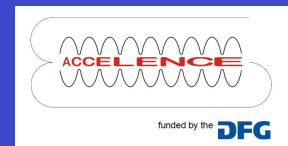


Systematic effects in the beam energy measurements by undulator radiation at MAMI

A1 Collaboration and friends

P.Achenbach
T. Gogami
P.Herrmann
M. Kaneta
Y. Konishi
W.Lauth
S. Nagao
S. Nakamura
J.Pochodzalla
Y. Toyama



Pascal Klag
05.11.2020



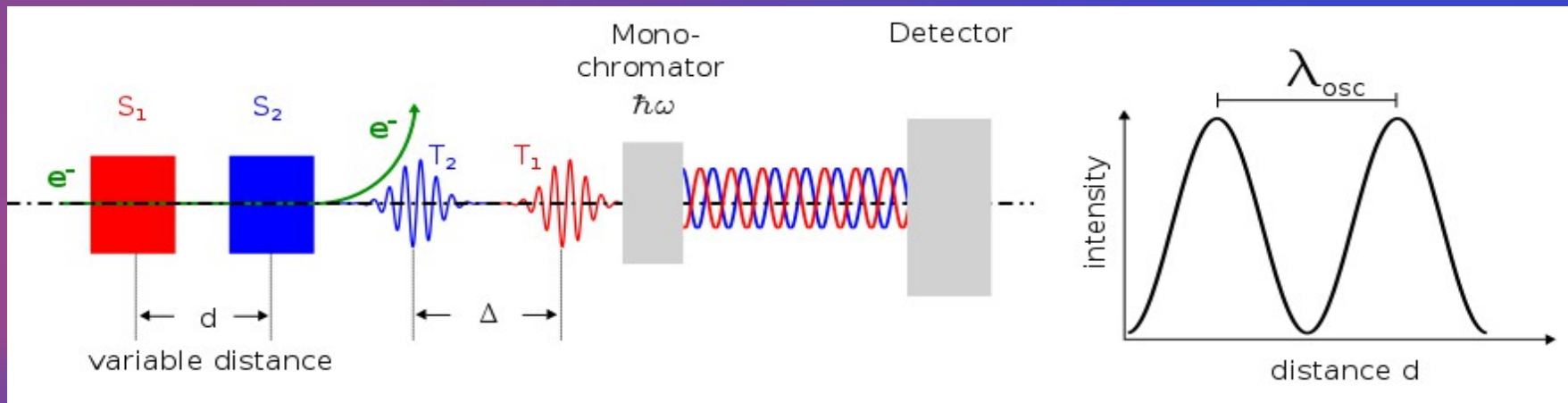
Method

Coherent sources

Wave packets

Monochromatic light

Light intensity of selected wavelength

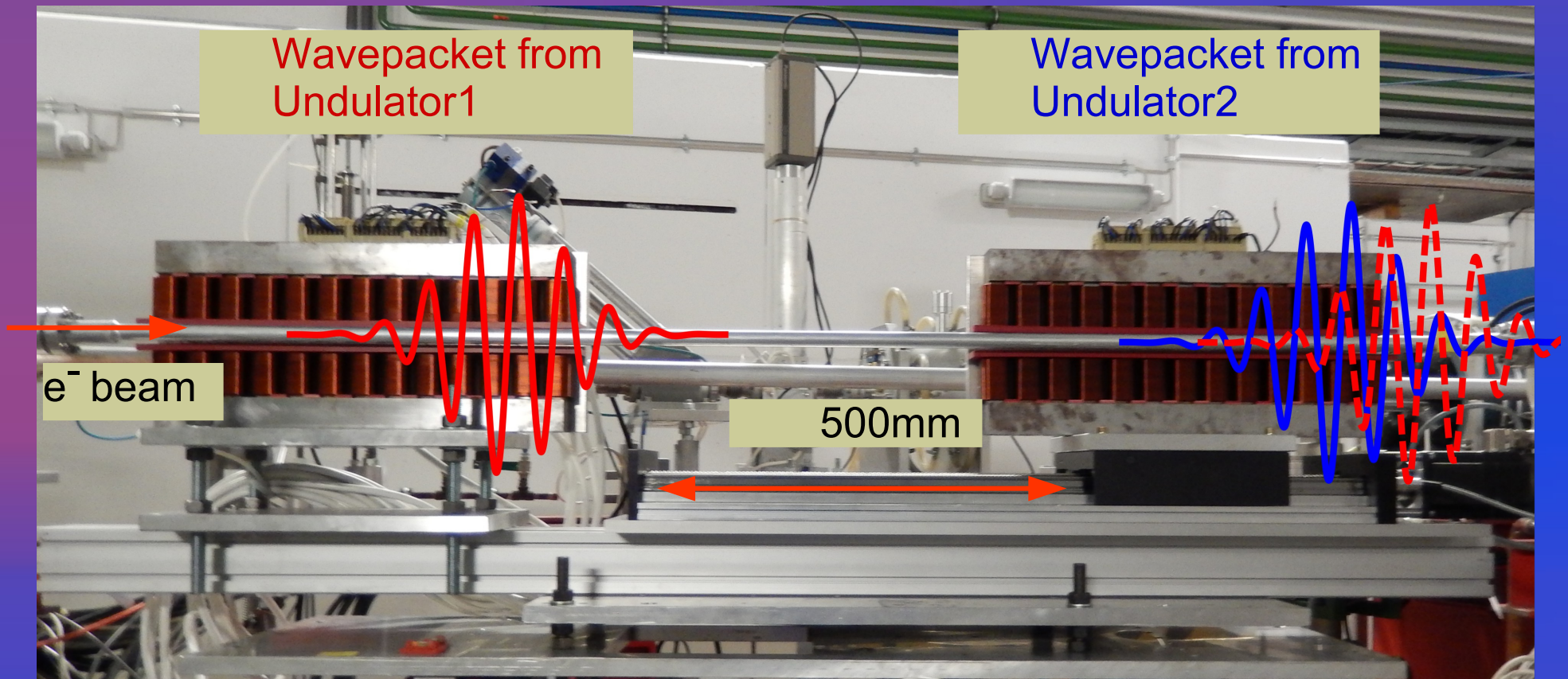


$$\lambda_{osc} = 2 \gamma^2 \lambda_L$$

Example for wavelength and period

$$\left. \begin{array}{l} \lambda_L \approx 400 \text{ nm} \\ \gamma \approx 381, E = 195 \text{ MeV} \end{array} \right\} \lambda_{osc} \approx 116 \text{ mm}$$

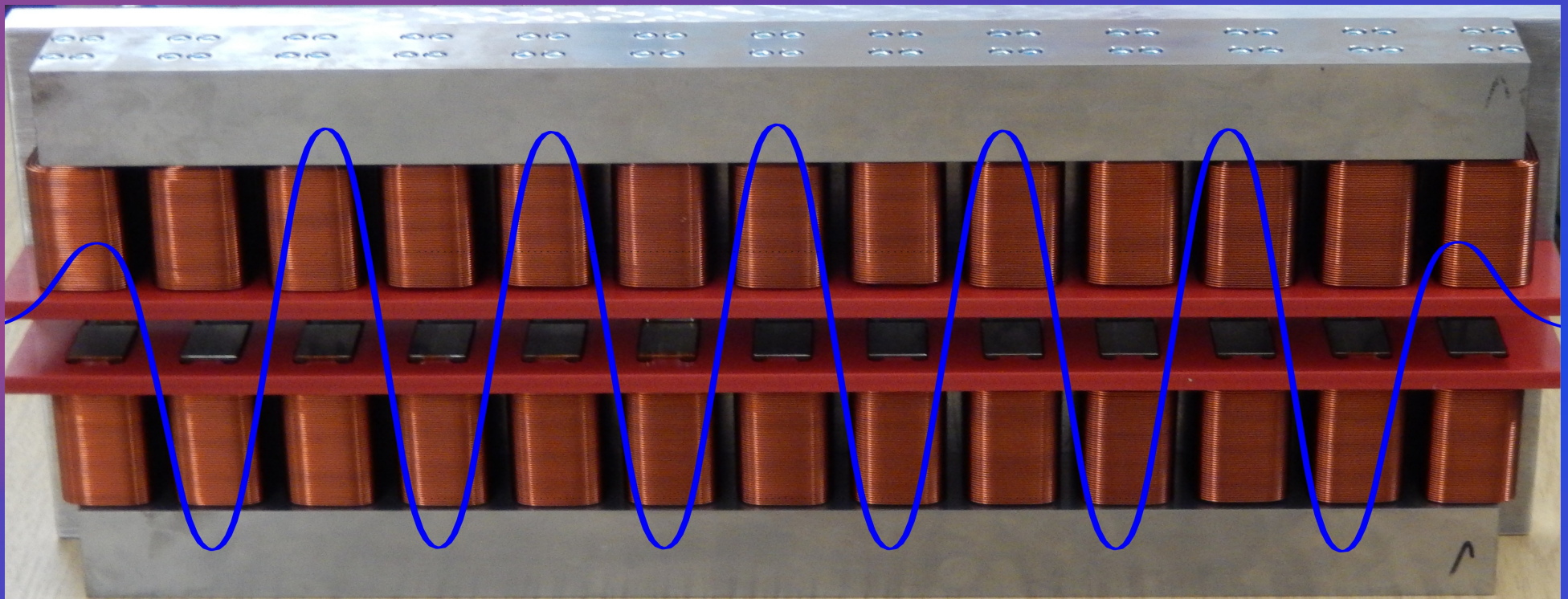
Undulators as sources for coherent radiation (former setup)



To Measure the oscillation period the second undulator is moved by a motorized stage

Undulatorfield

500mm

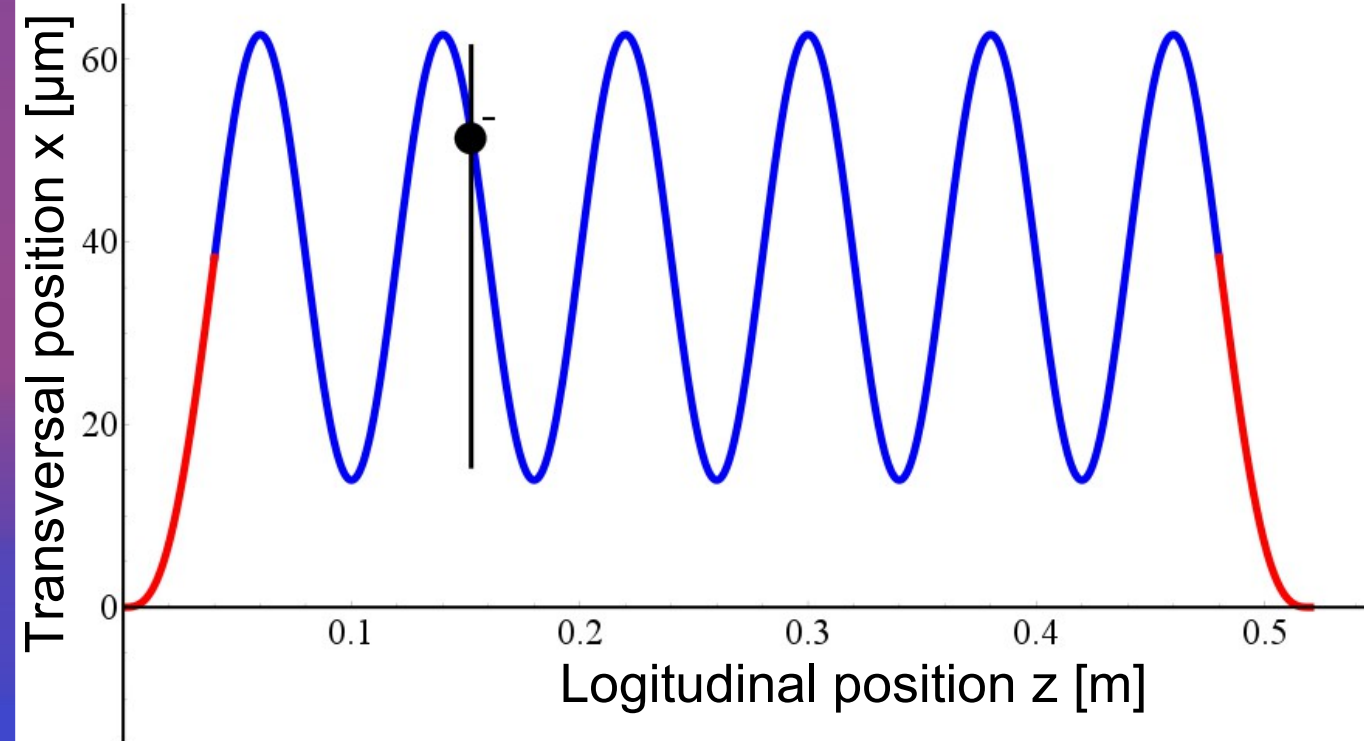


$B = \pm 100 \text{ mT}$

80mm

Undulator period λ_U

Emission of synchrotron radiation



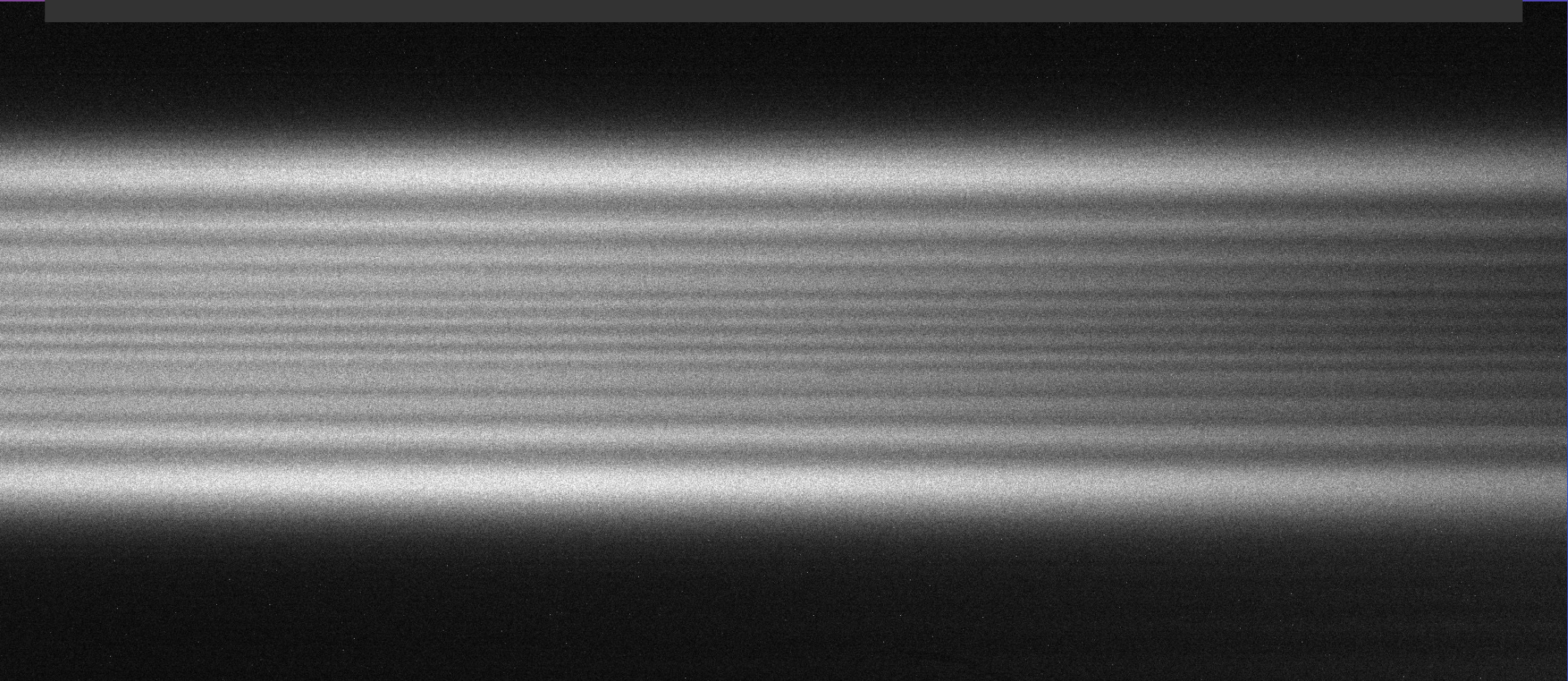
- Electrons oscillate perpendicular to the z -Axis
- The black bar suggests the idea of a high relativistic antenna moving towards the observer
- Emission takes place only in a finite length

Timeline of 2020

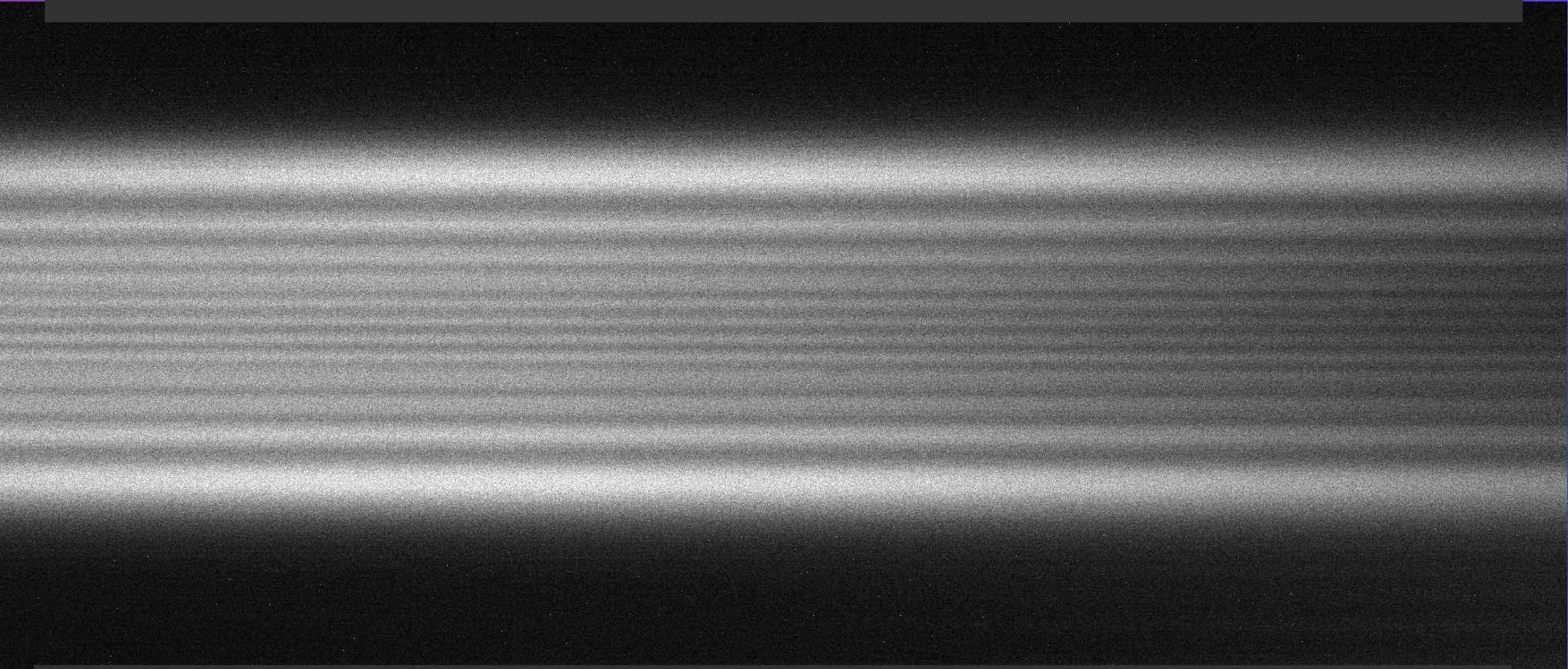
| | | | | |
|------------|--------------------|-----------------|---------------|-----------------------|
| March 2020 | 195 MeV 180 MeV | No regulation | +Spectrometer | MAMI Energy at 195MeV |
| | 180 MeV | With regulation | | |
| June 2020 | 195 MeV | No regulation | | MAMI Energy |
| | 195 MeV | With regulation | | MAMI Energy |

First Time in history of MAMI

Typical Undulator spectrum

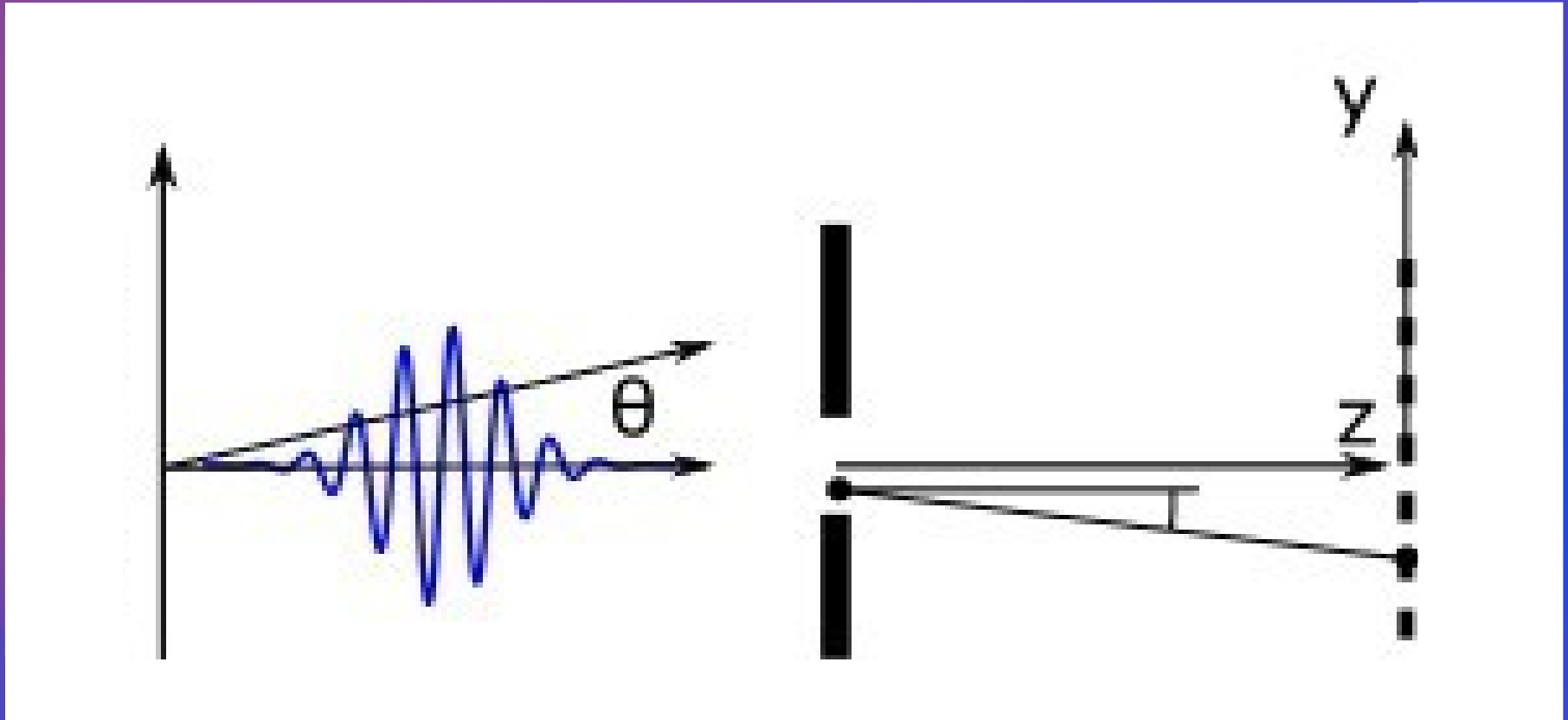


Typical Undulator spectrum

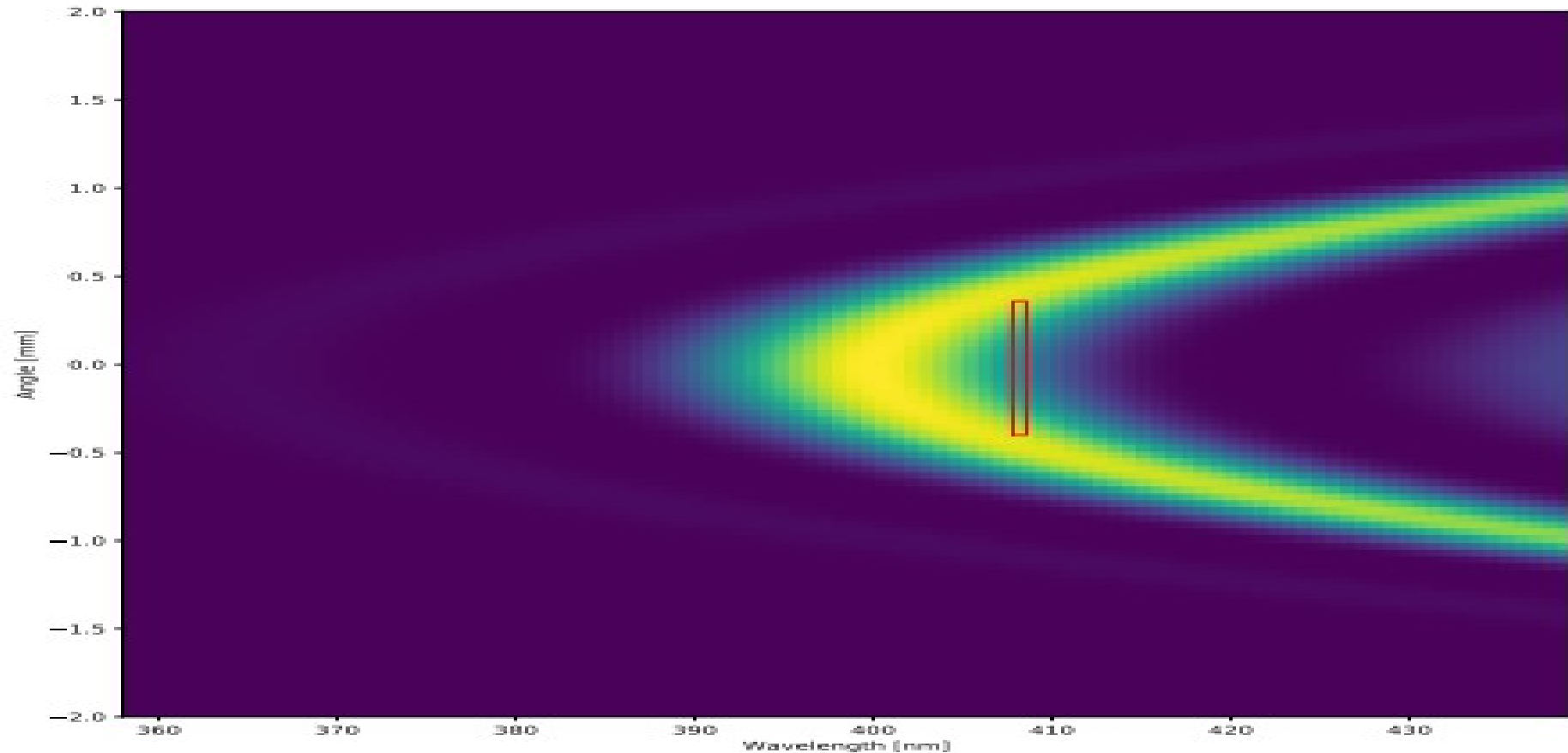


The stripes arise from Fresnel diffraction

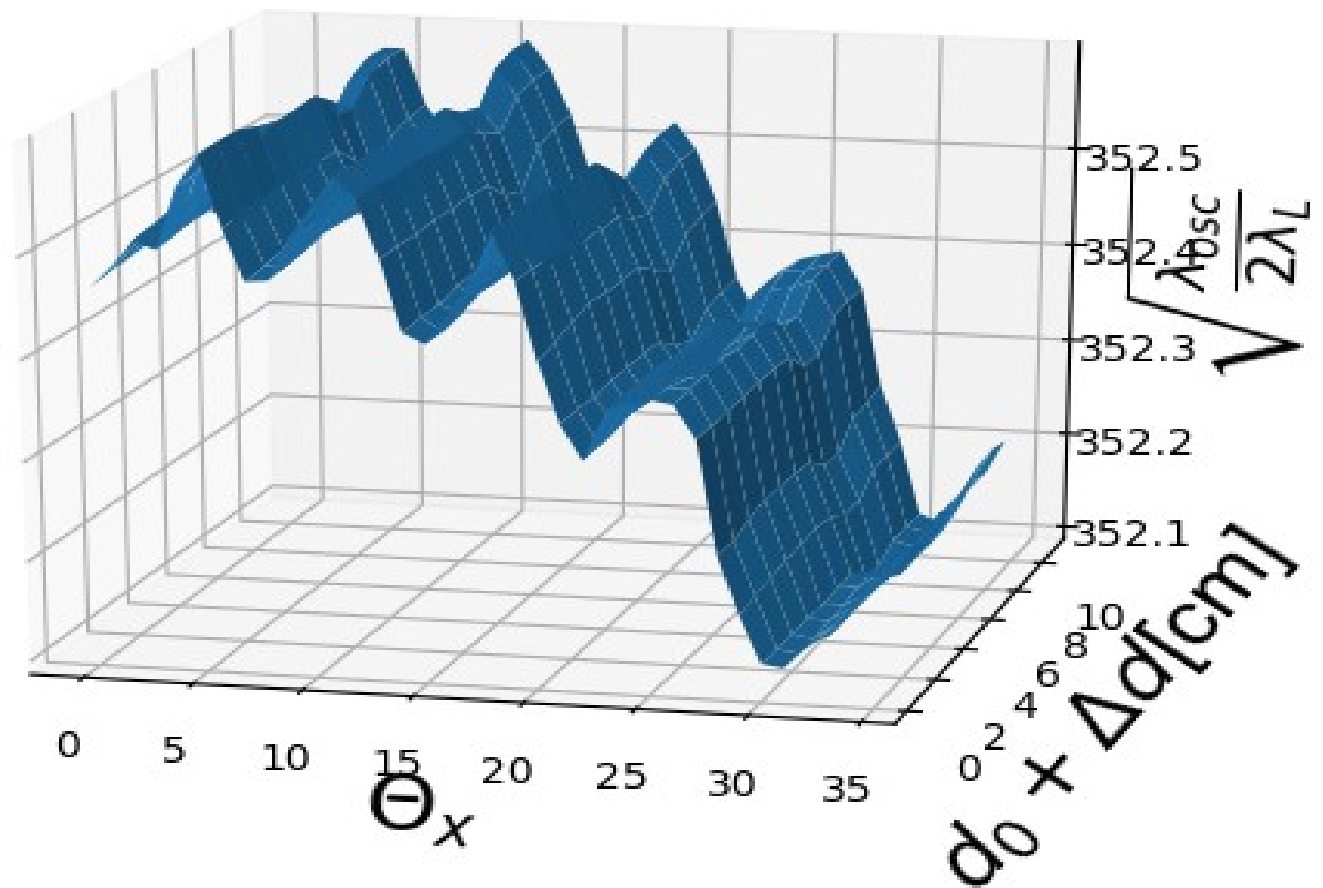
Where diffraction occurs

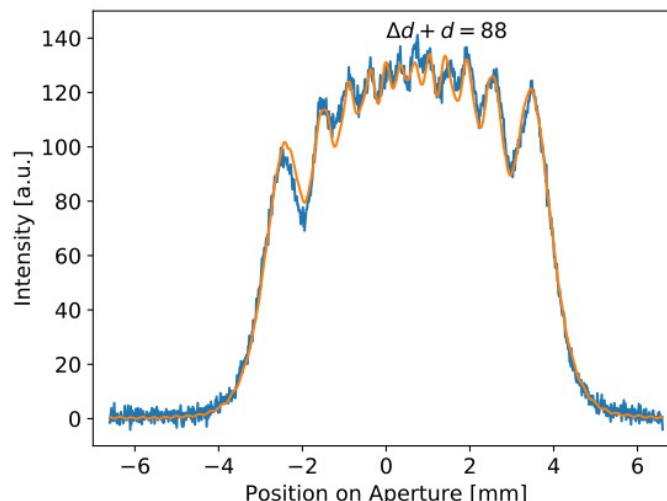
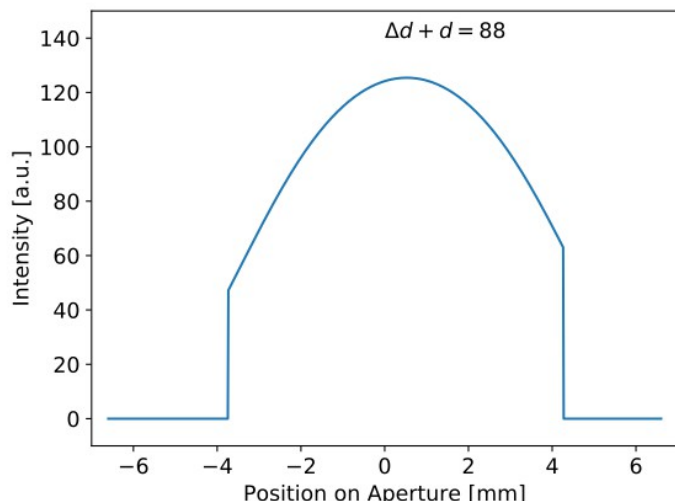
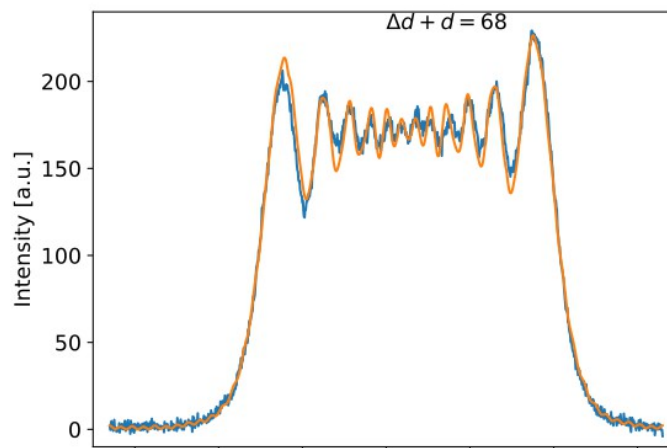
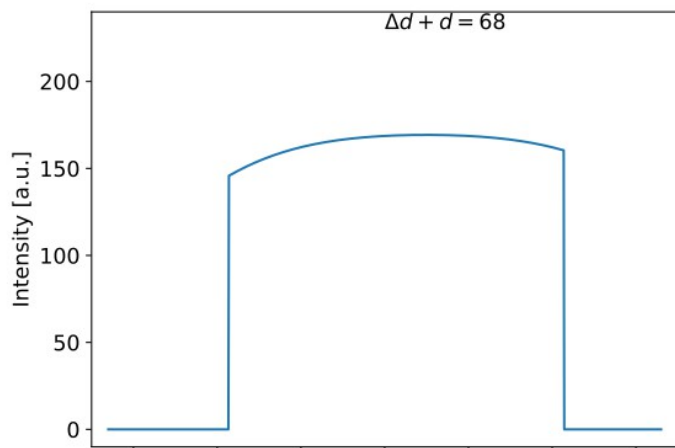
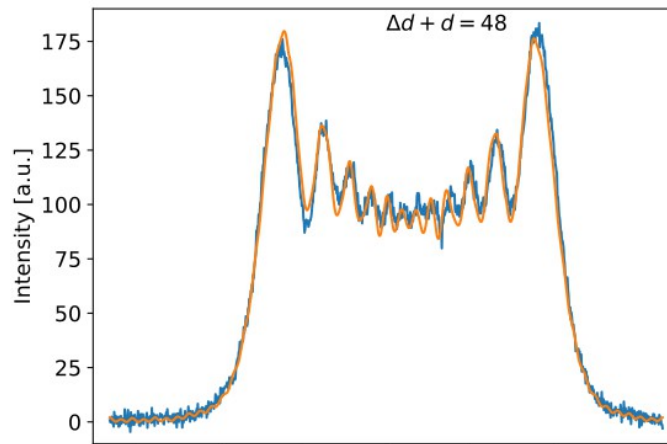
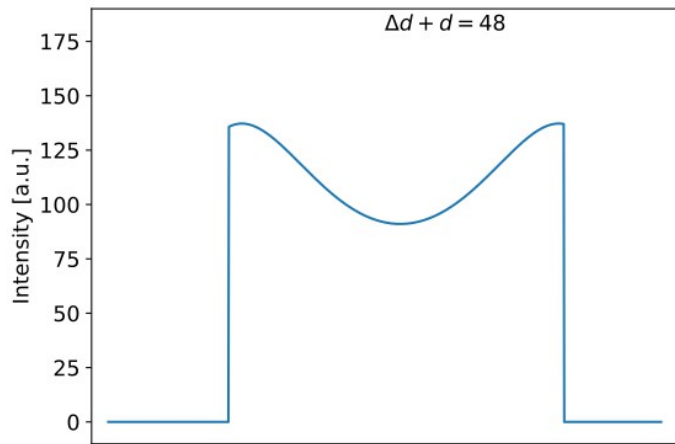


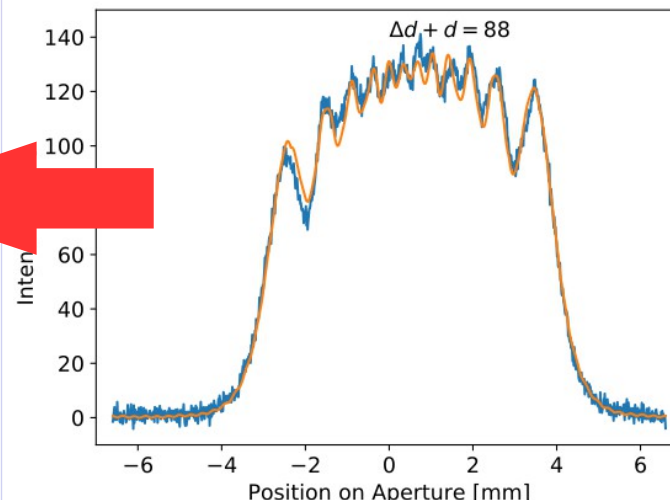
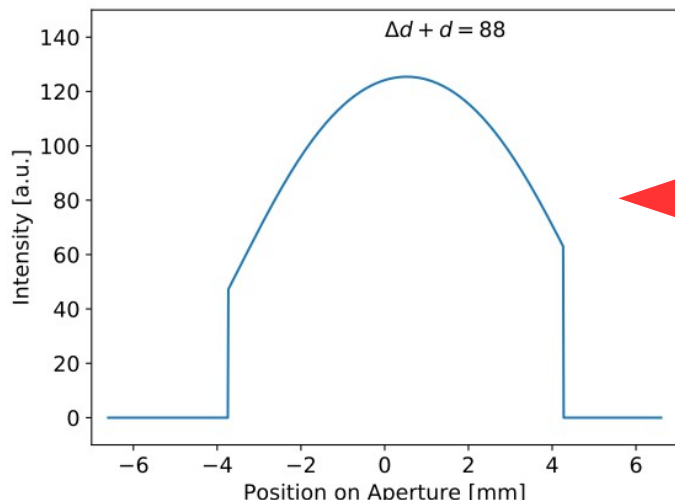
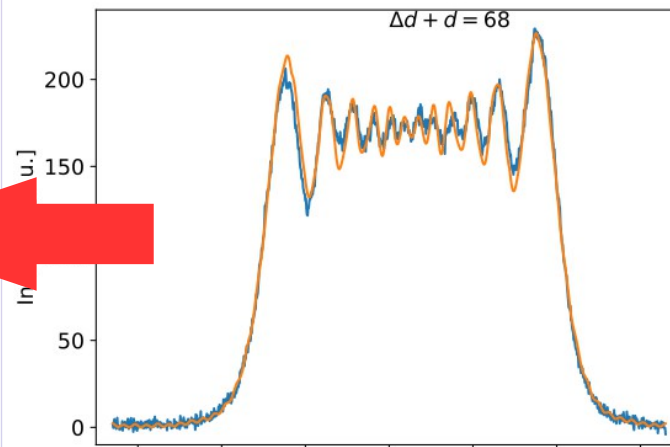
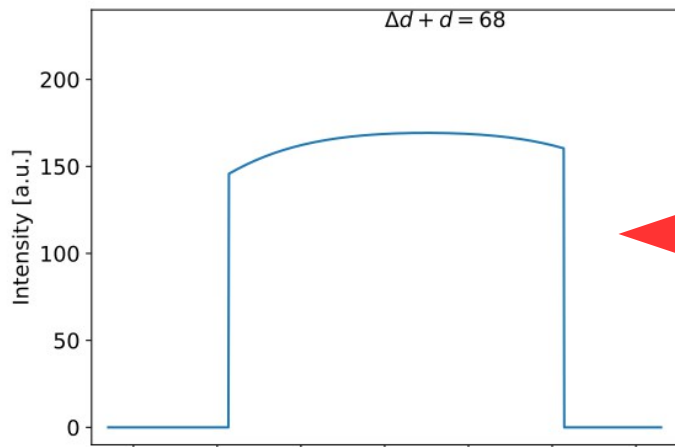
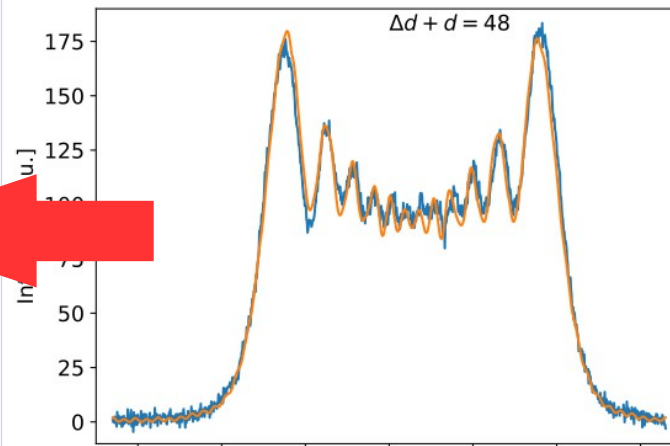
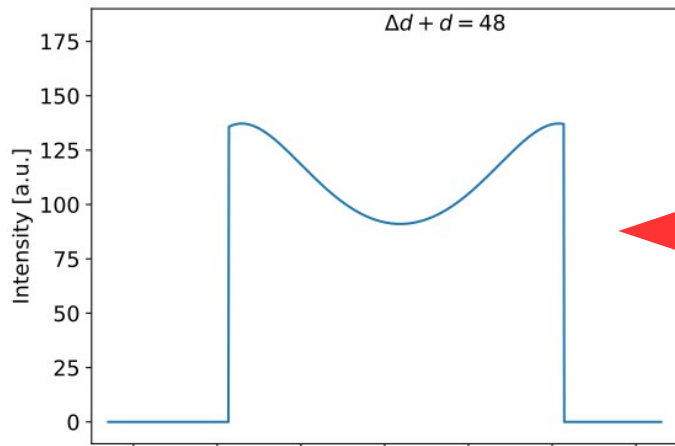
Undulator spectrum no Diffraction



Gamma is affected by the Pattern







Fourier optics

Rayleigh Sommerfeldintegral:

$$E(x', y', z_0) = \iint i \cdot \frac{\cos \theta}{\lambda} \cdot \frac{E(x, y, 0)}{r} e^{ikr} dx dy$$

Spherical wave



Fourier optics

Undulator spectrum
before aperture

$$E(x', y', z_0) = \iint i \cdot \frac{\cos \theta}{\lambda} \cdot \frac{E(x, y, 0)}{r} e^{ikr} dx dy$$

Undulator spectrum after
aperture

Fourier optics in Fresnel approx.

$$E(x', y', z_0) = \iint i \cdot \frac{\cos \theta}{\lambda} \cdot \frac{E(x, y, 0)}{r} e^{ikr} dx dy$$

$$r = \sqrt{z_0^2 + (x - x')^2 + (y - y')^2} \approx z_0 \left(1 + \frac{(x - x')^2}{2z_0^2} + \frac{(y - y')^2}{2z_0^2} \right)$$

With Beam Stabilisation



Without Beam Stabilisation



Thank you for your attention



Extremely small statistical fluctuations

