

Resonance Photoproduction of Pionic Atoms

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Based on: V. V. Flambaum, J. Jin, and D. Budker, [arXiv:2010.06912](https://arxiv.org/abs/2010.06912)

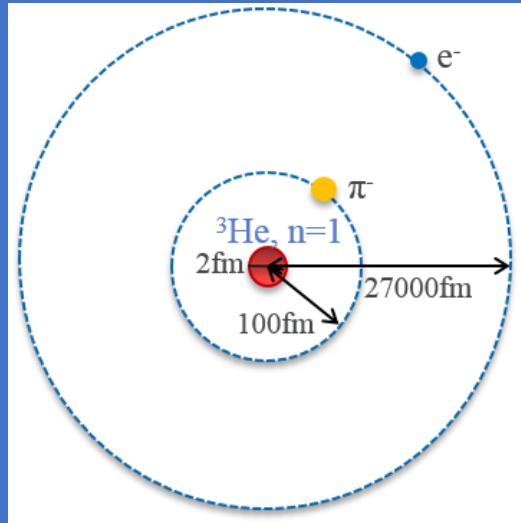
Outline

- **Pionic atoms**
- **Photoproduction cross-sections**
- **Production rates expected at GF**

Pionic atoms

➤ A negative pion orbiting the nucleus

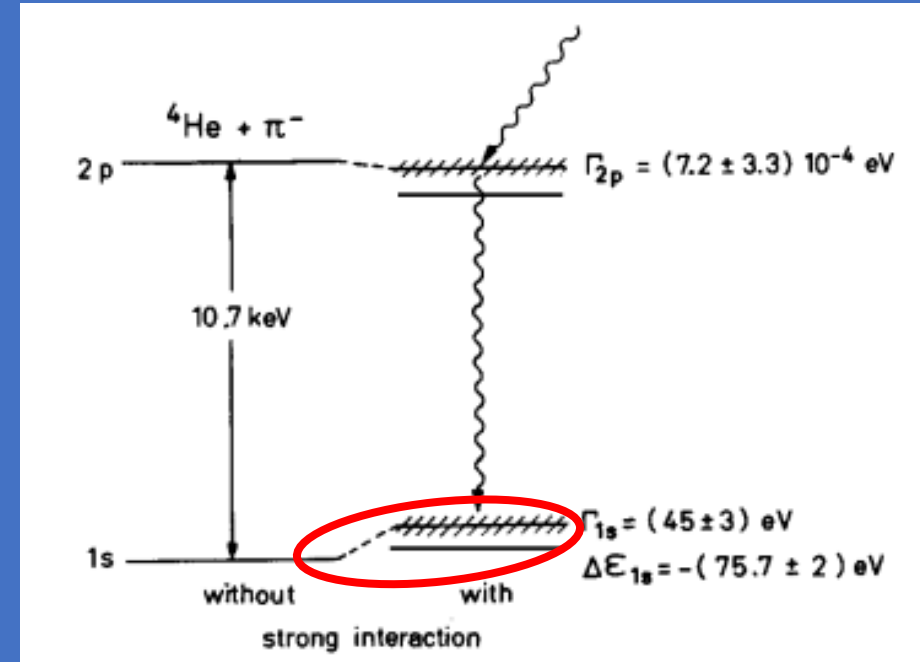
- hydrogen-like system
- $m_\pi c^2 \approx 140 \text{ MeV} \approx 270 m_e c^2$



Spin = 0. Critical charge for point nucleus $Z=68$!
 1s orbital radius is close to nuclear radius for $Z=40$

➤ Strong interaction effects

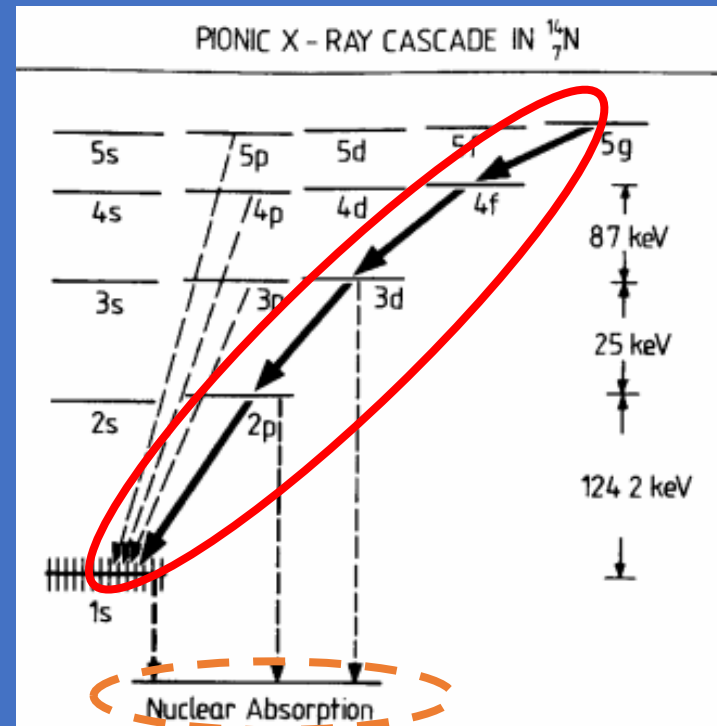
- pion absorption \longrightarrow width broadening
- energy shift *vs.* Coulomb



Methods for producing pionic atoms

➤ Stopping free π^- in a pion beam

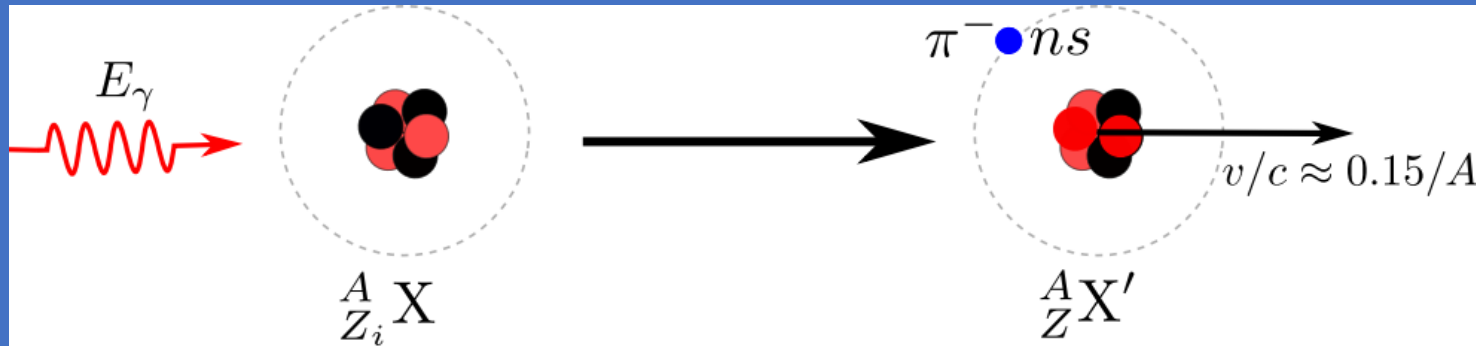
- produce $\sim 10^5$ pionic atoms per sec
- X-ray cascade between “circular” states
- deeply bound states cannot be produced
- population of higher ns states is suppressed



Methods for producing pionic atoms

➤ Our proposal

- resonance photoproduction of bound pions from the nucleus

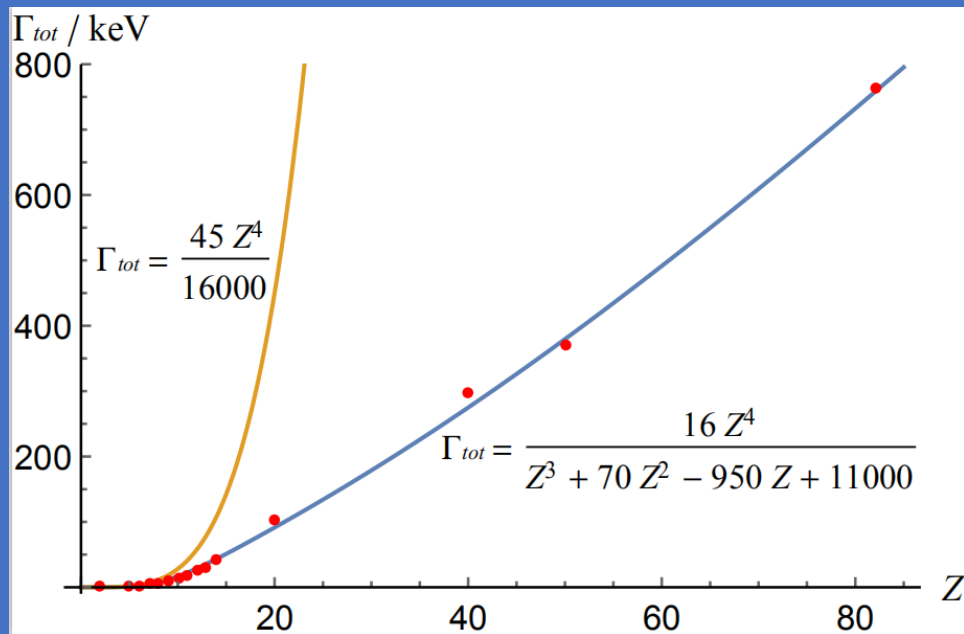


- $E_\gamma \approx 140$ MeV (final nucleus in its ground state)
- Γ_{ph} vs. Γ_{tot}

Methods for producing pionic atoms

➤ Total width of ns pionic states

- width: pion absorption, X-ray radiation, Auger electron emission
- fitting $1s$ width data



$$\Gamma_{tot}(Z, 1)$$

$$\Gamma_{tot}(Z, n) \approx \Gamma_{tot}(Z, 1) \frac{1}{n^3}$$

for pionic atoms with $1s$ orbital radius larger than nuclear radius

Photoproduction cross-sections

➤ Cross-section for monochromatic photons

- $\sigma_0 = 2\pi \frac{2I_f+1}{2I_i+1} \left(\frac{\hbar c}{E_\gamma}\right)^2 \frac{\Gamma_\gamma}{\Gamma_{tot}}$
- $E_\gamma \approx 140 \text{ MeV}$
- Γ_{tot} : dominated by pion absorption
- Γ_γ : radiative capture of the pion by nuclei, with final nuclei in the ground state
- $\frac{\Gamma_\gamma}{\Gamma_{tot}}$: α ($\sigma_0 \sim 1\text{mb}$, valid for light nuclei)
2% (radiative capture probability, upper estimate of $\frac{\Gamma_\gamma}{\Gamma_{tot}}$)

Photoproduction cross-sections

➤ bound pion vs. free pion

- Integrated cross-section: $\int \sigma(E)dE = \frac{\pi}{2} \sigma_0 \Gamma_{tot}$ (bound pion)
- $\int \sigma(E)dE = (Z\alpha)^2 mc^2 K \sigma_p$, $K = 1 - \exp(-2\pi Z\alpha mc/p)$ (near threshold)

➤ $\sigma_{p=0}$

- measurements of $\sigma_{p=0}$ (using quasi-monochromatic photons) are limited.
- light nuclei:

Z	^A X	^A Y' _{g.s.}	$\sigma_{p=0}$ (μb)	σ_0 (μb)	$[10^3 \times \Gamma_\gamma/\Gamma_{tot}]$	rate (s^{-1})
4	⁷ Li	⁷ Be _{g.s.}	8	1200	9.05	6.0×10^9
6	¹¹ B	¹¹ C _{g.s.}	4	260	1.90	2.7×10^9
7	¹² C	¹² N _{g.s.}	4	200	1.50	2.6×10^9
8	¹⁴ N	¹⁴ O _{g.s.}	0.2	8	0.057	1.3×10^8

- heavy nuclei: $\sigma_{p=0} \sim 1\mu\text{b}$

Photoproduction cross-sections

➤ $\sigma_{p=0}$

- yields for (γ, π^-) are A -independent for targets with $A \geq 40$ ($A \approx 2Z$)
- $\gamma + {}^{197}\text{Au} \rightarrow {}^{197}\text{Hg}_{g.s.} + \pi^-$, $\sigma_{p=0} \sim 1\mu\text{b}$

➡ $\sigma_{p=0} \sim 1\mu\text{b}$ for nuclei with $9 \leq Z \leq 92$ (rough estimate)

Photoproduction cross-sections

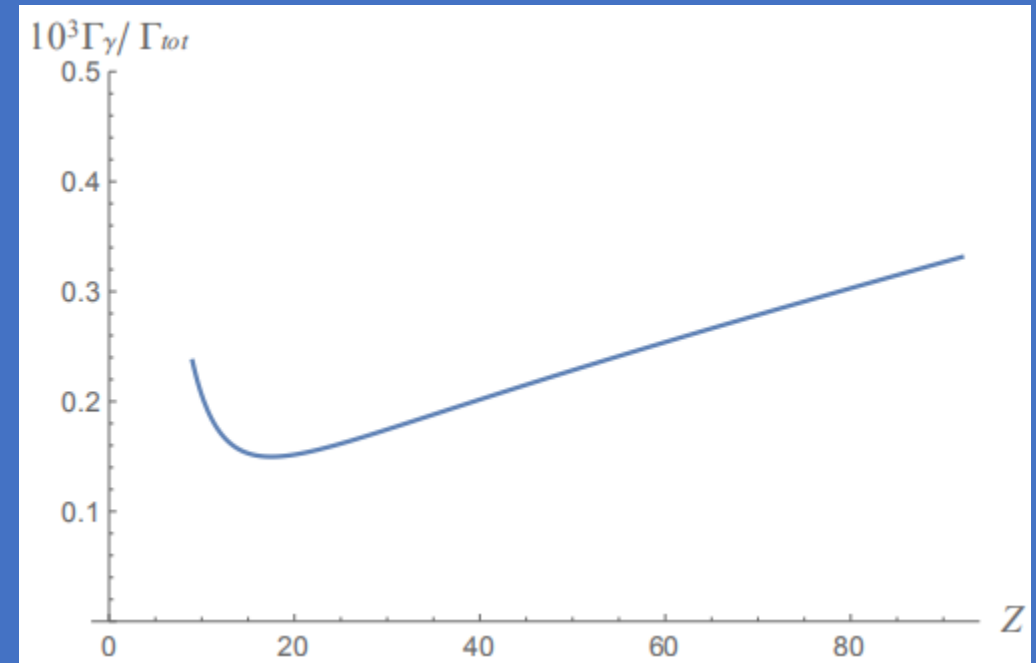
➤ bound pion vs. free pion

$\sigma_p \longrightarrow \Gamma_\gamma/\Gamma_{tot}, \sigma_0$, production rates

light nuclei:

Z	${}^A X$	${}^A X'_{g.s.}$	$\sigma_{p=0}$ (μb)	σ_0 (μb)	$[10^3 \times \Gamma_\gamma/\Gamma_{tot}]$	rate (s^{-1})
4	${}^7\text{Li}$	${}^7\text{Be}_{g.s.}$	8	1200	9.05	6.0×10^9
6	${}^{11}\text{B}$	${}^{11}\text{C}_{g.s.}$	4	260	1.90	2.7×10^9
7	${}^{12}\text{C}$	${}^{12}\text{N}_{g.s.}$	4	200	1.50	2.6×10^9
8	${}^{14}\text{N}$	${}^{14}\text{O}_{g.s.}$	0.2	8	0.057	1.3×10^8

$Z \geq 9: \sigma_p \approx 1\mu\text{b} \longrightarrow \Gamma_\gamma/\Gamma_{tot} \approx 0.25 \times 10^{-3}$



Photoproduction cross-sections

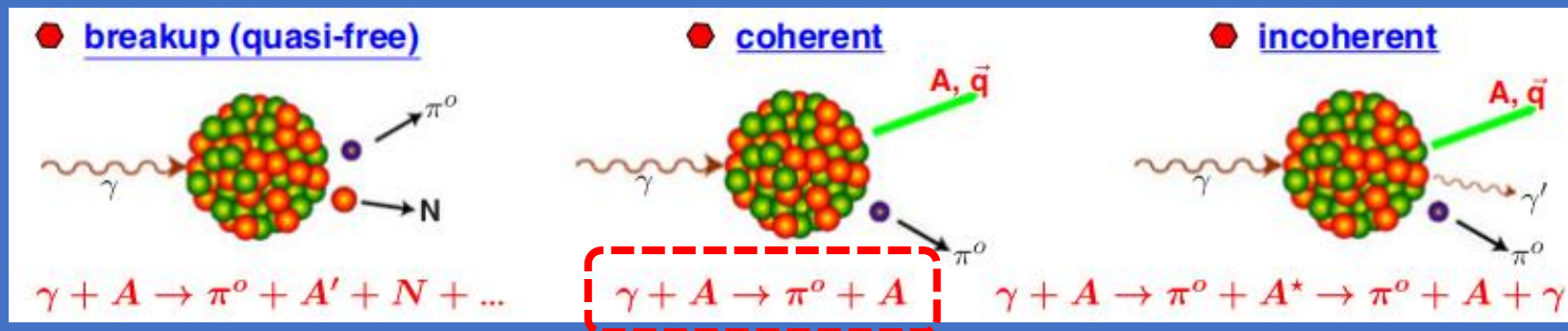
➤ Free π^- vs. π^0

- Coulomb interaction \longrightarrow Sommerfeld factor

$$\sigma_p(\pi^-)/\sigma_p(\pi^0) \sim \frac{2\pi f}{1-\exp(-2\pi f)}, \quad f = Z\alpha mc/p$$

- Coherent production of π^0

$$\sigma_p(\pi^-)/\sigma_p(\pi^0) \approx \frac{A-Z}{A^2} \frac{2\pi f}{1-\exp(-2\pi f)} \approx \frac{1}{4Z} \frac{2\pi f}{1-\exp(-2\pi f)}$$



Photoproduction cross-sections

➤ Background photon attenuation

- For 140 MeV photon:
pair production & Compton scattering
- $\sigma_{tot}(Z_i) \approx \sigma_{pp} + \sigma_{scat} \approx 0.6 \times 10^{-26} (Z_i^2 + Z_i) \text{ cm}^2 \gg \sigma_0$

Production rates at the GF

➤ GF photons: nearly uniformly distributed up to the maximal energy

➤ Proper collimation: suppress the background

$$j = 10^{17} \text{ ph/s} \xrightarrow{\text{collimation}} j_{eff} = j \frac{\Gamma_{ph}}{E_\gamma}$$

➤ Γ_{ph} : $\Gamma_{ph} = \Gamma_{tot}$ or $\Gamma_{ph} = E_{1s}$ (1s binding energy)

➤ $\sigma_{eff}(Z, n)$, $\sigma(E) = \sigma_0 \frac{(\Gamma_{tot}/2)^2}{(E-E_\gamma)^2 + (\Gamma_{tot}/2)^2}$

$$\sigma_{eff}(Z, n) \approx \sigma_0 \frac{\Gamma_{tot}}{\Gamma_{ph}}$$

Production rates at the GF

➤ Maximal production rates

$$p(Z, n) = j_{eff} \frac{\sigma_{eff}(Z, n)}{\sigma_{tot}(Z_i)} = 5.6 \times 10^8 \frac{\sigma_{p=0}(Z)/1\mu b}{n^3} s^{-1}$$

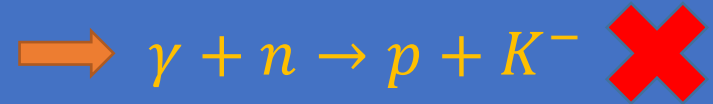
- light nuclei:

- $Z \geq 9: \sigma_p \approx 1\mu b \longrightarrow p(Z, 1) \approx 5.6 \times 10^8 s^{-1}$

Z	${}^A X$	${}^A X'_{g.s.}$	$\sigma_{p=0} (\mu b)$	$\sigma_0 (\mu b)$	$[10^3 \times \Gamma_\gamma / \Gamma_{tot}]$	rate (s^{-1})
4	${}^7 Li$	${}^7 Be_{g.s.}$	8	1200	9.05	6.0×10^9
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Kaonic atoms

➤ Strangeness conservation



(K^- : $\bar{u}s$. Require \bar{s} .)

➤ Possible methods

- $\gamma \rightarrow K^- + K^+ \longrightarrow \gamma + \frac{A}{Z} X \rightarrow (\frac{A}{Z} X' + K^-)_{nl} + K^+$
threshold energy, $E_\gamma \approx 1\text{GeV}$, beyond current scope of the GF
nonresonance (free K^+)

Summary

➤ High production rates

- light nuclei:

- $Z \geq 9: \sigma_p \approx 1\mu\text{b} \longrightarrow p(Z, 1) \approx 5.6 \times 10^8 \text{s}^{-1}$

Z	${}^A\text{X}$	${}^A\text{X}'_{g.s.}$	$\sigma_{p=0} (\mu\text{b})$	$\sigma_0 (\mu\text{b})$	$[10^3 \times \Gamma_\gamma/\Gamma_{tot}]$	rate (s^{-1})
4	${}^7\text{Li}$	${}^7\text{Be}_{g.s.}$	8	1200	9.05	6.0×10^9
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8	${}^{14}\text{N}$	${}^{14}\text{O}_{g.s.}$	0.2	8	0.057	1.3×10^8

➤ Deeply bound states ✓

➤ Higher ns states and nl states ✓

Thank you!