

# Cutting-edge issues of multi-dimensional core-collapse supernova simulations

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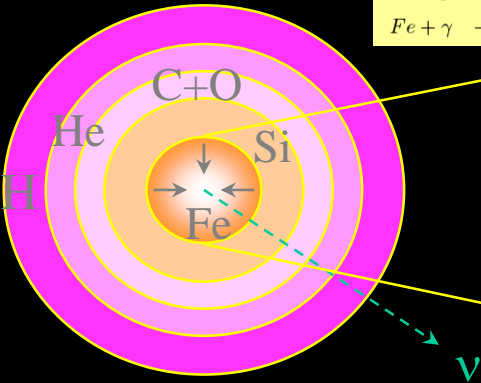
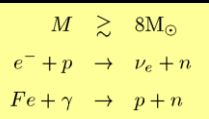
with Tomoya Takiwaki (NAOJ), Takami Kuroda(NAOJ), Yudai Suwa (Kyoto)  
Nobuya Nishimura (Univ. Basel), and Ko Nakamura (NAOJ)

NIC XII; satellite workshop on r-process  
nucleosynthesis

# Standard scenario of core-collapse SNe

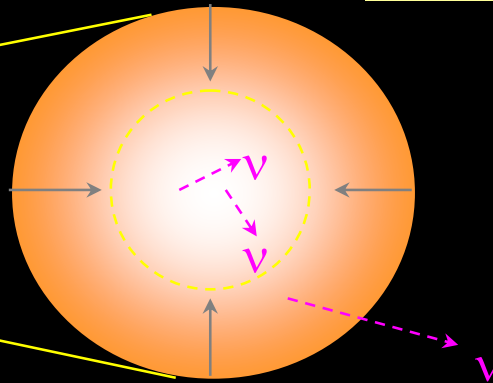
(e.g., Kotake+06, Janka+07 for a review)

core collapse



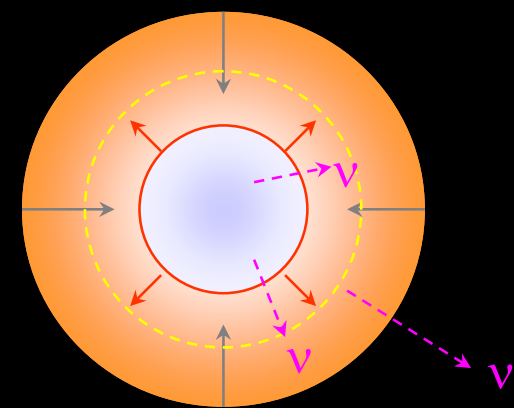
$\nu$  trapping

$$\rho_c \sim 10^{12} \text{g/cm}^3$$



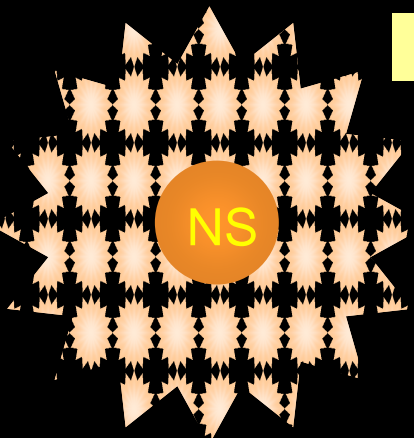
core bounce

$$\rho_c \sim 3 \times 10^{14} \text{g/cm}^3$$

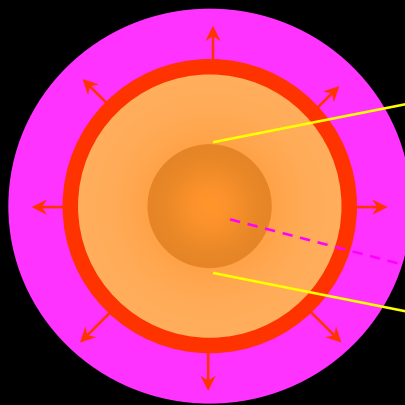


SN explosion

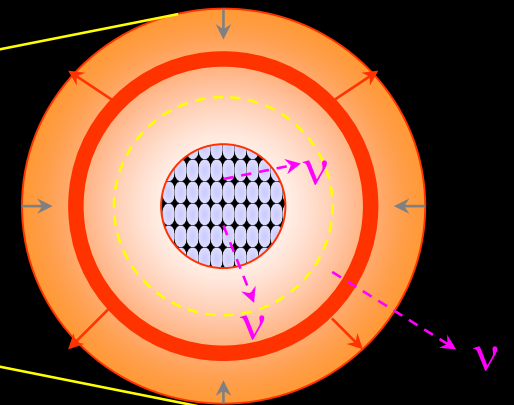
$$E_{exp} \sim 10^{51} \text{erg}$$



shock in envelope



shock propagation in core



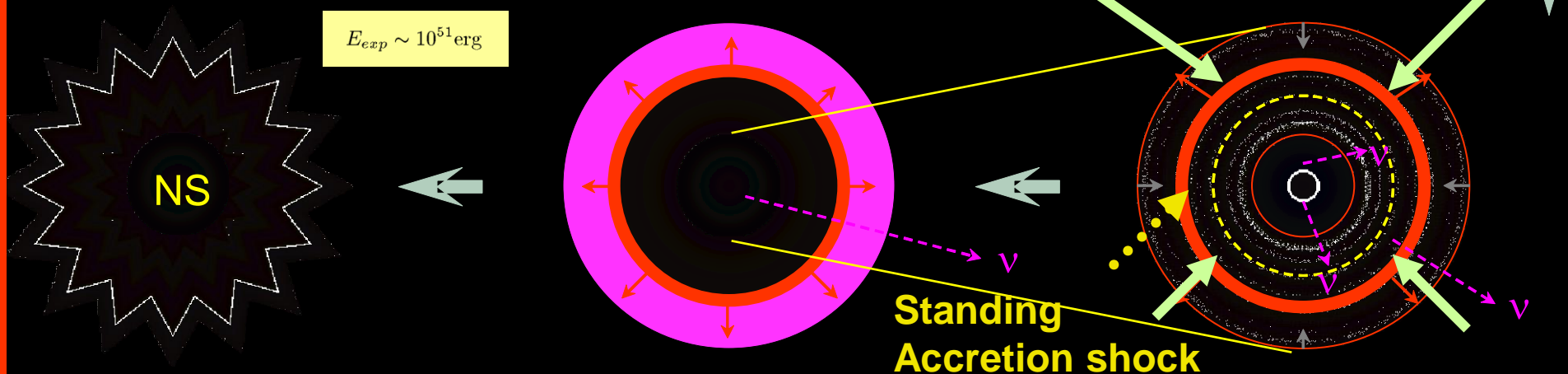
# Standard scenario of core-collapse SNe

- ✓ Have to find the way to revive the stalled bounce shock.
- ✓ The best-studied & most promising:  
**the neutrino-heating mechanism** (Bethe, Wilson 1985)  
: **neutrinos heat material to produce explosions.**
- ✓ Except for special cases (Kitaura + (06)), the simplest, 1D form of this mechanism does not work.  
(Liebendoerfer et al. (2001), Rampp & Janka (2000), Sumiyoshi et al. (2005))

SN explosion

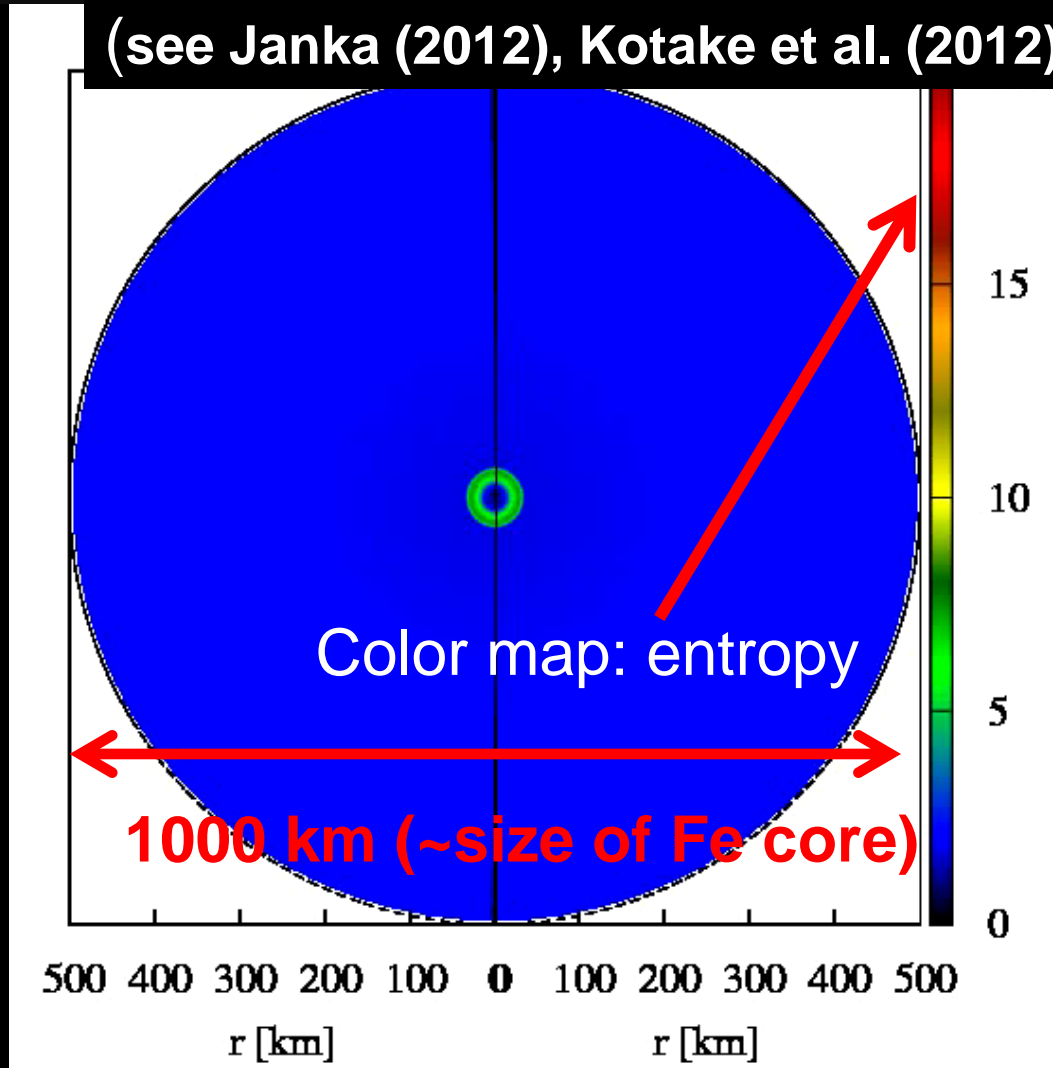
shock in envelope

shock propagation in core



# Current paradigm: multi-D neutrino-heating mechanism

(see Janka (2012), Kotake et al. (2012) for recent reviews)



**Suwa, KK+ (10,11)**  
15  $M_{\text{sun}}$  star (WW95)  
✓ 2D rad. hydro core-collapse simulation with spectral neutrino transport  
✓ Lattimer-Swesty EOS (K=180MeV)

- ✓ After bounce, the bounce shock stalls.
- ✓ “Standing Accretion Shock Instability (SASI)” develops.

- ✓ The dwell timescales of matter in the gain region  $\Rightarrow$  much longer in multi-D.
- ✓ At around  $O(100)$ s ms after bounce, the neutrino-driven explosion occurs.

# List of recent milestones reported “explosions”

Kotake arXiv:110.5107 Comptes Rendus Physique in press

Progenitor	Group (Year)	Mechanism	Dim. (Hydro)	$t_{\text{exp}}$ (ms)	$E_{\text{exp}}(\text{B})$ @ $t_{\text{pb}}$ (ms)	$\nu$ transport (Dim, $\mathcal{O}(v/c)$ )
8.8 $M_{\odot}$ (NH88[71])	MPA[51] (2006)	$\nu$ -driven	1D (PN)	$\sim 200$	0.1 ( $\sim 800$ )	Boltzmann 2, $\mathcal{O}(v/c)$
	Princeton+ [74](2006)	$\nu$ -driven	2D (N)	$\lesssim 125$	0.1 -	MGFLD 1, (N)
10 $M_{\odot}$ (WHW02[72])	Basel[75] (2009)	$\nu$ +(QCD transition)	1D (GR)	255	0.44 (350)	Boltzmann 2, (GR)
11 $M_{\odot}$ (WW95[73])	Princeton+ [74](2006)	Acoustic	2D (N)	$\gtrsim 550$	$\sim 0.1^*$ (1000)	MGFLD 1, (N)
11.2 $M_{\odot}$ (WHW02[72])	MPA[76] (2006)	$\nu$ -driven	2D (PN)	$\sim 100$	$\sim 0.005$ ( $\sim 220$ )	”RBR” Boltz- mann, 2, $\mathcal{O}(v/c)$
	Princeton+ [77] (2007)	Acoustic	2D (N)	$\gtrsim 1100$	$\sim 0.1^*$ (1000)	MGFLD 1, (N)
	NAOJ+ [78](2011)	$\nu$ -driven	<b>3D</b> (N)	$\sim 100$	0.01 (300)	IDSA 1, (N)
12 $M_{\odot}$ (WHW02[72])	Oak Ridge+ [79](2009)	$\nu$ -driven	2D (PN)	$\sim 300$	0.3 (1000)	”RBR” MGFLD 1, $\mathcal{O}(v/c)$
13 $M_{\odot}$ (WHW02[72])	Princeton+ [77](2007)	Acoustic	2D (N)	$\gtrsim 1100$	$\sim 0.3^*$ (1400)	MGFLD 1, (N)
(NH88[71])	NAOJ+ [80](2010)	$\nu$ -driven	2D (N)	$\sim 200$	0.1 (500)	IDSA 1, (N)

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Progenitor	Group (Year)	Mechanism	Dim. (Hydro)	$t_{\text{exp}}$ (ms)	$E_{\text{exp}}$ (B) @ $t_{\text{pb}}$ (ms)	$\nu$ transport (Dim, $\mathcal{O}(v/c)$ )
15 $M_{\odot}$ (WW95[73])	MPA[81] (2009)	$\nu$ -driven	2D (PN)	$\sim 600$	0.025 ( $\sim 700$ )	Boltzmann 2, $\mathcal{O}(v/c)$
(WHW02[72])	Princeton+ [77]	Acoustic	2D (N)	-	- (-)	MGFLD 1, (N)
	OakRidge+ [79](2009)	$\nu$ -driven	2D (PN)	$\sim 300$	$\sim 0.3$ (600)	”RBR” MGFLD 1, $\mathcal{O}(v/c)$
20 $M_{\odot}$ (WHW02[72])	Princeton+ [77](2007)	Acoustic	2D (N)	$\gtrsim 1200$	$\sim 0.7^*$ (1400)	MGFLD 1, (N)

## ☆ Fundamental problems remained !

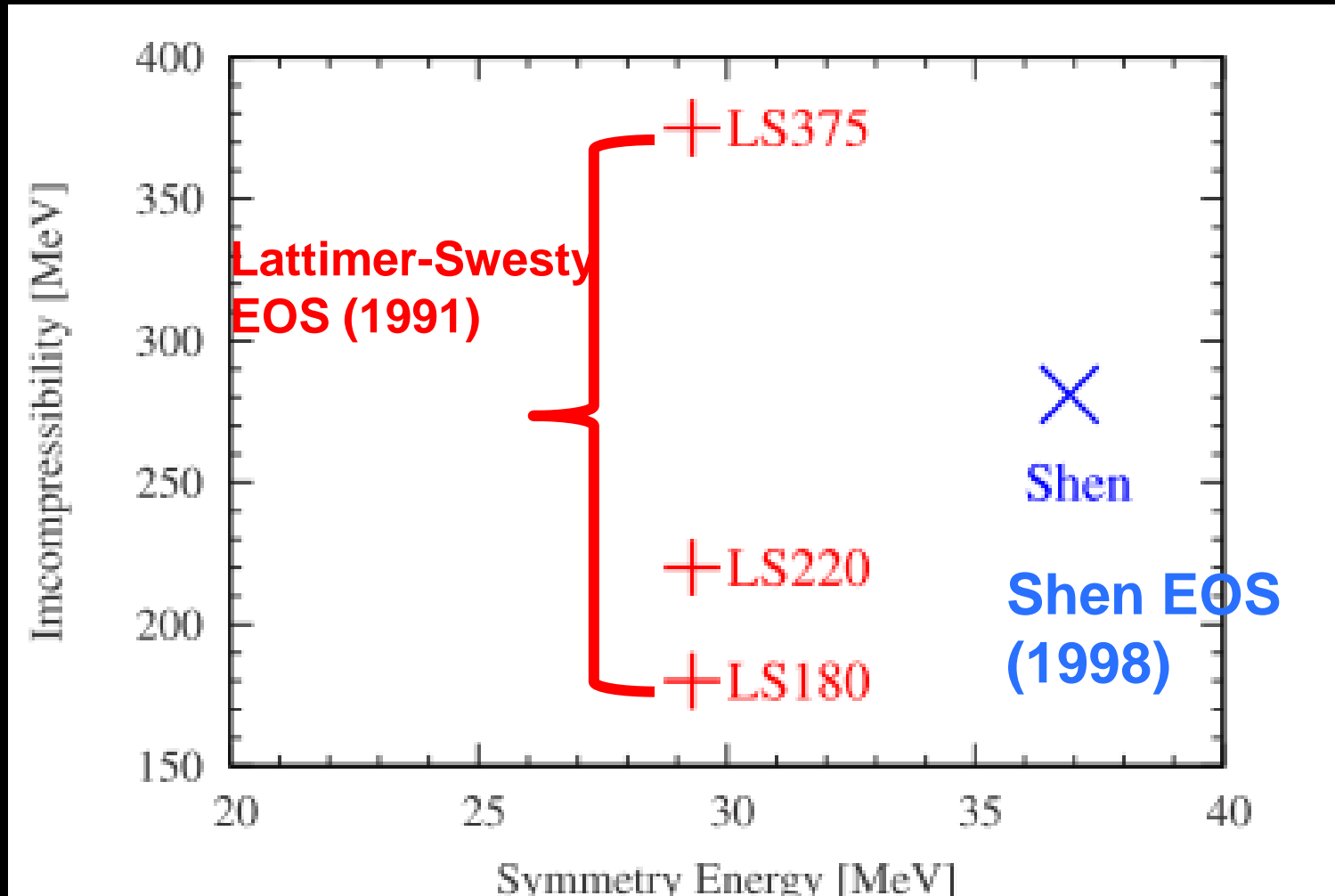
✓ The explosion energies are typically smaller by 1 or 2 orders-of-magnitudes compared to observation (SN kinetic energy of  $10^{51}$  erg).

✓ Most of the neutrino-driven exploding models have employed a very soft nuclear EOS (K=180 MeV).  
(K>220 MeV to explain the 2 Msun NS (e.g., Demorest+2010))

# 1<sup>st</sup> cutting-edge issue: Impacts of nuclear EOS

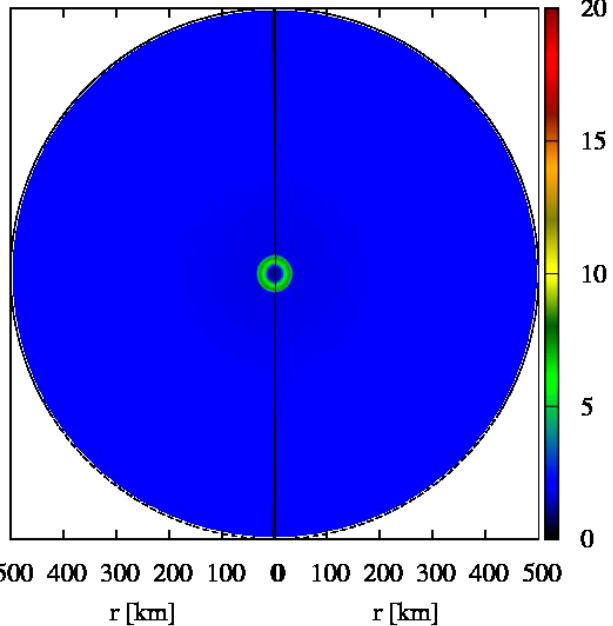
Suwa, Takiwaki, KK+ submitted to ApJ

## Features of SN EOS



@ saturation density

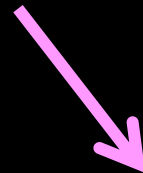
T= 188 ms



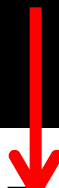
LS180



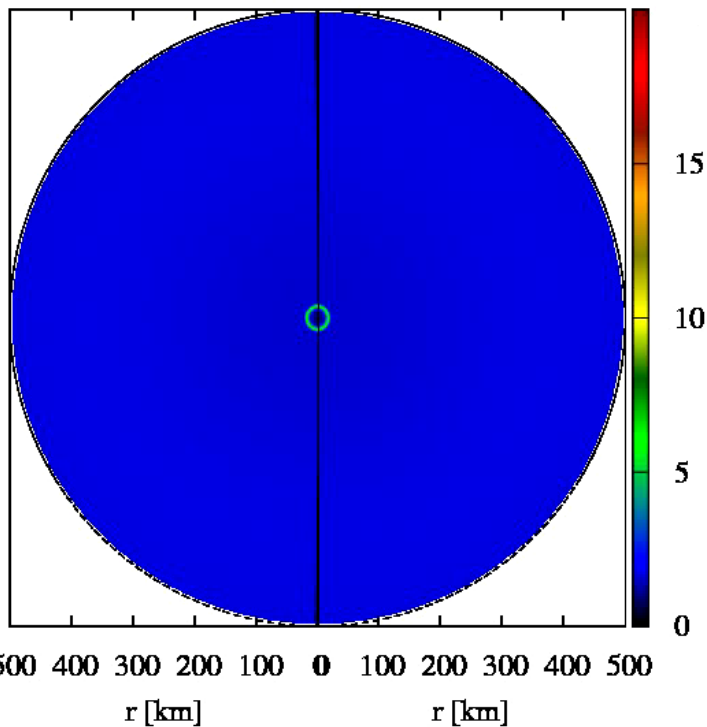
LS375



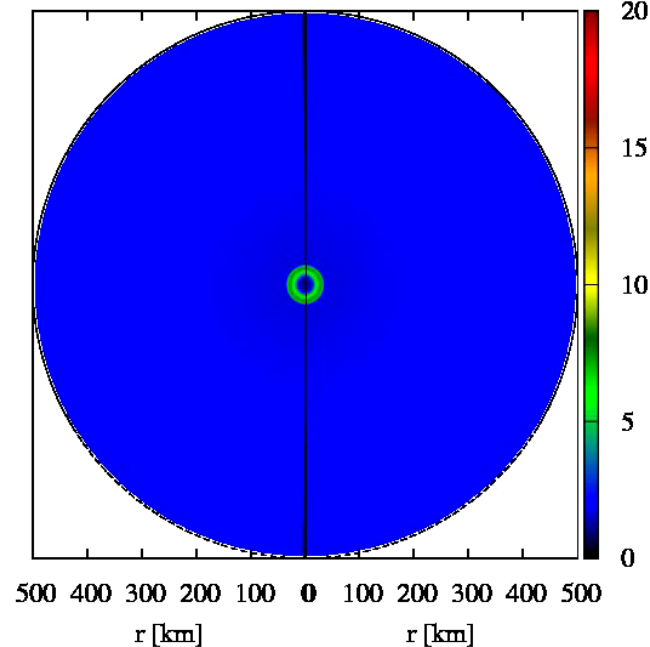
Shen



T= 154 ms



T= 185 ms



- ✓ Generally correct: easier to obtain explosions for softer EOSs.
- ✓ “K” is not the only quantity ! “symmetry energy” also important.

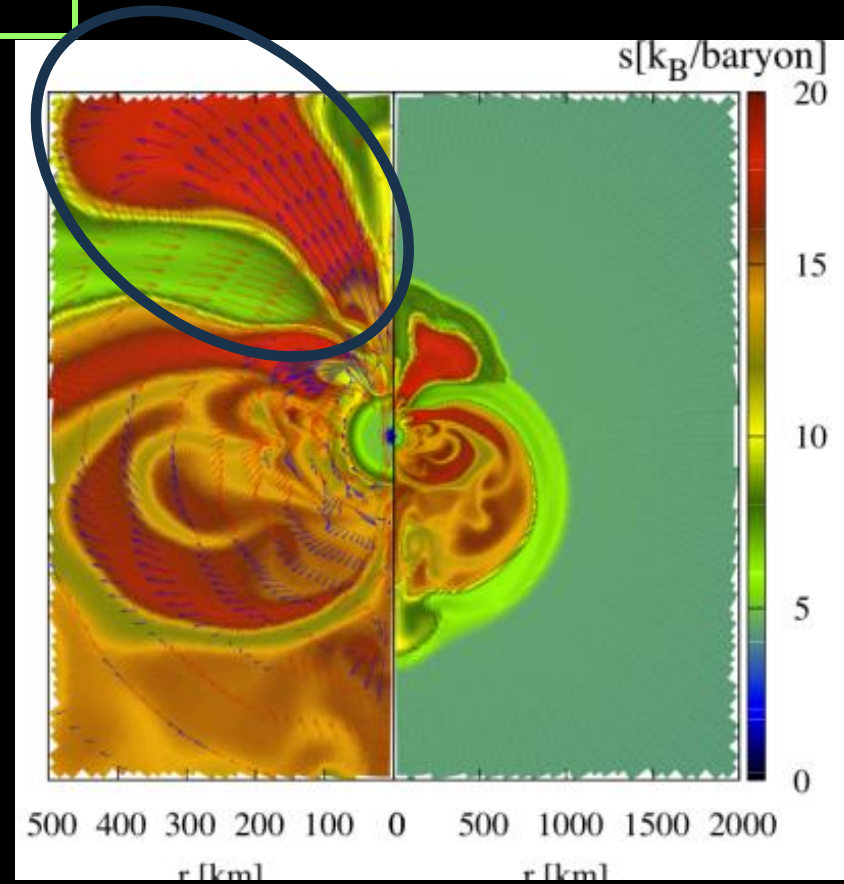
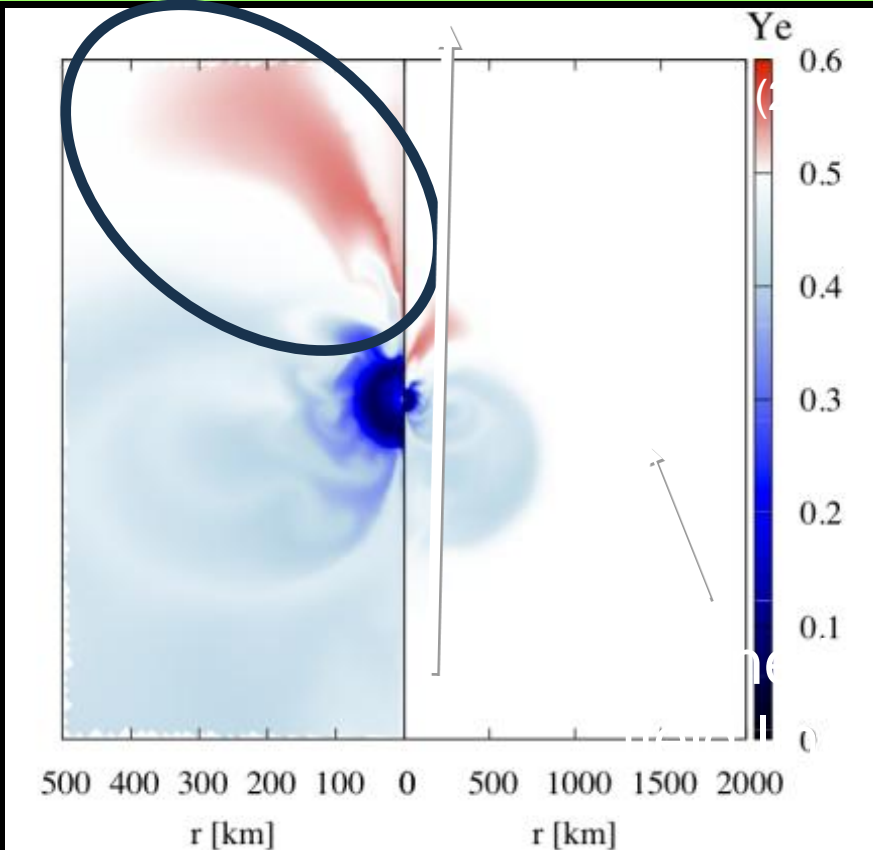
**1<sup>st</sup> issue**

⇒ details of nuclear forces  
:key

- ✓ Need precise description of nuclear theory!

# Ye profile in our 2D models (pioneered by Arcones et al. (2006) Fischer et al. (2010,2011), Arcones & Janka (2011), See talk by Arcones.)

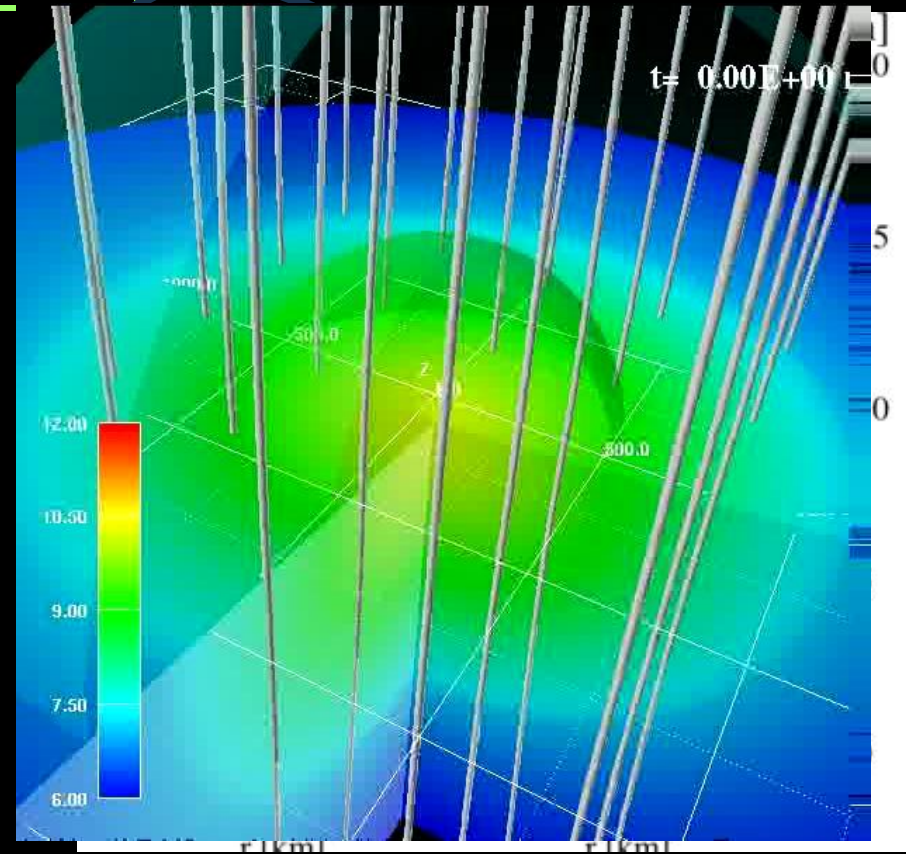
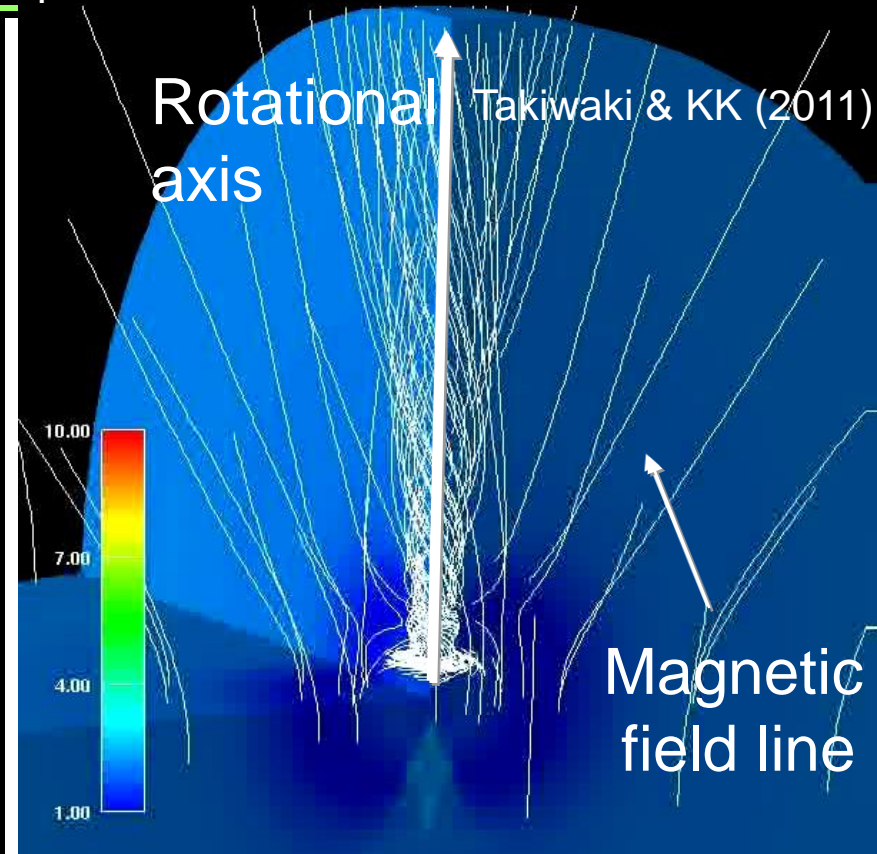
In the beginning of the neutrino-driven wind phase ( $t_{\text{pb}} \sim 550$  ms for  $15 M_{\text{sun}}$  progenitor (WW95))



- ✓ **The neutrino-driven wind  $\Rightarrow$  proton-rich in multi-D simulations.**  
(Interested in our multi-D data , Emails, start collaboration !)
- ✓ Link of MHD models to r-process cites(see talks by Thielemann, Nobuya)

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# A list of recent “rad-hydro” milestones making “explosions”

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- ✓ Still (far ...) behind to successfully produce explosions as energetic as  $10^{51}$  erg (= 1 Bethe)
- ✓ “Something” may be missing ....
- ✓ **Fostering the models needs new ideas/algorithms !**

[80](2010)

(N)

(500)

1, (N)

## 2<sup>nd</sup> cutting-edge issue: Multidimensionality

Is it easier to obtain explosions in 3D than in 2D !?

- ✓ 3D effects : very controversial.  
(Nordhaus+. (2010) Yes vs. Hanke+ (2011) No(so much) )
- ✓ In previous 3D simulations,  
the light-bulb scheme was employed. ( $L \nu = \text{const}$ )  
(neutrino heating was given by hand to trigger explosions).
- ✓ 3D simulations with spectral neutrino transport are (at least)  
needed to draw a robust conclusion.

### Our most up-to-date 3D results

Takiwaki, KK, and Suwa (2012) ApJ

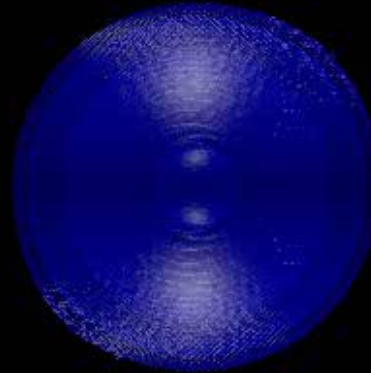
- ✓ 11.2 Msun progenitor (Woosley, Heger, Weaver (2002))
- ✓ Spectral neutrino transport is solved (IDSA: Liebendoerfer+09)
- ✓ 320(r)x64( $\theta$ )x128( $\phi$ )x20( $\epsilon$ ) (4 times finer than our ApJ paper)
- ✓ 8192 CPUs x 1 CPU month
- ✓ the world-2<sup>nd</sup> fastest “K” computers.



Animation hidden !  
Thanks to T. Wada (CfCA)

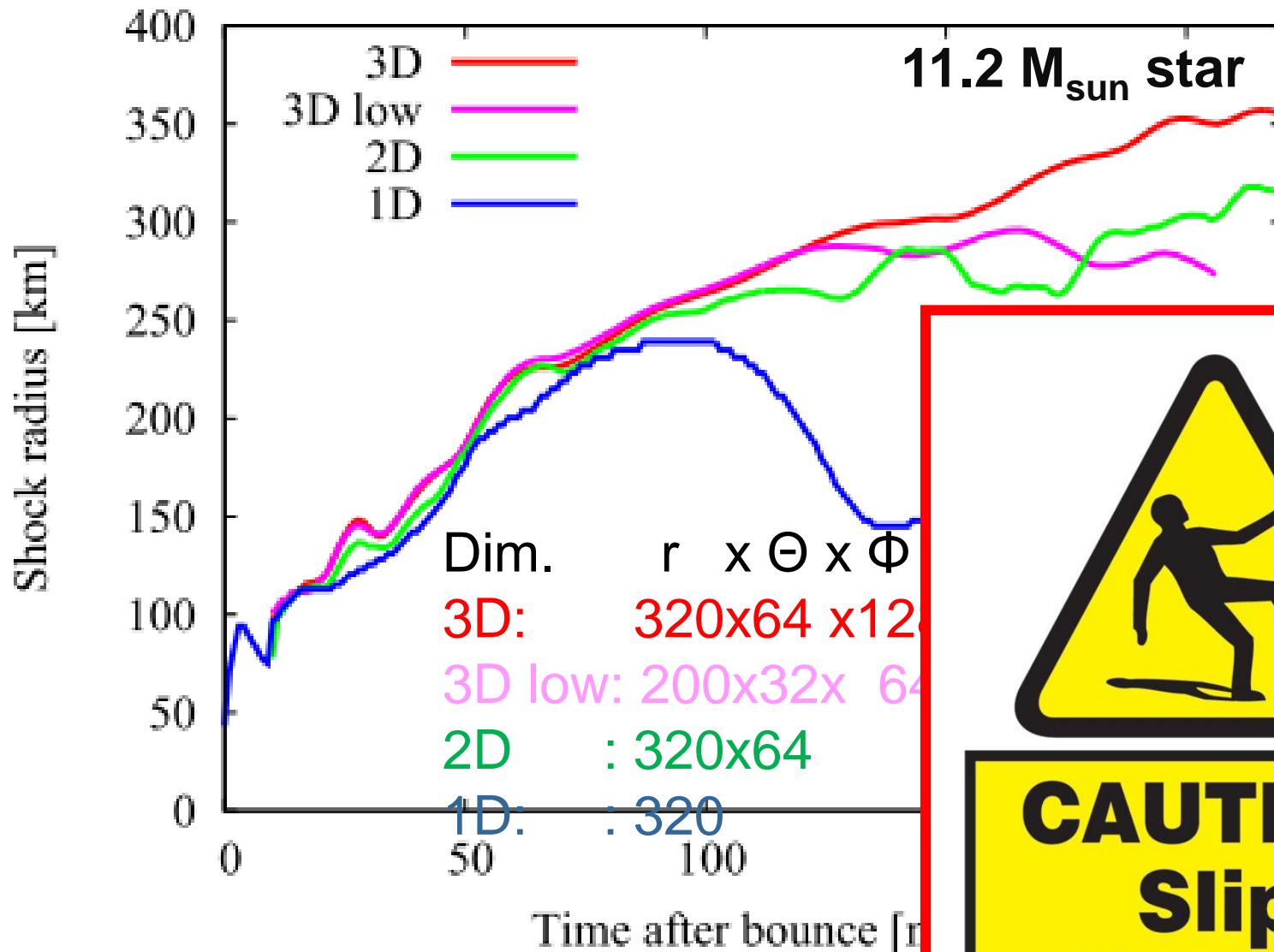
**3 msec**

Post-bounce time



Entropy (per baryon)

# Comparison of average shock radii

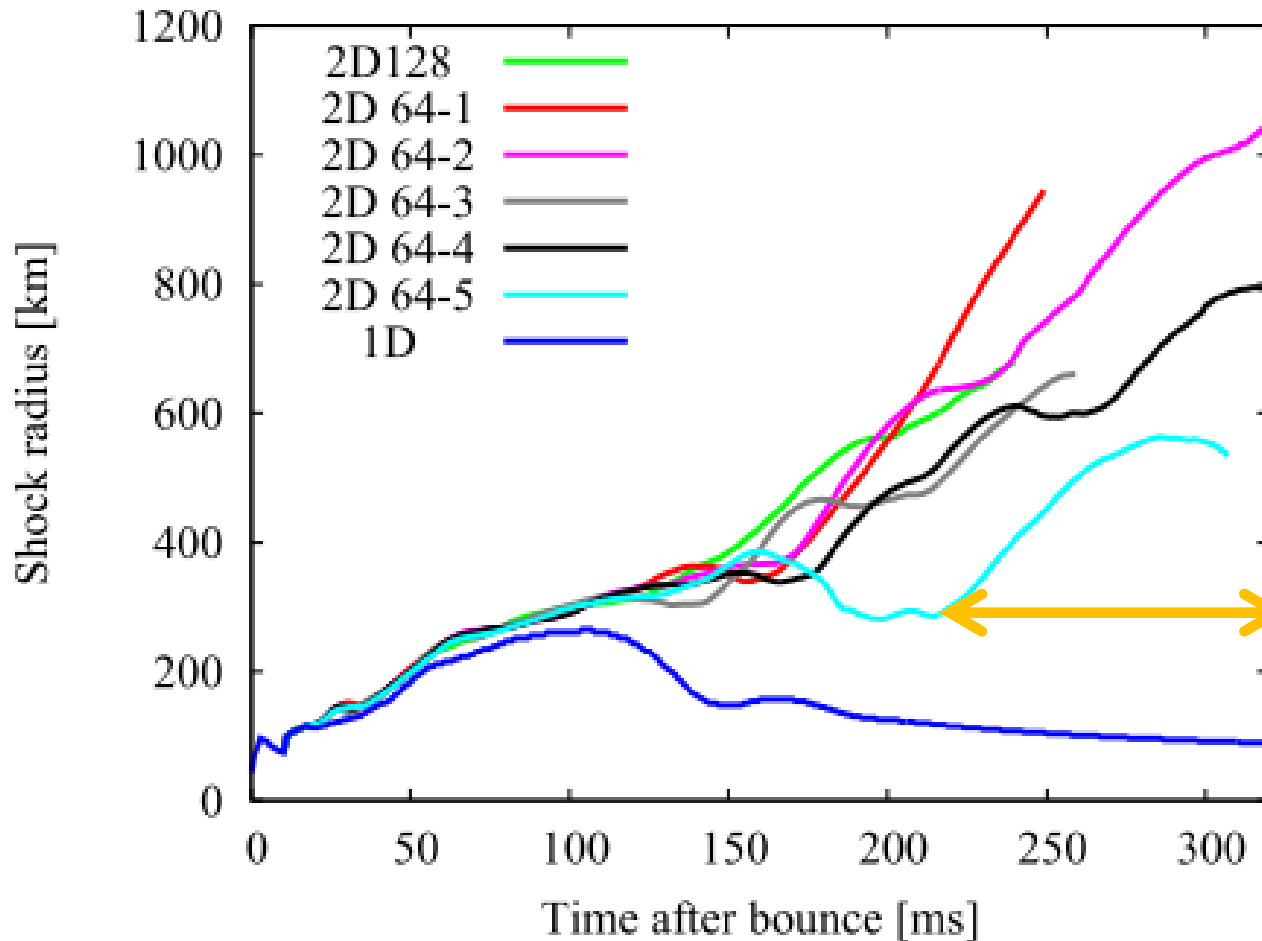


**CAUTION  
Slip  
Hazard**

✓ Our 3D model with highest resolution :  
the most energetic shock propagation.

# “Stochastic Nature” of neutrino-driven explosions

(see also KK+09, Iwakami+08)



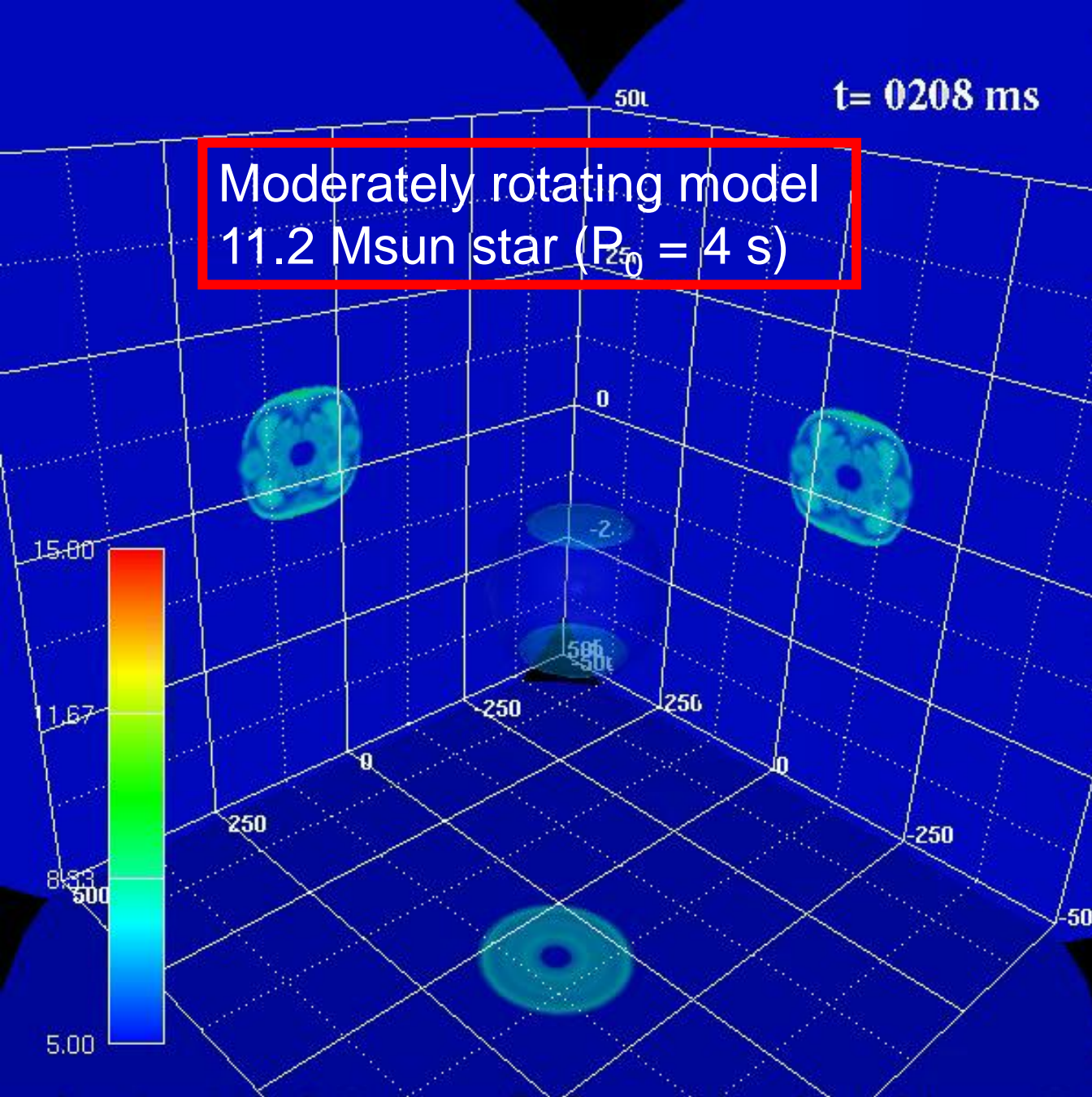
2D models with different random perturbations given after shock-stall (1% velocity perturbation)

- ✓ From only one realization of our 3D model, we cannot clearly figure out whether 3D is really helpful to produce explosions compared to 2D.
- ✓ Systematic study (num. resolution, perturbation) needed.
- ✓ Computationally hyper-expensive !

t= 0208 ms

Takiwaki, KK + in prep

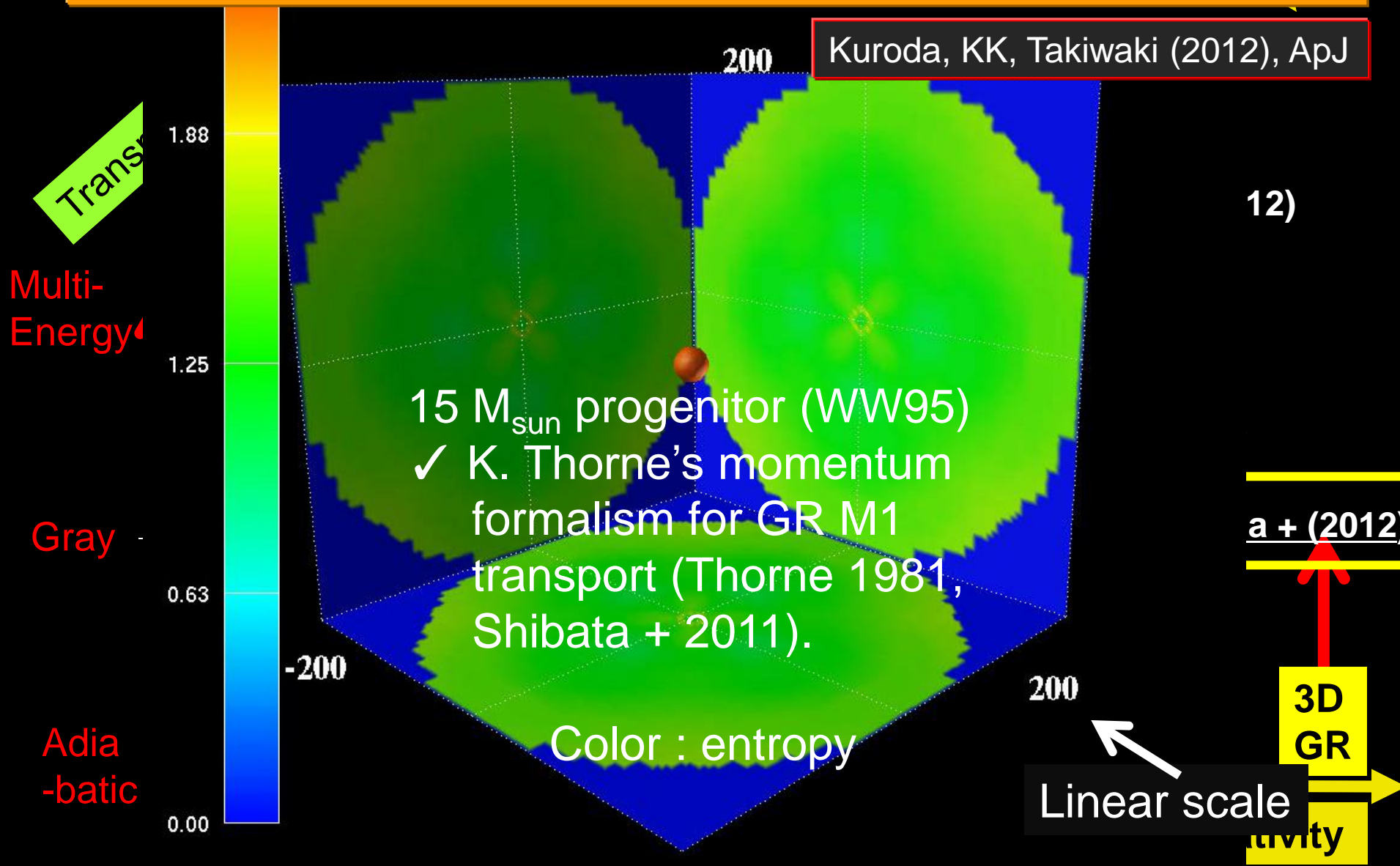
Moderately rotating model  
11.2 Msun star ( $P_0 = 4$  s)



Bipolar explosions:  
✓ Explosion energy higher !  
✓ Nucleosynthesis, neutrino, and GW signatures between rotating and non-rotating models exciting !

**3<sup>rd</sup> cutting-edge issue:  
Is general relativity (GR) helpful for explosions !?**

Kuroda, KK, Takiwaki (2012), ApJ

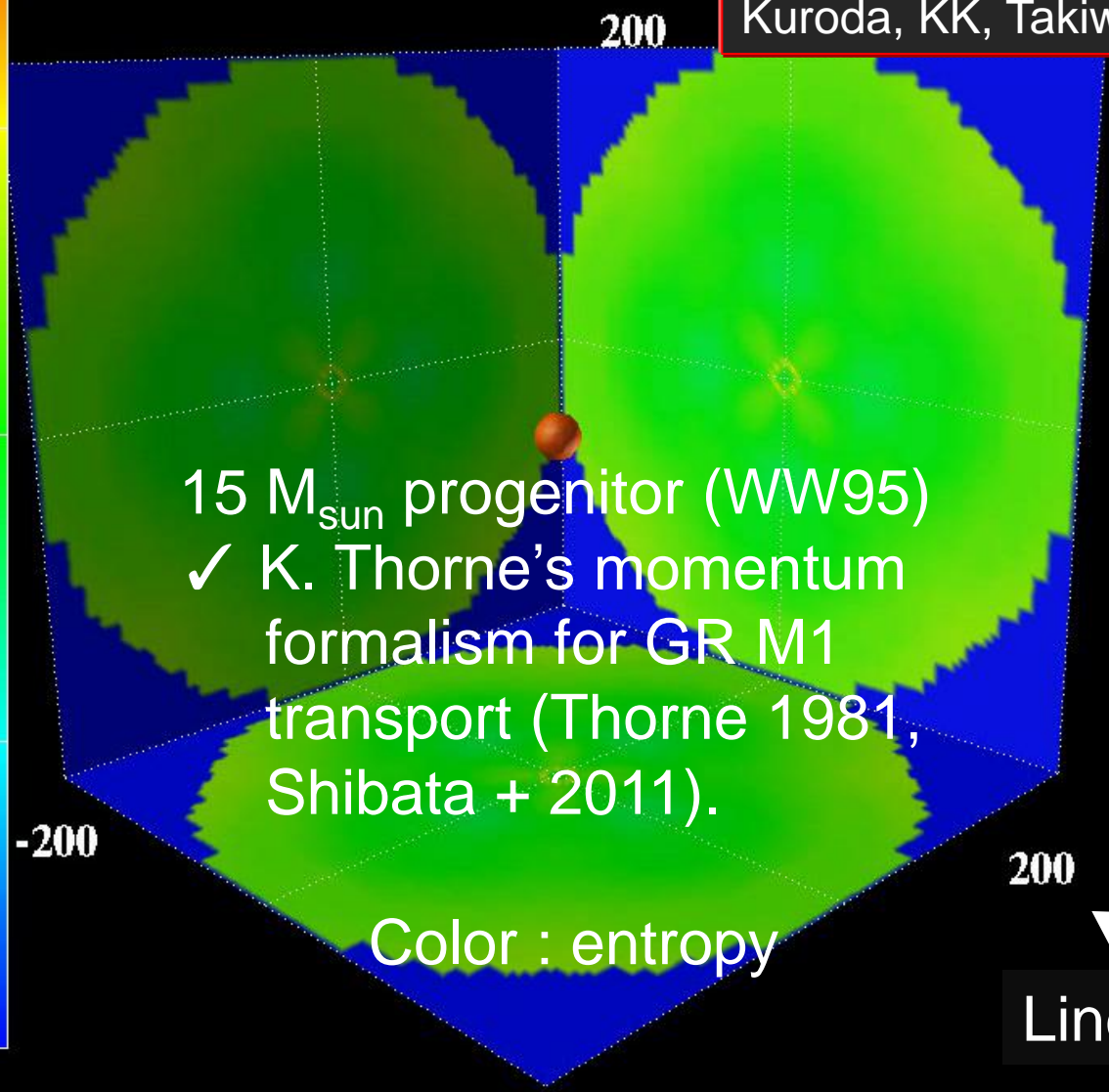


Trans

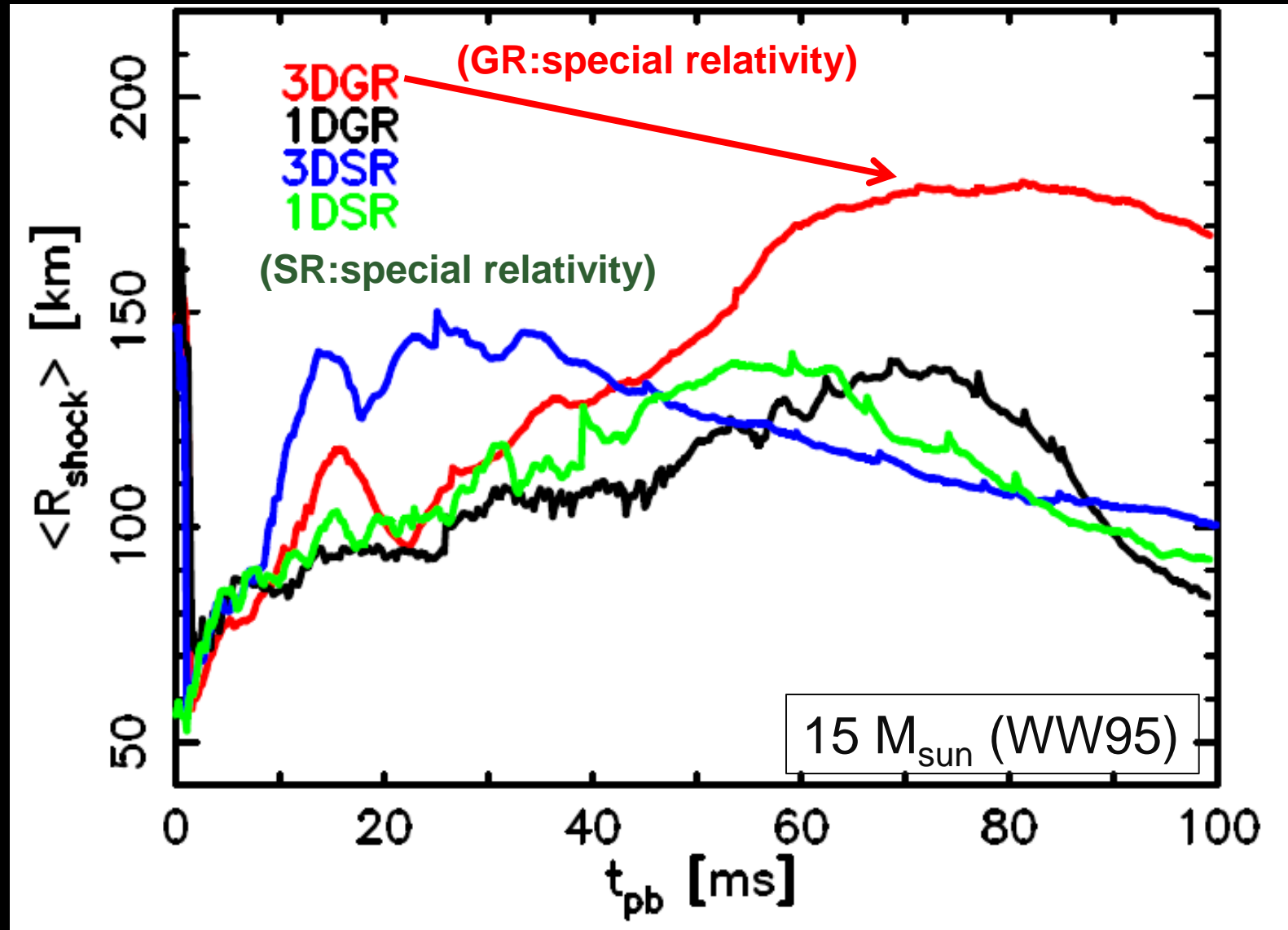
Multi-Energy

Gray

Adia-batic



# Comparison of average shock radii

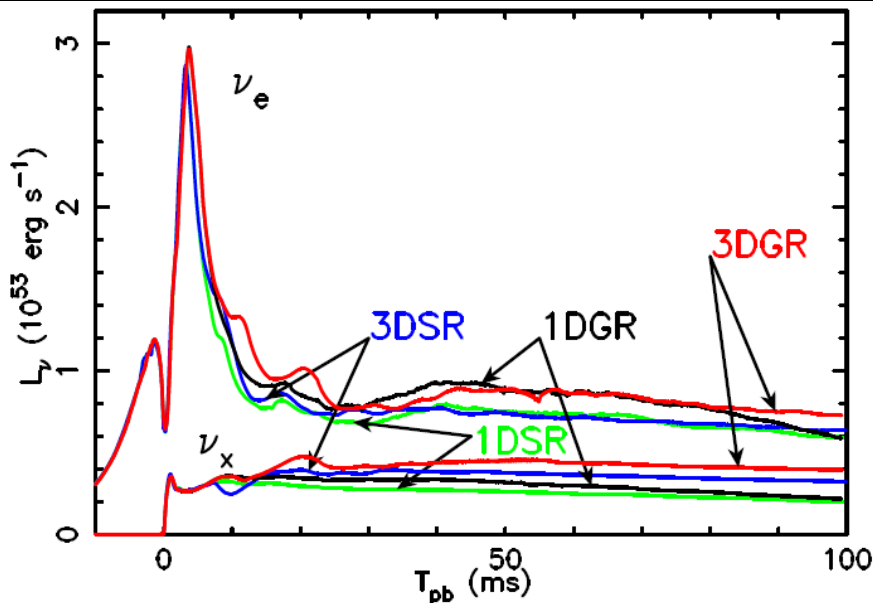


- ✓ Except for our 3D-GR model, the shock has shown a trend of recession.
- ✓ Important : why the shock can reach most further out for 3D-GR ?

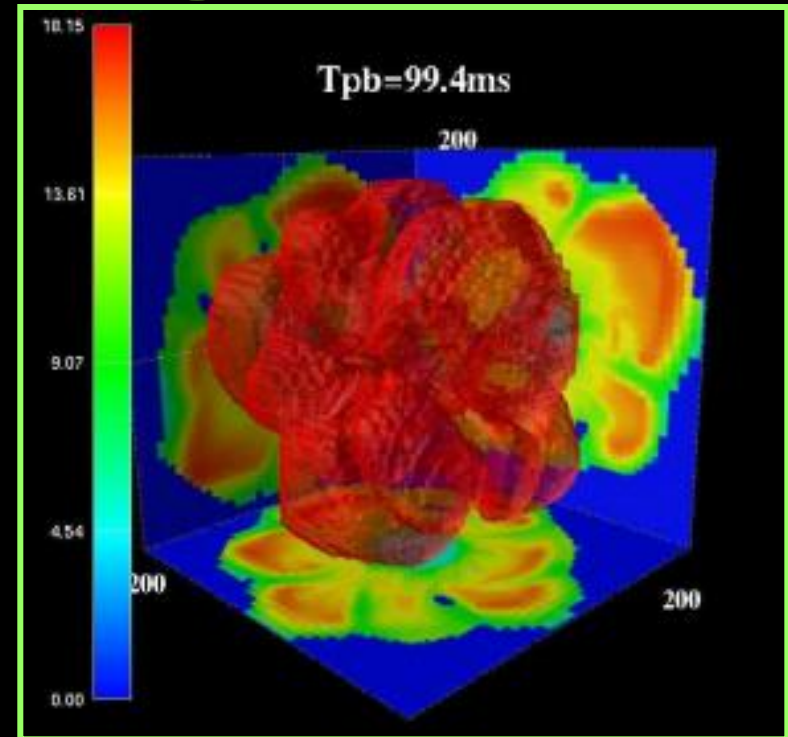
# Advantages in 3D-GR model to go explosions !

Two things : **GR** and **3D**

✓ Deeper potential well :  
core structures smaller  $\Rightarrow$   
making  $\langle E_\nu \rangle$  higher.

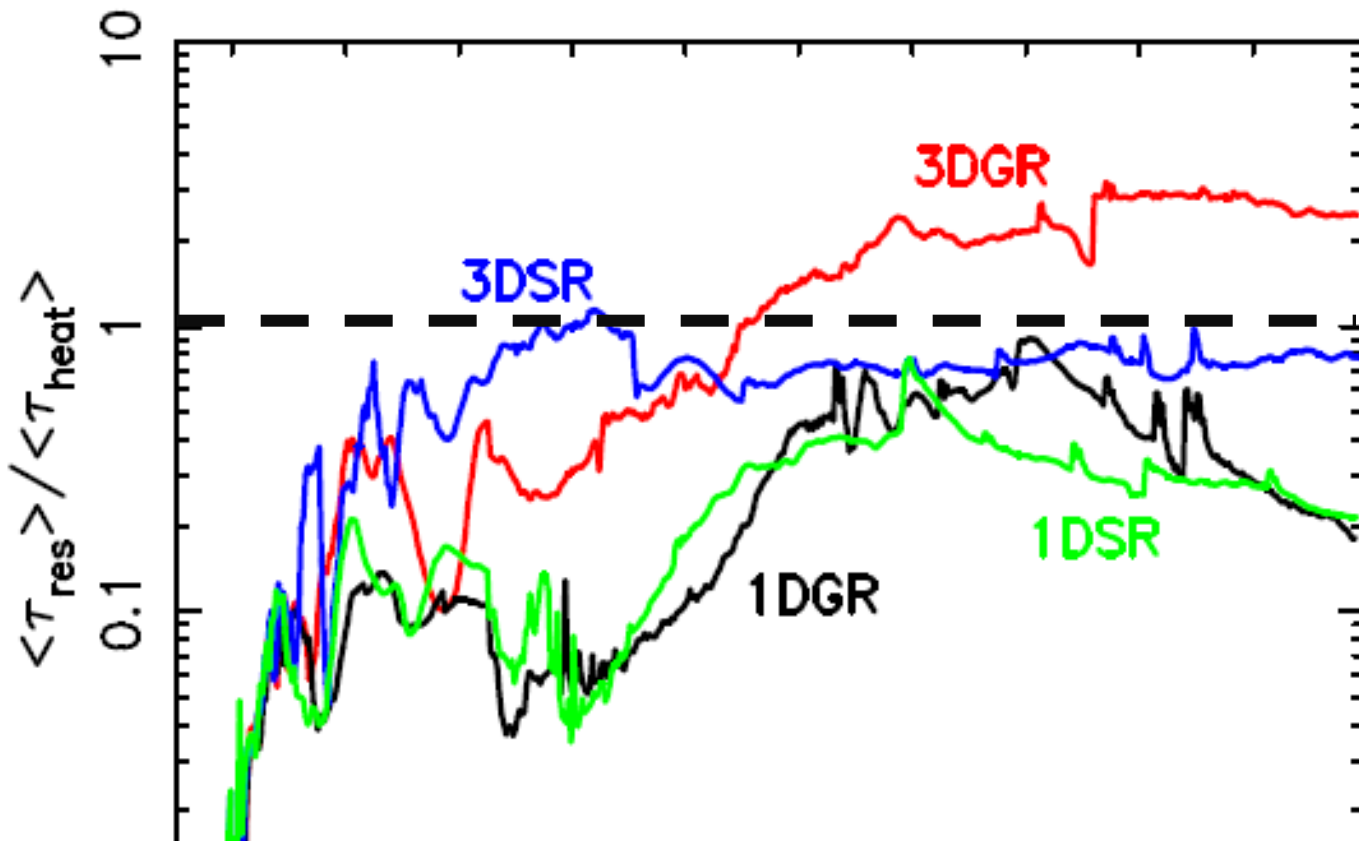


✓ GR can enhance the neutrino  
luminosity up to 40 % comp.to  
the SR counterpart.



Due to non-radial motions,  
the residency timescale :  
longer in 3D than in 1D.  
 $\Rightarrow$  Essential why 3D are  
supportive compared to 1D

# Diagnostic of explosion : residency timescale/heating timescale



- ✓ The combination of 3D and GR  
⇒ the most supportive condition of explosions !
- ✓ In order to extract hydro-data for nucleosynthesis...
- ✓  $1000\text{ms}/(2 \text{ ms per day}) \sim 500 \text{ days} \dots$

# Summary and Outlook

## ☆ On the 3D effects:

we've not obtained a clear-cut answer, hampered by stochastic nature of explosions.

✓ Systematic studies in the first-principle 3D simulations by changing resolutions, perturbations, and so on) should be done !

⇒ **Need peta- or exa-scale supercomputers!**

(see our recent review (accepted to PTEP: Kotake et al.

toward 6D simulations with exact Boltzmann transport in full general relativity !)

## ☆ Our 1<sup>st</sup> generation GR results: the combination of GR and 3D provides the most favorable condition.

✓ Just find the way to hold the **wedding** between spectral neutrino transport and GR hydro-code.

☆ **Significantly further to reach the goal !**

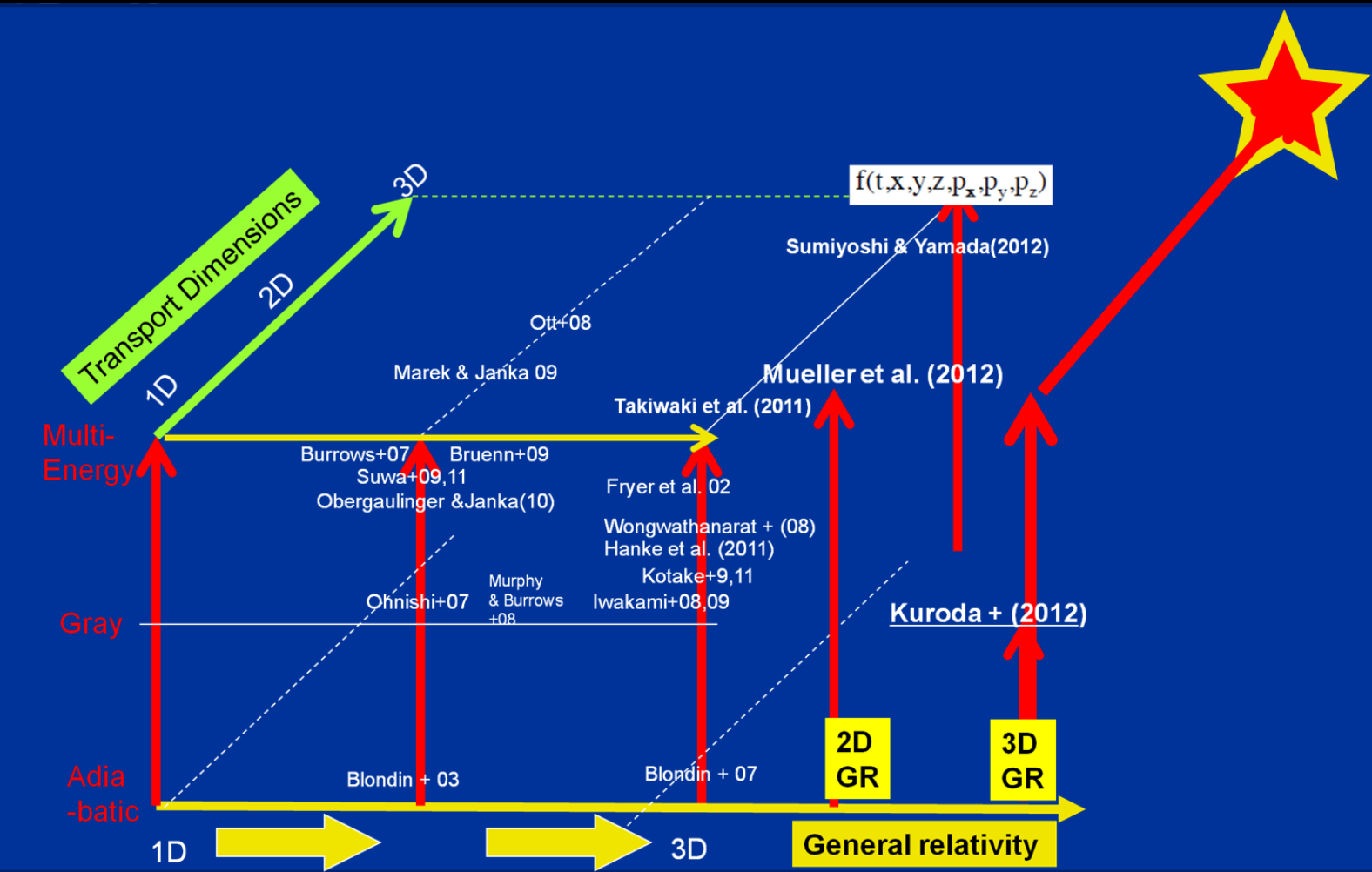
☆ Theoretical prediction of nucleosynthesis, GWs, neutrinos will be all updated.

✓ **More come in the “next” time !**

Thank you very much !

# Summary and Outlook

- ☆ On the we've stochastic
- ✓ System simulation and
- ⇒ Ne (se to)
- ☆ Our 1st GR and
- ✓ Just neut



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Thank you very much !