

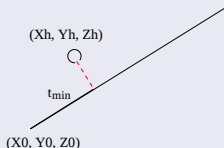
Status of Mainz-Simulations

Anastasia Karavdina

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Changes in track-fit

Least-squares method



$$x = p_0 + p_1 t, y = p_2 + p_3 t, z = Z_0 + t.$$

$$t_{min} = \frac{p_1(X_h - p_0) + p_3(Y_h - p_2) + (Z_h - Z_0)}{p_1^2 + p_3^2 + 1}$$

New χ^2 -function

$$\chi^2 = \frac{(X_h - (p_0 + p_1 t_{min}))^2}{\sigma_x^2} + \frac{(Y_h - (p_2 + p_3 t_{min}))^2}{\sigma_y^2} + \frac{(Z_h - (Z_0 + t_{min}))^2}{\sigma_z^2}$$

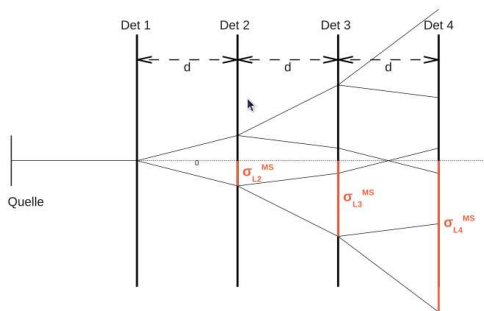
Instead of old χ^2 -function

$$\chi^2 = \frac{(x - (p_0 + p_1 z))^2}{\sigma_x^2} + \frac{(y - (p_2 + p_3 z))^2}{\sigma_y^2}$$

Changes in track-fit

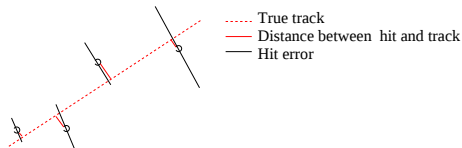
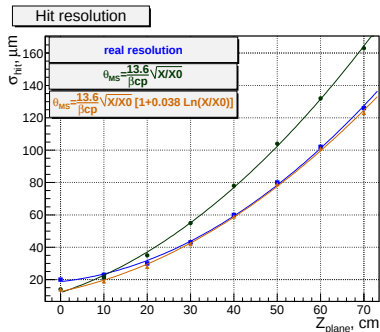
Taking into account multiple scattering in hit errors

$$\begin{aligned}\sigma_{L2} &= d \cdot \theta_{MS}, \\ \sigma_{L3} &= \sqrt{5}d \cdot \theta_{MS}, \\ \sigma_{L4} &= \sqrt{14}d \cdot \theta_{MS}.\end{aligned}$$



$$\sigma_{xi} = \sqrt{\sigma_{digi}^2 + \sigma_{Li}^2}$$

θ_{MS} calculation

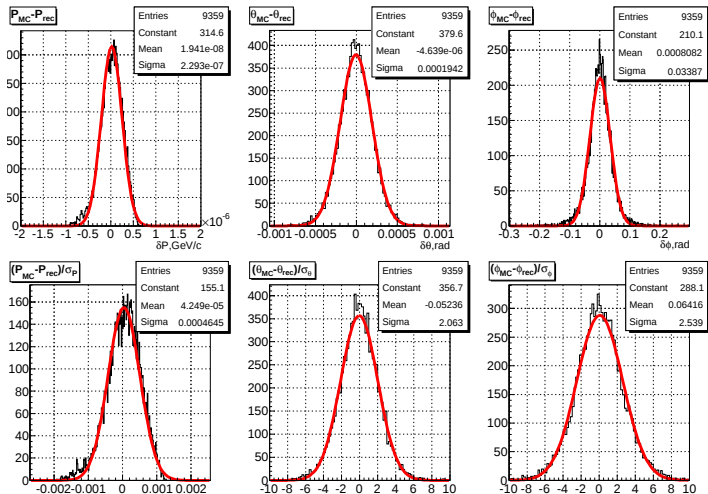


Estimation of hit errors with

$$\theta_{MS} = \frac{13.6}{\beta_{cp}} \sqrt{\frac{X}{X_0}} [1 + 0.038 \ln(\frac{X}{X_0})]$$

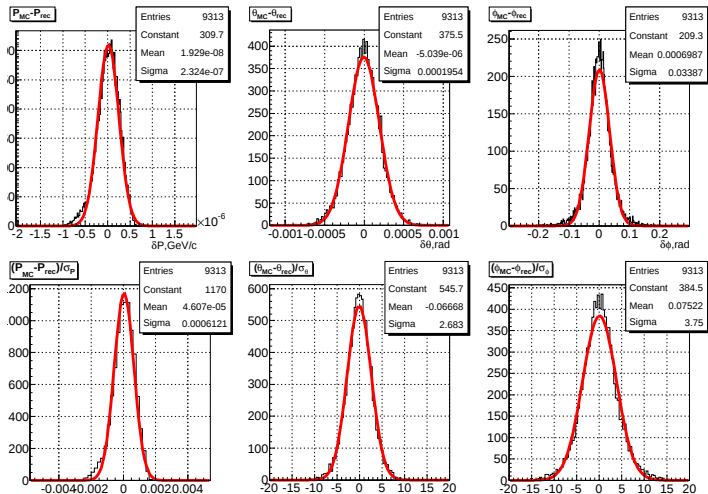
is in agreement with real resolution.

$|P|, \theta, \phi$ resolution for $p_{beam} = 4.06 \text{ GeV}/c$



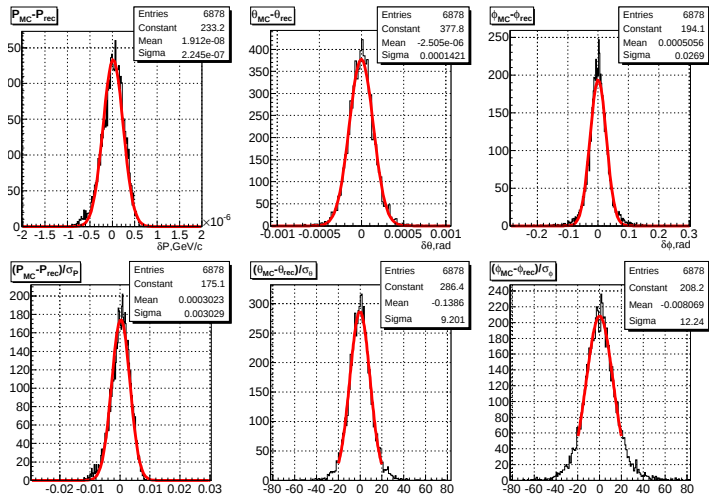
$$\sigma_P = 230 \text{ keV}/c, \sigma_\theta = 194 \text{ } \mu\text{rad}, \sigma_\phi = 34 \text{ mrad} \quad (\sigma_x = \sqrt{\sigma_{digi}^2 + \sigma_{MS}^2})$$

$|P|, \theta, \phi$ resolution for $p_{beam} = 4.06 \text{ GeV}/c$



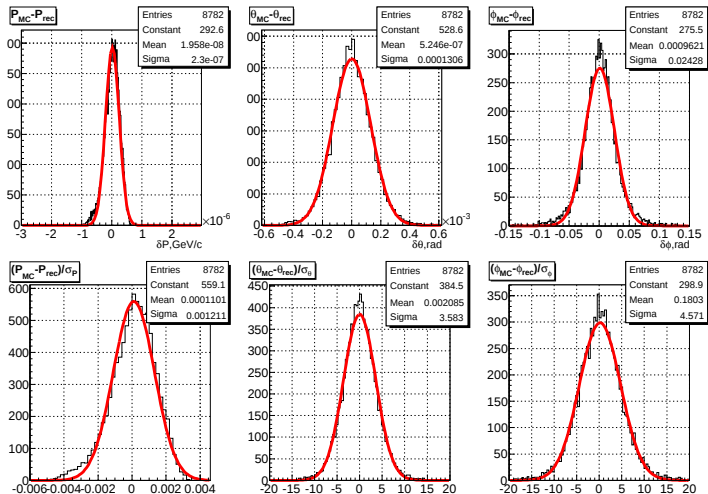
$$\sigma_P = 230 \text{ keV}/c, \sigma_\theta = 195 \text{ } \mu\text{rad}, \sigma_\phi = 34 \text{ mrad} \quad (\sigma_x = \sigma_{digi})$$

$|P|, \theta, \phi$ resolution for $p_{beam} = 4.06 \text{ GeV}/c$, $d = 50 \text{ cm}$



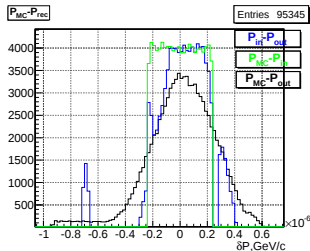
$$\sigma_P = 225 \text{ keV}/c, \sigma_\theta = 142 \text{ } \mu\text{rad}, \sigma_\phi = 27 \text{ mrad} \quad (\sigma_x = \sigma_{digi})$$

$|P|, \theta, \phi$ resolution for $p_{beam} = 4.06 \text{ GeV}/c$, $d = 50 \text{ cm}$



$$\sigma_P = 230 \text{ keV}/c, \sigma_\theta = 131 \text{ } \mu\text{rad}, \sigma_\phi = 24 \text{ mrad} \quad (\sigma_x = \sqrt{\sigma_{digi}^2 + \sigma_{MS}^2})$$

Accuracy of momentum magnitude determination



P_{MC} - true value

$P_{IN} = P_{fit}$,

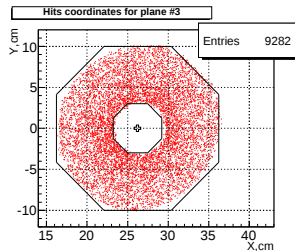
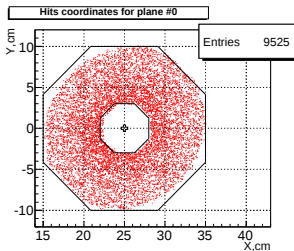
$$P_{fit} = |(p1, p3, 1) \cdot \frac{P_{beam}}{\sqrt{p1^2 + p3^2 + 1}}|$$

P_{OUT} - momentum magnitude after back-propagation with GEANE

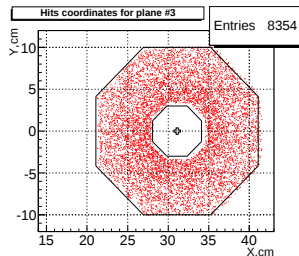
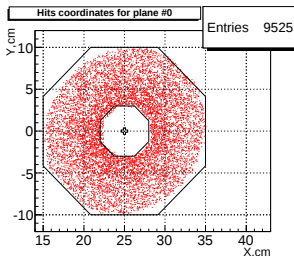
- Tail in momentum distribution appears after back-propagation.
- But error of determination momentum magnitude: $\sigma_P \sim 10^{-3} \text{GeV}/c$ (after track-fit), so difference $10^{-6} \text{GeV}/c$ **is not considerable**.

Hits distributions for different distance between planes

$d = 10 \text{ cm}$



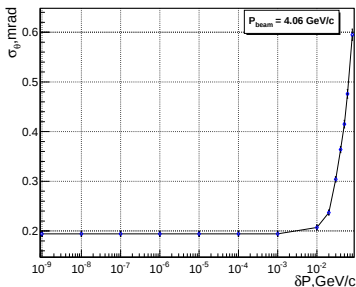
$d = 50 \text{ cm}$



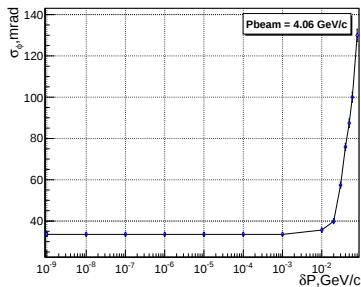
Uncertainties in determination θ and ϕ at IP due to uncertainty in momentum magnitude

$$|P_{IN}| = P_{beam} - \delta P$$

θ resolution vs. δP



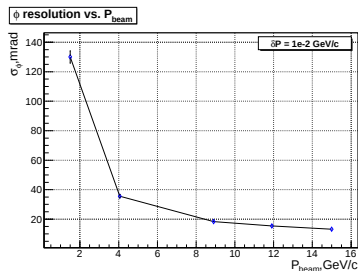
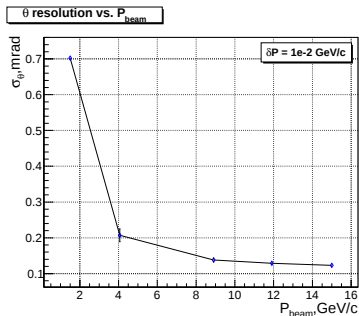
ϕ resolution vs. δP



σ_θ and σ_ϕ is insensitive to $\delta P < 10 \text{ MeV}/c$

Uncertainties in determination θ and ϕ at IP due to uncertainty in momentum magnitude

$$|P_{IN}| = P_{beam} - \delta P$$



Results & Plans

Results

- χ^2 function was changed in Track Fitter.
- Contribution of multiple scattering to hits errors was added and checked in Track Fitter.
- Uncertainties in determination θ and ϕ at IP due to uncertainty in momentum magnitude were studied with SimpleBox generator for:
 - * different δP ($P_{beam} = 4.06 GeV/c$).
 - * different P_{beam} ($\delta P = 10^{-2} GeV/c$)

Plans

- Optimization of Track-Finder & Track-Fitter procedures
- Study of efficiency (missed tracks, ghost tracks; different number of tracks per event etc.)
- Background study