Critical fluctuations studied with HADES

30/11/2021 FANI-2021 | R. Holzmann (GSI) for the HADES collaboration



- proton detection in HADES
- centrality estimators
- cumulants & correlators
- volume fluctuation corrections
- conclusions & outlook

HADES Au+Au at $\sqrt{s_{NN}} = 2.41$ GeV → Adamczewski-Musch et al. PRC 102 (2020)

Ag+Ag at $\sqrt{s_{NN}}$ = 2.55 GeV → analysis in progress ...

The HADES detector at GSI



Event cleaning in HADES

Segmented gold target:

- ¹⁹⁷Au material
- 15 discs of Ø = 2.2 mm mounted on kapton strips
- Δz = 3.6 mm
- 2.0% interaction prob.



Kindler et al., NIM A 655 (2011) 95

Remove Au+C bkgd on the kapton with a cut on $ERAT = \sum E_t / \sum E_l$



Particle ID in HADES





Hadron ID based on

- ToF
- momentum
- dE/dx





Proton fluctuation signal purity



Centrality selection with the Forward Wall



cross section of 1/6 HADES sector

4x4, 8x8, 16x16 cm² tiles

Proton distributions in Au+Au at $\sqrt{s} = 2.41 \ GeV$

HADES $y - p_t$ coverage for protons



E-by-E efficiency-corrected moments in Au+Au



From the moments we can calculate

- factorial moments
- cumulants
- reduced cumulants
- factorial cumulants - etc.

but ...

... are dominated by e-by-e variations of the source volume!

Centrality estimators in HADES



Volume fluctuation corrections (VFC)

V. Skokov, B. Friman & K. Redlich PRC 88 (2013), A. Rustamov et al. NPA 960 (2017), Sugiura, Nonaka & Esumi PRC 100 (2019), Esumi & Nonaka NIM A987 (2021)

Averaging the volume-dependent proton distribution moments

$$< N_{prot}^{n} > = \int P(V) \sum_{V \in V} \frac{N_{prot}^{n} P(N_{prot} | V) dV}{\langle N_{prot}^{n} \rangle_{V}}$$

one obtaines volume contributions to the observed reduced cumulants c_n :

observed true
$$c_1 = \kappa_1$$

$$c_2 = \kappa_2 + \kappa_1^2 v_2 \tag{2}$$

$$c_3 = \kappa_3 + \kappa_1^3 v_3 + 3\kappa_1 \kappa_2 v_2 \tag{3}$$

$$c_4 = \kappa_4 + \kappa_1^4 v_4 + 6\kappa_1^2 \kappa_2 v_3 + \left(4\kappa_1 \kappa_3 + 3\kappa_2^2\right) v_2 \tag{4}$$

where κ_n are true reduced cumulants, c_n are observed cumulants and ν_n are volume cumulants, and <u>assuming all κ_n are constant</u>! (1)

Reduced proton cumulants in transport models



→ Extend formalism to NLO: $\kappa_n \rightarrow \kappa_n + \kappa'_n \cdot (V - \overline{V})$ and N2LO: $\kappa_n \rightarrow \kappa_n + \kappa'_n \cdot (V - \overline{V}) + \kappa''_n (V - \overline{V})^2$

details given in Adamczewski-Musch et al. PRC 102 (2020)

Ad-hoc approach: N_{hit} as a proxy for N_{part}



IQMD simulation shows that N_{hit} is proportional to N_{part}

→ use N_{hit} as proxy for vol. flucs. i.e. rescale & adjust the v_n

Observed N_{hit} distributions (selected on FW) Reconstructed N_{part} distributions



Reduced proton cumulants in Au+Au data: $y = y_0 \pm 0.2$



- Vol. fluct. Corr. (VFC) are important!
- NLO terms are needed!
- Eventually, also N2LO terms

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Volume correction of proton nb. moments: IQMD scaled & adjusted N_{hit} K_{vol}



HADES, PRC 102 (2020)

Volume correction of proton nb. moments: IQMD scaled & adjusted N_{hit} K_{vol}



HADES, PRC 102 (2020)

Au+Au data: N2LO corrected cumulants & correlators



<N> scaling of volume-corrected correlators C_k

B. Ling & M. Stephanov PRC 93 (2016)

consider two extreme scenarios:

- (1) $\Delta y_{corr} \ll \Delta y \rightarrow C_n \propto \Delta y$
- (2) $\Delta y_{corr} \gg \Delta y \rightarrow C_n \propto (\Delta y)^n$





Alternative $N_{hit} \rightarrow N_{part}$ transformations based on a Glauber Monte Carlo



→ compute the $\kappa(N_{part})$ from the $\kappa(N_{hit})$ and expand N_{part}

 \rightarrow do a Bayesian reconstruction of the N_{part} distribution

True Poissonian process: $N_{hit} = Poisson(\lambda N_{part})$

Applying **total cumulance** to $X = N_{hit} = Poisson(X|_{Z=Npart})$ we obtain an analytic relation between the cumulants of N_{hit} and N_{part} :

See also Broniowski & Olszewski, PRC95 (2017)

$$\kappa_n[N_{hit}] = \sum_{i=1}^n \lambda^i S_2(n,i) \kappa_i[N_{part}]$$
 (1)

With the inverse:

$$\kappa_n[N_{part}] = \sum_{i=1}^n \lambda^{-i} S_1(n,i) \kappa_i[N_{hit}]$$
 (2)

where ${\rm S}_1$ and ${\rm S}_2$ are Stirling numbers



Bayesian reconstruction of centrality

PHYSICAL REVIEW C 97, 014905 (2018)

Relating centrality to impact parameter in nucleus-nucleus collisions

Sruthy Jyothi Das,12 Giuliano Giacalone,3 Pierre-Amaury Monard,1 and Jean-Yves Ollitrault1

PHYSICAL REVIEW C 98, 024902 (2018)

Editors' Suggestion

Reconstructing the impact parameter of proton-nucleus and nucleus-nucleus collisions

Rudolph Rogly, 12 Giuliano Giacalone,1 and Jean-Yves Ollitrault1

PHYSICAL REVIEW C 104, 034609 (2021)

Model independent reconstruction of impact parameter distributions for intermediate energy heavy ion collisions

J. D. Frankland 0,1," D. Gruver,7 E. Bonnet, B. Borderie, R. Bougault,2 A. Chbihi, J. E. Ducret, D. Durand,2 Q. Fable,² M. Henri,¹ J. Lemarié,¹ N. Le Neindre,² I. Lombardo,³ O. Lopez,² L. Manduci,^{2,6} M. Párlog,^{2,7} J. Quicray,2 G. Verde,1.8 E. Vient,2 and M. Vigilante8 (INDRA Collaboration)

Ollitrault et al.

- validated with
- simulations and applied to LHC data

INDRA collab.

 validated with low-energy GANIL data E_{beam}<100 MeV/u

Apply Bayes' theorem $\rightarrow P(B|A) = P(A|B) P(B)/P(A)$

Setting $A = N_{hit}$, $B = N_{part}$ with

- $P(B|A) \leftrightarrow \text{prob of } N_{\text{part}} \text{ for given } N_{\text{hit}} \leftarrow \text{to be reconstructed}$
- $P(A|B) \leftrightarrow \text{prob of } N_{hit} \text{ for given } N_{part} \leftarrow Glauber \text{ fit to } N_{hit} \text{ data}$
- $P(A) \leftrightarrow \min \text{ bias } N_{hit} \text{ distribution } \leftarrow \text{ data}$
- $P(B) \leftrightarrow \min \text{ bias } N_{\text{part}} \text{ distribution}$

- ← Glauber

minimal model (Glauber MC)

Glauber-based Monte Carlo of Au+Au data

for details, see HADES centrality paper EPJA 54 (2018)



Bayesian reconstruction of centrality

For the $N_{hit} \rightarrow N_{part}$ reconstruction we follow Frankland et al. PRC 104 (2021):

 $P(N_{part}|FW_c) = \frac{\sum_{N_{hit}} P(N_{hit}|N_{part}) P(N_{part}) w(FW_c \& LVL1 \& 2D)}{\sum_{N_{hit}} P(N_{hit}|FW_c)}$



Volume correction of proton nb. moments: Bayesian $N_{hit} \rightarrow N_{part}$



HADES re-analysis November 2021

Volume correction of proton nb. moments: Bayesian $N_{hit} \rightarrow N_{part}$



HADES re-analysis November 2021

HADES vs STAR: status of 2020



IQMD rescaled N_{hit} (used in HADES PRC 102 paper)

Note that STAR updated their data in 2021! → PRL & PRC 104

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Comparison with STAR 2021



STAR sees a "non-monotonic" trend of K_4/K_2 with N_{part} which they interpret as a sign of possible critical behavior

PRL (2021), PRC 104 (2021)

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Comparison with STAR 2021



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Hadron Resonance Gas + van der Waals forces

PHYSICAL REVIEW C 98, 024910 (2018)

Critical point of nuclear matter and beam-energy dependence of net-proton number fluctuations



Volodymyr Vovchenko,^{1,2} Lijia Jiang,² Mark I. Gorenstein,^{2,3} and Horst Stoecker^{1,2,4}

Proton cumulants: forward vs backward rapidities

Bayesian $N_{hit} \rightarrow N_{part}$



HADES re-analysis November 2021

Systematics!

Summary and Outlook:

- Analyzed proton number fluctuations with HADES in 1.23 AGeV Au+Au collisions
- Applied full (N2LO) volume corrections to observed proton cumulants using different N_{hit} → N_{part} transforms
- Found indications for strong long-range correlations (>1 in rapidity)

→ absolutely need to control volume corrections!
→ remnant effects of liquid-gas phase transition?
→ bound vs free protons?

→ very high-statistics Ag+Ag data are available for analysis
 → beam-energy scan <1 AGeV (SIS18) & >2 AGeV (SIS100)

Extra slides

How do bound protons contribute?

 $\begin{array}{c} \bullet \text{ STAR 0-10\% d/p} \\ \bullet \text{ STAR 0-10\% d/p} \\ \bullet \text{ STAR 0-10\% d/p} \\ \bullet \text{ EOS802 d/p} \\ = \text{ T} = 162.6 \pm 4.9 \text{ MeV} \\ \bullet \text{ NA49 d/p} \\ \hline \text{ PHENIX d/p} \\ \hline \text{ PHENIX d/p} \\ \hline \text{ PHENIX d/p} \\ \bullet \text{ ALICE d/p} \\ \hline \text{ 10^{-2}} \\ 10^{-3} \\ \hline \text{ 10^{-2}} \\ \hline \text{ 10^{$

Systematics of d/p from STAR collaboration (QM2017)



HADES 1.23 GeV/u Au+Au data

 $d/p \approx 0.37$ in 0-10% most central

Large fraction of protons are bound in nuclei: d, t, He, etc.

How do they contribute to proton-number fluctuations?

Investigation of light nucleus production in Au+Au is ongoing (M. Szala & M. Lorenz)

Correlations of N_{prot} & centrality selection



Pearson's linear correlation coefficient: $\rho_{xy} = \frac{cov(x,y)}{\sqrt{var(x) var(y)}}$

 \rightarrow Non-zero correlations have a damping effect volume fluctuations!

Correlations & volume fluctuations



A centrality selection on nb. of tracks is problematic

If N_{trks} and N_{prot} are correlated, a cut on N_{trks} will reduce the width of the selected proton distribution

Volume fluctuation cumulants v_n are modified by correlations!

Extended (NLO) Skokov volume corrections

 $c_1 = \kappa_1 + \kappa_1' v_2$ (1) $c_2 = \kappa_2 + \kappa_1^2 v_2 + \kappa_2' v_2 + 2\kappa_1 \kappa_1' V_2 + 2\kappa_1 \kappa_1' v_3$ (2) $+ 2\kappa_1^{\prime 2}v_2V_2 + \kappa_1^{\prime 2}V_1V_2 + 2\kappa_1^{\prime 2}V_3 + \kappa_1^{\prime 2}v_4$ $c_{3} = \kappa_{3} + \kappa_{1}^{3} v_{3} + 3\kappa_{1} \kappa_{2} v_{2} + 3(\kappa_{1} \kappa_{2}' + \kappa_{1}' \kappa_{2}) v_{3} + 6\kappa_{1}' (\kappa_{1}^{2} + \kappa_{2}') v_{2} V_{2}$ $+3\kappa_1'(\kappa_1^2+2\kappa_2')V_3+3\kappa_1'(\kappa_1^2+\kappa_2')v_4+12\kappa_1\kappa_1'^2V_2^2+3\kappa_1\kappa_1'^2V_1V_3$ $+24\kappa_1\kappa_1'^2v_2V_3+6\kappa_1\kappa_1'^2V_4+3\kappa_1\kappa_1'^2v_5+3(\kappa_1\kappa_2'+\kappa_1'\kappa_2)V_2$ (3) $+8\kappa_{1}^{\prime3}v_{2}V_{2}^{2}+6\kappa_{1}^{\prime3}V_{1}V_{2}^{2}+10\kappa_{1}^{\prime3}v_{3}V_{3}+\kappa_{1}^{\prime3}V_{1}^{2}V_{3}+24V_{2}V_{3}\kappa_{1}^{\prime3}V_{1}^{2}V_{3}+24V_{2}V_{3}\kappa_{1}^{\prime3}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}V_{3}+V_{2}+V_{2}V_{3}+V_{2}+V$ $+3\kappa_{1}^{\prime3}V_{1}V_{4}+12\kappa_{1}^{\prime3}v_{2}V_{4}+3\kappa_{1}^{\prime3}V_{5}+\kappa_{1}^{\prime3}v_{6}+3\kappa_{1}^{\prime}\kappa_{2}^{\prime}V_{1}V_{2}+\kappa_{2}^{\prime}v_{2}$ $c_4 = \kappa_4 + \kappa_1^4 v_4 + 6\kappa_1^2 \kappa_2 v_3 + (4\kappa_1 \kappa_3 + 3\kappa_2^2) v_2 + 24 (\kappa_1^3 \kappa_1' + 4\kappa_1 \kappa_1' \kappa_2' + 2\kappa_1'^2 \kappa_2) v_2 V_3$ + 4 $\left(\kappa_{1}^{3}\kappa_{1}'+6\kappa_{1}\kappa_{1}'\kappa_{2}'+3\kappa_{1}'^{2}\kappa_{2}\right)V_{4}$ + 2 $\left(2\kappa_{1}^{3}\kappa_{1}'+6\kappa_{1}\kappa_{1}'\kappa_{2}'+3\kappa_{1}'^{2}\kappa_{2}\right)v_{5}$ + 48 $\left(\kappa_{1}^{2}\kappa_{1}^{\prime2}+\kappa_{1}^{\prime2}\kappa_{2}^{\prime}\right)v_{2}V_{2}^{2}+12\left(4\kappa_{1}^{2}\kappa_{1}^{\prime2}+5\kappa_{1}^{\prime2}\kappa_{2}^{\prime}\right)v_{3}V_{3}$ + 72 $(\kappa_1^2 \kappa_1'^2 + 2\kappa_1'^2 \kappa_2') V_2 V_3 + 6 (\kappa_1^2 \kappa_1'^2 + 3\kappa_1'^2 \kappa_2') V_1 V_4 + 72 (\kappa_1^2 \kappa_1'^2 + \kappa_1'^2 \kappa_2') v_2 V_4$ + 6 $\left(2\kappa_1^2\kappa_1'^2 + 3\kappa_1'^2\kappa_2'\right)V_5$ + 6 $\left(\kappa_1^2\kappa_1'^2 + \kappa_1'^2\kappa_2'\right)v_6$ $+2\left(6\kappa_{1}^{2}\kappa_{2}^{\prime}+12\kappa_{1}\kappa_{1}^{\prime}\kappa_{2}+4\kappa_{1}^{\prime}\kappa_{3}^{\prime}+3\kappa_{2}^{\prime2}\right)v_{2}V_{2}$ + 2 $(3\kappa_1^2\kappa_2' + 6\kappa_1\kappa_1'\kappa_2 + 4\kappa_1'\kappa_3' + 3\kappa_2'^2)V_3$ + 2 $(3\kappa_1^2\kappa_2 + 2\kappa_1\kappa_3' + 2\kappa_1'\kappa_3 + 3\kappa_2\kappa_2')v_3$ + $(6\kappa_1^2\kappa_2' + 12\kappa_1\kappa_1'\kappa_2 + 4\kappa_1'\kappa_3' + 3\kappa_2'^2)v_4 + 96\kappa_1\kappa_1'^3V_2^3 + 96\kappa_1\kappa_1'^3V_3^2$ (4)+ $288\kappa_1\kappa_1'^3v_3V_2^2$ + $72\kappa_1\kappa_1'^3V_1V_2V_3$ + $4\kappa_1\kappa_1'^3V_1^2V_4$ + $144\kappa_1\kappa_1'^3V_2V_4$ + $128\kappa_1\kappa_1'^3v_3V_4$ + $12\kappa_1\kappa_1'^3V_1V_5$ + $72\kappa_1\kappa_1'^3v_2V_5$ + $12\kappa_1\kappa_1'^3V_6$ + $4\kappa_1\kappa_1'v_7$ + 24 $(2\kappa_1\kappa_1'\kappa_2' + \kappa_1'^2\kappa_2)V_2^2$ + 6 $(2\kappa_1\kappa_1'\kappa_2' + \kappa_1'^2\kappa_2)V_1V_3$ + 2 $(2\kappa_1\kappa_3' + 2\kappa_1'\kappa_3 + 3\kappa_2\kappa_2')V_2 + 48\kappa_1'^4v_2V_2^3 + 48\kappa_1'^4V_1V_2^3 + 48\kappa_1'^4V_1V_2^3$ $+240\kappa_{1}^{\prime4}v_{2}V_{3}^{2}+32\kappa_{1}^{\prime4}v_{4}V_{4}+288\kappa_{1}^{\prime4}V_{2}^{2}V_{3}+24\kappa_{1}^{\prime4}V_{1}^{2}V_{2}V_{3}+\kappa_{1}^{\prime4}V_{1}^{3}V_{4}$ $+ 144\kappa_{1}^{\prime4}v_{4}V_{2}^{2} + 72\kappa_{1}^{\prime4}V_{1}V_{2}V_{4} + 128\kappa_{1}^{\prime4}V_{3}V_{4} + 4\kappa_{1}^{\prime4}V_{1}^{2}V_{5} + 72\kappa_{1}^{\prime4}V_{2}V_{5}$ $+56\kappa_1'^4v_3V_5+6\kappa_1'^4V_1V_6+24V_2V_6\kappa_1'^4v_2V_6+4\kappa_1'^4V_7+\kappa_1'^4v_8+36\kappa_1'^2\kappa_2'V_1V_2^2$ $+ 6\kappa_1^{\prime 2}\kappa_2^{\prime}V_1^2V_3 + 4\kappa_1^{\prime}\kappa_3^{\prime}V_1V_2 + 3\kappa_2^{\prime 2}V_1V_2 + \kappa_4^{\prime}v_2$

Where the v_n are reduced volume, i.e. $N_{part,}$ cumulants, and the κ_n and κ_n' are obtained by fitting eq. (1) - (4) to the measured proton cumulants c_n

Note that v_n terms appear now up to 8th order!

NLO corr. proton moments in Au+Au data: $y = y_0 \pm 0.05$



Re-analysis of the proton fluctuations: proton correlators (IQMD based N_{part})



As published in PRC 102 (2020)

Re-analysis of the proton fluctuations: proton correlators (Poisson+CF of N_{part})



The n-particle correlators are very robust!

Re-analysis of the proton fluctuations: proton correlators (Bayesian N_{part})



The n-particle correlators are very robust!!