

# Proton-neutron interaction strength towards the $N=Z$ line

Israel Mardor

Tel Aviv University and Soreq Nuclear Research Center

NUSTAR Annual Meeting

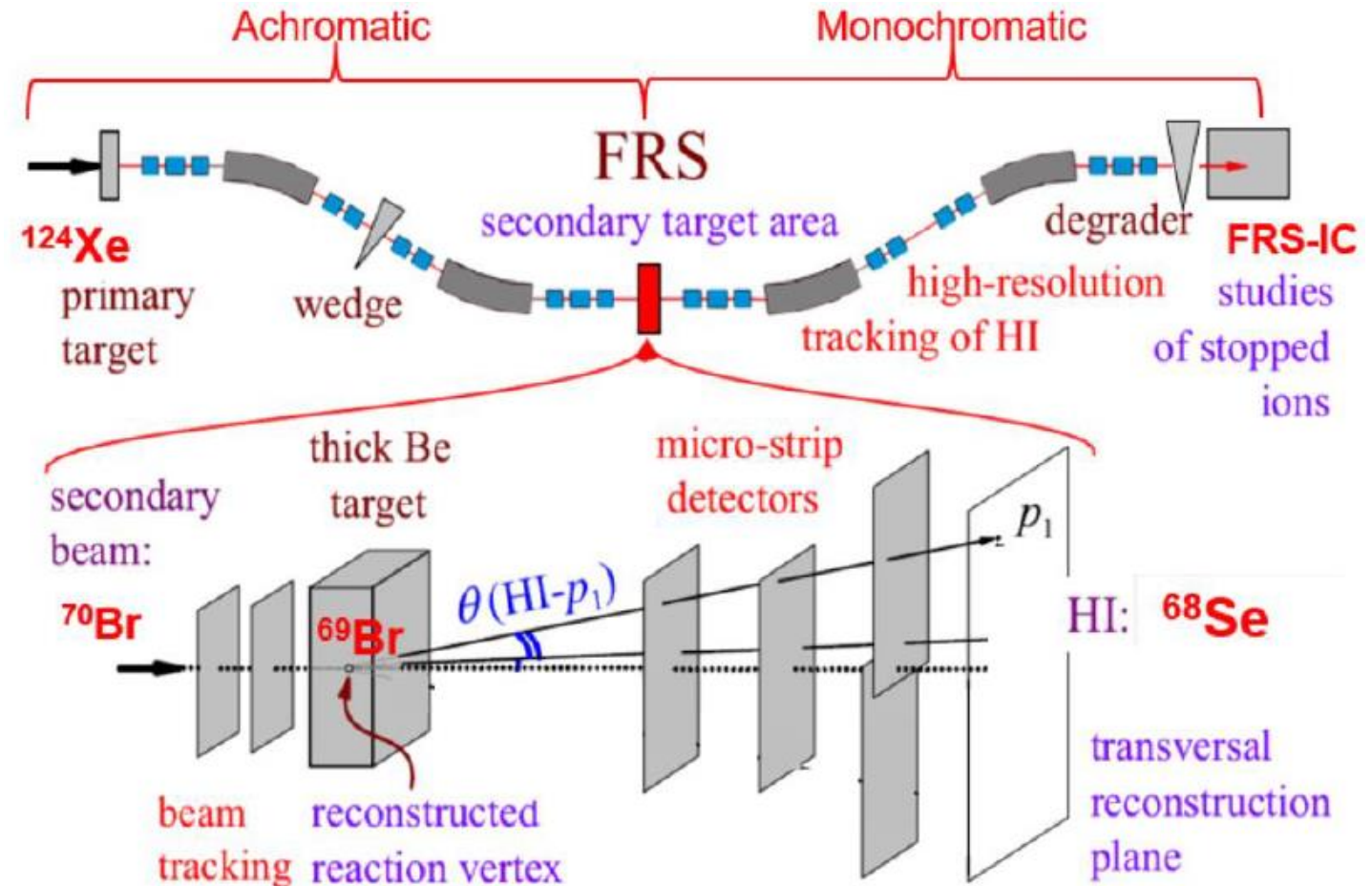
24 February 2021

# Talk Outline

- S459+ technical and mass measurement results
- Extraction of the proton-neutron interaction strength from masses
- Physics significance of our results
- Outlook
  - More measurements around the  $N = Z$  line
  - Extension to neutron-rich nuclei, around  $N_{\text{val}} \approx Z_{\text{val}}$  lines

# S459+: One beam, Two experiments

- Experiment **S472** of the FRS Ion Catcher Group and experiments **S459** and **S443** of the EXPERT group ran **jointly** in March 2020 (coined **S459+**)
- The two groups used **simultaneously the same primary beam** ( $^{124}\text{Xe}$ ), impinging on  $^9\text{Be}$ , to measure properties of exotic isotopes near and beyond the proton dripline
- The **FRS Ion Catcher** setup is at the final focus plane of the FRS (**S4**) whereas the **EXPERT** detectors are at its mid-focus (**S2**)

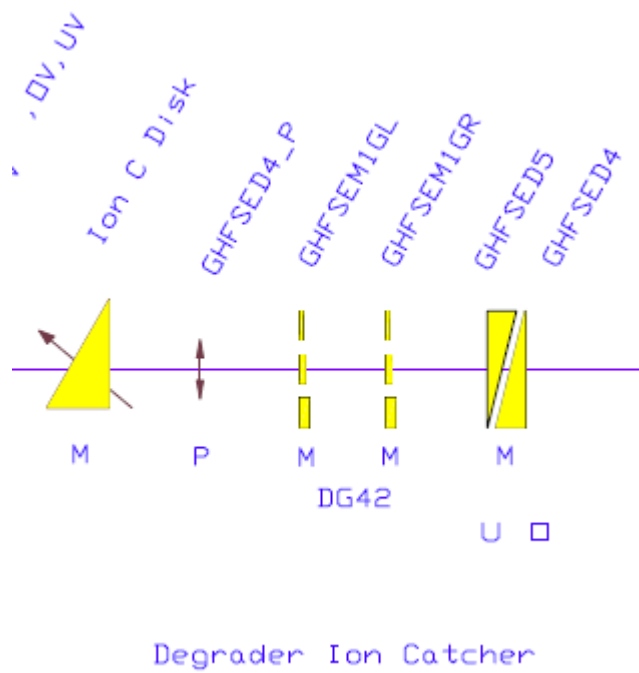


# Technical achievements

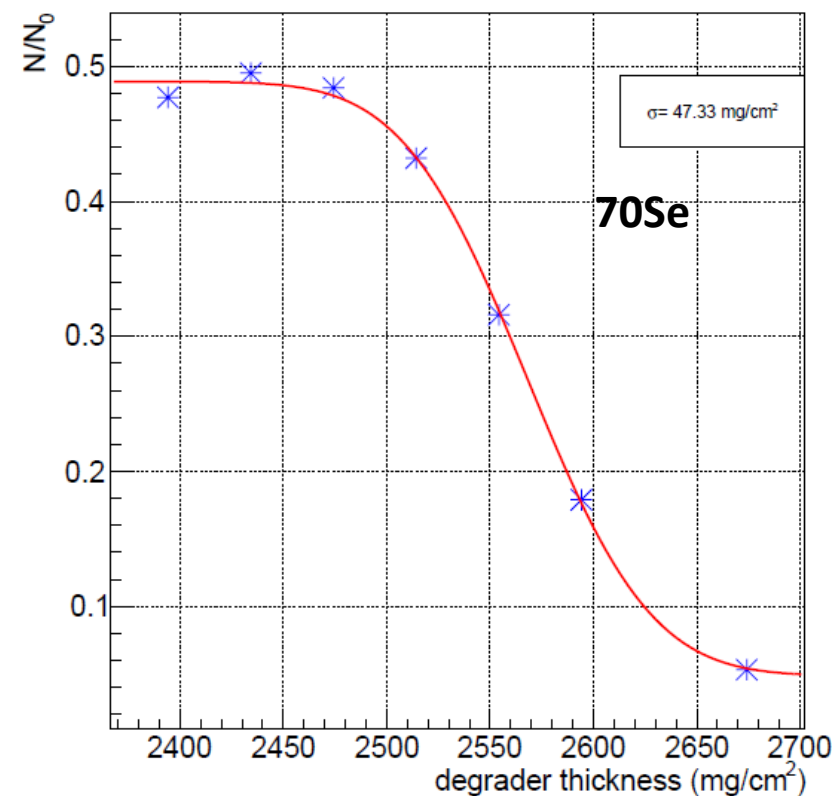
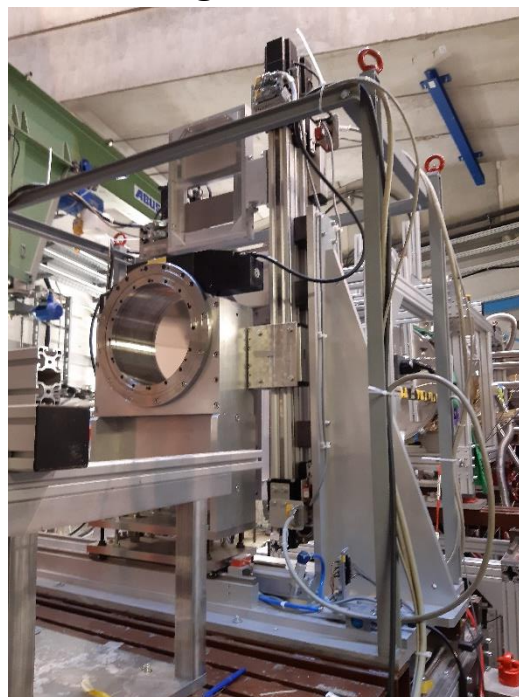
- Successful execution of two simultaneous experiments at the FRS, 're-using' part of the beam that went through EXPERT for technical and physics studies at the FRS Ion Catcher
- First **range bunching at S4** with the new degrader system

*C. Hornung talk tomorrow*

S4 degrader layout



S4 degrader ladder

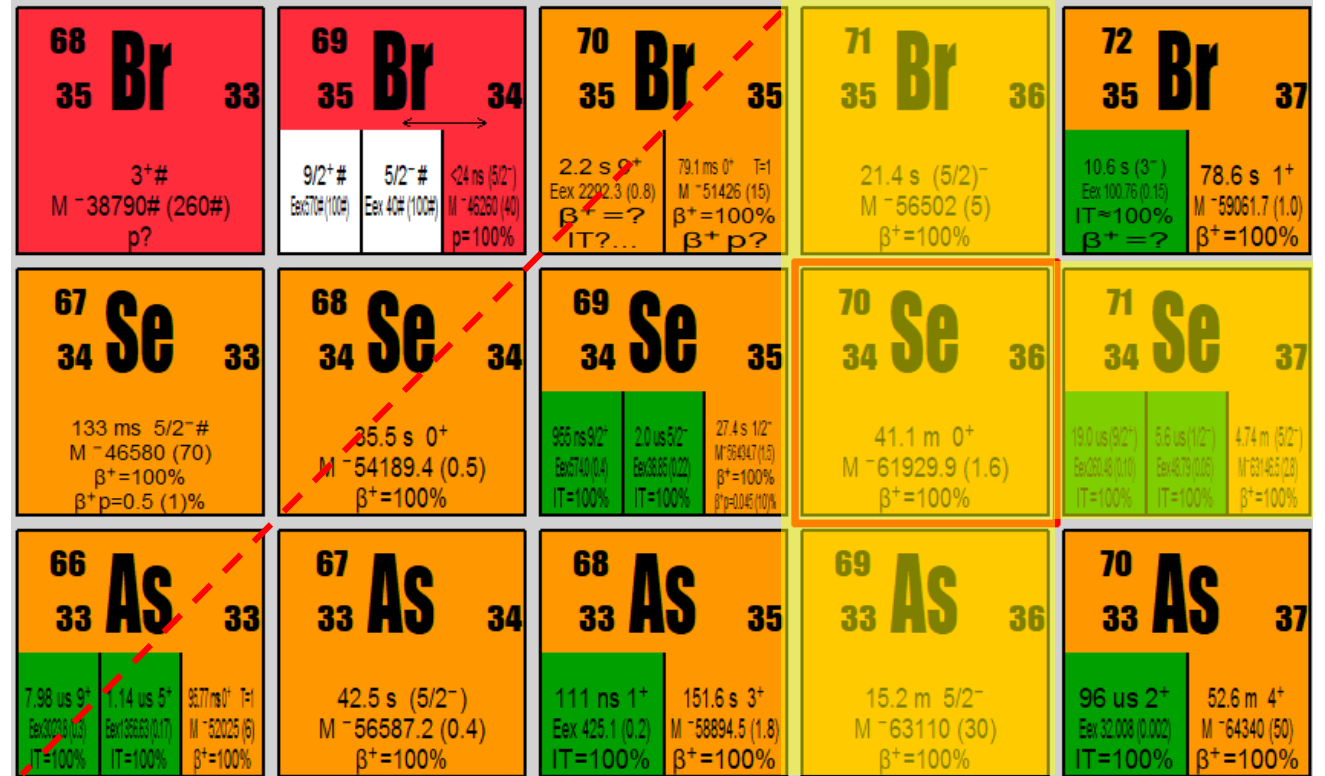


- **Mass tagging at  $A \sim 70$** , confirming particle ID system of the FRS and EXPERT
- Extension of Ion Catcher range down to  **$A \sim 70$  region** (Previous low was 94)

*L. Gröf*  
*M.Sc. Thesis*

# Mass measurements

- Measured the masses of  $^{69}\text{As}$ ,  $^{70,71}\text{Se}$ ,  $^{71}\text{Br}$
- The  $N \rightarrow Z$   $A \sim 70$  area is important for
  - The rp-process
  - Nuclear structure (isospin symmetry, Wigner energy, p-n interaction)
  - Nuclei in this region have rapidly changing varying shapes (the “Wild West”<sup>1</sup>)

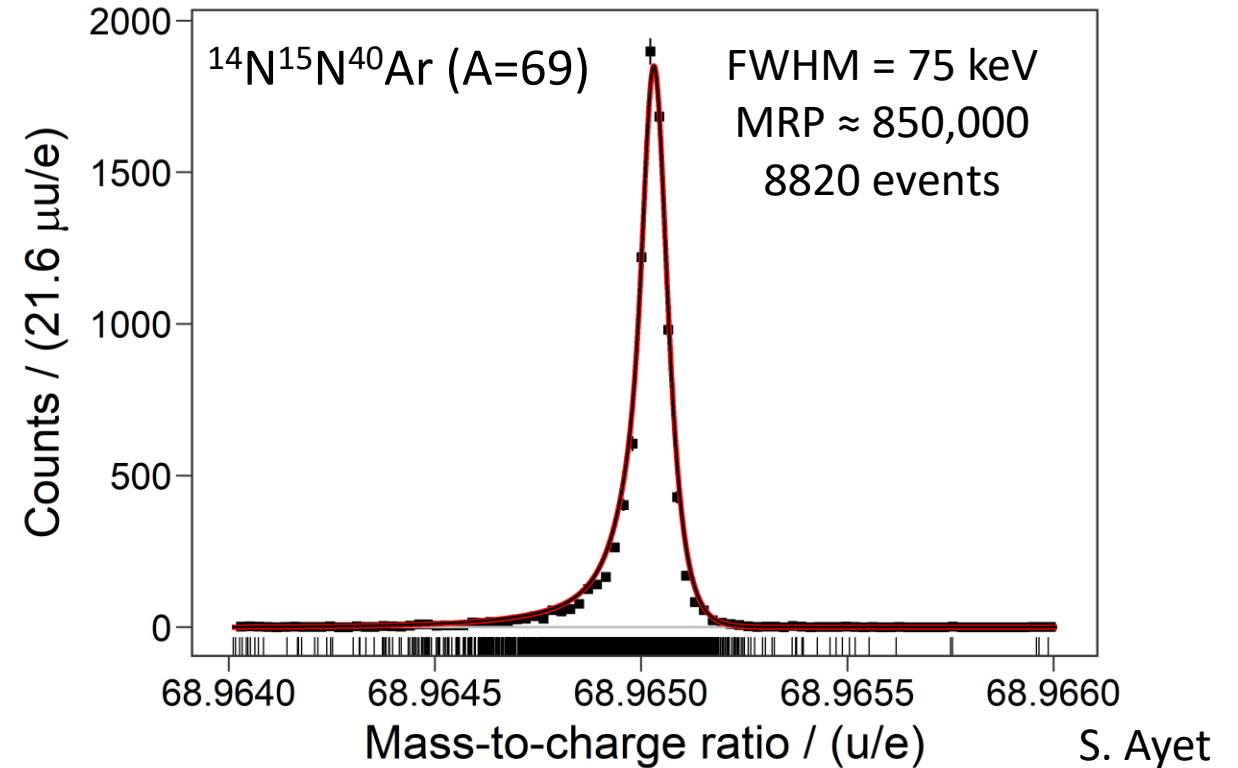


--- N=Z line

<sup>1</sup>W. Nazarewicz, High Spin Physics and Gamma-soft Nuclei, 1991

# Mass calibrations with stable molecules

- 4 stable molecules for same- and different-turn number with respect to ion-of-interest:
  - $^{12}\text{C}_5^1\text{H}_{10}$  ( $A=70$ )
  - $^{12}\text{C}_5^1\text{H}_9$  ( $A=69$ )
  - $^{14}\text{N}^{15}\text{N}^{40}\text{Ar}$  ( $A=69$ )
  - $^{12}\text{C}^{19}\text{F}_3$  ( $A=69$ ) (*most abundant*)
- Used  $^{12}\text{C}^{19}\text{F}_3$  ( $A=69$ ) and 2 others to calibrate 4<sup>th</sup> molecule's mass
- Literature mass values  $\sim 10^{-11}$  level

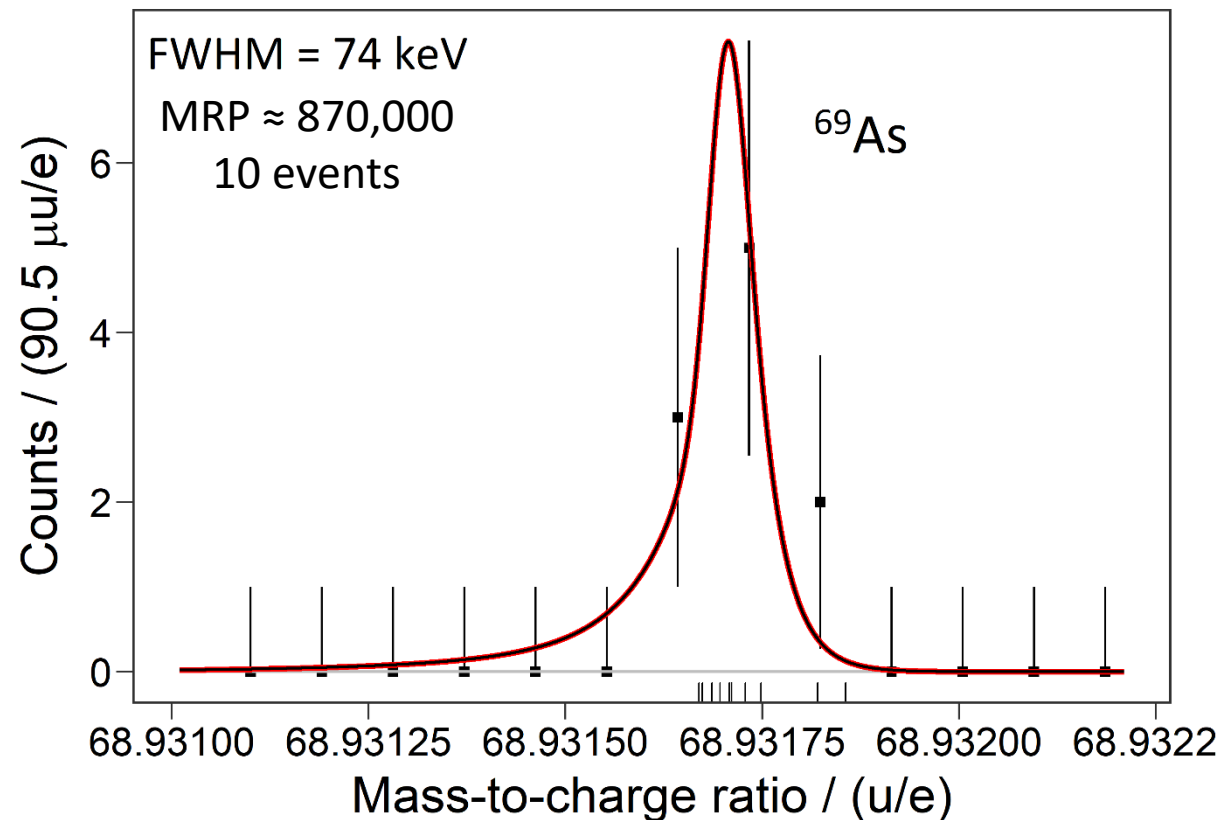


Molecule	Lit. Deviation [keV]	Relative unc. $\delta m/m$
$^{12}\text{C}_5^1\text{H}_9$	$0.9 \pm 2.9$	$4.5 \times 10^{-8}$
$^{12}\text{C}_5^1\text{H}_{10}$	$-1.2 \pm 2.9$	$4.4 \times 10^{-8}$
<b><math>^{14}\text{N}^{15}\text{N}^{40}\text{Ar}</math></b>	<b><math>0.1 \pm 1.1</math></b>	<b><math>1.7 \times 10^{-8}</math></b>

***World record for MR-TOF-MS!***

# Mass measurement of $^{69}\text{As}$

- First **direct** mass measurement of  $^{69}\text{As}$
- Previously : 3 indirect measurements (positron end-point), with  $\pm 50$  keV uncertainties, and inconsistencies amongst them
- Our value obtained with **10 events**
- Agreement with AME16, with improved uncertainty  $\pm 22$  keV ( $\delta m/m = 2.8 \times 10^{-7}$ )
  - AME16 is a weighted average of the 3 previous indirect measurement
  - Origin of the selected weights is not clear



S. Ayet

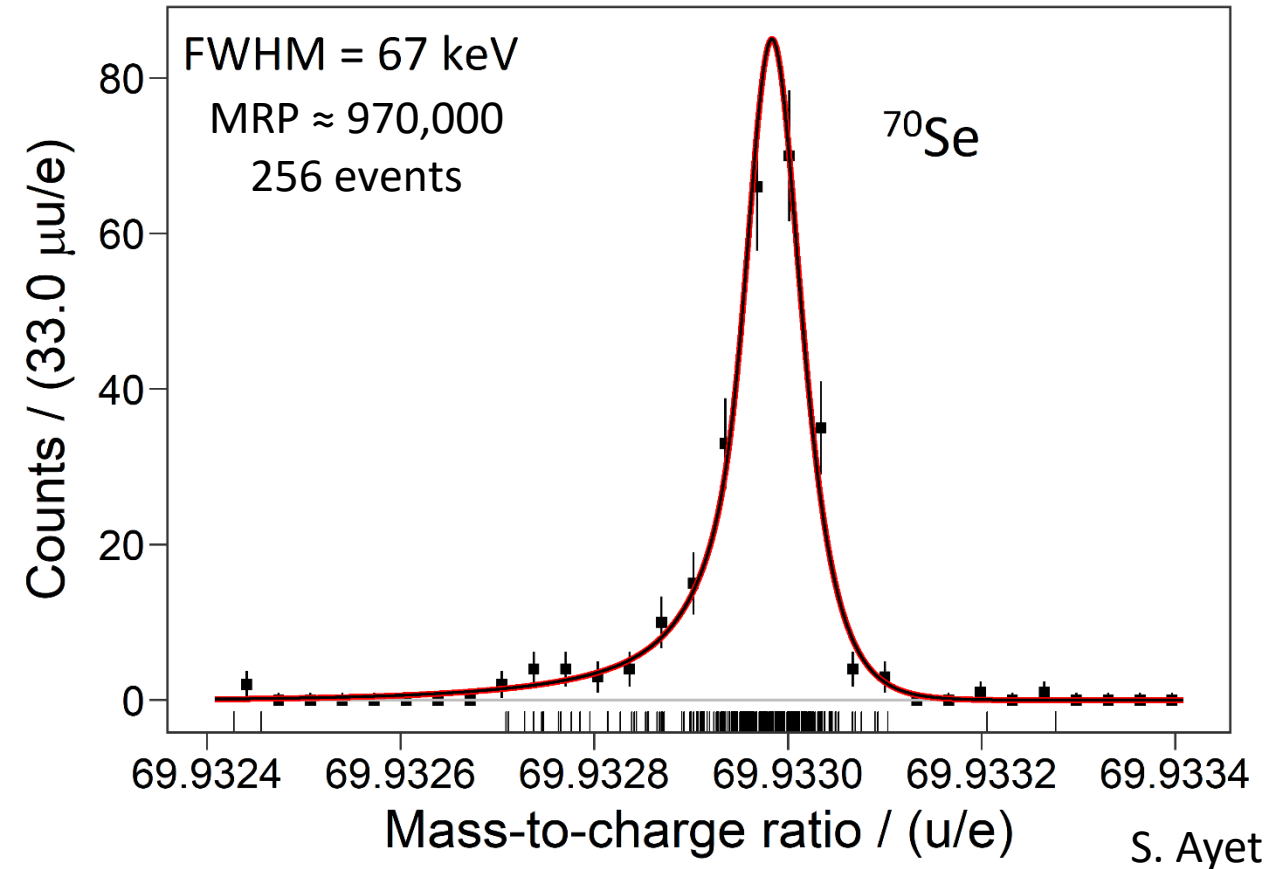
- Same turn-number calibration:  $^{12}\text{C}^{19}\text{F}_3$  (A=69)
- Total ToF: 23.1 ms

For all measurements:  **$\sim 900$  turns** in MR-TOF-MS

Mardor, Ayet, Dickel et al., 2011.13288 (2020)

# Mass measurement of $^{70}\text{Se}$

- 485 events collected
- Mass uncertainty **2.6 keV**  
( $\delta m/m = 4.0 \times 10^{-8}$ ), second only to MR-TOF-MS world record of  $3.5 \times 10^{-8}$  (for unstable nuclei)
- World record is with 19,000 events
- Agreement with AME16
- AME16 is based on one Penning trap measurement (others are with much higher uncertainty)
- Our result is the only high-accuracy confirmation

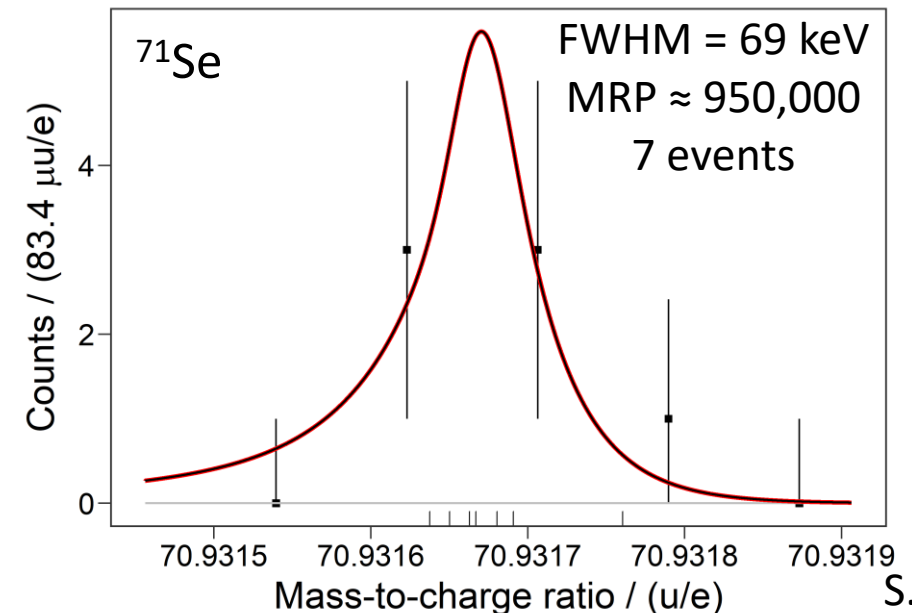
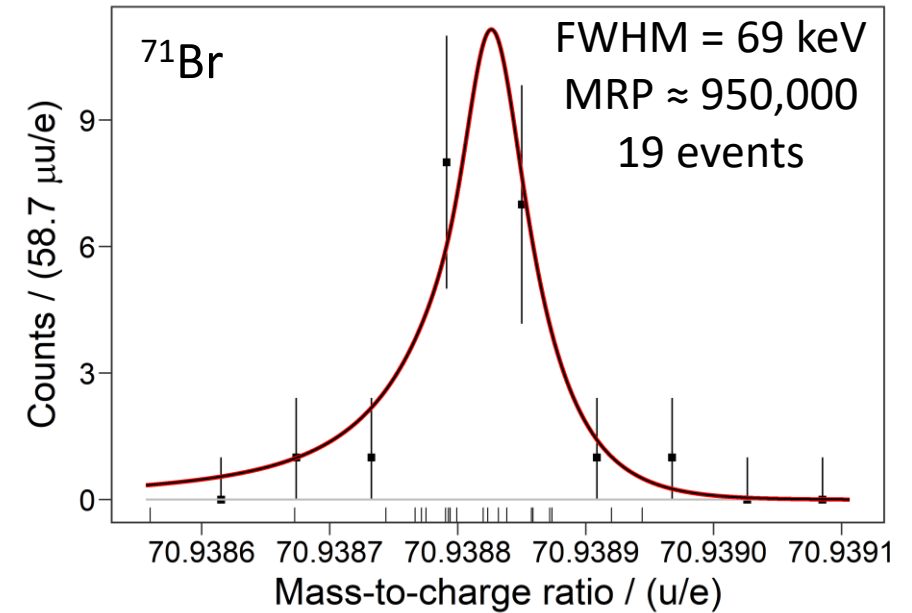


- Same- and multi-turn calibrations with four molecules
- Total ToF: 21.9 and 23.1 ms

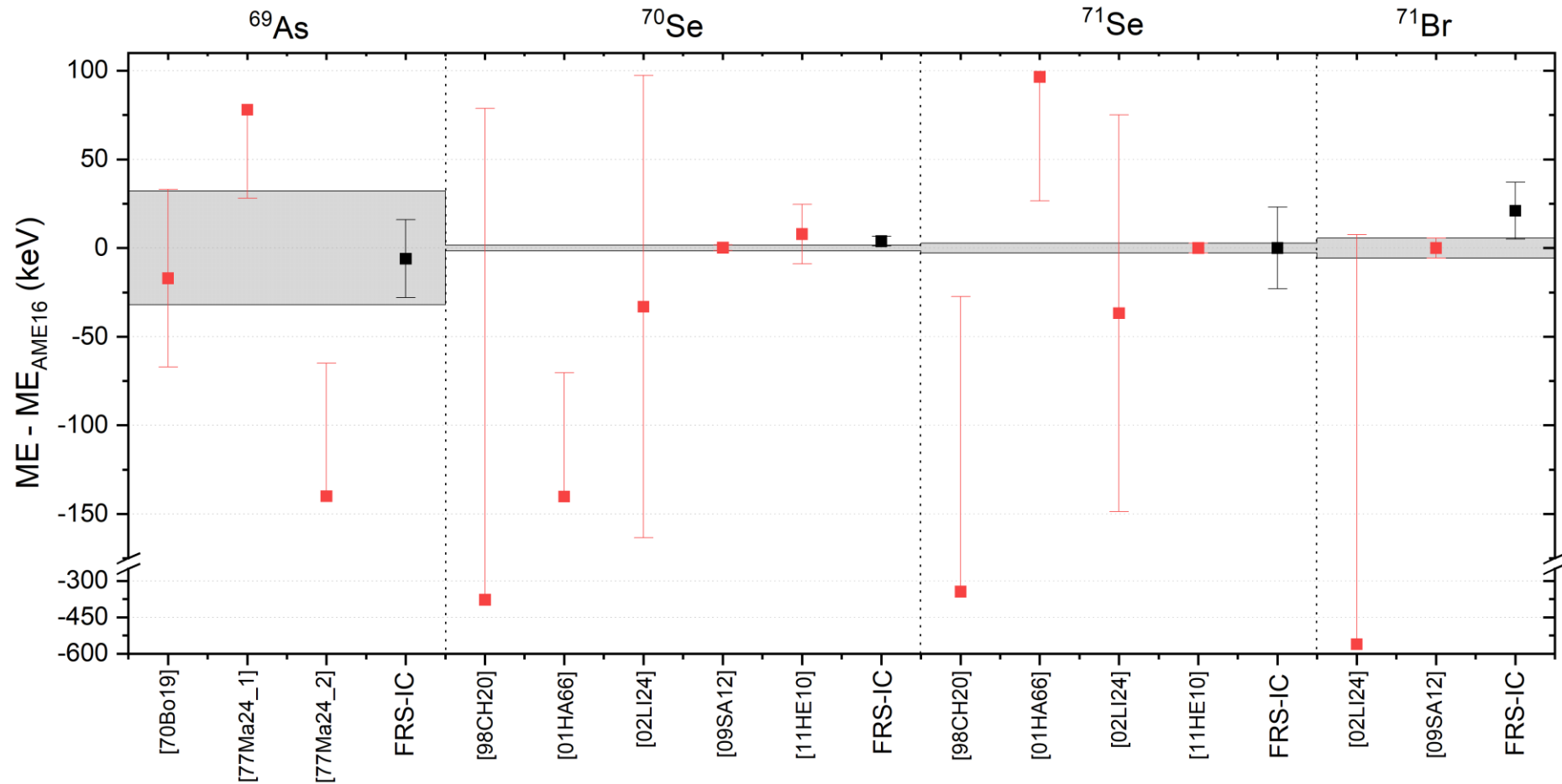
# Mass measurements of $^{71}\text{Se}$ , $^{71}\text{Br}$

- Obtained mass values with only **19 ( $^{71}\text{Br}$ )** and **7 ( $^{71}\text{Se}$ )** events, in the same measurement
- Mass uncertainties of **16** and **23 keV**
- Both results agree with AME16
- For both nuclei, AME16 values are based on one Penning trap result. Our result is the only high-accuracy confirmation

- Multi turn-number calibration:  $^{13}\text{C}^{19}\text{F}_3$  ( $A=70$ )
- Total ToF: 23.1 ms



# Mass measurements summary



Mardor, Ayet, Dickel  
et al., 2011.13288  
(2020)

Nuclei	Half-Life	$ME_{\text{FRS-IC}}$ [keV]	$ME_{\text{AME16}}$ [keV]	$ME_{\text{FRS-IC}} - ME_{\text{AME16}}$ [keV]	Events
$^{69}\text{As}$	$15.2 \pm 0.2 \text{ min}$	$-63\,116 \pm 22$	$-63\,110 \pm 30 \dagger$	$-6 \pm 37$	10
$^{70}\text{Se}$	$41.1 \pm 0.3 \text{ min}$	$-61\,926.0 \pm 2.6$	$-61\,929.9 \pm 1.6$	$3.9 \pm 3.0$	485
$^{71}\text{Se}$	$4.74 \pm 0.05 \text{ min}$	$-63\,147 \pm 23$	$-63\,146.5 \pm 2.8$	$0 \pm 23$	7
$^{71}\text{Br}$	$21.4 \pm 0.6 \text{ s}$	$-56\,481 \pm 16$	$-56\,502 \pm 5$	$21 \pm 17$	10 19

# Technical significance of our mass resolving power

- In principle, mass uncertainty could be improved indefinitely by accumulating more and more events, even with mediocre mass resolving power
- In practice, mass uncertainty is hindered by:
  - Unresolved overlapping peaks of isobars and isomers
  - Limited number of events for rare isotopes
- We achieved excellent uncertainties at low number of events due to the **FRS-IC MR-TOF-MS** unprecedented mass-resolving-power (MRP) of ***1,000,000***

# The “physics story” - proton-neutron interaction strength

- Average interaction strength the ‘last’ (valence) proton(s) and neutron(s):

$$\delta V_{np}^{ee} = \frac{1}{4} \{ [B(N, Z) - B(N - 2, Z)] - [B(N, Z - 2) - B(N - 2, Z - 2)] \} \quad \text{last two n + two p (4 combinations)}$$

$$\delta V_{np}^{eo} = \frac{1}{2} \{ [B(N, Z) - B(N - 2, Z)] - [B(N, Z - 1) - B(N - 2, Z - 1)] \} \quad \text{last two n + one p (2 combinations)}$$

$$\delta V_{np}^{oe} = \frac{1}{2} \{ [B(N, Z) - B(N, Z - 2)] - [B(N - 1, Z) - B(N - 1, Z - 2)] \} \quad \text{last one n + two p (2 combinations)}$$

$$\delta V_{np}^{oo} = \{ [B(N, Z) - B(N - 1, Z)] - [B(N, Z - 1) - B(N - 1, Z - 1)] \} \quad \text{last one n + one p (1 combination)}$$

Assuming that the **nuclear core remains essentially unchanged** for the four nuclei in each equation,

these double differences **cancel out** the **p-p** and **n-n pairing** interactions and the **mean field component** of the binding energy,

***isolating the empirical p-n interaction strength***

J.-Y. Zhang et al., Phys. Lett. B, 227, 1 (1989)

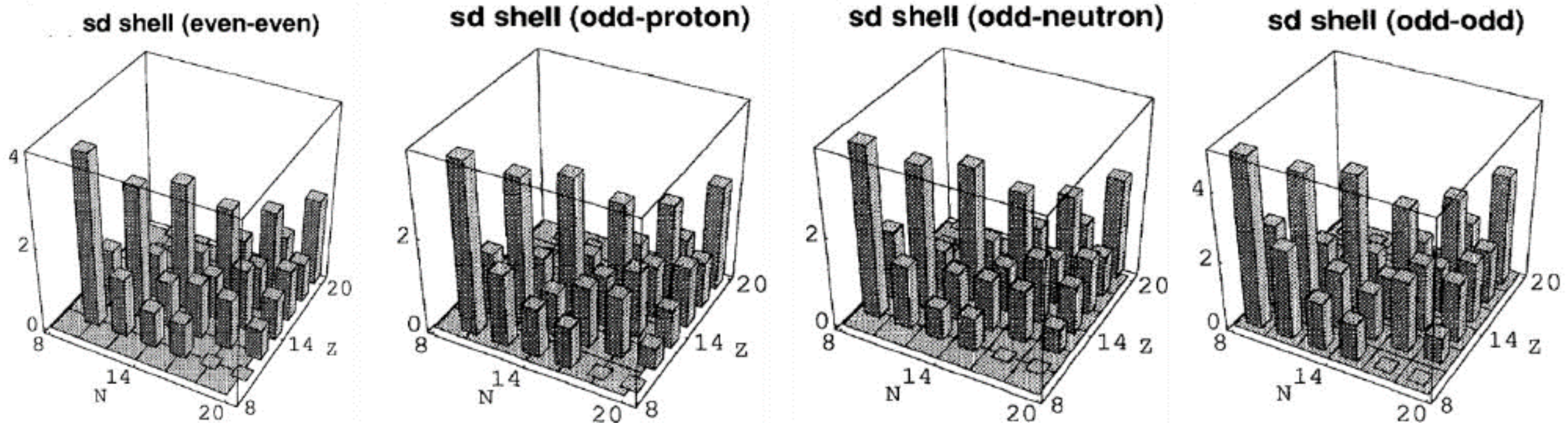
R. B. Cakirli et al., Phys. Rev. Lett., 94, 092501 (2005)

R. B. Cakirli, et al., Phys. Rev. Lett., 96 132501 (2006)

M. Stoitsov, et al., Phys. Rev. Lett., 98, 132502 (2007)

# Expected trends of $\delta V_{pn}$

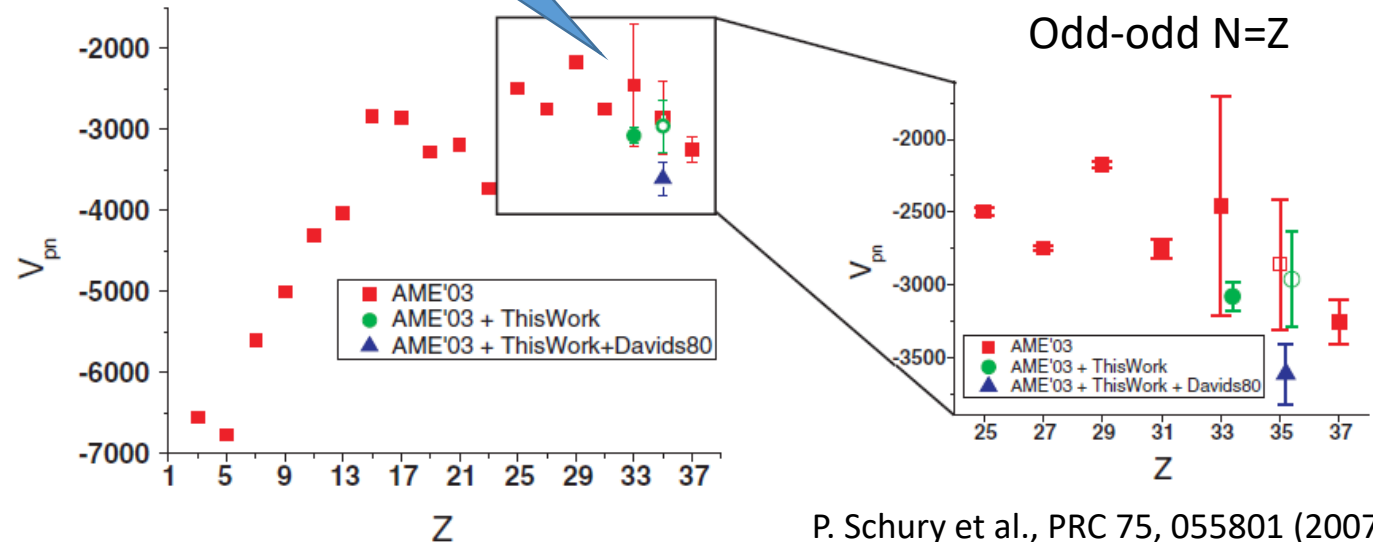
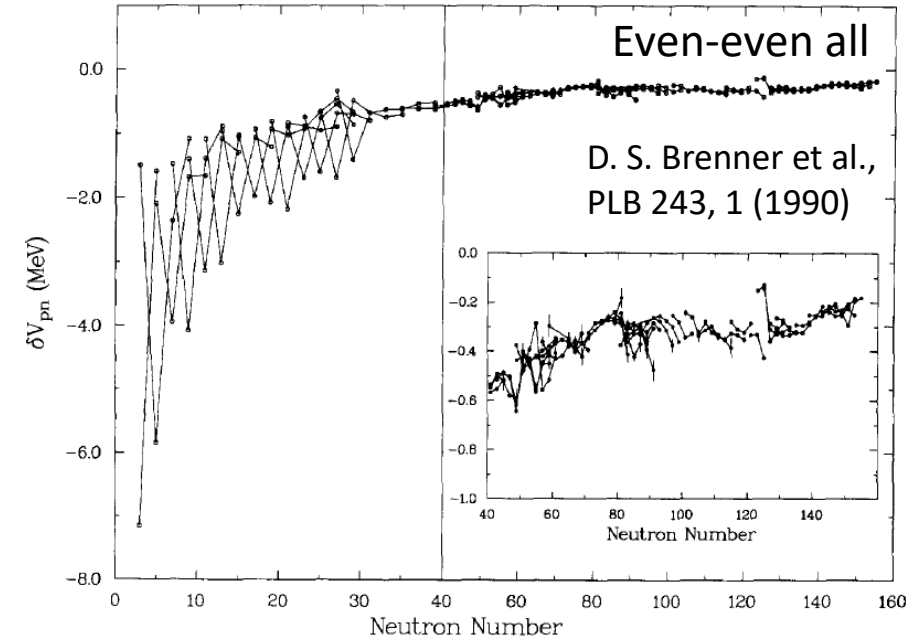
- $\delta V_{pn}$  has been related to the spatial overlap between the last p and n wave functions
  - N $\approx$ Z nuclei should have much higher  $\delta V_{pn}$  values than neighbors



# Expected trends of $\delta V_{pn}$

- $\delta V_{pn}$  has been related to the spatial overlap between the valence p and n wave functions
- $\delta V_{pn}$  should decrease with increasing mass because:
  1. Distance between p and n wave functions increase with nuclear radii
  2. Coulomb forces increase with Z, differentiating p and n wave functions
  3. Spin-orbit interaction increases, breaking spin-isospin SU(4) symmetry

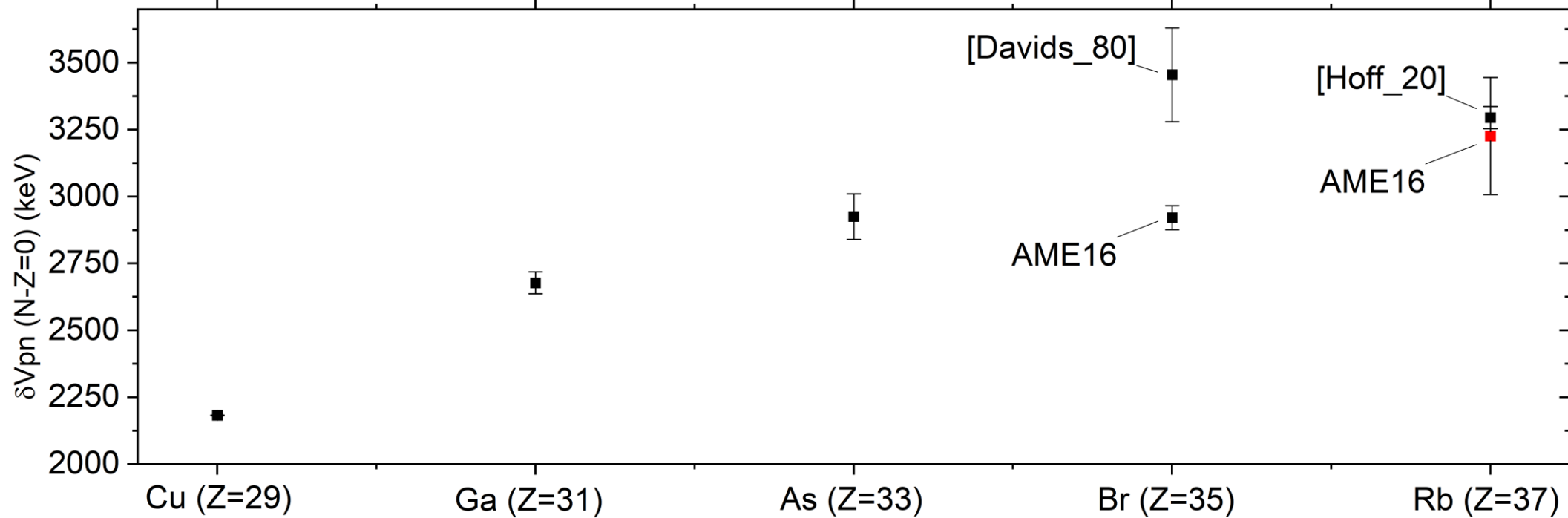
“indication of a trend toward the re-strengthening of  $\delta V_{np}$ ”



P. Schury et al., PRC 75, 055801 (2007)

# Odd-Odd N=Z $\delta V_{pn}$ from Z=29 to Z=37

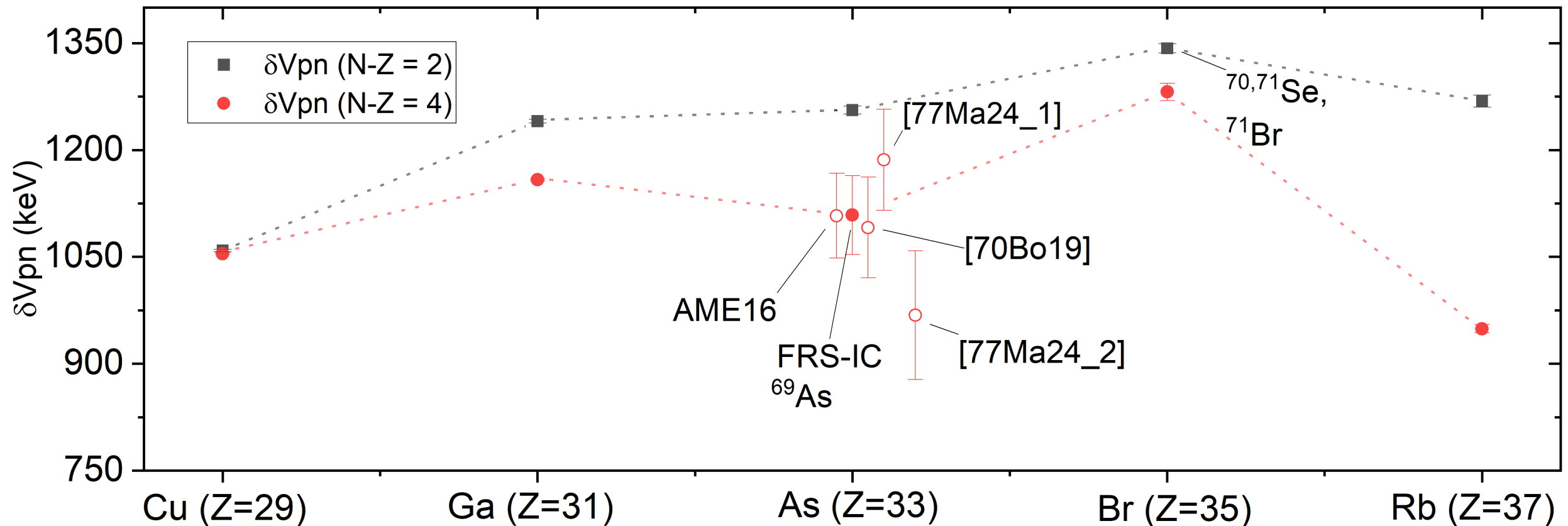
Use recent standard of positive  $\delta V_{pn}$



- Br: Included values from both  $^{70}\text{Br}$  mass measurements. [Davids\_80] is from the value that is consistent with the  $Ft$  world average
- Rb: Included values from AME16 evaluation of  $^{73}\text{Rb}$  mass (red) and very recent (October 2020) indirect measurement [Hoff\_20] (PRC 102, 045810 (2020), published 20 October 2020 )
- **The  $\delta V_{pn}$  re-strengthening trend may be confirmed**

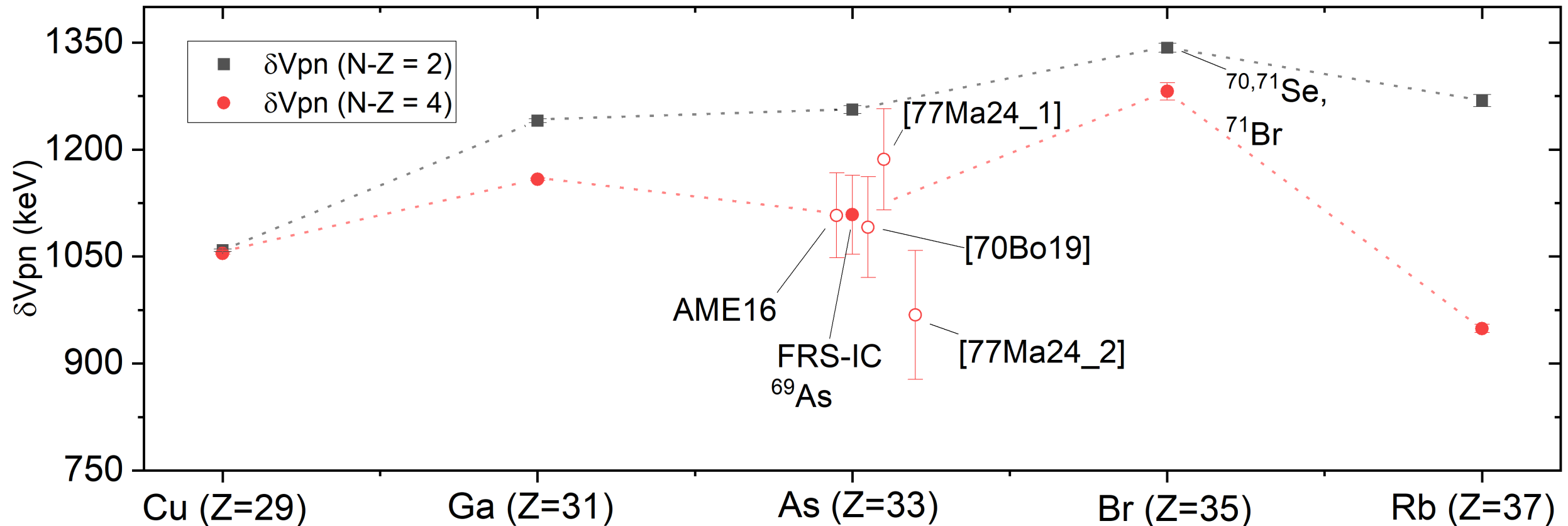
# Contribution of our measurements (goals)

- Investigate whether  $\delta V_{pn}$  restrengthening occurs also for odd-odd N-Z=2 and N-Z=4 nuclei
- Study detailed trends of N=Z+2 and N=Z+4 to obtain hints on  $^{70}\text{Br}$  discrepancy



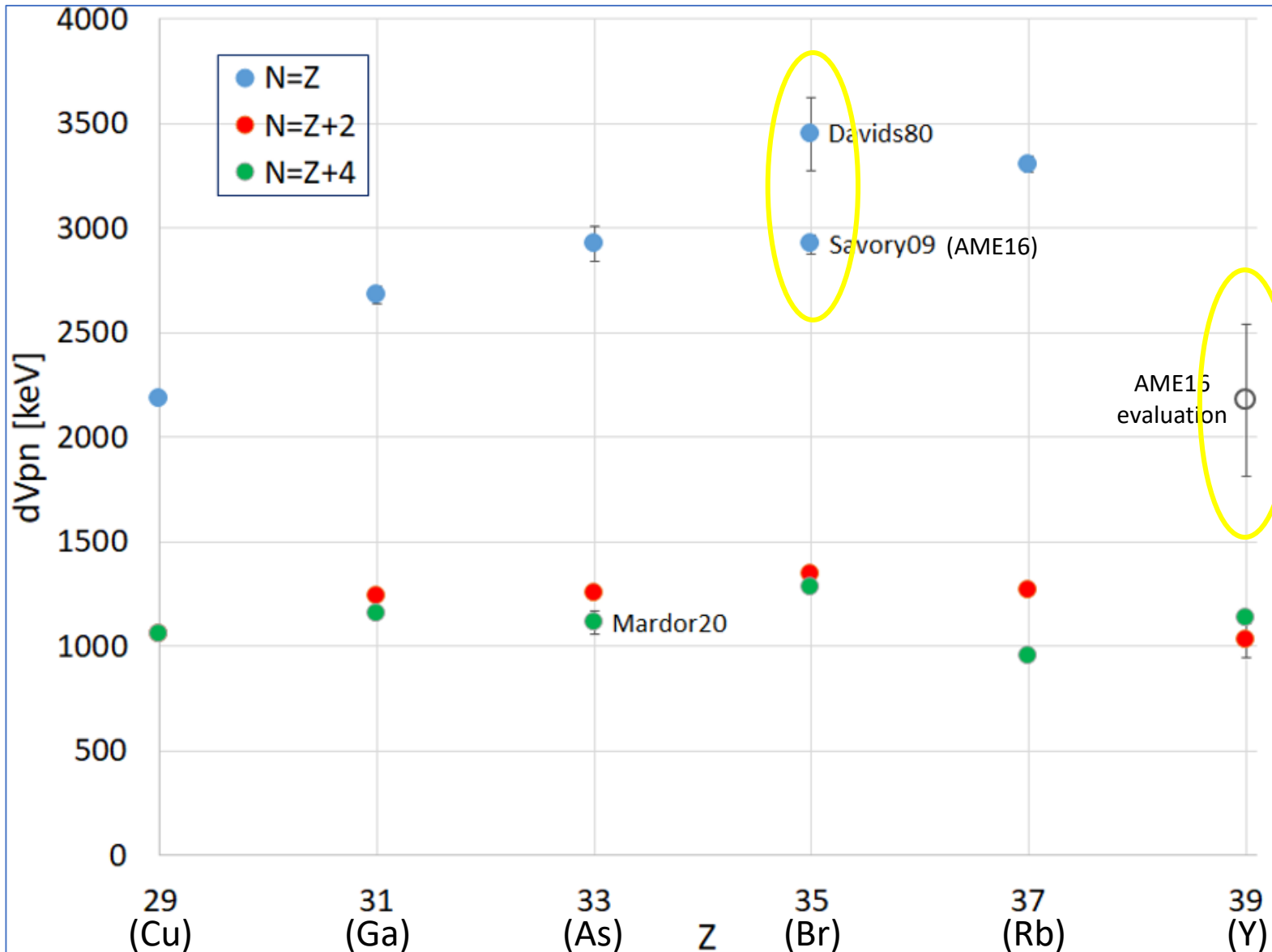
# Contribution of our measurements (results)

- $^{69}\text{As}$  measurement sets  $\text{As}(N-Z=4)$  value.  $^{70,71}\text{Se}$  and  $^{71}\text{Br}$  measurements confirm  $\text{Br}(N-Z=2)$  value.
- $N-Z=2$  and  $N-Z=4$   $\delta V_{pn}$  values much lower than  $N=Z$ . Restrengthening is hardly (non) evident at  $N-Z=2$  (4)
- Restrengthening is a sole property of the  $N=Z$  odd-odd nuclei



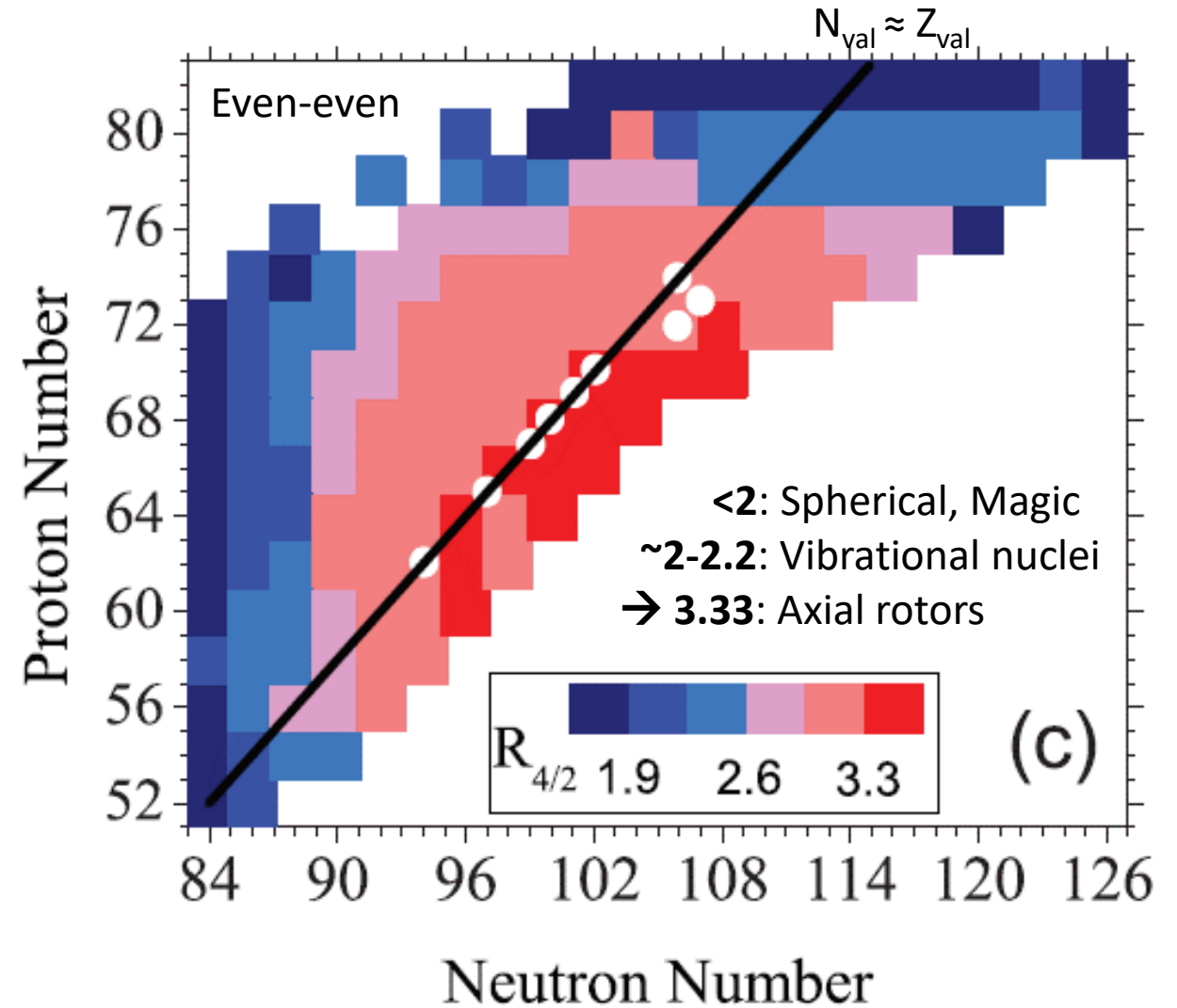
# Physics conclusions and outlook

- $\delta V_{pn}(N=Z)$  increase may be due to partial restoration of a symmetry that is unique to these nuclei
- It has been proposed that protons and neutrons occupying the pf-shell above the magic number 28 exhibit a **pseudo-SU(4) symmetry**. Perhaps this data supports this
- $\delta V_{pn}(N=Z+2)$  and  $\delta V_{pn}(N=Z+4)$  peak at Br. This may suggest that  $\delta V_{pn}(N=Z)$  should also peak at Br, meaning that  **$m(^{70}\text{Br})$  is closer to [Davids80]**
- **S526** measurements include  $^{70}\text{Br}$  and  $^{77,78}\text{Y}$ . Will 'straighten out' this plot
- $^{78}\text{Y}$  especially interesting, due to uncertainty in g.s. – isomer assignment



# $\delta V_{pn}$ measurements of n-rich nuclei

- It has been proposed that  $\delta V_{pn}$  should be enhanced also in neutron-rich nuclei with  $N_{\text{val}} \approx Z_{\text{val}}$  (above doubly-magic cores)
- Emergence of a reduced form of Wigner-like energy and SU(4) symmetry and/or onset of nuclear deformation
- related to the spatial overlap of the last neutron(s) and proton(s) wave functions



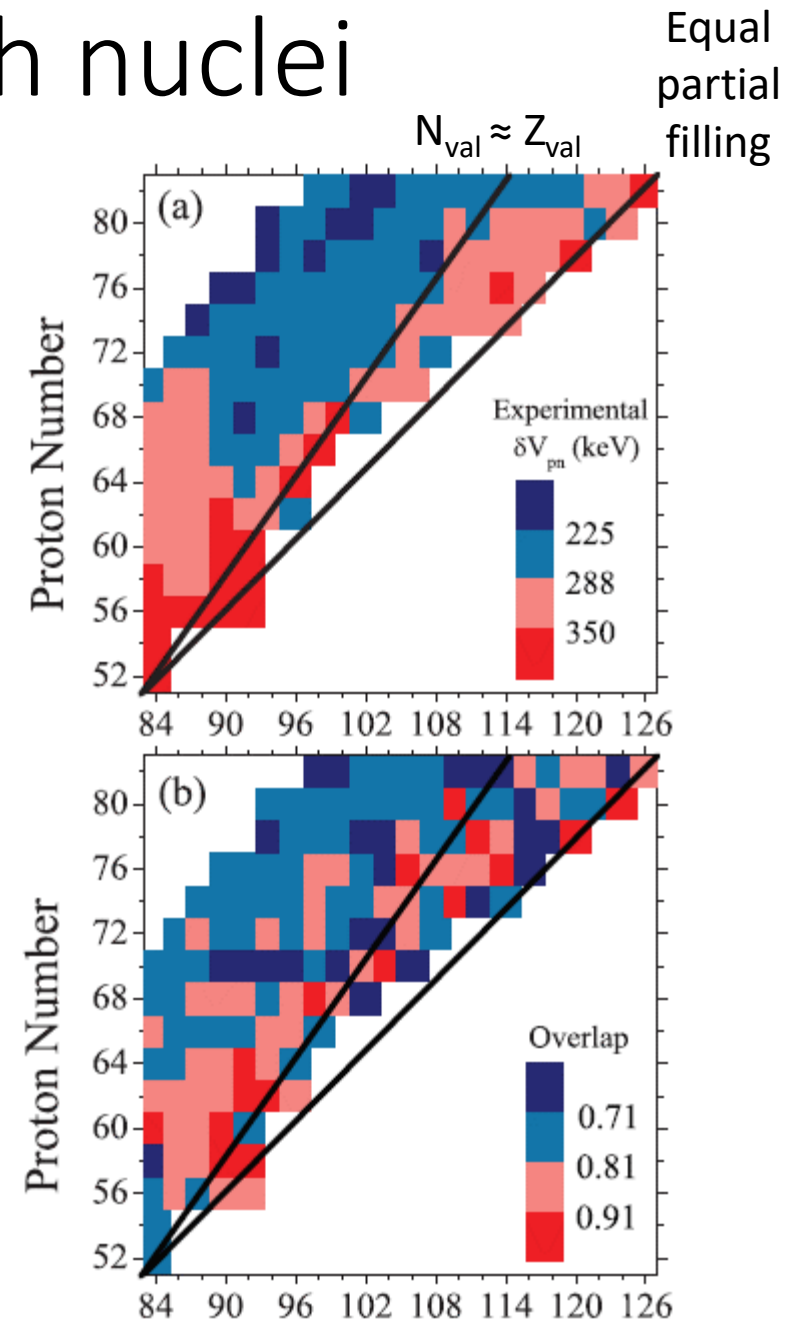
○ Highest  $\delta V_{pn}$  value in isotope chain

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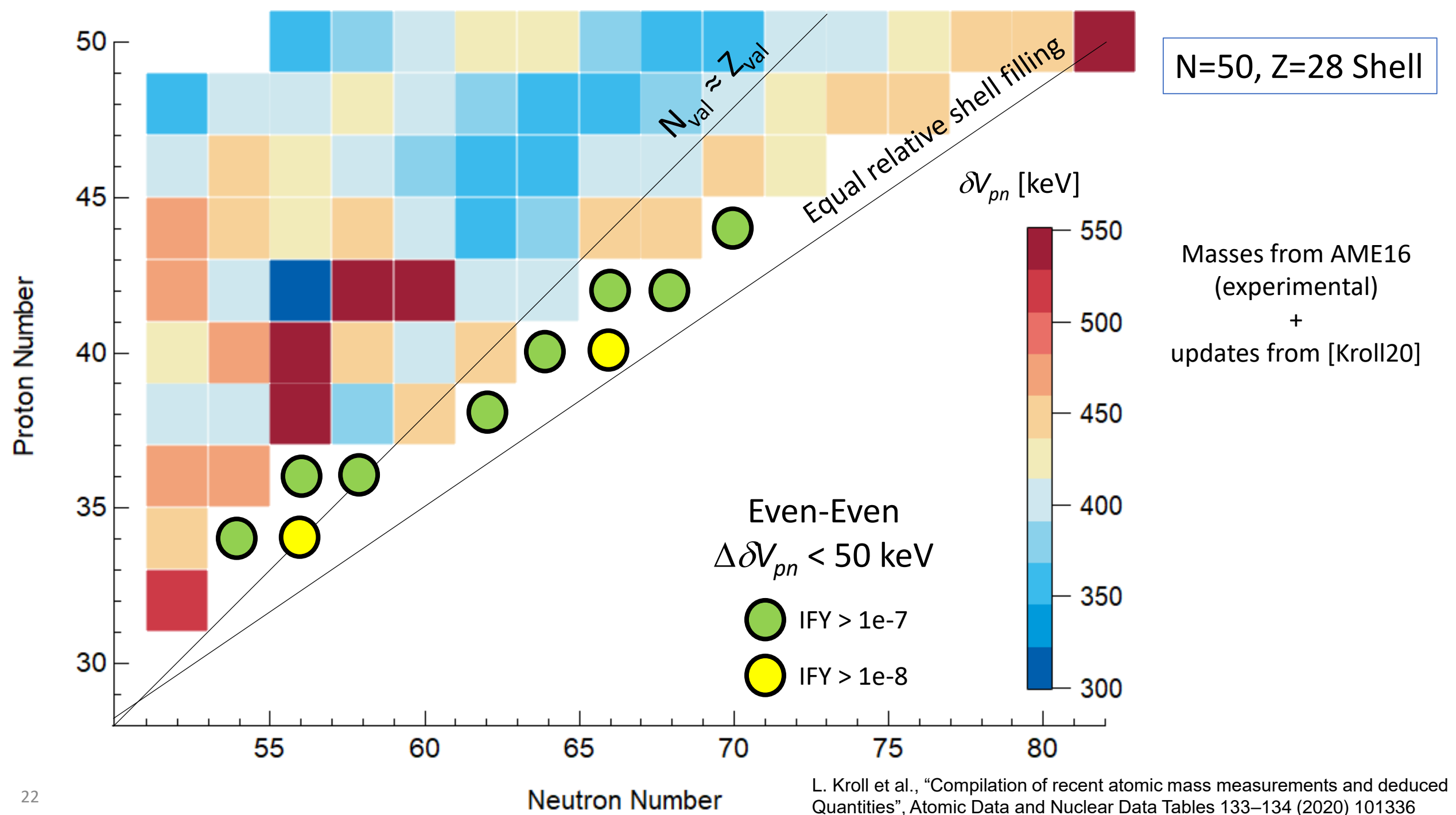
Even-even nuclei

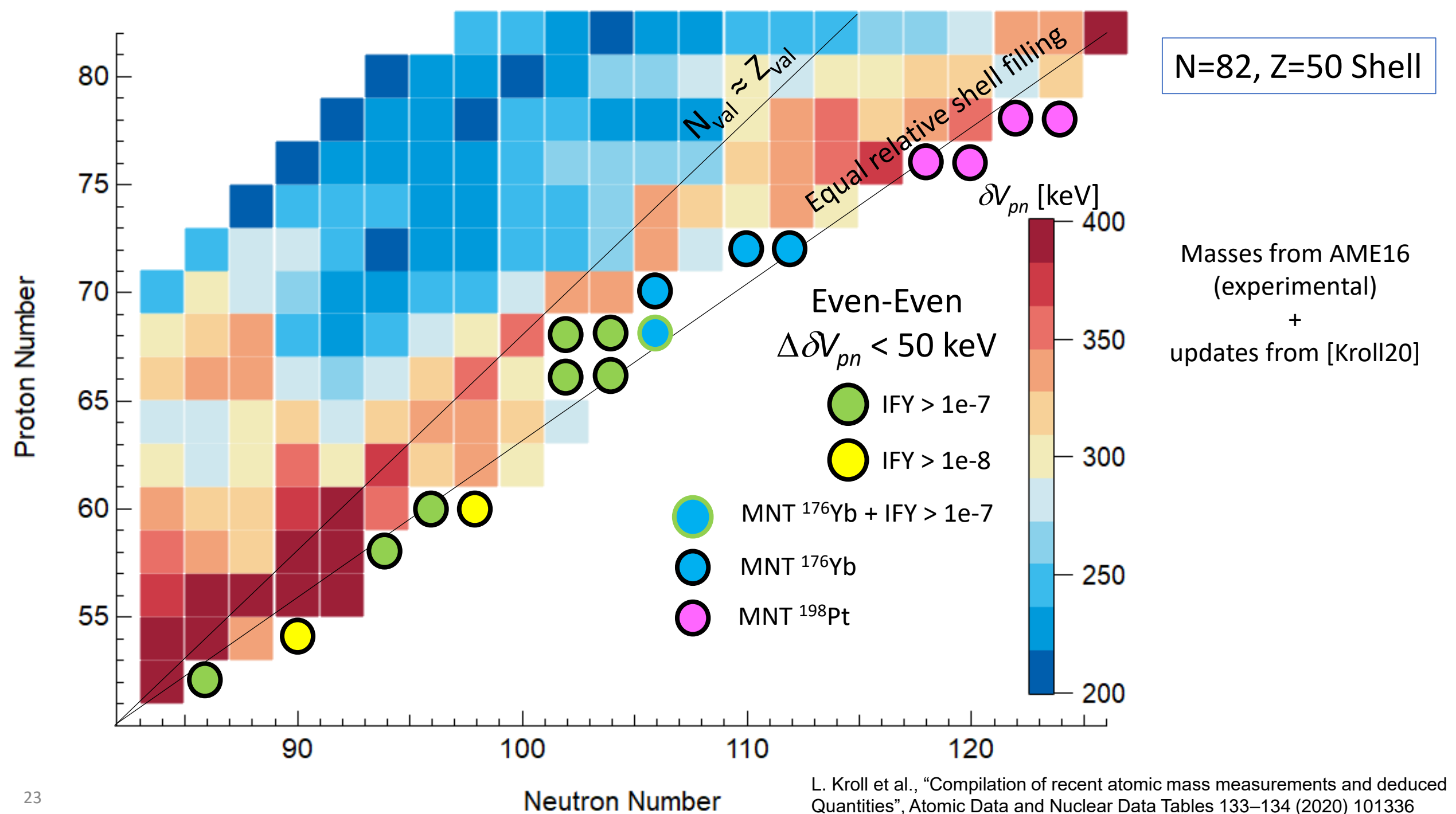
- Overlaps of Nilsson wave functions
- Deformation parameter chosen for each nucleus via its  $R_{4/2}$  value
- Theoretical extension to nuclei with unmeasured  $R_{4/2}$





# $\delta V_{pn}$ of n-rich nuclei at FRS Ion Catcher and IGISOL

- We plan to use spontaneous fission sources at the FRS Ion Catcher to measure more  $\delta V_{pn}$  values above **Z=50, N=82** and **Z=28, N=50** Magic shells
- Meaningful measurements are possible with fission yields of IFY  $\sim 10^{-6,7}$
- (Challenging) extension to IFY  $\sim 10^{-8}$  adds only a few more  $\delta V_{pn}$  values
- Values of heavier nuclei will be available from the proposed MNT experiments at IGISOL @ JYFLTRAP
- Following slides show most updated  $\delta V_{pn}$  experimental values, and our potential contributions





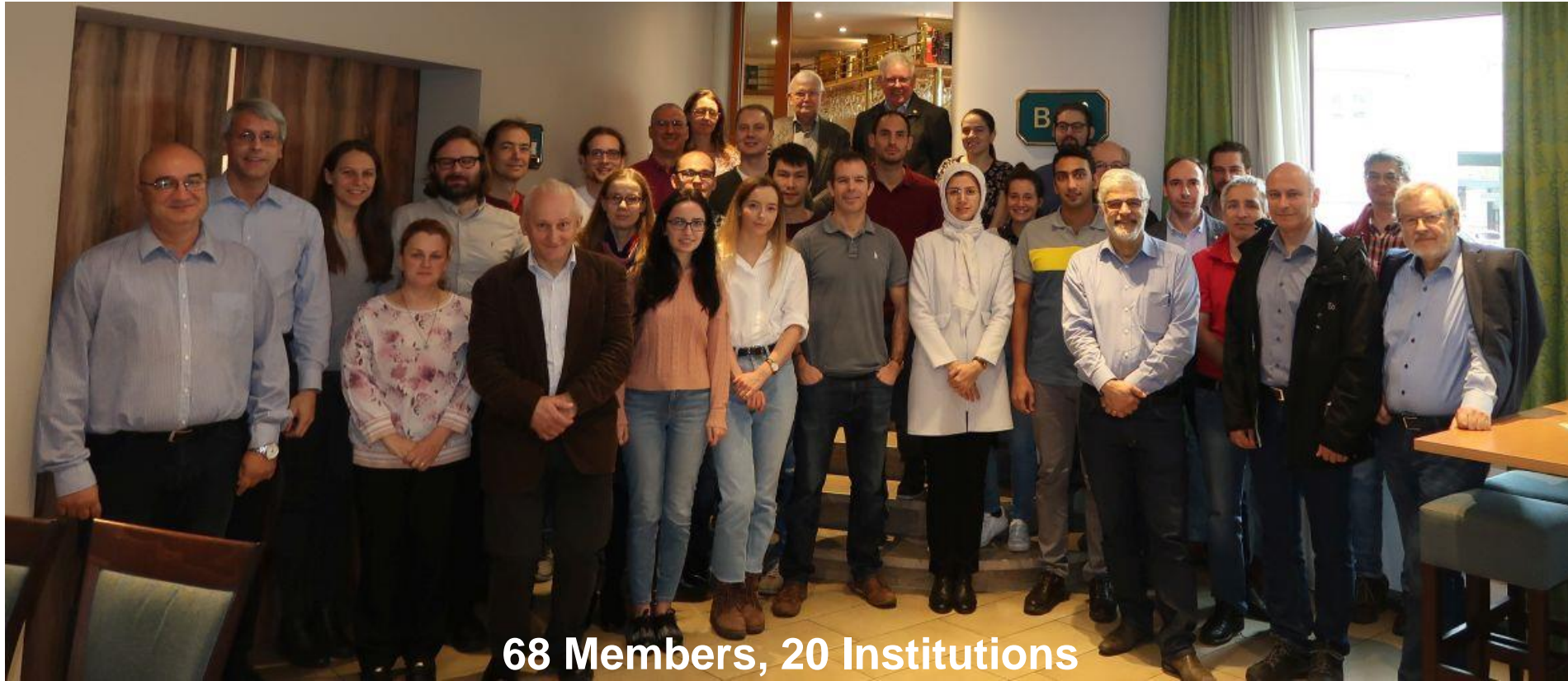
# Summary (1/2)

- Demonstrated possibility of **simultaneous experiments** with the **same FRS beam**
- Performed the **first range bunching** at the final focus of the **FRS (S4)**
- Reached a **mass resolving power** of **1,000,000** with an MR-TOF MS
  - **Mass uncertainty** of  $1.7 \times 10^{-8}$  for a **stable** molecule ( $\approx 9,000$  events) 
  - **Mass uncertainty** of  $4.0 \times 10^{-8}$  for an **unstable** nuclide ( $\approx 500$  events) 
- First direct mass measurement of  $^{69}\text{As}$ , resolving discrepancies in indirect ones
- First MR-TOF-MS mass measurements of  $^{70,71}\text{Se}$ ,  $^{71}\text{Br}$ , consistent with AME16
- Our results indicate a rise with mass of  $\delta V_{pn}$  of odd-odd  $N=Z$  nuclei from  $Z = 29$
- Overall trends of  $\delta V_{pn}$  at  $N \leq Z$  suggests a resolution to the  $^{70}\text{Br}$  mass discrepancy (towards 1980 end-point energy measurement, versus 2009 Penning Trap)

# Summary (2/2)

- $\delta V_{pn}$  values provide an interesting physics motivation for mass measurements of n-deficient nuclei around  $N=Z$  and also of n-rich nuclei around  $N_{\text{val}} \approx Z_{\text{val}}$
- Systematic surveys of  $\delta V_{pn}$  may point at emergence of
  - nuclear symmetries
  - collectivity / deformation
- They can also indicate
  - erroneous mass measurements and/or evaluations ( $\delta V_{pn}$  fluctuates or unphysical)
  - rapid nuclear shape changes ( $\delta V_{pn}$  interpretation relies on four nuclei having similar cores)
- More double differences of binding energies that exhibit the p-n interaction have been suggested (W. Satula et al., PLB 407, 103 (1997), Z. Wu et al., PRC 93. 034334 (2016), and more)
  - May further differentiate mean-field and residual contributions to the p-n interaction
  - Will analyze our present and future measurements according to these expressions as well

# Acknowledgement – The FRS Ion Catcher Collaboration



**68 Members, 20 Institutions**

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