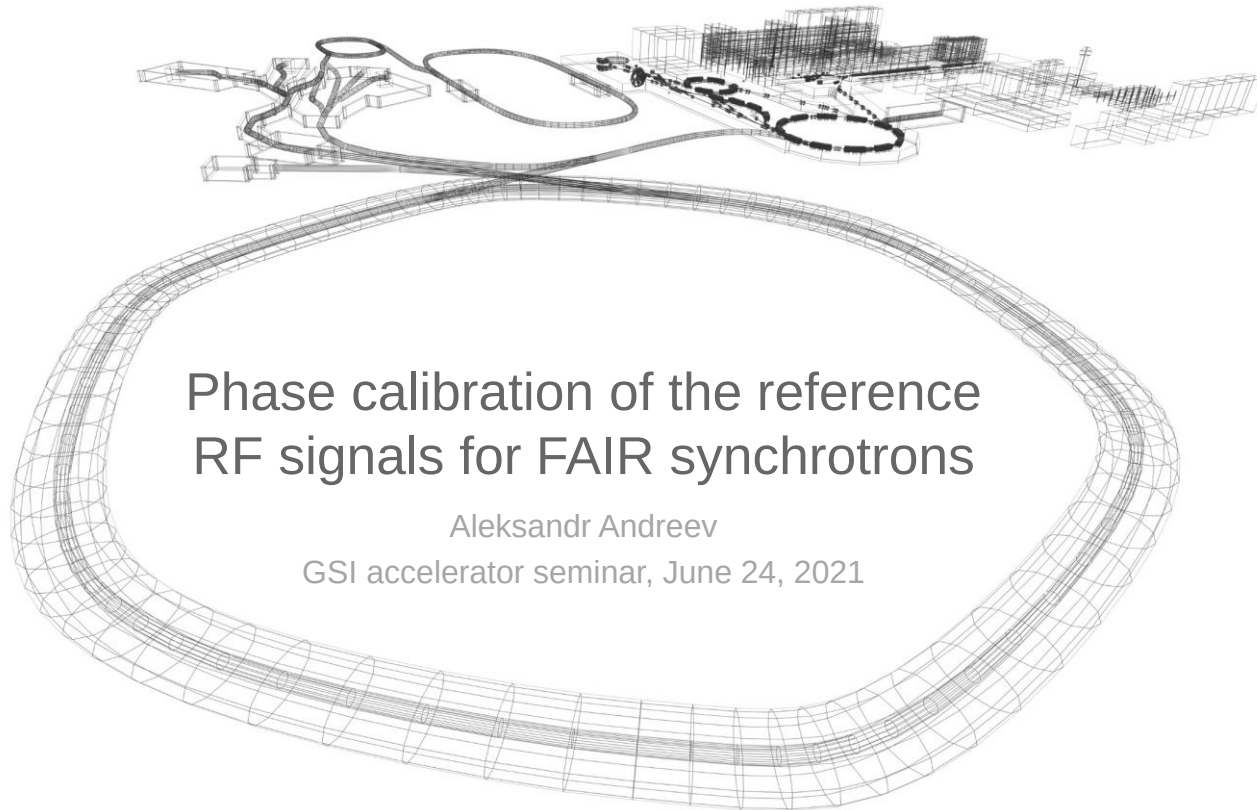




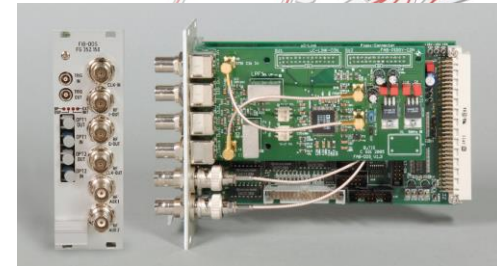
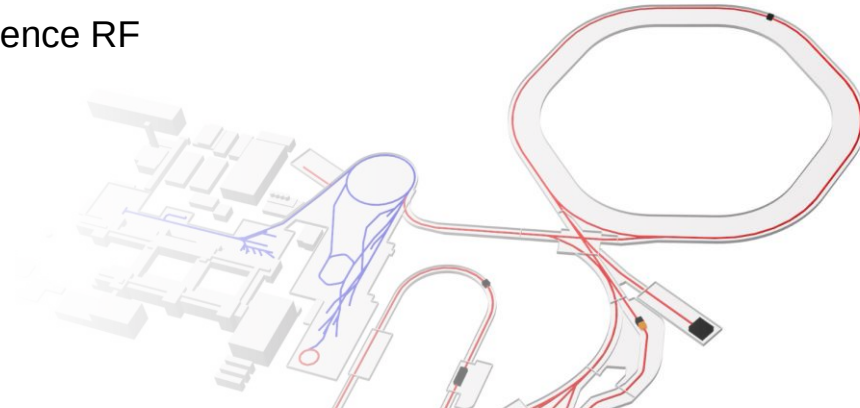
# Phase calibration of the reference RF signals for FAIR synchrotrons

Aleksandr Andreev

GSI accelerator seminar, June 24, 2021

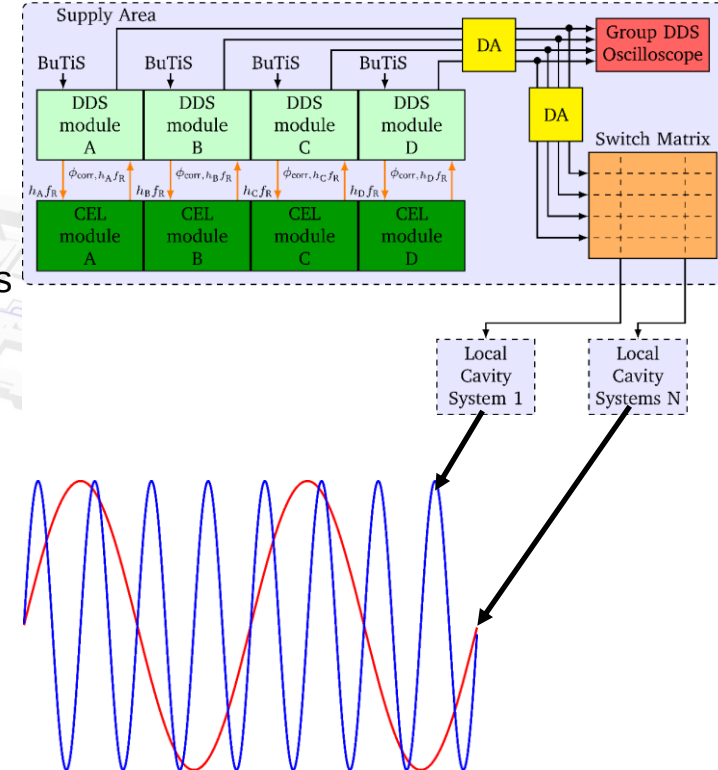
- Introduction and description of the problem
- Requirements for the calibration procedure
- Description of the developed method
- Convergence study and numerical optimization
- Uncertainty analysis of the method
- Application at SIS18 supply area
- Stability and environmental influences analysis

- Large circumference of the SIS100 and reference RF signals
- 8 RF supply areas distributed along the ring
- Direct Digital Synthesis (DDS) modules generate reference RF signals



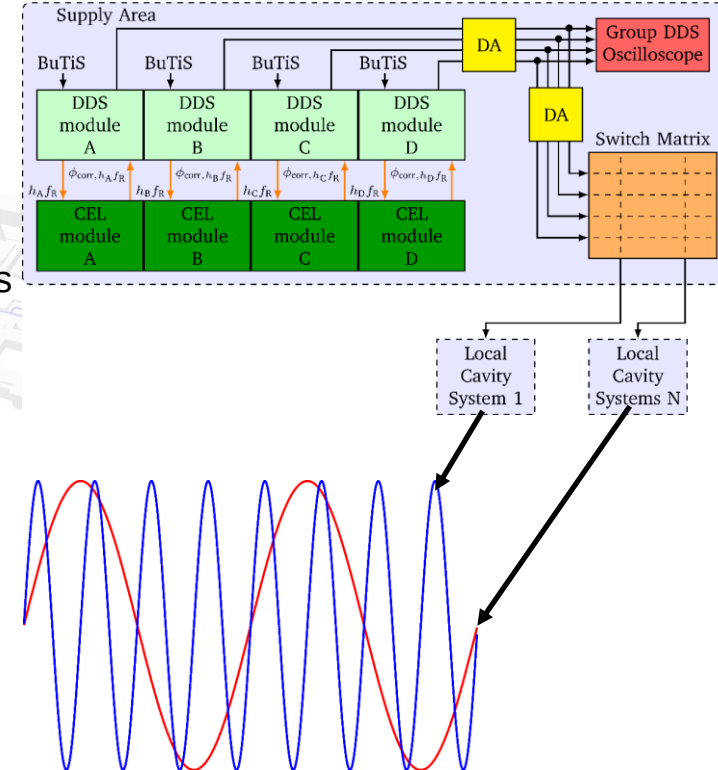
# Introduction II

- Large circumference of the SIS100 and reference RF signals
- 8 RF supply areas distributed along the ring
- Direct Digital Synthesis (DDS) modules generate reference RF signals
- 4 DDS modules mounted in one crate: multiharmonic operations
- Time synchronization: Bunch Phase Timing System (BuTiS)
- Revolution frequency ramp: Central Control System (CCS)
- Switch Matrix routes Group DDS signals to local cavity systems



# Introduction III

- Large circumference of the SIS100 and reference RF signals
- 8 RF supply areas distributed along the ring
- Direct Digital Synthesis (DDS) modules generate reference RF signals
- 4 DDS modules mounted in one crate: multiharmonic operations
- Time synchronization: Bunch Phase Timing System (BuTiS)
- Revolution frequency ramp: Central Control System (CCS)
- Switch Matrix routes Group DDS signals to local cavity systems
- Output stage: undesired phase deviations → reference signals → local cavity systems
- Calibration needed to reach the desired beam quality requirements



- Phase accuracy of the reference RF signals better than  $\pm 1^\circ$
- A method has to:
  - Reduce number of possible combinations
  - Calibrate of all the modules in the same way
  - Calibrate independent of harmonic number in operation
- Calibration during maintenance periods
- Long term stability: decrease time for maintenance
- Automatic system integrated into the existing control environment

→ Absolute phase calibration method based on sine wave fitting algorithms

- Advantages: high accuracy, robustness for noncoherent sampling, simplicity of implementation
- Sampled signal: a sequence of samples  $y_n$  taken at time instants  $t_n, n \in [1, \dots, N]$
- A set of unknown parameters  $\mathbf{x} = (\tilde{V}, \phi, C, \omega)^T$  characterizes its waveform

$$v(t_n) = A \cos(\omega t_n) + B \sin(\omega t_n) + C$$

where  $A = \tilde{V} \sin \phi$ ,  $B = \tilde{V} \cos \phi$  and  $\phi = \text{atan2}(A, B)$

- Including higher harmonics:

$$\begin{aligned} v(t_n) &= C + \sum_{h=1}^{h_{\text{fit max}}} \tilde{V}_h \sin(h\omega t_n + \phi_h) \\ &= C + \sum_{h=1}^{h_{\text{fit max}}} (A_h \cos(h\omega t_n) + B_h \sin(h\omega t_n)) \end{aligned}$$

- Estimate the unknown parameters  $\hat{\mathbf{x}}$  that minimize

$$\sum_{n=1}^N (y_n - v(t_n))^2$$

- Phase of harmonic  $h$ :

$$\phi_{h,f} = \text{atan2}(A_h, B_h)$$

- Parameters of  $h_{\text{fit max}}$  harmonics can be estimated
- Phase of the fundamental component  $\phi_{1,f}$  is relevant
- Three- and four parameter algorithm for known and unknown frequency, respectively



# Calculation of the phase correction

- BuTiS  $T_0$  signal as a reference
- For ideal (i.e. no phase deviations) signal:

$$\phi_f - \phi_{\text{init}} = 2\pi f_{\text{DDS RF}} (N_{\text{ref}} T_{\text{ref}} - \tau_\delta)$$

- Real signal with  $\phi_{e,f}$ :

$$\phi_{\text{meas},f} - \phi_{\text{init}} = 2\pi f_{\text{DDS RF}} (N_{\text{ref}} T_{\text{ref}} - \tau_\delta) + \phi_{e,f}$$

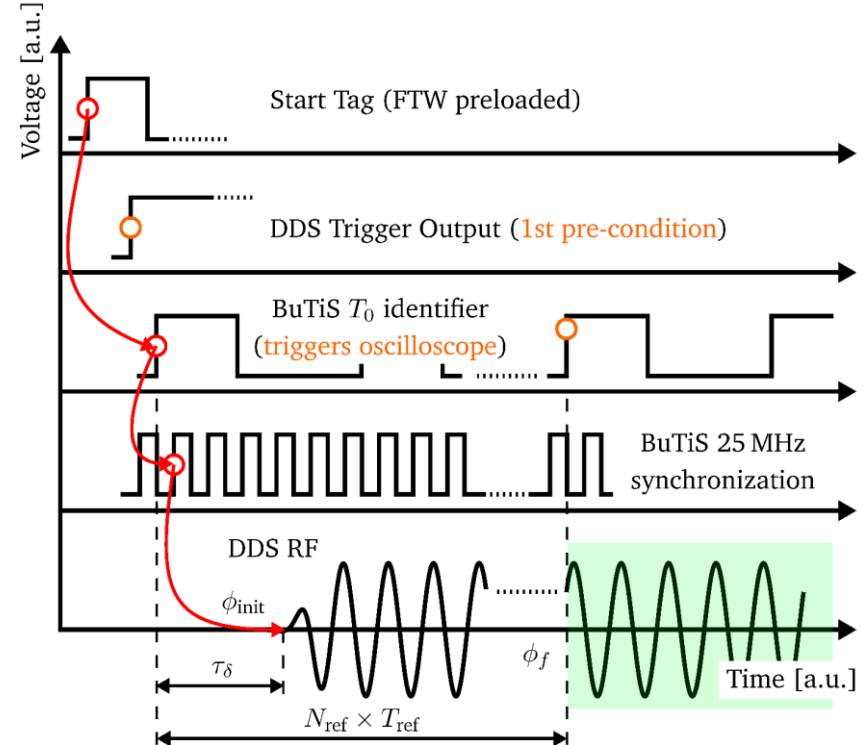
- To eliminate  $\phi_{e,f}$  modify initial phase that:

$$\phi_f - \phi_{\text{init, new}} = 2\pi f_{\text{DDS RF}} (N_{\text{ref}} T_{\text{ref}} - \tau_\delta) + \phi_{e,f}$$

- Phase error and phase correction:

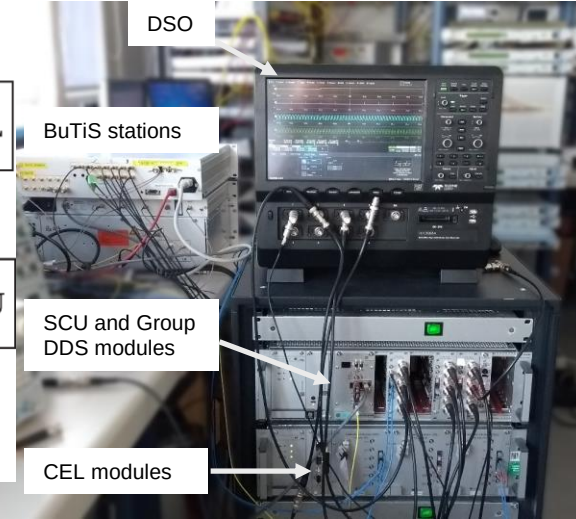
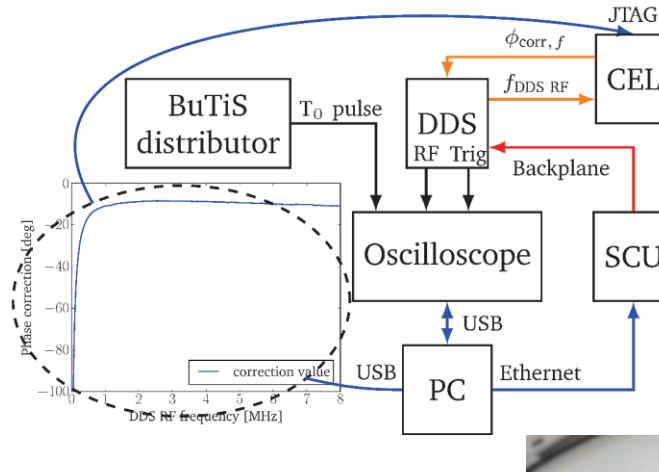
$$\phi_{e,f} = \phi_{\text{meas},f} - 2\pi f_{\text{DDS RF}} (N_{\text{ref}} T_{\text{ref}} - \tau_\delta)$$

$$\phi_{\text{corr},f} = \pi - [(-\phi_{e,f} + \pi) \bmod 2\pi]$$



# Measurement setup and procedure

- Calibration PC
- Front end controller: SCU
- DDS modules
- BuTiS stations:
  - Reference signal generator
  - Clock distribution amplifier
- DSO for data sampling and transferring
- CEL modules
- Signals connected to DSO:
  - DDS RF signal
  - BuTiS  $T_0$  pulse signal
  - DDS Trigger output

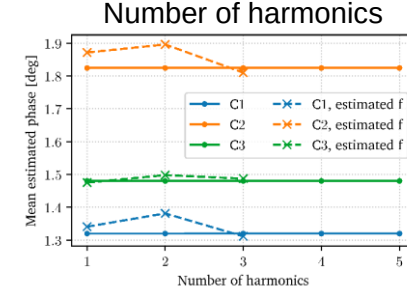
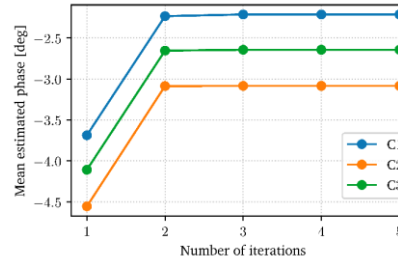
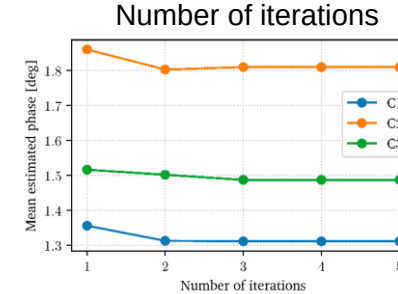


SCU – Scalable Control Unit  
DSO – Digital Storage Oscilloscope  
CEL – Calibration Electronic Module

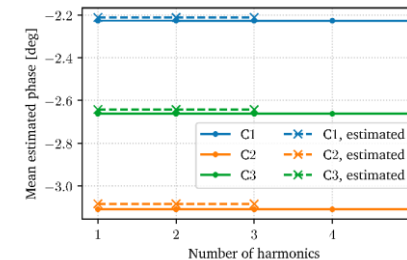
- Motivation:
  - Minimize time needed for the calibration
  - Guarantee convergence
  
- Sine fit parameters:
  - Number of iterations for frequency grid search
  - Number of harmonics included in the fitting function
  
- Amount of data for sine fit
  - Number of sine waves per measurement trace
  - Number of samples per sine wave

# Numerical optimization – Sine fit parameters

- Estimated phase converges after 3 iterations of the frequency grid search
- Estimated phase constant for 3PSF – first harmonic is sufficient
- Estimated phase improves with number of harmonics increased for 4PSF
- Difference between two approaches is below  $0.1^\circ$



f: 0.05 MHz

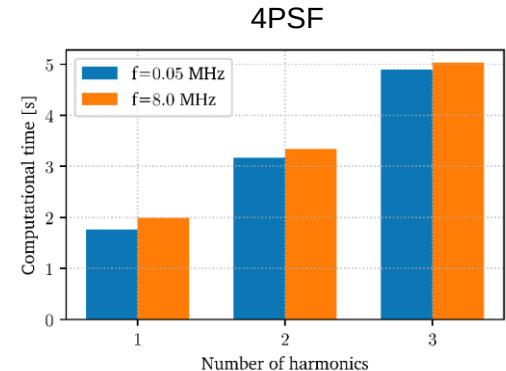
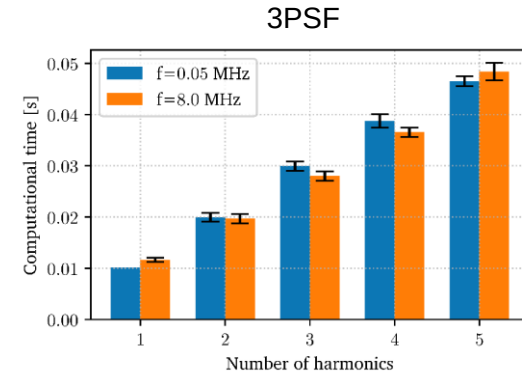


f: 8 MHz

# Processing time and choice of SFA

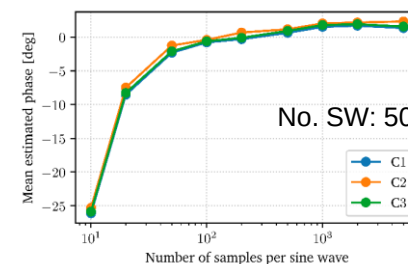
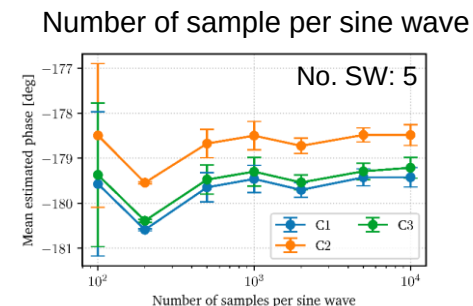
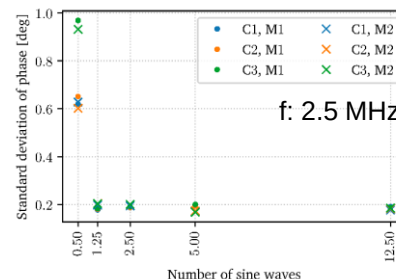
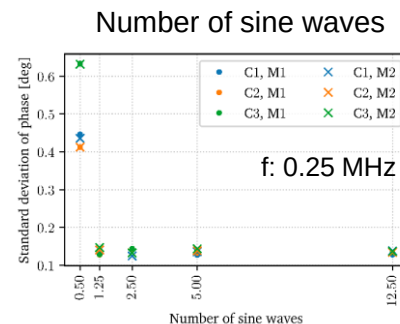
- Processing time increases with the number of harmonics for both methods
- Processing time is not a function of the frequency of the sampled signal
- 4PSF algorithm becomes impractical for harmonic numbers larger than 3
- Processing time: 3PSF is preferable to the 4PSF

| Number of harmonics           | 1       | 2       | 3     | 4       | 5       |
|-------------------------------|---------|---------|-------|---------|---------|
| Average processing time, 3PSF | 10.8 ms | 19.9 ms | 29 ms | 37.7 ms | 47.4 ms |
| Average processing time, 4PSF | 1.9 s   | 3.3 s   | 4.9 s | -       | -       |



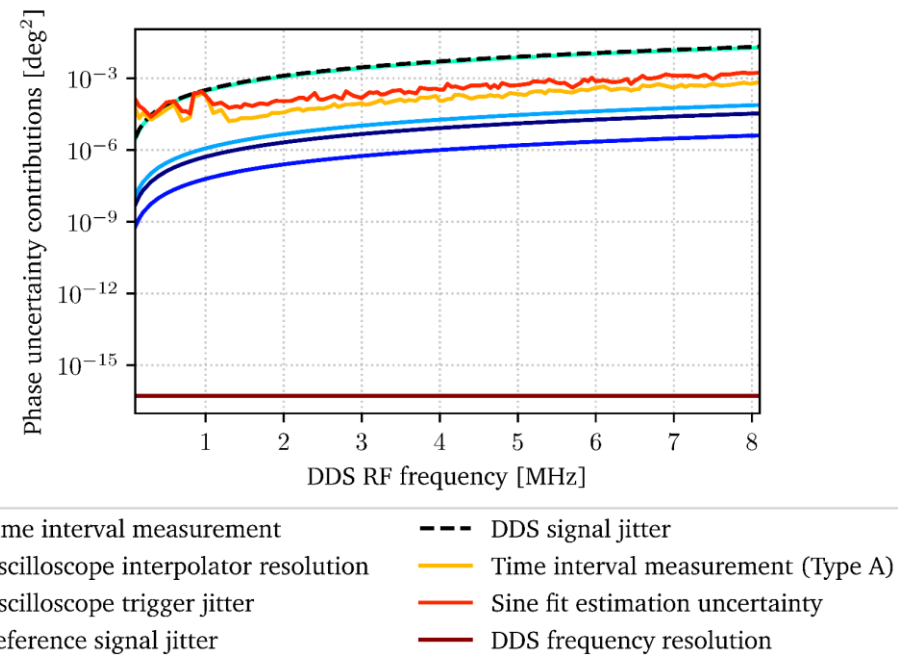
# Numerical optimization – Amount of data for sine fit

- 3PSF with one harmonic is used
- Constant standard deviation of phases if more than one RF period of the sine wave is sampled
- Possible to process data series with non-integer number of sine waves
- Calibration with an arbitrary frequency step
- Sufficient accuracy achieved with 2000 samples per sine wave
- Recommended measurement parameters obtained, maintained by a lookup table



# Uncertainty analysis

- Squared phase uncertainty contributions  
→ Combined phase measurement uncertainty
- Main uncertainty contributions:
  - DDS frequency resolution
  - Measurement instrument uncertainty
  - Sine fit estimation and oscilloscope time interval measurement (Type A evaluation)
  - Reference and DDS RF signals jitters
- Expanded uncertainty of the phase measurement ( $k=2$ , i.e.  $\sim 95\%$  coverage probability)  $\leq 0.5^\circ$
- To increase accuracy:
  - Jitters
  - DSO with better timebase accuracy and ADC resolution

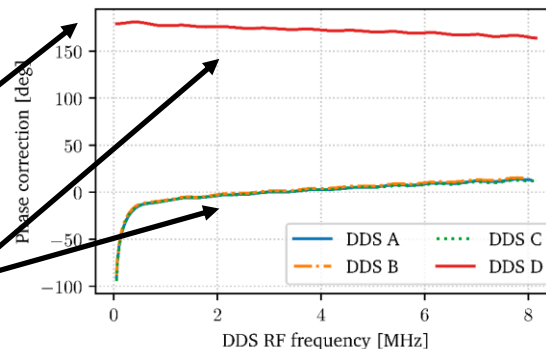


# Application at GSI: SIS18 Group DDS calibration

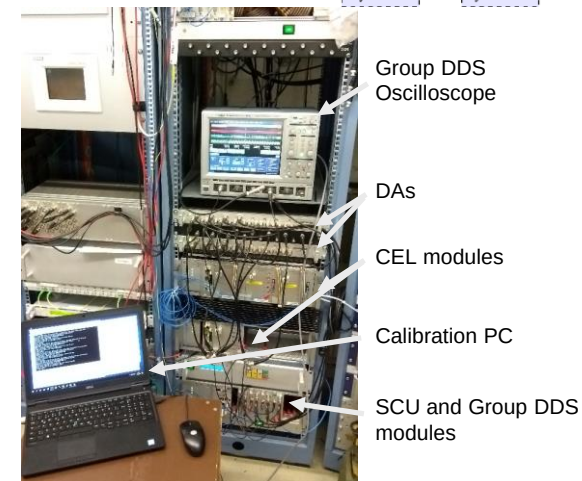
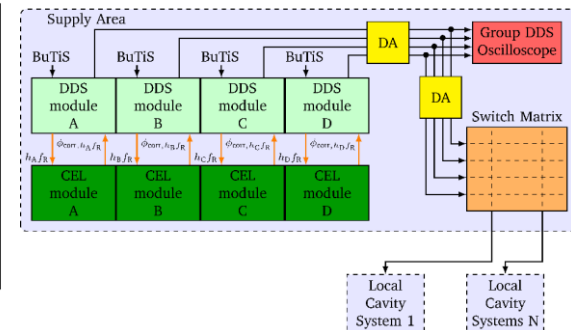
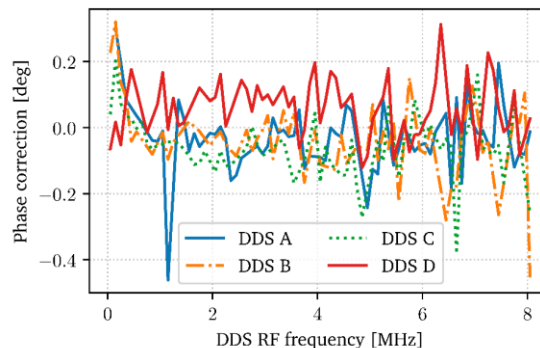
- DA influence is also compensated

Different HW revision

Reflections due to Half-wavelength ( $\lambda/2$ ) resonance



- Calibration time 12 minutes for one module
- Result is affected by the components after the calibration point
- Remaining phase error after the calibration is below  $\pm 0.5^\circ$



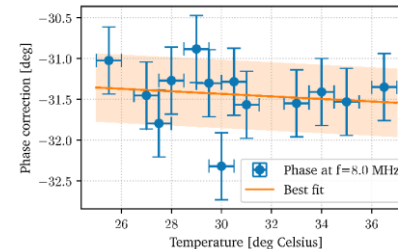
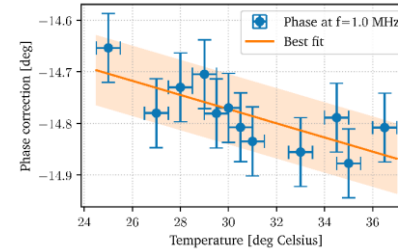
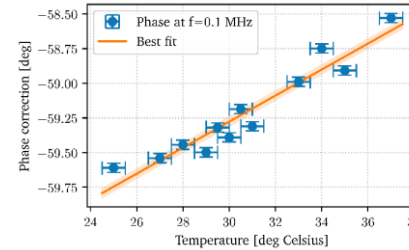


- Potential influence sources:
  - Supply voltage variations → Studied in detail
  - Ambient temperature variations → Studied in detail
  - Variations in cooling conditions (due to e.g. atmospheric pressure or humidity change) → Only seasonal changes; negligible
  - Degradation of components with time (aging) → Prevented by periodic repetitive calibrations

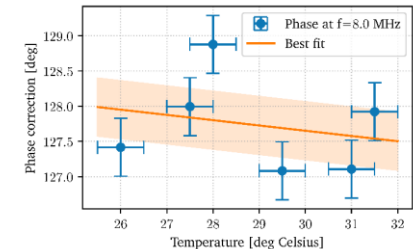
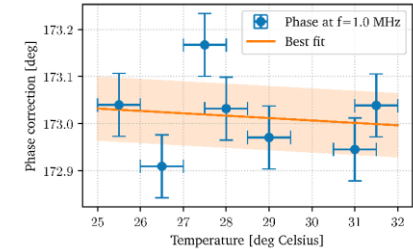
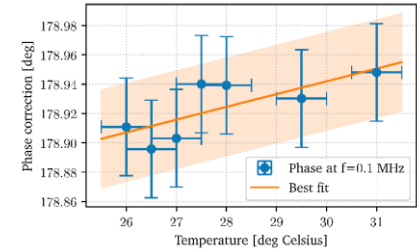
# Room temperature influence

- Temperature sensor measures air temperature in the vicinity of Group DDS crate
- Forced air cooling of crate is used
- Phase calibration data measured at different levels of the ambient temperature (temperature variations 25-36 °C)
- Data grouped by frequency and temperature
- 0.5° for each 5°C increase in temperature in the area where the calibration curve has the largest gradient
- Almost constant output phase for other regions
- Once per season calibration

DDS HW revision: 1.453

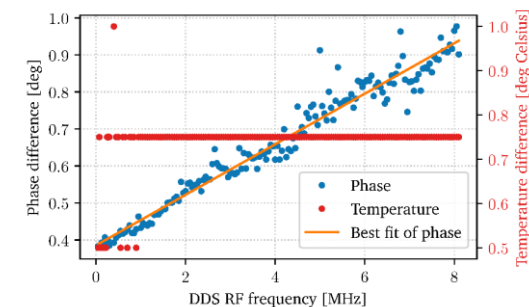
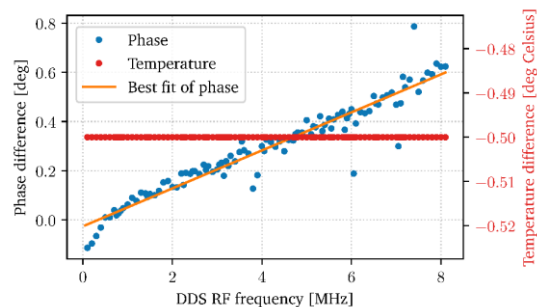
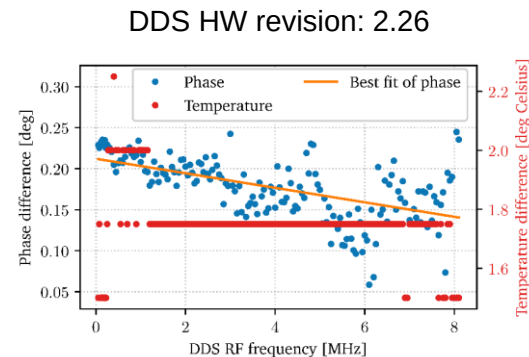
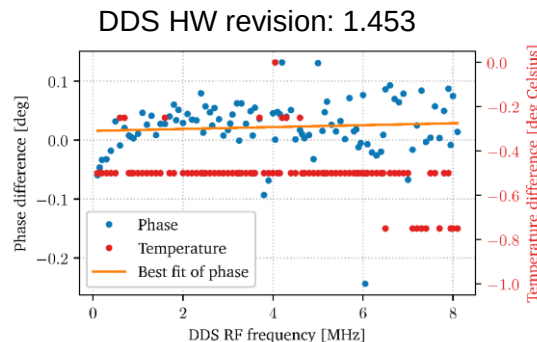


DDS HW revision: 2.26



# Supply voltage influence

- Values measured at two different levels of the supply voltages
- Temperature variations never exceeded  $2.5^{\circ}\text{C}$
- No influence of the analog supply voltage
- Linear increase of phase with the digital supply voltage
  - Phase deviation  $0.6^{\circ}$  @ 8 MHz for  $+0.5\text{ V}$
  - Time delay measurements: timing of the resynchronization process
- Monitoring or stabilization of the supply voltages, accuracy better than 10%



- Phase calibration method based on SFA is developed
- An approach to obtain phase corrections with respect to the reference pulse train is demonstrated
- Measurement parameters are analyzed
- Recommended parameters for the application at FAIR are derived
- Measurement uncertainty analysis is performed, uncertainty contributions are identified
- Application at SIS18 is demonstrated
- Stability and environmental influences are analyzed

# Acknowledgments



- Prof. Dr. Harald Klingbeil
  - Dr. Dieter Lens
  - Dr. Bernhard Zipfel
  - Stefan Schäfer
- 
- The department Ring RF systems

# Backup: Uncertainty analysis I

- DSO interpolates trigger location
- Trigger time compensation term to obtain a correct phase of the DDS module:

$$\Delta\tau_t = t_0 - t_t$$

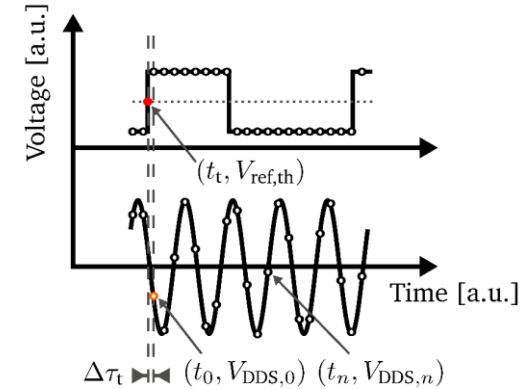
- Measurement model:

$$\phi_{e,f} = \phi_{\text{meas},f} - 2\pi f_{\text{DDS RF}} (N_{\text{ref}} T_{\text{ref}} - \tau_\delta + \Delta\tau_t)$$

- Combined uncertainty of the measured phase correction:

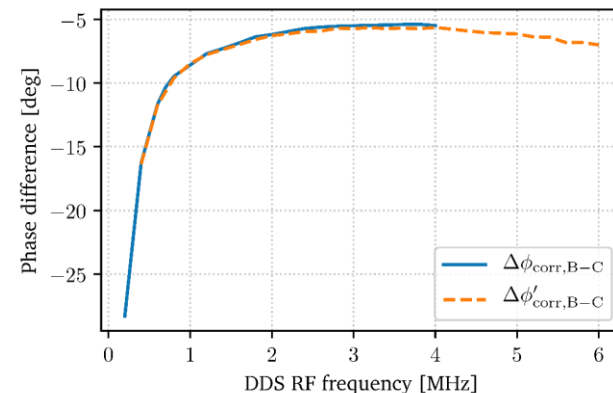
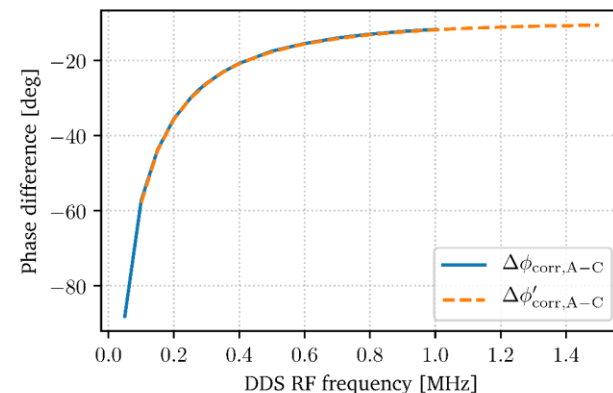
$$u_c(\phi_{e,f}) = \left( u^2(\phi_{\text{meas},f}) + (2\pi(\tau_\delta - N_{\text{ref}} T_{\text{ref}} - \Delta\tau_t))^2 u_c^2(f_{\text{DDS RF}}) + (2\pi f_{\text{DDS RF}})^2 u^2(\Delta\tau_t) \right)^{1/2}$$

- Identified elemental uncertainties can be combined



# Backup: Comparison with the formerly used calibration method

- 3 Group DDS modules operating at the harmonics 1, 4 and 8
- Phase calibration data measured with both methods



# Backup: Machine Development Experiment

- The method was used during the beam time operation
- Phases estimated from recorded traces
- Phase difference in the scale of the fundamental
- Phase deviation between modules A and B increases during the acceleration by about  $0.2^\circ$
- Phase deviations of modules are below  $0.5^\circ$
- Successful realization of multiharmonic operation over the complete acceleration cycle

