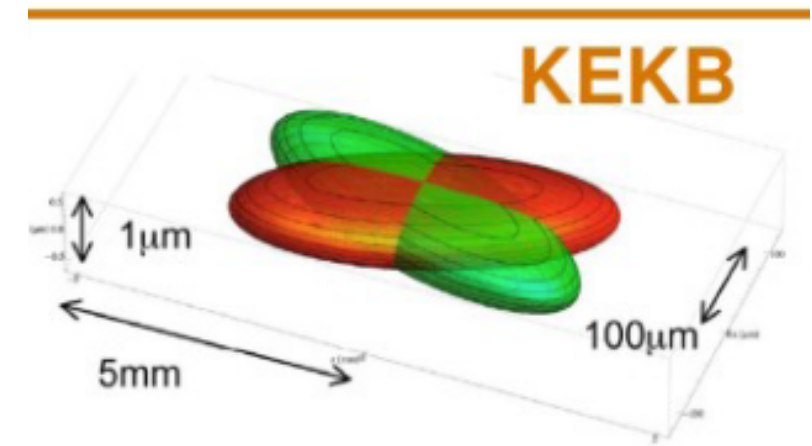
**Fairness 2022**  
**23-27 May 2022**

On behalf of the Belle II collaboration

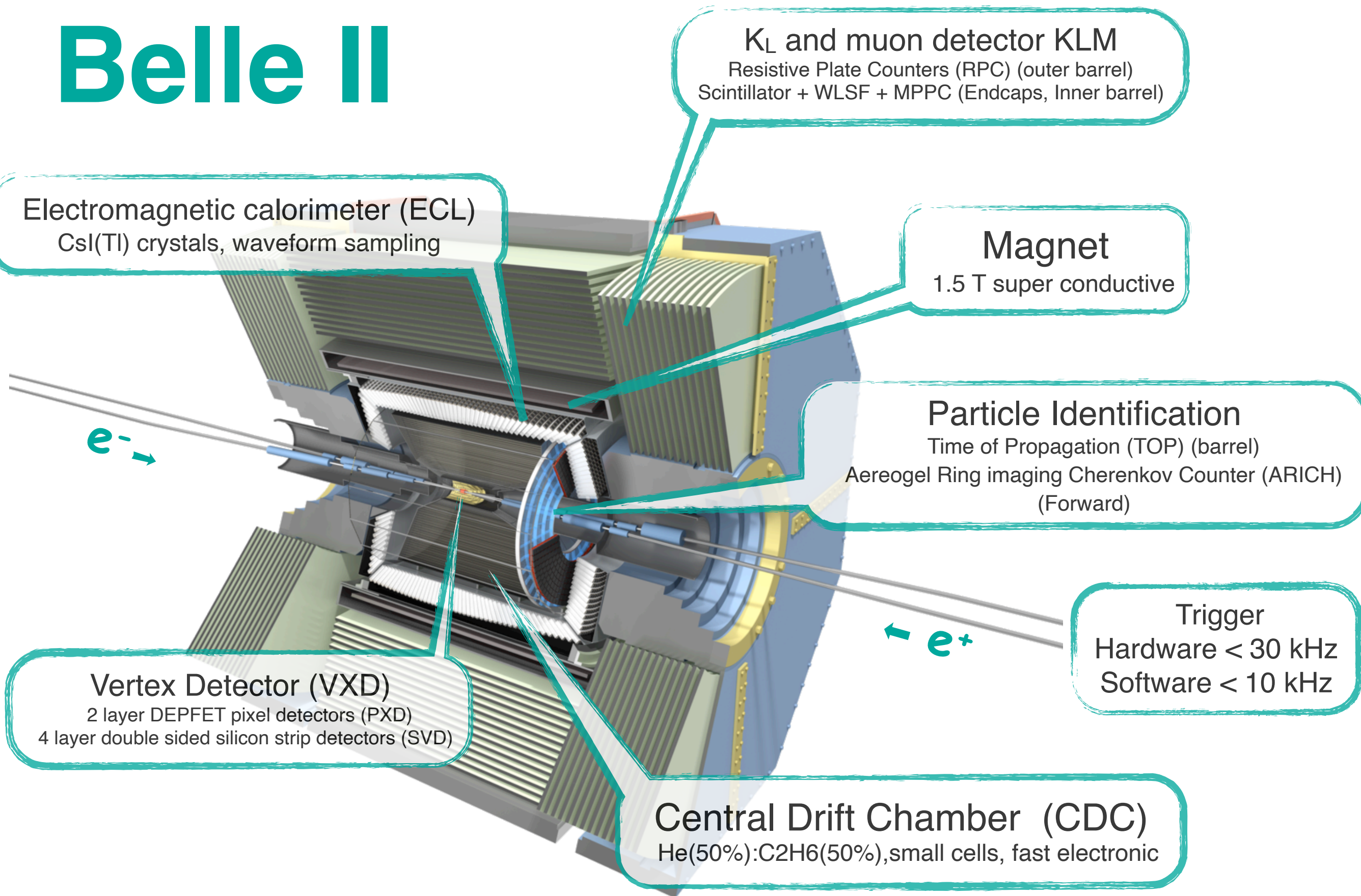


# SuperKEKB

- ▶ SuperKEKB is an asymmetric  $e^+$  (4 GeV)  $e^-$  (7 GeV) collider at Tsukuba, Japan.
- ▶ Energy limit  $\sim 11$  GeV
- ▶ Belle II detector is placed around the IP of SuperKEKB
- ▶ SuperKEKB goal:  $> \sim 40 \times$  KEKB instantaneous luminosity at cost of  $\mathcal{O}(10) \times$  higher backgrounds
  - Goal:  $\mathcal{L} = 6.5 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$
- ▶ Current world record:  $\mathcal{L} = 4.1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ 
  - May 2022 !!
- ▶ First collision physics runs in 2019.



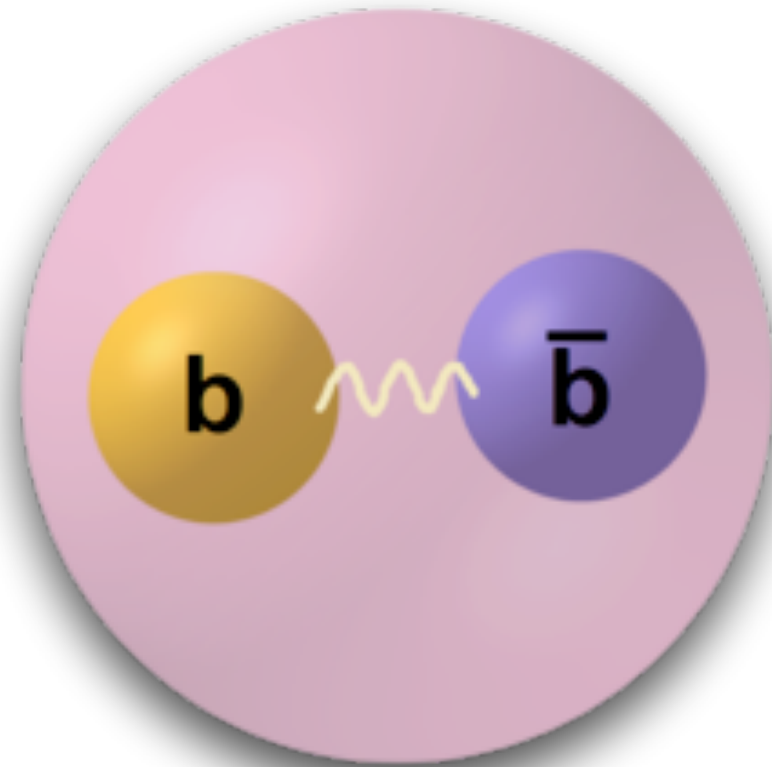
# Belle II





# Quarkonium

- ▶  $Q\bar{Q}$  meson with a heavy quark
  - $b\bar{b}$  Bottomonium
  - $c\bar{c}$  Charmonium
- ▶ Simple two body system
- ▶ Non-relativistic
  - $v_b^2 \sim 0.1 c$  ,  $v_c^2 \sim 0.3 c$
- ▶ Multiscale system covering all regimes of quantum chromodynamics (QCD)
  - Ideal framework to test Non-perturbative QCD and its interplay with perturbative QCD
- ▶ Bottomonium is simpler than charmonium





# Quarkonium

►  $Q\bar{Q}$  meson with a heavy quark

- $b\bar{b}$  Bottomonium

- $c\bar{c}$  Charmonium

► Simple two body system

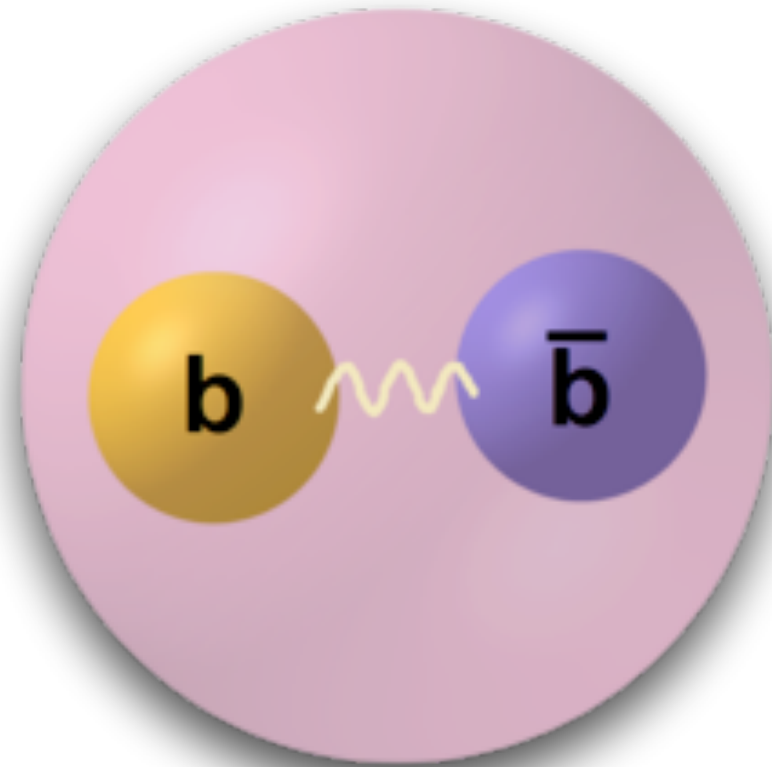
► Non-relativistic

► Mu

**Exotic quarkonium states, such hybrids,  
Tetraquark and molecules are usually  
studied/included in this category**

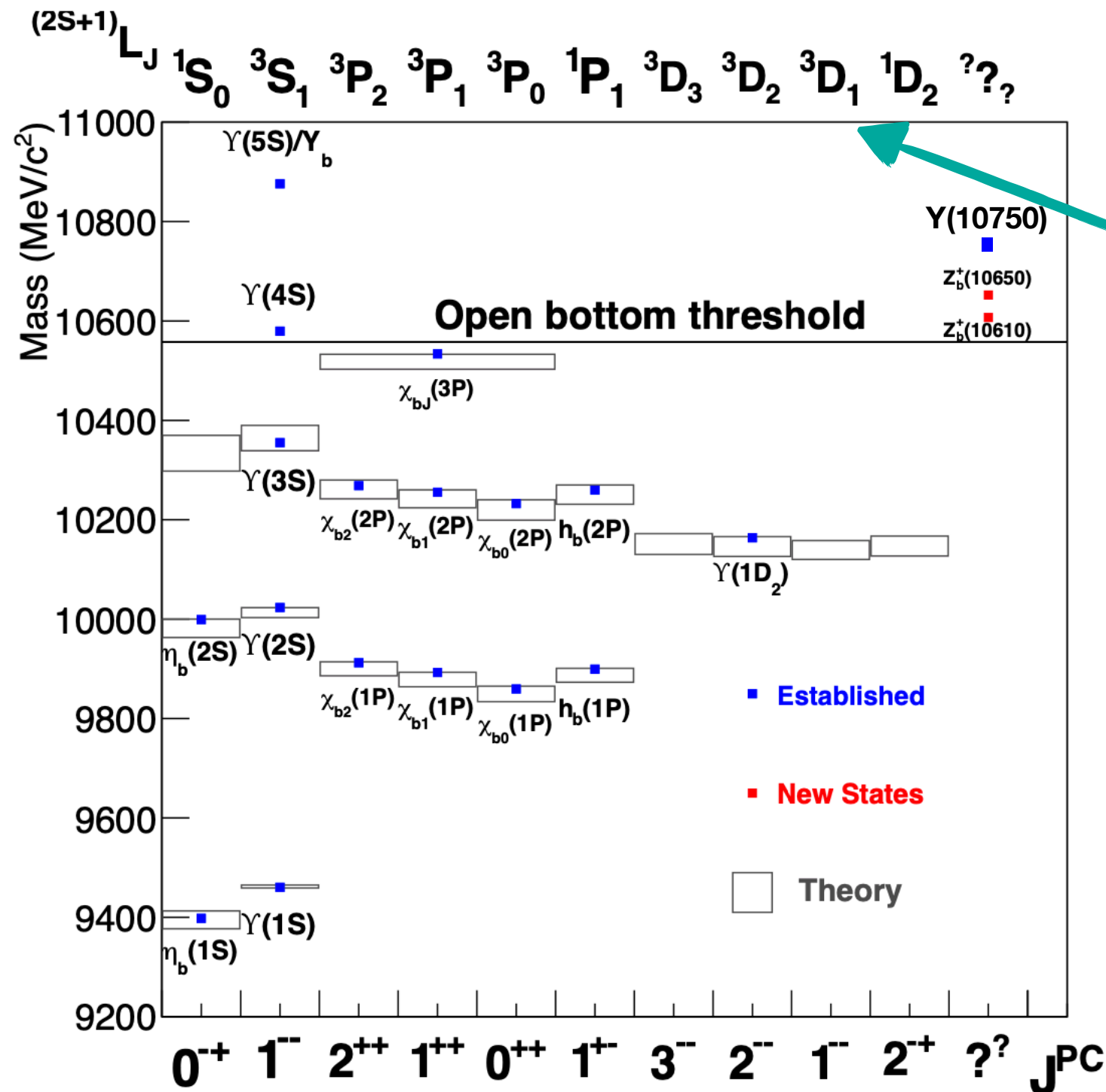
perturbative QCD

► Bottomonium is simpler than charmonium



(CD)

# Bottomonia

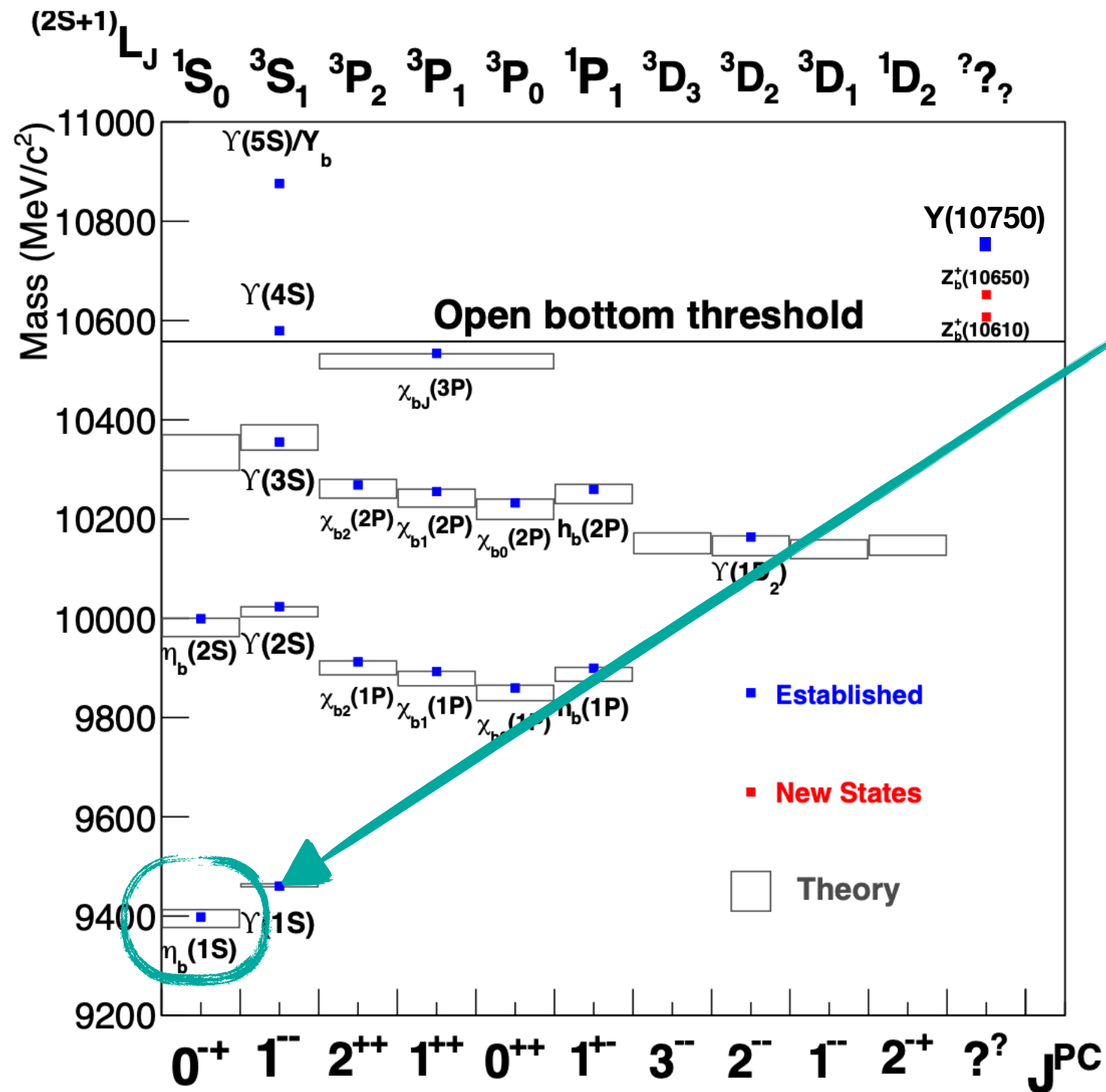


Spectroscopic notation  
from Schrödinger  
equation solutions

$$n(2S+1)L_J$$

- $n$  radial quantum number
- $S$  total spin of  $q\bar{q}$  system
- $L$  relative orbital ang. momentum
- $L = 0, 1, 2 \dots$  correspond to S, P, D
- $J = L + S$
- Parity  $P = (-1)^{L+1}$
- Charge Conj.  $C = (-1)^{L+S}$

# Bottomonia

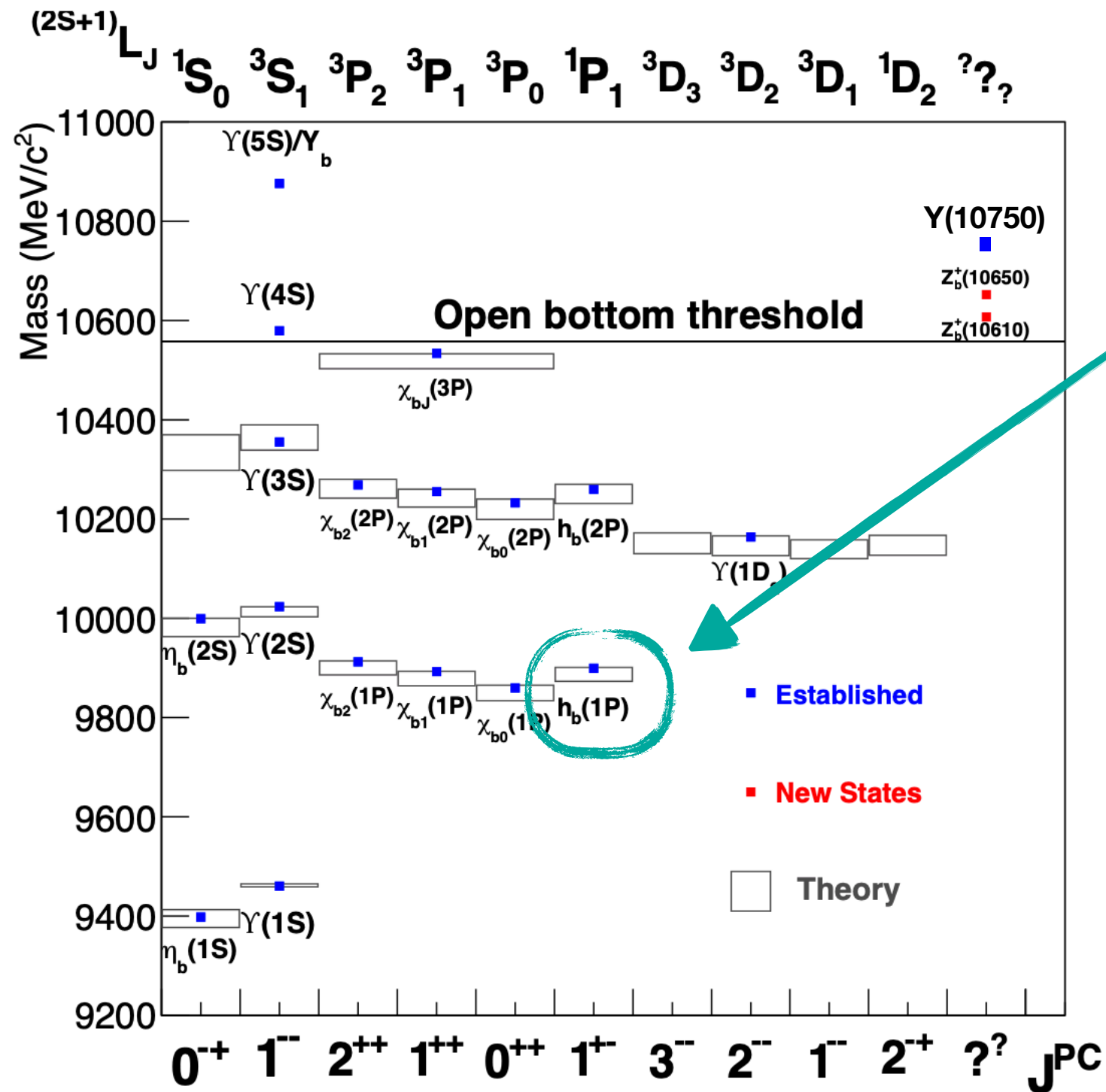


Ground state  
spin singlet S wave

$\eta_b(1S)$



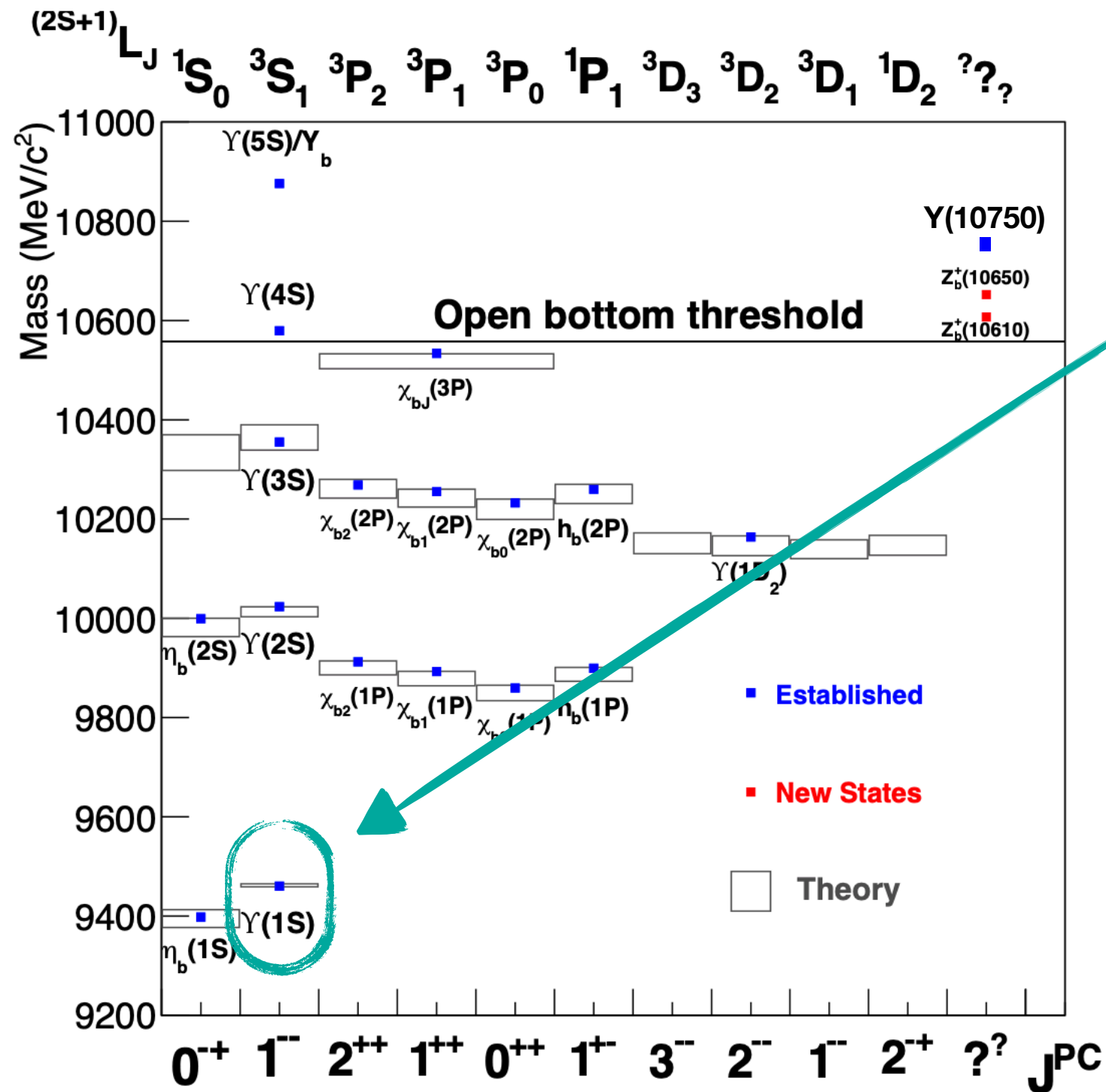
# Bottomonia



spin singlet P wave

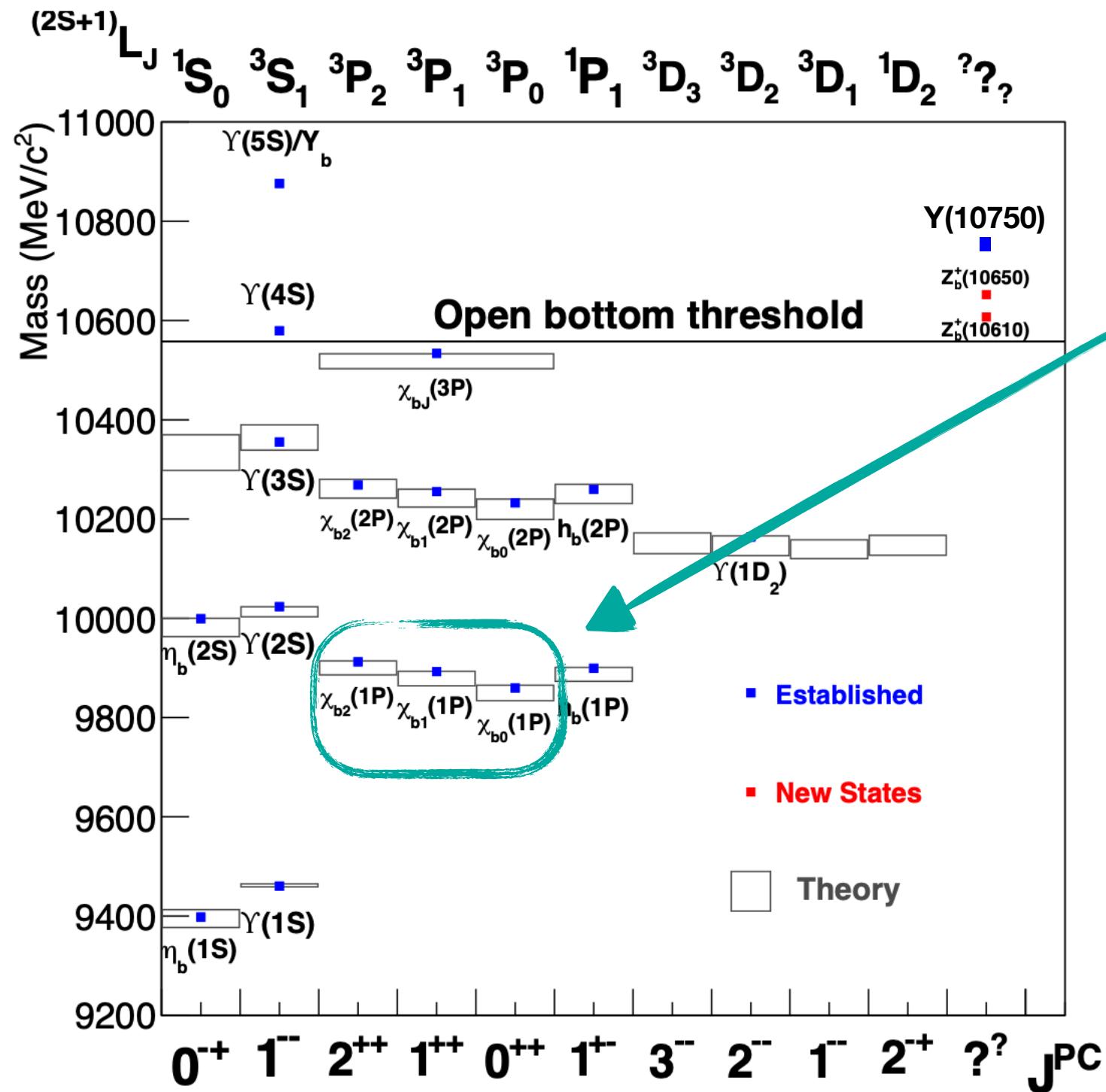
**$h_b(1P)$**

# Bottomonia



Hyper fine splitting  
spin triplet S wave  
 **$\Upsilon(1S)$**

# Bottomonia

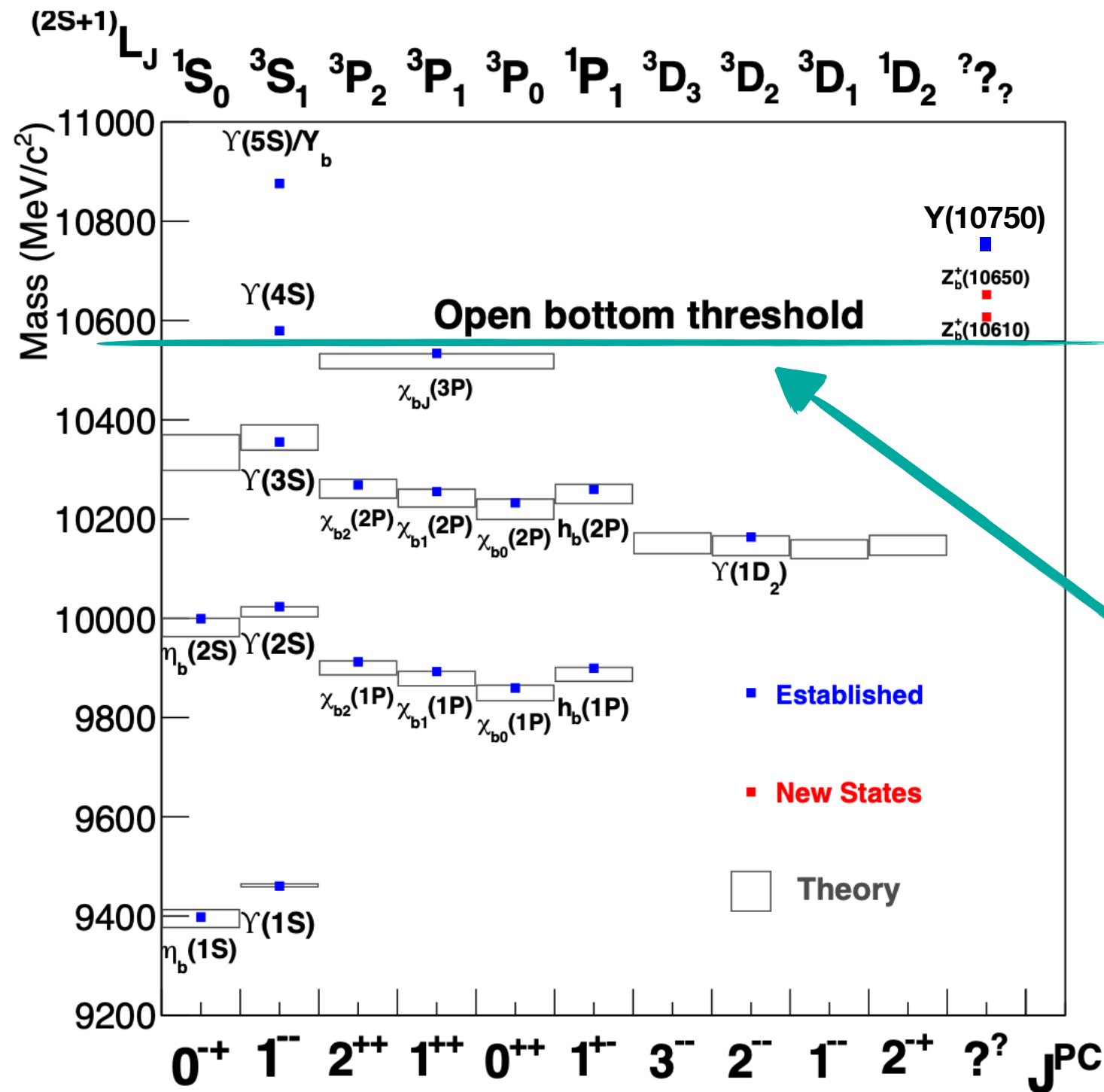


Fine splitting  
P wave spin triplet

$\chi_{b1,2,3}(1P)$



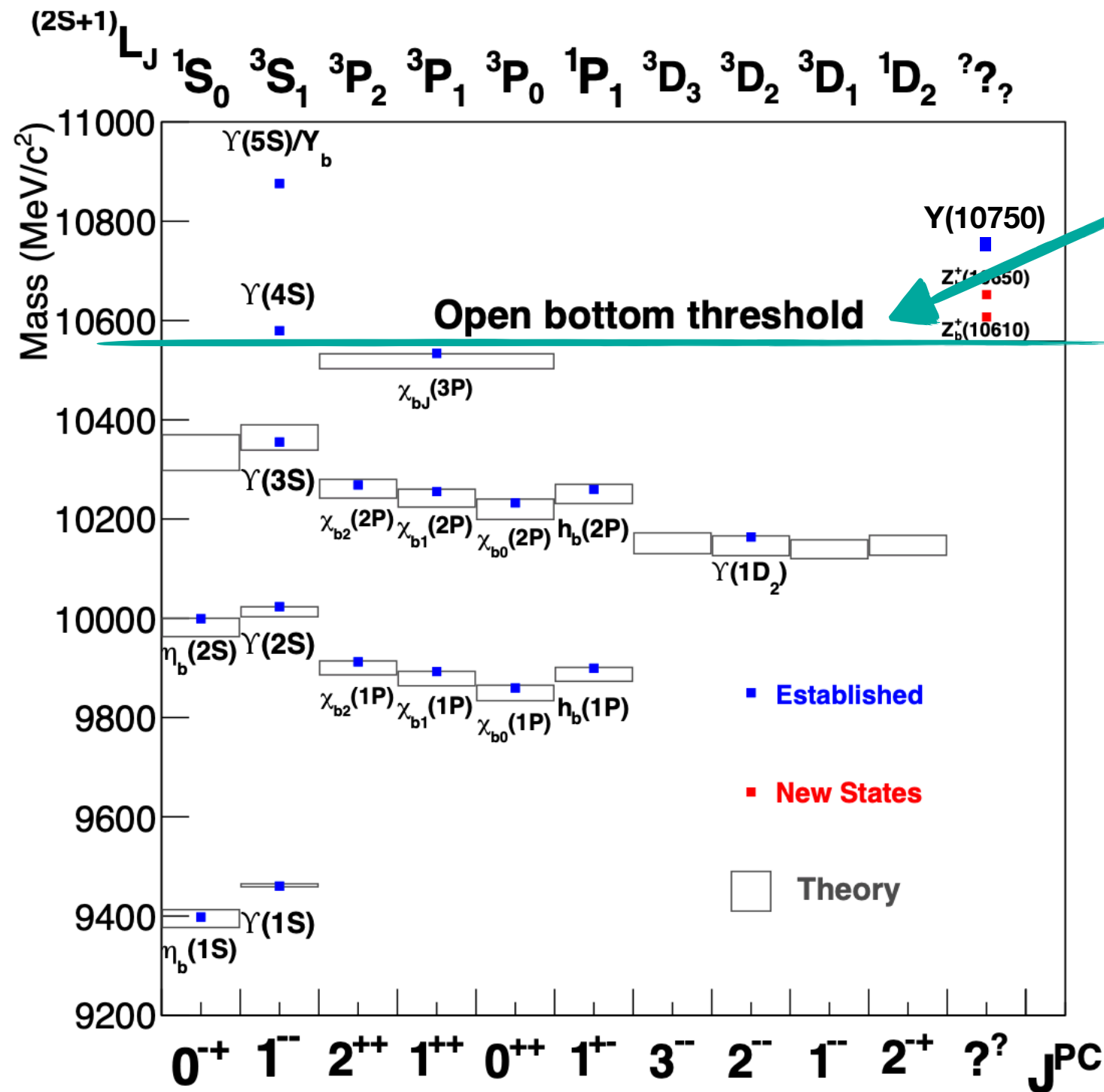
# Bottomonia



States below open flavour thresholds ( $B\bar{B}$ ) are in good agreement with a simple no relativistic  $Q\bar{Q}$  system.

Are generally narrow due to OZI rule  
 $\Gamma \sim 20\text{-}50 \text{ KeV}$

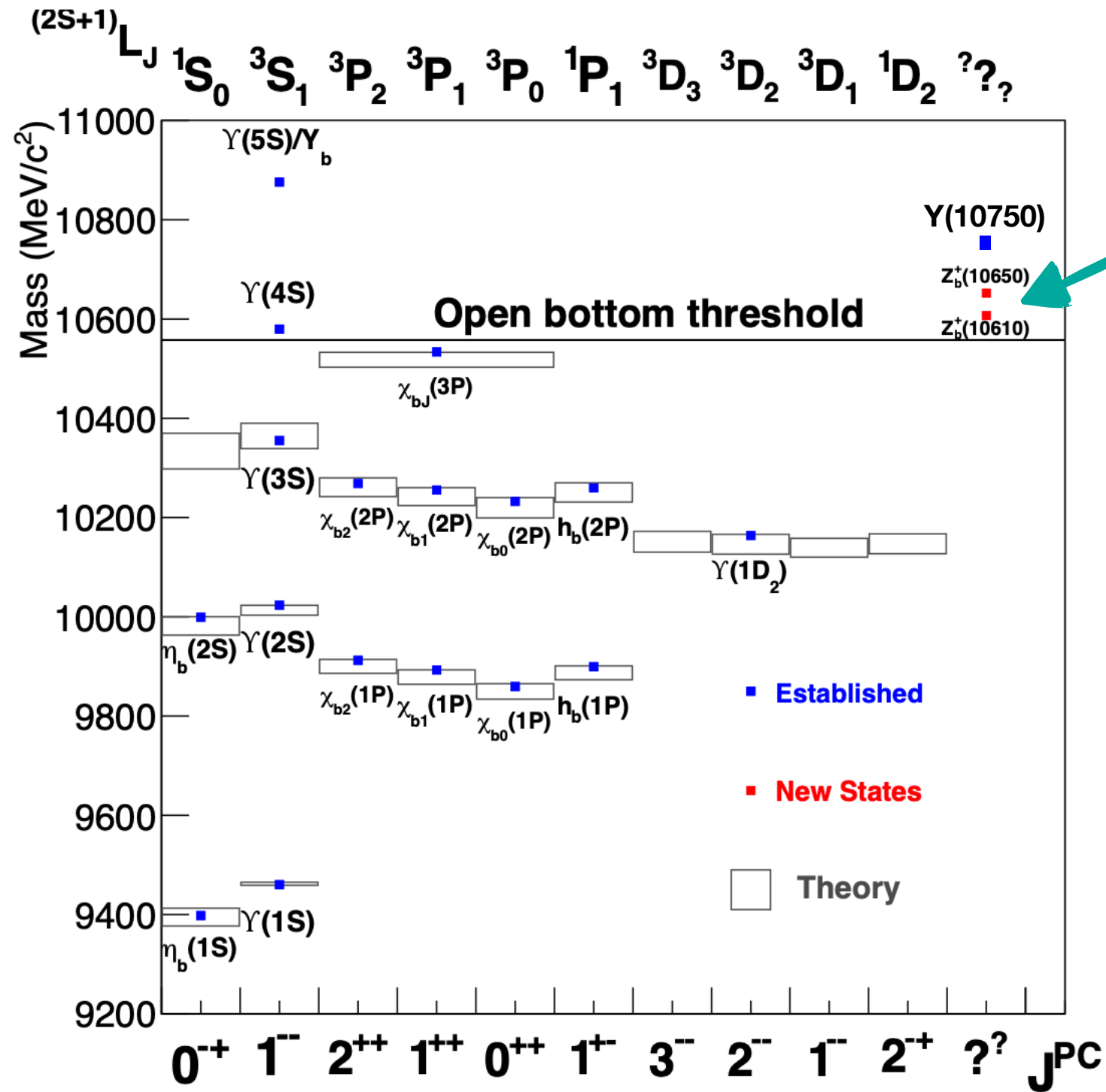
# Bottomonia



States with masses above open flavour thresholds have properties unexpected for a pure  $Q\bar{Q}$  state

Decay mostly to  $B^{(*)}B^{(*)}$  and are usually much larger  
 $\Gamma \sim 20\text{-}40 \text{ MeV}$

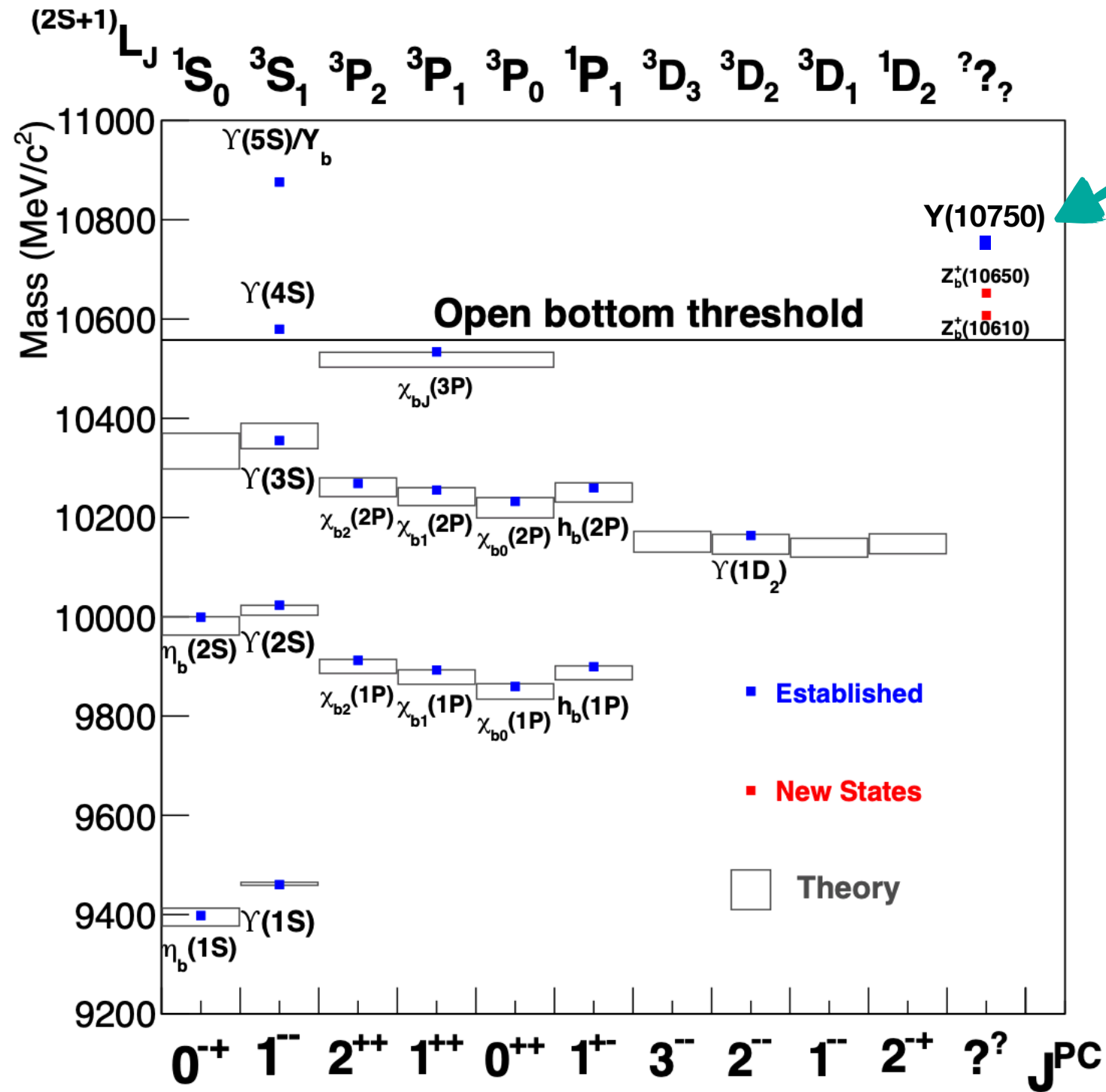
# Bottomonia



Exotic states  
 $Z_b^\pm(10650)$   
 $Z_b^\pm(10610)$



# Bottomonia



2019 new state with  
J<sup>PC</sup>=1<sup>--</sup>  
Details later

# How to produce them at $e^+e^-$ collider

## ► Directly from $e^+e^-$

- Only  $J^{PC}=1^{--}$  ( $\Upsilon(nS)$ )

## ► ISR production

- Only  $J^{PC}=1^{--}$  ( $\Upsilon(nS)$ )

## ► Hadronic transitions from $\Upsilon(nS)$ through $\eta, \pi\pi, \dots$

- $J^{PC}=1^{--}, 0^{-+}, 1^{+-} \dots$  ( $\Upsilon(nS), h_b(nS), \eta_b(nS), \dots$ )

## ► Radiative transitions from $\Upsilon(nS)$

- $J^{PC} = 0^{++}, 1^{++}, 2^{++}$  ( $\chi_{bj}$ )

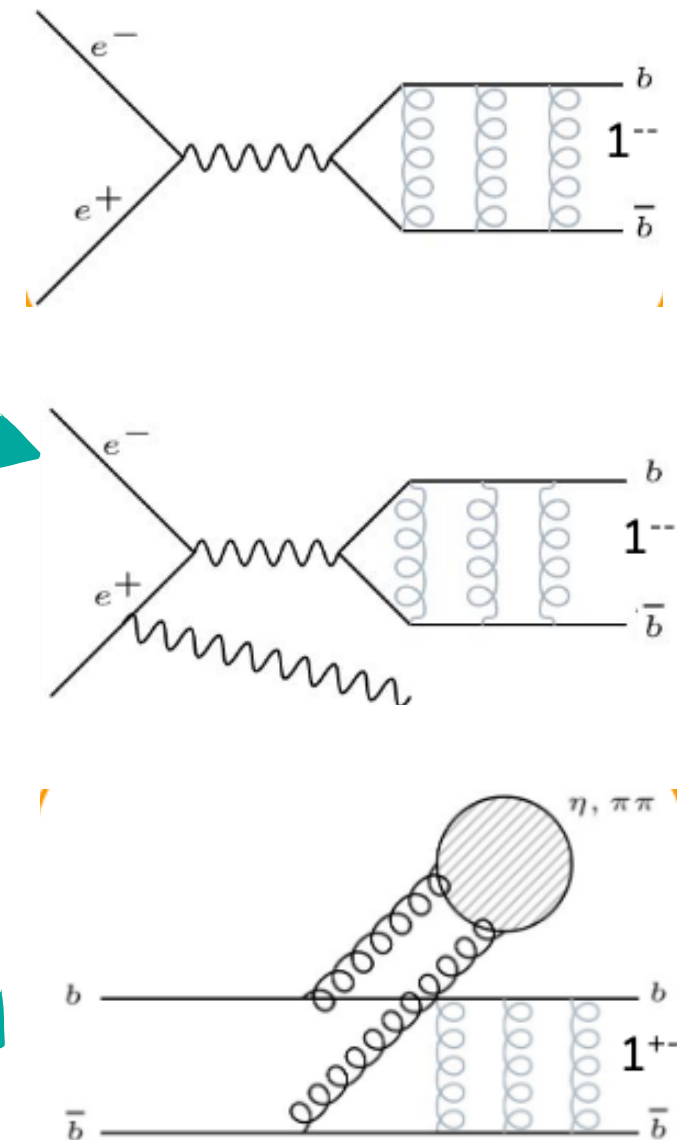
- Electric dipole transition (E1)

- $J^{PC} = 0^{-+}$  ( $\eta_b$ )

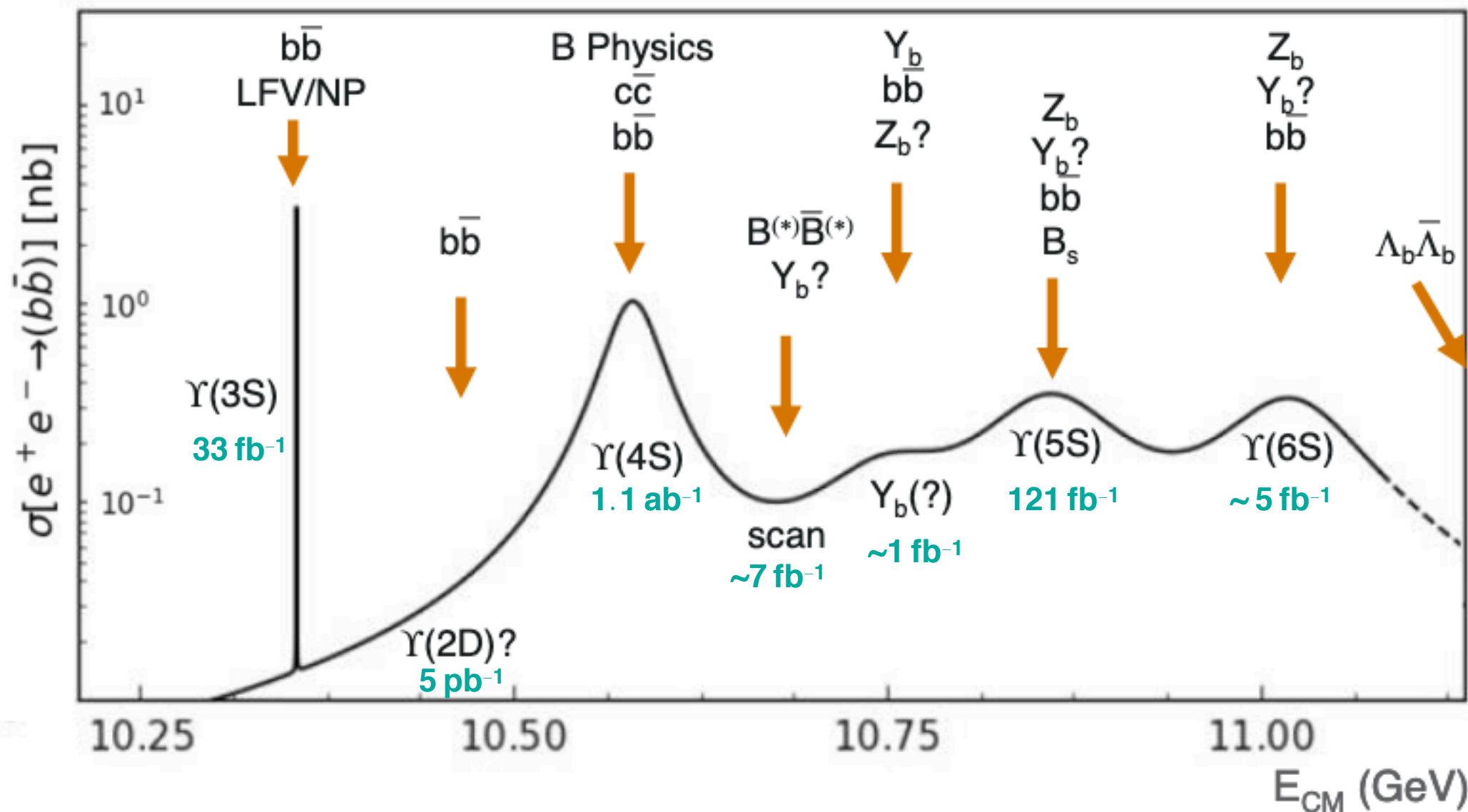
- Magnetic dipole (M1) transitions

## ► Secondary transition from these states

- E.g.  $h_b(nS) \rightarrow \gamma \eta_b$



# Available datasets before Belle II



- Small dataset outside  $\Upsilon(4S)$
- Even a small data set can make the difference



CLEO



# Belle II current status

## ▶ Running at $\Upsilon(4S)$

- Recorded  $387 \text{ fb}^{-1}$

- Many analyses already ongoing, just need more data

- Rediscovery analyses

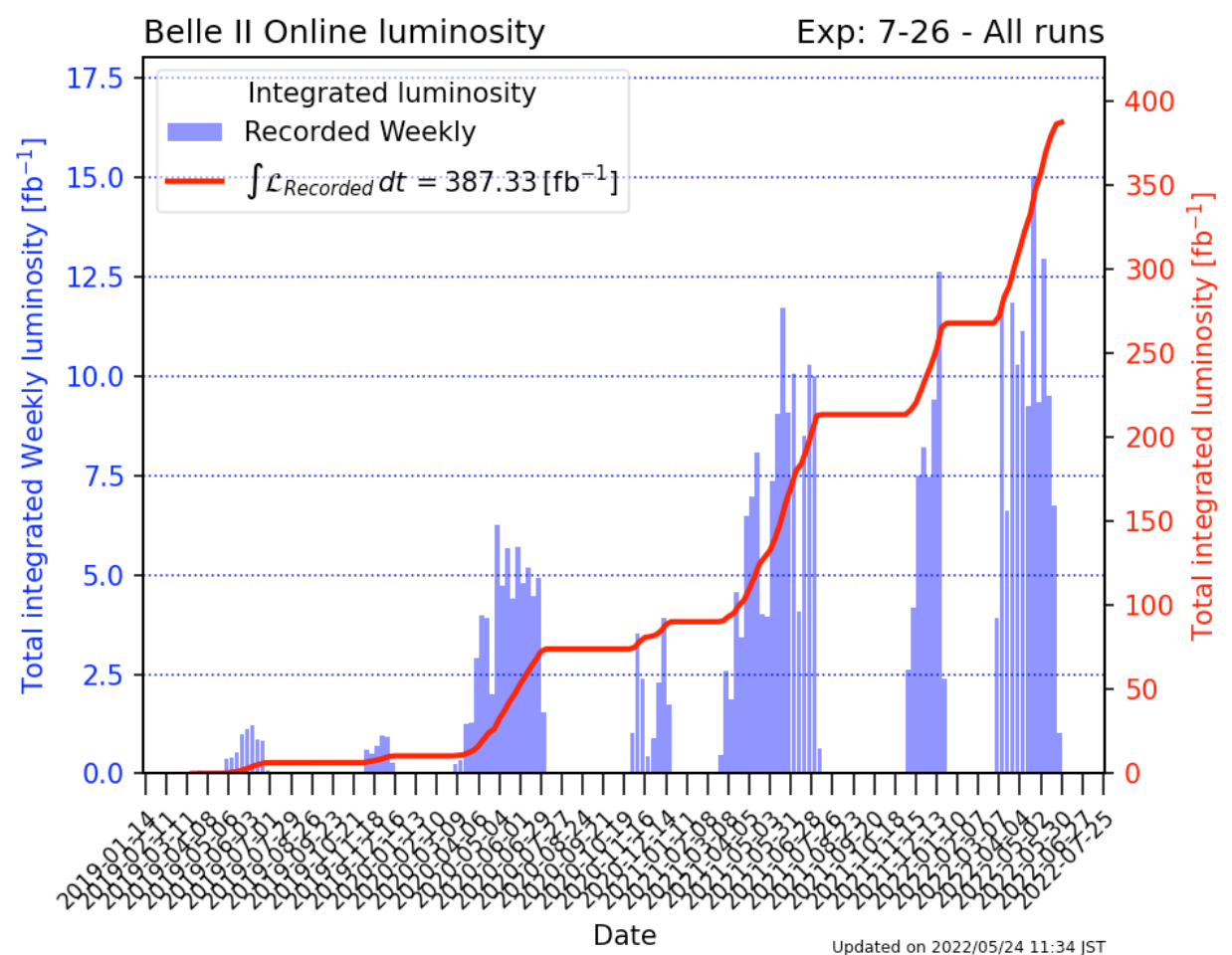
- ◆ Thanks to improved analysis techniques may need less data to have competitive/better results

## ▶ Early energy scan around $10.751 \text{ GeV}$

- Recorded  $\sim 19 \text{ fb}^{-1}$

- More details later

## ▶ Feasibility studies for future analysis



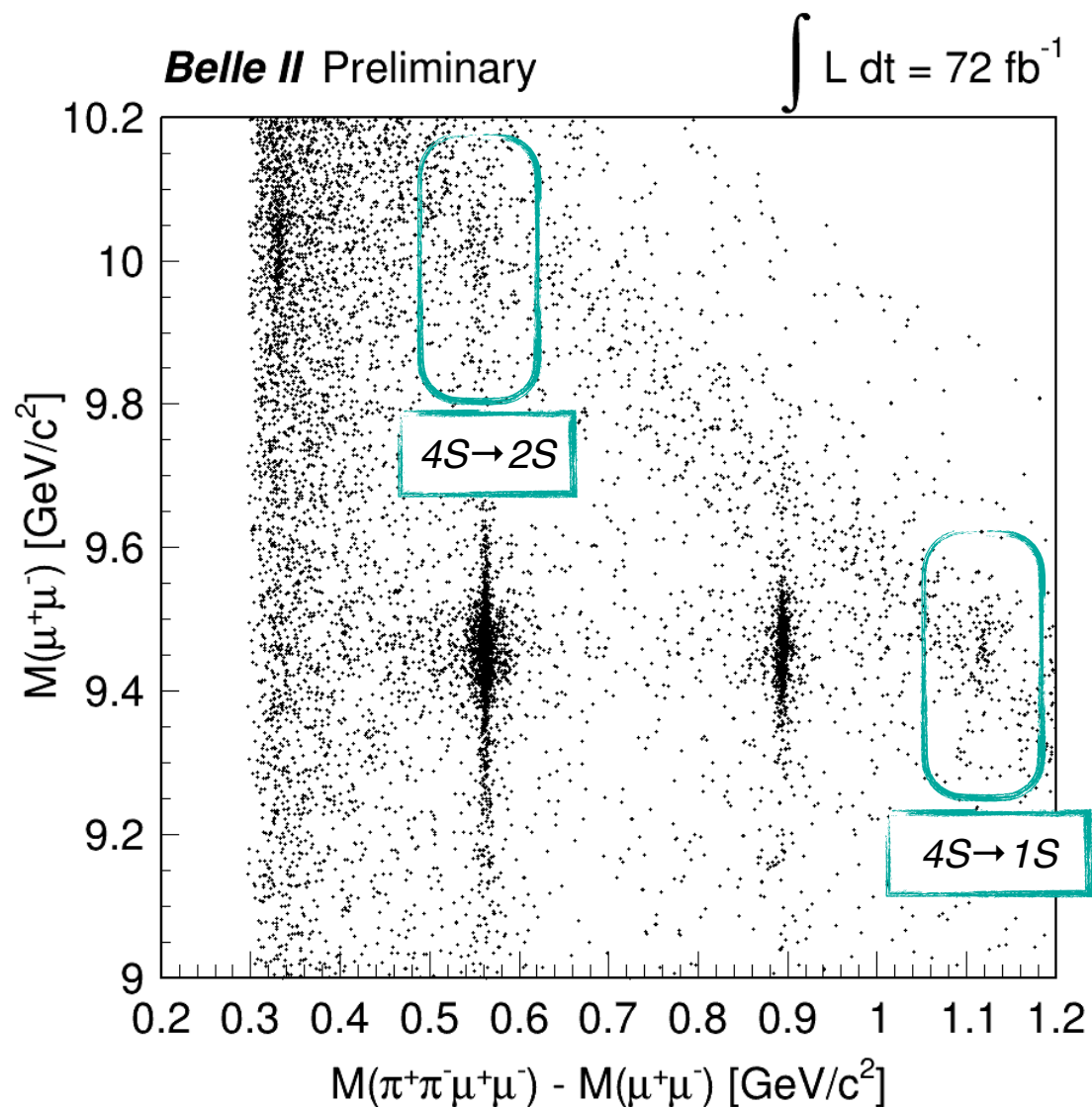
# Analyses at $\Upsilon(4S)$

# $\Upsilon(nS)$ dipion transitions

*BELLE2-NOTE-PL-2021-001*

$$\Upsilon(mS) \rightarrow \pi^+\pi^- [\Upsilon(nS) \rightarrow \mu\mu]$$

**final state:  $\pi^+\pi^- \mu^+\mu^-$  (+ $\gamma$  undetected)**



► Direct transitions:

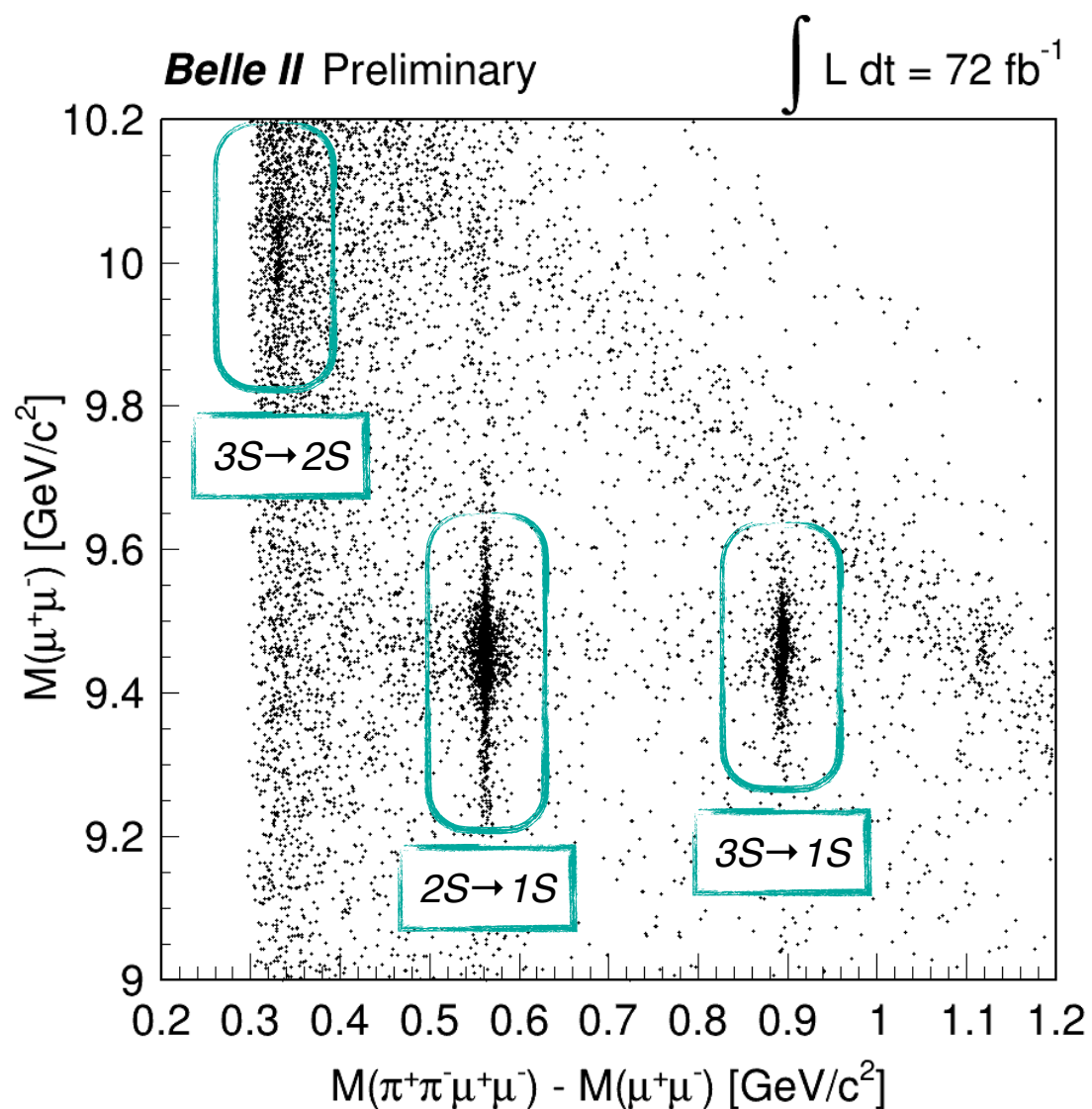
- $\Upsilon(4S) \rightarrow \pi^+\pi^- \Upsilon(1S, 2S)$

# $\Upsilon(nS)$ dipion transitions

*BELLE2-NOTE-PL-2021-001*

$$\Upsilon(mS) \rightarrow \pi^+\pi^- [\Upsilon(nS) \rightarrow \mu\mu]$$

**final state:  $\pi^+\pi^- \mu^+\mu^-$  (+ $\gamma$  undetected)**



►  $e^+e^- \rightarrow \Upsilon(nS) \gamma_{\text{ISR}} \rightarrow \pi^+\pi^-$  Initial State Radiation (ISR) production:

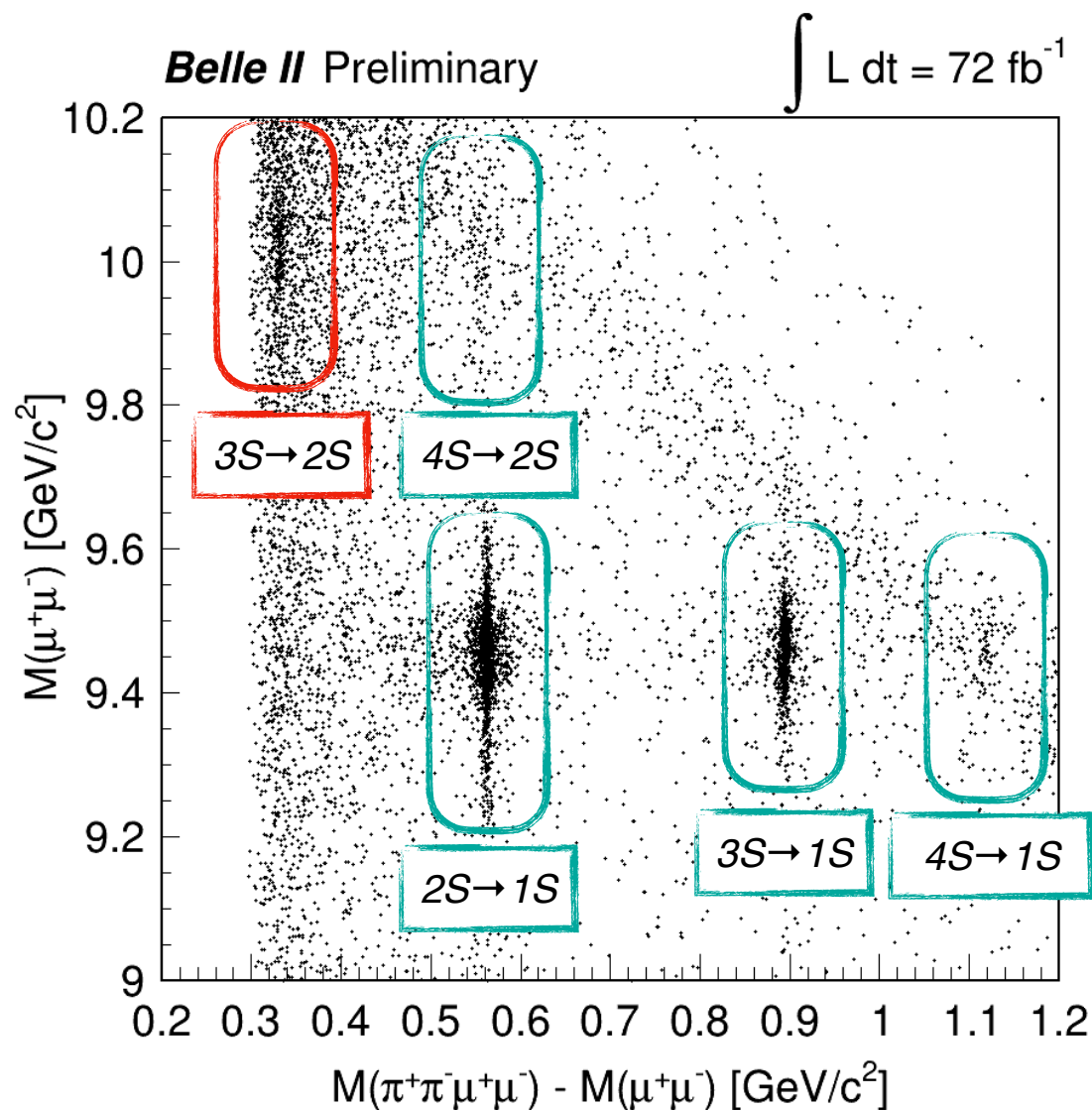
- $\gamma_{\text{ISR}} \Upsilon(3S) \rightarrow \pi^+\pi^- \Upsilon(1S, 2S) (\ell^+ \ell^-)$
- $\gamma_{\text{ISR}} \Upsilon(2S) \rightarrow \pi^+\pi^- \Upsilon(1S) (\ell^+ \ell^-)$

# $\Upsilon(nS)$ dipion transitions

*BELLE2-NOTE-PL-2021-001*

$$\Upsilon(mS) \rightarrow \pi^+\pi^- [\Upsilon(nS) \rightarrow \mu\mu]$$

**final state:  $\pi^+\pi^- \mu^+\mu^-$  (+ $\gamma$  undetected)**



► Done better than Belle analysis

- 496 fb<sup>-1</sup> [PRD 96 (2017) 5, 052005]
- $\Upsilon(3S) \rightarrow \pi^+\pi^- \Upsilon(2S)$  was not visible
- Retention of lower-momentum pion candidates in Belle II compared to Belle.

**Next step:**  
**Dalitz analysis of  $\Upsilon(4S) \rightarrow \pi^+\pi^- \Upsilon(nS)$**   
**Possible with a  $\sim 1 \text{ ab}^{-1}$  data set**

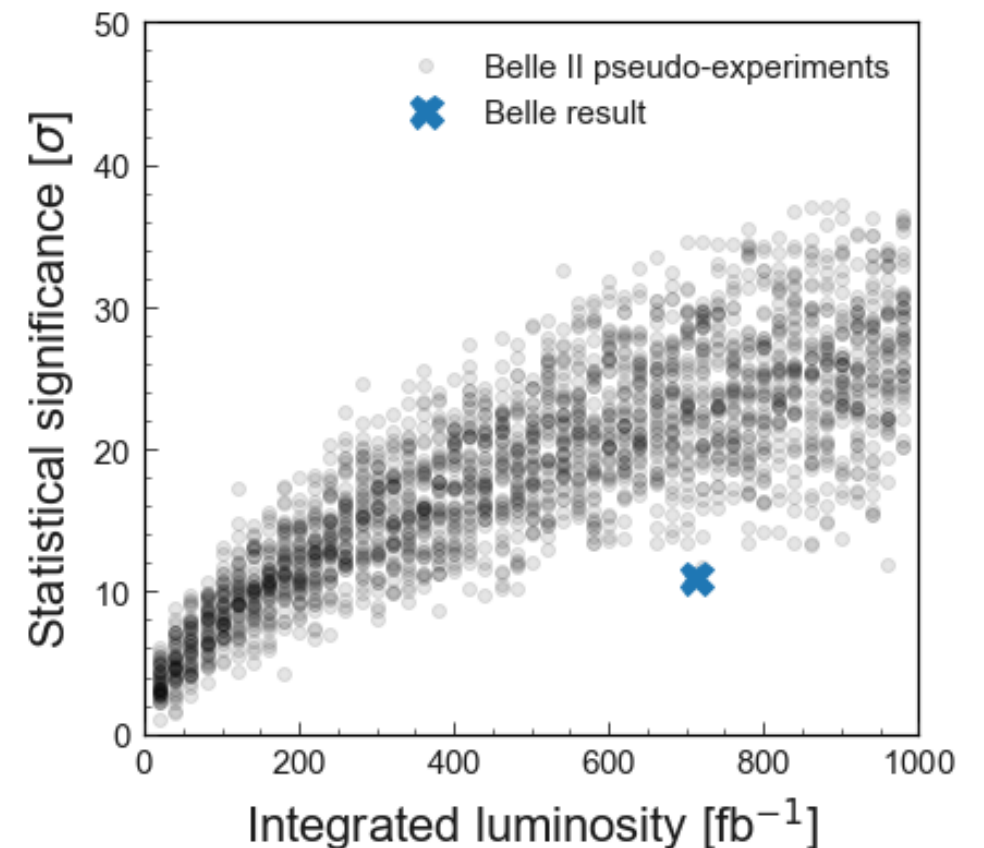
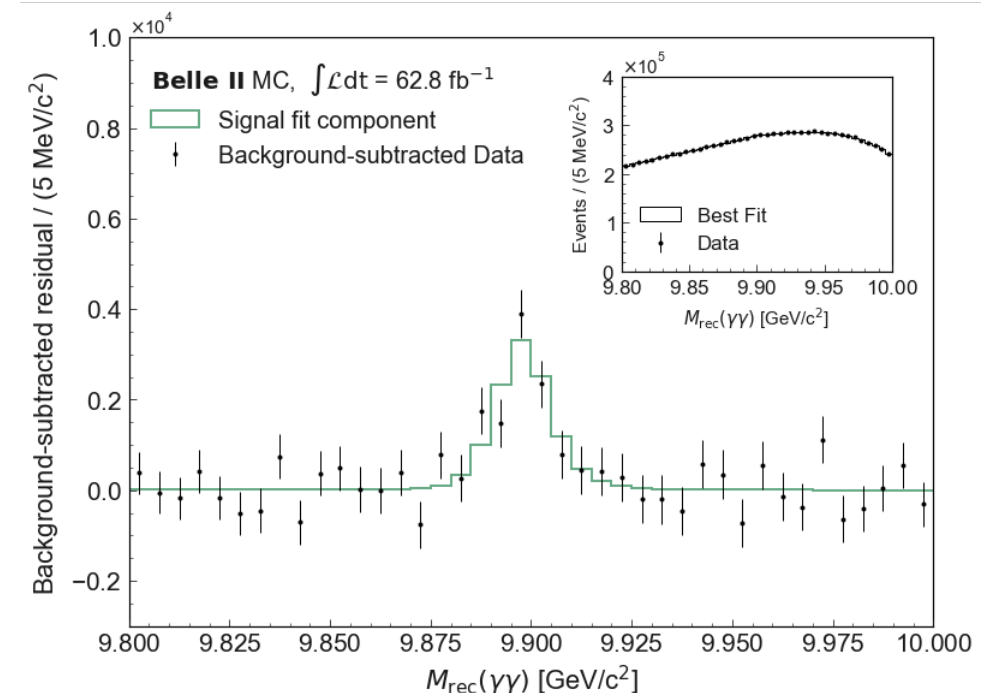


# MC study on rediscovery of the $\Upsilon(4S) \rightarrow \eta \ h_b(1P)$ transition

$$\Upsilon(4S) \rightarrow \eta \ [ \ h_b(1P) \rightarrow \gamma \eta_b(1S) \ ]$$

BELLE2-NOTE-PL-2021-007

- ▶  $\eta$  reconstructed in  $\gamma\gamma$
- ▶ Signal extracted fitting the recoil mass distribution of the  $\eta \rightarrow \gamma\gamma$  candidates.
- ▶ Belle already measured  
 $\text{BR}[\Upsilon(4S) \rightarrow \eta \ h_b(1P)] = 2.18 \times 10^{-3}$ 
  - [Phys. Rev. Lett. 115 (2015) 14, 142001]
- ▶ Belle II analysis:
  - Better background reduction
  - 25 % more efficiency
- ▶ Belle II should be able to re-observe the process with as little as  $50 \text{ fb}^{-1}$



**Can we exploit the huge dataset  
that will be taken at  $\Upsilon(4S)$   
(50  $\text{ab}^{-1}$ ) to do physics usually  
done at lower energies?**

# Feasibility study on lepton flavour universality

► MC sensitivity studies on the LFU in the channel  $\Upsilon(1,2,3 S) \rightarrow \ell\ell$  via initial-state radiation from run at  $\Upsilon(4S)$

► Potential new physic in  $B \rightarrow D^{(*)}\ell\nu$  affects also this process

► [Aloni et al, JHEP 06 (2017) 019]

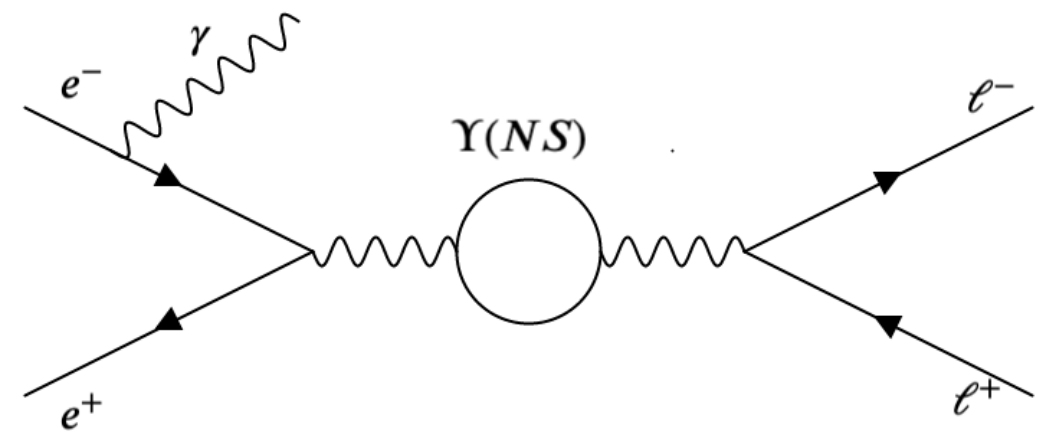
► Measure  $\Upsilon(1S) \rightarrow \tau\tau, \mu\mu$  by fitting the ISR peak in the recoil mass distribution

► Measure  $R = \frac{B(\Upsilon(1S) \rightarrow \tau\tau)}{B(\Upsilon(1S) \rightarrow \mu\mu)}$

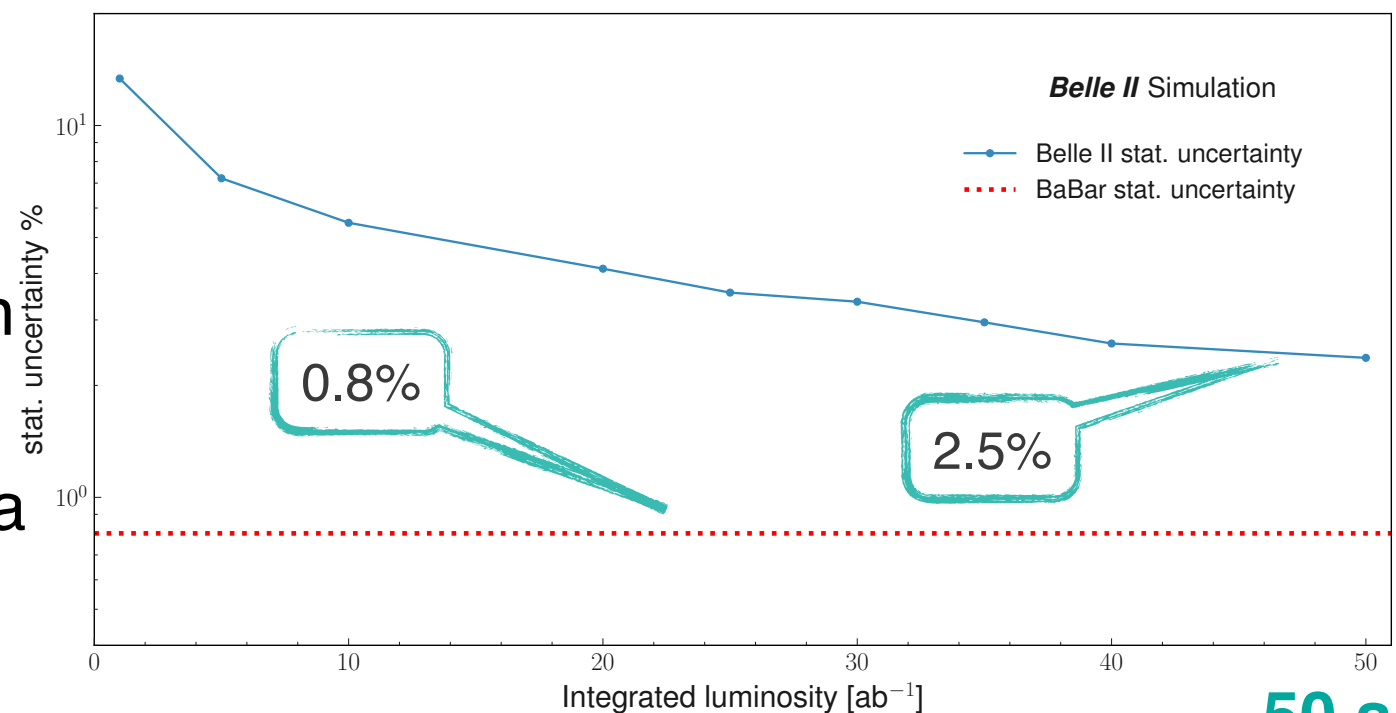
► Check statistical uncertainty as function of integrated luminosity

► More competitive BaBar result with data taken at  $\Upsilon(3S)$ :

► [Phys. Rev. Lett., 125:241801, 2020]



BELLE2-NOTE-PL-2021-006



50  $\text{ab}^{-1}$

# Feasibility study on lepton flavour universality

► MC sensitivity studies on the LFU in the channel  $\Upsilon(1,2,3 S) \rightarrow \ell\ell$  via initial-state radiation from run at  $\Upsilon(4S)$

► Potential new physic in  $B \rightarrow D^{(*)}\ell\nu$  affects also this process

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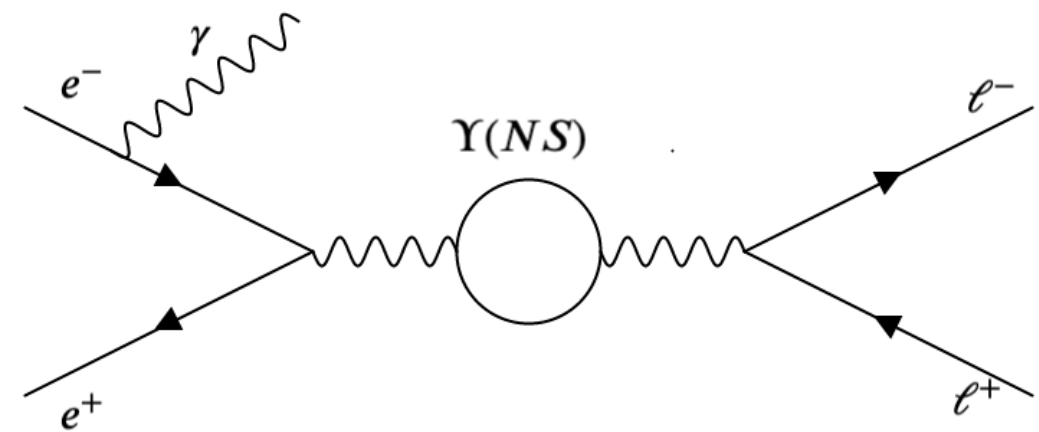
► Measure ISR peak

► Measure  $\frac{B(\Upsilon(1S) \rightarrow \tau\tau)}{B(\Upsilon(1S) \rightarrow \mu\mu)}$

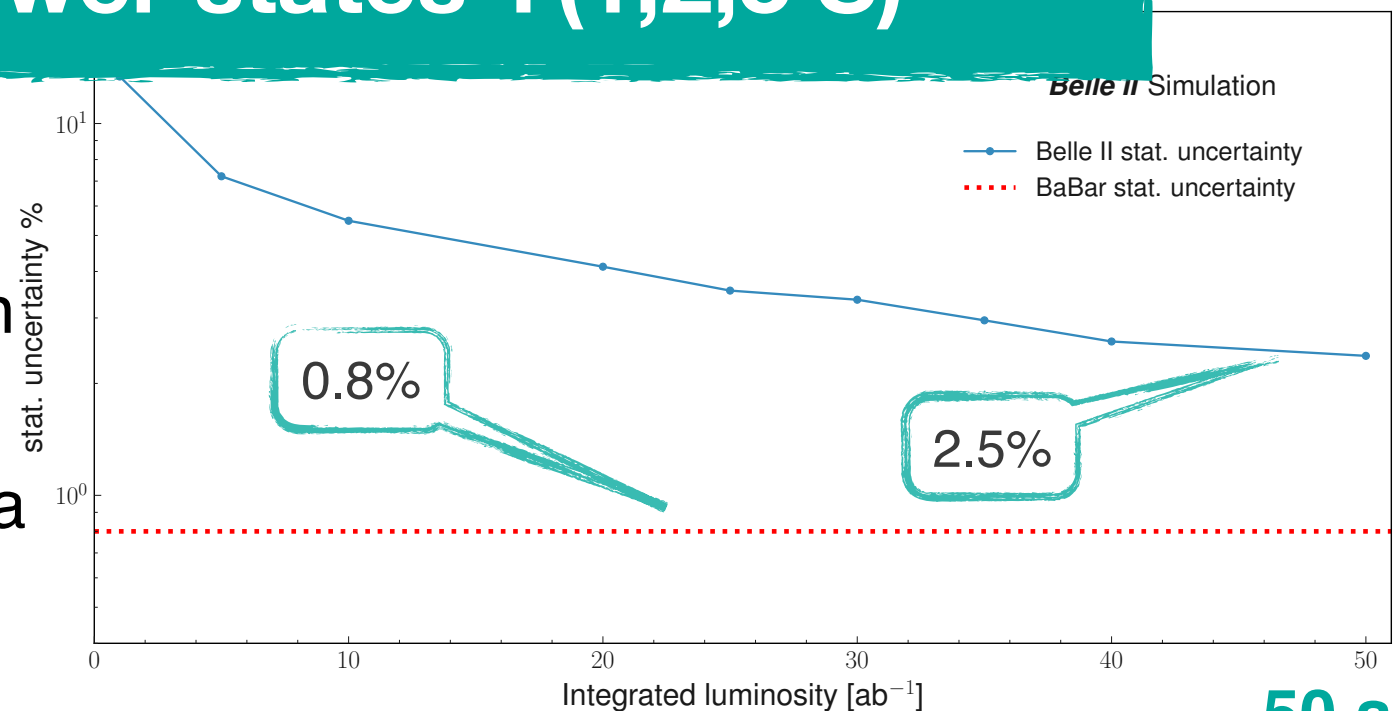
► Check statistical uncertainty as function of integrated luminosity

► More competitive BaBar result with data taken at  $\Upsilon(3S)$ :

► [Phys. Rev. Lett., 125:241801, 2020]



**Analysis not feasible with data at  $\Upsilon(4S)$   
Need data at lower states  $\Upsilon(1,2,3 S)$**



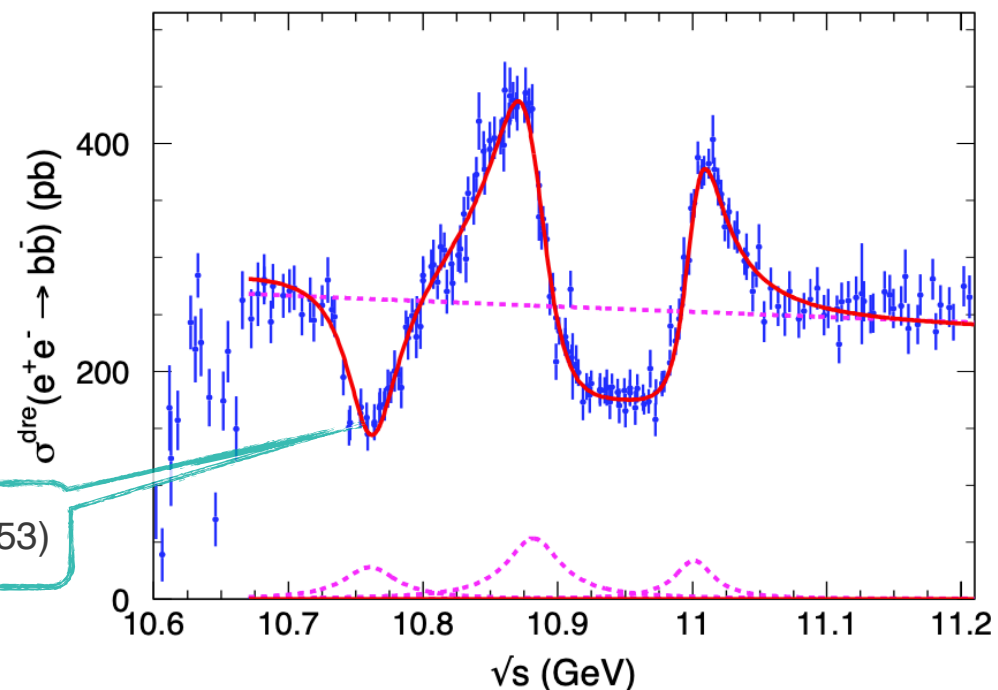
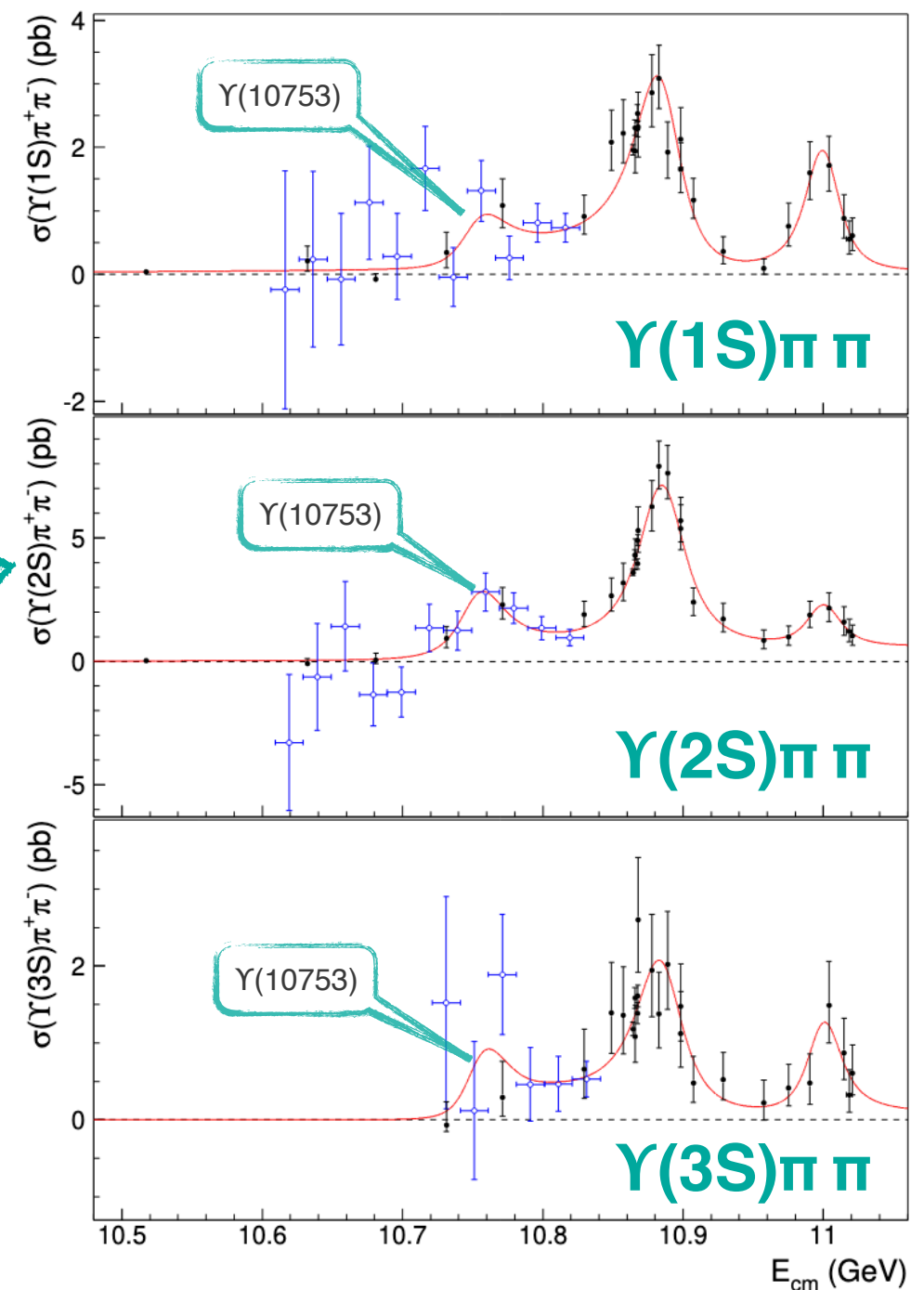
**50 ab<sup>-1</sup>**

**2021 energy scan  
around  $\Upsilon(10753)$**

# About $\Upsilon(10753)$

► JHEP10(2019)220 (Belle)

- $e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-$ 
  - $\Upsilon(nS) \rightarrow e^+e^-, \mu^+\mu^-$
  - $n = 1, 2, 3$
- High-stat scan points:  $1 \text{ fb}^{-1}$  each (**black**)
- + ISR process at the  $\Upsilon(10860)$  [ $\Upsilon(5S)$ ] (**blue**)
- Found new  $J^{PC}=1^{--}$  structure
  - significance of  $5.2 \sigma$



► Chin.Phys.C 44 8, 083001 (2020):

- Refit the Belle + BaBar  $R_b$  scan
- Evidence of  $\Upsilon(10753)$  in interference



# Possible interpretations

## ▶ Followed several Belle analyses:

- ▶  $B\bar{B}$ ,  $B^*\bar{B}$ ,  $B^*\bar{B}^*$  cross sections study,  $\Upsilon(10750) \rightarrow \omega\eta_b(1S)$  (Not published), ...
- ▶ Results inconclusive
- ▶ Need more data

## Conventional D- or S-D mixed state:

- ▶ Phys.Rev.D 101 (2020) 1, 014020
- ▶ Phys.Lett.B 803 (2020) 135340
- ▶ Eur.Phys.J.C 80 (2020) 1, 59
- ▶ arXiv:2106.14123v1 (2021)

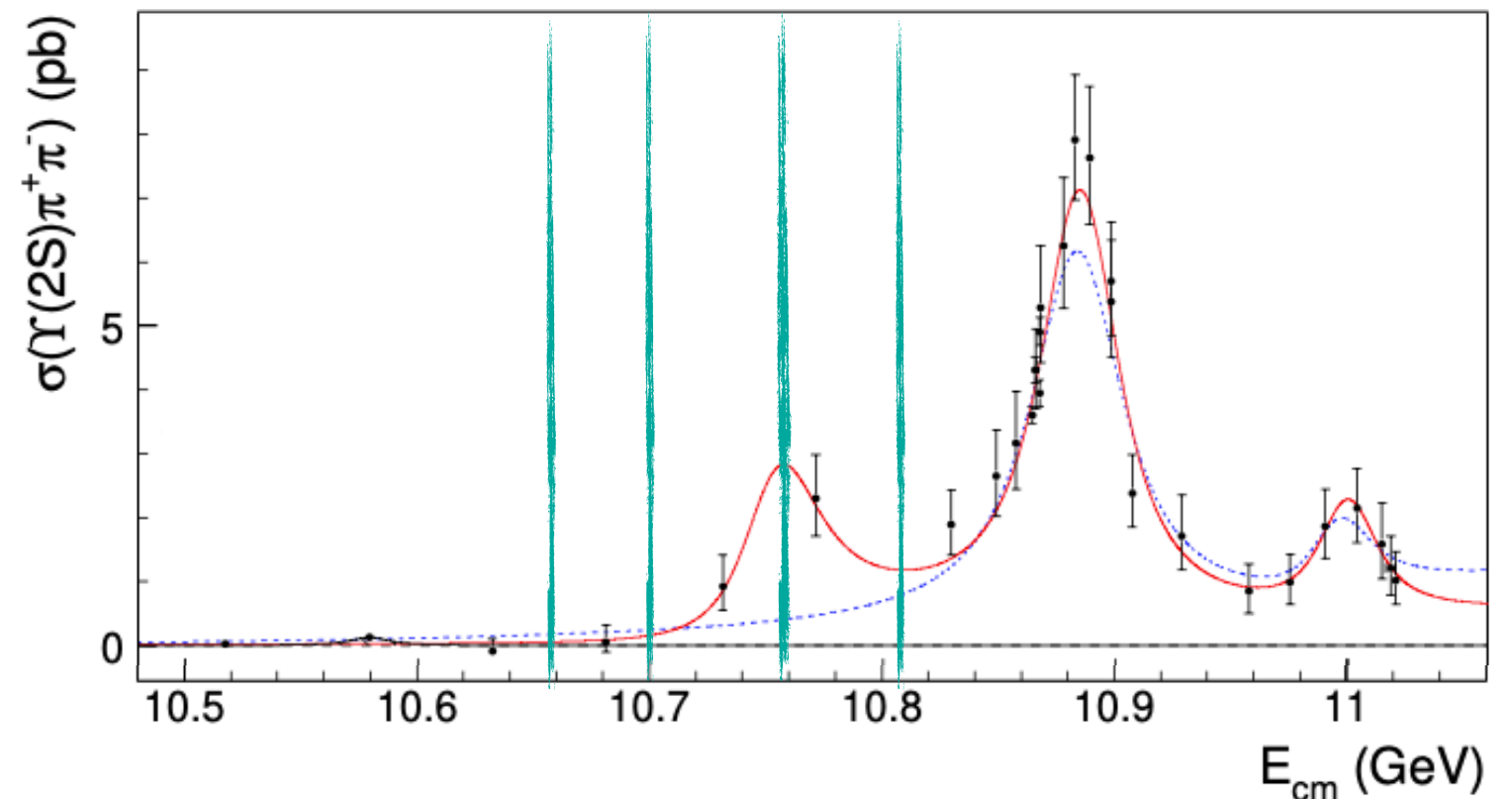
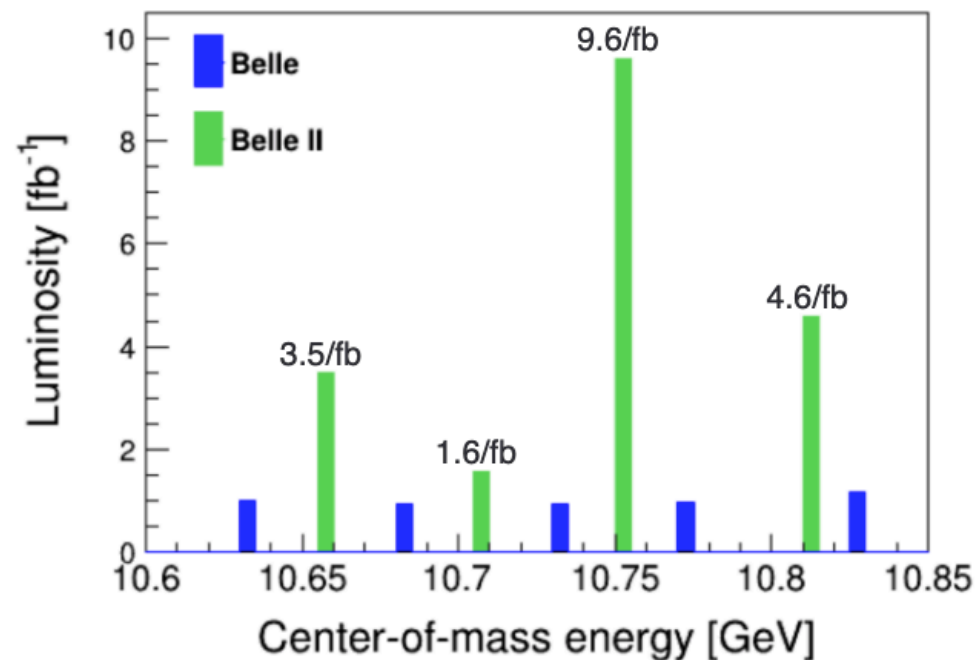
## Exotic:

- ▶ Arxiv:2008.05605 (Dynamic resonance)
- ▶ Chin.Phys.C 43 (2019) 12, 123102 (Tetraquark)
- ▶ Phys.Lett.B 802 (2020) 135217 (Tetraquark)
- ▶ Phys.Rev.D 102 (2020) 1, 014036 ( $\Upsilon(5S)$  is  $4q$ )

# 2021 Energy scan

3 weeks in November 2021

- 10.751 GeV (9.6 fb<sup>-1</sup>)(on resonance?)
- 3 scan point for energy-dependent  $B\bar{B}$  ,  $B^*\bar{B}$ ,  $B^*\bar{B}^*$  cross sections study:
  - 10.657 GeV (3.5 fb<sup>-1</sup>)
  - 10.706 GeV (1.6 fb<sup>-1</sup>)
  - 10.810 GeV (4.6 fb<sup>-1</sup>)
- BELLE2-NOTE-PL-2022-001



# $\Upsilon(10753)$ analyses

► No public results yet

Mode	Belle Status	Belle II Outcome
Golden Modes		
$e^+e^- \rightarrow \pi^+\pi^-\Upsilon(pS)(\rightarrow \ell^+\ell^-)$	Published	B+BII combined
$B\bar{B}$ decomposition	Published	B+BII combined
$\pi^+\pi^-$ Dalitz	Needs data	First result
$Y_b \rightarrow \omega\eta_b(1S)$	Ongoing	B+BII or BII update
$Y_b \rightarrow \omega\chi_{bJ}(1P)$	In pub./needs data/points	B+BII combined
Silver Modes		
$Y_b \rightarrow \pi^+\pi^-X$ (inclusive)	Needs data	First result
$Y_b \rightarrow \eta X$ (inclusive)	Needs data	First result
$Y_b \rightarrow \eta\Upsilon(1S, 2S)(\rightarrow \ell^+\ell^-)$	Needs data	First search
$Y_b \rightarrow \eta'\Upsilon(1S)(\rightarrow \ell^+\ell^-)$	Needs data	First search
$Y_b \rightarrow \Upsilon(1S)$ (inclusive)	Needs data	First result
Bronze Modes		
$Y_b \rightarrow \gamma X_b$	Needs data	First search
$Y_b \rightarrow \pi^0\pi^0\Upsilon(pS)(\rightarrow \ell^+\ell^-)$	Needs data	First search
$Y_b \rightarrow KK(\phi)\Upsilon(pS)(\rightarrow \ell^+\ell^-)$	Needs data	First search
$Y_b \rightarrow \pi^0\pi^0X$ (inclusive)	Needs data	First search
$Y_b \rightarrow \pi^0X$ (incl. or excl.)	Needs data	First search
...		

# BELLE II POTENTIAL

Far future

## ► Run at $\Upsilon(6S)$ and $\Upsilon(5S)$ and high energy scan

- Search for new, predicted, resonances such missing bottomonia, exotic states, etc..
- Improve precision of already known process and states.
  - $Z_b$  states were only found so far in  $\Upsilon(5S)$  decays.
- Measure the effect of the coupled channel contribution.
- Study  $B^{(*)}\bar{B}^{(**)}$  and  $B_s^{(*)}\bar{B}_s^{(**)}$  threshold regions.
  - Maybe challenging for SuperKEKB

Above  $\Upsilon(4S)$

## ► Run at $\Upsilon(3S)$ , $\Upsilon(2S)$ and $\Upsilon(1S)$

- Search for missing  $\pi\pi/\eta$  transitions to constrain further theoretical models.
- Search for new physics:
  - Lepton flavour universality, Lepton flavour violation, new scalars...

# BELLE II POTENTIAL *Far future*

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- Search for new physics:
  - Lepton flavour universality, Lepton flavour violation, new scalars...

*Below  $\Upsilon(4S)$*

# Summary

- ▶ Currently taking data at  $\Upsilon(4S)$ 
  - Rediscovery analyses going on
    - Shown results with only a small part of accumulated luminosity.
  - Feasibility studies shows how it's important to take data below the  $\Upsilon(4S)$  to perform studies on physics beyond standard model
- ▶ Took energy scan around 10.751 GeV
  - New structure studies going on
- ▶ Possible run at  $\Upsilon(6S)$ ,  $\Upsilon(5S)$ ,  $\Upsilon(3S)$ ,  $\Upsilon(2S)$  and  $\Upsilon(1S)$ 
  - Plans are under discussion

**Together with the capability of SuperKEKB, Belle II has a unique opportunity to study quarkonium(-like) particles and make an impact in this sector in the years to come.**





# Backup slides



# SuperKEKB Luminosity

► SuperKEKB goal:  $> \sim 40 \times$  KEKB instantaneous luminosity

- $\mathcal{L} = 6.5 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$

- Current world record:  $\mathcal{L} = 3.9 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$  (May 2022)

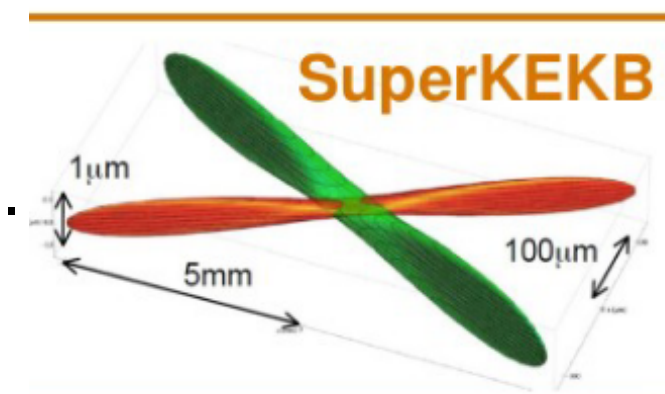
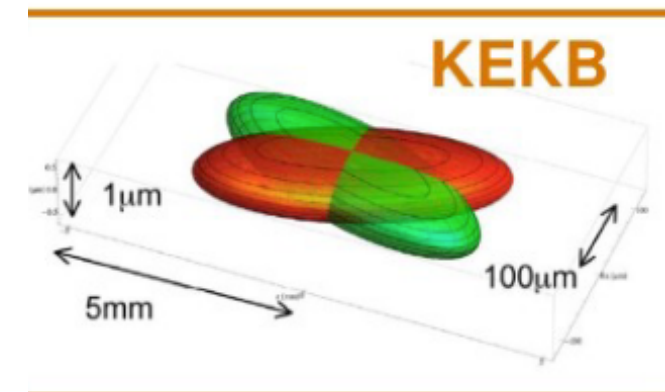
► How to achieve that?

- Beam current:

- 1.64/1.19 A (Belle)  $\rightarrow$  2.5/1.8 A (Belle II) for  $e^-/e^+$  beam.

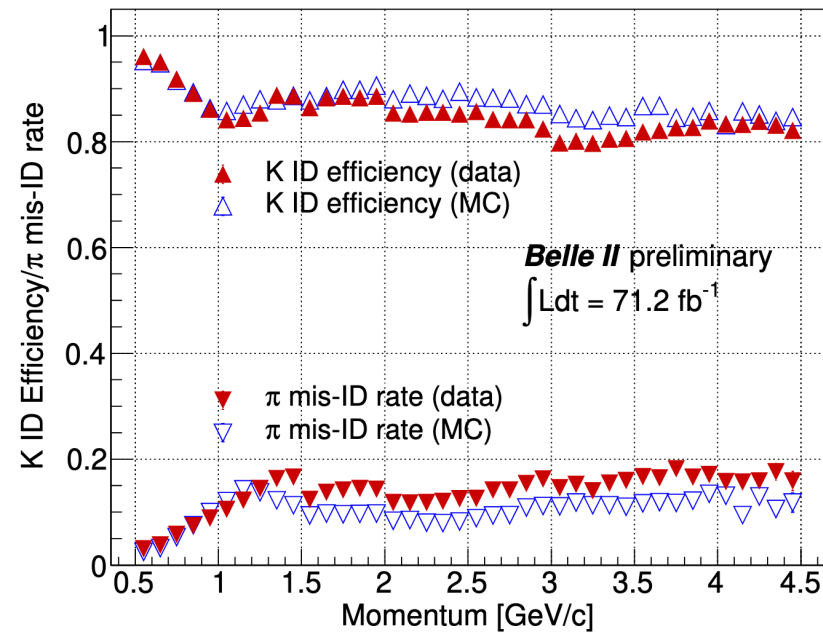
- Beta function at IP ( $\beta^{*y}$ ):

- 5.9/5.9 mm (Belle)  $\rightarrow$  0.27/0.30 mm (Belle II).



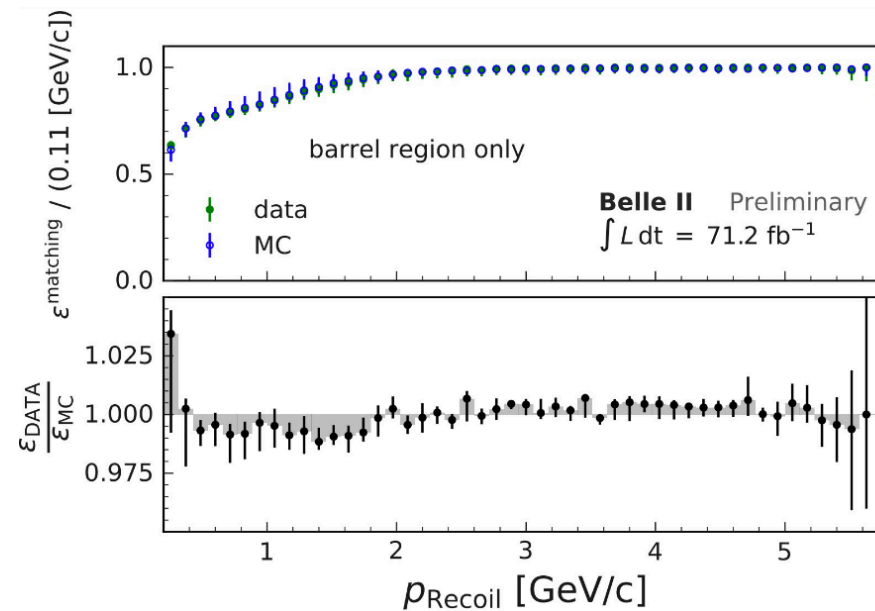
$$L = \frac{\gamma^{\pm}}{2er_e} \left( 1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \left( \frac{I_{\pm} \xi_{y\pm}}{\beta_y^*} \right) \left( \frac{R_L}{R_{\xi_{y\pm}}} \right)$$

# Belle II performance



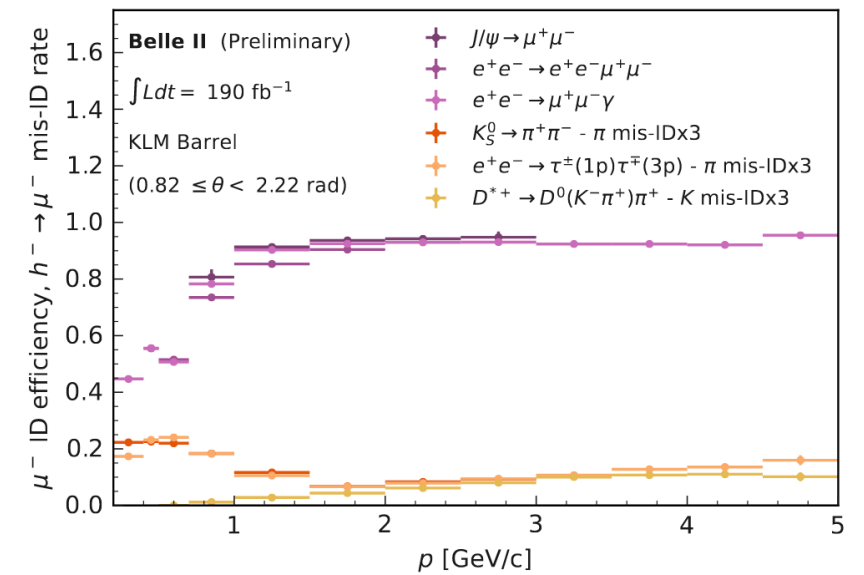
K  $\pi$  identification

BELLE2-NOTE-PL-2020-024



Photon matching efficiency

BELLE2-NOTE-TE-2020-026



$\mu$  e identification

BELLE2-CONF-PH-2022-003

# Potential models

- ▶ Use of stationary non-relativistic Schrödinger equation with appropriate potential:

- Cornell potential  $V = -\frac{a}{r} + br + c$

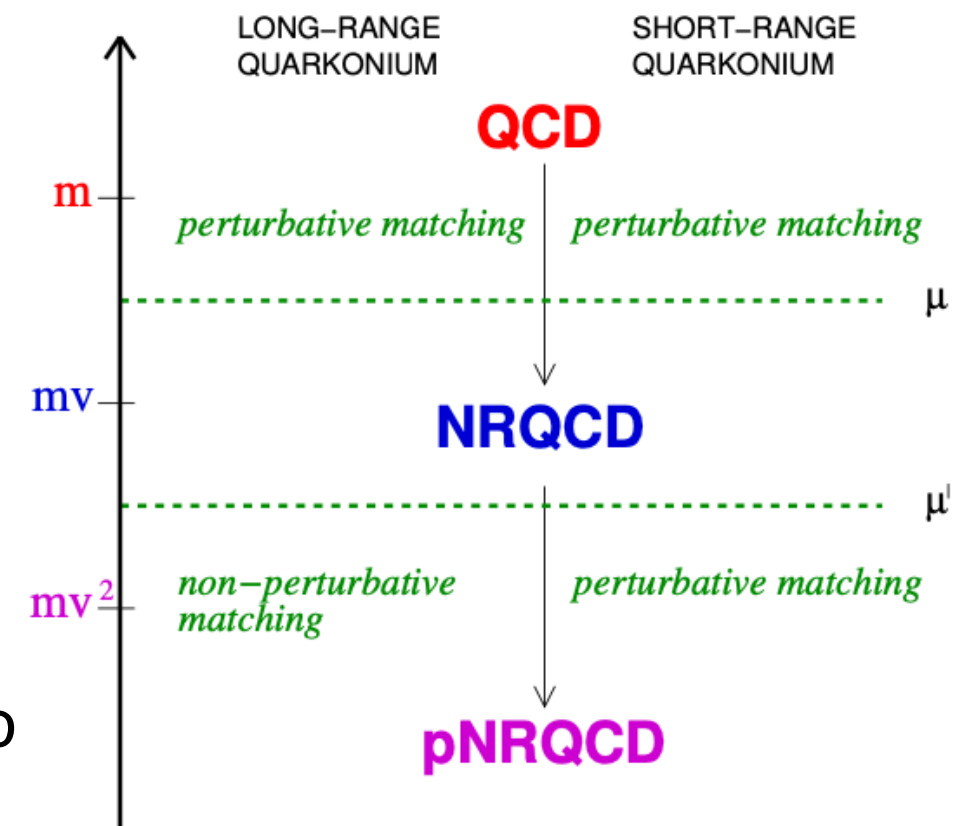
- $-\frac{a}{r}$  coincides with the QCD one-gluon exchange Coulomb potential

- $+br$  incorporates confinement

- ▶ Non relativistic potential model justified by the fact that the bottom and, to a lesser extent, the charm masses are large in comparison to  $\Lambda_{\text{QCD}}$
- ▶ Add extra terms to include relativistic effect, fine and hyper fine structure...
- ▶ Above two heavy-light meson threshold extra degrees of freedom are needed to account for possible mixing effects.
- ▶ Purely phenomenological, with no way to link the model parameters to QCD.

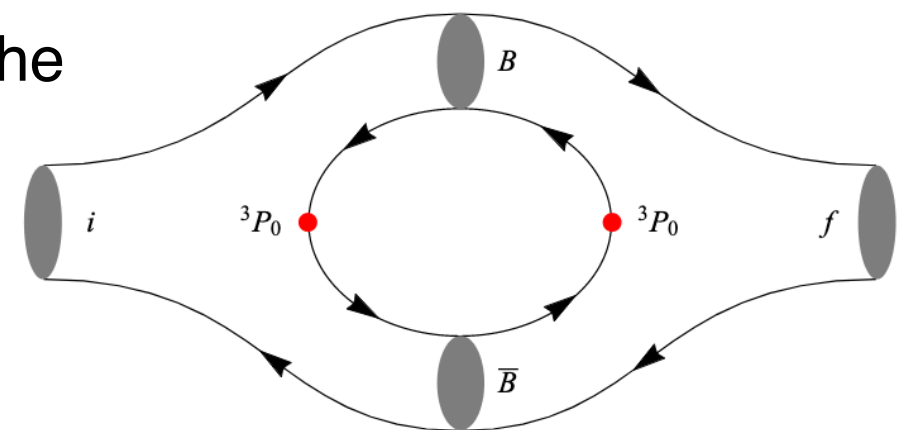
# Multiscale system

- ▶ Hard scale (the mass  $m$  of the heavy quarks)
  - Can be described in perturbation theory.
  - Quarkonium annihilation and production take place at the scale  $m$
- ▶ Soft scale (the relative momentum of the heavy-quark–antiquark  $\mathbf{p} \sim m\mathbf{v}$ )
  - Quarkonium binding
- ▶ Ultra soft scale (the typical kinetic energy  $E \sim m\mathbf{v}^2$  of the heavy quark and antiquark)
  - Very low-energy gluons and light quarks (also called ultrasoft degrees of freedom) live long enough that a bound state has time to form
- ▶ The description of the systems depends on the relation of  $\Lambda_{\text{QCD}}$  to the scales.



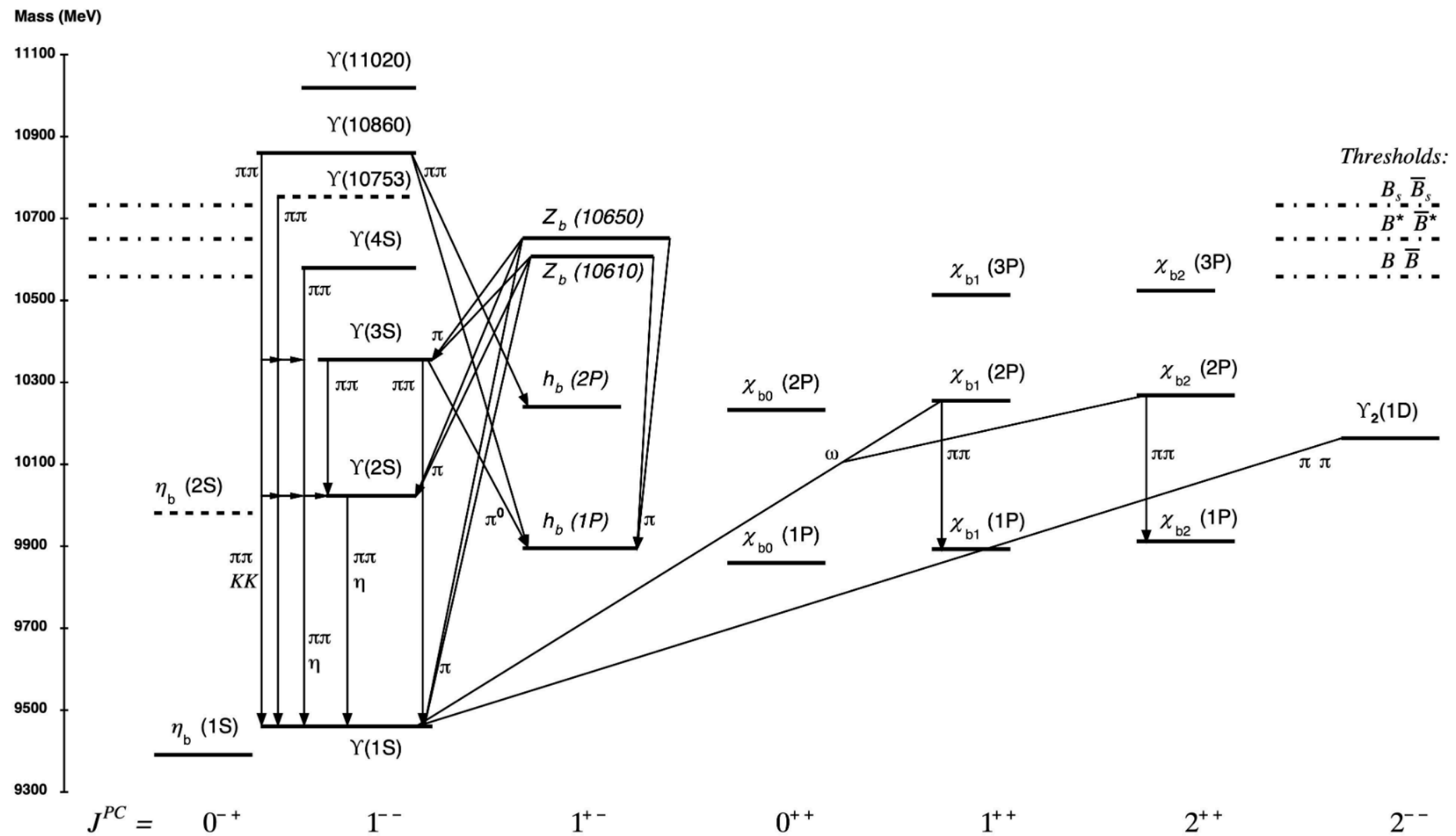
# Couple channel effect

- ▶ Framework used to describe the nature of the properties unexpected for a pure  $q\bar{q}$  state.
- ▶ Generate quark-antiquark pairs which enlarge the Fock space of the initial state.
- ▶ This formalism incorporate intermediate heavy mesons within hadrons.
- ▶ These multiquark components will change the Hamiltonian of the potential model:
  - Mass shift
  - Mixing between states with the same quantum numbers
  - Directly contribution to open channel strong decay if the initial state is above threshold.
- ▶ Above the BB threshold the states such 4S, 5S and Y6S are more affected.
  - These states can be modelled as mixture of  $q\bar{q}$  with two-meson continuum in a form of hadronic loop.





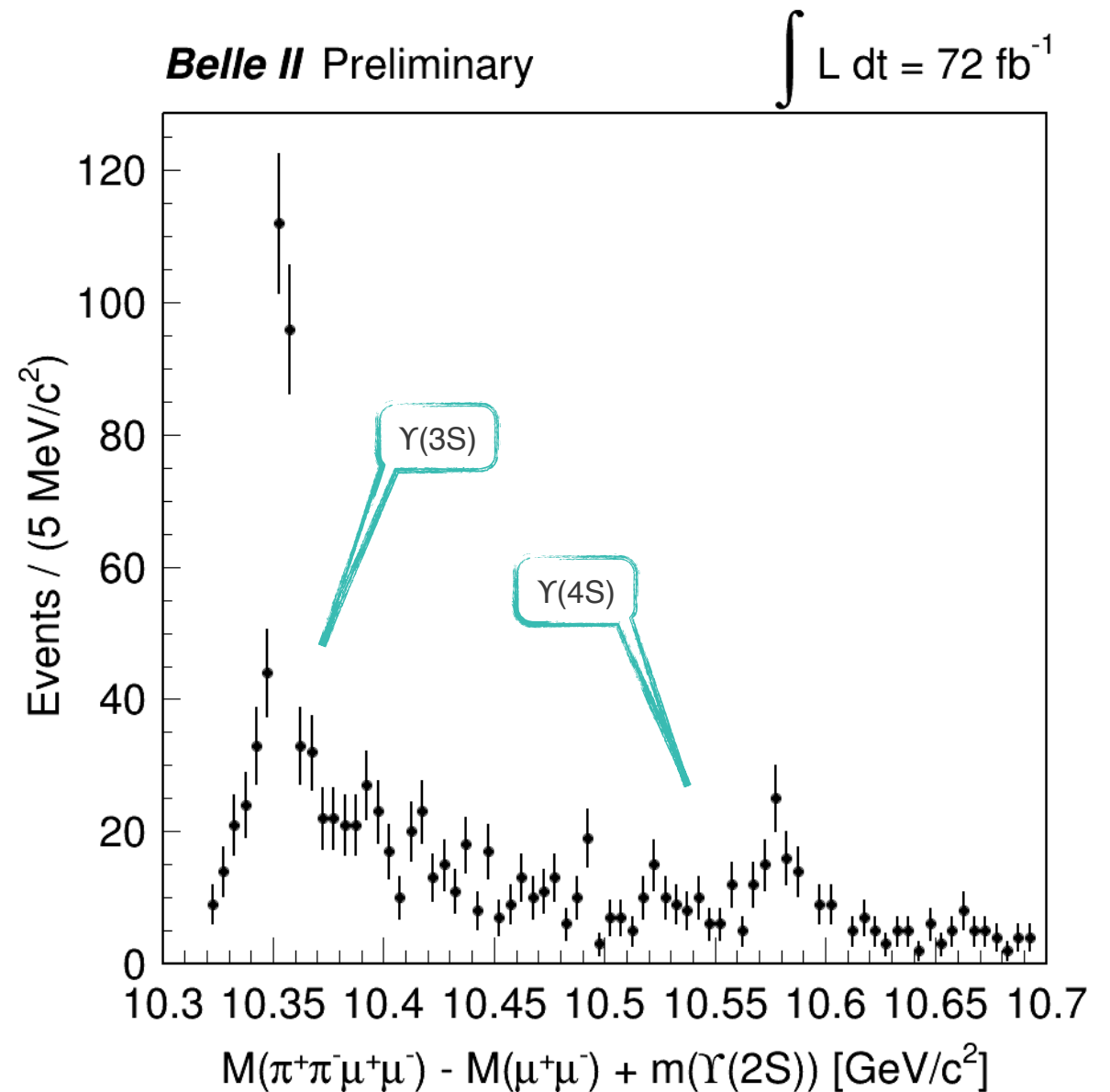
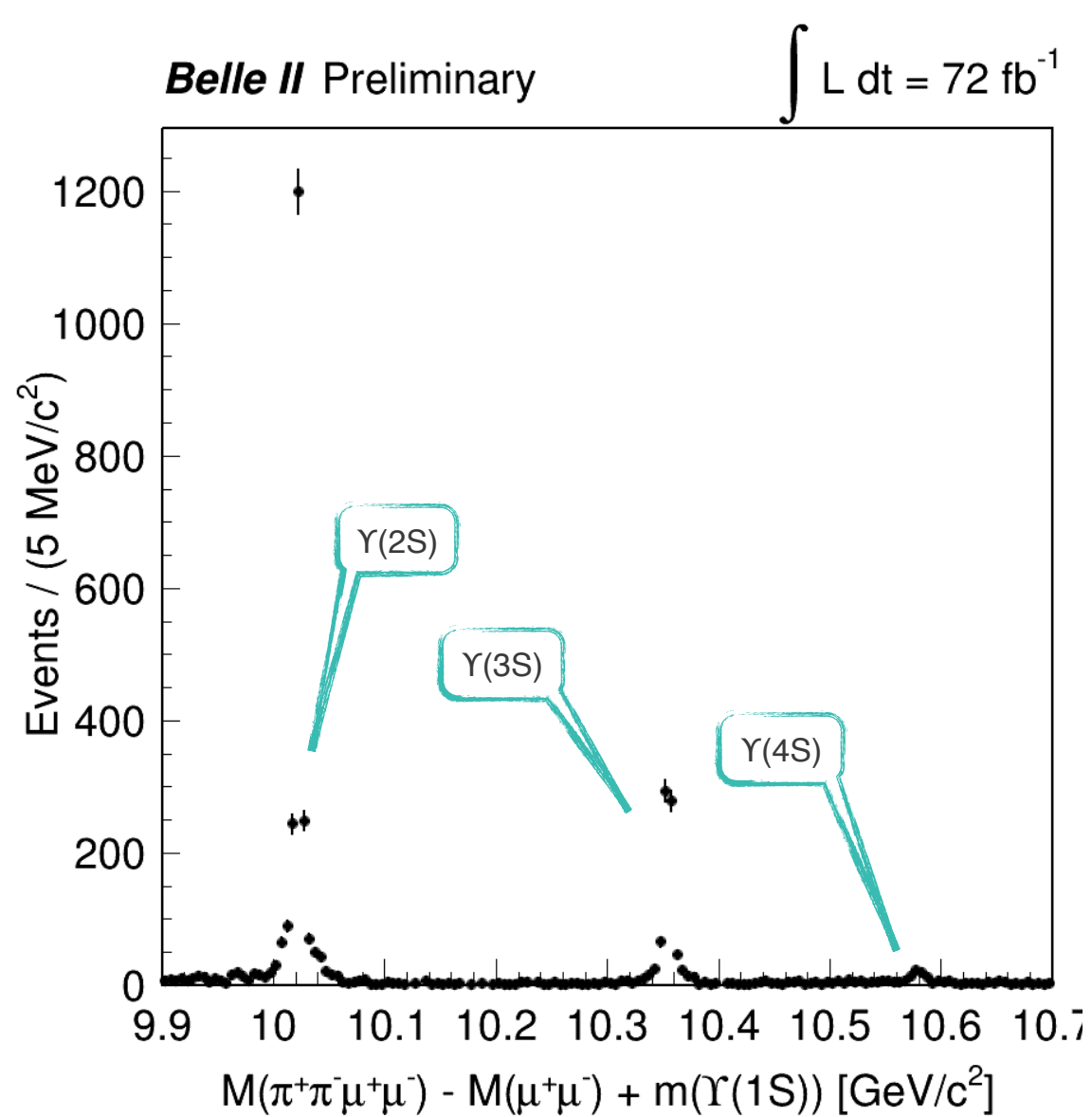
# Transitions



# $\Upsilon(nS)$ dipion transitions

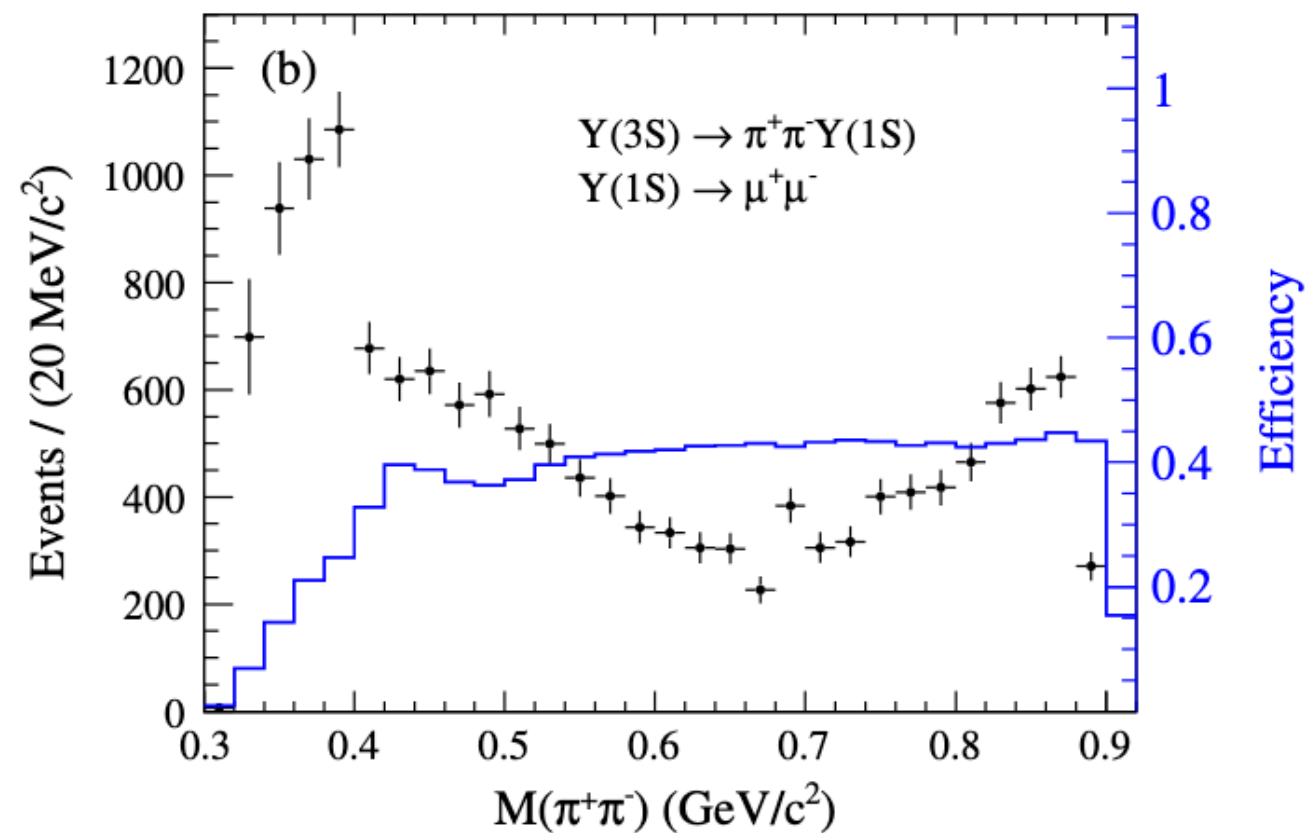
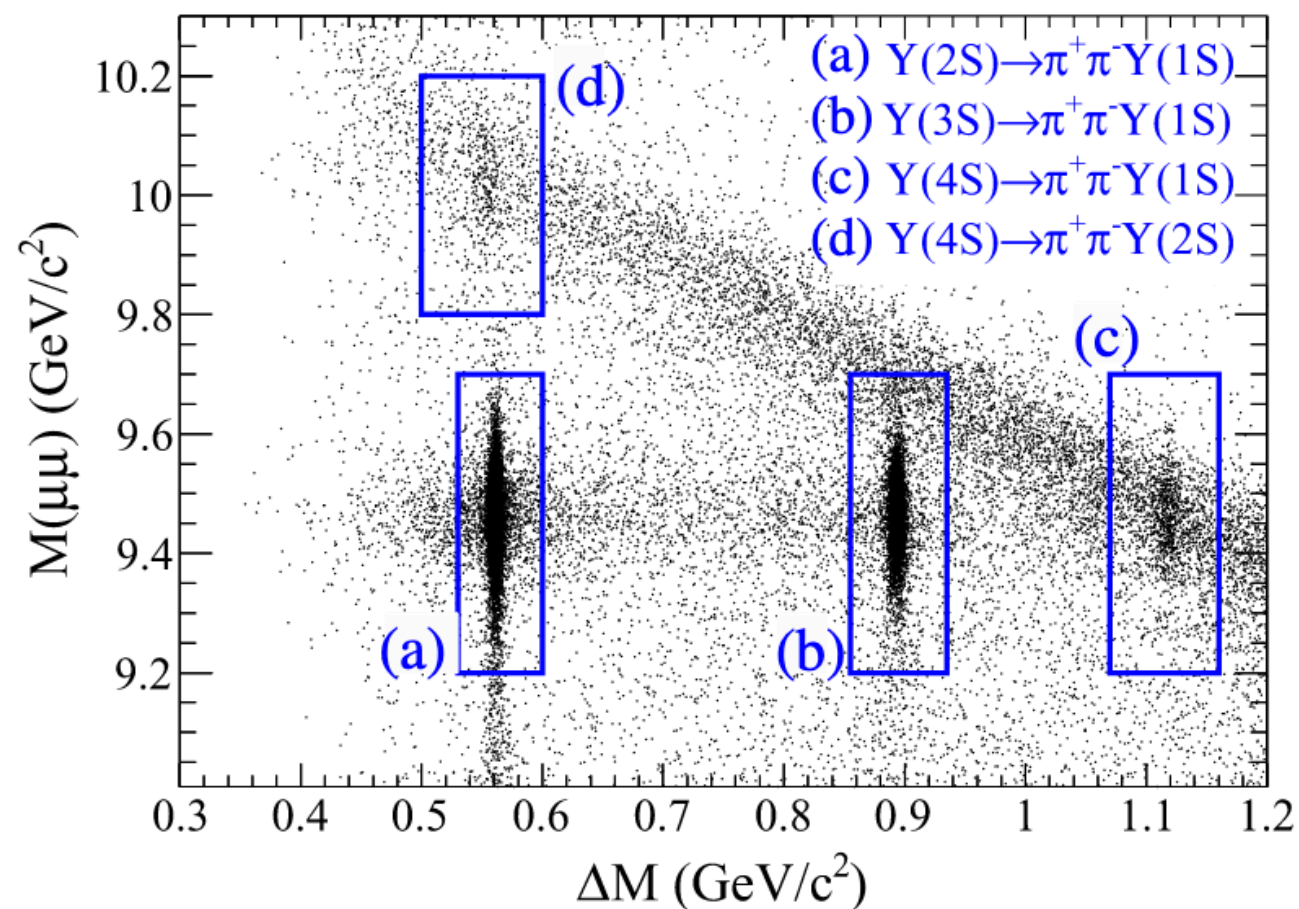
► Variable of interest:  $\Delta M = M(\pi^+\pi^-\ell\ell) - M(\ell\ell) + M(\text{PDG})$

●  $M(\text{PDG})$  = mass of the daughter



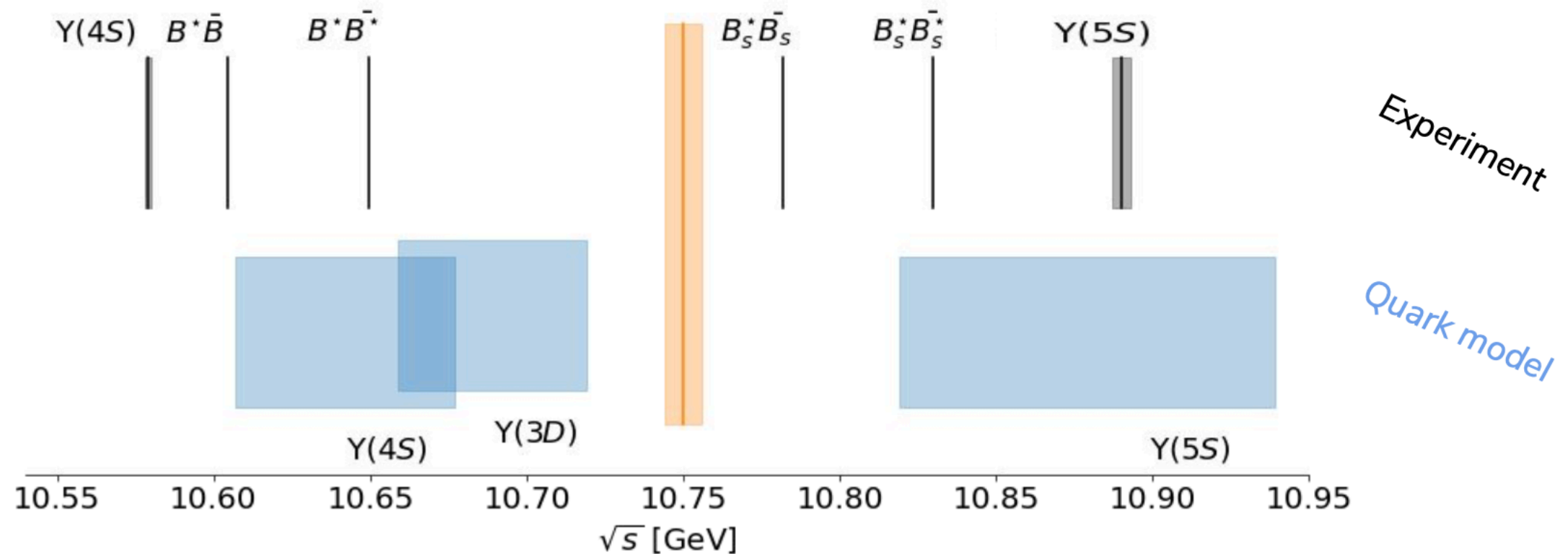
# Dipion transition at Belle

- ▶  $\Upsilon(3S) \rightarrow \pi^+\pi^-\Upsilon(2S)$  not visible
- ▶ Not yet understood behaviour of  $m_{\pi^+\pi^-}$  distributions



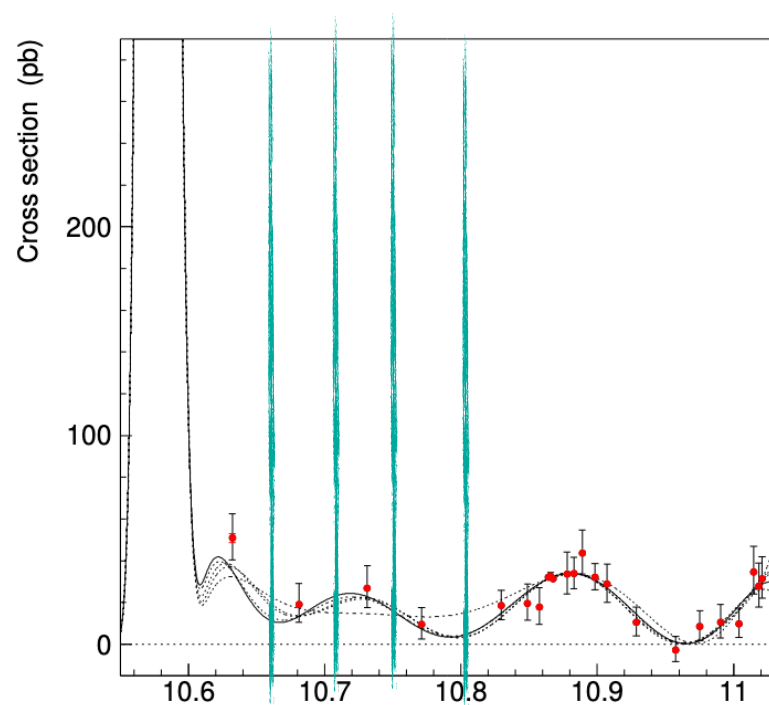
# $\Upsilon(10753)$

- ▶ Unlikely to be a molecule as it's far from any S- threshold
- ▶ No direct matching to conventional states (but may be an S-D mixing?)

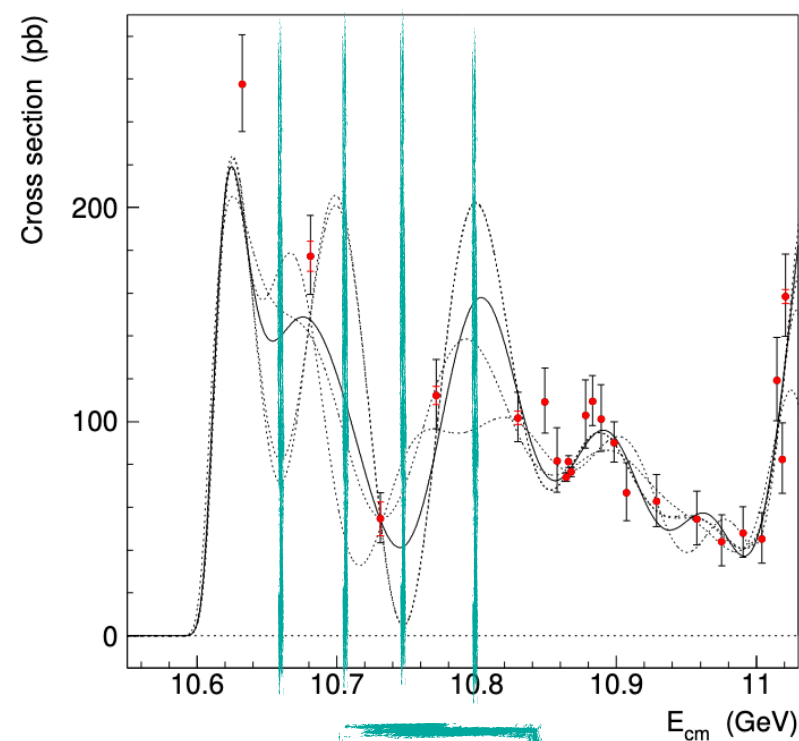


# $B\bar{B}$ Decomposition in energy scan

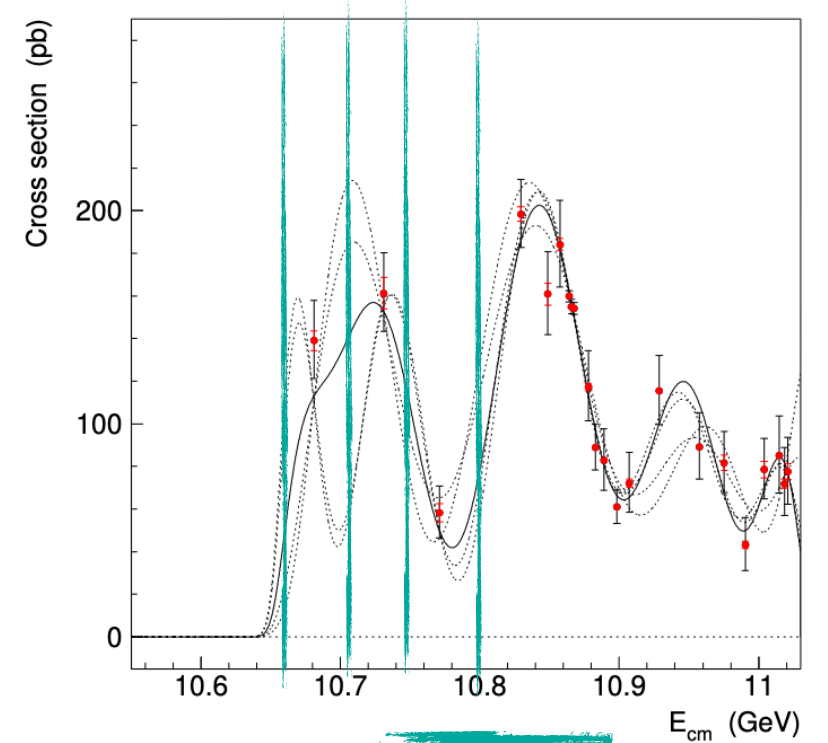
- ▶  $B\bar{B}$ ,  $B^*\bar{B}$ ,  $B^*\bar{B}^*$  cross section at various energies
- ▶ Higher statistic to improve fits
- ▶ JHEP06(2021)137



$B\bar{B}$

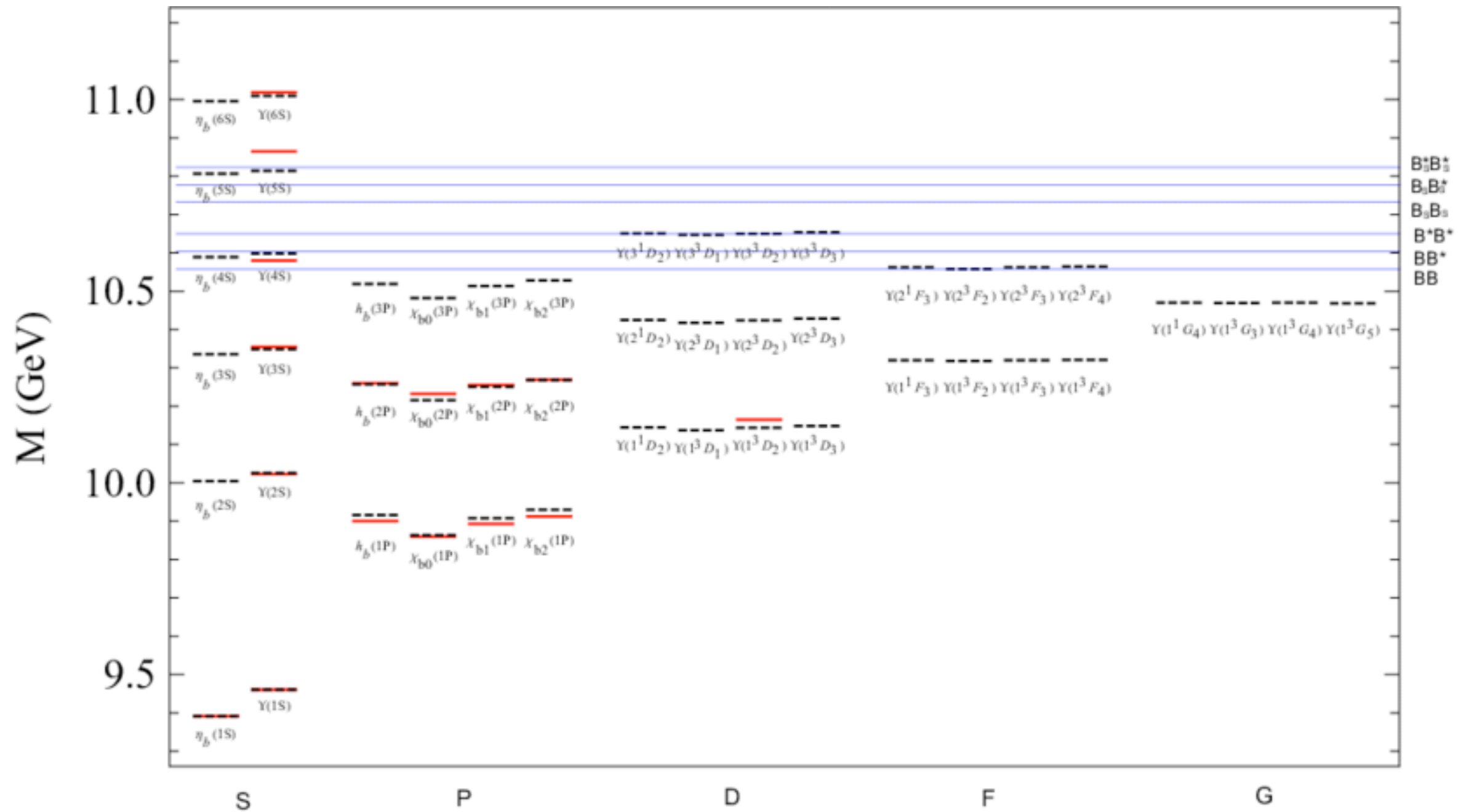


$B^*\bar{B}$



$B^*\bar{B}^*$

# B(\*)B(\*) thresholds





# Exotic states

- Many other possible states beyond Zb states are expected

