

New physics searches in quarkonium decays - theory -

Grigoris Panotopoulos and Miguel-Angel Sanchis-Lozano

IFIC

University of Valencia – CSIC

Spain

QWG 2011
GSI, Darmstadt October 2011

Next-to-Minimal-Supersymmetric Standard Model (NMSSM)

Higgs sector

Things should be as simple as possible, but not simpler

A. Einstein

$$\hat{H}_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}, \quad \hat{H}_d = \begin{pmatrix} H_d^+ \\ H_d^0 \end{pmatrix}, \quad \hat{S}$$

↑
New gauge-singlet superfield

$$W = \lambda S H_u H_d + \frac{1}{3} \kappa S^3 + \dots$$

$$V_{soft} = \lambda A_\lambda S H_u H_d + \frac{1}{3} \kappa A_\kappa S^3 + h.c. + \dots$$

Six “free” parameters vs three in the MSSM :

$$\kappa \quad \lambda \quad A_\kappa \quad A_\lambda \quad \mu \quad \tan \beta$$

$$B_{eff} = A_\lambda + \kappa s$$

Physical Higgs bosons: (seven)

2 neutral CP-odd Higgs bosons ($A_{1,2}$)

3 neutral CP-even Higgs bosons ($H_{1,2,3}$)

2 charged Higgs bosons (H^\pm)

PQ symmetry or $U(1)_R$ slightly broken



light pseudoscalar Higgs

Non-singlet component

Singlet component

$$A_1 = \cos \theta_A A_{MSSM} + \sin \theta_A A_s$$

$$\tan \beta = v_u / v_d$$



$$A_1 \text{ coupling to down type fermions } \propto X_d = \cos \theta_A \tan \beta$$

Might be not too small for high $\tan \beta$

$$\begin{aligned}
 A_\lambda &= -200 \text{ GeV} \\
 A_\kappa &= -15 \text{ GeV} \\
 \mu &= 150 \text{ GeV} \\
 \tan \beta &= 40
 \end{aligned}$$

$$\begin{aligned}
 A_\lambda &\sim -K \mu / \lambda \\
 K - (4/3) \lambda &= 0
 \end{aligned}$$

$$0.1 \leq |\cos \theta_A| \leq 0.5$$

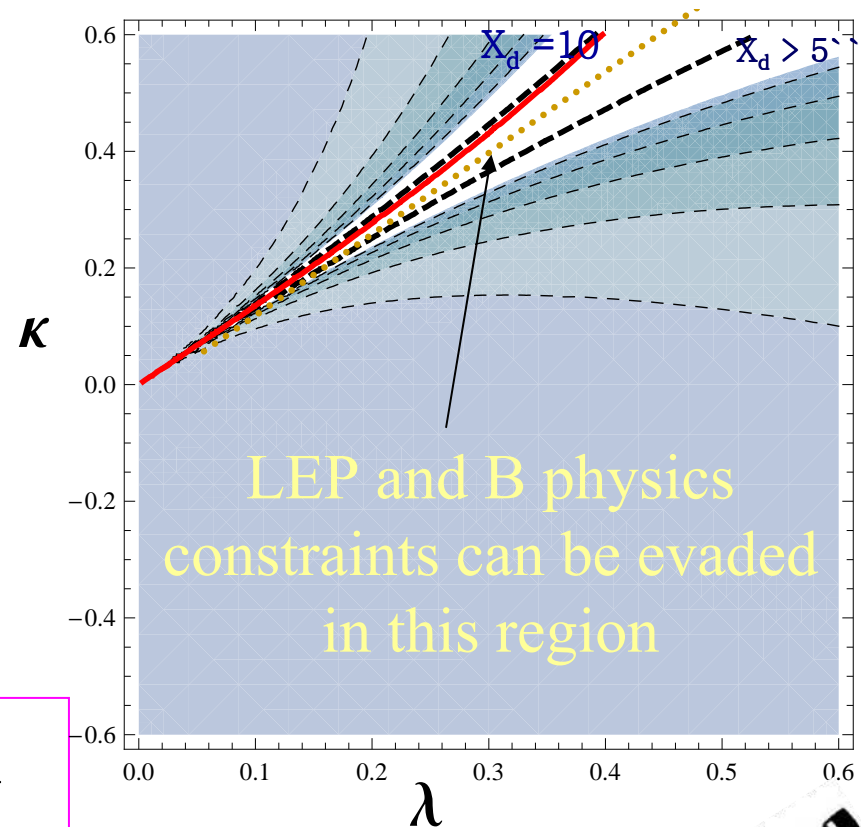
$$X_d = \cos \theta_A \tan \beta$$

At large $\tan \beta$: $\sin 2\beta \approx \frac{2}{\tan \beta}$

$$\begin{aligned}
 \cos \theta_A &\cong - \frac{\lambda v (A_\lambda - 2\kappa s) \sin 2\beta}{2\lambda s (A_\lambda + \kappa s) + 3\kappa A_\kappa s \sin 2\beta} \\
 &\quad B_{eff}, (\lambda A_\lambda + \kappa \mu) \rightarrow 0 \\
 m_{A_1}^2 &\cong 3s \left(\frac{3\lambda A_\lambda \cos^2 \theta_A}{3 \sin 2\beta} - 2\kappa A_\kappa \sin^2 \theta_A \right)
 \end{aligned}$$

$$\tan \beta \sim 1 / [A_\lambda + K \mu / \lambda]$$

Ananthanarayan & Pandita, hep-ph/9601372



The same region of the parameter space of the NMSSM yields simultaneously:

A_1 mass near 10 GeV
Large X_d (at high $\tan \beta$)

$$M_{A_1}^2 = \frac{2\mu B_{eff}}{\sin 2\beta} = \frac{A_\lambda + \kappa s}{\sin 2\beta} \Rightarrow \text{Moderate!}$$

The (somewhat old) Proposal

Since 2002

- 1) Test of Lepton Universality* in $\Upsilon(1S,2S,3S)$ decays to taus at (below) the few percent level @ a (Super) B factory

Mod. Phys. Lett. A17 (2002) 2265

Int. J. Mod. Phys. A19 (2004) 2183

More recently

- 2) Possible Distorsion of Bottomonium Spectroscopy due to mixing of η_b states and a light CP-odd Higgs

Phys. Rev. Lett. 103 (2009) 111802



It is hard to find a black cat in a dark room, especially if there is no cat

Confucius

* Lepton universality: Gauge bosons couple to all lepton species with equal strength in the SM

Present status of Lepton Universality (PDG)

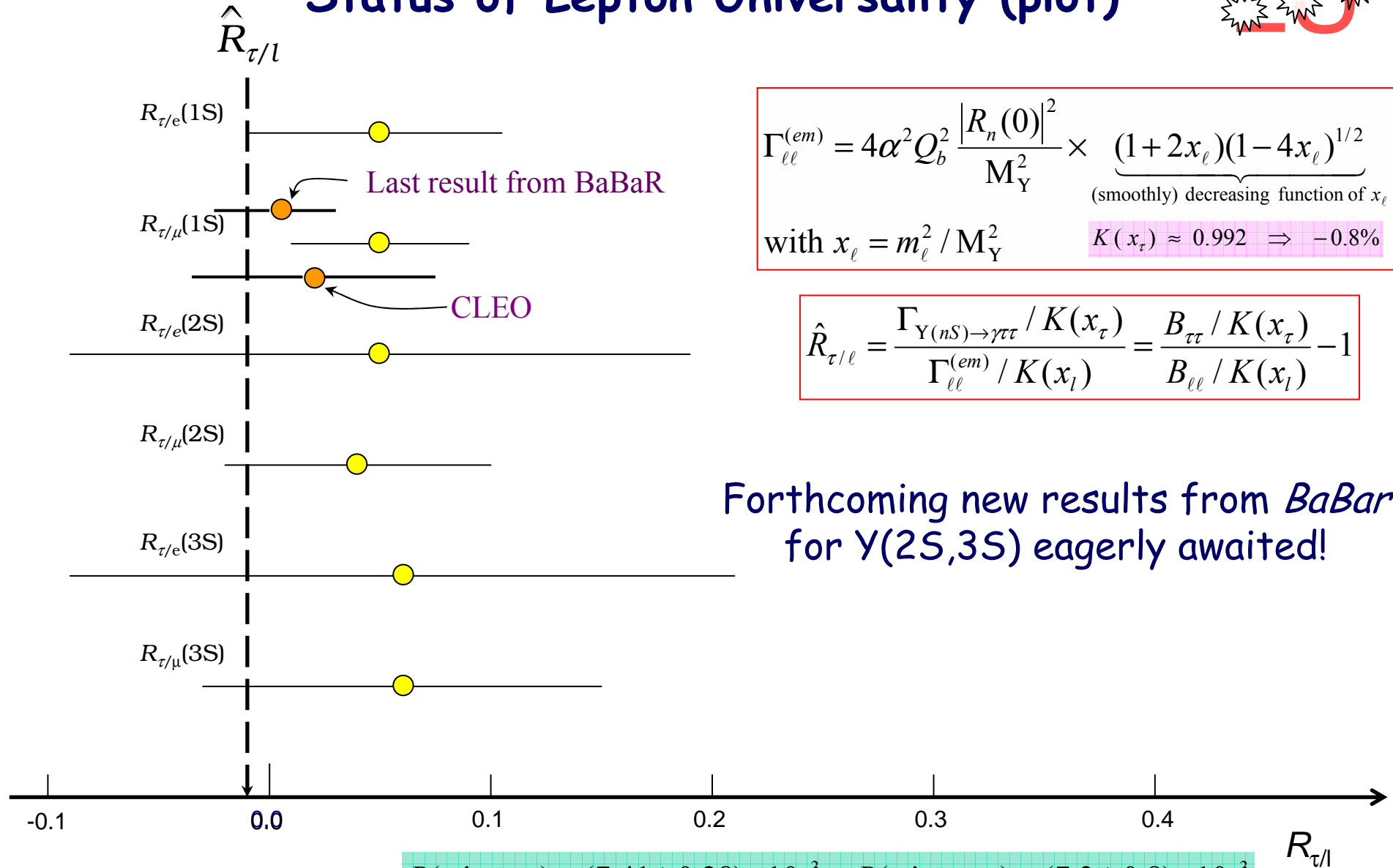
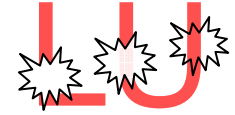
$$\text{BF} [Y \rightarrow e^+ e^-] = \text{BF} [Y \rightarrow \mu^+ \mu^-] = \text{BF} [Y \rightarrow \tau^+ \tau^-]$$

Channel	$BF [e^+ e^-]$	$BF [\mu^+ \mu^-]$	$BF [\tau^+ \tau^-]$	$R_{\tau/e}$	$R_{\tau/\mu}$
$\Upsilon(1S)$	$2.48 \pm 0.11 \%$	$2.48 \pm 0.05 \%$	$2.62 \pm 0.10 \%$	0.05 ± 0.06	0.05 ± 0.04
$\Upsilon(2S)$	$1.91 \pm 0.16 \%$	$1.93 \pm 0.17 \%$	$2.01 \pm 0.21 \%$	0.05 ± 0.14	0.04 ± 0.06
$\Upsilon(3S)$	$2.18 \pm 0.21 \%$	$2.18 \pm 0.21 \%$	$2.30 \pm 0.30 \%$	0.06 ± 0.16	0.06 ± 0.09

$$R_{\tau/\ell} = \frac{\Gamma_{Y(nS) \rightarrow \gamma_s \tau\tau}}{\Gamma_{\ell\ell}^{(em)}} = \frac{B_{\tau\tau} - B_{\ell\ell}}{B_{\ell\ell}} = \frac{B_{\tau\tau}}{B_{\ell\ell}} - 1$$

Lepton Universality in
Upsilon decays implies $\langle R_{\tau/\ell} \rangle = 0$
(actually -0.08)

Status of Lepton Universality (plot)

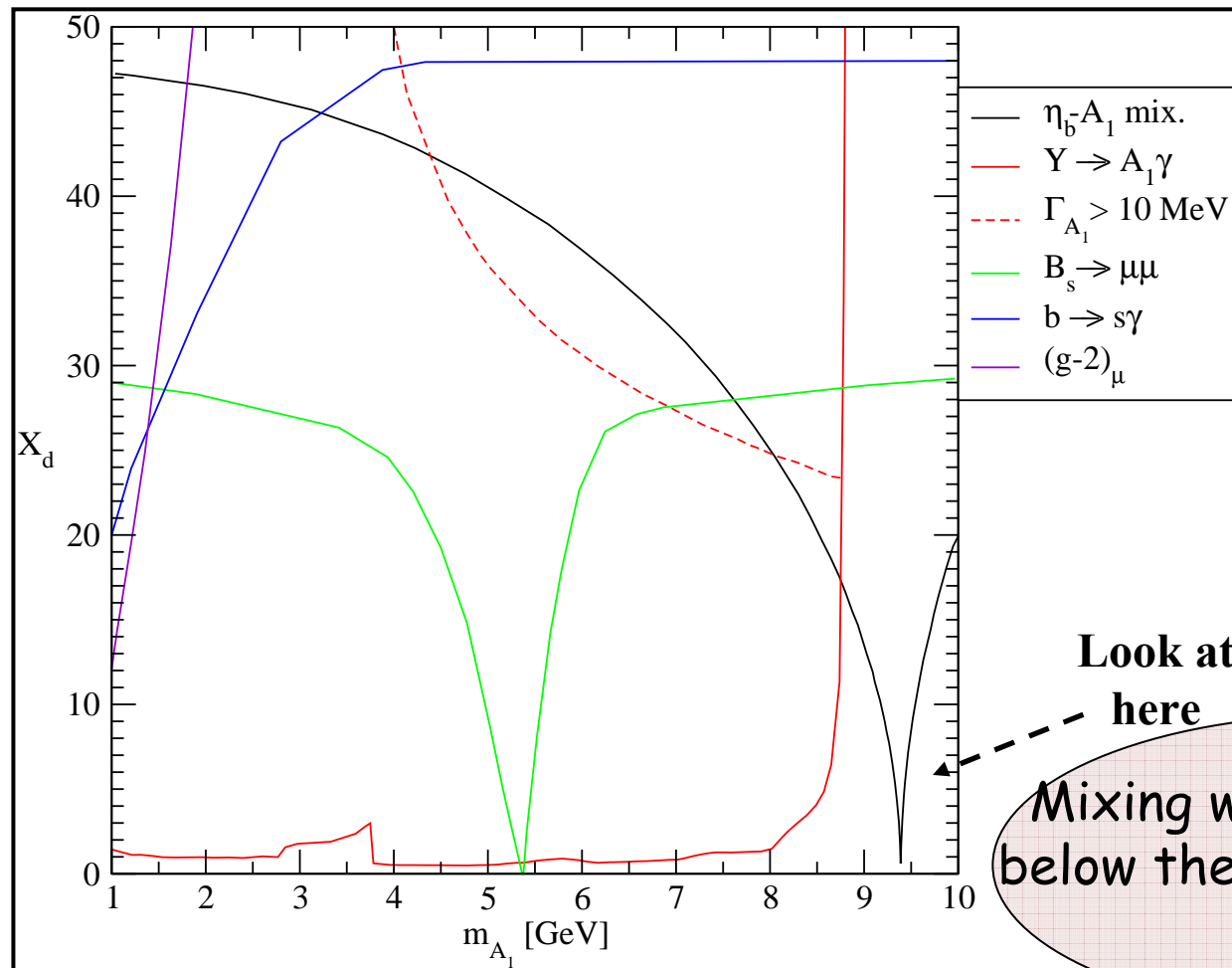


For charmonium

$$B(\psi' \rightarrow ee) = (7.41 \pm 0.28) \times 10^{-3} \approx B(\psi' \rightarrow \mu\mu) = (7.3 \pm 0.8) \times 10^{-3} > B(\psi' \rightarrow \tau\tau) = (2.8 \pm 0.7) \times 10^{-3}$$

Upper bounds for all parameters scanned in the NMSSM

F.Domingo, U. Ellwanger, E. Fullana, C. Hugonie and M.A.S.L., arXiv: 0810.4736



$B_s \rightarrow \mu\mu$ puts limits
about the B_s mass

CLEO, BaBar searches for
 $Y \rightarrow \gamma A_1$
puts stringent limits
for $m_{A_1} < 9 \text{ GeV}$

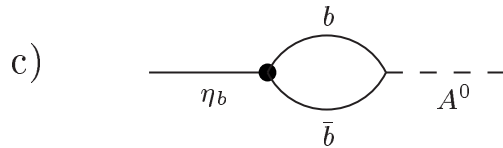
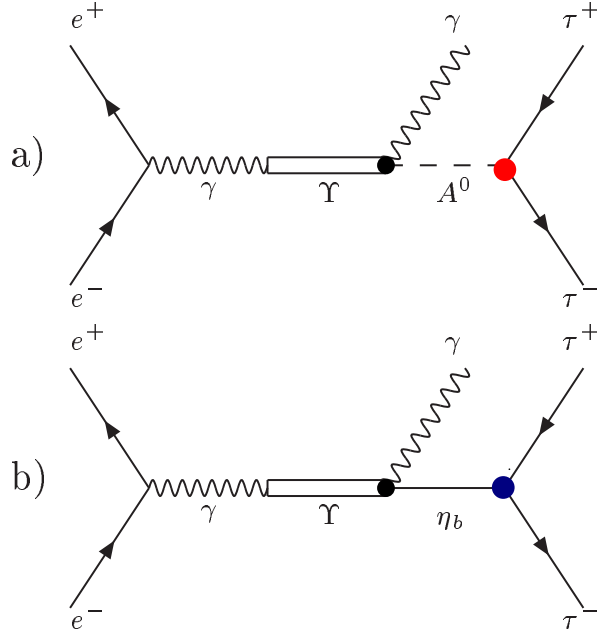
BaBar discovery
of $\eta_b(1S)$
puts limits about 9.4 GeV

Look at
here

Mixing with η_b resonances
below the b - \bar{b} threshold
can occur

Mixing of a pseudoscalar Higgs A_1 and a η_b resonance

$$e^+ e^- \rightarrow \Upsilon \rightarrow \gamma \tau^+ \tau^-$$



$$\delta m^2 \approx \left(\frac{3m_{\eta_b}^3}{4\pi v^2} \right)^{1/2} |R_{\eta_b}(0)| \times X_d \quad \sin 2\alpha \approx \delta m^2$$

Drees & Hikasa
PRD 41 (1990) 1547

hep-ph/0702190

$$\mathbf{M}^2 = \begin{pmatrix} m_{A_{10}}^2 - im_{A_{10}} \Gamma_{A_{10}} & \delta m^2 \\ \delta m^2 & m_{\eta_{b0}}^2 - im_{\eta_{b0}} \Gamma_{\eta_{b0}} \end{pmatrix}$$

$$A_1 = \cos \alpha A_{10} + \sin \alpha \eta_{b0}$$

$$\eta_b = \cos \alpha \eta_{b0} - \sin \alpha A_{10}$$

$$g_{A^0 \tau \tau} = \cos \alpha g_{A_{10}^0 \tau \tau} + \sin \alpha g_{\eta_{b0} \tau \tau}$$

$$g_{\eta_b \tau \tau} = \cos \alpha g_{\eta_{b0} \tau \tau} - \sin \alpha g_{A_{10}^0 \tau \tau}$$

A_{10}, η_{b0}
unmixed states

A_1, η_b
mixed (physical)
states

The η_b decays to leptons because of its mixing with the CP-odd Higgs

$$\Gamma_{A^0} = |\cos \alpha|^2 \Gamma_{A_{10}^0} + |\sin \alpha|^2 \Gamma_{\eta_{b0}}$$

$$\Gamma_{\eta_b} = |\cos \alpha|^2 \Gamma_{\eta_{b0}} + |\sin \alpha|^2 \Gamma_{A_{10}^0}$$

Resonant and non-resonant decays with $\eta_b(nS) - A_1$ mixing

The “Higgs” is to be **produced** through the **A_1 - components of the mixed states** no matter which production mechanism is considered.

In turn, the **decay** of physical pseudoscalar states into taus should also take place via their **A_1 - components**.

Non-resonant

$$R_{\tau/\ell} = R_{\tau/\ell}^{A_1} + R_{\tau/\ell}^{\eta_b}$$

$$R_{\tau/\ell} = \frac{B[Y(nS) \rightarrow \gamma A_1]}{B[Y(nS) \rightarrow \ell^+ \ell^-]} \times B[A_1 \rightarrow \tau^+ \tau^-] + \frac{B[Y(nS) \rightarrow \gamma \eta_b(kS)]}{B[Y(nS) \rightarrow \ell^+ \ell^-]} \times B[\eta_b(kS) \rightarrow \tau^+ \tau^-]$$

Resonant

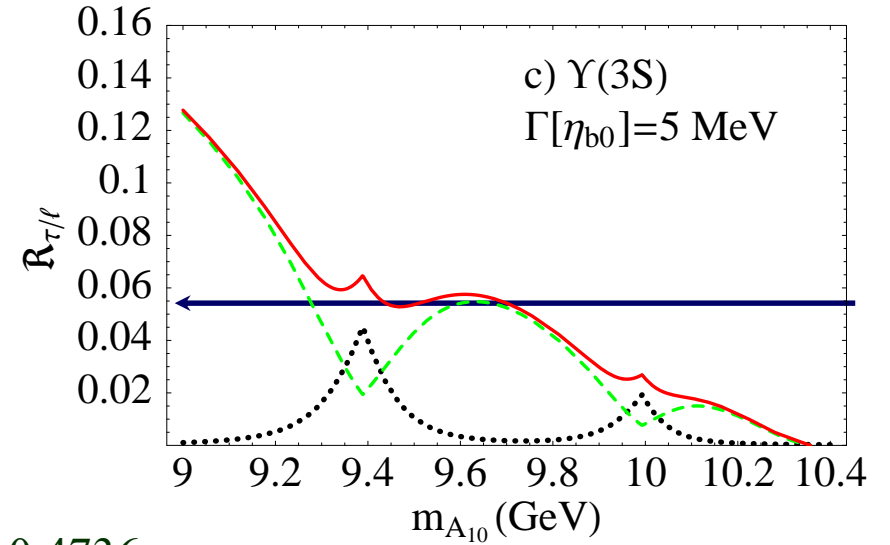
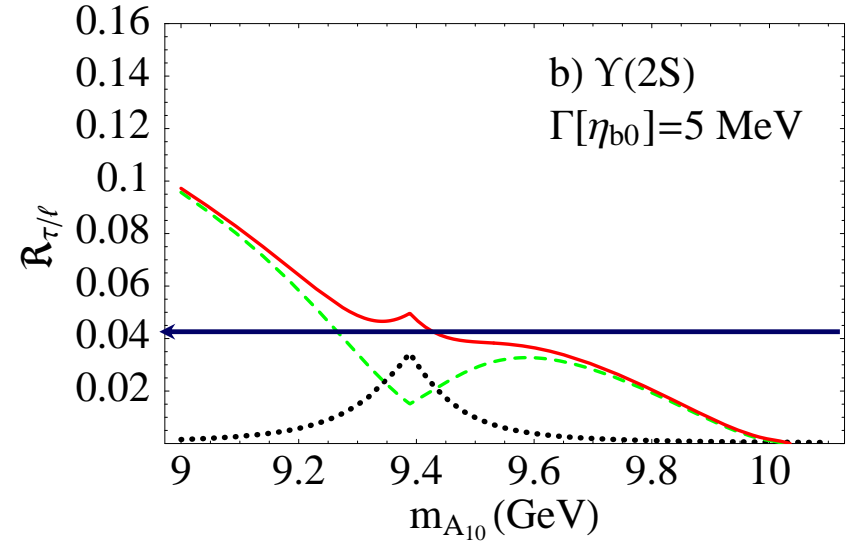
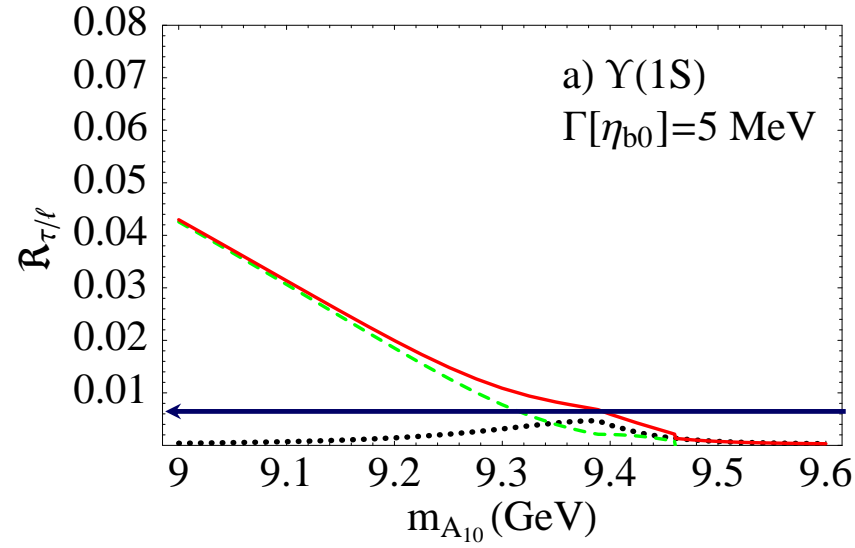
$$B[A_1 \rightarrow \tau\tau] = B[A_{10} \rightarrow \tau\tau] \times \frac{\cos^2 \alpha \Gamma_{A_{10}}}{\cos^2 \alpha \Gamma_{A_{10}} + \sin^2 \alpha \Gamma_{\eta_{b0}}}$$

$$B[\eta_b(nS) \rightarrow \tau\tau] = B[A_{10} \rightarrow \tau\tau] \times \frac{\sin^2 \alpha \Gamma_{A_{10}}}{\cos^2 \alpha \Gamma_{A_{10}} + \sin^2 \alpha \Gamma_{\eta_{b0}}}$$

Mixing effect in the decay

Expected LU breaking

$$R_{\tau/\ell}^{non-res} + R_{\tau/\ell}^{res} = R_{\tau/\ell}$$



$$X_d=12, \Gamma_{\eta_{b0}} = 5 \text{ MeV}$$

Green line: non-resonant decay
Black line: resonant decay
Red line: sum

arXiv: 0810.4736

Spectroscopic consequences for the bottomonium family

General mixing matrix

(in collaboration with F. Domingo & U. Ellwanger)

$$\mathcal{M}^2 = \begin{pmatrix} m_{\eta_b^0(1S)}^2 & 0 & 0 & \delta m_1^2 \\ 0 & m_{\eta_b^0(2S)}^2 & 0 & \delta m_2^2 \\ 0 & 0 & m_{\eta_b^0(3S)}^2 & \delta m_3^2 \\ \delta m_1^2 & \delta m_2^2 & \delta m_3^2 & m_A^2 \end{pmatrix} .$$

$$\delta m_1^2 \simeq (0.14 \pm 10\%) \text{ GeV}^2 \times X_d ,$$

$$\delta m_2^2 \simeq (0.11 \pm 10\%) \text{ GeV}^2 \times X_d ,$$

$$\delta m_3^2 \simeq (0.10 \pm 10\%) \text{ GeV}^2 \times X_d .$$

Non-relativistic
calculation

Physical states = (mass) eigenstates of the above matrix

$$\eta_i = P_{i,1} \eta_b^0(1S) + P_{i,2} \eta_b^0(2S) + P_{i,3} \eta_b^0(3S) + P_{i,4} A .$$

$i=1,2,3,4$

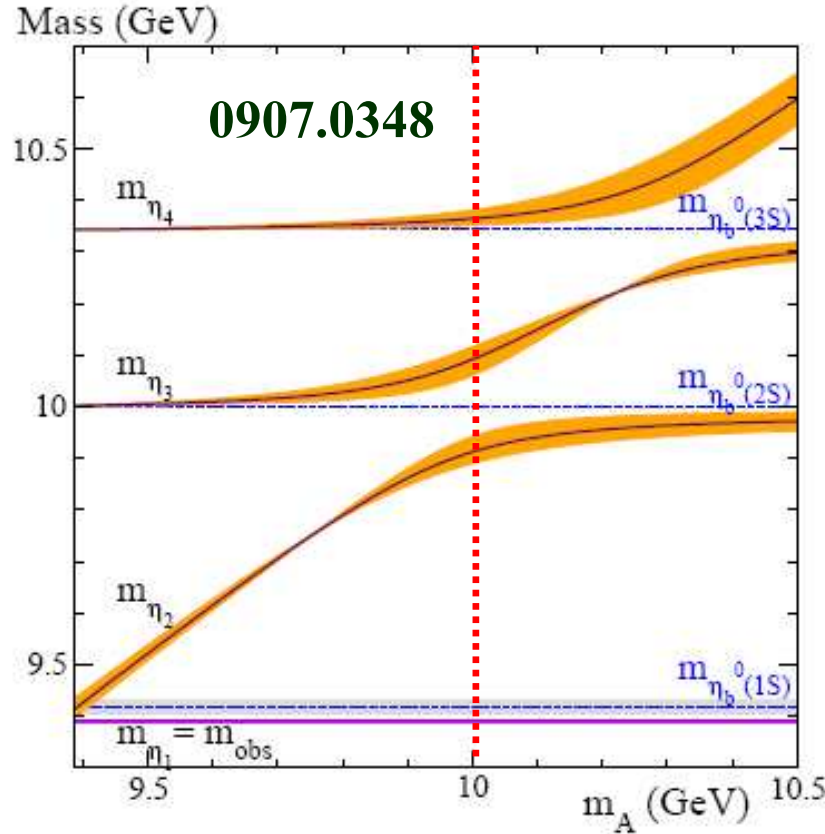
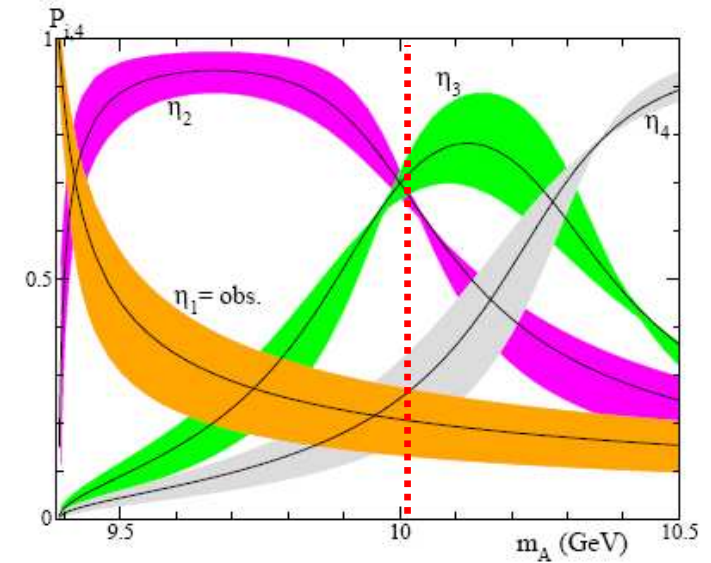


FIG. 2: The masses of all eigenstates as function of m_A .

*Possible scenarios:
deeply entangled with
search strategies*



G. 3: The A -components $|P_{i,4}|$ for all 4 eigenstates as functions of m_A .

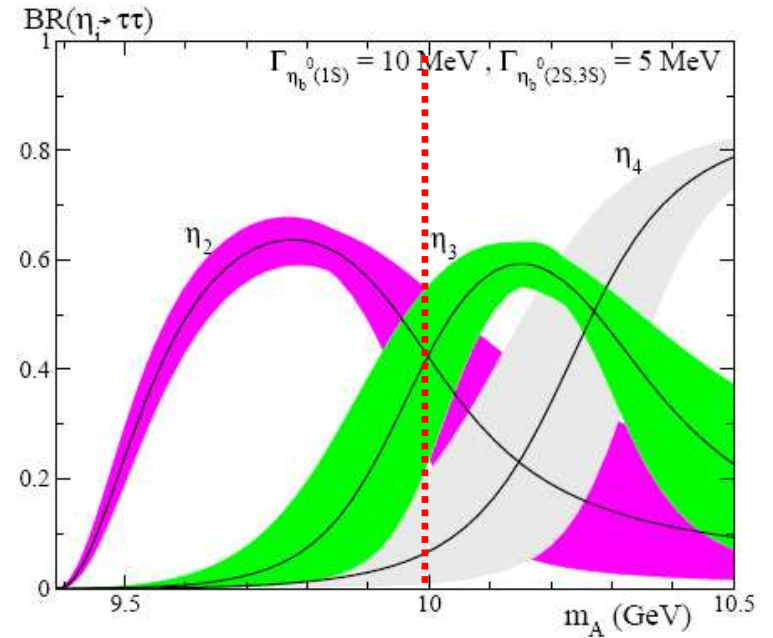


FIG. 4: The branching ratios into $\tau^+ \tau^-$ for the eigenstates η_2 , η_3 and η_4 as functions of m_A .



(Light) Dark Matter @ the NMSSM

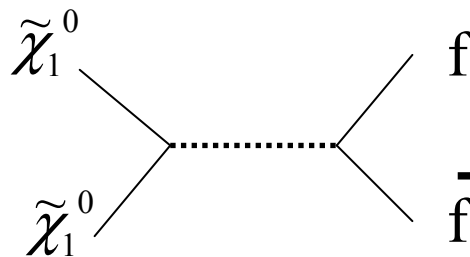
with a singlet component

WIMP candidate = lightest neutralino $\tilde{\chi}_1^0$

J.F. Gunion, D. Hooper, B. McElrath: hep-ph/0509024

For a recent analysis see Das and Ellwanger, [arXiv:1007.1151](#) [hep-ph]

- Efficient annihilation could happen through a **light CP-odd Higgs A_1** yielding the observed relic abundance



However it may eventually lead to an **exceedingly efficient annihilation** if $m_{A_1} \approx 2 m_{\tilde{\chi}}$

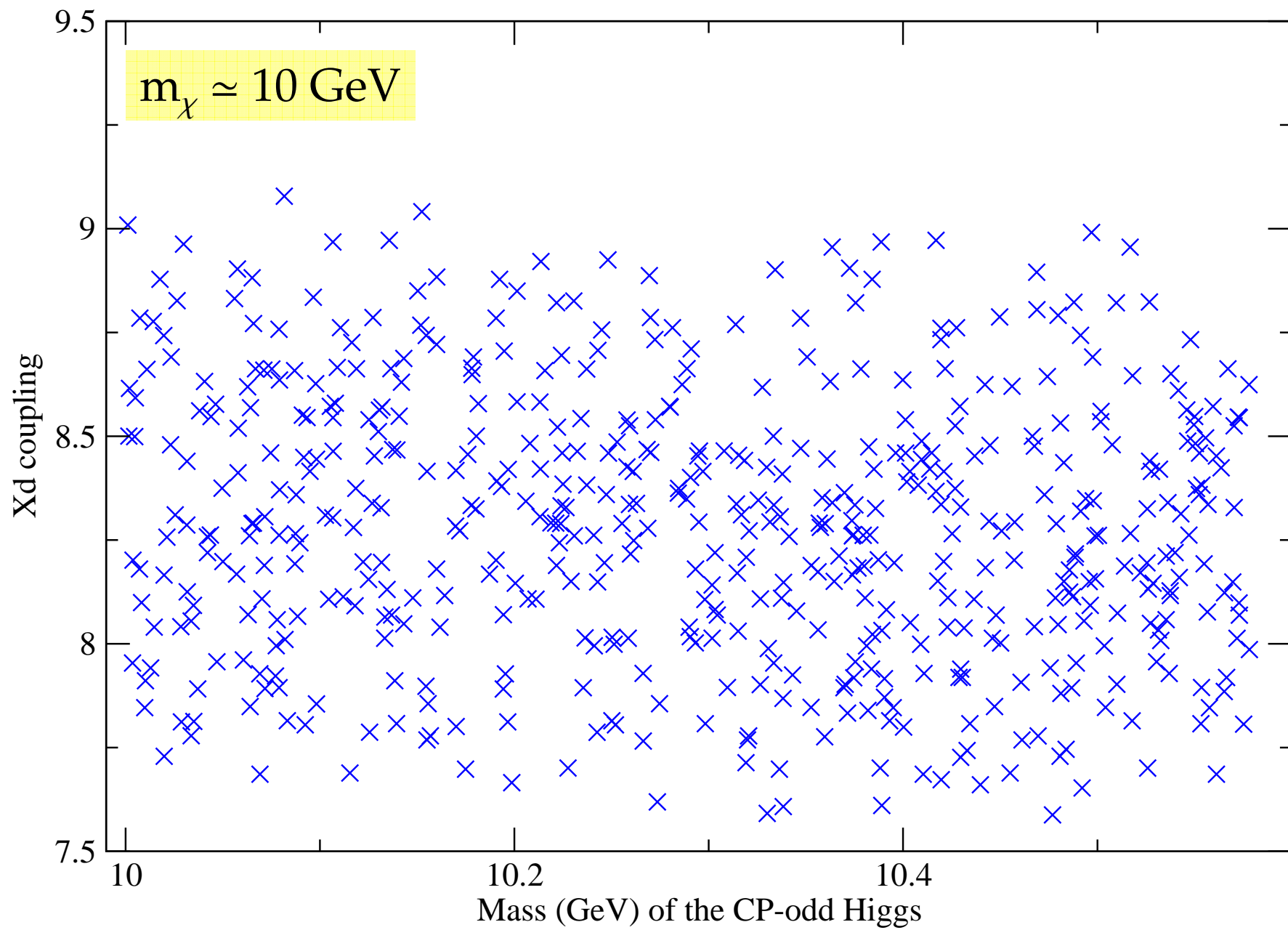
- Scattering off nuclei
 - Spin-independent: through CP-even Higgs exchange
 - Spin-dependent: through Z^0 vector meson exchange

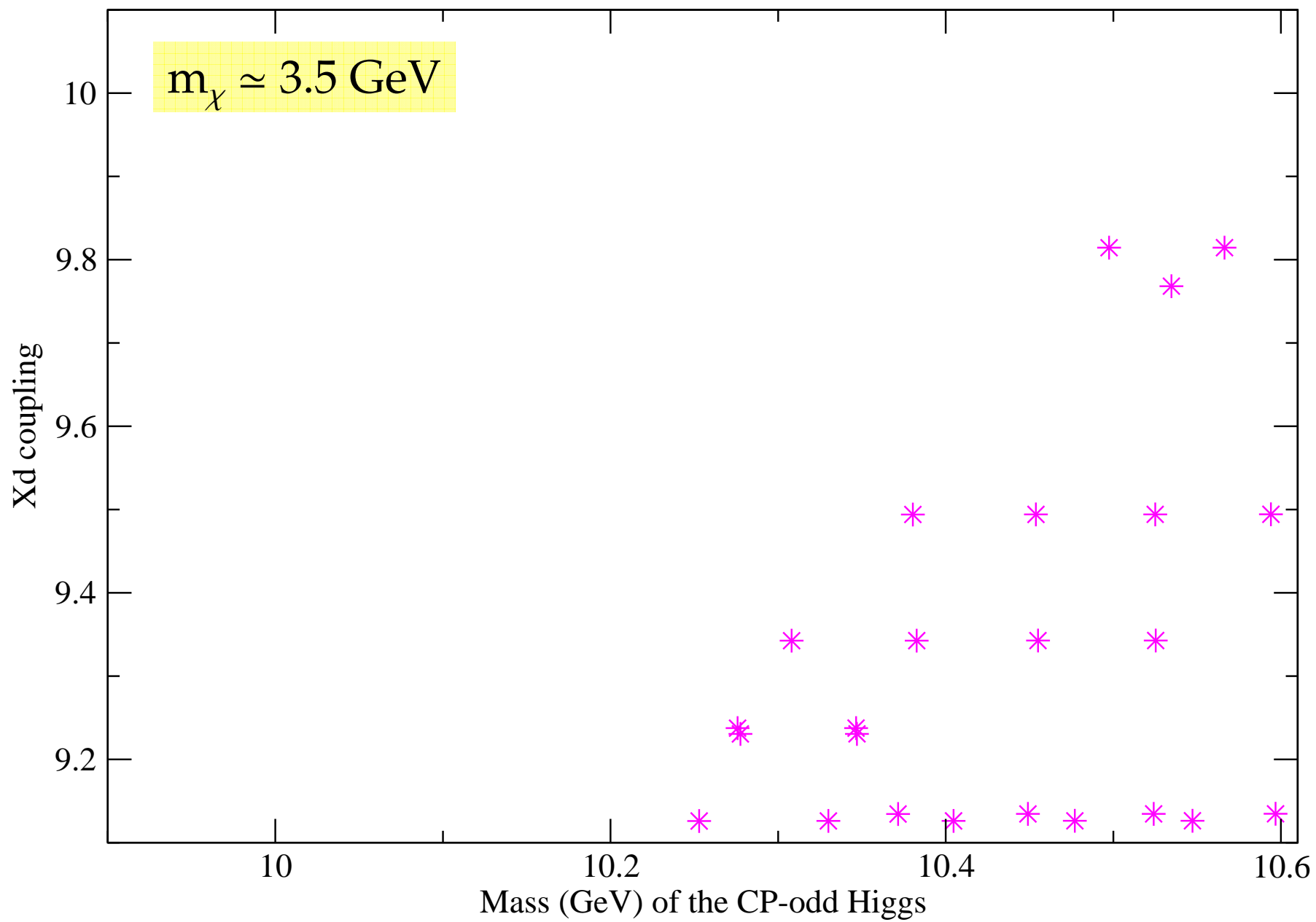
Scan of the NMSSM parameter space

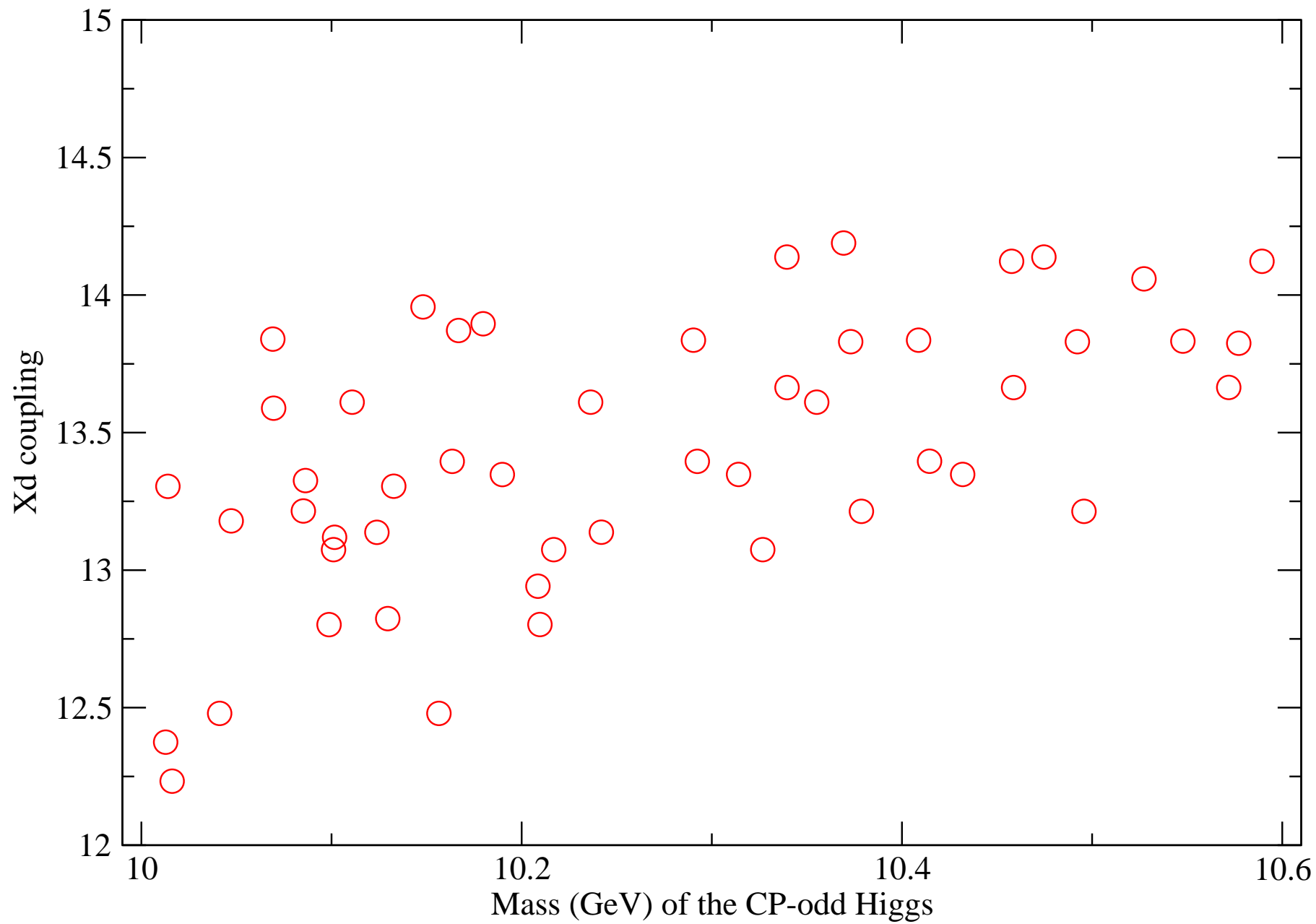
Using **NMSSMTools_2.3.6** (with WMAP bounds on)
(by Ellwanger, Gunion and Hugonie)

There are regions of the parameter space of the NMSSM where the following conditions can be satisfied simultaneously:

- All LEP and B physics bounds
- DM relic abundance (WMAP bounds) for a neutralino mass $\lesssim 10$ GeV
- Mass of the lightest pseudoscalar Higgs A_1 of order of 10 GeV
- coupling of the CP-odd Higgs A_1 to down-type fermions of order 10 implying a sizable lepton universality breaking in Upsilon decays
- The mixing of the A_1 with η_b resonances might change dramatically the analysis of the scattering of neutralinos by nuclei, especially the **spin-dependent cross section** due a **pseudoscalar mediator**
(commonly neglected)

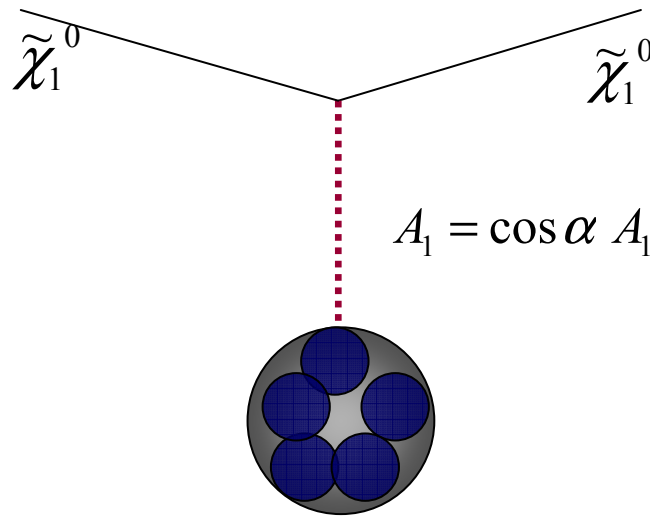






Direct observation of dark matter

WIMP scattering off a nucleus



$$A_1 = \cos \alpha A_{10} + \sin \alpha \eta_{bo}$$

Possible enhancement

$$\text{BF}[\eta_c \rightarrow p \bar{p}] \approx 10^{-3} \quad \text{PDG}$$

Perhaps
substantial coupling
of η_b to nucleons too

EMC nuclear effect 

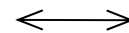
Vector Meson Dominance for the photon:
the physical photon as a superposition of
a bare photon and $\rho, \omega, \phi, \dots$

Pseudoscalar meson dominance
The mediator is a mixing of A_1 and η_b

Spin-dependent interaction 

Velocity suppression factor

$$(v/c)^2 \sim 10^{-6}; \quad v \text{ neutralino velocity}$$



$$(m_b/m_s)^2 \sim 10^2$$

$$(m_Z/m_A)^2 \sim 10^2$$

$g_{\eta_b pp}$ *not small?*

Still negligible contribution (?)

Conclusions

The search for the $\eta_b(2S)$ state(s) by BaBar is *crucial*
to rule out/discover a light CP-odd Higgs
in the range $2m_T < m_{A_1} < 2m_B$ (open window: 9.6-10.5 GeV)

The $\eta_b(2S)$ -like state mass measurement might
yield a hyperfine splitting $m_{Y(2S)} - m_{\eta_b(2S)}$
in disagreement with SM expectations

Test of lepton universality in $Y(2S, 3S)$ decays
should be another hint of NP
LU breaking expectedly larger than for the $Y(1S)$

A light neutralino with mass (GeV) $3 \lesssim m_\chi \lesssim 10$ and coupling $X_d \simeq 8-14$
is viable in a special region of the parameter space of the NMSSM

Physical (mixed) states η_i ($i=1,2,3,4$) might modify
the coupling of neutralinos to ordinary matter
(affecting annihilation and scattering cross sections)

Back-up

Next-to-Minimal Supersymmetric Standard Model (NMSSM)

A new singlet superfield is added to the Higgs sector: $\hat{H}_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}, \quad \hat{H}_d = \begin{pmatrix} H_d^+ \\ H_d^0 \end{pmatrix}, \quad \hat{S}$
 In general more extra SM singlets can be added: [hep-ph/0405244](#)

The μ -problem of the MSSM would be solved by introducing in the superpotential the term

$$W_{Higgs} = \lambda \hat{S} (\hat{H}_u \hat{H}_d) + \frac{\kappa}{3} \hat{S}^3 \Rightarrow V_{soft} = \lambda A_\lambda S (H_u \circ H_d) + \frac{\kappa}{3} A_\kappa S^3 + h.c.$$

Spontaneous breaking of the PQ symmetry Breaks explicitly the PQ symmetry

where $\mu = \lambda x$, $x = \langle S \rangle = \mu / \lambda$ If $\kappa = 0 \rightarrow U(1)$ Peccei-Quinn symmetry

Spontaneous breaking \rightarrow NGB (massless), an “axion” (+QCD anomaly) ruled out experimentally

If the PQ symmetry is not exact but explicitly broken \rightarrow provides a mass to the (pseudo) NGB leading to a light CP-odd scalar for small κ

If λ and κ zero $\rightarrow U(1)_R$ symmetry; if $U(1)_R$ slightly broken \rightarrow a light pseudoscalar Higgs boson too

Higgs sector in the NMSSM: (seven)

- 2 neutral CP-odd Higgs bosons ($A_{1,2}$)
- 3 neutral CP-even Higgs bosons ($H_{1,2,3}$)
- 2 charged Higgs bosons (H^\pm)

The A_1 would be the lightest Higgs:

$$M_{A_1}^2 \cong -3 \left(\frac{\kappa}{\lambda} \right) A_\kappa \mu$$

Favored decay mode: $H_{1,2} \rightarrow A_1 A_1$
 hard to detect at the LHC [\[hep-ph/0406215\]](#)

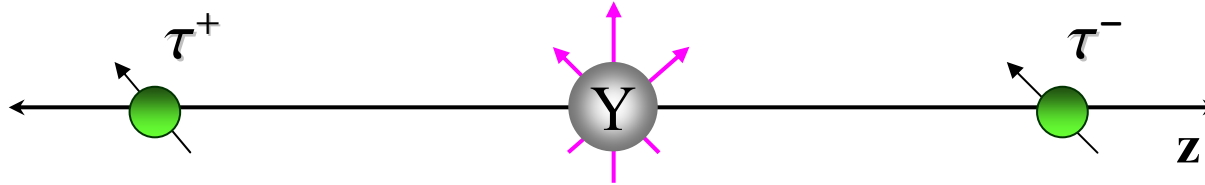
$$A_1 = \cos \theta_A A_{MSMS} + \sin \theta_A A_s$$

Coupling of A_1 to down type fermions:

$$\propto \frac{m_f^2 v}{x} \delta, \Rightarrow \cos \theta_A \tan \beta \quad [\text{hep-ph/0404220}]$$

$$\cos^2 \theta_A \cong \frac{v^2}{x^2 \tan^2 \beta} \delta^2, \quad \delta = \frac{A_\lambda - 2\kappa x}{A_\lambda + \kappa x}$$

Leptonic decay mode: $Y(nS) \rightarrow \tau^+ \tau^-$ vs $Y(nS) \rightarrow \mu^+ \mu^-$



- For transverse polarization of $Y(nS)$, the helicity of leptons gives no difference
- For longitudinal polarization of $Y(nS)$, **lepton helicity favours the tauonic mode**
(as e.g. in $\pi \rightarrow \mu \nu_\mu$ versus $\pi \rightarrow e \nu_e$)
- **Phase space favours the muonic decay mode**

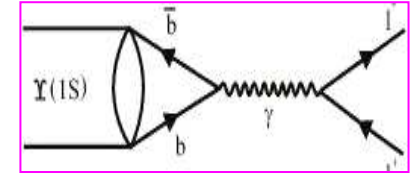
$$\Gamma_{\ell\ell}^{(em)} = 4\alpha^2 Q_b^2 \frac{|R_n(0)|^2}{M_Y^2} \times \underbrace{(1+2x_\ell)(1-4x_\ell)^{1/2}}_{\text{(smoothly) decreasing function of } x_\ell}$$

with $x_\ell = m_\ell^2 / M_Y^2$ $K(x_\ell) \approx (1-6x_\ell)$

For $Y(1S)$:

$$K(x_\tau) \approx 0.992 \Rightarrow -0.8\%$$

Leptonic width of Υ resonances



Lowest Feynman diagram

- Γ_{ll} (as presented in the PDG tables) is an ***inclusive*** quantity:

$\Upsilon \rightarrow l^+ l^-$ is accompanied by an infinite number of soft photons

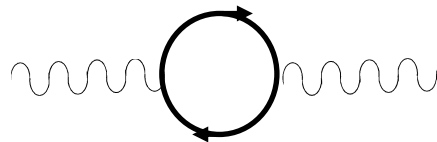
The test of lepton universality can be seen as complementary to searches for a (monochromatic) photon in the $\Upsilon \rightarrow \gamma \tau \tau$ channel

- To order α^3 : $\Gamma_{ll} = \Gamma_{ll}^0 [1 + \delta_{\text{vac}} + \delta_{\text{vertex}}] \sim \Gamma_{ll}^0 [1 + \delta_{\text{vac}}]$

$$3\alpha/4\pi \sim 0.17\%$$

$$7.6\%$$

$$\delta_{\text{vac}} = \delta_{ee} + \delta_{\mu\mu} + \delta_{\tau\tau} + \delta_{\text{quarks}}$$



Warning!

Contribution potentially dangerous for testing lepton universality if **final-state radiation is not properly taken into account in the MC to obtain the detection efficiency** in the analysis of experimental data
Albert et al. Nucl. Phys. B 166 (1980) 460

- Divergencies/singularities free at any order: Bloch and Nordsieck theorem & Kinoshita-Sirlin-Lee-Nauenberg theorem

“Requirement” on X_d from the $\eta_b(1S)$ mass measurement

Hyperfine splitting $M_{Y(1S)} - M_{\eta_b(1S)} = 69.9 \pm 3.1$ MeV (BABAR)

Hyperfine splitting $M_{Y(1S)} - M_{\eta_b(1S)} = 42 \pm 13$ MeV (pQCD)

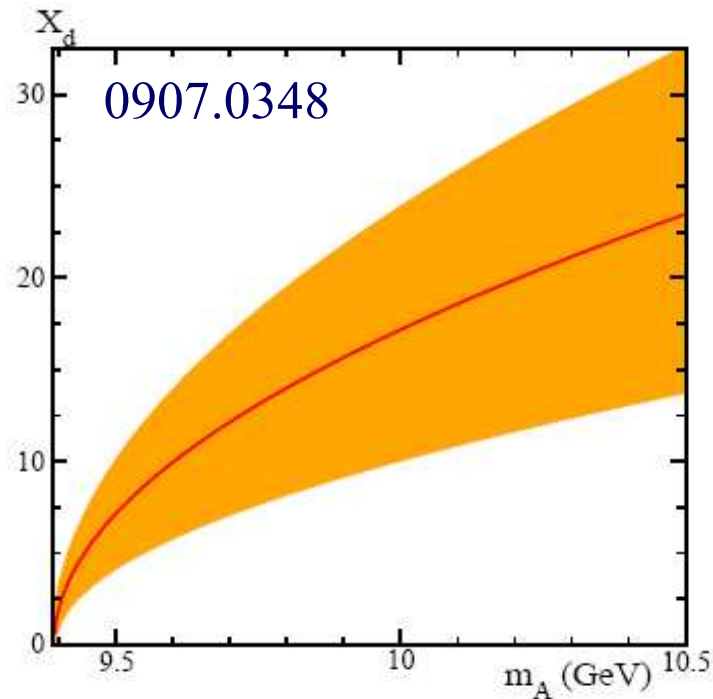


FIG. 1: X_d as a function of m_A (in GeV) such that one eigenvalue of \mathcal{M}^2 coincides with the BABAR result (1).

Resonant and non-resonant decays without mixing

$$R_{\tau/\ell} = \frac{\Gamma_{Y(nS) \rightarrow \gamma_s \tau \tau}}{\Gamma_{\ell\ell}^{(em)}} = \frac{B_{\tau\tau} - B_{\ell\ell}}{B_{\ell\ell}} = \frac{B_{\tau\tau}}{B_{\ell\ell}} - 1$$

QCD+binding energy effects
small for a pseudoscalar A^0
Polchinski, Sharpe and Barnes
Pantaleone, Peskin and Tye
Nason

Leading-order Wilczek formula
with binding-state, QCD + relativistic corrections: $F = \frac{1}{2}$

quite uncertain
especially ~ 9 GeV

- Non-resonant decay

$$R_{\tau/\ell}^{non-res} = \frac{G_F m_b^2 X_d^2}{\sqrt{2} \pi \alpha} \left(1 - \frac{m_{A^0}^2}{m_Y^2} \right) \cdot F$$

- Resonant decay

$$R_{\tau/\ell}^{res} = \frac{B[Y \rightarrow \gamma \eta_b]}{B[Y \rightarrow l^+ l^-]}$$

Wavefunction
overlap

M1 transition probability

$$B(Y \rightarrow \gamma_s \eta_b) = \frac{\Gamma_{Y \rightarrow \gamma \eta_b}^{M1}}{\Gamma_Y} \cong \frac{1}{\Gamma_Y} \times \frac{4\alpha I^2 Q_b^2 k^3}{3m_b^2}$$

Naïve view!

Why should LU be useful to search for a light CP-odd Higgs?

- **Direct observation of monochromatic photons from radiative decays** of Upsilon resonances may not be that easy especially for

$$m_{A_1} \in [9.4, 10.5] \text{ GeV}$$

*As suggested by J. Gunion
hep-ph/0502105*

- The peak in the photon energy spectrum could be **broader than expected**

*also historically employed in
the search for a light Higgs*

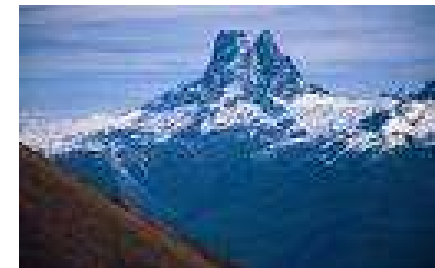
because **two (or more)** peaks resulting from both A_1 and η_b channels
might not be easily disentangled

Naive approach

$$\Upsilon(nS) \rightarrow \gamma A_1 (\rightarrow \tau^+ \tau^-) \quad n, n' = 1, 2, 3$$

$$\Upsilon(nS) \rightarrow \gamma \eta_b (n'S) [\rightarrow A_1^* \rightarrow \tau^+ \tau^-]$$

Cerro dos picos - Argentina



A_1 - η_b mixing yields additional difficulties for exp detection as we shall see! ₂₆

An analogy: the Nile delta



A “naïve” explorer moving across the delta:
The Nile river does not exist!

Dark matter: bounds from B factories

BaBar

$$BF[Y(1S) \rightarrow \text{invisible}] < 3 \times 10^{-4}$$

arXiv:0908.2840 [hep-ex]

scalar mediator

$$BF[Y(3S) \rightarrow \gamma + \text{invisible}] < (0.7 - 31) \times 10^{-6}, \quad m_A < 7.8 \text{ GeV}$$

(pseudo) scalar mediator

arXiv:0808.0017 [hep-ex]

Effort should be put on the search for
light dark matter (e.g. **neutralinos**)
such that

$$2m_\chi \sim m_{A_1} \sim 10 \text{ GeV}$$

$$Y(3S) \rightarrow \gamma A_1 (\rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0)$$

Small photon energy
Detection not that easy!

NOT YET EXCLUDED
by B factories searches