

# **Study the $\bar{p}p \rightarrow e^+e^-\pi^0$ process at low $e^+e^-$ - invariant masses at PANDA**

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# Outline

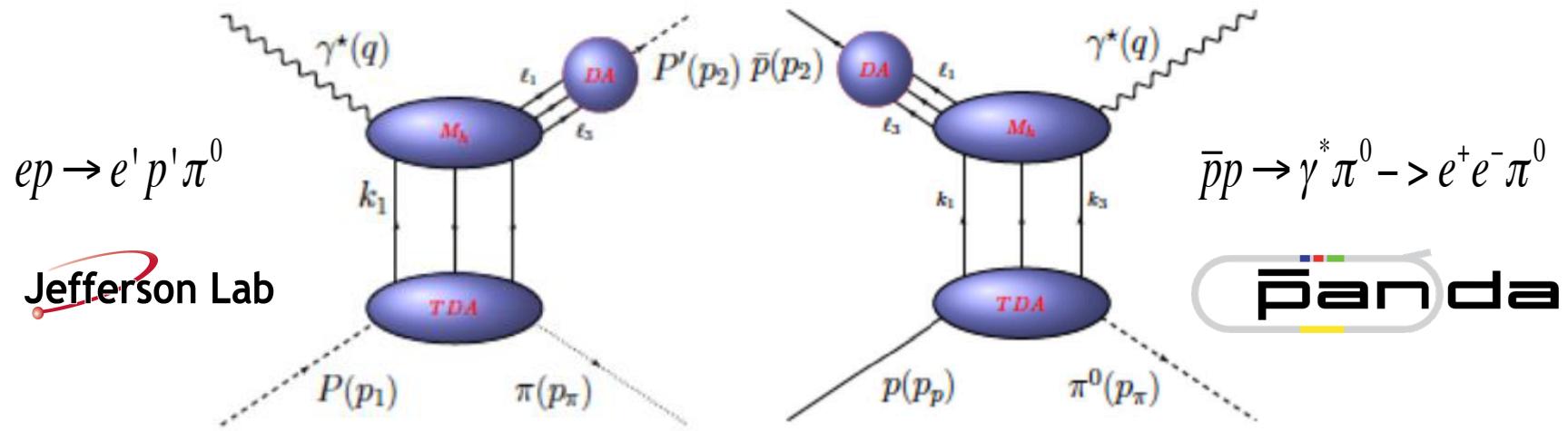
- Model description of the process  $\bar{p}p \rightarrow \gamma^* \pi^0 \rightarrow e^+ e^- \pi^0$  within the framework of
  - Transition Distribution Amplitudes (TDAs)
  - Regge pole description (baryon exchange and form factors)
- Feasibility measurements at PANDA

I.  $P_{\text{lab}} = 1.7 \text{ GeV}/c$  ( $s=5 \text{ GeV}^2$ );  $q^2 = 0.605 \pm 0.01 (\text{GeV}/c^2)^2$

II.  $P_{\text{lab}} = 1.7 \text{ GeV}/c$  ( $s=5 \text{ GeV}^2$ );  $q^2 = 2.0 \pm 0.125 (\text{GeV}/c^2)^2$

- Determination of the signal efficiency (PANDAROOT)
- Study of the reaction mechanism at PANDA – determination of the statistical precisions on the differential cross sections
- Proton form factors in the unphysical region

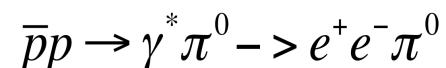
# Nucleon to meson TDAs



J.P. Lansberg et al. (2012), B. Pire, L. Szymanowski, K. Semenov-Tian-Shansky (2013)

- New class of non-perturbative structure functions
- Occur in collinear factorization description of various hard exclusive processes
- Are independent of reaction type,  $s$  and  $q^2$

Experimental checks of the collinear factorization regime in hard exclusive reactions:



$$\frac{d\sigma}{dt dq^2 d \cos \theta_\ell^*} \Big|_{\text{Leading twist}} = \frac{K}{s - 4M^2} \frac{1}{(q^2)^5} (1 + \cos^2 \theta_\ell^*)$$

# Nucleon to meson TDAs at PANDA

**Collinear factorization-TDAs**

**Large  $q^2 \sim s$  (hard scale)**

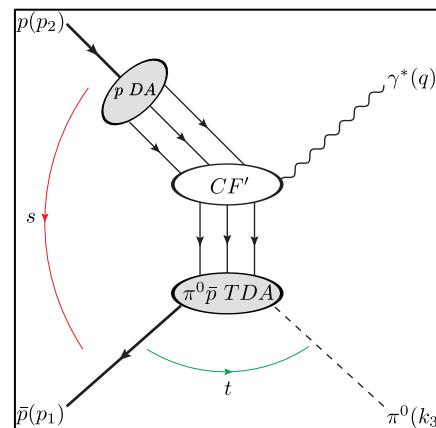
$|t| \ll q^2, s, |u| \ll q^2, s$

- Feasibility studies performed for  $q^2$  above 3  $(\text{GeV}/c^2)^2$
- Simplified model for TDAs – based on soft pion theorem: independent of  $t$  and  $u$
- **Test QCD factorization**

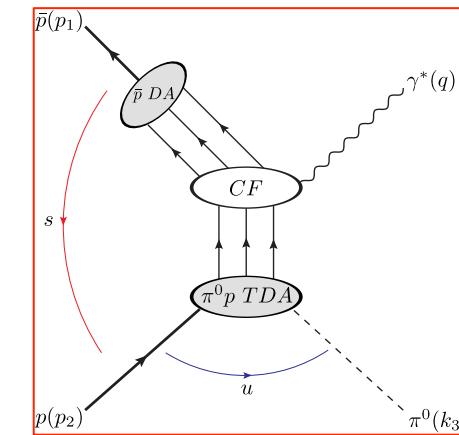
$$d\sigma / dq^2 = 1 / (q^2)^5$$

$$d\sigma / \cos \theta_e^* \sim D \times (1 + C \cos^2 \theta_e^*), C = 1$$

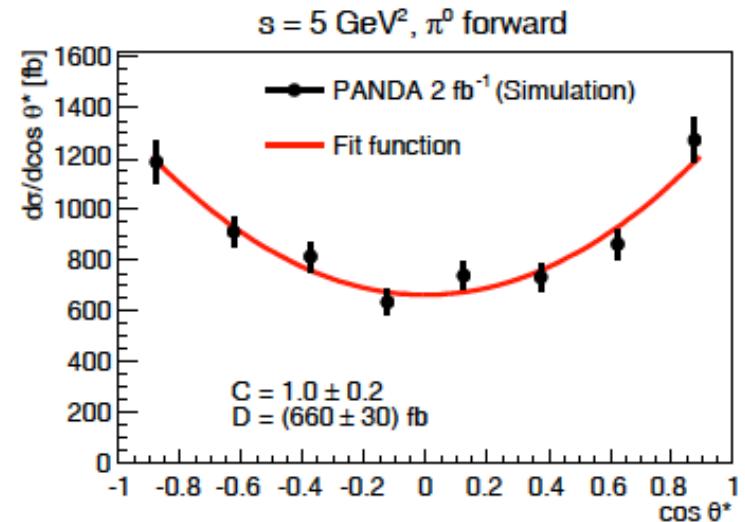
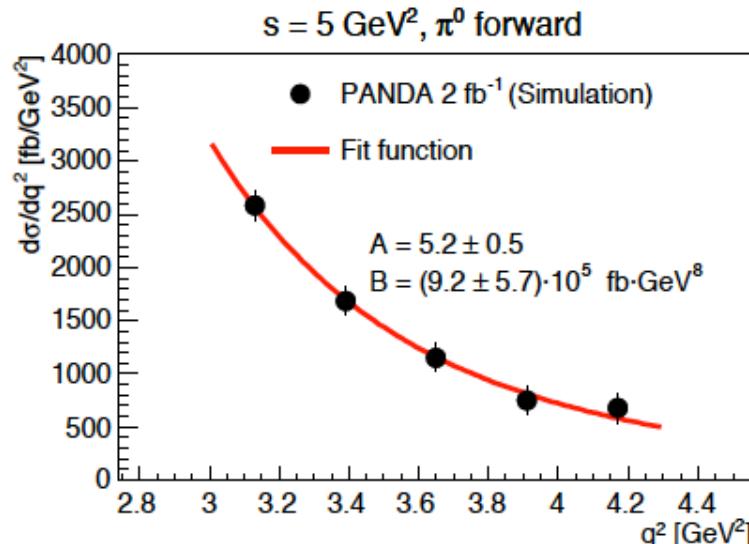
$t$  is small  
(near forward regime)



$u$  is small  
(near backward regime)



**PANDA Collaboration**  
**EPJA 51 (2015) 8, 107**

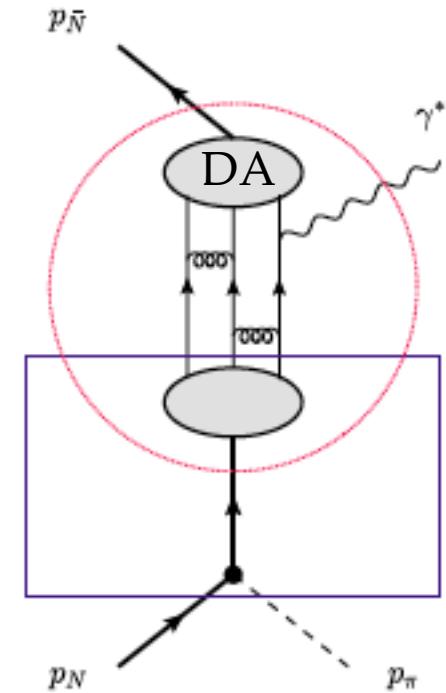
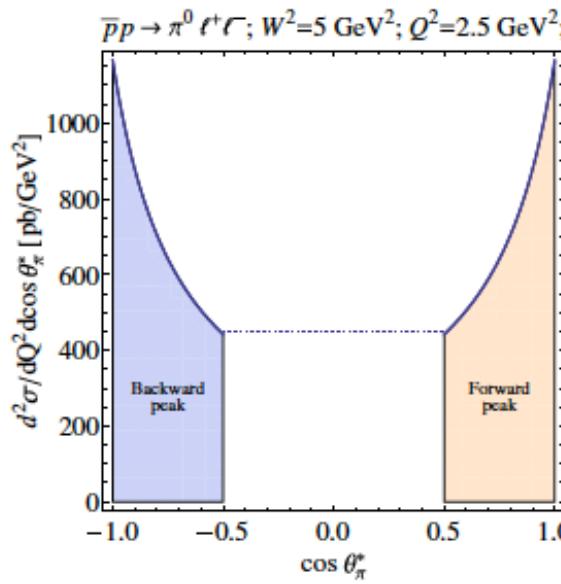
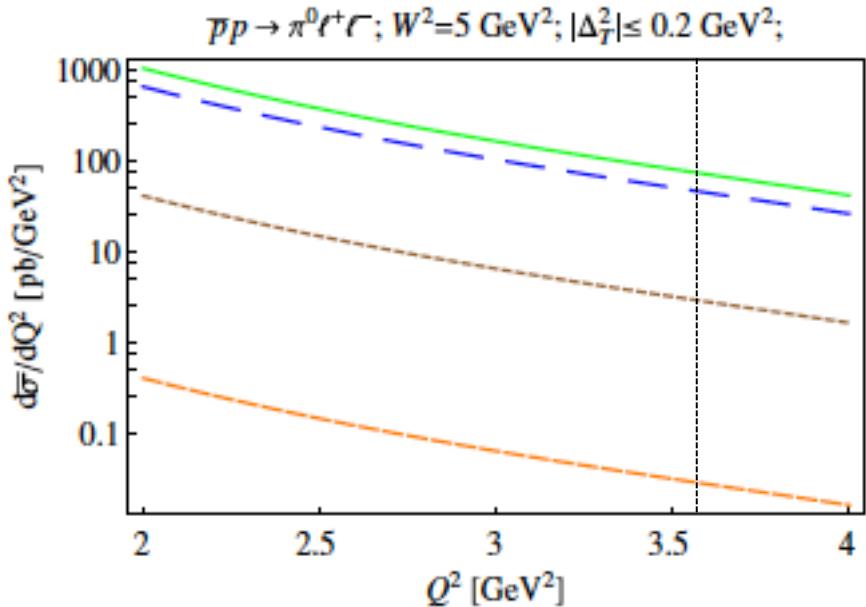


# Nucleon to meson TDAs

PRD 86, 114033 (2012)

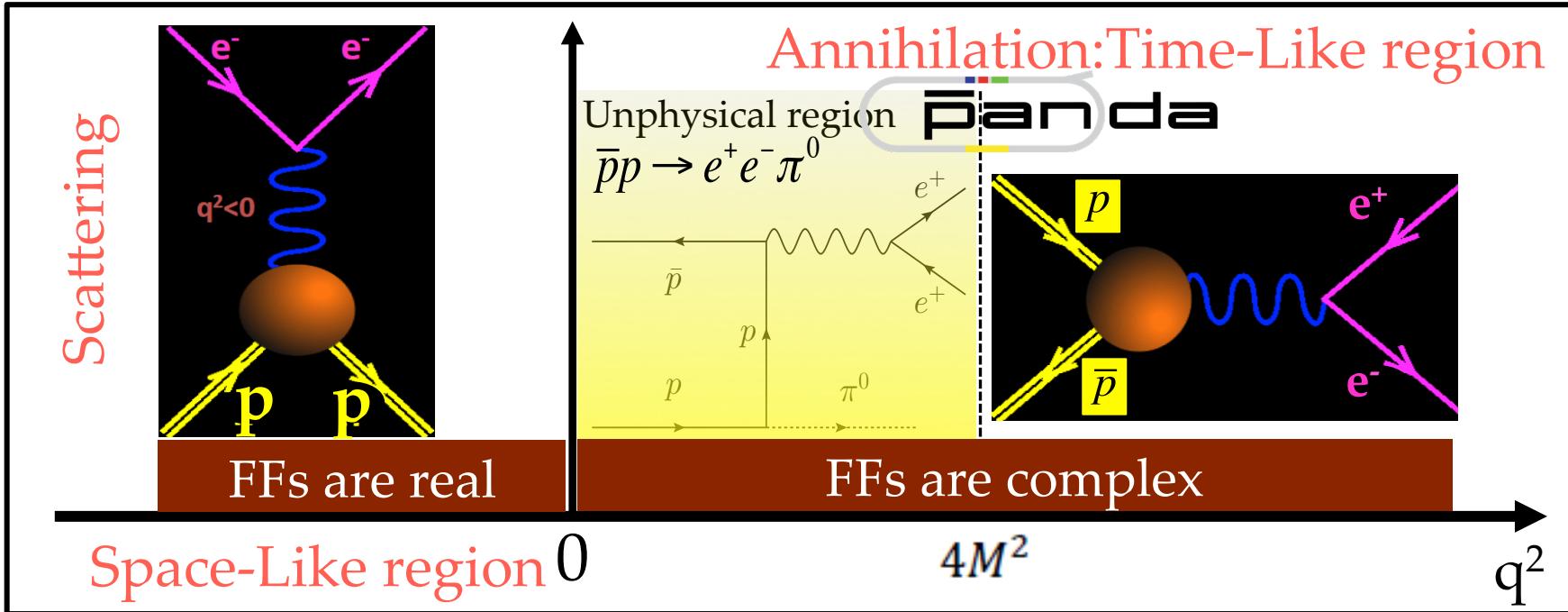
B. Pire et al. [arXiv:2103.01079 [hep-ph]]  
(2020).

- More general model was proposed taking into account the dependence on  $t$  and  $u$
- Contribution due to nucleon pole exchange was added



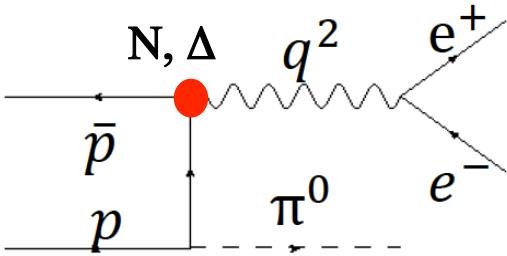
- Strong dependence of the cross section on proton distribution amplitude (DA) models
- For the same model used in previous feasibility studies, cross section is 2 order of magnitude larger
- Predictions down to  $2 \text{ (GeV/c}^2)^2$  were given

# Proton electromagnetic form factors

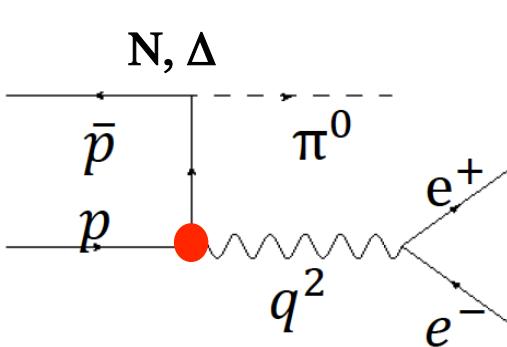


- M. P. Rekalo, Sov. J. Nucl. Phys. 1 (1965) 760
- C. Adamuscin et al., Phys. Rev. C 75, 045205 (2007)
- A.Z. Dubnickova , S. Dubnicka , M.P. Rekalo, Z. Phys. C 70, 473–481 (1996)
- G. I. Gakh et al. PHYSICAL REVIEW C 83, 025202 (2011)
- Feasibility studies by J. Boucher; PhD thesis (BaBar Framework)
- J. Guttmann, M. Vanderhaeghen, PLB B 719 (2013) 136–142

# Differential cross section and hadronic tensors

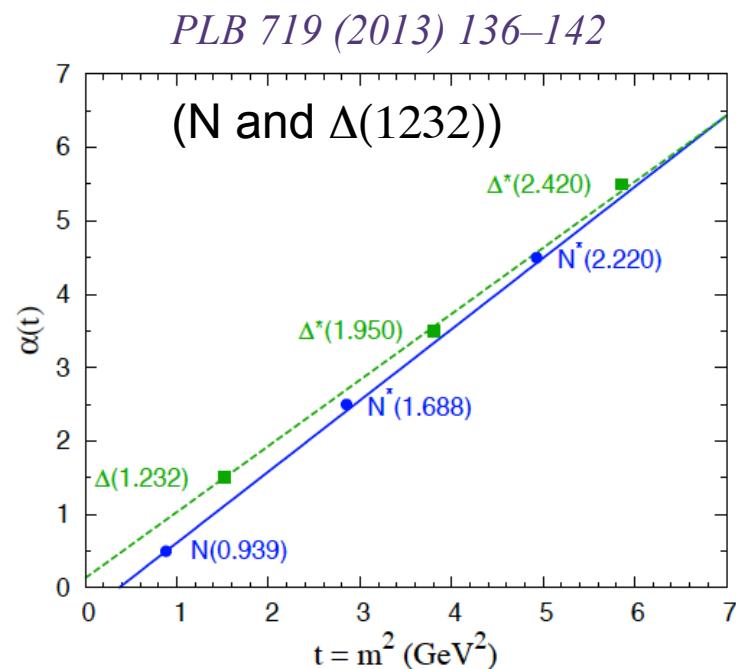


$$\frac{d\sigma}{dq^2 d\cos\theta_{\pi^0} d\Omega_e^*} \propto L^{\mu\nu} H_{\mu\nu}$$



Regge pole description at forward ( $|t| \ll s$ ) and backward ( $|u| \ll s$ ) regions (Regge limit)

Exchange of dominant baryon Regge trajectories



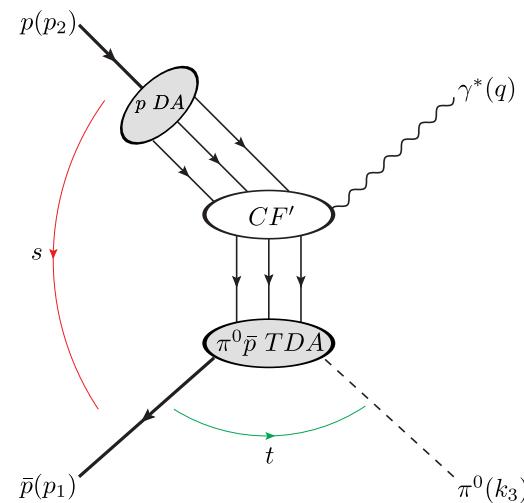
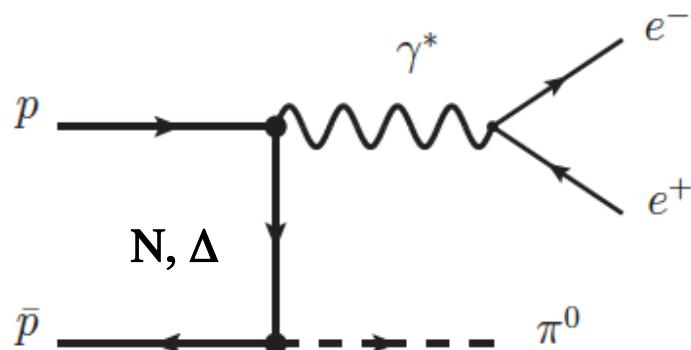
$$\begin{aligned} \frac{d\sigma}{dq^2 d\cos\theta_{\pi^0} d\Omega_e^*} &= 4\pi e^2 q^2 (H_{11} + H_{22} + H_{33}) - 8e^2 p_e^{*2} \left( \frac{H_{11} + H_{22}}{2} \right. \\ &\quad \left. + \frac{H_{11} - H_{22}}{2} \sin^2 \theta_e^* \cos 2\varphi_e^* + 2H_{13} \sin \theta_e^* \cos \theta_e^* \cos \varphi_e^* + \frac{1}{2} (2H_{33} - H_{11} - H_{22}) \cos^2 \theta_e^* \right) \end{aligned}$$

$\theta_{\pi^0}$  in the laboratory frame  
 $\theta_e^*$ ,  $\varphi_e^*$  in the  $\gamma^*$  rest frame

- $d\sigma/dq^2$  is predicted by the time-like form factors ( $\sim 1/q^5$  for TDAs)
- $d\sigma/dt$ ,  $d\sigma/du$  by the  $N$  and  $\Delta$  propagators (given by TDA model in collinear factorization)
- $d\sigma/d\cos\theta_e^*$  is a function of the process kinematical variables and the form factors (for TDAs  $\sim 1 + \cos\theta_e^*$ )

## A. Study of the production mechanism

Measurements of the differential cross sections  $d\sigma/dt$ ,  $d\sigma/du$ ,  $d\sigma/d\cos\theta_e^*$  at PANDA



# Description of the Monte Carlo simulations

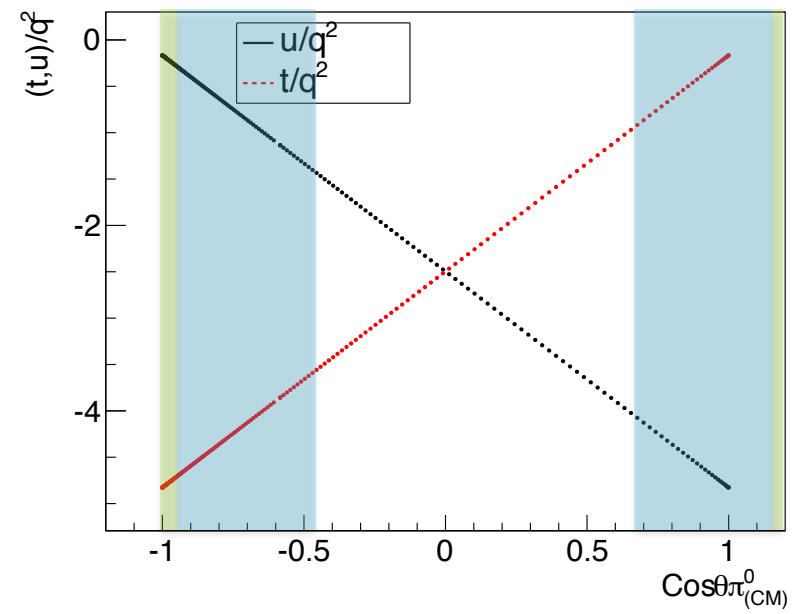
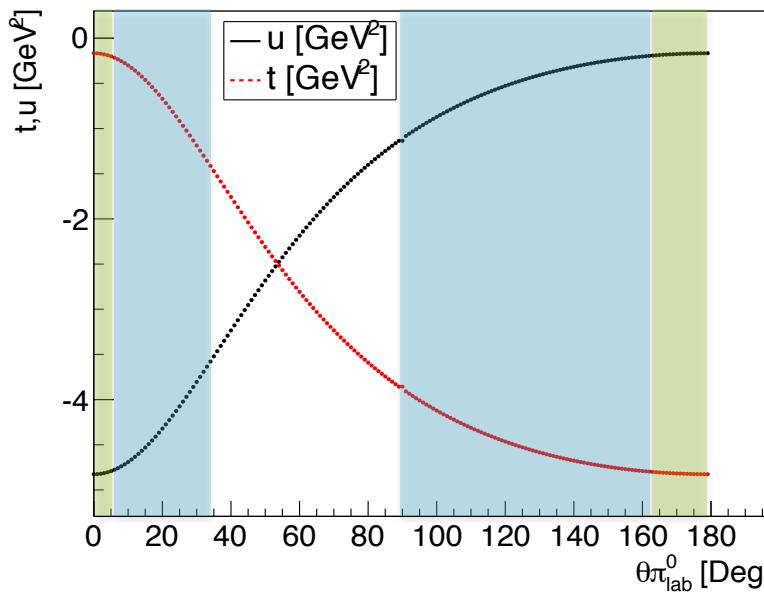
- Signal  $\bar{p}p \rightarrow e^+e^-\pi^0$ ; Main background  $\bar{p}p \rightarrow \pi^+\pi^-\pi^0$
- PANDARoot version **oct19**, FairSoft **jun19p1**, FairRoot **v18.2**
- **Event generation**
  - Antiproton momentum (lab)  $p_{p\bar{p}} = 1.7 \text{ GeV}/c$ 
    - $q^2 = 0.605 \pm 0.015 (\text{GeV}/c^2)^2$ ;  $q^2 = 2.0 \pm 0.375 (\text{GeV}/c^2)^2$
  - PHSP angular distributions, PHOTOS switched on
  - $5.10^7$  ( $10^8$ ) events for the signal (background) in each  $q^2$  interval
- **Event selection**
  - PID probability for  $e^+/e^-$  larger than **99% or 99.8%** (**EMC+STT+MVD+DRC**)
  - $E_{\text{EMC}}/p > 0.8$  and  $dE/dx(\text{STT}) > 5.8$
  - 4C kinematic fit ( $\chi^2 < 50$  or  $\chi^2 < 30$ )
- **Signal efficiency in bins of  $q^2$ ,  $\theta_{\pi^0}$ ,  $\cos\theta_e^*$ , and  $\varphi_e^*$** 
  - Integrated signal efficiency between 13% and 15%
  - Signal contamination from the main background at the order or below 1%

# Feasibility studies – Case I

- $P_{\text{lab}} = 1.7 \text{ GeV}/c$  ( $s=5.4 \text{ GeV}^2$ );  $q^2 = 0.605 \pm 0.01 \text{ (GeV}/c^2)^2$

- Regge description expected for  $|\cos\theta_{\pi^0}|_{\text{CM}} > 0.5 \text{ && } |t,u|/q^2 > 20\%$   
 $\theta_{\pi^0}(\text{Lab}) = [5^\circ - 32^\circ], [83^\circ - 160^\circ]$

- TDAs description expected for  $|\cos\theta_{\pi^0}|_{\text{CM}} > 0.5 \text{ && } |t,u|/q^2 < 20\%$   
 $\theta_{\pi^0}(\text{Lab}) = [0^\circ - 5^\circ], [160^\circ - 180^\circ]$

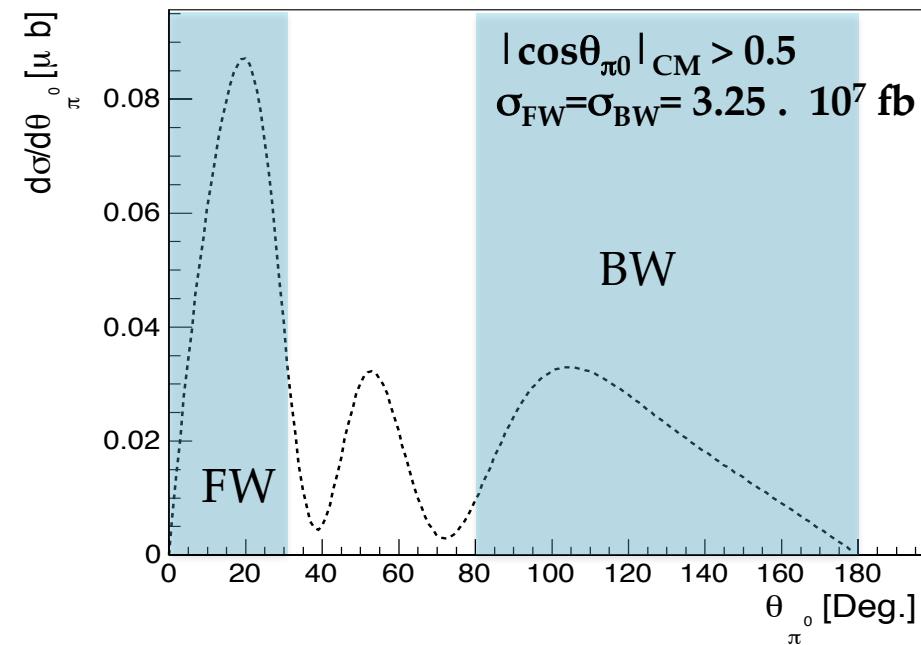


- At small  $s$  and  $q^2$  below  $1 \text{ (GeV}/c^2)^2$  the process is expected to occur through the exchange of dominant baryons
  - Region for Time-like form factor measurements**

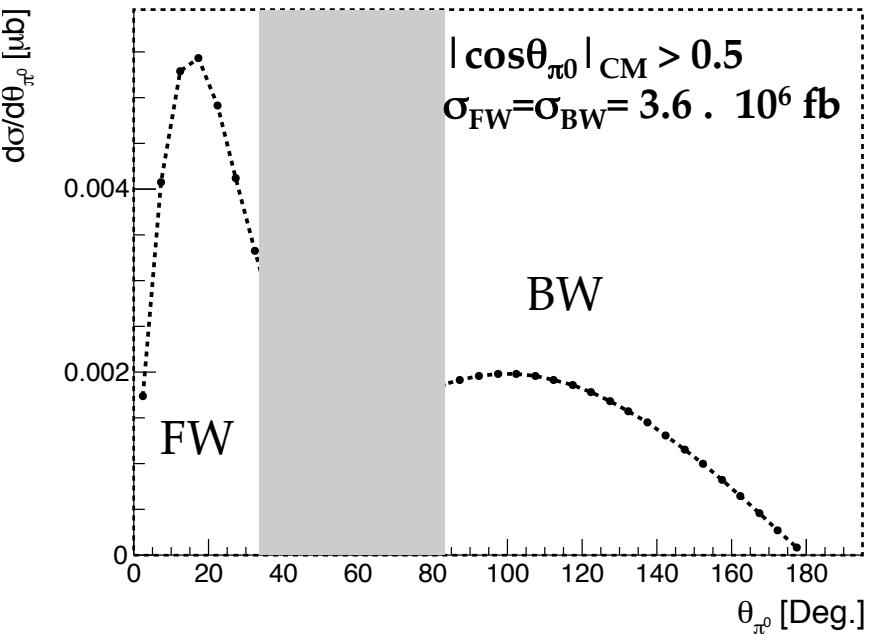
# Theoretical cross sections- Case I

- $P_{\text{lab}} = 1.7 \text{ GeV}/c$  ( $s=5.4 \text{ GeV}^2$ );  $q^2 = 0.605 \pm 0.01 \text{ (GeV}/c^2)^2$

Regge description



TDA-model

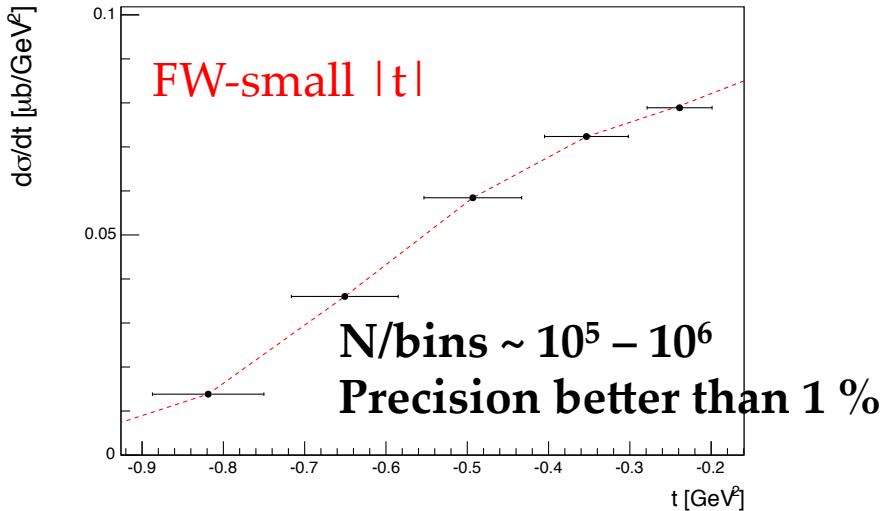


- Large cross section
- Form factors Vector Meson Dominance; F. Iachello, PRC 69, 055204 (2004)

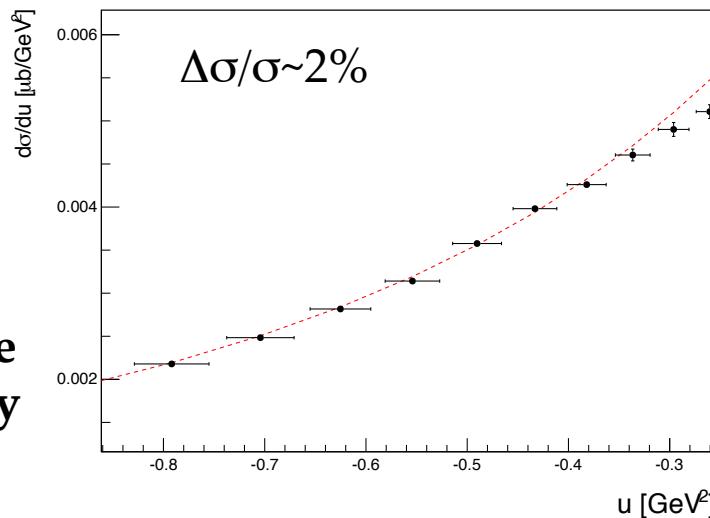
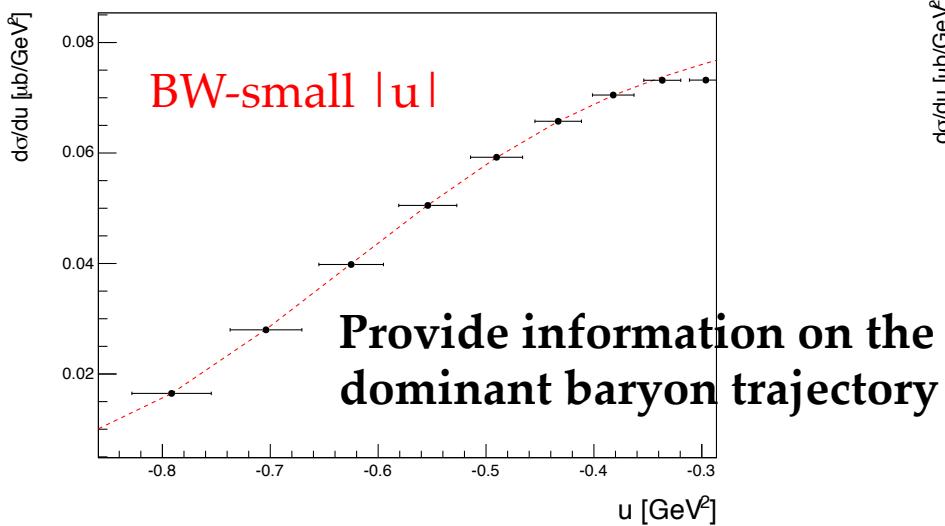
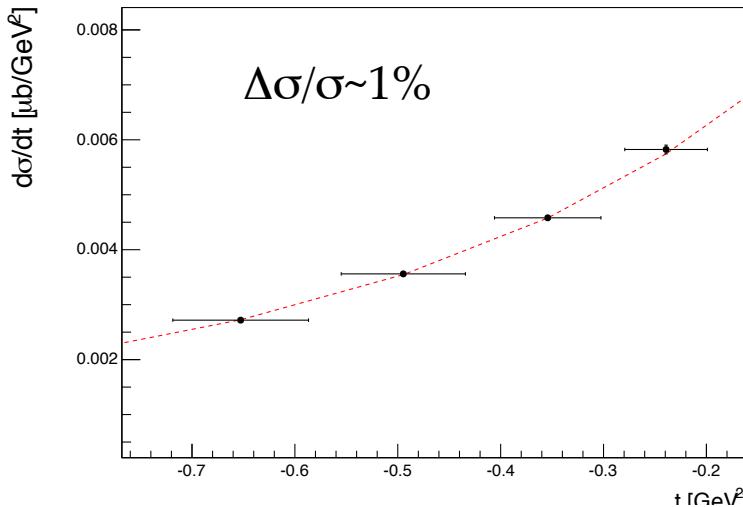
- TDA model shown only to compare the distributions with Regge description;
- non physical counting rate ( $|t,u| \sim q^2$ )

# Feasibility studies – Case I - $d\sigma/dt$ , $d\sigma/du$

Regge description



TDA-model



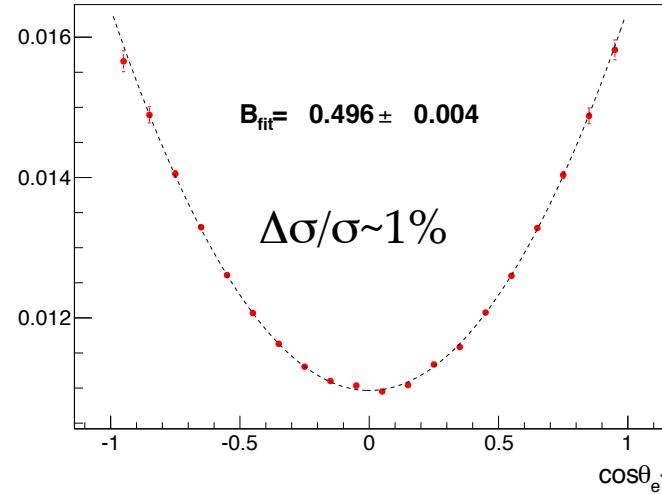
# Feasibility studies – Case I - $d\sigma/d\cos\theta_e^*$

Regge description

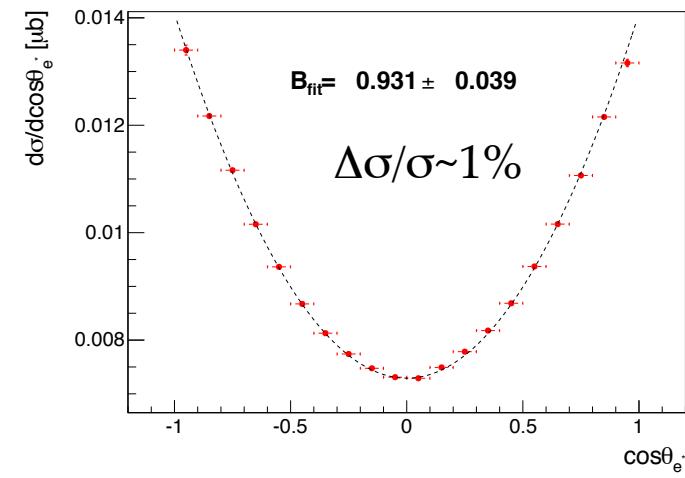
$$d\sigma / \cos\theta_e^* \sim A \times (1 + B \cos^2 \theta_e^*)$$

TDA-model (B=1)

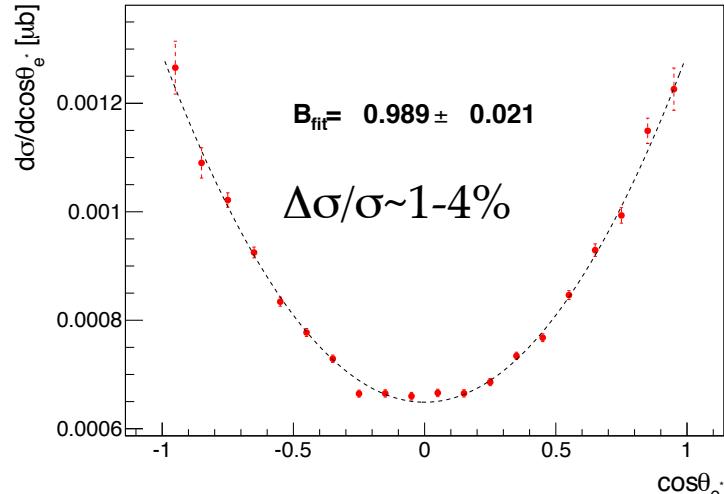
FW-Regge



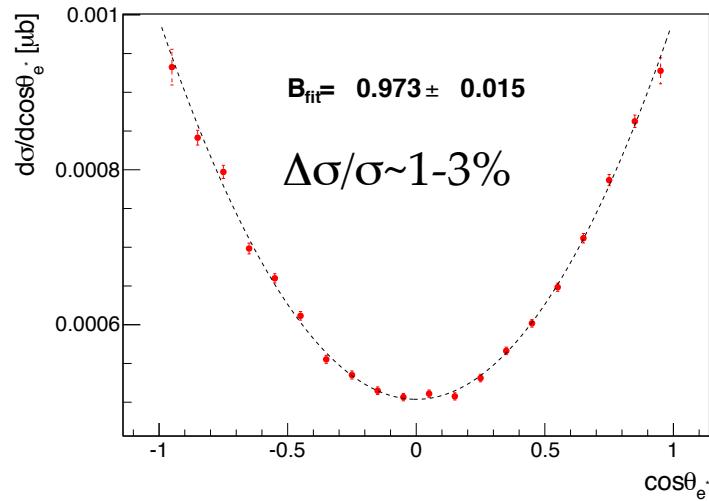
BW-Regge



FW-TDAs

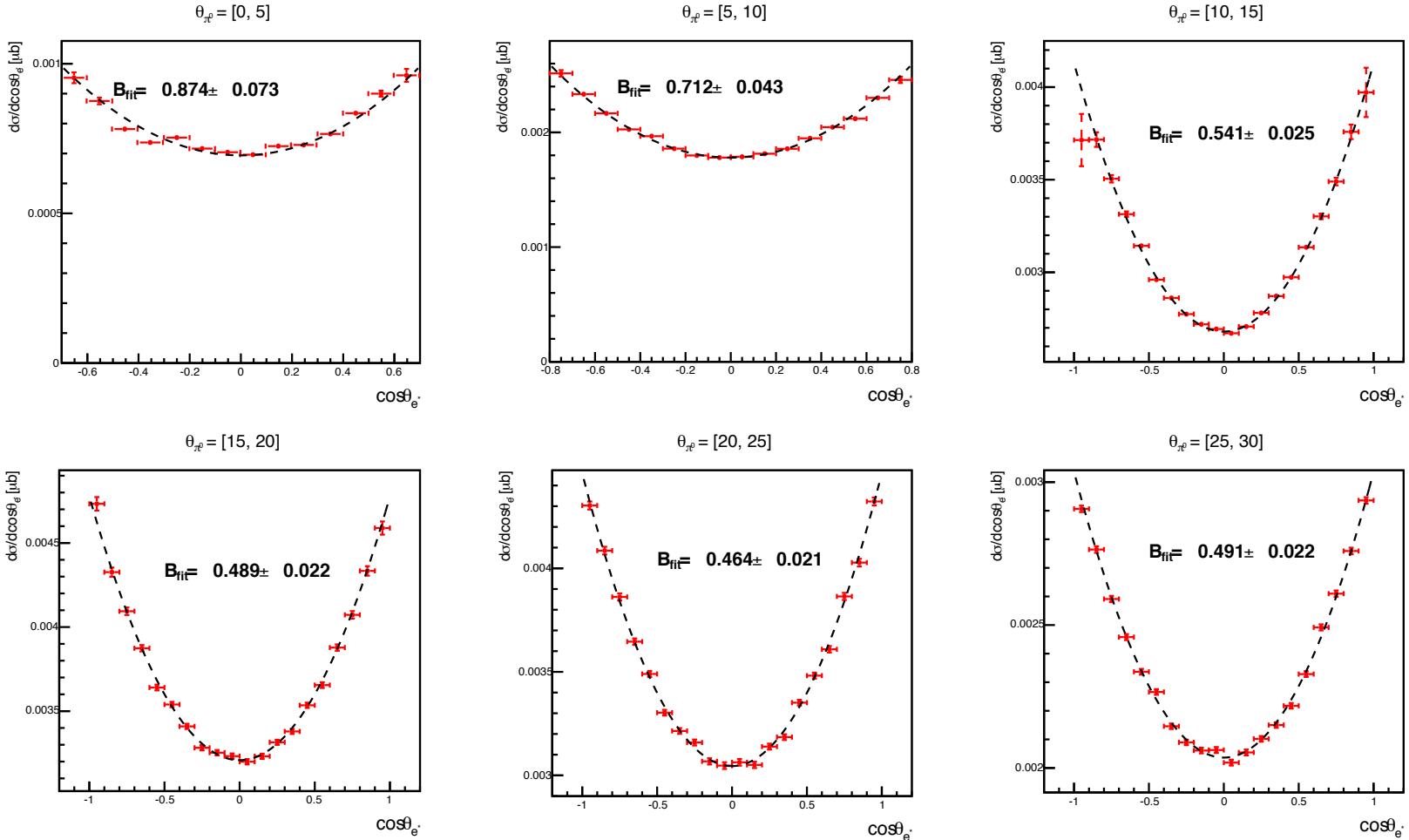


BW-TDAs



# Feasibility studies – Case I - $d\sigma/d\cos\theta_e^*$

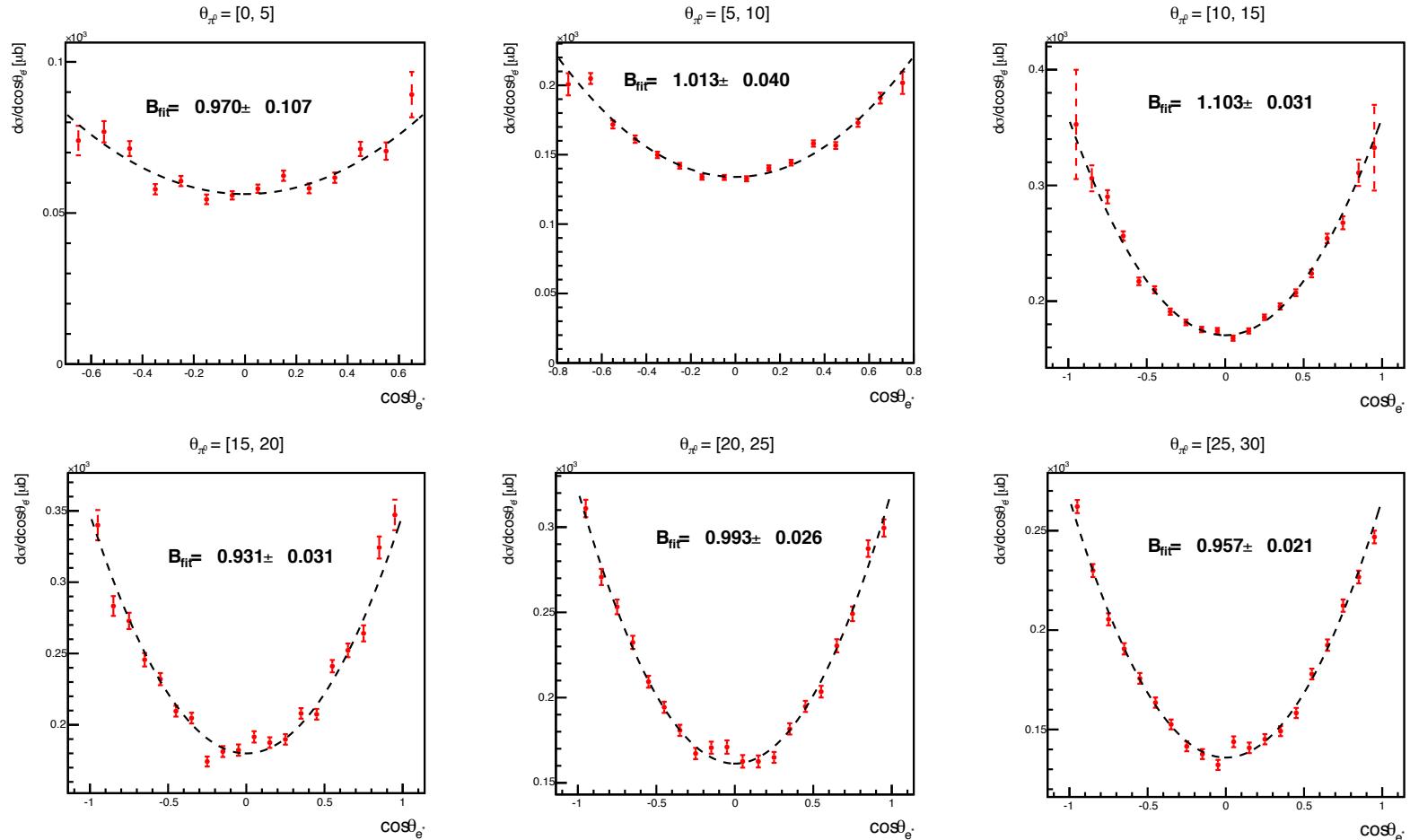
## Regge description



- The evolution of “B” as a function of t and u ( $\theta_{\pi^0}$ ) is independent of the form factors: test of the model

# Feasibility studies – Case I - $d\sigma/d\cos\theta_e^*$

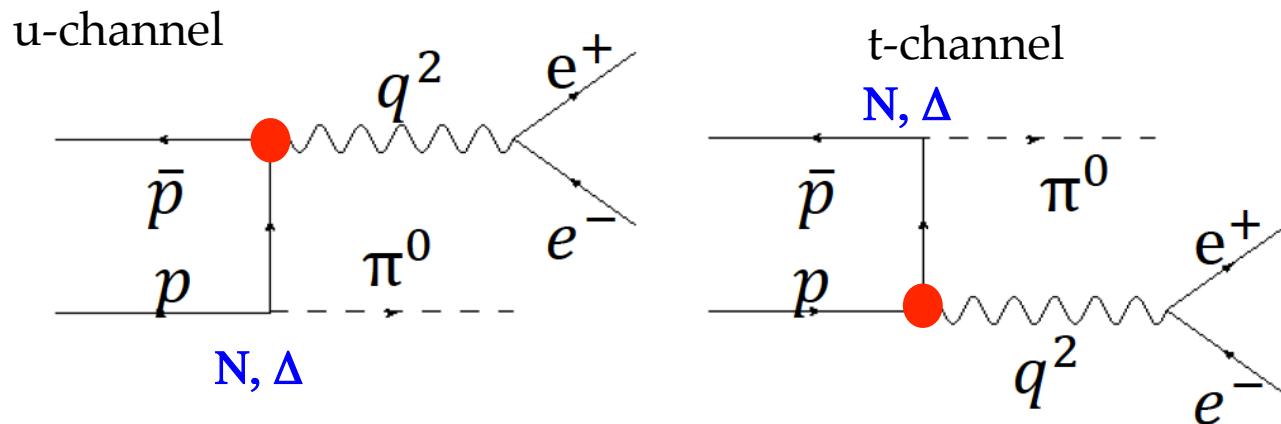
## TDA description



Possibility to scan t and u bins ( $\theta_{\pi^0}$ ) and detect any transition of production mechanism

## B. Studies within the Regge-pole frame work

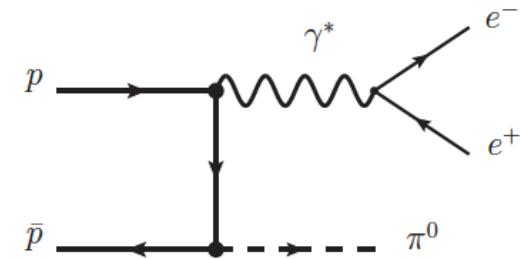
Measurements of the hadronic tensors and the proton form factors in the unphysical region



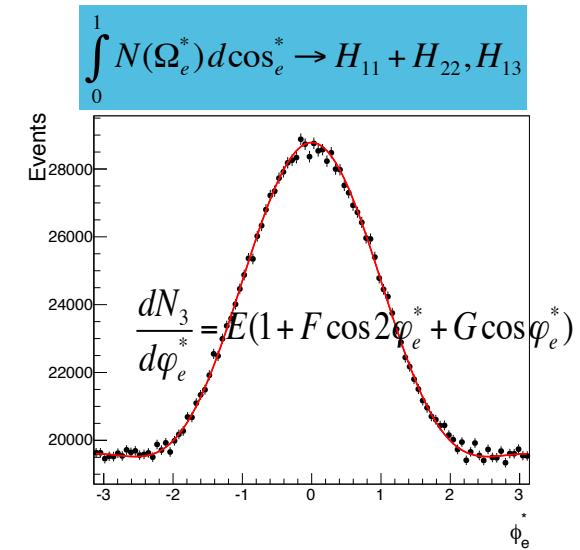
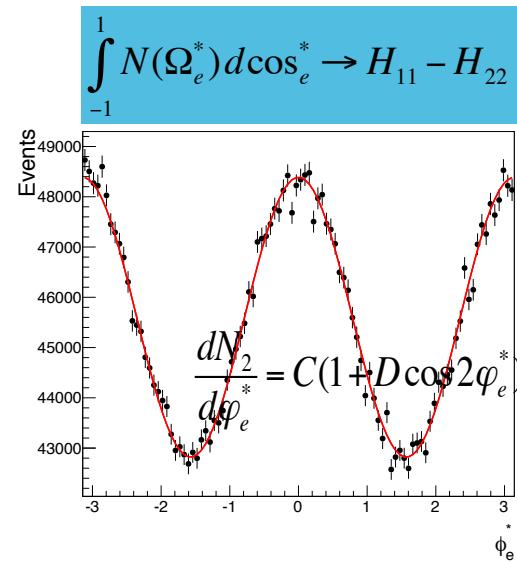
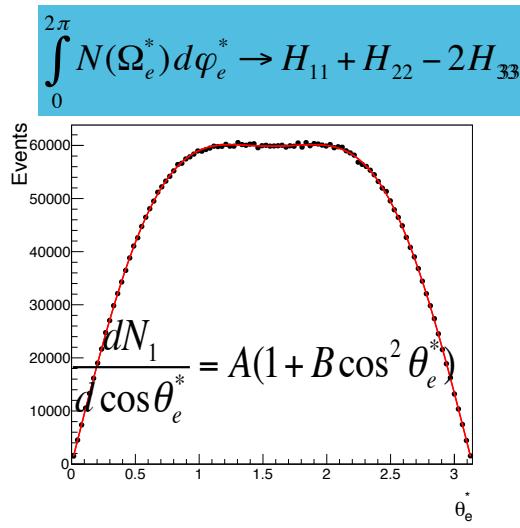
# Differential cross section and hadronic tensors

Model independent form (assuming no factorization of the process):

$$\frac{d\sigma}{dq^2 d\cos\theta_{\pi^0} d\Omega_e^*} = 4\pi e^2 q^2 (H_{11} + H_{22} + H_{33}) - 8e^2 p_e^{*2} \left( \frac{H_{11} + H_{22}}{2} \right. \\ \left. + \frac{H_{11} - H_{22}}{2} \sin^2 \theta_e^* \cos 2\varphi_e^* + 2H_{13} \sin \theta_e^* \cos \theta_e^* \cos \varphi_e^* + \frac{1}{2} (2H_{33} - H_{11} - H_{22}) \cos^2 \theta_e^* \right)$$



- In each interval of  $\theta_{\pi^0}$ , projections to obtain three 1D-distrbutions:

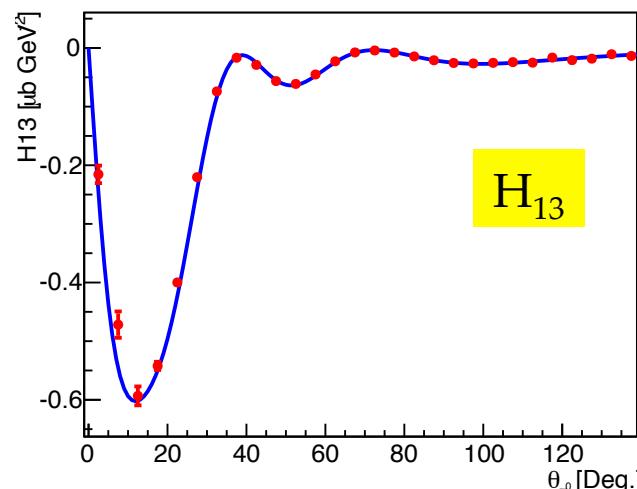
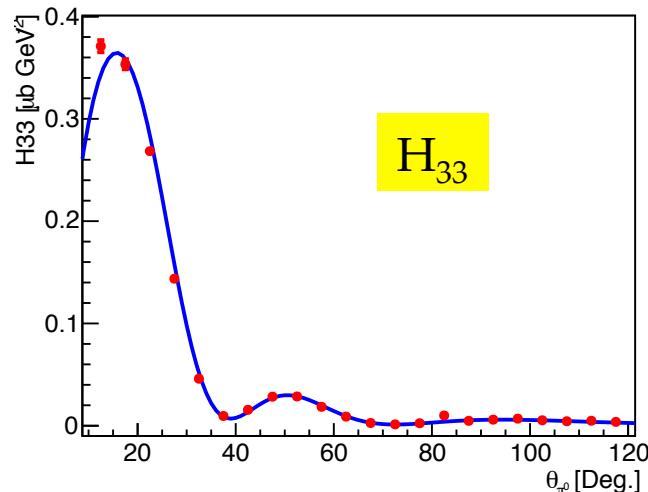
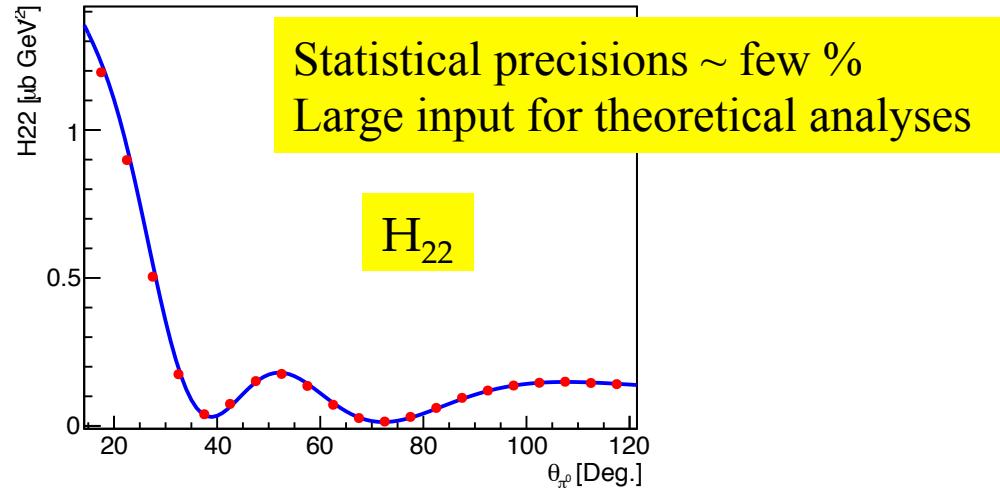
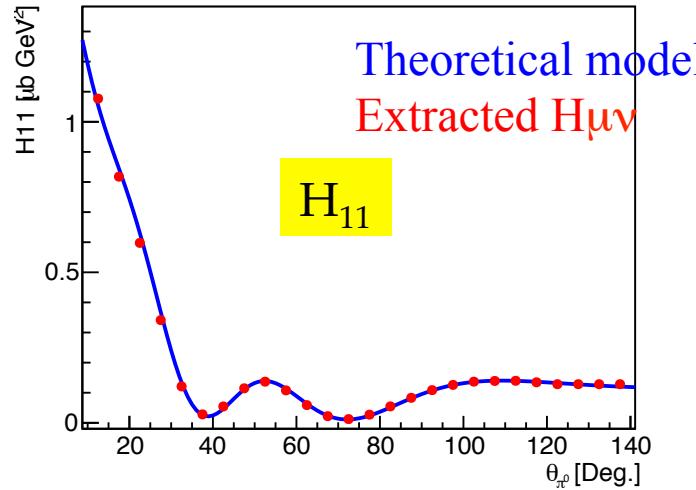


- Extract the hadronic tensors  $H_{\mu\nu}$  by fitting the three 1D-distrubtions simultaneously

# Extraction of the hadronic tensors- Case I

- $q^2 = 0.605 \pm 0.015 \text{ (GeV/c}^2)^2$ ,  $\Delta\theta_{\pi 0} = 5^\circ$ ,

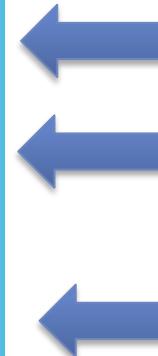
→ Direct access to  $H_{\mu\nu}$  whatever the model is

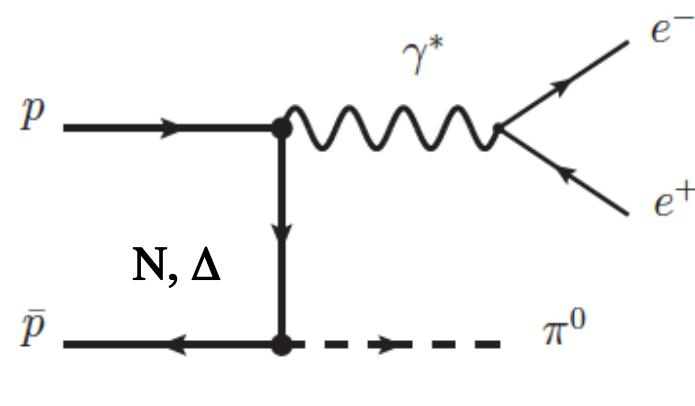


# Extraction of the proton form factors

## Model dependent calculations of the hadronic tensors

$$H_{\mu\nu} = |G_M|^2 \left[ \alpha_{\mu\nu} R^2 + \beta_{\mu\nu} + \gamma_{\mu\nu} R \cos(\phi_E - \phi_M) \right] \\ + \eta_{\mu\nu} |G_D|^2 \\ + |G_D| |G_E| \left[ \tau_{\mu\nu} \cos(\phi_E - \phi_D) + \xi_{\mu\nu} \sin(\phi_E - \phi_D) \right] \\ + |G_D| |G_M| \left[ \kappa_{\mu\nu} \cos(\phi_M - \phi_D) + \rho_{\mu\nu} \sin(\phi_M - \phi_D) \right]$$


 N-exchange  
 Δ(1232)-exchange  
 N-Δ(1232)- interference



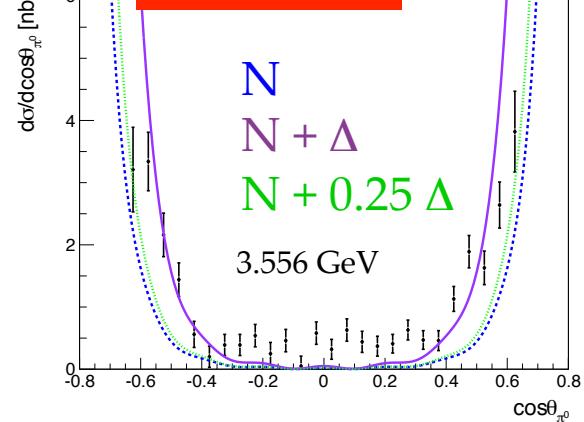
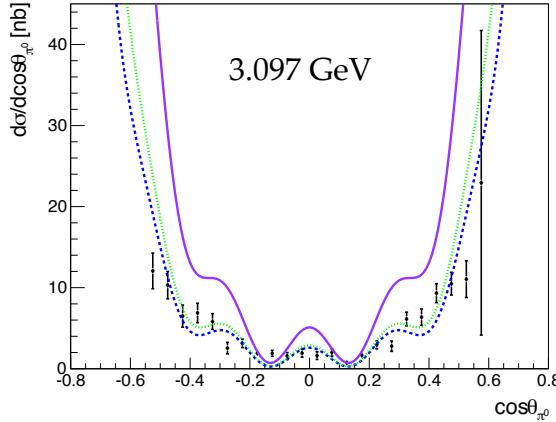
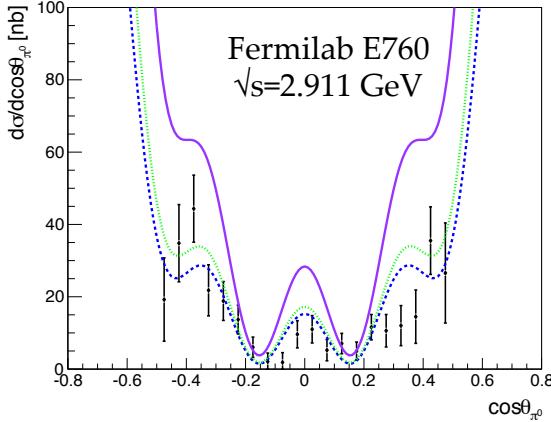
- $\alpha_{\mu\nu}, \beta_{\mu\nu}, \gamma_{\mu\nu}, \tau_{\mu\nu}, \xi_{\mu\nu}, \kappa_{\mu\nu}, \rho_{\mu\nu}, \gamma_{\mu\nu}$  depend on  $s, q^2$  and  $\theta_{\pi^0}$  and pion coupling type (pseudo-scalar or pseudo-vector)

$$V_{\pi NN} = g_{\pi NN} \left[ \gamma_5, \frac{\gamma_5 \gamma_\alpha p_\pi^\alpha}{2M} \right]$$

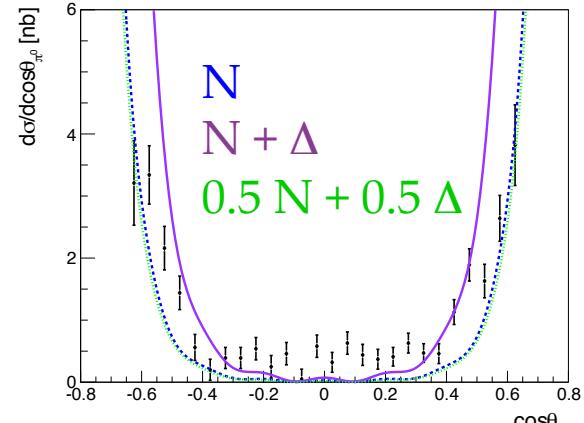
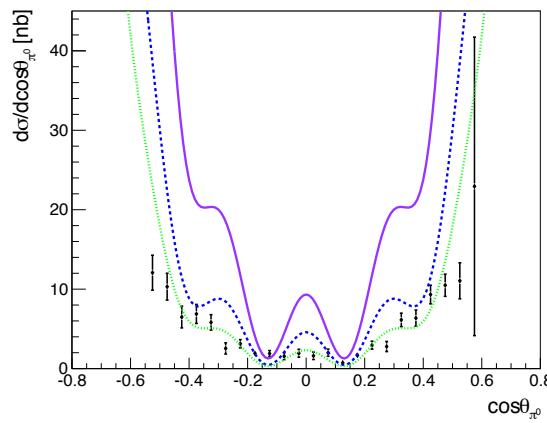
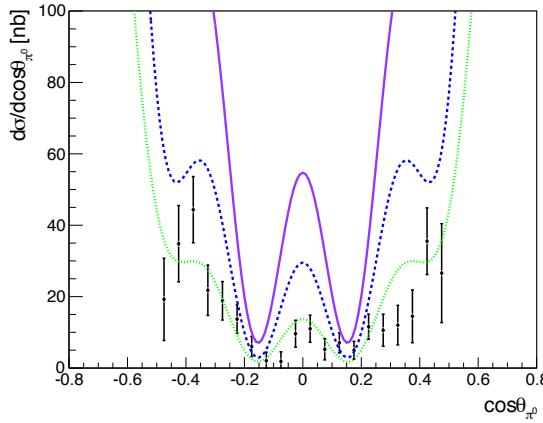
- Determination of the proton form factors requires precise knowledge of the pion coupling type and the effective contributions of the dominant baryon trajectories
  - Test of the model using  $p\bar{p} \rightarrow \pi^0\gamma$  data (no form factors)

# Differential cross section within Regge framework

- Pseudo-vector pion coupling and Regge ( $N + 0.25 \Delta$ ):



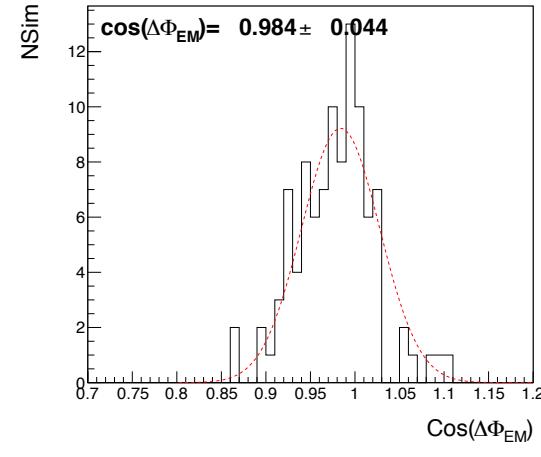
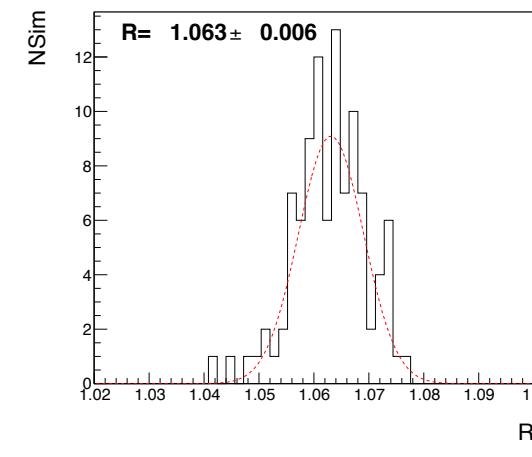
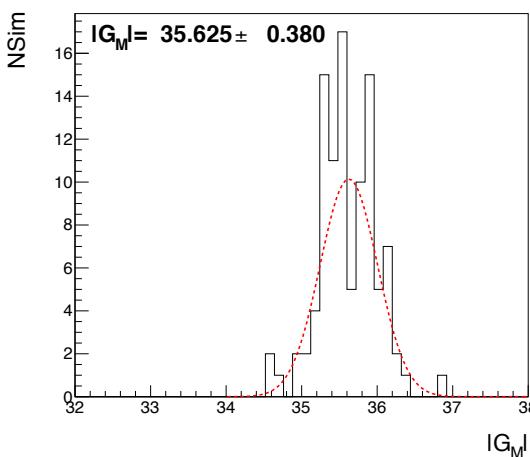
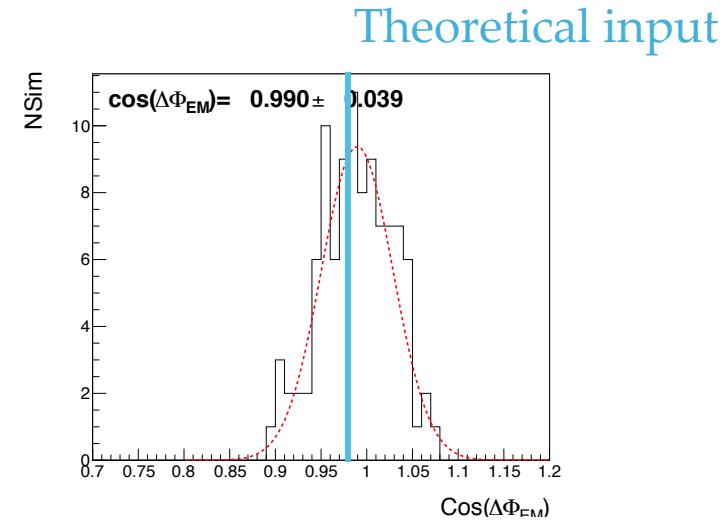
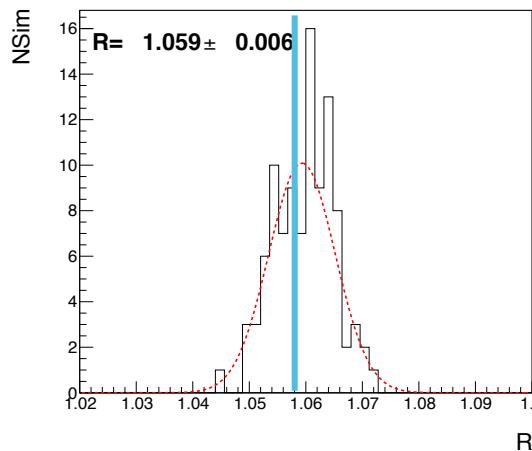
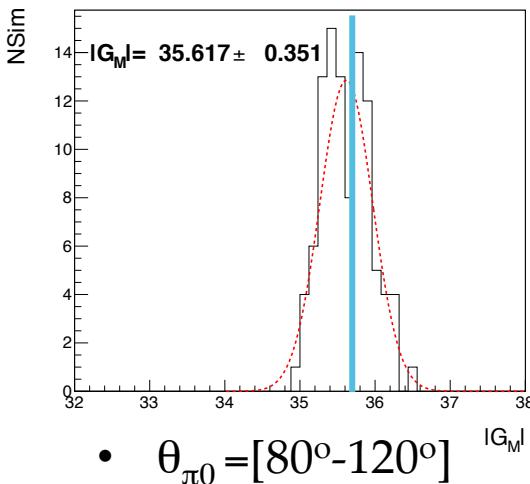
- Pseudo-scalar pion coupling and Regge ( $0.5 N + 0.5 \Delta$ ):



The  $\Delta$  is further away from the pole position than in the nucleon case, the description of the residues of the Regge poles through their on-shell couplings can be expected to be modified: **Pseudo-vector case is more probable**

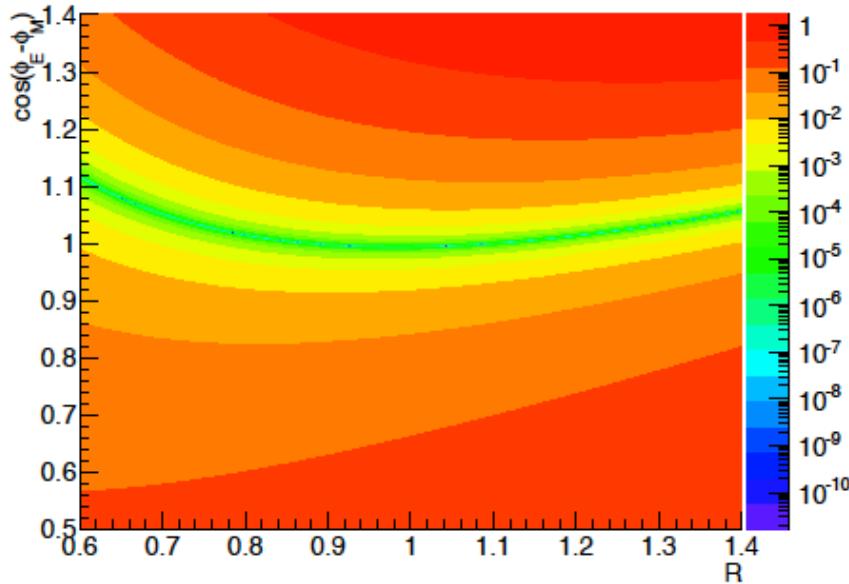
# Determination of proton form factors – Case I

- Form factors are determined by minimizing the  $H_{\mu\nu}$
- Data are generated using complete Regge model (N and Delta), PV pion coupling
- Fit model for  $H_{\mu\nu}$  based only on N exchange
  - $\theta_{\pi 0} = [10^\circ - 30^\circ]$



# Determination of proton form factors – Case I

- Form factors are determined by minimizing the  $H_{\mu\nu}$
- Data are generated using complete Regge model (N and Delta), PS pion coupling
- Fit model for  $H_{\mu\nu}$  based only on N exchange

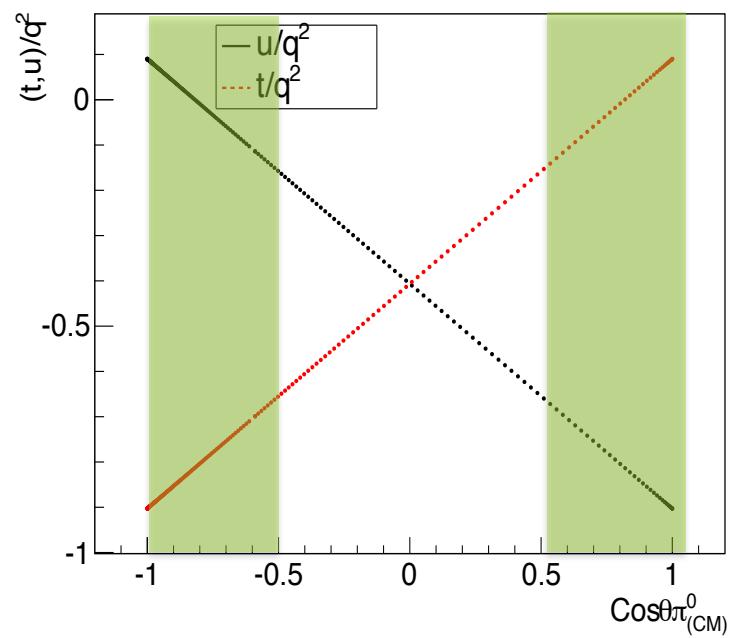
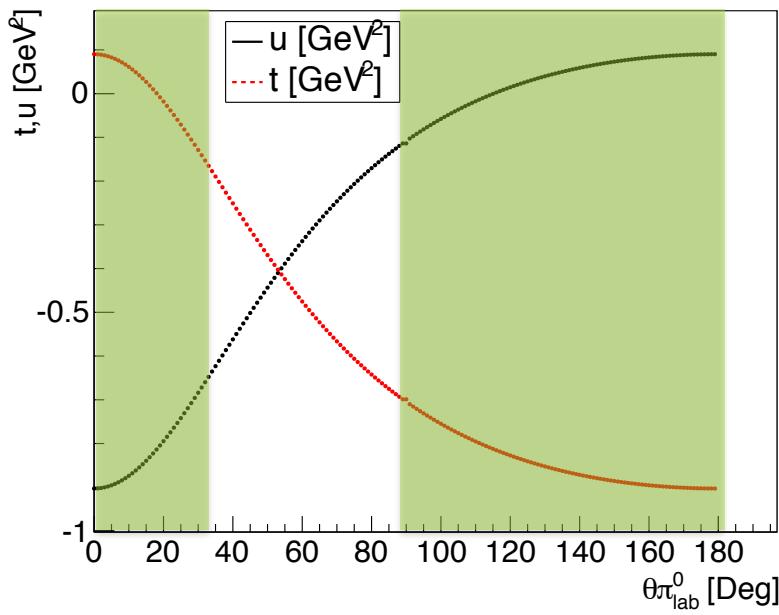


- Many solutions for the minimization function
- Ratio and relative phase can not be separated

- $|G_M|$  can be precisely measured ( $\sim 1\%$ )
- Ratio can be measured based on a assumption of the relative phase
- Upper and lower limits of the ratio and the relative phase can be determined; in the present case:  $0.98 < \cos(\Phi_{EM}) < 1$  and  $0.8 < R < 1.3$

## Feasibility studies – Case II

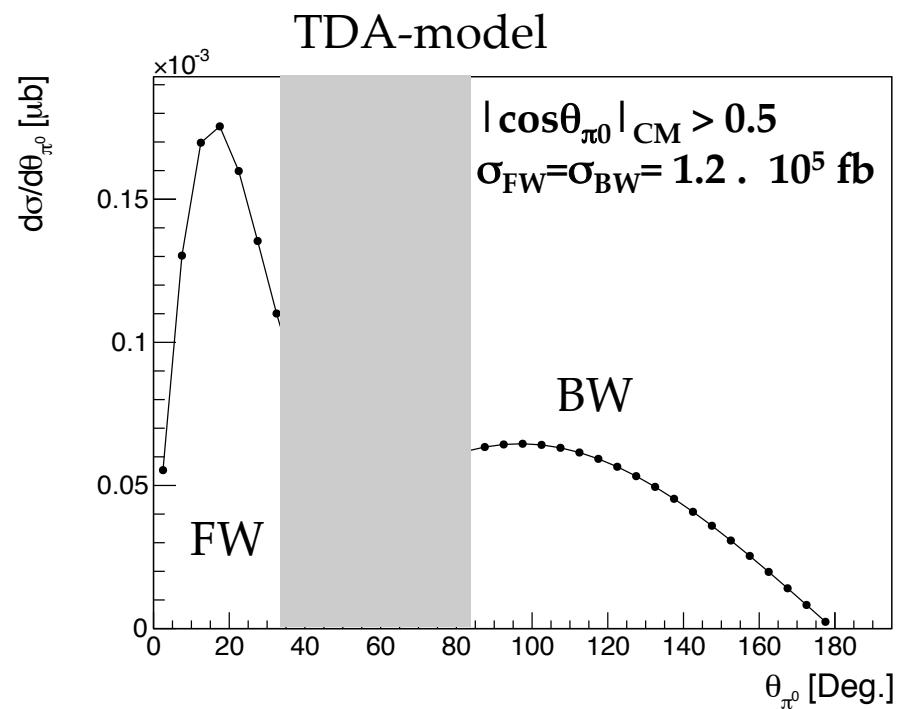
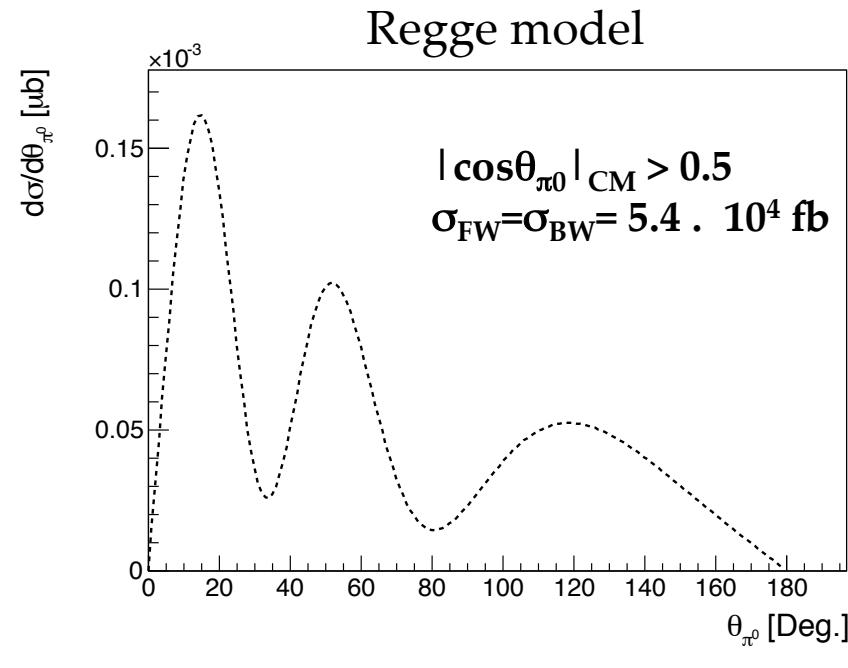
- $P_{\text{lab}} = 1.7 \text{ GeV}/c$  ( $s=5.4 \text{ GeV}^2$ );  $q^2 = 2 \pm 0.125 (\text{GeV}/c^2)^2$
- Regge description expected for  $|\cos\theta_{\pi^0}|_{\text{CM}} > 0.5 \text{ && } |t,u|/q^2 > 20\%$
- TDAs description expected for  $|\cos\theta_{\pi^0}|_{\text{CM}} > 0.5 \text{ && } |t,u|/q^2 < 20\%$   
 $\theta_{\pi^0}(\text{Lab}) = [0^\circ - 32^\circ], [83^\circ - 180^\circ]$



- At small  $s$  and  $q^2 \sim 2 (\text{GeV}/c^2)^2$  the process is expected to occur through the collinear factorization description
  - Region for TDA studies**

# Theoretical cross sections – Case II

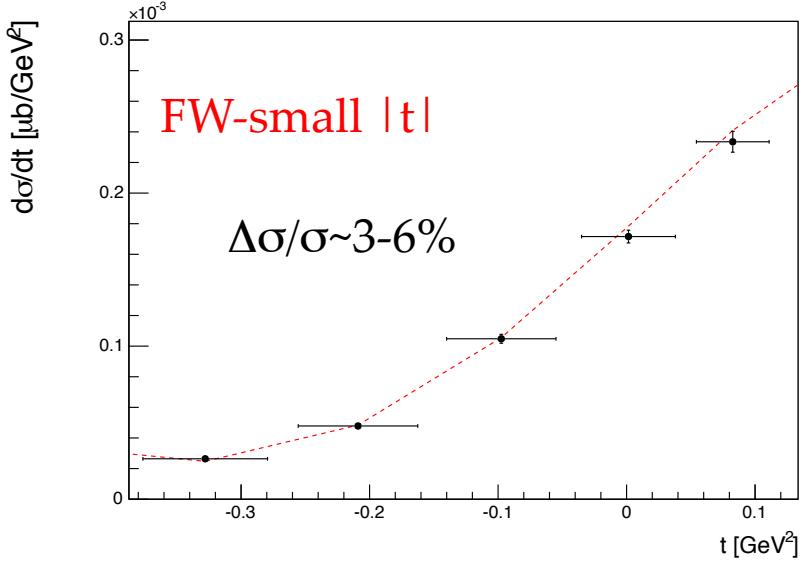
- $P_{\text{lab}} = 1.7 \text{ GeV}/c$  ( $s=5.4 \text{ GeV}^2$ );  $q^2 = 2 \pm 0.125 (\text{GeV}/c^2)^2$



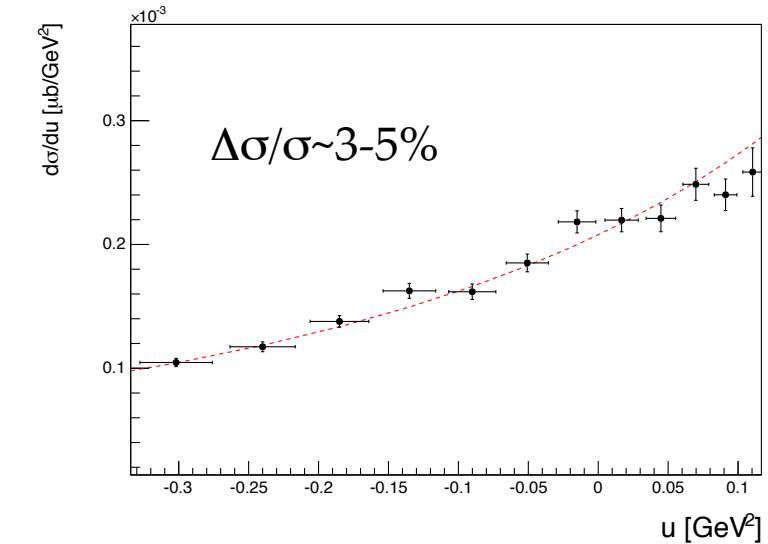
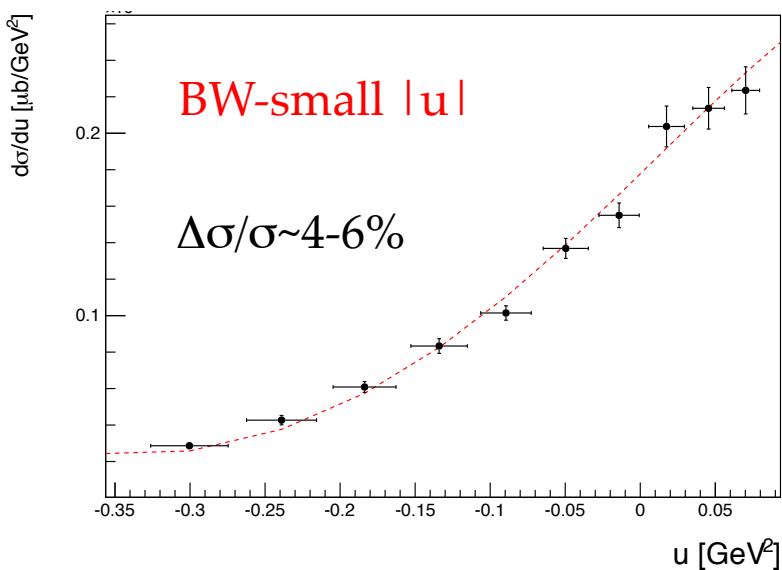
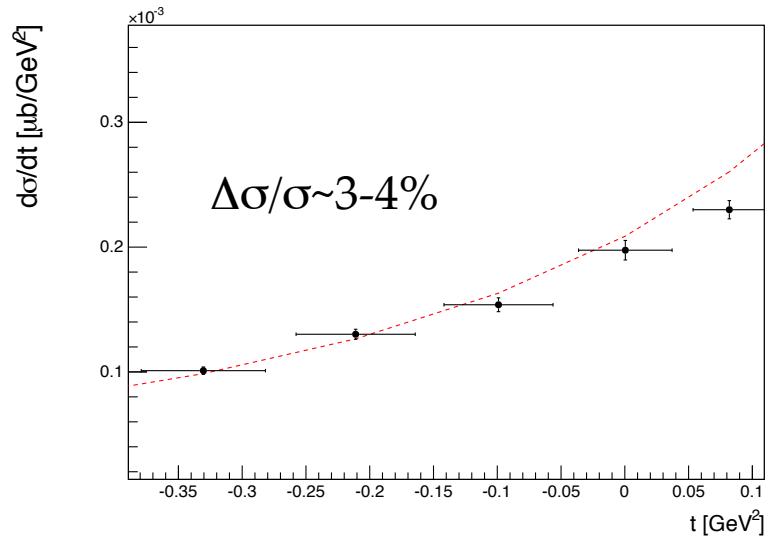
- Smaller cross section than **case I** due to the form factors
- Smaller cross section than **case I** due to the scaling characteristic of the cross section in  $q^2$

# Feasibility studies – Case II - $d\sigma/dt$ , $d\sigma/du$

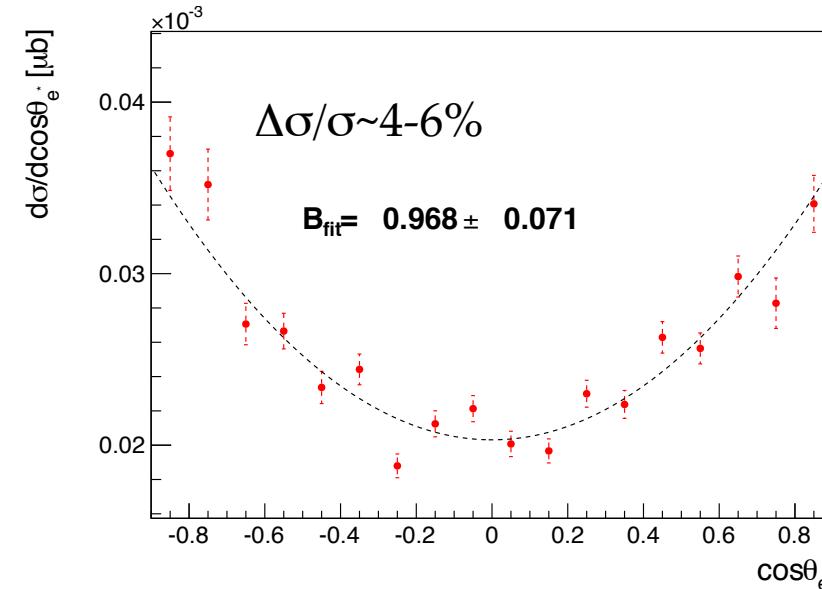
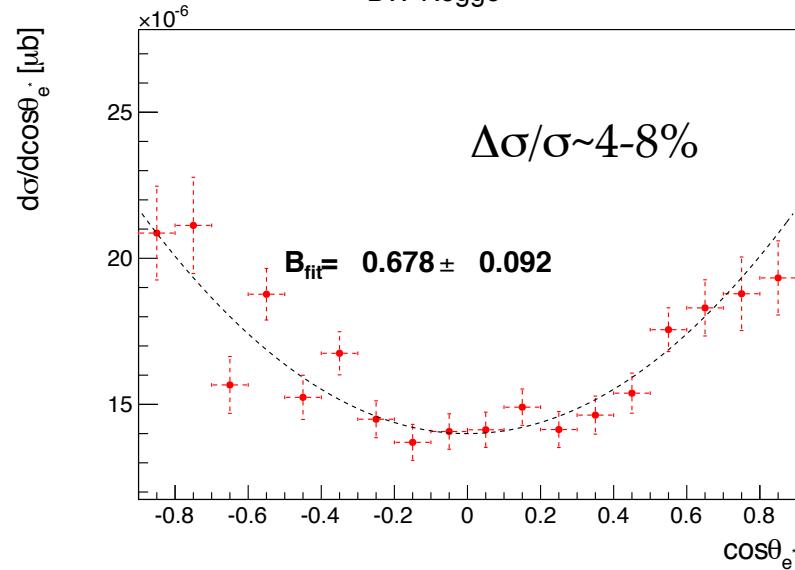
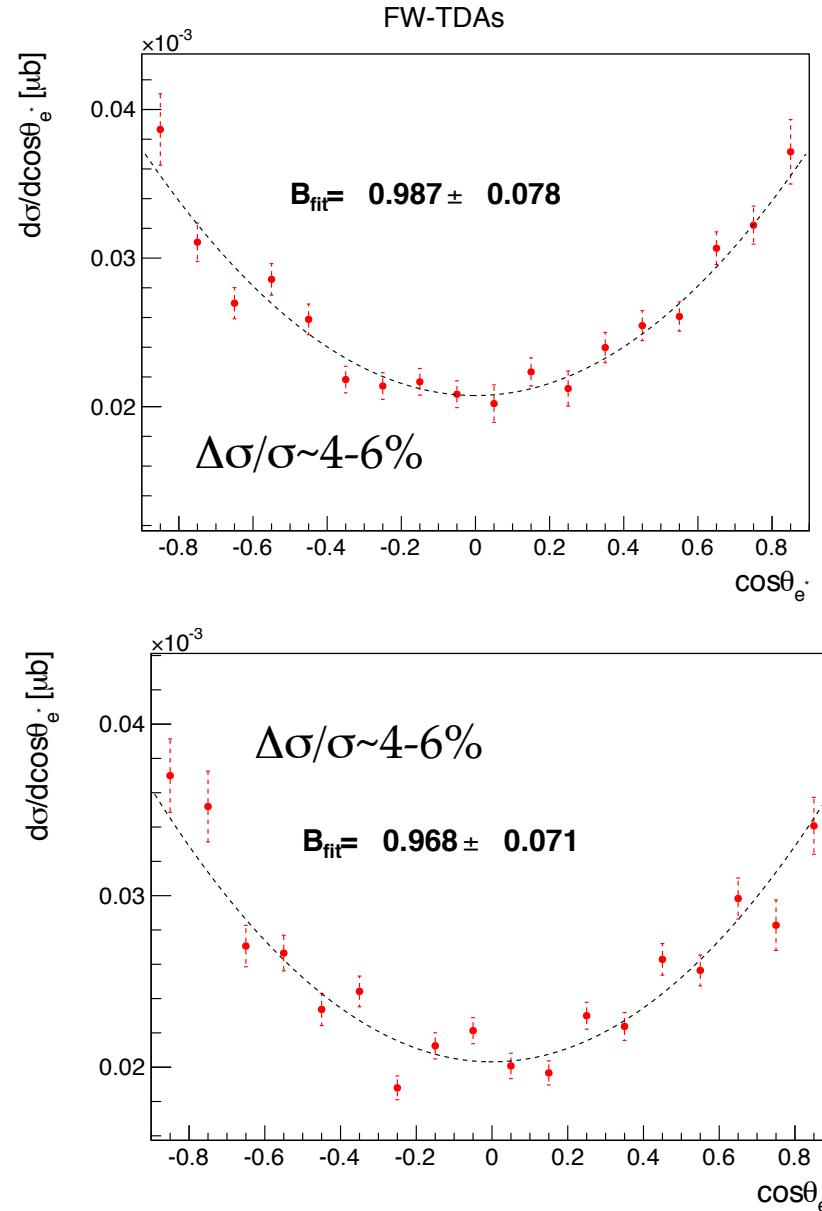
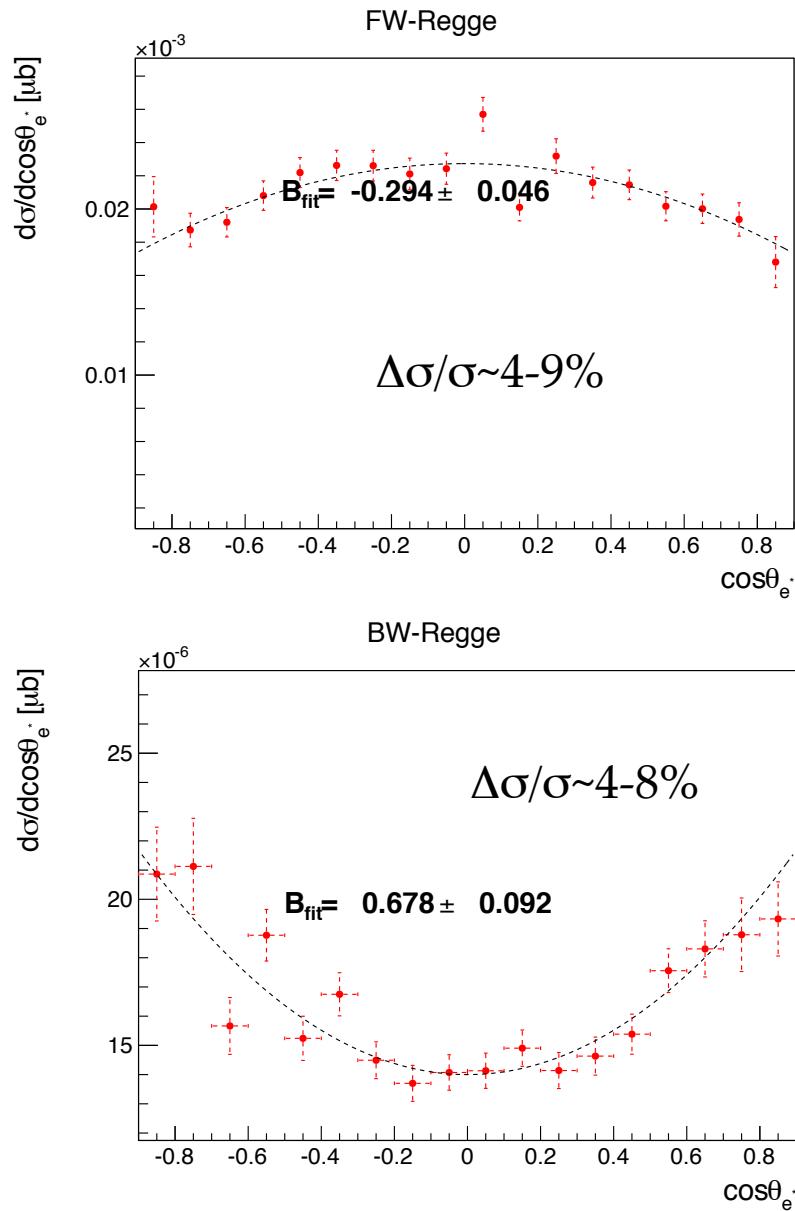
## Regge description



## TDA-model

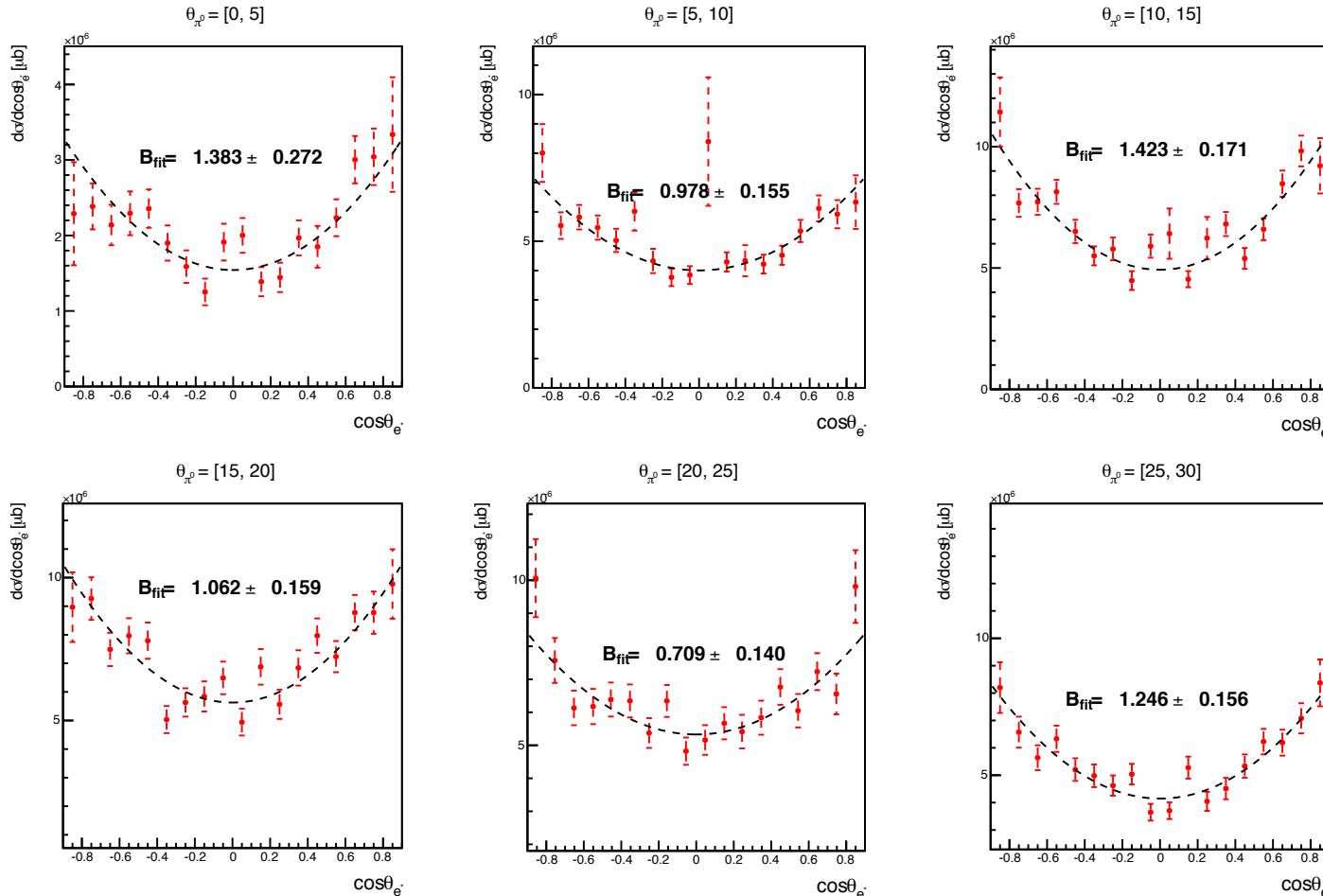


# Feasibility studies – Case II - $d\sigma/d\cos\theta_e^*$



# Feasibility studies – Case II - $d\sigma/d\cos\theta_e^*$

## TDA description



- Possibility to scan t and u bins ( $\theta_{\pi^0}$ ) and detect any transition of the production mechanism

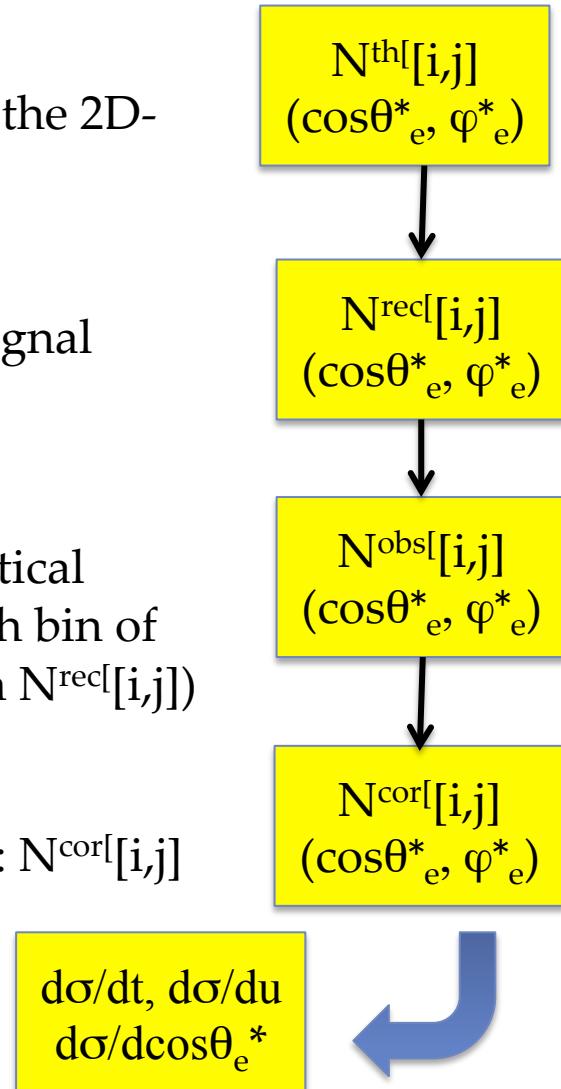
# Summary

- First experimental indications of the TDA factorization was recently observed in backward p-and backward  $\omega$ - electroproduction at Jlab: more statistics are needed for confirmation
- TDA model can be studied at PANDA in proton-anitproton annihilation into  $e^+e^- \pi 0$  final state (in collinear factorization regime): test of the TDA universality
- The same process can be used to perform first measurements of the proton time-like form factors in the unphysical region (outside the collinear factorization regime).
- Feasibility measurements of this process have been performed using two models: Regge pole description and TDA-factorization at low  $q^2$  values ( $0.605$  and  $2 (\text{GeV}/c^2)^2$ )
- Precise measurements of the differential cross sections are feasible at PANDA
- Valuable information on the proton form factors can be extracted
  - Simulations using dedicated event generators (for low statistics and non full acceptance regions)
  - Simulations with new PANDAROOT version and also at higher center of mass energies

# Measurements of the differential cross sections

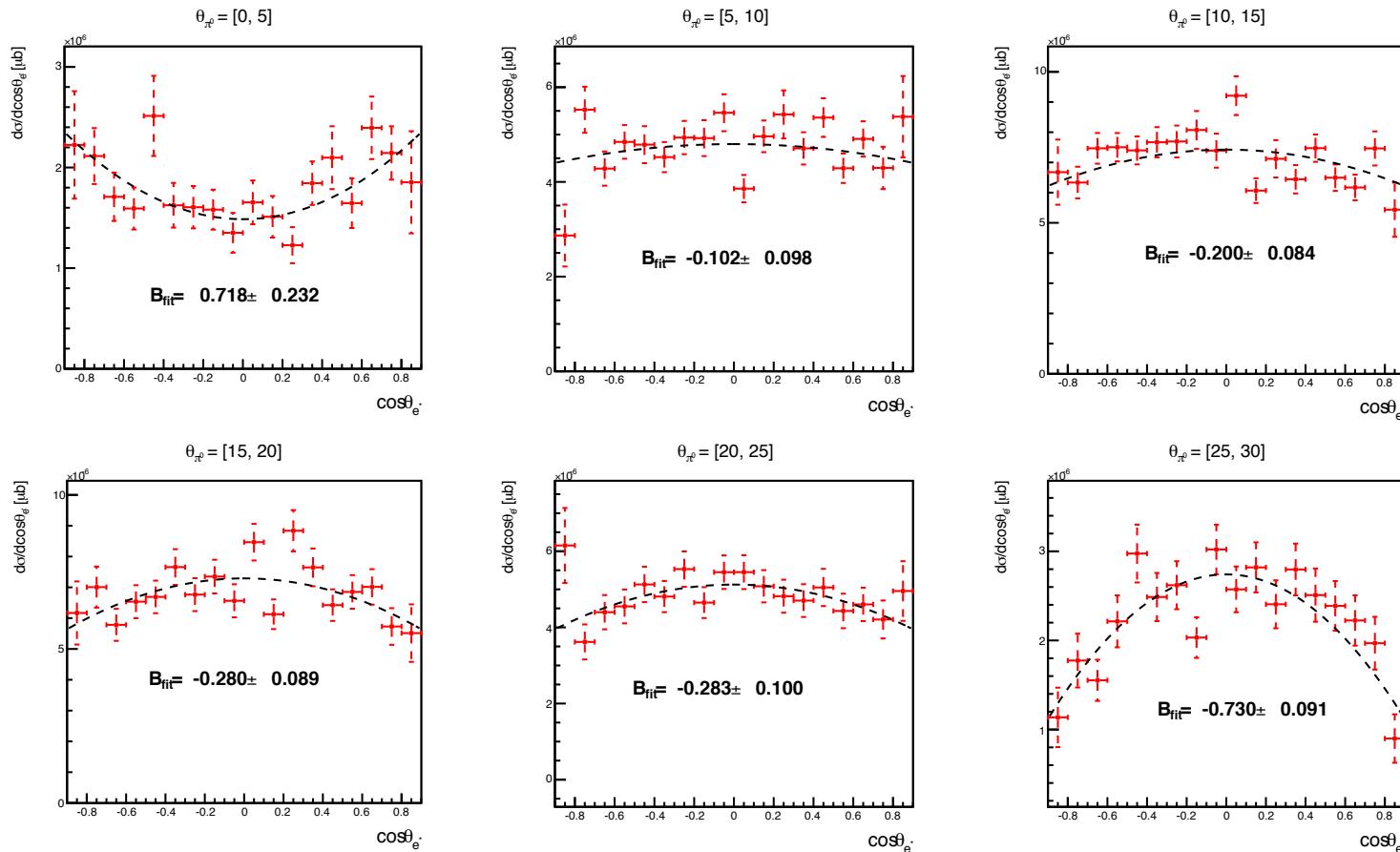
For each interval of  $q^2$  and  $\theta_{\pi0}$ :

- Theoretical number of counts  $N^{th}[i,j]$  in each bin of the 2D-distribution  $(\cos\theta_e^*, \varphi_e^*)$
- Reconstructed events  $N^{rec}[i,j]$  taking into account signal efficiency
- Observed events  $N^{obs}[i,j]$  taking into account statistical fluctuations by generating a random number in each bin of the 2D-distribution (Poisson distribution with mean  $N^{rec}[i,j]$ )
- Correct the observed events by the signal efficiency:  $N^{cor}[i,j]$
- Projections to obtain 1D-distributions



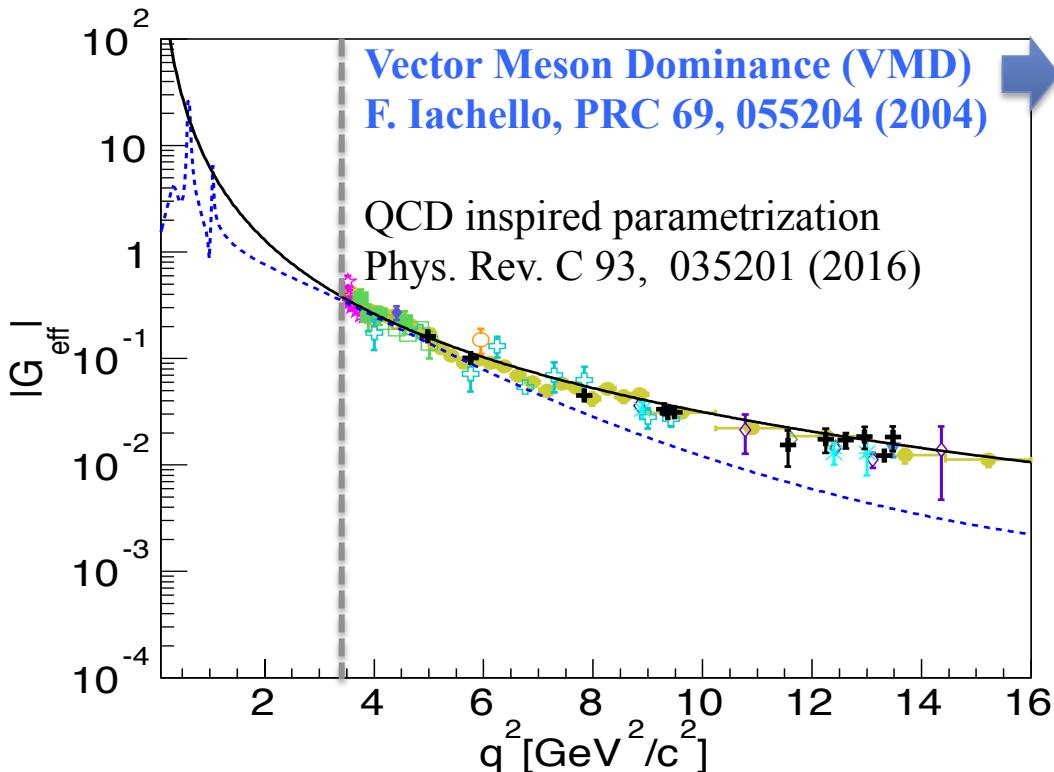
# Feasibility studies – Case II - $d\sigma/d\cos\theta_e^*$

## Regge description



- Possibility to scan t and u bins ( $\theta_{\pi 0}$ ) and detect any transition of production mechanism

# Proton and Delta(1232) form factor model



Photon couples to the nucleon through the exchange of intermediate vector mesons ( $\omega, \varphi, \rho, \dots$ ) :

$$F(q^2) \sim g(q^2) \left[ \sum_v A_v \frac{M_v^2}{q^2 - M_v^2} \right]$$

The magnetic dipole form factor of the  $N \rightarrow \Delta$  transition

$$G_D(q^2) = \frac{G_D(0)}{\kappa_V} (F_2^p(q^2) - F_2^n(q^2))$$

$$q^2 = 0.605 \pm 0.005 \text{ (GeV/c}^2\text{)}^2$$

$$|G_E| = 35.72, |G_M| = 35.56$$

$$R = 1.066, \cos(\phi_E - \phi_M) = 0.998 \text{ (4°)}$$

$$|G_D| = 3.8$$

$$q^2 = 2 \pm 0.125 \text{ (GeV/c}^2\text{)}^2$$

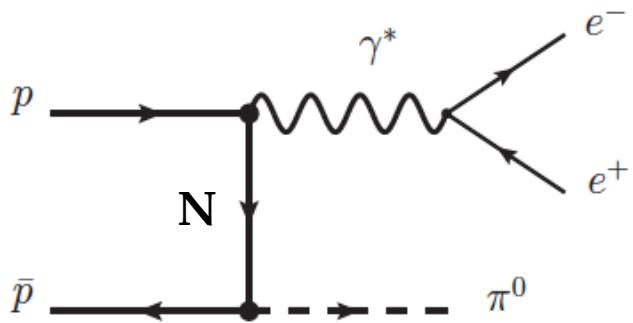
$$|G_E| = 0.67, |G_M| = 0.84$$

$$R = 0.802, \cos(\phi_E - \phi_M) = 0.999 \text{ (3°)}$$

$$|G_D| = 0.74$$

# Differential cross section within Regge framework

J. Guttman, M. Vanderhaeghen /  
PLB 719 (2013) 136–142



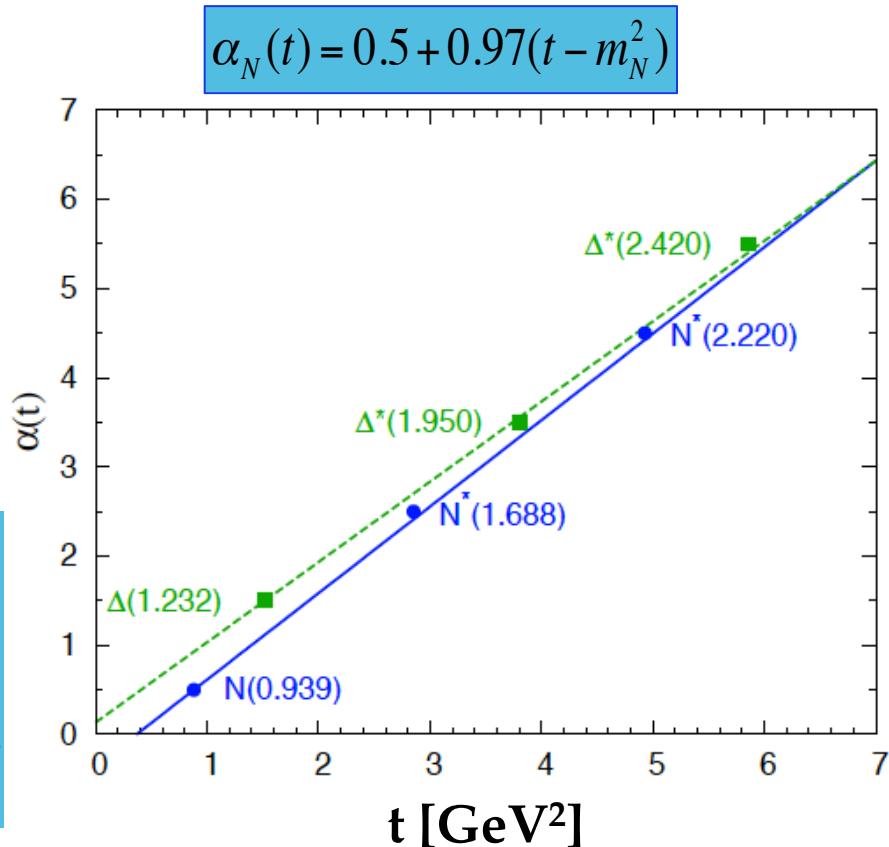
- Modification of the exchanged nucleon propagator:

$$t\text{-channel: } \frac{1}{t - m_N^2} \rightarrow$$

$$D_N^{\text{Regge}}(t, s) = \frac{s^{\alpha_N(t)-0.5}}{\Gamma[\alpha_N(t)+0.5]} \pi \alpha_N \frac{e^{-i\pi(\alpha_N(t)+0.5)}}{\sin[\pi(\alpha_N(t)+0.5)]}$$

- $\Gamma_\mu$  remain unchanged - no additional unknown parameters are introduced

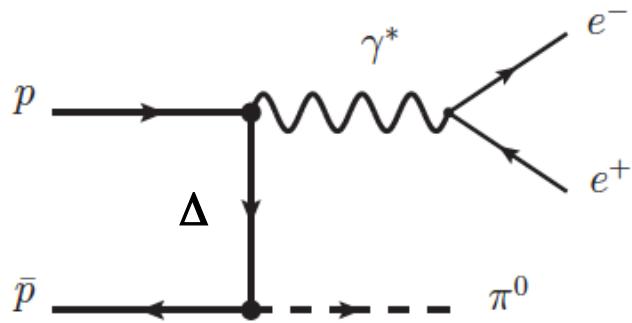
Regge trajectory for the nucleon



$$\Gamma_\mu(q) = e \left[ F_1(q^2) \gamma_\mu - \frac{i}{2M} F_2(q^2) \sigma_{\mu\nu} q^\nu \right]$$

# Differential cross section within Regge framework

J. Guttman, M. Vanderhaeghen /  
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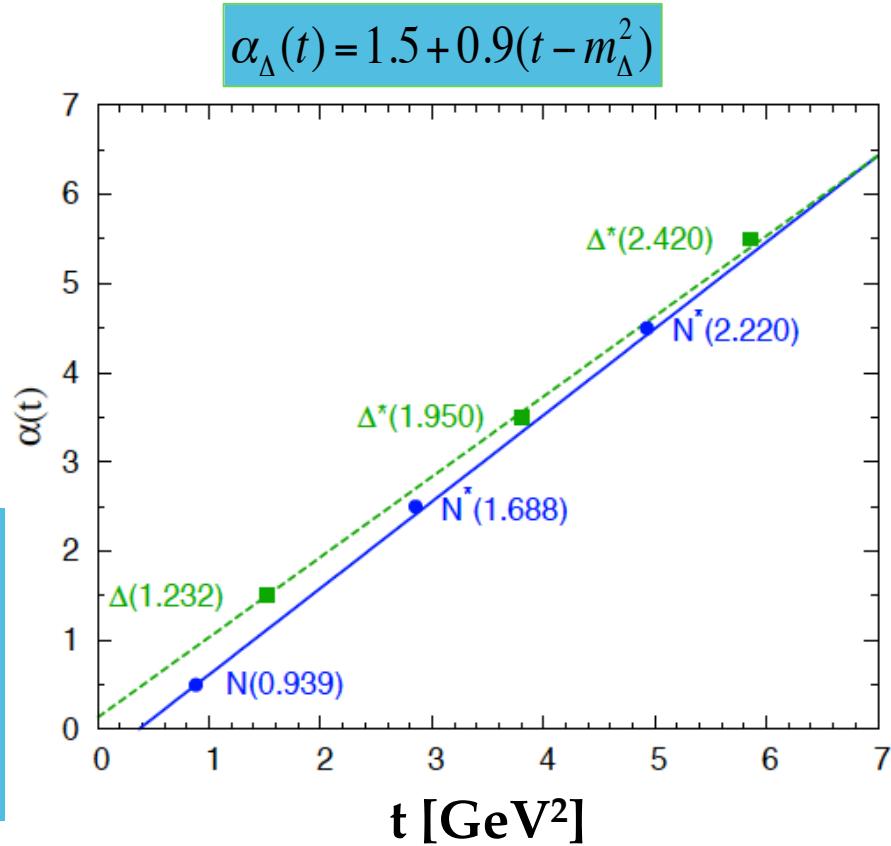
- Modification of the exchanged  $\Delta(1232)$  propagator:

$$t\text{-channel: } \frac{1}{t - m_\Delta^2} \rightarrow$$

$$D_\Delta^{\text{Regge}}(t, s) = \frac{s^{\alpha_\Delta(t)-1.5}}{\Gamma[\alpha_\Delta(t)+0.5]} \pi \alpha_\Delta \frac{e^{-i\pi(\alpha_\Delta(t)-0.5)}}{\sin[\pi(\alpha_\Delta(t)-0.5)]}$$

- $\Gamma_{\gamma N \Delta}$  introduces the magnetic dipole form factor  $G_D$

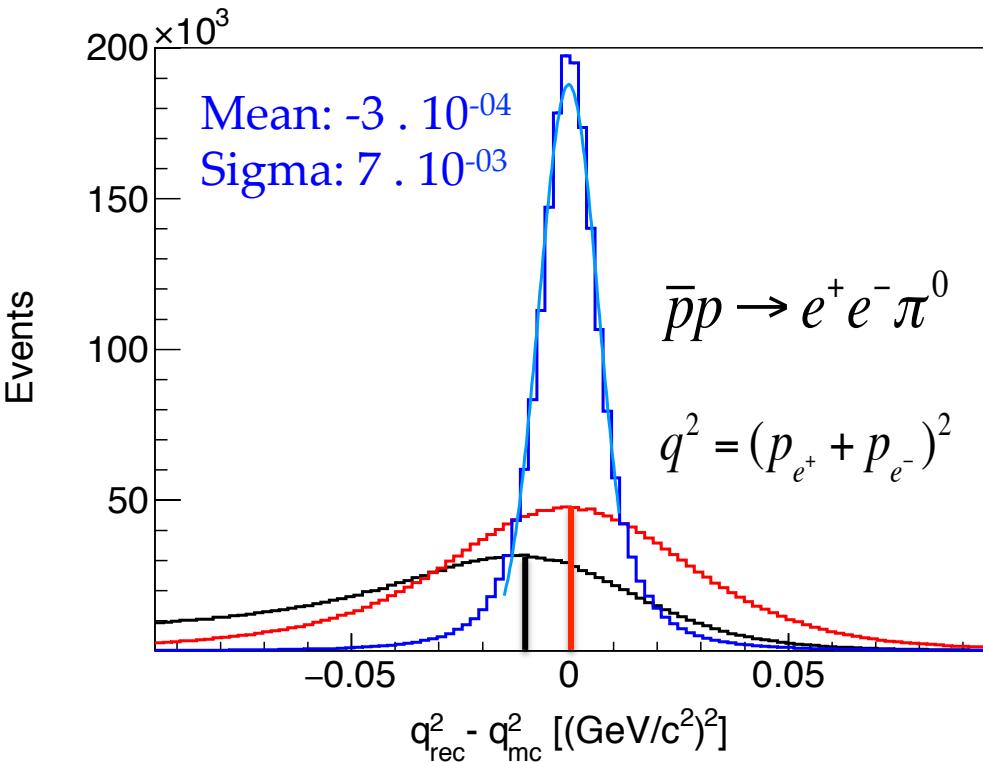
Regge trajectory for the nucleon



$$\Gamma_{\gamma N \Delta}^\alpha = i \sqrt{\frac{2}{3}} \frac{3e(m_\Delta + m_N)}{2m_N((m_\Delta + m_N)^2 - q^2)} G_D(q^2) \epsilon^{\alpha\mu\rho\sigma} p_\Delta q_\sigma$$

# Invariant mass squared of the selected $e^+e^-$

- $q^2 = 0.605 \pm 0.015 \text{ (GeV/c}^2\text{)}^2$



"Before Bremsstrahlung correction,  
without 4C kinematic fit"

"After Bremsstrahlung correction  
without 4C kinematic fit"

(Methode described in:  
E. ATOMSSA TN-STT-2015-001)

"After Bremsstrahlung correction  
with 4C kinematic fit"

**Measurement of the proton FFs in small intervals of  $q^2$  (in the unphysical region) is possible at PANDA**