

# **SIS100 Working Point Study: Magnet Errors and Space Charge**

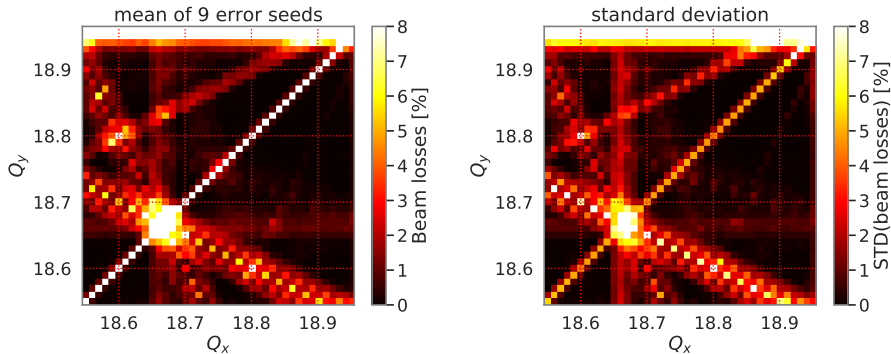
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Definitions of space charge (SC) models:

- **fixed frozen SC:** a semi-analytic Gaussian field map in the transverse plane (employing the Bassetti-Erskine formula), and a Gaussian longitudinal line charge density
  - typically run with 1000 macro-particles
  - computed once in the beginning with a certain  $\sigma_{x,y,z}$ , no updates
  - **fixed** center of the field-map, no centroid offset taken into account
- **centroid-aware frozen SC:** same as *fixed frozen SC*, but the centroid offset is subtracted before and re-added directly after the kick
- **adaptive frozen SC:** same as *fixed frozen SC*, no update of the centroid offset, but the  $\sigma_{x,y,z}$  are continuously updated (at regular turn intervals or even each kick)
- **self-consistent PIC:** 2.5D slice-by-slice transverse Poisson solver
  - typically run with  $1 \times 10^6$  macro-particles on  $128 \times 128 \times 64$  grid cells
  - extends to a fixed size of  $2 \times 12\sigma_{x,y}$  in the transverse and  $2 \times 2 \times 1.5\sigma_z$  in the longitudinal plane

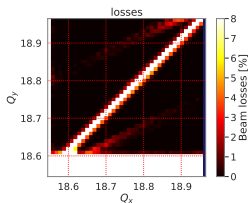
## With all errors, no SC

Adding all magnet errors (multipoles, misalignments) for 9 error seeds:

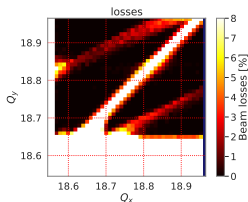


# No errors, with fixed frozen SC

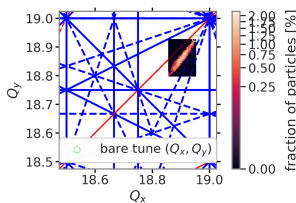
Loss width of half-integer resonance stop-band changes with  $\Delta Q_y^{SC}$ :



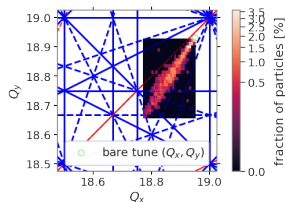
(a) losses for  $\Delta Q_y^{SC} = 0.13$



(c) losses for  $\Delta Q_y^{SC} = 0.30$

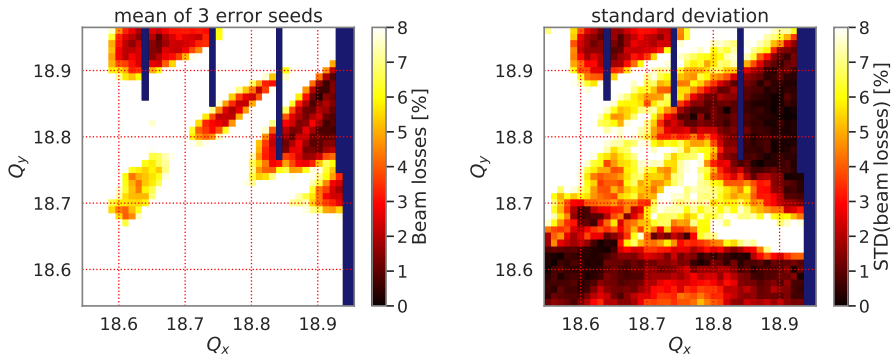


(b) corresponding tune footprint



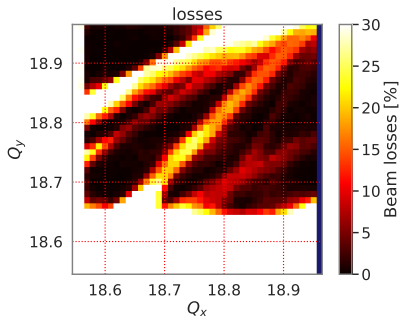
(d) corresponding tune footprint

Adding all magnet errors (multipoles, misalignments) for 3 error seeds:

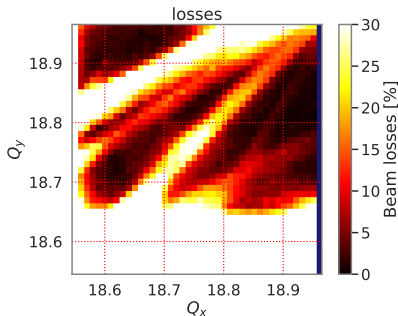


# Comparison: linear errors vs. all errors, with fixed frozen SC

All misalignment errors but only up to linear errors,  $\mathcal{O}(k_n) \leq k_1^l, k_1^s$ , behaves almost the same as all higher-order multipole errors included – for the fixed frozen SC model:



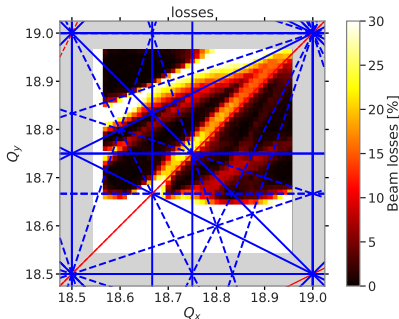
(a) up to linear error order



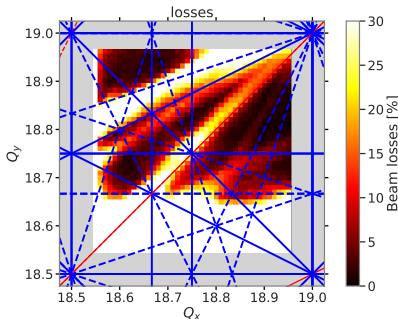
(b) all error orders

# Comparison: linear errors vs. all errors, with fixed frozen SC

All misalignment errors but only up to linear errors,  $\mathcal{O}(k_n) \leq k_1^l, k_1^s$ , behaves almost the same as all higher-order multipole errors included – for the fixed frozen SC model:



(a) up to linear error order



(b) all error orders

To do:

- ✗ cold lattice only, with fixed frozen SC – no magnet errors
- ✗ all errors (warm lattice), with centroid-aware frozen SC
- ⚠ all errors (warm lattice), with PIC
  - running but need to cross-check loss mechanism between SixTrackLib and PyHEADTAIL