

Momentum Dependent Mean-Fields for (Anti-)Hyperons

Th. Gaitanos, A. Choroziou



ΤΜΗΜΑ ΦΥΣΙΚΗΣ

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ΠΑΝΕΠΙΣΤΗΜΙΟ
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Gaitanos & Kaskulov, NPA 940 (2015) 181, NPA 899 (2013) 133
Gaitanos & Choroziou, NPA (2021) in press

Momentum Dependent Mean-Fields for (Anti-)Hyperons

- Introduction
- The Non-Linear Derivative (NLD) model
- Basic properties: nuclear EoS & p, \bar{p} -optical potentials
- Υ properties: density & momentum dependent optical potentials
- $\bar{\Upsilon}$ properties: density & momentum dependent optical potentials

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RMF + MDI

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- Λ properties: density & momentum dependent optical potentials
- $\bar{\Lambda}$ properties: density & momentum dependent optical potentials

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RMF + MDI

Re & Im parts

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- Υ properties: density & momentum dependent optical potentials
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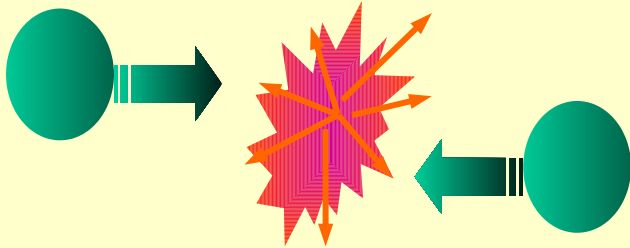
Introduction...

Important for astrophysics

explore EoS far beyond saturation (high ρ , high τ -asymm, $\Lambda/\Sigma/\Xi/\Omega$)

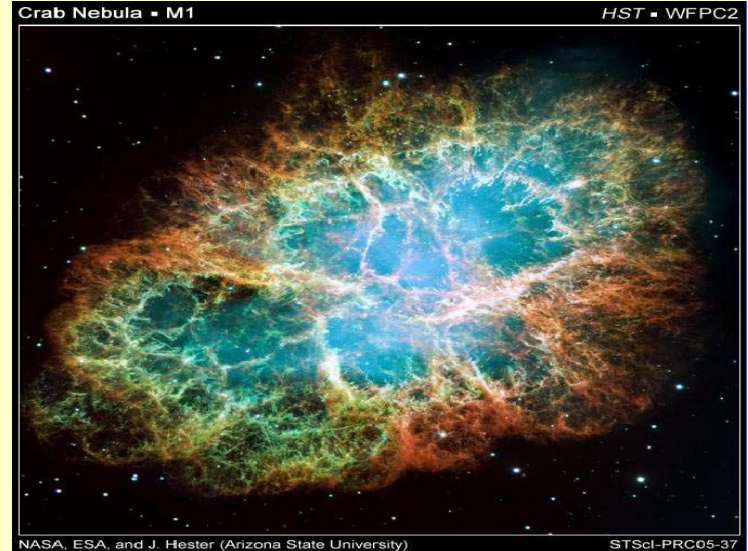
Heavy-ion collisions

(collective flow, meson production)



Densities of fireball for HIC@SIS:
 $\rho \sim (2-3)\rho_0$

Neutron stars (mass & radius)

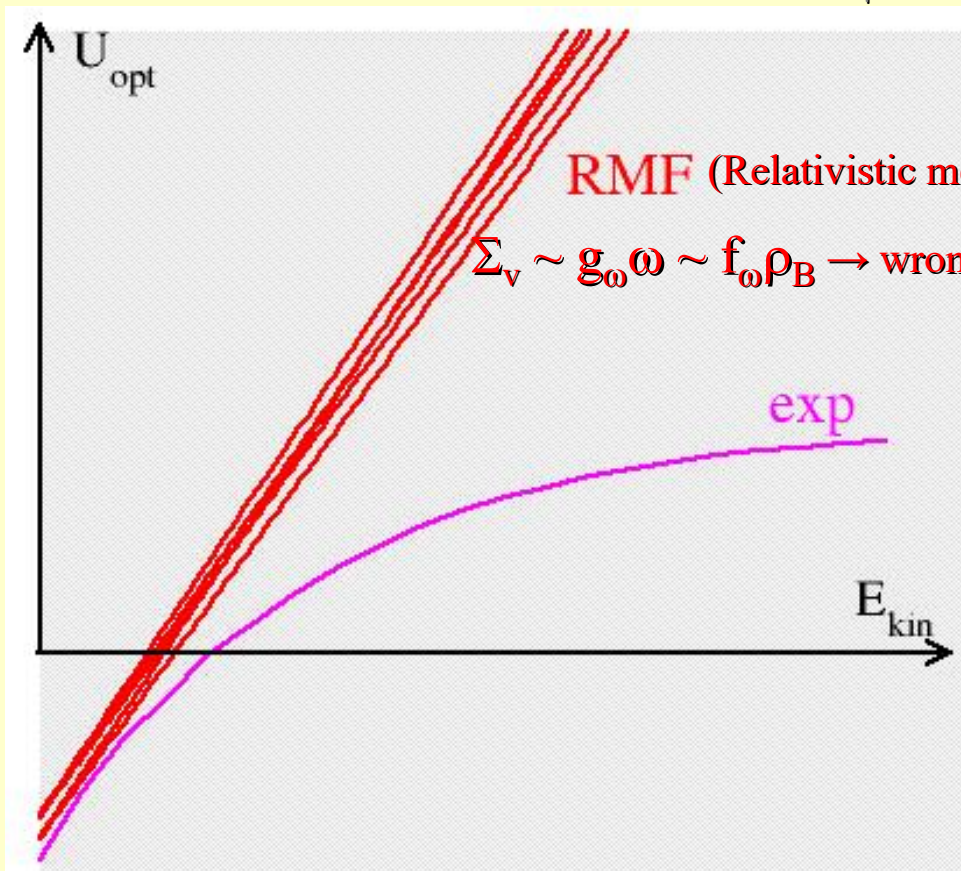


Densities in static NS: $\rho \sim (8-10)\rho_0$

- In high-density matter (+kinematics) \rightarrow particles with high-momenta p
- Not only density dependence, but also **momentum dependence (MD)** essential
-
- Not only nucleon-EoS, but also **hyperon-EoS** essential
-
- Not only hyperon-density dependence, but also **hyperon-momentum dependence** essential

Introduction...

In-medium proton Schrödinger-equivalent $Re(U_{opt})$



$$U_{opt} = \frac{E}{m} \Sigma_v - \Sigma_s + \frac{1}{2m} (\Sigma_s^2 - \Sigma_v^2)$$

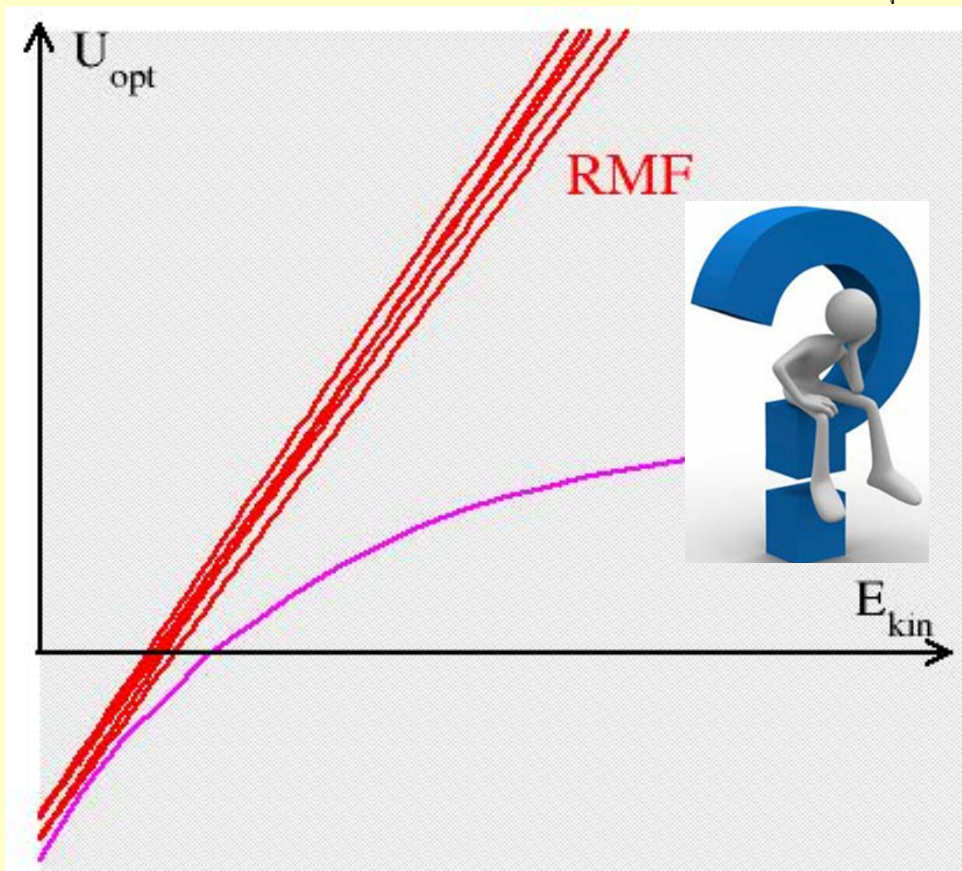
DBHF & Dirac-phenomenology for nucleons:
Proton-opt. pot. well known
saturating fields (particular vector) with rising p

Solutions so far:

- non-local (Hartree-Fock) contributions to RMF (Hartree) mean-field
Weber, Blättel, Cassing et al., Nucl. Phys. A539 (1992) 713
- first-order derivative coupling terms into the interaction Lagrangian
S. Typel, Phys. Rev. C71, 064301 (2005)

Introduction...

In-medium hyperon Schrödinger-equivalent $\text{Re}(U_{\text{opt}})$



$$U_{\text{opt}} = \frac{E}{m} \Sigma_v - \Sigma_s + \frac{1}{2m} (\Sigma_s^2 - \Sigma_v^2)$$

Dirac-phenomenology for hyperons:
?
rare experimental scattering data so far

The Non-Linear Derivative (NLD) model...

NLD Lagrangian : as in conventional Relativistic Hydrodynamics (RHD)

$$\mathcal{L} = \frac{1}{2} \sum_B \left[\bar{\Psi}_B \gamma_\mu^i \overrightarrow{\partial}^\mu \Psi_B - \bar{\Psi}_B i \overleftarrow{\partial}^\mu \gamma_\mu \Psi_B \right] - \sum_B m_B \bar{\Psi}_B \Psi_B + \sum_{m=\sigma,\omega,\rho} \mathcal{L}_{int}^m.$$

For the baryon octet: $\Psi_B = (\Psi_N, \Psi_\Lambda, \Psi_\Sigma, \Psi_\Xi)^T$

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$$\mathcal{L}_{int}^m = \sum_B \frac{g_{mB}}{2} \left[\bar{\Psi}_B \Gamma_m \Psi_B \varphi_m + \varphi_m \bar{\Psi}_B \Gamma_m \Psi_B \right],$$

For $(\varphi_m = \sigma, \omega, \rho)$ -baryon interaction with corresponding vertices $\Gamma_m = \mathbb{1}, \gamma^\mu, \dots$

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Non-linear derivative operators : Taylor expansion of partial derivatives ξ

$$\overrightarrow{\mathcal{D}}_B := \mathcal{D} \left(\overrightarrow{\xi}_B \right), \quad \overleftarrow{\mathcal{D}}_B := \mathcal{D} \left(\overleftarrow{\xi}_B \right) \quad \text{with} \quad \overrightarrow{\xi}_B = -\frac{v^\alpha i \vec{\partial}_\alpha}{\Lambda_B}, \quad \overleftarrow{\xi}_B = \frac{i \overleftarrow{\partial}_\alpha v^\alpha}{\Lambda_B}$$

v^α auxiliary 4-vector chosen such to get p-dependence

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cut-off, will regulate the high-momentum tail of RMF fields

The Non-Linear Derivative (NLD) model...

NLD Lagrangian: contains higher field derivatives: $\mathcal{L}(\varphi_r, \partial_{\alpha_1}\varphi_r, \partial_{\alpha_1\alpha_2}\varphi_r, \dots, \partial_{\alpha_1\dots\alpha_n}\varphi_r)$

→ Generalized Euler-Lagrange equations:

$$\frac{\partial \mathcal{L}}{\partial \varphi_r} + \sum_{i=1}^n (-)^i \partial_{\alpha_1 \dots \alpha_i} \frac{\partial \mathcal{L}}{\partial (\partial_{\alpha_1 \dots \alpha_i} \varphi_r)} = 0$$

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→ Generalized Noether-Theorem: conserved current

$$J^\mu = -i \left[\mathcal{K}_r^\mu \varphi_r + \mathcal{K}_r^{\mu\sigma_1} \partial_{\sigma_1} \varphi_r + \mathcal{K}_r^{\mu\sigma_1\sigma_2} \partial_{\sigma_1\sigma_2} \varphi_r + \dots + \mathcal{K}_r^{\mu\sigma_1\dots\sigma_n} \partial_{\sigma_1\dots\sigma_n} \varphi_r \right]$$

with the following tensors

$$\mathcal{K}_r^{\mu\sigma_1\dots\sigma_m} = \sum_{i=1}^m (-)^{i+1} \prod_{j=1}^{i-1} \partial_{\alpha_j} \frac{\partial \mathcal{L}}{\partial (\partial_{\mu\alpha_j\sigma_1\dots\sigma_m}\varphi_r)}$$

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infinite series resp. to higher-order field derivatives, but...

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All infinite series can be resummed to compact expressions

The Non-Linear Derivative (NLD) model...

→ Dirac equation for nucleons $\gamma_\mu (i\partial^\mu - \Sigma^\mu) - (m - \Sigma_s) \Psi = 0$ with selfenergies

$$\Sigma^\mu = g_\omega \omega^\mu \vec{\mathcal{D}} + g_\rho \vec{\tau} \cdot \vec{\rho}^\mu \vec{\mathcal{D}} + \dots$$

$$\Sigma_s = g_\sigma \sigma \vec{\mathcal{D}} + \dots \quad (\text{up to terms containing derivatives of the meson fields})$$

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→ Meson field equations:

$$\partial_\alpha \partial^\alpha \sigma + m_\sigma^2 \sigma + \frac{\partial U}{\partial \sigma} = \frac{1}{2} g_\sigma \left[\bar{\Psi} \overleftarrow{\mathcal{D}} \Psi + \bar{\Psi} \vec{\mathcal{D}} \Psi \right],$$

$$\partial_\mu F^{\mu\nu} + m_\omega^2 \omega^\nu = \frac{1}{2} g_\omega \left[\bar{\Psi} \overleftarrow{\mathcal{D}} \gamma^\nu \Psi + \bar{\Psi} \gamma^\nu \vec{\mathcal{D}} \Psi \right],$$

$$\partial_\mu \vec{G}^{\mu\nu} + m_\rho^2 \vec{\rho}^\nu = \frac{1}{2} g_\rho \left[\bar{\Psi} \overleftarrow{\mathcal{D}} \gamma^\nu \vec{\tau} \Psi + \bar{\Psi} \vec{\tau} \gamma^\nu \vec{\mathcal{D}} \Psi \right]$$

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→ Energy-momentum tensor:

$$T^{\mu\nu} = \frac{1}{2} \bar{\Psi} \gamma^\mu i \overrightarrow{\partial}^\nu \Psi - \frac{1}{2} \bar{\Psi} i \overleftarrow{\partial}^\nu \gamma^\mu \Psi$$

$$+ \frac{1}{2} \sum_m g_m \left[\bar{\Psi} \Gamma_m \overrightarrow{\partial}^\mu i \overrightarrow{\partial}^\nu \Psi + \bar{\Psi} i \overleftarrow{\partial}^\nu \overleftarrow{\partial}^\mu \Gamma_m \Psi \right] \varphi_m - g^{\mu\nu} \mathcal{L} + \dots$$

The NLD model: RMF approach to INM...

→ Plane wave Ansatz for Ψ and $\bar{\Psi}$ with $\mathcal{D} = \mathcal{D}(p)$

$$\Sigma_{vi}^\mu = g_\omega \omega^\mu \mathcal{D} + g_\rho \tau_i \rho^\mu \mathcal{D}, \quad \Sigma_{si} = g_\sigma \sigma \mathcal{D}$$

$$m_\sigma^2 \sigma + \frac{\partial U}{\partial \sigma} = g_\sigma \sum_{i=p,n} \langle \bar{\Psi}_i \mathcal{D} \Psi_i \rangle = g_\sigma \rho_s$$

$$m_\omega^2 \omega = g_\omega \sum_{i=p,n} \langle \bar{\Psi}_i \gamma^0 \mathcal{D} \Psi_i \rangle = g_\omega \rho_0$$

$$m_\rho^2 \rho = g_\rho \sum_{i=p,n} \tau_i \langle \bar{\Psi}_i \gamma^0 \mathcal{D} \Psi_i \rangle = g_\rho \rho_I$$

$$T^{\mu\nu} = \sum_{i=p,n} \frac{\kappa}{(2\pi)^3} \int_{|\vec{p}| \leq p_{F_i}} d^3 p \frac{\Pi_i^\mu p^\nu}{\Pi_i^0} - g^{\mu\nu} \langle \mathcal{L} \rangle$$

$$\Pi_i^\mu = p_i^{*\mu} + m_i^* \left(\partial_p^\mu \Sigma_{si} \right) - \left(\partial_p^\mu \Sigma_{vi}^\beta \right) p_{i\beta}^*$$

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meson-field equations

$$m_{\sigma}^2 \sigma + \frac{\partial U}{\partial \sigma} = g_{\sigma} \sum_{i=p,n} \langle \bar{\Psi}_i \mathcal{D} \Psi_i \rangle = g_{\sigma} \rho_s$$

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Equation of State (EoS)

$$\varepsilon = \sum_{i=p,n} \frac{\kappa}{(2\pi)^3} \int_{|\vec{p}| \leq p_{F_i}} d^3 p E(\vec{p}) - \langle \mathcal{L} \rangle$$

$$P = \frac{1}{3} \sum_{i=p,n} \frac{\kappa}{(2\pi)^3} \int_{|\vec{p}| \leq p_{F_i}} d^3 p \frac{\vec{\Pi}_i \cdot \vec{p}}{\Pi_i^0} + \langle \mathcal{L} \rangle$$

Features of NLD...

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cut-off Λ regulates:

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2) DD of meson-field sources
(particularly for ω -field)

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cut-off Λ regulates:

1) DD & MD of selfenergies

2) DD of meson-field sources
(particularly for ω -field)

3) fully thermodynamic consistent

Basic properties: nuclear EoS & opt. potentials...

Parameters

	\vec{D}	cut-off	Λ_s [GeV]	Λ_v [GeV]	g_σ	g_ω	g_ρ	b [fm ⁻¹]	c	m_σ [GeV]	m_ω [GeV]	m_ρ [GeV]
NLD	$\frac{1}{1 + \sum_{j=1}^4 (\zeta_j^\alpha i \vec{\partial}_\alpha)^2}$	$\frac{\Lambda^2}{\Lambda^2 + \vec{p}^2}$	0.95	1.125	10.08	10.13	3.50	15.341	-14.735	0.592	0.782	0.763

Comparison with other models

Model	ρ_{sat} [fm ⁻³]	E_b [MeV/A]	K [MeV]	a_{sym} [MeV]	L [MeV]	K_{sym} [MeV]	K_{asy} [MeV]
NLD	0.156	-15.30	251	30	81	-28	-514
NL3*	0.150	-16.31	258	38.68	125.7	104.08	-650.12
DD	0.149	-16.02	240	31.60	56	-95.30	-431.30
D ³ C	0.151	-15.98	232.5	31.90	59.30	-74.7	-430.50
DBHF	0.185	-15.60	290	33.35	71.10	-27.1	-453.70
	0.181	-16.15	230	34.20	71	87.36	-340
empirical	0.167 ± 0.019	-16 ± 1	230 ± 10	31.1 ± 1.9	88 ± 25	-	-550 ± 100

→ Lalazissis

→ Typel

→ Li, Machleidt, Brockmann

→ Fuchs

Basic properties: nuclear EoS & opt. potentials...

Parameters

	\vec{D}	cut-off	[GeV]		g_ρ	b [fm ⁻¹]	c	m_σ [GeV]	m_ω [GeV]	m_ρ [GeV]
NLD	$\frac{1}{1 + \sum_{j=1}^4 (\zeta_j^\alpha i \vec{\partial}_\alpha)^2}$	$\frac{\Lambda^2}{\Lambda^2 + \vec{p}^2}$	0.95	1.125	10.08	10.13	3.50	15.341	-14.735	0.592 0.782 0.763

Note: A blue callout bubble labeled "monopole form" points to the cut-off parameter $\frac{\Lambda^2}{\Lambda^2 + \vec{p}^2}$.

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Model	ρ_{sat} [fm ⁻³]	E_b [MeV/A]	K [MeV]	a_{sym} [MeV]	L [MeV]	K_{sym} [MeV]	K_{asy} [MeV]
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Basic properties: nuclear EoS & opt. potentials...

Parameters

	\vec{D}	cut-off	Λ_s [GeV]	Λ_v [GeV]	g_σ	g_ω	g_ρ	b [fm ⁻¹]	c	m_σ [GeV]	m_ω [GeV]	m_ρ [GeV]
NLD	$\frac{1}{1 + \sum_{j=1}^4 (\zeta_j^\alpha i \vec{\partial}_\alpha)^2}$	$\frac{\Lambda^2}{\Lambda^2 + \vec{p}^2}$	0.95	1.125	10.08	10.13	3.50	15.341	-14.735	0.592	0.782	0.763

Comparison with other models

Model	ρ_{sat} [fm ⁻³]	E_b [MeV/A]	K [MeV]	a [MeV]	b [MeV]	c [MeV]	d [MeV]
NLD	0.156	-15.30	251	30	81	-28	-514
NL3*	0.150	-16.31	258	38.68	125.7	104.08	-650.12
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	0.181	-16.15	230	34.20	71	87.36	-340
empirical	0.167 ± 0.019	-16 ± 1	230 ± 10	31.1 ± 1.9	88 ± 25	-	-550 ± 100

soft EoS at ρ_{sat} ,
but stiff at high ρ relevant for NS!

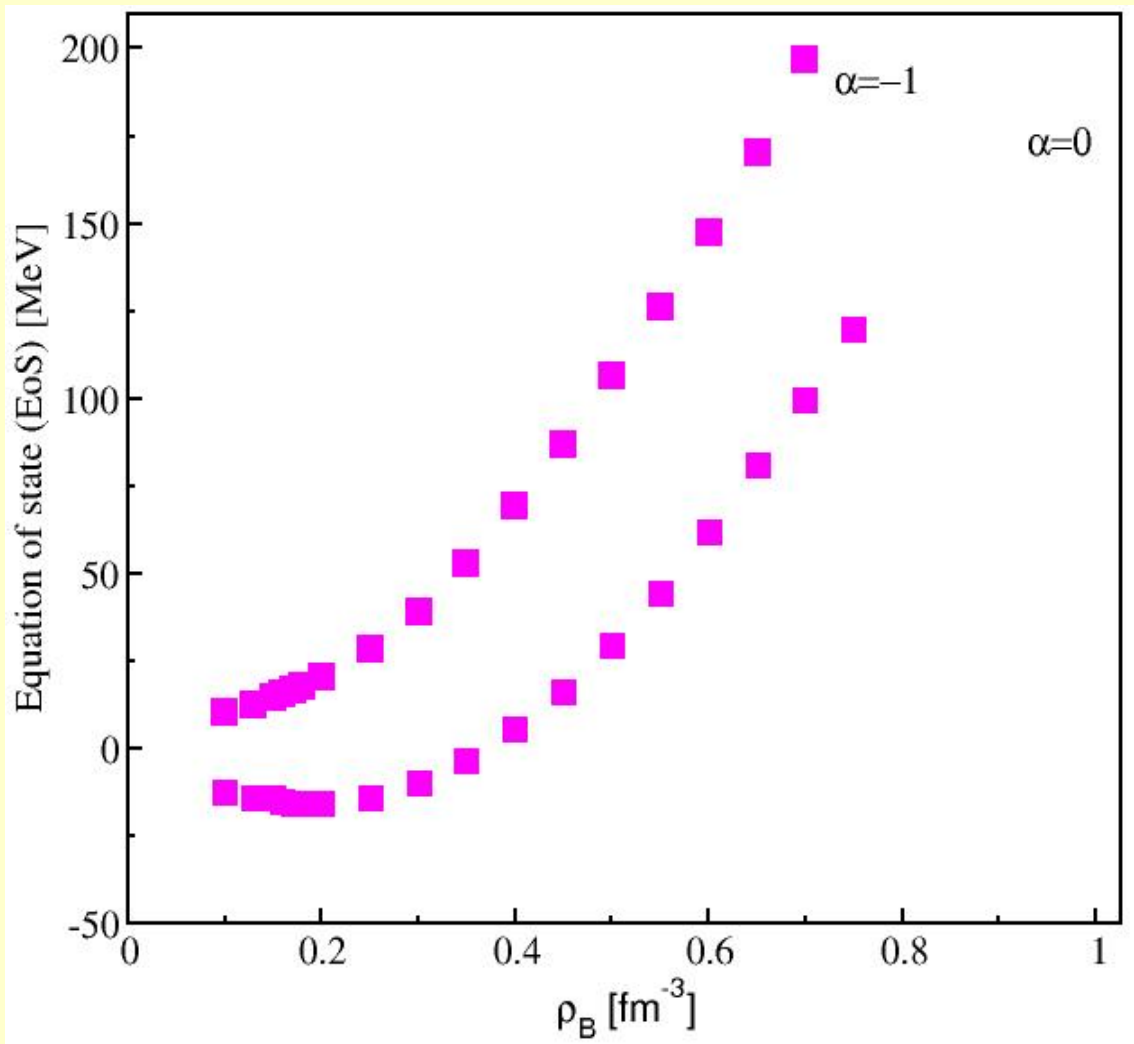
→ Lalazissis

→ Typel

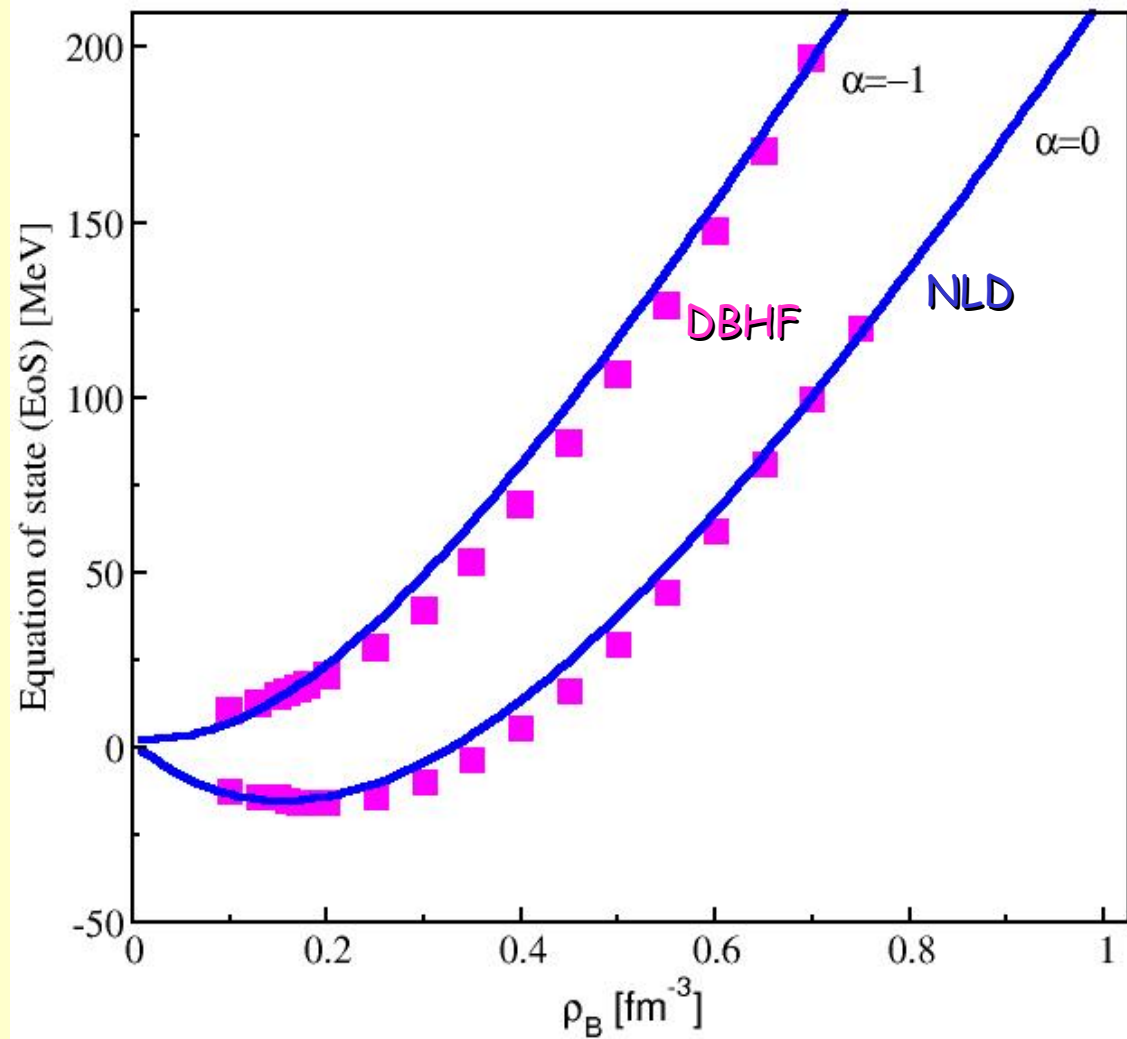
→ Li, Machleidt, Brockmann

→ Fuchs

Basic properties: nuclear EoS & opt. potentials...



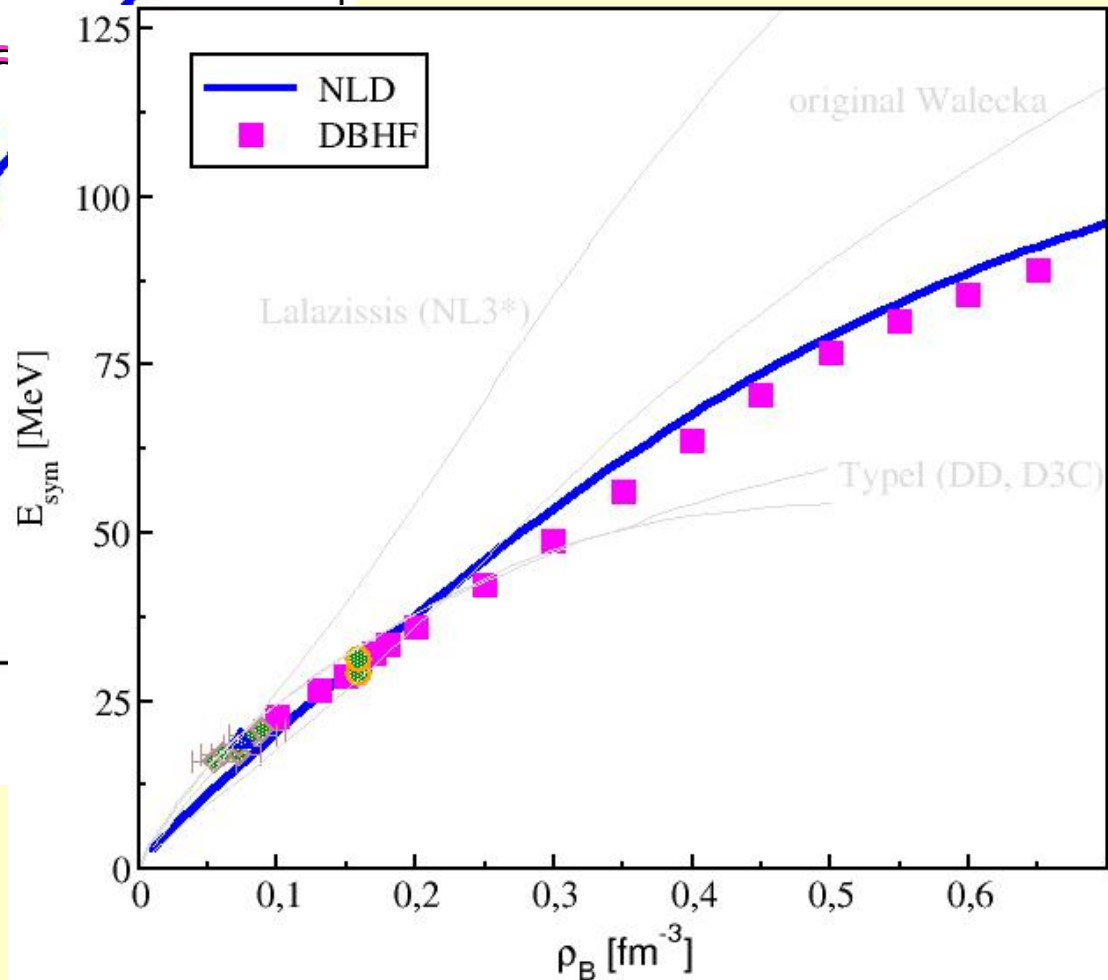
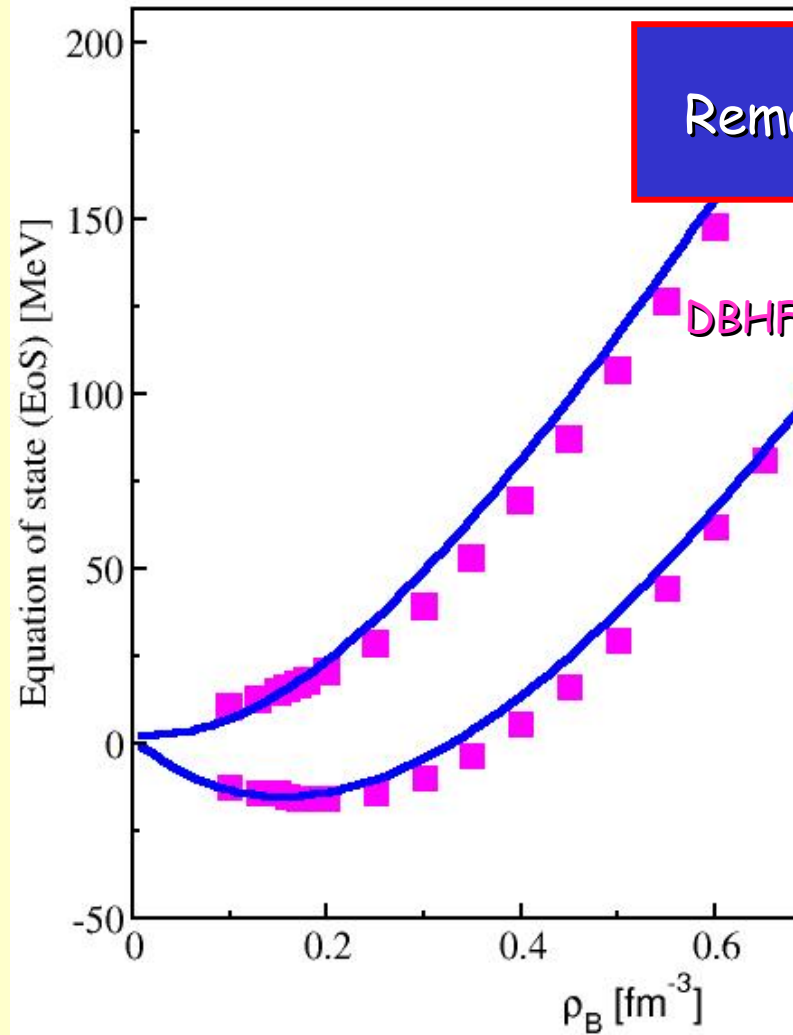
Basic properties: nuclear EoS & opt. potentials...



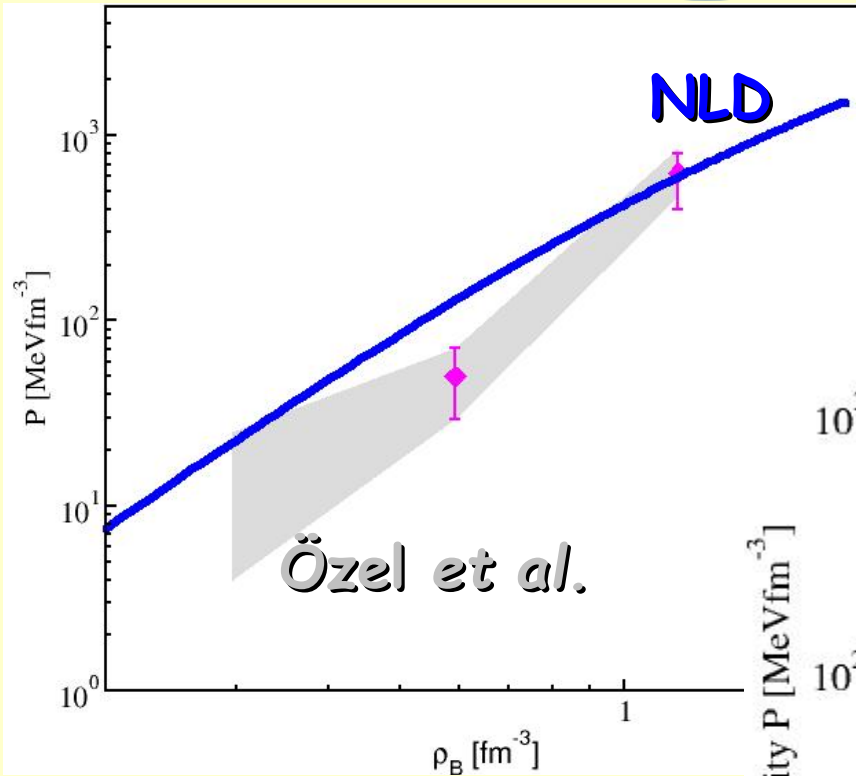
Remarkable comparison with microscopic DBHF!

Basic properties: nuclear EoS & opt. potentials...

Remarkable comparison with microscopic DBHF!



Basic properties: nuclear EoS & opt. potentials...

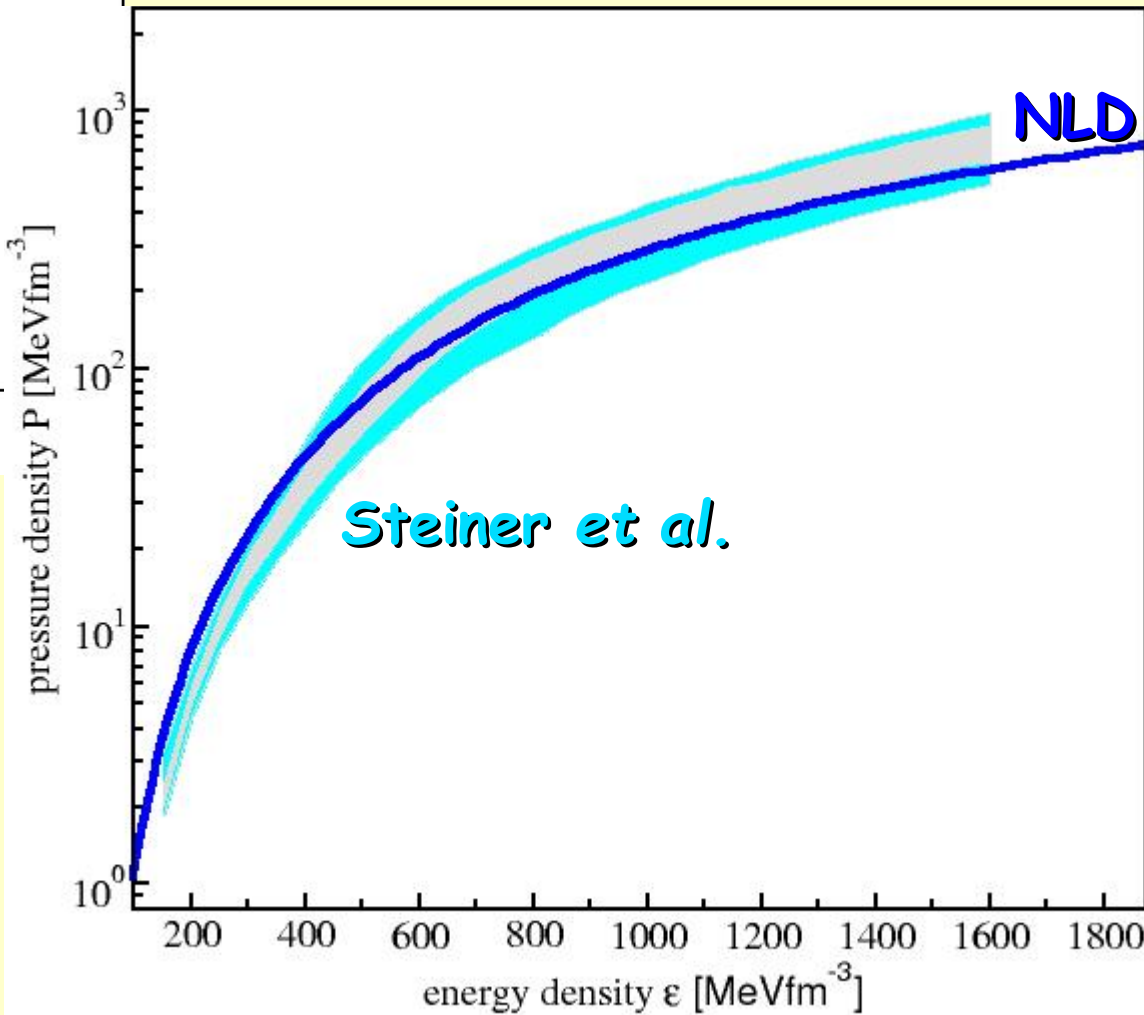


Consistent with analyses of F. Özel..!

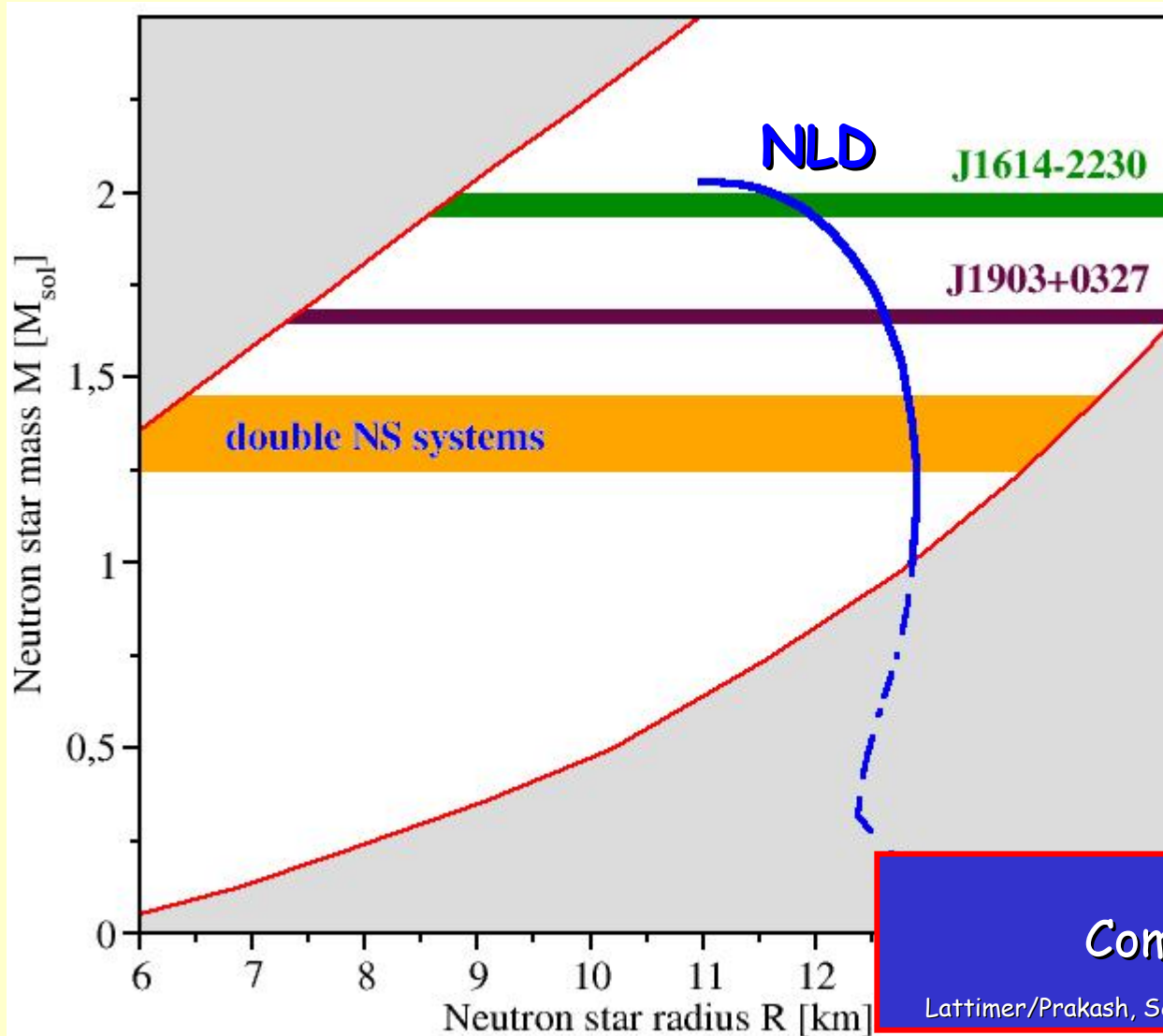
Phys. Rev. D82, 101301 (2010).

... and A.W. Steiner

Astrophys. J. 722, 33 (2010).



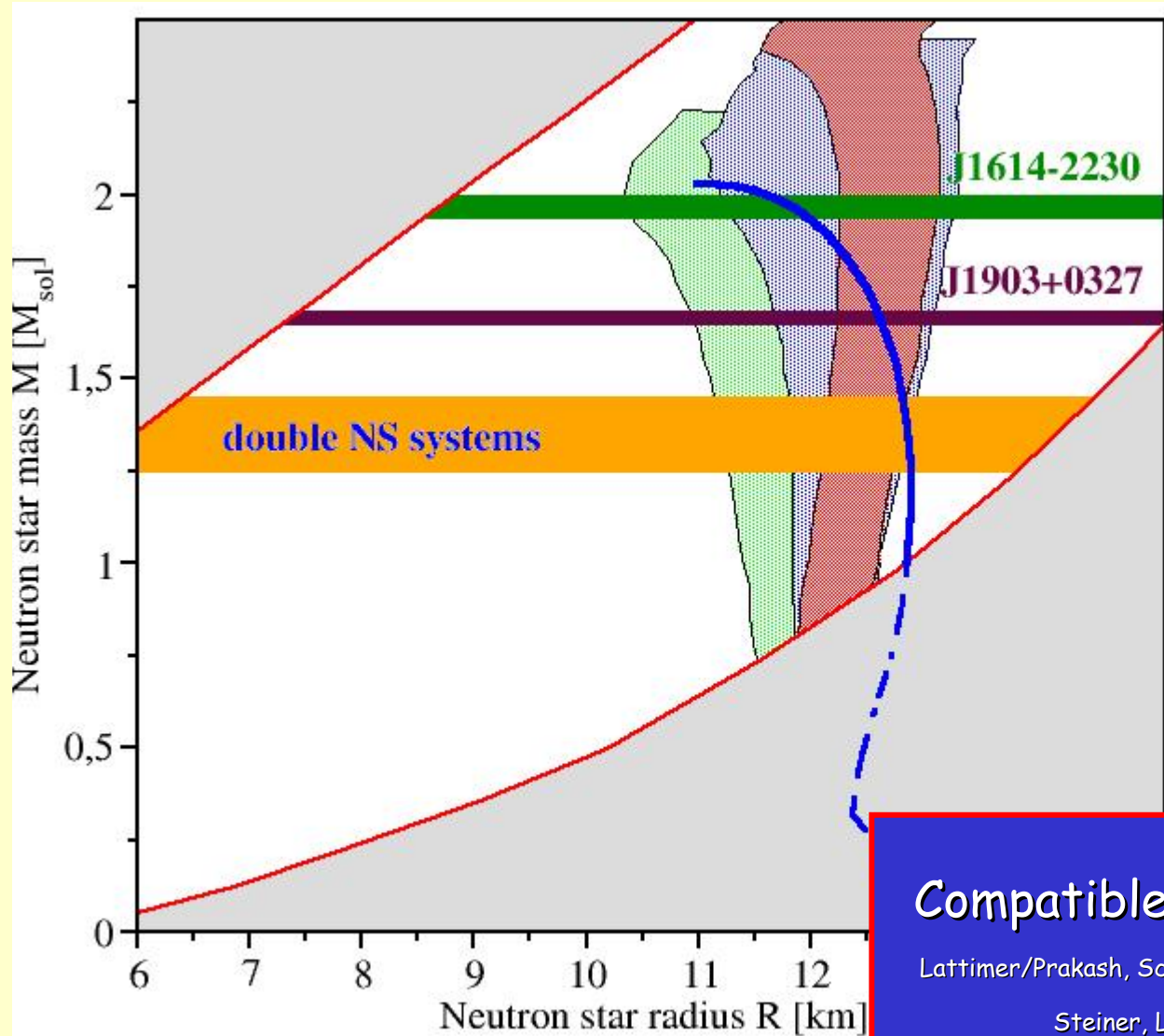
Basic properties: nuclear EoS & opt. potentials...



Compatible with ...

Lattimer/Prakash, Science 304 ('04) 536, Phys. Rep. 442 ('07) 109

Basic properties: nuclear EoS & opt. potentials...

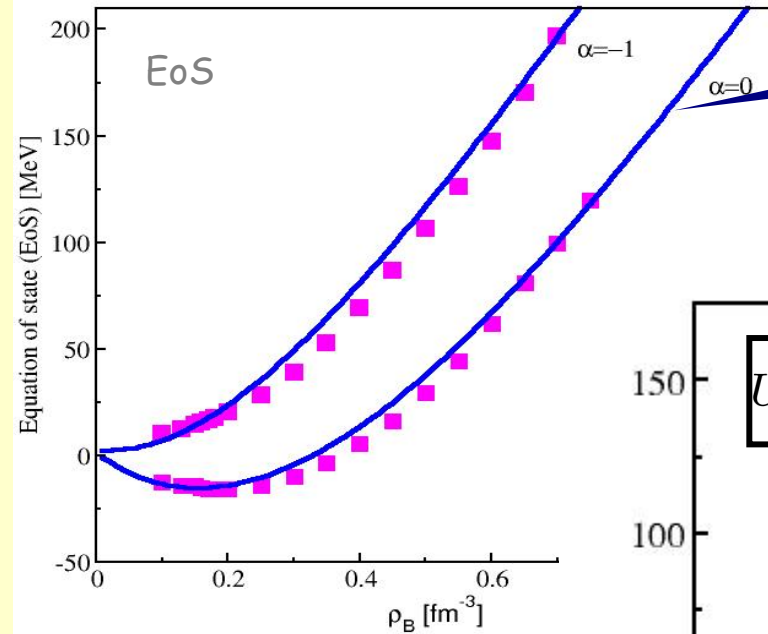


Compatible with all observations

Lattimer/Prakash, Science 304 ('04) 536, Phys. Rep. 442 ('07) 109

Steiner, Lattimer, Brown, arXiv: 1205.6871

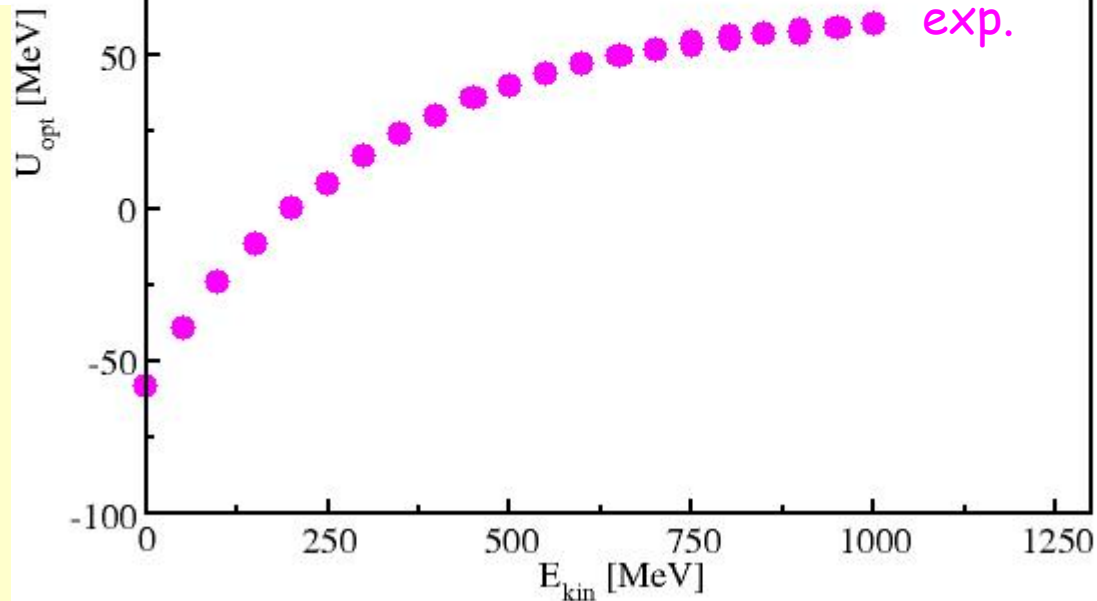
Basic properties: nuclear EoS & opt. potentials...



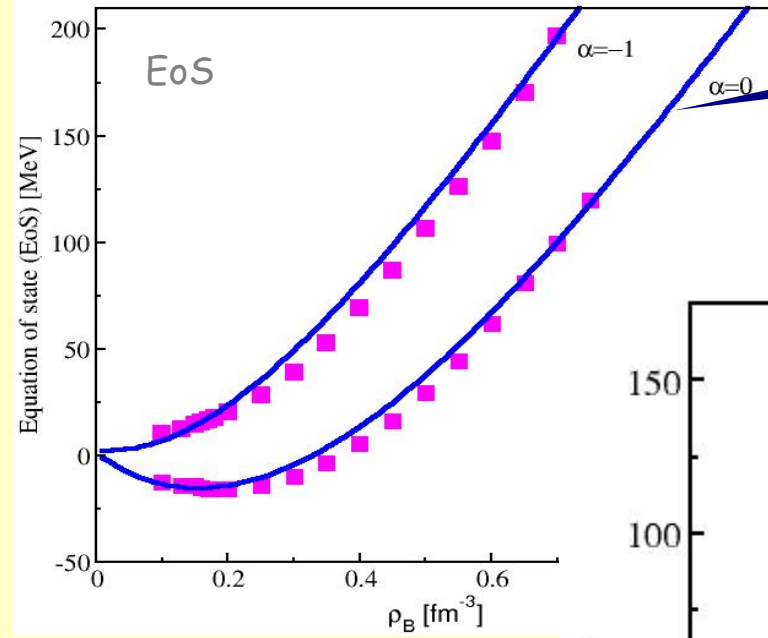
high $\rho \rightarrow$ high momenta

In-medium proton SEP (real part)

$$U_{\text{opt}} = \frac{E}{m} \Sigma_v - \Sigma_s + \frac{1}{2m} (\Sigma_s^2 - \Sigma_v^2)$$

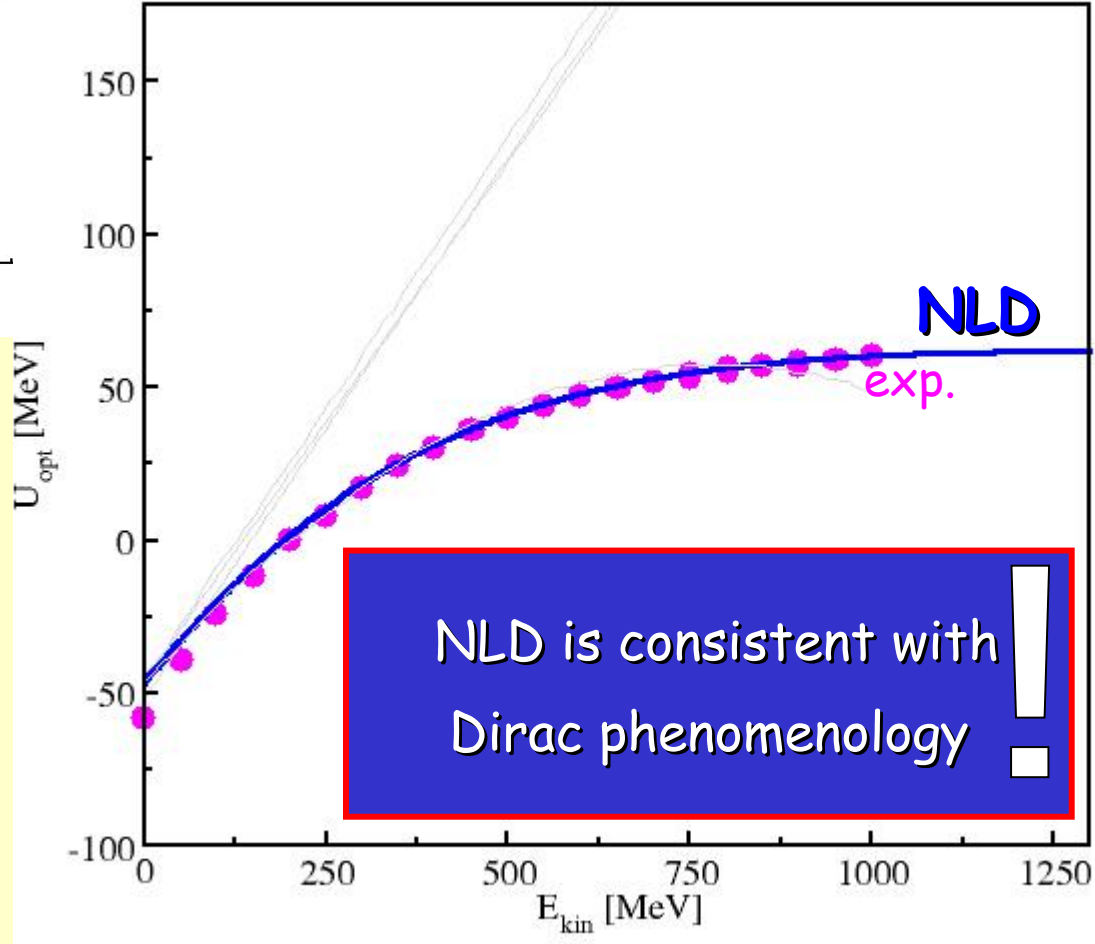


Basic properties: nuclear EoS & opt. potentials...



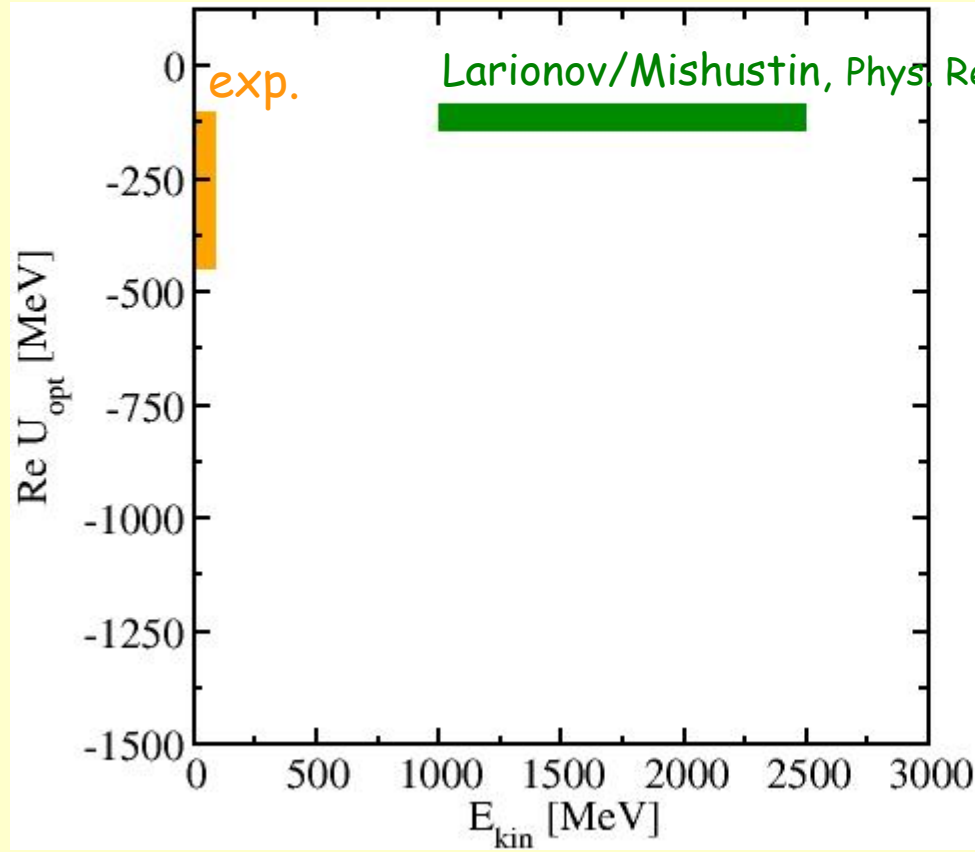
high $\rho \rightarrow$ high momenta

In-medium proton SEP (real part)



Basic properties: nuclear EoS & opt. potentials...

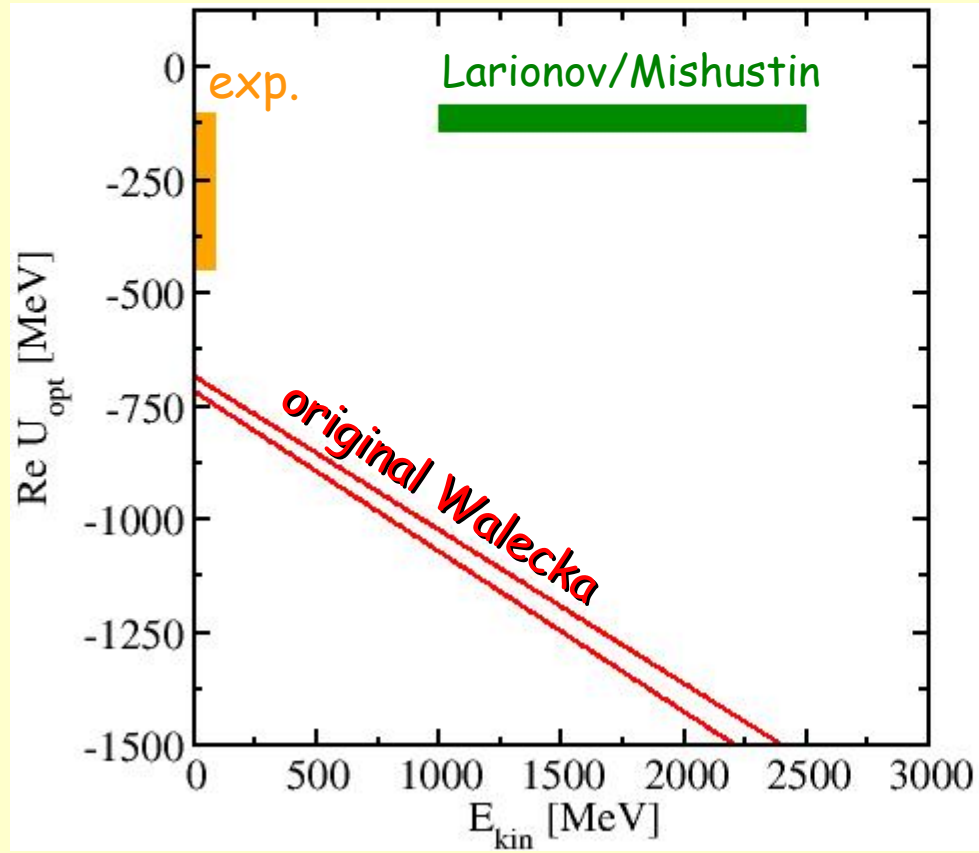
In-medium anti-proton SEP (real part)



Larionov/Mishustin, Phys. Rev. C80 ('09) 021601(R).

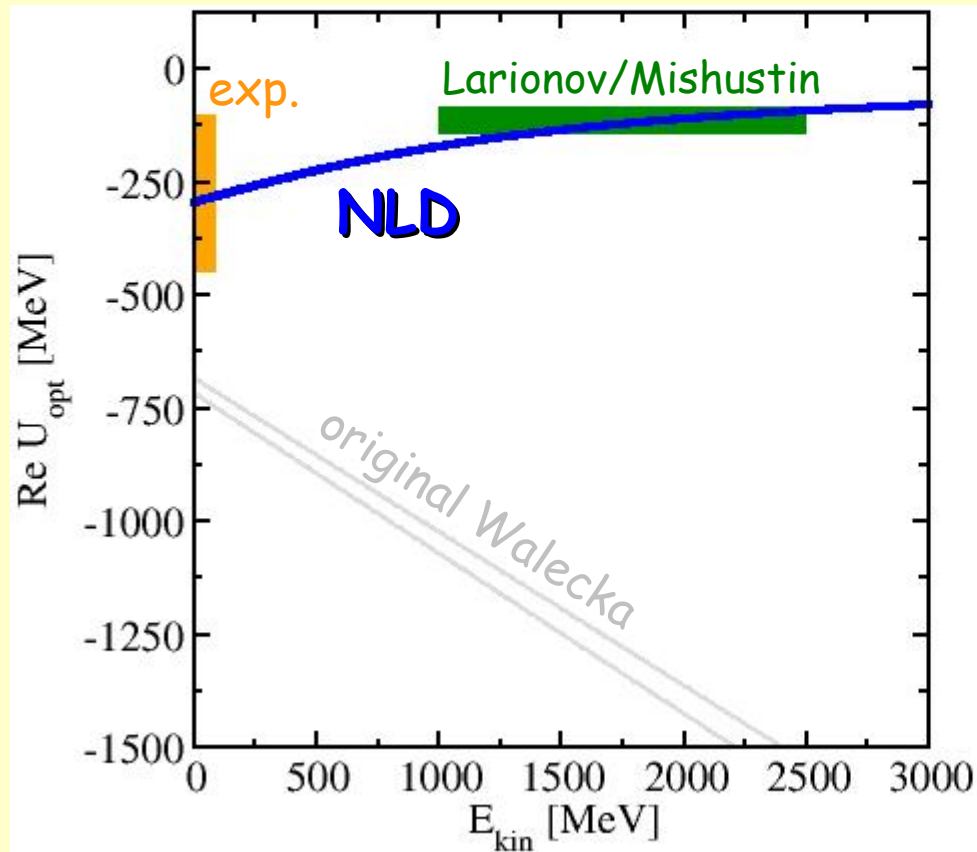
Basic properties: nuclear EoS & opt. potentials...

In-medium anti-proton SEP (real part)



Basic properties: nuclear EoS & opt. potentials...

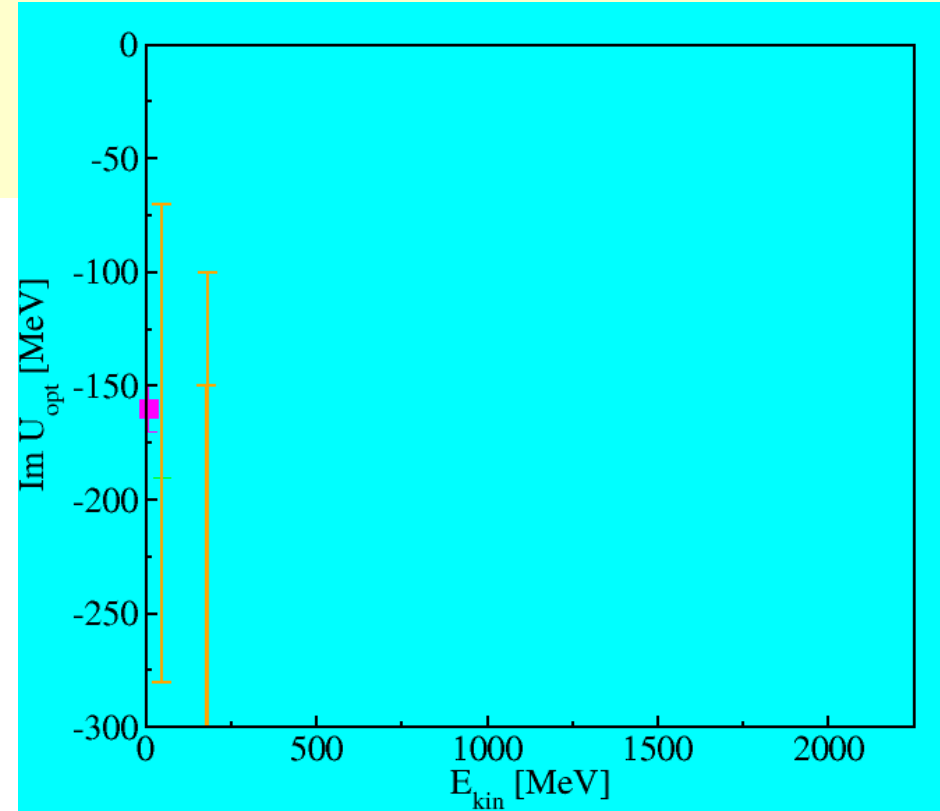
In-medium anti-proton SEP (real part)



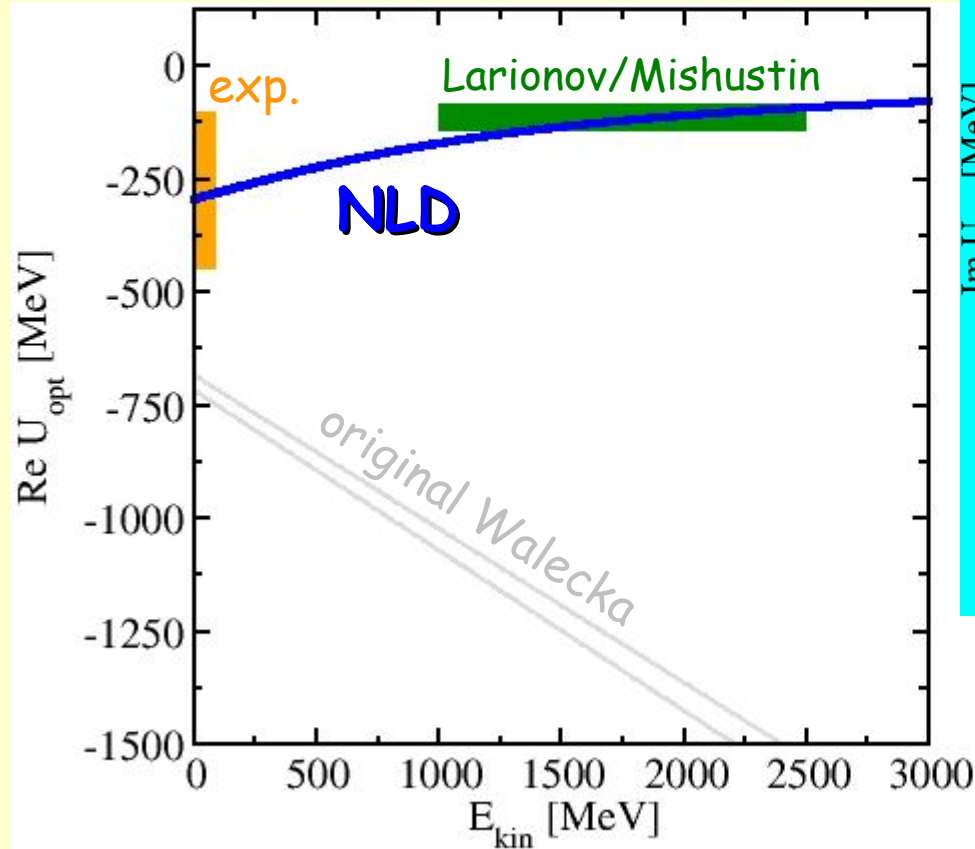
Also: NLD provides the imaginary part of SEP for anti-proton in-medium interactions using dispersion relation (without subtractions)

Basic properties: nuclear EoS & opt. potentials...

In-medium anti-proton SEP (imag. part)



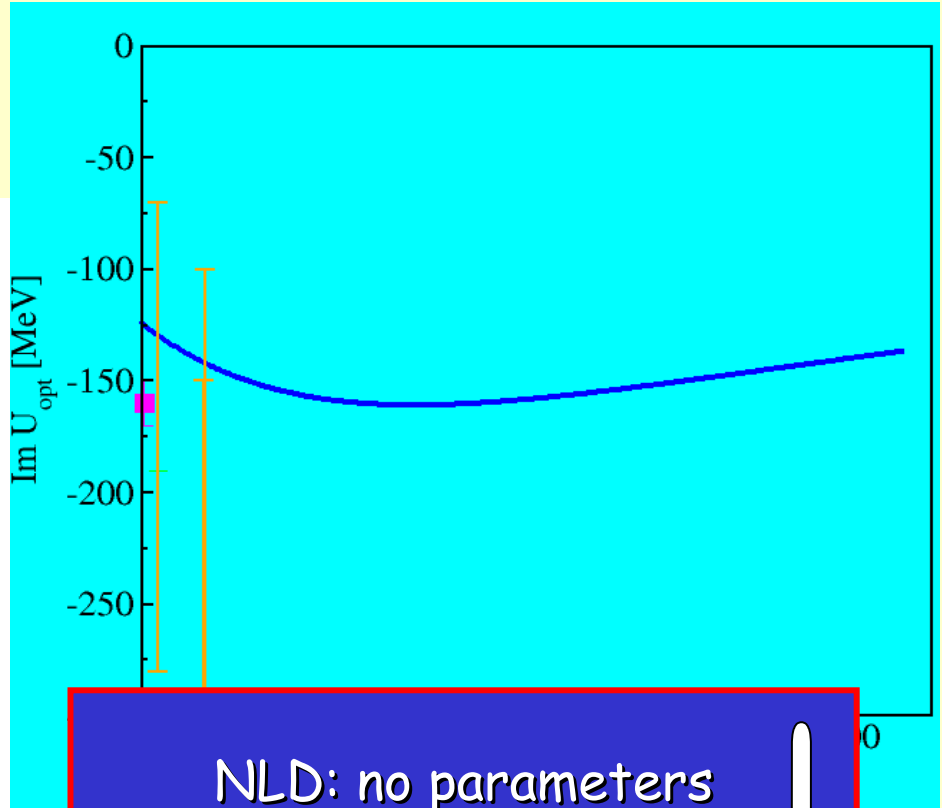
In-medium anti-proton SEP (real part)



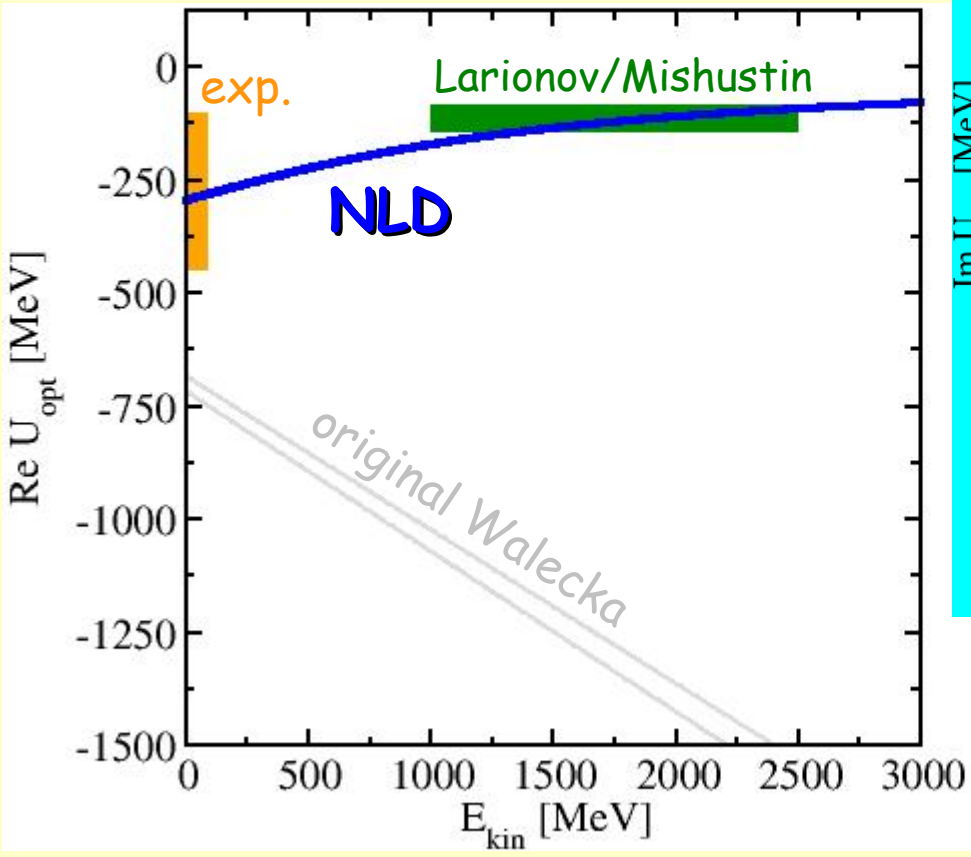
Also: NLD provides the imaginary part of SEP for anti-proton in-medium interactions using dispersion relation (without subtractions)

Basic properties: nuclear EoS & opt. potentials...

In-medium anti-proton SEP (imag. part)



In-medium anti-proton SEP (real part)



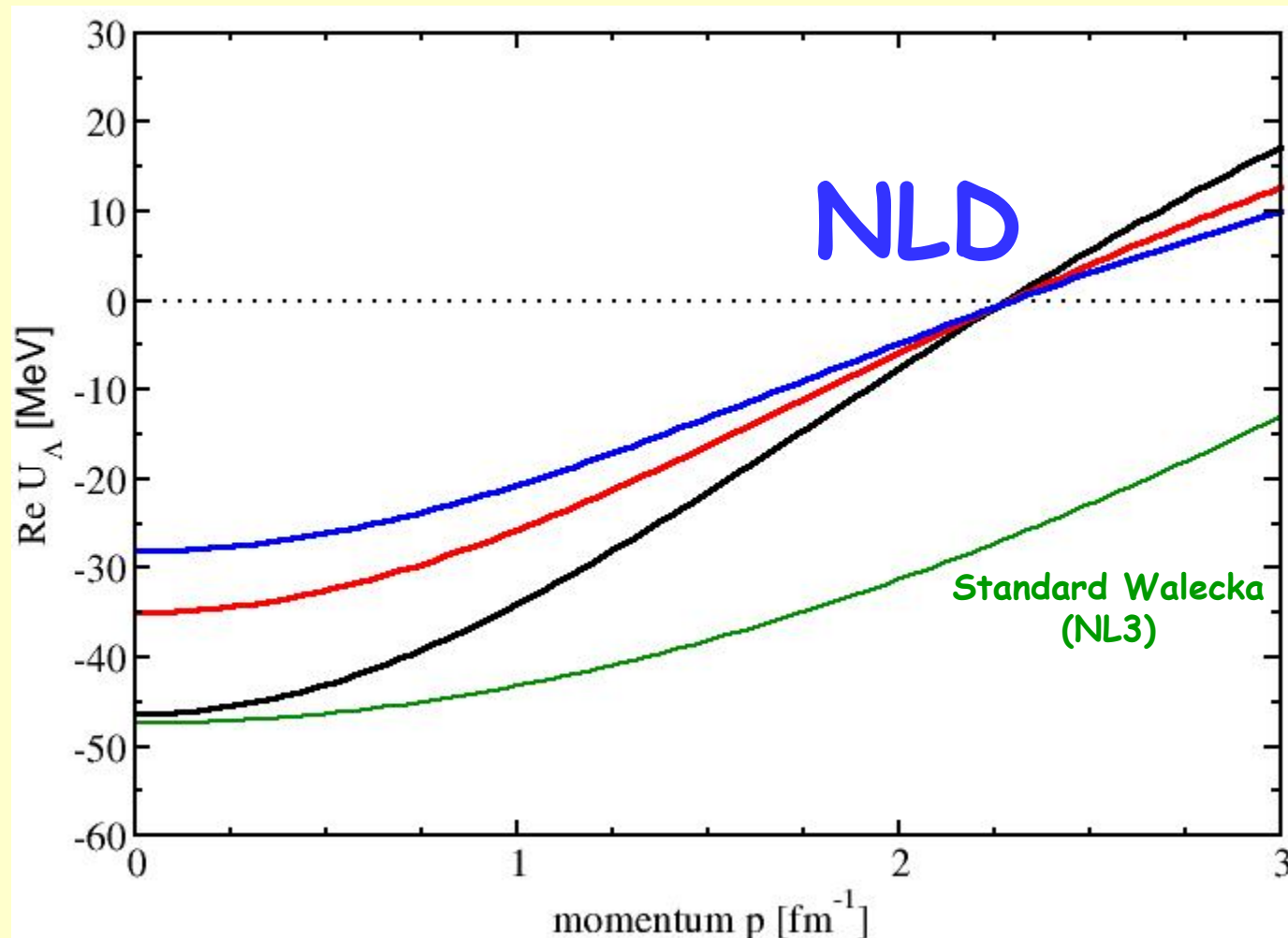
NLD: no parameters
good description of
phenomenology
also for in-medium
anti-proton interaction

Also: NLD provides the imaginary part of SEP for anti-p using dispersion relation (without subtractions)

Hyperon properties: optical potentials...

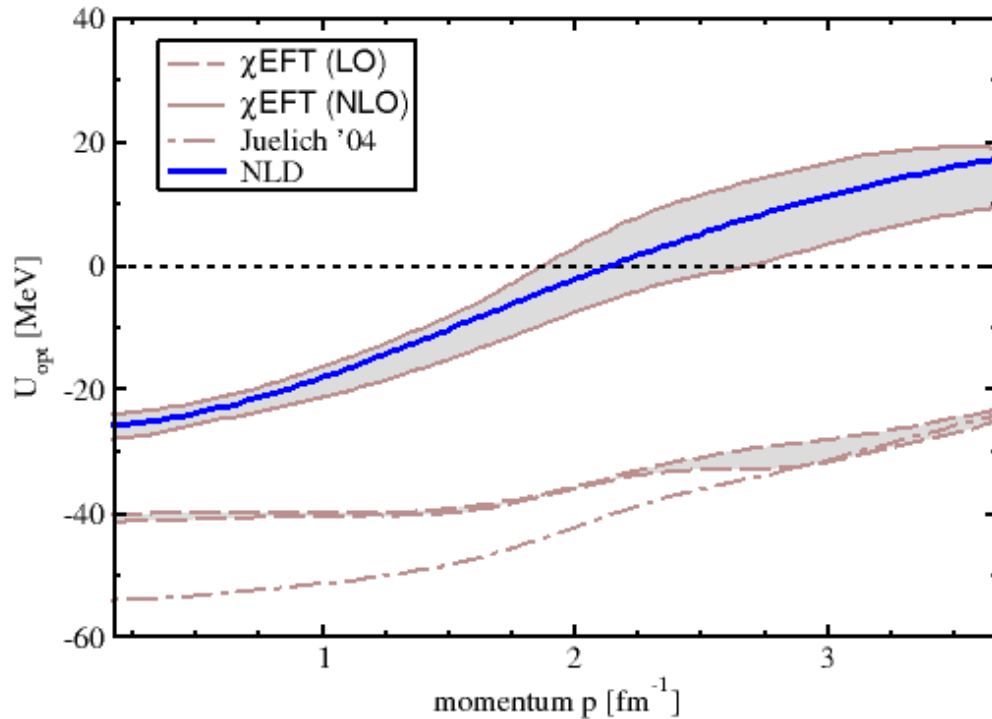
NLD + SU(6) for standard meson-nucleon couplings

Hyperon cut-off regulates MDI



Hyperon properties: Λ -optical potentials...

SU(6) for standard meson-nucleon couplings + NLD (monopole forms)
SNM, saturation density, adjust to χ EFT

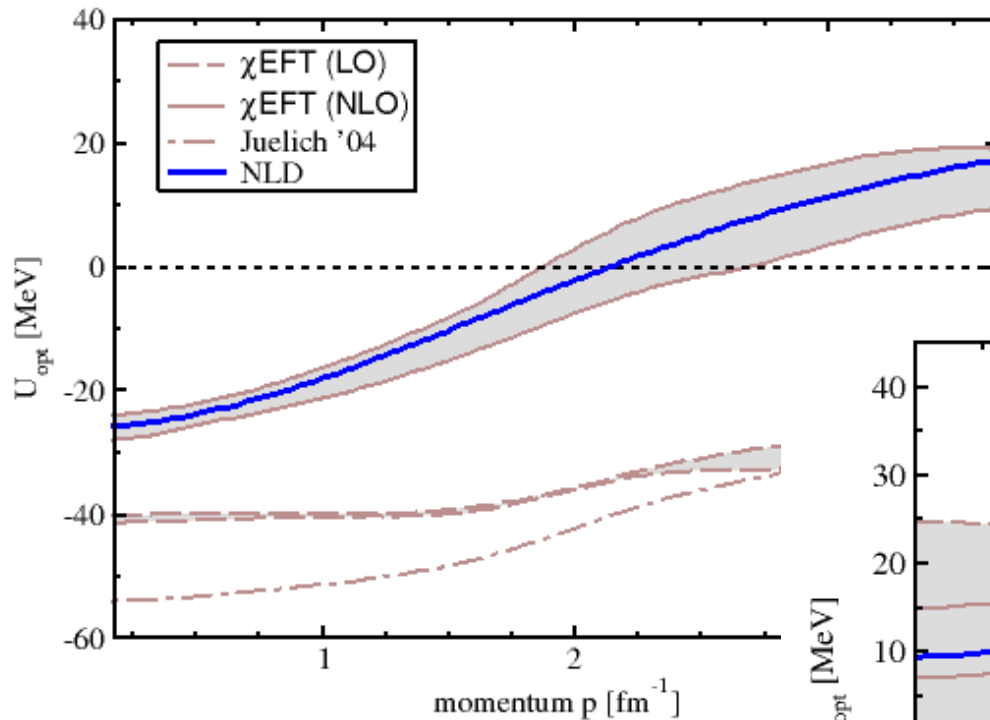


Λ U_{opt} : cut-offs ~ 0.75 GeV

Hyperon properties: Λ, Σ -optical potentials...

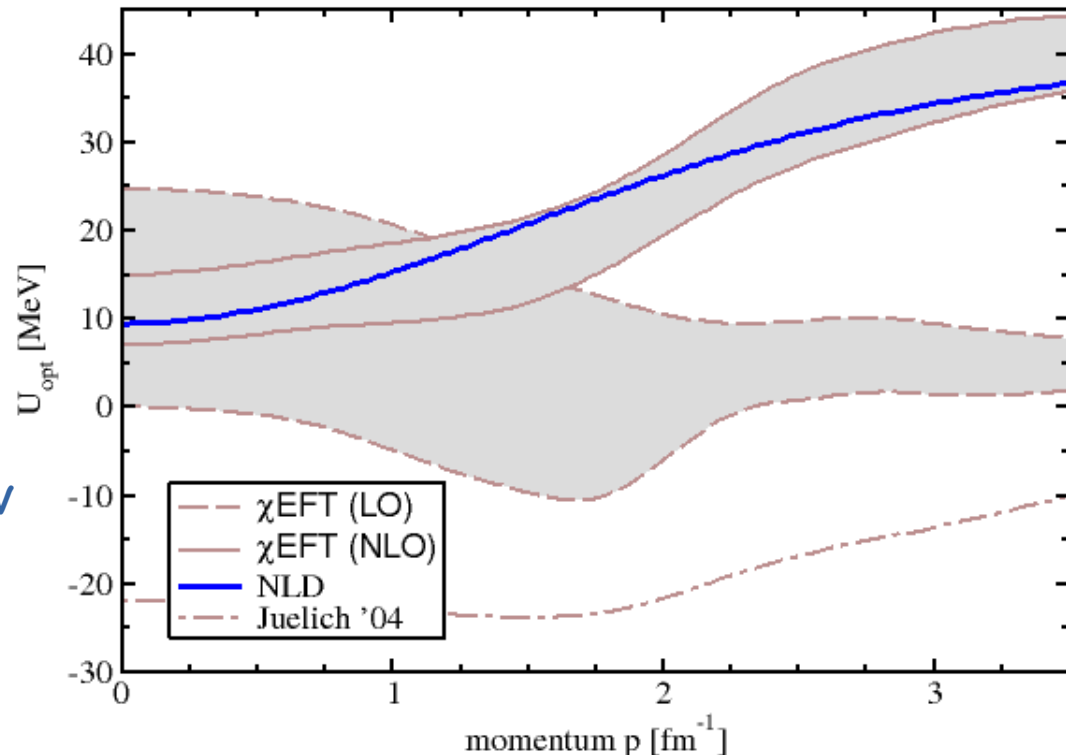
SU(6) for standard meson-nucleon couplings + NLD (monopole forms)
SNM, saturation density, adjust to χ EFT

χ EFT: EPJA52 (2016) 15



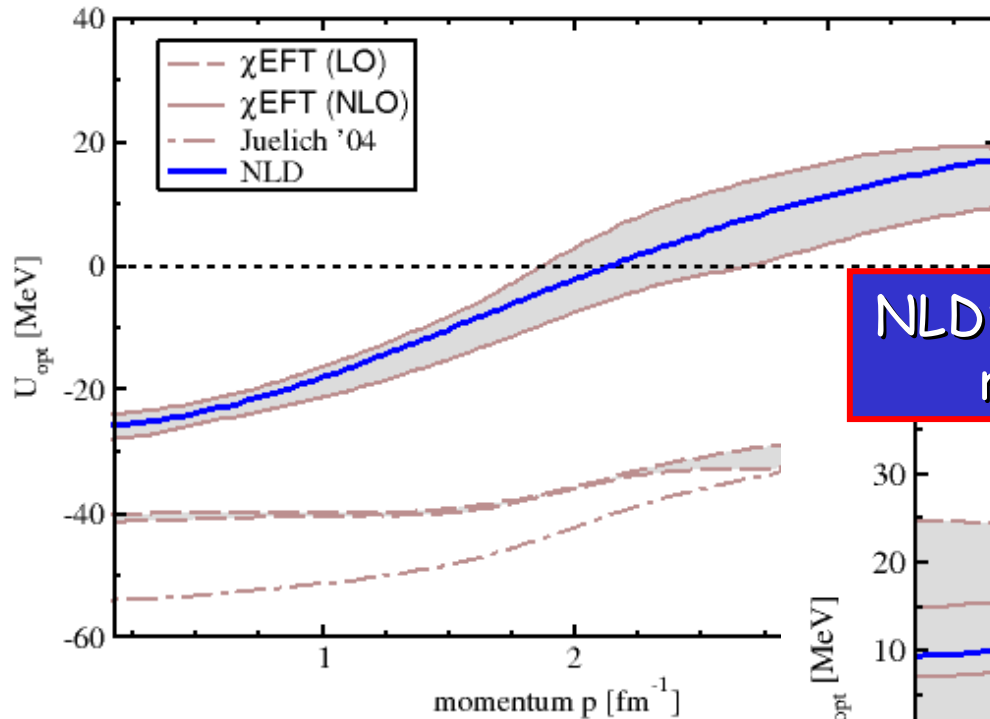
Λ U_{opt} : cut-offs ~ 0.78 GeV

Σ U_{opt} : cut-offs ~ 0.8 GeV



Hyperon properties: Λ, Σ -optical potentials...

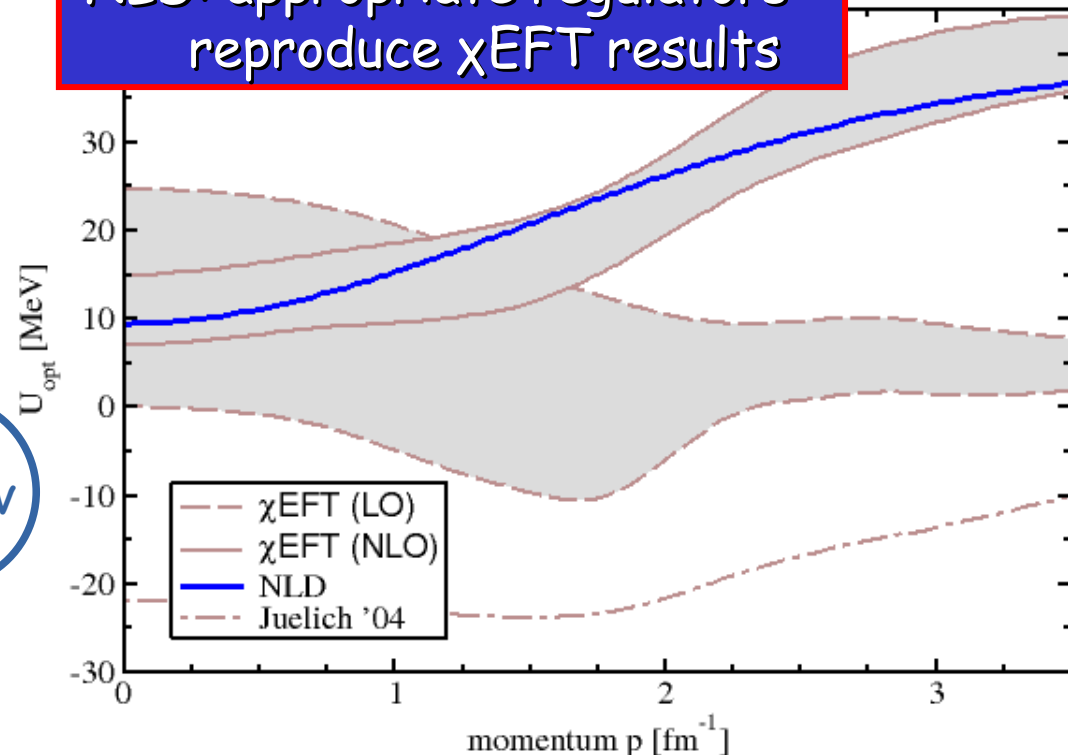
SU(6) for standard meson-nucleon couplings + NLD (monopole forms)
SNM, saturation density, adjust to χ EFT



χ EFT: EPJA52 (2016) 15

Λ U_{opt} : cut-offs ~ 0.78 GeV

NLD: appropriate regulators reproduce χ EFT results

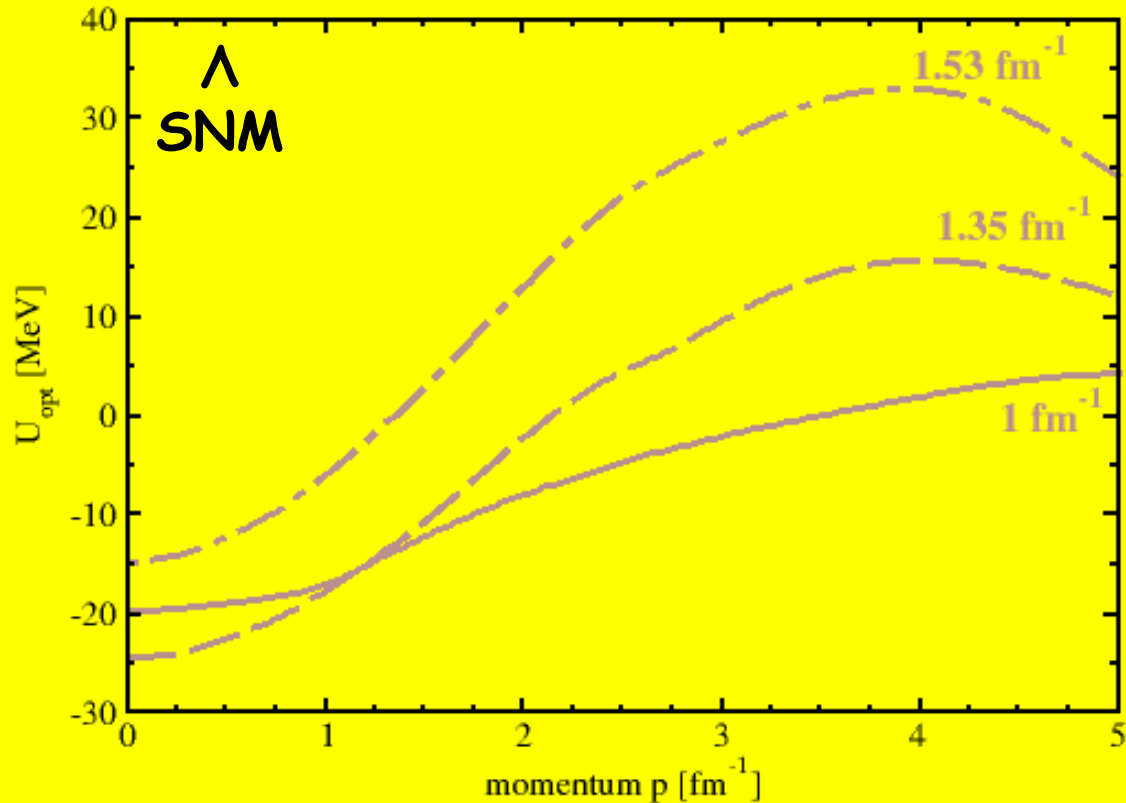


Σ U_{opt} : cut-offs ~ 0.8 GeV

Hyperon properties: Λ -optical potentials...

NLD predictions: density & momentum dependence

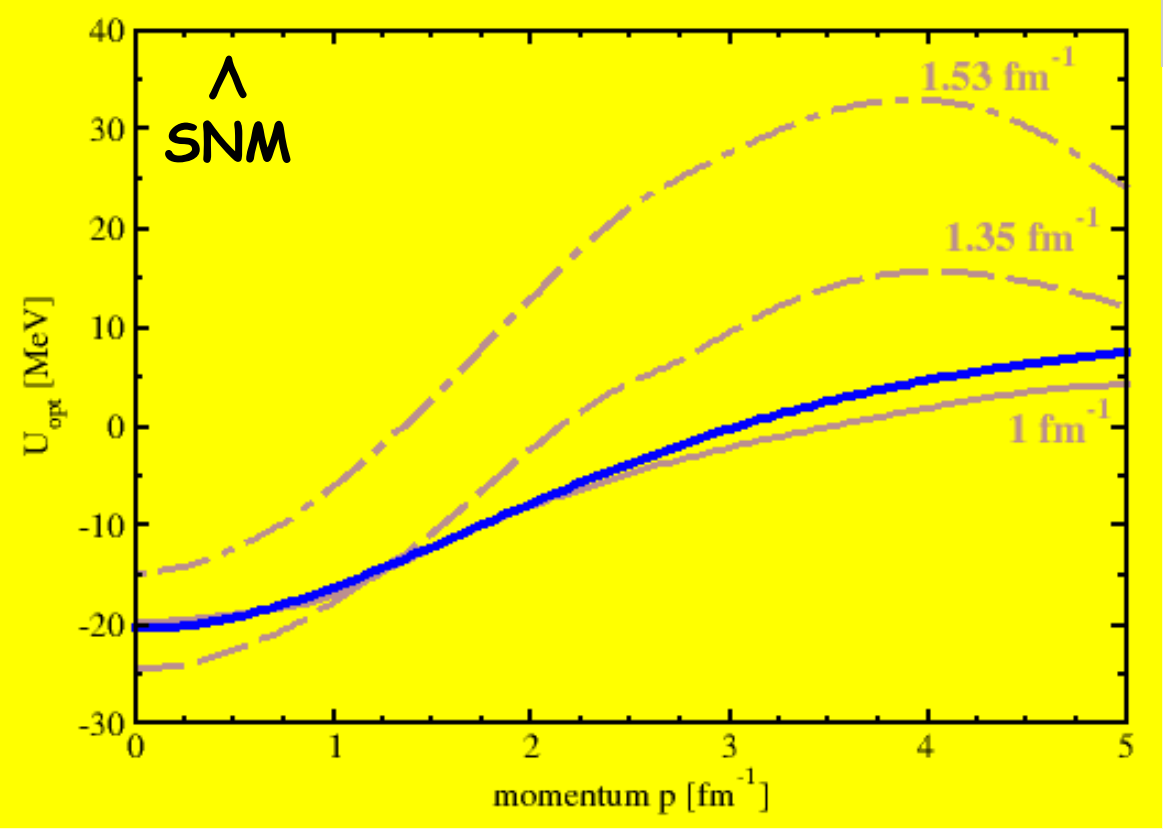
χ EFT: EPJA52 (2016) 15



Hyperon properties: Λ -optical potentials...

NLD predictions: density & momentum dependence

χ EFT: EPJA52 (2016) 15

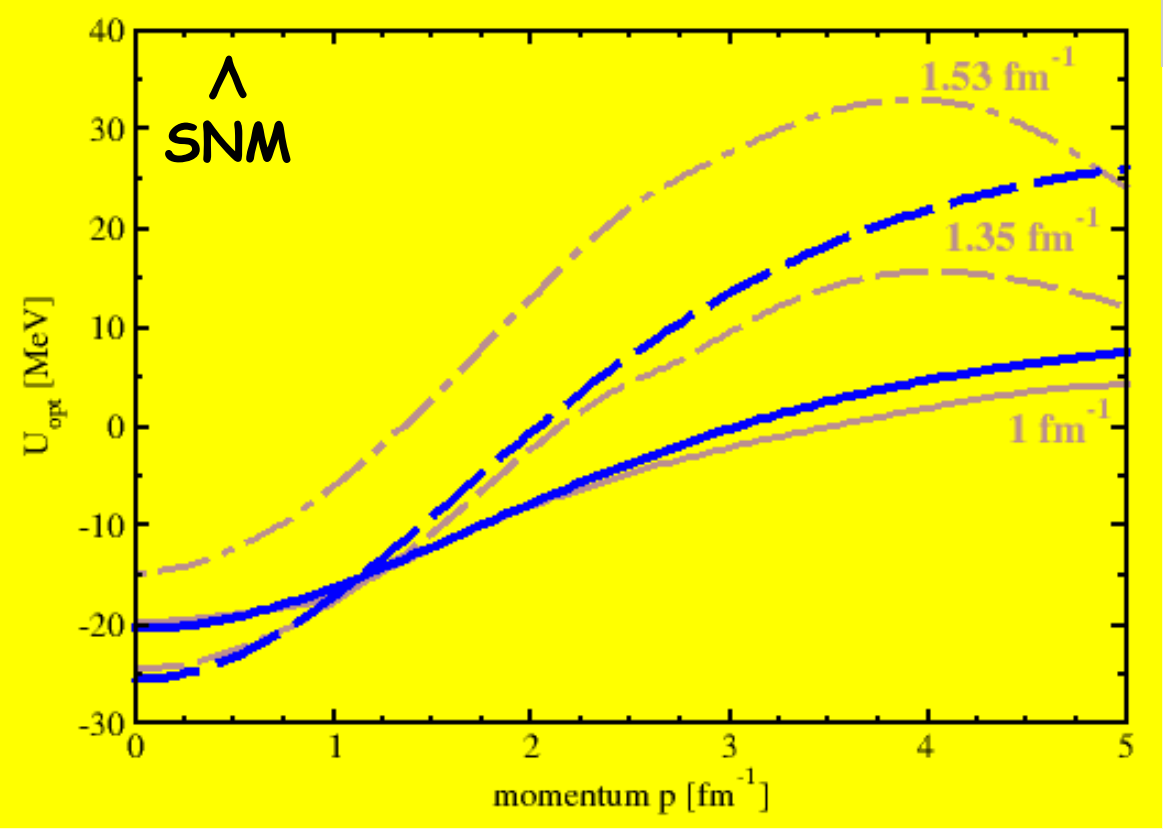


NLD results

Hyperon properties: Λ -optical potentials...

NLD predictions: density & momentum dependence

χ EFT: EPJA52 (2016) 15

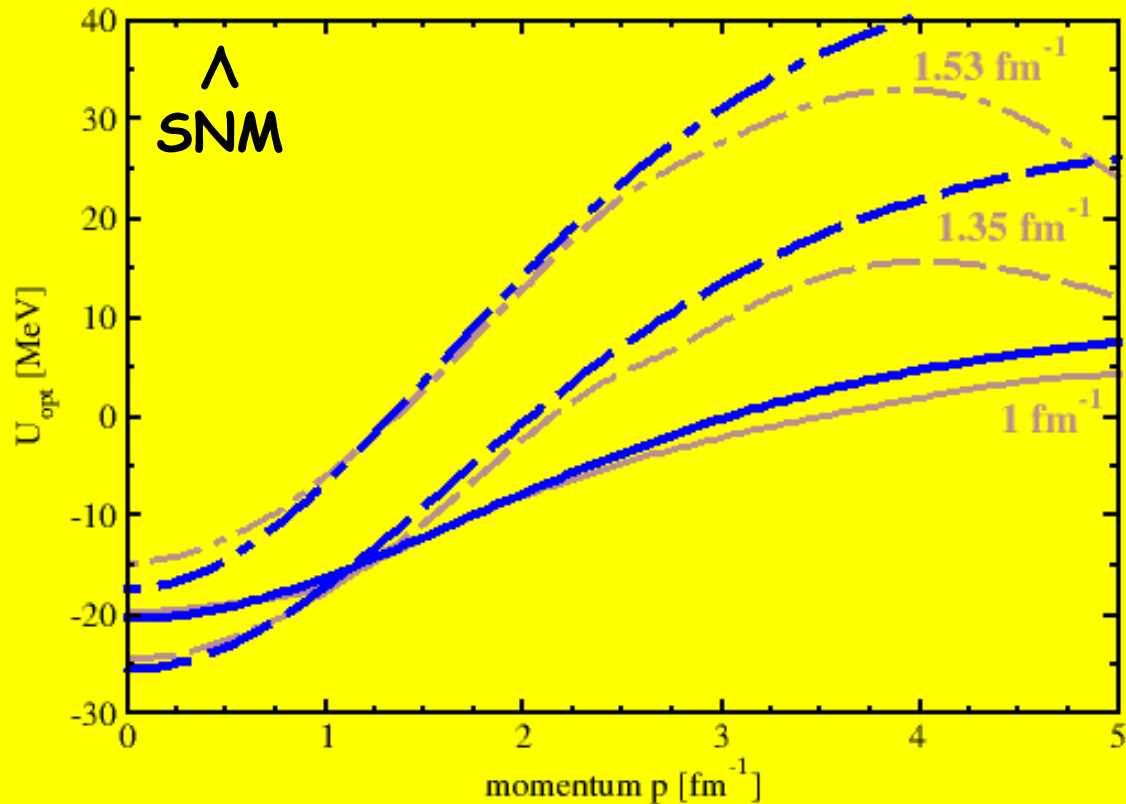


NLD results

Hyperon properties: Λ -optical potentials...

NLD predictions: density & momentum dependence

χ EFT: EPJA52 (2016) 15

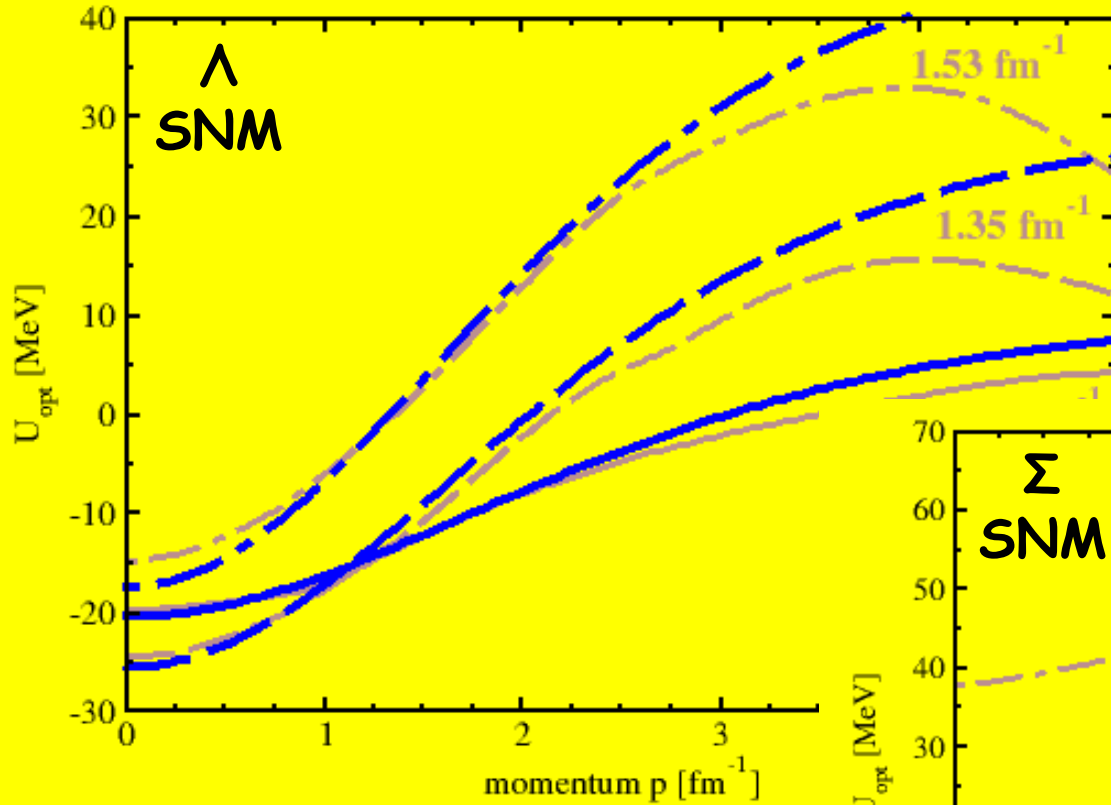


NLD results

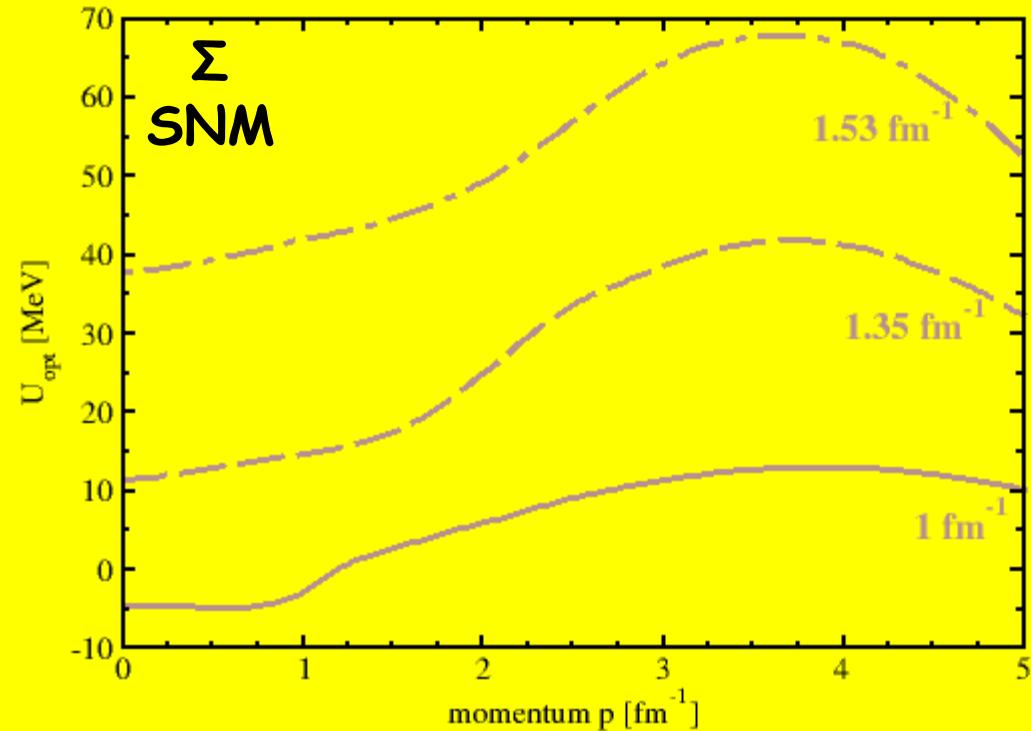
Hyperon properties: Λ, Σ -optical potentials...

NLD predictions: density & momentum dependence

χ EFT: EPJA52 (2016) 15



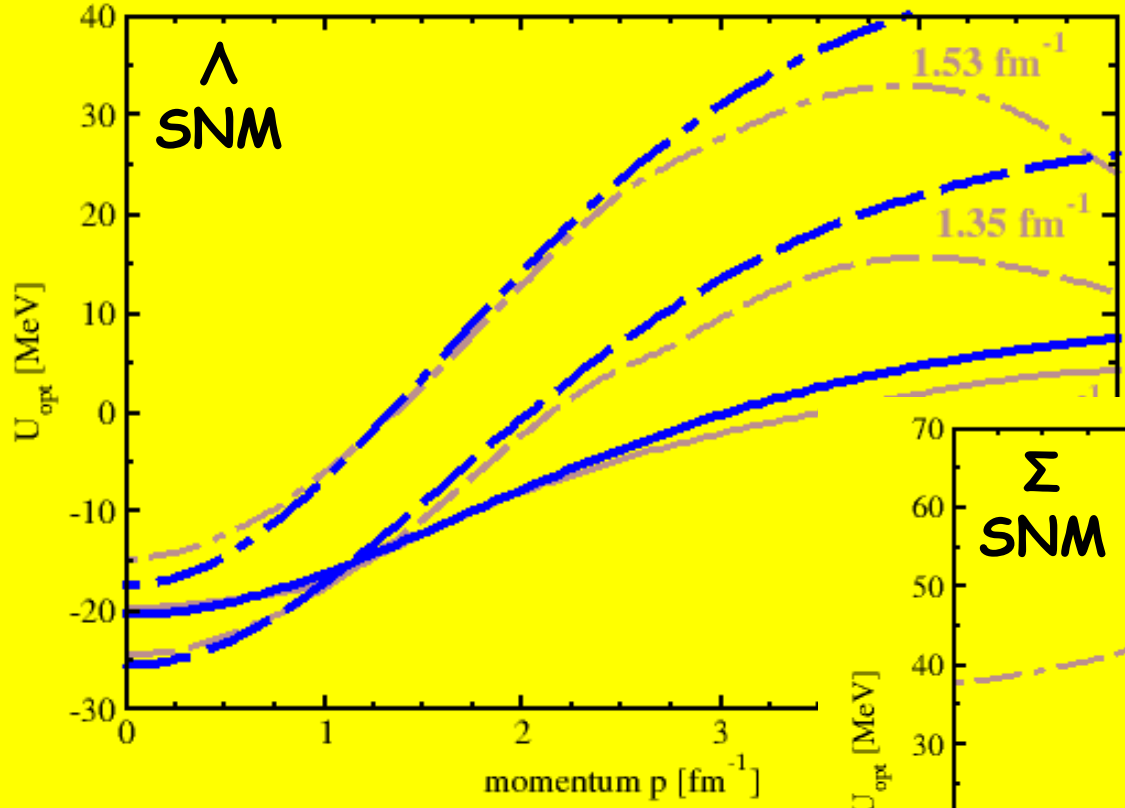
NLD results



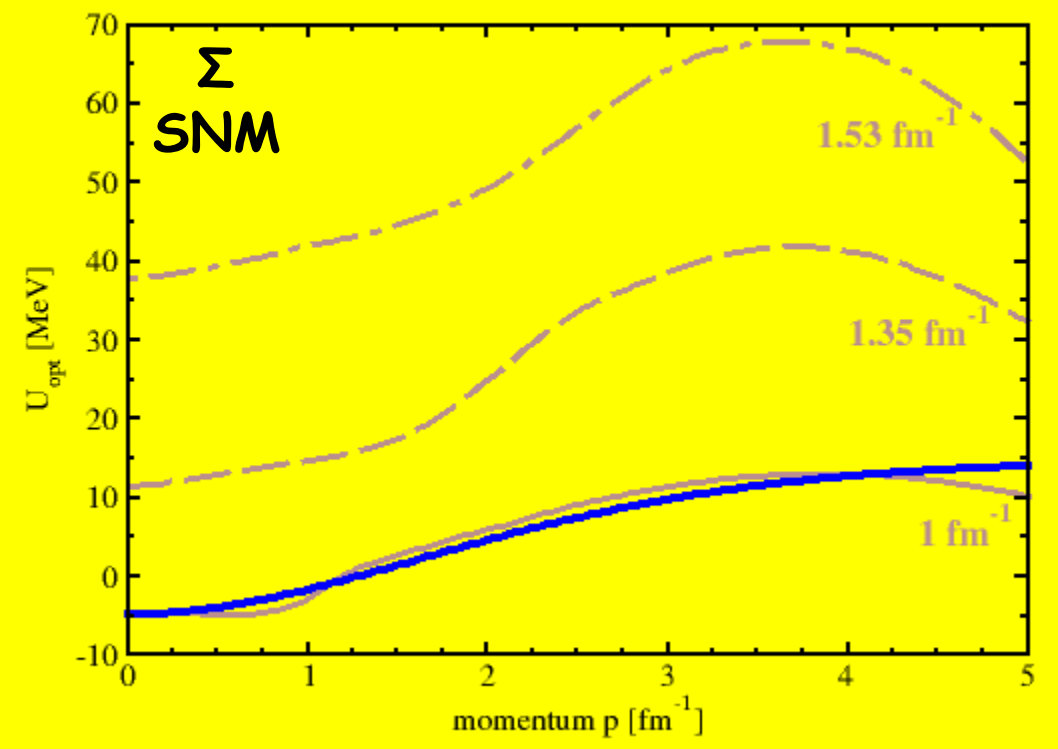
Hyperon properties: Λ, Σ -optical potentials...

NLD predictions: density & momentum dependence

χ EFT: EPJA52 (2016) 15



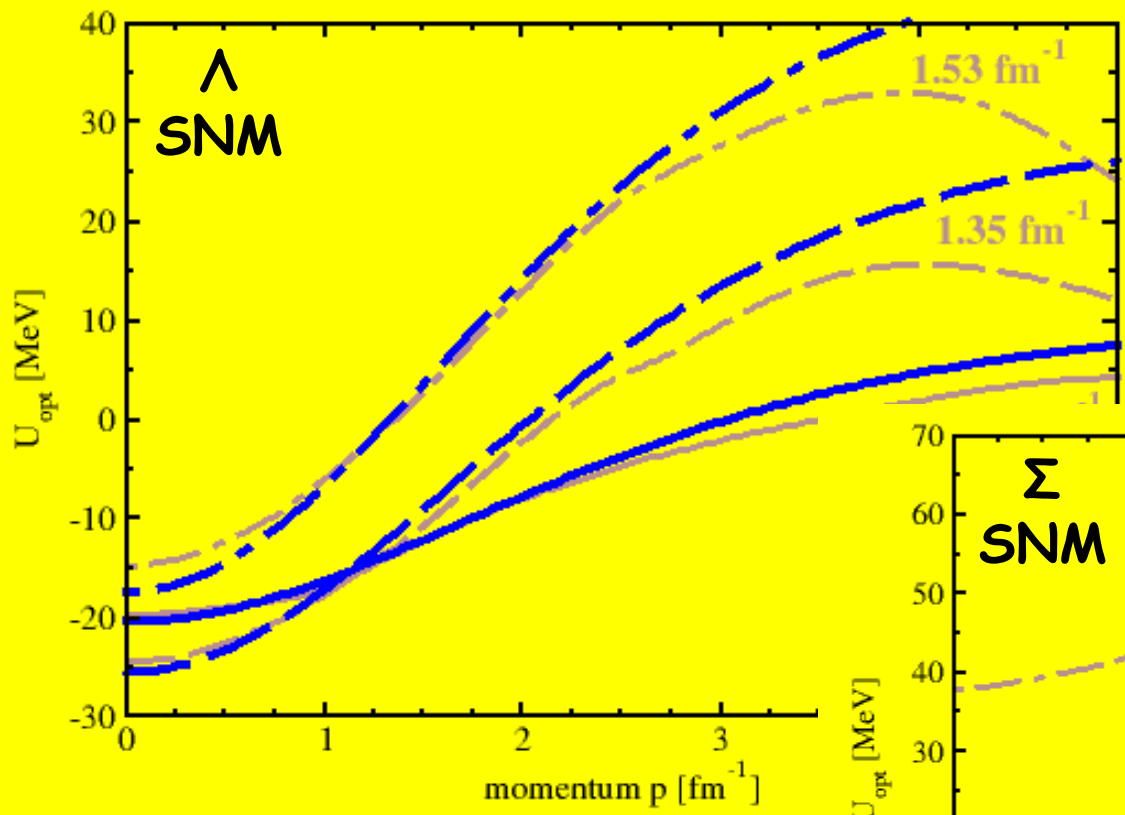
NLD results



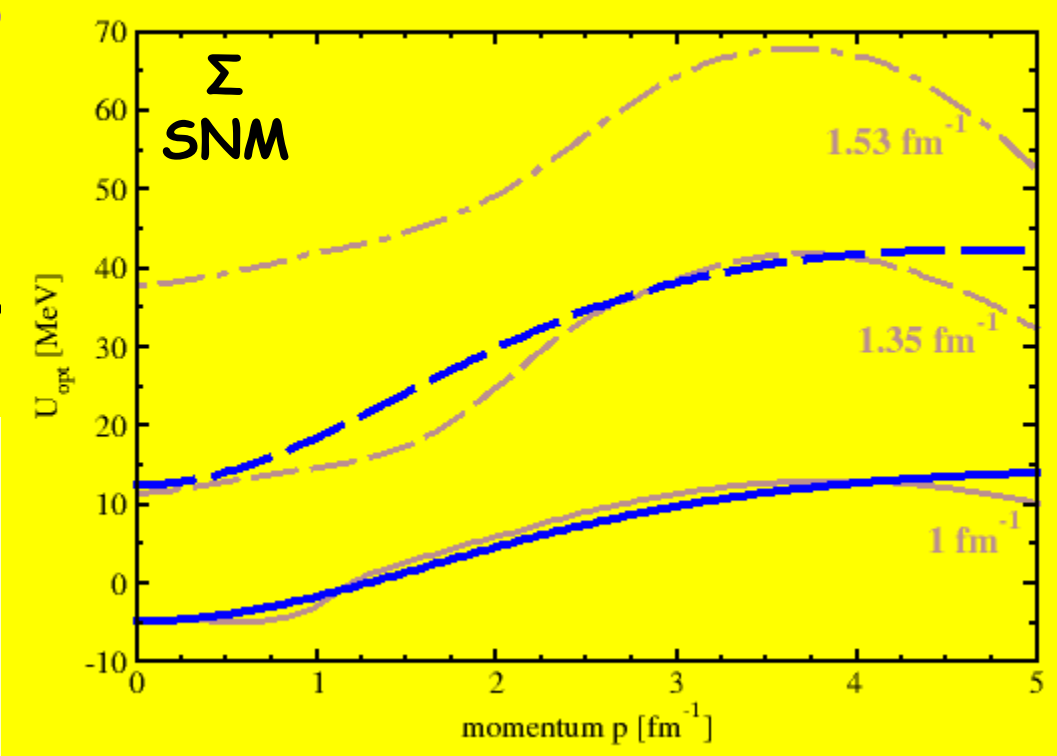
Hyperon properties: Λ, Σ -optical potentials...

NLD predictions: density & momentum dependence

χ EFT: EPJA52 (2016) 15



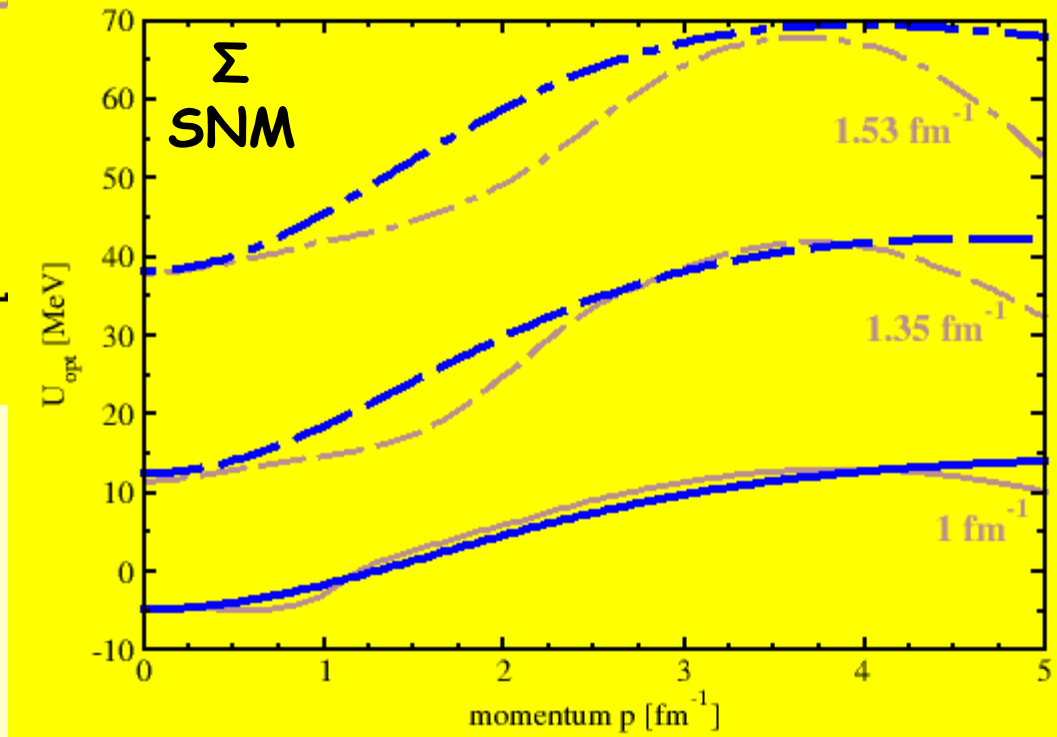
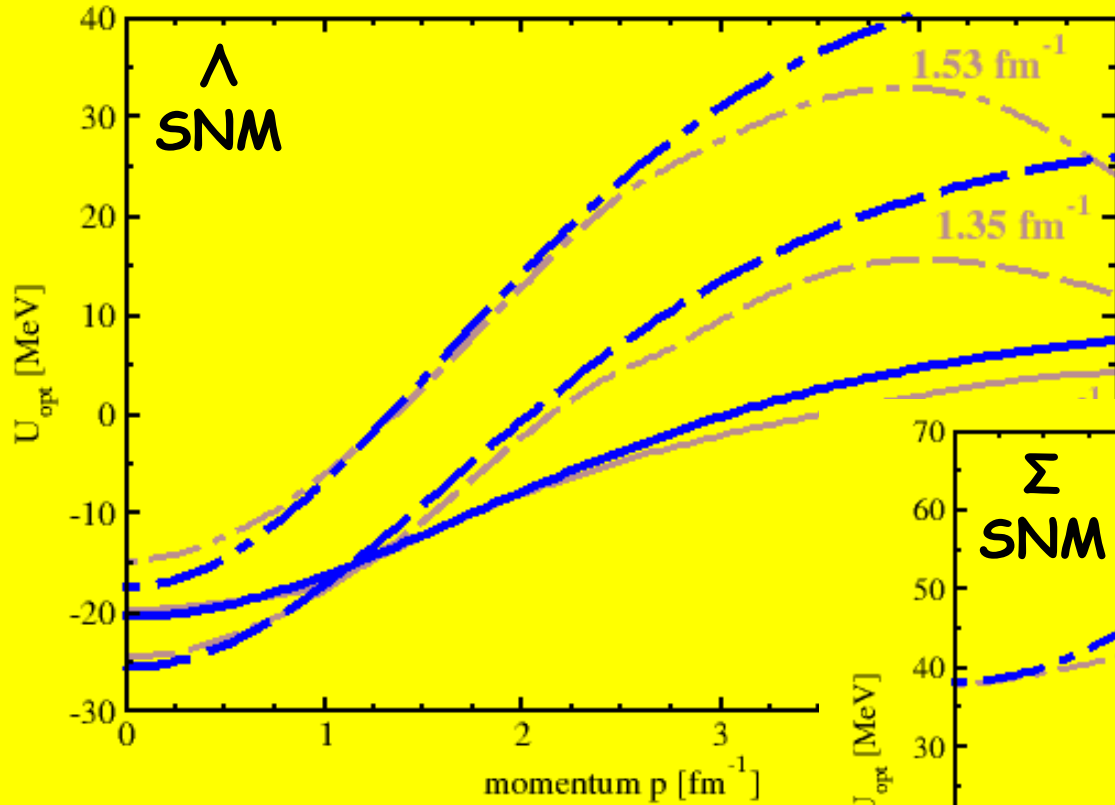
NLD results



Hyperon properties: Λ, Σ -optical potentials...

NLD predictions: density & momentum dependence

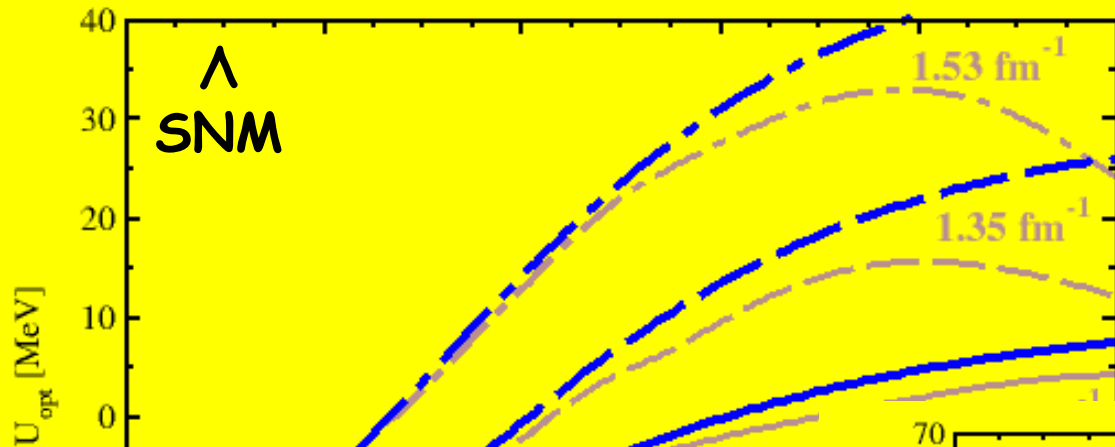
χ EFT: EPJA52 (2016) 15



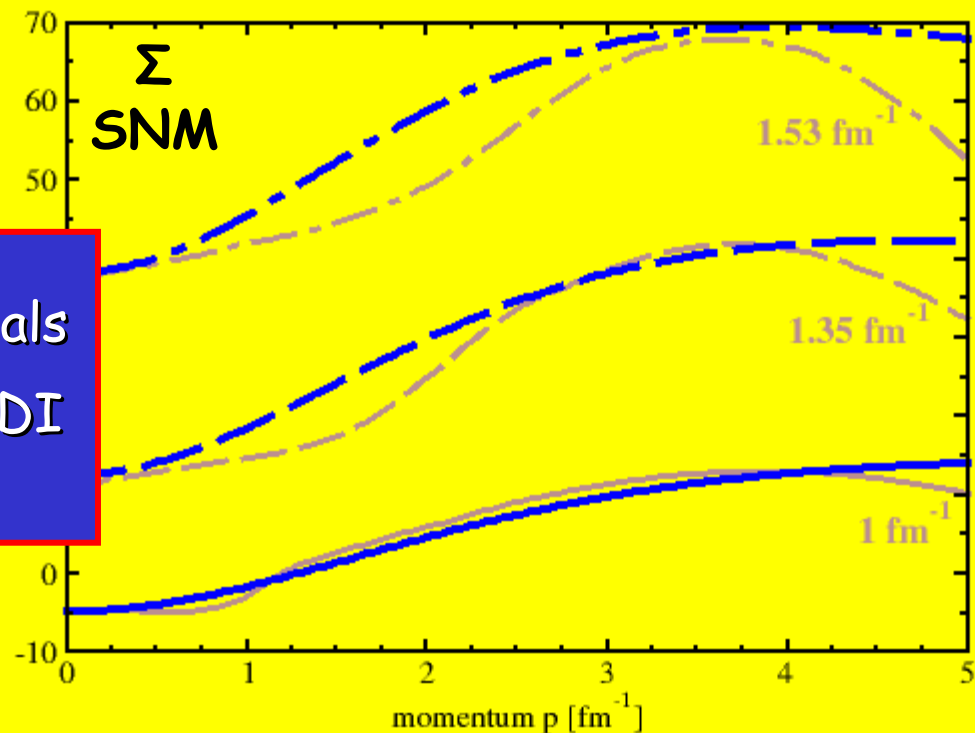
Hyperon properties: Λ, Σ -optical potentials...

NLD predictions: density & momentum dependence

χ EFT: EPJA52 (2016) 15



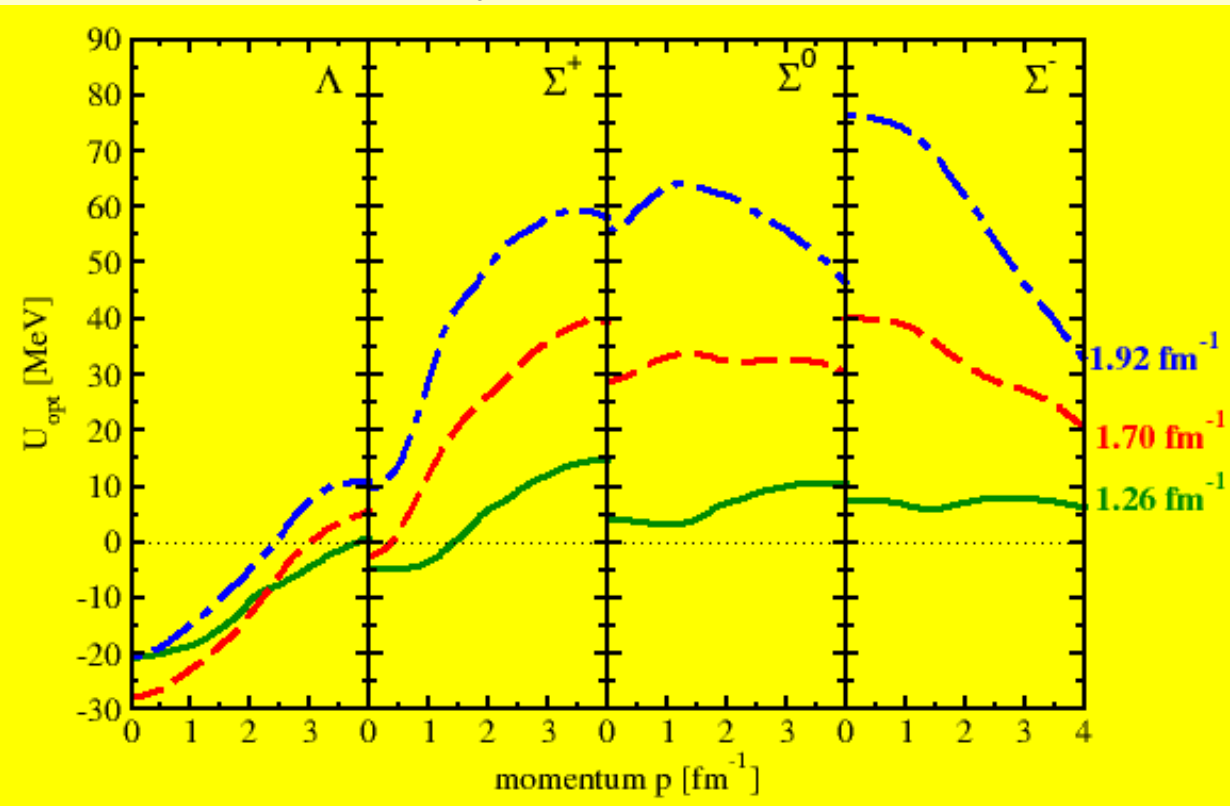
NLD results



NLD: Λ, Σ in-medium potentials predicts non-trivial DD & MDI according χ -EFT

Hyperon properties: Λ, Σ -optical potentials...

NL ρ predictions: density & momentum dependence
pure neutron matter



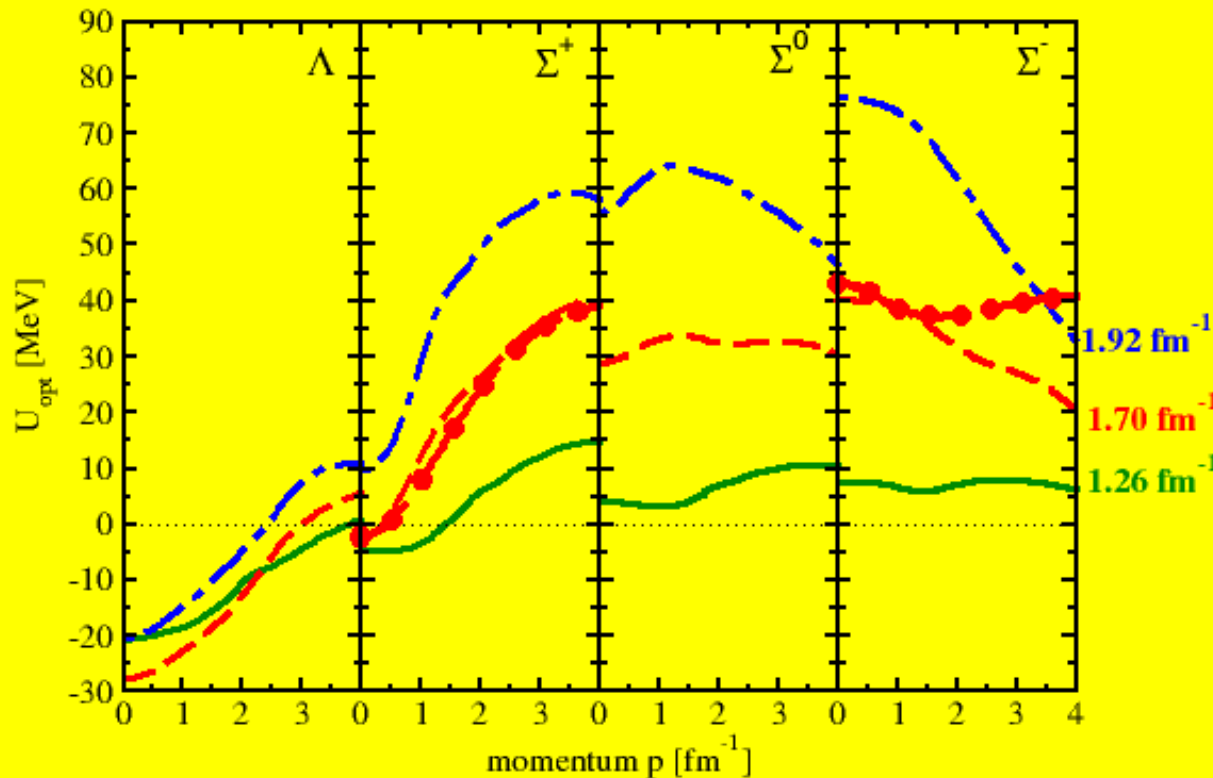
χ EFT: EPJA52 (2016) 15

χ -EFT: non-trivial MDI

Hyperon properties: Λ, Σ -optical potentials...

NLD fit:

density & momentum dependence
pure neutron matter

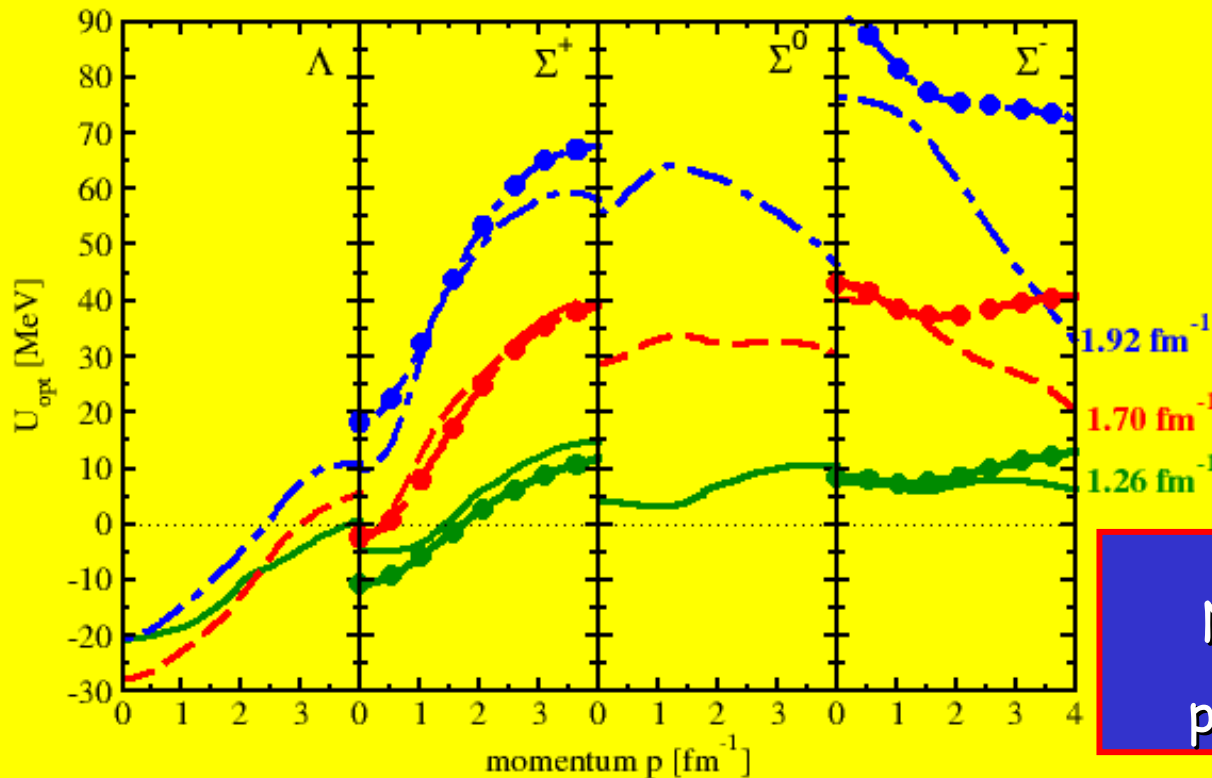


Curves: χ -EFT
symbols: NLD

χ -EFT: non-trivial MDI

Hyperon properties: Λ, Σ -optical potentials...

NLD predictions: density & momentum dependence
pure neutron matter



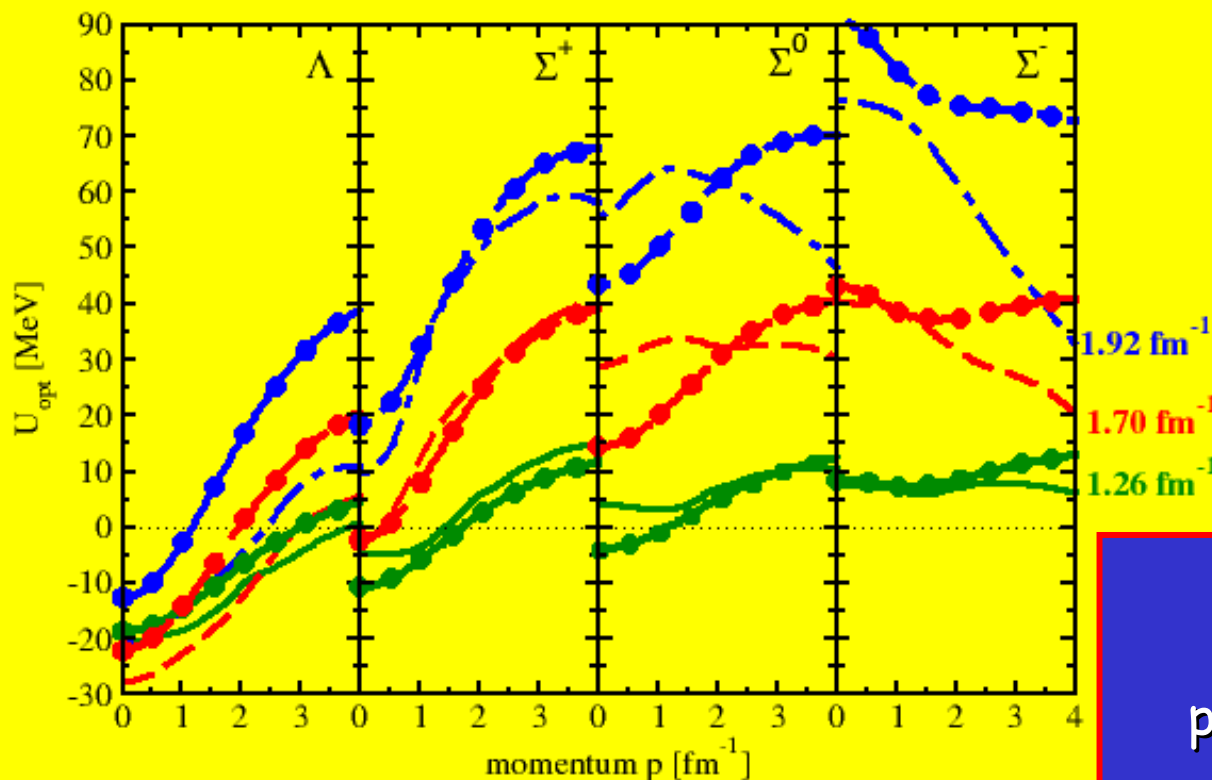
Curves: χ -EFT
symbols: NLD

χ -EFT: non-trivial MDI

NLD: charged hyperons
predicts non-trivial MDI

Hyperon properties: Λ, Σ -optical potentials...

NLD predictions: density & momentum dependence
pure neutron matter



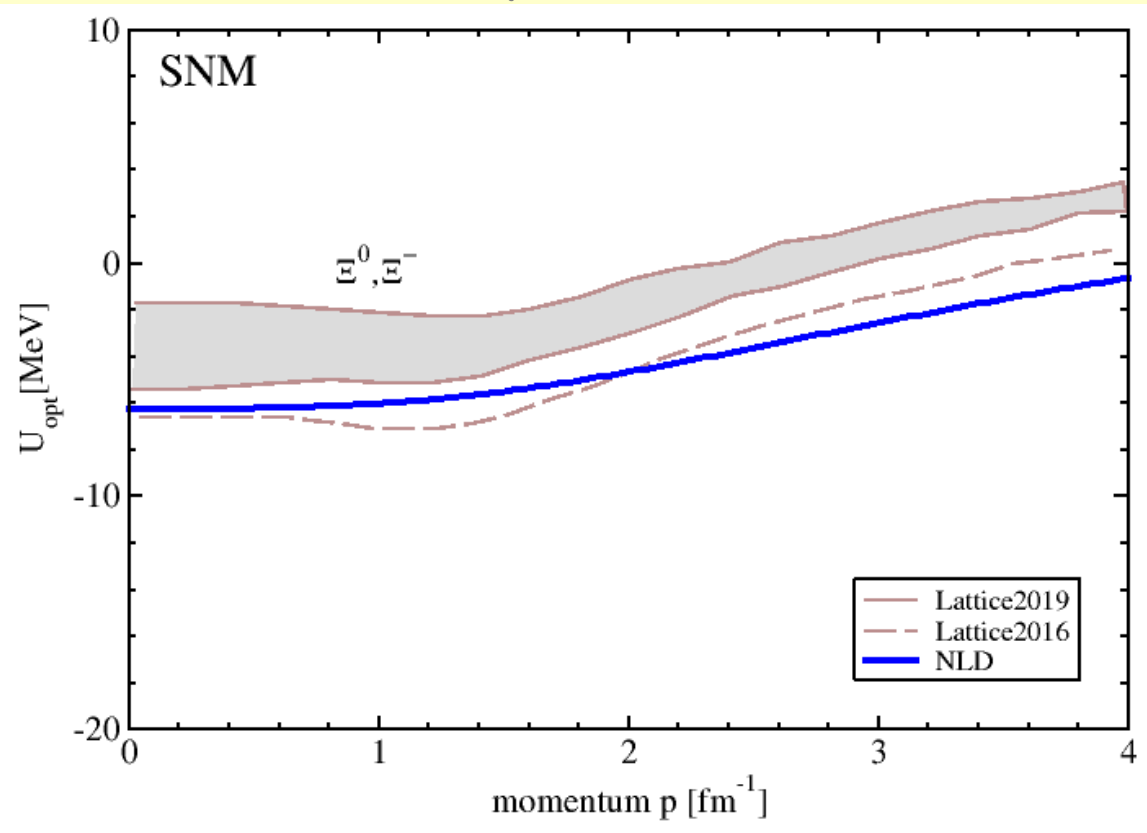
Curves: χ -EFT
symbols: NLD

χ -EFT: non-trivial MDI

NLD: all hyperons
predicts non-trivial MDI
adequate description

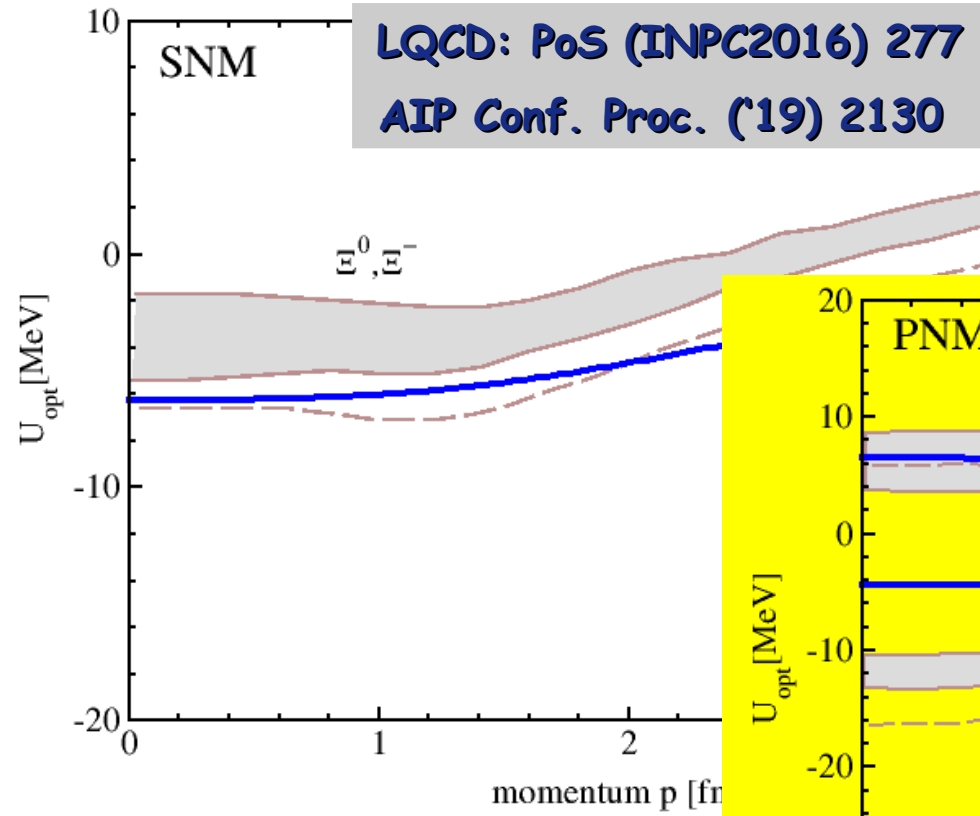
Hyperon properties: Ξ -optical potentials...

NLD fit: density & momentum dependence
symmetric NM

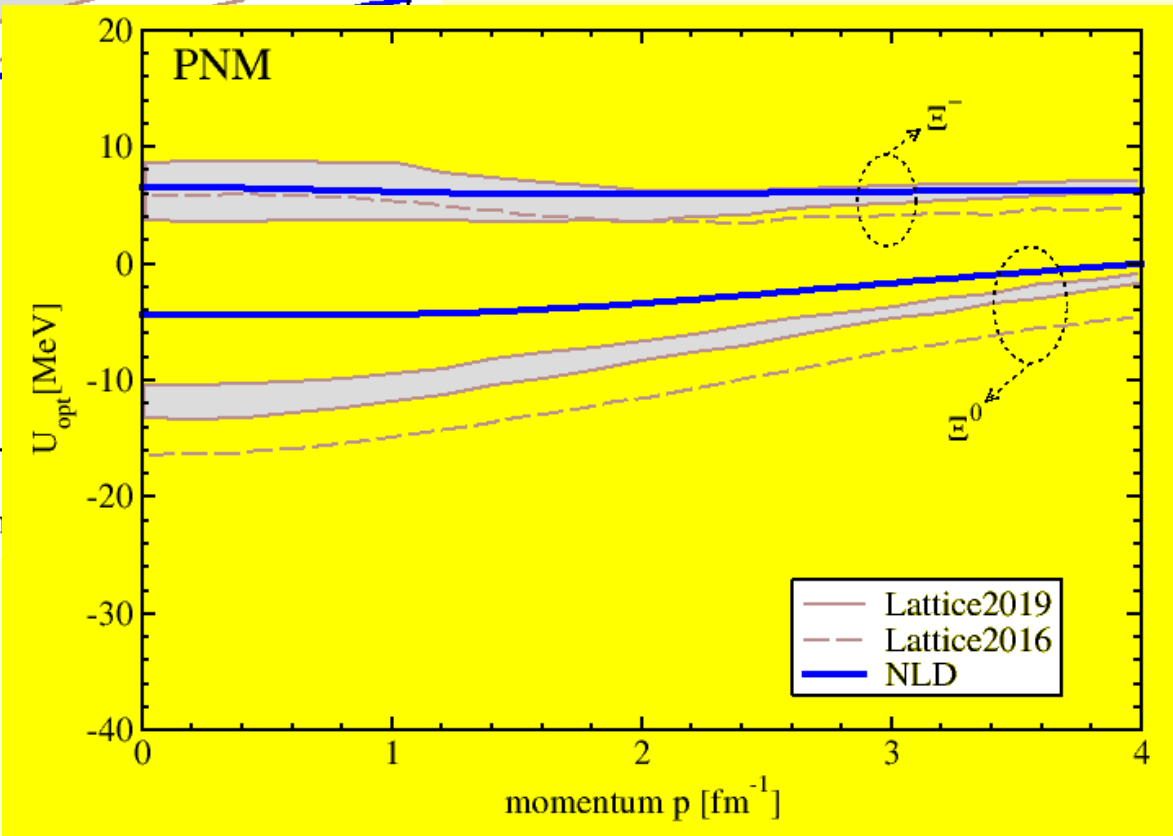


Hyperon properties: Ξ -optical potentials...

NLD predictions: density & momentum dependence
SNM & pure neutron matter



NLD: Ξ hyperons
predicts weak MD



Anti-Hyperon properties: optical potentials...

NLD predictions: density & momentum dependence
G-parity

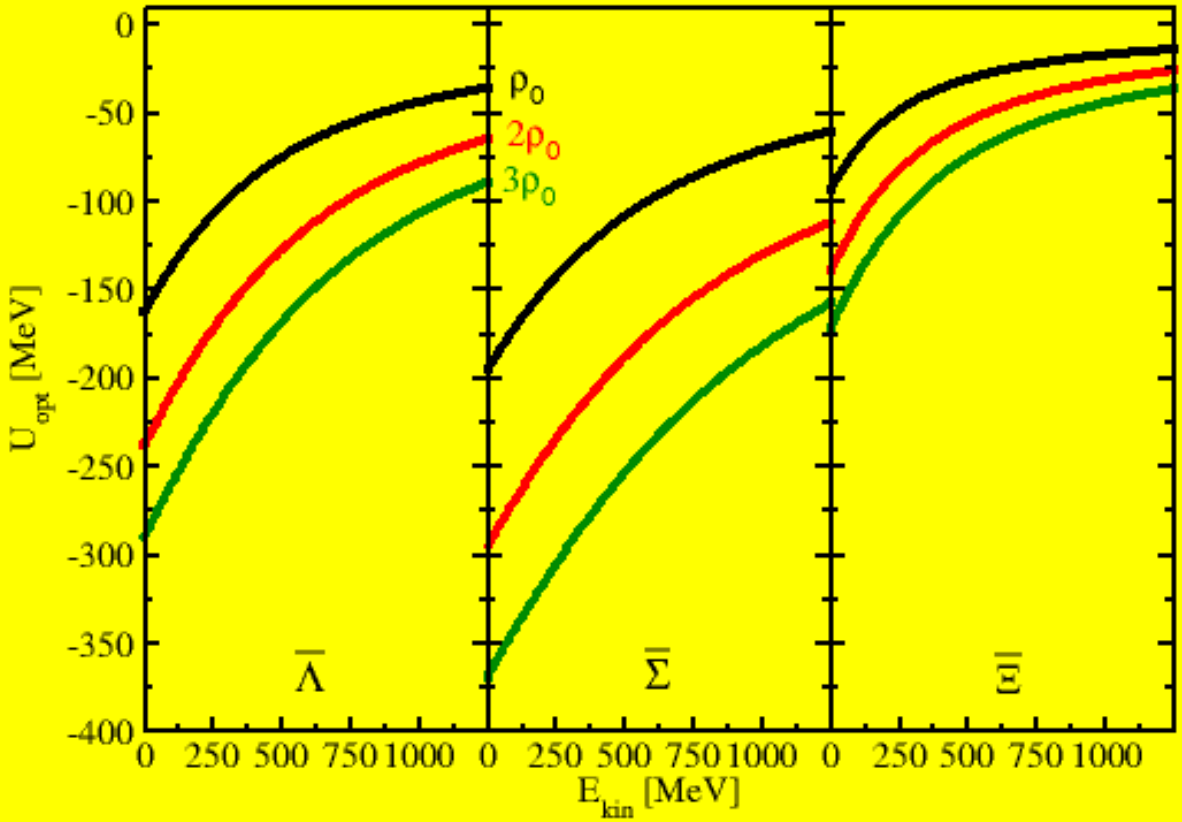
Anti-Hyperon properties: optical potentials...

NLD predictions: density & momentum dependence
G-parity, no parameters

Anti-Hyperon properties: optical potentials...

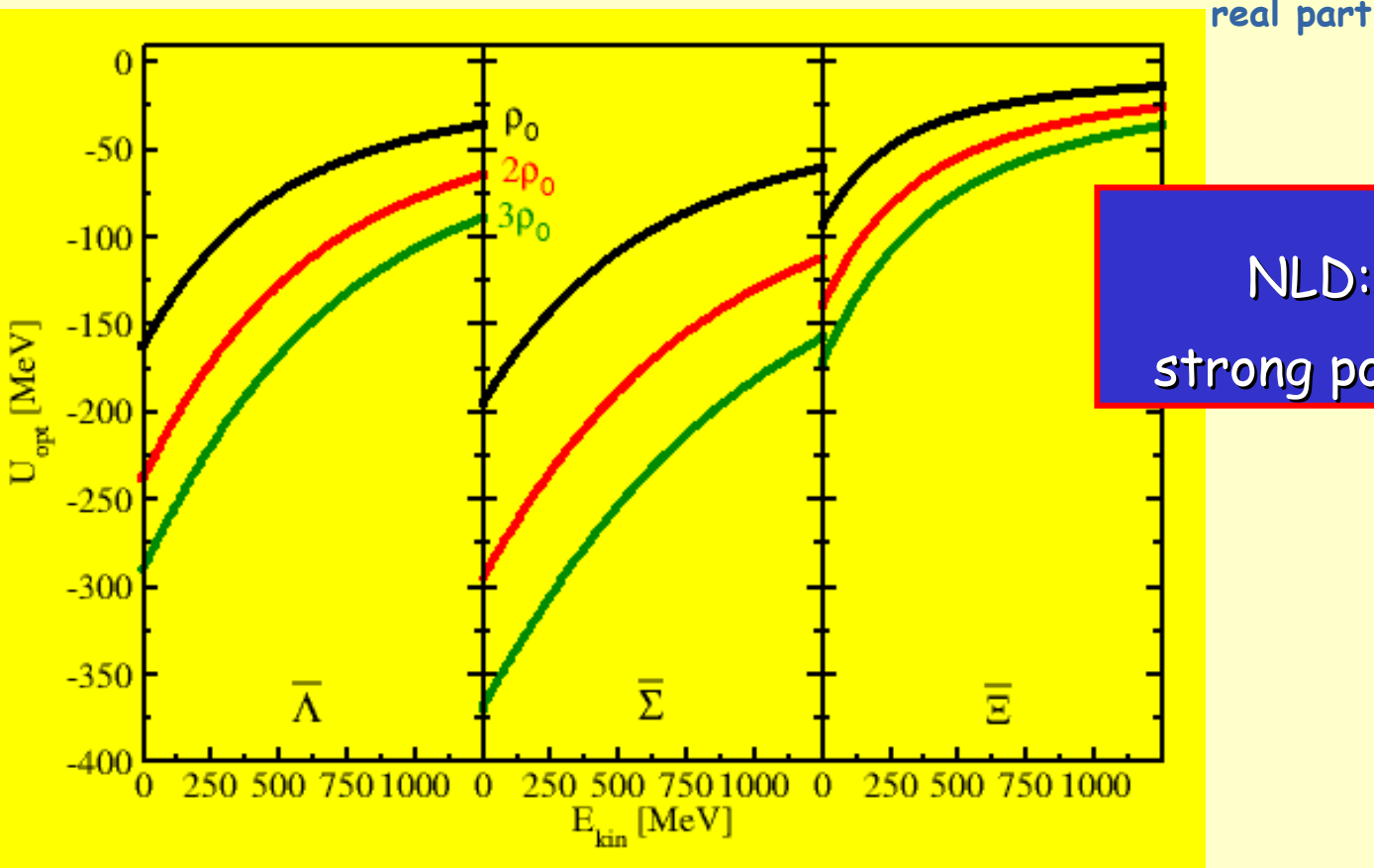
NLD predictions: density & momentum dependence
G-parity, no parameters

real part



Anti-Hyperon properties: optical potentials...

NLD predictions: density & momentum dependence
G-parity, no parameters

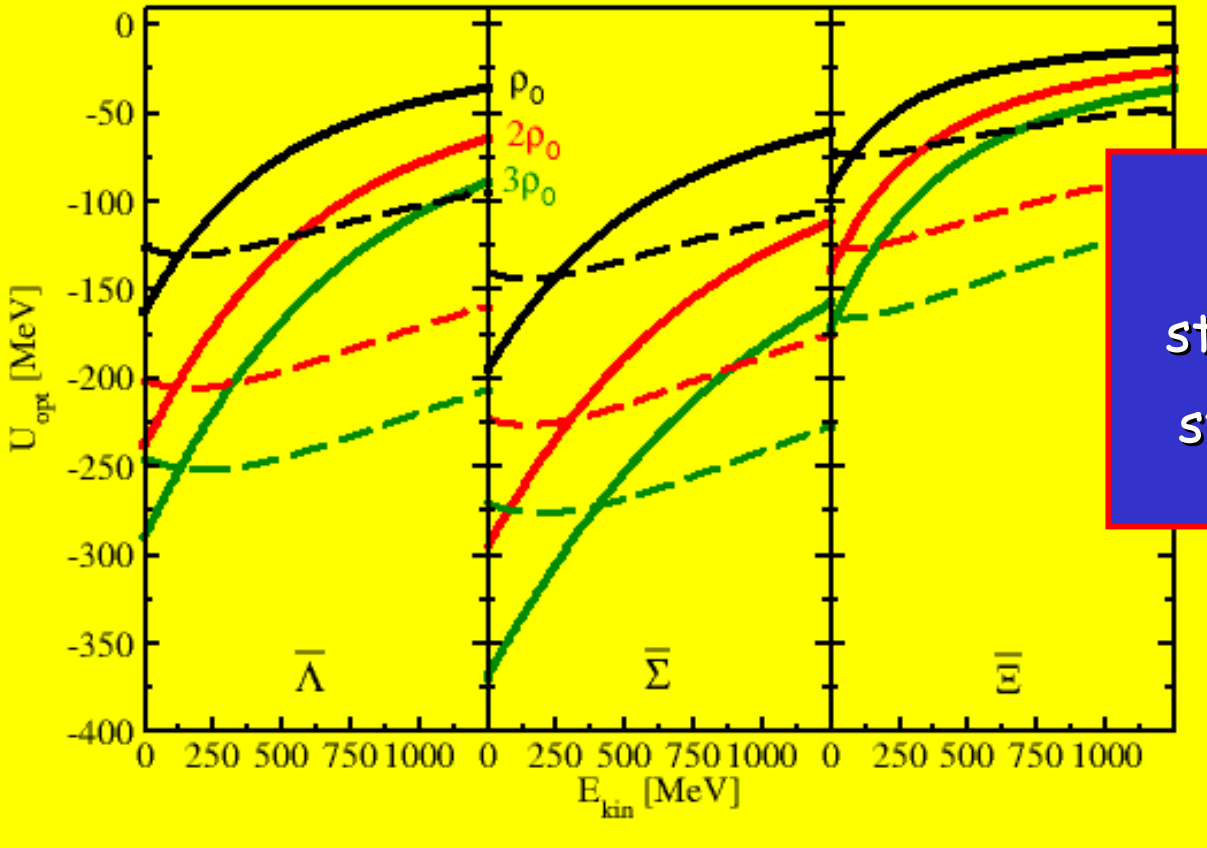


NLD: anti-hyperons
strong potential (real part)

Anti-Hyperon properties: optical potentials...

NLD predictions: density & momentum dependence
G-parity, no parameters

real part & imag part



NLD: anti-hyperons
strong potential (real part)
strong contributions from
imaginary part

Final remarks & outlook...

➤ NLD model

- keeping simplicity (RMF) to describe complexity (non-linear ρ & p dependences)
- realized by covariant introduction of regulators on a Lagrangian level
- in RMF: cut-off Λ regulates high ρ - & p -components of mean-fields
- cut-off Λ regulates also p -dependence of hyperon opt. pot.!

➤ NLD Results

- EoS soft at low ρ ($K \sim 250$ MeV), but stiff at high ρ
compatible with all recent observations of EoS & NS
- Correct MD for in-medium proton (!) and (!) antiproton interactions
- compatible with recent results from χ -EFT for hyperons in matter
- strong potentials for anti- Σ & strong contributions from imag. parts

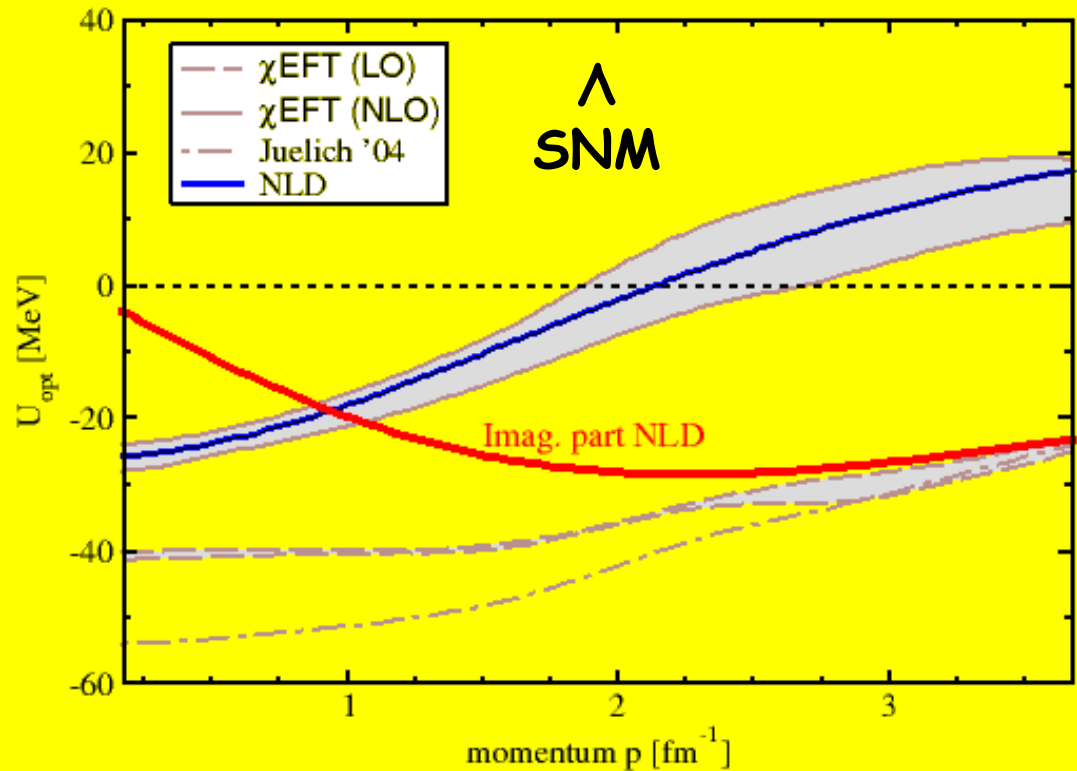
➤ Under progress developments: include NLD mean-fields in...

- transport model for HADES (π^+A induced reactions)
- transport model for PANDA ($\bar{p}-A$ & Ξ^-A induced reactions)
- application to β -equilibrated matter for NS

Back up slides

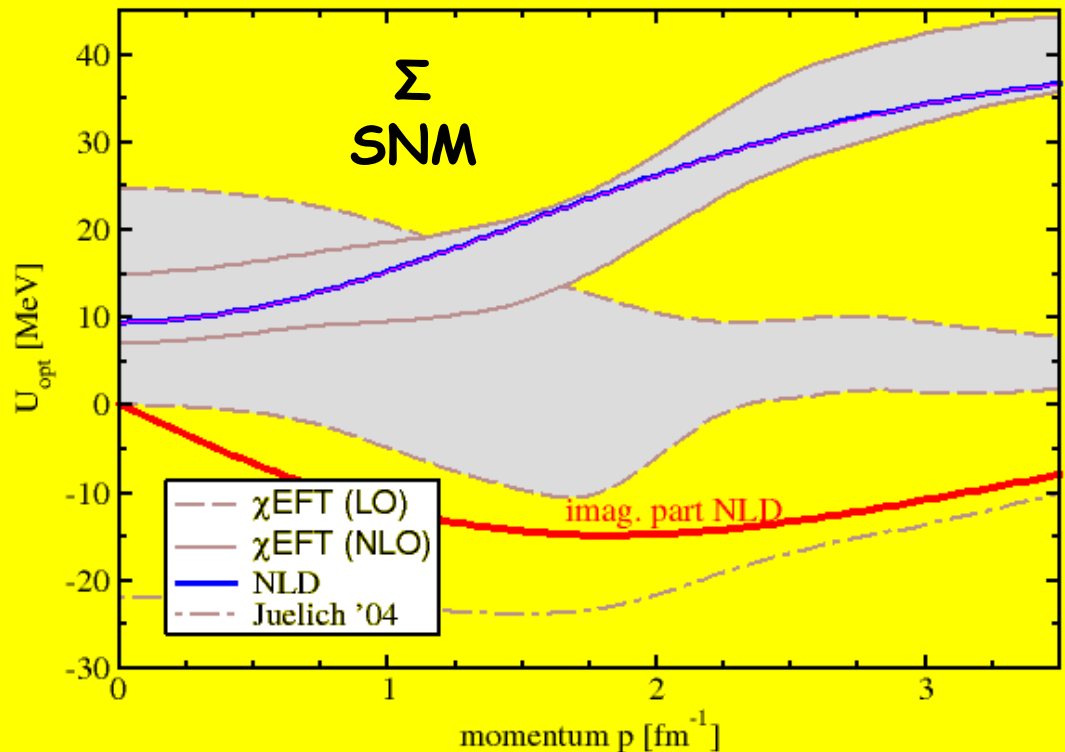
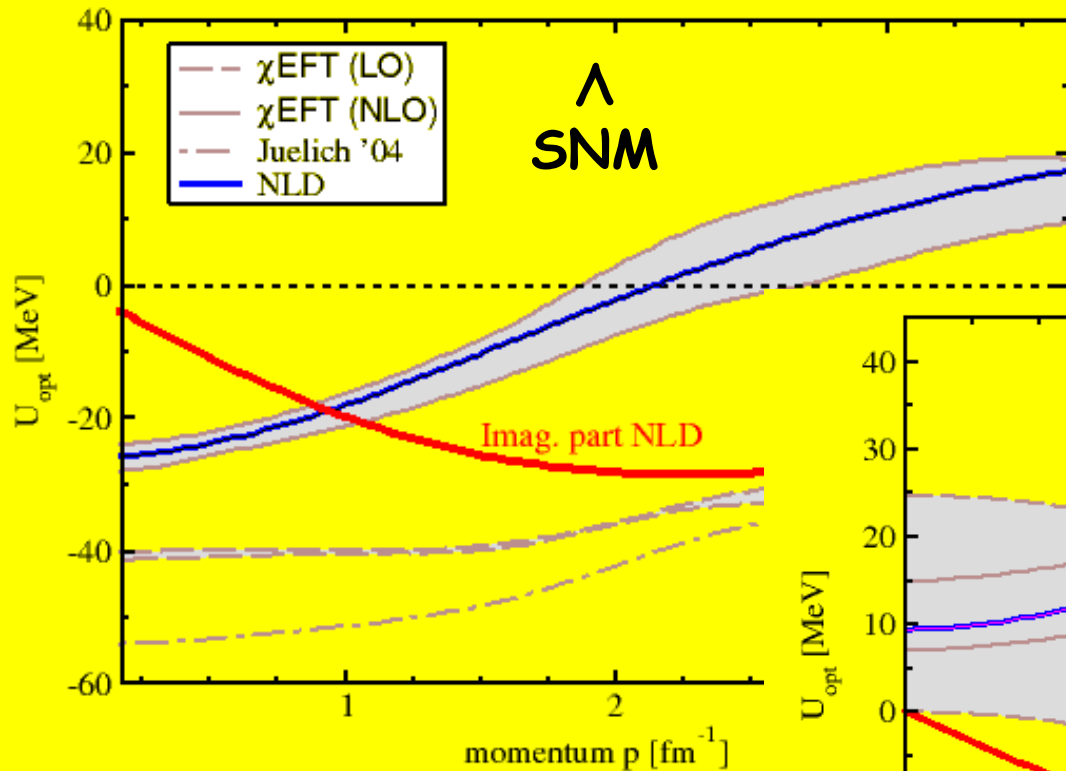
Anti-Hyperon properties: optical potentials...

NLD predictions: density & momentum dependence
G-parity, no parameters



Anti-Hyperon properties: optical potentials...






NLD predictions: density & momentum dependence
 G -parity, no parameters



Explore in-medium Λ -pot: HADES experiment...

Key Information

- ▶ HADES Spectrometer at GSI
- ▶ Secondary π^- -beam 1.7 GeV/c

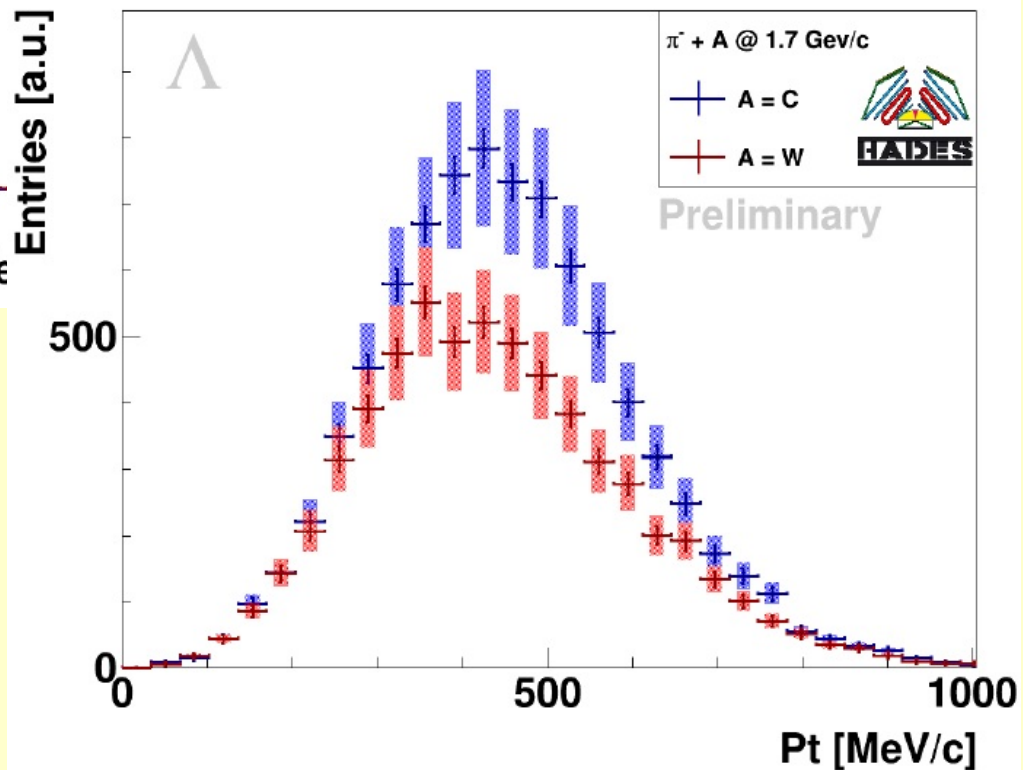
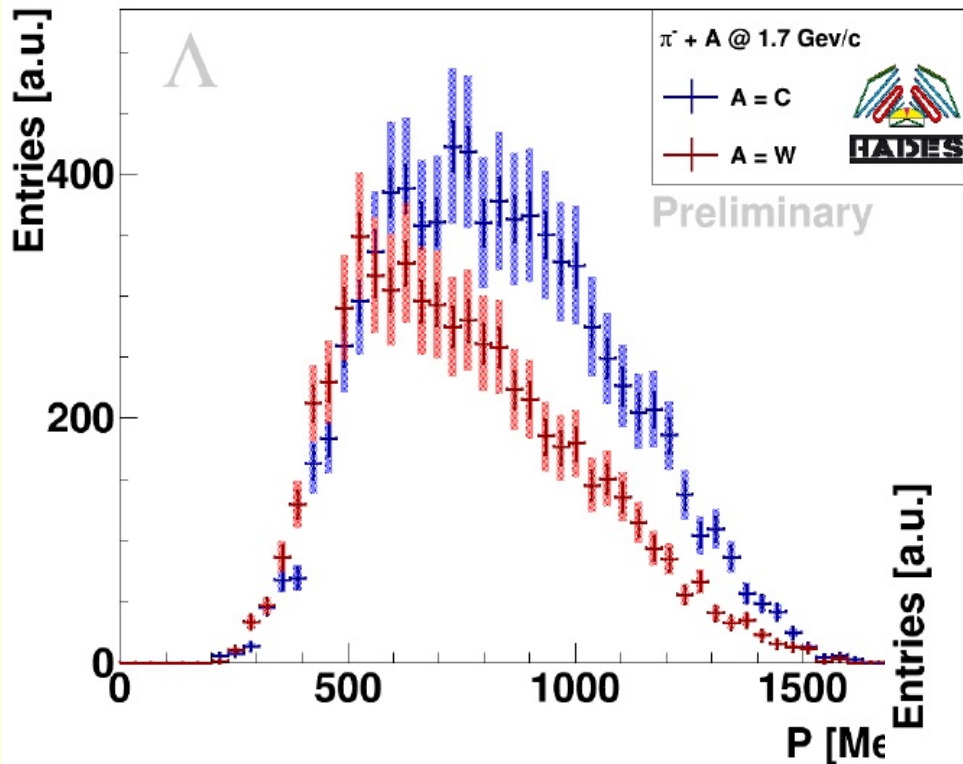
 Target	W	C
 Segment Length [mm]	2.4	7.2
 ρ [g/cm ³]	19.3	1.85
 A	183.84	12.011
 Statistics [$\times 10^8$]	1.69	2.00

Idea:

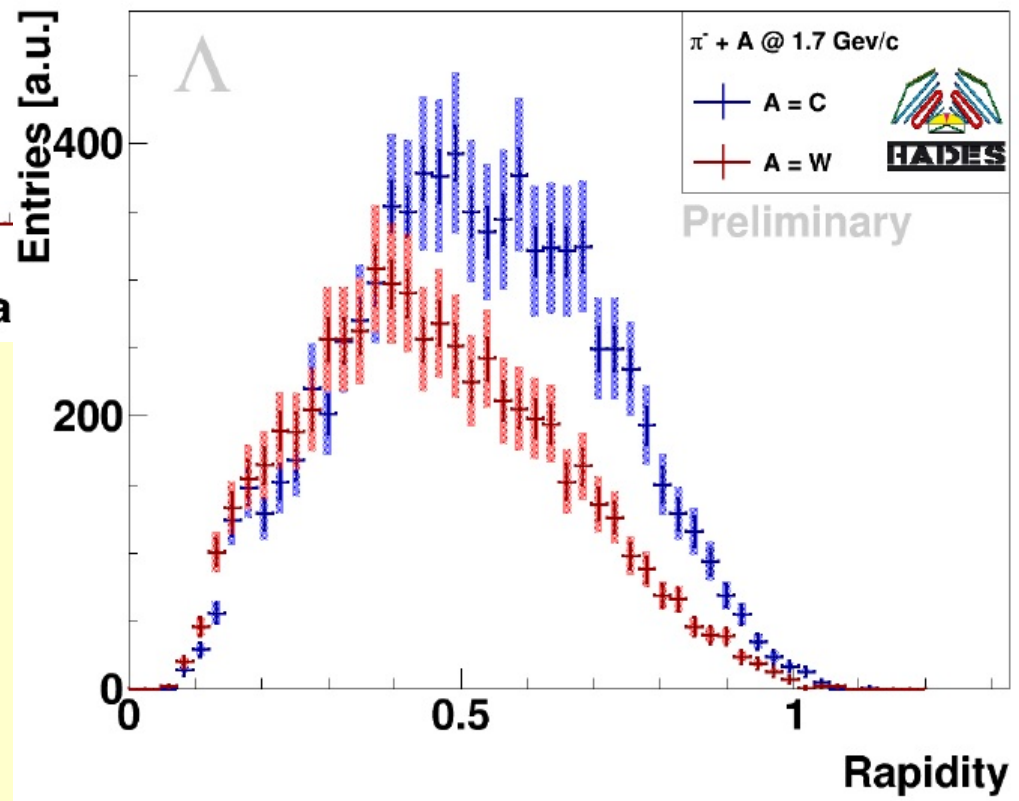
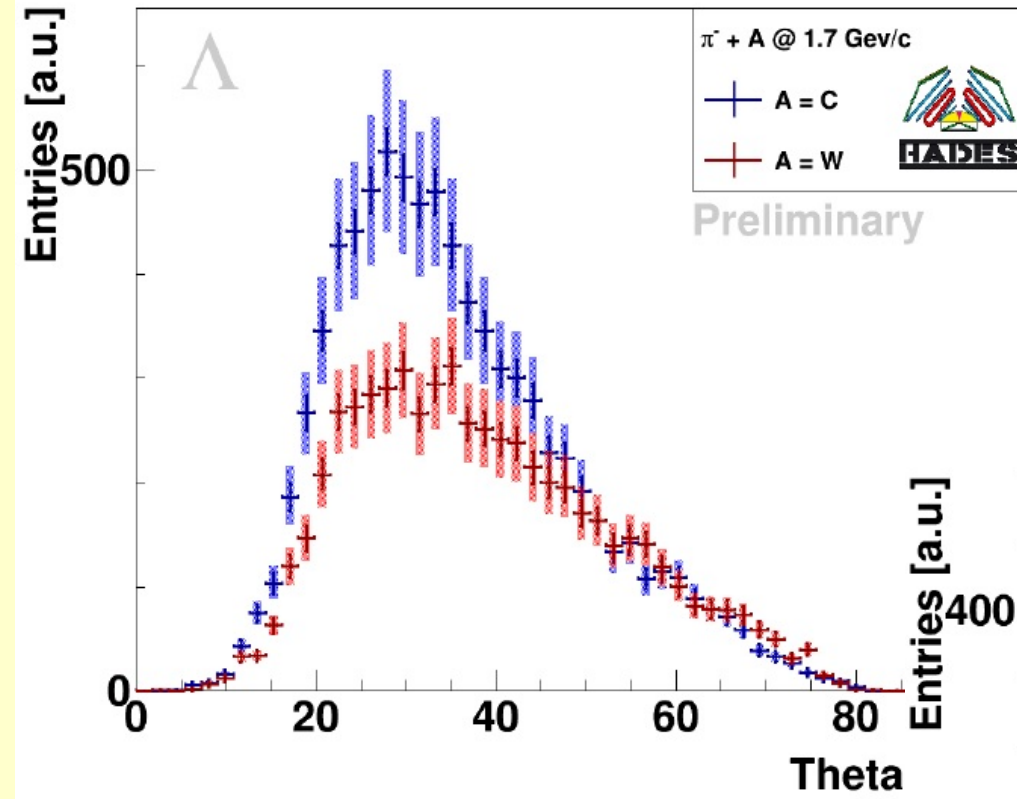
- ▶ Search for Charge Pattern 2+ 2- ($\Lambda \rightarrow p + \pi^-, K^0 \rightarrow \pi^+ + \pi^-$)
- ▶ Make best assignment of double π^- occurrence by minimizing:
$$\Delta M_\Lambda = M_{INV}(p + \pi^-) - M(\Lambda)_{PDG}$$
$$\Delta M_{K^0} = M_{INV}(\pi^+ + \pi^-) - M(K^0)_{PDG}$$
For all π^- Combination
- ▶ Cut on 2D ΔM_Λ vs. ΔM_{K^0}

Icons from: <https://www.flaticon.com/>

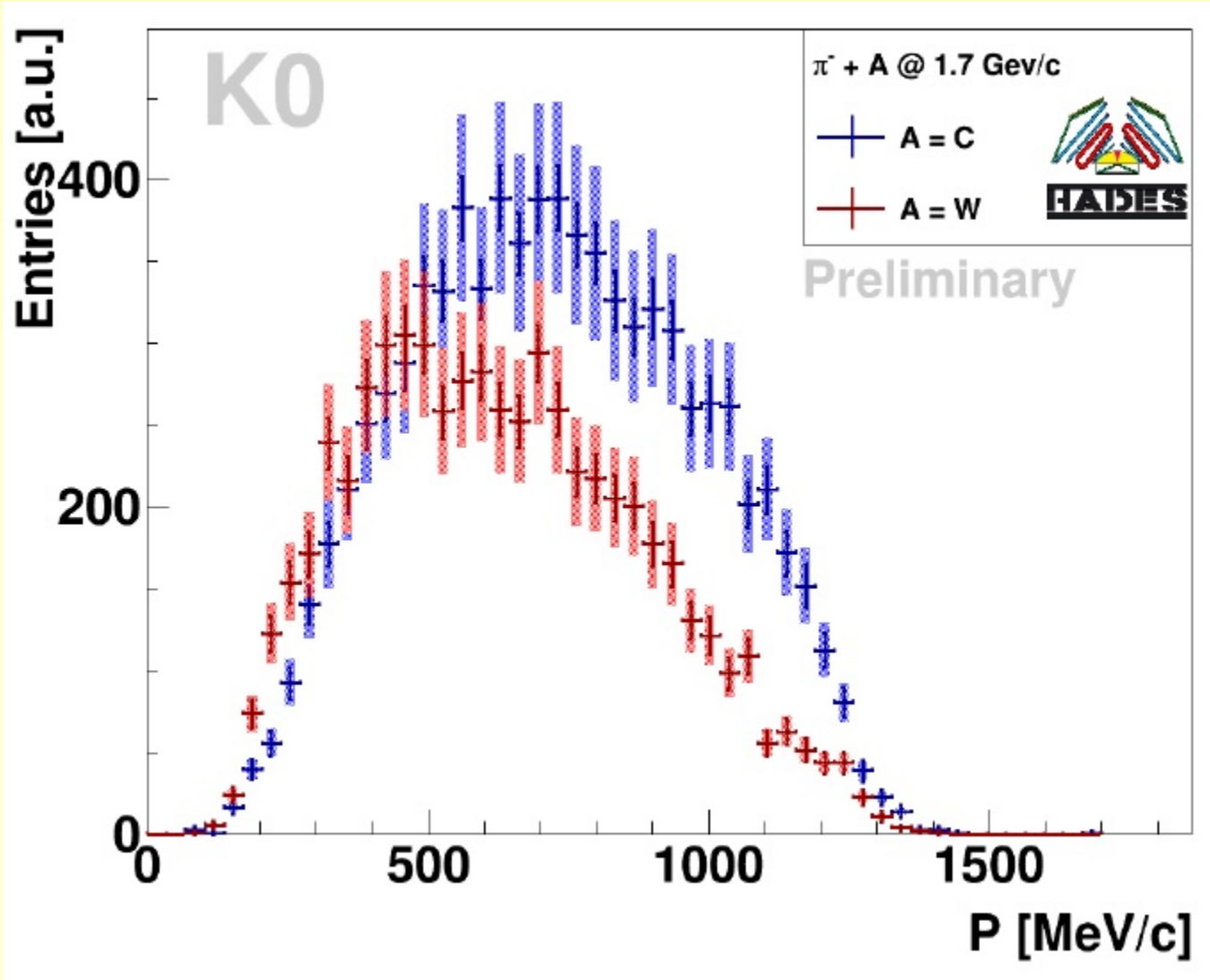
Explore in-medium Λ -pot: HADES new data...



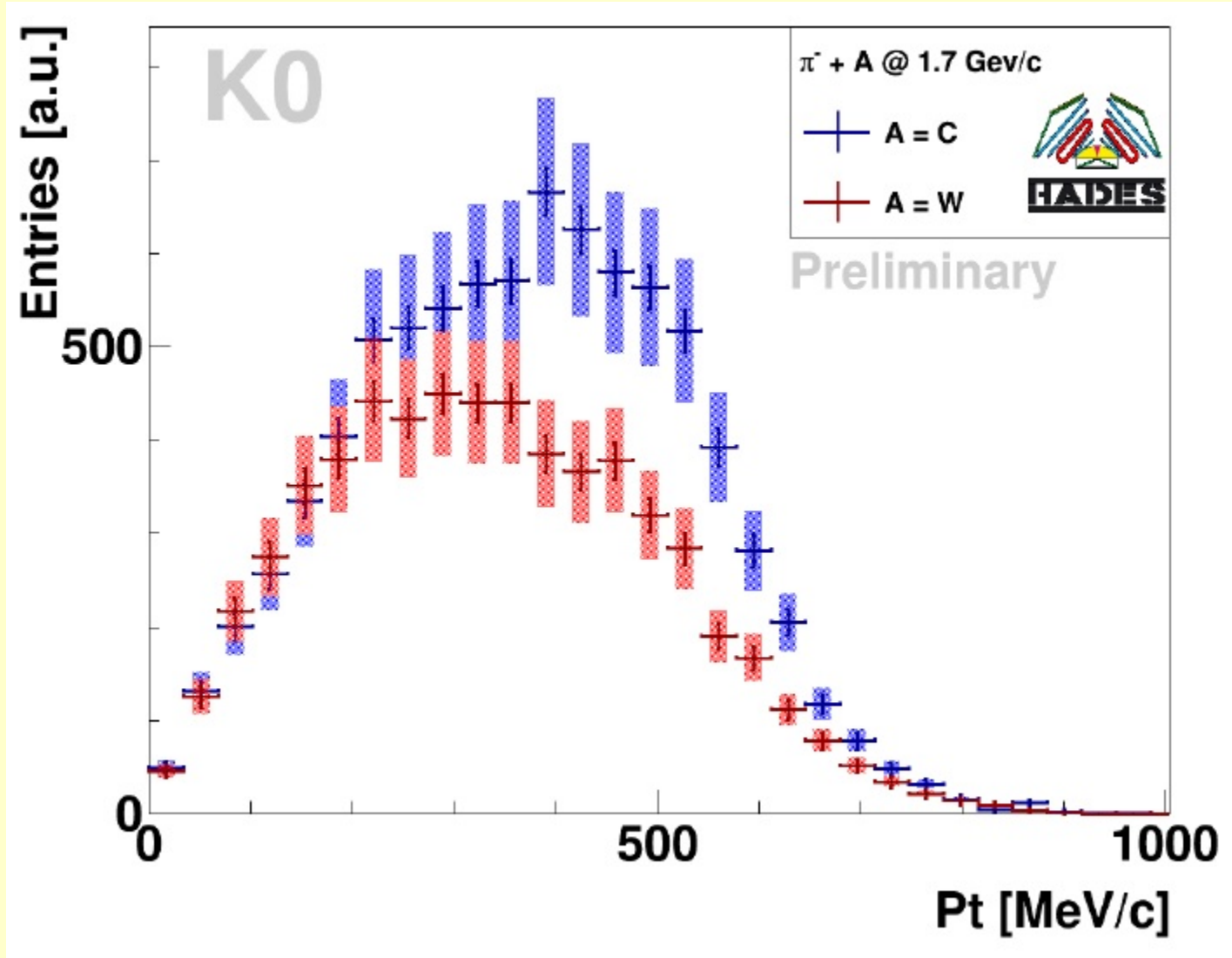
Explore in-medium Λ -pot: HADES new data...



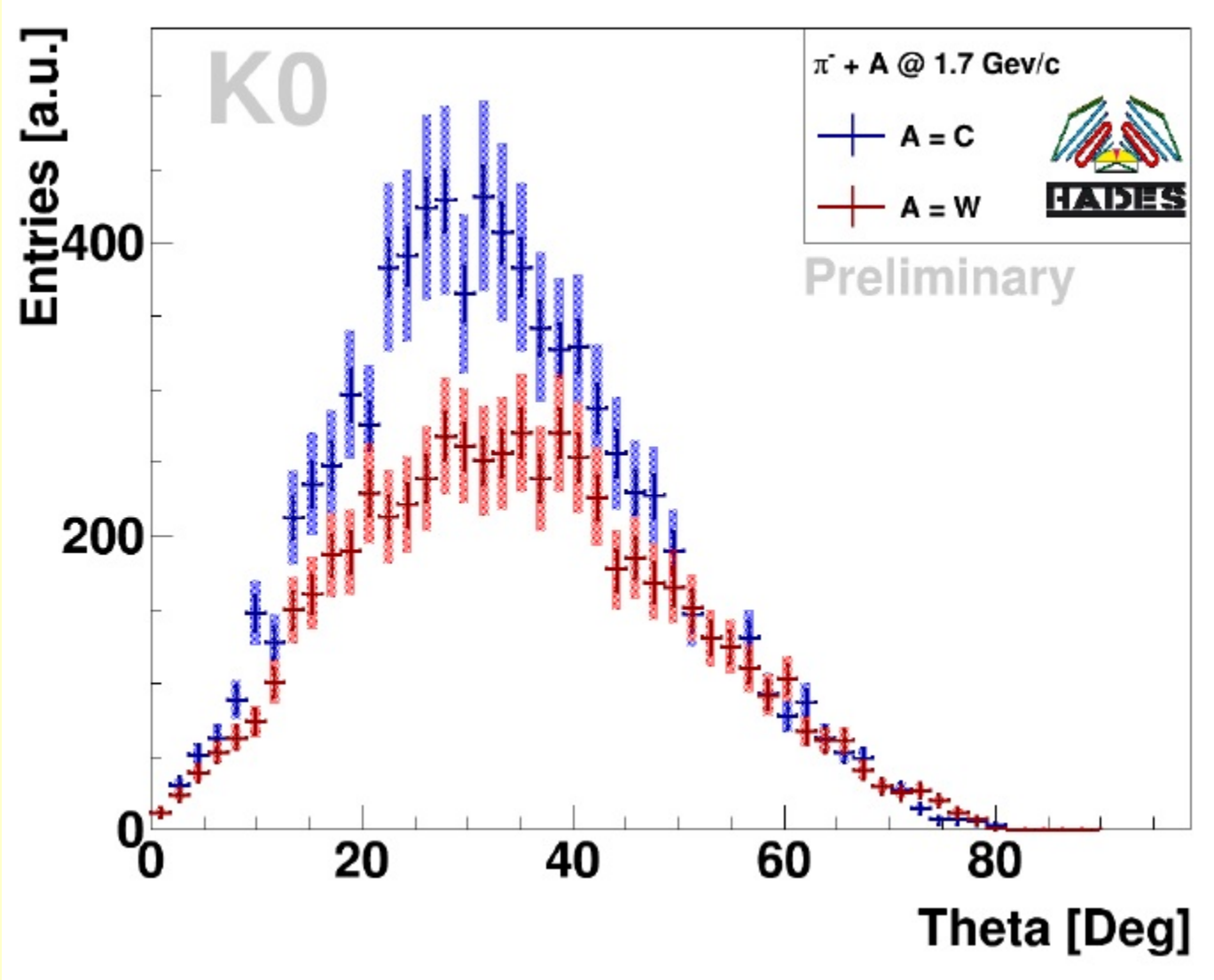
Explore in-medium K-pot: HADES new data...



Explore in-medium K-pot: HADES new data...



Explore in-medium K-pot: HADES new data...



Explore in-medium K-pot: HADES new data...

