

Microscopic model of K^-NN absorption and its application in kaonic atoms calculations

Jaroslava Óbertová

*Nuclear Physics Institute, Řež
& FNSPE, CTU in Prague*

Àngels Ramos

University of Barcelona

Eli Friedman

Hebrew University, Jerusalem

Jiří Mareš

Nuclear Physics Institute, Řež

Joint THEIA-STRONG2020 and JAEA/Mainz REIMEI Web-Seminar

3 February, 2021

Outline

- Introduction
- Microscopic model for $K^- NN$ absorption in nuclear matter
- Kaonic atoms calculations
- Conclusions

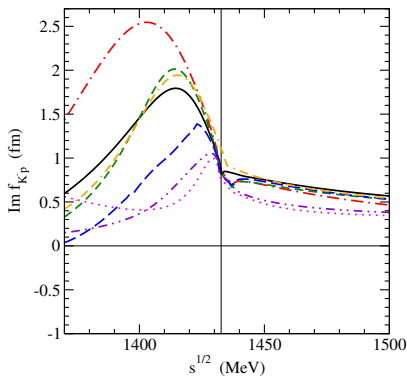
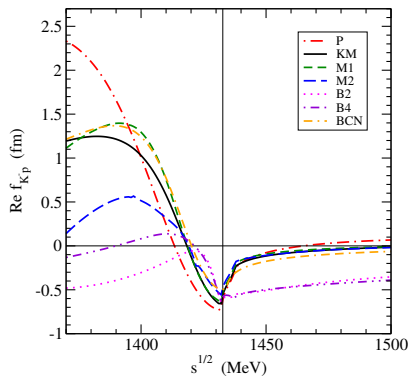
My current project 'Ema'



Introduction

- K^- multi-nucleon absorption fraction in the surface region of atomic nuclei represents about 20%
NC 53 (1968) 313 (Berkeley), NPB 35 (1971) 332 (BNL), NC 39A (1977) 538 (CERN)
- K^- multi-nucleon absorption in atoms described by phenomenological optical potential
E. Friedman, A. Gal, NPA 959 (2017) 66
- Model for K^-NN absorption in nuclear matter using free-space chiral amplitudes
T. Sekihara et al., PRC 86 (2012) 065205
- New experimental data on K^-NN absorption (AMADEUS@DAΦNE)
K. Piscicchia et al., PLB 782 (2018) 339
R. Del Grande et al., EPJ C79 (2019) 190
- Solid microscopic model for K^-NN absorption needed

Free-space K^-p amplitudes in various chiral models



Prague (P)

Kyoto-Munich (KM)

Murcia (M1 and M2)

Bonn (B2 and B4)

Barcelona (BCN)

A. Cieply, J. Smejkal, *Nucl. Phys. A* 881 (2012) 115

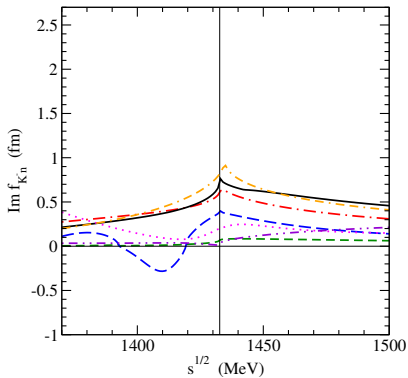
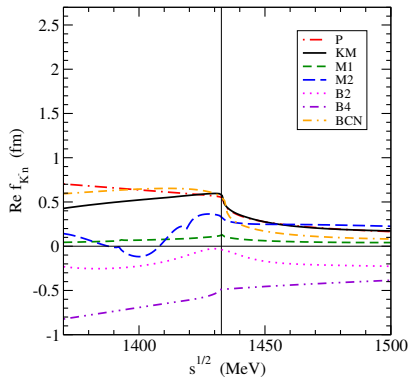
Y. Ikeda, T. Hyodo, W. Weise, *Nucl. Phys. A* 881 (2012) 98

Z. H. Guo, J. A. Oller, *Phys. Rev. C* 87 (2013) 035202

M. Mai, U.-G. Meißner, *Nucl. Phys. A* 900 (2013) 51

A. Feijoo, V. Magas, A. Ramos, *Phys. Rev. C* 99 (2019) 035211

Free-space K^-n amplitudes



Kaonic atoms

- Info about K^-N interaction below threshold provided by kaonic atoms
65 data points (energy shifts, widths, yields=upper level widths)
from CERN, Argonne, RAL, BNL
- Chirally motivated models fail to describe kaonic atom data
E. Friedman, A. Gal, NPA 959 (2017) 66

| model | B2 | B4 | M1 | M2 | P | KM |
|--------------|------|------|------|------|------|------|
| $\chi^2(65)$ | 1174 | 2358 | 2544 | 3548 | 2300 | 1806 |

Multinucleon processes

- Chiral models include only $K^- N \rightarrow \pi Y$ ($Y = \Lambda, \Sigma$) decay channel
- K^- interactions with two and more nucleons should be included, (e.g., $K^- + N + N \rightarrow Y + N$) \leftarrow analysis of kaonic atom data

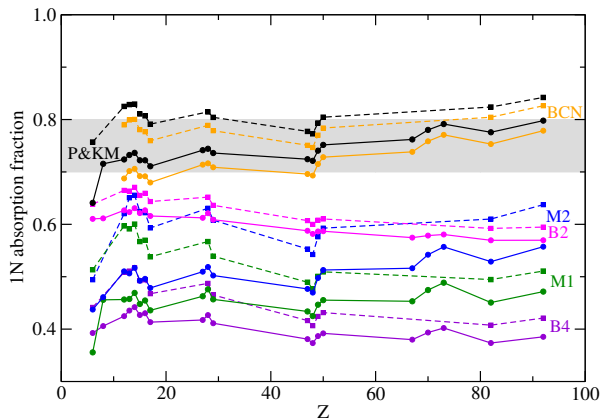
E. Friedman, A. Gal, NPA 959 (2017) 66

$$2\text{Re}(\omega_{K^-})V_{K^-}^{(2)} = -4\pi B\left(\frac{\rho}{\rho_0}\right)^\alpha \rho ,$$

where B is a **complex** amplitude, ρ is nuclear density distribution, ρ_0 is saturation density and α is positive

- Amplitude B fitted for each chiral model separately
- $\chi^2(65)$ goes down to 105 - 125

Single- vs. multi-nucleon processes



- Fraction of *single-nucleon* absorption 0.75 ± 0.05 (average value) used as an **additional constraint**.

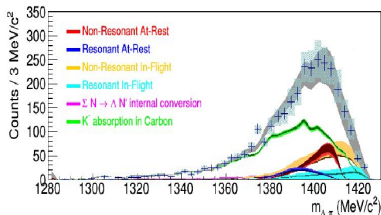
→ Only **P**, **KM** and **BCN** models found acceptable in kaonic atom analysis

E. Friedman, A. Gal, NPA 959 (2017) 66

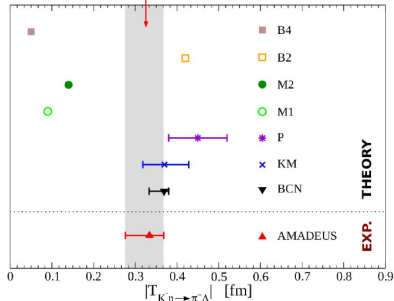
K. Piscicchia, talk at THEIA-STRONG2020 Web-Seminar, 20 December 2020

Outcome of the measurement

Investigated using: $K^- "n" {}^3\text{He} \rightarrow \Lambda \pi^- {}^3\text{He}$



$$|f_{ar}^s| = (0.334 \pm 0.018 \text{ stat}^{+0.034}_{-0.058} \text{ syst}) \text{ fm.}$$



[K. Piscicchia, S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345]

[K. Piscicchia, S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

Microscopic model for K^-NN absorption in nuclear matter

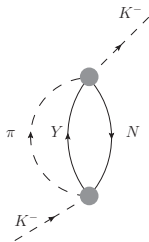
We have developed a microscopic model for K^- two-nucleon absorption in symmetric nuclear matter

J. Hrtánková, Á. Ramos, PRC 101 (2020) 035204

- based on a meson-exchange approach
H. Nagahiro et al., PLB 709 (2012) 87
- employing **P** and **BCN** chiral K^-N amplitudes
- considering **Pauli correlations** in the medium for K^-N amplitudes
- **real part of the K^-NN optical potential** evaluated as well
- K^-N optical potential derived within the same approach

K^-N absorption in nuclear matter

$$K^-N \rightarrow \pi Y \quad (Y = \Lambda, \Sigma)$$



- K^-N self-energy

$$\Pi_{K^-N \rightarrow \pi Y}(\vec{p}, p_0) = i |t_{K^-N \rightarrow \pi Y}|^2 \int \frac{d^4 q}{(2\pi)^4} U_{YN}(p - q) \frac{1}{q^2 - m_\pi^2 + i\eta}$$

t - two-body t-matrix; U - Lindhard function

p - kaon 4-momentum; q - meson 4-momentum

$K^- NN$ absorption in nuclear matter

$$K^- + N + N \rightarrow Y + N \quad (Y = \Lambda, \Sigma)$$

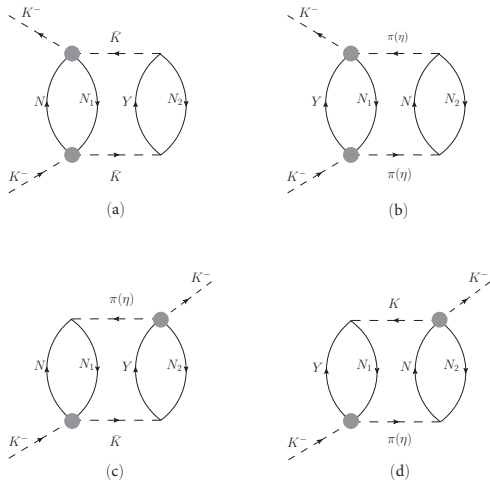


Fig.1: Two-fermion-loop (2FL) Feynman diagrams for non-mesonic K^- absorption on two nucleons N_1 , N_2 in nuclear matter. The shaded circles denote the $K^- N$ t-matrices derived from a chiral model.

$K^- NN$ absorption in nuclear matter

- $K^- NN$ self-energy from a direct 2FL diagram

$$\begin{aligned} \Pi_{K^- NN}^{2\text{FL}}(\vec{p}, p_0) = & -i t_{B_1 x} t_{B_1 x}^* V_{B_2 N_2 x} V_{B_2 N_2 x} \int \frac{d^4 q}{(2\pi)^4} U_{B_1 N_1}(p-q) U_{B_2 N_2}(q) \\ & \times (-\vec{q}^2) \frac{F(\vec{q})}{q^2 - m_x^2 + i\eta} \frac{F(\vec{q})}{q^2 - m_x^2 + i\eta}, \end{aligned}$$

$x = K^-, \bar{K}^0, \pi, \eta$; t - two-body t -matrices; $B_1, B_2 = N, Y$

V - meson-baryon-baryon couplings; U - Lindhard function

p - kaon 4-momentum, q - meson 4-momentum,

$F(\vec{q}) = \frac{\Lambda_C^2}{\Lambda_C^2 + \vec{q}^2}$ - form factor, Λ_C - cut-off parameter

- Contributions from diagrams (c) and (d) are zero due to null trace over spins

K^- - NN absorption in nuclear matter

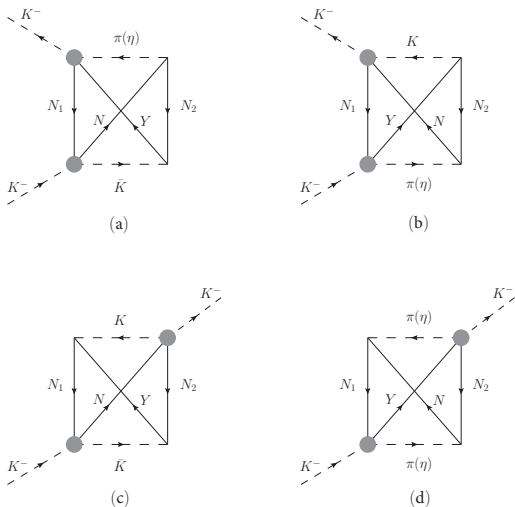


Fig.2: One-fermion-loop (1FL) Feynman diagrams for non-mesonic K^- absorption on two nucleons N_1 , N_2 in nuclear matter. The shaded circles denote the K^-N t-matrices derived from a chiral model.

K^-NN absorption in nuclear matter

- K^-NN self-energy from an exchange 1FL diagram

$$\begin{aligned}\Pi_{K^-NN}^{1FLA}(\vec{p}, p_0) &= -it_{B_1x_1}t_{B_2x_2}^*V_{B_2N_2x_1}V_{B_1N_2x_2}\int\frac{d^4q}{(2\pi)^4}(+2\vec{q}^2) \\ &\quad \times\int\frac{d^4j}{(2\pi)^4}G_{N_1}(j)G_{B_1}(j+p-q)\int\frac{d^4k}{(2\pi)^4}G_{N_2}(k)G_{B_2}(q+k) \\ &\quad \times\frac{1}{q^2-m_{x_1}^2+i\eta}\frac{1}{q'^2-m_{x_2}^2+i\eta}= \\ &= it_{B_1x_1}t_{B_2x_2}^*V_{B_2N_2x_1}V_{B_1N_2x_2}\frac{1}{2}\int\frac{d^4q}{(2\pi)^4}U_{B_1N_1}(p-q)U_{B_2N_2}(q) \\ &\quad \times\vec{q}^2\frac{F(\vec{q})}{q^2-m_{x_1}^2+i\eta}\frac{F(\vec{q}')}{q'^2-m_{x_2}^2+i\eta}\end{aligned}$$

G - baryon propagator in the medium; j, k - nucleon 4-momenta

$K^- NN$ absorption in nuclear matter

- K^- self-energy related to optical potential $V_{K^-} = \frac{\Pi_{K^-}}{2E_{K^-}}$
- $V_{K^-N} = \sum_{channels} V_{K^-N \rightarrow \pi Y}$
- $V_{K^-NN} = \sum_{channels} V_{K^-NN}^{2FL} + V_{K^-NN}^{1FL}$
 → contributions from 37 2FL and 28+33 1FL diagrams

Table 1: All considered channels for mesonic and non-mesonic K^- absorption in matter.

| $K^- N$ | $\rightarrow \pi Y$ | $K^- N_1 N_2$ | $\rightarrow YN$ |
|---------|------------------------------|---------------|--------------------------|
| $K^- p$ | $\rightarrow \pi^0 \Lambda$ | $K^- pp$ | $\rightarrow \Lambda p$ |
| | $\rightarrow \pi^0 \Sigma^0$ | | $\rightarrow \Sigma^0 p$ |
| | $\rightarrow \pi^+ \Sigma^-$ | | $\rightarrow \Sigma^+ n$ |
| | $\rightarrow \pi^- \Sigma^+$ | $K^- pn(np)$ | $\rightarrow \Lambda n$ |
| $K^- n$ | $\rightarrow \pi^- \Lambda$ | | $\rightarrow \Sigma^0 n$ |
| | $\rightarrow \pi^- \Sigma^0$ | | $\rightarrow \Sigma^- p$ |
| | $\rightarrow \pi^0 \Sigma^-$ | $K^- nn$ | $\rightarrow \Sigma^- n$ |

K^-N free-space vs. Pauli blocked scattering amplitudes

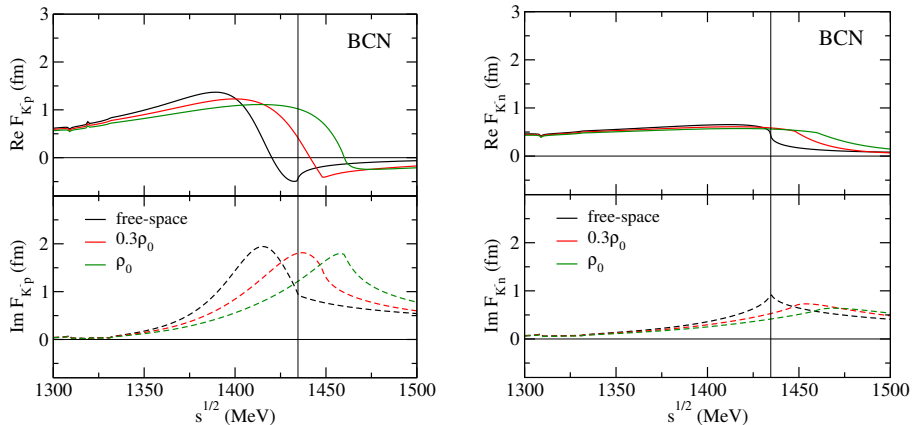


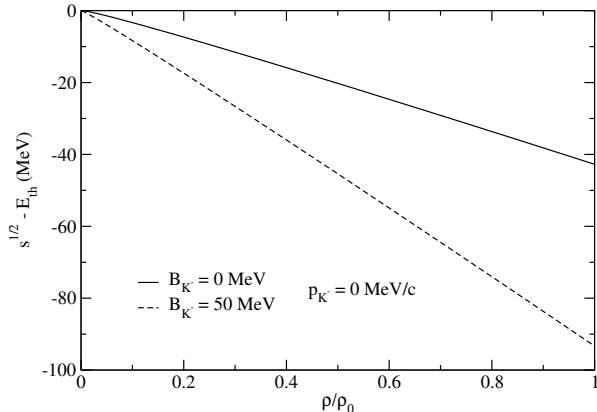
Fig.3: Comparison of K^-p and K^-n free-space (black) and Pauli blocked amplitudes at two different nuclear matter densities: $0.3\rho_0$ (red) and ρ_0 (green), calculated in the BCN model.

Energies probed below K^-N threshold

- Energy shift $\delta\sqrt{s} = \sqrt{s} - E_{\text{th}}$ where $\sqrt{s} = \sqrt{(E_{K^-} + E_F)^2 - \frac{3}{5}k_F^2 - p_{K^-}^2 \frac{\rho}{\rho_0}}$,

$$E_{\text{th}} = m_N + m_{K^-}, E_F = \sqrt{m_N^2 + \frac{3}{5}k_F^2} + V_N \frac{\rho}{\rho_0} \text{ with } V_N = -50 \text{ MeV},$$

$$k_F - \text{Fermi momentum, } \rho_0 = 0.169 \text{ fm}^{-3}, E_{K^-} = m_{K^-} - B_{K^-} \frac{\rho}{\rho_0}$$



K^- potential in nuclear matter - medium effects

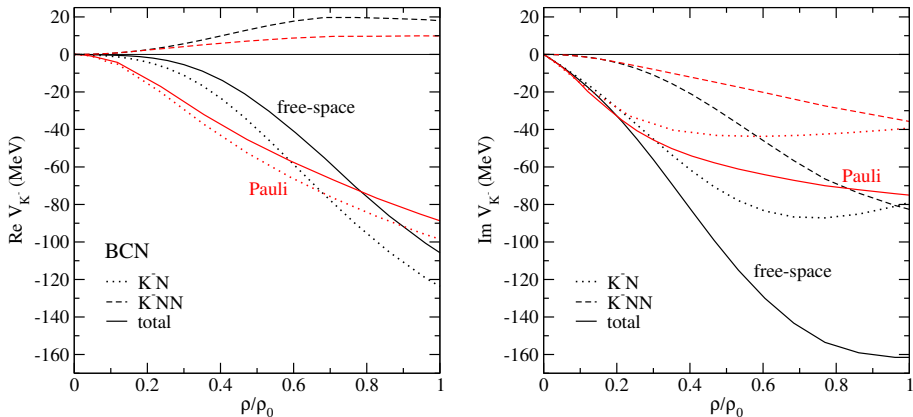


Fig.4: The real (left) and imaginary (right) parts of the K^-N , K^-NN , and total optical potentials as a function of relative density, calculated using the free-space (black) and Pauli blocked (red) BCN amplitudes for $B_{K^-} = 0$ MeV and $p_{K^-} = 0$ MeV/c.

Momentum dependence

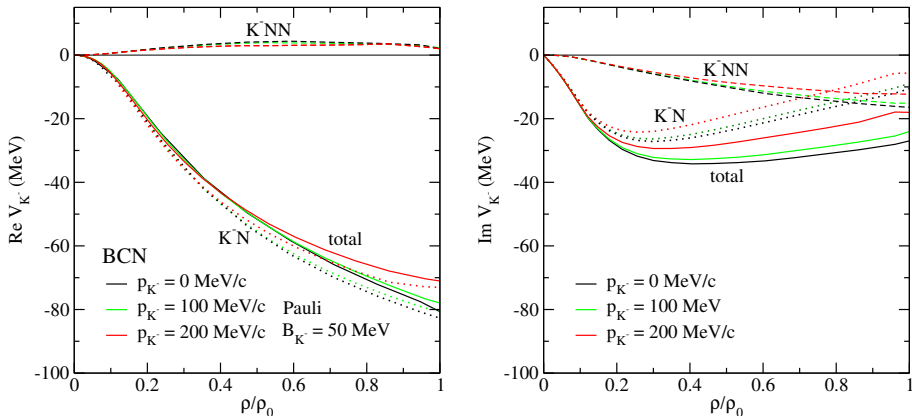


Fig.5: The real (left) and imaginary (right) parts of the K^-N (dotted), K^-NN (dashed), and total (solid) optical potentials as a function of relative density ρ/ρ_0 , calculated for $B_{K^-} = 50$ MeV at ρ_0 and three different kaon momenta p_{K^-} using the Pauli blocked BCN amplitudes.

K^-N and K^-NN absorption fractions

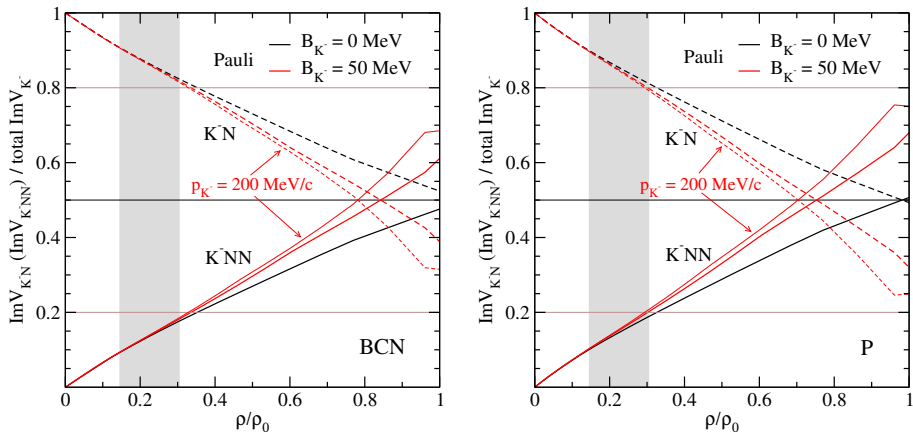


Fig.6: Ratio of K^- single-nucleon (K^-N) and two-nucleon (K^-NN) absorptive potentials to the total K^- absorptive potential as a function of relative density, calculated using the Pauli blocked amplitudes and for $B_{K^-} = 0$ and 50 MeV and $p_{K^-} = 0$ MeV/c and for $B_{K^-} = 50$ MeV and $p_{K^-} = 200$ MeV/c.

Cut-off dependence

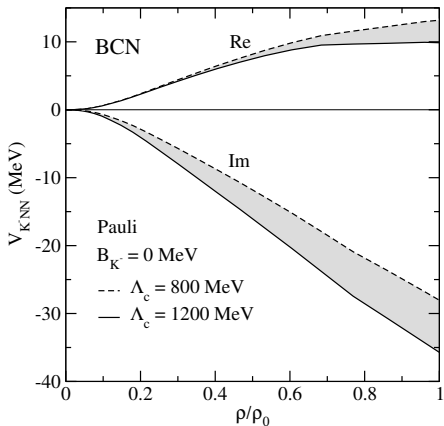


Fig.7: Dependence of the K^-NN potential on the value of the cut-off parameter Λ_c used in the form factors $F(\vec{q}) = \frac{\Lambda_c^2}{\Lambda_c^2 + \vec{q}^2}$, calculated for $B_{K^-} = 0$ MeV and $p_{K^-} = 0$ MeV/c with Pauli blocked BCN amplitudes.

AMADEUS data

- New measured ratio *R. Del Grande et al., EPJ C79 (2019) 190*

$$R = \frac{\text{BR}(K^- pp \rightarrow \Lambda p)}{\text{BR}(K^- pp \rightarrow \Sigma^0 p)} = 0.7 \pm 0.2(\text{stat.})_{-0.3}^{+0.2}(\text{syst.})$$

- Assumption that dominant contribution for $K^- pp \rightarrow \Lambda p$ and $K^- pp \rightarrow \Sigma^0 p$ channels comes from π^0 exchange leads to relation

$$\frac{\text{BR}(K^- pp \rightarrow \Lambda p)}{\text{BR}(K^- pp \rightarrow \Sigma^0 p)} = \frac{\text{BR}(K^- p \rightarrow \pi^0 \Lambda)}{\text{BR}(K^- p \rightarrow \pi^0 \Sigma^0)}$$

- However, the dominant contribution for $K^- pp \rightarrow \Lambda p$ channel comes from K^- exchange!

T. Sekihara, D. Jido, Y. Kanada-En'yo, PRC 79 (2009) 062201(R)

J. Hrtánková, Æ. Ramos, PRC 101 (2020) 035204

Ratio R for $2N$ absorption

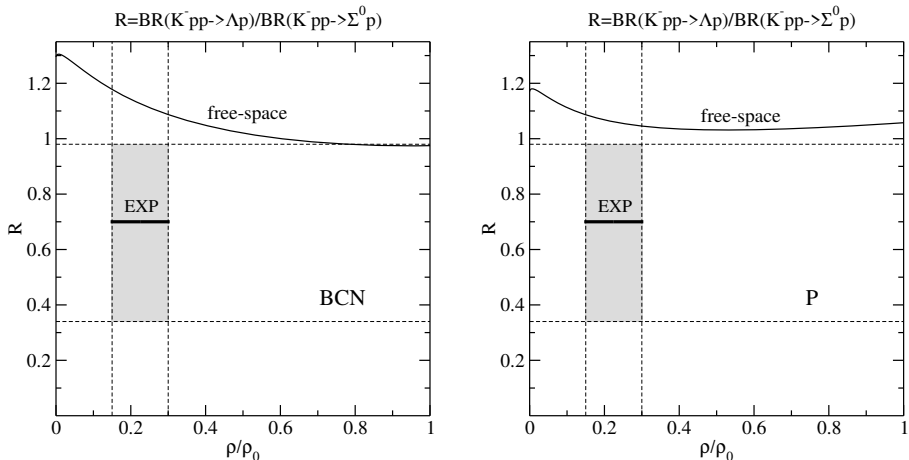


Fig.8: The ratio R as a function of relative density, calculated using the free-space amplitudes for $B_{K^-} = 0$ MeV. The dashed vertical lines denote the region of densities probed in experiments with low-energy K^- including the experimental value of the ratio with corresponding error bar.

Ratio R for 2N absorption

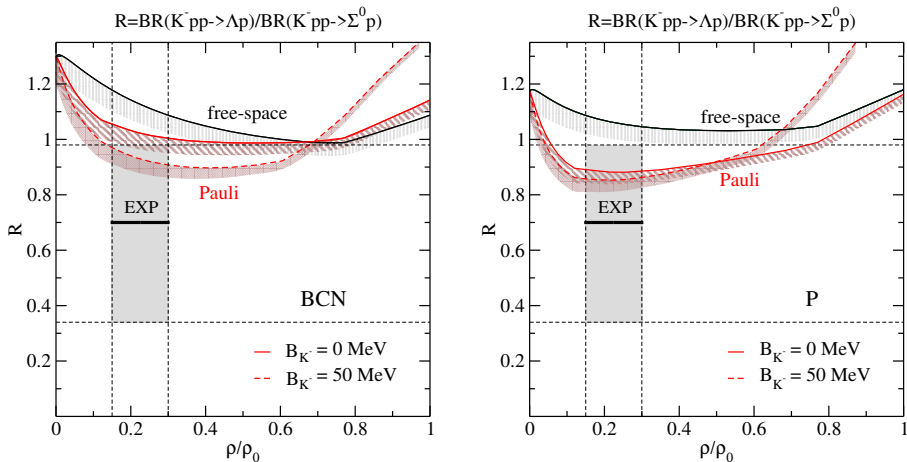


Fig.9: The ratio R as a function of relative density, calculated using the free-space and Pauli blocked amplitudes for $B_{K^-} = 0$ MeV and $B_{K^-} = 50$ MeV. Color bands denote the uncertainty due to different cut-off values $\Lambda_c = 800 - 1200$ MeV.

Ratio R^* for 1N absorption

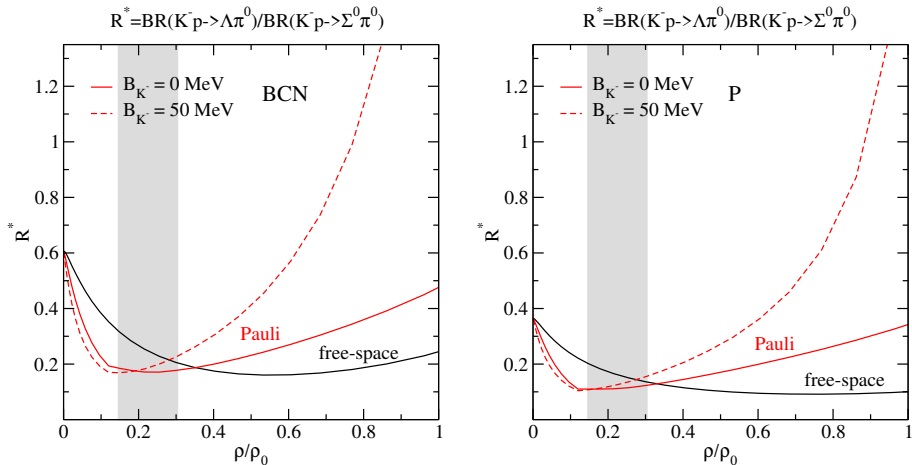


Fig.10: The ratio R^* as a function of relative density, calculated using the free-space and Pauli blocked amplitudes for $B_{K^-} = 0 \text{ MeV}$ and $B_{K^-} = 50 \text{ MeV}$. The gray band denotes the region of densities probed in experiments with low-energy K^- .

Comparison with experimental data

Table 2: Primary-interaction ratios (in %) for mesonic absorption of K^- in nuclear matter, calculated with free-space and Pauli blocked BCN amplitudes for $B_{K^-} = 0$ MeV $\rho_{K^-} = 0$ MeV/c. The errors denote the uncertainty due to the cut-off dependence. The experimental data corrected for primary^a interaction are shown for comparison.

| BCN mesonic ratio | 0.3 ρ_0 | | Exp. [1] | |
|------------------------|----------------|----------------|-----------------|-----------------|
| | f.s. | Pauli | ⁴ He | ¹² C |
| $\Sigma^+ \pi^- / K^-$ | 19.6 \pm 0.6 | 28.8 \pm 0.7 | 31.2 \pm 5.0 | 29.4 \pm 1.0 |
| $\Sigma^- \pi^0 / K^-$ | 6.2 \pm 0.2 | 5.7 \pm 0.1 | 4.9 \pm 1.3 | 2.6 \pm 0.6 |
| $\Sigma^- \pi^+ / K^-$ | 21.9 \pm 0.6 | 14.8 \pm 0.4 | 9.1 \pm 1.6 | 13.1 \pm 0.4 |
| $\Sigma^0 \pi^- / K^-$ | 6.2 \pm 0.2 | 5.7 \pm 0.1 | 4.9 \pm 1.3 | 2.6 \pm 0.6 |
| $\Sigma^0 \pi^0 / K^-$ | 18.1 \pm 0.5 | 19.2 \pm 0.5 | 17.7 \pm 2.9 | 20.0 \pm 0.7 |
| $\Lambda \pi^0 / K^-$ | 3.8 \pm 0.1 | 3.5 \pm 0.1 | 5.2 \pm 1.6 | 3.4 \pm 0.2 |
| $\Lambda \pi^- / K^-$ | 7.6 \pm 0.2 | 7.0 \pm 0.2 | 10.5 \pm 3.0 | 6.8 \pm 0.3 |
| total 1N ratio | 83.3 \pm 2.4 | 84.6 \pm 2.2 | 83.5 \pm 7.1 | 77.9 \pm 1.6 |

^a Corrected for secondary interactions of the primary particles created in the absorbing nucleus.

[1] C. Vander Velde-Wilquet et al., *Nuovo Cimento* 39 A (1977) 538

Comparison with experimental data

Table 3: Primary-interaction total ratios (in %) for non-mesonic and total (1N+2N) K^- absorption in matter and corresponding ratios corrected for Σ - Λ conversion with different conversion rates, a) - 60% for Σ^+ - Λ , 22.5% for Σ^- - Λ , 72% for Σ^0 - Λ , b) - 50% for all Σ 's, calculated with Pauli blocked BCN amplitudes for $B_{K^-} = 0$ MeV. The errors denote the uncertainty due to the cut-off dependence.

| BCN | $0.3\rho_0$ | $0.3\rho_0 + \Sigma$ - Λ conv. | | Exp. [1] ${}^4\text{He}$ |
|--------------------------------|-----------------|--|------------------|-----------------------------|
| | | a) | b) | |
| non-mesonic ratio | | | | |
| $(\Lambda N + \Sigma^0 N)/K^-$ | 7.2 ± 1.1 | 10.5 ± 1.5 | 11.3 ± 1.6 | 11.7 ± 2.4 |
| $(\Sigma^- N)/K^-$ | 4.3 ± 0.6 | 3.4 ± 0.4 | 2.2 ± 0.3 | 3.6 ± 0.9 |
| $\Sigma^+ n/K^-$ | 3.8 ± 0.5 | 1.5 ± 0.2 | 1.9 ± 0.3 | 1.0 ± 0.4 |
| $(\Sigma^0 N)/K^-$ | 3.7 ± 0.5 | 1.0 ± 0.1 | 1.9 ± 0.2 | 2.3 ± 1.0 |
| total 2N ratio | 15.4 ± 2.2 | 15.4 ± 2.2 | | 16.4 ± 2.6 |
| total ratio | | | | |
| Σ^+/K^- | 32.6 ± 0.2 | 13.0 ± 0.1 | 16.3 ± 0.1 | 17.0 ± 2.7 |
| Σ^-/K^- | 24.8 ± 0.1 | 19.21 ± 0.04 | 12.39 ± 0.03 | 13.8 ± 1.8 |
| Σ^0/K^- | 28.7 ± 0.1 | 8.03 ± 0.04 | 14.3 ± 0.1 | 10.8 ± 5.0 |
| Λ/K^- | 14.0 ± 0.3 | 59.7 ± 0.1 | 57.0 ± 0.2 | 58.4 ± 5.7 |
| Σ^+/Σ^- | 1.31 ± 0.01 | 0.68 ± 0.01 | 1.31 ± 0.01 | 1.2 ± 0.2 |

[1] *P. A. Katz et al., PRD 1 (1970) 1267*

Application to kaonic atoms

- K^-NN model applied in calculations of shifts and widths in kaonic atoms
- BCN amplitudes used \rightarrow in-medium modifications included (Pauli or WRW) *T. Wass, M. Rho, W. Weise, NPA 617 (1997) 449*
- RMF densities and 2-parameter Fermi density distributions tested
- subthreshold kinematics taken from K^-NN model with $p_{K^-} = 150 \text{ MeV}/c$

$$\sqrt{s} = \sqrt{(E_{K^-} + E_F)^2 - \frac{3}{5}k_F^2 - p_{K^-}^2}$$

RMF vs. 2pF densities check

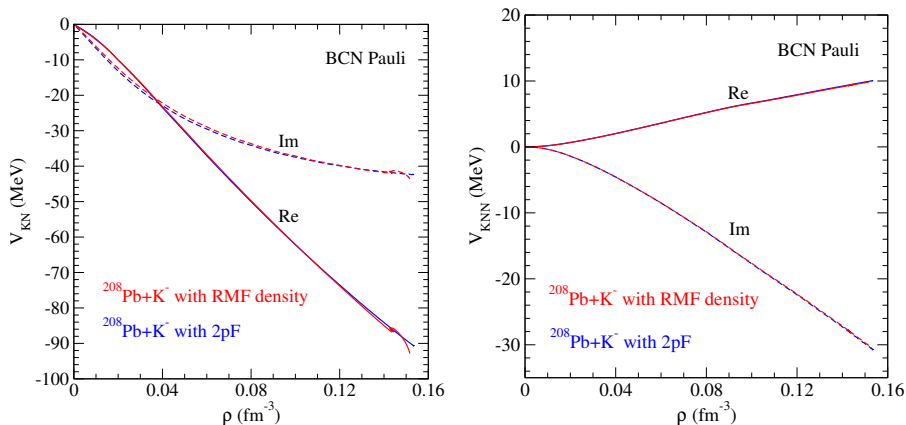


Fig.11: K^-N (left) and K^-NN (right) potentials in ^{208}Pb evaluated using RMF (red) and 2pF (blue) densities, calculated using Pauli BCN amplitudes.

Kaonic atoms calculations

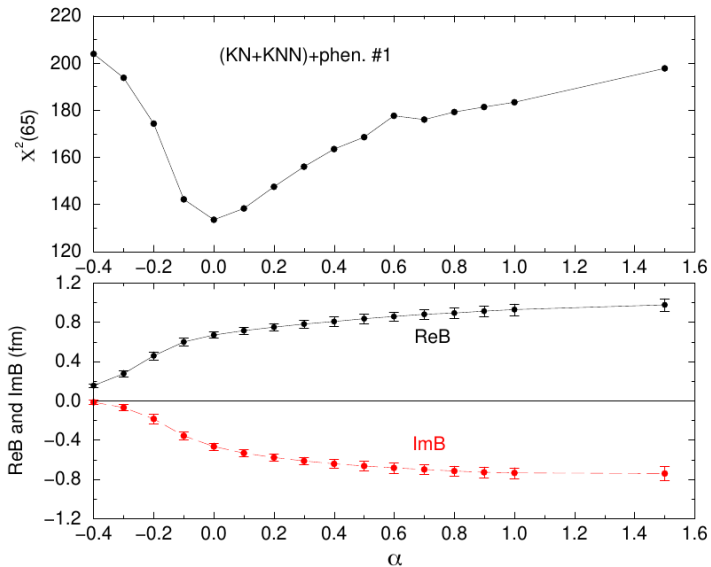
Table 4: Values of χ^2 for shifts, widths and yields in selected K^- atoms, calculated with K^-N , $K^-N + K^-NN$ and $K^-N + \text{phen. multiN}$ potentials based on BCN Pauli or WRW modified amplitudes. Experimental data are shown for comparison.

| BCN | | WRW | | Pauli | | phen. | EXP |
|------------|-----------------------|--------|--------|--------|--------|-------------------|----------------|
| | | KN | +KNN | KN | +KNN | KN + phen. multiN | |
| C^{12} | $\Delta(\epsilon)$ | 74.81 | 20.85 | 8.46 | 4.63 | 0.53 | -0.59 (0.08) |
| | Γ | 22.68 | 21.38 | 9.46 | 5.27 | 1.77 | 1.73 (0.15) |
| | Γ^* | 1.29 | 1.17 | 0.06 | 0.57 | 2.45 | 0.99 (0.20) |
| P^{31} | $\Delta(\epsilon)$ | 23.23 | 6.14 | 1.84 | 1.82 | 0.07 | -0.33 (0.08) |
| | Γ | 10.49 | 12.96 | 6.02 | 4.63 | 0.78 | 1.44 (0.12) |
| | Γ^* | 7.40 | 5.96 | 0.70 | 0.42 | 0.42 | 1.89 (0.30) |
| S^{32} | $\Delta(\epsilon)$ | 324.03 | 134.55 | 74.54 | 77.37 | 15.81 | -0.494 (0.038) |
| | Γ | 20.73 | 40.37 | 5.35 | 3.50 | 0.57 | 2.19 (0.10) |
| | Γ^* | 37.82 | 31.30 | 20.62 | 14.05 | 6.47 | 3.03 (0.44) |
| Cl^{35} | $\Delta(\epsilon)$ | 18.81 | 7.4 | 0.80 | 1.15 | 0.00 | -0.99 (0.17) |
| | Γ | 0.26 | 6.08 | 3.60 | 2.70 | 0.27 | 2.91 (0.24) |
| | Γ^* | 8.78 | 5.32 | 0.60 | 0.24 | 0.17 | 5.8 (1.70) |
| Cu^{63} | $\Delta(\epsilon)$ | 9.31 | 0.43 | 0.20 | 0.56 | 1.23 | -0.370 (0.047) |
| | Γ | 0.05 | 0.46 | 1.33 | 1.40 | 2.23 | 1.37 (0.17) |
| | Γ^* | 1.39 | 0.16 | 0.25 | 0.47 | 1.44 | 5.2 (1.1) |
| Sn^{118} | $\Delta(\epsilon)$ | 2.52 | 2.57 | 4.71 | 5.12 | 3.23 | -0.41 (0.18) |
| | Γ | 0.06 | 0.06 | 0.06 | 0.25 | 0.45 | 3.18 (0.64) |
| | Γ^* | 22.83 | 14.44 | 6.31 | 5.72 | 4.09 | 15.1 (4.4) |
| Pb^{208} | $\Delta(\epsilon)$ | 0.12 | 0.50 | 0.13 | 0.41 | 1.14 | -0.02 (0.012) |
| | Γ | 0.09 | 0.06 | 0.21 | 0.29 | 0.41 | 0.37 (0.15) |
| | Γ^* | 0.11 | 0.26 | 0.39 | 0.44 | 0.50 | 4.1 (2) |
| χ^2 | total | 586.82 | 312.43 | 145.62 | 131.01 | 44.00 | |
| | S_{32}^{out} | 204.24 | 106.20 | 45.10 | 36.09 | 21.16 | |

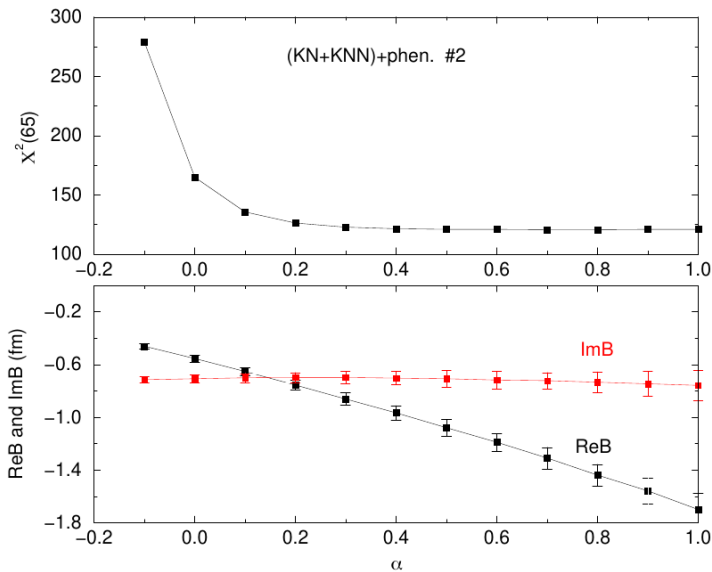
Kaonic atoms calculations

- best χ^2 obtained for $K^-N + \text{mic. } K^-NN$ potentials evaluated using Pauli blocked BCN amplitudes and $p_{K^-} = 150 \text{ MeV}/c$ (other values of p_{K^-} were considered as well)
- these $K^-N + K^-NN$ potentials were calculated for 23 targets and confronted with kaonic atom data $\rightarrow \chi^2(65)=338.2$ (5.20 per point)
- $K^-N + K^-NN$ potentials then supplemented by phenomenological term describing 3 and 4 nucleon processes $\sim -4\pi B(\frac{\rho}{\rho_0})^\alpha \rho$
- values of α and complex amplitude B fitted to data

Fit to kaonic atom data #1: $\text{Re}B > 0$



Fit to kaonic atom data #2: $\text{Re}B < 0$



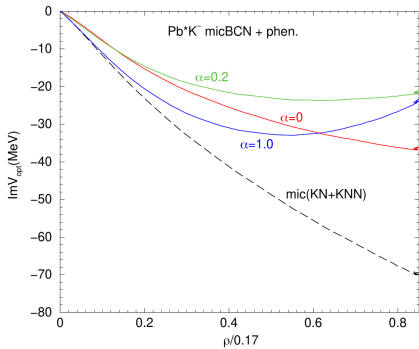
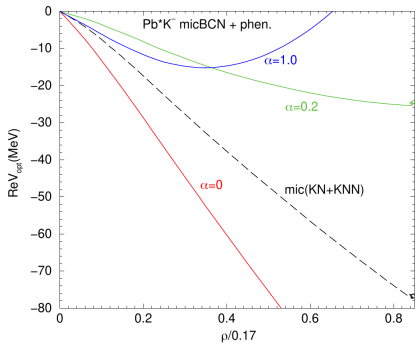
Results

- #1 $\alpha = 0.00 \pm 0.04$, $\text{Re}B = 0.66 \pm 0.04$ fm, $\text{Im}B = -0.46 \pm 0.04$ fm
- #2 $\alpha > 0.3$, $\text{Re}B$ and $\text{Im}B < 0$
- $K^-N \rightarrow K^-N + K^-NN \rightarrow K^-N + K^-NN + \text{phen. term}$

| | K^-N | $K^-N + K^-NN$ | + phen. | $K^-N + \text{phen.}$ |
|----------------------|--------|----------------|---------|-----------------------|
| $\chi^2(65)$ | 2829 | 338.2 | 133 | 112.3 |
| $\chi^2/\text{d.p.}$ | 43.8 | 5.2 | 2.1 | 1.7 |

- additional fit with rescaled potential $\beta_{SF}(K^-N + K^-NN) \rightarrow$
 $\text{Re}\beta_{SF} = 1.68 \pm 0.027$ and $\text{Im}\beta_{SF} = 0.57 \pm 0.022$ and $\chi^2(65) = 113$

Results



Conclusions: $K^- NN$ model

- Interaction of K^- with two and more nucleons important for realistic description of K^- -nucleus interaction
- We have developed a microscopic model for $K^- NN$ absorption in nuclear matter using scattering amplitudes derived from P and BCN chiral meson-baryon interaction models
J. Hrtánková, A. Ramos, PRC 101 (2020) 035204
- Pauli blocked amplitudes included \rightarrow medium effects non-negligible
- Calculated ratios in a good agreement with experimental data!

Conclusions: kaonic atoms calculations

- The microscopic K^-NN model was applied in the calculations of kaonic atoms
- Preliminary results:
 - data are best described by $K^-N + K^-NN$ potentials based on Pauli blocked BCN amplitudes
 - $K^-N + K^-NN$ potentials supplemented by a phenomenological term describing 3 and 4 nucleon processes
 - fit to the data suggests that $\text{Re}(K^-N + K^-NN)$ should be more attractive and $\text{Im}(K^-N + K^-NN)$ should be less absorptive

What to do next?

- test more values for p_{K^-} ($= 0, 100 \text{ MeV}/c$, LDA...)
- different approach to \sqrt{s} from studies of kaonic atoms
- confront with data $K^-N + K^-NN$ potentials based on WRW modified amplitudes
- include missing baryon self-energies in in-medium modified amplitudes
- self-consistent approach