TECHNISCHE UNIVERSITÄT DARMSTADT

On the Hypertriton Lifetime

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GEFÖRDERT VOM

Bundesministerium
für Bildung
und Forschung

Outline

TECHNISCHE UNIVERSITÄT DARMSTADT

- Theoretical Framework
- Motivation for our Calculation

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- Weak interaction and Final State Interactions
- Phase Space

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- Phase Space

- Our Results
- Analysis and Summary

Theoretical Framework
$\Rightarrow$ Pionless EFT

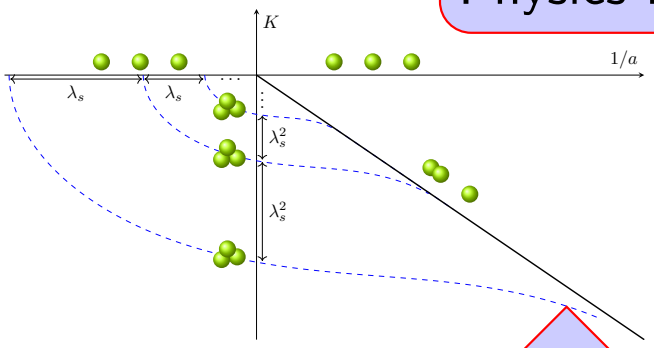
Shallow S-Wave State

$J^P = \frac{1}{2}^+$

Distinguishable

Theoretical Framework
$\Rightarrow$ Pionless EFT

Physics Determined by a and Λ_*



Large Scattering Length

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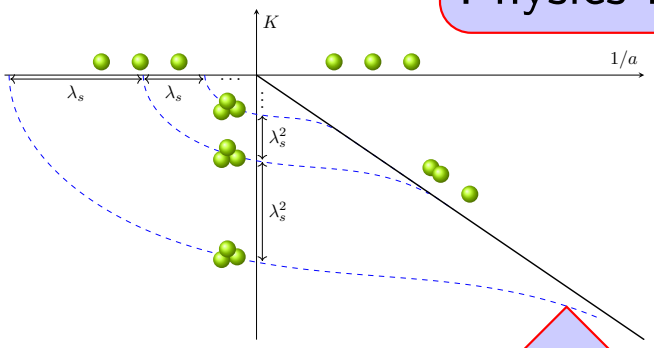

Universal Relations Between Observables

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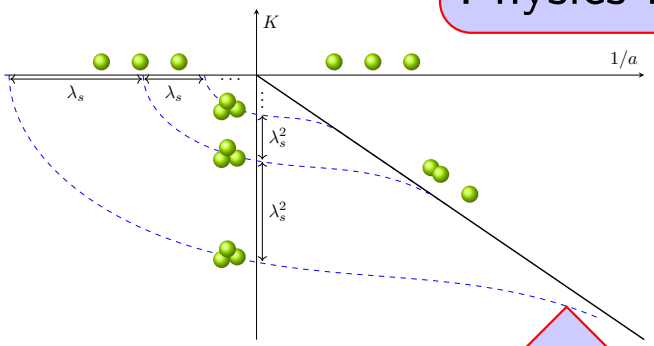

Universal Relations Between Observables

- B_Λ and $< r^2 >$
- B_Λ and τ
- B_Λ and $a_{\Lambda d}$

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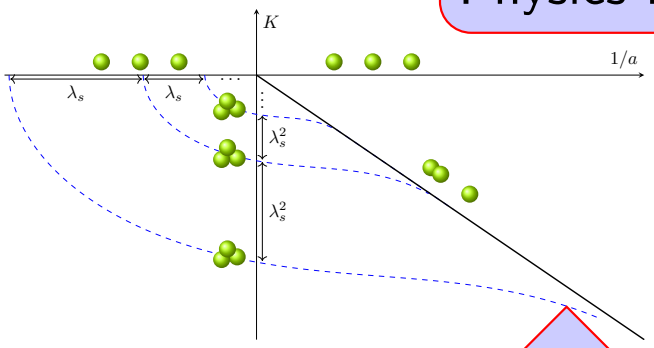

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Pionless EFT
Controllable Uncertainties
Systematic Improvement

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$J^P = \frac{1}{2}^+$

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Theoretical Framework
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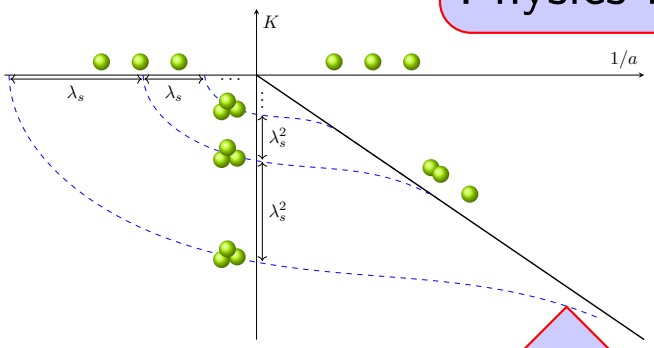

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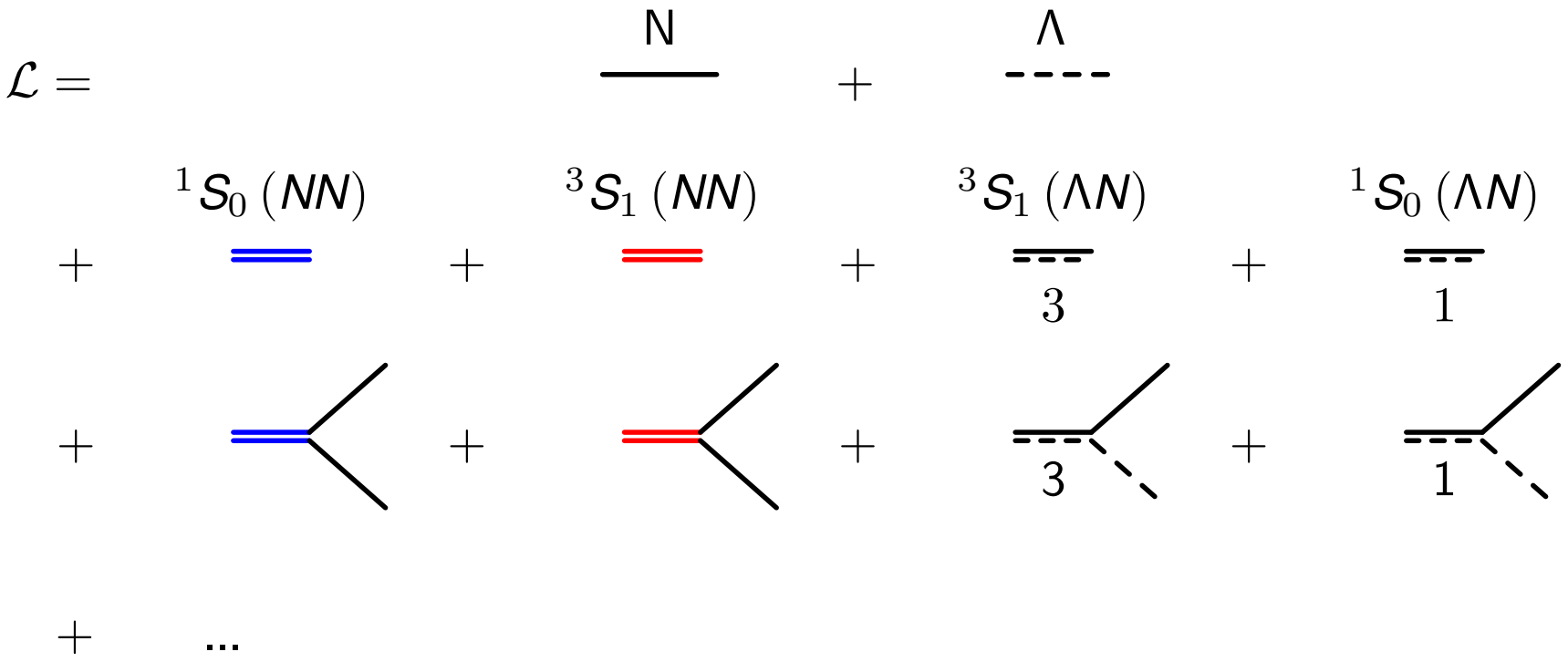
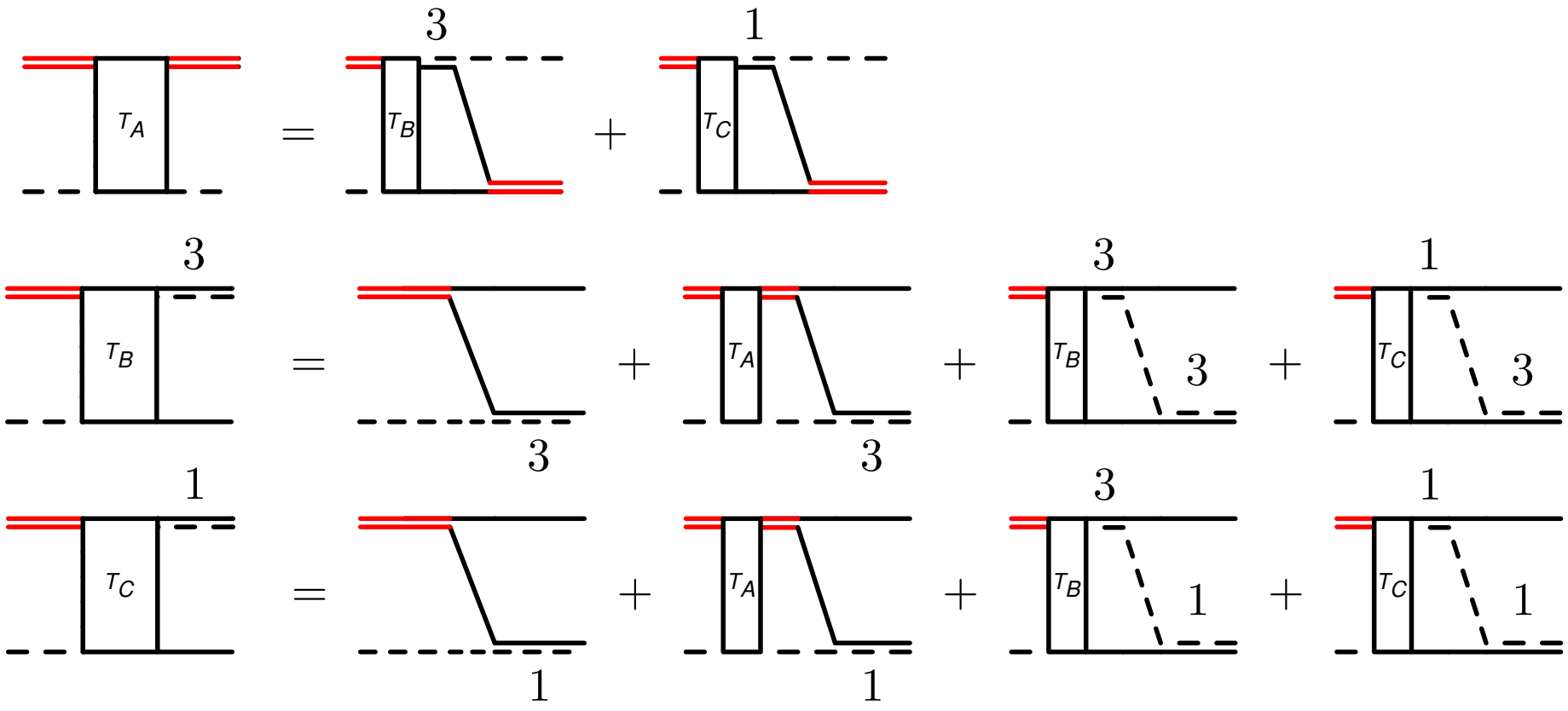
Systematic Improvement

Last time B_Λ and $a_{\Lambda d}$
Today B_Λ and τ

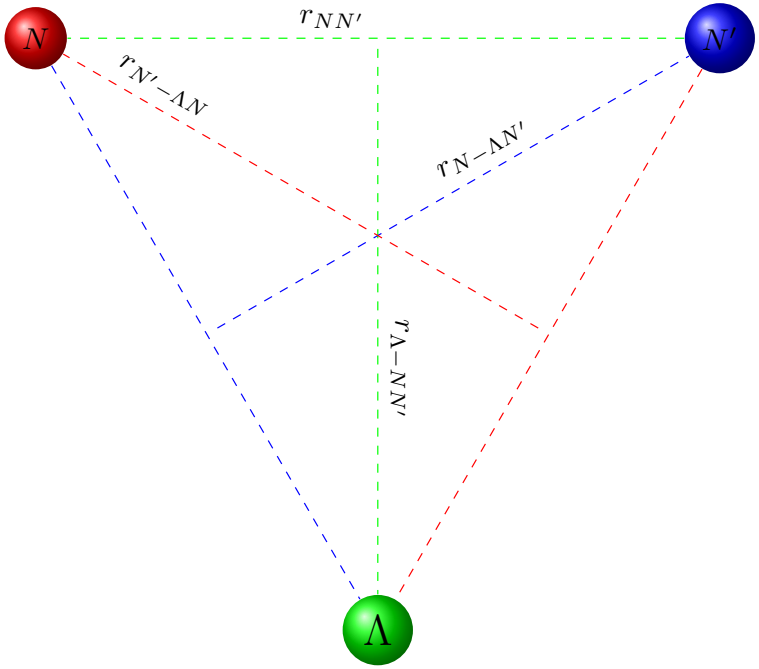
Lagrangian Hypertriton and Λnn



Integral Equations Hypertriton



Matter Radii



Calculation of Form Factors out of the Wave Functions:

$$F_i\left(\mathbf{k}^2\right) = \int \mathrm{d}^3p \int \mathrm{d}^3q\, \Psi_i\left(p,q\right) \Psi_i\left(p, |\mathbf{q}-\mathbf{k}|\right)$$

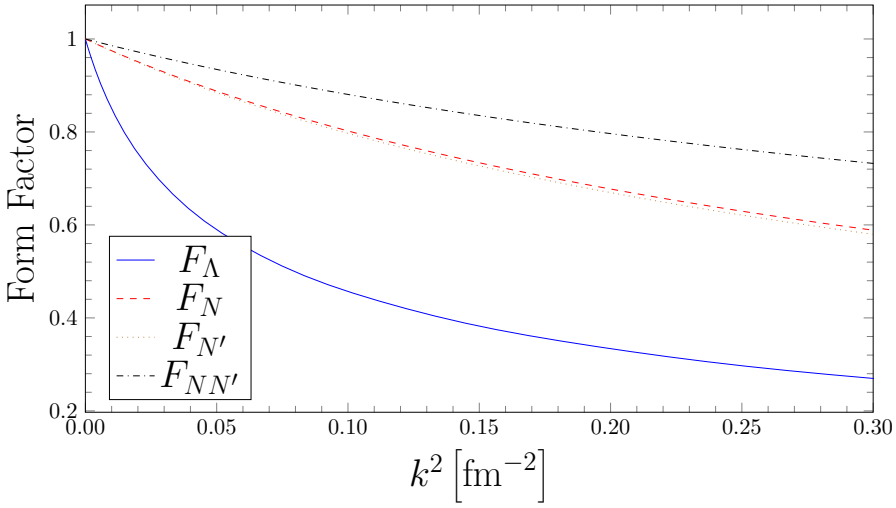
Directly Related to Different Matter Radii as Expansion in k^2

$$F_i\left(\mathbf{k}^2\right) = 1 - \frac{1}{6}\mathbf{k}^2 \langle r^2_{i-jk}\rangle + \ldots$$

2-Body$\Rightarrow$ One Radius
3-Body$\Rightarrow$ Many Radii

Most Interesting
$r_{\Lambda-NN'} \Leftrightarrow r_{\Lambda d}$

Matter Radii Hypertriton



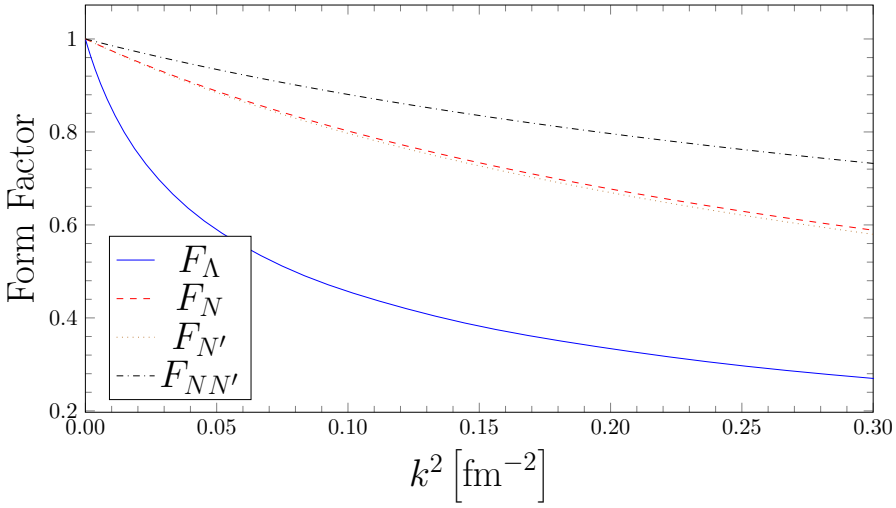
Expectation from Two-Body Calculation:

$$B_2 = \frac{1}{2\mu a^2} \quad \text{and} \quad \langle r^2 \rangle = \frac{a^2}{2}$$

$$\Rightarrow \sqrt{\langle r^2_{NN'} \rangle} \approx 3.04 \text{ fm}$$

$$\sqrt{\langle r^2_{\Lambda-NN'} \rangle} \approx 10.34 \text{ fm}$$

Matter Radii Hypertriton



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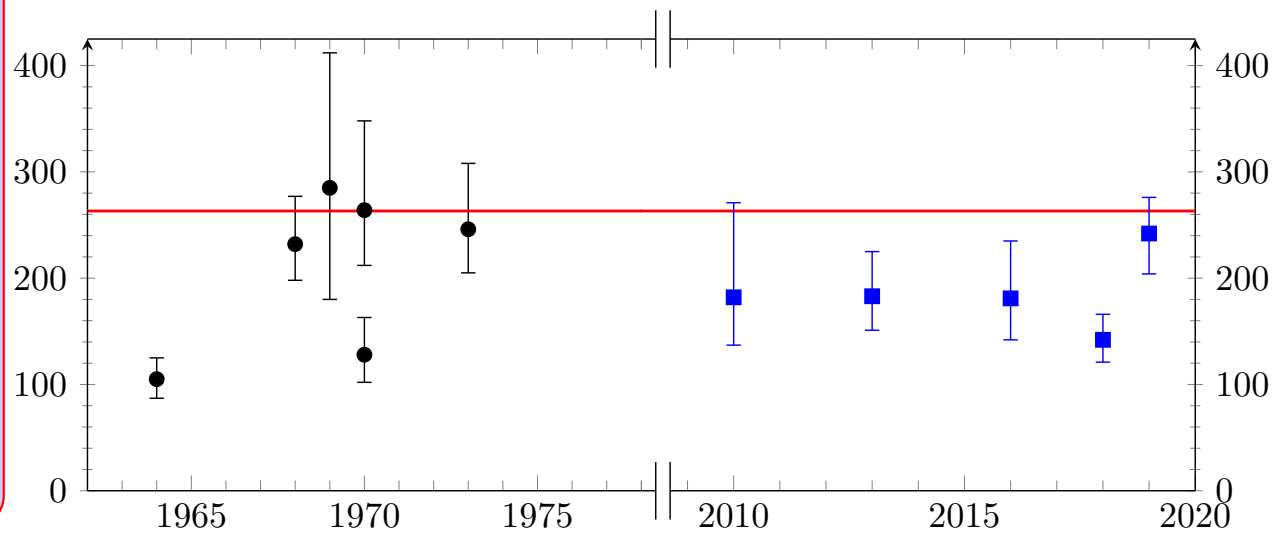
$$\sqrt{\langle r^2_{\Lambda-NN'} \rangle} \approx 10.34 \text{ fm}$$

$\sqrt{\langle r^2_{\Lambda-NN'} \rangle}$[fm]	$\sqrt{\langle r^2_{N'-\Lambda N} \rangle}$[fm]	$\sqrt{\langle r^2_{N-N'\Lambda} \rangle}$[fm]	$\sqrt{\langle r^2_{NN'} \rangle}$[fm]
10.79	3.96	4.02	2.96
$+3.04/-1.53$	$+0.40/-0.25$	$+0.41/-0.25$	$+0.06/-0.05$

Insensitive to Details of Λ-N Interaction

Lifetime Hypertriton Channels and Isospin Rule

- Two-Body Picture Works
- Calculate Lifetime in a Theory with Fundamental Deuteron
- Focus on B_Λ Dependence



Lifetime Hypertriton Channels and Isospin Rule

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$^3_\Lambda\mathrm{H} \mapsto \pi^- + {}^3\mathrm{He}$, $^3_\Lambda\mathrm{H} \mapsto \pi^0 + {}^3\mathrm{H}$,

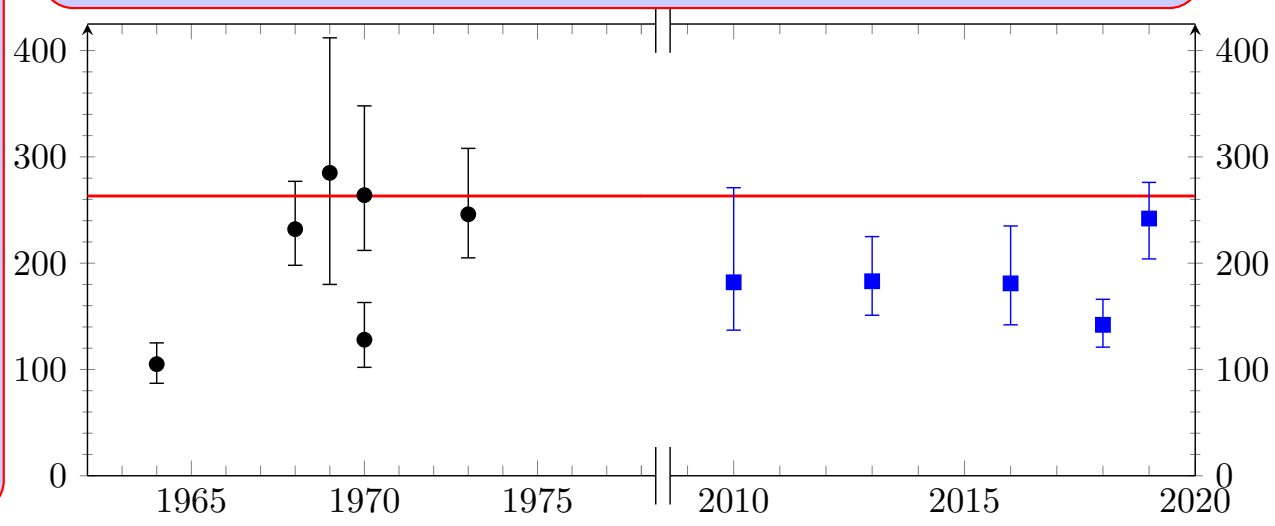
$^3_\Lambda\mathrm{H} \mapsto \pi^- + d + p$, $^3_\Lambda\mathrm{H} \mapsto \pi^0 + d + n$,

$\cancel{^3_\Lambda\mathrm{H} \mapsto \pi^- + p + n + p}$, $\cancel{^3_\Lambda\mathrm{H} \mapsto \pi^0 + p + n + n}$

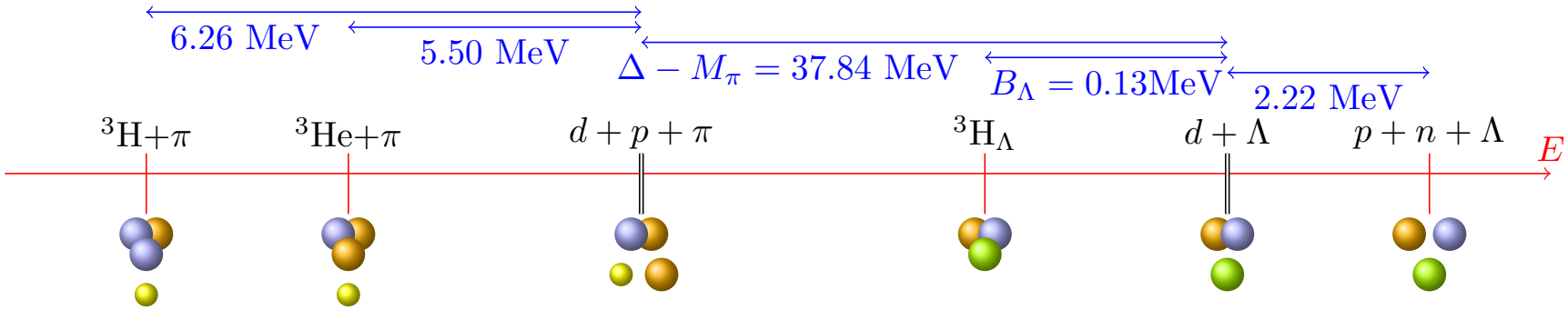
Charged and Uncharged Channel Are Related by the $\Delta I = \frac{1}{2}$ Rule
$\Rightarrow$ Calculate only one

- Two-Body Picture Works
- Calculate Lifetime in a Theory with Fundamental Deuteron
- Focus on B_Λ Dependence

Leptonic and Non-Mesonic Decays are Negligible



Lifetime Hypertriton
Thresholds and Feynman Diagrams



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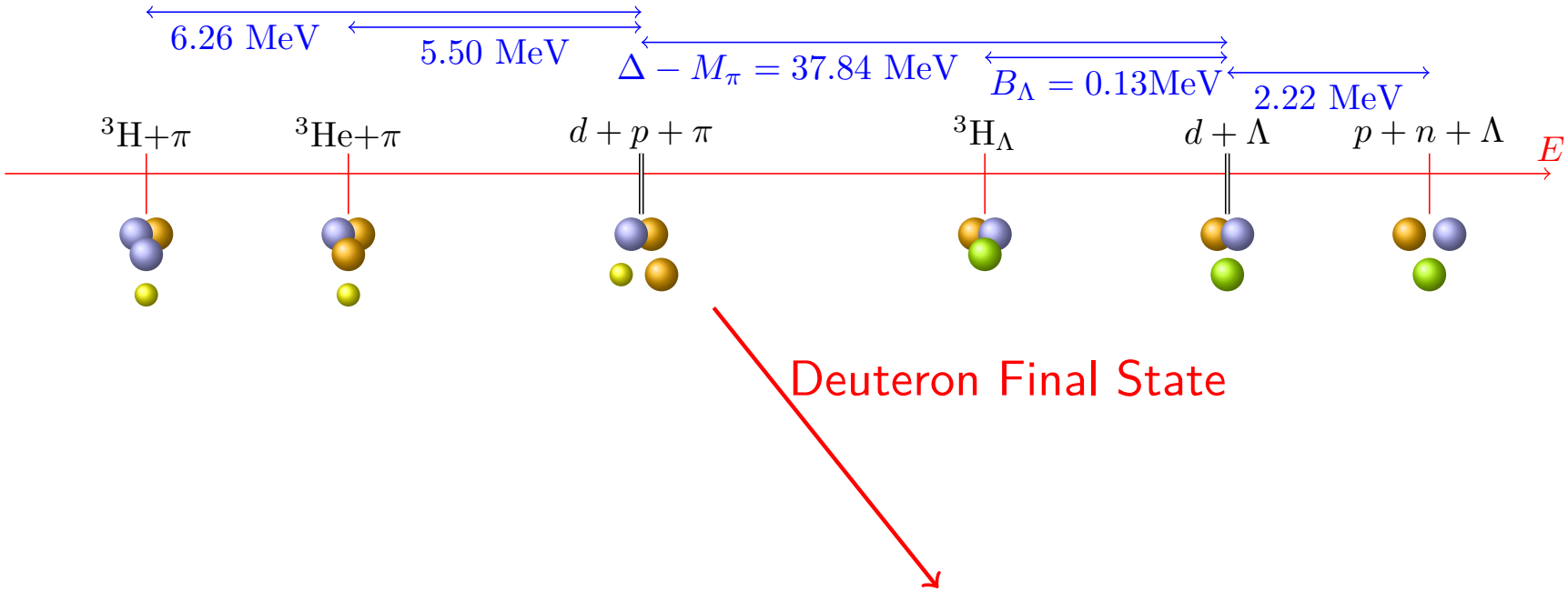

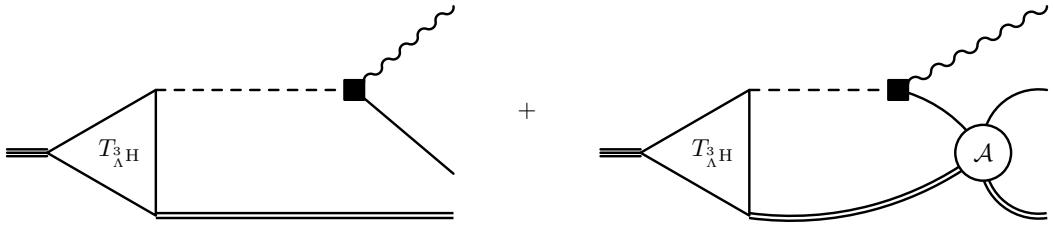

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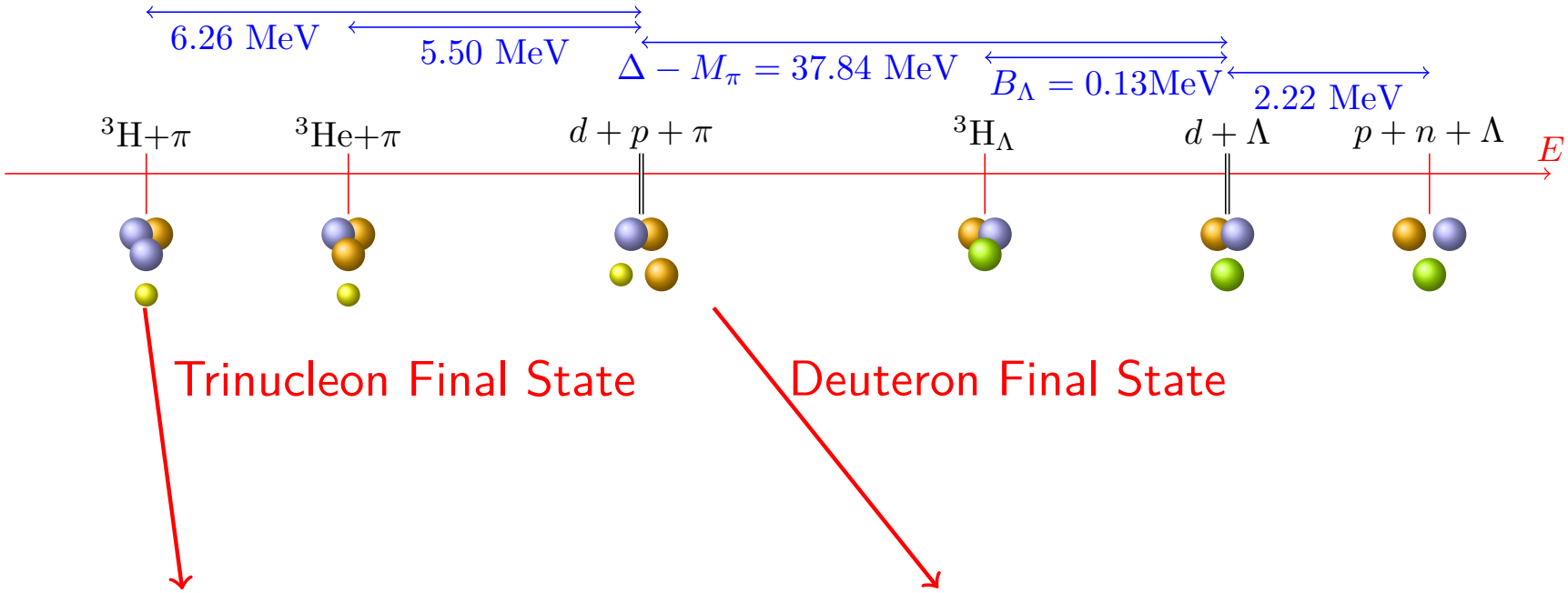
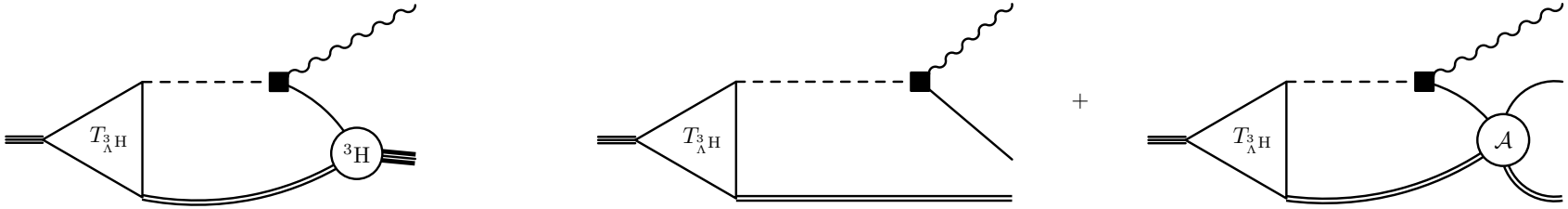




Weak Interaction

$$\mathcal{M}_{\Lambda \mapsto n\pi^0} = -iG_F M_\pi^2 \bar{u}\left(\mathbf{p}'\right)\left[\tilde{A}_\pi + \tilde{B}_\pi \gamma_5\right] u\left(\mathbf{p}\right)$$

non-relativistic reduction

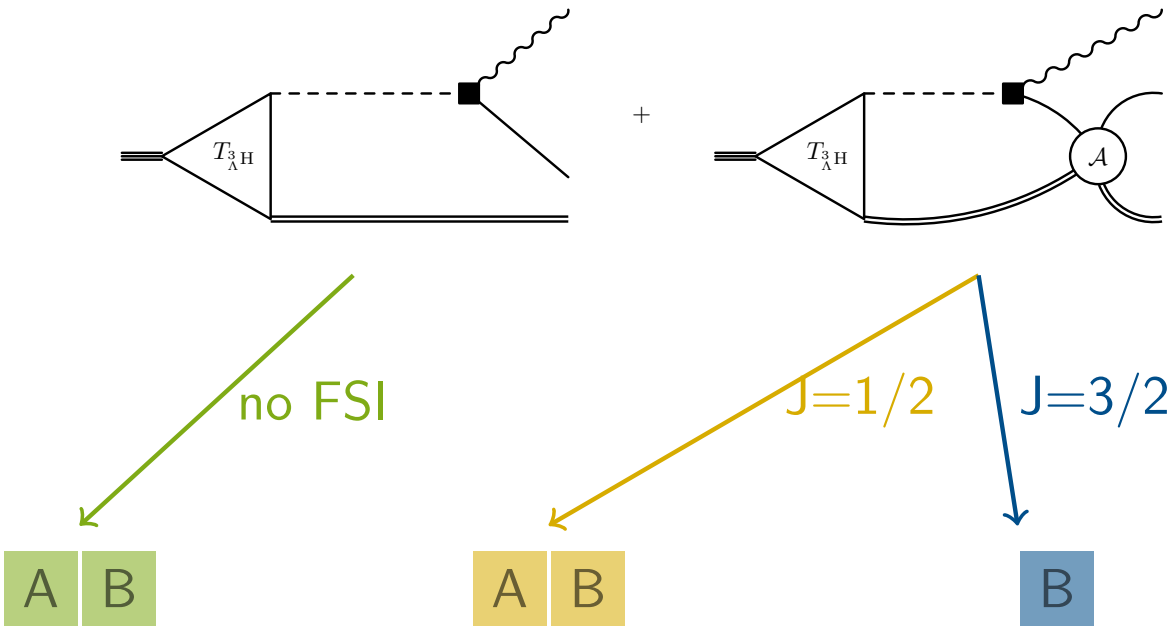
$$\mathcal{M}^{\text{reduced}}_{\Lambda \mapsto n\pi^0} = -iG_F M_\pi^2 \left(A_\pi + \frac{B_\pi}{M_\Lambda + m}\boldsymbol{\sigma}\cdot\mathbf{k}\right)$$

two contributions A_π and B_π

A

B

Contributions to the Deuteron Final State



square product leads towards interference terms

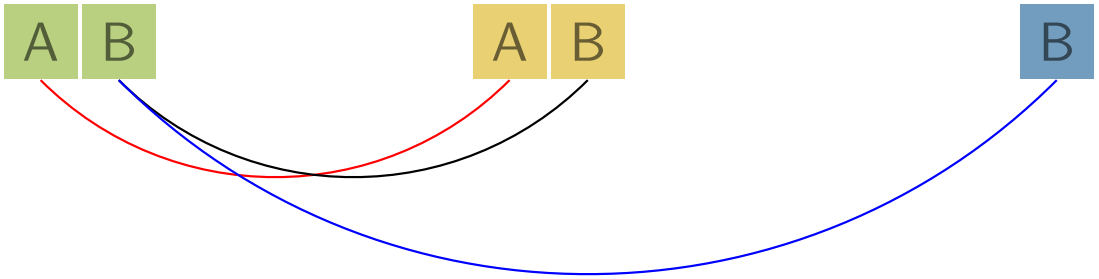
Contributions to the Deuteron Final State

A B

A B

B

Contributions to the Deuteron Final State



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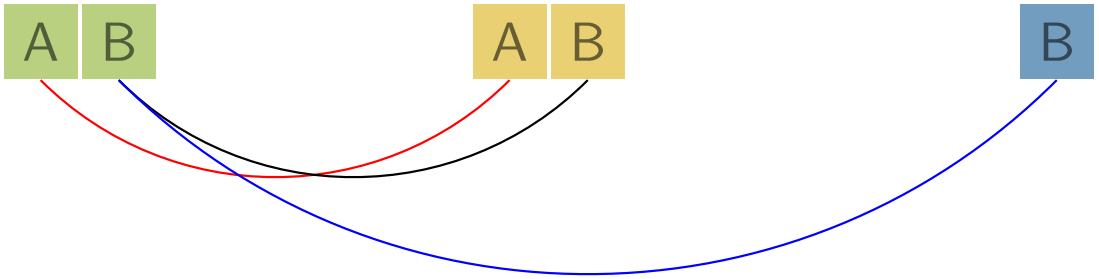
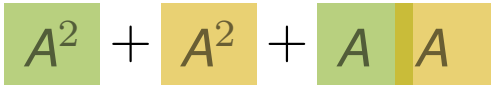


$\Gamma =$ 

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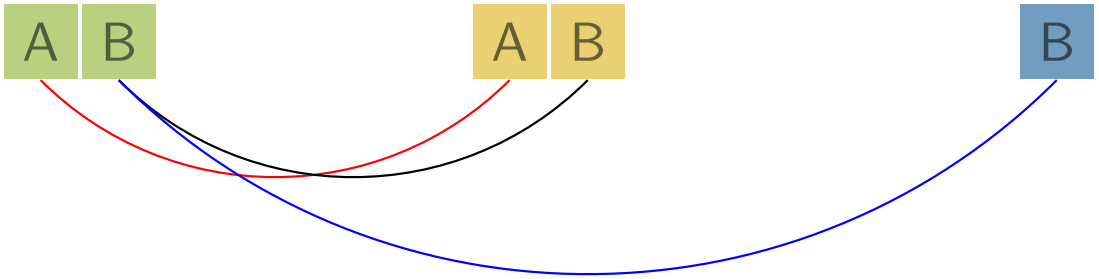

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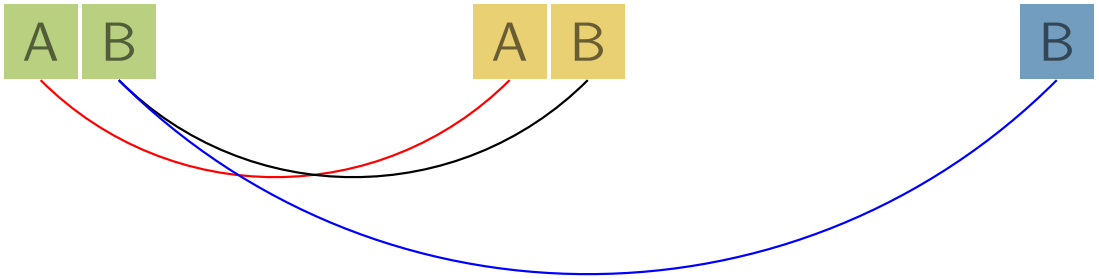

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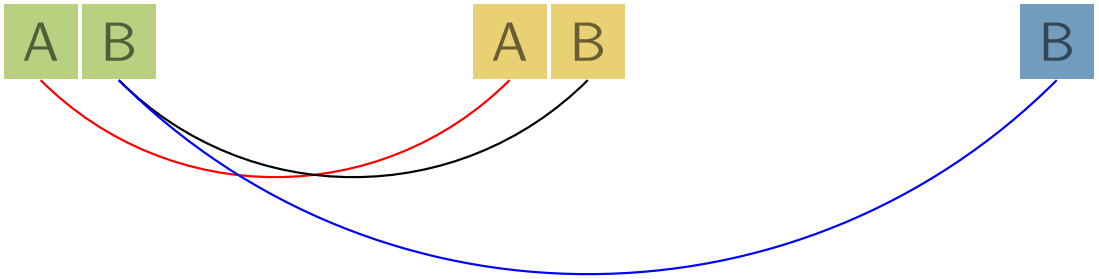
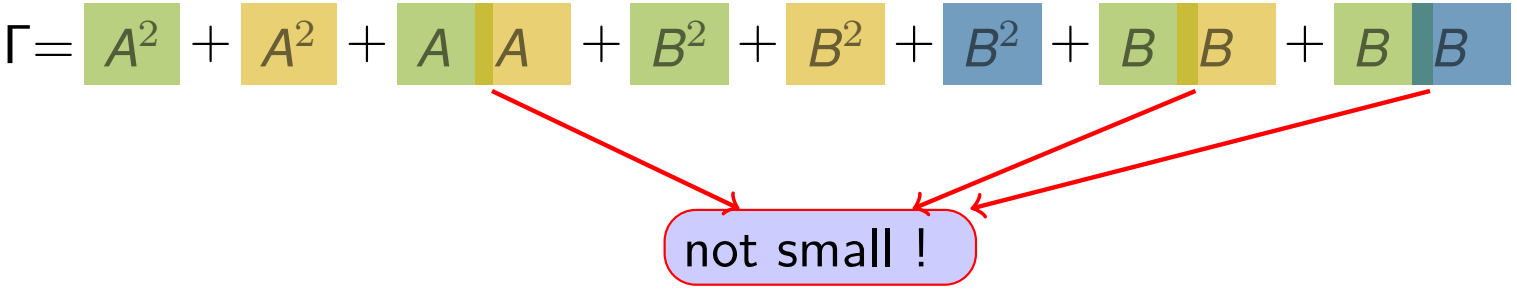
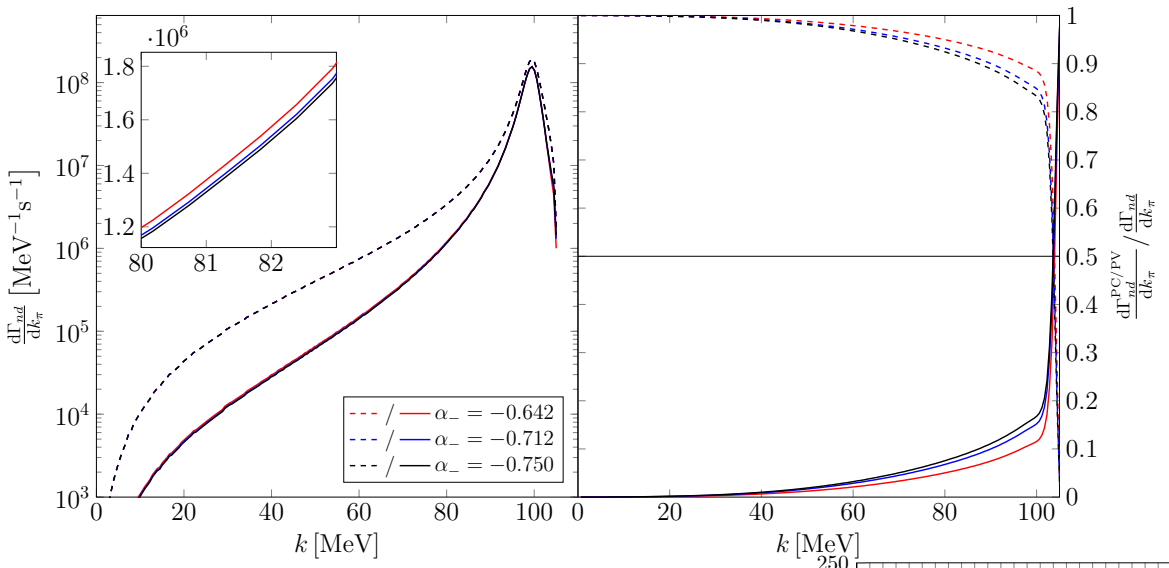


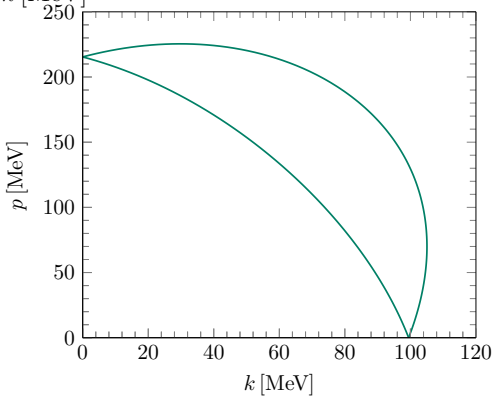


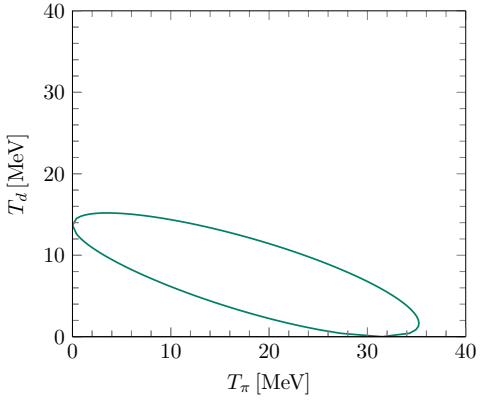
Phase Space and α dependence



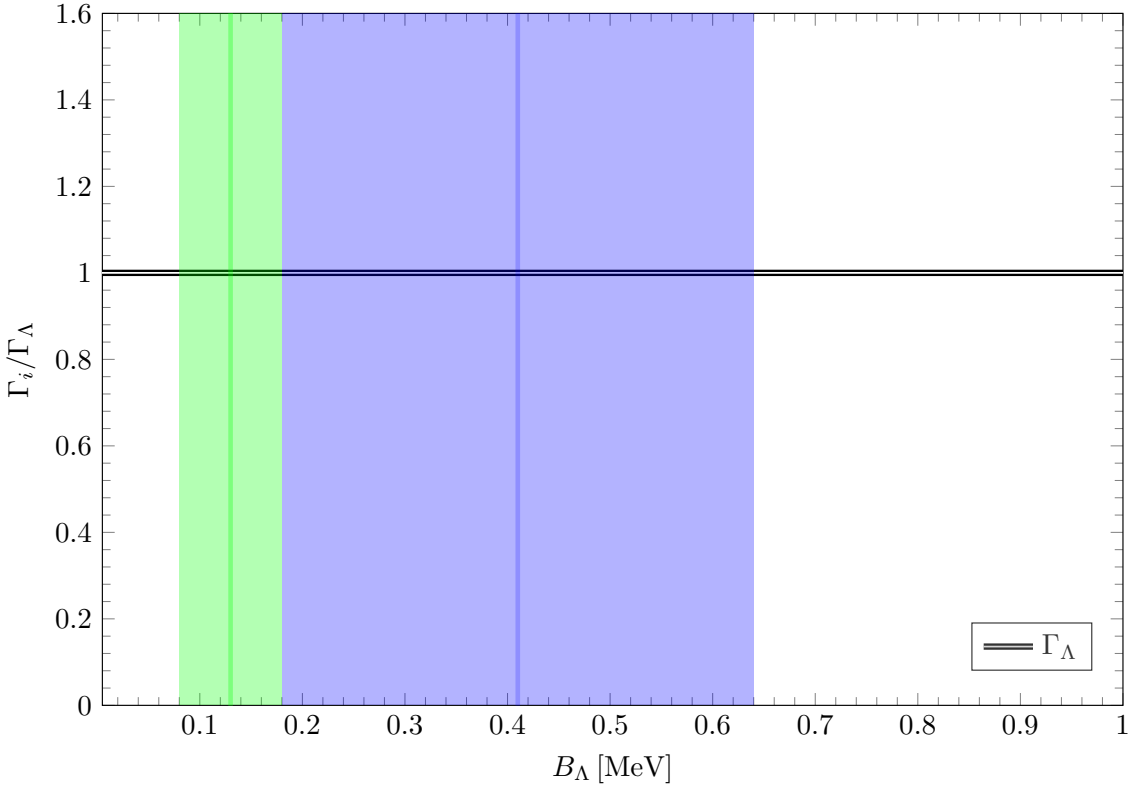
- dependence on α negligible
- small changes in PC and PV contributions
- final state interactions are important

- main contribution at high k_π
- full phase space calculation





Hypertriton Width and Branching Ratios



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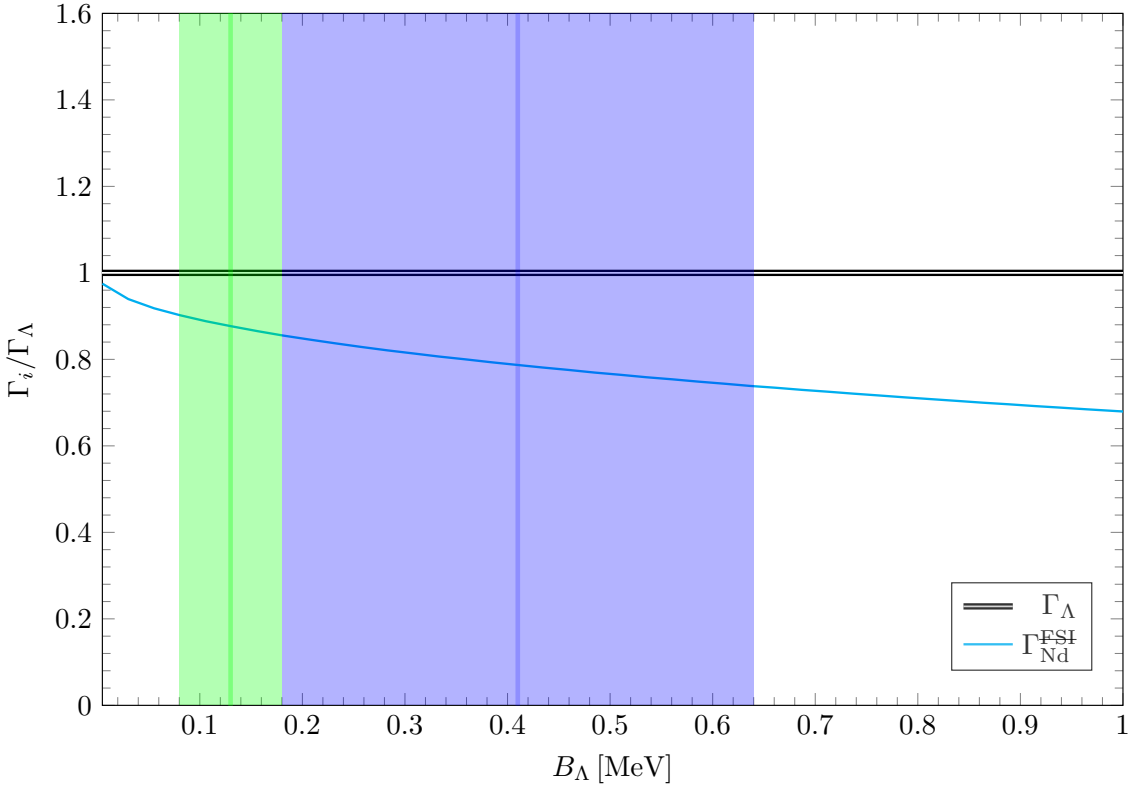

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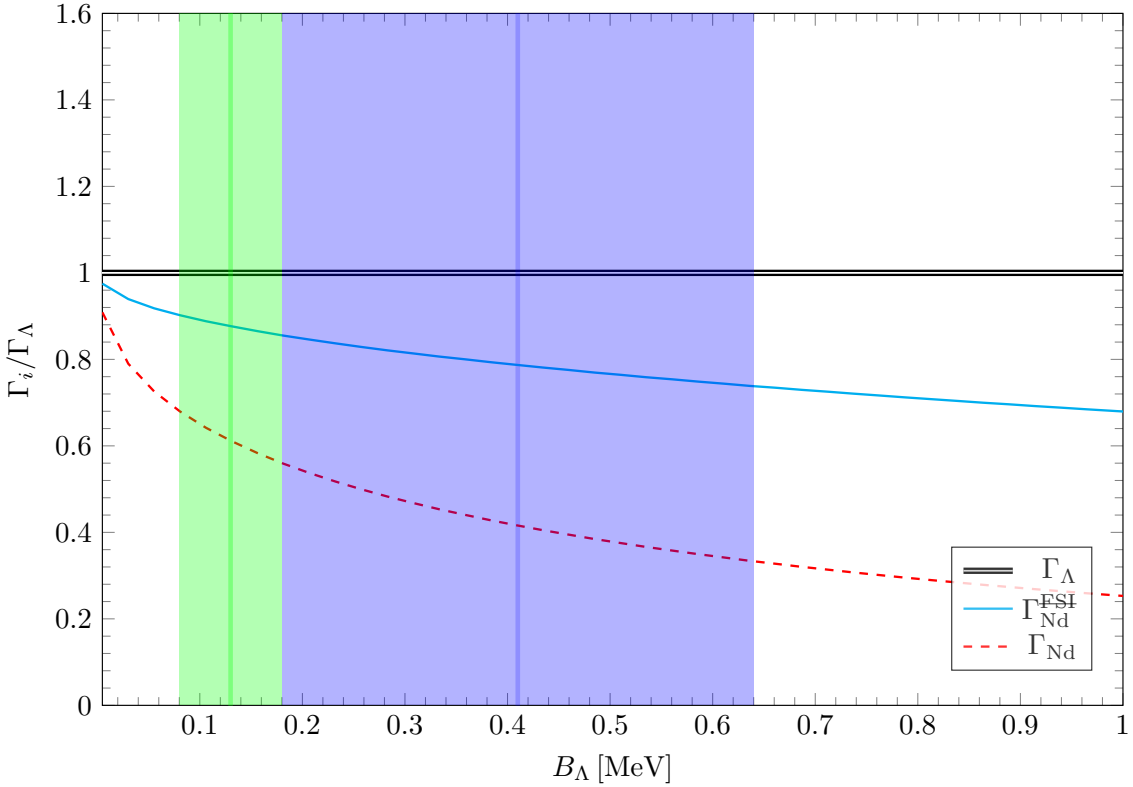

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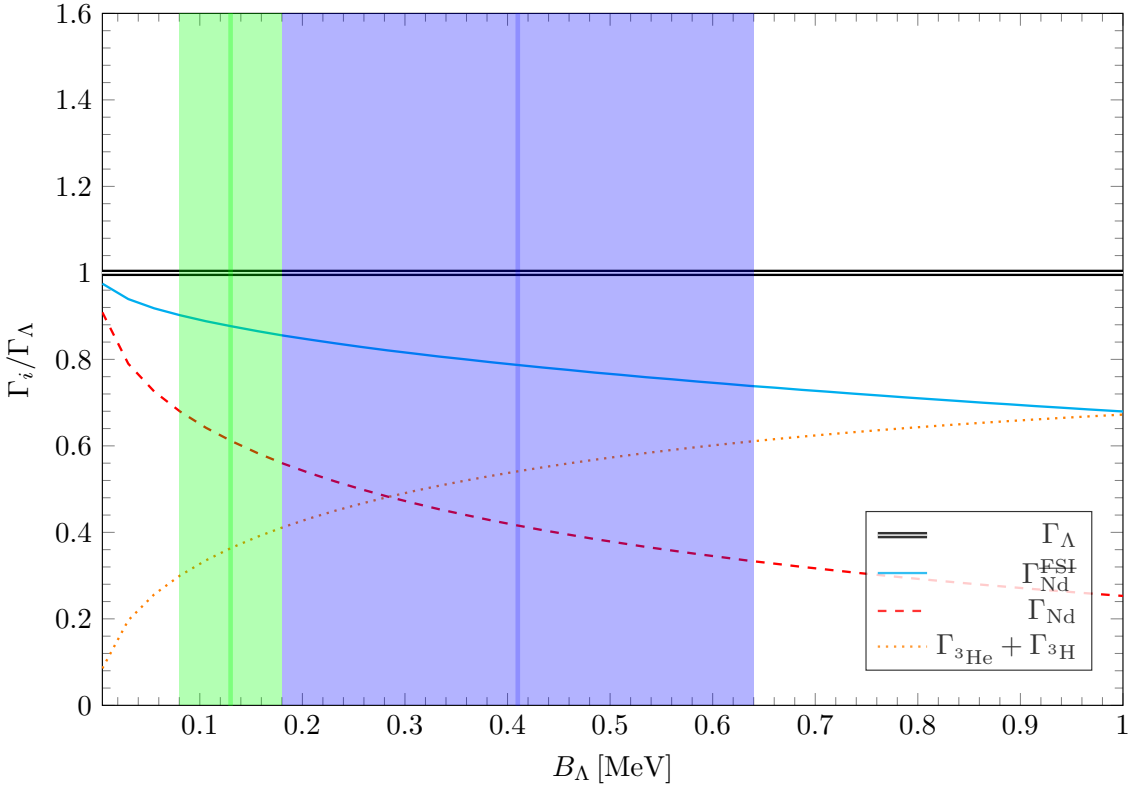

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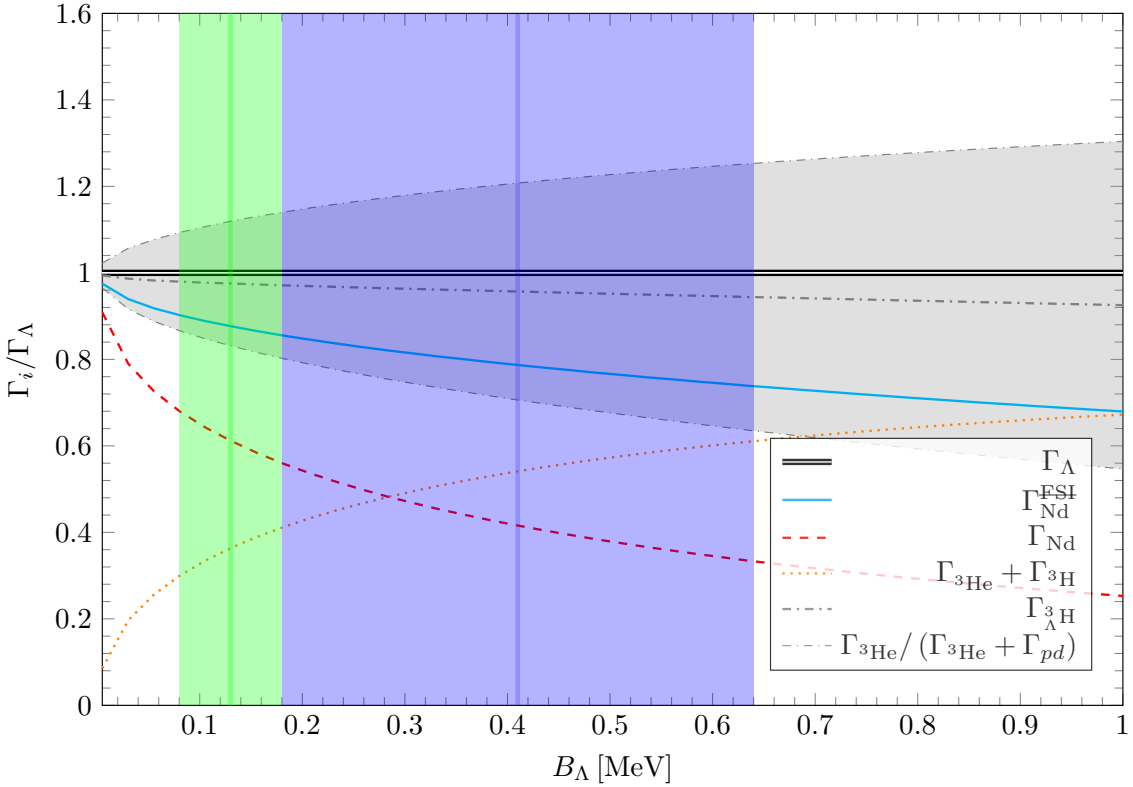

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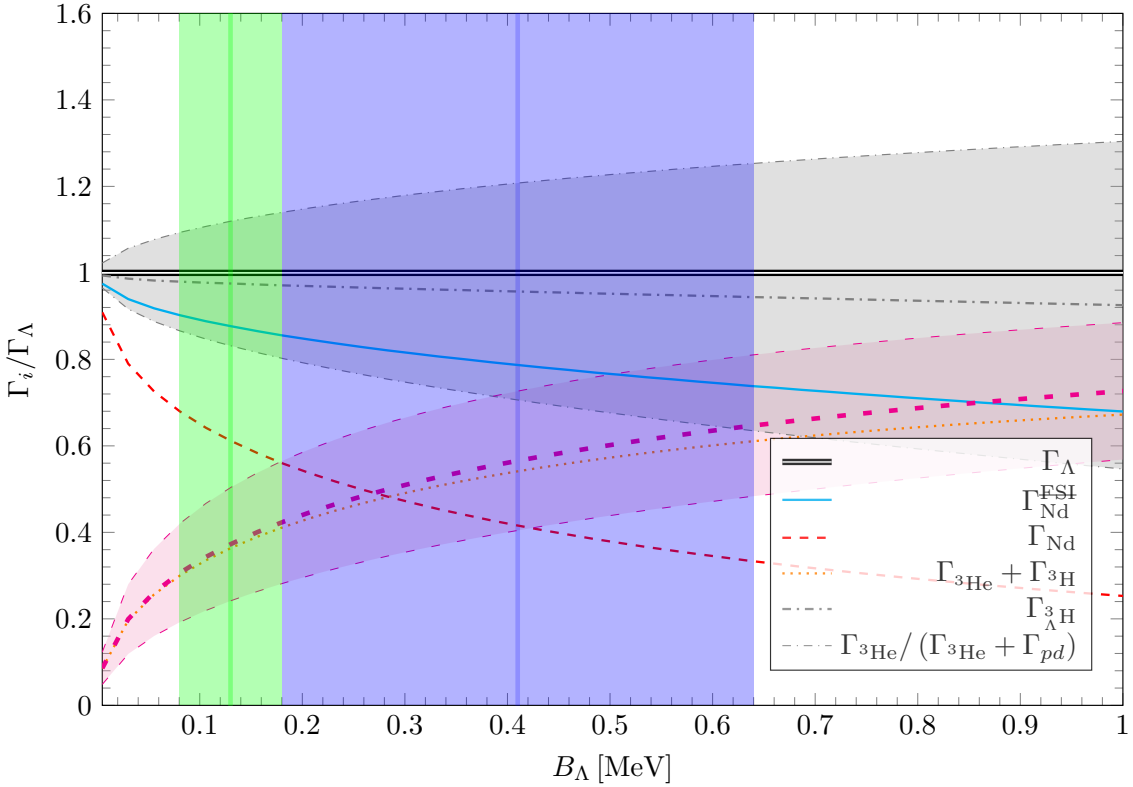

- $\Gamma_{^3_\Lambda H}$ Barely Depends on B_Λ
- Final State Interactions are Important
- $\Gamma_{^3\mathrm{He}}/(\Gamma_{^3\mathrm{He}} + \Gamma_{pd})$ Depends Strongly on B_Λ
- STAR Branching ratio $0.32(5)(8)$

Emulsion Data: $R = \Gamma_{^3\mathrm{He}}/(\Gamma_{^3\mathrm{He}} + \Gamma_{pd}) = 0.3 - 0.4$

Hypertriton Width and Branching Ratios

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Our Results:

- $\Gamma_{^3_\Lambda H}(0.13) = 0.98 \pm 0.15 \Gamma_\Lambda$
- $\Gamma_{^3_\Lambda H}(0.41) = 0.98 \pm 0.25 \Gamma_\Lambda$
- $R(0.13) = 0.38 \pm 0.05$
- $R(0.41) = 0.57 \pm 0.11$

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Consistent:

- Calculation by Congleton for Γ and R
- Calculation by Kamada for Γ and R
- Emulsion Data $0.05\text{MeV} \lesssim B_\Lambda \lesssim 0.2\text{MeV}$

Hypertriton Width and Branching Ratios

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Slight Tension:

- STAR results Branching ratio $R = 0.32 \pm 0.05 \pm 0.08$

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Good part:

- EFT systematic improvment possible
- Go to NLO or three-body

Summary

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- Elegant theory with few input parameters
- Branching ratio as results and not as input
- Consistent results with a fundamental deuteron including the full three-body phase space
- Branching ratio favors small binding energies
- Systematic improvement possible in the future
- Important to combine different observables: binding energy, lifetime and branching ratios to resolve the hypertriton puzzle