

# Study of a PWA of the $\bar{\Xi}^+ \Lambda K^-$ Final State with PAWIAN

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# Motivation

## Partial Wave Analysis

- Up to know: worked on analysis of  $\bar{p}p \rightarrow \bar{\Xi}^+ \Xi^{*-}$  with  $\Xi^{*-} \rightarrow \Lambda K^-$  (& c.c.)<sup>1)</sup>
- Quantum number of most  $\Xi$  resonances unknown or only estimated
- No experimental data and theoretical predictions
- PWA: possibility to determine those quantum numbers



Table 1. The status of the  $\Xi$  resonances. Only those with an overall status of \*\*\* or \*\*\*\* are included in the Baryon Summary Table.

Particle	$J^P$	Overall status	Status as seen in —				
			$\Xi\pi$	$\Lambda K$	$\Sigma K$	$\Xi(1530)\pi$	Other channels
$\Xi(1318)$	1/2+	****					Decays weakly
$\Xi(1530)$	3/2+	****	****				
$\Xi(1620)$		*	*				
$\Xi(1690)$		***		***	**		
$\Xi(1820)$	3/2-	***	**	***	**	**	
$\Xi(1950)$		***	**	**		*	
$\Xi(2030)$		***		**	***		
$\Xi(2120)$		*		*			
$\Xi(2250)$		**					3-body decays
$\Xi(2370)$		**					3-body decays
$\Xi(2500)$		*		*	*		3-body decays
****	Existence is certain, and properties are at least fairly well explored.						
***	Existence ranges from very likely to certain, but further confirmation is desirable and/or quantum numbers, branching fractions, <i>etc.</i> are not well determined.						
**	Evidence of existence is only fair.						
*	Evidence of existence is poor.						

PDG2014

1) See plenary talk and talk in Hyperon Session at CM 18/3



# What is PAWIAN?



- **P**Artial **W**ave **I**nteractive **A**Nalysis software
- Different spin formalisms and dynamics
- Event-based maximum likelihood fit (MINUIT2)
- Generates events based on user-defined decay model or on fit results obtained with real data

For further information: <https://panda-wiki.gsi.de/foswiki/bin/view/PWA/PawianPwaSoftware>



# Work Done In The Past



Until CM 20/3

Investigations on

- Single resonance channel ( $\Xi(1690)^-$  &  $\Xi(1820)^-$ ):
  - $L_{\max} = 2,3$ ; Fit of 30,000 events
  - Input values were reconstructable
- Data Sample with crossed channel ( $\bar{p}p \rightarrow \bar{\Lambda} (1890) \Lambda$ ):
  - $L_{\max} = 1$ ; Fit of 30,000 events
  - Only 7% of events were  $\Xi$  resonances
- First tests for single resonances using PAWIAN and PandaRoot

See talk in hyperon session at CM 20/3 <https://indico.gsi.de/event/11482>



# What is New?



- Crossed channel: 50% contribution for  $E$  resonances generated
- Finished investigations of single resonances using PAWIAN and PandaRoot
- Study of a sample with  $E(1690)^-$  AND  $E(1820)^-$



# How are Results Compared?



- Different criteria used: BIC and AIC
  - BIC: Bayesian information criterion
    - model selection among a finite set of models
  - AIC: Akaike information criterion
    - Estimates quality of model relative to set of models
  - In both cases, model with lowest value is preferred
- 
- Final selection based on :  $\Delta AIC = AIC_i - AIC_{min}$
  - $\Delta AIC < 2$ : evidence for the model;  $\Delta AIC > 10$  : model unlikely
  - Special case: AIC and BIC show different tendencies => AIC+BIC

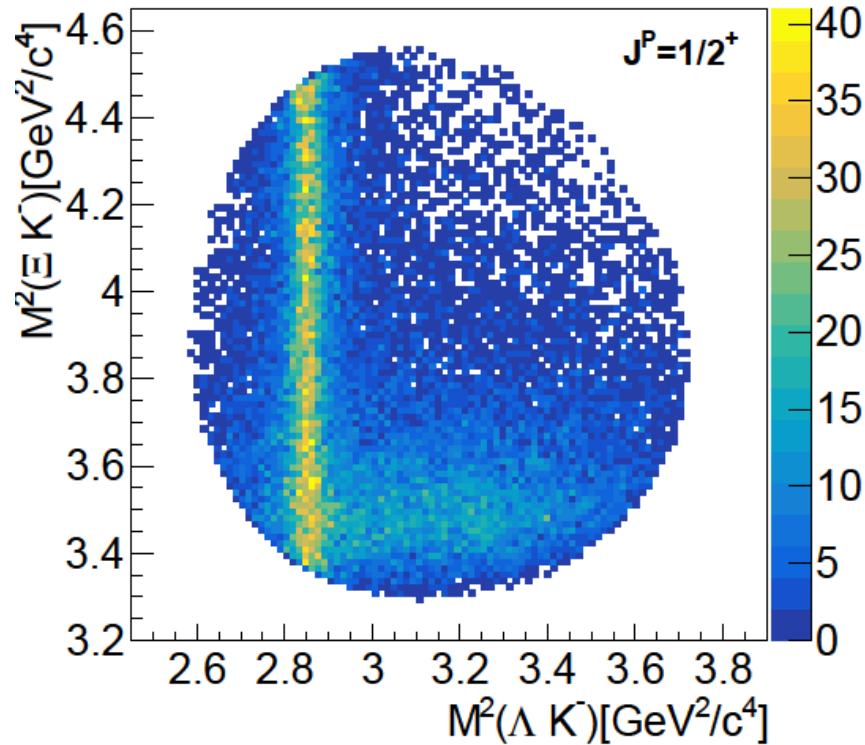


# Crossed Channel

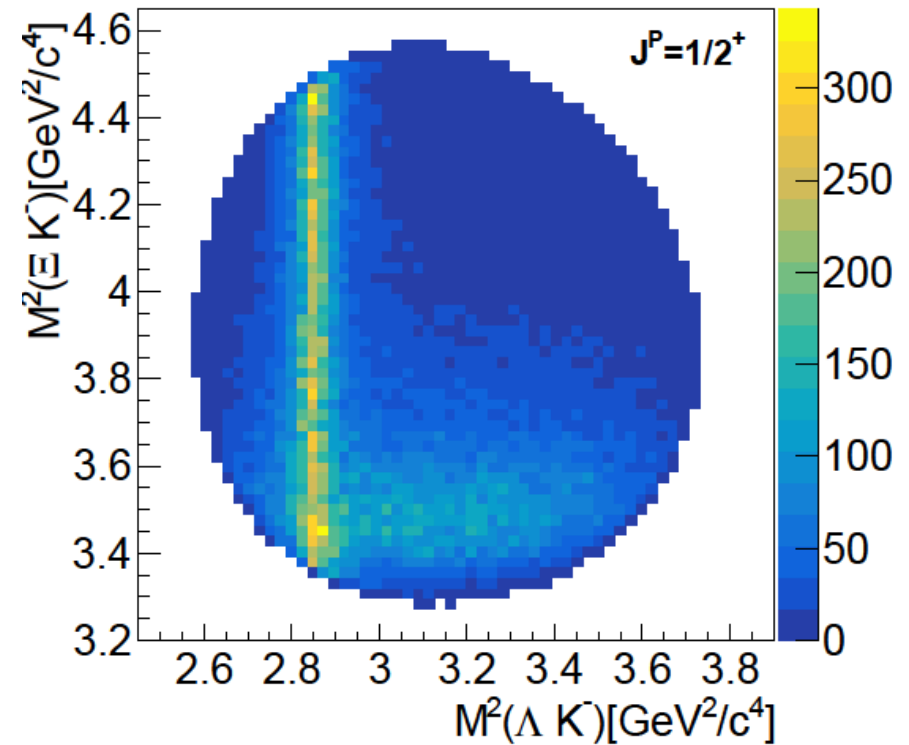


# $\Xi(1690)^-$

Input Data



Fit Results



$$\bar{\Lambda}(1890): \Gamma \approx 120 \text{ MeV}/c^2 \quad J^P = 3/2^+$$



# Results



$\Xi(1690)^-$   $\Delta$ AIC Values 30,000 Events

Fit $\rightarrow$ Gen $\downarrow$	$1/2^+$	$1/2^-$	$3/2^+$	$3/2^-$
$1/2^+$	0.0	42.6	35.6	103.2
$1/2^-$	84.2	0.0	102.8	378.4
$3/2^+$	1,598.6	3,195.4	0.0	175.8
$3/2^-$	1,908.5	2,132.6	840.1	0.0



# Results



$E(1820)^-$   $\Delta AIC$  Values 30,000 Events

Fit $\rightarrow$ Gen $\downarrow$	$1/2^+$	$1/2^-$	$3/2^+$	$3/2^-$
$1/2^+$	0.0	56.5	49.1	48.8
$1/2^-$	24.6	0.0	41.0	11.5
$3/2^+$	1,075.6	1,054.9	0.0	42.5
$3/2^-$	1,417.8	1,443.2	124.8	0.0



# PAWIAN & PandaRoot

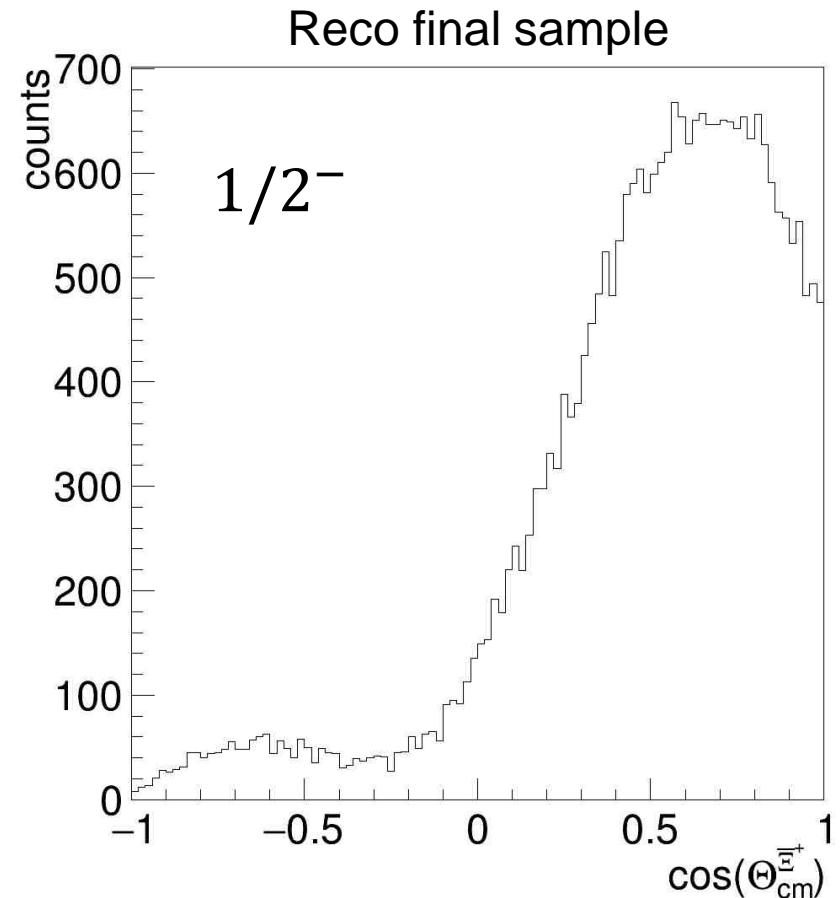
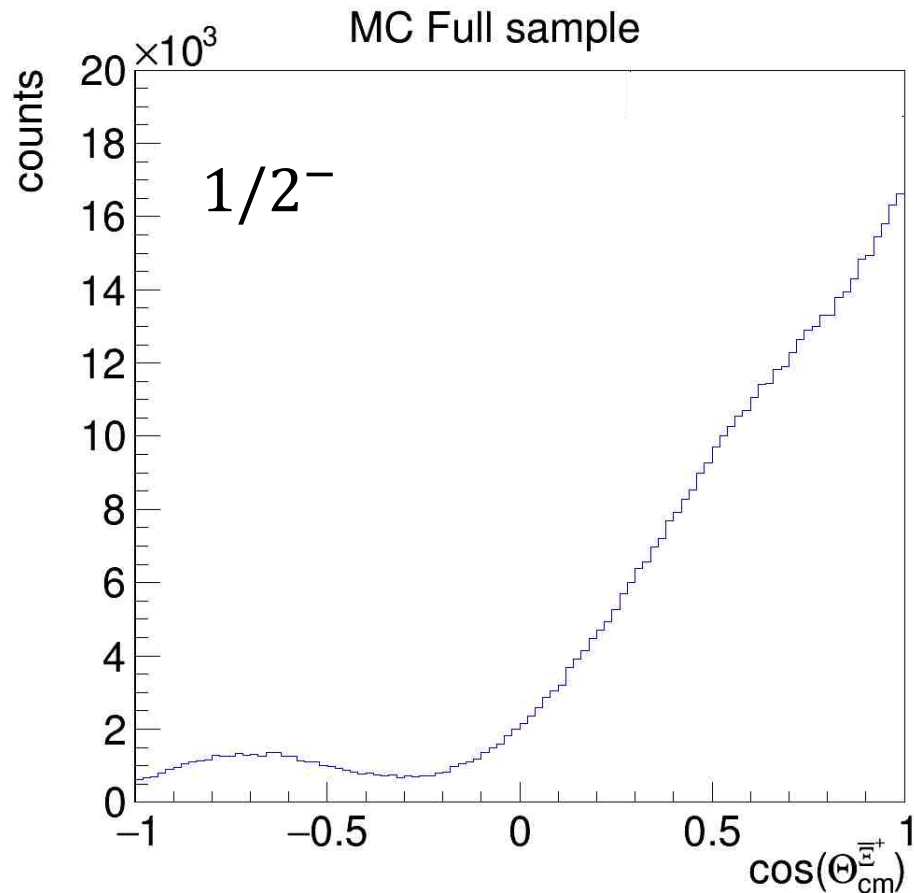


## Simulations

- Generated ~600,000 events for both  $E(1690)^-$  &  $E(1820)^-$  with PAWIAN included event generator
- Used as input for the full sim + reco chain in PandaRoot
- ~26,000 events reconstructed in analysis with DecayTreeFitter
- Reconstructions efficiency: 5%
- Fraction of pure signal events: 94.2%



## Angular Distribution $\Xi^+$ in center-of-mass Frame



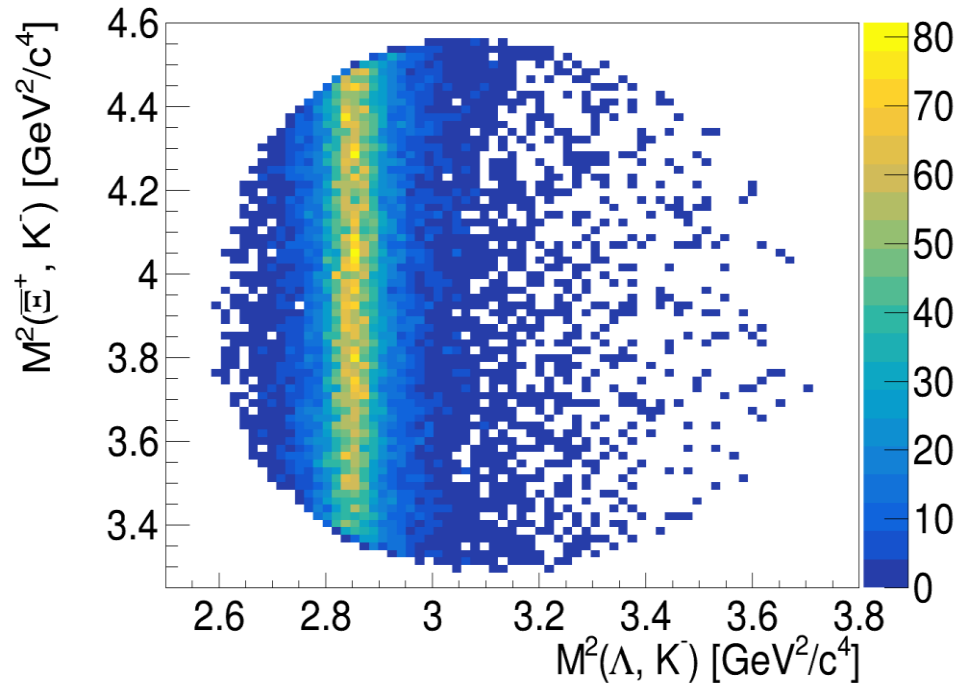


# PAWIAN & PandaRoot

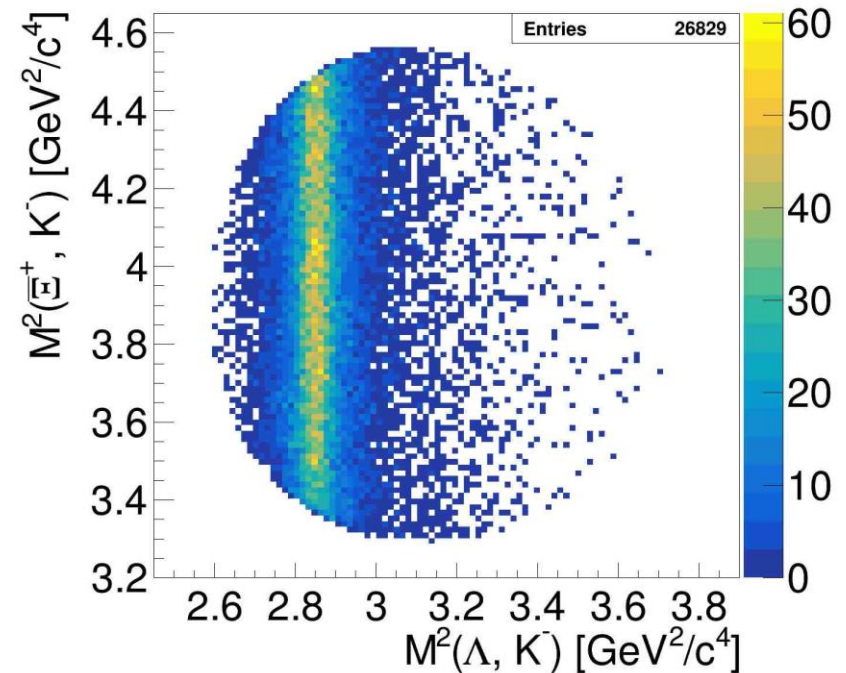


## Dalitz Plots $\Xi(1690)^-$

MC full sample



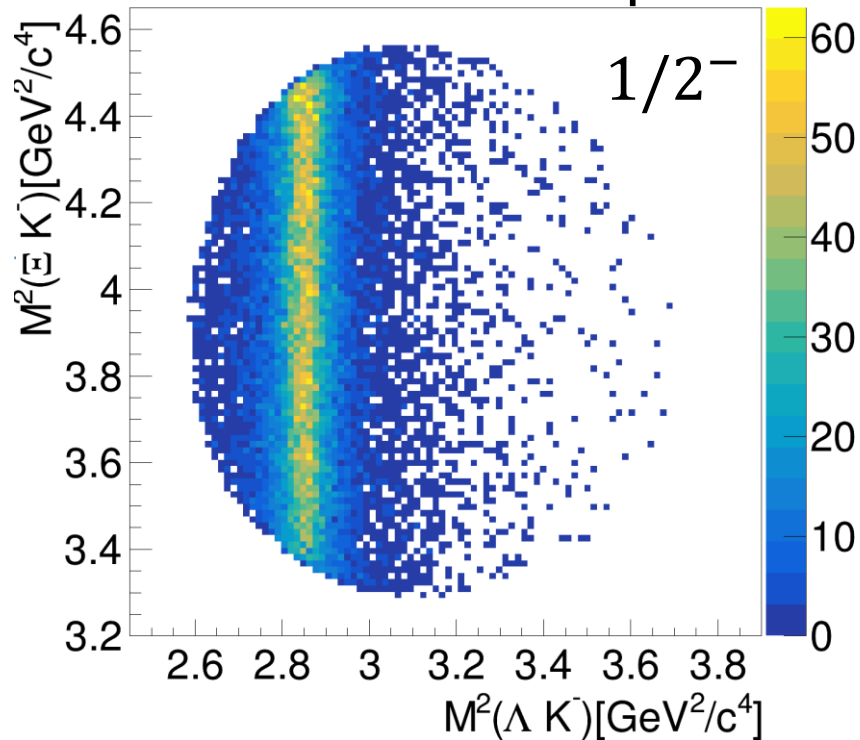
reco final sample



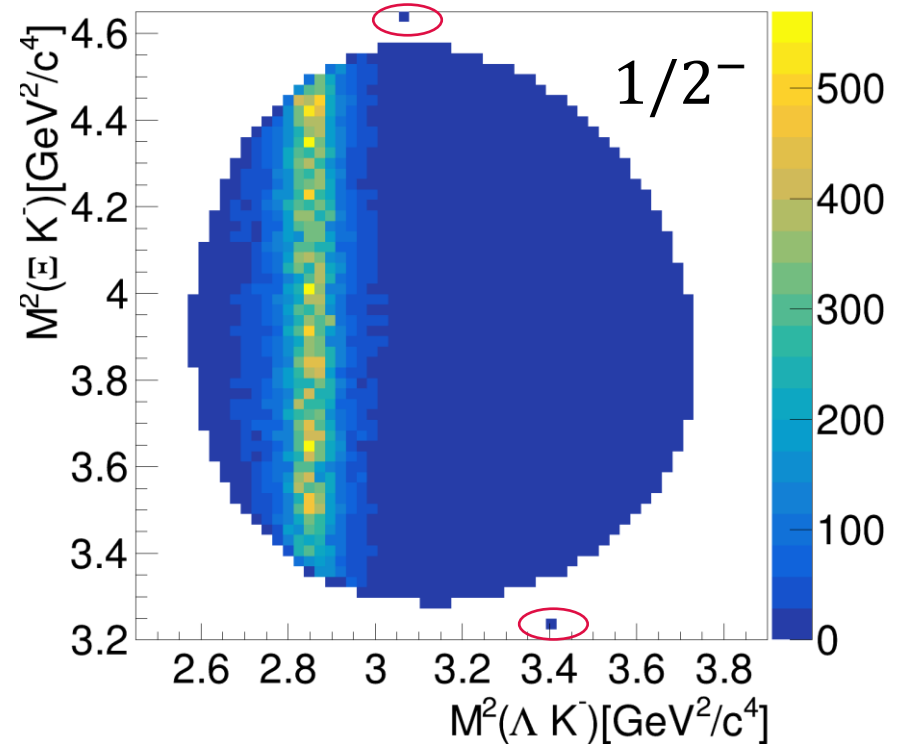


## Dalitz Plots $\Xi(1690)^-$

Reco final sample



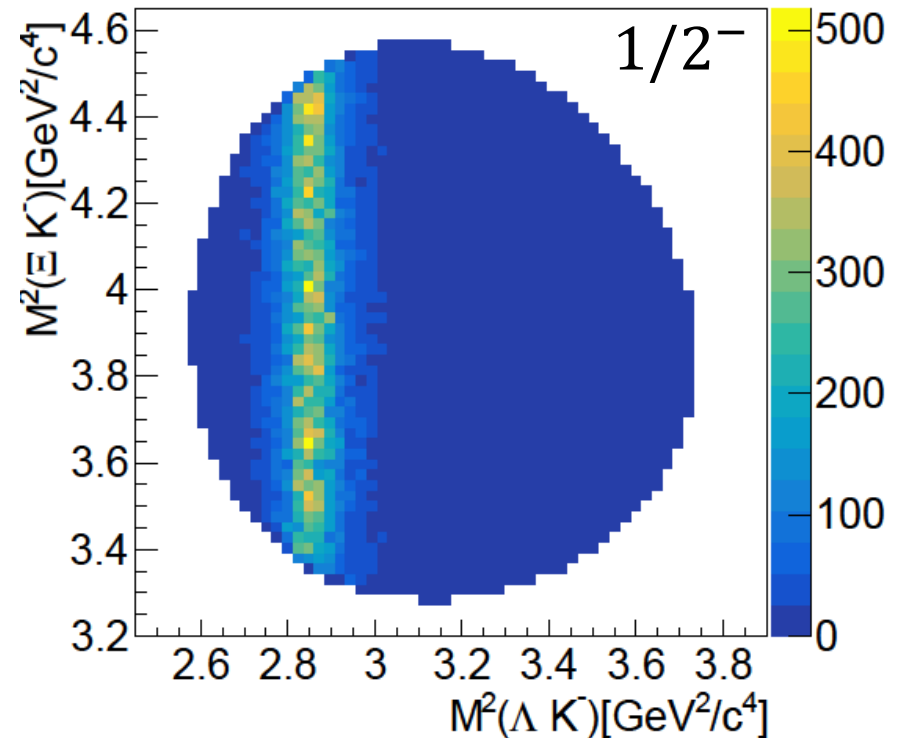
Fit Results





## Mass Window Selection

- Outliers caused by  $\Xi^-$  mass far off nominal mass after DTF of continuum sample
- Additional mass window selection:  
 $(1.319 < M_{\Xi} < 1.323) \text{ GeV}/c^2$
- Removes all outliers in continuum sample and up to 3 signal events





# PAWIAN & PandaRoot



$E(1690)^-$   $\Delta AIC$  Values (PandaRoot+ PAWIAN)

Fit $\rightarrow$ Gen $\downarrow$	$1/2^+$	$1/2^-$	$3/2^+$	$3/2^-$
$1/2^+$	0.0	2,550.6	2,310.6	2,706.8
$1/2^-$	316.7	0.0	328.2	2,332.2
$3/2^+$	4,973.9	5,228.0	0.0	584.6
$3/2^-$	5,345.6	3,118.6	833.1	0.0



# PAWIAN & PandaRoot



$\Xi(1820)^-$  AIC + BIC Values (PandaRoot+ PAWIAN)

Fit → Gen ↓	$1/2^+$	$1/2^-$	$3/2^+$	$3/2^-$
$1/2^+$	-133,352.4	-133,121.5	-133,193.7	-133,144.3
$1/2^-$	-130,496.3	-130,593.1	-130,382.0	-129,705.7
$3/2^+$	-119,599.4	-119,468.2	-127,072.7	-126,874.3
$3/2^-$	-132,767.8	-133,484.6	-139,895.2	-140,385.4



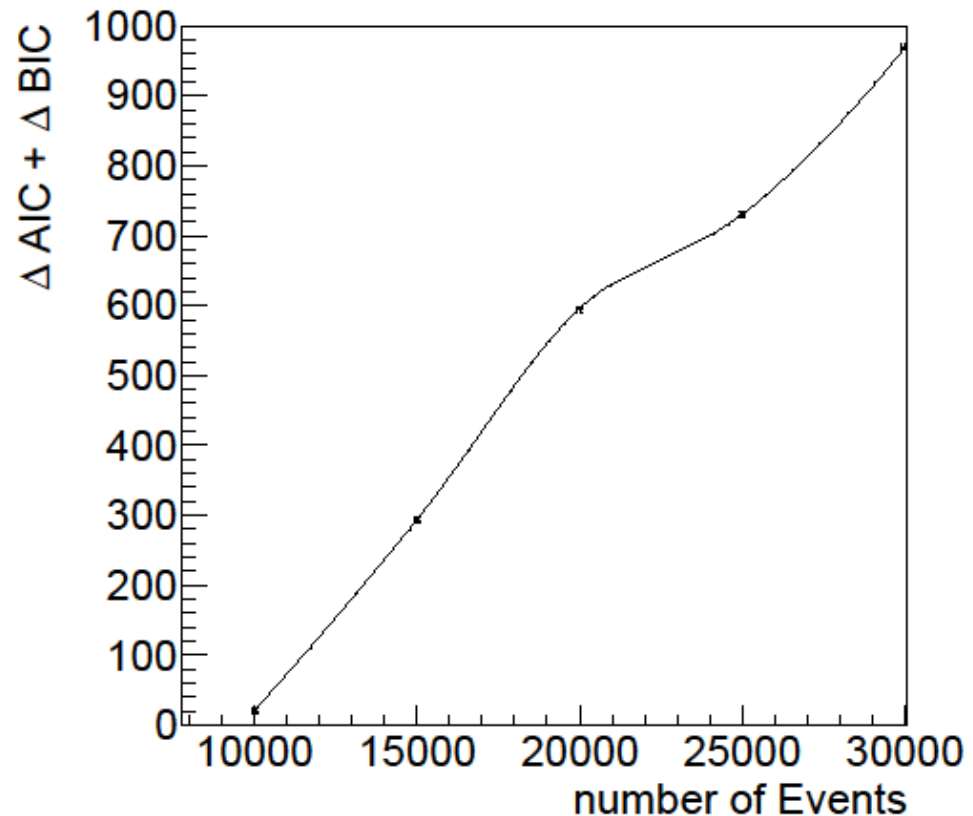
# $E(1690)^-$ and $E(1820)^-$ Sample



# Combined Sample

## Event Generation and Fit Results Ideal Case

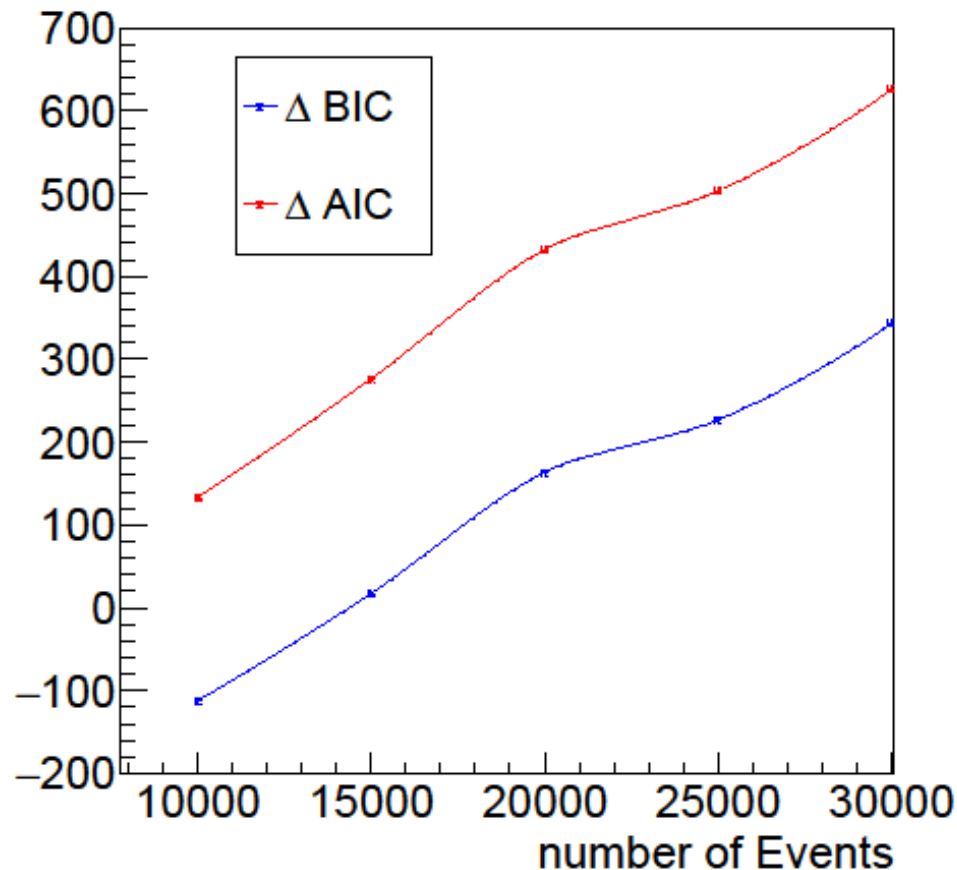
- Generated 10,000 events only  $J^P(\Xi(1690)) = 1/2^+$  and  $J^P(\Xi(1820)) = 3/2^-$
- Fitted with all possible combinations
- $1/2^+ 1/2^-$  can not be safely excluded
- How much statistics needed to exclude it?





# Combined Sample

## Event Generation and Fit Results Ideal Case

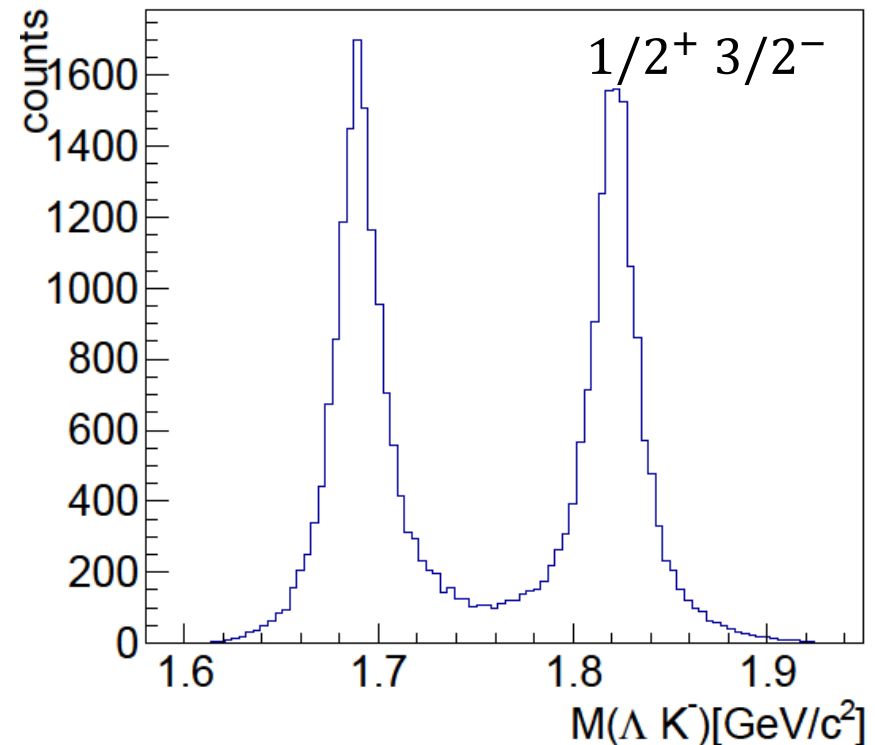
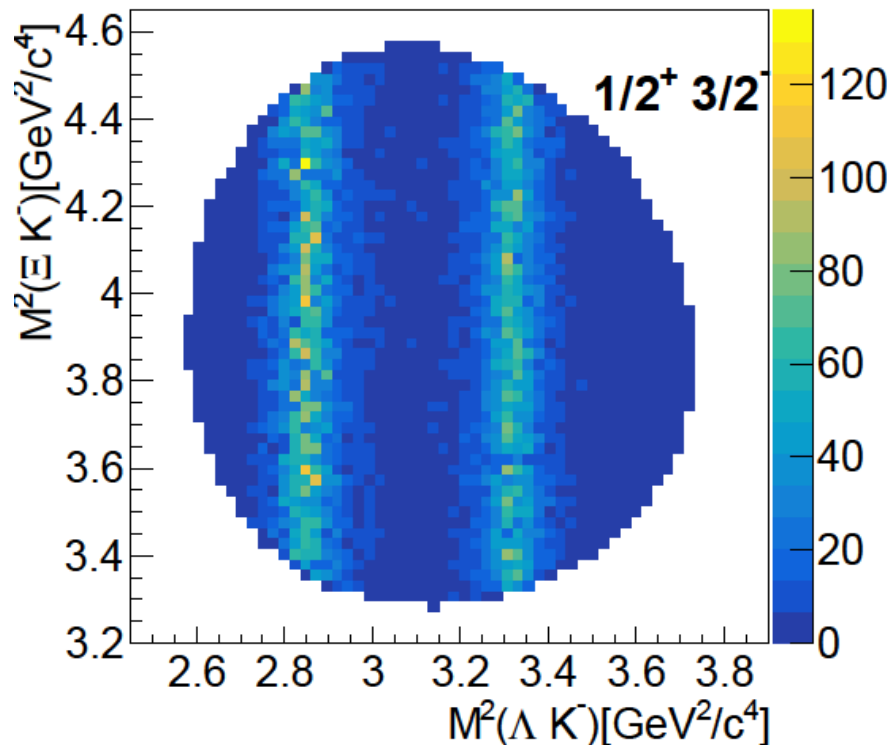




# Combined Sample



## Dalitz Plot and Mass Distribution

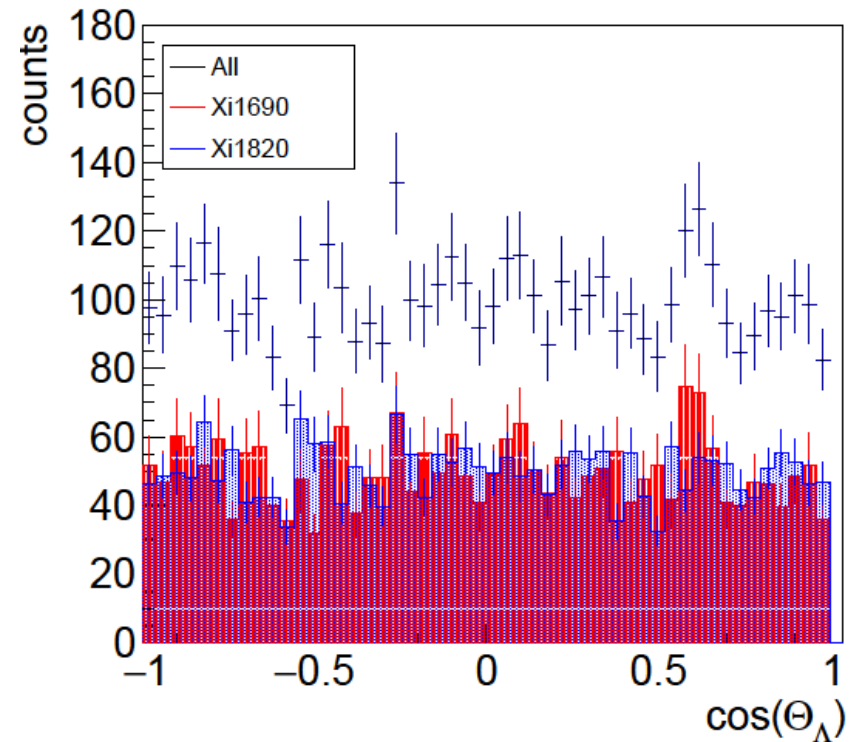
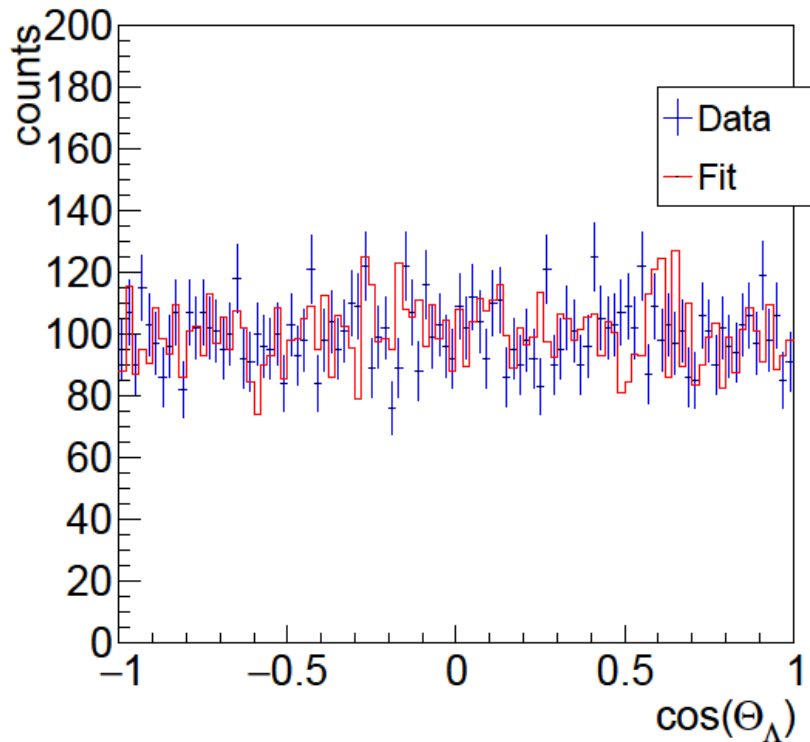




# Combined Sample



## Cos $\Theta$ distribution of $\Lambda$ from $\Lambda K^-$ System in Helicity Frame





# Summary & Outlook



- Performed test to reproduce quantum numbers
- “Single” resonances & crossed channel: promising
- PandaRoot & PAWIAN:
  - in good agreement with feasibility study
  - Input QN can be reproduced
- Combined Sample: first test with 10,000 events leads to promising results -> more statistics needed
- Verify results for combined sample with other QN
- PandaRoot & PAWIAN should be used for combined sample
- Same tests should be done for charge conjugate particles



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  - in good agreement with feasibility study
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- Combined Sample: first test with 10,000 events leads to promising results -> more statistics needed

**Release note under review and  
paper in preparation**





**Thank you for your attention**



## Backup



# Results



## $E(1690)^-$ $\Delta AIC$ Values

Fit $\rightarrow$ Gen $\downarrow$	$1/2^+$	$1/2^-$	$3/2^+$	$3/2^-$
$1/2^+$	0.0	310.0	23.0	347.0
$1/2^-$	274.0	0.0	281.0	2,256.0
$3/2^+$	60,320.7	4,861.9	0.0	503.9
$3/2^-$	81,128.3	25,893.9	19,541.6	0.0

First fit with fixed mass and width



# Results



## $E(1820)^-$ $\Delta AIC$ Values

<b>Fit</b> → <b>Gen</b> ↓	$1/2^+$	$1/2^-$	$3/2^+$	$3/2^-$
$1/2^+$	0.0	46,427.9	3.9	35,374.6
$1/2^-$	72.9	0.0	40,135.0	446.6
$3/2^+$	3,911.2	3,969.3	0.0	36,377.4
$3/2^-$	3,457.7	3,698.0	201.0	0.0



- Is it possible to reconstruct the input values?
- Event Generation:
  - 1 data set for  $\bar{\Xi}\Lambda K^-$
  - 1 data set for each resonance
- $p_{\bar{p}} = 4.6 \text{ GeV}/c$
- Different quantum numbers generated for  $\Xi(1690)^-$  and  $\Xi(1820)^-$   
 $\frac{1}{2}^-, \frac{1}{2}^+, \frac{3}{2}^-, \frac{3}{2}^+$
- Fit all hypotheses to each generated data set
- At later stage: included crossed channel  $\bar{p}p \rightarrow \bar{\Lambda}(1890)\Lambda$



- **Bayesian information criterion (BIC):**

is a criterion for model selection among a finite set of models; the model with the lowest BIC is preferred.

$$BIC = 2 \cdot (-LHH) + k \cdot \ln(n)$$

with LHH: maximal loglikelihood value, k: number of free fit parameters and n: number of events in the sample

- **Akaike information criterion (AIC):**

is a measure of the relative quality of statistical models for a given set of data. Given a collection of models for the data, AIC estimates the quality of each model, relative to each of the other models

$$AIC = 2k + 2 \cdot (-LLH)$$



# Event Generation



## Maximum Angular Momentum of $\bar{p}p$

- Beam momentum of 4.6 GeV/c<sup>2</sup> corresponds to a momentum in center-of-mass frame of:
  - $p_{\text{cm}} \approx 600 \text{ MeV/c}$  for  $\Xi(1690)^- \rightarrow L_{\text{max}} = 3$
  - $p_{\text{cm}} \approx 410 \text{ MeV/c}$  for  $\Xi(1820)^- \rightarrow L_{\text{max}} = 2$



# Helicity Frame

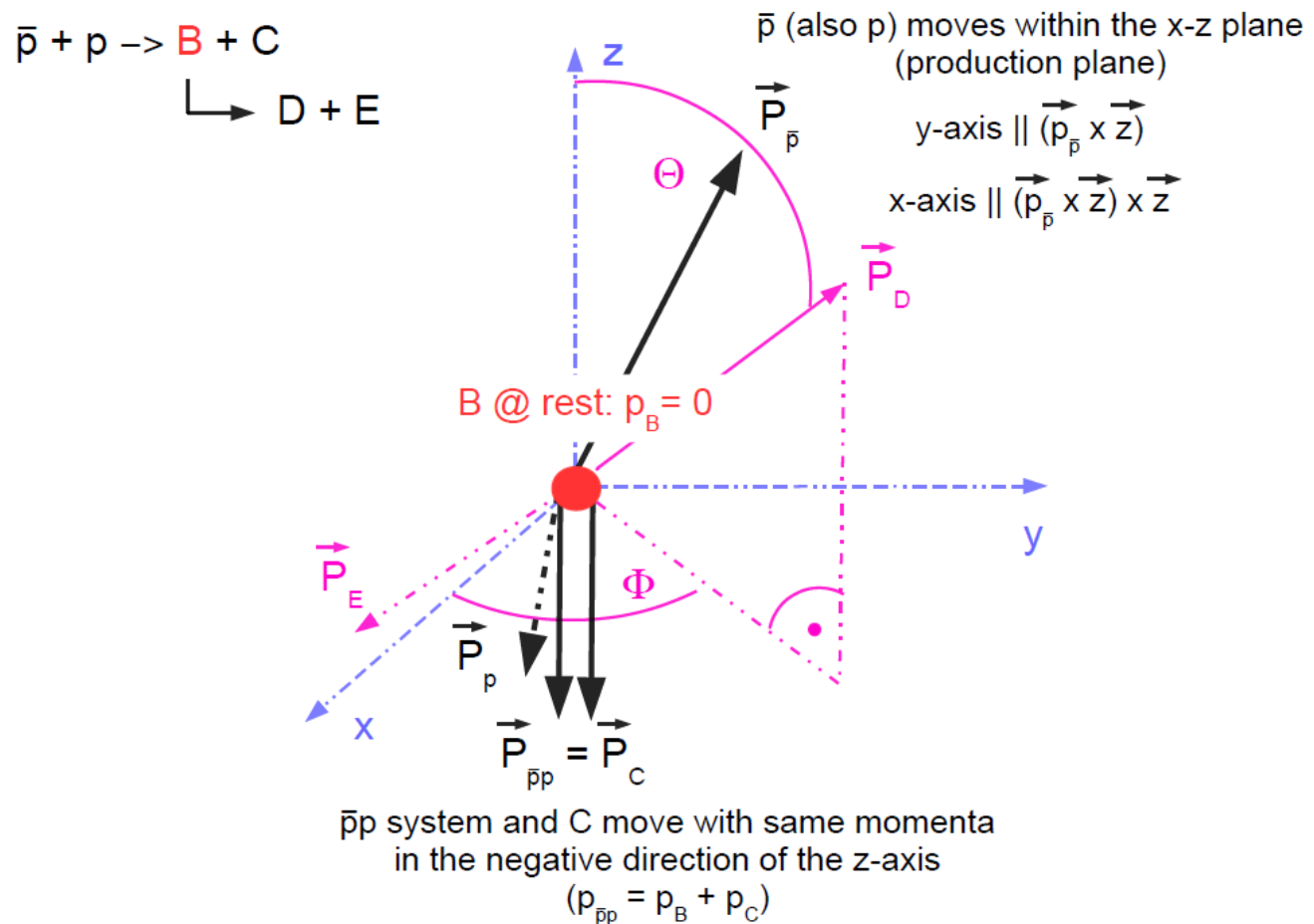


Image from Bertram Kopf



# Gottfried-Jackson Frame

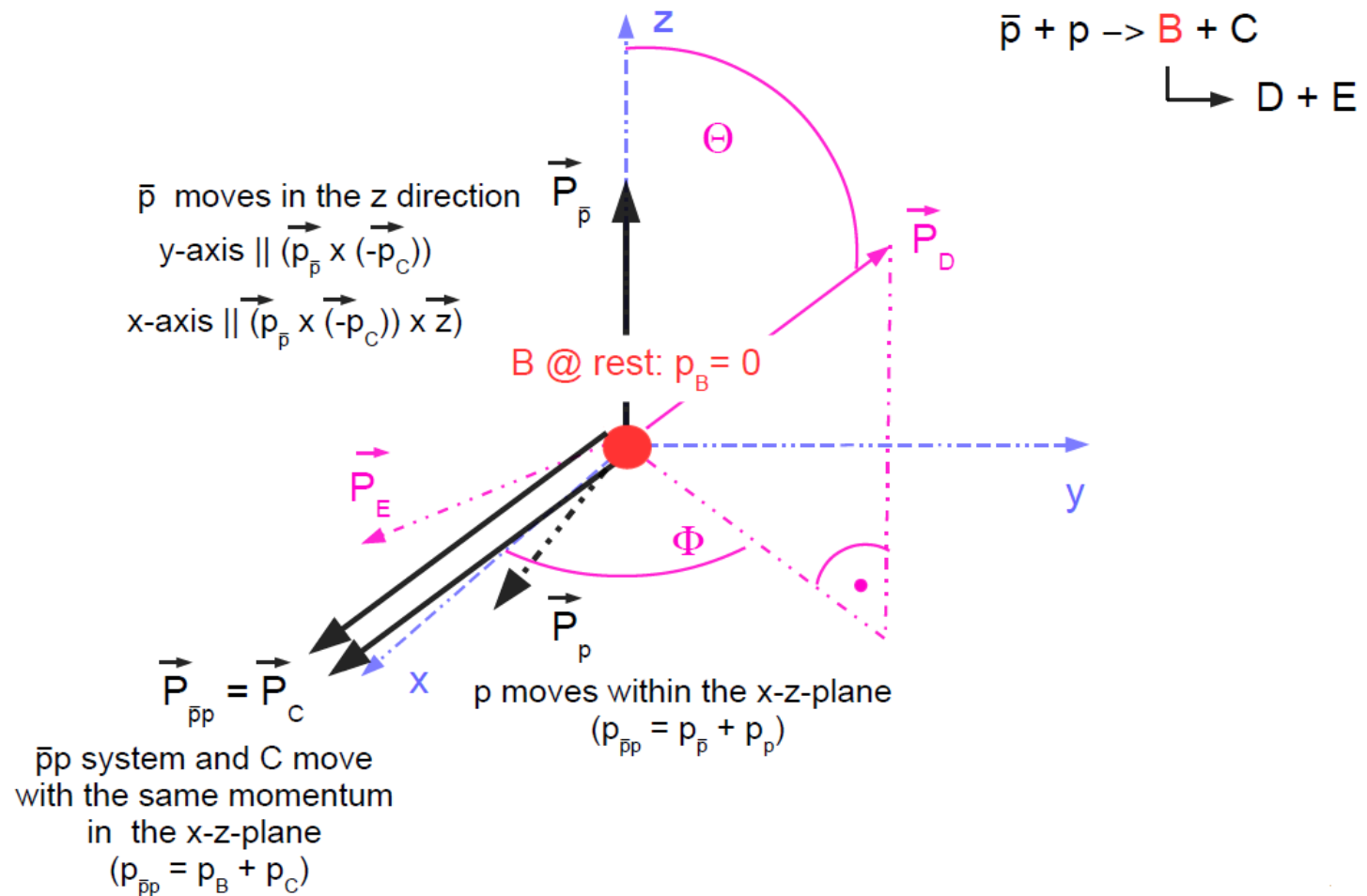


Image from Bertram Kopf