

Matter under Extreme Conditions

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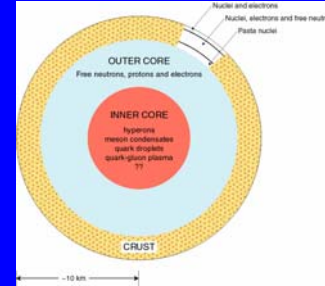
The ExtreMe Matter Institute (EMMI)

16 July 2008

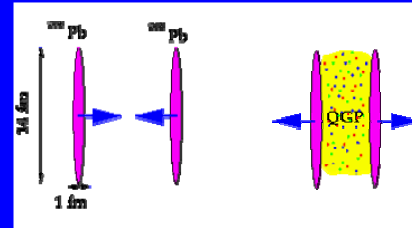


Milestones in study of matter under extreme conditions

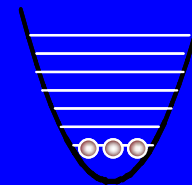
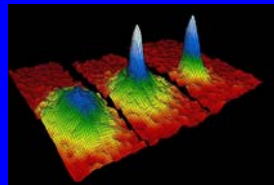
Discovery of pulsars and neutron stars, 1967-68



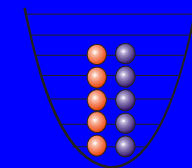
Ultrarelativistic heavy ion collisions, ca. 1985



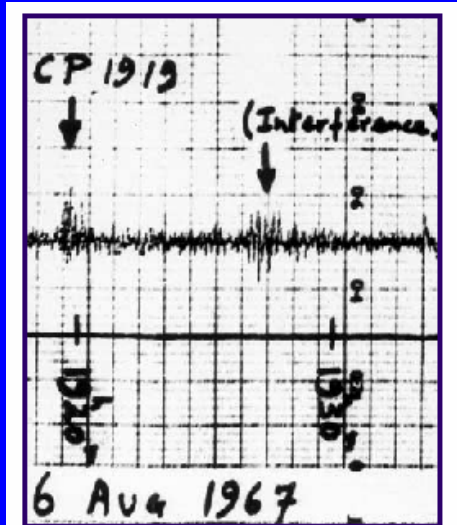
Ultracold atomic Bose-Einstein condensates, 1995



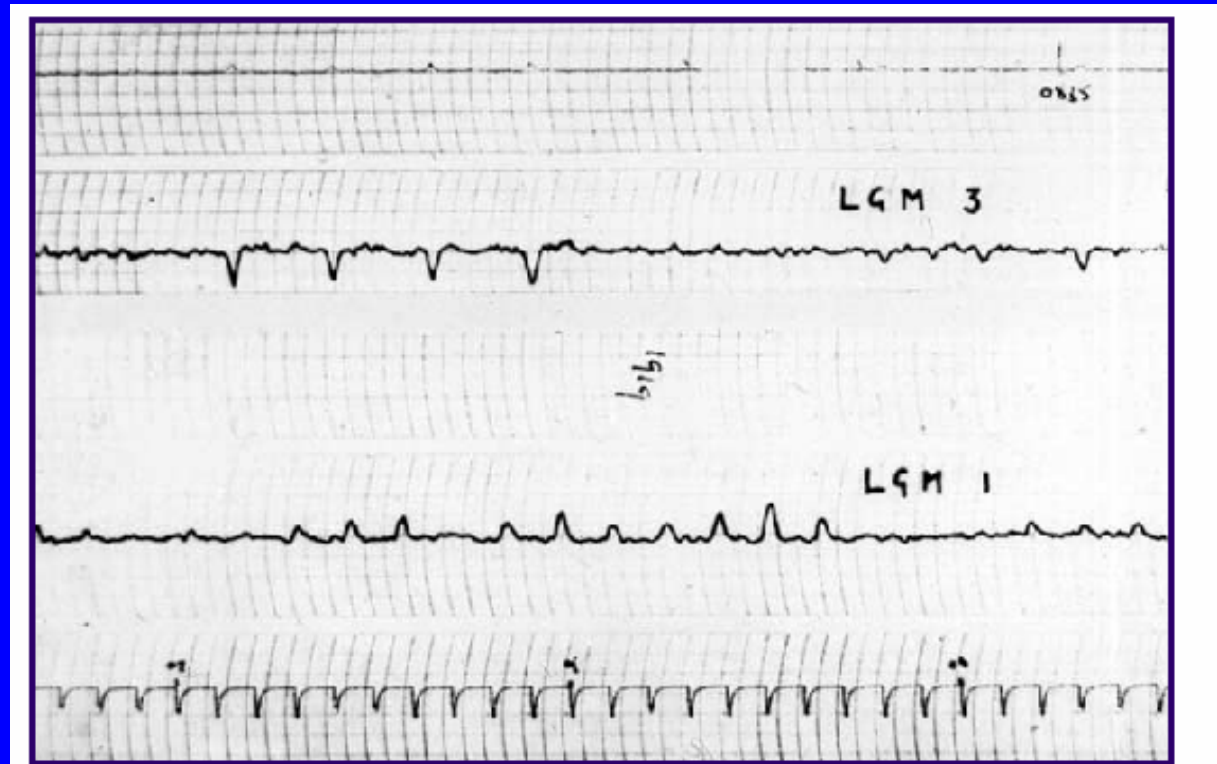
Degenerate (\Rightarrow superfluid) atomic Fermi gases, 1999-2004



1967 First pulsar detection: PSR1919+21 *Bell & Hewish*



2: The first detection of the first pulsar, occupying about one-quarter inch of chart paper. About five minutes later is a short burst of low level interference. This signal has been high-pass filtered, to remove the telescope's interference pattern. (Mullard Radio Astronomy Observatory.)



3: The bottom trace is of broadcast one-second time pips. The middle trace shows the first recording to reveal the pulsed nature of the pulsar PSR1919. The top trace is of the third pulsar discovered, PSR0834.

“It was highly unlikely that there would be two lots of little green men on opposite sides of the universe both deciding to signal at the same time to a rather inconspicuous star on a rather curious frequency.” Jocelyn Bell

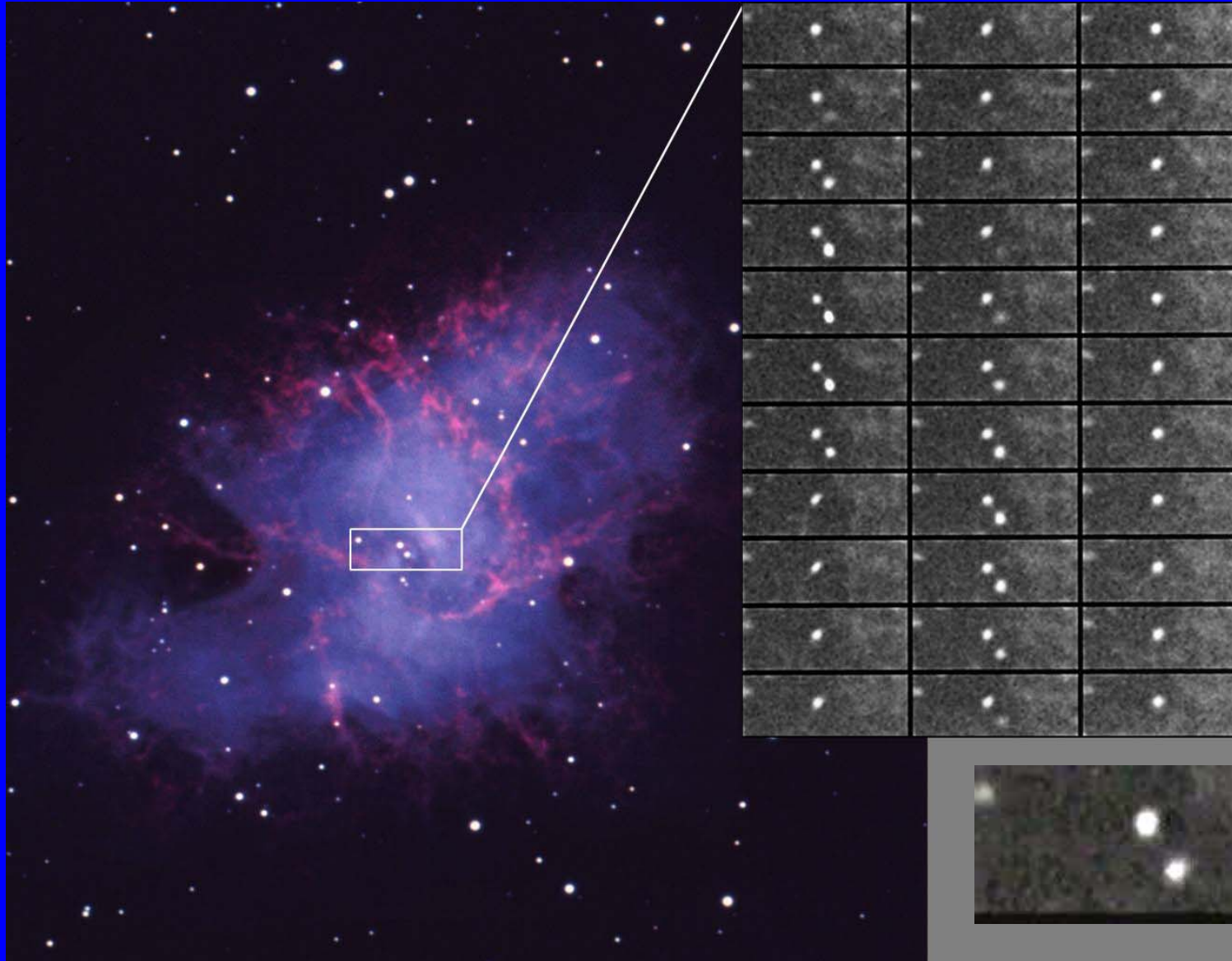


Crab nebula
in optical

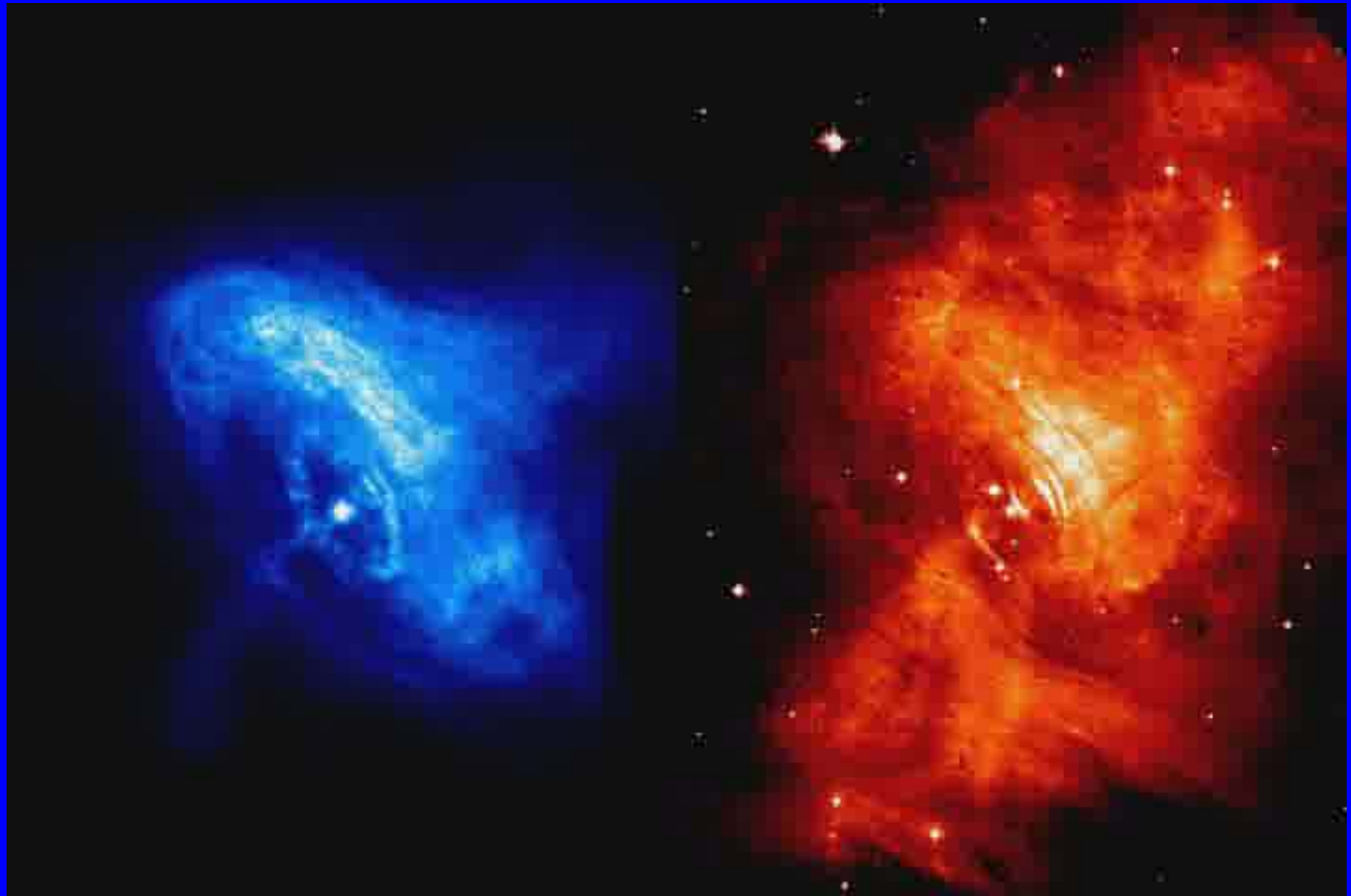
Supernova
July 4, 1054

Observed in
China, Japan,
Korea

Crab Pulsar (period = 1/30 sec)



1 msec
per frame



Crab nebula in x-ray (Chandra)

and in optical (Hubble)

Observed neutron stars

> 1400 ns in isolated rotation-powered radio pulsars
~ 30 millisecond pulsars

> 100 ns in accretion-powered x-ray binaries
~ 50 x-ray pulsars

intense x-ray bursters (thermonuclear flashes)

Short (10-100 s) gamma-ray bursts (ns-ns, ns-bh mergers)

Soft gamma-ray repeaters -- magnetars ($B \sim 10^{14}$ - 10^{15} G)

Astrophysical impetus for studying dense matter

Neutron stars

$\rho > \rho_{\text{nm}}$, $T < 1-10 \text{ MeV}$, $R \sim 10-12 \text{ km}$, $M \sim 1.2-2 M_{\odot}$

--birth, evolution and cooling (x-ray satellite observations)

--upper mass limits, black hole identification

Supernova and gravitational collapse

-- bounce above ρ_{nm} , energy release

-- hot n-rich nuclei

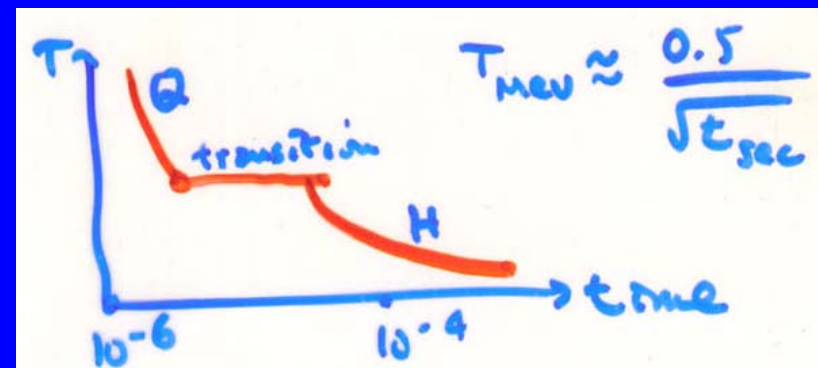


Cosmology

-- mini- black holes

$$M \sim M_{\text{jupiter}} \sim 10^{-2} M_{\odot}$$

Cosmic rays

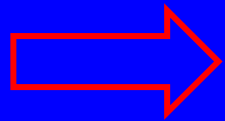


Maximum neutron star mass -- and black holes

Equation of state of matter at high baryon density determines maximum possible neutron star mass, and thus the cut on black holes. Conventional cut on black hole candidates: $M_{\max} = 3.2M_{\odot}$. Improved knowledge of properties of dense matter leads to lower cut:

Knowing equation of state to

$$\rho = 2\rho_{\text{nm}} \Rightarrow M_{\text{ns}} < 2.9 M_{\odot}$$
$$\text{and to } 4\rho_{\text{nm}} \Rightarrow M_{\text{ns}} < 2.2\text{-}2.3 M_{\odot}.$$



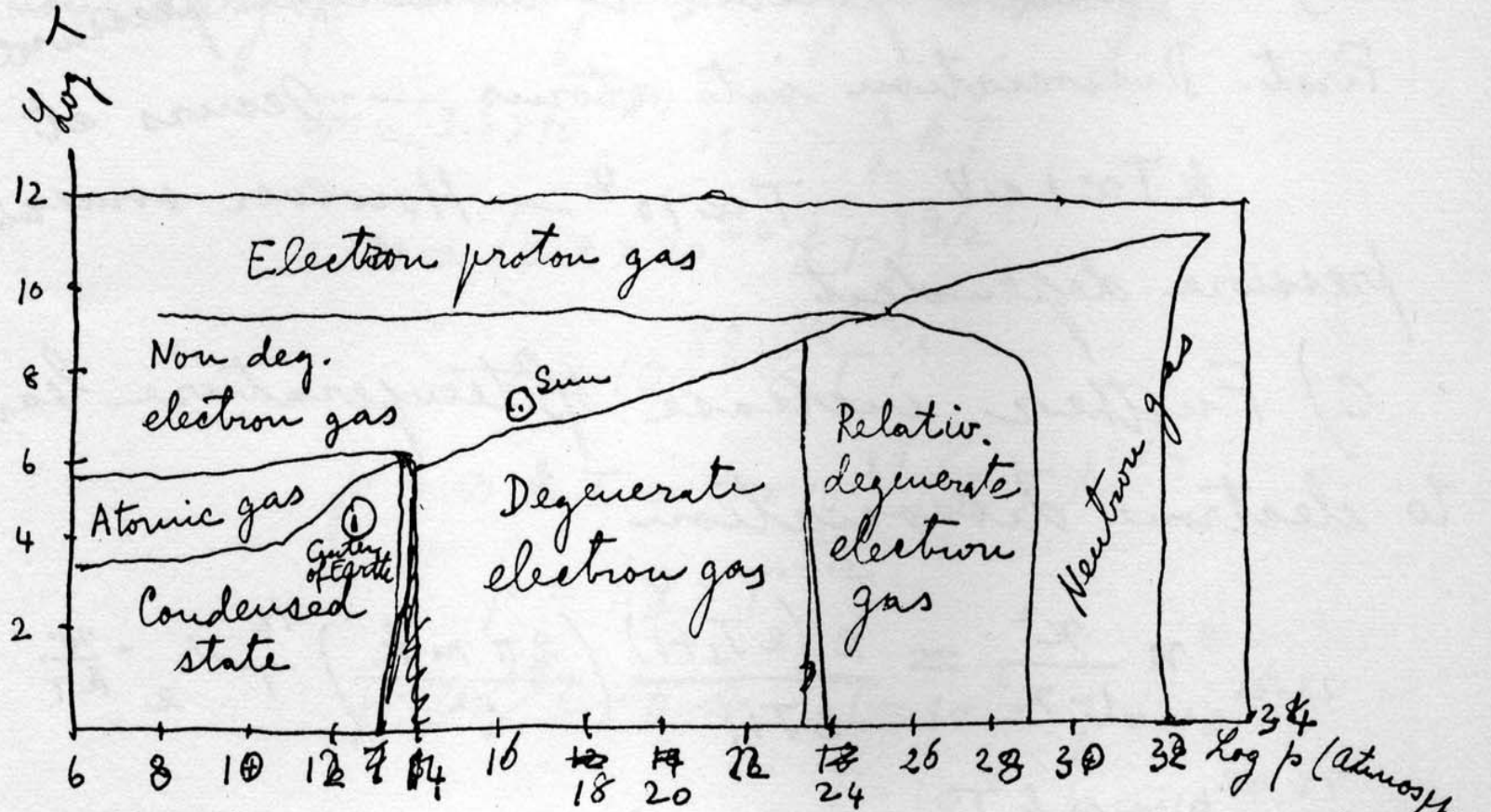
many new small mass black hole candidates

Mass function: $f_{\text{opt}} = (M_x^3 \sin i) / (M_x + M_{\text{optical}})^2 < M_x$
in low mass x-ray binaries

ex. Nova muscae, $f_{\text{opt}} = 3.1 \pm 0.4$
GRO J1655-40, $f_{\text{opt}} = 3.16 \pm 0.15$

70 - Matter in unusual conditions

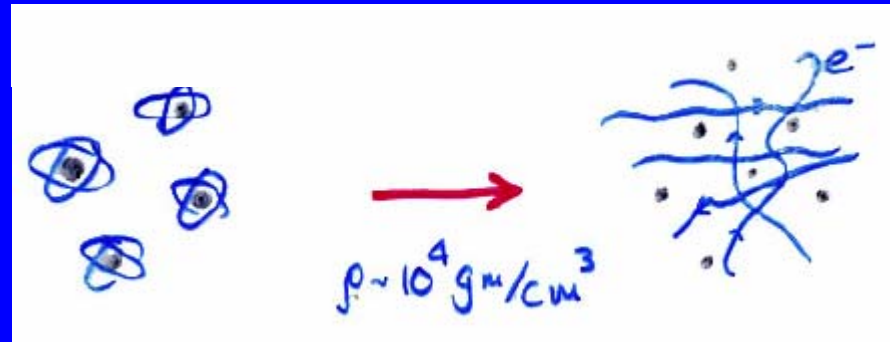
70 a



Start from ordinary condensed matter with ~~ordinary~~ equation of state controlled by ordinary chemical forces.

Compress matter to form new states

Atoms



Plasma

Nuclei

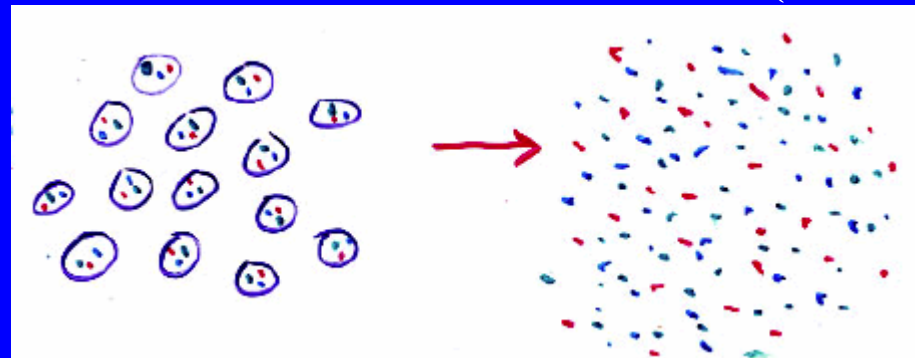


Nuclear matter

$$\rho \sim 2.5 \times 10^{14} \text{ gm/cm}^3 = \rho_{\text{nm}} = 0.17 \text{ baryons/fm}^3$$

(1 fm = 10^{-13} cm)

Nucleons



Quark matter

Quark degrees of freedom

Quarks = fractionally charged spin-1/2 fermions,
baryon no. = 1/3, with internal SU(3) **color** degree of freedom.

Flavor	Charge/ e	Mass(MeV)
u	2/3	5 (2.1-3.5)
d	-1/3	10 (2.1-3.5)
s	-1/3	150 (54-92)
c	2/3	1300
b	-1/3	4200
t	2/3	175000



Hadrons are composed of quarks:

$$\text{proton} = u + u + d$$

$$\text{neutron} = u + d + d$$

$$\pi^+ = u + \bar{d}, \text{ etc.}$$

Form of baryons in the early universe at $t < 1\mu \text{ sec}$ ($T > 100 \text{ MeV}$).

Possibly basic degrees of freedom in deep interiors of neutron stars.

Evolution of early universe

History of the Universe

Accelerators: CERN-LHC
 FNAL-Tevatron
 high-energy cosmic rays
 BNL-RHIC
 CERN-LEP
 SLAC-SLC

BIG BANG

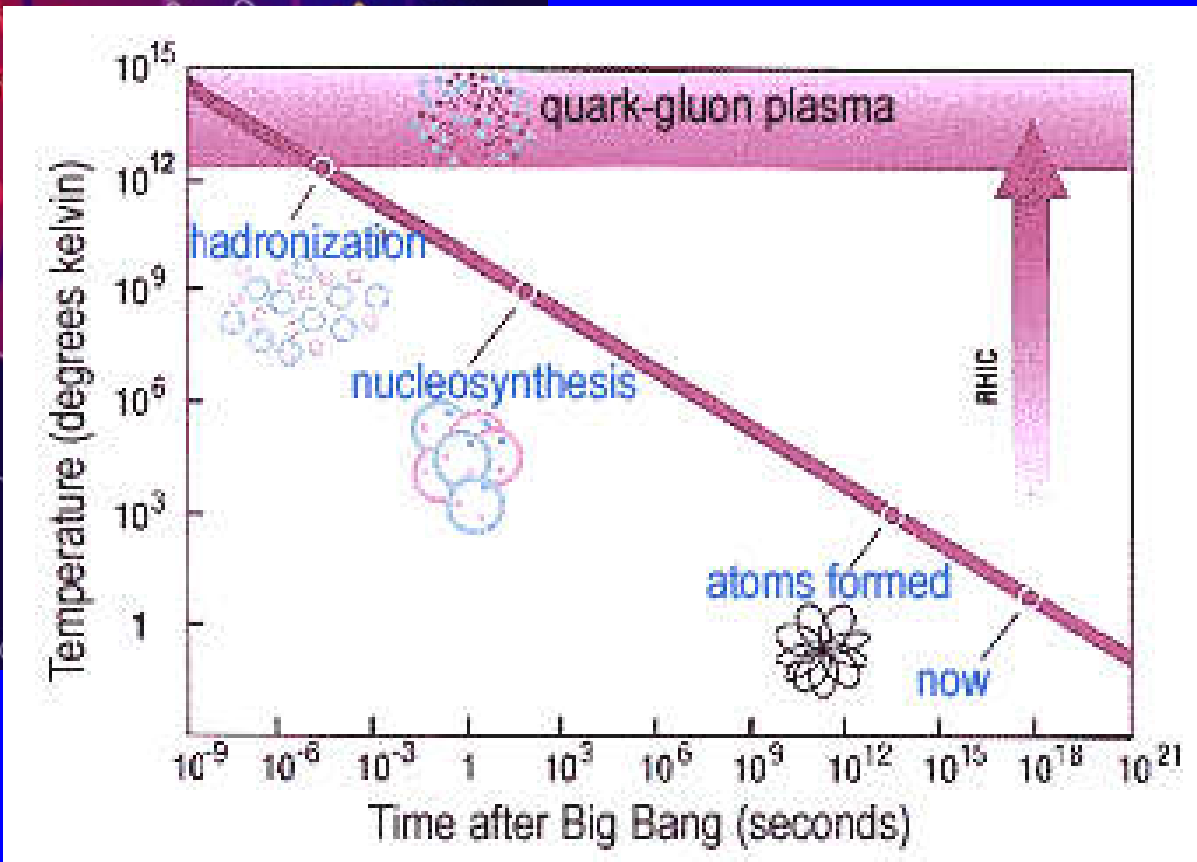
Inflation



Key:

W, Z bosons	photon
quark	meson
gluon	baryon
electron	ion
muon	atom
tau	star
neutrino	galaxy
	black hole

Particle Data Group, LBNL, ...



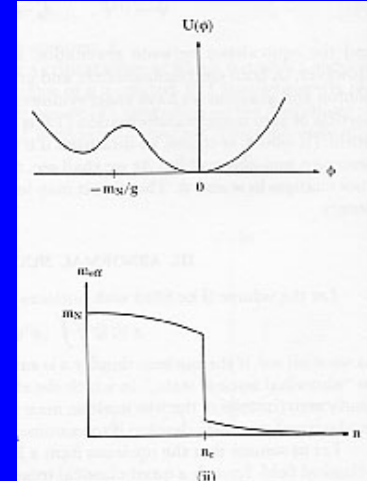
What are the properties of matter under extreme conditions? High temperature, high densities!

Early hadronic pictures:

Lee-Wick abnormal matter

Hagedorn hadronic resonance gas

Walecka mean field model

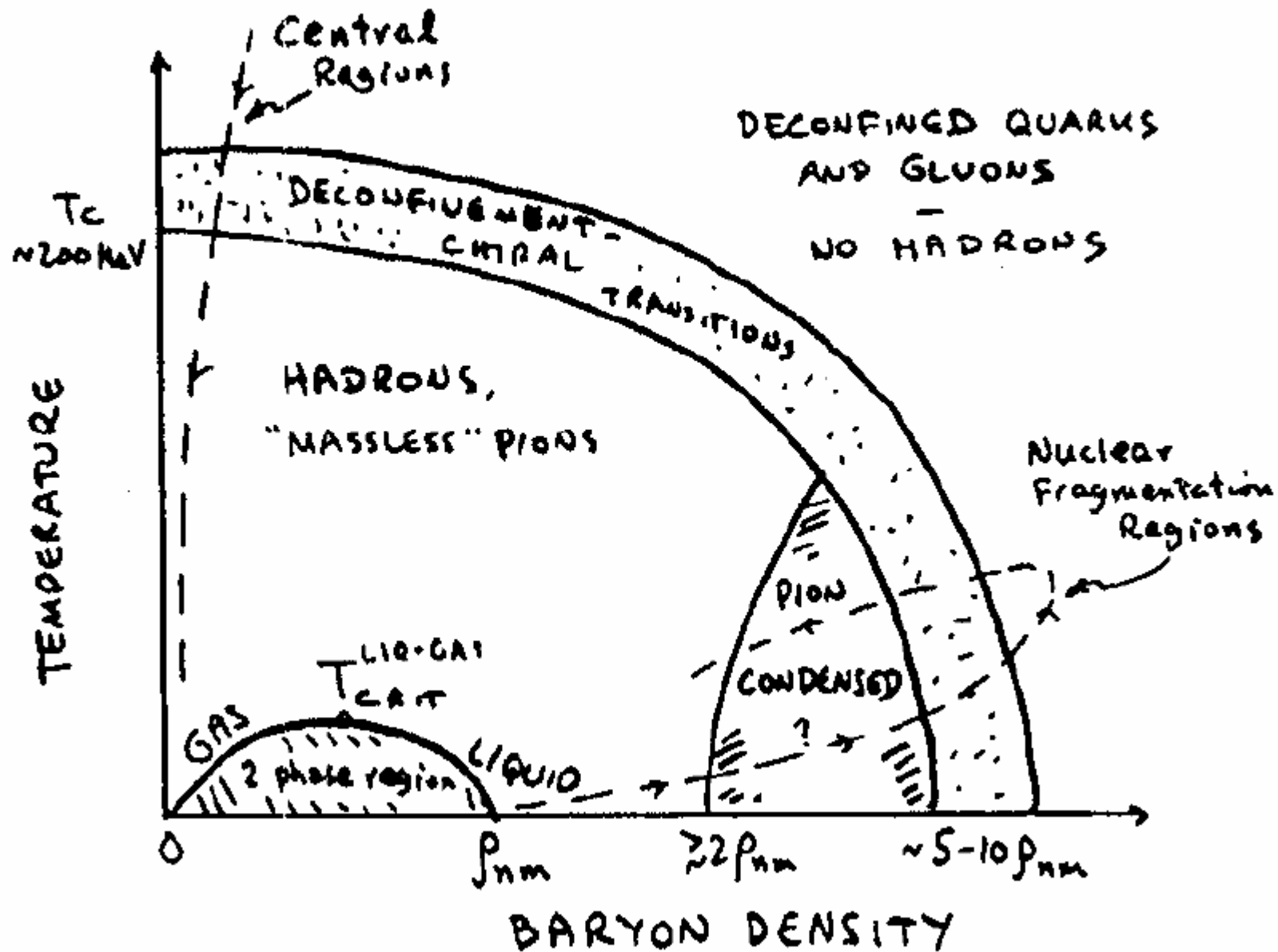


Quark matter (“quark soup”) as ultimate state (1970-75):

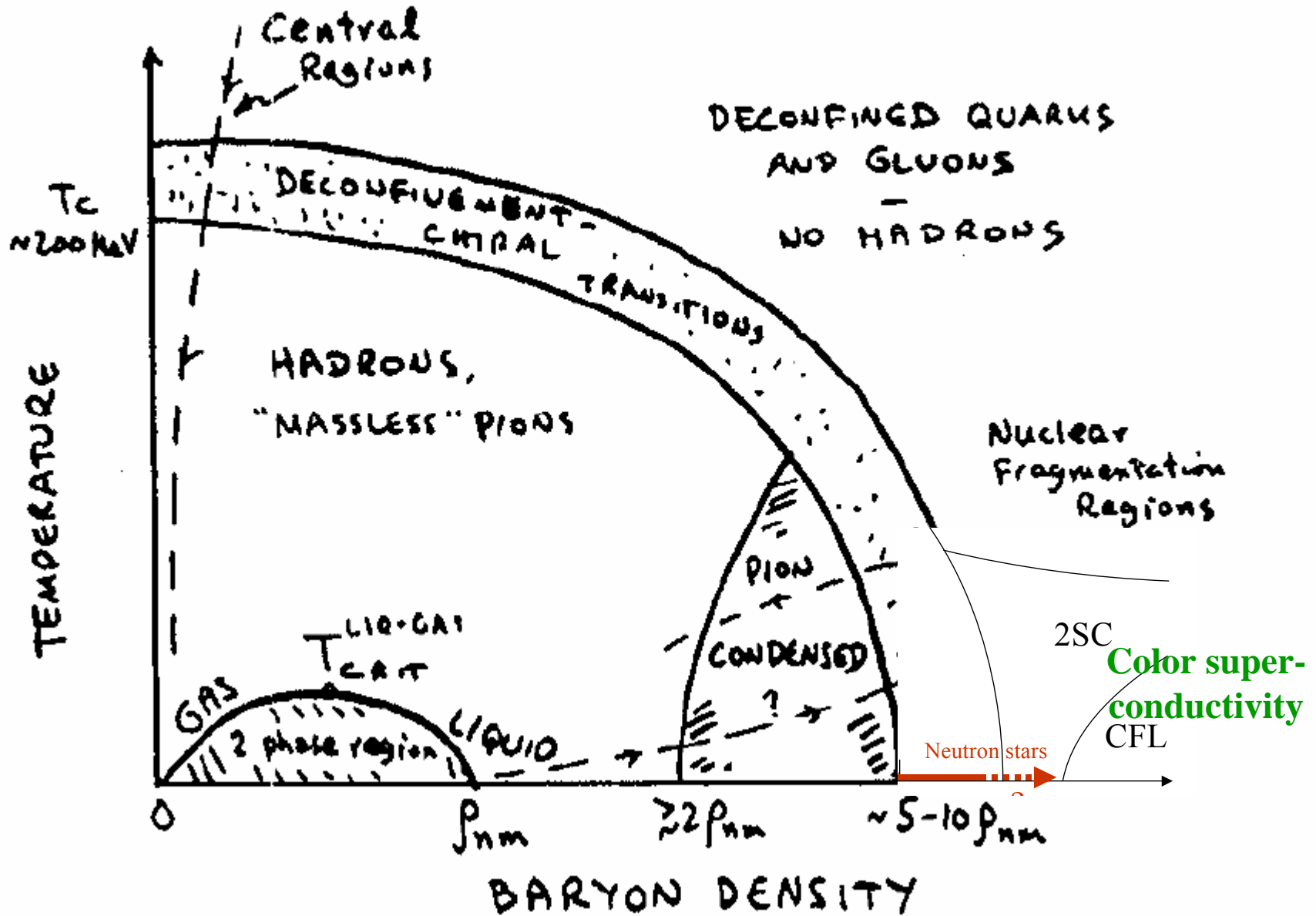
Asymptotic freedom of QCD \Leftrightarrow at ultrahigh densities or temperatures “quarks interact weakly.”

Quark matter in neutron stars: “Can a neutron star be a giant MIT bag?”

PHASE DIAGRAM OF NUCLEAR MATTER



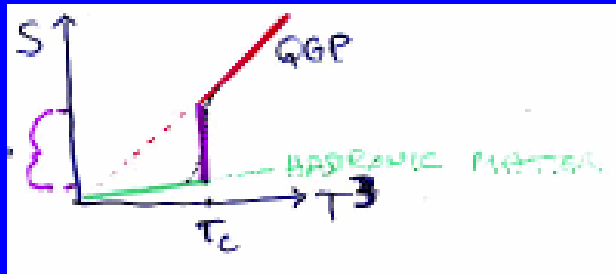
PHASE DIAGRAM OF NUCLEAR MATTER



Quark-gluon plasma state

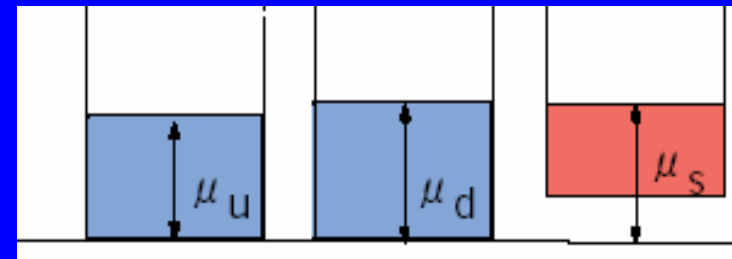
Degrees of freedom are **deconfined** quarks and gluons

Many more degrees of freedom than hadronic matter (color, spin, particle-antiparticle, & flavor); much larger entropy at given temperature.



\Leftarrow Large latent heat (or sharp rise at least)

At low temperatures form Fermi seas of degenerate u, d, and s quarks: (e.g., in neutron stars?)



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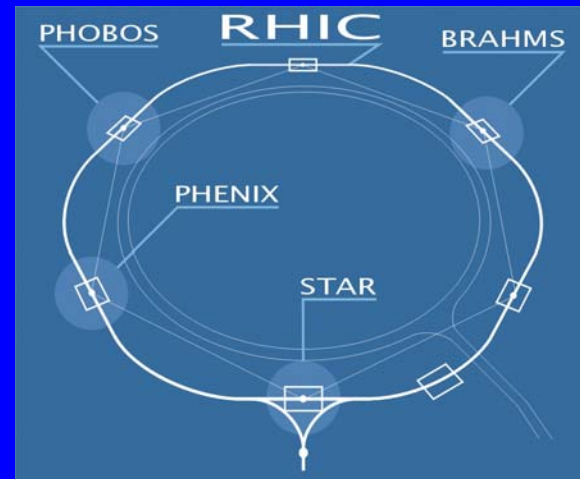
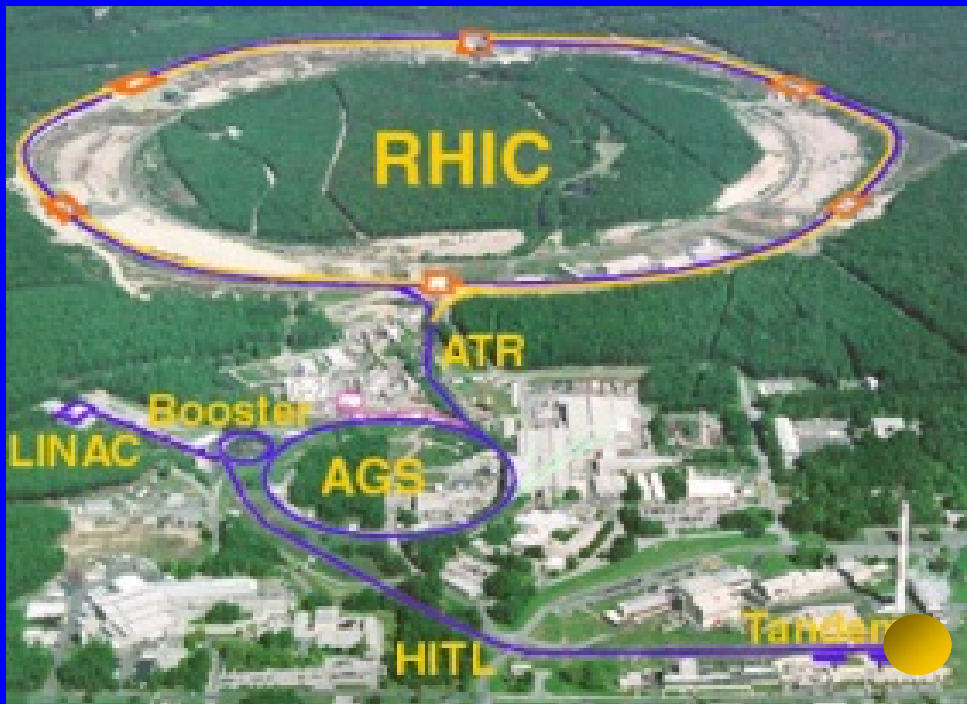
*Nuclei as heavy as bulls
Through collision
Generate new states of matter*

核
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如
牛

T.D. Lee

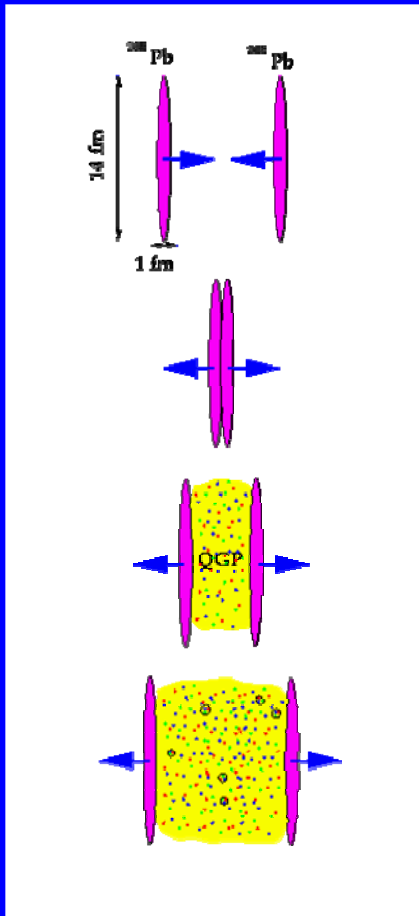
Creating high energy density matter in the lab

Relativistic Heavy Ion Collider (Brookhaven) since 2000. Colliding beams 100 GeV/A
Large Hadron Collider (CERN) in 2008-9. 2700 GeV/A
FAIR (GSI) ca. 2015 to 45 GeV/A



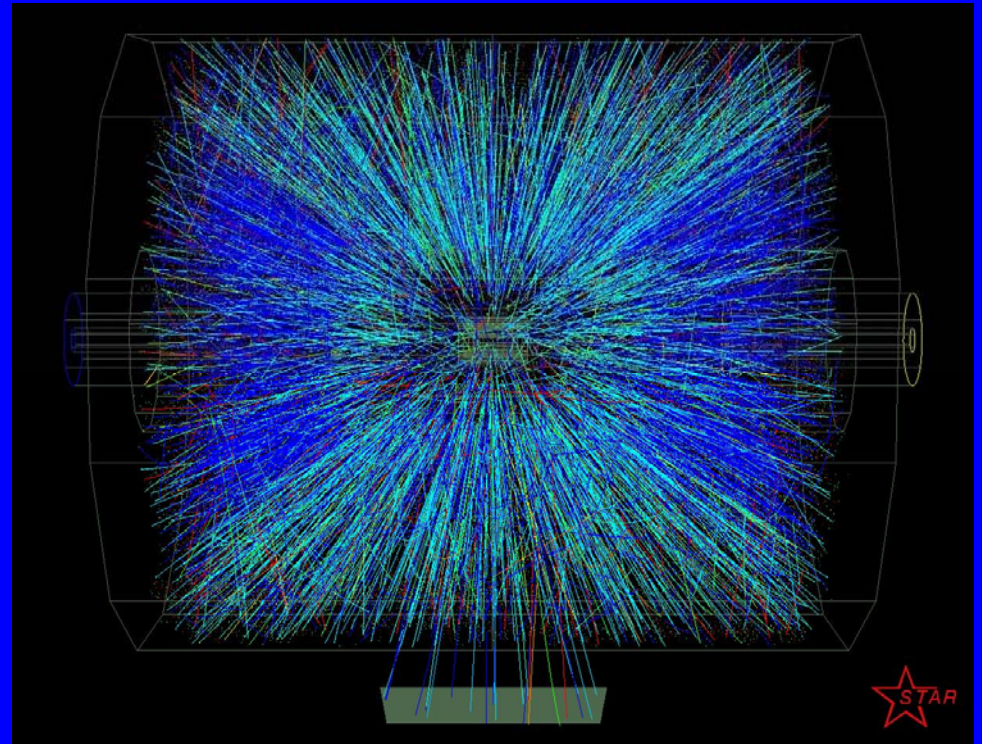
T. Hirano

$\text{Au}(197 \times 100\text{GeV}) + \text{Au}(197 \times 100\text{GeV})$

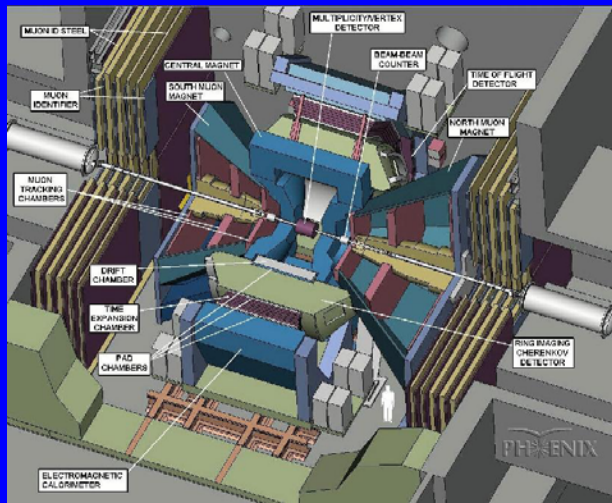


Schematic collision:

Two Lorentz contracted nuclei collide, pass through each other, leaving highly excited state of vacuum in between.

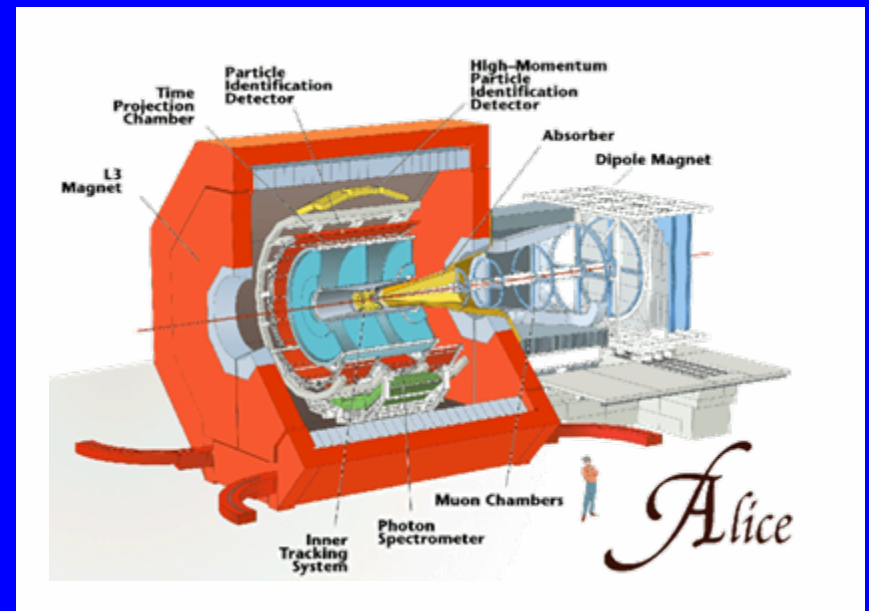


What collisions actually look like in the lab. STAR detector



Two major detectors at RHIC
PHENIX
STAR

Two smaller detectors
BRAHMS
PHOBOS



ALICE detector at LHC

A few crucial observations at RHIC:

Produce matter with energy densities $\sim 5 \text{ GeV/fm}^3$

$\sim 10\text{-}30 \times$ energy density of ordinary nuclei $\sim 0.15 \text{ GeV/fm}^3$

Certainly produce quark-gluon plasma.

Fast quarks traversing medium lose energy rapidly. “Opaque” medium

Very rapid build-up of pressure in collisions:

Large collective flow, fast thermalization, large interaction cross sections.

Hydrodynamics \Rightarrow small viscosity

Ultracold trapped atomic clouds

Deconfined quark-gluon plasmas

made in ultrarelativistic heavy ion collisions

$T \sim 10^2 \text{ MeV} \sim 10^{12} \text{ K}$ (temperature of early universe at $\sim 1 \mu \text{ sec}$)

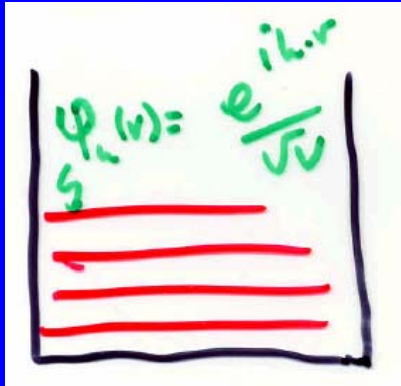
Trapped cold atomic systems:

Bose-condensed and BCS fermion superfluid states

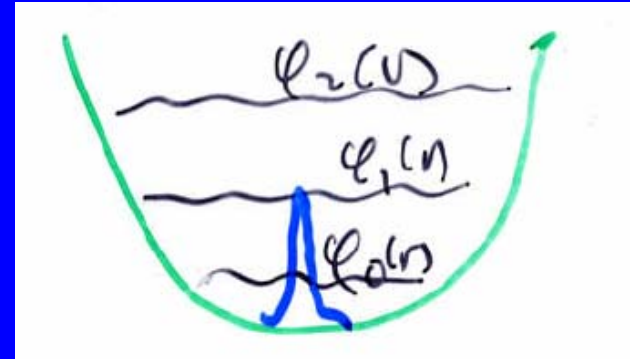
$T \sim \text{nanokelvin}$ (traps are the coldest places in the universe!)

Although these systems are separated by ~ 21 decades in characteristic energy scales, they have intriguing and unexpected overlaps.

Cold atoms: trapped bosons and fermions



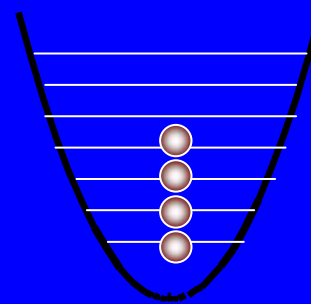
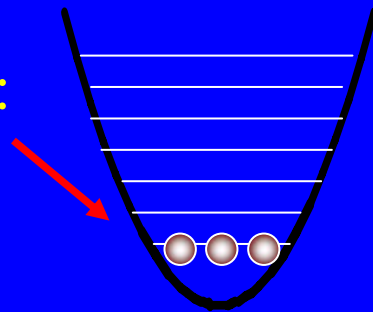
Box



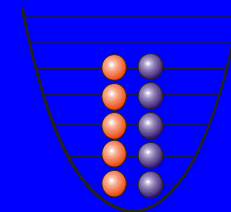
Potential well (trap)

Statistics:

Bose condensate:
macroscopic
occupation of
single mode
(generally lowest)



Degenerate
Fermi gas



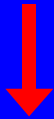
=> BCS pairing

Trapped atomic experiments in a nutshell

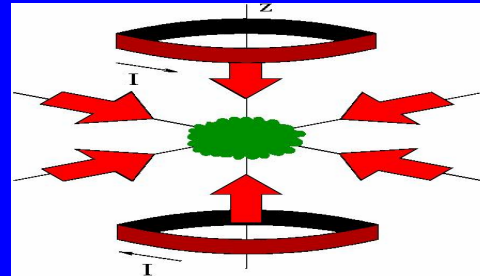
Warm atomic vapor



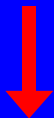
$T=300\text{K}$, $n\sim 3\times 10^6/\text{cm}^3$



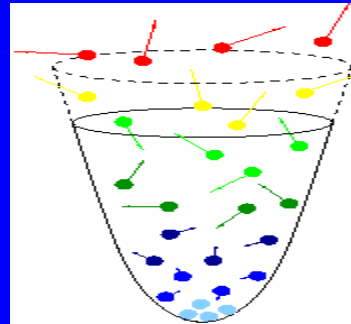
Magneto-optical trap



Laser cool to $T\sim 50\mu\text{K}$
 $n\sim 10^{11}/\text{cm}^3$



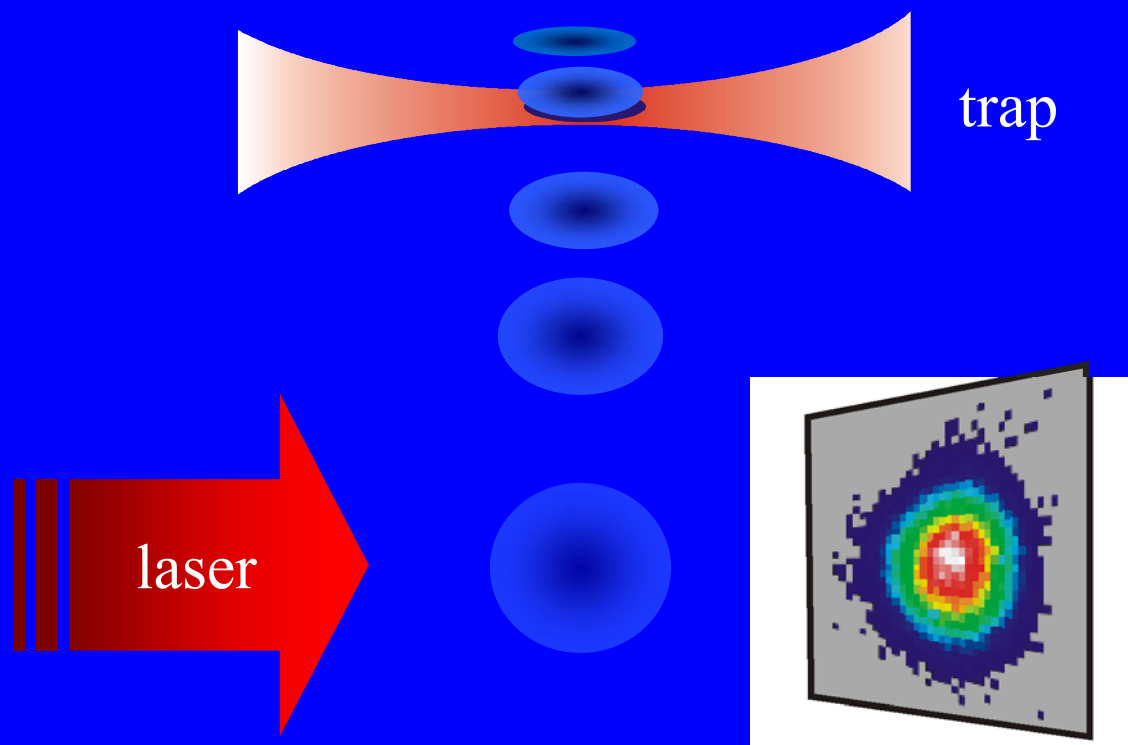
Evaporatively cool in
magnetic (or optical)
trap



Bosons condense,
Fermions BCS-pair
 $T\sim 1-10^3\text{ nK}$
 $n\sim 10^{14-15}/\text{cm}^3$
 $N\sim 10^5-10^8$

Experiment, and then measure :

To probe system, release from trap, let expand and then image with laser:



Long-Lived Alkali Atoms

BOSONS (Spin, lifetime)
(Z-N=odd-even nuclei)

${}^7\text{Li}$ 3/2-

${}^{23}\text{Na}$ 3/2-

${}^{39}\text{K}$ 3/2+

${}^{41}\text{K}$ 3/2+

${}^{85}\text{Rb}$ 5/2-

${}^{87}\text{Rb}$ 3/2- 4.75x10¹⁰y

${}^{131}\text{Cs}$ 5/2+ 9.7d

${}^{133}\text{Cs}$ 7/2+

${}^{135}\text{Cs}$ 7/2+ 2.3x10⁶y

${}^{209}\text{Fr}$ 9/2- 50.0s

FERMIONS
(Z-N=odd-odd nuclei)

${}^6\text{Li}$ 1+

${}^{22}\text{Na}$ 3+ 2.6y

${}^{40}\text{K}$ 4- 1.3x10⁹y

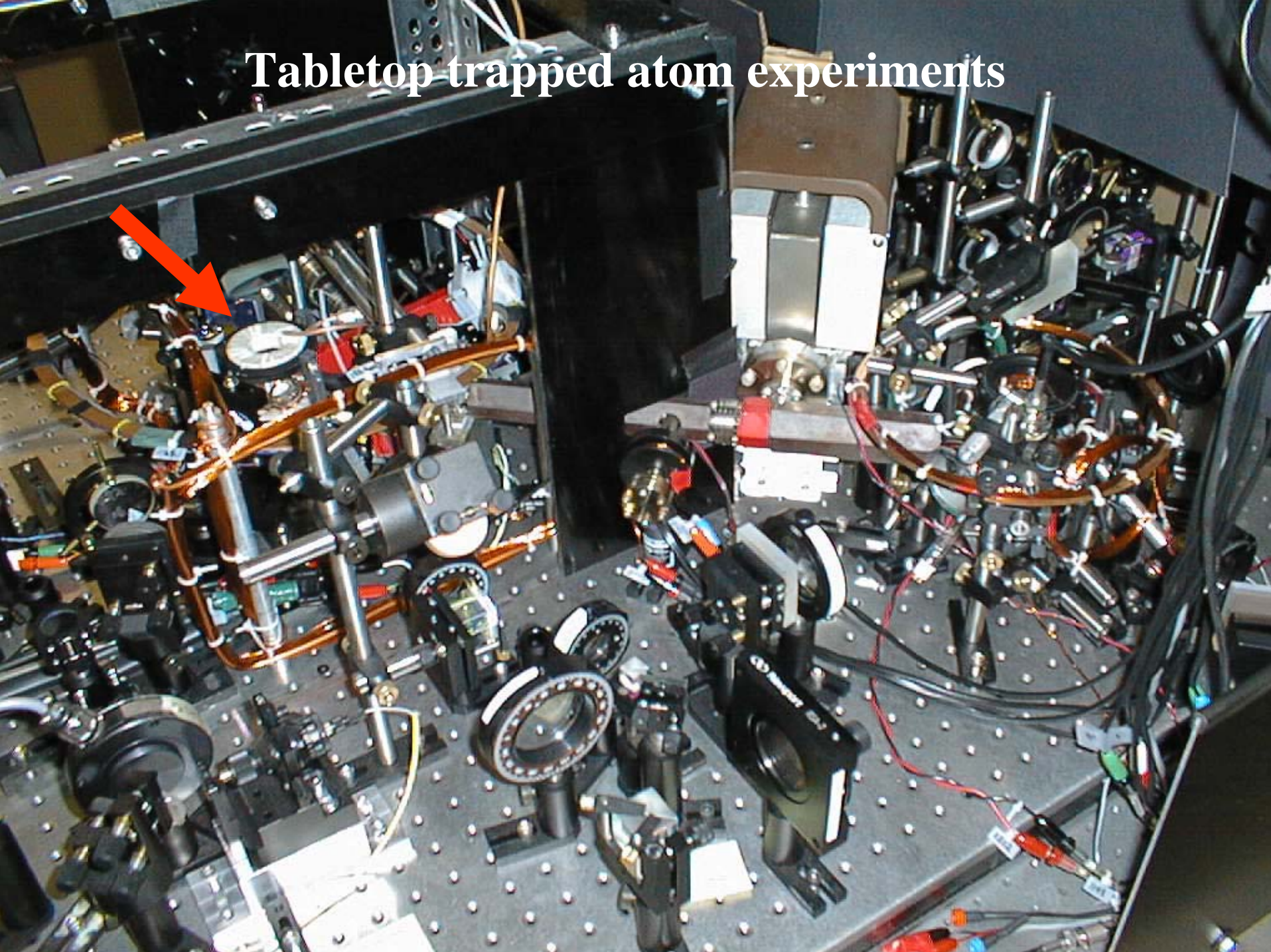
${}^{86}\text{Rb}$ 2- 18.6d

${}^{132}\text{Cs}$ 2+ 6.5d

${}^{134}\text{Cs}$ 4+ 2.06y

${}^{208}\text{Fr}$ 7+ 59.1s

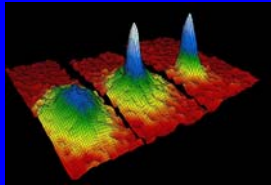
Tabletop-trapped atom experiments



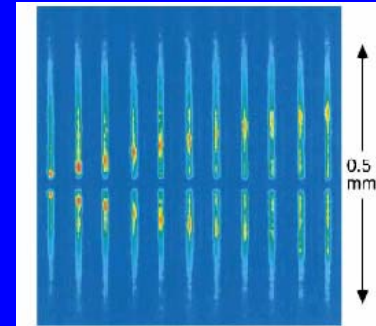
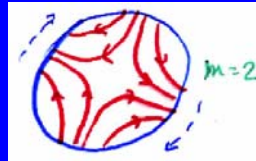
Early days of ultracold trapped atomic gases

≥ 1995 = first Bose condensation of ^{87}Rb , ^{23}Na and ^7Li

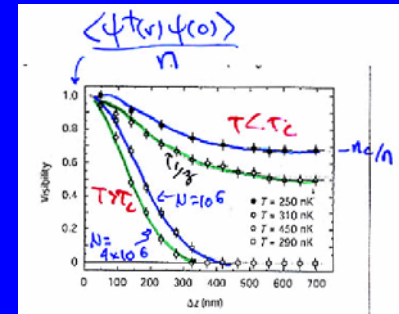
*Structure of condensate.



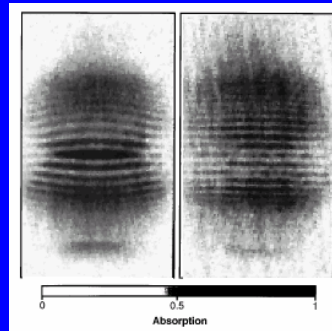
*Elementary modes: breathing, quadrupole, short wave sound, ...



*1, 2 and 3 body correlations \Rightarrow evidence for BEC rather than simply condensation in space.



*Interference of condensates.



Primarily described in terms of mean field theory – Gross-Pitaevskii eq.

$$i\hbar \partial \psi(\mathbf{r}, t) / \partial t = [-\hbar^2 \nabla^2 / 2m + V(\mathbf{r}) + g|\psi(\mathbf{r}, t)|^2] \psi(\mathbf{r}, t)$$

Newer directions in ultracold atomic systems, I

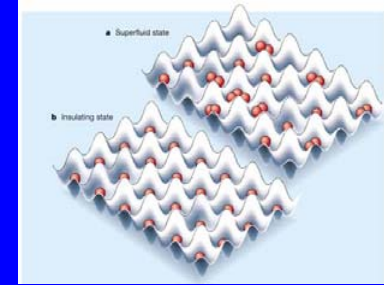
Strongly correlated systems

- * **Rapidly rotating bosons:** how do many-particle Bose systems carry extreme amounts of angular momentum?
- **Trapping and cooling clouds of fermionic atoms**
 - Degenerate Fermi gases and molecular states
 - BCS pairing => new superfluid
 - Crossover from BEC of molecules to BCS paired state
- * **Physics in the strong interaction limit:**
 - scale-free regime where $r_0 \ll n^{-1/3} \lesssim a$
 - r_0 = range of interatomic potential \sim few Å
 - n = particle density
 - a = s-wave scattering length
 - Realize through **atomic Feshbach resonances**

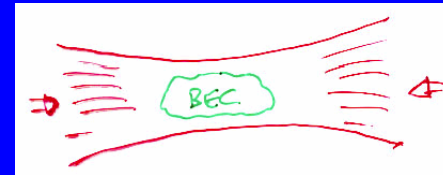
Newer directions in ultracold atomic systems, II

Novel systems

* **Physics in optical lattices:** Mott transition from superfluid to insulating states; low dimensional systems; 2D superfluids



* **Spinor gases:** trapped by laser fields. Physics of spin degrees of freedom
Fragmented condensates



* **Mixtures of bosons and fermions**

* **Ultracold molecules:**

coherent mixtures of atoms and molecules,

e.g., ^{87}Rb atoms and $^{87}\text{Rb}_2$ molecules;

heteronuclear molecules: $^6\text{Li}+^{23}\text{Na}$, $^{40}\text{K}+^{87}\text{Rb}$

Future applications:

Trapped ions for
quantum computing

Slow light

Atom lithography

Matter lasers



Common problems of cold atom and high energy nuclear physics:

Small clouds with many degrees of freedom $\sim 10^4$ - 10^7

Strongly interacting systems

Infrared (long wavelength) problems in qcd and condensed bosons

Recent connections:

Crossover: BEC \Leftrightarrow BCS and hadron \Leftrightarrow quark-gluon plasma

Viscosity: heavy-ion elliptic flow \Leftrightarrow Fermi gases near unitarity

Superfluidity and pairing in unbalanced systems:
trapped fermions \Leftrightarrow color superconductivity

Ultracold ionized atomic plasma physics

Strong interactions

In quark-gluon plasma,

$$\alpha_s(p) = \frac{g_s^2}{4\pi} = \frac{6\pi}{(33 - 2N_f) \ln(p/\Lambda)}$$

Even at GUT scale, 10^{15}GeV , $g_s \sim 1/2$

$\Lambda \sim 150 \text{ MeV}$

(cf. electrodynamics: $e^2/4\pi = 1/137 \Rightarrow e \sim 1/3$)

QGP is always strongly interacting

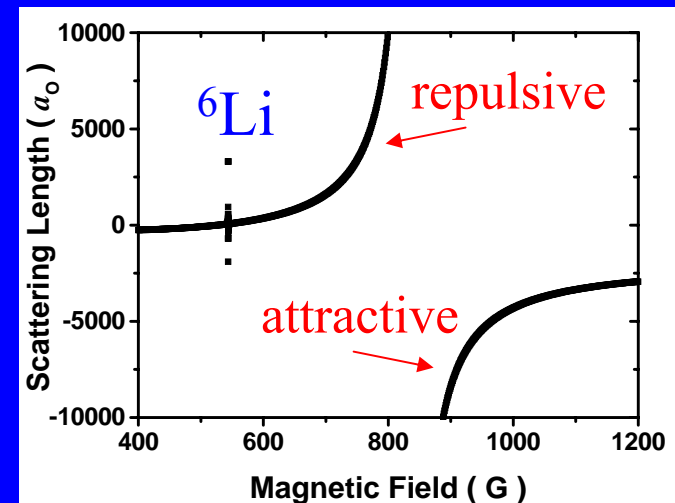
In cold atoms, effective atom-atom interaction is short range and s-wave:

$$V(\mathbf{r}_1 - \mathbf{r}_2) = (4\pi\hbar^2 a/m) \delta(\mathbf{r}_1 - \mathbf{r}_2)$$

a = s-wave atom-atom scattering length.

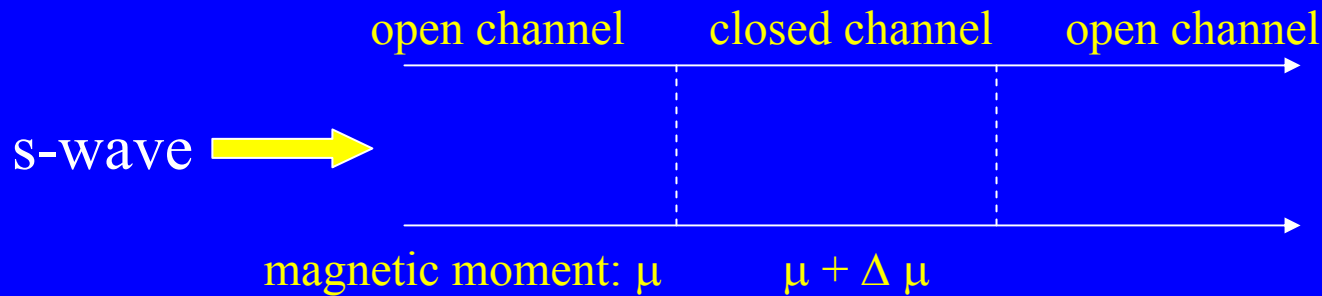
Cross section: $\sigma = 8\pi a^2$

Go from weakly repulsive to strongly repulsive to strongly attractive to weakly attractive by dialing external magnetic field through **Feshbach resonance**.



Resonance at $B = 830 \text{ G}$

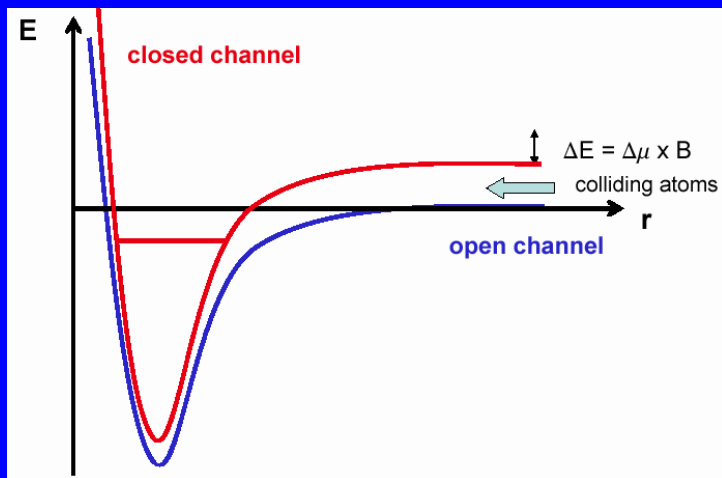
Feshbach resonance in atom-atom scattering



$$\text{Scattering amplitude} \propto \frac{|M|^2}{E_c - E_0}$$

$$E_c - E_0 \sim \Delta\mu B + \dots$$

Low energy scattering dominated by bound state closest to threshold

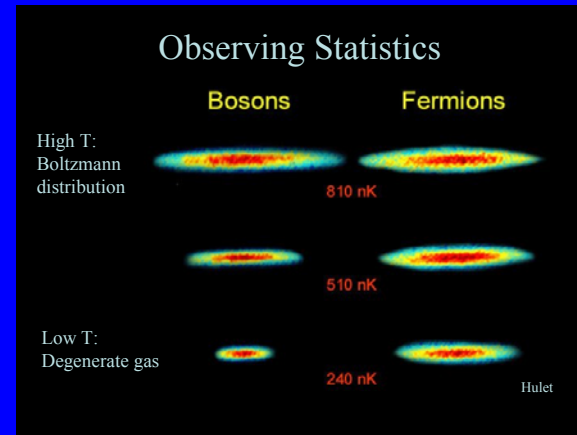


Adjusting magnetic field, B , causes level crossing and resonance, seen as divergence of s-wave scattering length, a :

$$a(B) = a_{bg} \left(1 - \frac{\Delta}{B - B_{Feshbach}} \right)$$

Degenerate ultracold atomic Fermi gases

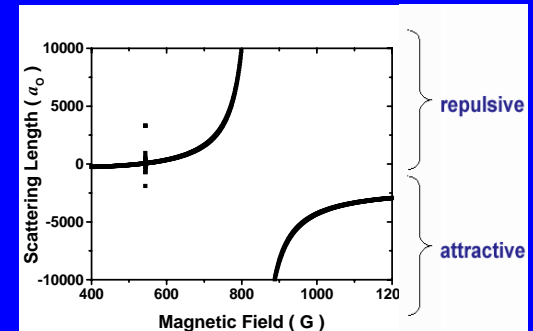
Produce trapped degenerate Fermi gases: ${}^6\text{Li}$, ${}^{40}\text{K}$



${}^7\text{Li}$ vs. ${}^6\text{Li}$

Increase attractive interaction with Feshbach resonance

At resonance have “unitary regime,”
force range \ll interparticle spacing \ll scattering length,
only relevant length scale is the interparticle spacing.



At temperatures ~ 0.2 of the degeneracy temperature (T_f), create BCS paired superfluids

Both systems scale-free in strongly coupled regime

$$F_{\text{qgp}} \sim \text{const } n_{\text{exc}}^{4/3} \quad E_{\text{cold atoms}} \sim \text{const } n^{2/3}/m$$

In cold atoms near resonance only length-scale is density.
No microscopic parameters enter equation of state:

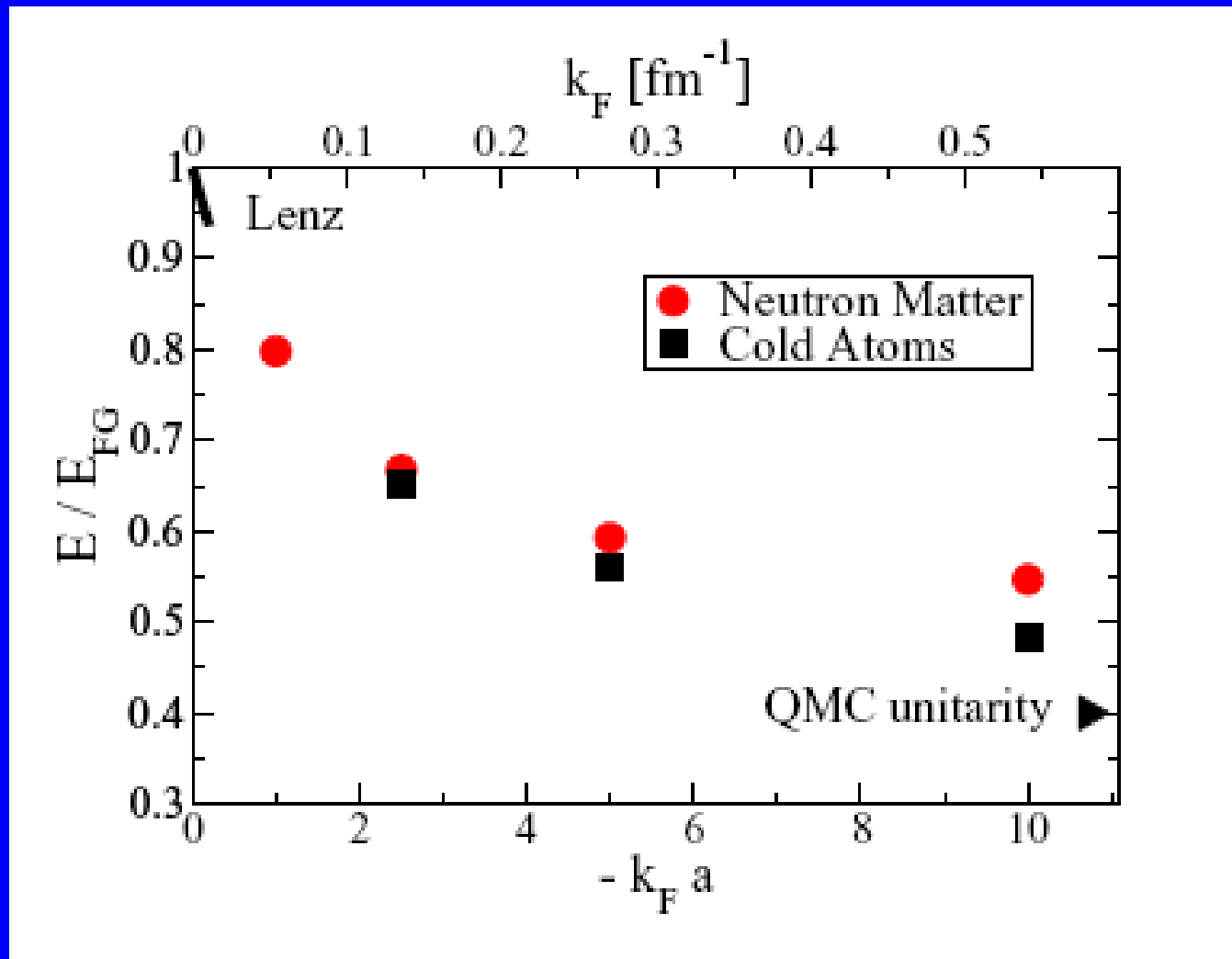
$$\frac{E}{N} = \frac{3}{5} E_F (1 + \beta)$$

β is a universal parameter. No systematic expansion

Theory: $\beta = -0.60$ (0.2) *Green's Function Monte Carlo, Gezerlis & Carlson (2008)*

Experiment: $-0.54(5)$ *Rice*

Remarkably similar behavior of ultracold fermionic atoms and low density neutron matter ($a_{nn} = -18.5$ fm)



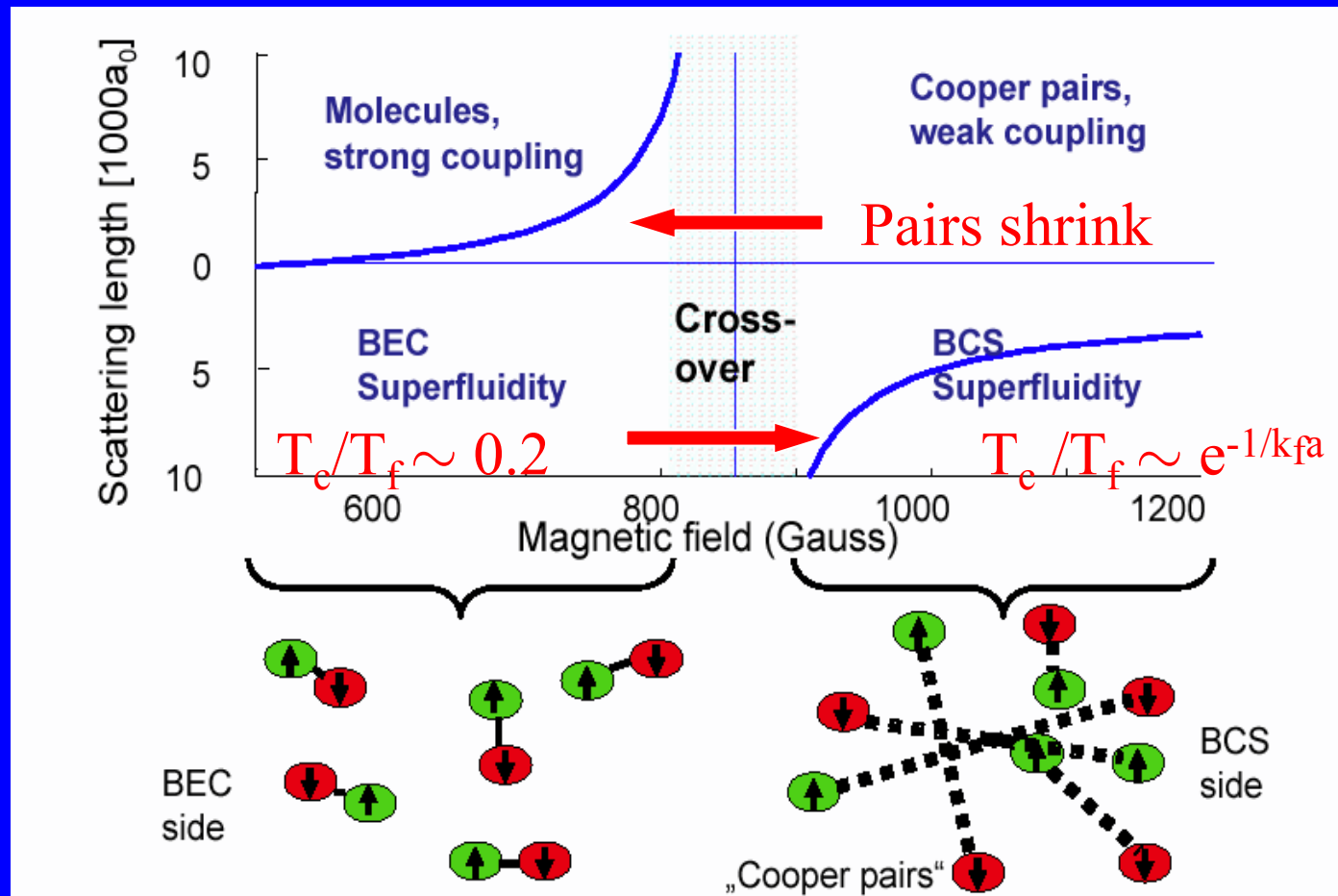
BEC-BCS crossover in Fermi systems

Continuously transform from molecules to Cooper pairs:

D.M. Eagles (1969)

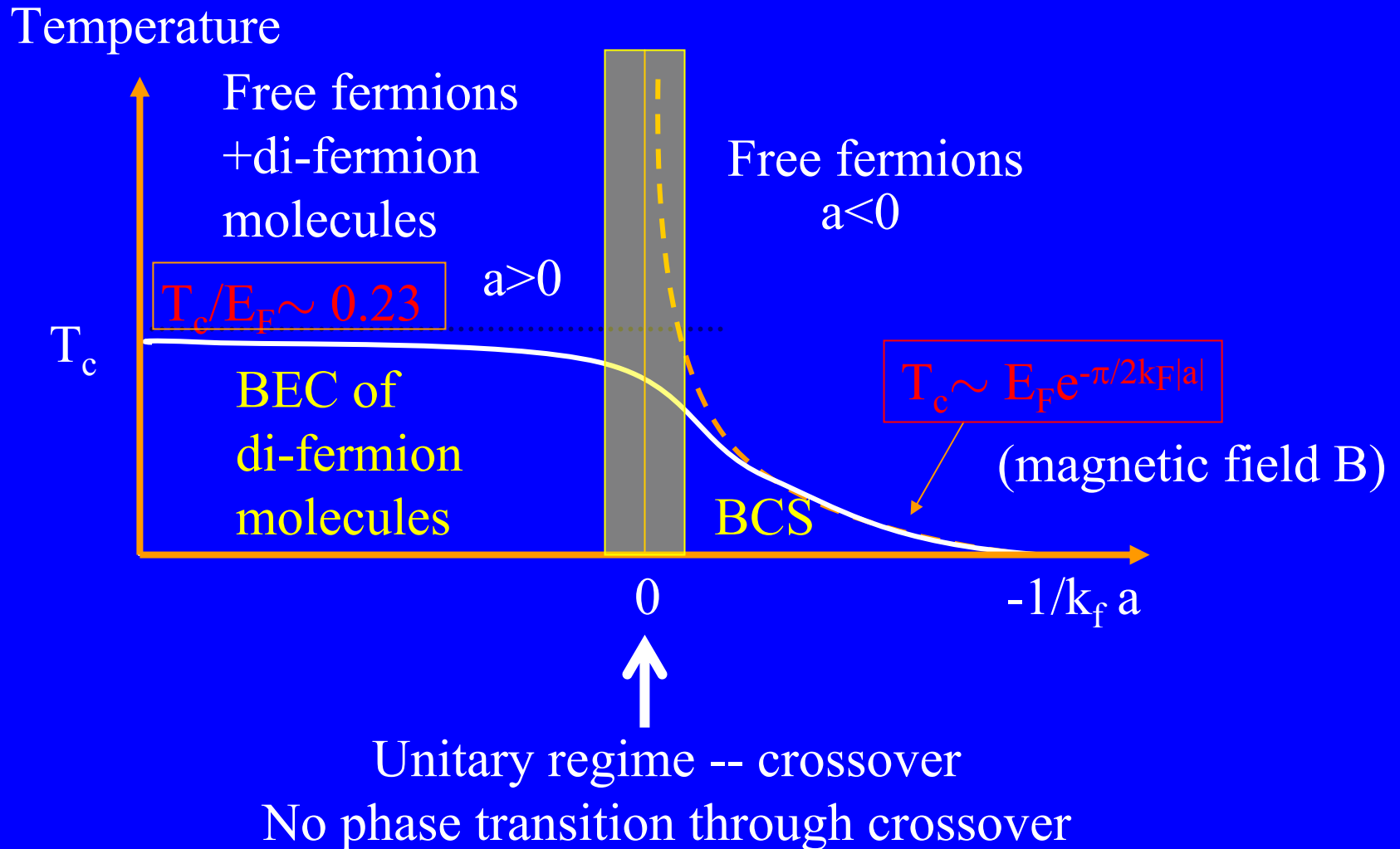
A.J. Leggett, J. Phys. (Paris) C7, 19 (1980)

P. Nozières and S. Schmitt-Rink, J. Low Temp Phys. 59, 195 (1985)



⁶Li

Phase diagram of cold fermions vs. interaction strength



Striking relation of Bose-Einstein condensation and BCS pairing

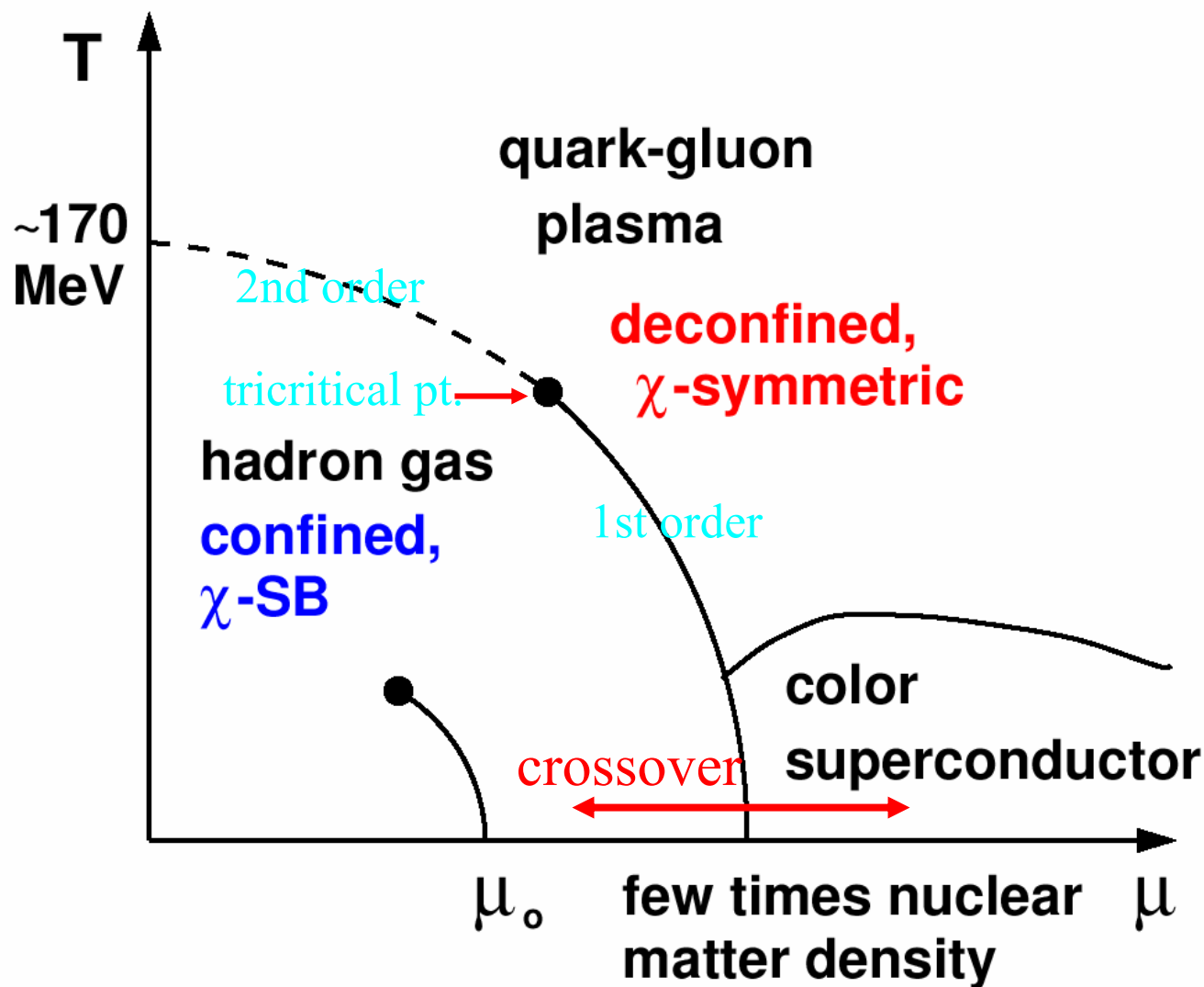
The two phenomena developed along quite different paths

“Our pairs are not localized ..., and our transition is not analogous to a Bose-Einstein condensation.”

BCS paper Oct. 1957

“We believe that there is no relation between actual superconductors and the superconducting properties of a perfect Bose-Einstein gas. The key point in our theory is that the virtual pairs all have the same net momentum. The reason is not Bose-Einstein statistics, but comes from the exclusion principle... .” *Bardeen to Dyson, 23 July 1957*

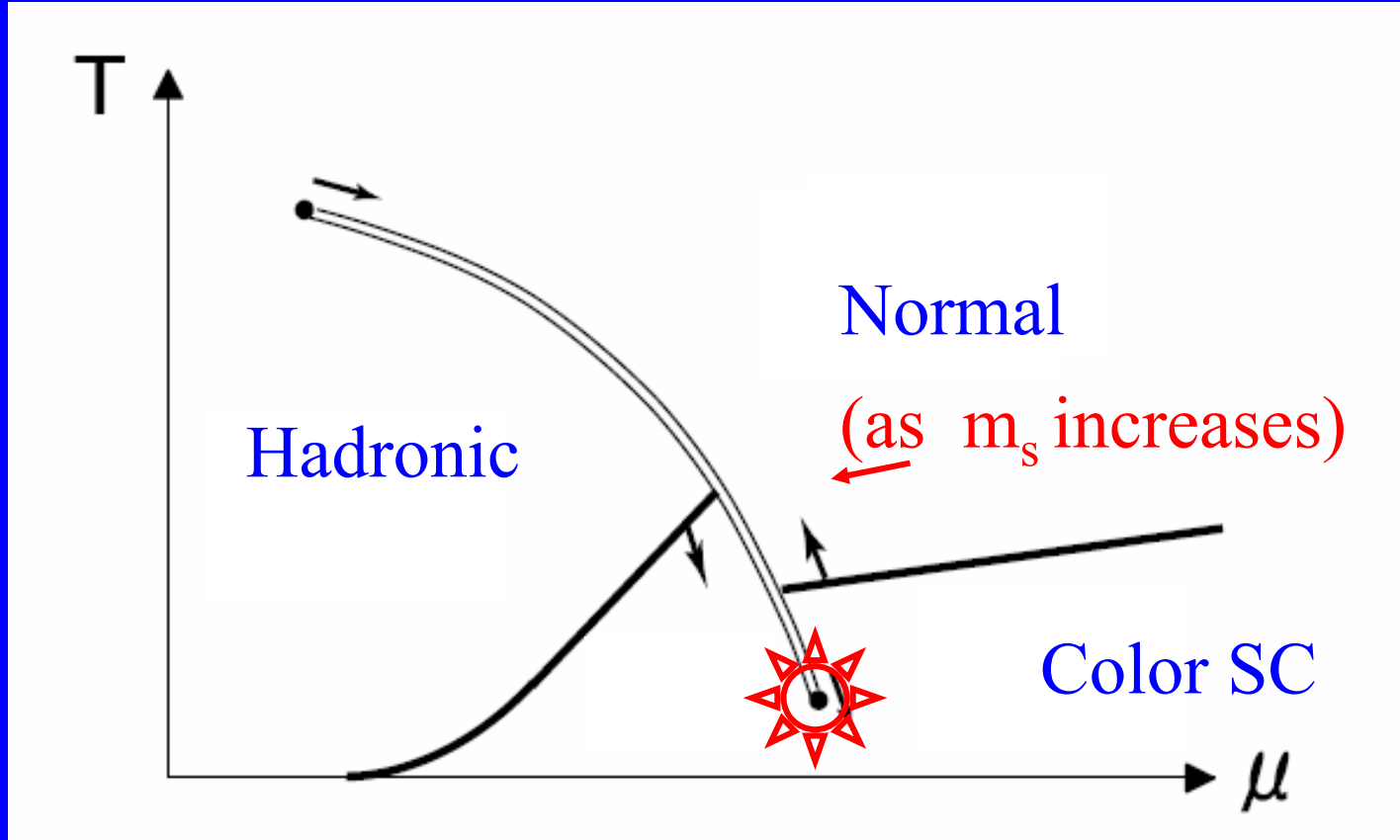
Phase diagram of quark gluon plasma



New critical point in phase diagram:

induced by chiral condensate – diquark pairing coupling
via axial anomaly

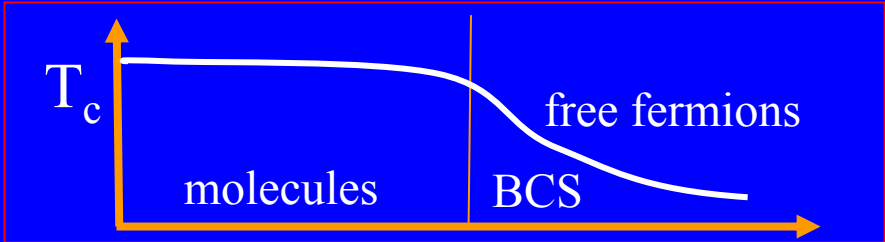
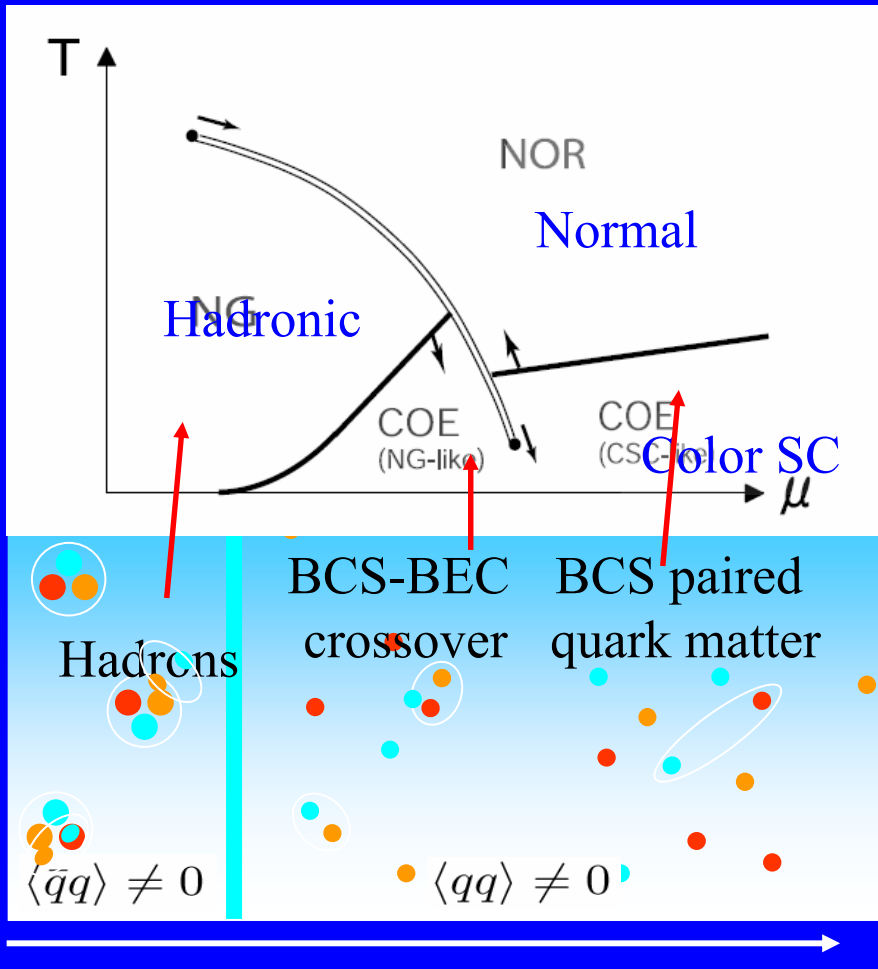
*Hatsuda, Tachibana, Yamamoto & GB, PRL 97, 122001 (2006);
PRD 76, 074001 (2007)*



Deconfinement transition vs. BEC-BCS crossover

In $SU(2)_C$: Hadrons \Leftrightarrow 2 fermion molecules.
 Paired deconfined phase \Leftrightarrow BCS paired fermions

In $SU(3)_C$



Abuki, Itakura & Hatsuda, PRD65, 2002

Limitations of equation of state based on nucleon-nucleon interactions

Accurate for neutron star matter in neighborhood of n_{nm} .

Beyond few n_{nm} :

cannot describe forces in terms of static few-body potentials.

Characteristic range of nuclear forces $\sim 1/2m_{\pi} \Rightarrow$

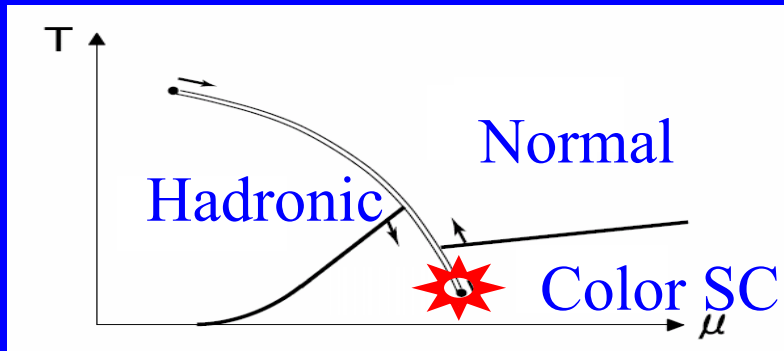
importance of 3 and higher body forces $\sim n/(2m_{\pi})^3 \sim 0.4n/\{\text{fm}\}^{-3}$.

For $n \gg n_{\text{nm}}$, no well defined expansion.

Further hadronic degrees of freedom enter

Cannot describe high density matter in terms of well-defined “asymptotic” laboratory particles.

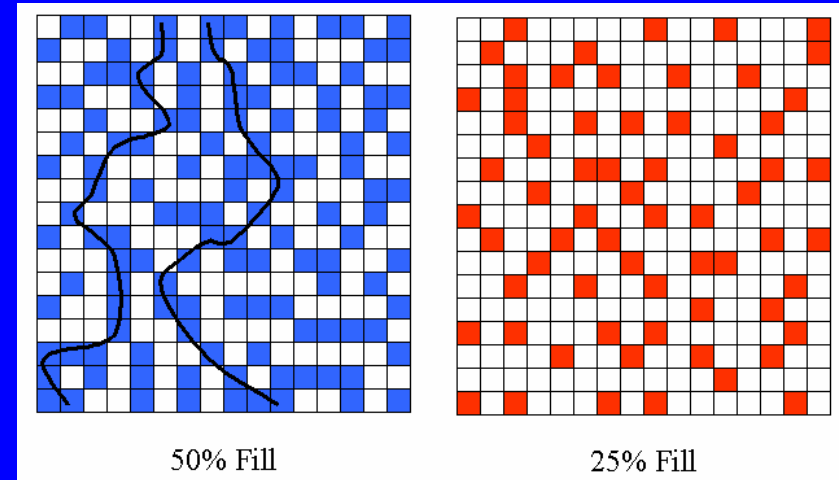
More realistically, expect gradual onset of quark degrees of freedom in dense matter



New critical point suggests transition to quark matter is a crossover at low T

Consistent with percolation picture, that as nucleons begin to overlap, quarks percolate [GB, *Physica* (1979)] :

$$n_{\text{perc}} \sim 0.34 (3/4\pi r_n^3) \text{ fm}^{-3}$$

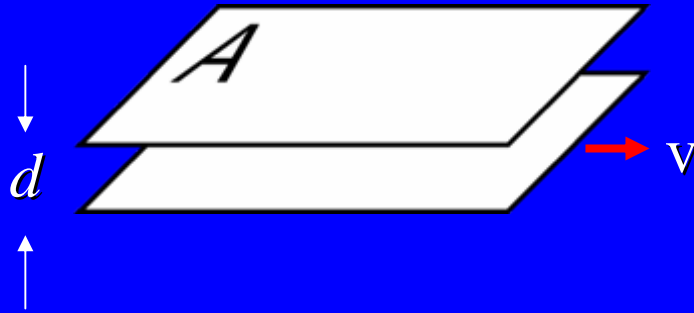


Quarks can still be bound even if deconfined.



Viscosity in elliptic flow in heavy ion collisions and in Fermi gases near unitarity

Strong coupling leads to low first viscosity η ,
seen in expansion in both systems



Shear viscosity η :

$$F = \eta A v / d$$

Stress tensor

$$T_{diss}^{ij} = \eta \left(\frac{\partial v_i}{\partial x^j} + \frac{\partial v_j}{\partial x^i} - \frac{2}{3} \delta_{ij} \nabla \cdot v \right) + \zeta \delta_{ij} \nabla \cdot v$$

First viscosity

$$\eta \sim \rho \bar{v}^2 \tau \sim \frac{1}{|M|^2}$$

$\tau =$ scattering time

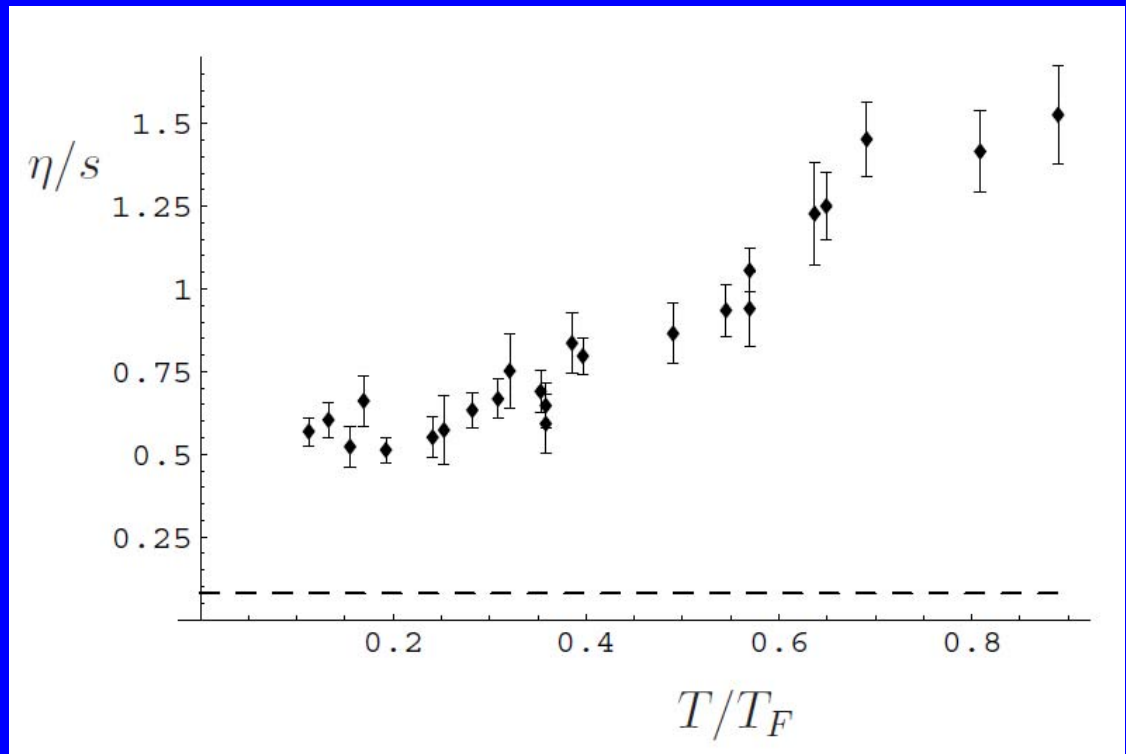
Strong interactions \Rightarrow small η

Viscosity extracted from radial breathing mode

Expt: J. Kinast, A. Turlapov, J.E. Thomas, PRL 94, 170404 (2005)

Theory: T. Schaefer, Phys. Rev. A 76, 063618 (2007)

Ratio of shear viscosity to entropy density ($\hbar=1$)



Temperature/ Fermi temperature

Strongly coupled ${}^6\text{Li}$ expansion

100 μs

200 μs

400 μs

600 μs

800 μs

1000 μs

1500 μs

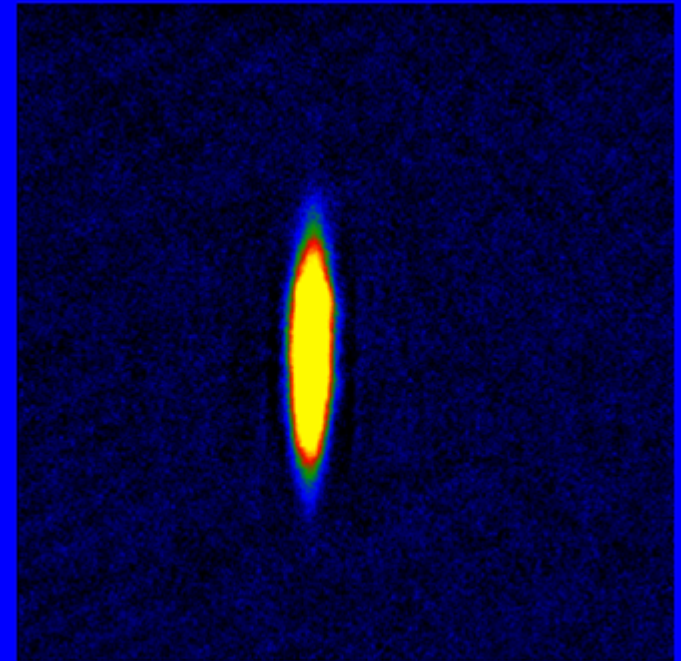
2000 μs

Free Expansion:

K. M. O'Hara, S. L. Hemmer, M. E. Gehm, S. R. Granade, and J. E. Thomas, Science Dec 13 2002: 2179

Turn off trap: cloud expands

Compare with
expansion of weakly
coupled system \rightarrow



Strongly coupled ${}^6\text{Li}$ expansion

Free Expansion:

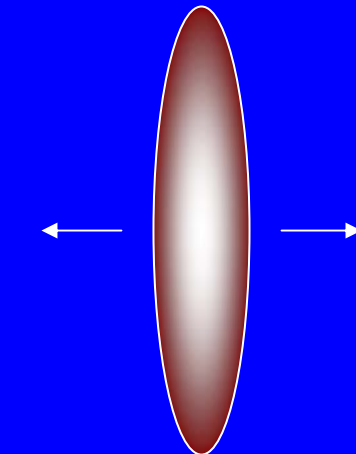
K. M. O'Hara, S. L. Hemmer, M. E. Gehm, S. R. Granade, and J. E. Thomas, Science Dec 13 2002: 2179

Turn off trap: cloud expands

Pressure gradient largest in narrow direction

Expands asymmetrically

Similar to elliptic flow in heavy ion collisions



Find equation of state by fitting expansion with **ideal (zero viscosity) hydrodynamics**

100 μs

200 μs

400 μs

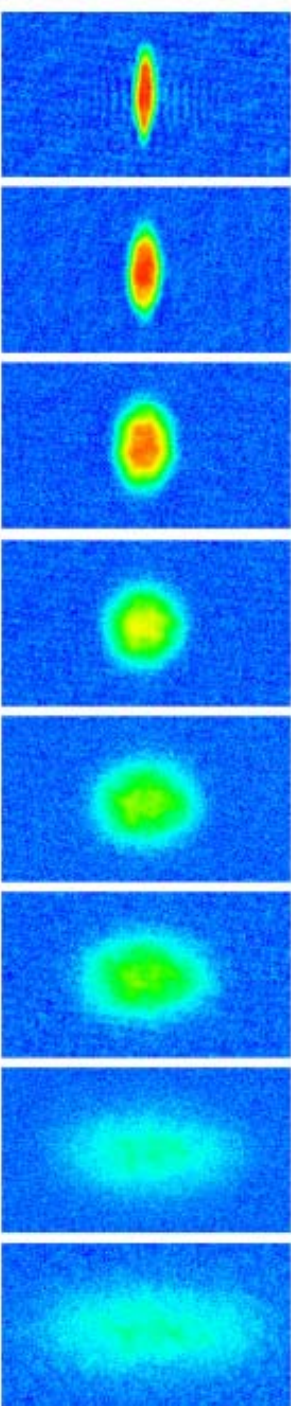
600 μs

800 μs

1000 μs

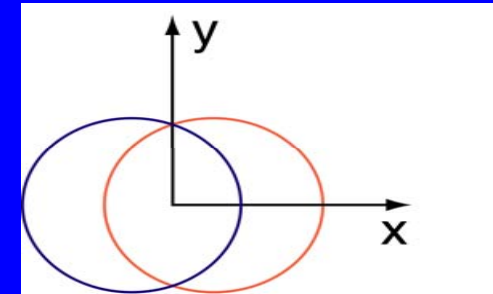
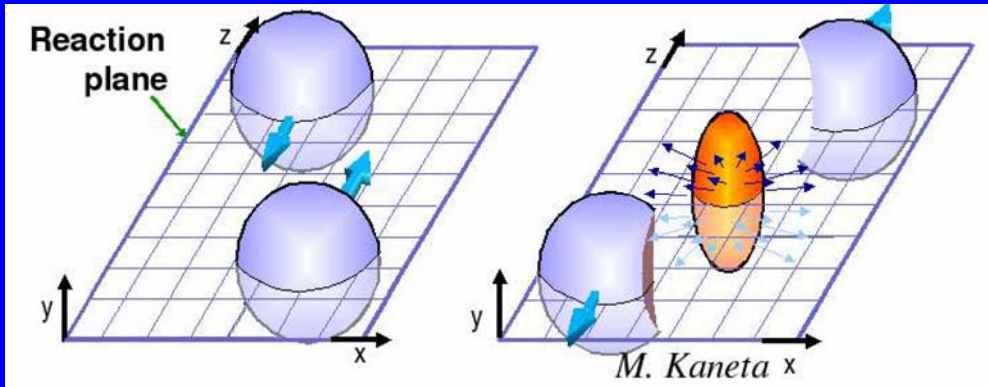
1500 μs

2000 μs

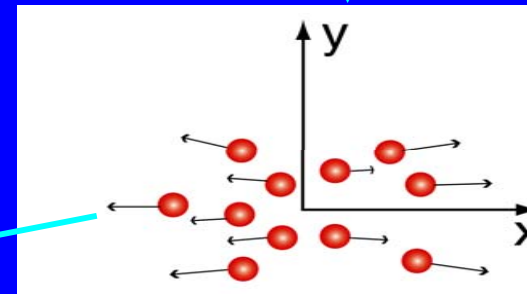


Collectivity: Elliptic flow in non-central collisions:

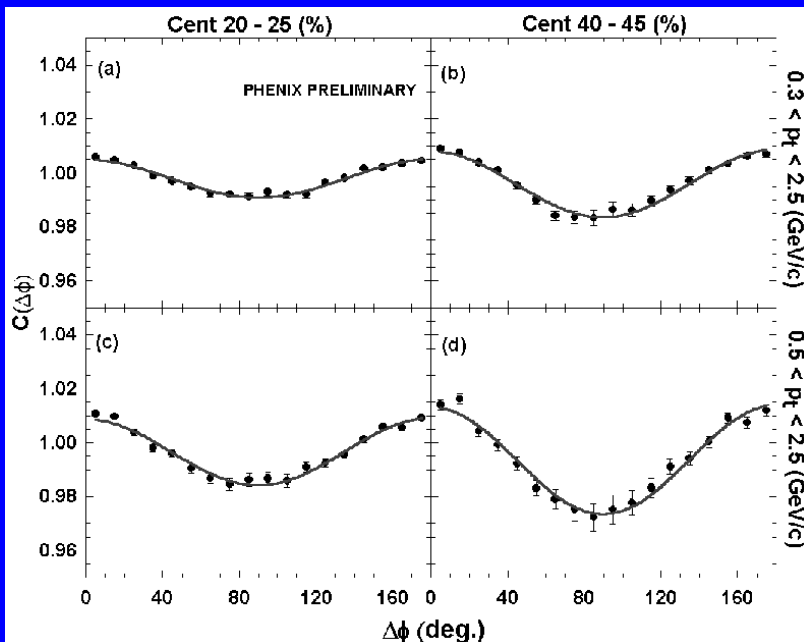
anisotropic in ϕ (= azimuthal angle in x,z plane)



Almond shape
overlap region in
coordinate space



momentum
space

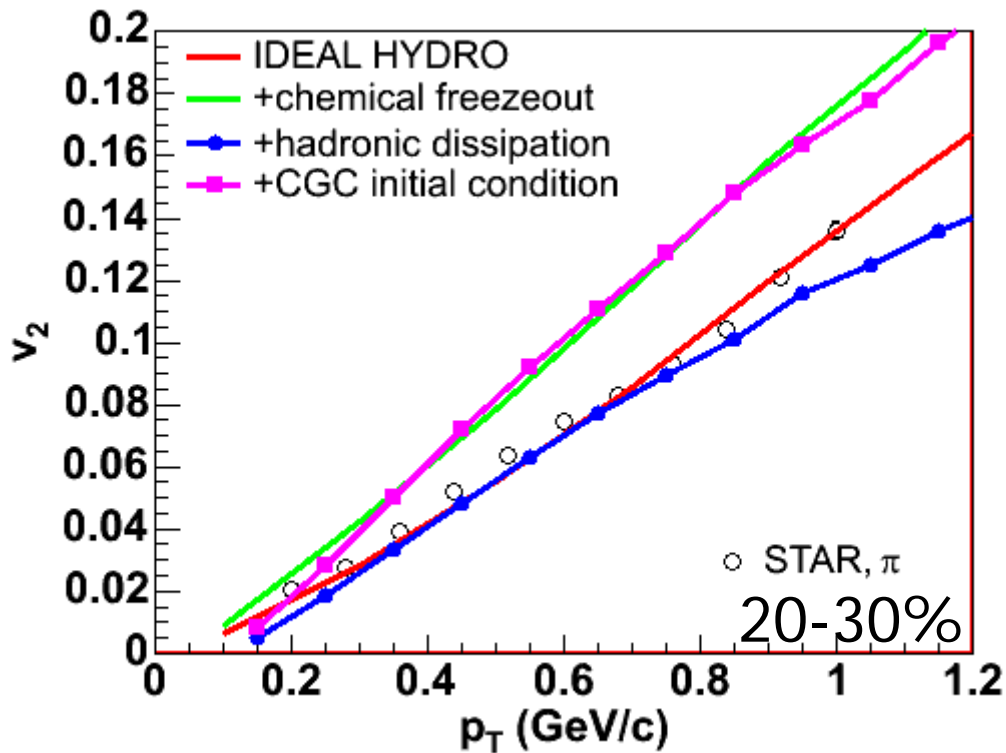


$$dN/d\phi \sim 1 + 2 v_2(p_T) \cos(2\phi) + \dots$$

where p_{\perp} = momentum in x,y plane

Hydrodynamic predictions of $v_2(p_T)$

Elliptic flow \Rightarrow almost vanishing viscosity in quark-gluon plasma



T. Hirano



Conjectured lower bound on ratio of first viscosity to entropy density, s :

$$\eta > \hbar s / 4\pi$$

*Kovtun, Son, & Starinets,
PRL 94, 111601 (2005)*

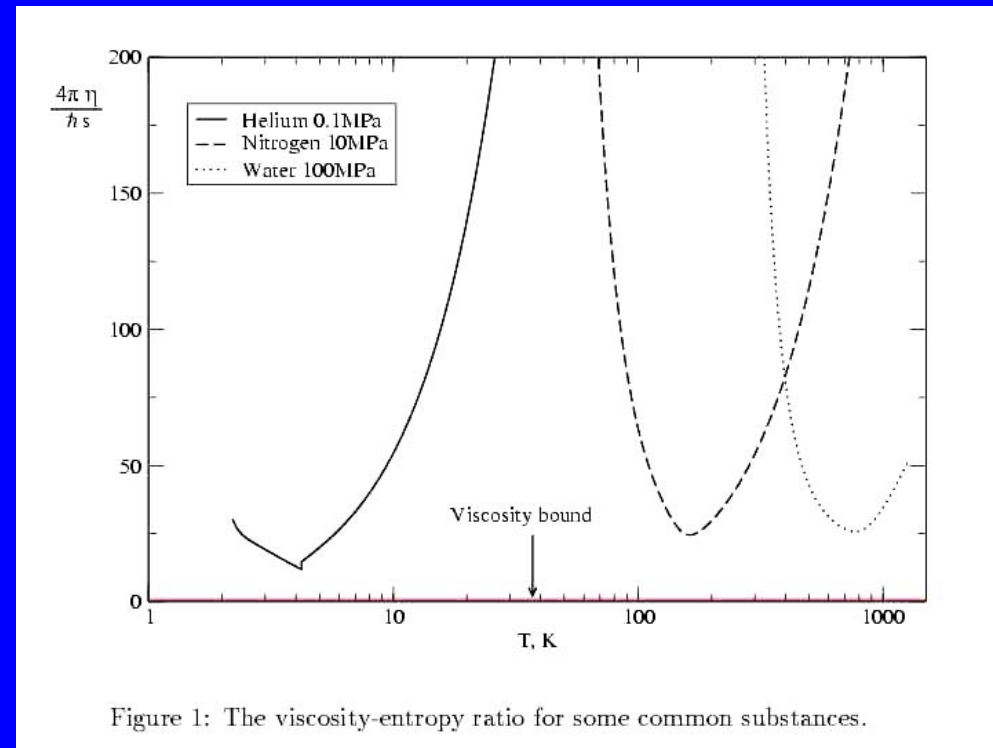


Figure 1: The viscosity-entropy ratio for some common substances.

(Exact result in $\mathcal{N}=4$ supersymmetric Yang-Mills theory in large N_c)

$$\eta \sim n_t m v^2 \tau = n p \lambda, \quad s \sim n_t$$

n_t = no. of degrees of freedom producing viscosity

$p = mv =$ mean particle momentum $> \hbar /$ (interparticle spacing)

$\lambda =$ mean free path

Bound \Leftrightarrow mean free path $>$ interparticle spacing

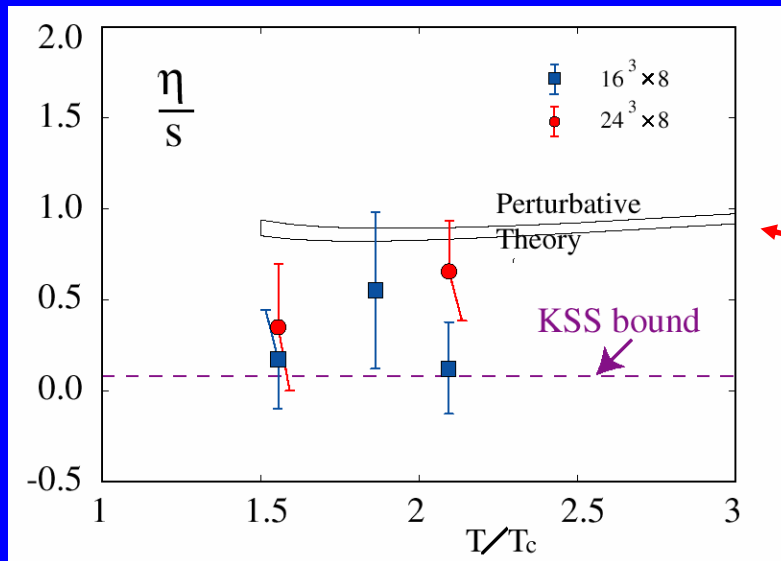
Strongly coupled systems approach viscosity lower bound

Cold fermions in normal state at unitarity:

$$\eta \sim n \hbar T/T_f, \quad s \sim n T/T_f \Rightarrow \eta/s \sim \hbar$$

G. Bruun and H. Smith, Phys. Rev. A 75, 043612 (2007)

Lattice calculations of first viscosity in qcd:



Perturbative qcd limit:

$$\eta \sim T^3/(\alpha_s^2 \ln \alpha_s)$$

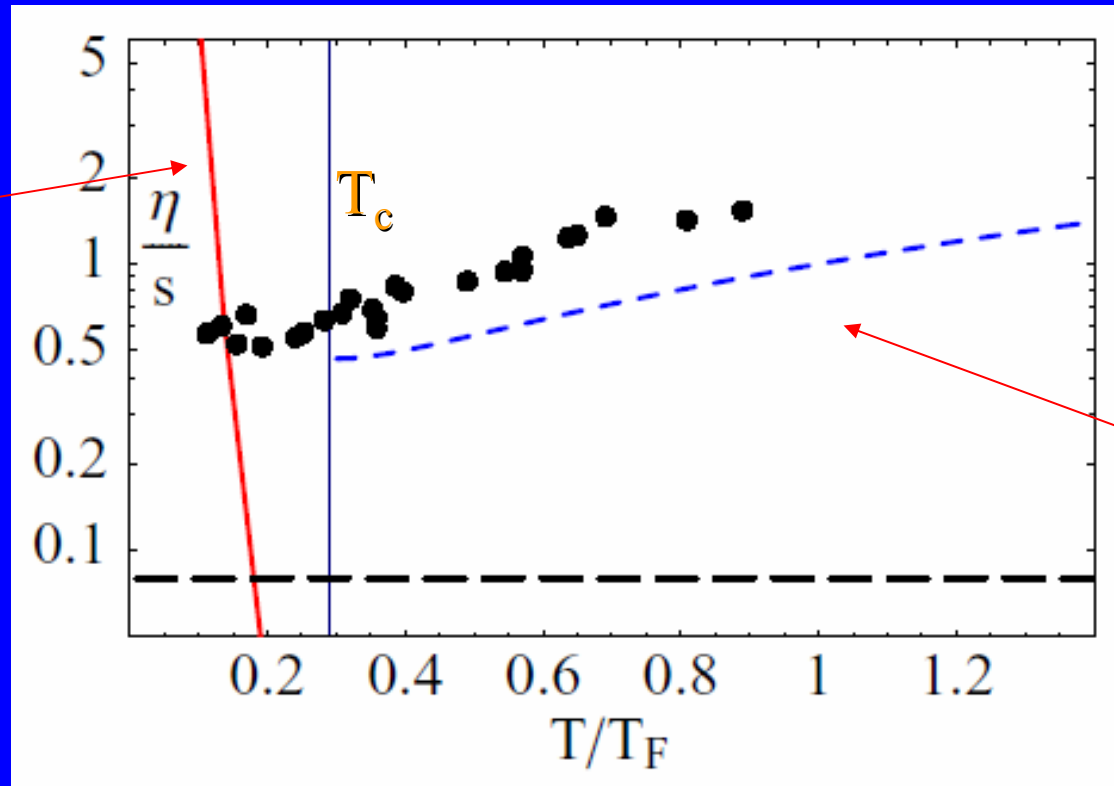
$$\eta/S \sim 1/\alpha_s^2 \ln \alpha_s$$

*GB, Monien, Pethick & Ravenhall,
PRL 64(1990)*

Nakamura & Sakai, hep-lat/0510039

Shear viscosity of Fermi gas at unitarity

G. Rupak & T. Schaefer, PRA 76, 053607 (2007)

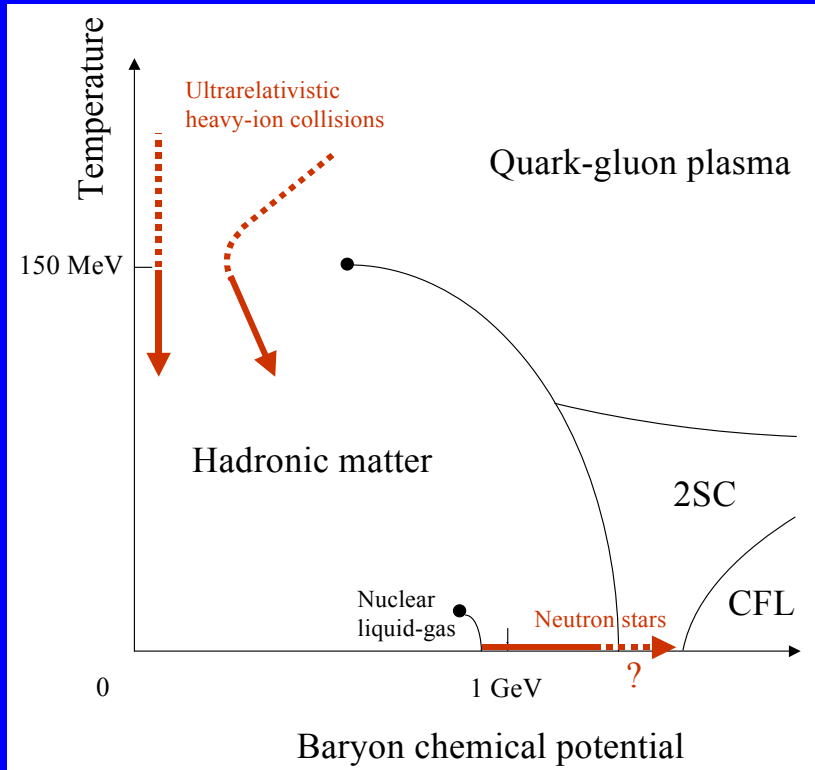


G. M. Bruun & H. Smith, PRA 75, 043612 (2007)

Shear viscosity/ entropy density ratio vs. T/T_F

Color pairing in quark matter

Review: Alford, Rajagopal, Schaefer, & Schmitt, RMP (in press); arXiv:0709.4635

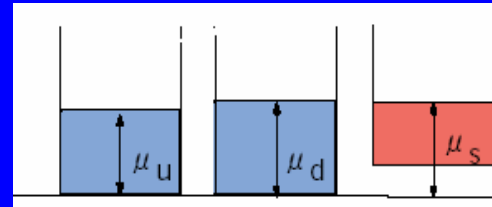


Superfluidity

condensate of paired quarks => superfluid baryon density (n_s)

Color Meissner effects

transverse color fields screened on spatial scale \sim London penetration depth $\sim (\mu/g^2 n_s)^{1/2}$



Two interesting phases:

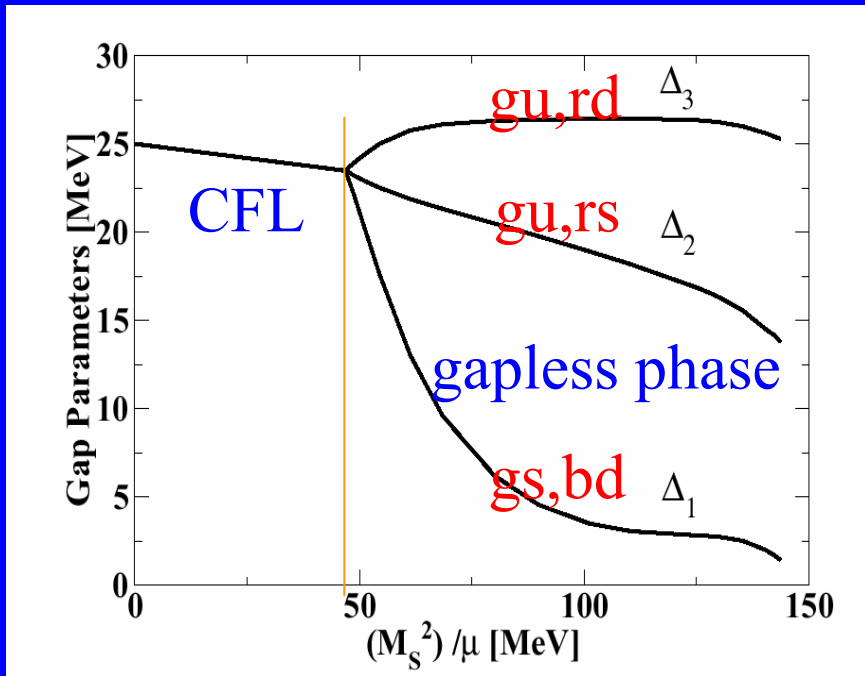
2SC (u,d)



Color-flavor locked (CFL) ($m_u = m_d = m_s$)

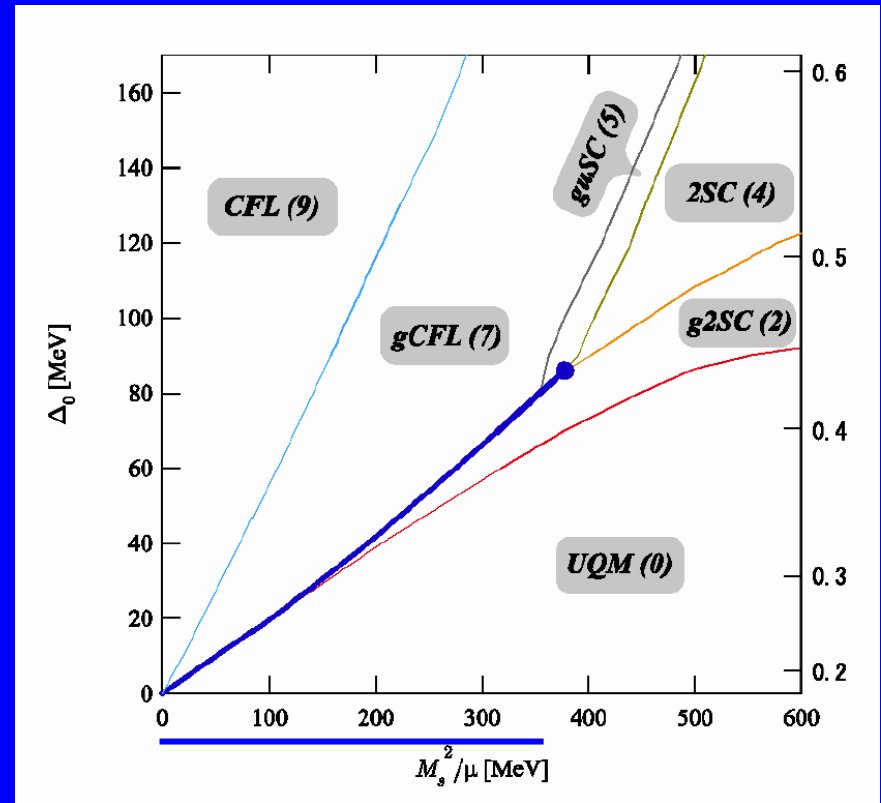


Color superconductor with $m_{\text{strange}} \neq m_{\text{light}}$



Decreasing pairing of strange quarks with increasing m_s

Alford, Kovaris & Rajagopal,
Phys.Rev.Lett. 92 (2004) 222001



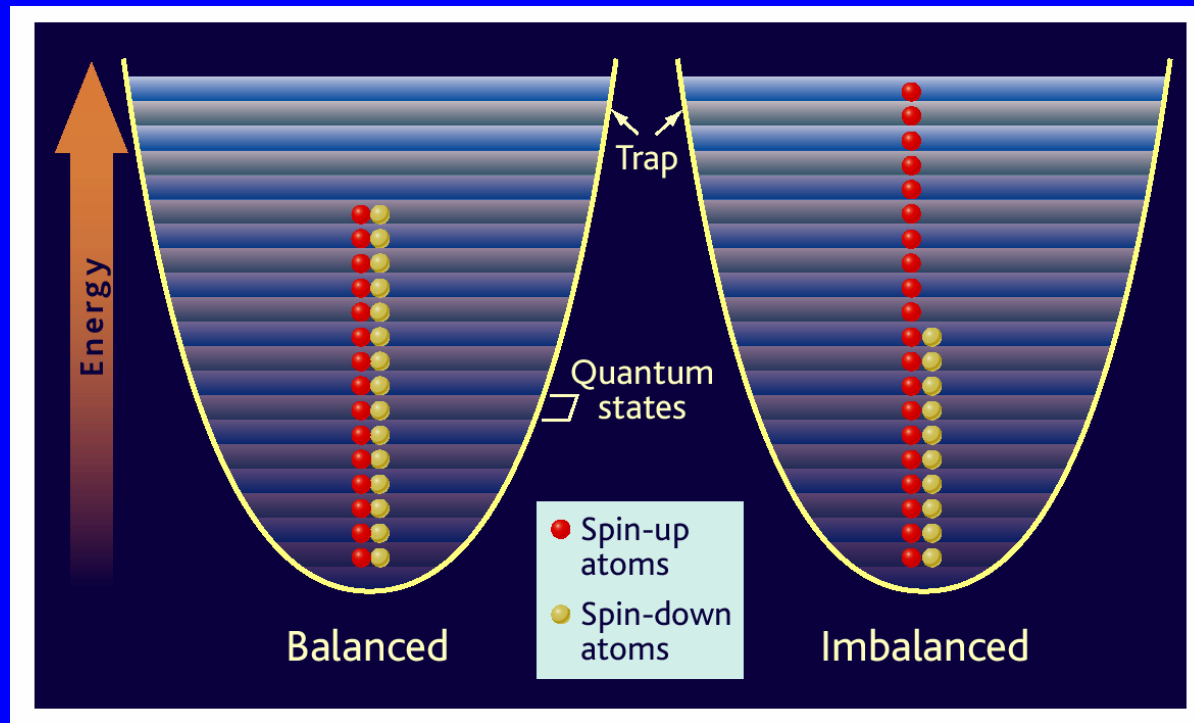
Phase diagram in Δ_{CFL}, m_s^2 plane

Abuki, Kitazawa, & Kunihiro,
PLB 615, 102 (2005)

In gapless phase for unbalanced color superconductors,
Meissner screening length can be imaginary (superfluid mass density < 0)

M. Huang; M. Alford; and collaborators

Superfluidity and pairing for unbalanced systems



Trapped atoms: change relative populations of two states by hand

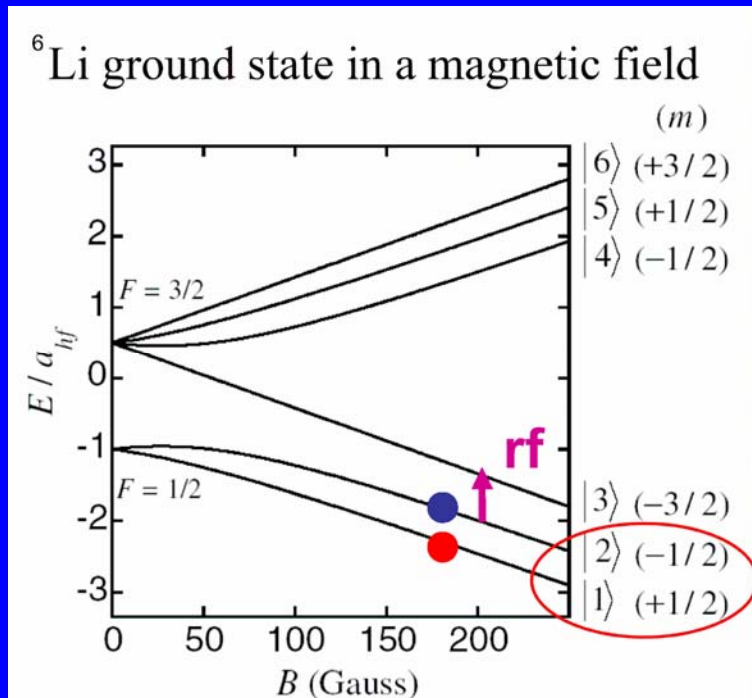
QGP: balance of strange (s) quarks to light (u,d) depends on

ratio of strange quark mass m_s to chemical potential μ (>0)

Experiments on ${}^6\text{Li}$ with imbalanced populations of two hyperfine states, $|1\rangle$ and $|2\rangle$

MIT: Zwierlein et al., *Science* 311, 492 (2006); *Nature* 442, 54 (2006);
Shin, Schnuck, Schirotzek, & Ketterle, arxiv/0709.3027

Rice: Partridge et al., *Science* 311, 503 (2006) cond-mat/0605581

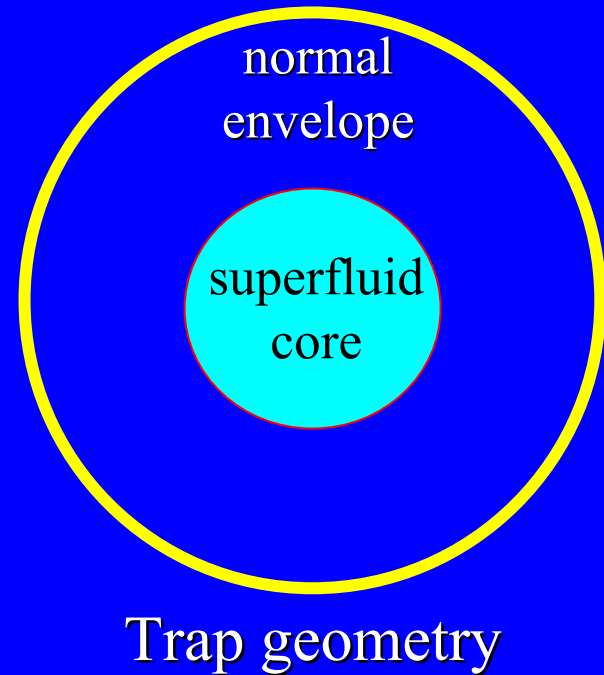
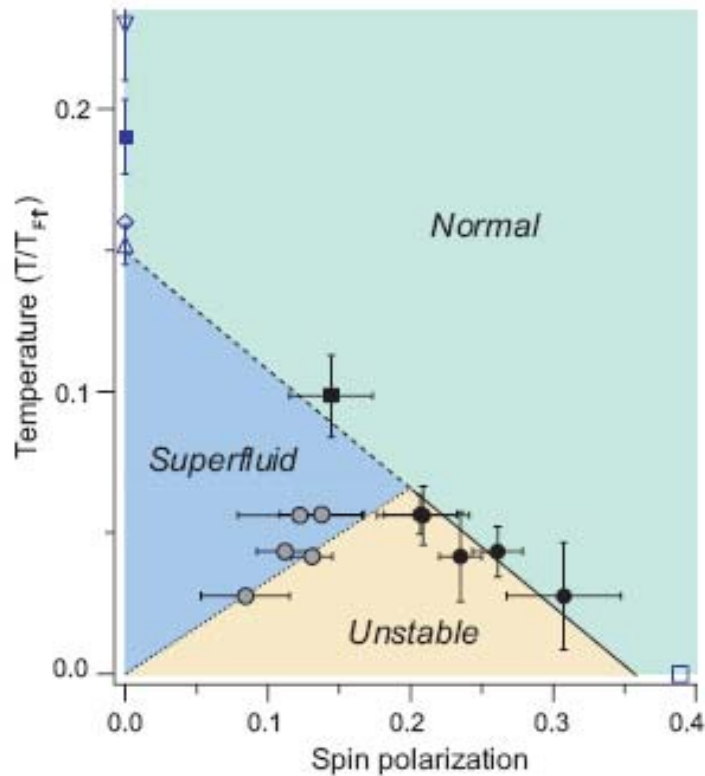


Fill trap with n_1 $|1\rangle$ atoms, and n_2 $|2\rangle$ atoms, with $n_1 > n_2$.

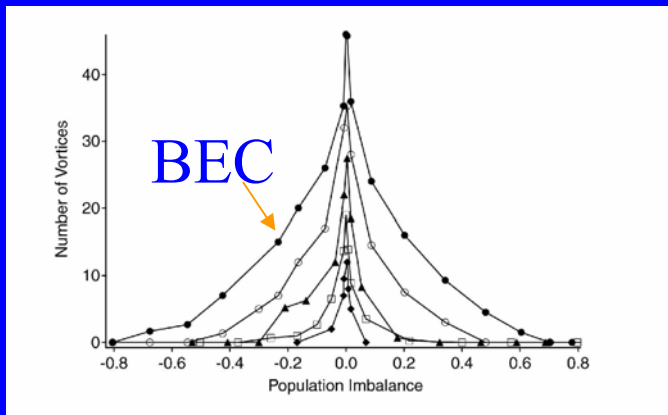
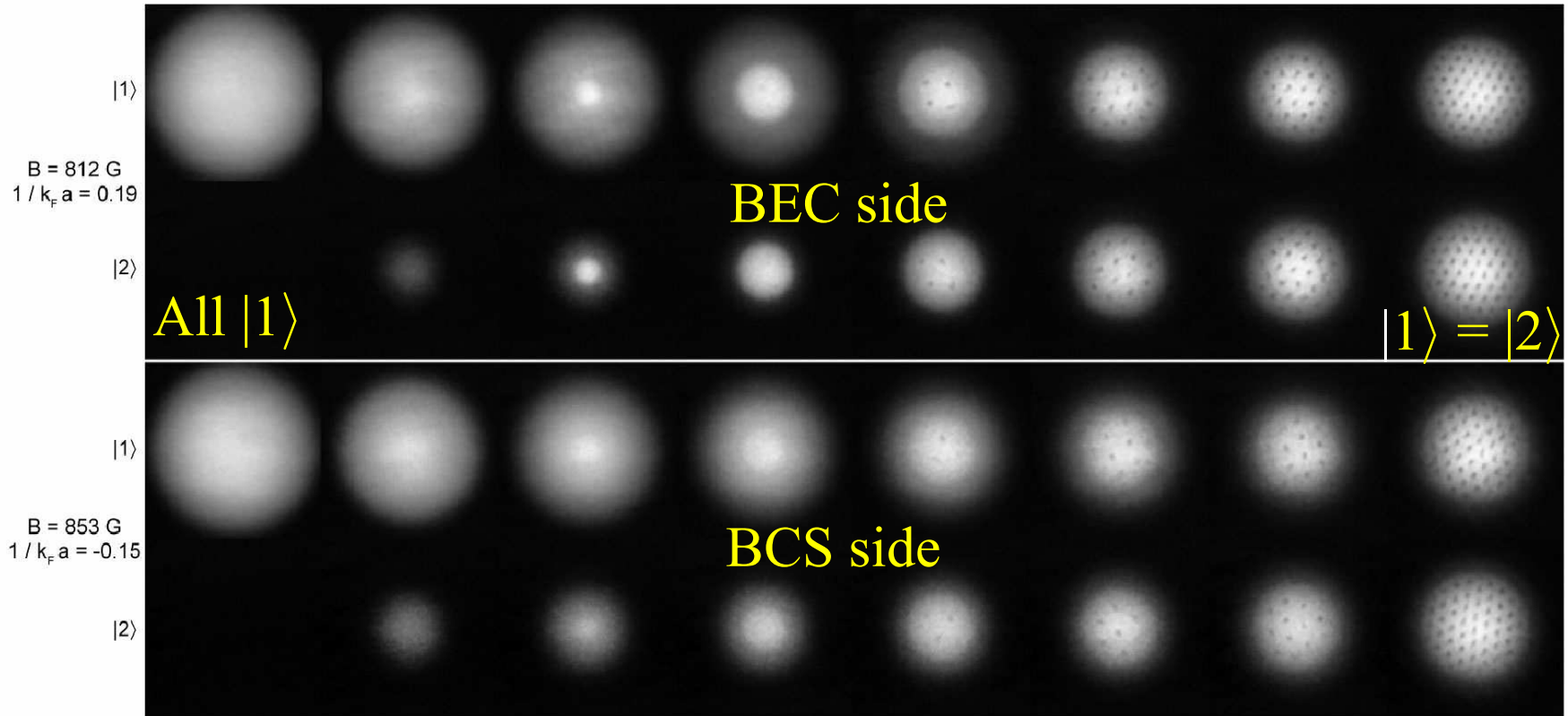
Study spatial distribution, and existence of superfluidity for varying $n_1:n_2$.

Phase diagram of trapped imbalanced Fermi gases

Shin, Schnuck, Schirotzek, & Ketterle, arxiv/0709.3027



Vortices as marker of superfluidity (MIT)



No. of vortices vs. population imbalance

Strongly coupled plasmas: $\Gamma = E_{\text{interaction}} / E_{\text{kinetic}} \gg 1$

Electrons in a metal

$$E_{\text{int}} \sim e^2/r_0 \quad r_0 = \text{interparticle spacing} \sim \hbar / k_f$$

$$E_{\text{ke}} \sim k_f^2/m \Rightarrow \Gamma \sim e^2/\hbar v_f = \alpha_{\text{eff}}$$

$$v_f \sim 10^{-2}-10^{-3}c \Rightarrow \alpha_{\text{eff}} \sim 1-5$$

Dusty interstellar plasmas

Laser-induced plasmas (NIF, GSI)

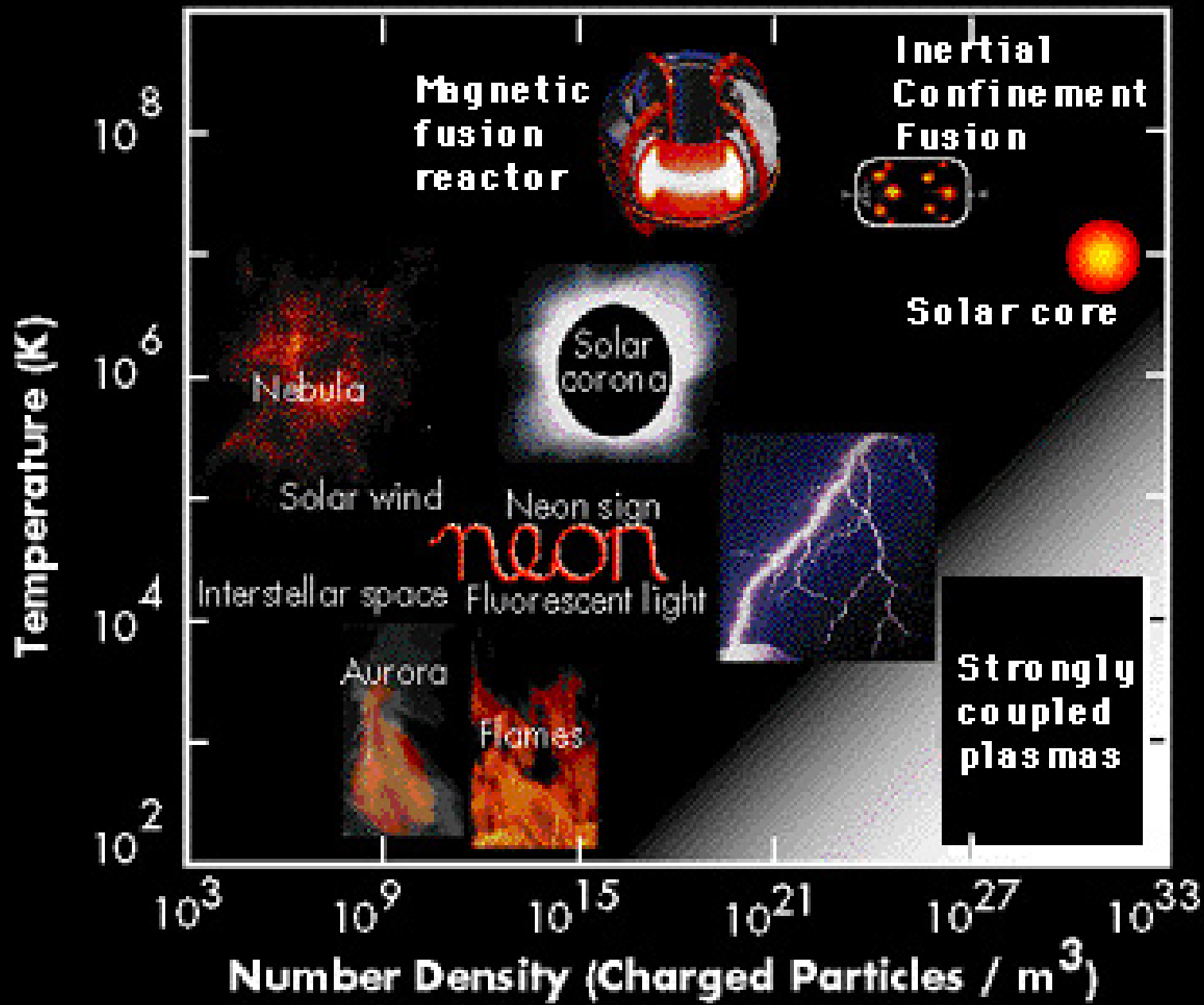
Quark-gluon plasmas

$$E_{\text{int}} \sim g^2/r_0, \quad r_0 \sim 1/T, \quad E_{\text{ke}} \sim T \Rightarrow \Gamma \sim g^2 \gg 1$$

Ultracold trapped atomic plasmas

$$\Gamma \sim n_9^{1/3}/T_K \quad [\text{where } n_9 = n/10^9 \text{ /cm}^3 \text{ and } T_K = (T/1\text{K})]$$

$$\text{Non-degenerate plasma, } E_{\text{ke}} \sim T \Rightarrow \Gamma = E_{\text{int}}/E_{\text{ke}} \sim e^2/r_0 T$$



Ultracold neutral atomic plasmas

Killian, Kulin, Bergeson, Orozco, Orzel, & Rolston, *PRL* 83, 4776 (1999),

Kulin, Killian, Bergeson, & Rolston, *PRL* 85, 318 (2000),

Killian, Chen, Gupta, Laha, Martinez, Mickelson, Nagel, Saenz, & Simien,
Proc. 12th Int. Cong. on Plasma Phys., 2004, physics/0410019,

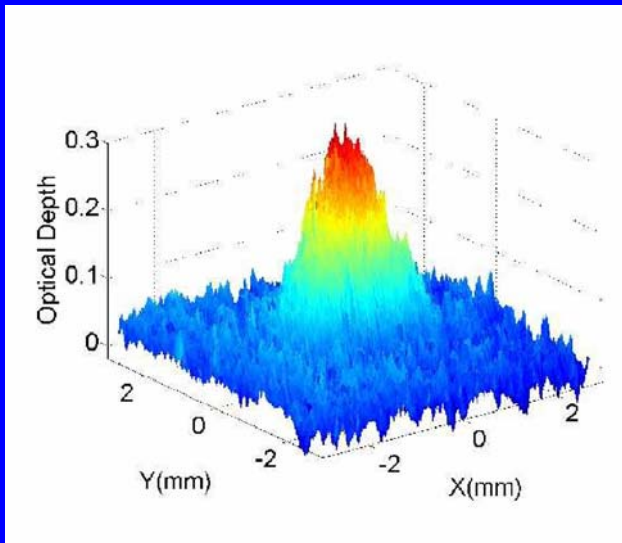
Roberts, Fertig, Lim, & Rolston, physics/0402041.

Produce by photoionizing trapped cold atomic gas., e.g., Xe, Sr.

In Xe, reach

$$T_e = 0.1 - 10^3 \text{ K}, T_{\text{ion}} = 10 \mu\text{K} - 4 \text{ mK}, n = 2 \times 10^9 / \text{cm}^3, N \sim 2 \times 10^5$$

Expand plasma to measure



Optical depth of an Sr plasma

$$N = 7 \times 10^7, n \sim 2 \times 10^{10} / \text{cm}^3$$

Ultracold plasmas analog systems for gaining understanding of plasma properties relevant to heavy-ion collisions:

- kinetic energy distributions of electrons and ions
- modes of plasmas: plasma oscillations
- screening in plasmas
- nature of expansion – flow, hydrodynamical (?)
- thermalization times
- correlations
- interaction with fast particles
- viscosity
- ...

THE END