

Joint THEIA-STRONG2020  
and JAEA/Mainz REIMEI Web-Seminar

Spectroscopy of  ${}^3_{\Lambda}\text{H}$ ,  ${}^4_{\Lambda}\text{H}$  and other  
hypernuclei with electron beam at JLab

Graduate School of Science, Kyoto University, Japan

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Oct 21, 2020



京都大学  
KYOTO UNIVERSITY

科研費  
KAKENHI

**SPIRITS**  
SUPPORTING PROGRAM FOR INTERACTION-BASED  
INITIATIVE TEAM STUDIES

# CONTENTS

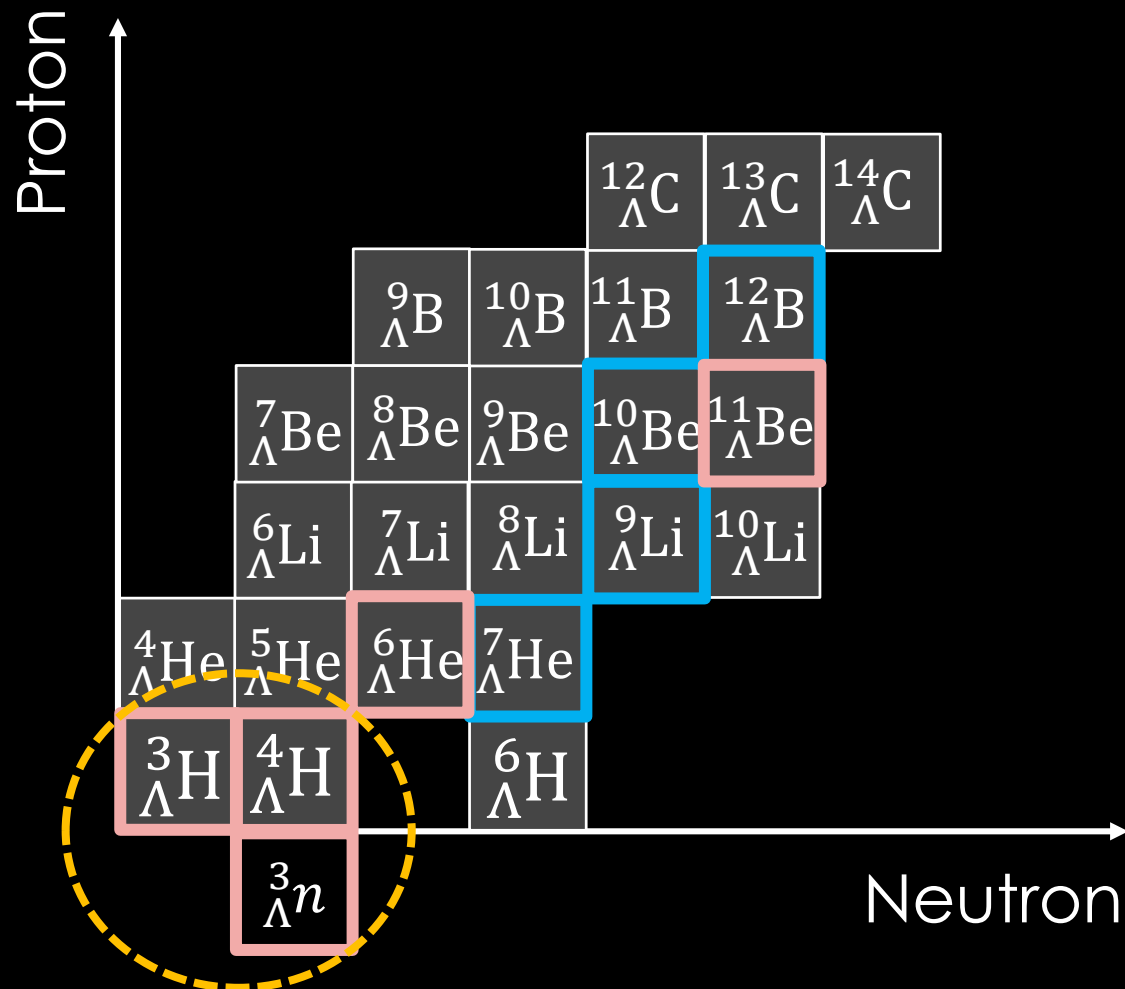
## 1. Brief Introduction

## 2. Experiments at JLab Hall A

- nn $\Lambda$  Search (E12-17-003)
- ${}^{3,4}\text{H}$  (C12-19-002)

## 3. Summary

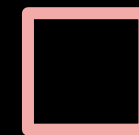
# HYPERNUCLEAR CHART FOR LIGHT MASS REGION ( $Z < 7$ )



( $e, e'K^+$ ) experiment



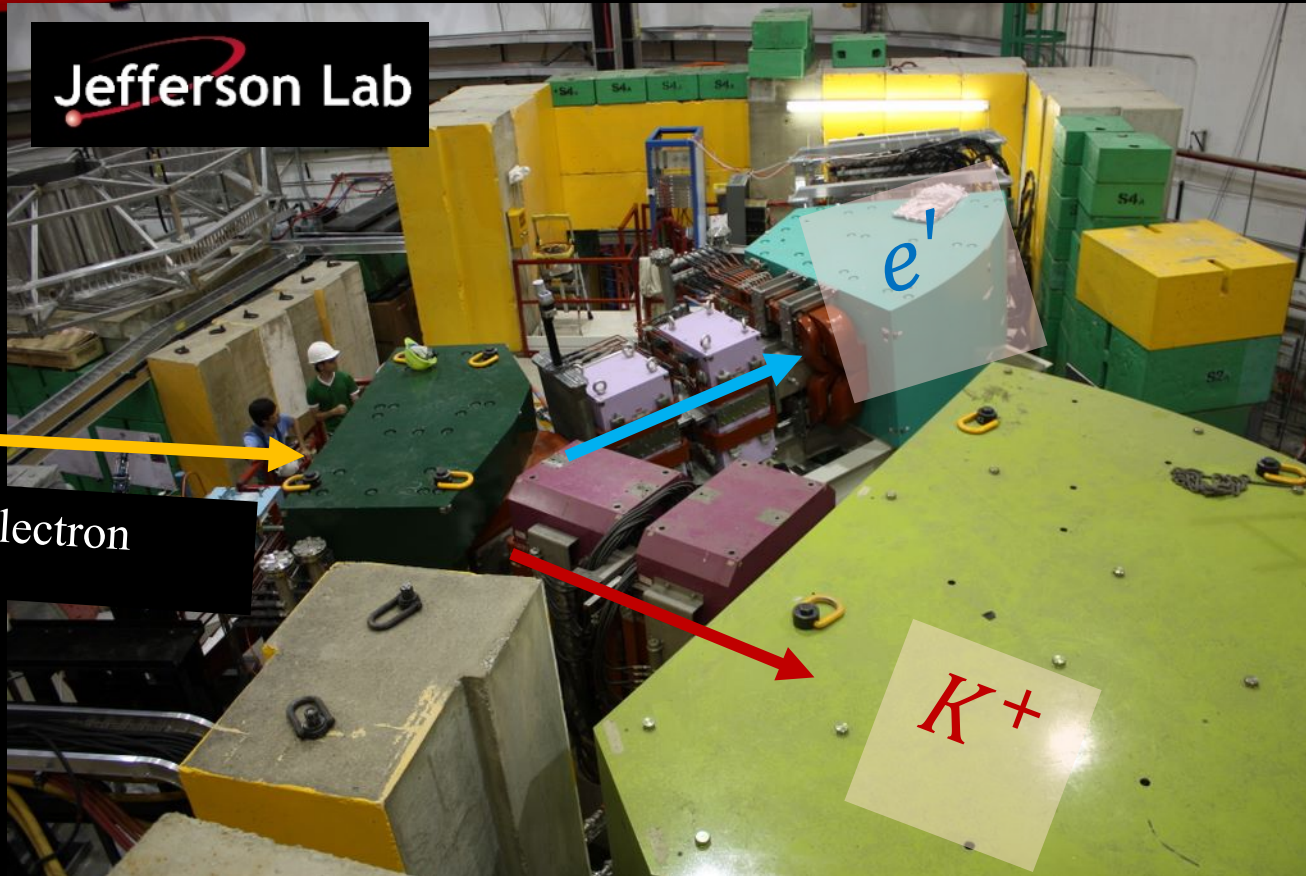
Published



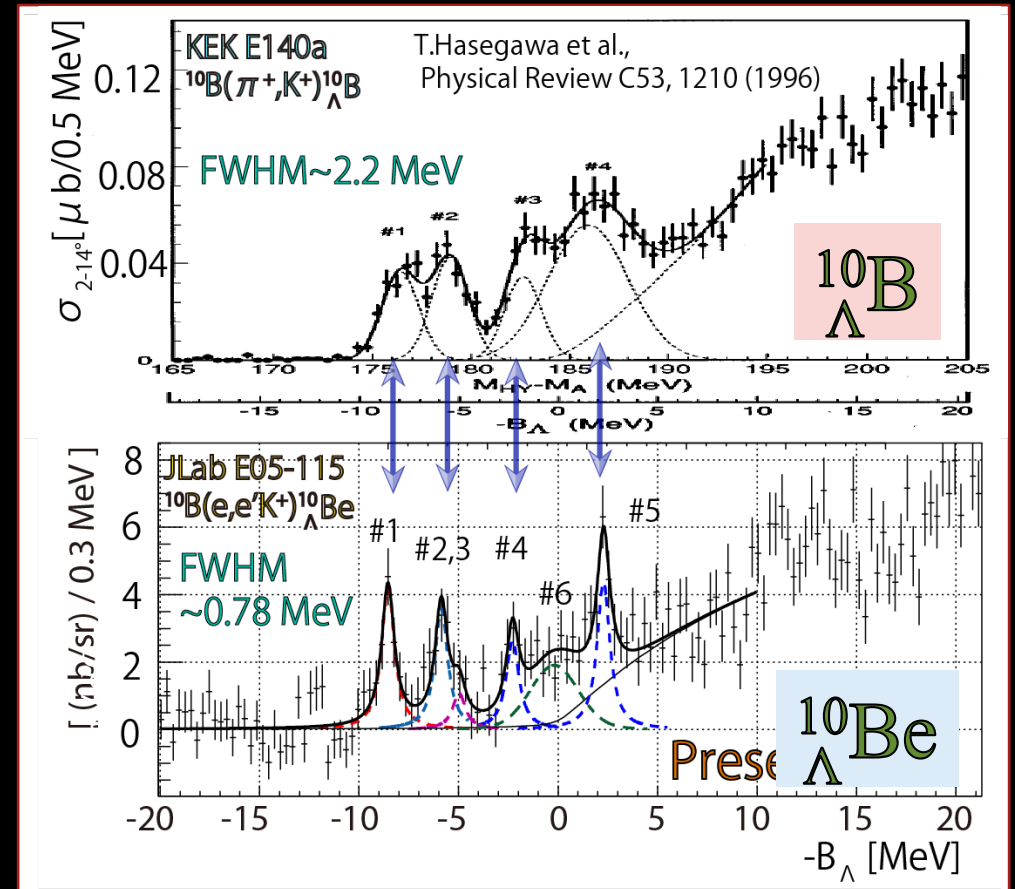
In Analysis/  
Future Plan

This talk

# High precision measurement $^{10}_{\Lambda}\text{B}$ and $^{10}_{\Lambda}\text{Be}$

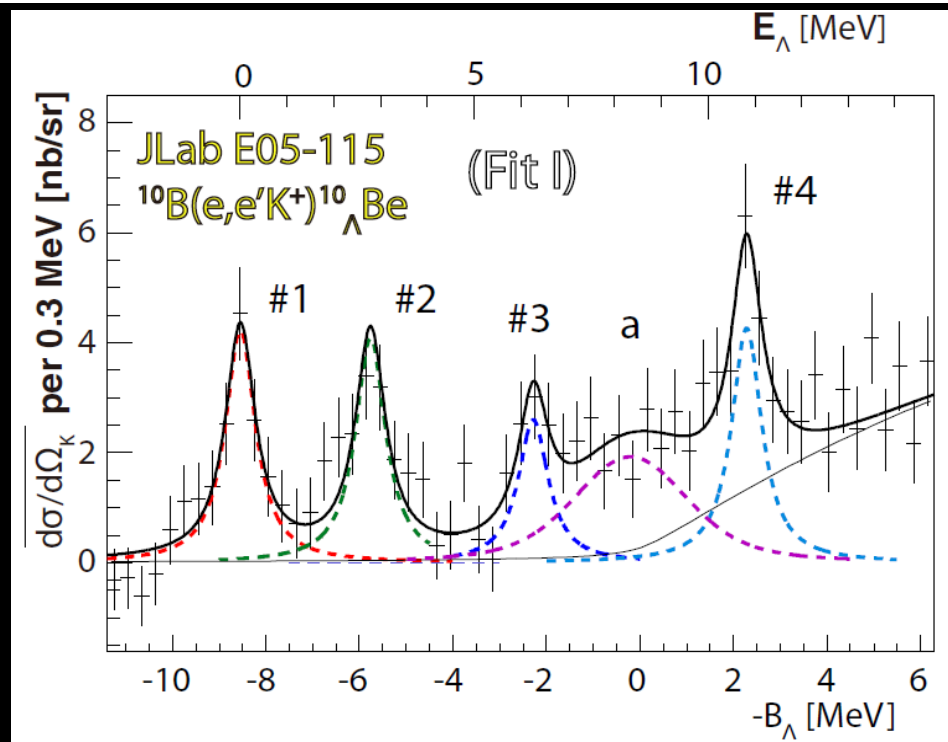
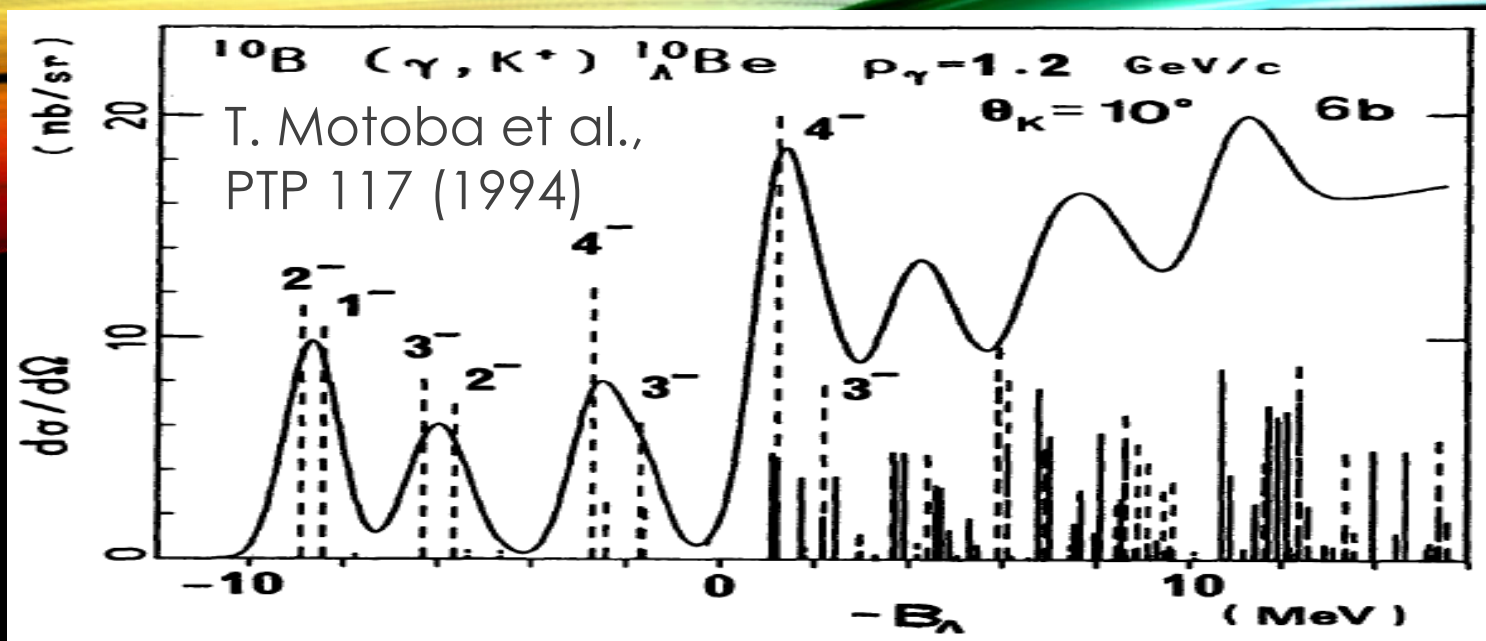


- ✓ High resolution
- ✓ High accuracy



RPC 93 (2016) 034314.





TG et al., PRC 93 (2016) 034314.

What's surplus, a ?

- Conventional shell model did not predict the state
- It was found that model space needs to be extended (A. Umeya et al., JPS Conf. Proc. 26, 023016 (2019)).

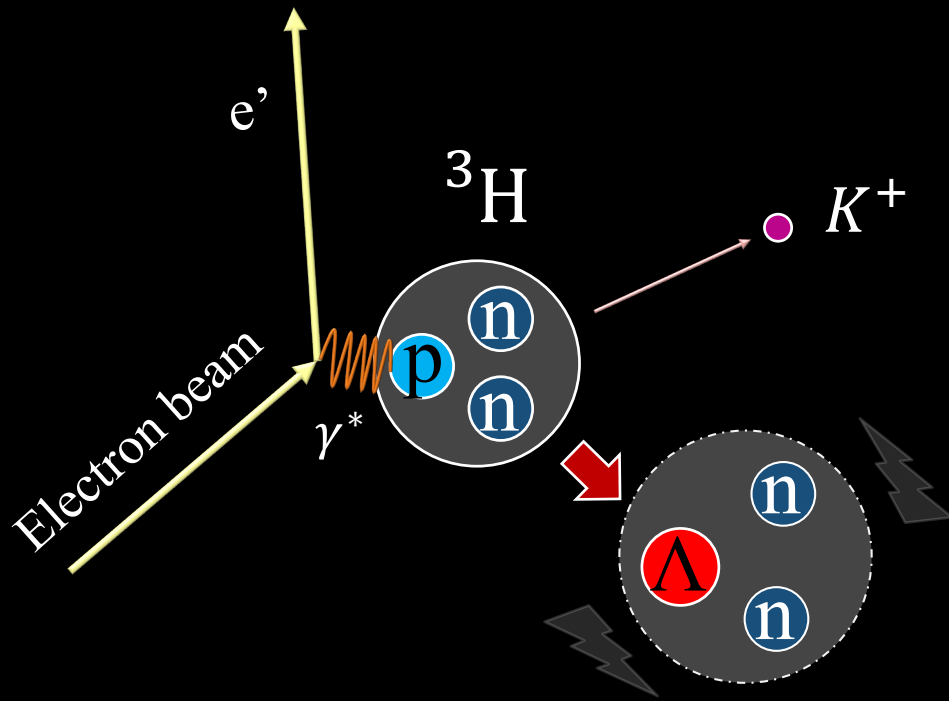


*nnΔ*

# nn $\Lambda$ search experiment at JLab

$^3\text{H}(e, e'K^+)nn\Lambda$  with HRSs

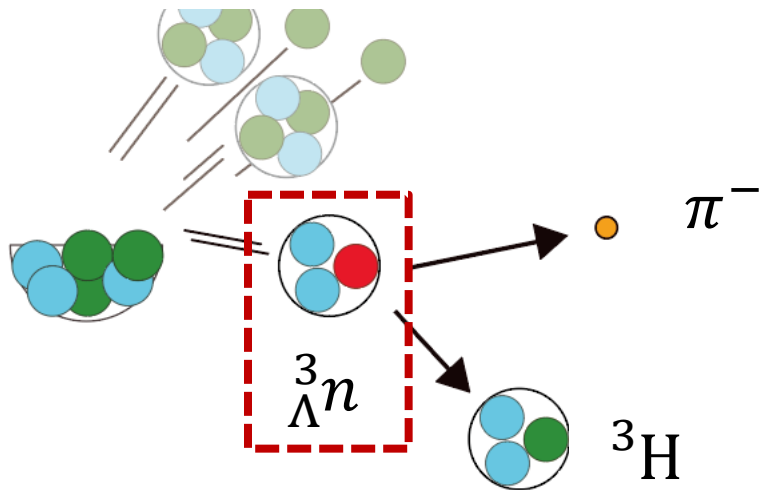
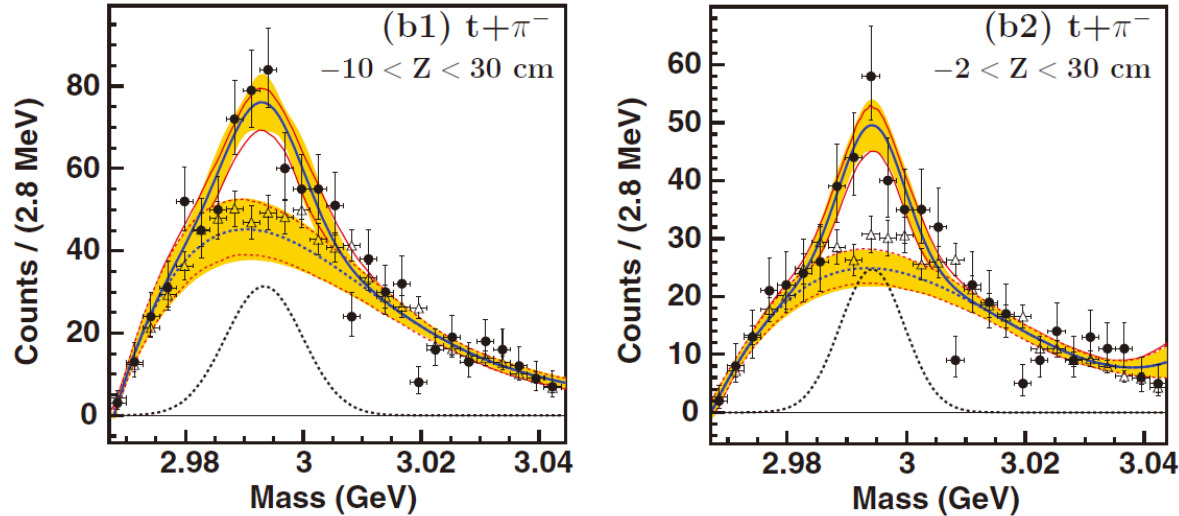
E12-17-003 (Oct 30—Nov 25, 2018)



We have sensitivity to both bound and resonant states

# $nn\Lambda$ ( $T=1$ )

C. Rappold et al. (HypHI Collaboration),  
Phys. Rev. C 88, 041001(R) (2013).



Dr. T.R. Saito presented last week

Bound state is hard to reproduce by  
current theoretical models

Theories support a resonant state of  $nn\Lambda$ :

- A. Gal et al., PLB 736, 93—97 (2014)
- I.R. Afnan et al. PRC92, 054608 (2015).
- E.Hiyama et al., PRC 89, 061302(R) (2014)
- H. Kamada et al., EPJ Web Conf. 113, 07004 (2016)
- M.Schäfer et al., PLB 88, 135614 (2020)



# STUDENTS WHO ANALYZE DATA

Independent analyses are in progress by students to doublecheck (triplecheck) results



K. Itabashi



K. Okuyama



E. Umezaki



K.N. Suzuki



B. Pandey



東北大学

Tohoku Univ., Japan



Kyoto Univ., Japan



Hampton Univ., US

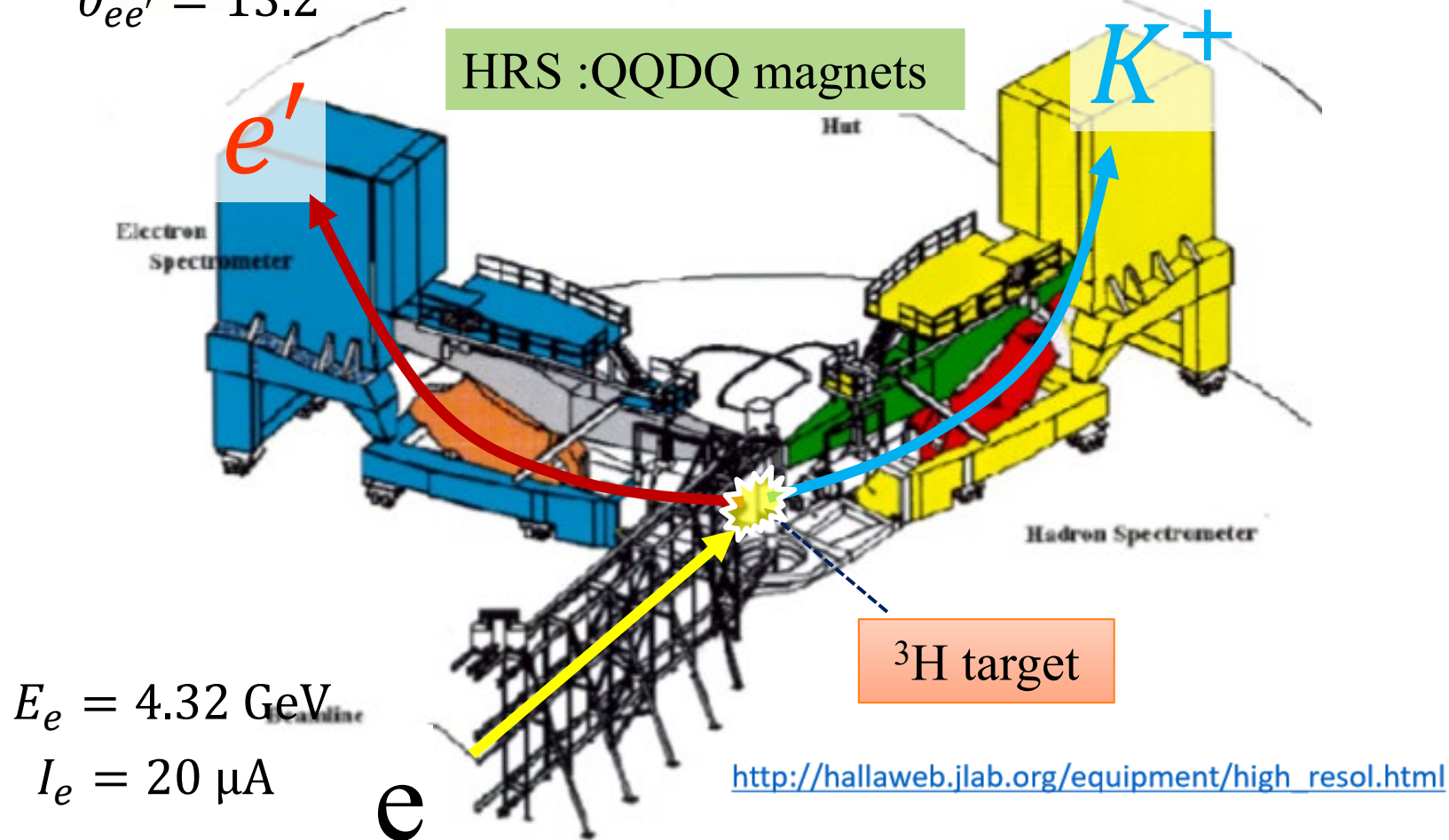
# EXPERIMENTAL SETUP (JLAB E12-17-003)

$$p_{e'} = 2.22 \text{ GeV}/c \pm 4.5\%$$

$$\theta_{ee'} = 13.2^\circ$$

$$p_K = 1.82 \text{ GeV}/c \pm 4.5\%$$

$$\theta_{eK} = 13.2^\circ$$



$$E_e = 4.32 \text{ GeV}$$

$$I_e = 20 \mu\text{A}$$

- High resolution
  - $\frac{\Delta p}{p} = 2 \times 10^{-4}$
- Long path length
  - $R_K \approx 17\%$   
(c.f.  $R_K \approx 30\%$  at  $p = 1.2 \text{ GeV}/c$  by HKS)



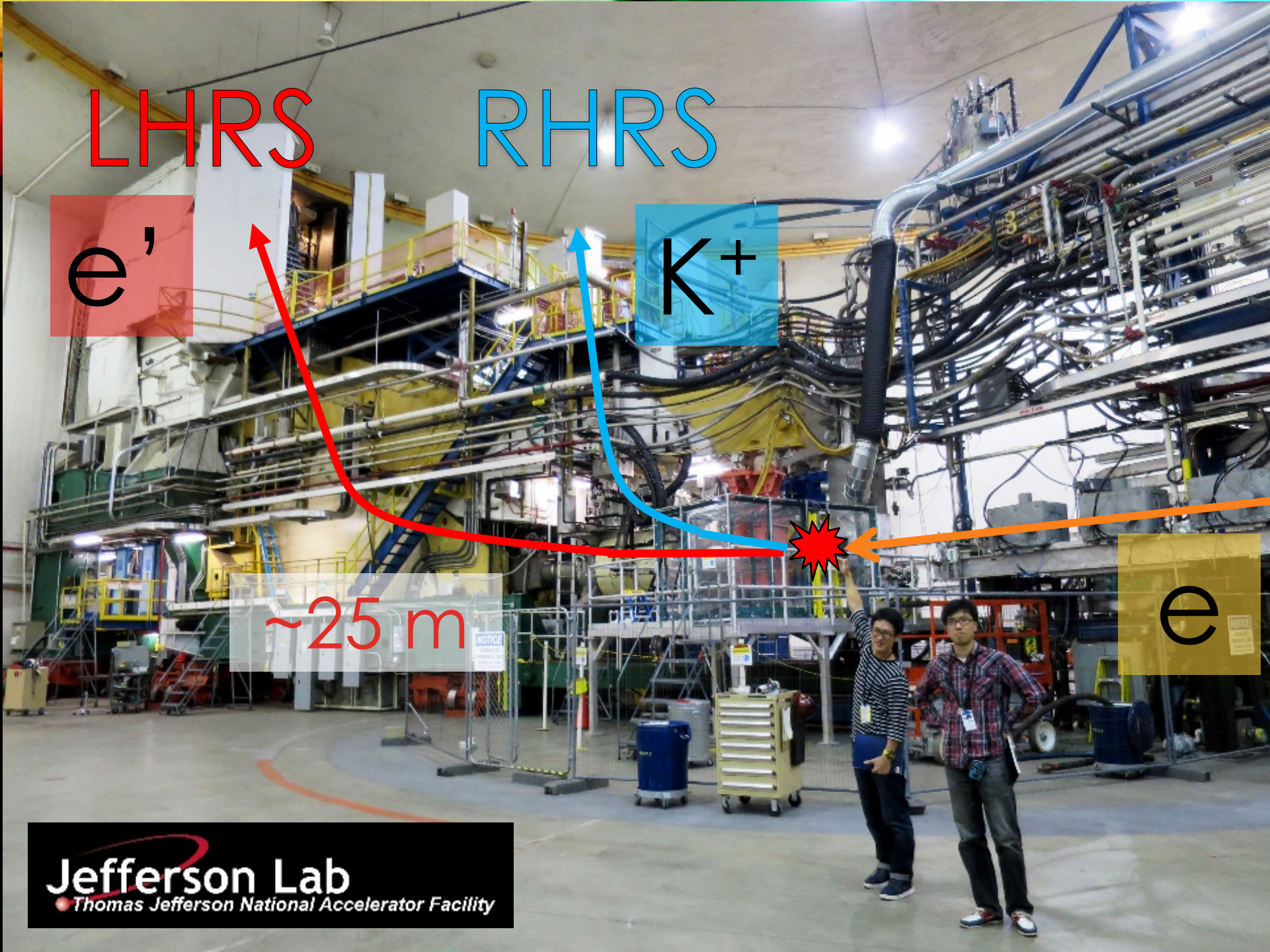
LHRS RHRS

$e'$

$K^+$

$e$

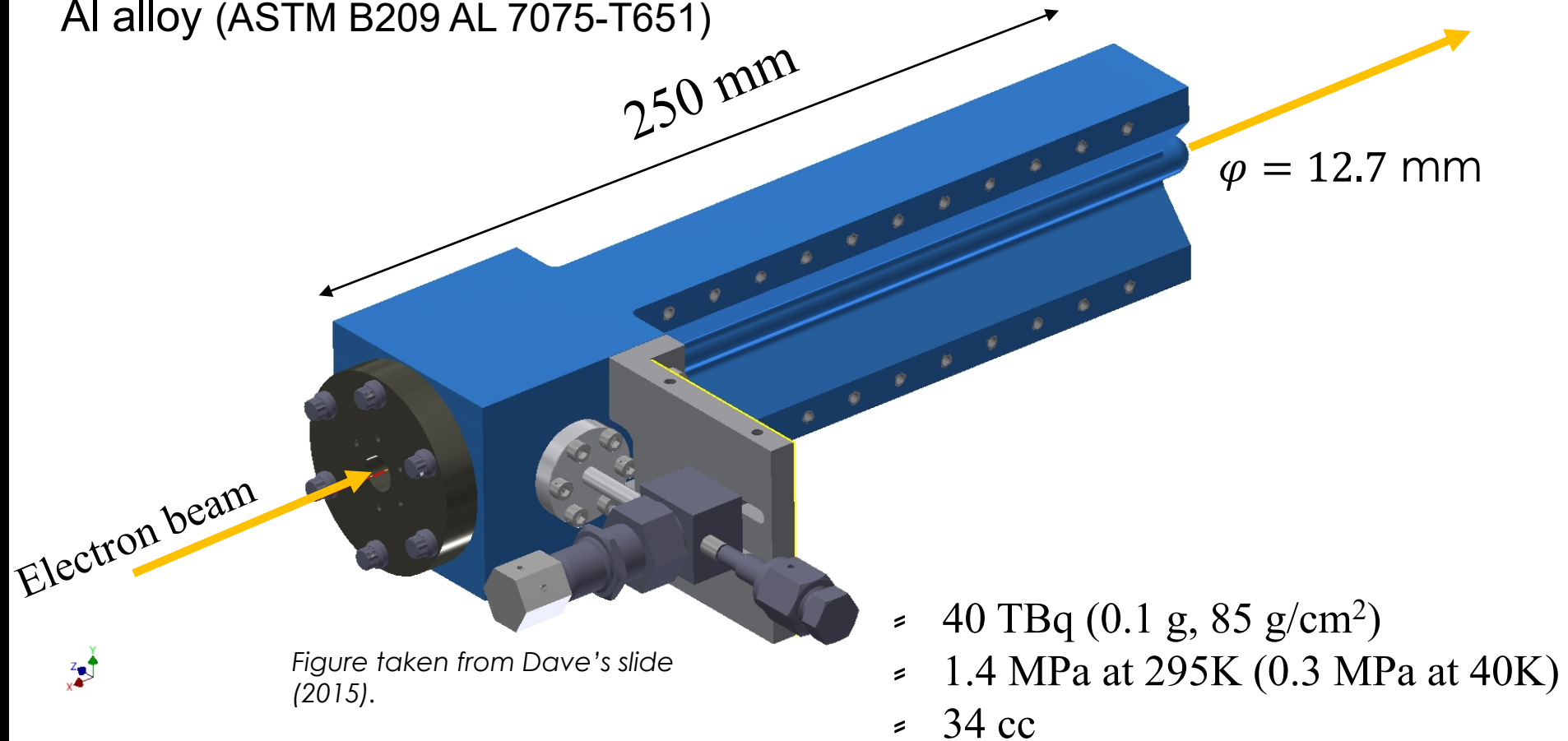
$\sim 25\text{ m}$



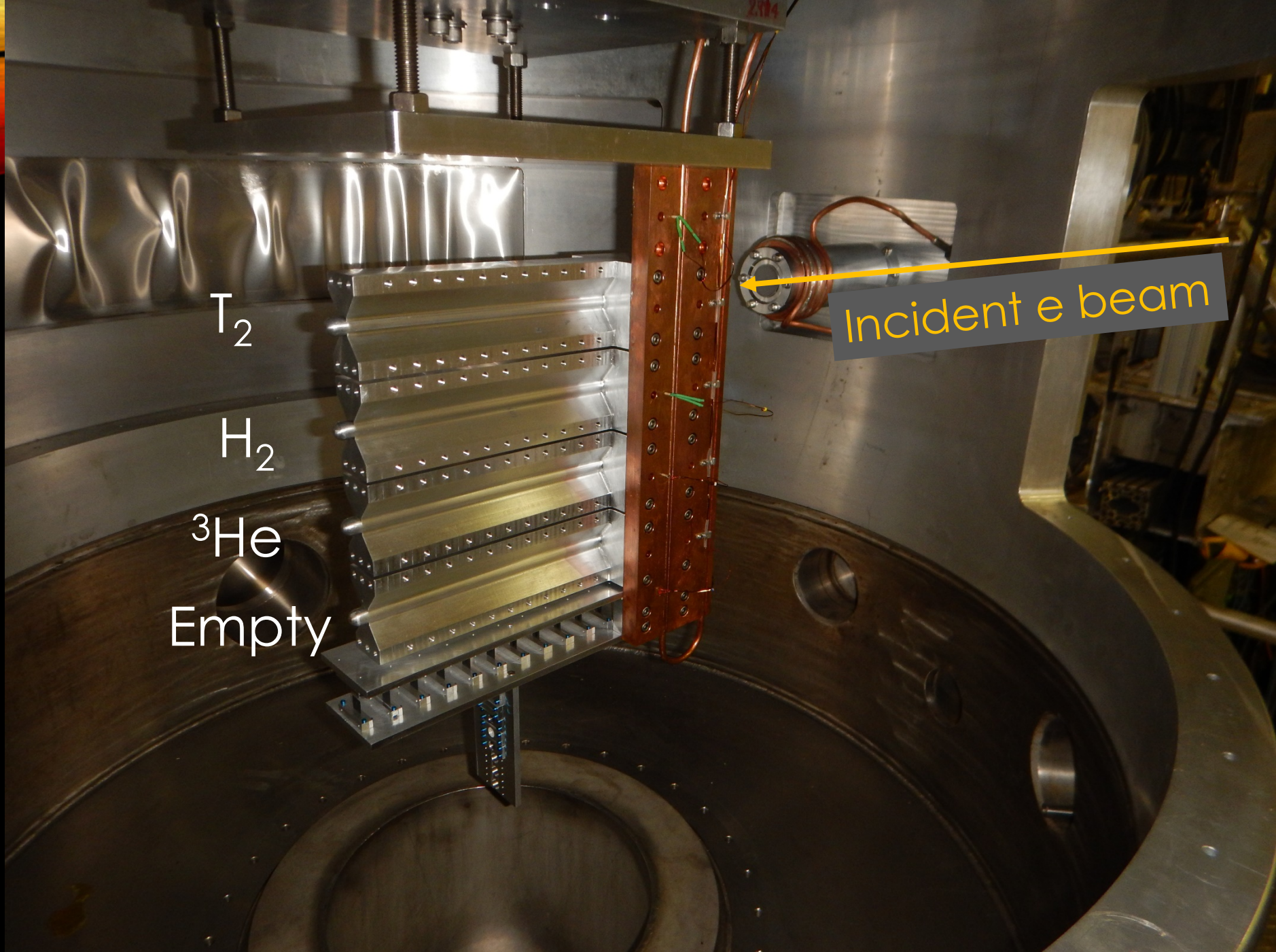


# TARGET CELL OF TRITIUM GAS

Cell material:  
Al alloy (ASTM B209 AL 7075-T651)







$T_2$

$H_2$

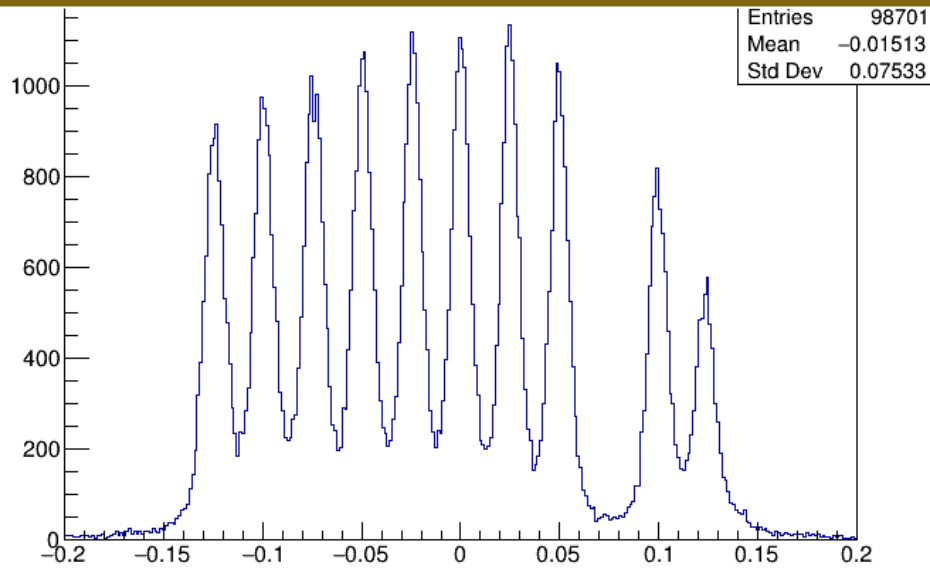
${}^3\text{He}$

Empty

Incident e beam



# Particle vertex z (Left HRS)

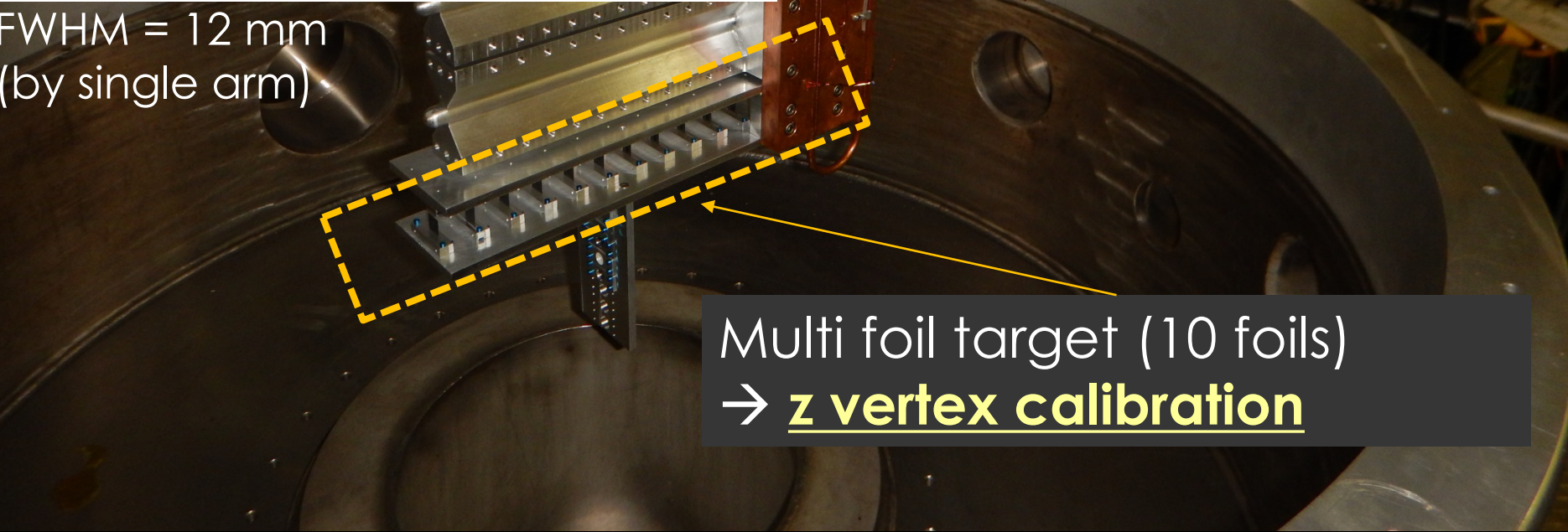


vertex z (m)

FWHM = 12 mm  
(by single arm)

$$Z_T^{L,R} = \begin{pmatrix} p_1^z & p_2^z & p_3^z & p_4^z & \dots \end{pmatrix} \begin{pmatrix} x_{RP} \\ x'_{RP} \\ y_{RP} \\ y'_{RP} \\ x_{RP}^2 \\ \dots \end{pmatrix}$$

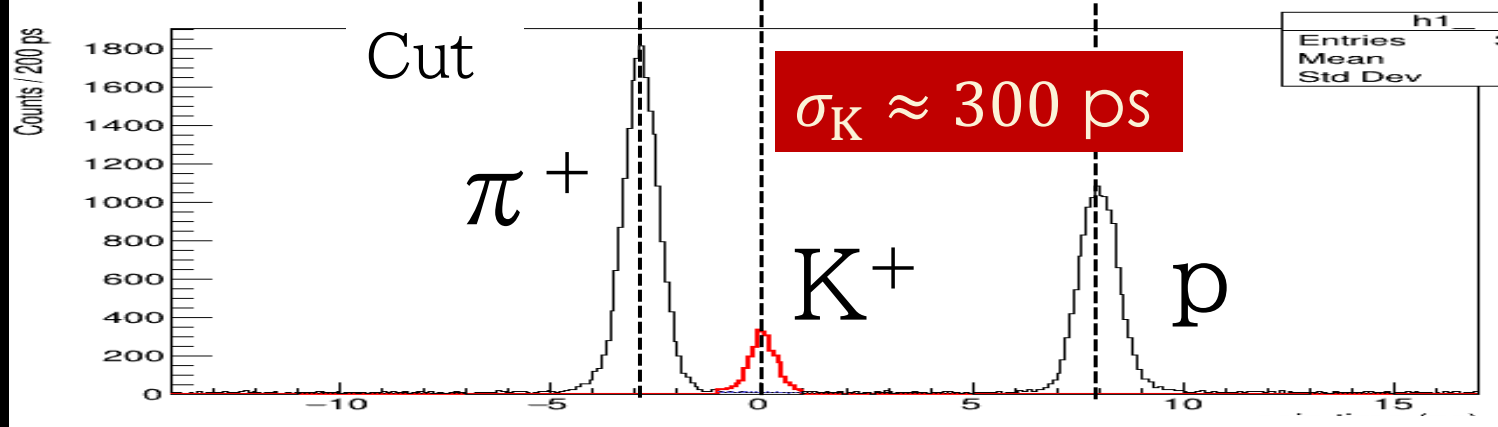
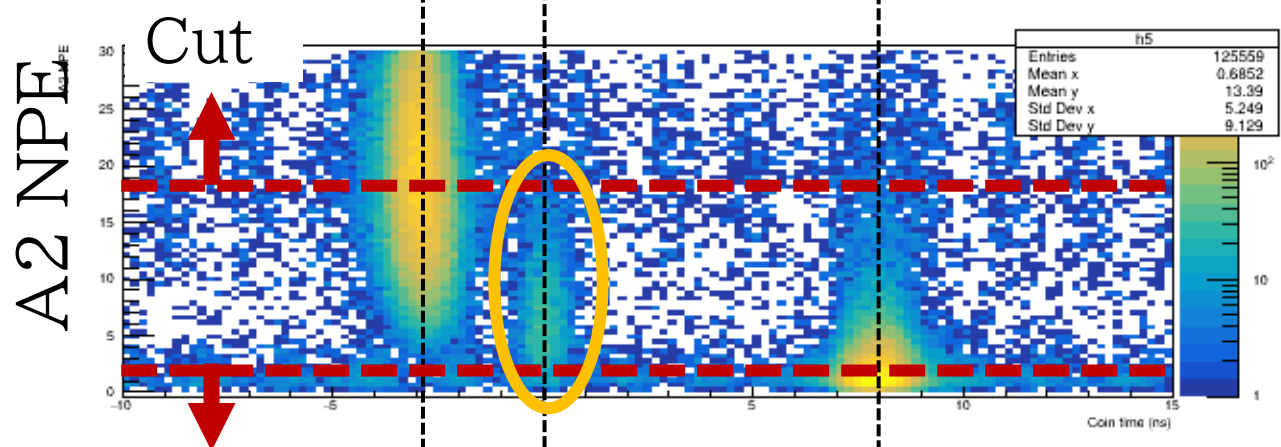
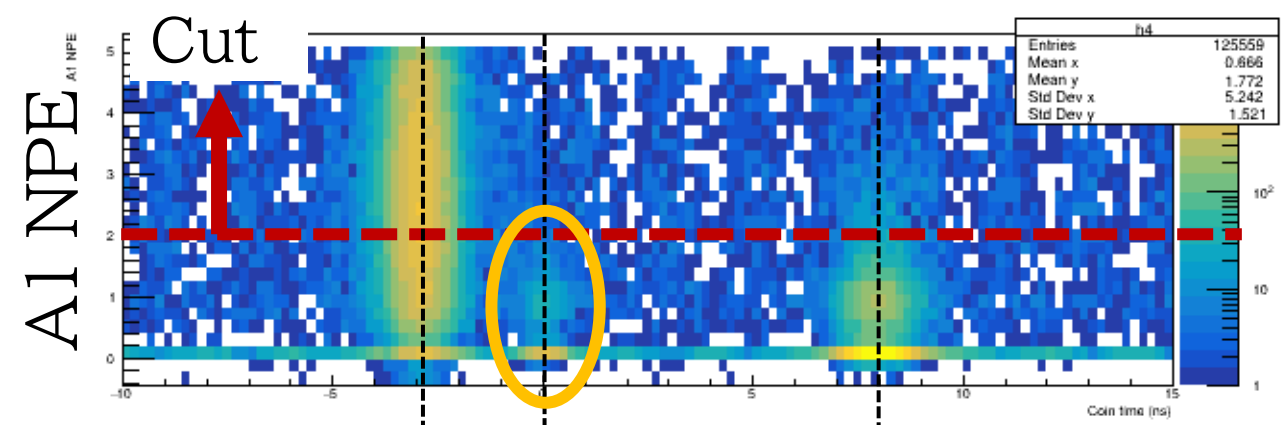
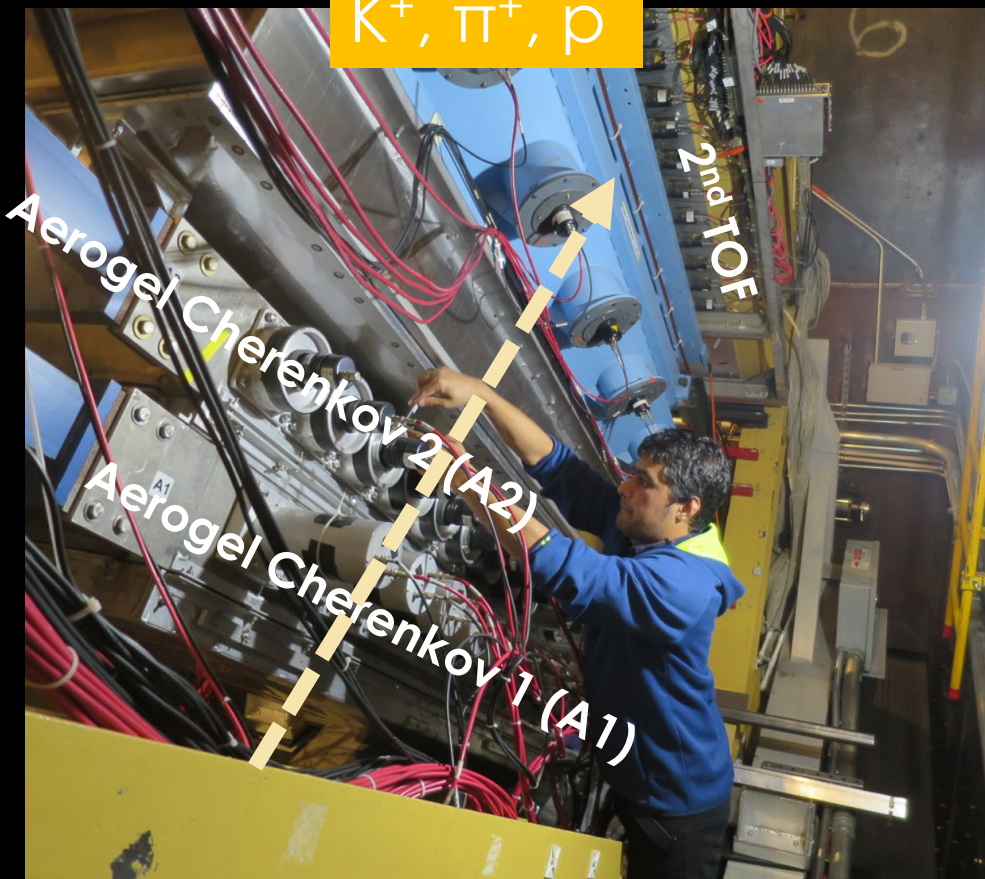
3<sup>rd</sup> order:  
35 parameters



Multi foil target (10 foils)  
→ z vertex calibration

# KAON IDENTIFICATION

$K^+$ ,  $\pi^+$ , p



Timing consistency between L and R assuming  $m_K$  → Coin time (ns)



# CALIBRATION

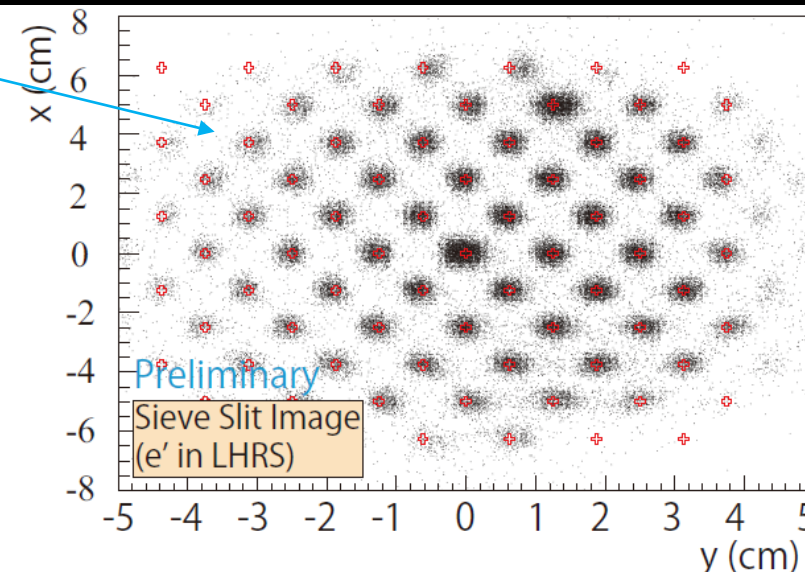
5<sup>th</sup> order matrix ( $z_t < 2$ )

Angle calibration

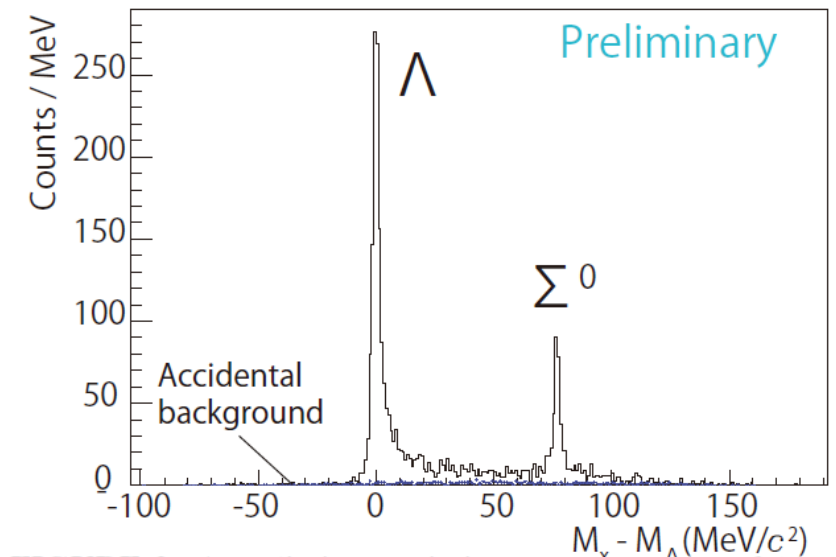
5<sup>th</sup> order matrix ( $z_t < 2$ )

Momentum calibration

Sieve Slit



**FIGURE 1.** A reconstructed particle image at the sieve slit for the sieve slit data in LHRS ( $e'$ ). Matrix parameters for reconstruction of angle at target were calibrated by using the sieve slit image.  $\pi^-$ s were eliminated by an event selection of light yield of a gas Cherenkov detector ( $\text{CO}_2$ ) [41] installed in LHRS.



**FIGURE 2.** A preliminary missing mass spectrum of  $\Lambda$  and  $\Sigma^0$  from a  $71\text{-mg}/\text{cm}^2$   $\text{H}_2$  gas target for a kinematics condition of M-Kine in JLab E12-17-003. The beam charge on the  $\text{H}_2$  target with M-Kine was about 2.5 C. The mass resolution is about  $3.5 \text{ MeV}/c^2$  (FWHM).



# Data vs. Geant4 (sim) for T<sub>2</sub> target

Momentum

$x_{FP}$  (cm)

$y_{FP}$  (cm)

$x'_{FP}$

$y'_{FP}$

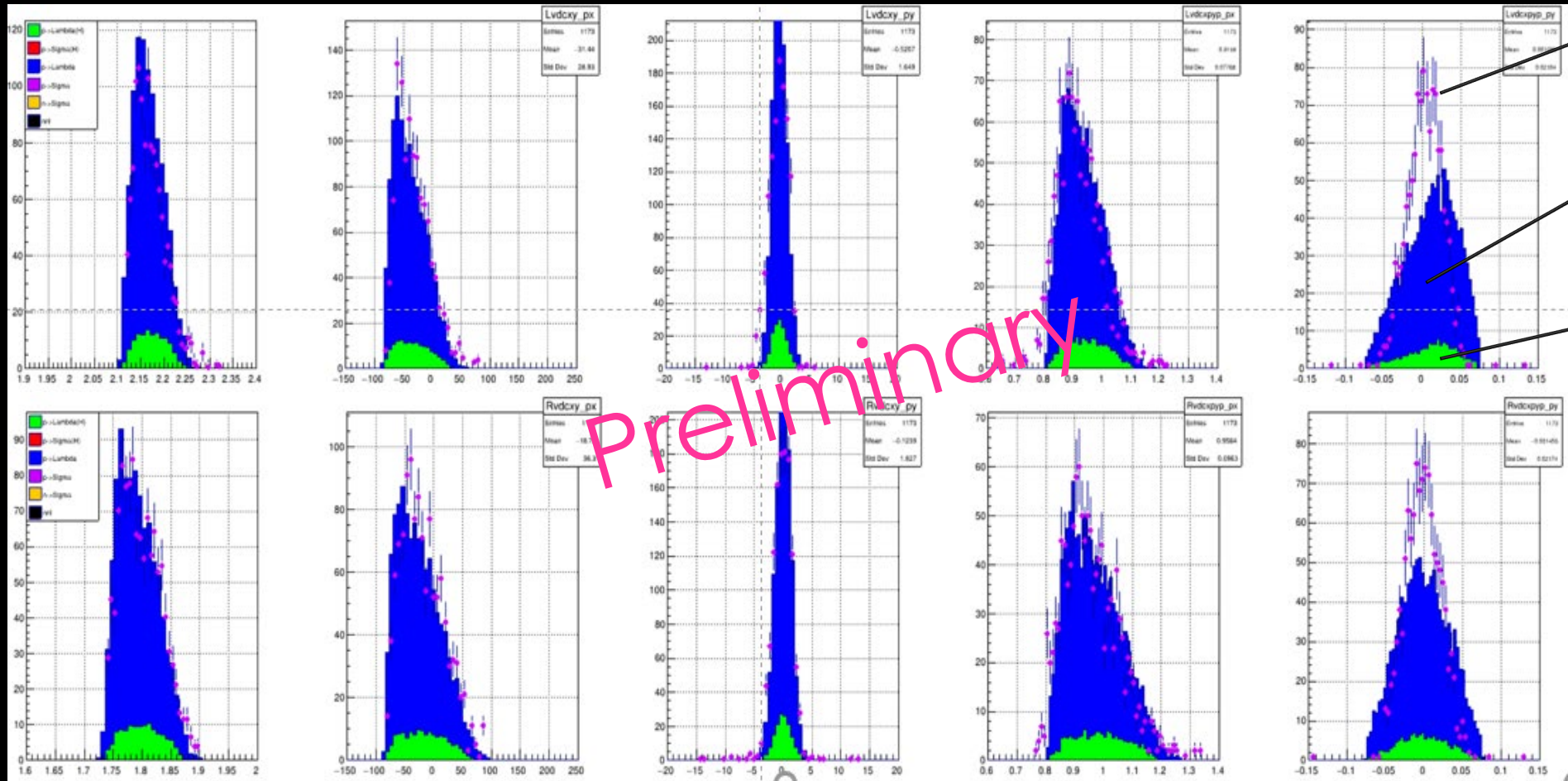
DATA ( $\Lambda$ ,  $\Sigma$ )

G4 SIM. (T2)

G4 SIM. (H)  
H contamination  
(~3%)

→ Acceptance  
evaluation  
→ Cross section

Preliminary



Simulation by K.N. Suzuki (Kyoto)

L-HRS  
(e')

R-HRS  
(K<sup>+</sup>)

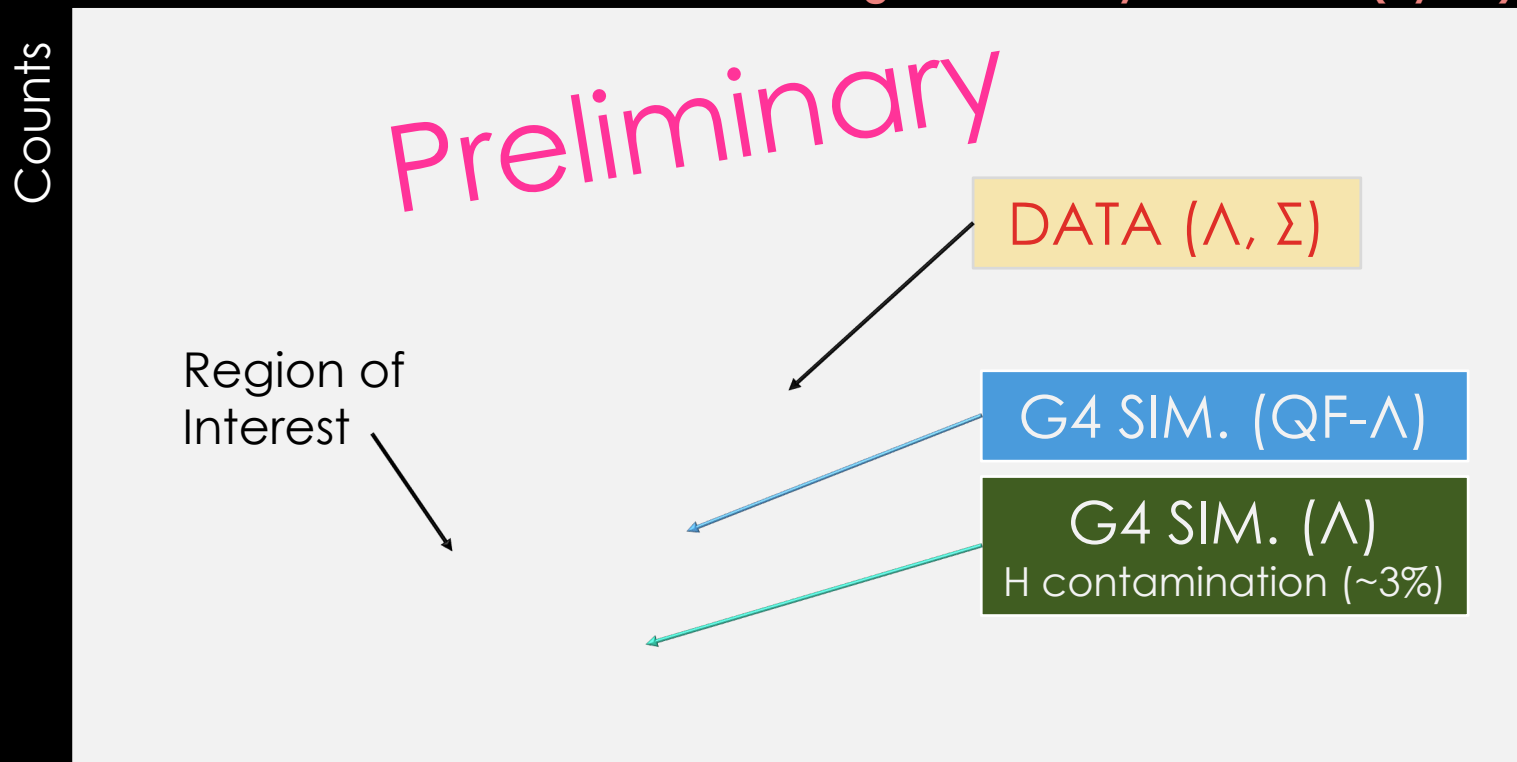
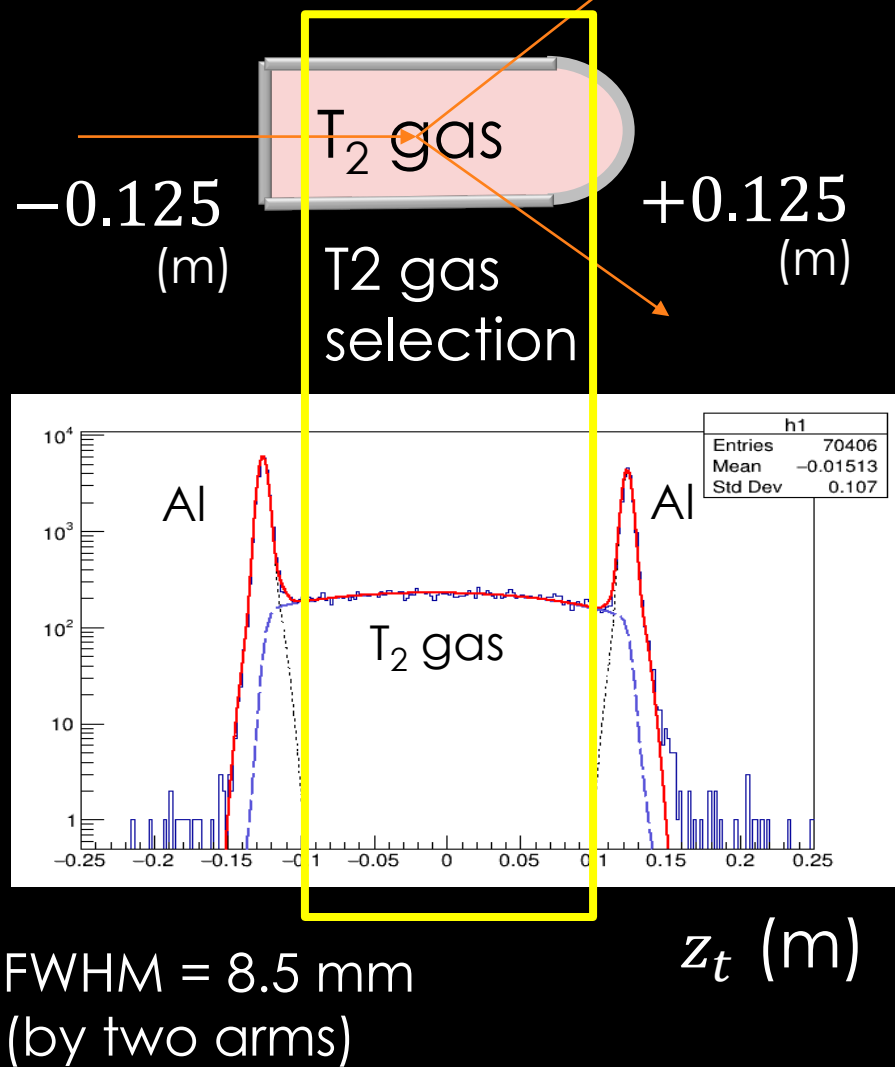
# PRELIMINARY EFFICIENCIES EVALUATED

Item	Efficiency / factor etc.	Remark
Tracing		Data + MC simulation
DAQ		Data
Aerogel Cherenkov selection		Data
Coincidence time selection		Data
Vertex z selection		Data
Acceptance		MC sim. (that reproduces data)
K survival ratio		MC sim. (that reproduces data)
K absorption factor		MC sim. (that reproduces data)
Gas density reduction @22.5 $\mu$ A		Data (NIMA 940 (2019)351—358 )
Virtual photon flux		MC sim. (that reproduces data)

Preliminary

# PRELIMINARY ${}^3\text{H}(e, e'K^+)nn\Lambda$

Figure made by K.N. Suzuki (Kyoto)



$$-B_{\Lambda} [= M_x - (M_{\Lambda} + 2M_n)] \text{ (MeV)}$$



${}_{\Lambda}^{3,4}\text{H}$



# HYPERTRITON ( ${}^3_{\Lambda}\text{H}$ ) PUZZLE

Small  $B_{\Lambda}$

vs.

Short Lifetime



$$\left\{ \begin{array}{l} B_{\Lambda} = 0.13 \pm 0.05 \text{ MeV (emulsion}^1) \\ B_{\Lambda} = 0.41 \pm 0.12 \pm 0.11 \text{ MeV (STAR}^2) \end{array} \right.$$

➔ RMS radius,  $\sqrt{\langle r^2 \rangle} \cong \frac{\hbar}{\sqrt{4\mu B_{\Lambda}}}$

$$\tau = (0.5 \sim 0.92) \tau_{\Lambda}$$

(HypHI, STAR, ALICE)

Fadееv calculation with realistic NN/YN interactions

$$\rightarrow \tau = 0.97 \tau_{\Lambda}$$

(H. Kamada *et al.*, *Phys. Rev. C* **57**, 4 (1998))

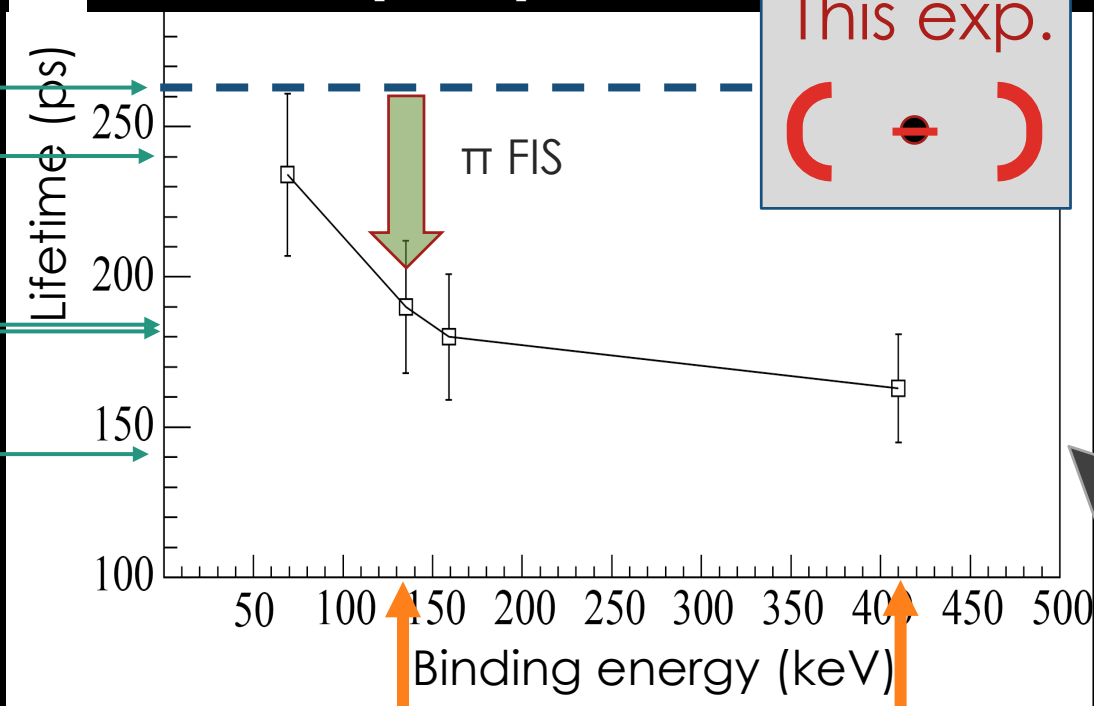
<sup>1</sup> M. Juric *et al.*, *Nucl. Phys. B* **52**, 1-30 (1973).

<sup>2</sup> The STAR Collaboration, *Nature Physics* (2020); <https://doi.org/10.1038/s41567-020-0799-7>

# LIFETIME VS. BINDING ENERGY OF ${}^3_{\Lambda}\text{H}$

arXiv:2006.16718v2 [nucl-th] 8 Jul 2020

Free  $\Lambda$   
ALICE 2  
HypHI  
ALICE 1  
STAR



**Emulsion**  
NPB52 (1973)1—30  
2BD:  $60 \pm 110$  keV  
3BD:  $230 \pm 110$  keV

**STAR**  
PRA982 (2019)811—814  
2BD:  $176 \pm 150$  keV  
3BD:  $586 \pm 160$  keV

ex.) Decay width of 2BD channel:

$$\frac{\Gamma_{\Lambda^3\text{H} \rightarrow {}^3\text{He} + \pi^-}}{(G_F m_\pi^2)^2} \approx \frac{q}{\pi} \frac{M_{^3\text{He}}}{M_{^3\text{He}} + \omega_{\pi^-}(q)} \times \left[ \mathcal{A}_\Lambda^2 + \frac{1}{9} \mathcal{B}_\Lambda^2 \left( \frac{k_{\pi^-}}{2M} \right)^2 \right] 3|F^{\text{PV}}(q)|^2$$

Spin indep. amp.

Form factor  
( $\pi$  FSI is included)

Spin dep. amp.

$$\propto \sqrt{B_\Lambda}$$

Proposed experiment (C12-19-002)

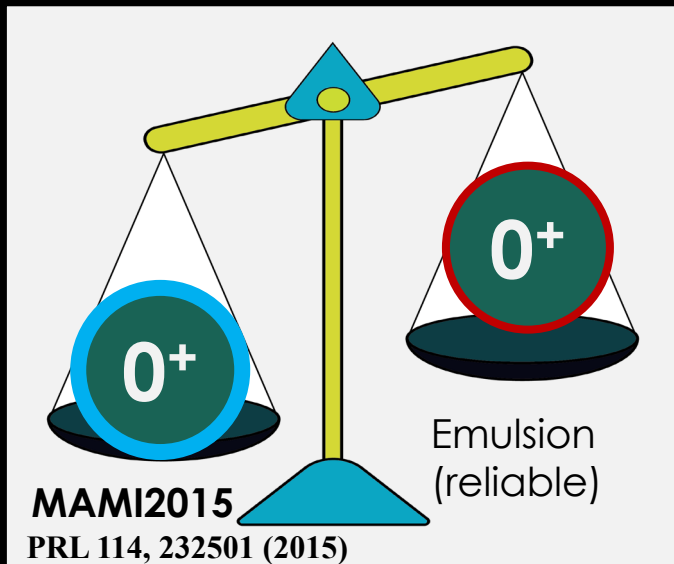
$|\Delta B^{\text{stat.}}| = 30$  keV,  $|\Delta B^{\text{sys.}}| = 70$  keV

**Best Accuracy on  $B_\Lambda({}^3_{\Lambda}\text{H})$**

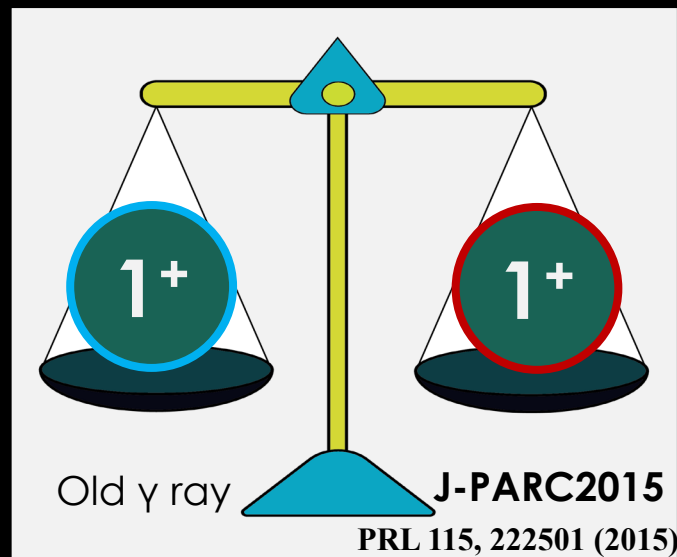
→ Pin down the hyperon puzzle

# CHARGE SYMMETRY BREAKING IN THE $\Lambda N$ INTERACTION

Unbalanced



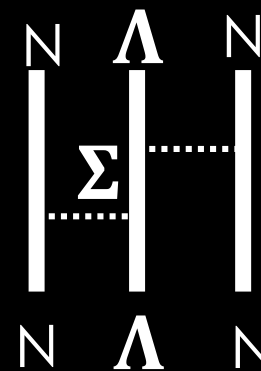
Balanced



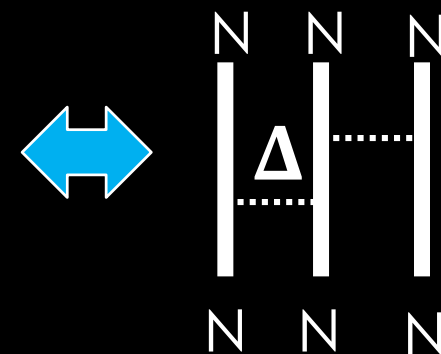
Mirror  
↔



$\Lambda N$ - $\Sigma N$  3BF<sup>(1)</sup>



Fujita-Miyazawa 3BF<sup>(2)</sup>



$\Sigma$  may admix in the  
 $\Lambda N/\Lambda NN$  interaction

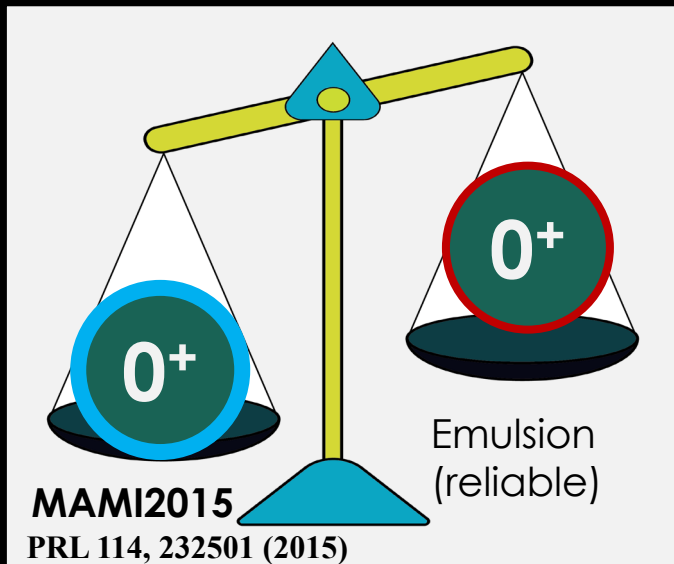
(1) Y. Akaishi et al., PRL 84, 3539 (2000)

(2) J. Fujita and H. Miyazawa,  
Prog. Theor. Phys., 17, 3, 360–365 (1957)

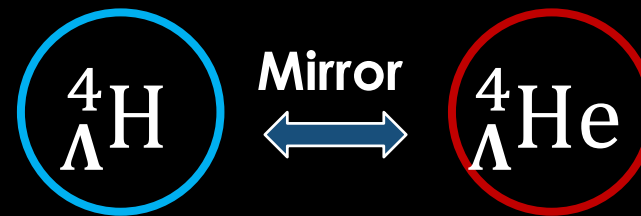
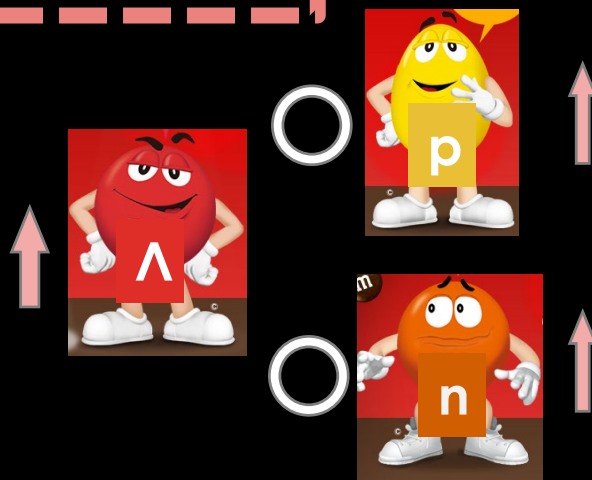
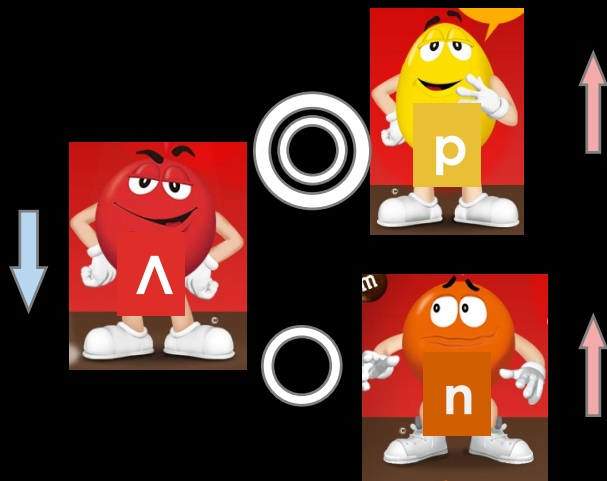
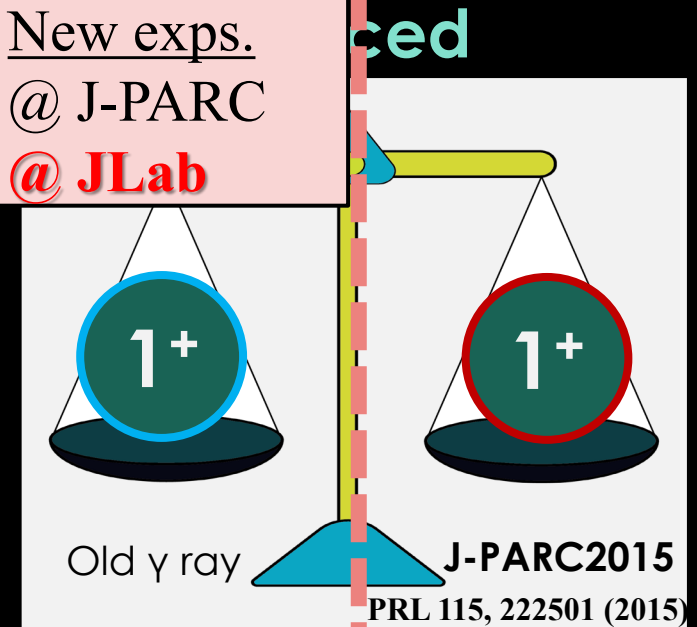


# CHARGE SYMMETRY BREAKING IN THE $\Lambda N$ INTERACTION

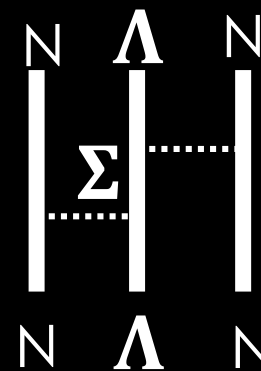
Unbalanced



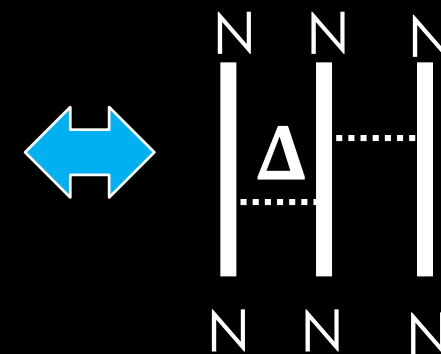
New exps.  
@ J-PARC  
@ JLab



$\Lambda N$ - $\Sigma N$  3BF<sup>(1)</sup>



Fujita-Miyazawa 3BF<sup>(2)</sup>



$\Sigma$  may admix in the  
 $\Lambda N/\Lambda NN$  interaction

(1) Y. Akaishi et al., PRL 84, 3539 (2000)

(2) J. Fujita and H. Miyazawa,  
Prog. Theor. Phys., 17, 3, 360-365 (1957)

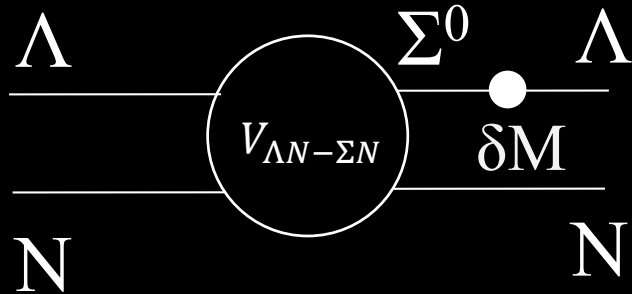
# BASIC INFORMATION FOR THE $\Lambda N$ CSB STUDY: ${}^4_{\Lambda}\text{He} - {}^4_{\Lambda}\text{H}$

## Explicit inclusion of $\Sigma$

A. Gal, Phys. Lett. B 744, 352 (2015)

D. Gazda and A. Gal, Phys. Rev. Lett. 116, 122501 (2016)

A. Gal et al., IOP Conf. Series: Jour. Phys.: Conf. Ser. 966 (2018) 012006



$$\langle N\Lambda | V_{CSB} | N\Lambda \rangle = -0.0297 \tau_{Nz} \frac{1}{\sqrt{3}} \langle N\Sigma | V_{CS} | N\Lambda \rangle$$

## Phenomenological potential

E. Hiyama et al., Phys. Rev. C 80, 054321 (2009).

M. Isaka et al., Phys. Rev. C 101, 024301 (2020).

$$V_{\Lambda N}^{\text{CSB}}(r) = -\frac{\tau_z}{2} \left[ \frac{1 + P_r}{2} \left( v_0^{\text{even,CSB}} + \sigma_{\Lambda} \cdot \sigma_N v_{\sigma_{\Lambda} \cdot \sigma_N}^{\text{even,CSB}} \right) e^{-\beta_{\text{even}} r^2} + \frac{1 - P_r}{2} \left( v_0^{\text{odd,CSB}} + \sigma_{\Lambda} \cdot \sigma_N v_{\sigma_{\Lambda} \cdot \sigma_N}^{\text{odd,CSB}} \right) e^{-\beta_{\text{odd}} r^2} \right]$$

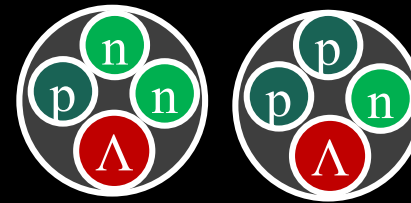
**Fundamental benchmark**



**CSB interaction**

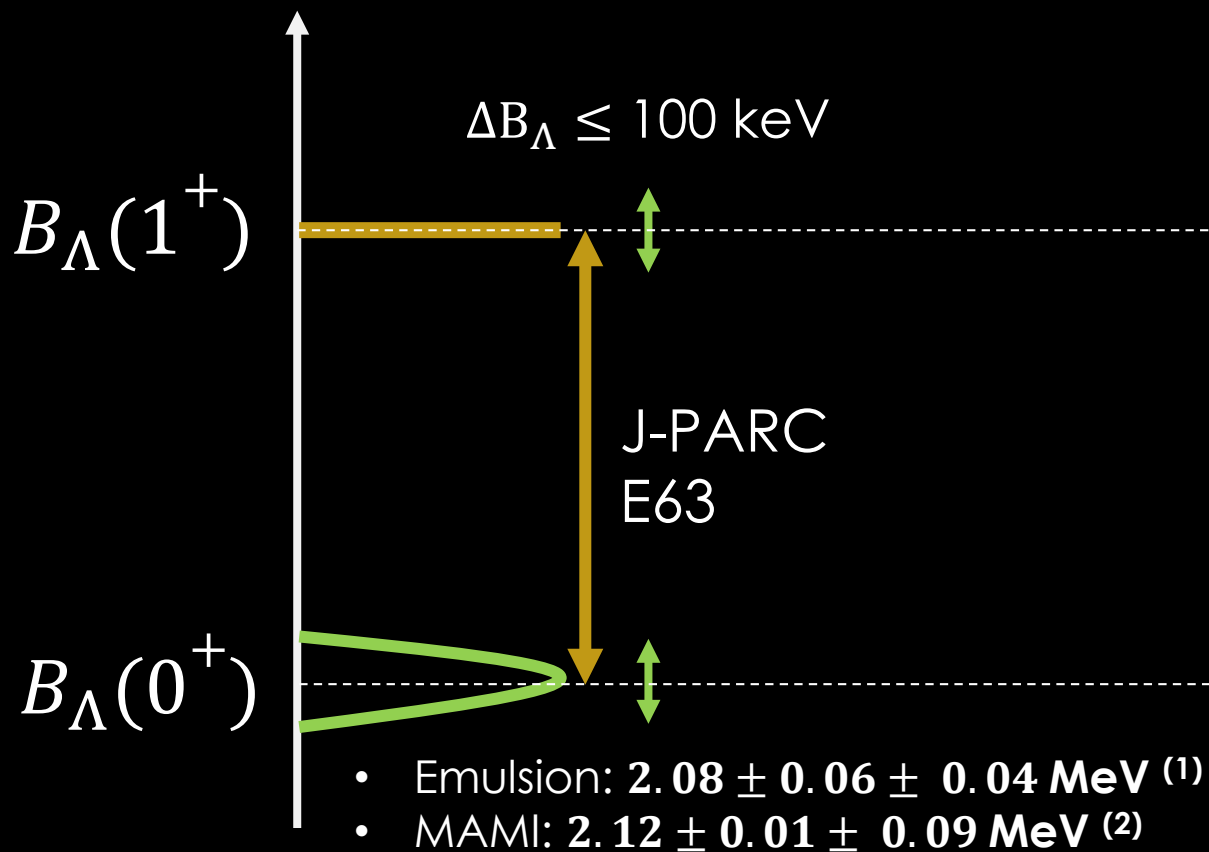
- $A=5$  HKS, PRL 110, 012502 (2013)
- $A=7$  HKS, PRC 94, 021302(R) (2016)
- $A=9$  Hall A, PRC 91, 034308 (2015)
- $A=10$  HKS, PRC 93, 034314 (2016)
- ... HKS, PRC 90, 034320 (2014) ...

# HOW WE CONFIRM THE $B_{\Lambda}({}_{\Lambda}^4\text{H}; 1^+)$



Conventional way

Proposed exp.



$\Delta B_{\Lambda} \leq 100 \text{ keV}$

This proposal  
(2 days)



Absolute Energy Measurement:

- Very unique (direct meas.)
- Complementary with other data

(1) NPB 52, 1-30 (1973)

(2) PRL 114, 232501 (2015)

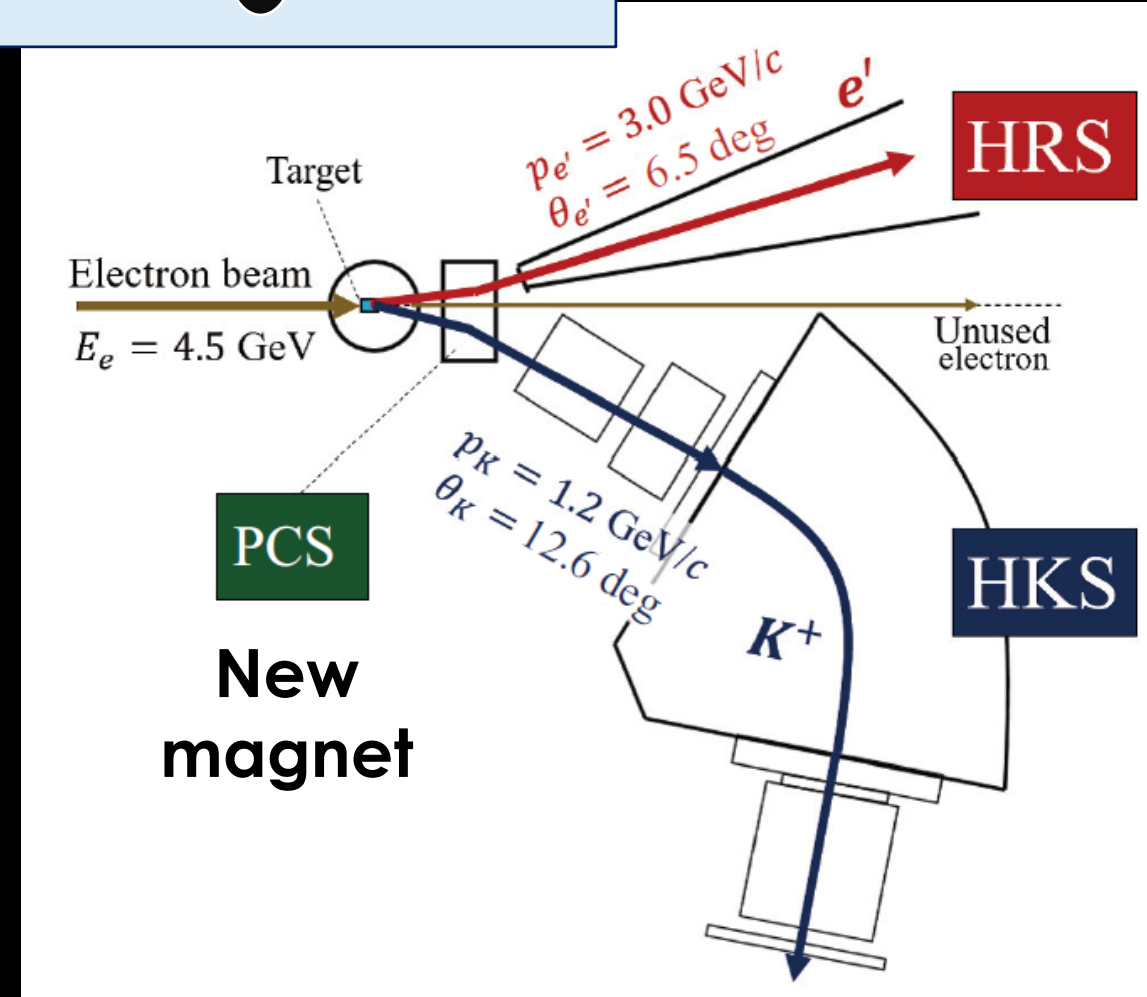
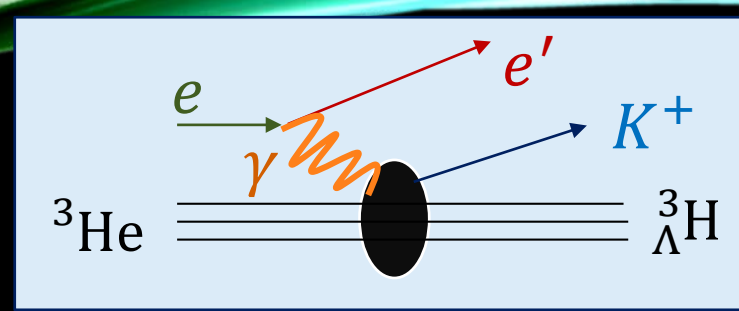


# EXPERIMENTAL SETUP

- Same as E12-15-008 ( ${}^{40,48}_{\Lambda}\text{K}$ )
- PCS  $\rightarrow$  constructed in Japan
- Proposed targets
  - Physics:  ${}^3\text{He}$ ,  ${}^4\text{He}$  gases
  - Calibration:  ${}^1\text{H}$  gas, Multi-C, Empty
- Target ladder may be separated from others

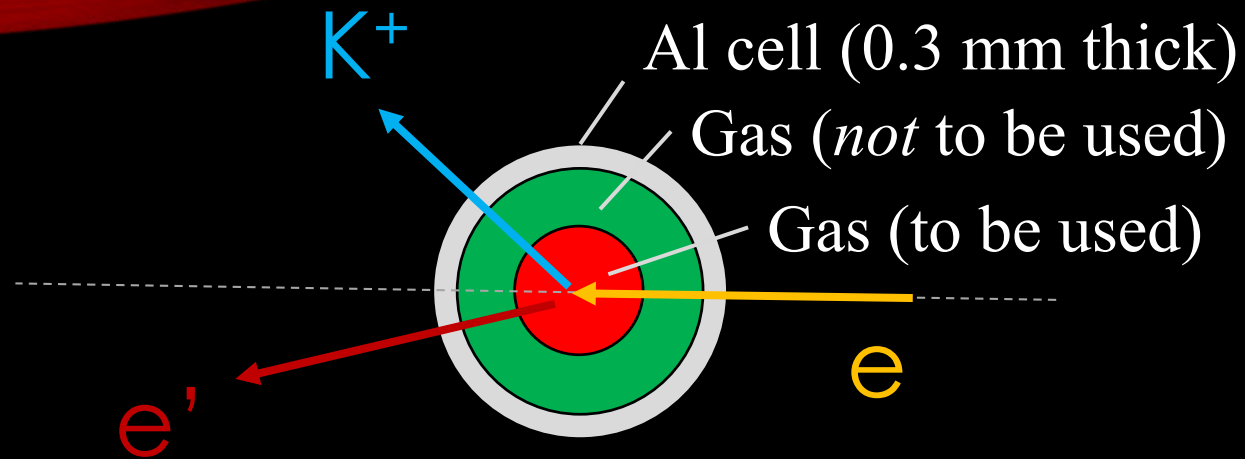


PCS @ TOKIN, Sendai, Japan (March 2020)



HKS magnet: Y. Fujii et al., NIMA 795 (2015) 351—363  
Kaon ID: TG et al., NIMA 729 (2013) 816—824

# TARGET

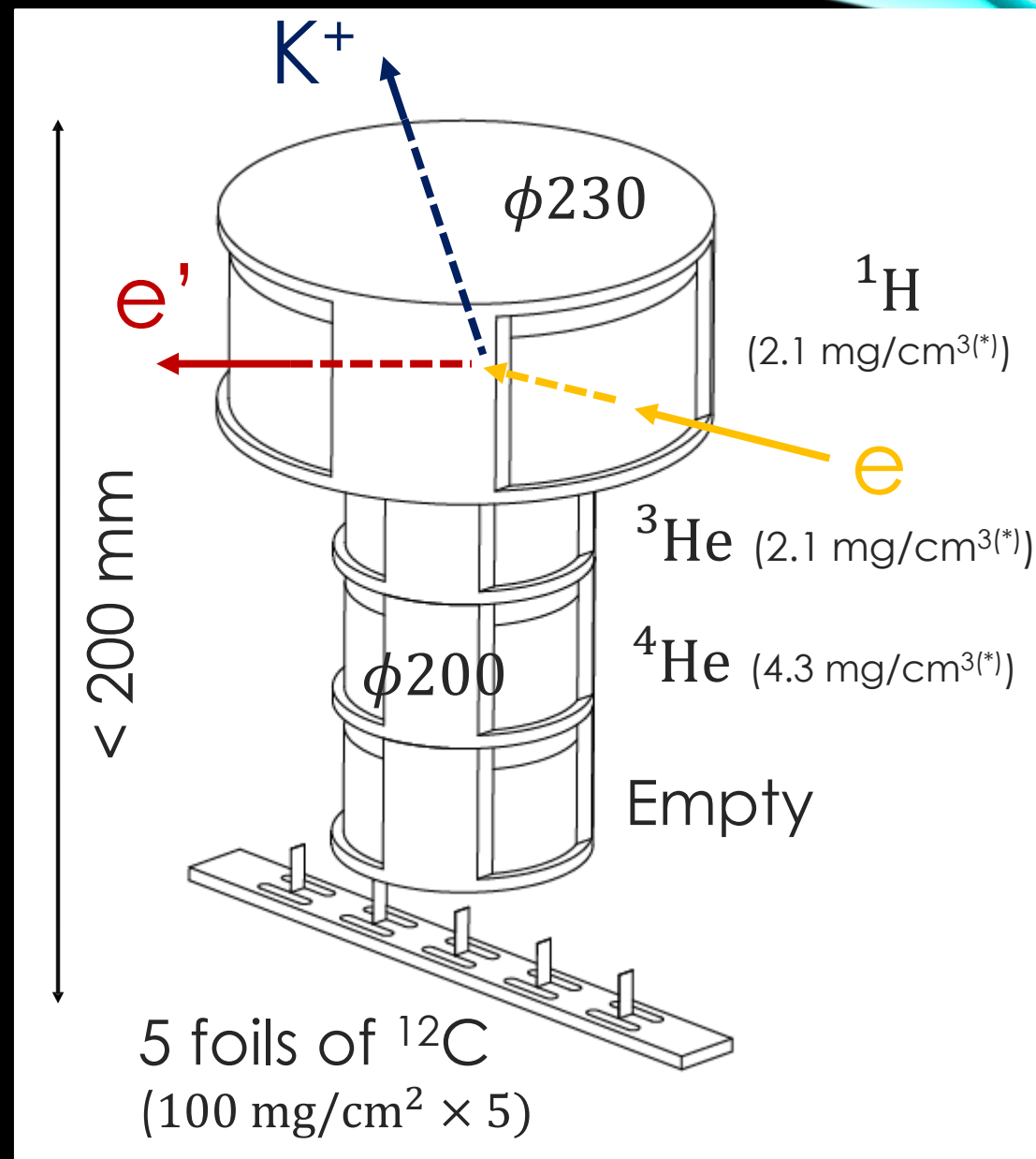


## To minimize systematic error on $B_{\Delta}$

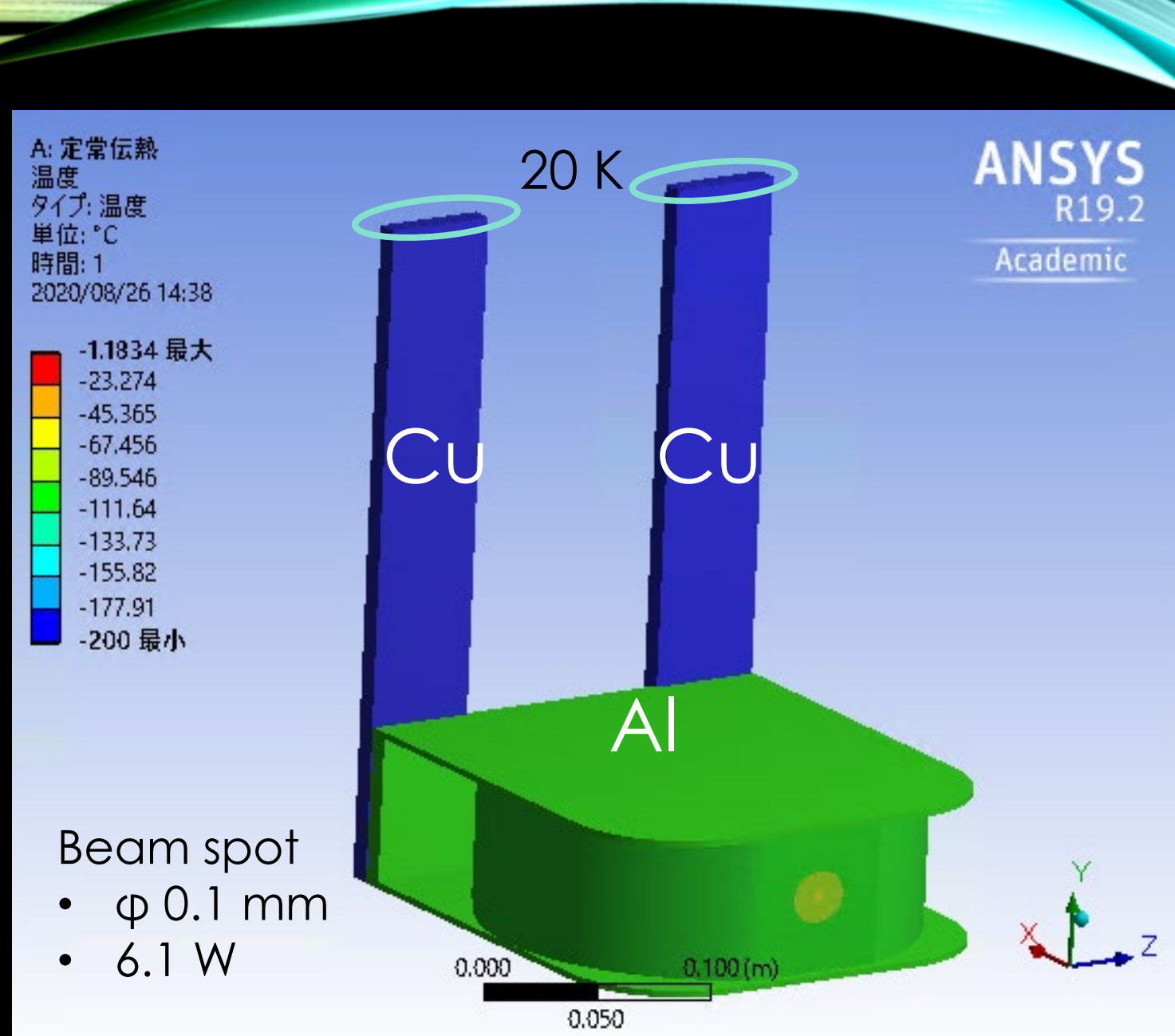
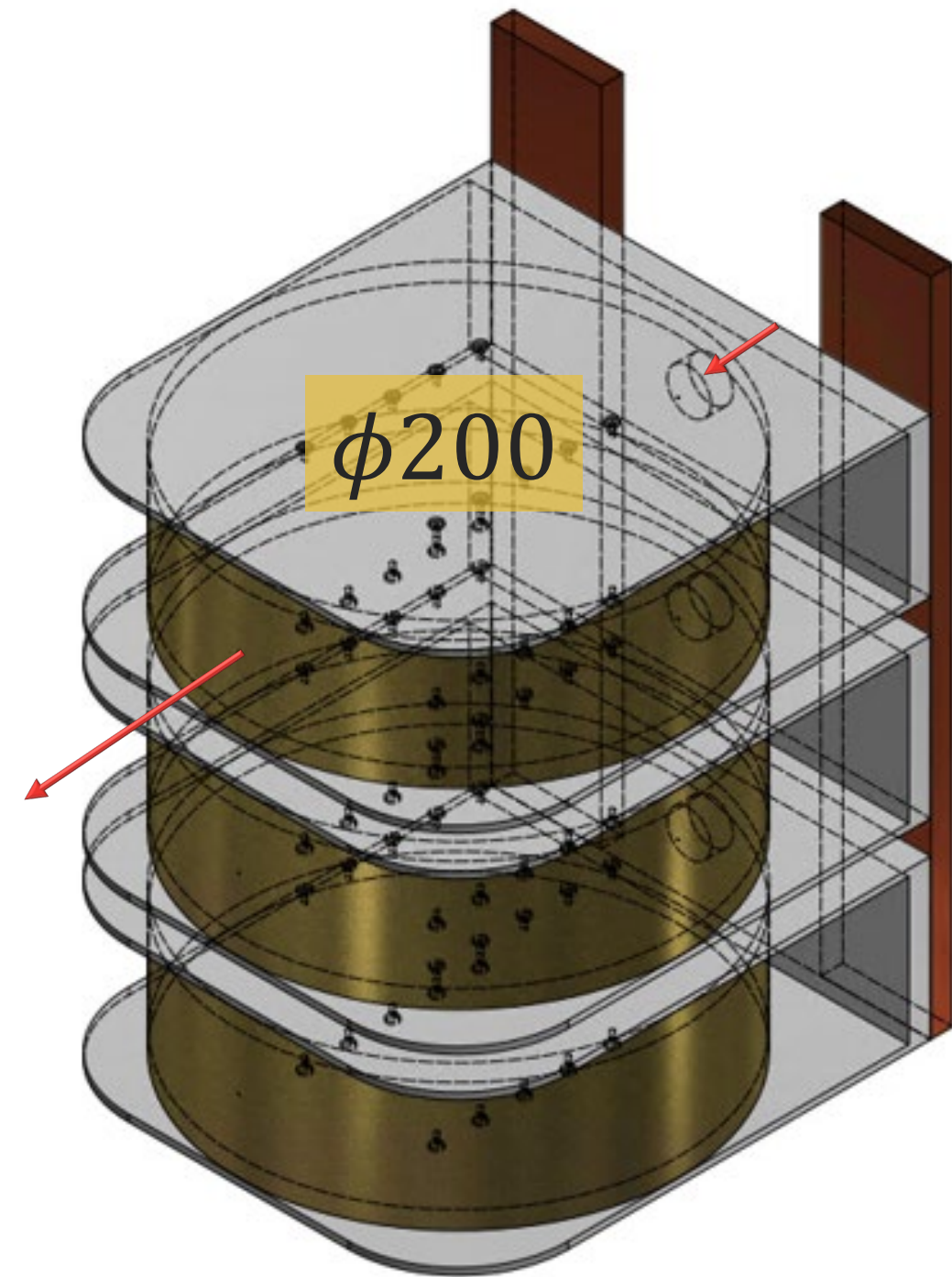
- Tuna-can type of cell
- Path length in Al cell wall  $\ni$   
(Multiple scattering effect  $\ni$ ;  $\frac{x}{X_0} \simeq 3.4 \times 10^{-3}$ )

## To achieve better S/N

- Center part will be used for analysis  
( $\Delta z_t = 15$  mm FWHM is expected)

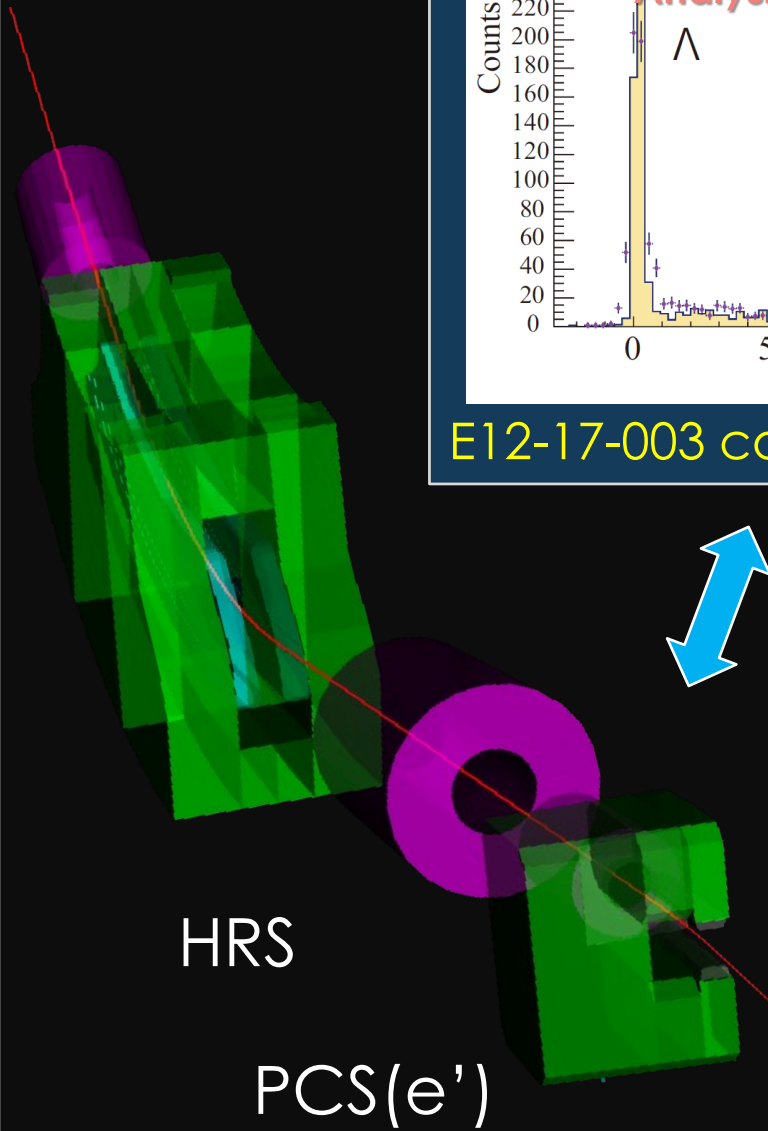
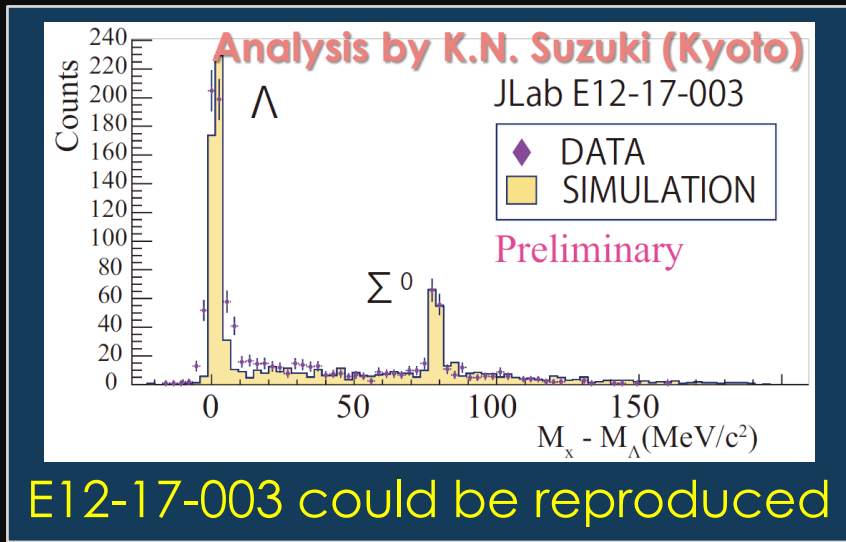


(\*) S.N. Santiesteban et al., NIMA 940 (2019)351—358





# EXPECTED MISSING MASS RESOLUTION



Same framework

Geant4 simulation for C12-19-002

$$Z_{T,HRS} = \sum_{i+j+k+l=0}^{n_1} a_{ijklm} x_{FP}^i x'_{FP}{}^j y_{FP}^k y'_{FP}{}^l$$

$$\overrightarrow{p}^{HRS,HKS} = \sum_{i+j+k+l+m=0}^{n_2} a_{ijklm} x_{FP}^i x'_{FP}{}^j y_{FP}^k y'_{FP}{}^l Z_{T,HRS}^m$$

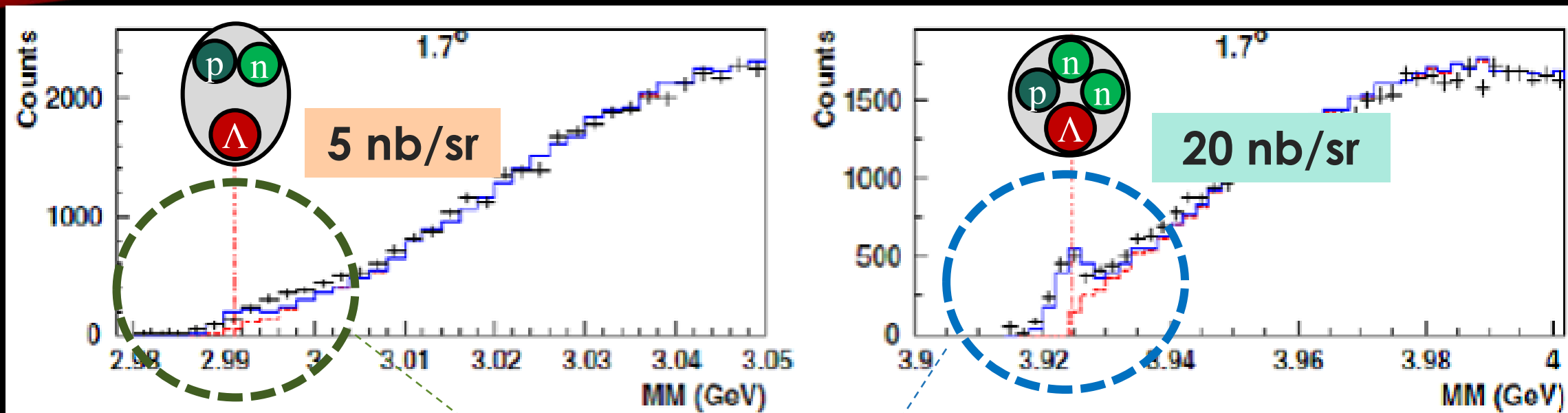
	$\Delta p/p$	$\Delta\theta$ (mrad)
HRS	$2.6 \times 10^{-4}$	0.6
HKS	$4.2 \times 10^{-4}$	1.5

w/ materials (e.g. target):  
 $\frac{\Delta p}{p} \Rightarrow \frac{\Delta p}{p} \times 1.1, \Delta\theta \Rightarrow \Delta\theta \times 1.4$

**$\Delta M_{HYP} = 1 \text{ MeV (FWHM)}$**

# YIELD ESTIMATION

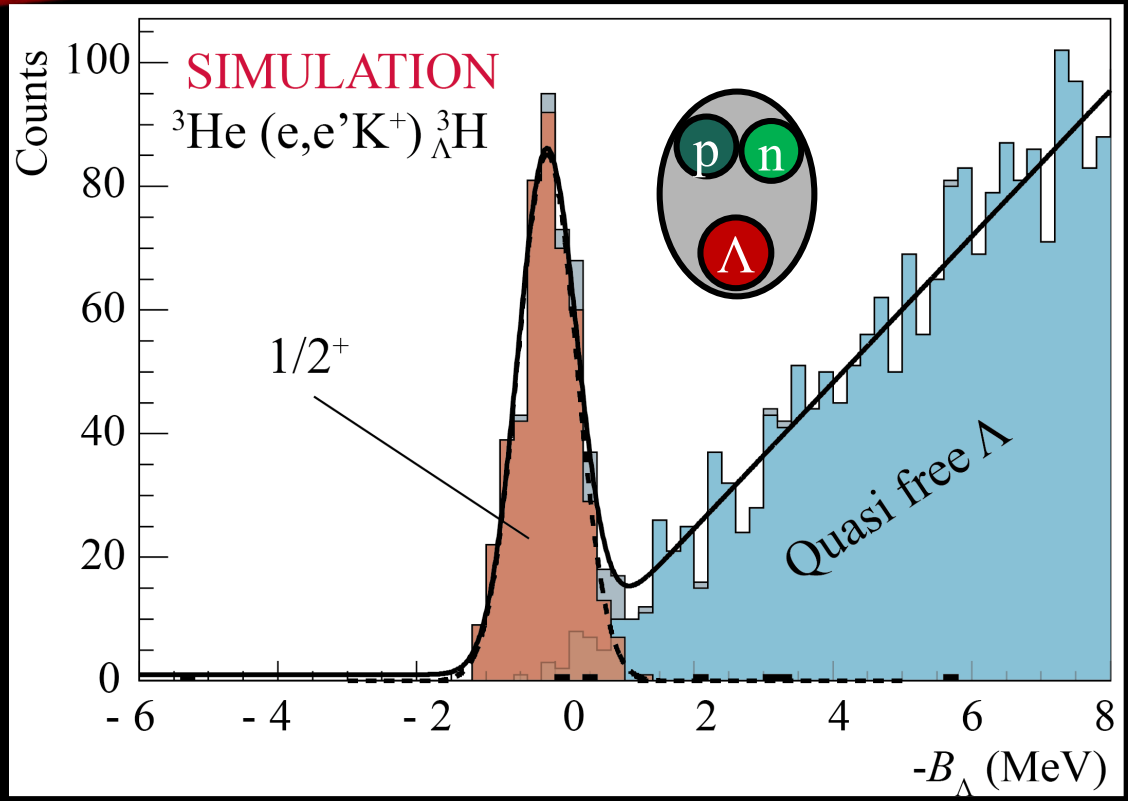
F. Dohrmann et al., *Phys. Rev. Lett.* **93**, 242501 (2004).



Product	Target (mg/cm <sup>2</sup> )	$I_{beam}$ ( $\mu A$ )	CS (nb/sr)	Yield / day	Beamtime (day)	Total yield
${}^3_{\Lambda}H$	${}^3He$ (37)	50	5	23	20	<b>464</b>
${}^4_{\Lambda}H$	${}^4He$ (74)		20	139	2	<b>278</b>

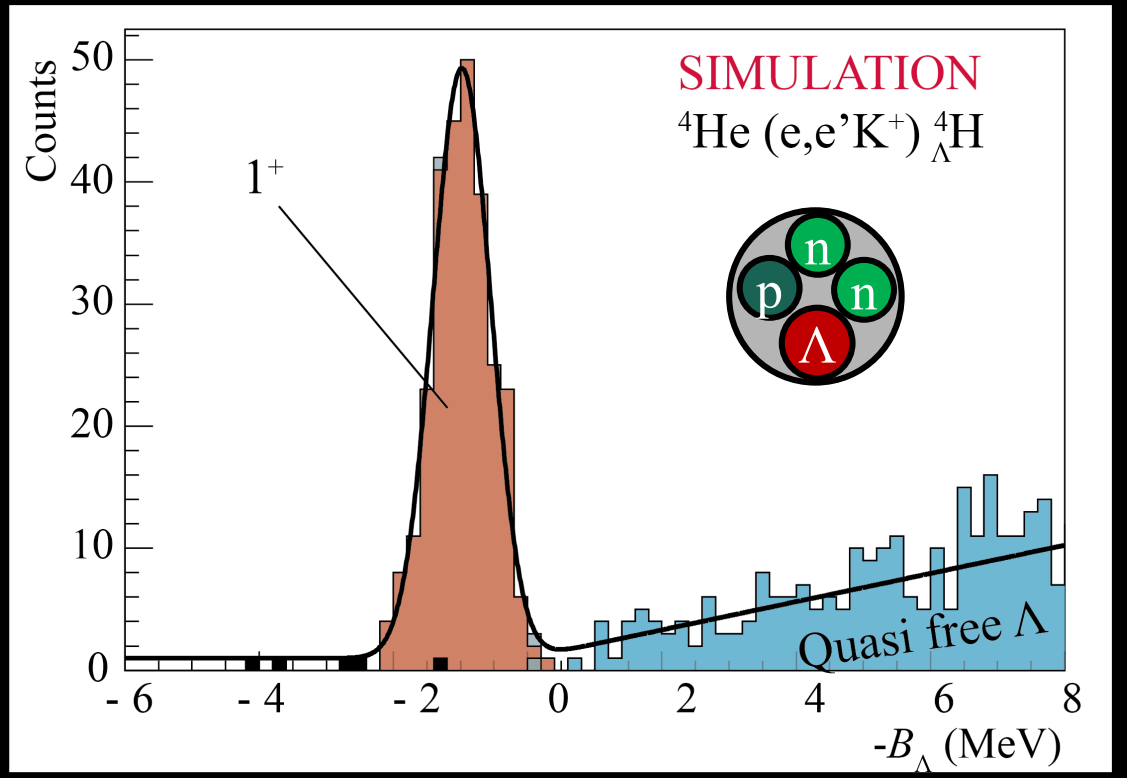
$$VP \text{ flux} = 2 \times 10^{-5} (/e), \epsilon_{det} = 0.75, f_{density} = 0.85, f_{Kdecay} = 0.26, \Omega_K = 7 \text{ msr}$$

# EXPECTED SPECTRA AND STATISTICAL ERRORS



$|\Delta B_\Lambda^{\text{stat.}}| = 20 \text{ keV}$

➔ Hypertriton Puzzle +  $\Lambda\text{N}$  int.  
 (g.s. or excited states)



$|\Delta B_\Lambda^{\text{stat.}}| = 30 \text{ keV}$

➔  $\Lambda\text{N}$  CSB in  $A = 4$

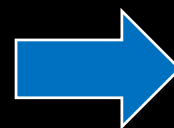


# CALIBRATIONS AND A SYSTEMATIC ERROR ON $B_\Lambda$

Calibration	Target + Sieve Slit	Reaction	$z_t$ range (mm)	Beamtime (day)	Remarks
Mom. + $z_t$	H	$p(e, e' K^+) \Lambda, \Sigma^0$	$-115 < z_t < 115$	1	$\Lambda$ : 6100, $\Sigma^0$ : 2030
Mom. + $z_t$	$^{12}\text{C}$ (multi foils)	$^{12}\text{C}(e, e' K^+) ^{12}_\Lambda\text{B}$		1	$^{12}_\Lambda\text{B}^{\text{g.s.}}$ : $300 \times 5$
Angle + $z_t$	$^{12}\text{C}$ (multi foils) + SS	-		0.2	
$z_t$	Empty	-	$-100 < z_t < 100$	0.1	+ Background study
	Empty (or gas) + SS	-		0.2	+ Angle resolution check
Physics	$^{3,4}\text{He}$	$^{3,4}_\Lambda\text{H}$	$-100 < z_t < 100$	22	

## Major contributions to a systematic error on $B_\Lambda$

- Energy scale calibration<sup>(\*)</sup>:  $\pm 50$  keV
- Energy loss correction:  $\pm 40$  keV
  - target density  $|\Delta d| = 3\%$
  - cell thickness uniformity  $|\Delta t| = 10\%$

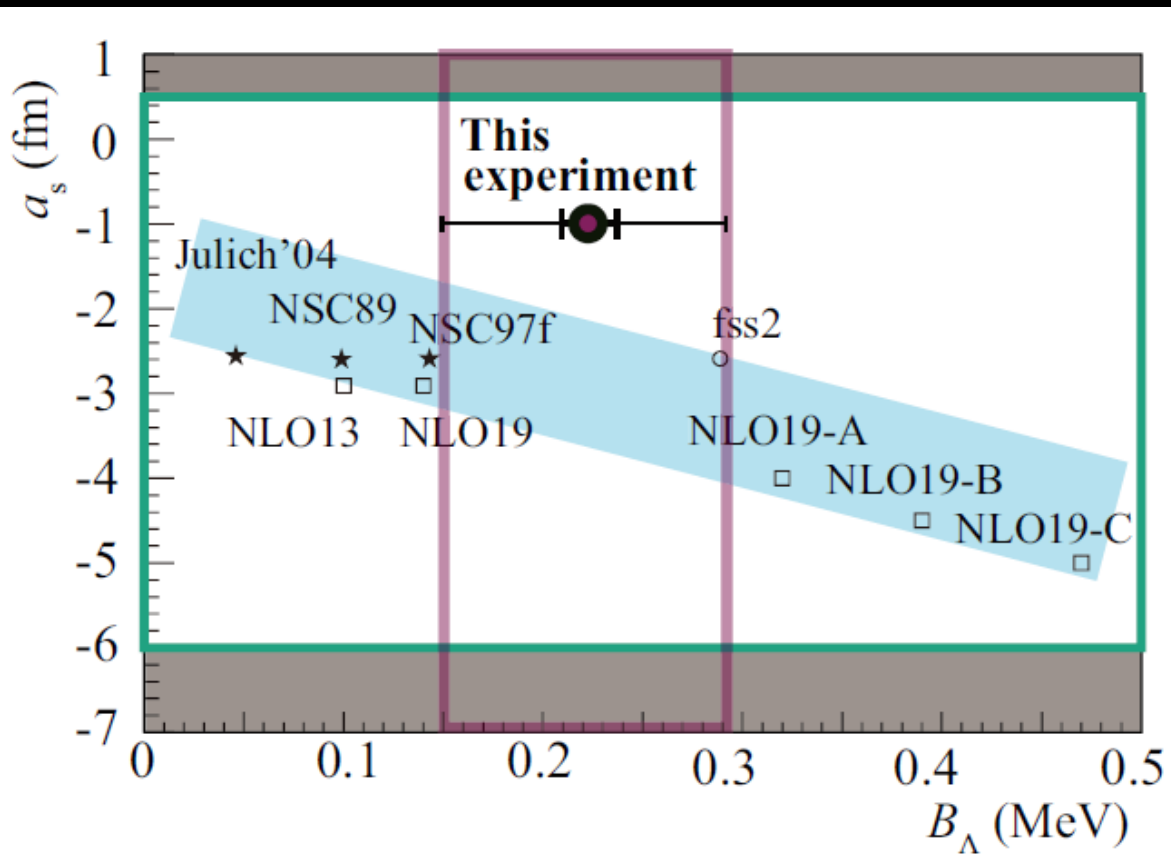


$$|\Delta B_\Lambda^{\text{sys.}}| = 70 \text{ keV}$$

<sup>(\*)</sup> TG et al., NIMA 900 (2018) 69—83



# GROUND STATE OF ${}^3_{\Lambda}\text{H}$ ( $T = 0, J^{\pi} = 1/2^{+}$ )



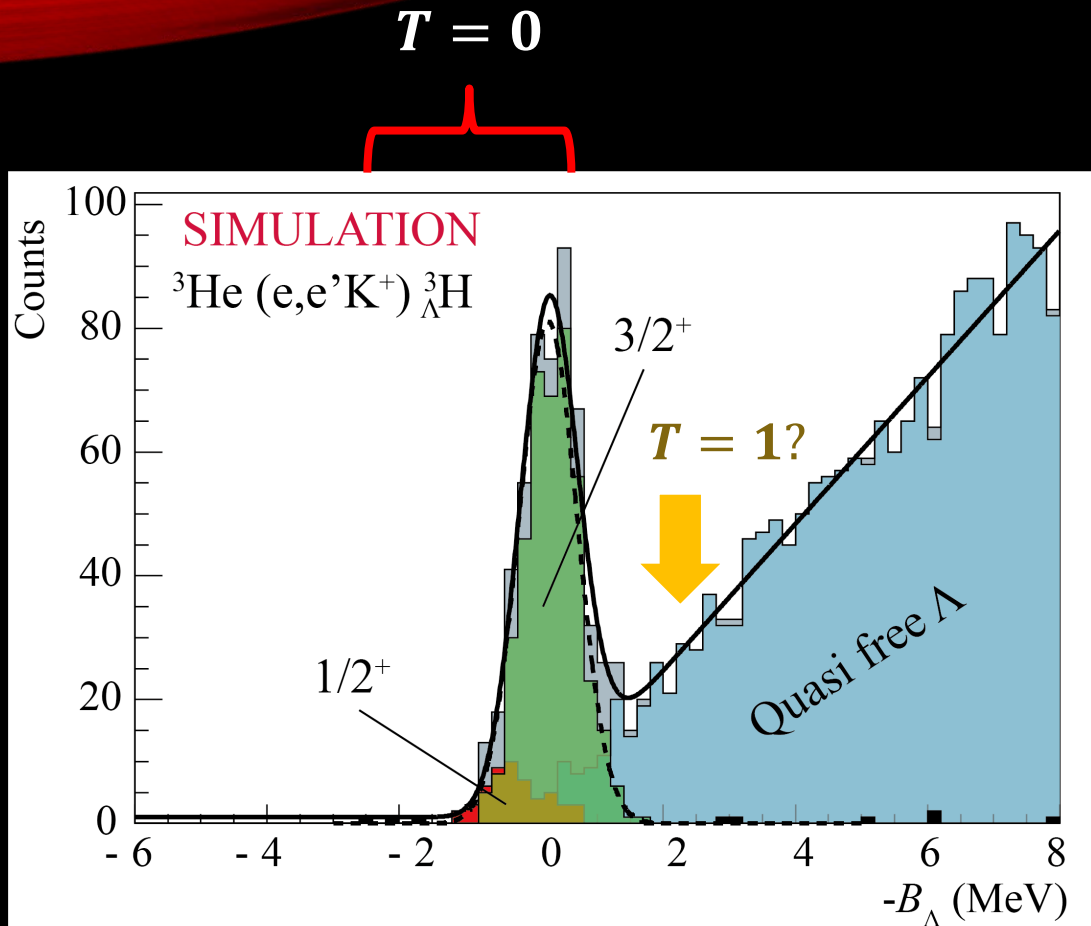
## Hypertriton Puzzle

- $\Lambda$  d m radius ( $|\Delta r| \leq 1$  fm)  
 → Better estimation for the lifetime

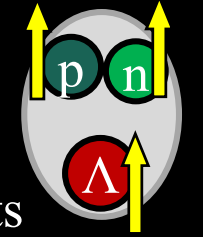
## $\Lambda\text{N}$ interaction

- Constraint for
  - Interaction models
  - The  $\Lambda\text{N}$  spin singlet scattering length ( $|\Delta a_s| \sim 1$  fm; cf.  $a_s = 1.8^{+2.3}_{-4.2}$  fm)

# EXCITED STATES OF ${}^3_{\Lambda}\text{H}$



## ${}^3_{\Lambda}\text{H} (T = 0, J^{\pi} = 3/2^{+})$



- Has NOT been measured
- Hard to measure by emulsion / HI experiments
- Does it exist?
  - If yes, the CS is larger than  $1/2$  by a factor of 8 <sup>(1)</sup>
  - If no, only the  $1/2^{+}$  state will be observed
- $\leftarrow$   $\bar{\kappa}$ EFT predicts  $3/2^{+}$  as a virtual state <sup>(2)</sup>
- Strong constraint for the  $\Lambda\text{N}$  spin triplet interaction

## ${}^3_{\Lambda}\text{H} (T = 1, J^{\pi} = 1/2^{+})$



- Isospin partner of  $nn\Lambda$  (and  $pp\Lambda$ )
  - $\rightarrow$  significant information on the existence of  $nn\Lambda$
- CSB study in the  $A = 3$  hypernuclear system
- If the CS is 0.5 nb/sr  $\rightarrow |\Delta B_{\Lambda}^{\text{stat.}}| \sim 70$  keV

(1) T. Mart *et al*, *Nucl. Phys. A* **640**, 235-258 (1998)

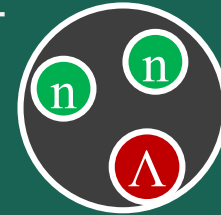
(2) M. Schäfer *et al.*, *Phys. Lett. B* **808**, 135614 (2020)



# SUMMARY

## HRS-HRS @ Hall A (JLab E12-17-003, 2018)

- ${}^3\text{H}(e, e'K^+)nn\Lambda$
- Analysis in progress (by 3 independent teams)
  - Peak search,  $n(n)\text{-}\Lambda$  FSI, reaction cross section



## HRS-HKS @ Hall A (JLab C12-19-002, 2022/2023)

- $B_{\Lambda}({}^{3,4}\text{H})$  with an accuracy of

$$\Delta B_{\Lambda}^{\text{tot.}} = \sqrt{|\Delta B_{\Lambda}^{\text{sys.}}|^2 + |\Delta B_{\Lambda}^{\text{stat.}}|^2} < 80 \text{ keV}$$

- Hypertriton Puzzle / Charge Symmetry Breaking

