

# Evolution of the $N=32$ shell closure through mass observables

Erich Leistenschneider

*FRIB / NSCL*

*Michigan State University*



NSCL



FRIB

NUSTAR Annual meeting 2021



U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science

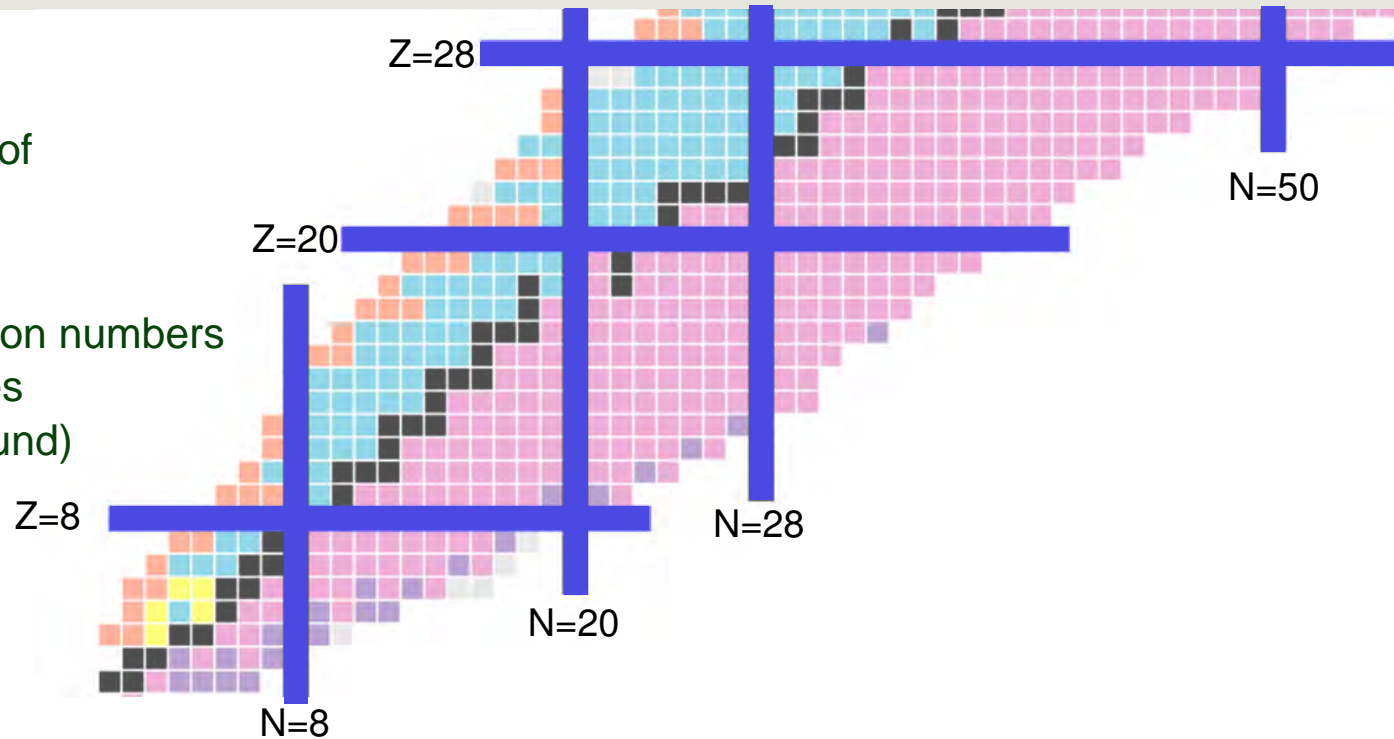
**MICHIGAN STATE**  
UNIVERSITY

# Nuclear Shells

**Backbone** of models of nuclear structure

Nuclei at **magic** nucleon numbers have special properties (e.g. exceptionally bound)

Discovered well over half century ago!

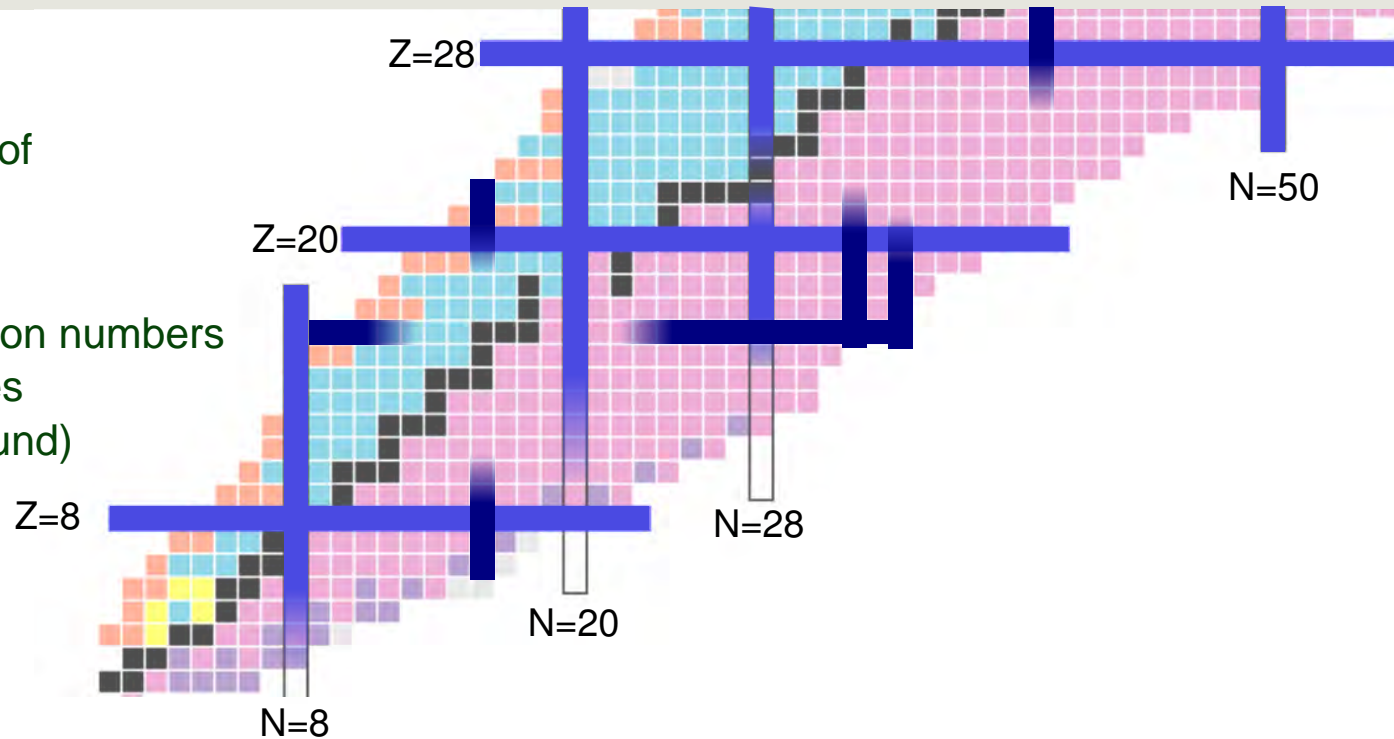


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Shells are **not immutable!**

Several instances of "non-canonical" behavior

Shell evolution is currently one of the most active fields in nuclear structure.

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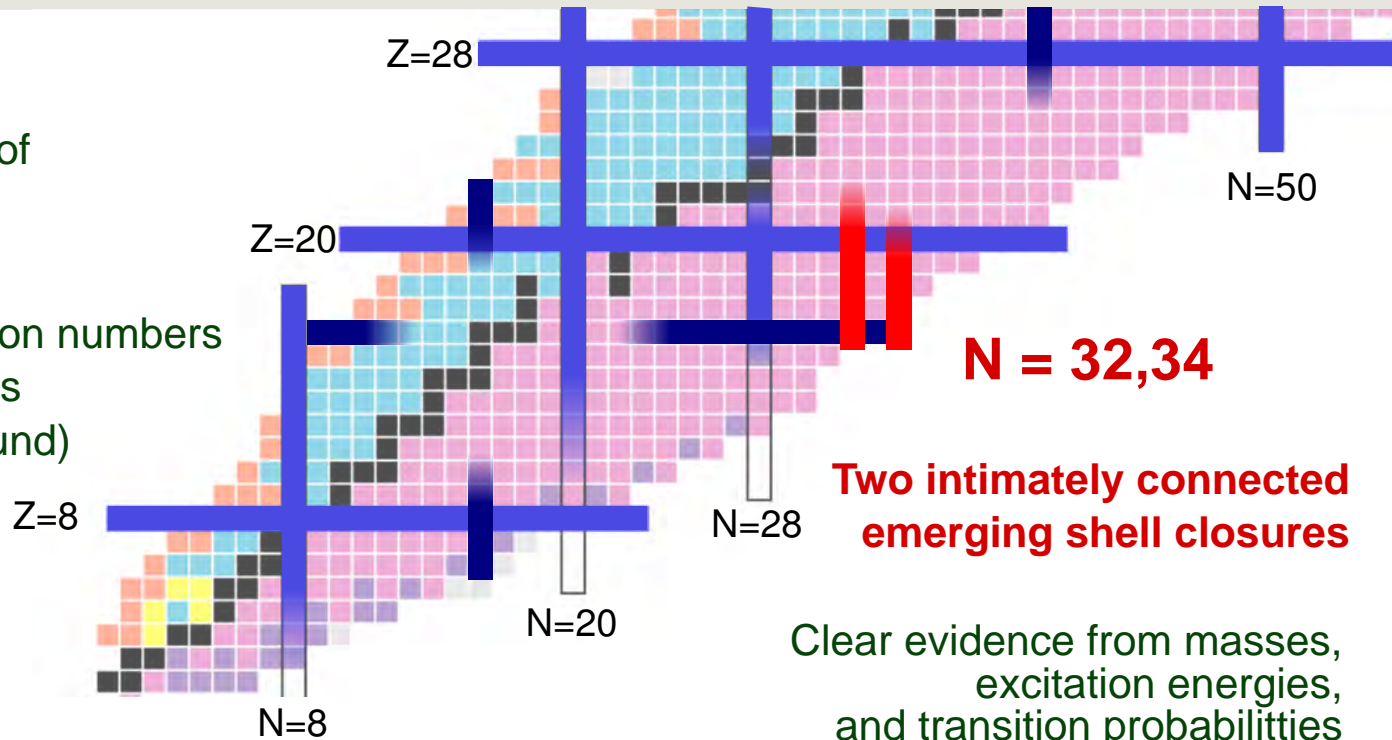
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Clear evidence from masses, excitation energies, and transition probabilities

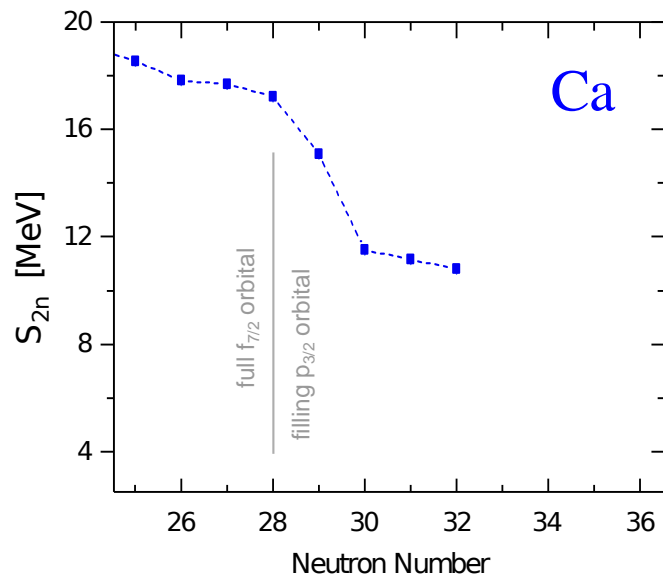
A rich test bench for nuclear theories

# Shell Closures in the Mass Surface

**How to spot:** systematic changes in the binding energy surface

**A common signature:** sudden decreases in 2-neutron separation energy

$$S_{2n}(N,Z) = B(N,Z) - B(N-2,Z)$$

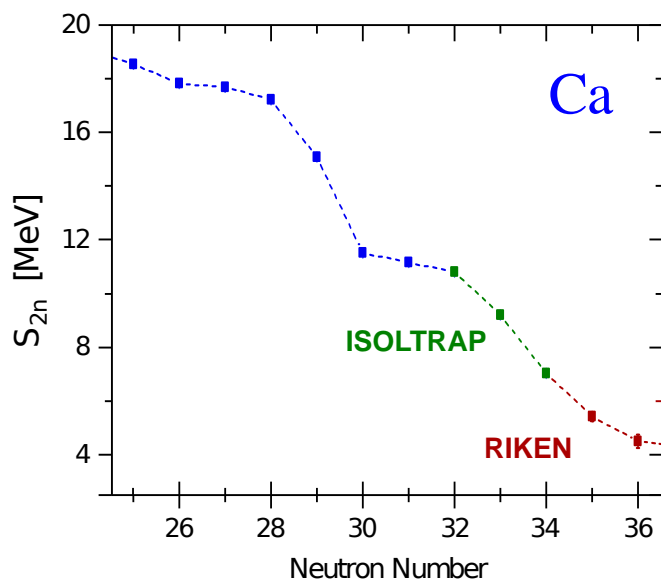


Mass data from AME16

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F. Wienholtz *et al.* - Nature (London) 498, 346 (2013).

First evidence of N=34 shell closure in the mass surface: **RIKEN -  $^{54}\text{Ca}$**

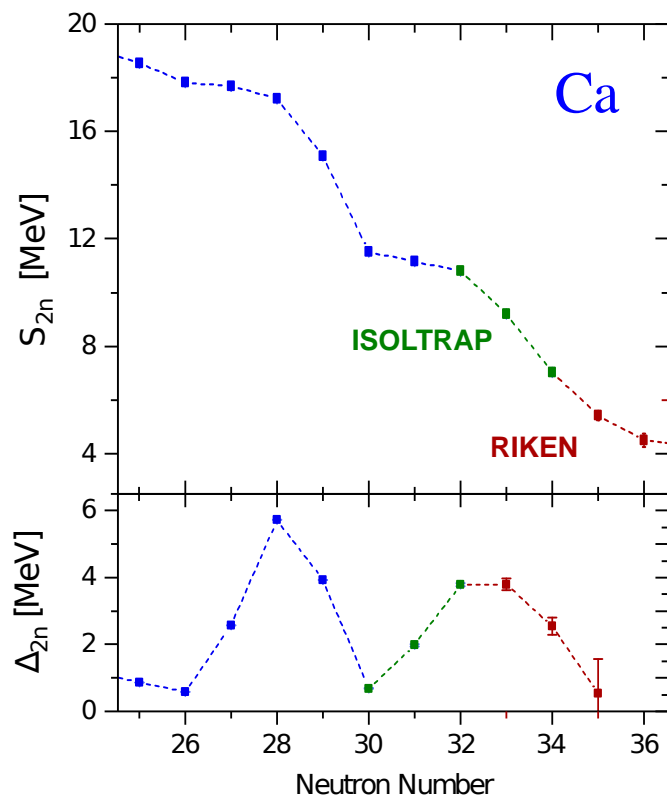
S. Michimasa *et al.*, -Phys. Rev. Lett. 121, 022506 (2018)

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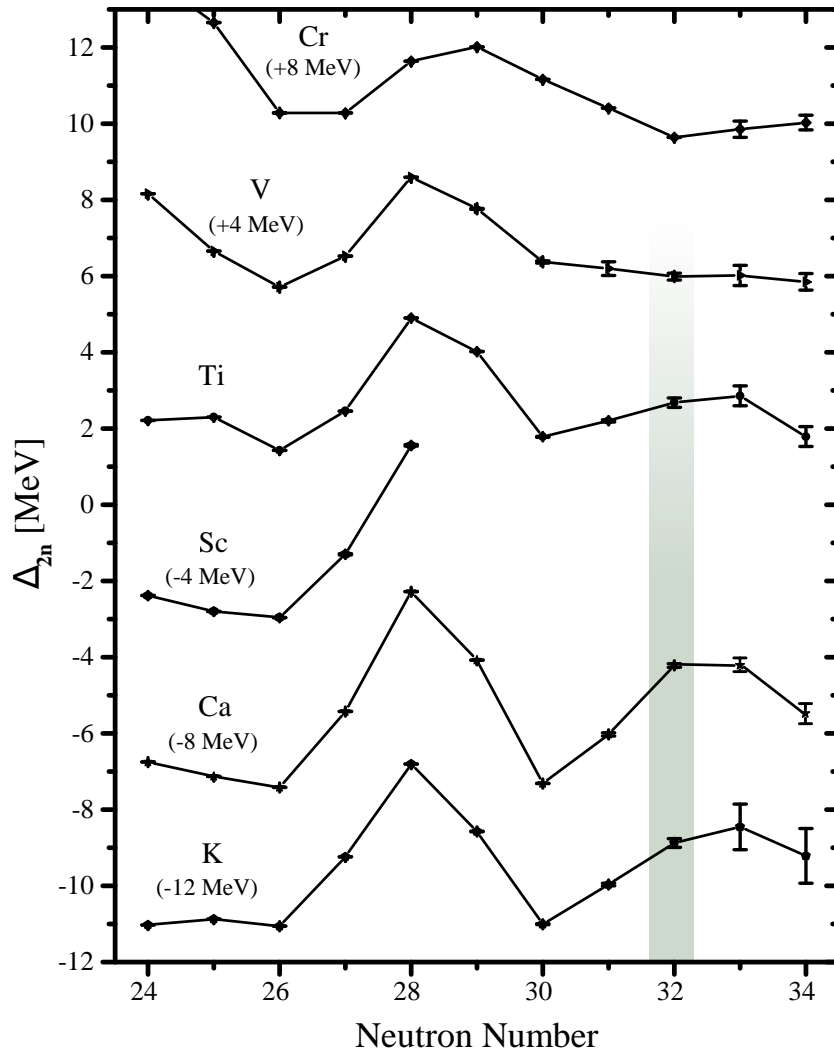
S. Michimasa *et al.*, -Phys. Rev. Lett. 121, 022506 (2018)

**Clearer view:**

$$\Delta_{2n}(N,Z) = S_{2n}(N,Z) - S_{2n}(N+2,Z)$$

Mass data from AME16

# Evolution of N=32 Shell Closure



Cr: absent

V: absent

TITAN / TRIUMF - M. P. Reiter *et al.*, Phys. Rev. C 98, 024310 (2018)

Ti: weak / transitional

TITAN / TRIUMF - E. Leistenschneider *et al.*, Phys. Rev. Lett. 120, (2018).

Ca: doubly-magic

ISOLTRAP / CERN - F. Wienholtz *et al.* - Nature (London) 498, 346 (2013).

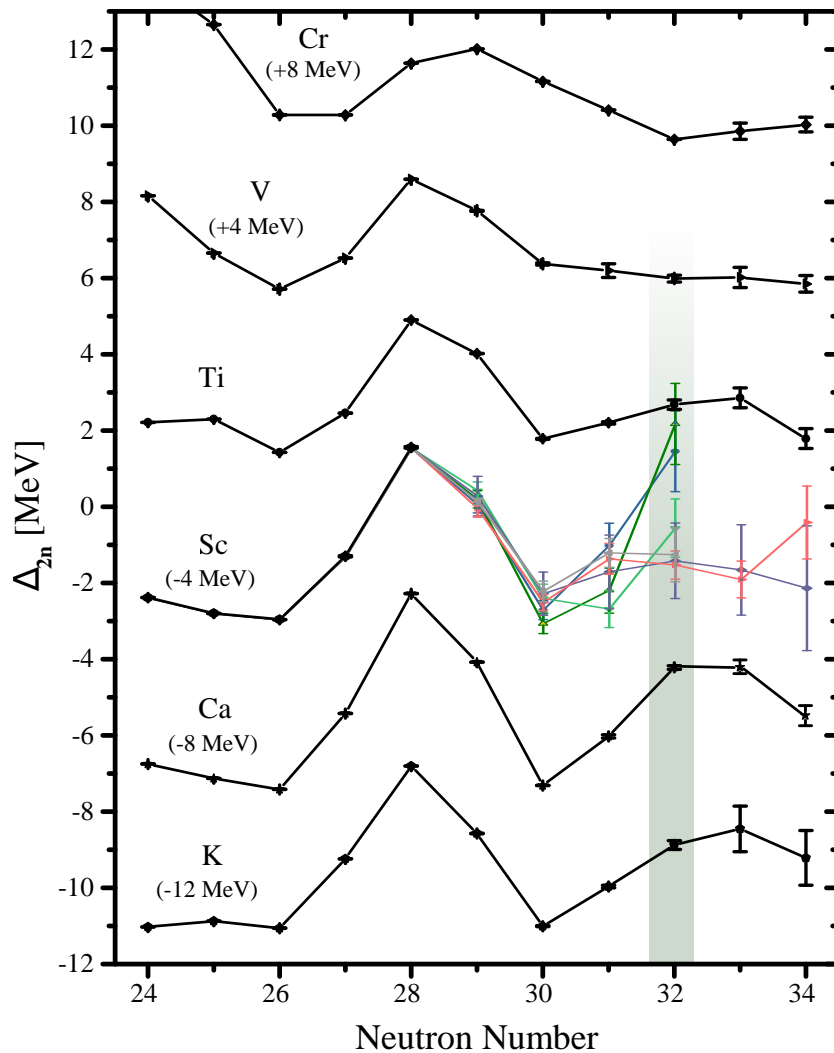
K: strong

ISOLTRAP / CERN - M. Rosenbusch *et al.*, Phys. Rev. Lett. 114,202501 (2015)

Mass data from AME16



# Evolution of N=32 Shell Closure



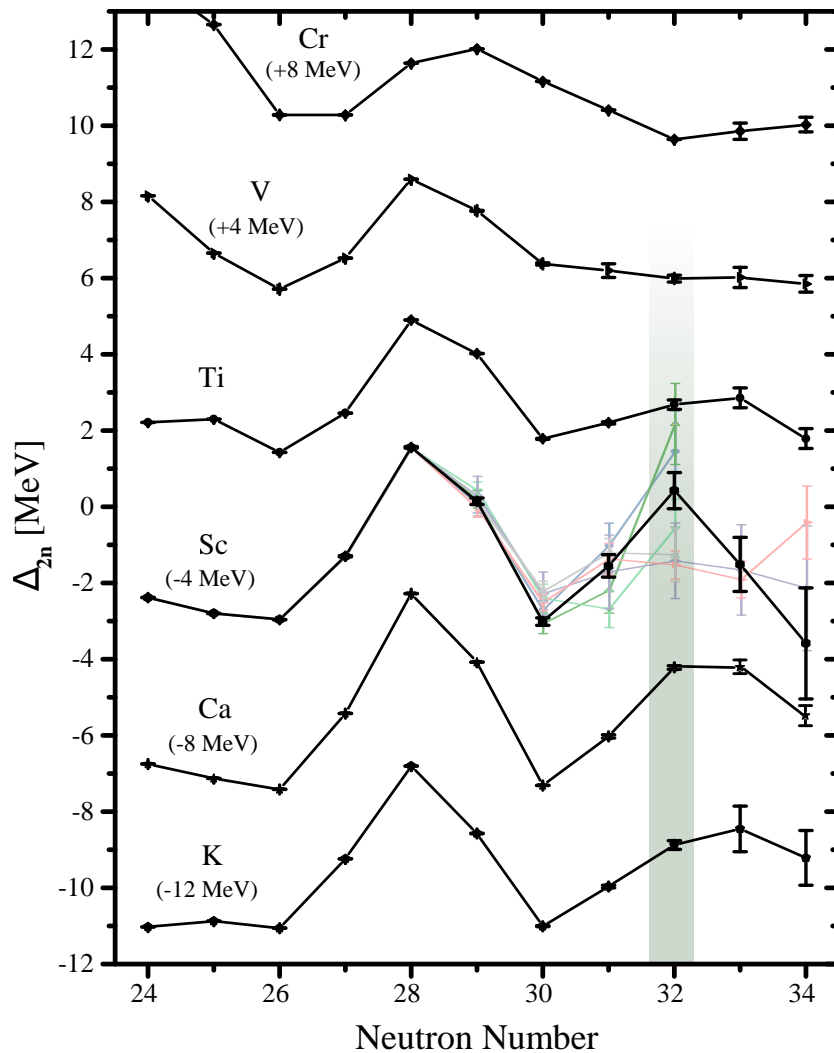
- TOFI Los Alamos 1990  
X. L. Tu et al., Z. Phys. A: At. Nucl. 337, 361 (1990)
- ▲ TOFI Los Alamos 1994  
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- ▼ TOFI Los Alamos 1998  
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- ◄ TOF-Bp NSCL 2011  
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- ◆ TOF-Bp NSCL 2015  
Z. Meisel et al., Phys. Rev. Lett. 115, 162501 (2015).
- TOF-Bp NSCL 2020 (re-evaluation)  
Z. Meisel et al., Phys. Rev. C 101, 052801(R) (2020)

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U.S. Department of Energy Office of Science  
National Science Foundation  
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- TOFI Los Alamos 1990  
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## Isochronous Mass Spectrometry at CSRe (Lanzhou)

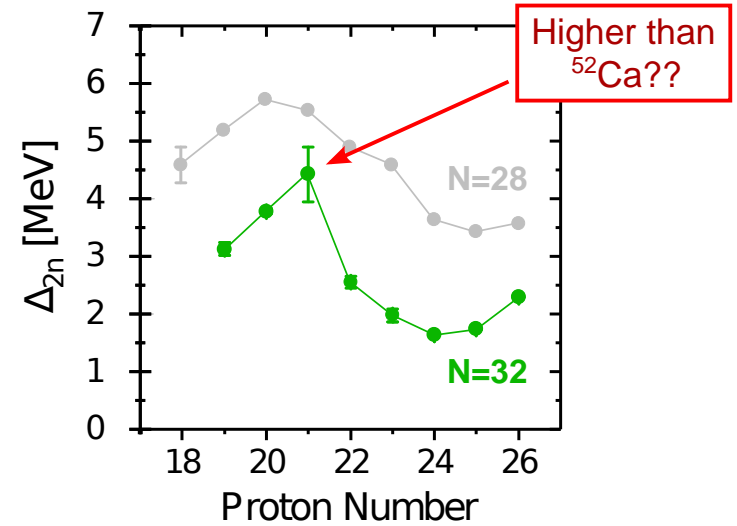
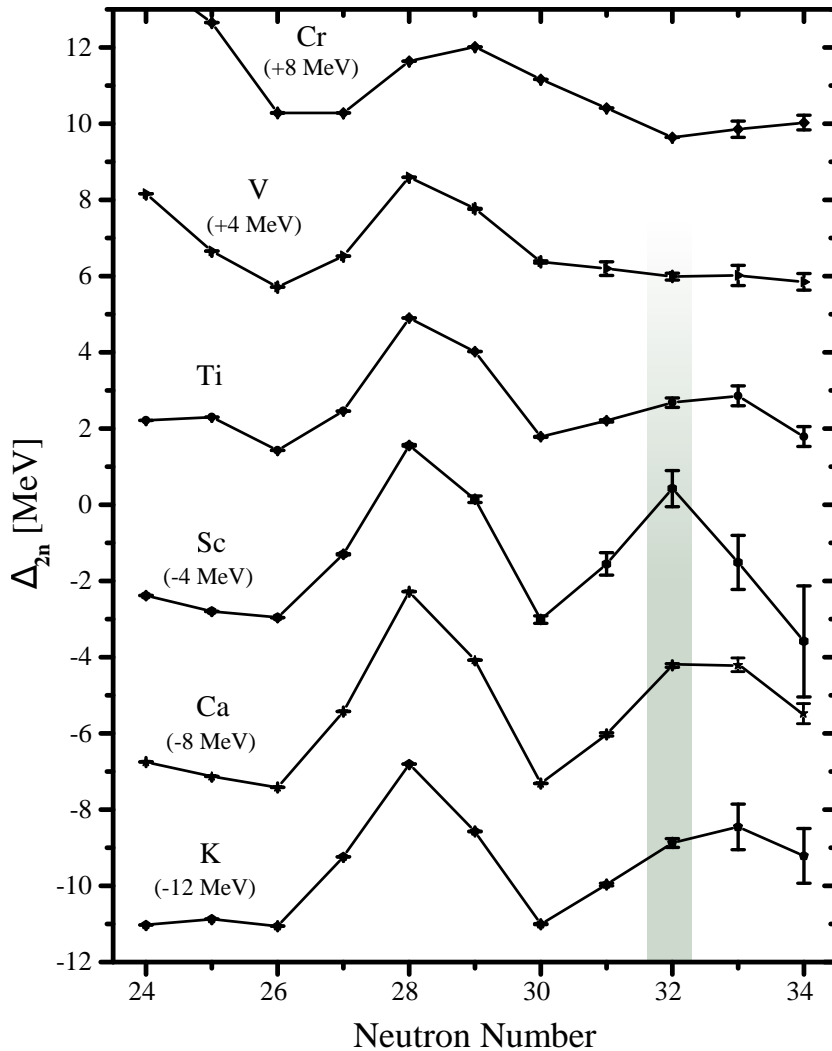
X. Xu *et al.*, Phys. Rev. C 99, 064303 (2019).

Strong shell closure in  $^{53}\text{Sc}$ !

... But how strong?

Mass data from AME16

# Evolution of N=32 Shell Closure



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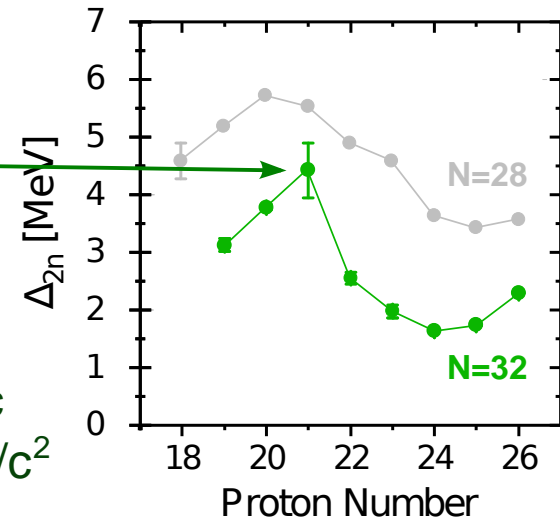
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# Evolution of N=32 Shell Closure

**GOAL:** measure  $\Delta_{2n}$  in  $^{53}\text{Sc}$  (N=32) using precision mass spectrometry to refine shell evolution.

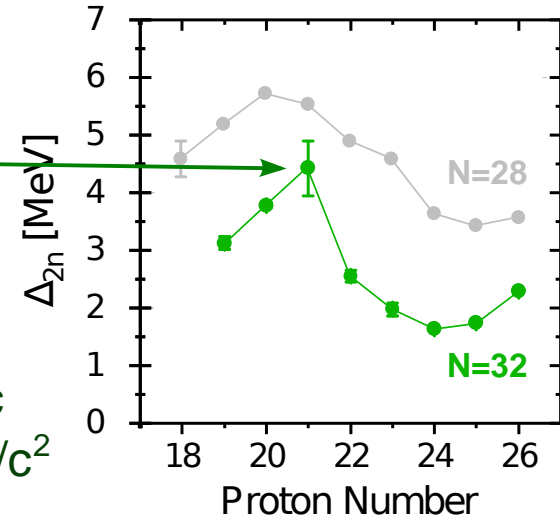
**REQUIRES:** masses of neutron-rich  $^{51}\text{Sc}$  to  $^{55}\text{Sc}$  to a precision much better than  $100 \text{ keV}/c^2$



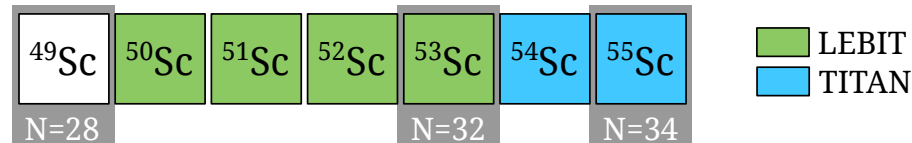
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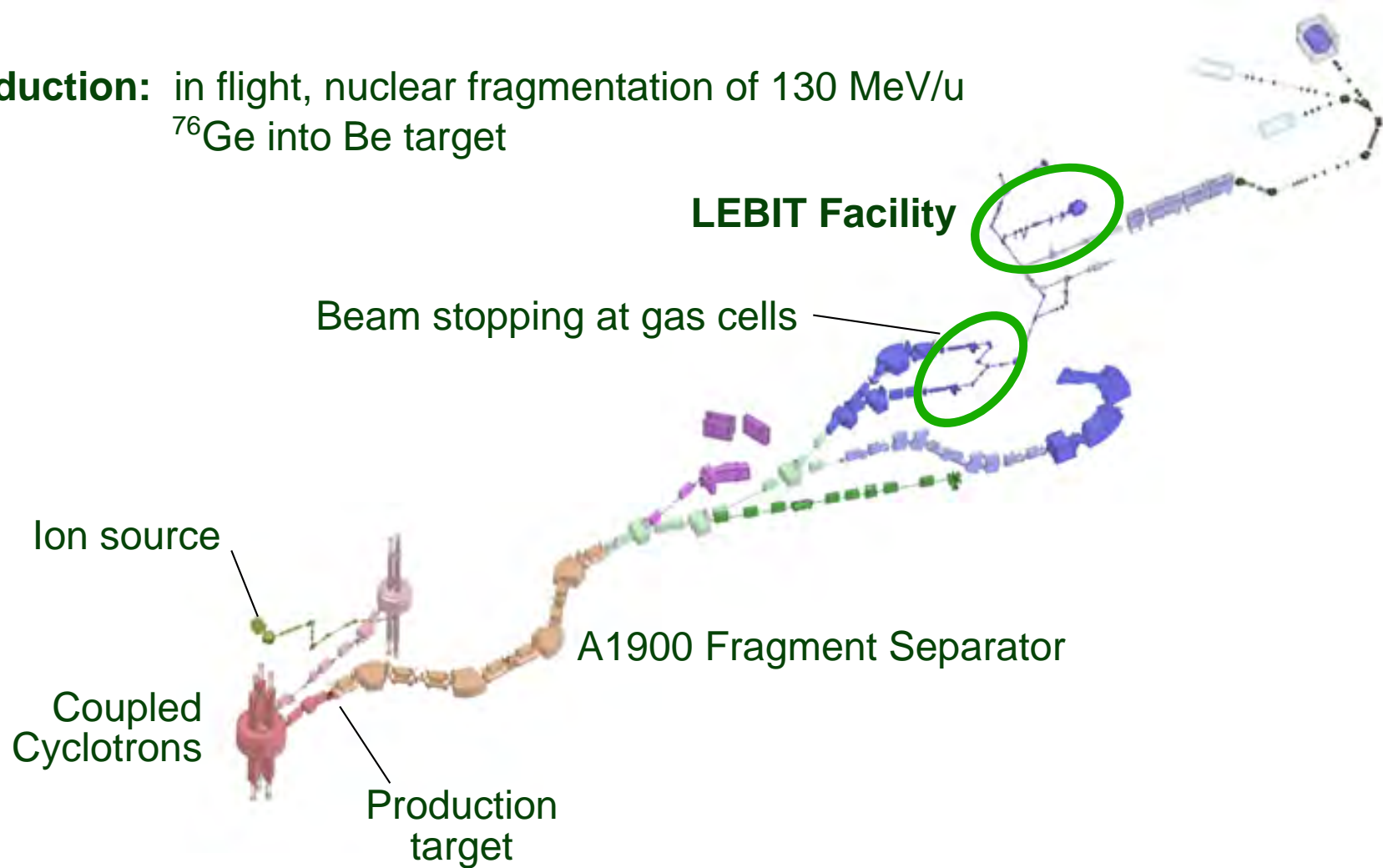


Two experiments performed at different facilities and employing distinct techniques:  
**LEBIT** at NSCL (Penning traps) and **TITAN** at TRIUMF (MR-TOF-MS)

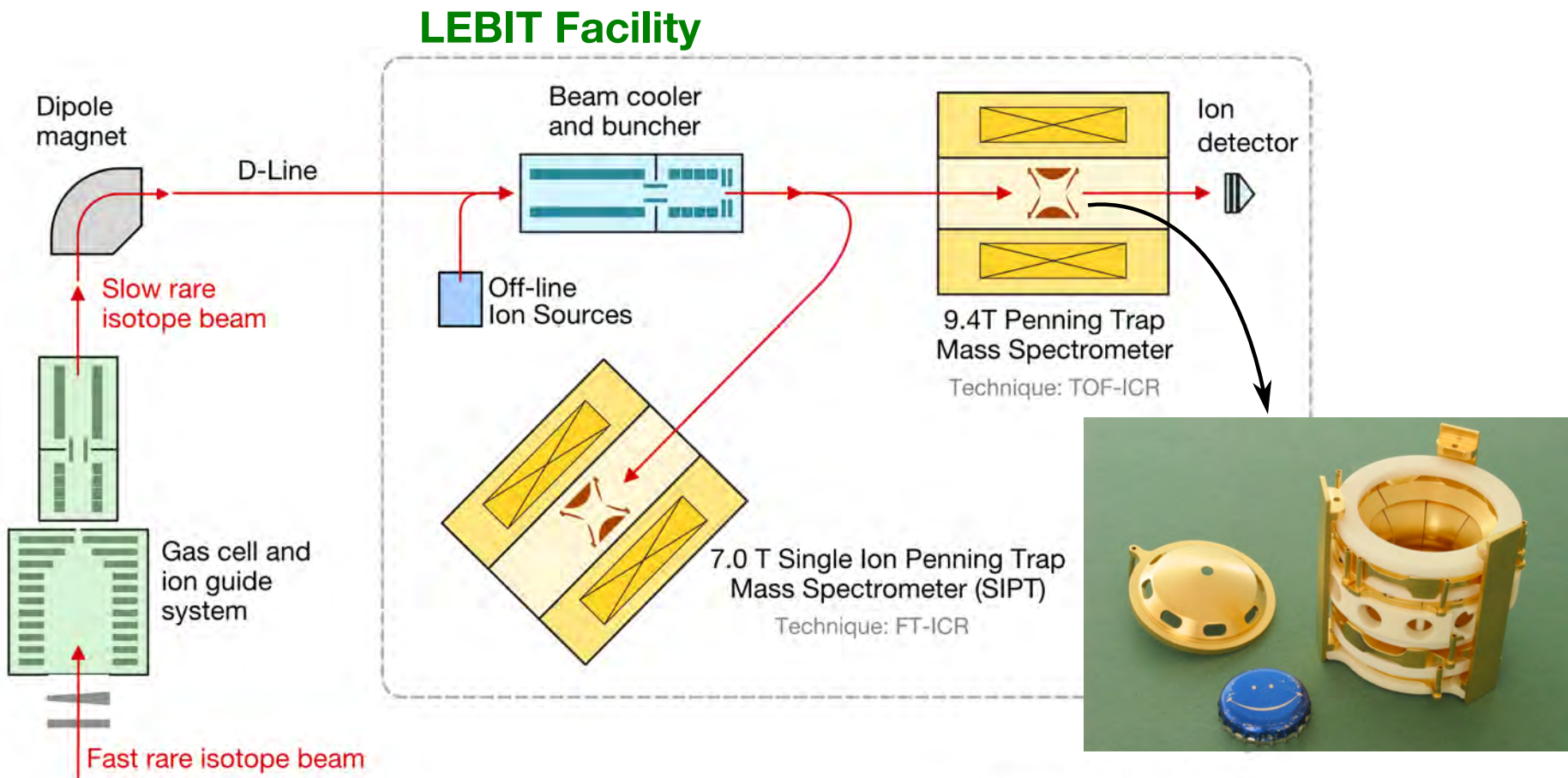


# The Experiment at LEBIT (NSCL)

**Production:** in flight, nuclear fragmentation of 130 MeV/u  $^{76}\text{Ge}$  into Be target

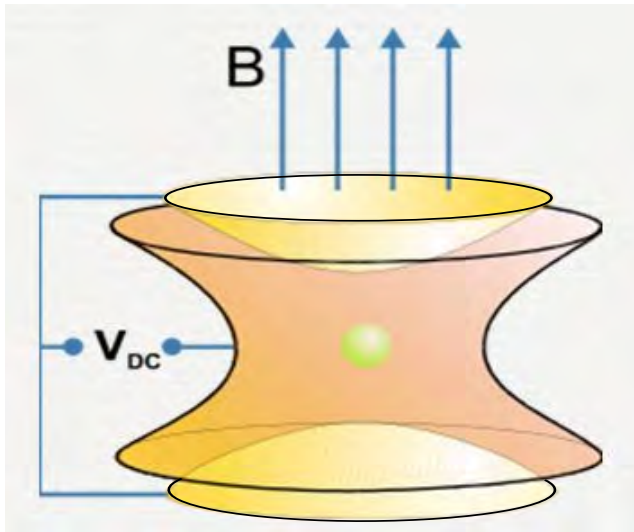


# The Experiment at LEBIT (NSCL)



# The Experiment at LEBIT (NSCL)

## Penning Trap Mass Spectrometry



Confinement: strong B field (**9.4 T**)  
+ weak E field

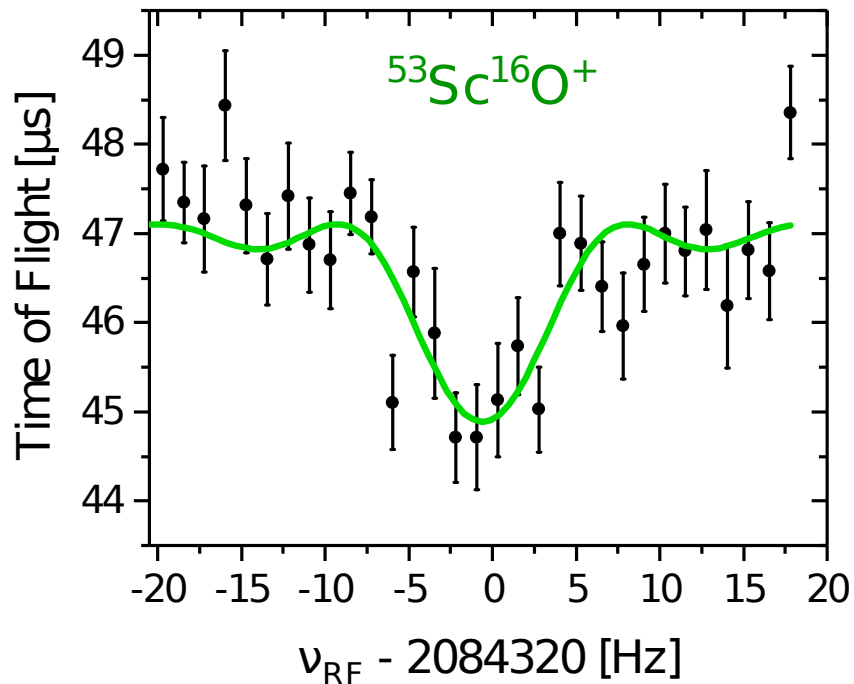
Mass meas. through cyclotron frequency:

$$\nu_c = \frac{q B}{2\pi m}$$



# The Experiment at LEBIT (NSCL)

## Penning Trap Mass Spectrometry



Cyclotron frequency:  $\nu_c = \frac{q B}{2\pi m}$

### Time-of-Flight Ion Cyclotron Resonance:

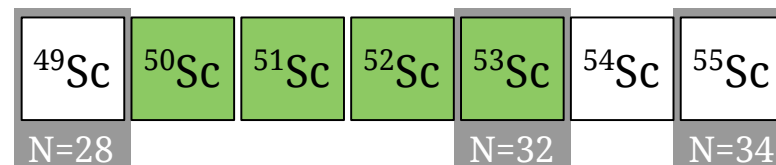
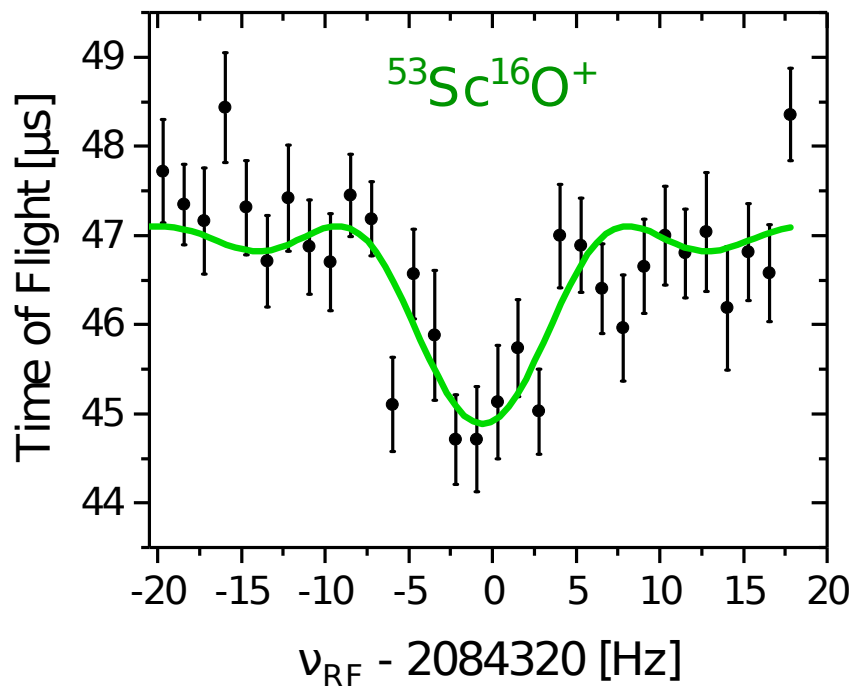
External driving field applied with frequency  $\nu_{rf}$

On resonance if  $\nu_{rf} = \nu_c$

Gain in energy translates into a faster time-of-flight to detector

# The Experiment at LEBIT (NSCL)

## Penning Trap Mass Spectrometry

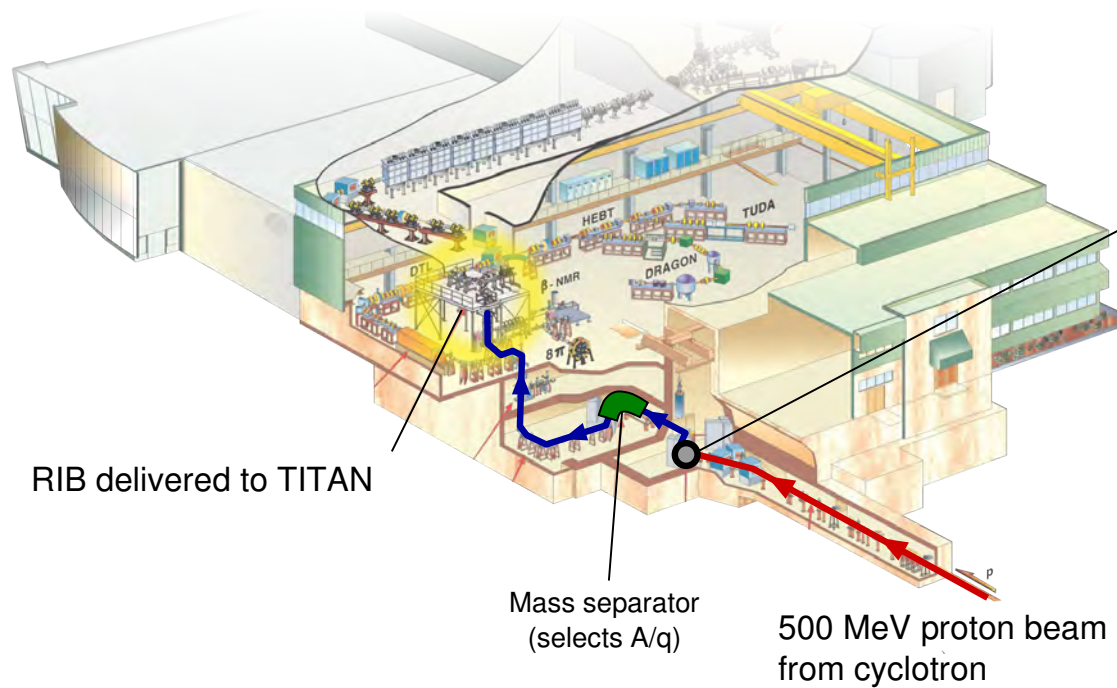
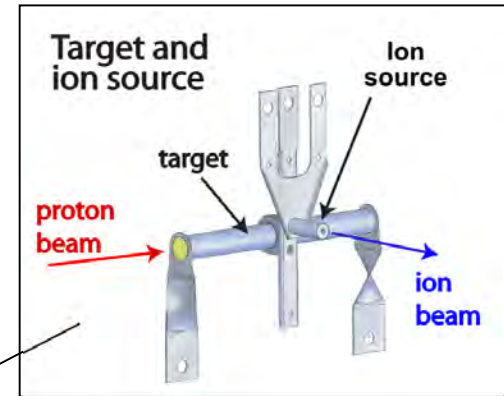


Measurement possible up to  $^{53}\text{Sc}$   
Contaminants were too abundant at  $^{54,55}\text{Sc}$

# The Experiment at TITAN (TRIUMF)

## ISAC Facility at TRIUMF

**Production:** ISOL method, proton beam on Ta target aiming Ti and V isotopes (Sc came as a contaminant)



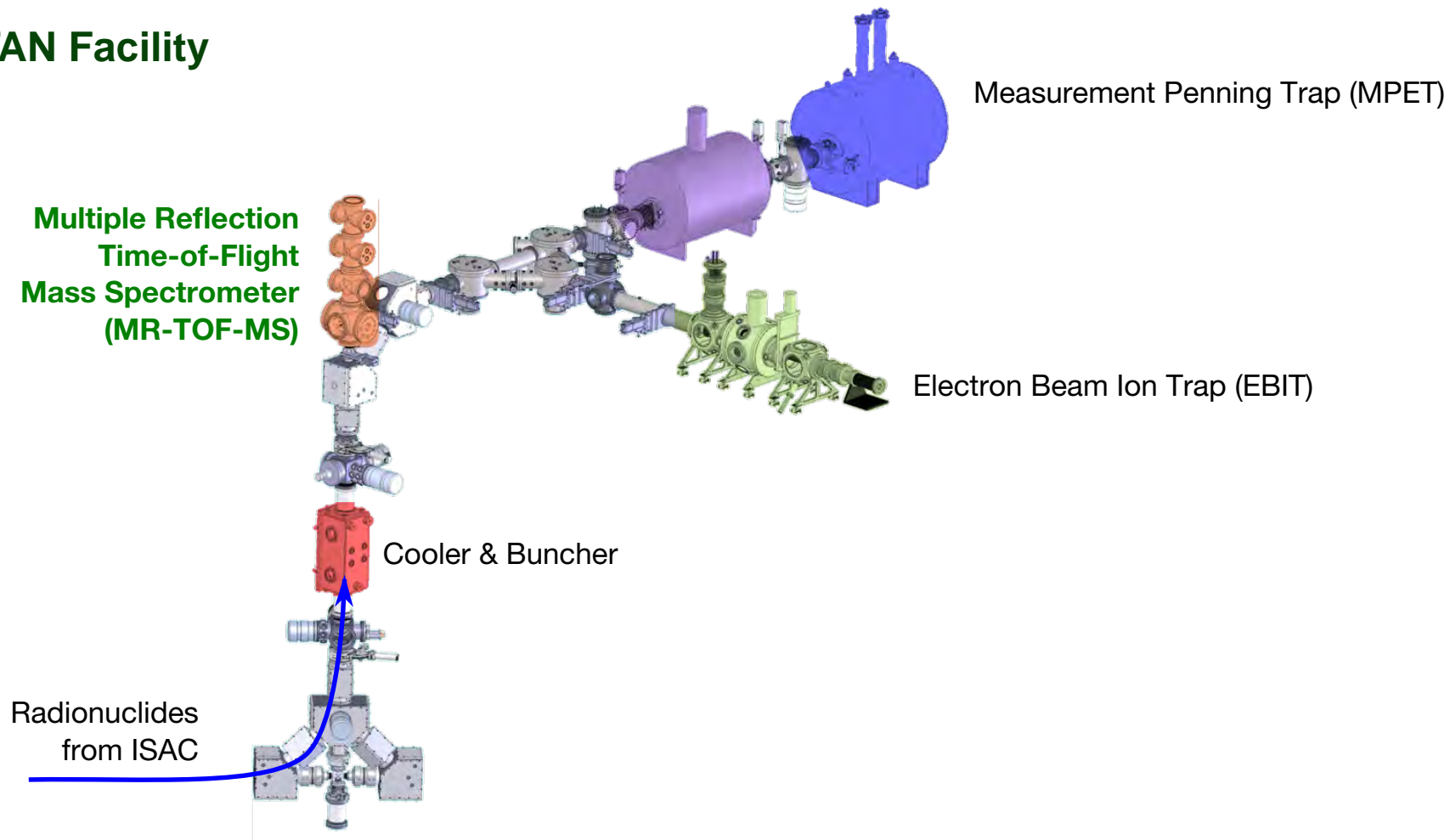
**In flight:** reaction products are separated, then stopped

**ISOL:** products are stopped, then separated

Completely different final beam composition

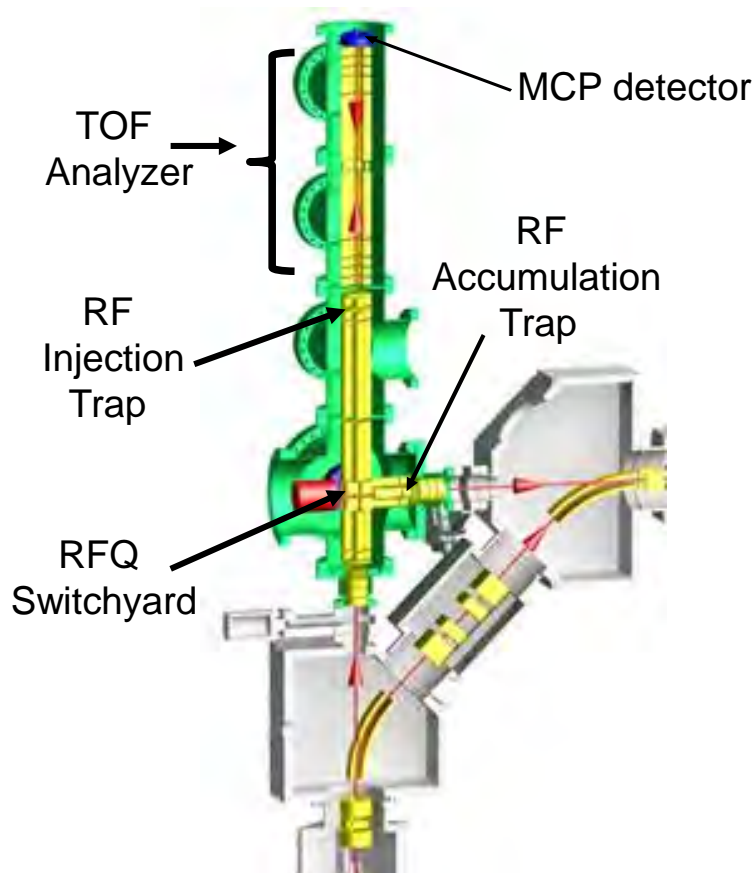
# The Experiment at TITAN (TRIUMF)

## TITAN Facility



# The Experiment at TITAN (TRIUMF)

## Multiple-Reflection Time-Of-Flight Mass Spectrometer (MR-TOF-MS)



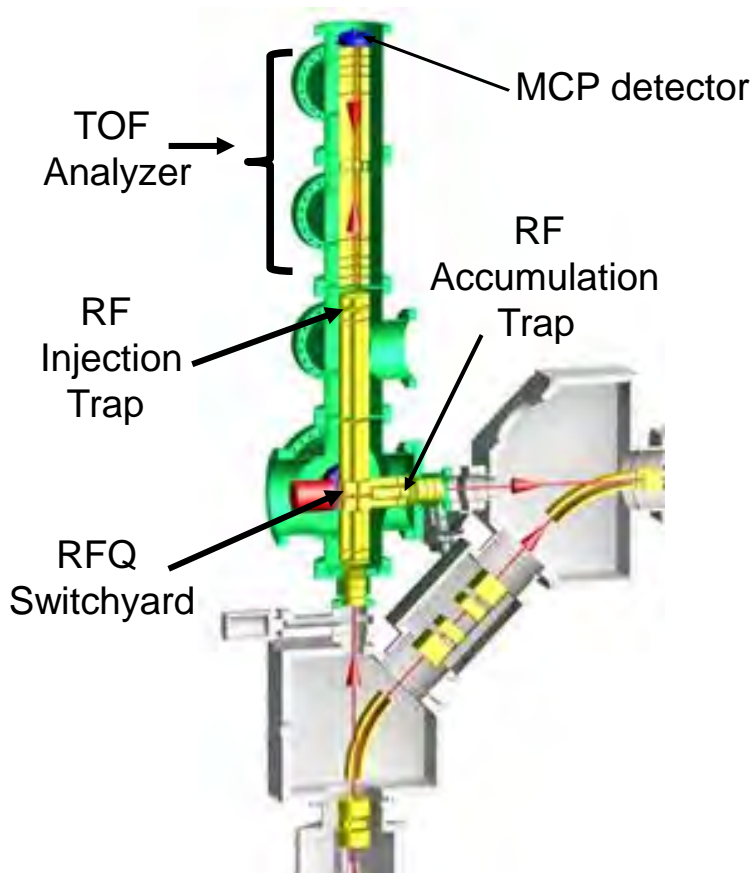
### Mass analyzer

- Two gridless, electrostatic mirrors
- Time-of-flight separation
- Over 200 000 resolving power  
(well enough to separate most isobars)



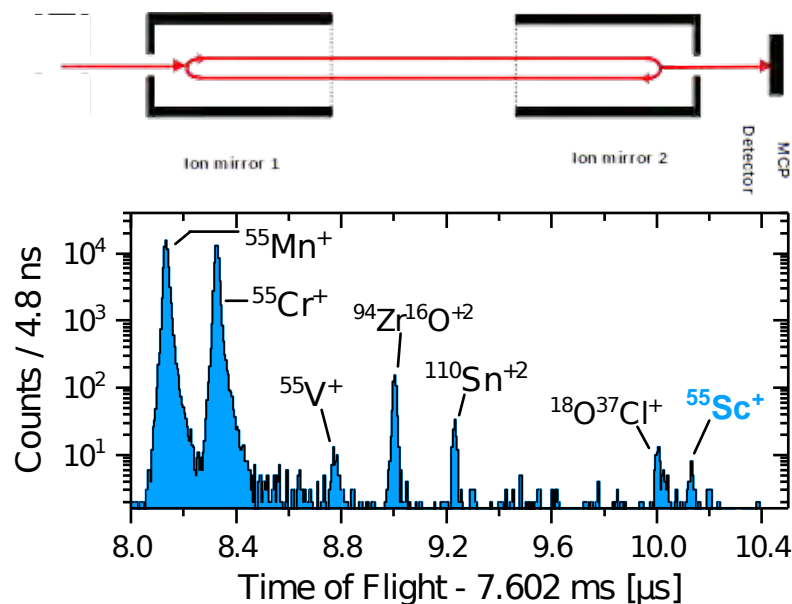
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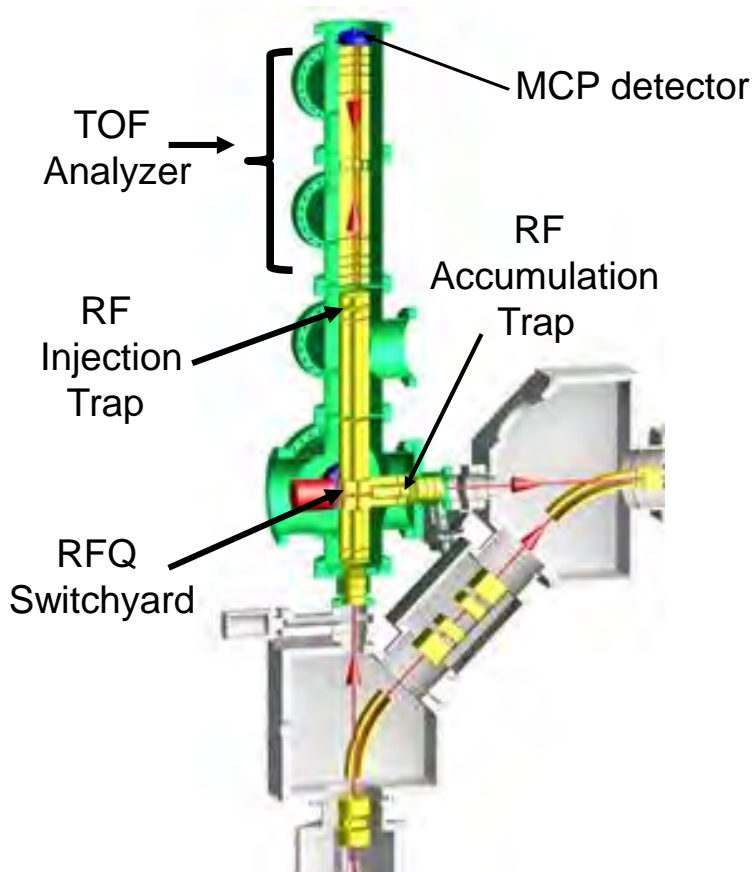
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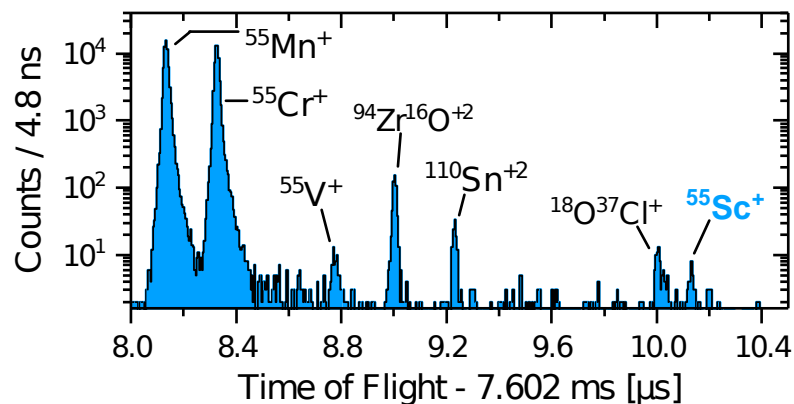
## Multiple-Reflection Time-Of-Flight Mass Spectrometer (MR-TOF-MS)



- Fast technique
- Non-scanning and sensitive
- Only 35 counts of  $^{55}\text{Sc}$  were sufficient

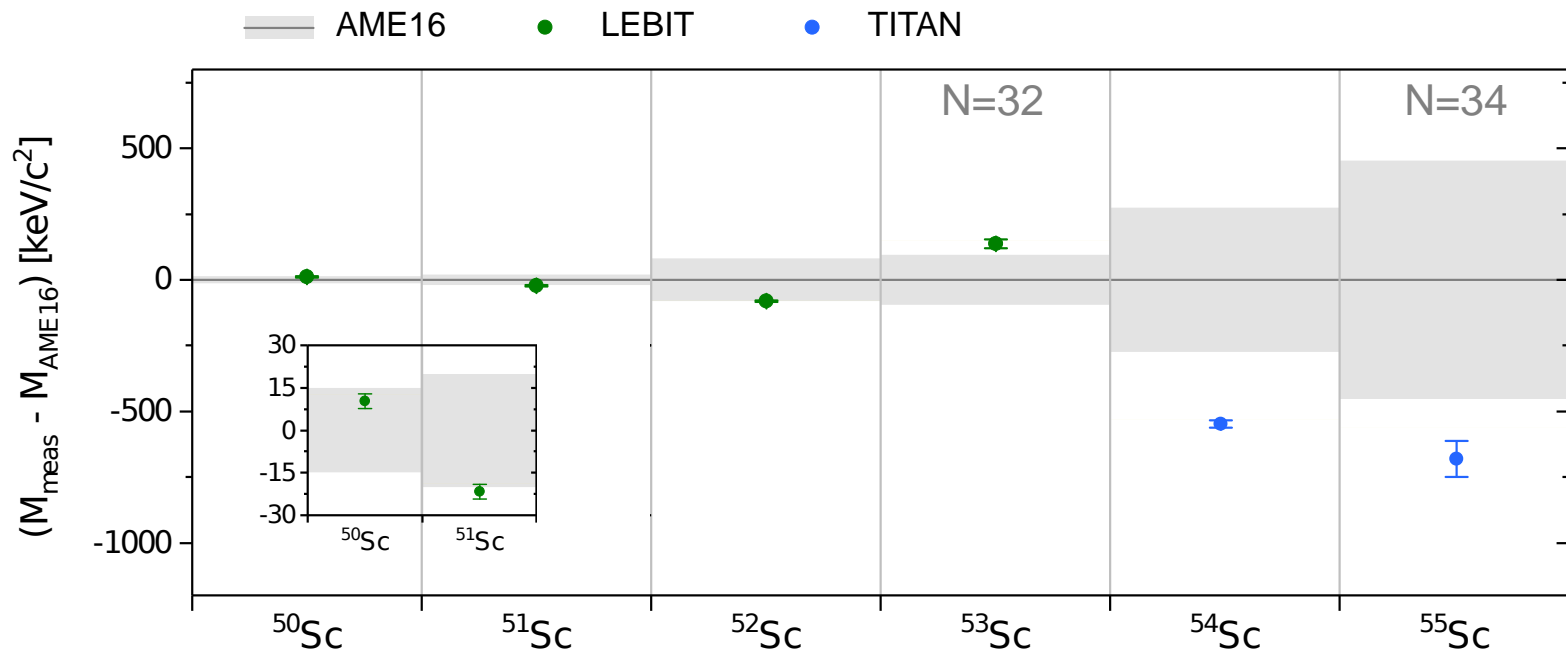
$^{49}\text{Sc}$	$^{50}\text{Sc}$	$^{51}\text{Sc}$	$^{52}\text{Sc}$	$^{53}\text{Sc}$	$^{54}\text{Sc}$	$^{55}\text{Sc}$
N=28				N=32		N=34

$$M_a = [C(t_{ion} - t_0)^2 + m_e] q$$



# Results

Our results compared to the literature:

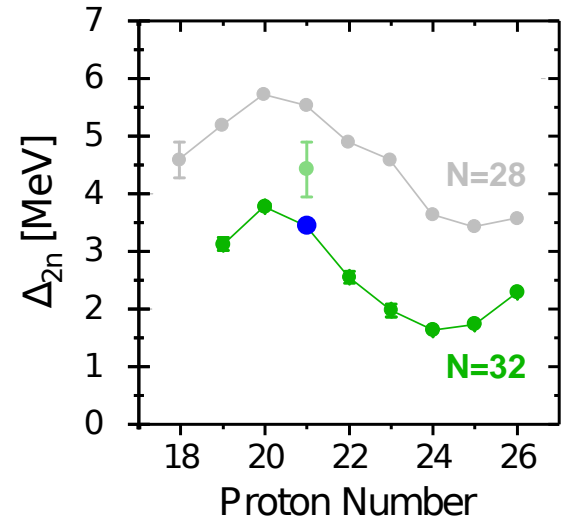
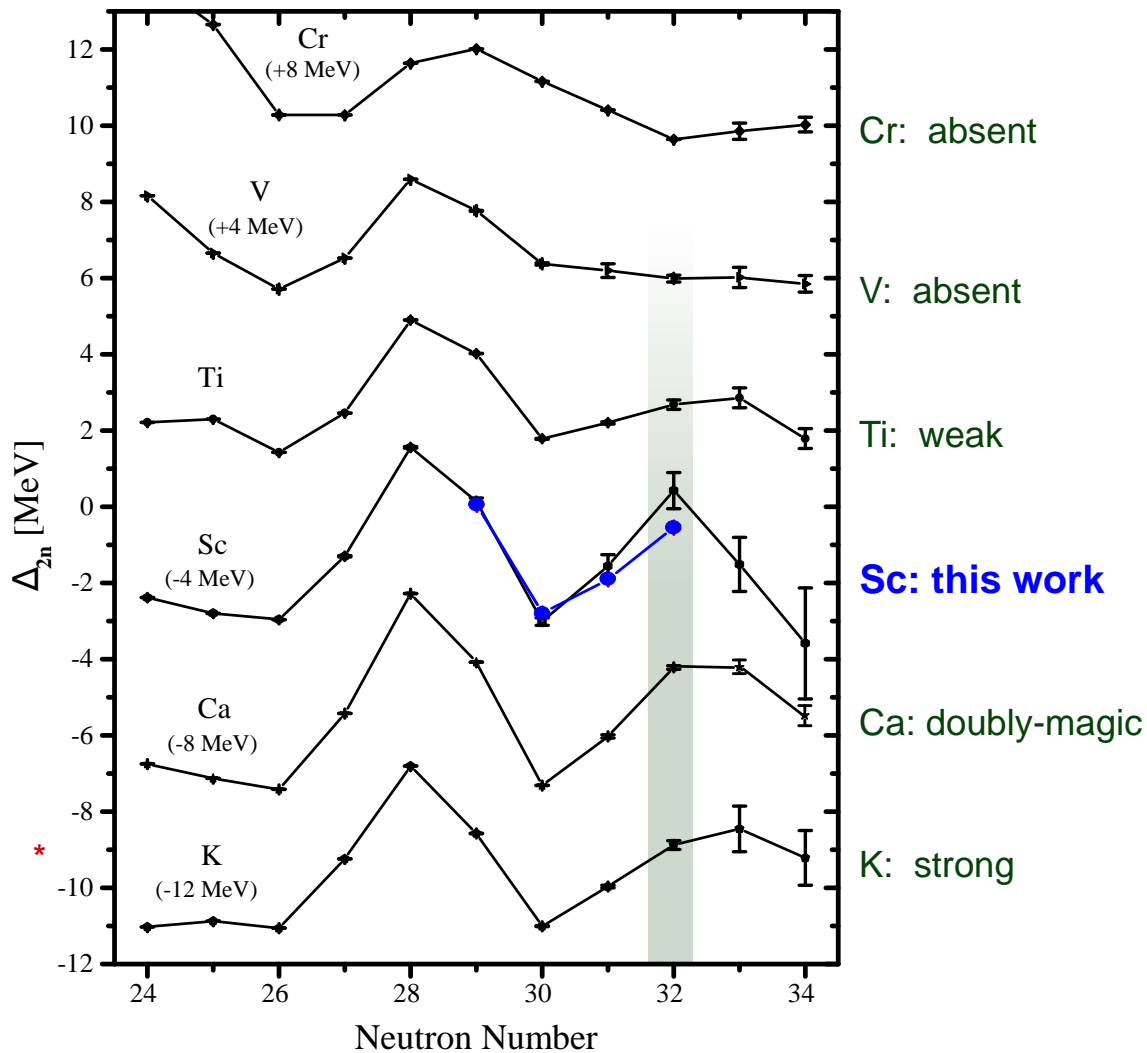


Uncertainties improved in all cases

Over 0.5 MeV deviation



# Results



$\Delta_{2n}(N=32)$  presents a smooth evolution through  $^{53}\text{Sc}$

$\Delta_{2n}(N=32)$  seems to mirror  $\Delta_{2n}(N=28)$ , but  $\sim 2$  MeV lower

# Results

PHYSICAL REVIEW LETTERS **126**, 042501 (2021)

## Precision Mass Measurements of Neutron-Rich Scandium Isotopes Refine the Evolution of $N=32$ and $N=34$ Shell Closures

E. Leistenschneider<sup>1,2,\*</sup>, E. Dunling<sup>3,4</sup>, G. Bollen<sup>1,2,5</sup>, B. A. Brown<sup>1,2,5</sup>, J. Dilling<sup>3,6</sup>, A. Hamaker<sup>1,2,5</sup>, J. D. Holt<sup>3,7</sup>, A. Jacobs<sup>3,6</sup>, A. A. Kwiatkowski<sup>3,8</sup>, T. Miyagi<sup>3</sup>, W. S. Porter<sup>3,6</sup>, D. Puentes<sup>1,2,5</sup>, M. Redshaw<sup>9,2</sup>, M. P. Reiter<sup>3,10,11</sup>, R. Ringle<sup>1,2</sup>, R. Sandler<sup>9</sup>, C. S. Sumithrarachchi<sup>1,2</sup>, A. A. Valverde<sup>12</sup> and I. T. Yandow<sup>1,2,5</sup>

The LEBIT Collaboration and the TITAN Collaboration

<sup>1</sup>Facility for Rare Isotope Beams, Michigan State University, East Lansing, Michigan 48824, USA

<sup>2</sup>National Superconducting Cyclotron Laboratory, Michigan State University, East Lansing, Michigan 48824, USA

<sup>3</sup>TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia V6T 2A3, Canada

<sup>4</sup>Department of Physics, University of York, York YO10 5DD, United Kingdom

<sup>5</sup>Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824, USA

<sup>6</sup>Department of Physics & Astronomy, University of British Columbia, Vancouver, British Columbia V6T 1Z1, Canada

<sup>7</sup>Department of Physics, McGill University, 3600 Rue University, Montréal, Québec H3A 2T8, Canada


<sup>8</sup>Department of Physics and Astronomy, University of Victoria, Victoria, British Columbia V8P 5C2, Canada

<sup>9</sup>Department of Physics, Central Michigan University, Mount Pleasant, Michigan 48859, USA

<sup>10</sup>II. Physikalisches Institut, Justus-Liebig-Universität, 35392 Gießen, Germany

<sup>11</sup>School of Physics and Astronomy, University of Edinburgh, Edinburgh EH9 3FD, United Kingdom

<sup>12</sup>Department of Physics & Astronomy, University of Manitoba, Winnipeg, Manitoba R3T 2N2, Canada

 (Received 1 June 2020; revised 28 September 2020; accepted 14 December 2020; published 26 January 2021)

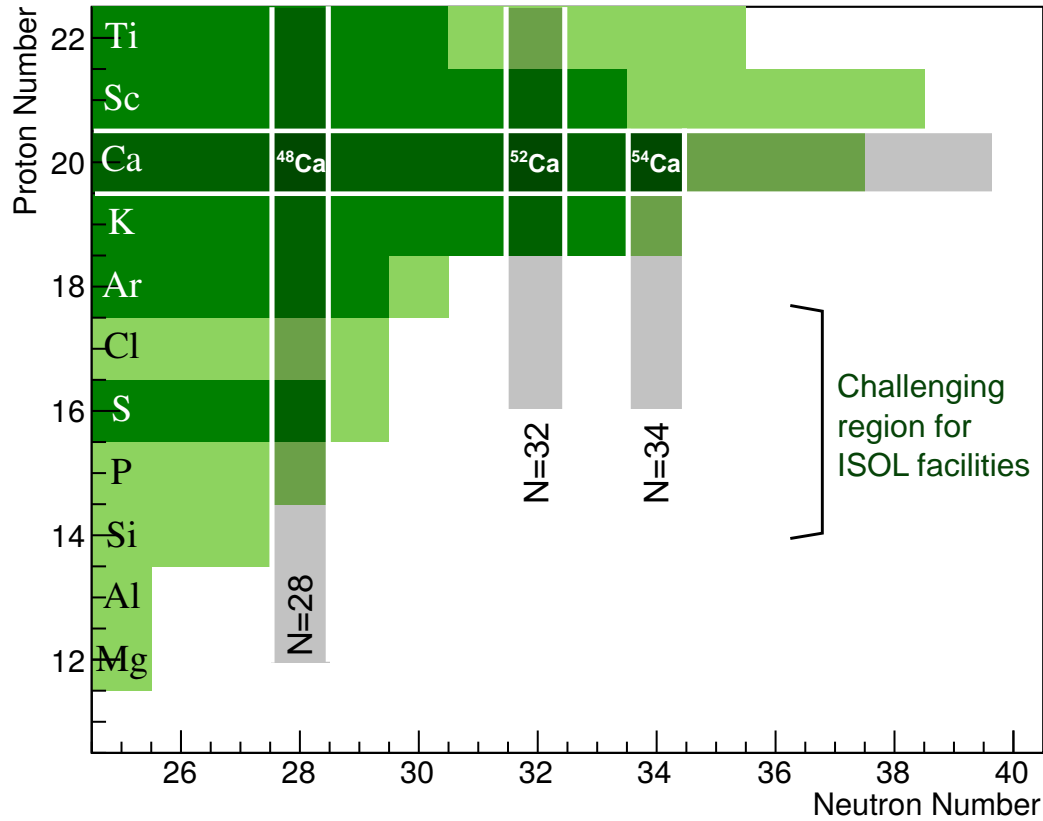
We report high-precision mass measurements of  $^{50-55}\text{Sc}$  isotopes performed at the LEBIT facility at NSCL and at the TITAN facility at TRIUMF. Our results provide a substantial reduction of their uncertainties and indicate significant deviations, up to 0.7 MeV, from the previously recommended mass values for  $^{53-55}\text{Sc}$ . The results of this work provide an important update to the description of emerging closed-shell phenomena at neutron numbers  $N=32$  and  $N=34$  above proton-magic  $Z=20$ . In particular, they finally enable a complete and precise characterization of the trends in ground state binding energies along the  $N=32$  isotone, confirming that the empirical neutron shell

Further discussion on:

Implications for a possible  $N=34$  shell gap in Sc

Conjoint theoretical descriptions of  $N=32,34$

# Future



A lot yet to be explored!

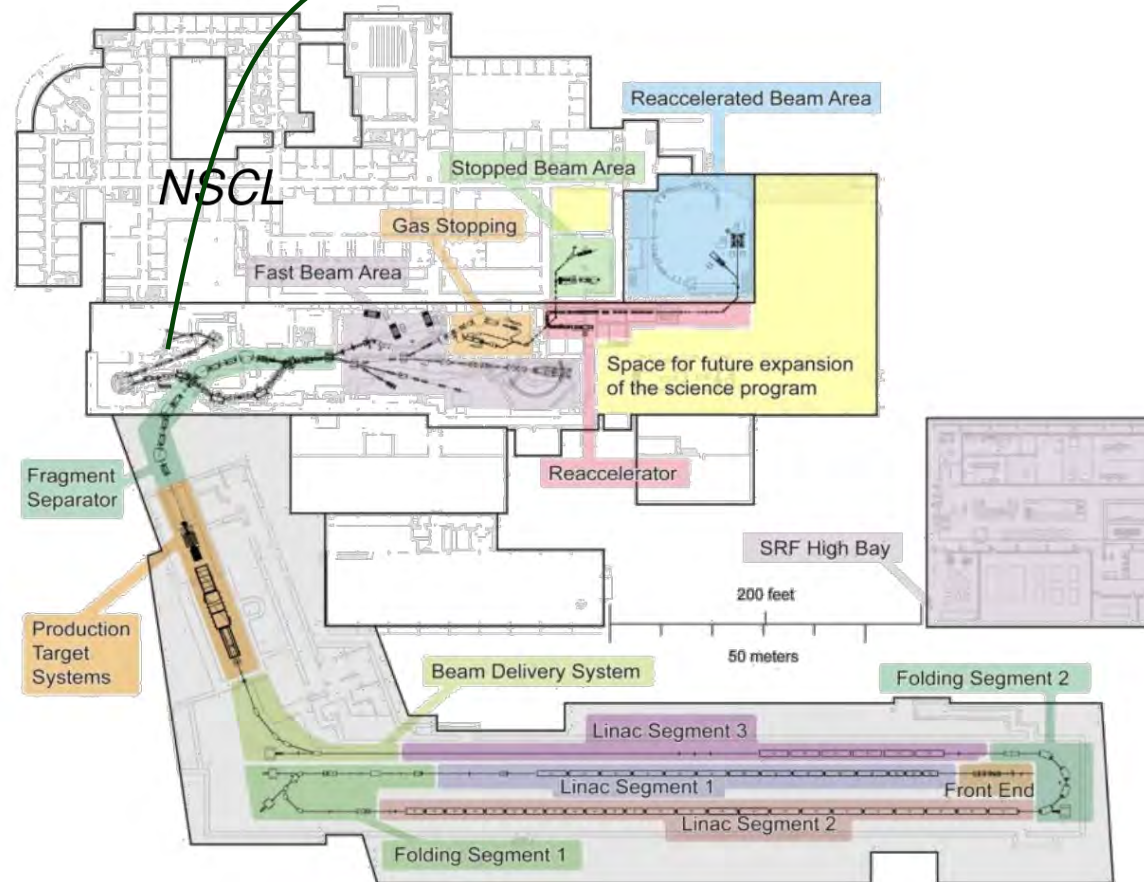
# Towards higher yields: FRIB

## Facility for Rare Isotope Beams

Rare isotope production via in-flight technique with intense primary beams up to 400 kW

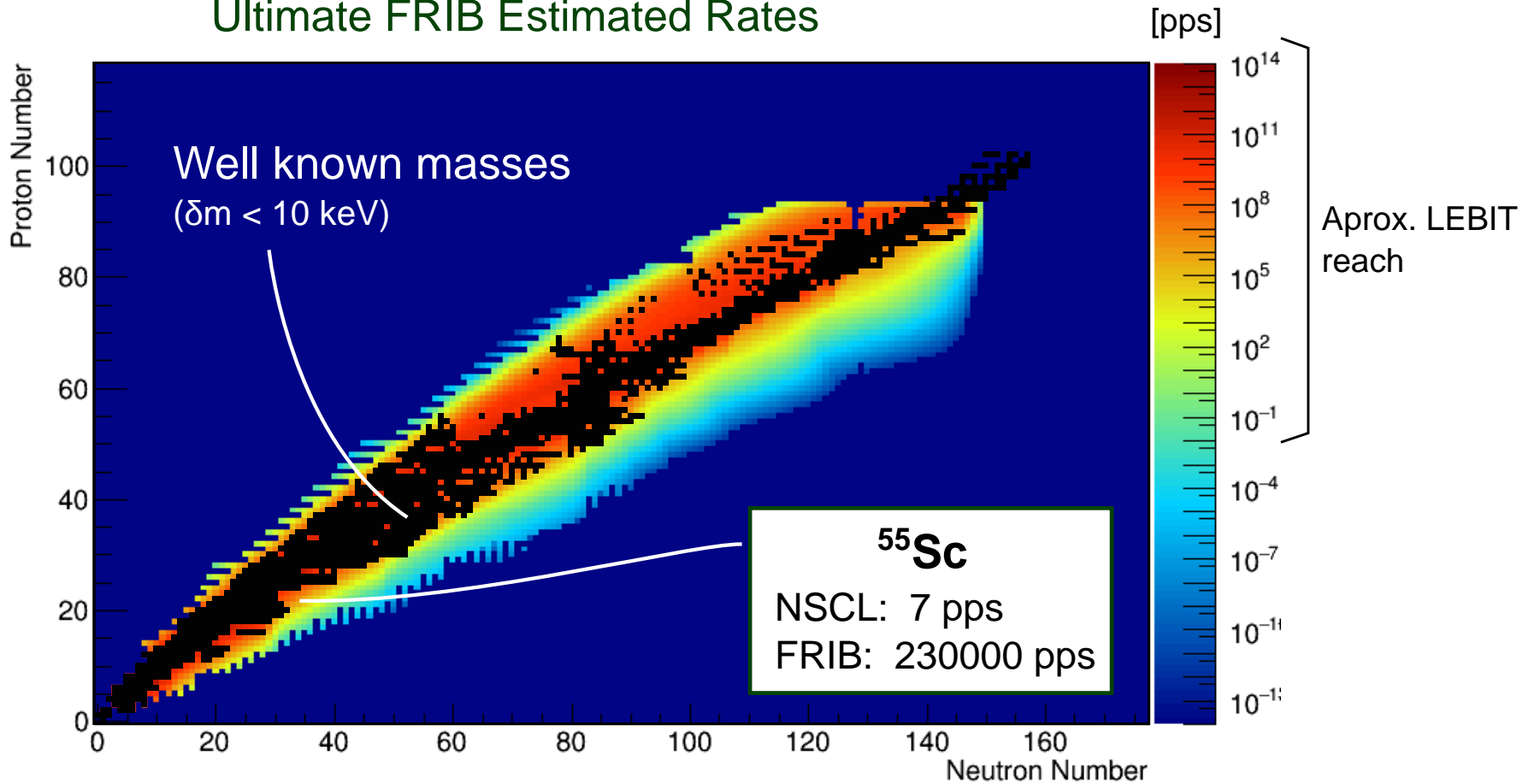
First PAC proposals received last Monday for experiments to run in **2022**.

NSCL Coupled Cyclotron Facility  
Last Beam: November 15<sup>th</sup>, 2020



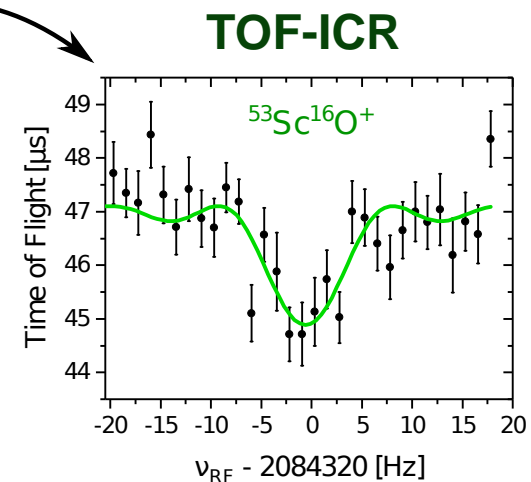
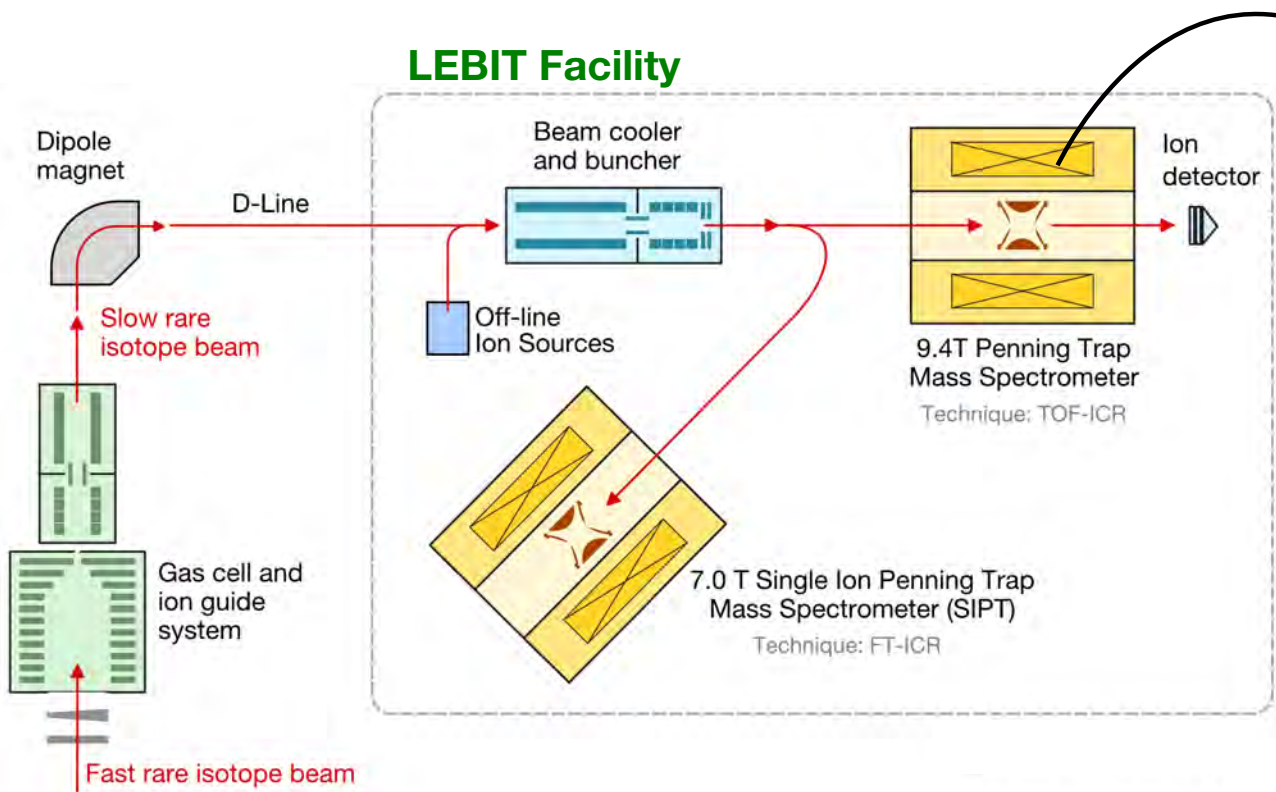
# Towards higher yields: FRIB

## Ultimate FRIB Estimated Rates



# Towards Ultimate Sensitivity: SIPT

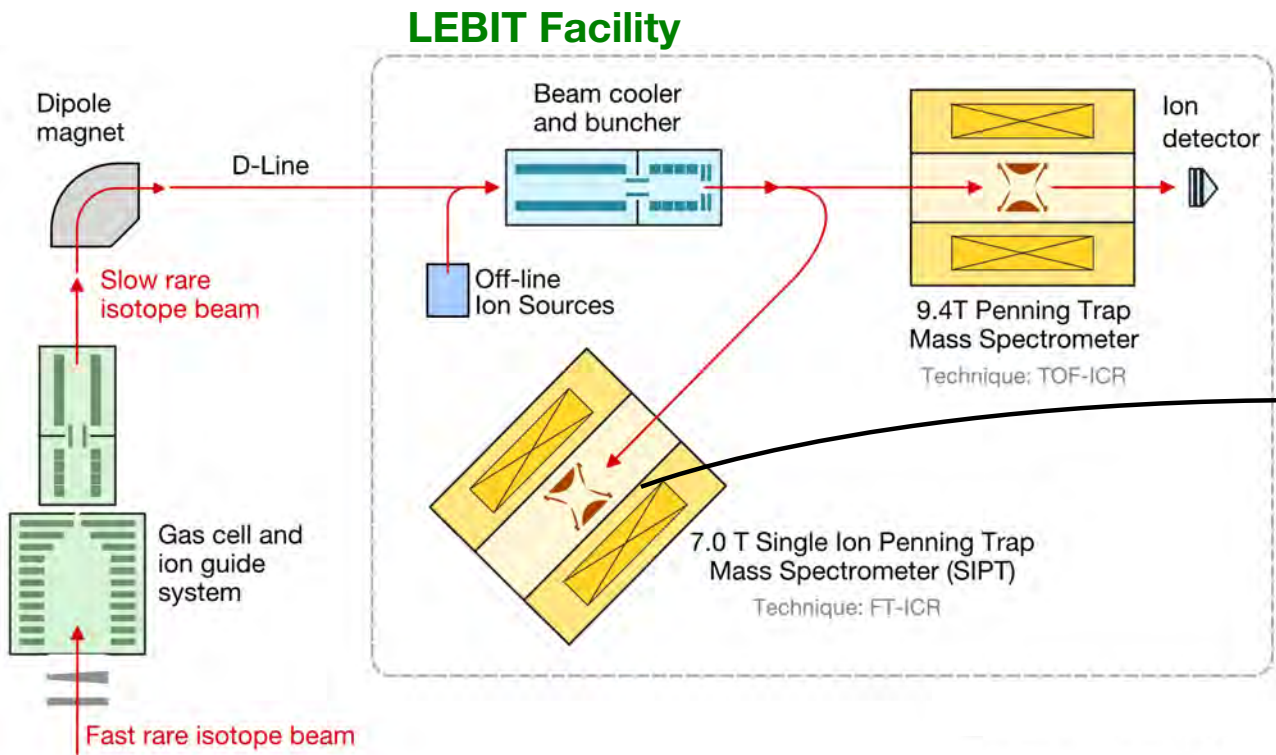
## Single Ion Penning Trap



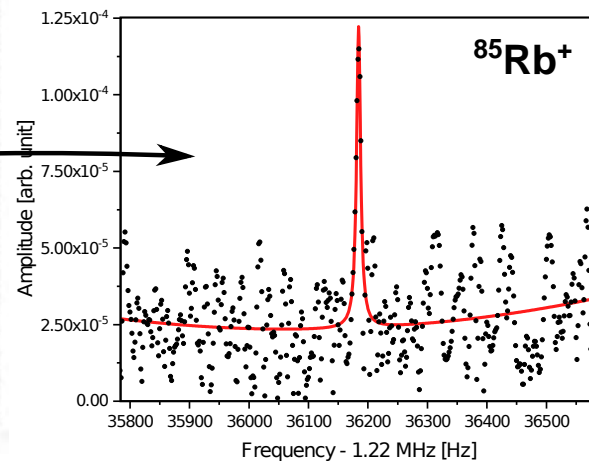
Scanning technique,  
Requires  $\sim 400$  ions for  
a measurement

# Towards Ultimate Sensitivity: SIPT

## Single Ion Penning Trap



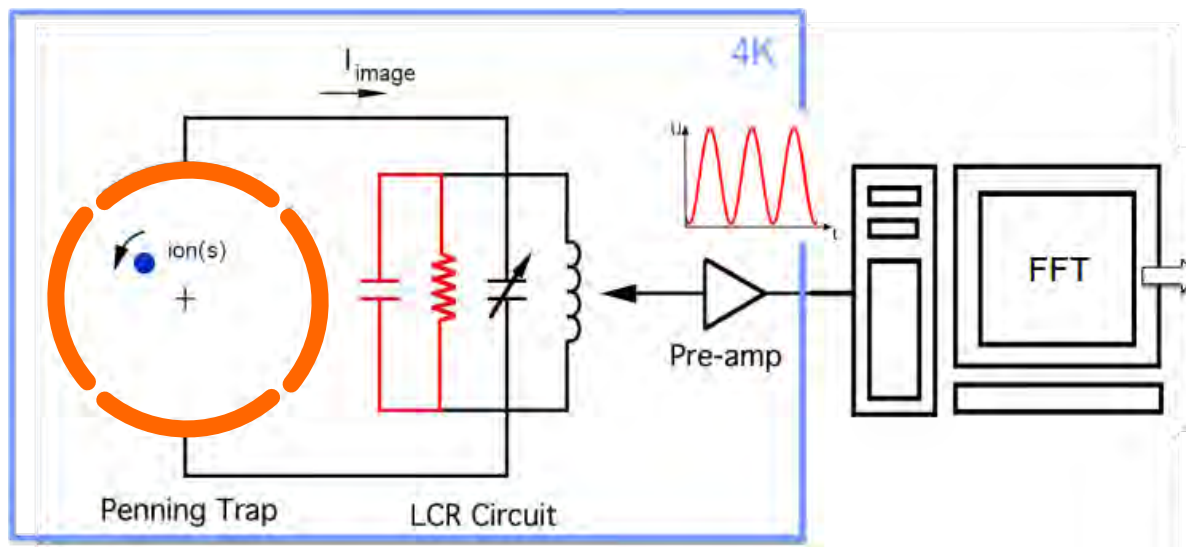
## Fourier Transform -ICR



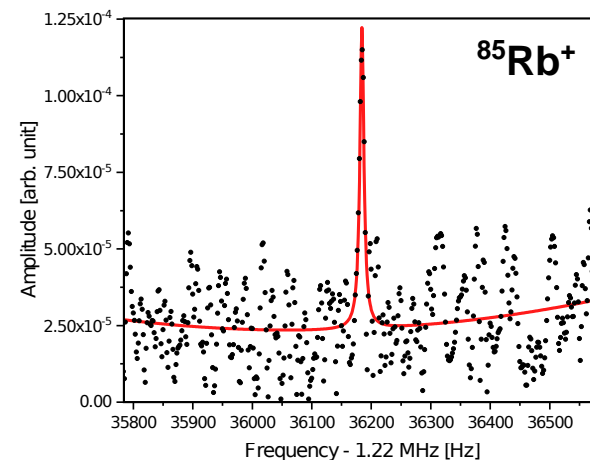
Non-Scanning technique,  
Ultimately requires 1 ion for  
a measurement

# Towards Ultimate Sensitivity: SIPT

## Fourier-Transform Ion-Cyclotron-Resonance Technique



Single ion signal!



1. Ion induces a weak (fA) signal into trap electrodes

2. Signal amplification and noise suppression (Cryogenic circuit)

3. Signal processing

4. Frequency determination

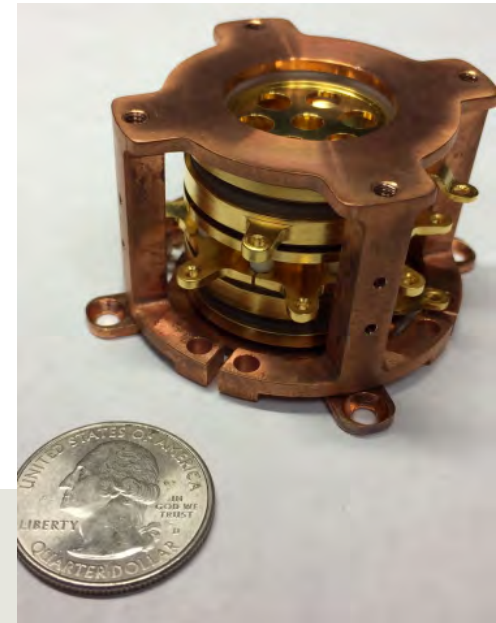
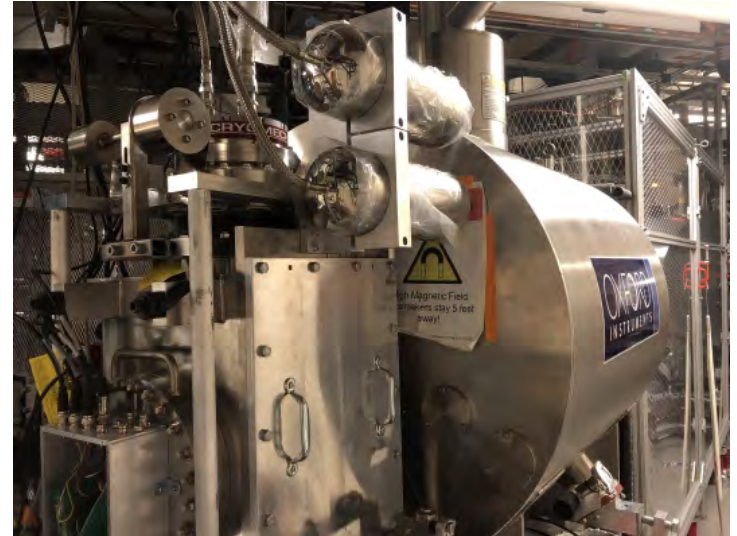
\* Can perform the measurement of many species at once



# Towards Ultimate Sensitivity: SIPT

## Current status

- Commissioned with stable beam
- Mass spectra from external beams acquired (2020)
- Signals from single ions detected (2021)
- **Currently:** improving signal quality to reach ultimate performance



PhD thesis work of A. Hamaker

# Summary

- Performed precision mass spectrometry of  $^{50-53}\text{Sc}$  at LEBIT (NSCL) and of  $^{54,55}\text{Sc}$  at TITAN (TRIUMF)
- Results help refine the evolution of N=32 shell closure at  $Z \geq 20$   
Smooth raise of  $\Delta_{2n}(N=32)$  through  $^{53}\text{Sc}$
- New state-of-the-art techniques will make best use of the intense FRIB beams

# Thank you!

## LEBIT/NSCL Team:

G. Bollen, B.A. Brown, E. Leistenschneider, A. Hamaker, C. Nicoloff, D. Puentes, M. Redshaw, R. Ringle, R. Sandler, C.S. Sumithrarachchi, A.A. Valverde, and I.T. Yandow.

## TITAN/TRIUMF Team:

E. Dunling, J. Dilling, J.D. Holt, A. Jacobs, A.A. Kwiatkowski, T. Miyagi, W.S. Porter, and M.P. Reiter

## Support:



U.S. DEPARTMENT OF  
**ENERGY**

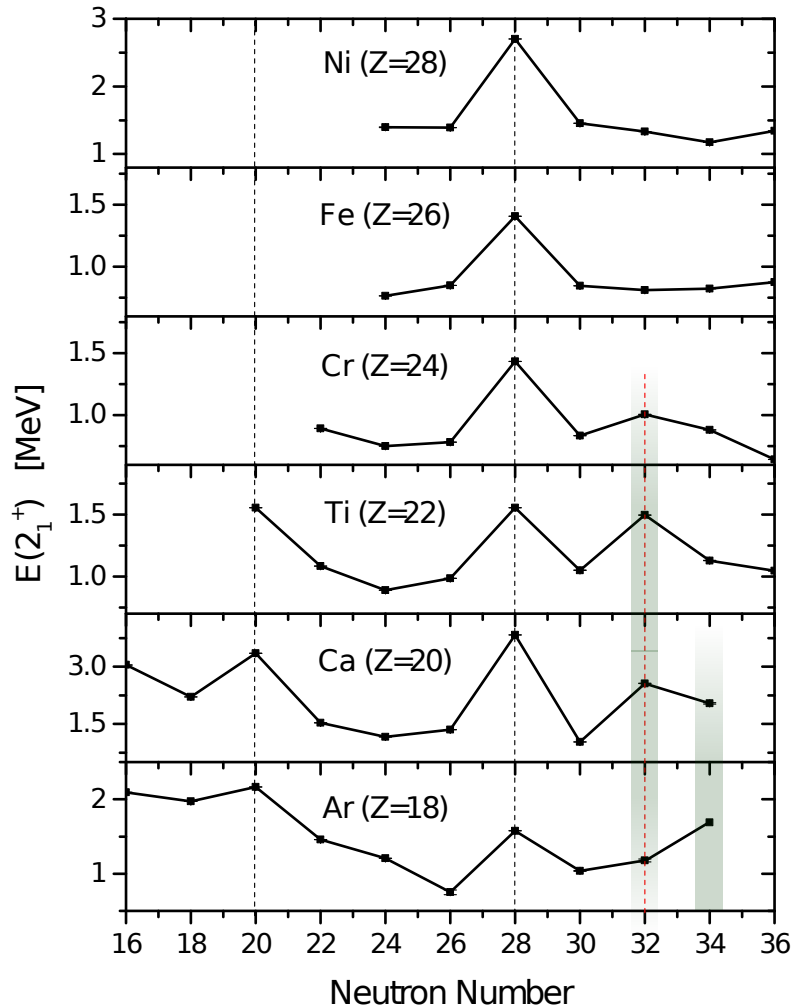
Office of  
Science

**MICHIGAN STATE**  
UNIVERSITY



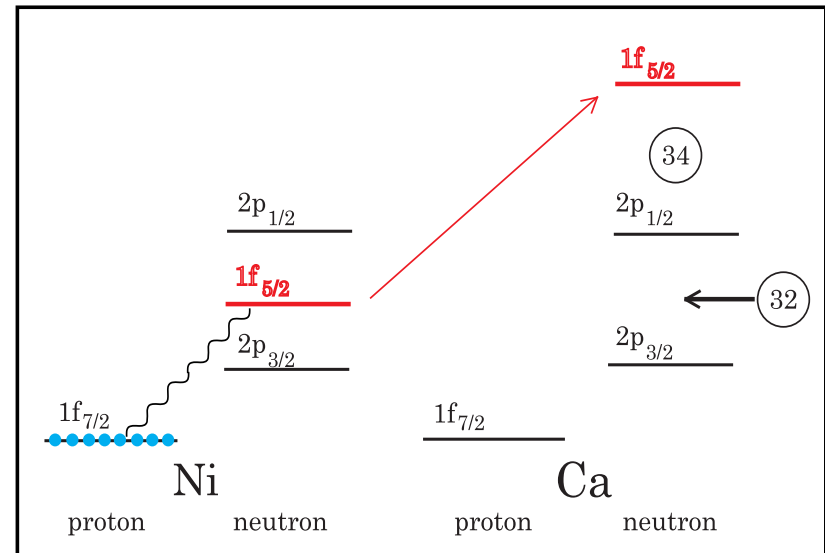
U.S. Department of Energy Office of Science  
National Science Foundation  
Michigan State University

# The emerging magic number 32 (and 34)



**First signatures:** excitation energies of  $2^+$  states of even-even nuclei

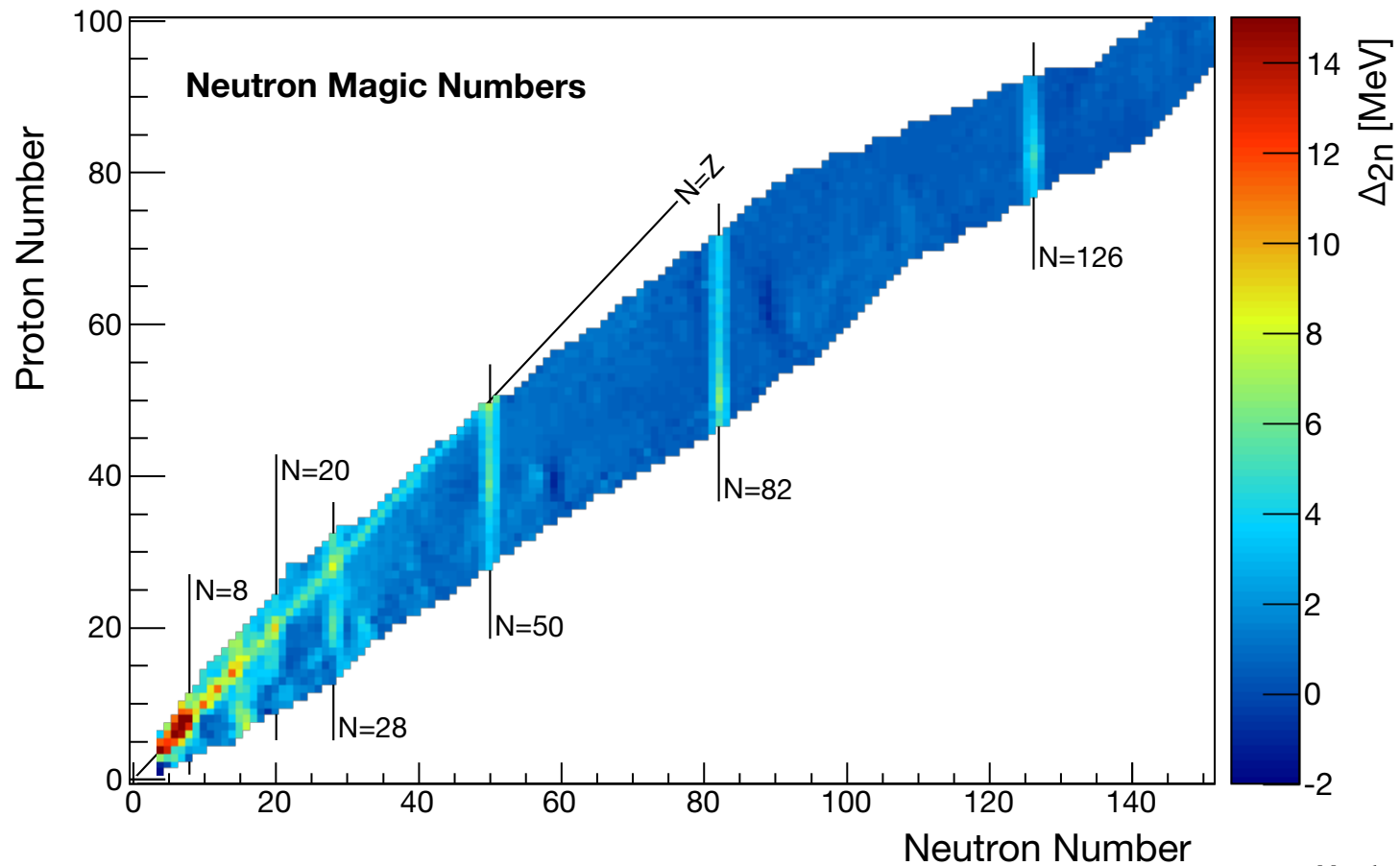
**Mechanism:** weakening of  $\pi f_{7/2} - \nu f_{5/2}$  interaction drives level inversion and appearance of energy gaps



T Otsuka and Y Tsunoda J. Phys. G: Nucl. Part. Phys. 43 024009 (2016)

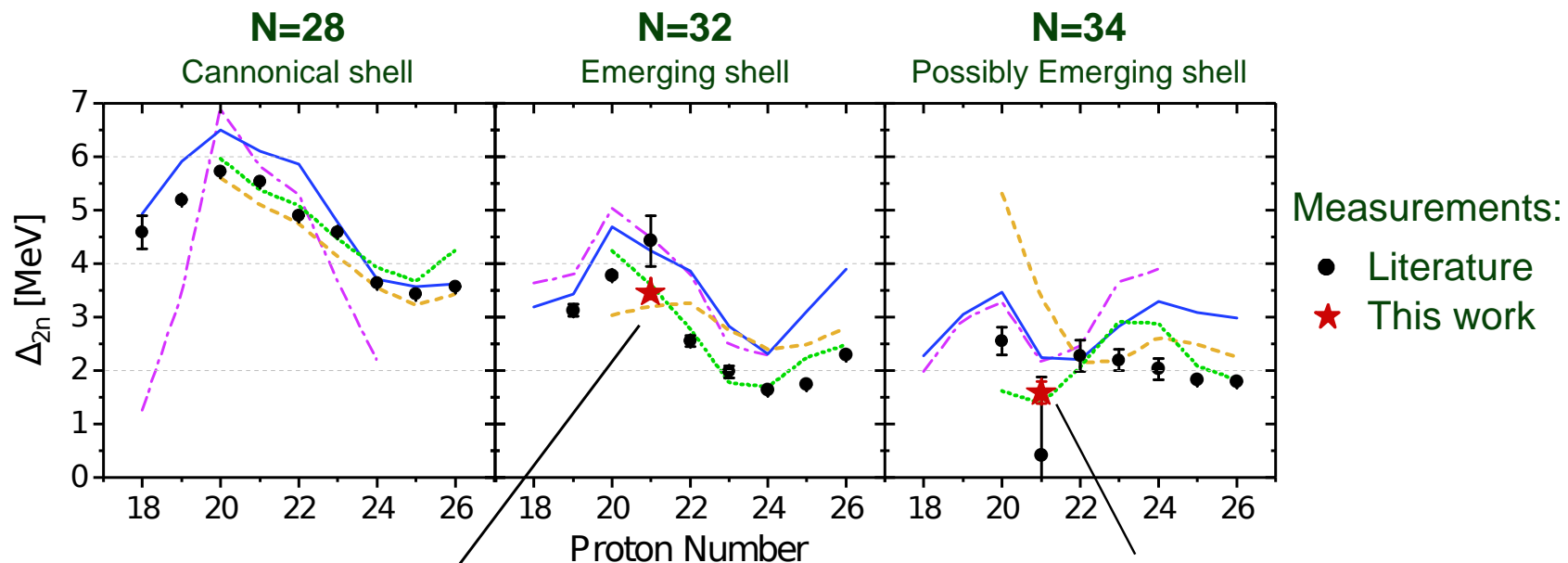
# Shell Closures in the Mass Surface

$$\Delta_{2n}(N,Z) = S_{2n}(N,Z) - S_{2n}(N+2,Z)$$



Mass data from AME16

# N=32 Shell Closure in Scandium



Smooth evolution of N=32

No evidence for N=34 shell effects above Z=20

## Predictions:

- 1.8/2.0(EM) }  $\chi$ EFT
- - - NN+3N(Inl) }  $\chi$ EFT
- - - GX1A } Phenomenological
- ..... KB3G } Phenomenological

Theories have good success at describing N=32, but deficiencies are found in the description of N=34