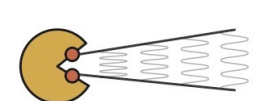




Accessing the coupled-channels dynamics using femtoscopic correlations at LHC

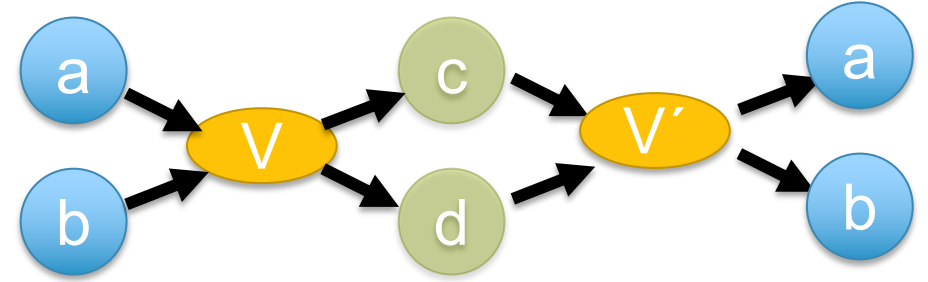
V. Mantovani Sarti (TUM)

THEIA Strong seminar – 08.12.2021

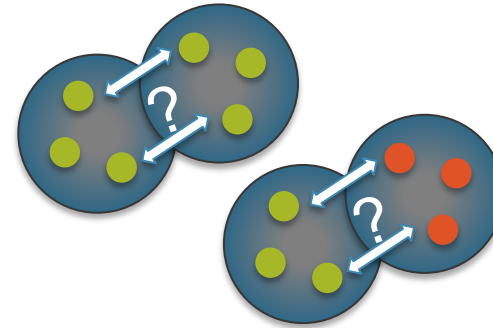
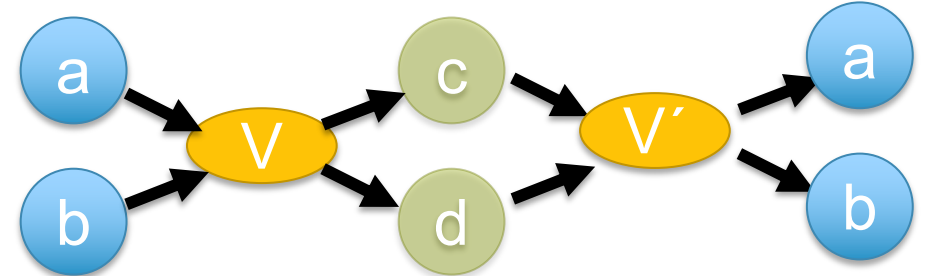


Coupled-channel dynamics in h-h interactions

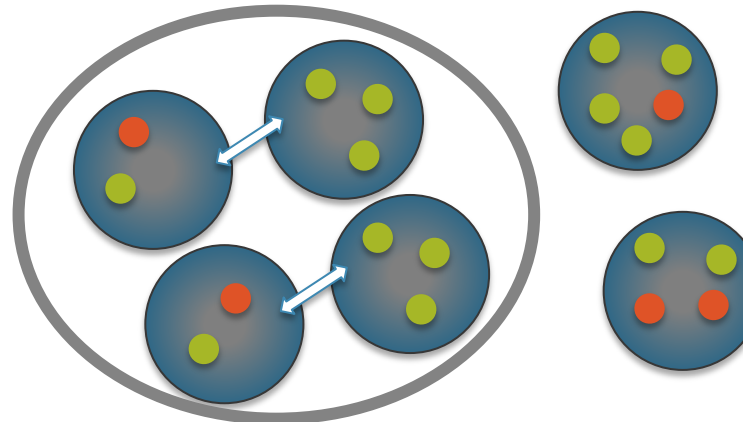
- Coupled-channel dynamics widely present in hadron-hadron strong interactions
 - Close in mass and same quantum numbers (e.g. B,S,Q)
 - On-shell and off-shell processes from one channel to the other



- Coupled-channel dynamics widely present in hadron-hadron strong interactions
 - Close in mass and same quantum numbers (e.g. B,S,Q)
 - On-shell and off-shell processes from one channel to the other
- Constraints on inelastic part crucial for:
 - existence of bound states
 - di-baryon
 - nature of resonances
 - hadron molecules
 - exotic hadrons (pentaquarks,...)

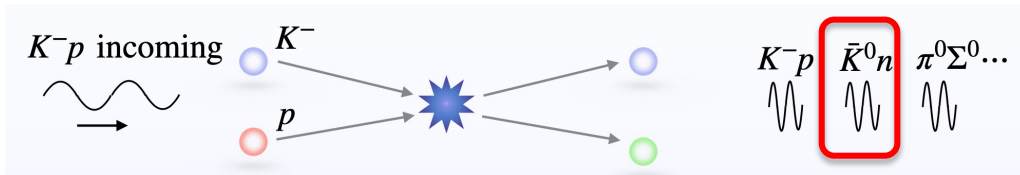


- $N\Omega$, $\Omega\Omega$, $\Lambda\Lambda$, $B\bar{B}$, ...



- $\Lambda(1405)$ in $\bar{K}N$, charmonium states, ...

- Fixed initial state (e.g K^-) and different final states:
 - elastic scattering: $1 \rightarrow 1$
 - inelastic scattering: $1 \rightarrow 2, 3, \dots$



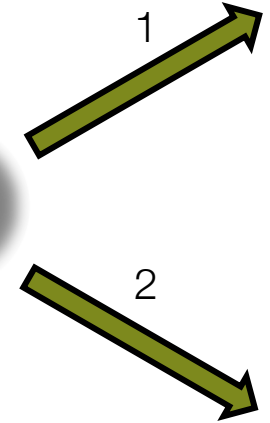
- Measurement of the cross-section in different channels

- Disadvantages:
 - not accessible down to zero momenta
 - large uncertainties
 - limited to few h-h interactions

Initial state

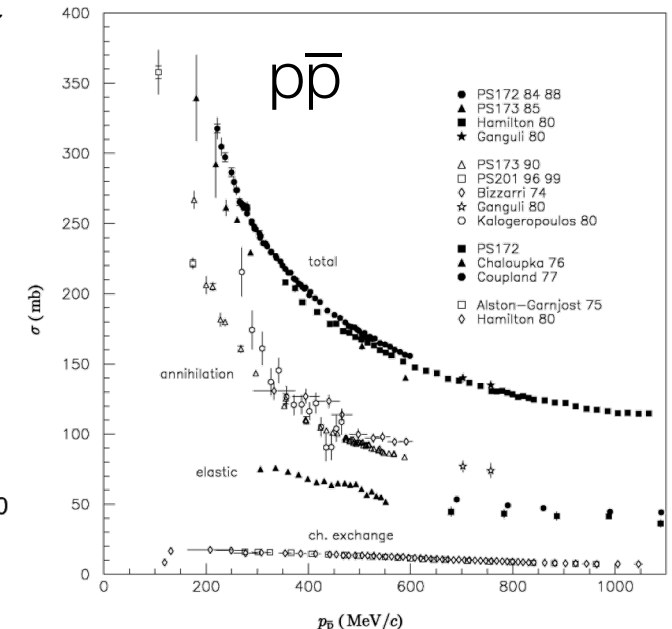
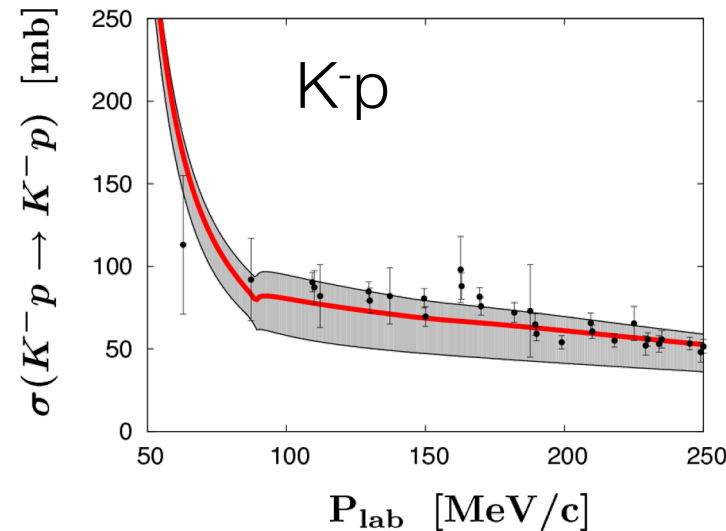


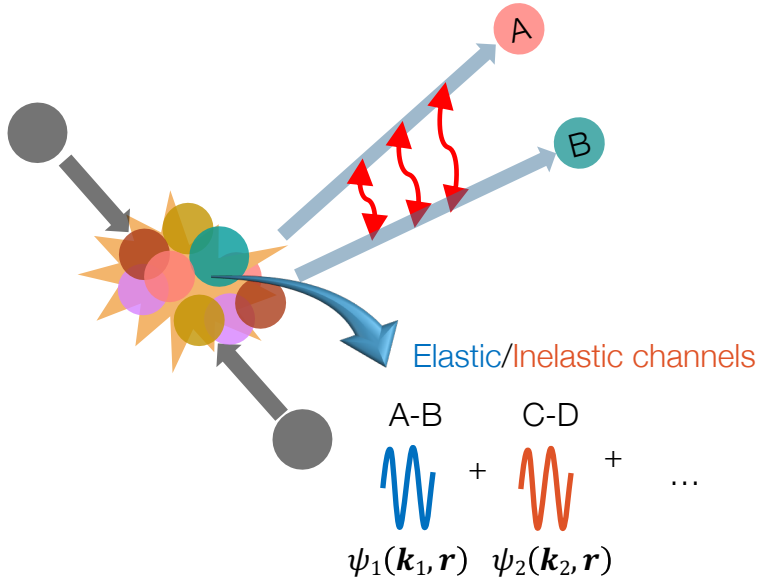
Final state



E.Klempt et al. Phys.Rept. 368 (2002) 119-316

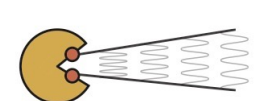
G.S. Abrams et al. Phys.Rev. 139 (1965) B454-B457

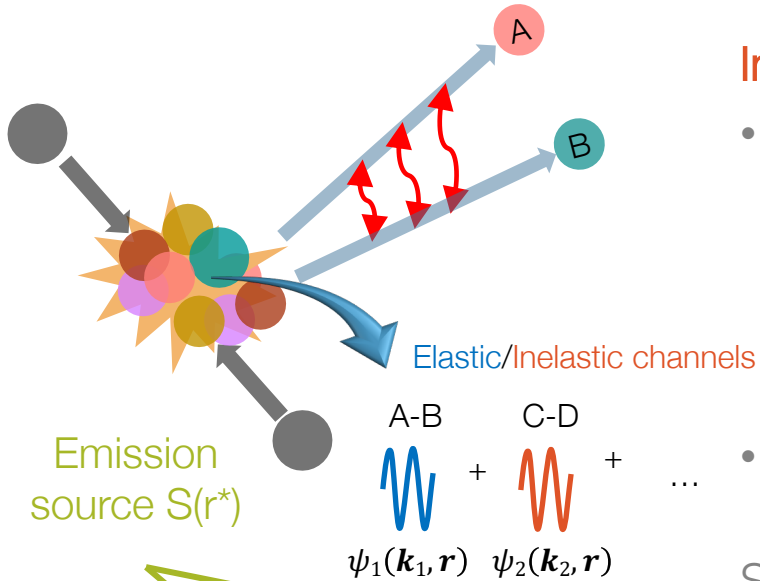




- Conversion weights w_j
 - produced pairs in j channel as initial states
→ yields + kinematics
 - thermal models and transport models

$$C_{A-B}(k^*) = \underbrace{\int S(r) |\psi_{1 \rightarrow 1}(k^*, r)|^2 d^3r}_{\text{elastic } A-B \rightarrow A-B} + \sum_{j \neq 1} w_j^{\text{prod}} \underbrace{\int S_j(r) |\psi_{j \rightarrow 1}(k_j^*, r)|^2 d^3r}_{\text{inelastic } C-D \rightarrow A-B, \dots} = \mathcal{N}(k^*) \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

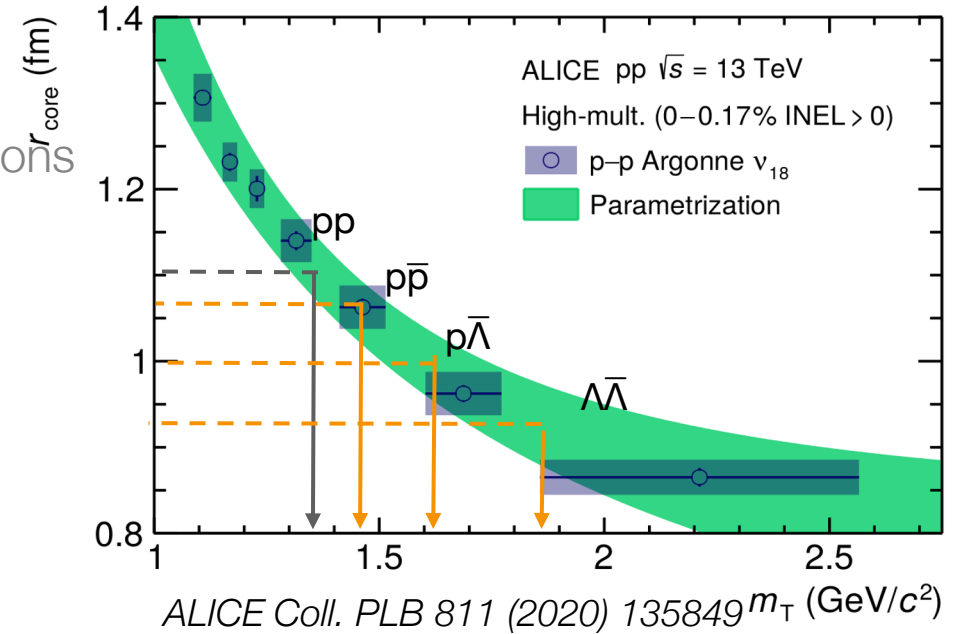




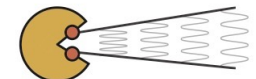
In small colliding systems:

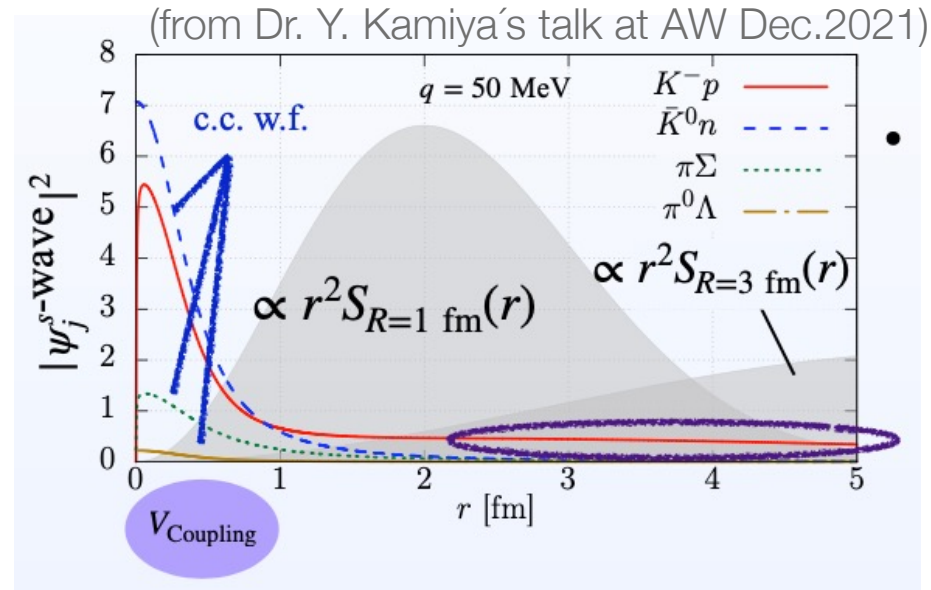
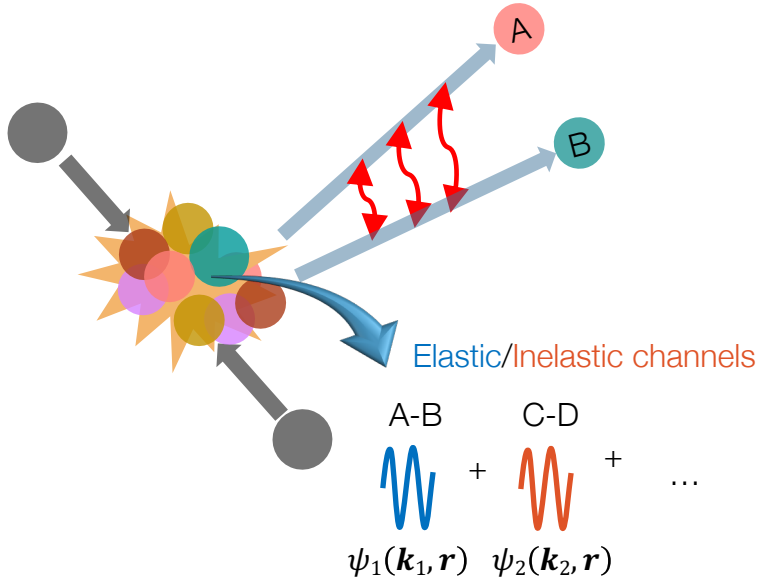
- Gaussian r_{core} + resonance source model anchored to known interactions
 - Universal emitting source for particles
- Effective Gaussian with $r_G \sim 1\text{-}2$ fm

See more in Dimitar's talk



$$C_{A-B}(k^*) = \underbrace{\int S(r) |\psi_{1 \rightarrow 1}(k^*, r)|^2 d^3r}_{\text{elastic } A-B \rightarrow A-B} + \sum_{j \neq 1} w_j^{\text{prod}} \underbrace{\int S_j(r) |\psi_{j \rightarrow 1}(k_j^*, r)|^2 d^3r}_{\text{inelastic } C-D \rightarrow A-B, \dots} = \mathcal{N}(k^*) \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

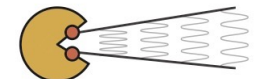


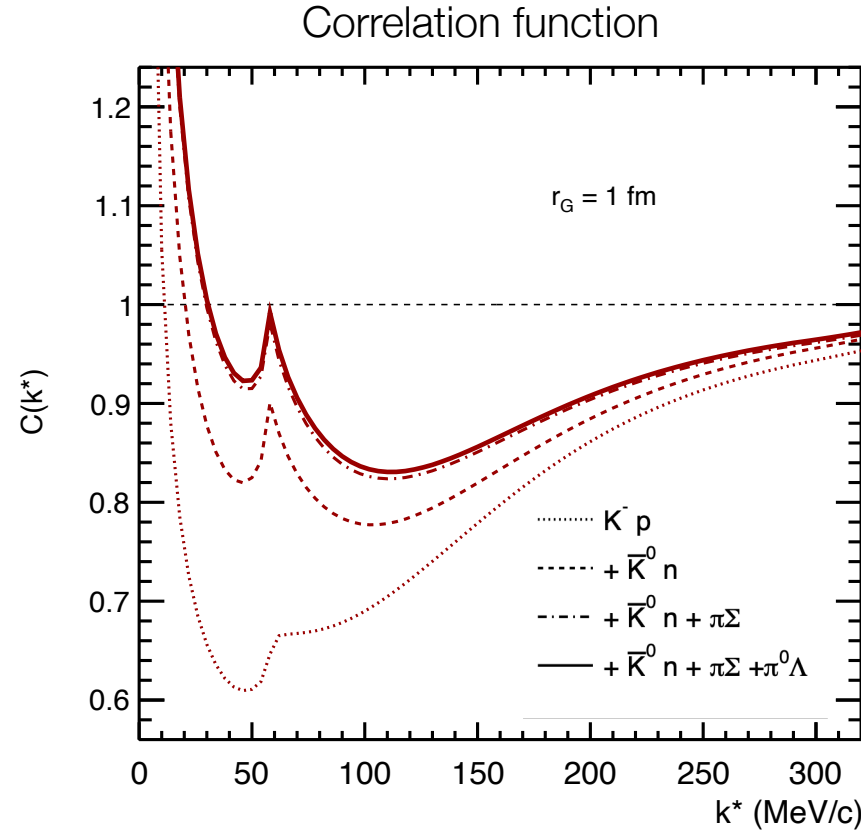
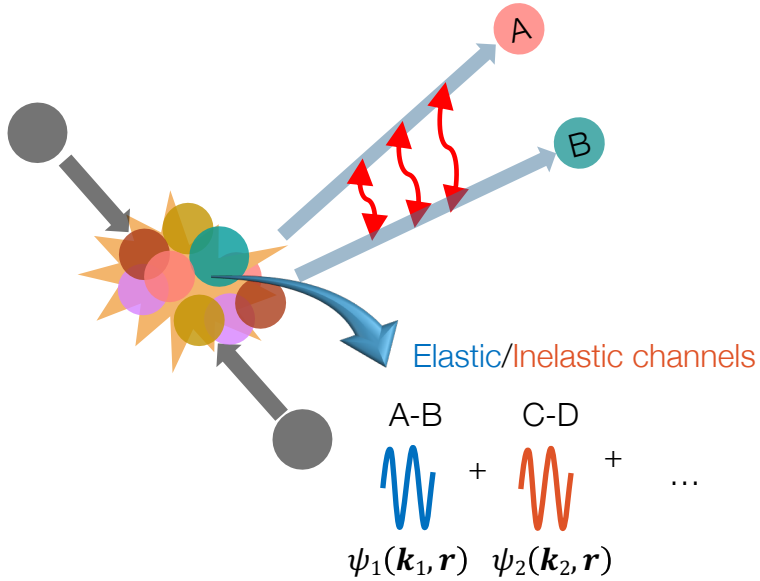


- Coupled-channel wfs playing a role at low distances

Elastic/Inelastic wave functions

$$C_{A-B}(k^*) = \underbrace{\int S(r) |\psi_{1 \rightarrow 1}(k^*, r)|^2 d^3r}_{\text{elastic } A-B \rightarrow A-B} + \sum_{j \neq 1} w_j^{\text{prod}} \underbrace{\int S_j(r) |\psi_{j \rightarrow 1}(k_j^*, r)|^2 d^3r}_{\text{inelastic } C-D \rightarrow A-B, \dots} = \mathcal{N}(k^*) \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$



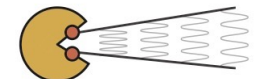


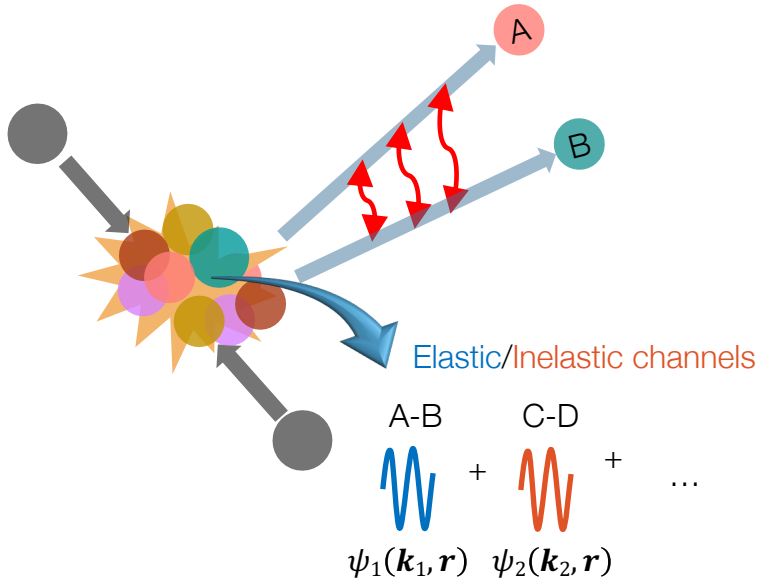
$$C_{A-B}(k^*) = \underbrace{\int S(r) |\psi_{1 \rightarrow 1}(k^*, r)|^2 d^3r}_{\text{elastic}} + \sum_{j \neq 1} \underbrace{w_j^{\text{prod}} \int S_j(r) |\psi_{j \rightarrow 1}(k_j^*, r)|^2 d^3r}_{\text{inelastic}} = \mathcal{N}(k^*) \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

elastic
A-B $\rightarrow$ A-B

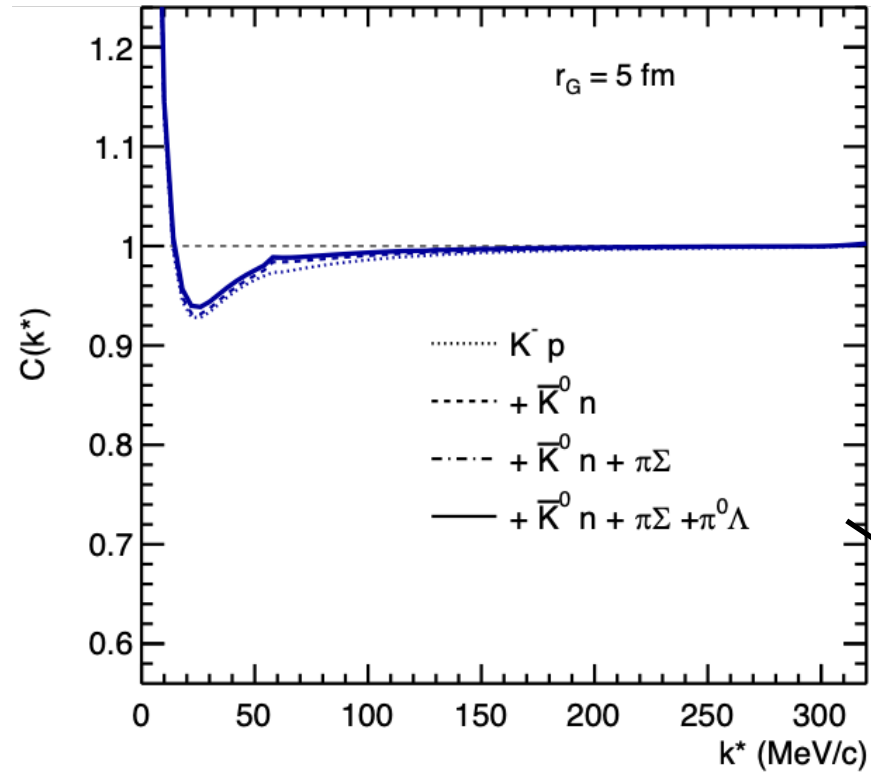
inelastic
C-D $\rightarrow$ A-B, ...

J. Haidenbauer Nucl.Phys.A 981 (2019)
Y. Kamiya et al. Phys.Rev.Lett. 124 (2020)
V.M.S., L. Fabbietti, O. Vazquez-Doce 2012.09806





Correlation function



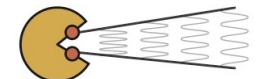
- Inelastic contributions negligible as the source size increases

$$C_{A-B}(k^*) = \underbrace{\int S(r) |\psi_{1 \rightarrow 1}(k^*, r)|^2 d^3r}_{\text{elastic}} + \sum_{j \neq 1} w_j^{\text{prod}} \underbrace{\int S_j(r) |\psi_{j \rightarrow 1}(k_j^*, r)|^2 d^3r}_{\text{inelastic}} = \mathcal{N}(k^*) \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

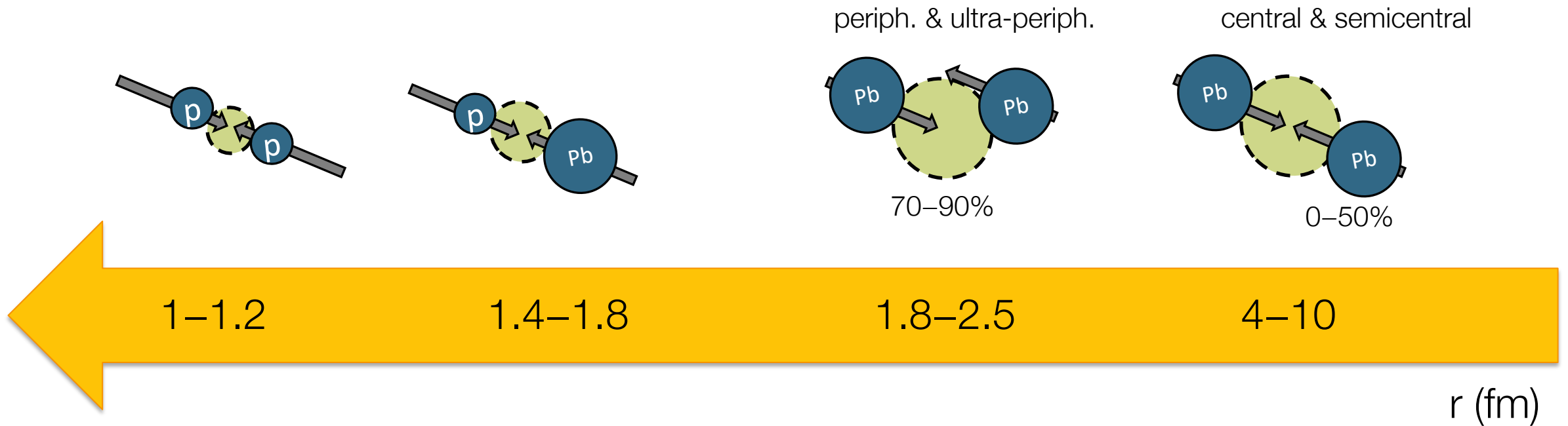
elastic
A-B $\rightarrow$ A-B

inelastic
C-D $\rightarrow$ A-B, ...

J. Haidenbauer Nucl.Phys.A 981 (2019)
Y. Kamiya et al. Phys.Rev.Lett. 124 (2020)
V.M.S., L. Fabbietti, O. Vazquez-Doce 2012.09806

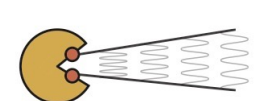


- At ALICE by changing the colliding system we can probe distances ranging from 1 fm up to 10 fm

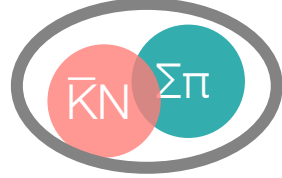


K^- -p and K^+ -p in pp 5,7,13 TeV, p-Pb and Pb-Pb 70–90% 5.02 TeV
 p - $\bar{p}$, p - $\bar{\Lambda}$ and Λ - $\bar{\Lambda}$ in pp HM 13 TeV and Pb-Pb 5.02 TeV

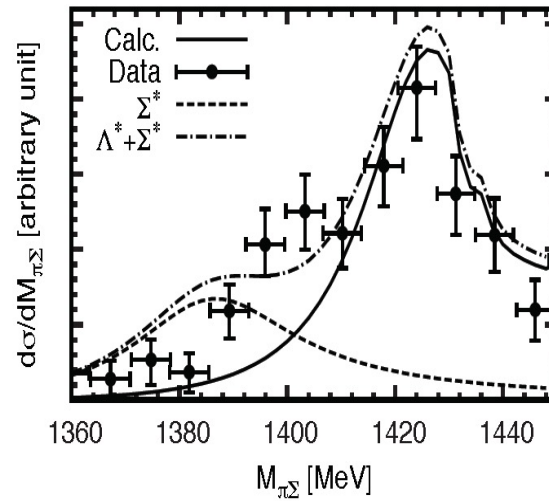
K⁻-p and K⁺-p femtoscopy



$\Lambda(1405)$ molecular state



$\Lambda(1405) \rightarrow \Sigma \pi$

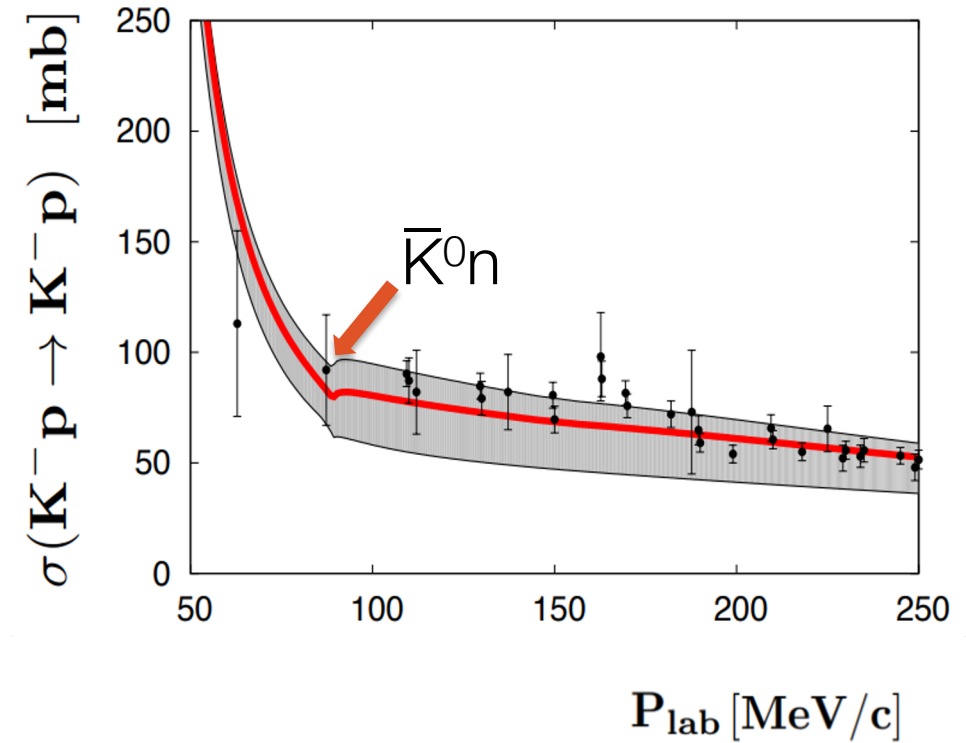


Kaonic hydrogen

SIDDHARTA Coll. PLB 704 (2011)

Scattering Experiments

Ikeda et al. Nucl.Phys.A 881 (2012)



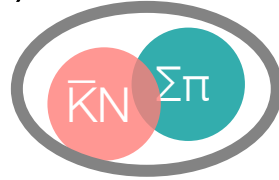
$\Sigma \pi$

$\bar{K} N$

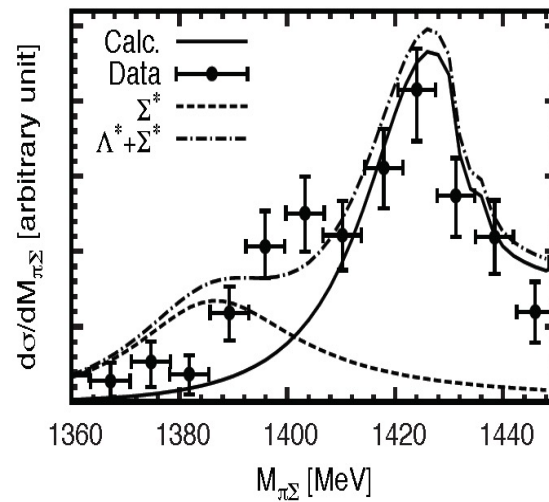
27 MeV

Energy

$\Lambda(1405)$ molecular state

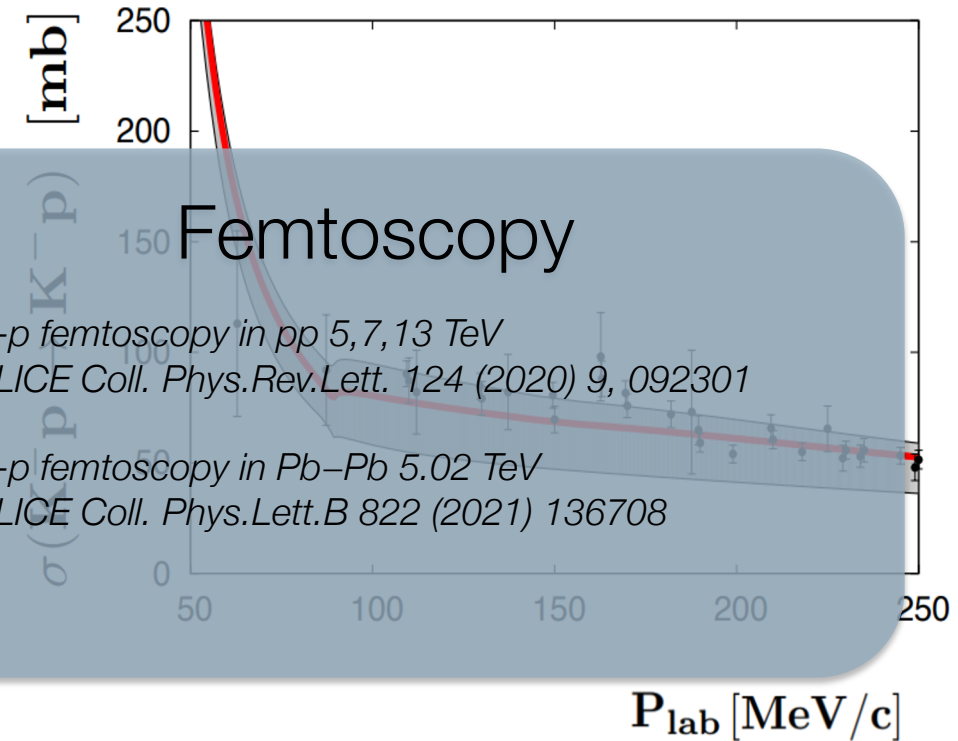


$\Lambda(1405) \rightarrow \Sigma\pi$



Scattering Experiments

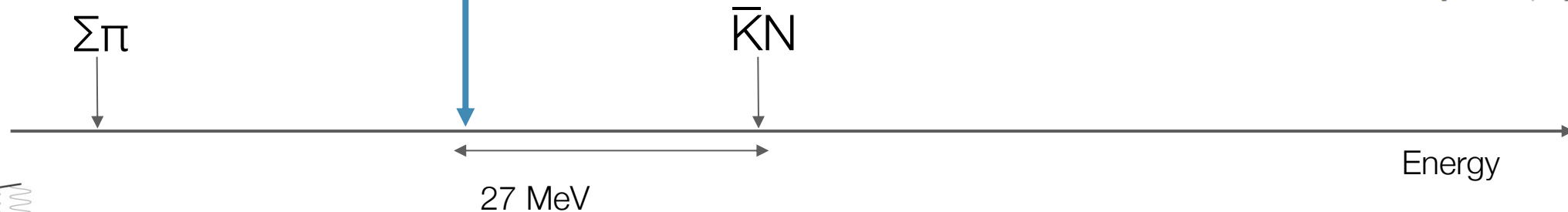
Ikeda et al. Nucl.Phys.A 881 (2012)



Femtoscopy

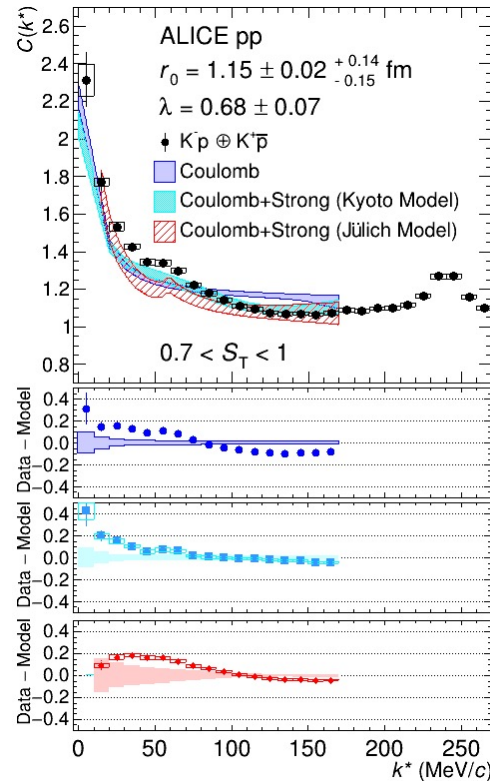
*K-p femtoscopy in pp 5, 7, 13 TeV
ALICE Coll. Phys.Rev.Lett. 124 (2020) 9, 092301*

*K-p femtoscopy in Pb-Pb 5.02 TeV
ALICE Coll. Phys.Lett.B 822 (2021) 136708*

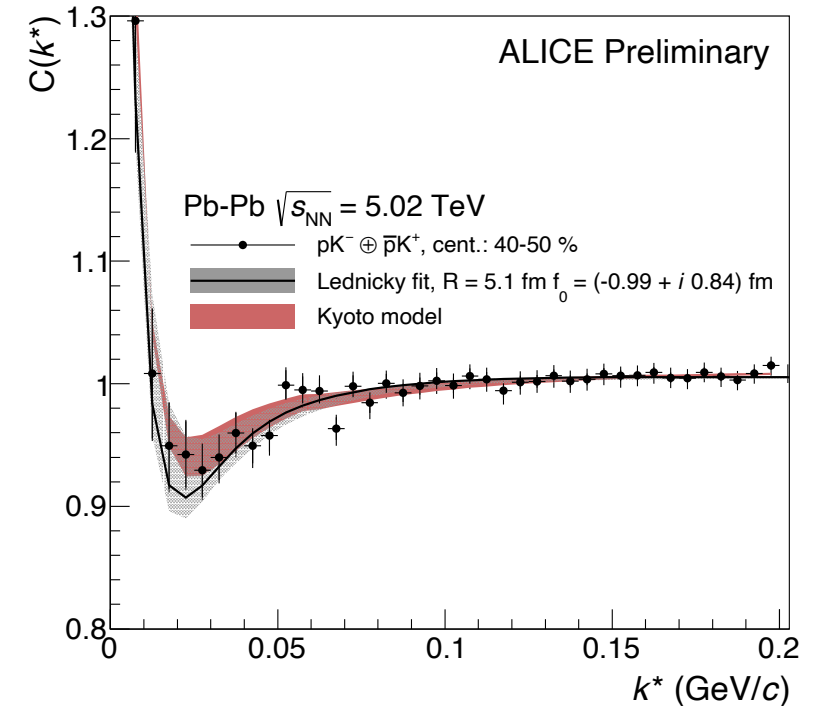


$$C(k^*) = \int S(r) |\psi_{1 \rightarrow 1}(k^*, r)|^2 d^3r + \sum_{j=\Sigma\pi, \bar{K}^0n} w_j^{\text{prod}} \int S_j(r) |\psi_{j \rightarrow 1}(k_j^*, r)|^2 d^3r$$

χ EFT Kyoto model:
 Ikeda et al. NPA 881 (2012),
 PLB706 (2011)
 Kamiya et al. PRL 124 (2020)
 Miyahara et al. PRC95 (2017)

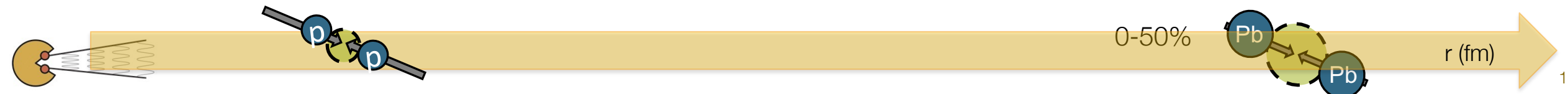


ALICE Coll. Phys.Rev.Lett. 124 (2020) 9, 092301

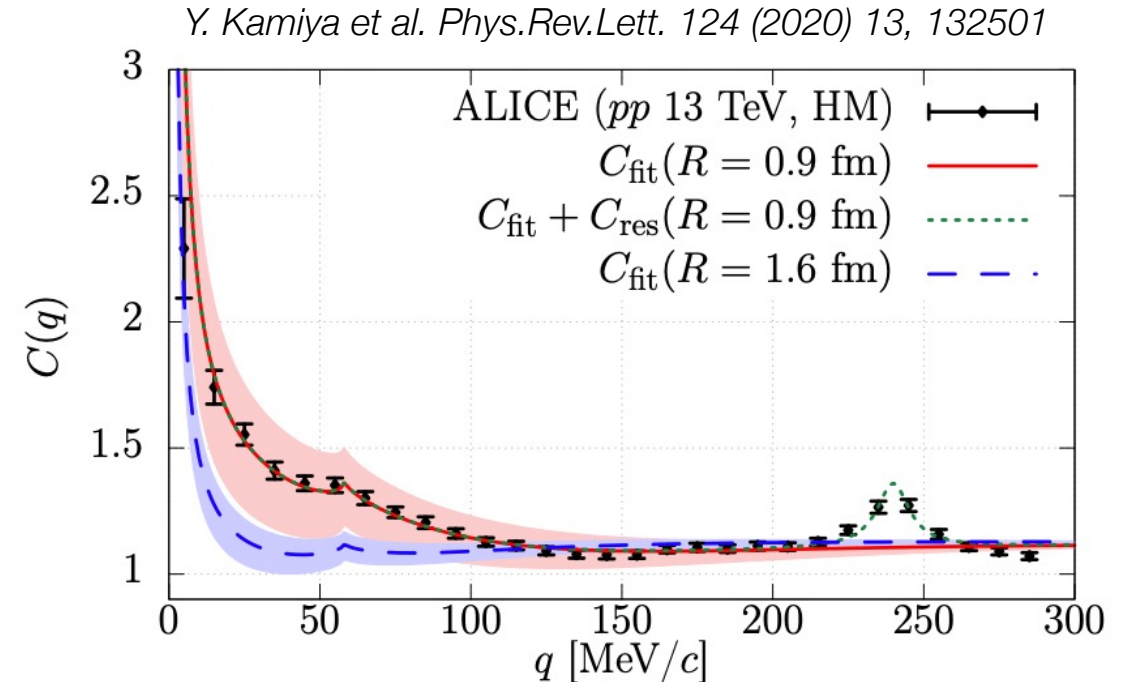


ALI-PREL-354647

ALICE Coll. Phys.Lett.B 822 (2021) 136708



- Modification of the conversion weights leads to a better agreement with the data
 - see *Phys.Rev.Lett.* 124 (2020) 13, 132501
- Conversion weights extracted from kinematics and thermal model predictions in pp, p-Pb and Pb-Pb
 - still agreement data/model?
 - provide constraints for the $\bar{K}^0$ n coupling
- Perform the measurements in peripheral p-Pb and Pb-Pb collisions → access intermediate source sizes



Paper in preparation

Dr. R. Lea

Dr. Y. Kamiya

Prof. Fabbietti

Prof A. Ohnishi

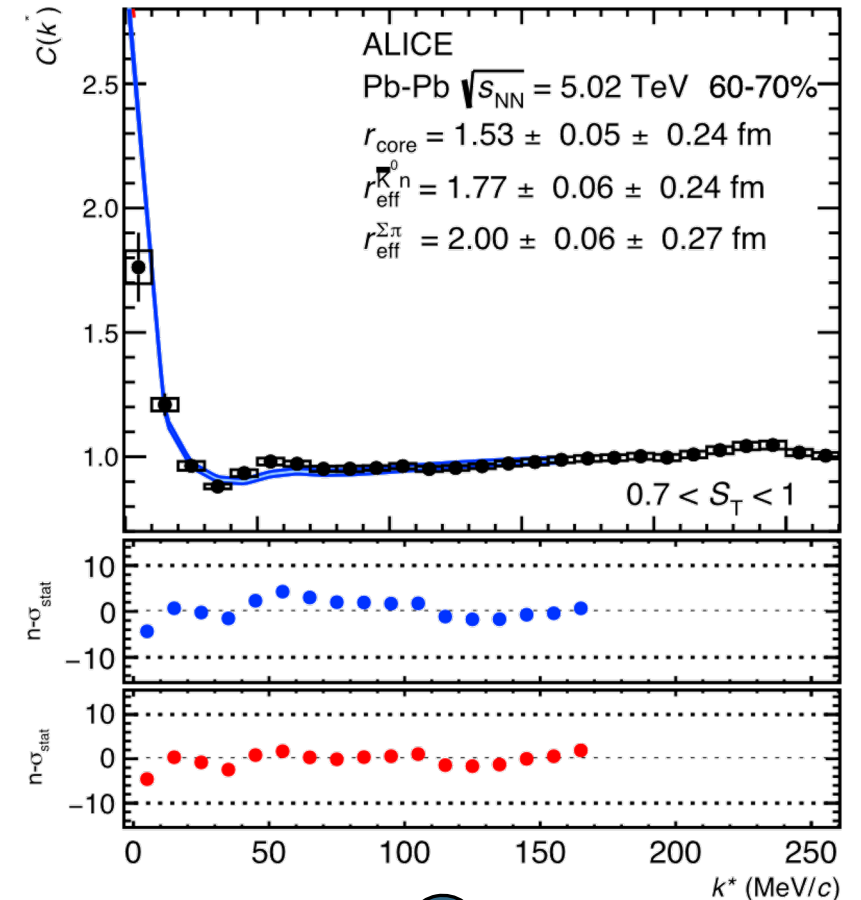
Prof. T.Hyodo

Maximilian Korweiser

Fixed from statistical model and Monte Carlo simulations with Blast-wave fits to data

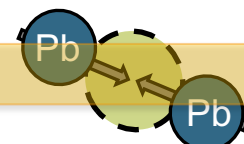
$$C(k^*) = \int S(r) |\psi_{1 \rightarrow 1}(k^*, r)|^2 d^3r + \sum_{j=\Sigma\pi, \bar{K}^0n} w_j^{\text{prod}} \int S_j(r) |\psi_{j \rightarrow 1}(k_j^*, r)|^2 d^3r$$

χEFT Kyoto model:
 Ikeda et al. NPA 881 (2012),
 PLB706 (2011)
 Kamiya et al. PRL 124 (2020)
 Miyahara et al. PRC95 (2017)



Paper in preparation

60-70%

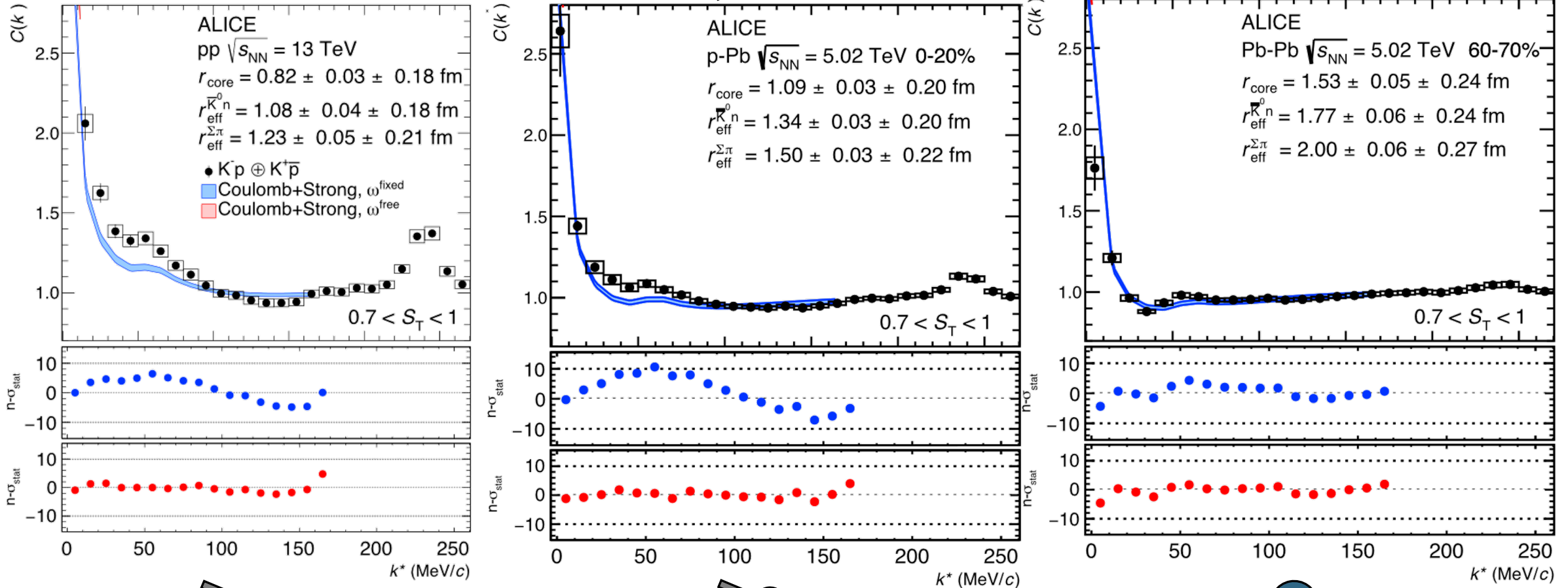


r (fm)

Fixed from statistical model and Monte Carlo simulations with Blast-wave fits to data

$$C(k^*) = \int S(r) |\psi_{1 \rightarrow 1}(k^*, r)|^2 d^3r + \sum_{j=\Sigma\pi, \bar{K}^0n} w_j^{\text{prod}} \int S_j(r) |\psi_{j \rightarrow 1}(k_j^*, r)|^2 d^3r$$

χ EFT Kyoto model:
Ikeda et al. NPA 881 (2012),
PLB706 (2011)
Kamiya et al. PRL 124 (2020)
Mihayara et al. PRC95 (2017)



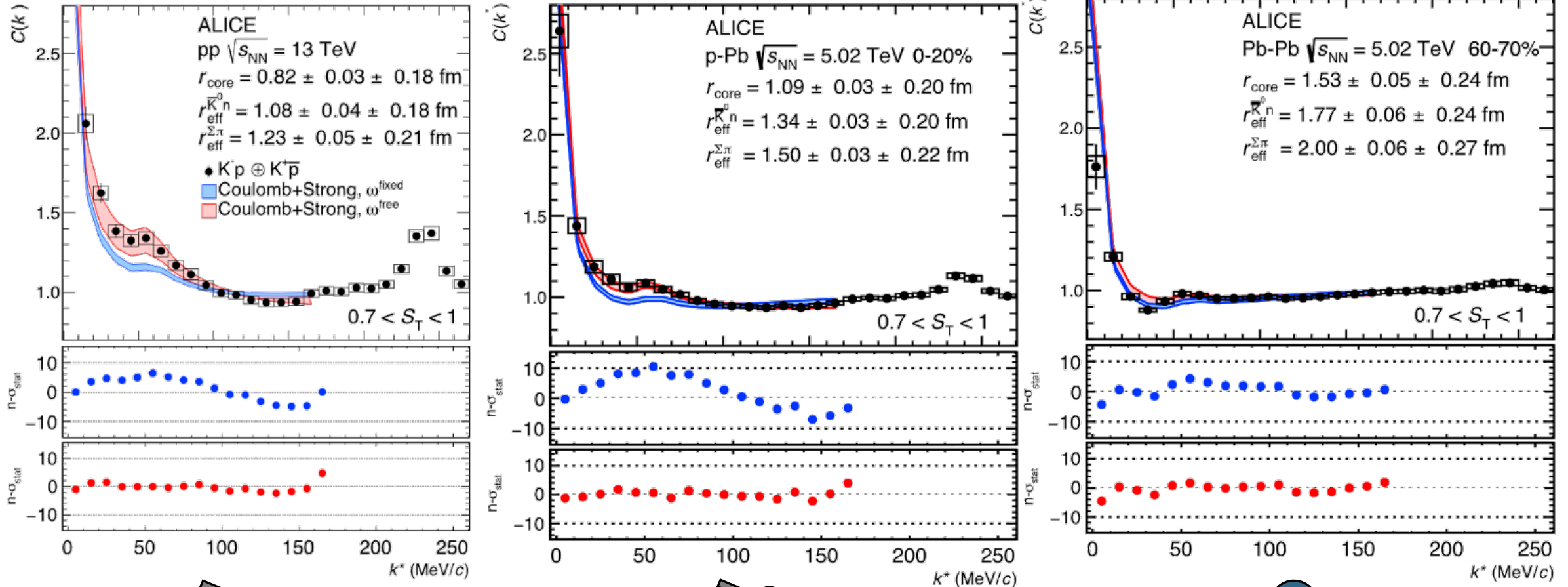
Paper in preparation



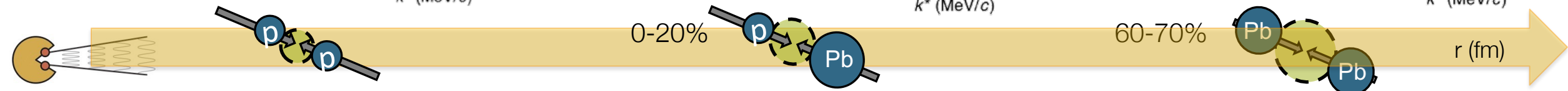
Fixed from statistical model and Monte Carlo simulations with Blast-wave fits to data

$$C(k^*) = \int S(r) |\psi_{1 \rightarrow 1}(k^*, r)|^2 d^3r + \sum_{j=\Sigma\pi, \bar{K}^0n} w_j^S \cdot w_j^{\text{prod}} \int S_j(r) |\psi_{j \rightarrow 1}(k_j^*, r)|^2 d^3r$$

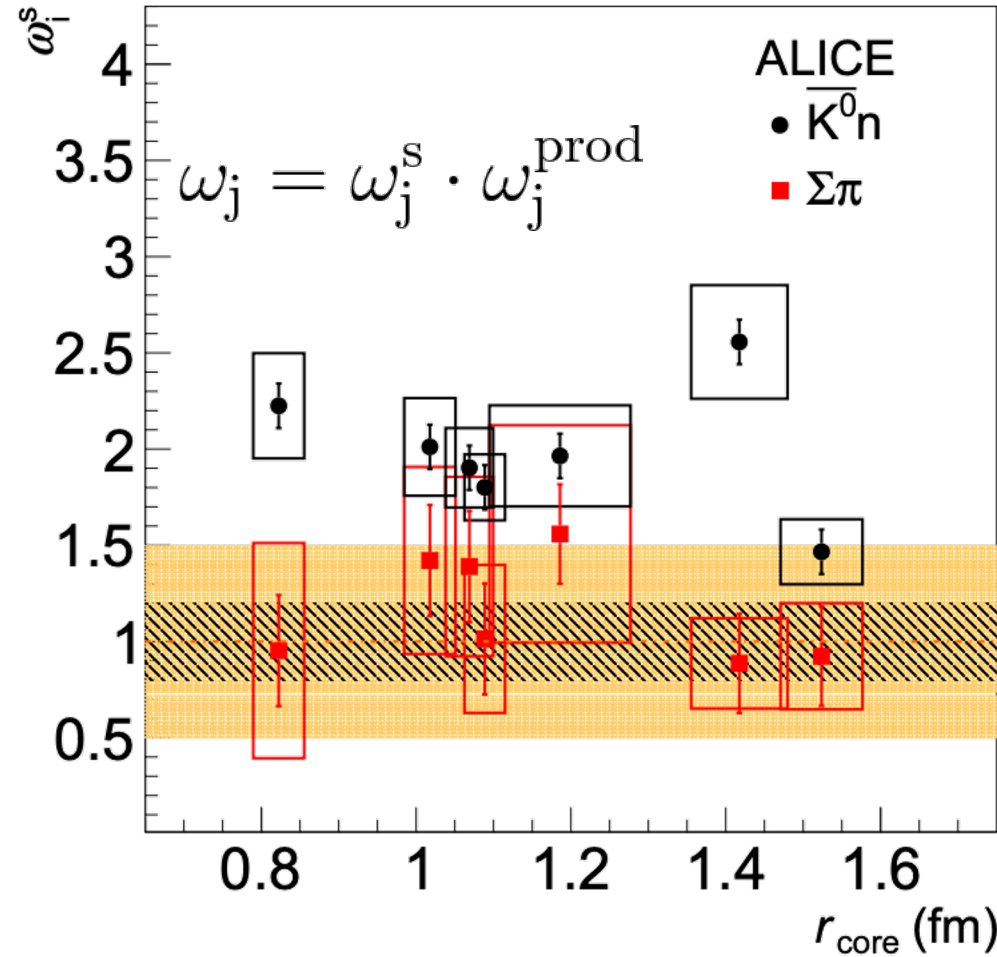
χEFT Kyoto model:
Ikeda et al. NPA 881 (2012),
PLB706 (2011)
Kamiya et al. PRL 124 (2020)
Mihayara et al. PRC95 (2017)



Paper in preparation



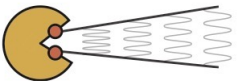
Paper in preparation



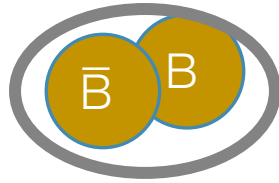
- deviation from unity for $\bar{K}^0 n$
- $K^-p - \bar{K}^0 n$ too weak in chiral potentials
- $\Sigma\pi$ consistent with unity



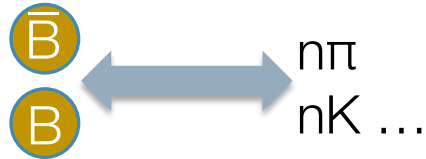
Baryon-antibaryon femtoscopy



Predictions for Baryonia??



?



Annihilation dynamics
 $n\pi, nK, \pi K, \dots$

antiproton atoms

$p-\bar{p}$

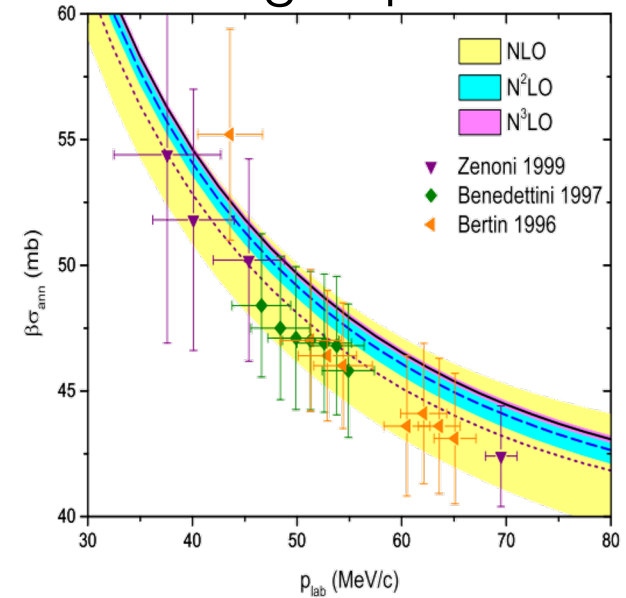
$p-\bar{\Lambda}$

$\Lambda-\bar{\Lambda}$

177 MeV

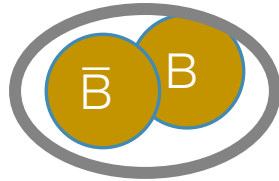
Energy

Scattering Experiments

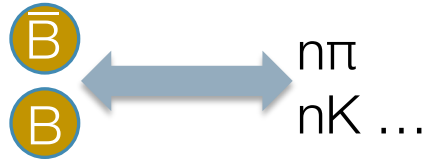


E. Klempt et al. Phys. Rept. 413 (2005)
E. Klempt et al. Phys. Rept. 368 (2002)
D. Zhou and R.G. E. Timmermans PRC86 (2012)
J. Haidenbauer et al. JHEP 1707 (2017)

Predictions for Baryonia??

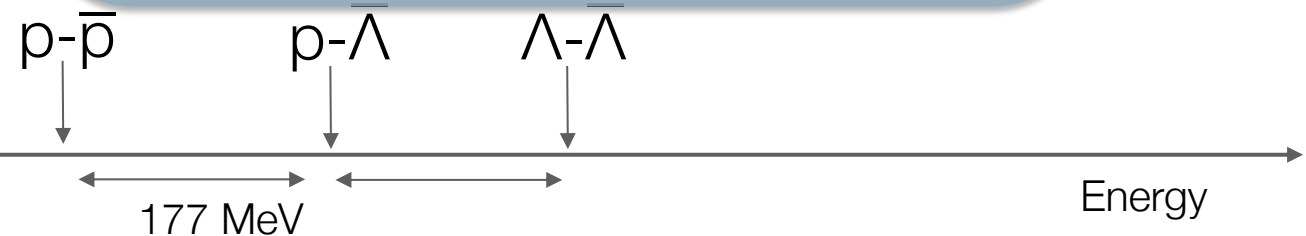
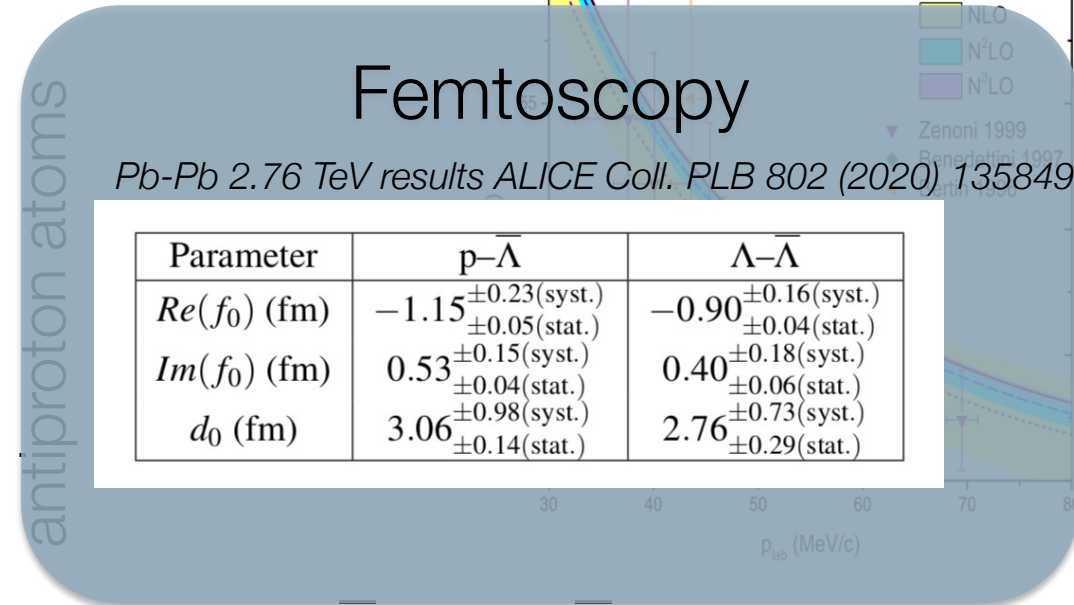


?



Annihilation dynamics
 $n\pi, nK, \pi K, \dots$

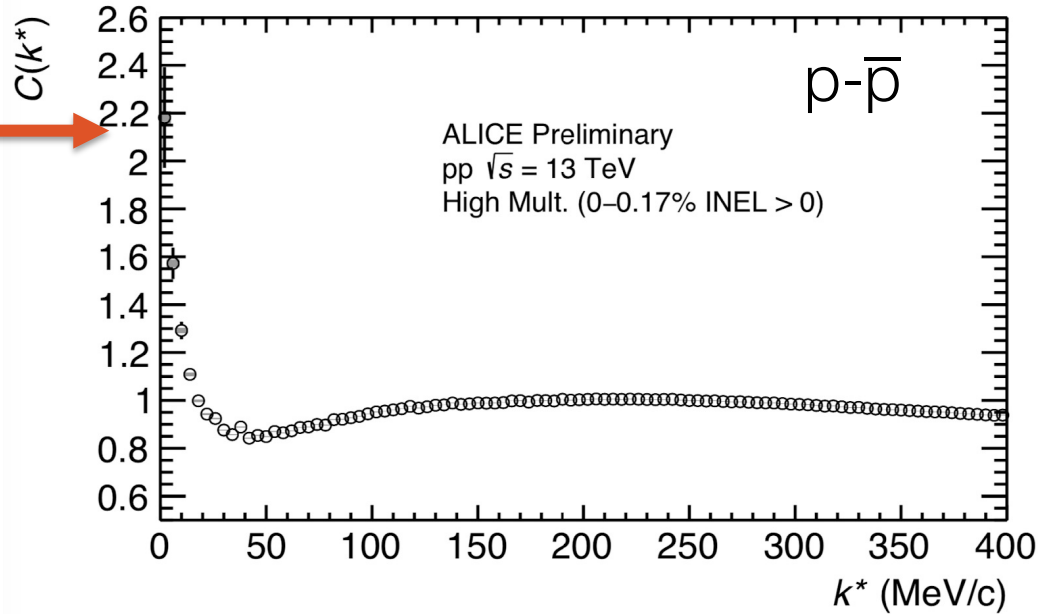
Scattering Experiments



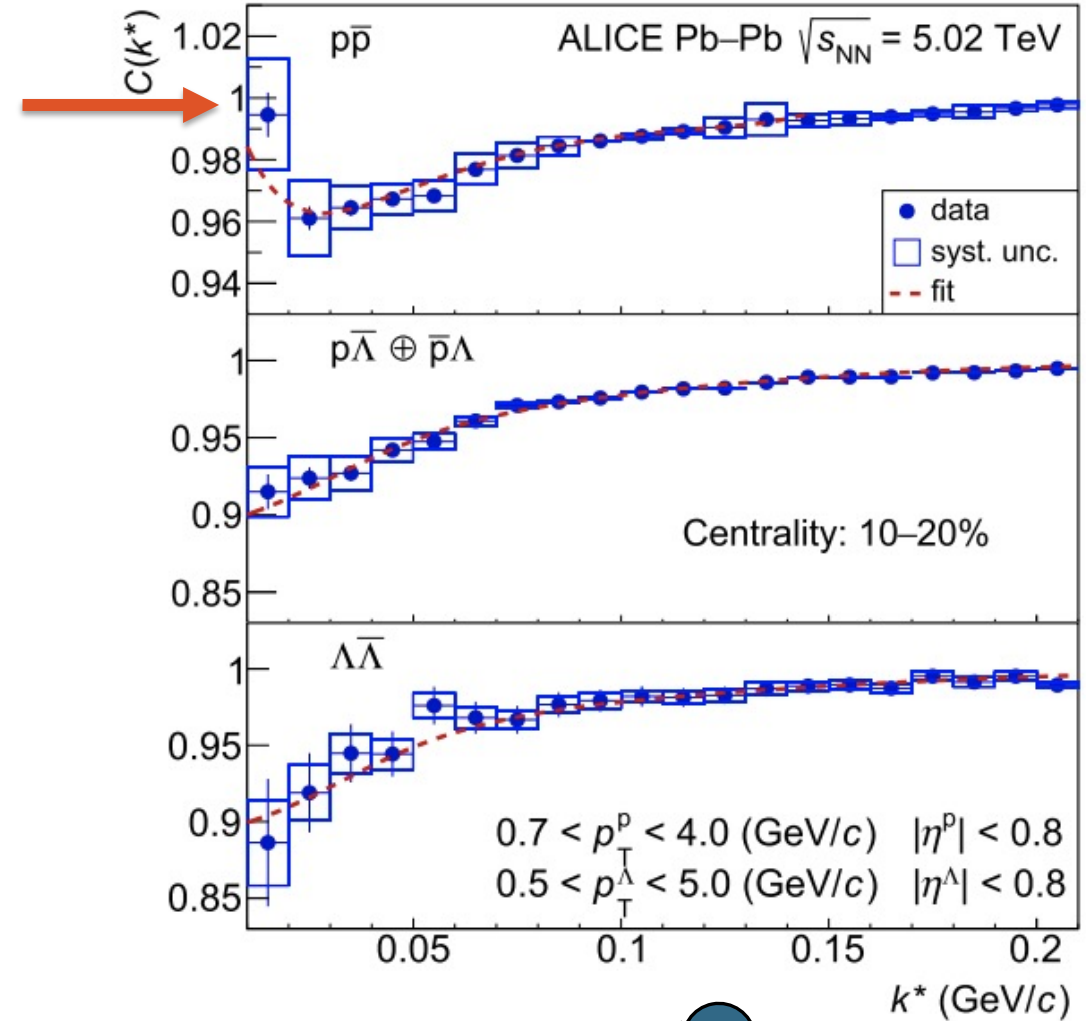
E. Klempt et al. Phys. Rept. 413 (2005)
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D. Zhou and R.G. E. Timmermans PRC86 (2012)
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ALICE Coll. arXiv: 2105.05190

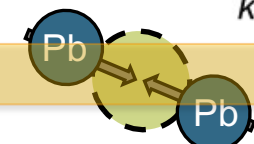
ALICE Coll. PLB 802 (2020) 135849



- Increase at low k^*
 - Coulomb only?
 - feeding from annihilation channels?

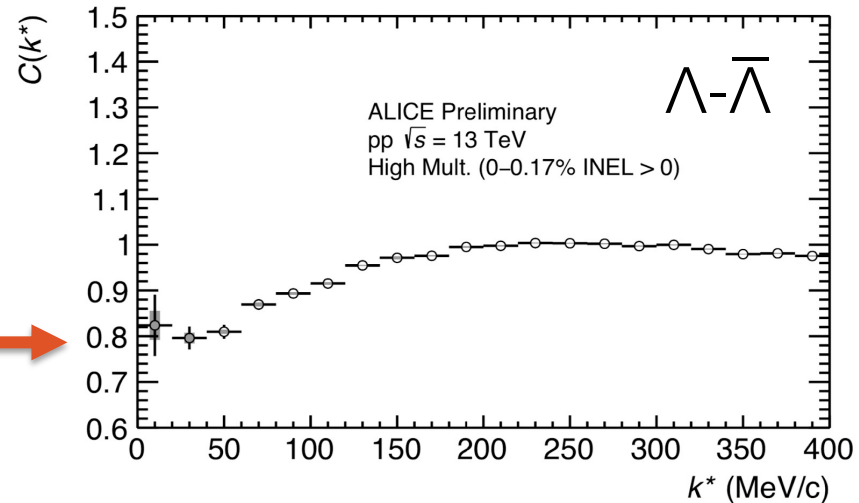
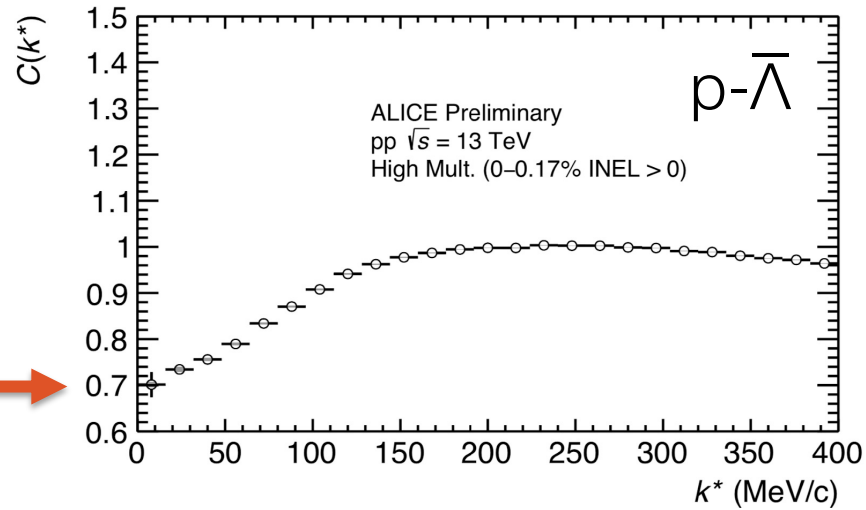


0–50%

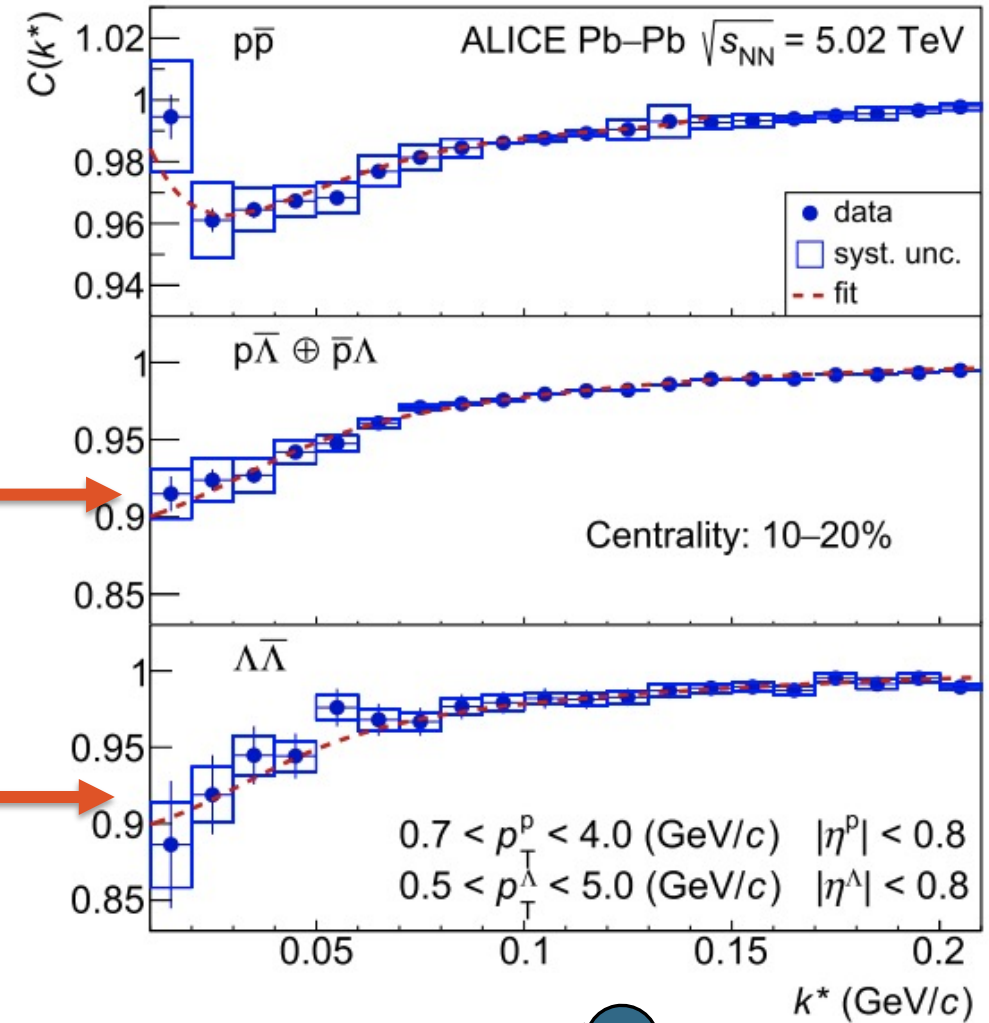


r (fm)

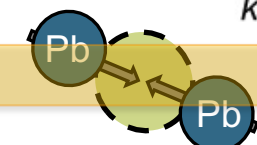
ALICE Coll. arXiv: 2105.05190



ALICE Coll. PLB 802 (2020) 135849



0-50%



$r \text{ (fm)}$

$$C_{p\text{-}\bar{p}}(k^*) = \overset{\text{elastic}}{\int S(r) |\psi_{p\bar{p} \rightarrow p\bar{p}}|^2 d^3 r} + \overset{n\text{-}\bar{n} \rightarrow p\text{-}\bar{p}}{\int S(r) |\psi_{n\bar{n} \rightarrow p\bar{p}}|^2 d^3 r}$$

- Chiral Effective Field Theory at $N^3\text{LO}$ (with $n\text{-}\bar{n}$ coupled-channel) wavefunctions with Coulomb
 - S and P waves, tuned to scattering data and protonium

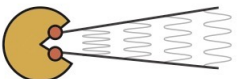
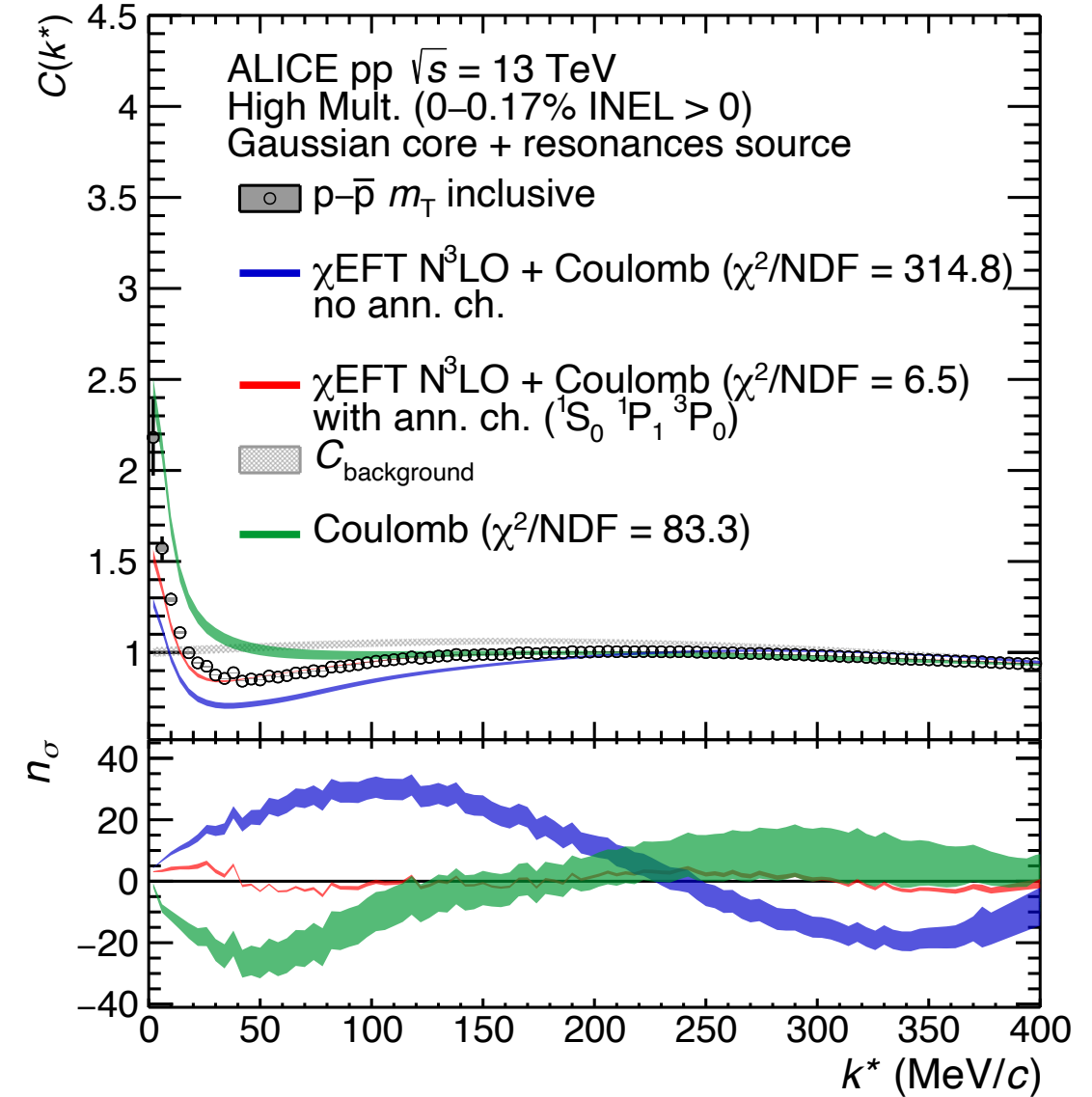
J. Haidenbauer et al. JHEP 1707 (2017)
D.Mihailov et al. Eur.Phys.J.C 78 (2018) 5, 394
Haidenbauer et al., PRD 92 (2015) 5, 054032

$$C_{p\bar{p}}(k^*) = \overset{\text{elastic}}{\int S(r) |\psi_{p\bar{p} \rightarrow p\bar{p}}|^2 d^3 r} + \overset{n\bar{n} \rightarrow p\bar{p}}{\int S(r) |\psi_{n\bar{n} \rightarrow p\bar{p}}|^2 d^3 r} + \overset{\text{multi-meson annihilation channels}}{\sum_{PW} \rho_{PW} \omega_{PW} \int S(r) |\psi_{p\bar{p} \rightarrow p\bar{p}}^{PW}|^2 d^3 r}$$

- **Chiral Effective Field Theory at N³LO** (with $n\bar{n}$ coupled-channel) wavefunctions with Coulomb
 - S and P waves, tuned to scattering data and protonium
- **Approximate inclusion of annihilation channels** ($X \rightarrow p\bar{p}$) using the Migdal-Watson approximation
 - elastic WF rescaled by a coupling weight ω_{PW} to be fitted to data
 - Investigation on the shape of each PWs to reduce number of parameters
 - 1S_0 for S states
 - 3P_0 and 1P_1 for P states
- Calculations performed with CATS framework

J. Haidenbauer et al. JHEP 1707 (2017)
D.Mihailov et al. Eur.Phys.J.C 78 (2018) 5, 394
Haidenbauer et al., PRD 92 (2015) 5, 054032

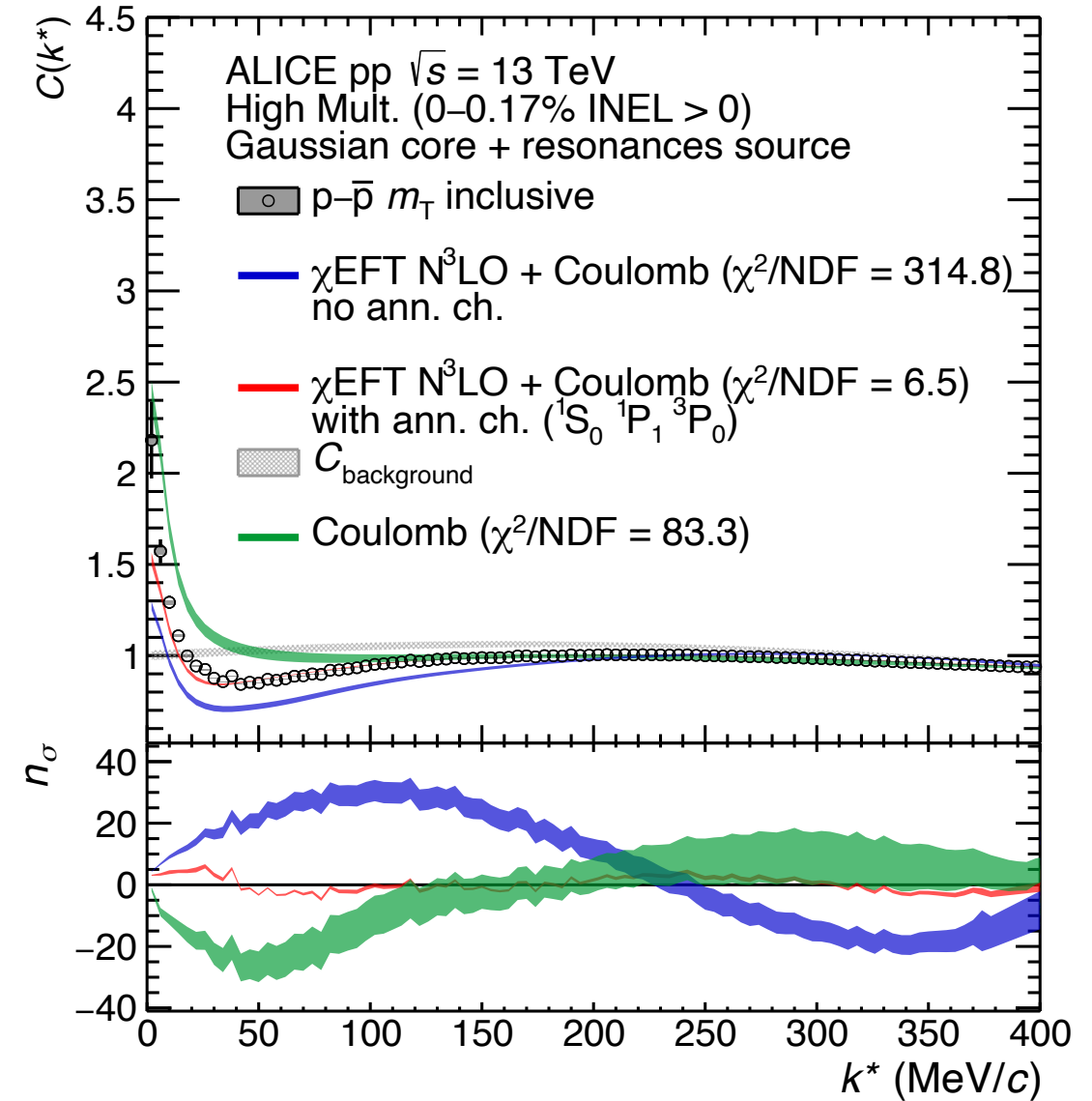
- No cusp of $n\text{-}\bar{n}$ opening at $k^* \sim 50 \text{ MeV}/c \rightarrow$ in agreement with charge-exchange cross-sections
- rise of CF at low k^*
 - no agreement with Coulomb only
 - χEFT calculations with no explicit CC terms do not reproduce the data at low k^*
 - evidence of annihilation channels feeding into $p\text{-}\bar{p}$ pairs



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 - evidence of annihilation channels feeding into $p\text{-}\bar{p}$ pairs
- **Annihilation channels $X \rightarrow p\text{-}\bar{p}$ included**
 - better agreement with the data is obtained
 - Dominant coupling weights in 3P_0 and 1S_0

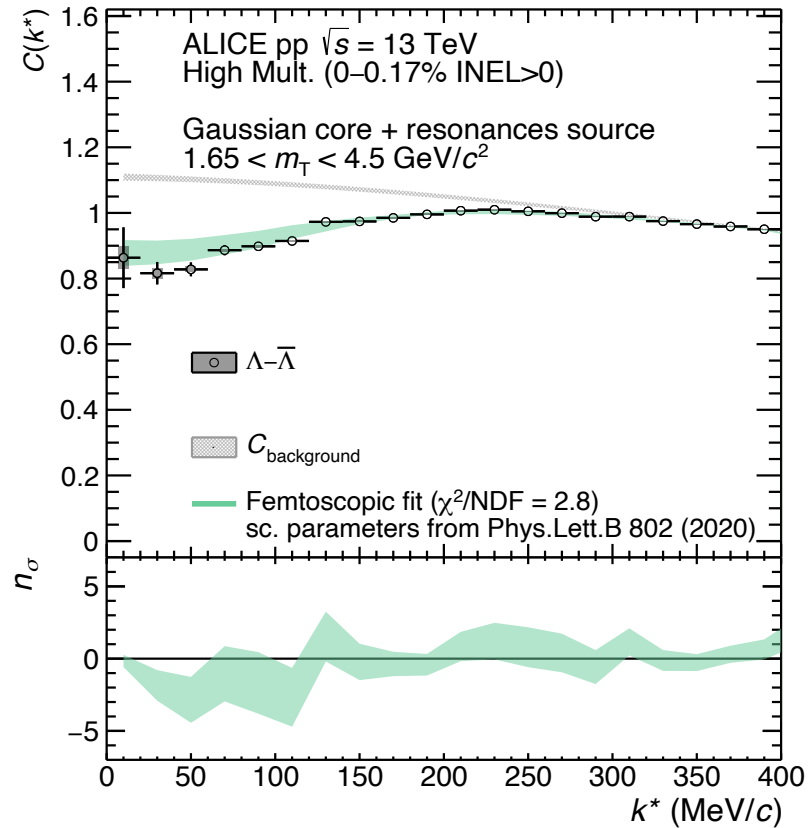
$$\omega_{^3P_0} = 40.04 \pm 4.06 \text{ (stat)} \pm 4.24 \text{ (syst)}$$

$$\omega_{^1S_0} = 1.19 \pm 0.10 \text{ (stat)} \pm 0.19 \text{ (syst)}$$

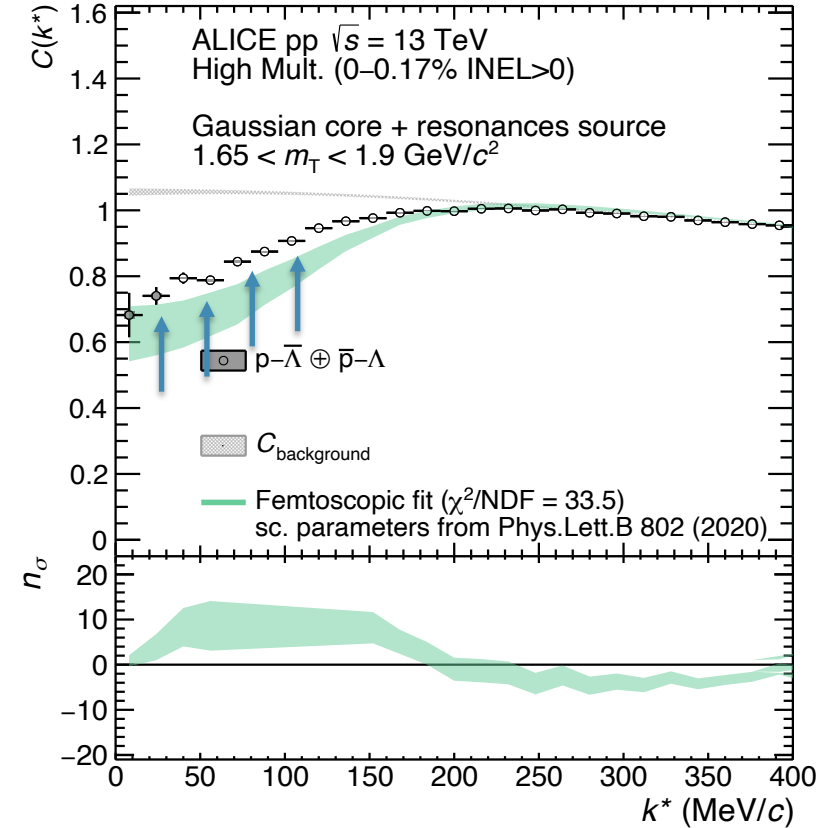
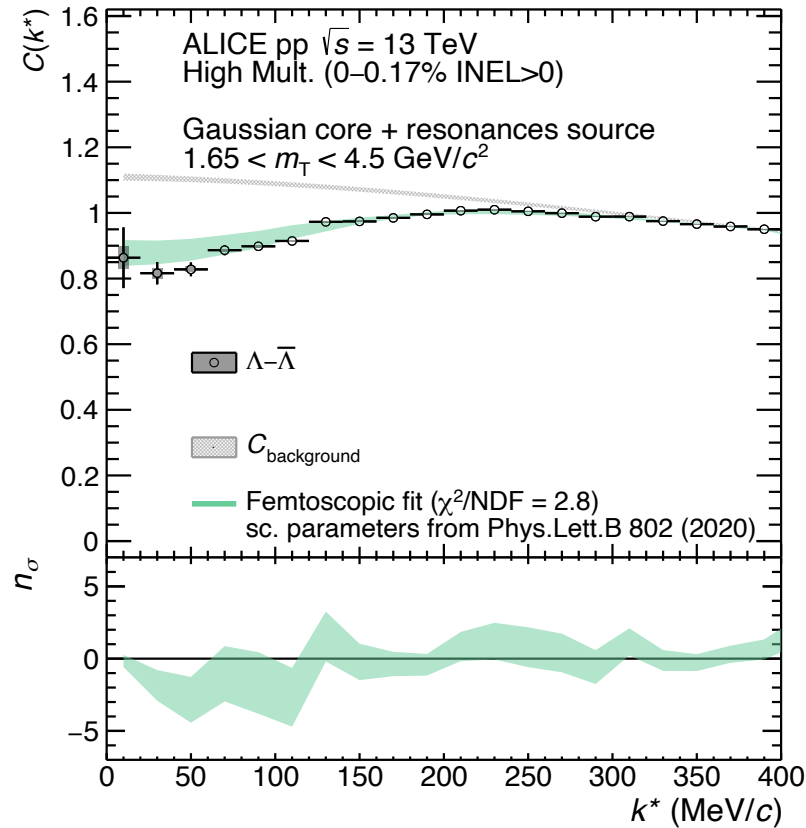


Results on Λ - $\bar{\Lambda}$ and p - $\bar{\Lambda}$ femtoscopy

- No exact wavefunctions available $\rightarrow$ single-channel Lednický-Lyuboshits formula ($\text{Re}(f_0)$, $\text{Im}(f_0)$)
- Assuming the scattering parameters obtained in Pb-Pb
 - nice agreement with Λ - $\bar{\Lambda}$ data $\rightarrow$ inelastic part present but not dominant

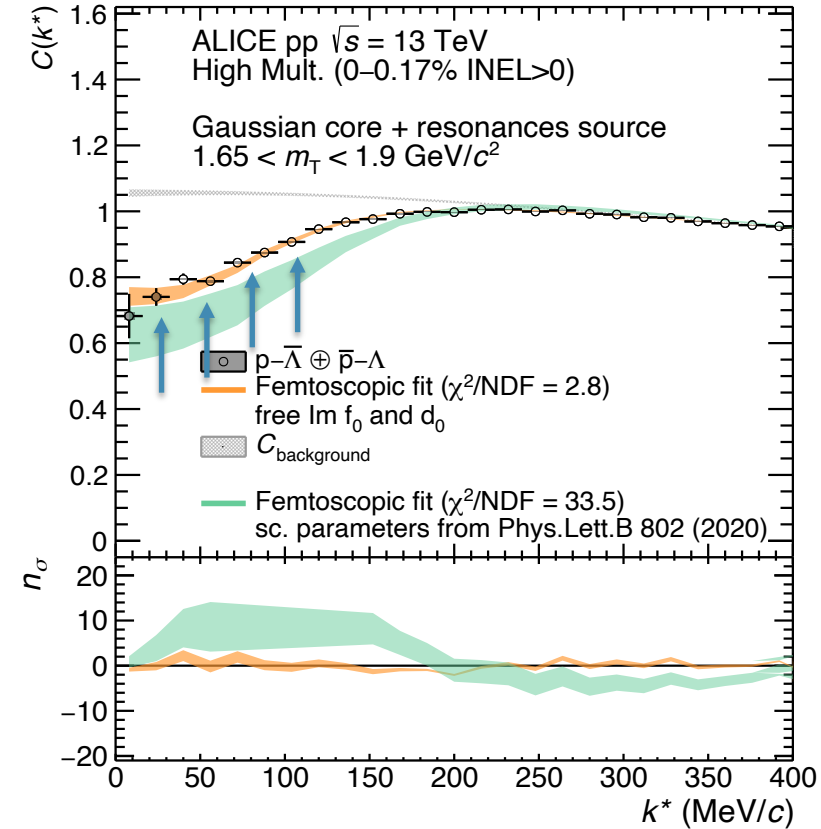
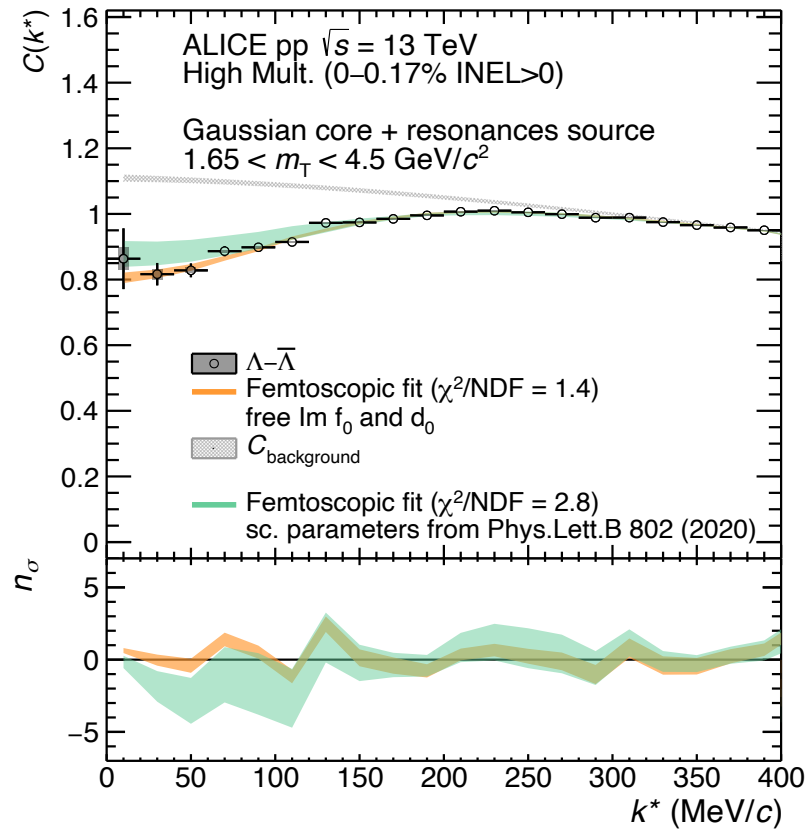


- No exact wavefunctions available $\rightarrow$ single-channel Lednicky'-Lyuboshits formula
- Assuming the scattering parameters obtained in Pb-Pb
 - nice agreement with Λ - $\bar{\Lambda}$ data $\rightarrow$ inelastic part present but not dominant
 - underestimate of p - $\bar{\Lambda}$ data $\rightarrow$ large coupling to multi-meson annihilation channels



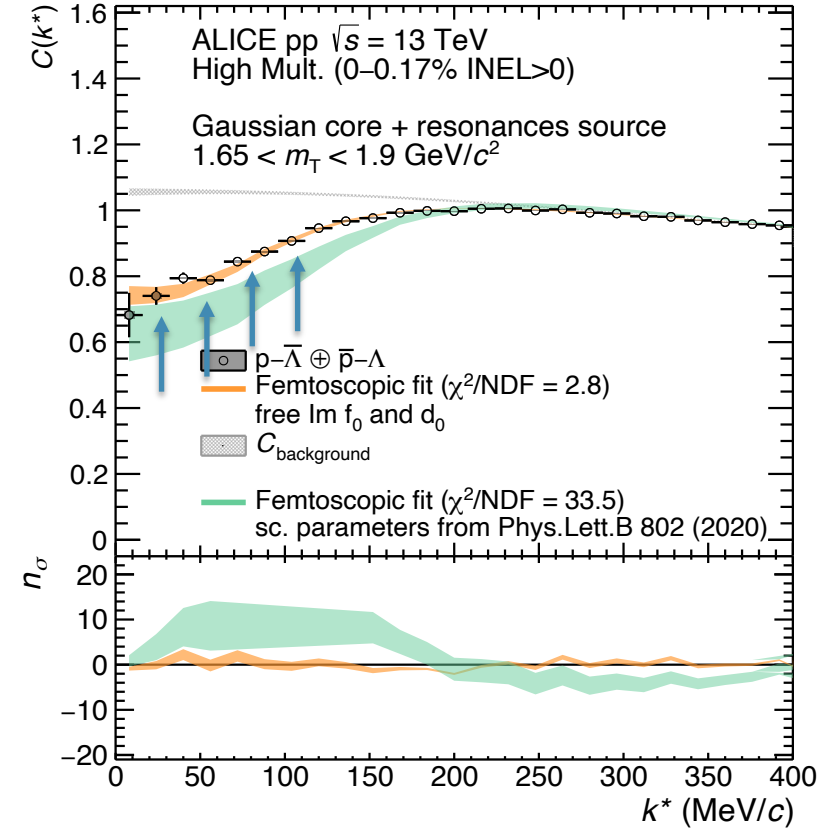
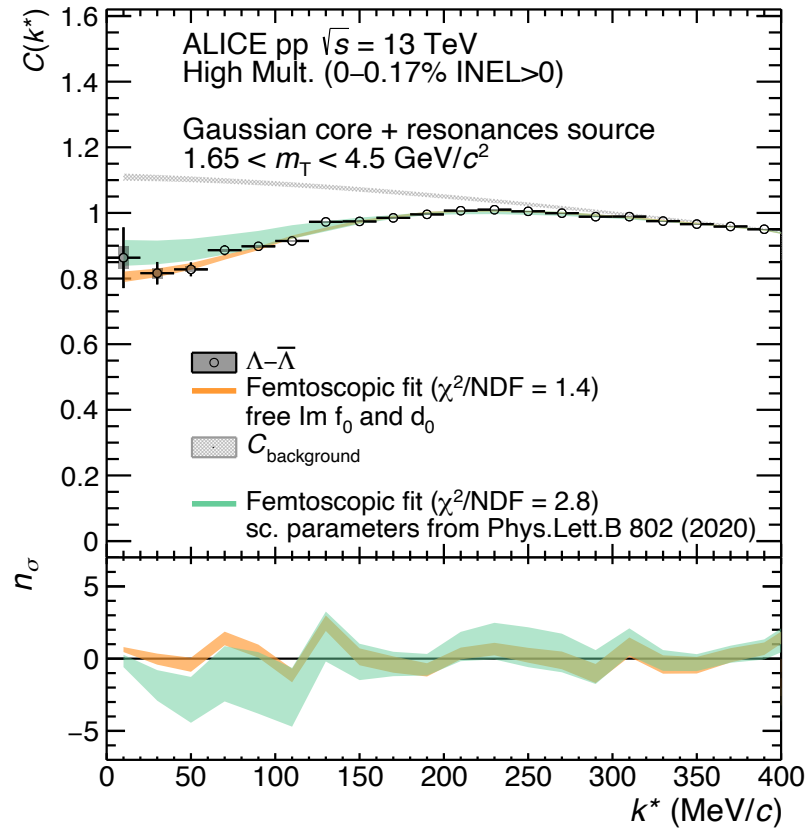
ALICE Coll. arXiv: 2105.05190

- Elastic part $\text{Re}(f_0)$ fixed from Pb–Pb data, free inelastic $\text{Im}(f_0)$ and d_0
 - extracted values for Λ - $\bar{\Lambda}$ are compatible with Pb–Pb scattering parameters
 - to reproduce p - $\bar{\Lambda}$ data $\text{Im}(f_0)$ has to be increased by a factor ~ 5.3
- Larger presence of multi-meson annihilation channels in p - $\bar{\Lambda} \rightarrow$ no bound states?

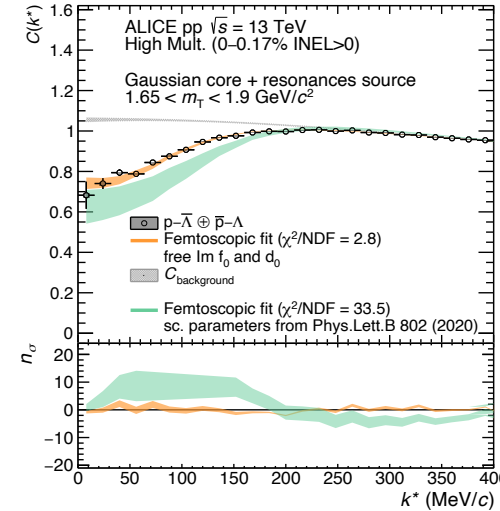
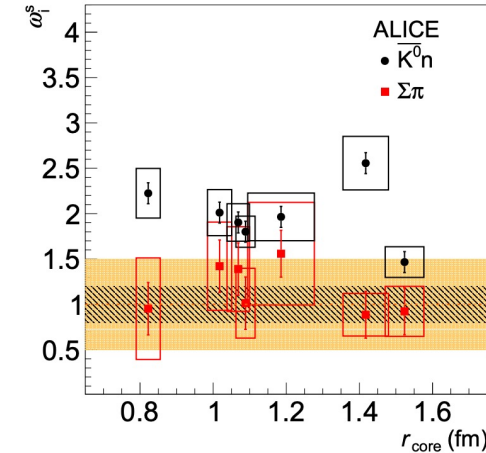


- Estimates based on kinematics (EPOS) and SU(3) flavour symmetry for 2-meson channels ($\pi\pi, \pi K$)
 - similar amount of p - $\bar{\Lambda}$ and Λ - $\bar{\Lambda}$ pairs at low k^* ($\sim 6.4\%$)
 - coupling strength from meson-baryon SU(3) lagrangian for p - $\bar{\Lambda} \sim 3$ times larger than Λ - $\bar{\Lambda}$

$$\frac{g_{2M \rightarrow p-\bar{\Lambda}} \times N_{2M \rightarrow p-\bar{\Lambda}}}{g_{2M \rightarrow \Lambda-\bar{\Lambda}} \times N_{2M \rightarrow \Lambda-\bar{\Lambda}}} \approx 6.3$$



- Femtosceny in small colliding systems
 - high-precision data at low momenta
 - sensitivity to inelastic channels as a function of the source size
- K-p in pp, peripheral p-Pb and ultra-per. Pb-Pb collisions
 - direct constraints on coupling to $\Sigma\pi$ and $\bar{K}^0 n$
 - data suggests a stronger coupling to $\bar{K}^0 n$
- Baryon-antibaryon in pp collisions
 - $\Lambda\bar{\Lambda}$ results annihilation not dominant and room for baryonia
 - $p\bar{\Lambda}$ large presence of annihilation channels $\rightarrow$ no formation of bound states?
 - need for theoretical input on $p\bar{\Lambda}$ and $\Lambda\bar{\Lambda}$ interactions

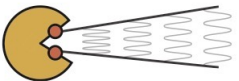


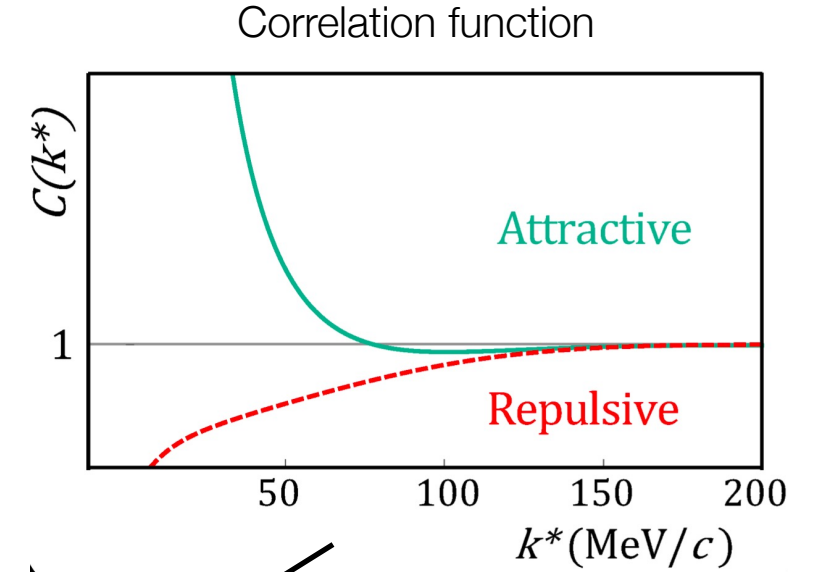
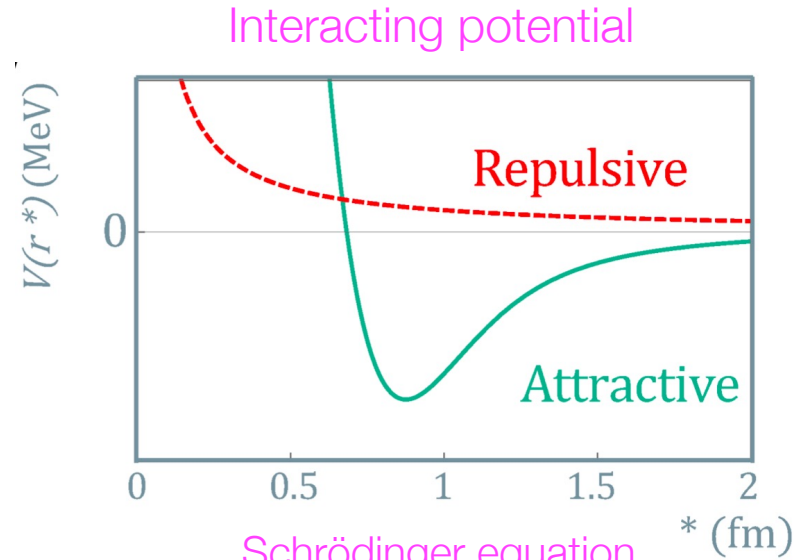
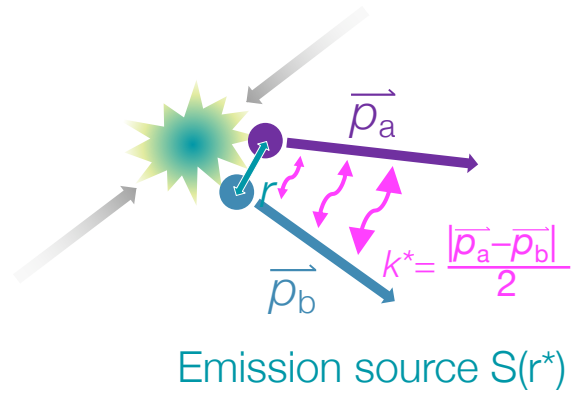
Run 1

$\Lambda\bar{\Lambda}$	PRC 99 (2019) 024001
$p\bar{\Xi}$	PLB 797 (2019) 134822
$p\bar{K}$ in pp	PRL 123 (2019) 112002
$p\bar{\Sigma}^0$	PRL 124 (2020) 09230
source	PLB 805 (2020) 135419
$p\bar{\Omega}$, $p\bar{\Xi}$	PLB 811 (2020) 135849
$p\bar{\Lambda}$	Nature 588 (2020) 232-238
$p\bar{\phi}$	arXiv:2104.04427
$p\bar{K}$ in Pb-Pb	PRL 127 (2021) 172301
$B\text{-anti}B$ in pp	PLB 822 (2021) 136708
	arXiv:2105.05190

more to come in the next months:
charm sector, 3-body correlations, $p\bar{d}$, $\Lambda\bar{\Xi}$,...

Additional slides



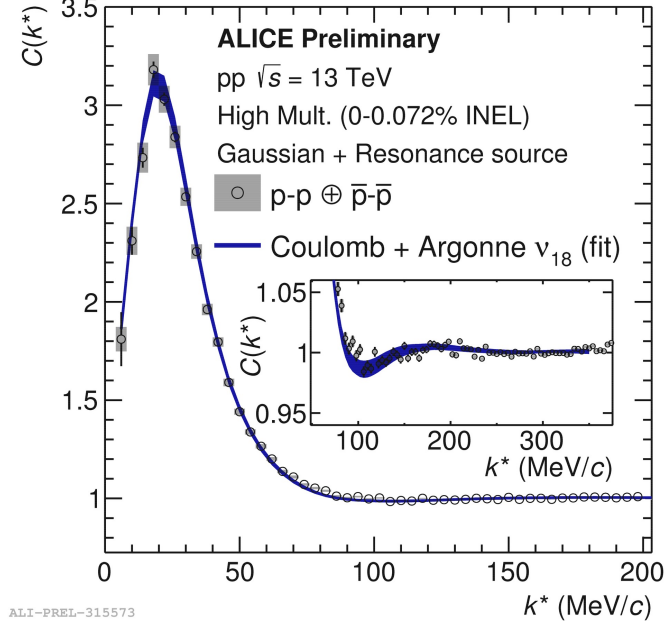


Schrödinger equation

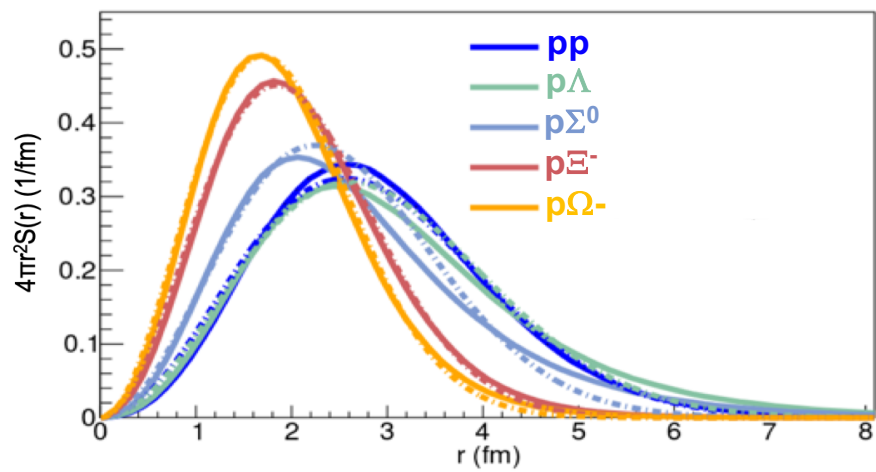
Two-particle wave function

$$C(k^*) = \int \underbrace{S(\vec{r}^*)}_{\text{Emission source}} \underbrace{|\psi(\vec{k}^*, \vec{r}^*)|^2}_{\text{Two-particle wave function}} d^3\vec{r}^* = \mathcal{N}(k^*) \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

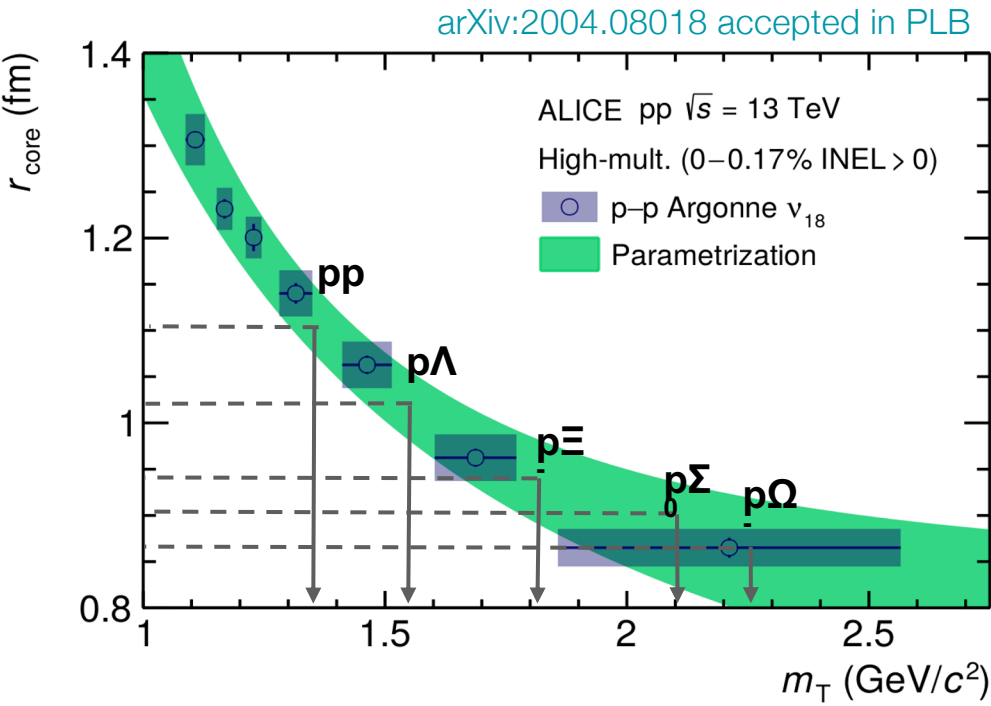
Fit with a ‘core’ Gaussian + Resonances



Effective Radius



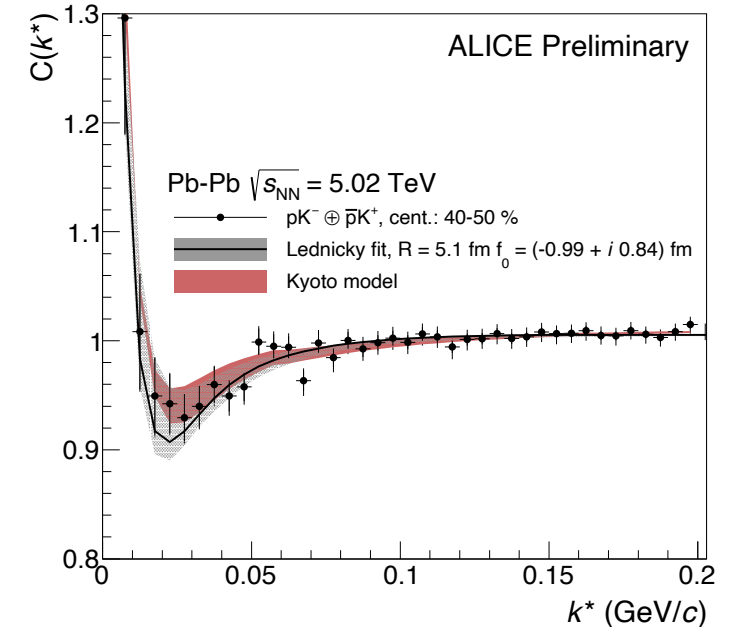
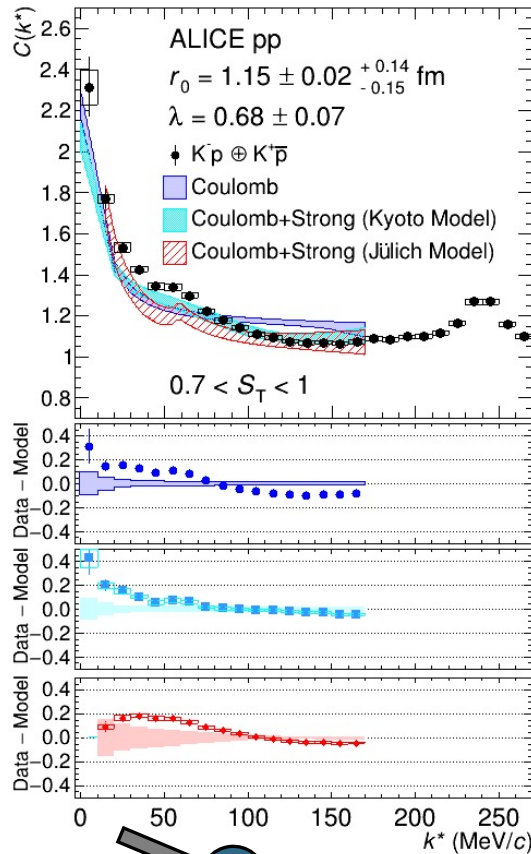
Core Radius



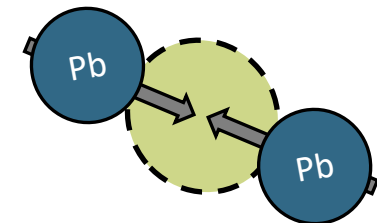
Pair	r_{Core} [fm]	r_{Eff} [fm]
pp	0.96	1.28
p Λ	0.88	1.3
p Σ^0	0.75	1.12
p Ξ^-	0.8	0.92
p Ω^-	0.73	0.85

- Disappearance of $\bar{K}^0$ -n cusp at $k^* \sim 60$ MeV/c as the source increases
- χ EFT Kyoto potential describes the data in all three systems
- Pb-Pb data well described by Lednicky single channel $\rightarrow$ negligible contribution from inelastic channels
- Pb-Pb results in agreement with scattering parameters from kaonic hydrogen

*Ikeda et al. Nucl.Phys.A 881 (2012),
PLB706 (2011)
Kamiya et al. PRL 124 (2020)
Mihayara et al. PRC95 (2017)*

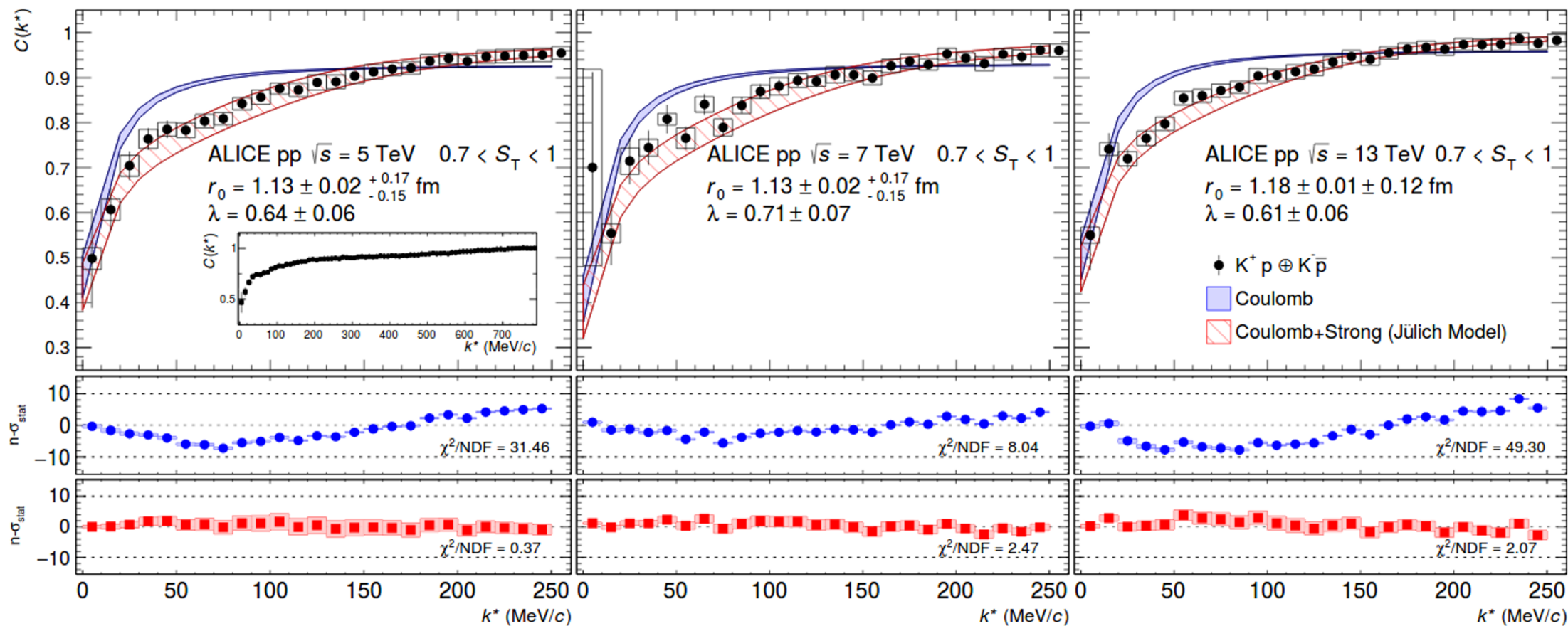


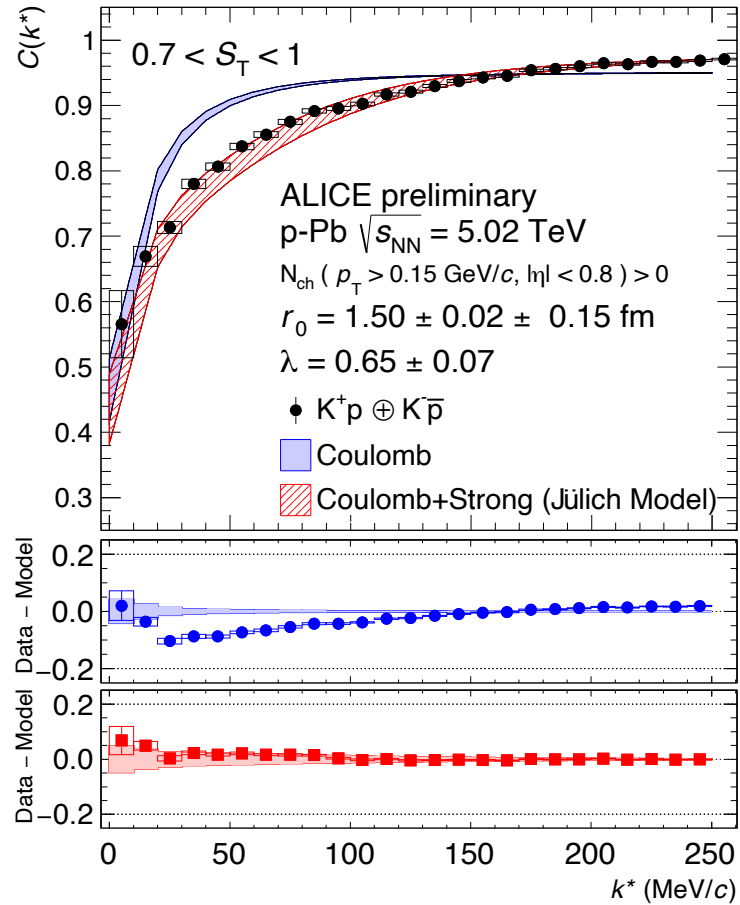
ALI-PREL-354647



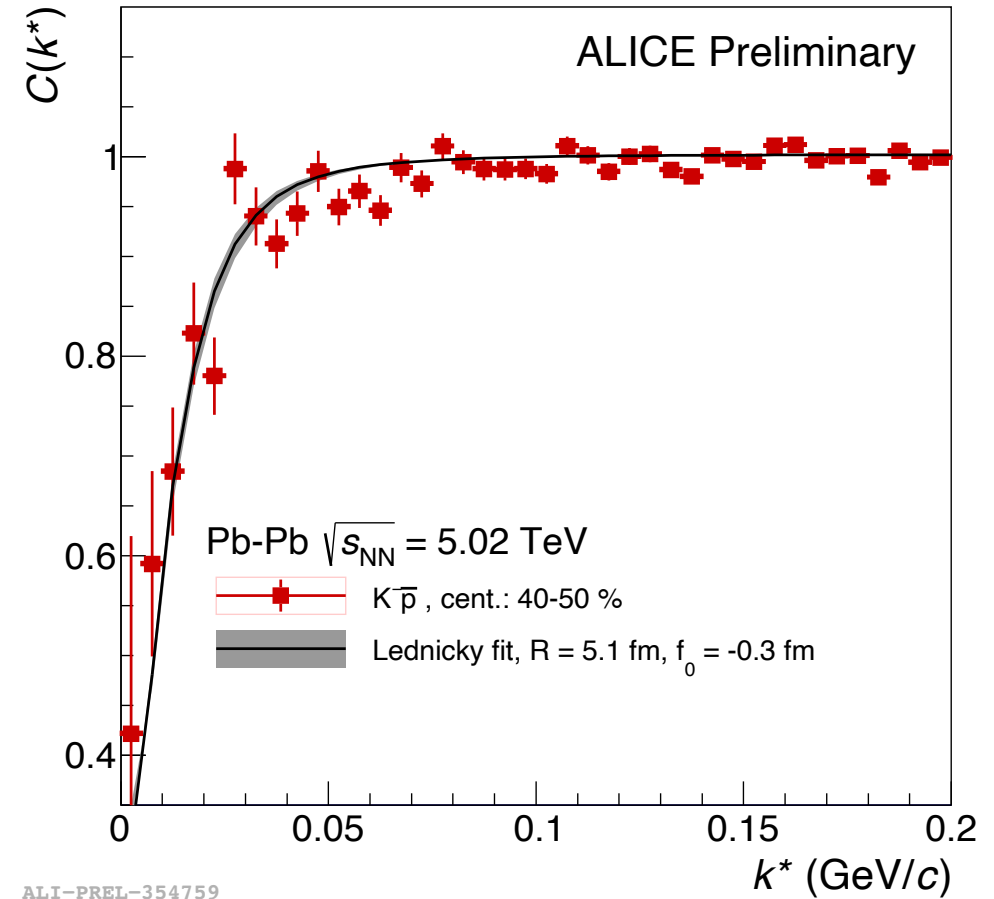
assuming $w_j = 1$

ALICE Coll. Phys.Rev.Lett. 124 (2020) 9, 092301

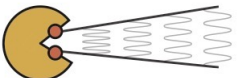




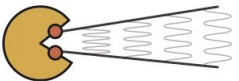
ALI-PREL-316319



ALI-PREL-354759



$$C(k^*) = 1 + \sum_{\sigma} \rho_{\sigma} \left[\frac{1}{2} \left| \frac{f(k^*)}{R} \right|^2 \left(1 - \frac{d_0^{\sigma}}{2\sqrt{\pi}R} \right) + \frac{2\Re f(k^*)}{\sqrt{\pi}R} F_1(2k^*R) - \frac{\Im f(k^*)}{R} F_2(2k^*R) \right]$$

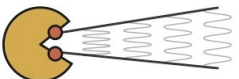


$$P = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{\eta_N + \pi^0}{\sqrt{2}} & \pi^+ & K^+ \\ \pi^- & \frac{\eta_N - \pi^0}{\sqrt{2}} & K^0 \\ K^- & \bar{K}^0 & \eta_S \end{pmatrix} \quad B = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{\Lambda}{\sqrt{6}} + \frac{\Sigma^0}{\sqrt{2}} & \Sigma^+ & p \\ \Sigma^- & \frac{\Lambda}{\sqrt{6}} - \frac{\Sigma^0}{\sqrt{2}} & n \\ \Xi^- & \Xi^0 & -\frac{2\Lambda}{\sqrt{6}} \end{pmatrix} \quad \bar{B} = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{\bar{\Lambda}}{\sqrt{6}} + \frac{\bar{\Sigma}^0}{\sqrt{2}} & \bar{\Sigma}^- & \bar{\Xi}^+ \\ \bar{\Sigma}^+ & \frac{\bar{\Lambda}}{\sqrt{6}} - \frac{\bar{\Sigma}^0}{\sqrt{2}} & \bar{\Xi}^0 \\ \bar{p} & \bar{n} & -\frac{2\bar{\Lambda}}{\sqrt{6}} \end{pmatrix}$$

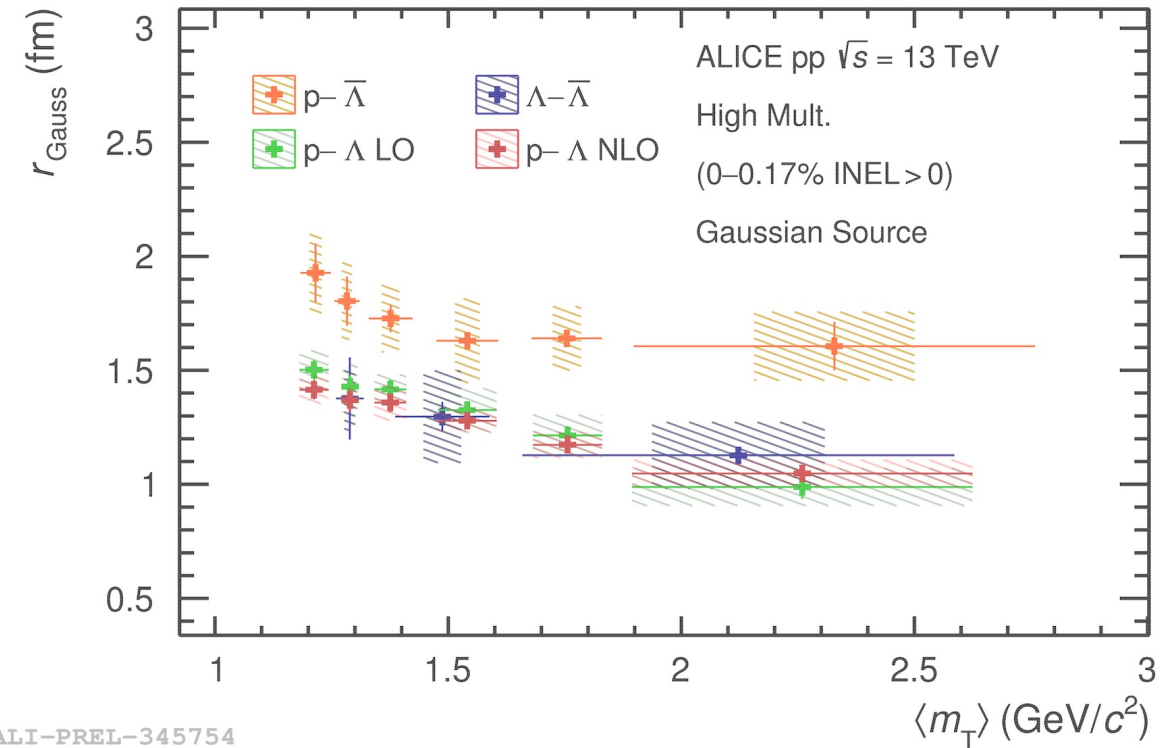
The Lagrangian describing the processes from B-antiB (p-antip, p-antiΛ, Λ-antiΛ) to Mesons-AntiMesons (π-antiπ, π-antiK) is typically written in the following form:

$$\mathcal{L} = g \text{Tr}\{B \cdot \bar{B} \cdot P \cdot P\}$$

g is the coupling constant, same for all processes, typically determined by experiments (see e.g the nucleon-pion coupling $g_{\pi NN}$ from scattering data)



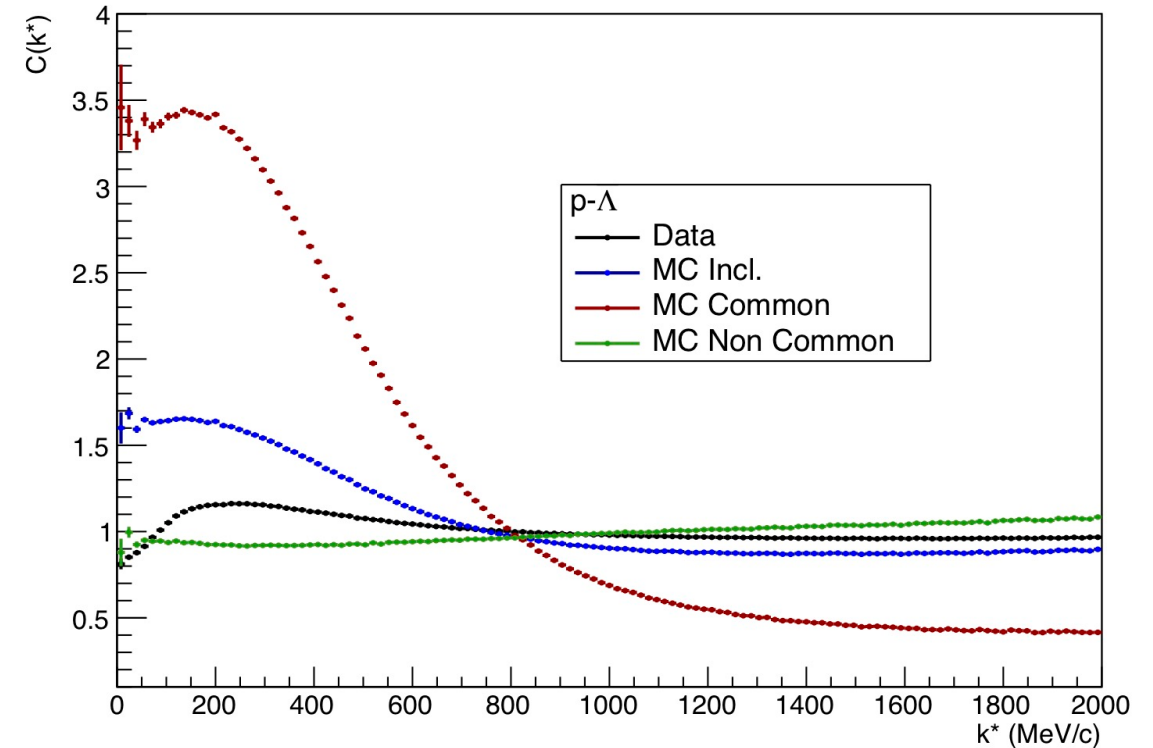
- $\Lambda\text{-anti}\Lambda$ correlation function: well reproduced by Lednicky-Lyuboshits (Pb–Pb), extracted radius in agreement with B-B scaling
- $p\text{-anti}\Lambda$ correlation function: well reproduced by Lednicky-Lyuboshits, **BUT** extracted radius larger wrt to B-B scaling
- **Physical interpretation:** $p\text{-anti}\Lambda$ is more coupled-channels contributions (supported by $SU(3)_f$ considerations) $\Rightarrow$ larger amount of inelastic channels translates into larger radius



- Large background that cannot be removed by applying S_T / S_0 cuts $\Rightarrow$ results are obtained WITHOUT any S_T/S_0 cuts
- Use of Pythia to model the background:
 - jetty contributions $\Rightarrow$ particles from Common ancestors
 - non-jetty part $\Rightarrow$ particles from Non Common Ancestors

$$C_{mini-jet}(k^*) = [w_C C_C(k^*) + (1 - w_C) C_{NC}(k^*)]$$

- Weights w_C to be fitted to data since they cannot be anchored to $\Delta\eta\Delta\phi$ correlations (more than a rescaling is needed)

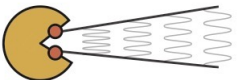


- Residual contributions included through λ parameters (DCA/CPA Template Fits)
- Non-femtoscopic background:
 - Mini-jet background $\Rightarrow$ Shape fixed by Ancestors Template
 - Large k^* kinematics effects $\Rightarrow$ Pol1/Pol2 (prefit in k^* [400-2500] MeV/c and kept fixed in the final fit)

$$C_{BCKG}(k^*) = [w_C C_C(k^*) + (1 - w_C) C_{NC}(k^*) + (a + b k^* + c (k^*)^2)]$$

- Total correlation function:
 - Free parameters: weights w_C , Norm N_D
 - Coupled-channel modeling affects ONLY C_{model}

$$C_{\text{tot}}(k^*) = N_D \cdot C_{\text{model}}(k^*) \cdot C_{BCKG}(k^*),$$



- Pairs close in mass with the same quantum numbers: e.g. $p-\Xi^-$ and $\Lambda-\Lambda$
- Schrödinger equation of one pair $\rightarrow$ Equation system of all 1, ..., N pairs

$$\hat{\mathcal{H}} \cdot \psi = E \cdot \psi \mapsto \begin{pmatrix} \hat{\mathcal{H}}_{11} & \cdots & \hat{\mathcal{H}}_{1N} \\ \vdots & \ddots & \vdots \\ \hat{\mathcal{H}}_{N1} & \cdots & \hat{\mathcal{H}}_{NN} \end{pmatrix} \cdot \begin{pmatrix} \psi_1 \\ \vdots \\ \psi_N \end{pmatrix} = E \cdot \begin{pmatrix} \psi_1 \\ \vdots \\ \psi_N \end{pmatrix}$$

•

1) Coupled channels influence the elastic channels of the two-particle wave function ψ_j

