

Relativistic dynamics of (slow) highly-charged ions

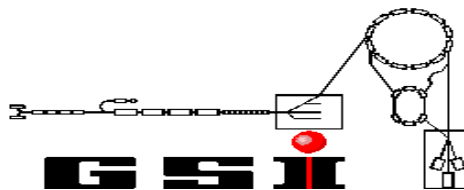
Stephan Fritzsche
GSI Darmstadt & Oulu University
Eisenach, 28th June 2010

electron-photon
interaction



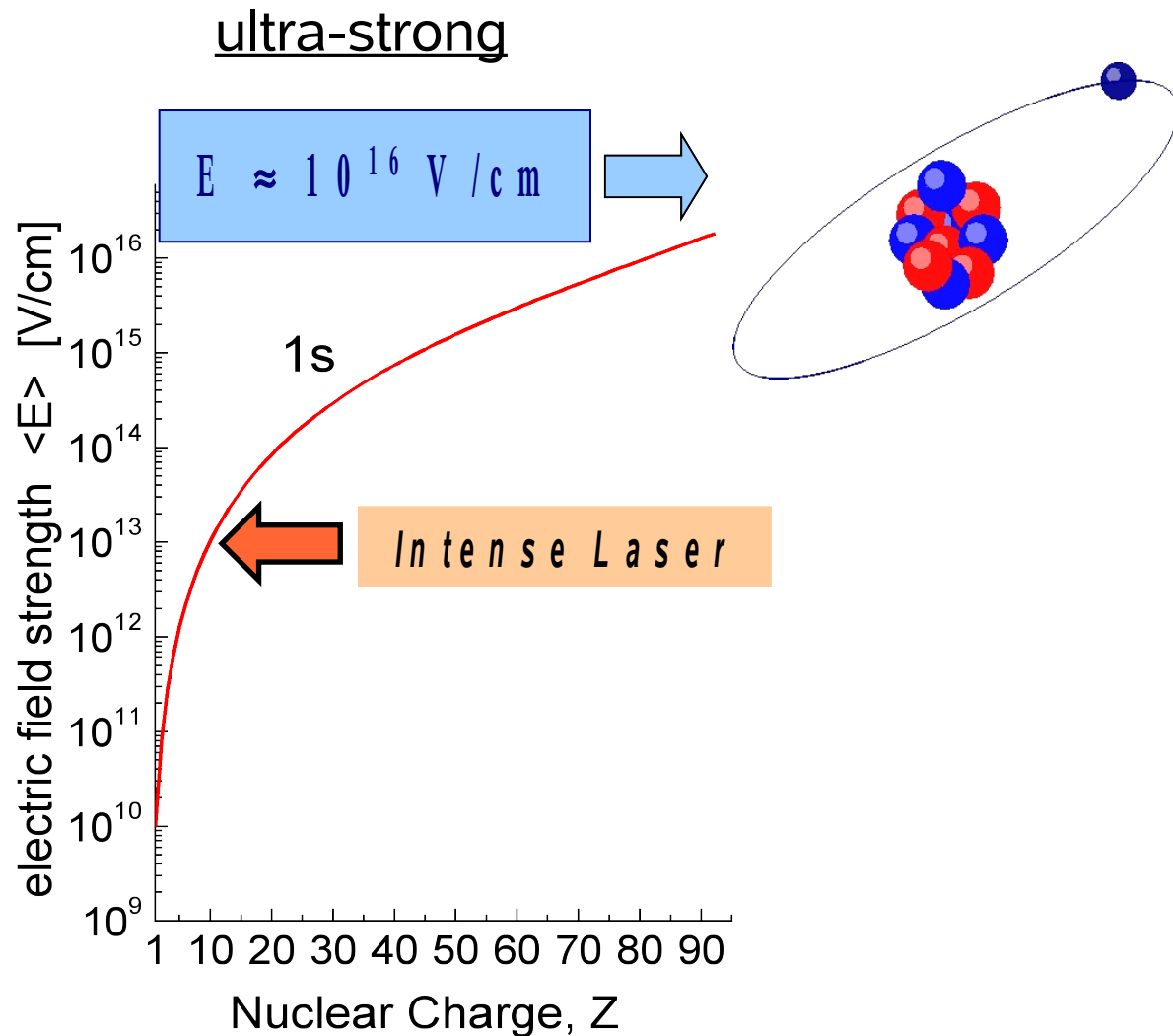
electron-electron
interaction

Thanks to: N.M. Kabachnik, A. Surzhykov, T. Stöhlker and GSI Atomic Physics Group



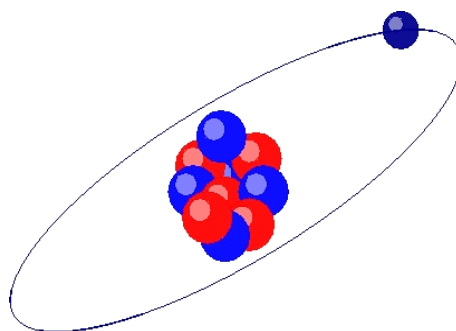
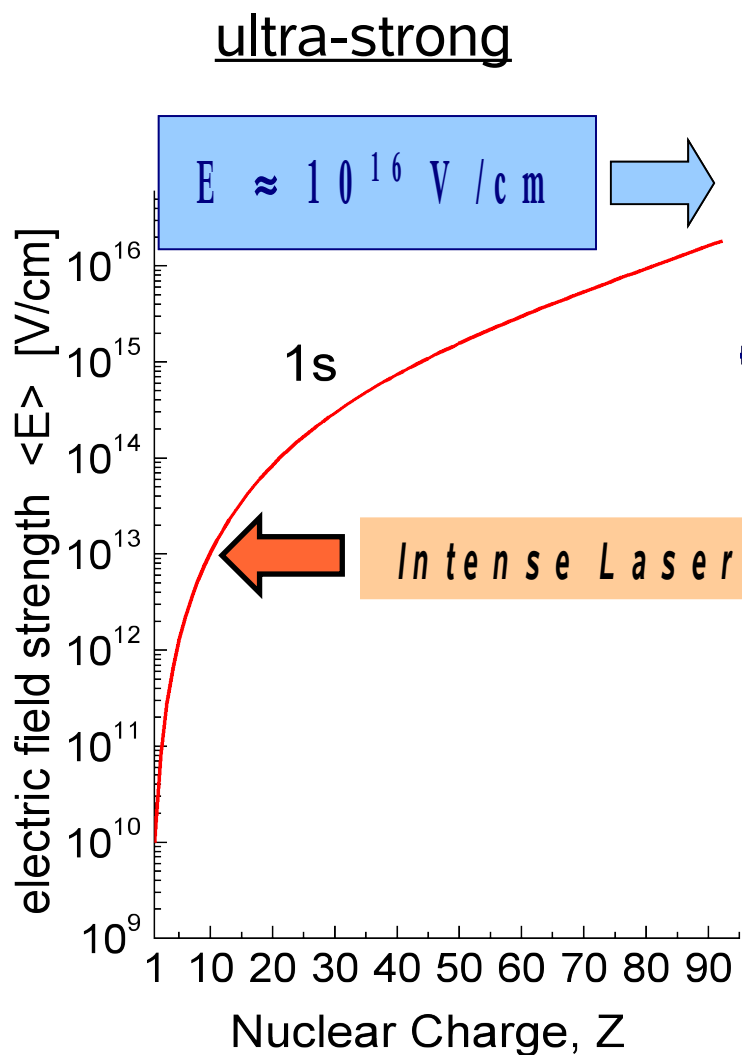
Highly-charged ions provide a unique tool

-- for probing strong electro-magnetic fields

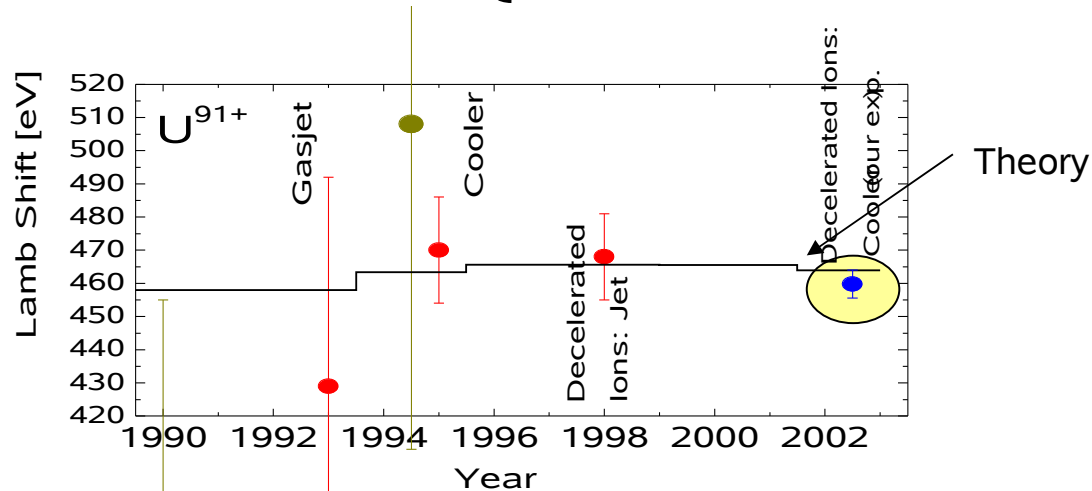
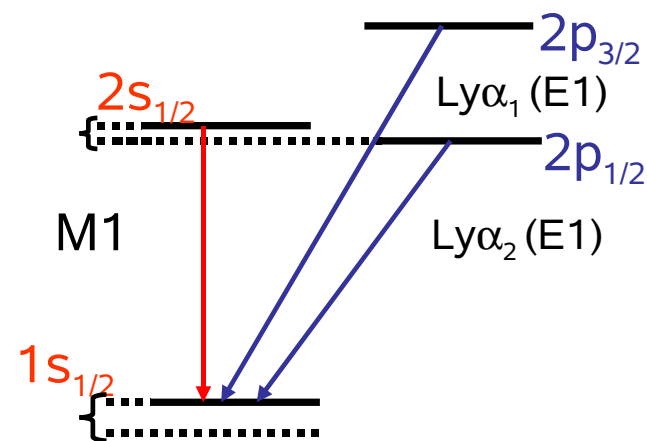


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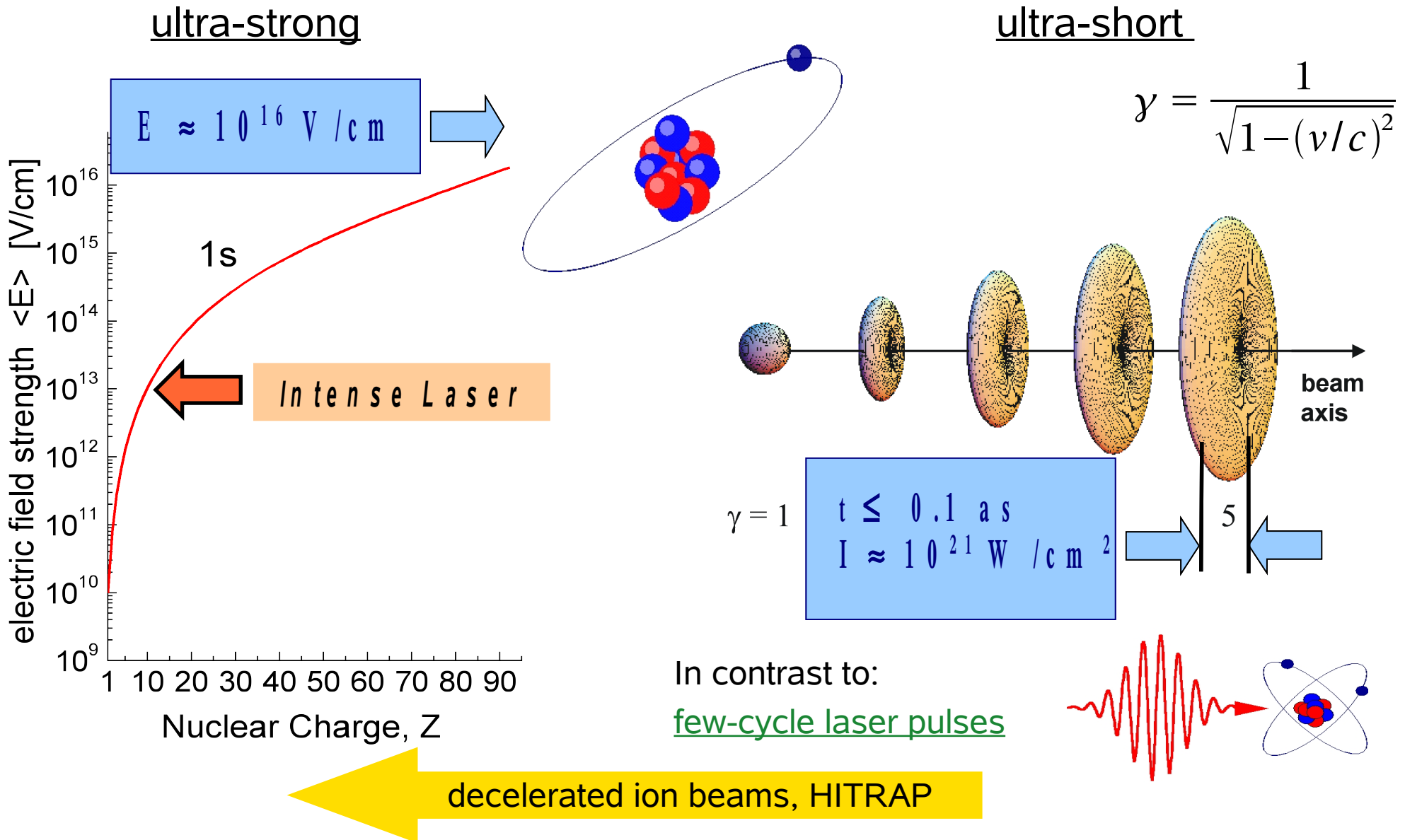


1s-Lamb Shift
Experiment: $459.8 \text{ eV} \pm 4.6 \text{ eV}$
Theory: 463.95 eV



Highly-charged ions provide a unique tool

-- for probing strong electro-magnetic fields



Relativistic dynamics of (slow) highly-charged ions

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electron-photon
interaction



electron-electron
interaction

Plan of this talk

- Electron capture: angular correlations & polarization
- Multipole mixing in strong fields
- Two-step processes: Capture vs. excitation
- Atomic PNC: Two-photon processes
- Spectroscopy of (super-) heavy elements
- Conclusions

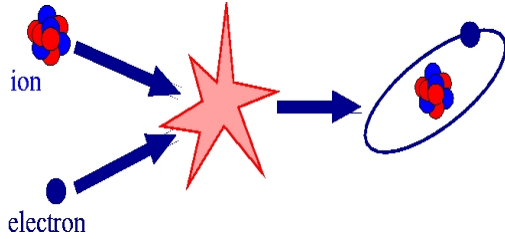
Thanks to: N.M. Kab

Electron capture by bare ions

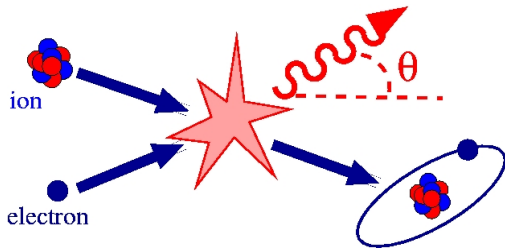
-- angular correlation and polarization studies

Electron capture into bare high-Z ions

So far...

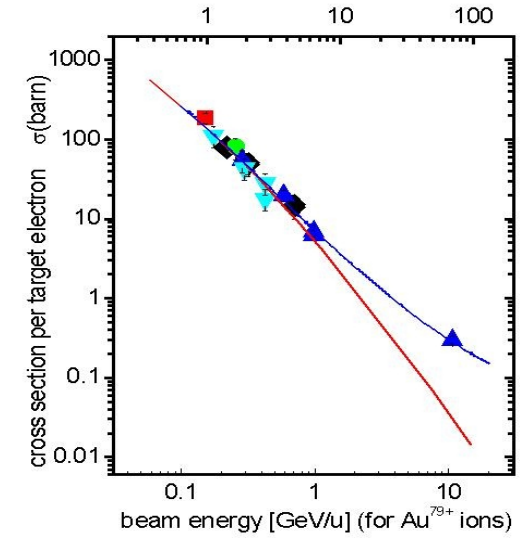
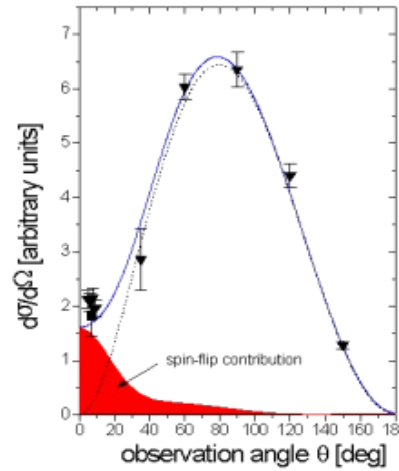


total cross sections



angular distributions

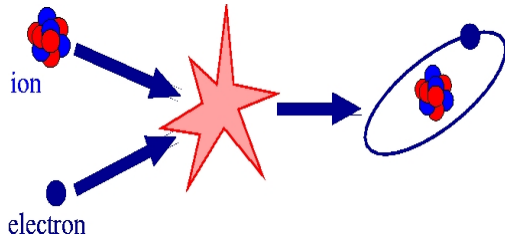
$$\sigma \sim \sum_{\text{polarization}} \int d\Omega |M|^2$$



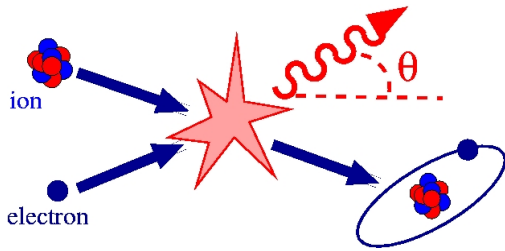
$$\frac{d\sigma}{d\Omega}(\theta) \sim \sum_{\text{polarization}} |M|^2$$

Electron capture into bare high-Z ions

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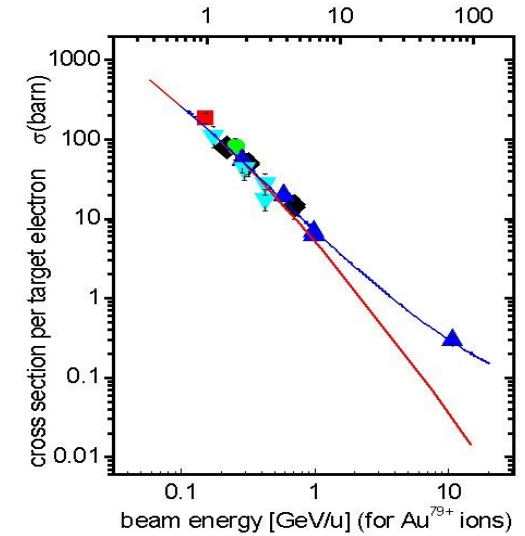
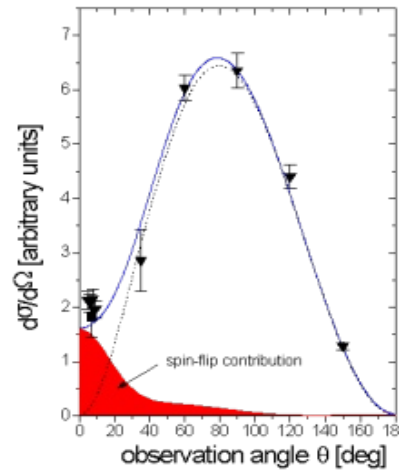


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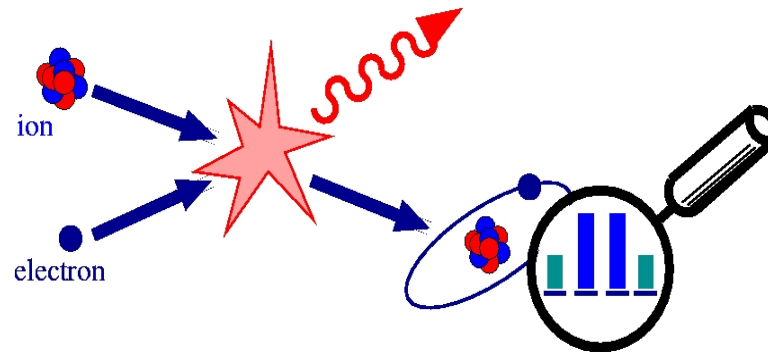
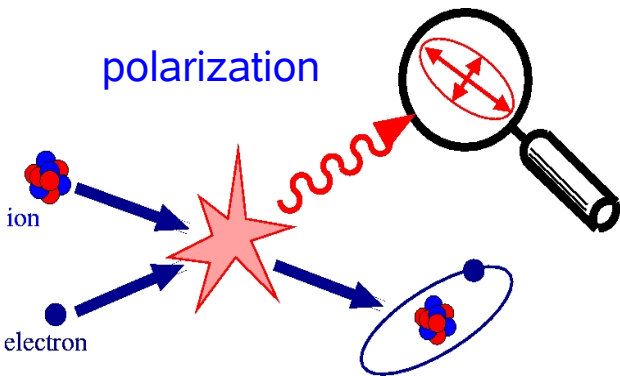
angular distributions

$$\sigma \sim \sum_{\text{polarization}} \int d\Omega |M|^2$$



$$\frac{d\sigma}{d\Omega}(\theta) \sim \sum_{\text{polarization}} |M|^2$$

New directions...



Alignment studies

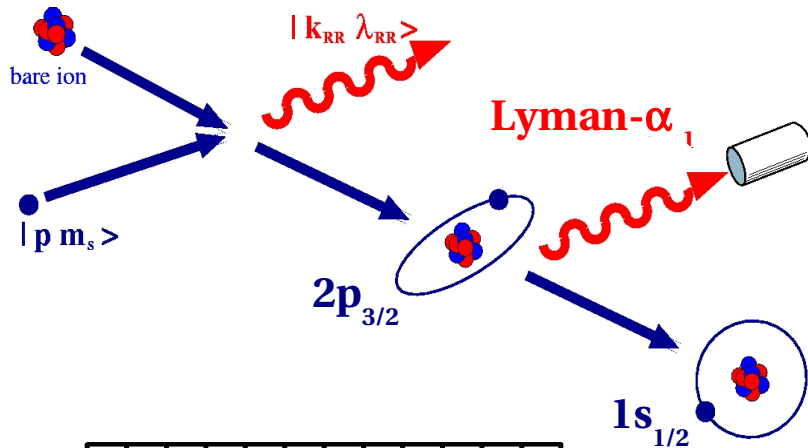
$$\sim |M|^2$$

No summation over polarization states !

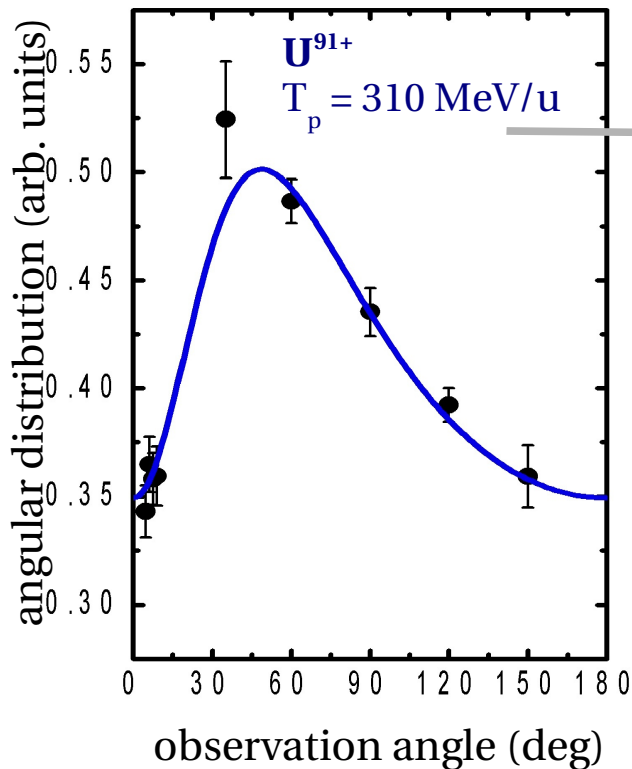
Multipole mixing of the radiation field

-- in the capture and decay of highly-charged ions

Capture into the $2p_{3/2}$ excited states of initially bare ions

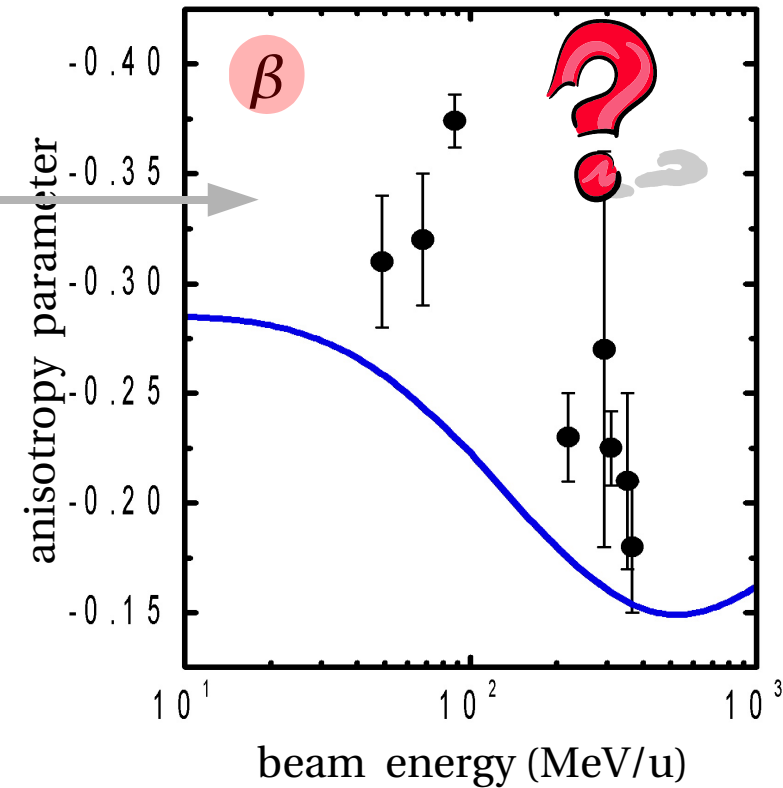


- Magnetic sublevel population of the residual ion can not be measured **directly**
- **But:** knowledge on population of excited ion state may be derived from the properties of subsequent decay

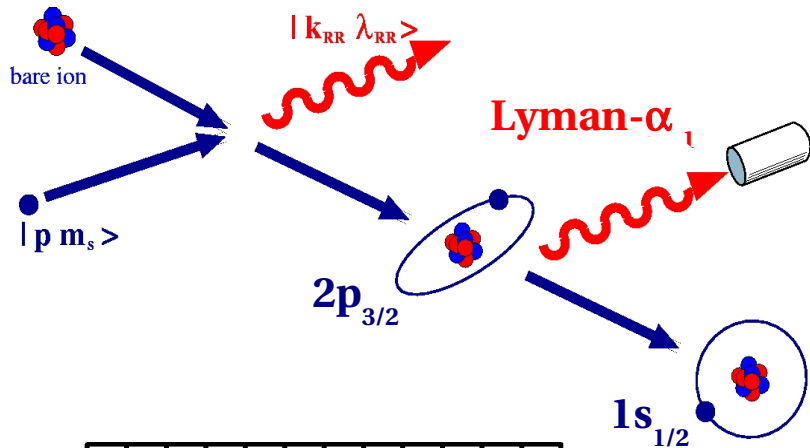


fitting

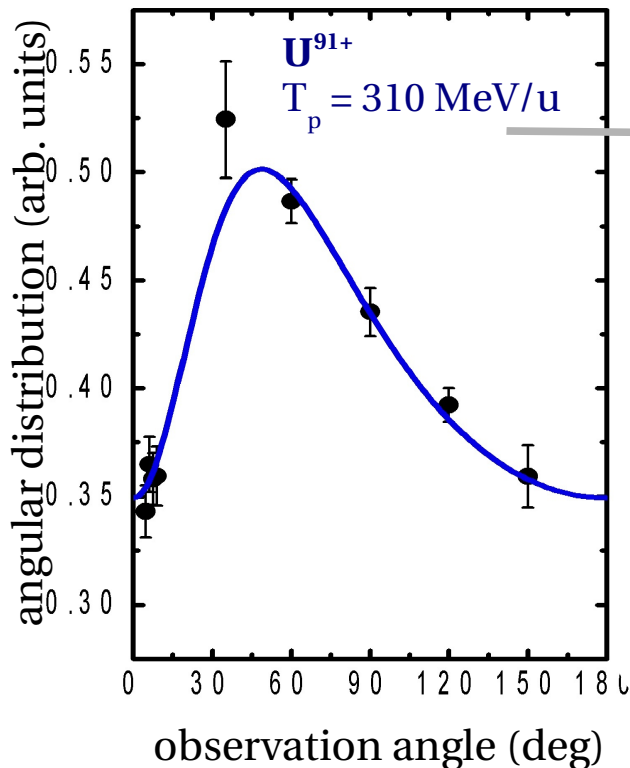
$$W(\theta) \propto 1 + \beta P_2(\cos \theta)$$



Capture into the $2p_{3/2}$ excited states of initially bare ions



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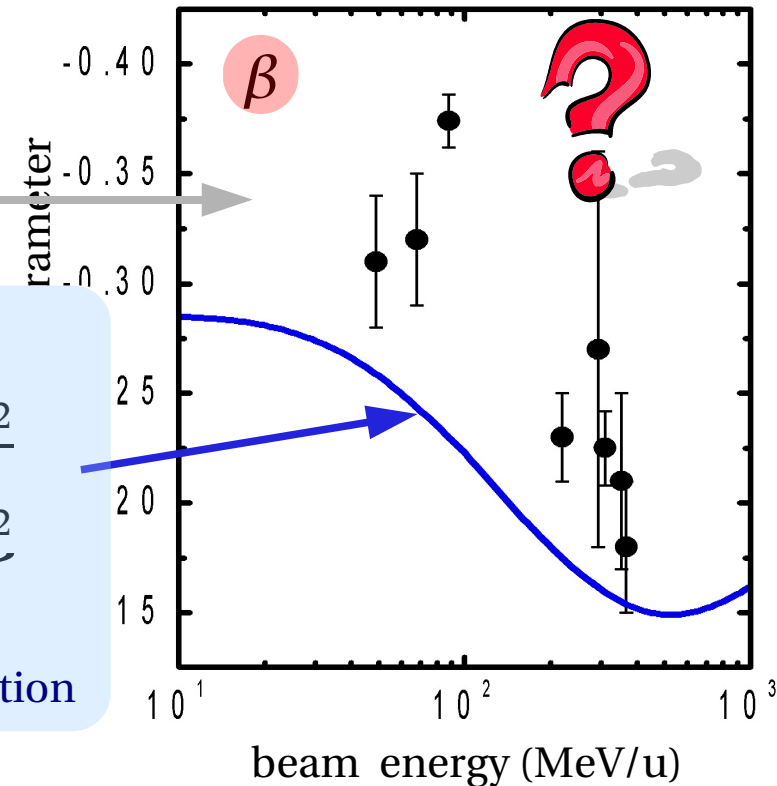
fitting

$$W(\theta) \propto 1 + \beta P_2(\cos \theta)$$

Theory:

$$\beta = \frac{1}{2} \frac{\sigma_{\mu_b = \pm 3/2} - \sigma_{\mu_b = \pm 1/2}}{\sigma_{\mu_b = \pm 3/2} + \sigma_{\mu_b = \pm 1/2}}$$

alignment of the $2p_{3/2}$ state:
relative sublevel $|j_b m_b\rangle$ population



Effective anisotropy parameter: Multipole contributions

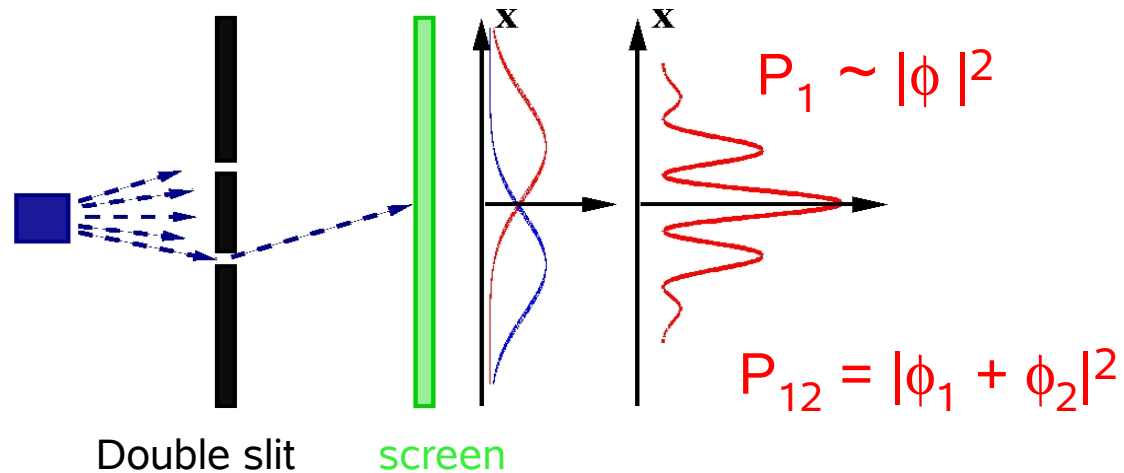
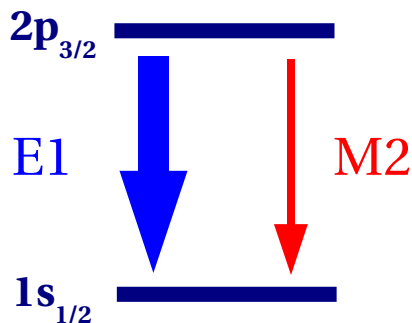
$$W(\theta) \propto 1 + \beta_{\text{eff}} P_2(\cos \theta)$$

effective anisotropy parameter



$$\beta_{\text{eff}} = \underbrace{\frac{1}{2} \frac{\sigma(\pm 3/2) - \sigma(\pm 1/2)}{\sigma(\pm 3/2) + \sigma(\pm 1/2)}}_{\text{alignment parameter}} \underbrace{f(E1, M2)}_{\text{structure function}}$$

$$f(E1, M2) \propto 1 + 2\sqrt{3} \frac{\langle |M2| \rangle}{\langle |E1| \rangle}$$



Effective anisotropy parameter: Multipole contributions

$$W(\theta) \propto 1 + \beta_{eff} P_2(\cos \theta)$$

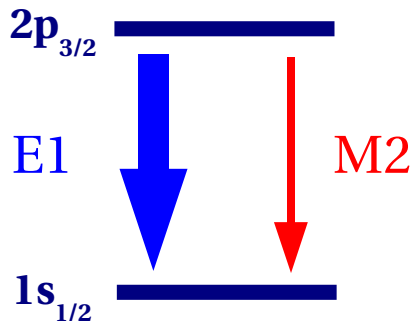
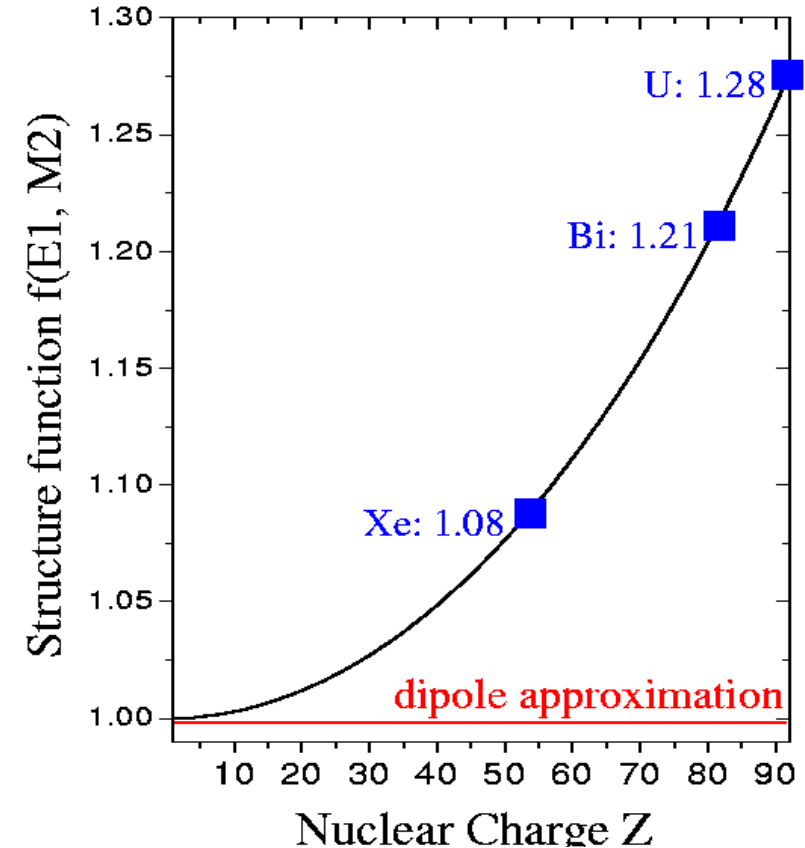
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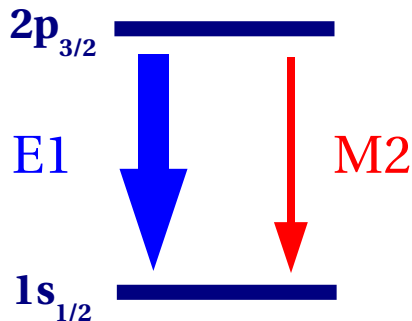
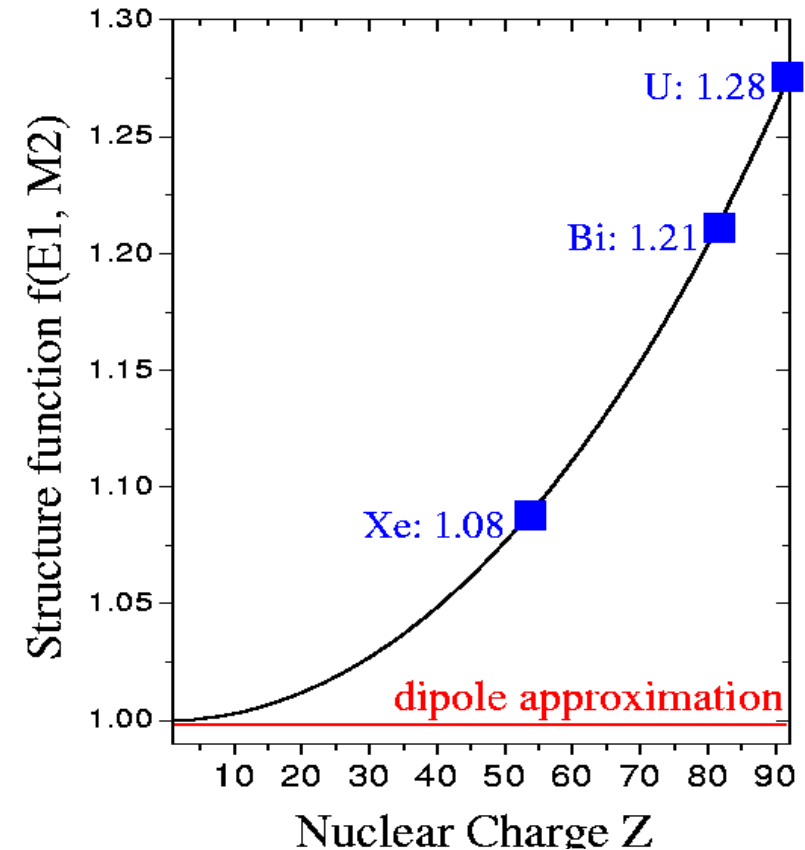
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➔ In contrast, contributions to decay rates appear additive:

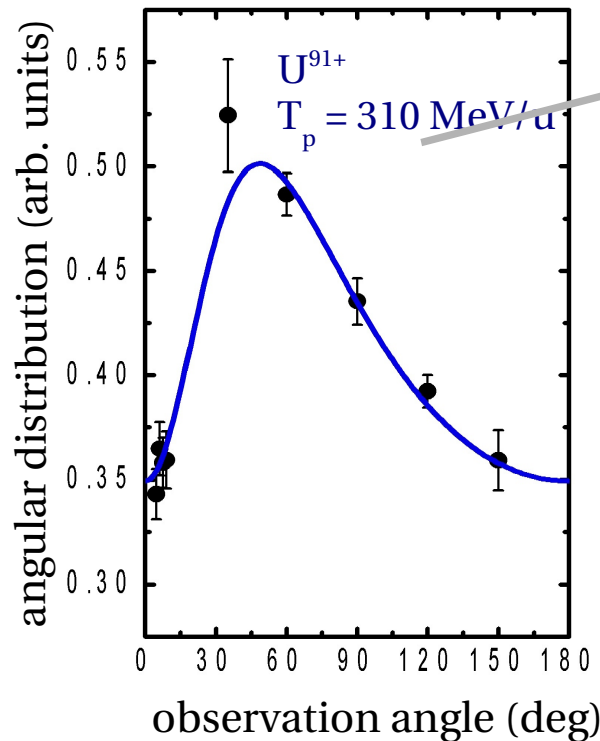
$$\frac{\Gamma_{M2}}{\Gamma_{tot}} \propto \frac{\langle |M2| \rangle^2}{\langle |E1| \rangle^2} \propto 0.008$$



even for U⁹¹⁺

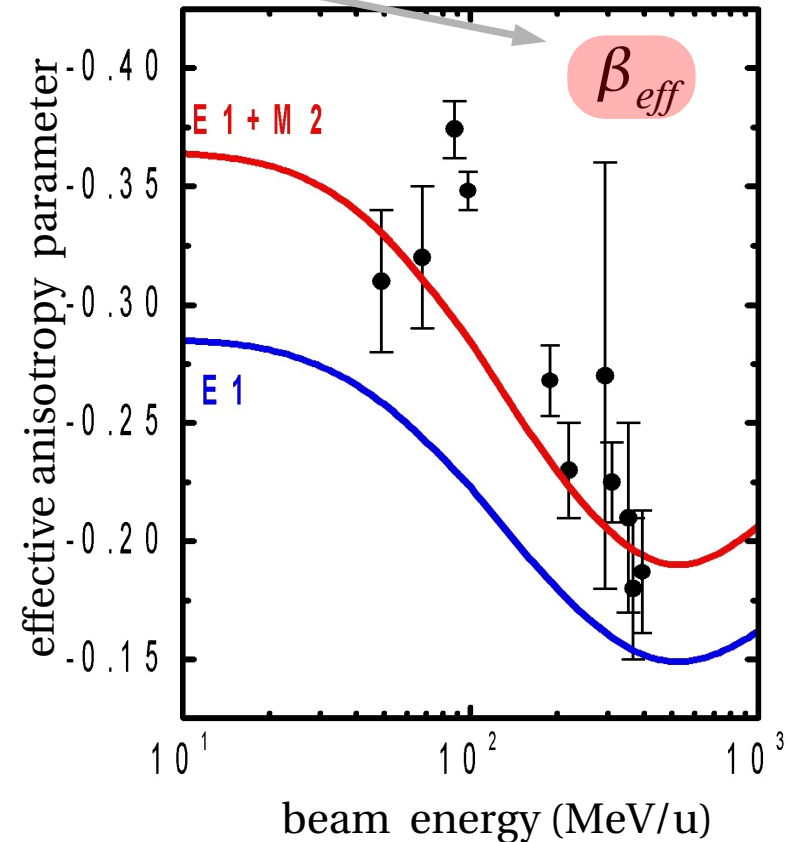
E1-M2 multipole mixing: Alignment of the $2p_{3/2}$ state

A. Surzhykov et al. PRL 88 (2002) 153001



fitting

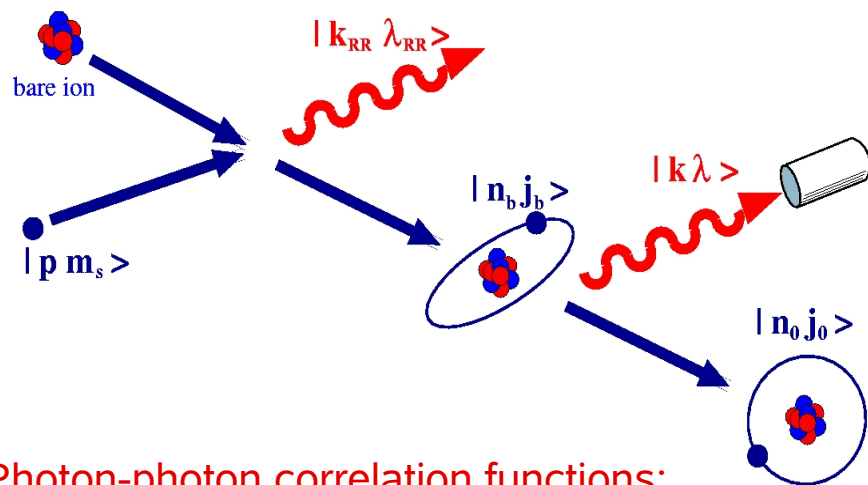
$$W(\theta) \propto 1 + \beta_{eff} P_2(\cos \theta)$$



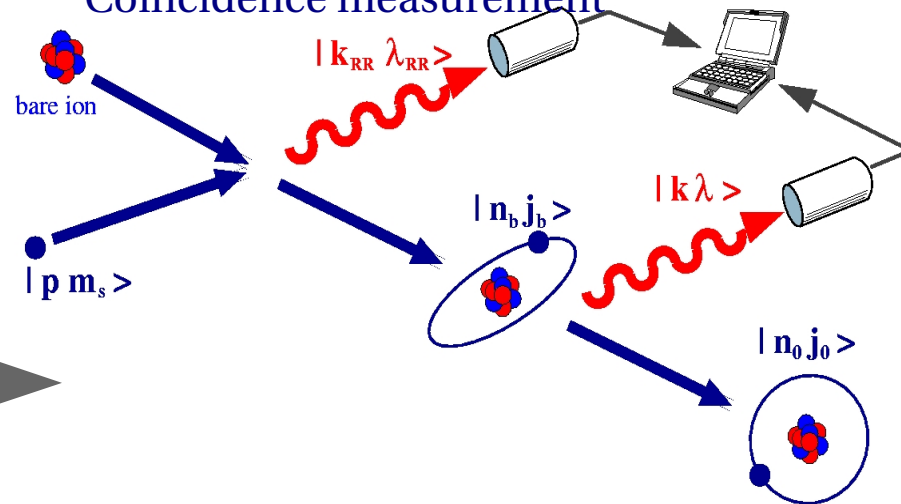
➡ Dynamical alignment studies enables one to explore magnetic interactions in the bound-bound transitions in H-like ions !

Two-photon coincidence studies

Normal (independent) measurement



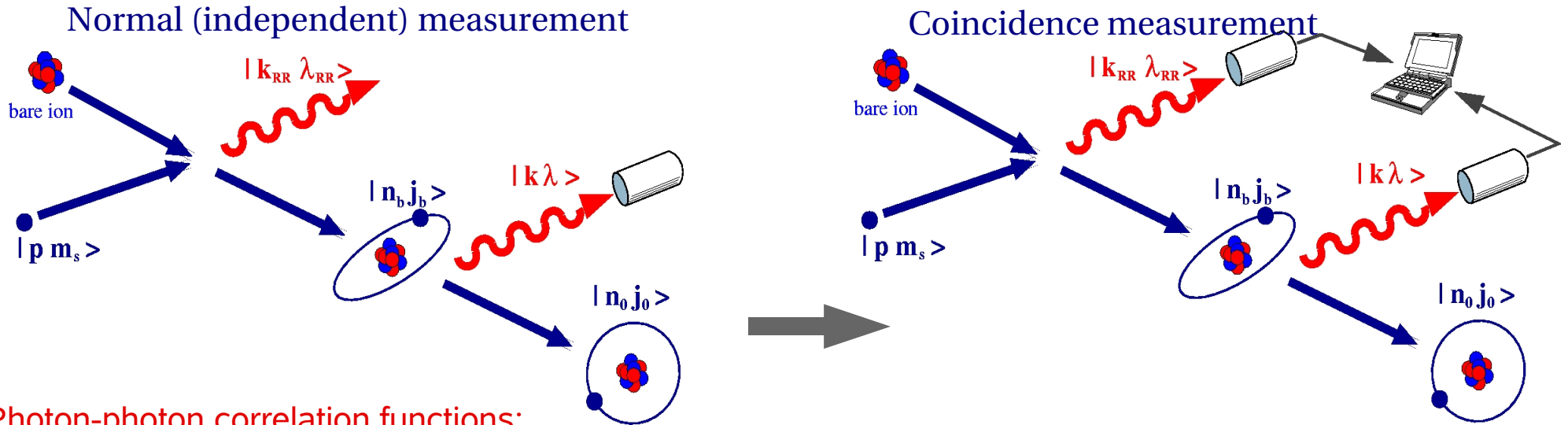
Coincidence measurement



Photon-photon correlation functions:

$$W(\theta_{RR}, \theta) = ?$$

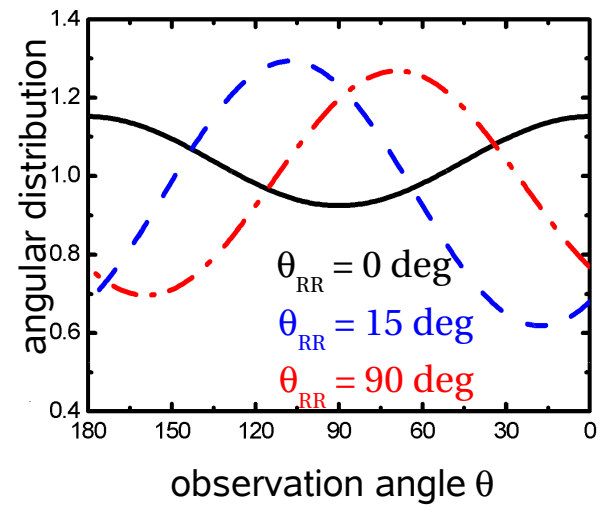
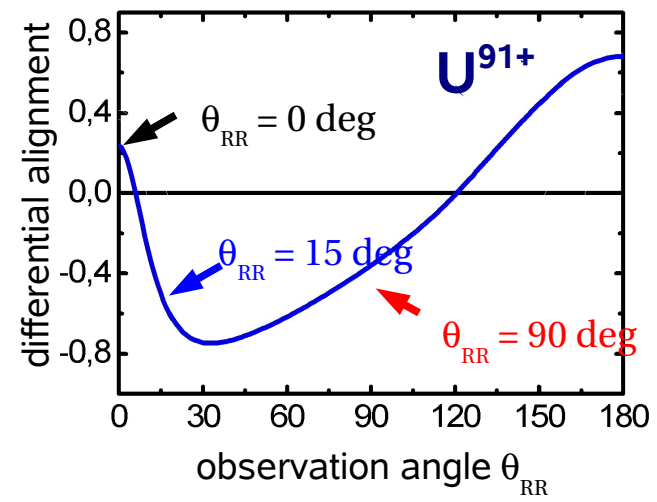
Two-photon coincidence studies



Photon-photon correlation functions:

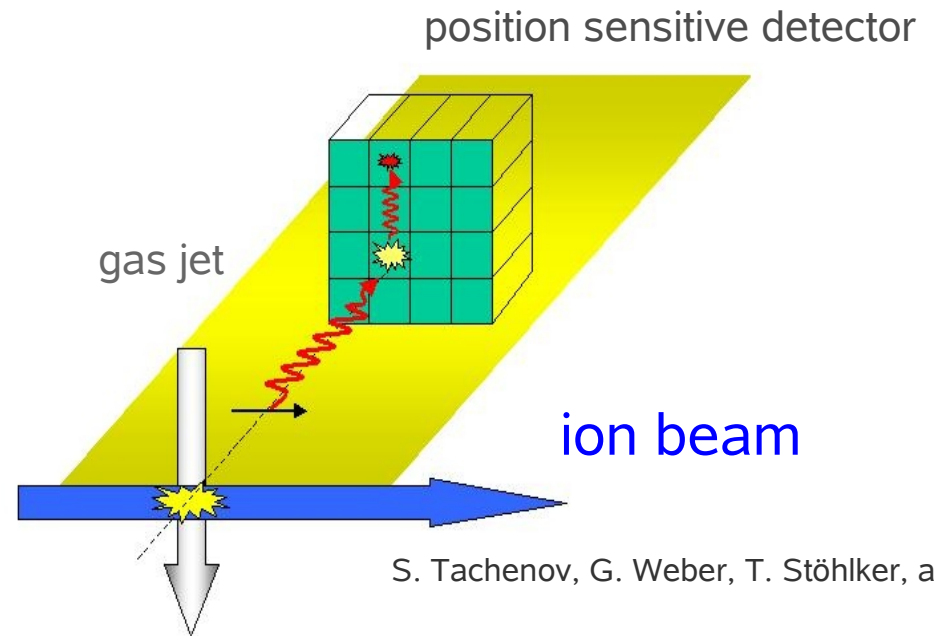
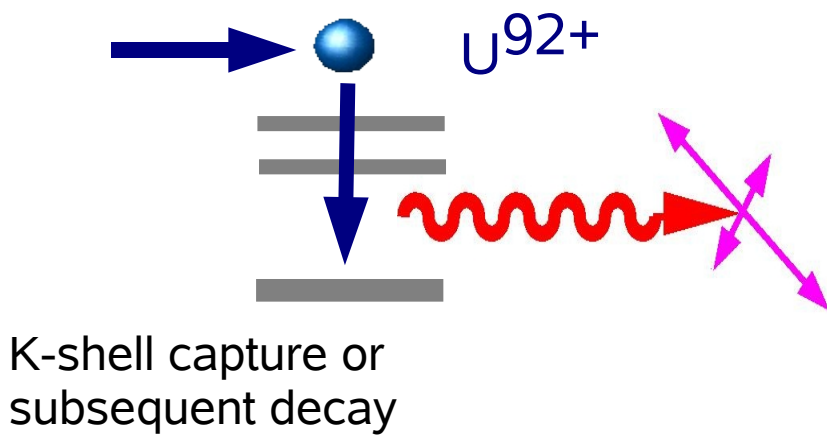
$$W(\theta_{RR}, \theta) \propto 1 + \sqrt{\frac{4\pi}{5}} \sum_q A_{2q}(\theta_{RR}) Y_{2q}(\theta)$$

Lengthy derivation in the framework of the density matrix theory.



X-ray polarimetry for HCI

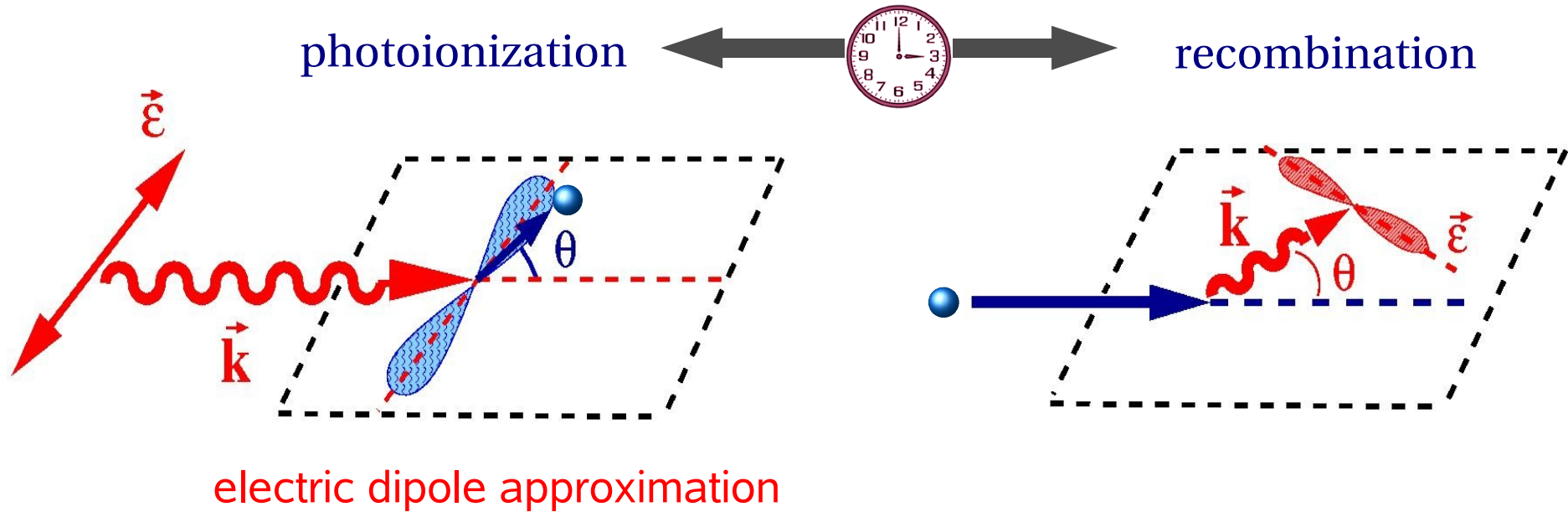
-- exploring a new 'dimension' in the electron-photon interaction



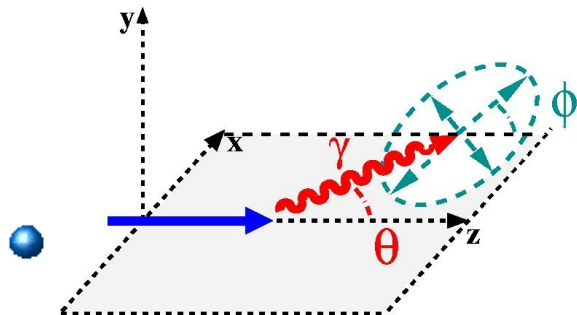
S. Tachenov, G. Weber, T. Stöhlker, a.o.

Linear polarization of emitted x-ray photons

-- theoretical expectation



Linear polarization is described in the plane, perpendicular to the photon momentum.

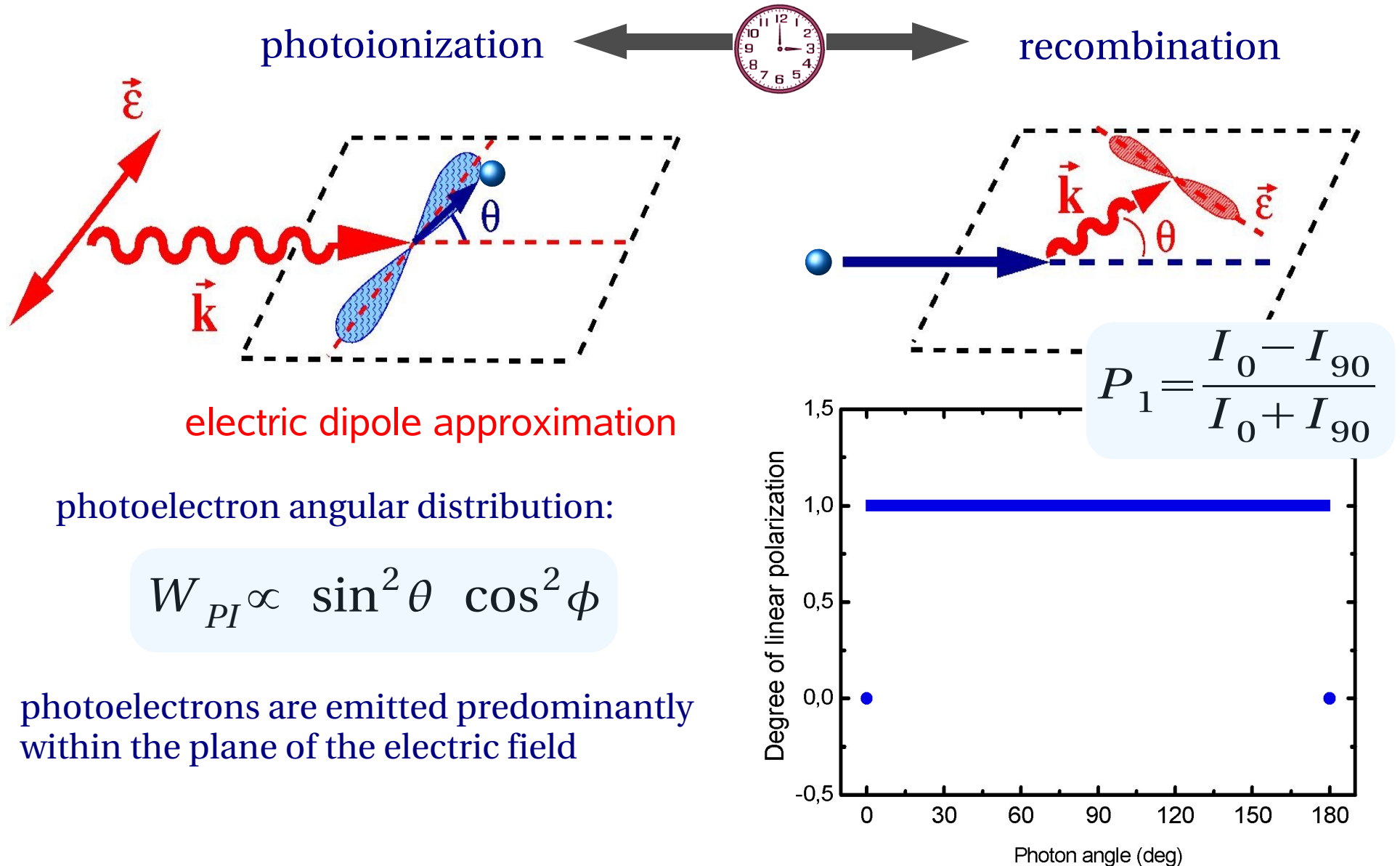


only 2 (Stokes) parameters are required !

$$P_L = \sqrt{P_1^2 + P_2^2} \quad \cos(2\phi) = \frac{P_1}{P_L}$$

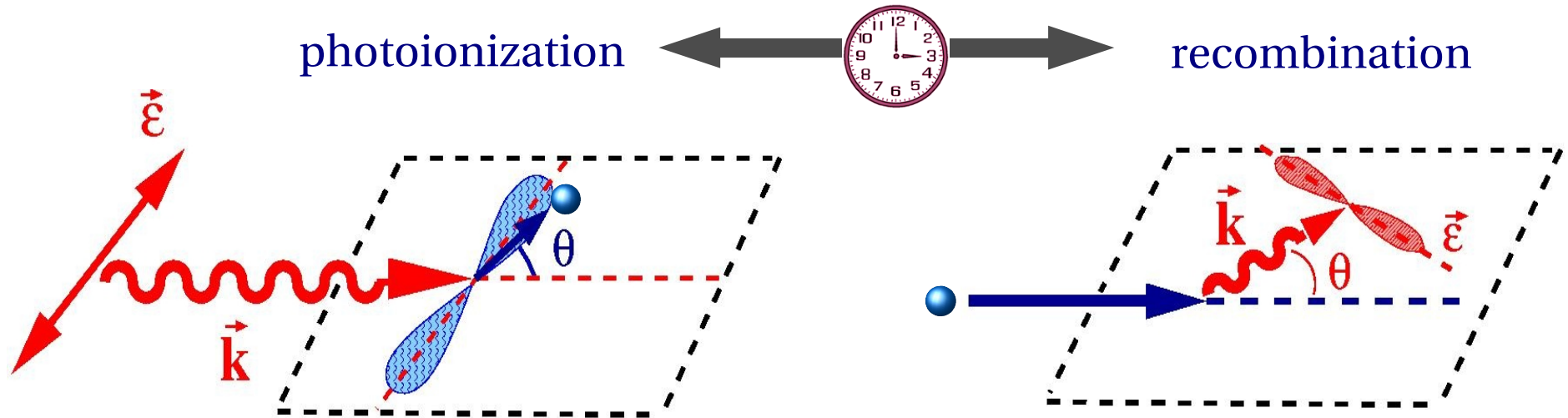
Linear polarization of emitted x-ray photons

-- Statistical characteristics for photon ensembles



Linear polarization of emitted x-ray photons

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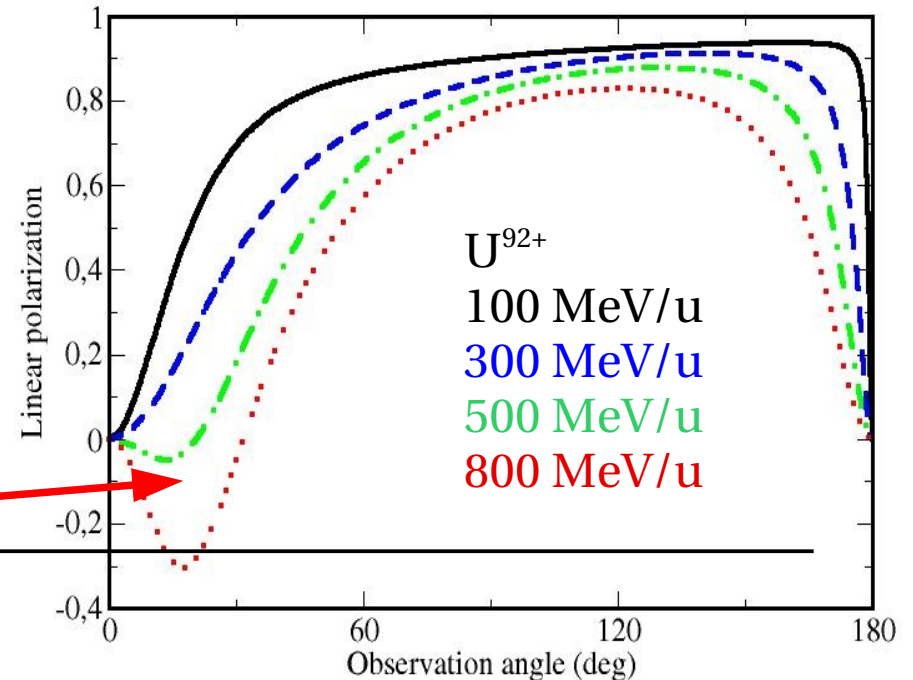


electric dipole approximation

- Relativistic effects decrease the linear polarization !

- Cross-over behaviour !!

F. Sauter, Ann. Phys. 9 (1931) 217
U. Fano, Phys. Rev. 116 (1959) 1156

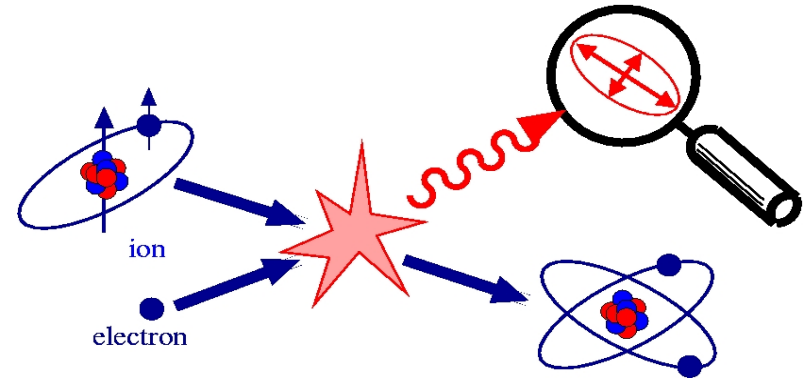
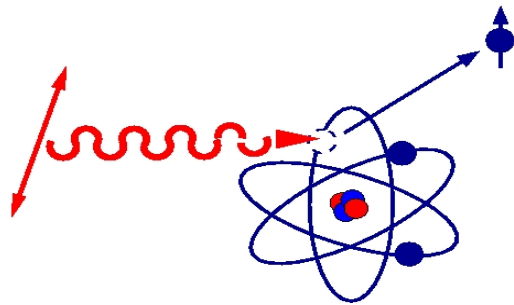


Linear polarization of emitted x-ray photons: Applications

-- Diagnostics of highly-charged ion beams

● **Proposal:** to use REC linear polarization as a probe for ion spin polarization.

● Established theory from the “polarization transfer” in atomic photoionization.



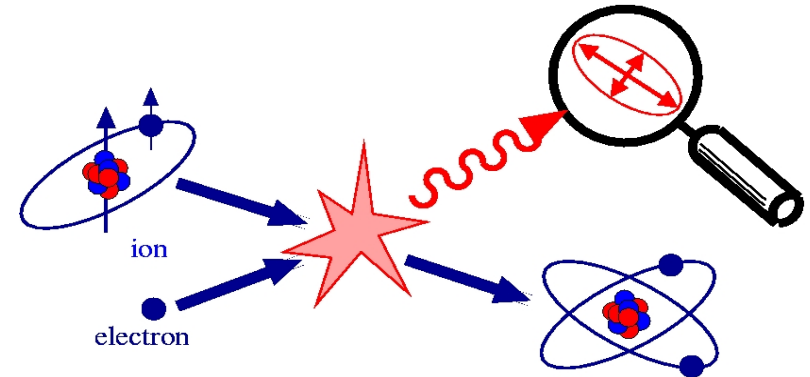
U. Fano *et al.*, Phys. Rev. **116** (1959) 1147;
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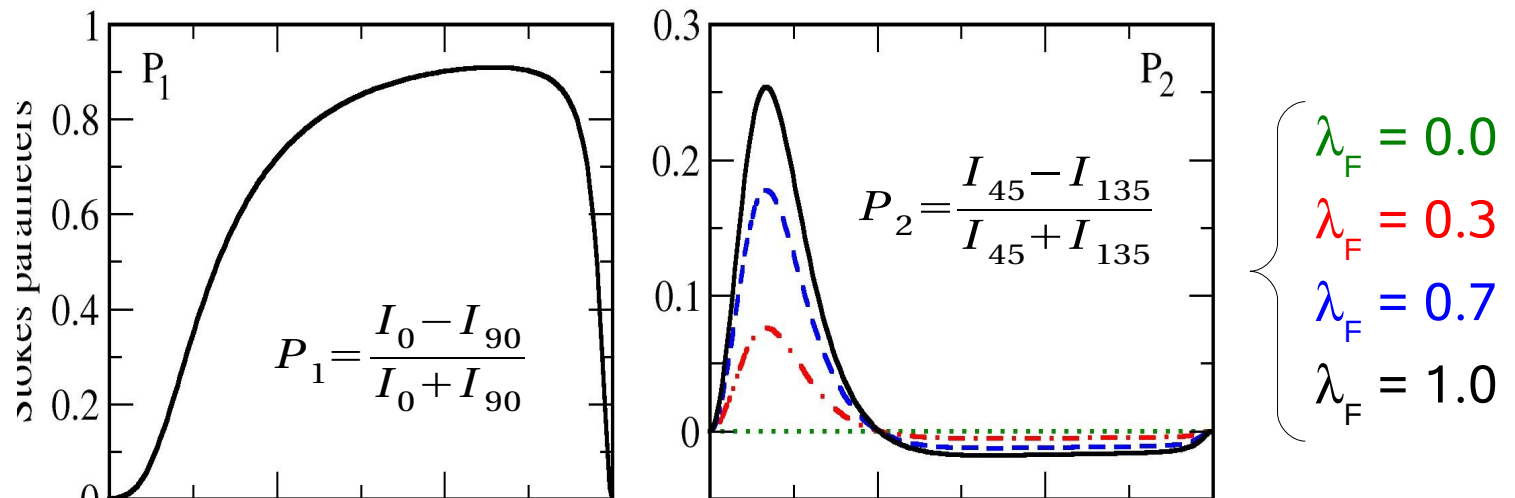
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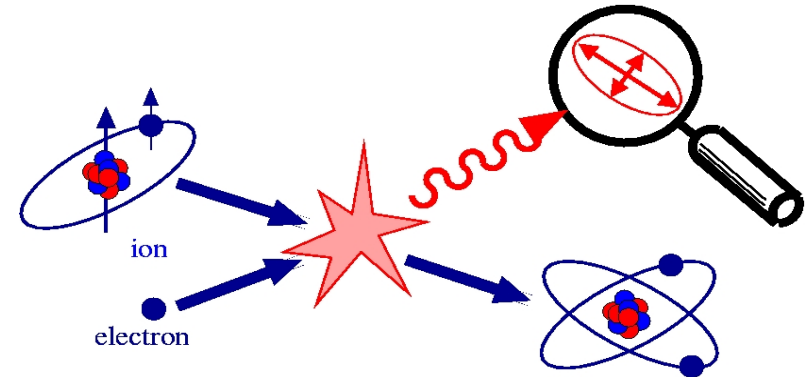
● Calculations performed for the REC into (initially) hydrogen-like bismuth Bi^{82+} ions ($I = 9/2$) for the energy $T_p = 420$ MeV/u.



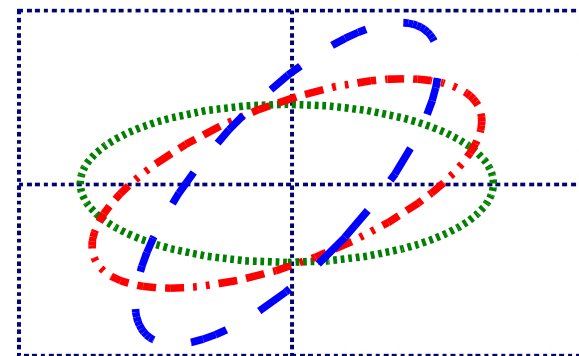
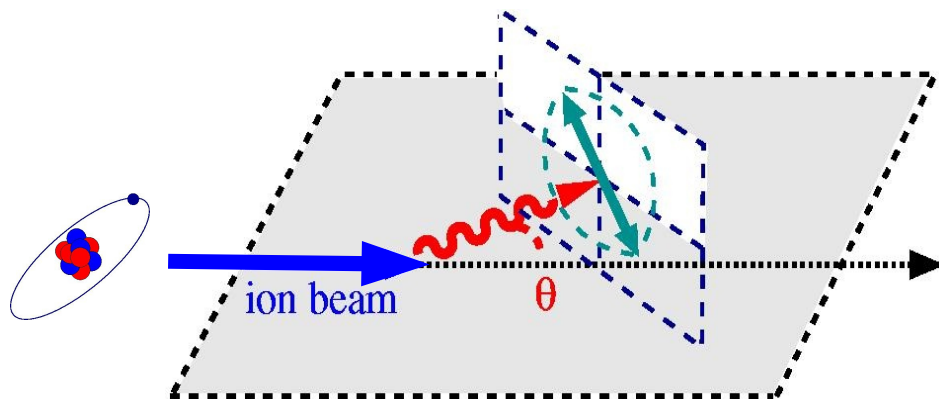
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$$\tan(2\phi) = \frac{P_2}{P_1}$$

direction of polarization

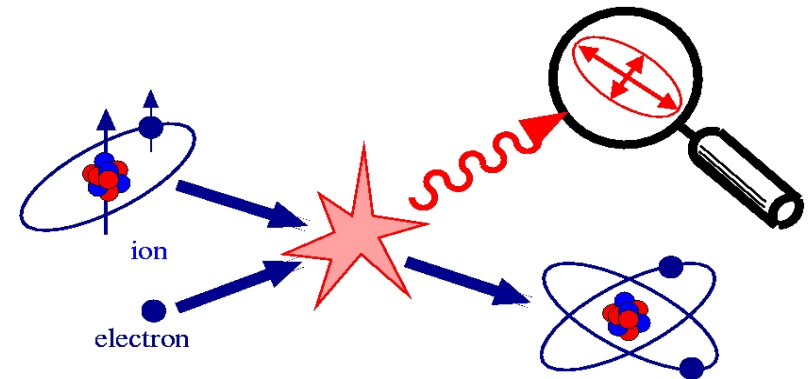
A. Surzhykov *et al.*, Phys. Rev. Lett. **94** (2005) 203202

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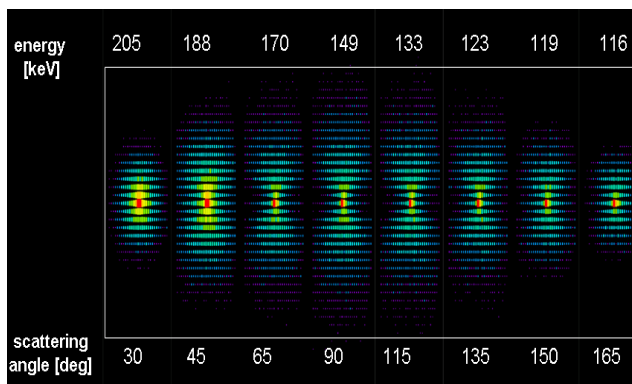
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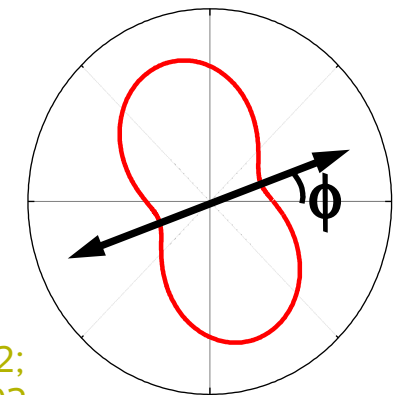


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$$\tan 2\phi = \frac{P_2}{P_1} \sim \lambda_F \frac{I-1/2}{I+1/2}$$

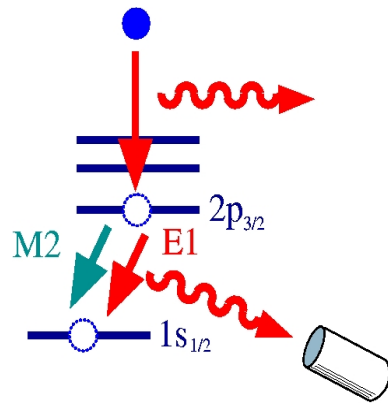


S. Tashenov *et al.*, PRL **97** (2006) 223202;
A. Surzhykov *et al.*, PRL **94** (2005) 203202.

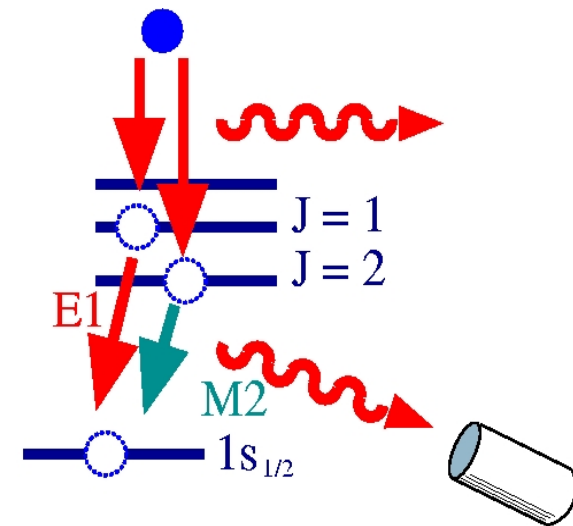
➡ Rotation angle ϕ provides information on the degree of ion polarization !

Two-step processes: Capture vs. excitation

-- Do we get more by following the dynamics of the ions ?

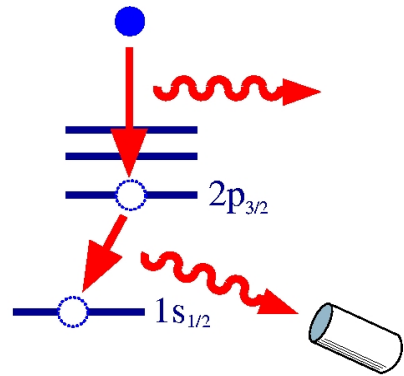


(initially) bare ion



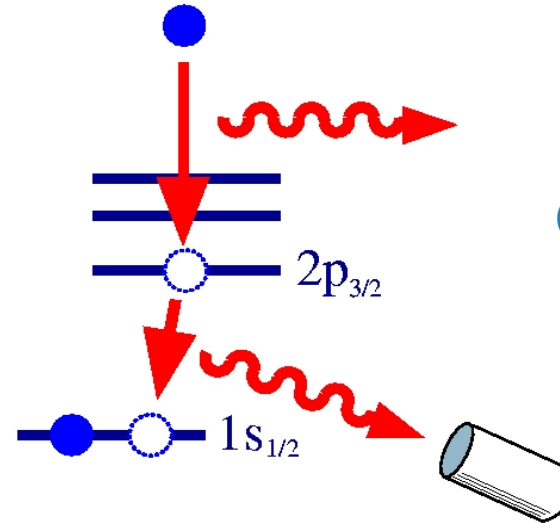
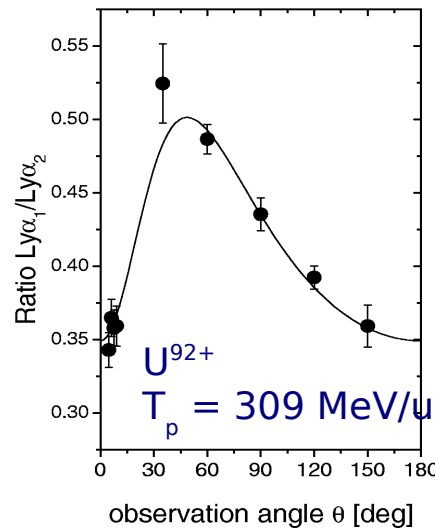
(initially) H-like ion

Lyman- α vs. K- α emission from high-Z ions



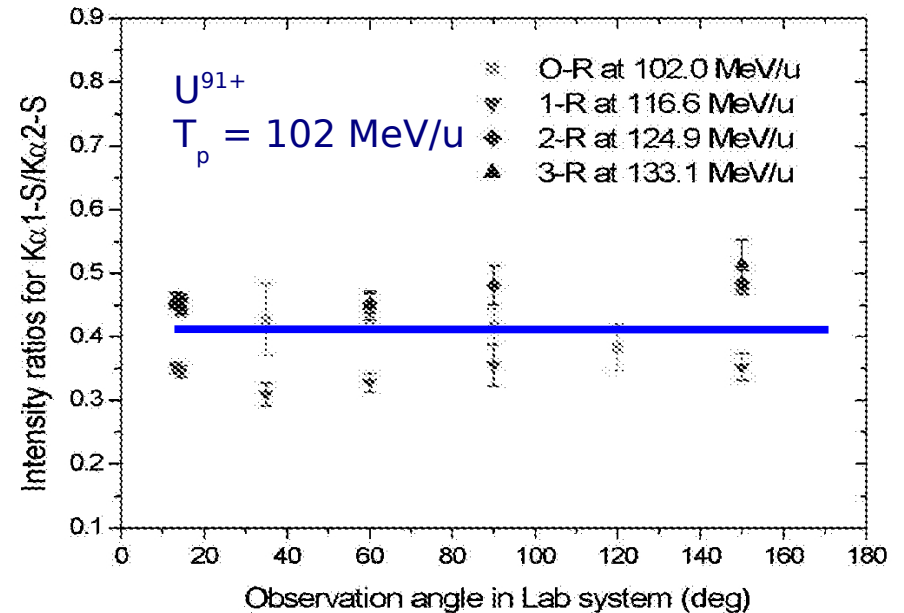
(initially) bare ion

Ly- α_1 is strongly anisotropic



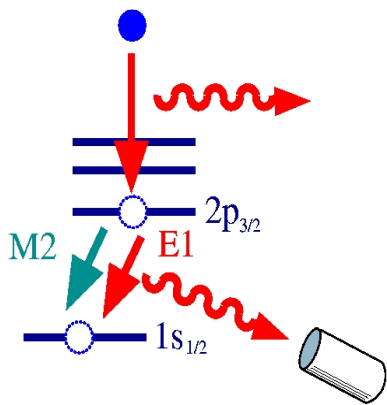
(initially) H-like ion

X. Ma et al, PRA 68 (2003) 042712.



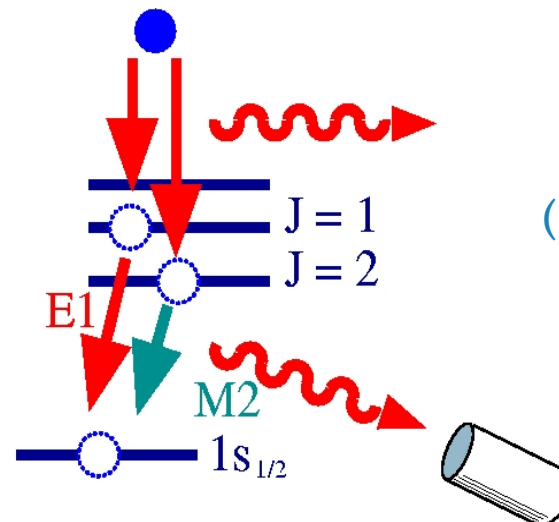
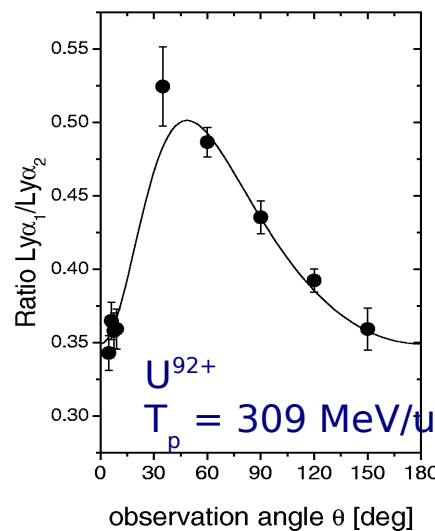
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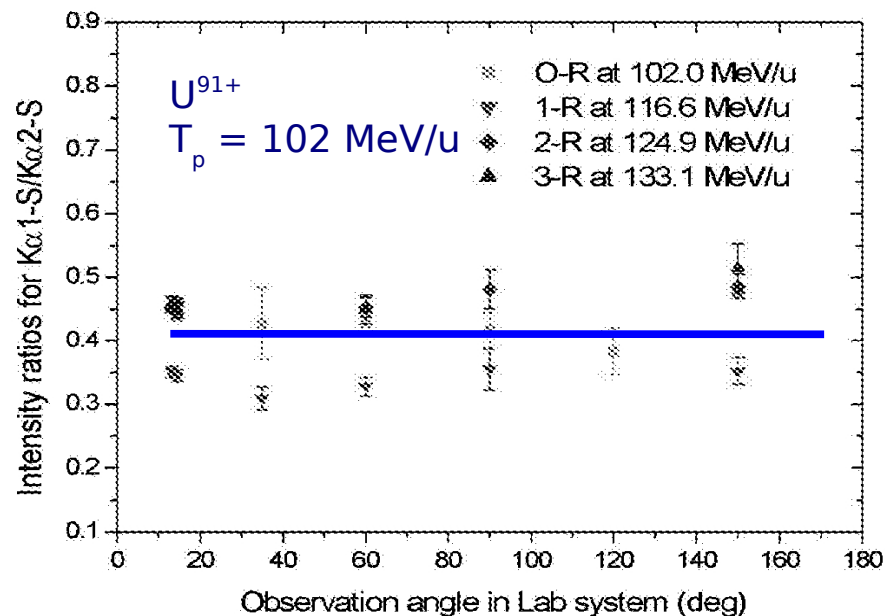
(initially) bare ion

Ly- α_1 is strongly anisotropic



(initially) H-like ion

X. Ma et al, PRA 68 (2003) 042712.



$$E1: W(\theta)_{E1} \sim 1 + \frac{1}{\sqrt{2}} A_2(J=1) P_2(\cos\theta)$$

$$M2: W(\theta)_{M2} \sim 1 - \sqrt{\frac{5}{14}} A_2(J=2) P_2(\cos\theta)$$

K- α_1 is isotropic

K- α decay of highly-charged ions

-- angular distribution as „observed“ in experiment

$$W(\theta)_{K\alpha_1} \sim N_{J=1} W_{E1}(\theta) + N_{J=2} W_{M2}(\theta)$$

A. Surzhykov et al., PRA 73 (2006) 032716.

$$= 1 + (N_{J=1} \frac{1}{\sqrt{2}} A_2(J=1) - N_{J=2} \sqrt{\frac{5}{14}} A_2(J=2)) P_2(\cos \theta)$$

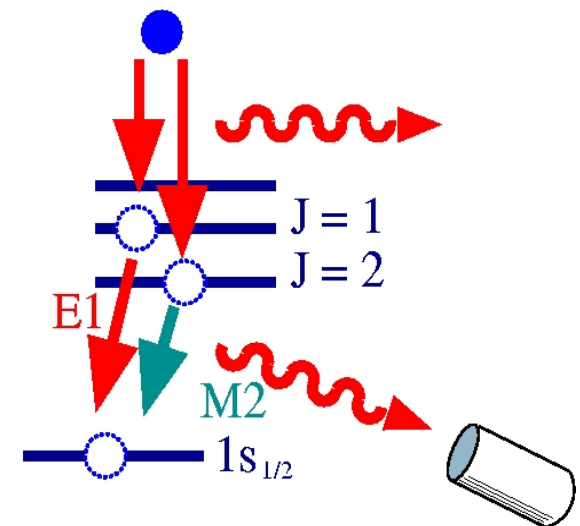
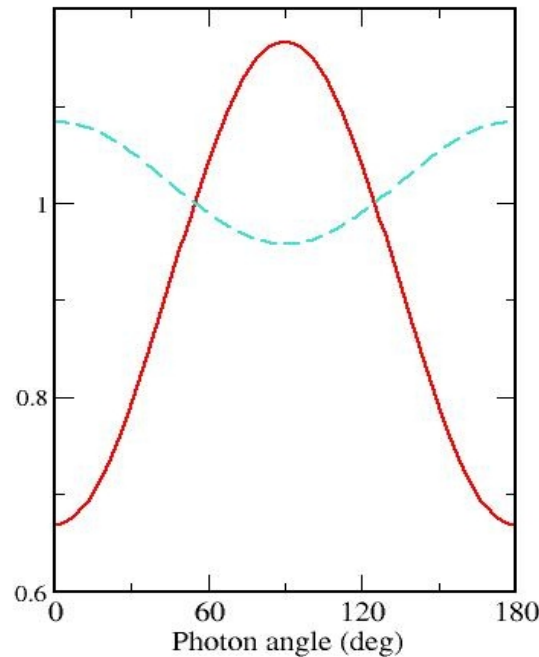
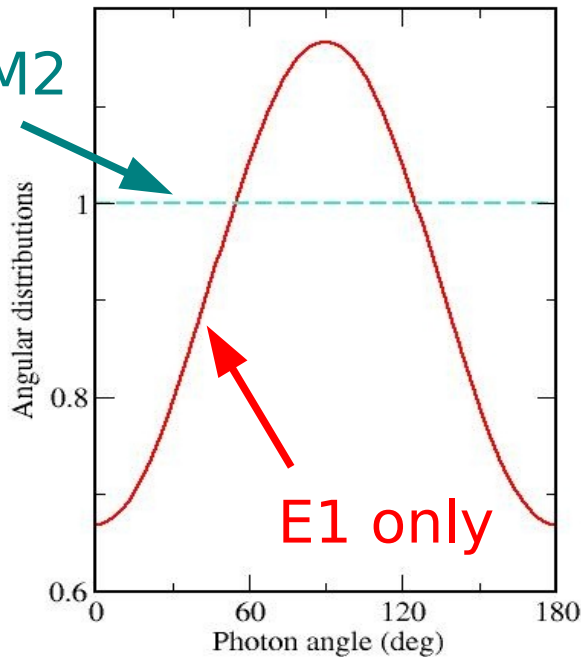
$N_{J=1}, N_{J=2}$ relative populations of J=1, 2 states

$$N_{J=1} = N_{J=2} = \frac{1}{2}$$

$$N_{J=1} = \frac{3}{8} \quad N_{J=2} = \frac{5}{8}$$

Calculations have been done for L-REC of U^{91+} with $T_p = 100$ MeV/u

E1+M2



K- α decay of highly-charged ions

-- for 220 MeV/u U⁹⁰⁺ ions following REC

$$W(\theta)_{K\alpha_1} \sim N_{J=1} W_{E1}(\theta) + N_{J=2} W_{M2}(\theta)$$

A. Surzhykov et al., PRA 73 (2006) 032716.

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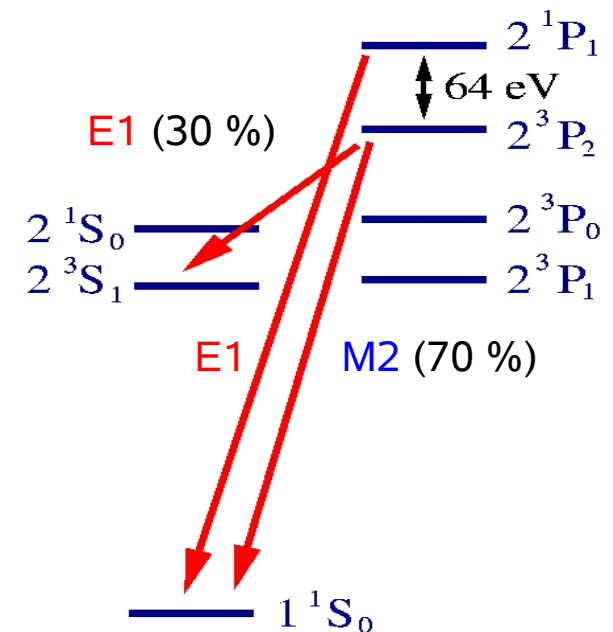
- Relative populations of the J = 1, 2 levels following REC (IPM model):

$$\frac{N_{J=1}}{N_{J=2}} = \frac{3}{5}$$

- By taking into account $^3P_2 \rightarrow ^3S_1$ channel:

$$\frac{N_{J=1}}{N_{J=2}} = \frac{6}{7}$$

$$\left(\frac{N_{J=1} - N_{J=2}}{N_{J=1} + N_{J=2}} \right)_{theory} \approx -0.08$$



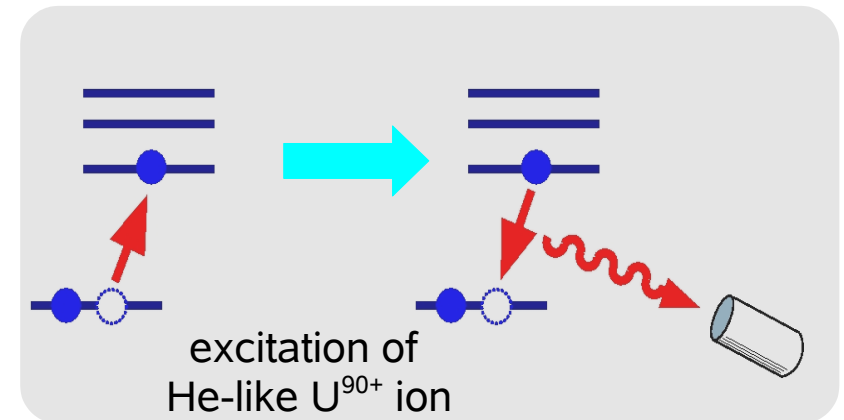
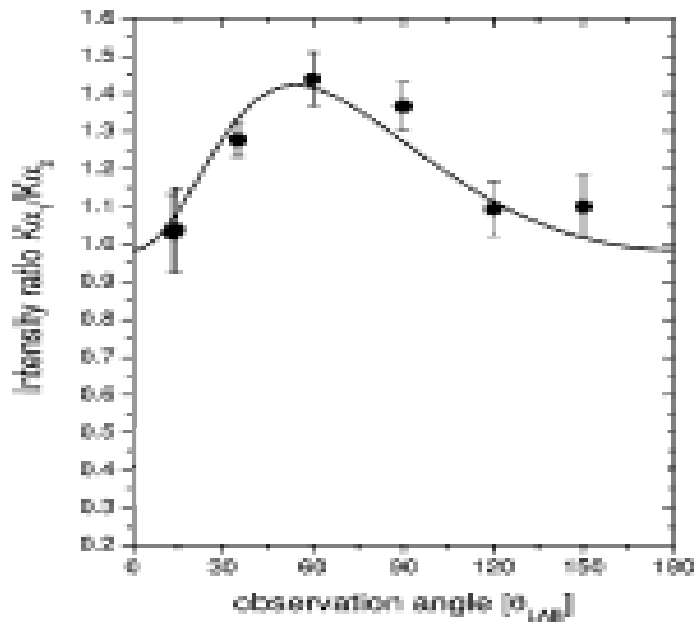
K- α decay of highly-charged ions

-- following the **Coulomb excitation** of the projectiles

$$W(\theta)_{K\alpha_1} \sim N_{J=1} W_{E1}(\theta) + N_{J=2} W_{M2}(\theta)$$

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- Excited states of He-like heavy ions can be produced also by the Coulomb excitation of the projectile in the field of target atoms.
- Experiments were already performed at the GSI storage ring for He-like uranium ions U^{90+} .
- Strong anisotropy of the subsequent $K\alpha_1$ radiation** has been observed!

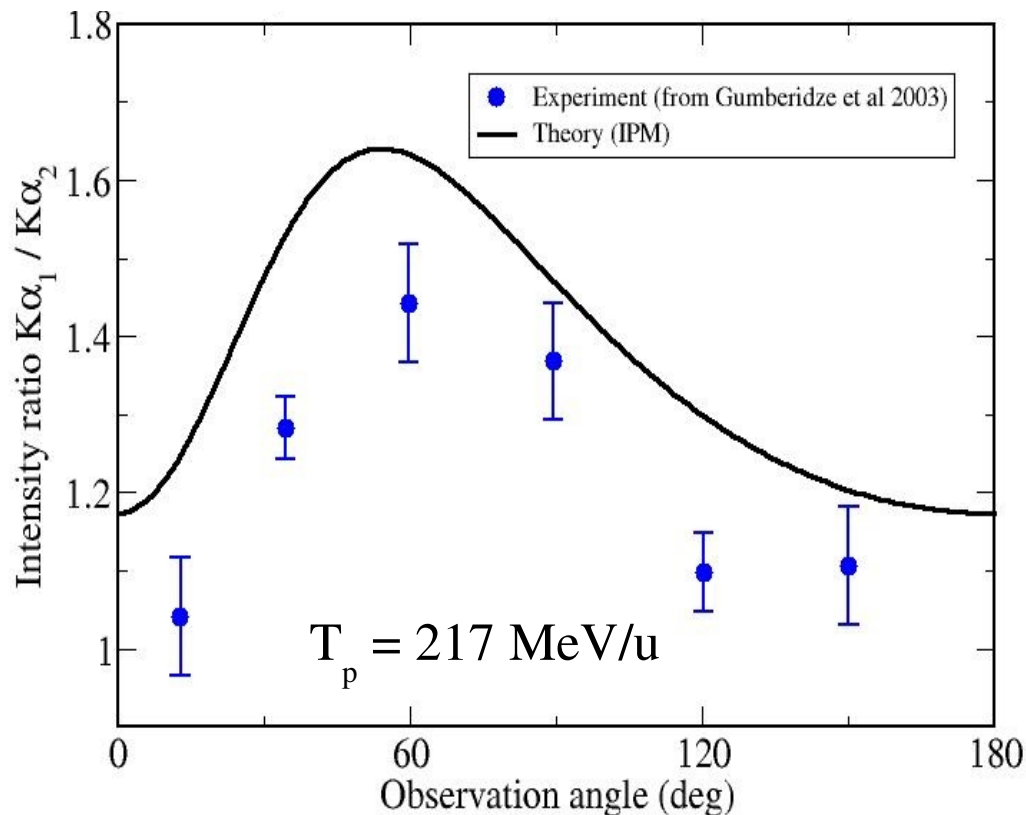
K- α decay of highly-charged ions

-- following the **Coulomb excitation** of the projectiles

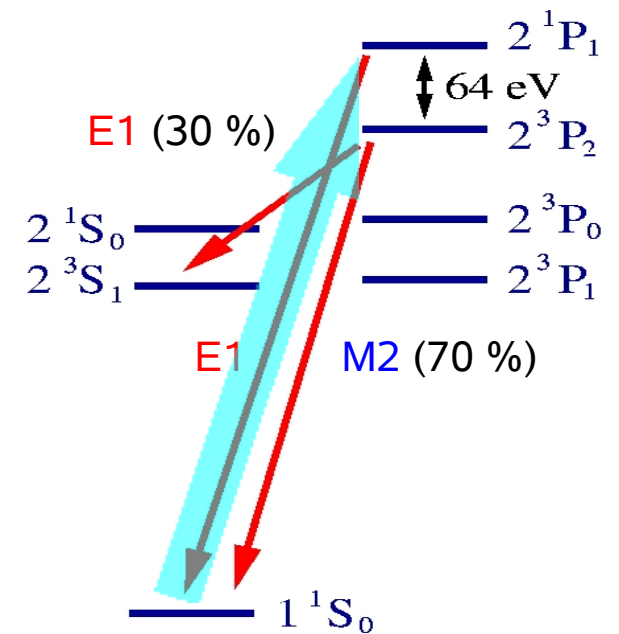
$$W(\theta)_{K\alpha_1} \sim N_{J=1} W_{E1}(\theta) + N_{J=2} W_{M2}(\theta)$$

$$= 1 + \left(N_{J=1} \frac{1}{\sqrt{2}} A_2(J=1) - N_{J=2} \sqrt{\frac{5}{14}} A_2(J=2) \right) P_2(\cos \theta)$$

$N_{J=1}, N_{J=2}$ **relative populations of J=1, 2 states**

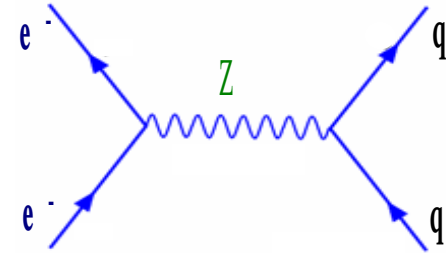
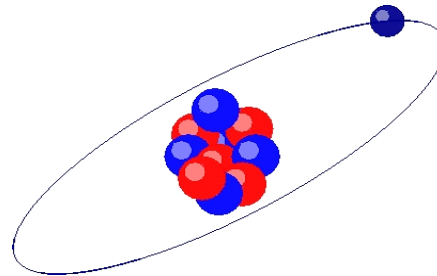
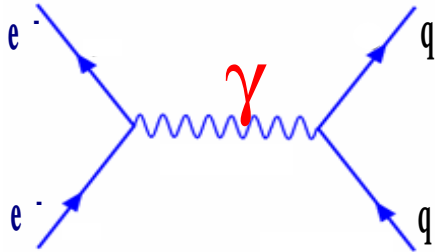


- Angular distribution results dominantly from the decay of the J=1 level.
- Role of electron-electron interactions still unexplored.



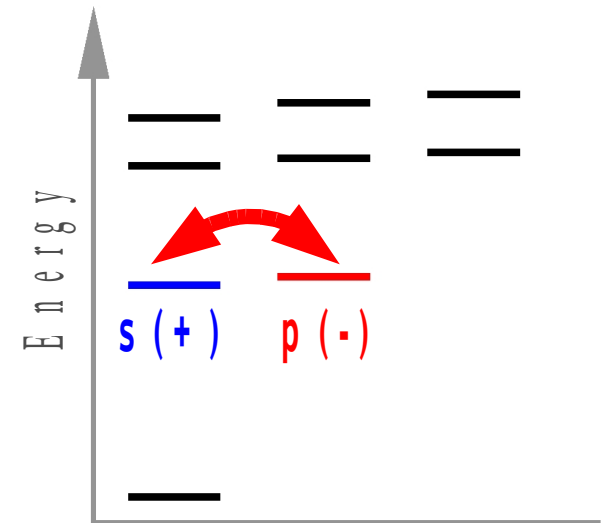
Atomic parity non-conservation processes

-- Two-photon processes for HCl



● Exchange of Z-boson leads to the mixing of atomic levels with different parities.

$$\eta = \frac{\langle \Psi_s | G_F / 2\sqrt{2} (1 - 4\sin^2\theta_w - N/Z) \rho_{el} \gamma_5 | \Psi_p \rangle}{E_s - E_p}$$

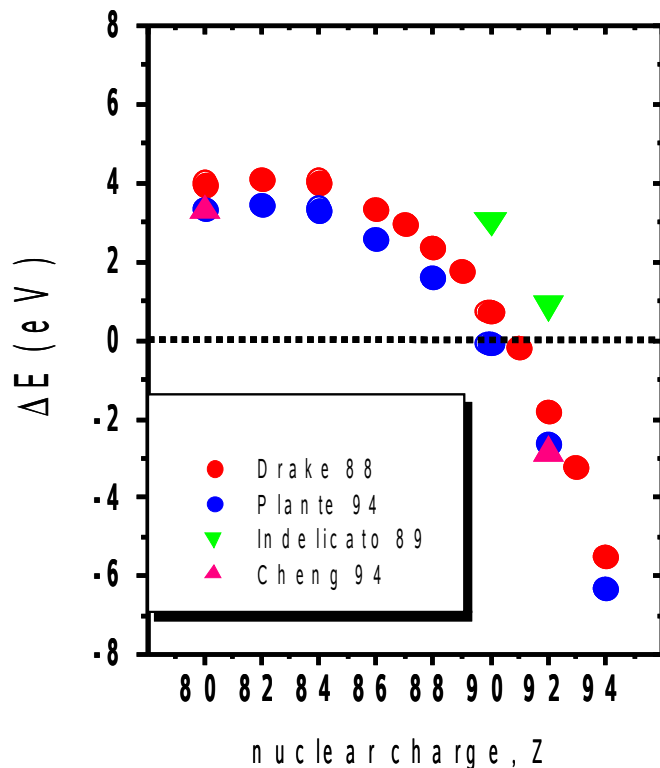
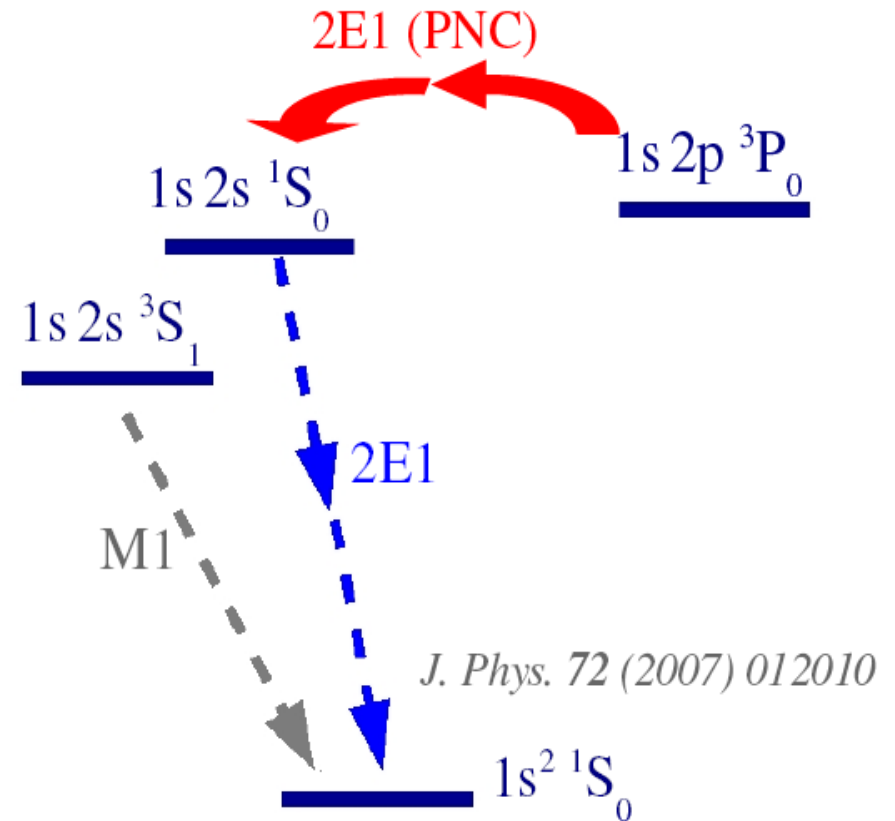


PNC studies with heavy, few-electron ions

-- enhancement of parity and time-reversal violating interactions

● Helium-like uranium U^{90+} is a perfect candidate for PNC studies:

- ➔ Simple system (only 2 electrons)
- ➔ Large electron-nucleus overlap
- ➔ Small 2^1S_0 - 2^3P_0 energy splitting



● Still many open questions:

- ➔ How big is the 2^1S_0 - 2^3P_0 energy splitting?
- ➔ How strong laser fields do we need?
- ➔ What is the role of e-e interactions?

There is a need for accurate many-electron calculations !

- Analysis and interpretation of optical and x-ray spectra (astro physics)
- Diagnostics of astro physical and laboratory plasmas
- Development of UV/EUV light sources and lithography
- Frequency standards and atomic clocks

„many but not so accurate“

➔ Spectroscopy on heavy and superheavy elements (actinides, transactinides)

➔ Isotope shifts and hyperfine structures

• Nonradiative (inner-shell) transitions and autoionization

➔ Ion recombination and photon emission

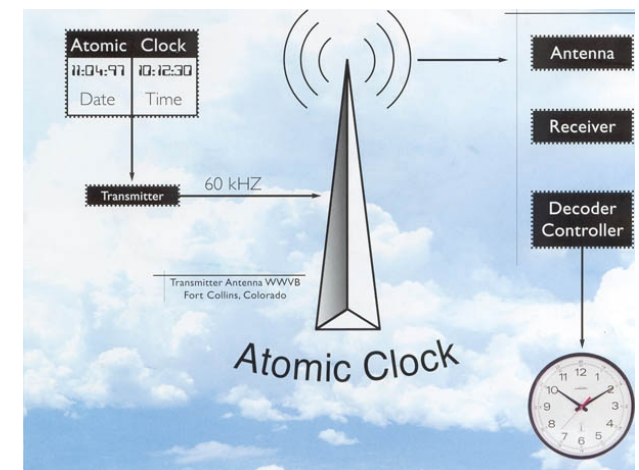
• Multi-photon processes

• ...

• „Complete experiments“

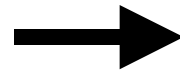
➔ Parity nonconservation (PNC)

• Search for electric dipole moments

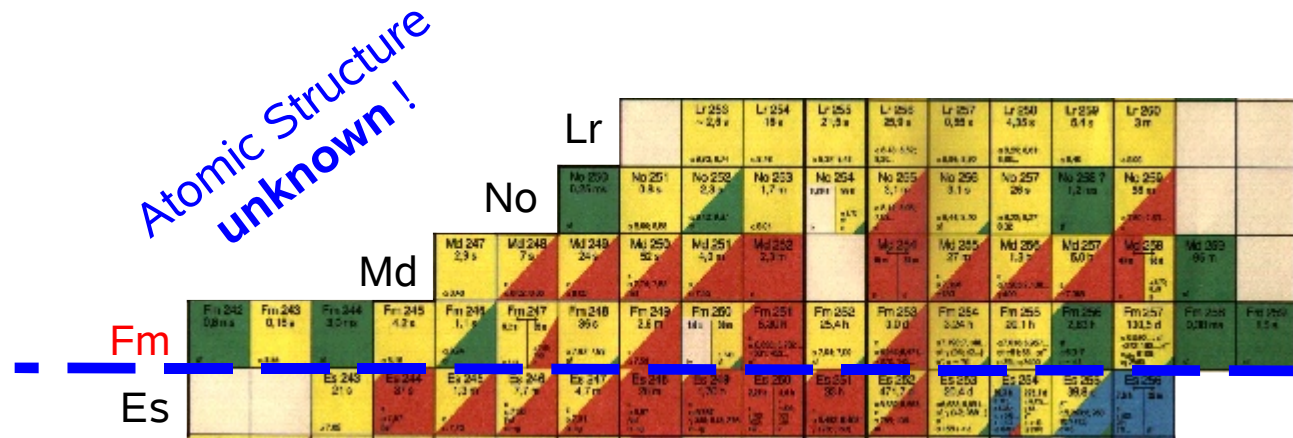


Spectroscopy of heavy and super-heavy elements

Atomic Levels



Atomic Physics : Atomic Structure
Ionization Potentials
Nuclear Physics : Nuclear Spins, Moments



Backe, Lauth, Sewtz (Mainz)

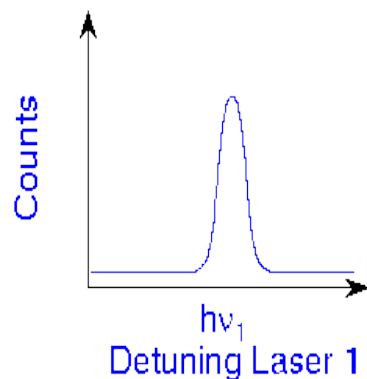
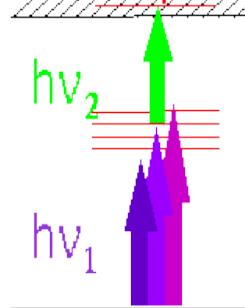
Theoretical challenges:

- strong relativistic and QED effects
- systems with open d- and f-shells
- many overlapping and nearly degenerate configurations
- large number of electron

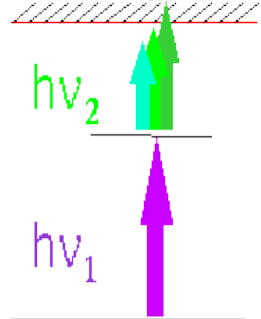
Optical spectroscopy of atomic Fermium ($Z = 100$)

First observation and classification of atomic levels

Determination of hfs and isotope shifts



Determination of the IP



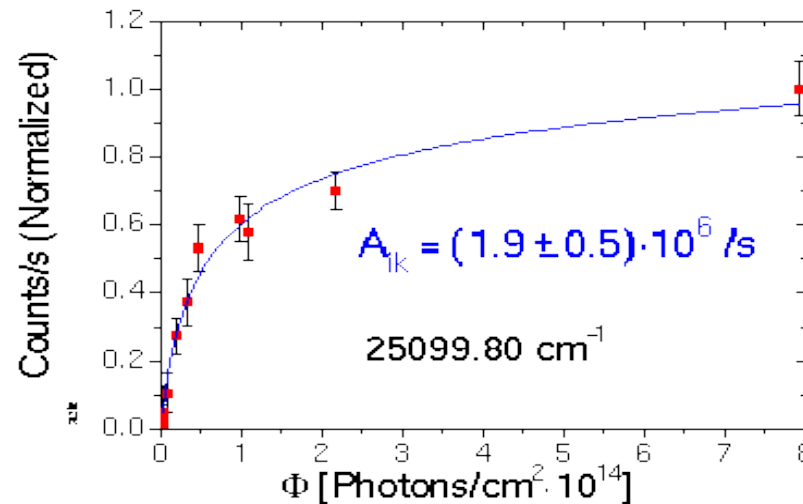
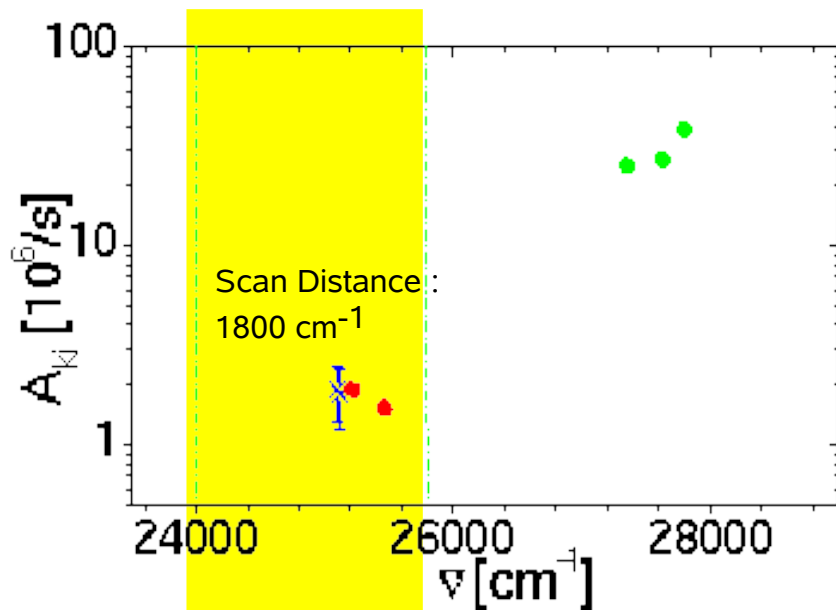
Atomic Physics:

- ➔ Atomic Structure
- ➔ Ionization potentials

Nuclear Physics:

- ➔ Nuclear spins
- ➔ Moments
- ➔ Changes of charge radii

Theoretical request: Energies, lifetimes, transition rates



$5f^{12} 7s 7p, JP = 6^-, 5$ $5G_{6,5^0}$
 ES: $5f^{12} 7s 7p, JP = 6^-, 5^-, 7^-$ $3H_{6,5,7^0} (?)$

Breeding in High Flux Reactors
 $N_{Fm} < 10^{12}$; ^{255}Fm ; $t_{1/2} = 20.1$ h

Experimental proposal: Optical spectroscopy of nobelium (Z=102)

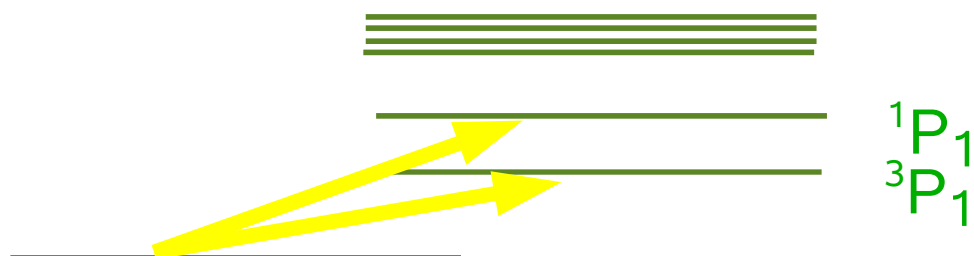
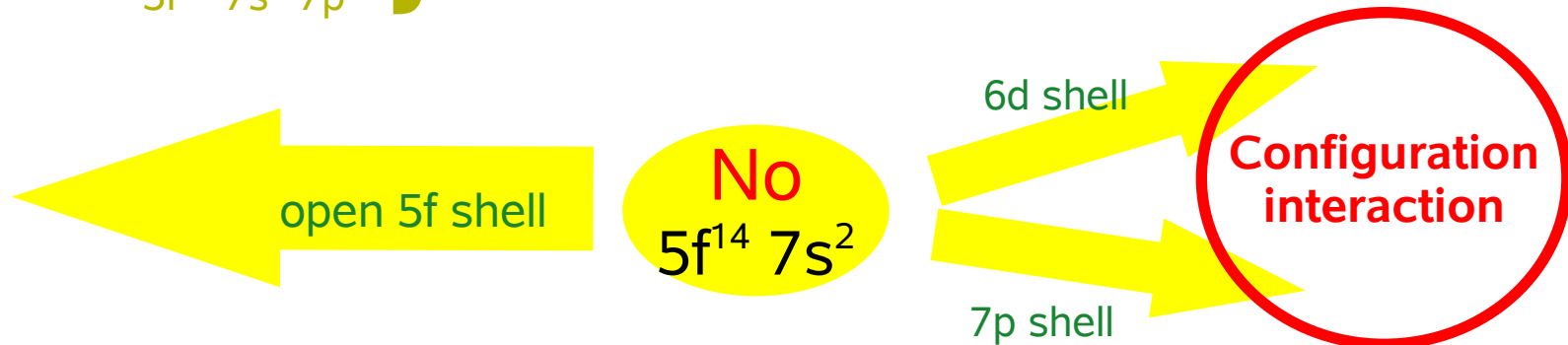
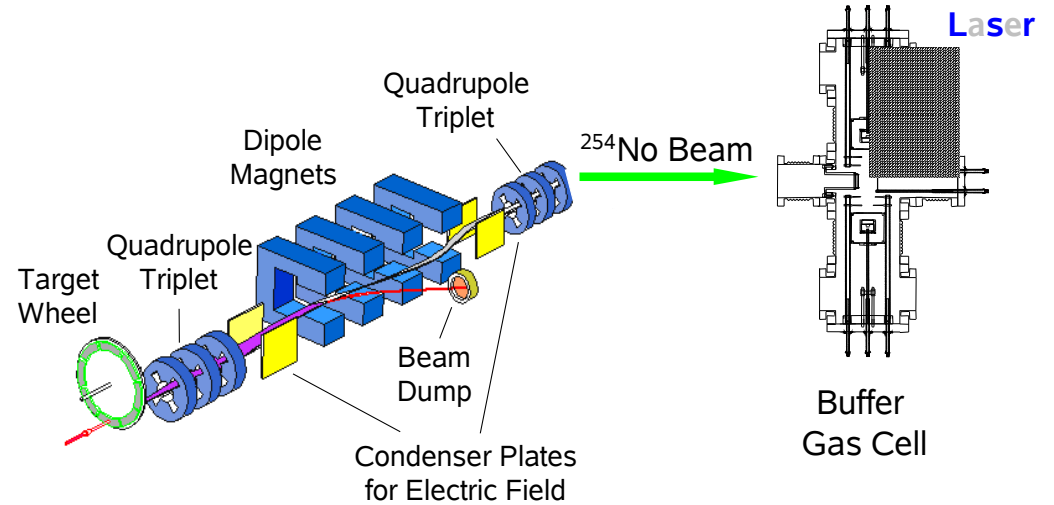
Ground-state configuration:



Low-lying excitations:



2 ... 5 eV



	Level	$2S+1 L_J$	Excitation energy (eV)	
			Model I	Model II
No	$5f^{14} 7s 7p$	$^3 P_1$	2.34	2.60
	$5f^{14} 7s 7p$	$^1 P_1$	3.49	3.36

Low-lying resonances of (super-) heavy elements

... for lutetium (Z=71) and lawrencium (Z=103)

TABLE I. The transition energies in cm^{-1} of $nd\ ^2D_{3/2} - (n+1)p\ ^2P_{1/2,3/2}^o$ and the size of CSF expansions for Lu ($n=5$) and Lr ($n=6$).

Expansion	$^2D_{3/2} - ^2P_{1/2}^o$	$^2D_{3/2} - ^2P_{3/2}^o$	CSF ($^2D_{3/2}/^2P_{1/2}^o/^2P_{3/2}^o$)
Lu			
VV + CV($4f^{14}$)	3989	7276	4354/2071/3813
VV + CV($5p^64f^{14}$)	8004	11 483	5600/2764/5073
VV + [(CV + CC) ($5p^64f^{14}$)]	3857	7130	128 763/36 974/100 277
VV + [(CV + CC) ($4d^{10}5s^25p^64f^{14}$)]	4186	7462	305 717/87 241/236 554
RCC [7]	3828	7140	
DFT [10]	3862		
Exp.	4136	7476	
DHF Breit Correction	87	53	
DHF Breit & QED Correction	76	43	
Lr			
VV + CV($5f^{14}$)	-1298	9137	3659/1842/3338
VV + CV($6p^65f^{14}$)	1339	12 761	4708/2495/4495
VV + [(CV + CC) ($6p^65f^{14}$)]	-1953	6469	125 325/37 333/97 500
VV + [(CV + CC) ($5d^{10}6s^26p^65f^{14}$)]	-1127	7807	330 252/95 969/246 376
RCC	-1388	6960	
RCC with Breit	-1263	7010	
DHF Breit Correction	97	4	
DHF Breit & QED Correction	59	-26	

Low-lying resonances of (super-) heavy elements

... oscillator strengths in different gauges

TABLE II. The oscillator strengths of $nd\ ^2D_{3/2} - (n+1)p\ ^2P_{1/2,3/2}^o$ for Lu ($n=5$) and Lr ($n=6$).

Expansion	$^2D_{3/2} - ^2P_{1/2}^o$			$^2D_{3/2} - ^2P_{3/2}^o$		
	gf_L	gf_V	Scaled gf_L	gf_L	gf_V	Scaled gf_L
Lu						
VV + CV($4f^{14}$)	0.0304	0.0582	0.0315	0.0111	0.0219	0.0114
VV + CV($5p^6 4f^{14}$)	0.0511	0.1552	0.0264	0.0144	0.0467	0.0094
VV + [(CV + CC) ($5p^6 4f^{14}$)]	0.0908	0.3835	0.0974	0.0322	0.0856	0.0337
VV + [(CV + CC) ($4d^{10} 5s^2 5p^6 4f^{14}$)]	0.1043	0.3345	0.1031	0.0354	0.0742	0.0355
Lr						
VV + CV($5f^{14}$)	-0.0162	-0.0076		0.0210	0.0313	
VV + CV($6p^6 5f^{14}$)	0.0144	0.2359		0.0227	0.0839	
VV + [(CV + CC) ($6p^6 5f^{14}$)]	-0.0624	-0.0002		0.0414	0.0867	
VV + [(CV + CC) ($5d^{10} 6s^2 6p^6 5f^{14}$)]	-0.0378	-0.0024		0.0519	0.0685	

Good accuracy of the (atomic) energies is a necessary, but not a sufficient criterion !

RATIP

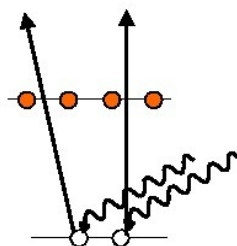
Relativistic Atomic Transition and Ionization Properties

(CPC library)

$$\Psi_{\alpha}(P J M) = \sum_r^{n_c} c_r(\alpha) |y_r P J M\rangle$$

Many-electron basis (wave function expansions)

- Construction and classification of N-particle Hilbert spaces
- Shell model:** Systematically enlarged CSF basis
- Interactions**
 - Dirac-Coulomb Hamiltonian
 - Breit interactions + QED
 - Electron continuum; scattering phases
- Coherence transfer and Rydberg dynamics**



Relativistic CI wave functions
including QED estimates and
mass polarization

REL CI, CPC 148 (2002) 103

LSJ spectroscopic notation
from jj-coupled
computations

LSJ, CPC 157 (2003) 239

Auger rates, angular distribu-
tions and spin polarization;
level widths

AUGER

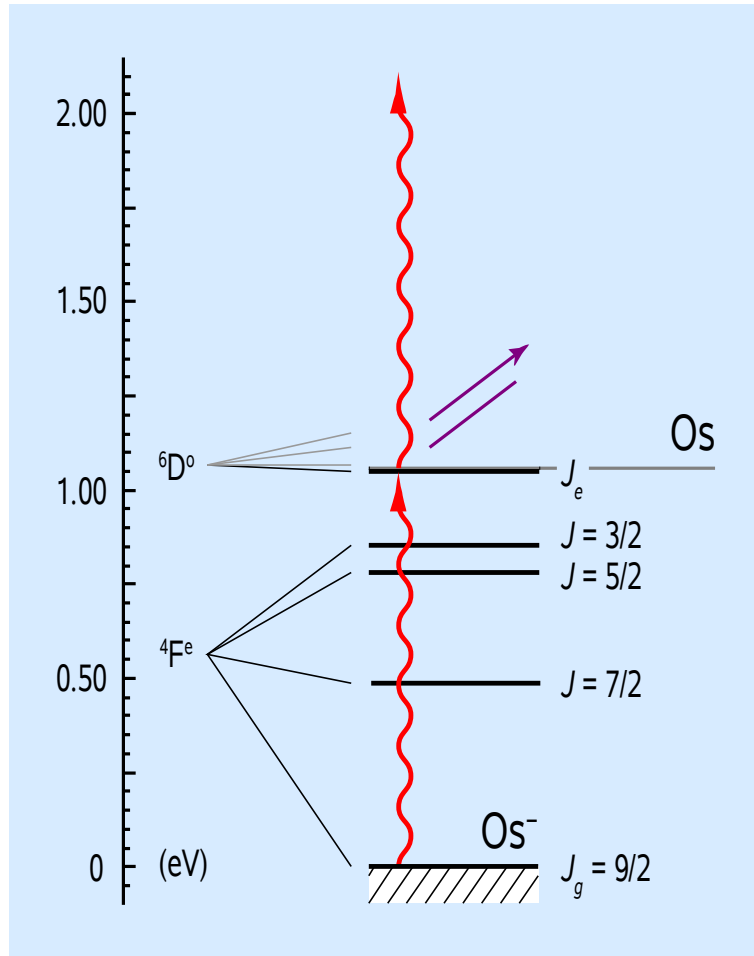
Photoionization cross sect-
ions and (non-dipole) angular
parameters

PHOTO

Radiative and dielectronic
recombination; angle-angle
correlations

...

HFS & Isotope shift measurements for Os⁻



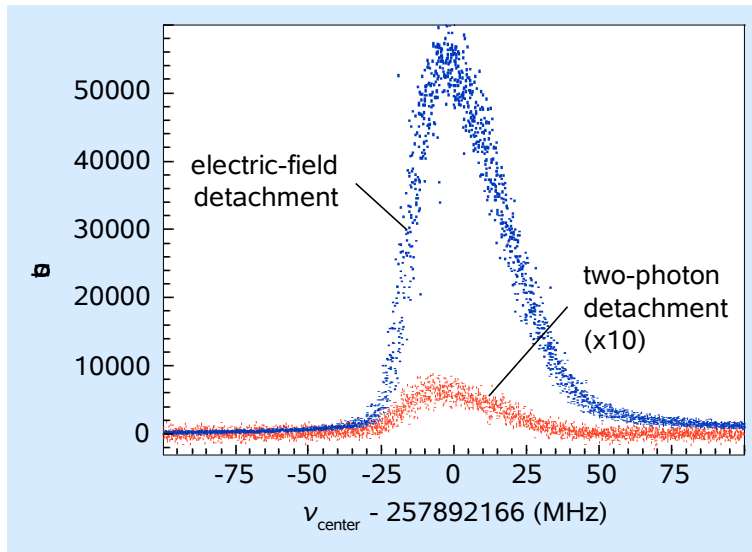
Typical spectrum ${}^{192}\text{Os}^-$:

Signal: Neutral atoms as function
of laser frequency

$$\Rightarrow \nu = 257.831190(30) \text{ THz}$$
$$\lambda = 1162.74706(14) \text{ nm}$$

U. Warring *et al.*, Phys. Rev. Lett. **102** (2009) 043001

HFS & Isotope shift measurements for Os-



Typical spectrum $^{192}\text{Os}^-$:

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U. Warring *et al.*, Phys. Rev. Lett. **102** (2009) 043001

$$M_{\text{NMS}} = \nu_0 \frac{m_e}{1u} = 0.14 \text{ THz u}$$

Experiment:

$$M_{\text{SMS}} = 2(11) \text{ THz u}$$

$$F = 16(9) \text{ GHz fm}^{-2}$$

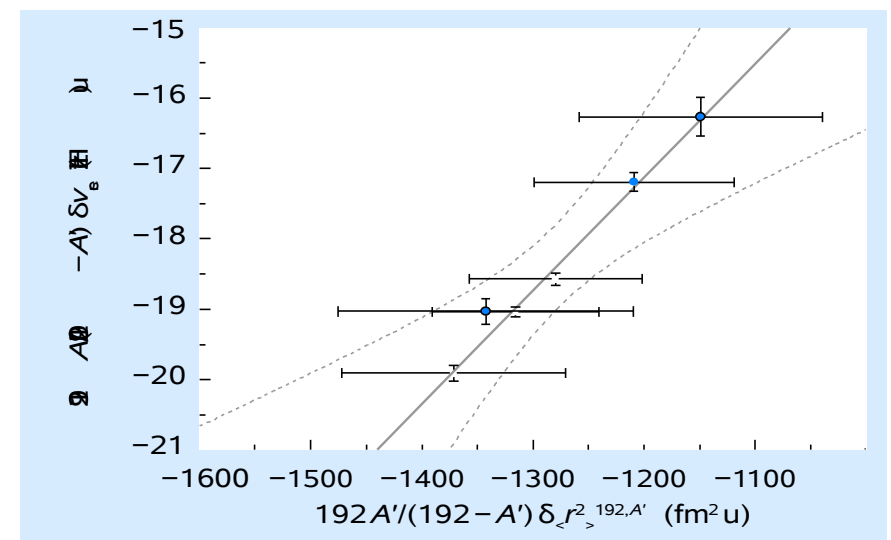
Theory:

$$M_{\text{SMS}} = 4.9 \text{ THz u}$$

$$F = 12.4 \text{ GHz fm}^{-2}$$

preliminary

Transition for all stable isotopes:

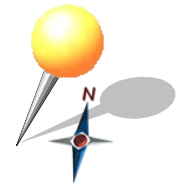
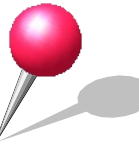


Atomic and heavy-ion theory @ SPARC collaboration

-- Recent developments and progress

Key topics of this collaboration:

- Test of quantum electrodynamics in strong fields for light and high-Z ions
 - ... two-times Green's functions; 2-photon, 3-photon (??) diagrams; differences with experiment especially for the HFS; systematic QED approach in the MBPT framework
- Collision & capture dynamics in strong fields at relativistic energies
 - ... U28+ electron loss; few-body dynamics; polarization effects; multi-electron processes
- Atomic physics techniques applied to nuclear physics
- Multi-photon processes
- Antiproton physics
- Test of fundamental interactions and symmetries beside of QED
- Interaction of ions with intensive (laser) light
 - ... dynamics in strong fields, high-harmonics generation



Atomic and heavy-ion theory @ SPARC collaboration

-- Recent developments and progress

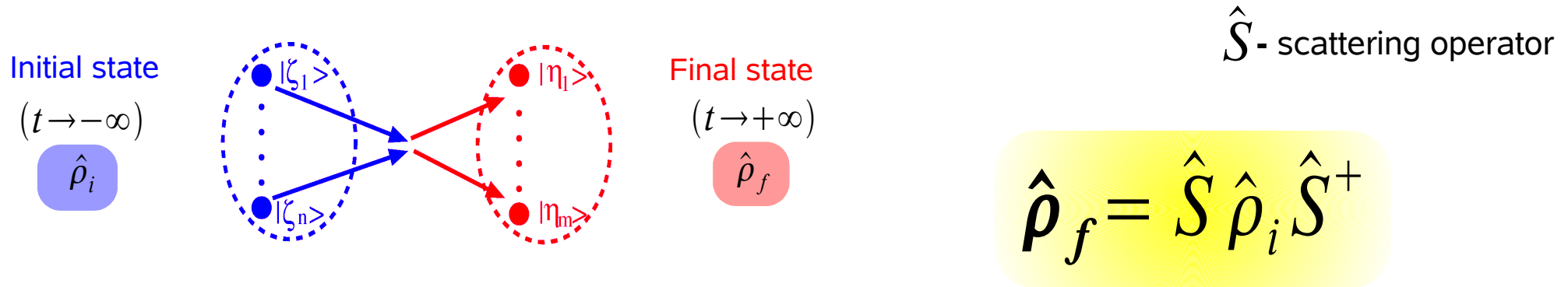
Key topics of this collaboration:

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 - ... two-times Green's functions; 2-photon, 3-photon (??) diagrams; differences with experiment especially for the HFS; systematic QED approach in the MBPT framework
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 - ... U28+ electron loss; few-body dynamics; polarization effects; multi-electron processes
- Atomic physics techniques applied to nuclear physics
- Multi-photon processes
- Antiproton physics
- Test of fundamental symmetries beyond QED
- Interaction of ions with intense laser fields
 - ... dynamics in strong fields

Thank you



Time-independent density matrix theory



$$\langle \eta_1 \dots \eta_m | \hat{\rho}_f | \eta'_1 \dots \eta'_m \rangle = \sum_{\xi_1, \xi_2, \dots} \langle \xi_1 \dots \xi_n | \hat{\rho}_i | \xi'_1 \dots \xi'_n \rangle \langle \eta_1 \dots \eta_m | \hat{R} | \xi_1 \dots \xi_n \rangle \langle \eta'_1 \dots \eta'_m | \hat{R} | \xi'_1 \dots \xi'_n \rangle^+$$

↙ initial-state density matrix ↘ transition amplitudes

Measurement of physical properties:

- 'detector operator' describes the experimental setup:
- probability to get a 'click' at the detectors:

$$\hat{P} = |\epsilon\rangle \langle \epsilon|$$

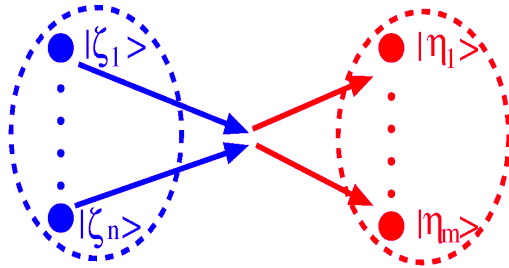
$$W = \text{Tr}(\hat{P} \hat{\rho}_f) = \sum_{\eta_1 \dots \eta_m} \langle \eta_1 \dots \eta_m | \hat{P} \hat{\rho}_f | \eta_1 \dots \eta_m \rangle$$

Time-independent density matrix theory

Initial state

($t \rightarrow -\infty$)

$$\hat{\rho}_i$$



Final state

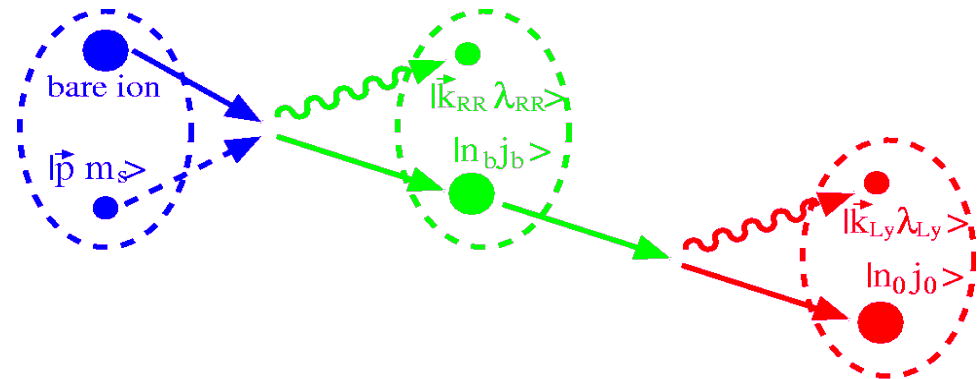
($t \rightarrow +\infty$)

$$\hat{\rho}_f$$

\hat{S} - scattering operator

$$\hat{\rho}_f = \hat{S} \hat{\rho}_i \hat{S}^+$$

Great advantage!



Using the density matrix, the system can be accompanied through several steps of the interaction which may lead to the emission of photons, electrons, ...

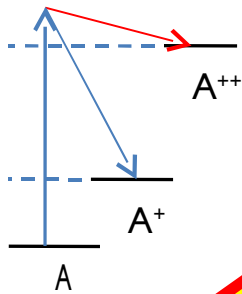
Weak- vs. strong-field (light-matter) interactions

Weak-field photoexcitation and ionization

cross sections, angular distributions

for example: single-photon double ionization

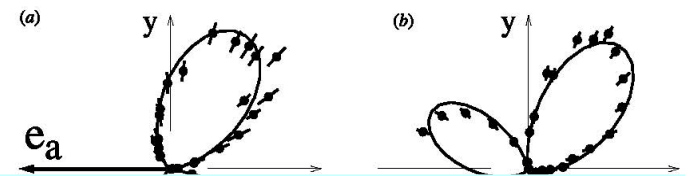
'experiments', ...;



Domain of precision physics

parity and time-reversal violating interactions.

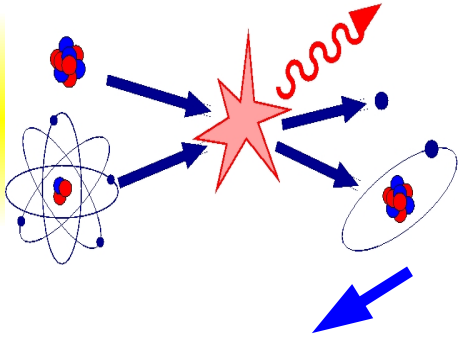
(Briggs and Schmidt, 2000)



Current interests and challenges

- Atomic processes and multipole mixing in strong fields
- Multi-electron coincidences (magnetic bottle)
- Second-order emission processes
- Creation and control of entangled photon pairs
- Parity non-conservation and time-reversal violation
- Studying fundamental constants (time variations, ...)

Different mechanisms: shall



Ion-Atom Stöße

schnelle Stöße

„Einteilchenbild“

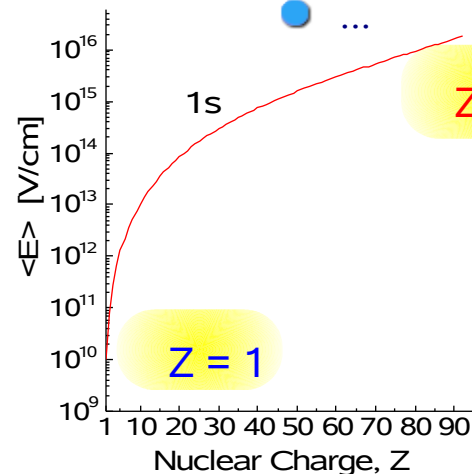
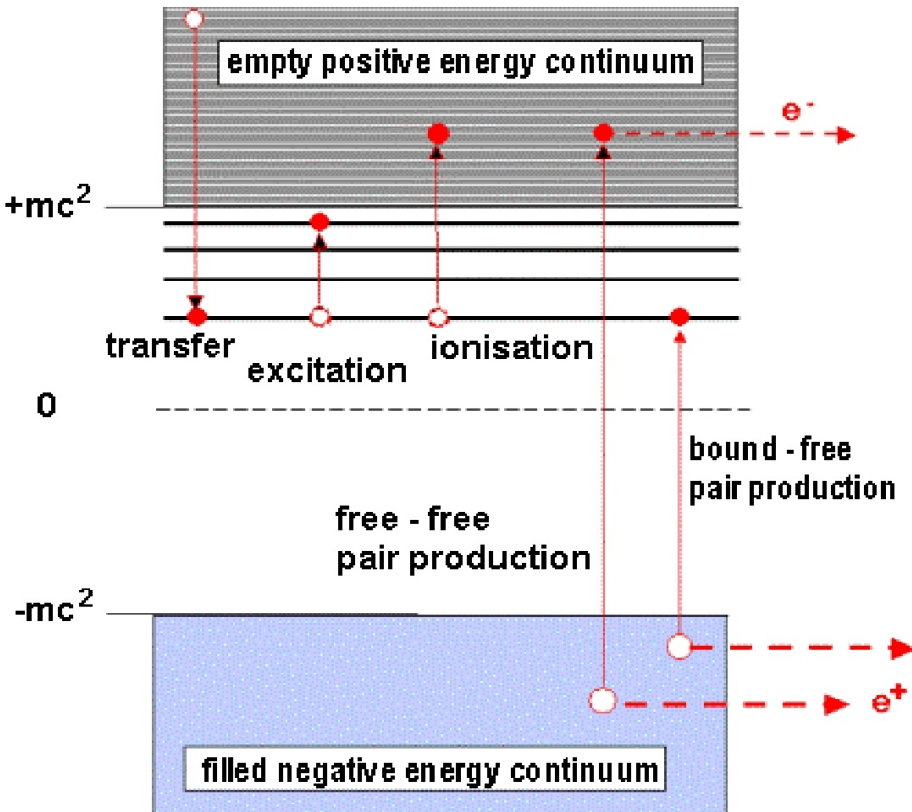
- ▶ Hochgeladene Ionen sind sehr gut geeignet, um die elementaren Prozesse in (extrem) starken Feldern zu verstehen.

langsame Stöße

„Vielteilchenbild“

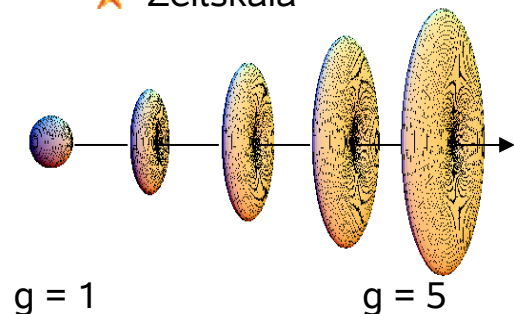
- ▶ Besseres Verständnis der Vielteilchendynamik erforderlich.

- Verstärkung des REC bei langsamen Ionen (!)
- Resonante (dielektronische) Rekombination.
- Abbremsen und Einfang in Fallen.
- Wichtig für Ionen-Oberflächen Prozesse.
- ...

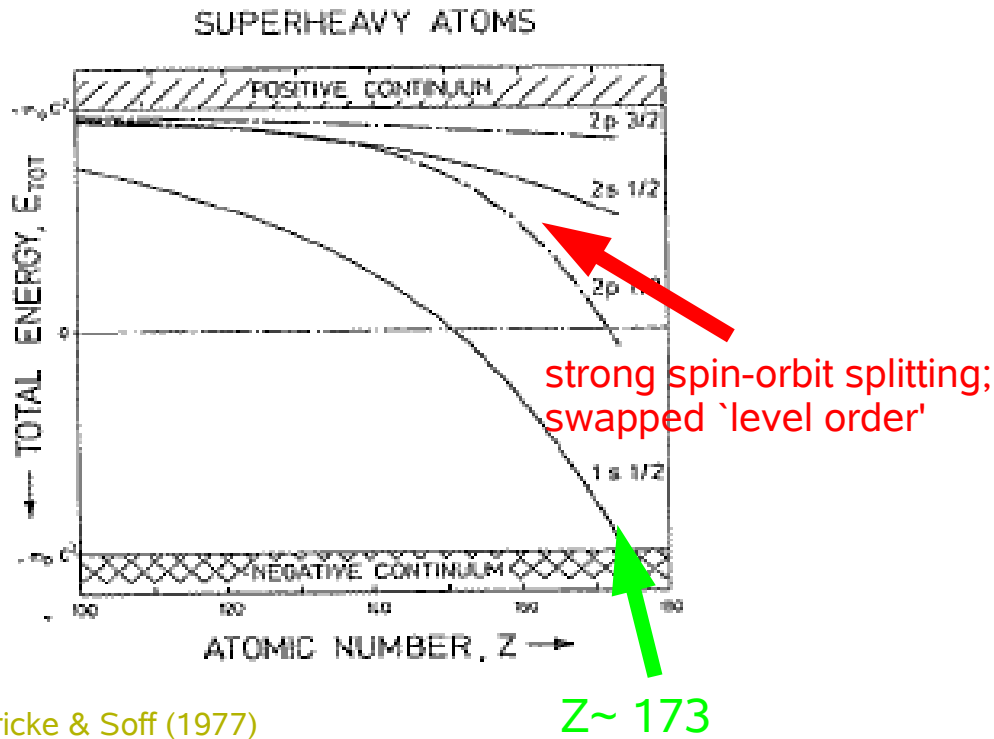


Ionen sind variabel:

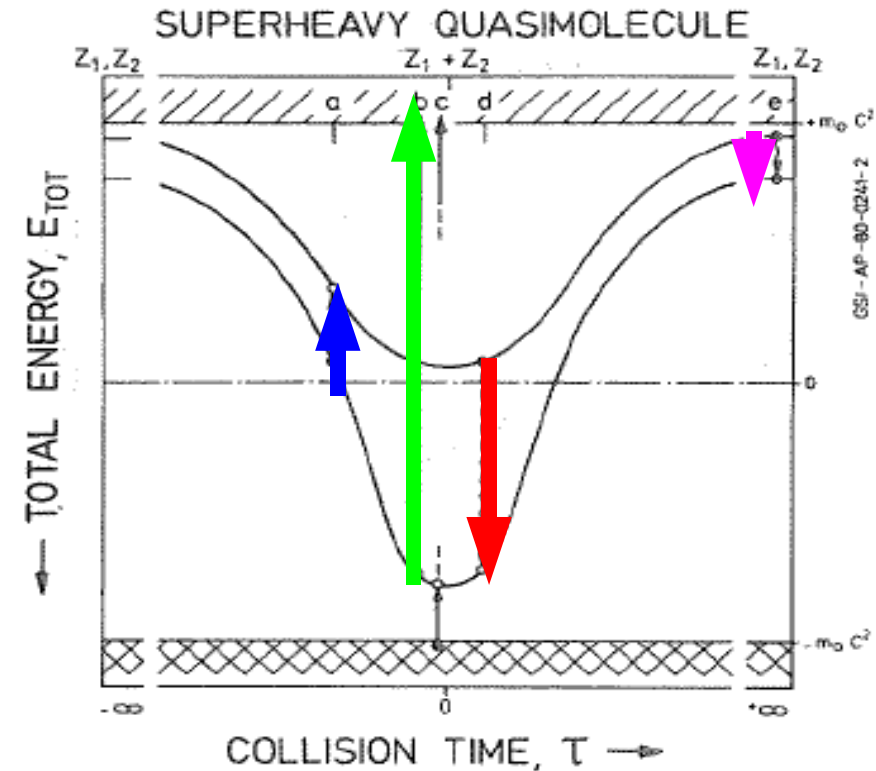
- ★ Feldstärke
- ★ Zahl der Elektronen
- ★ Zeitskala



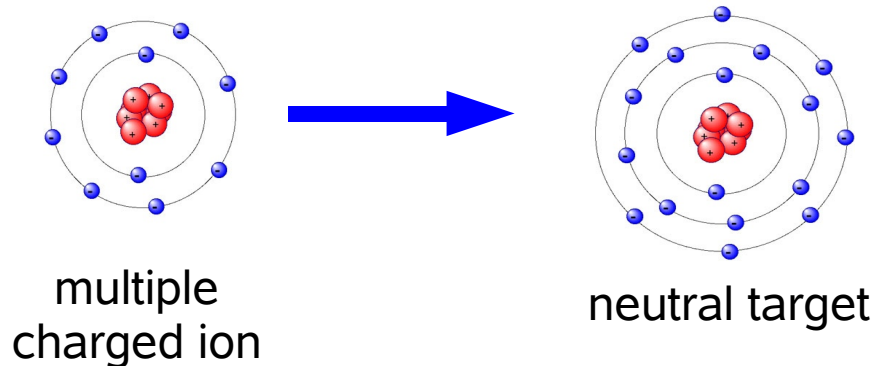
Supercritical fields in ion-atom collisions



Fricke & Soff (1977)



Mokler & Liesen (1982)

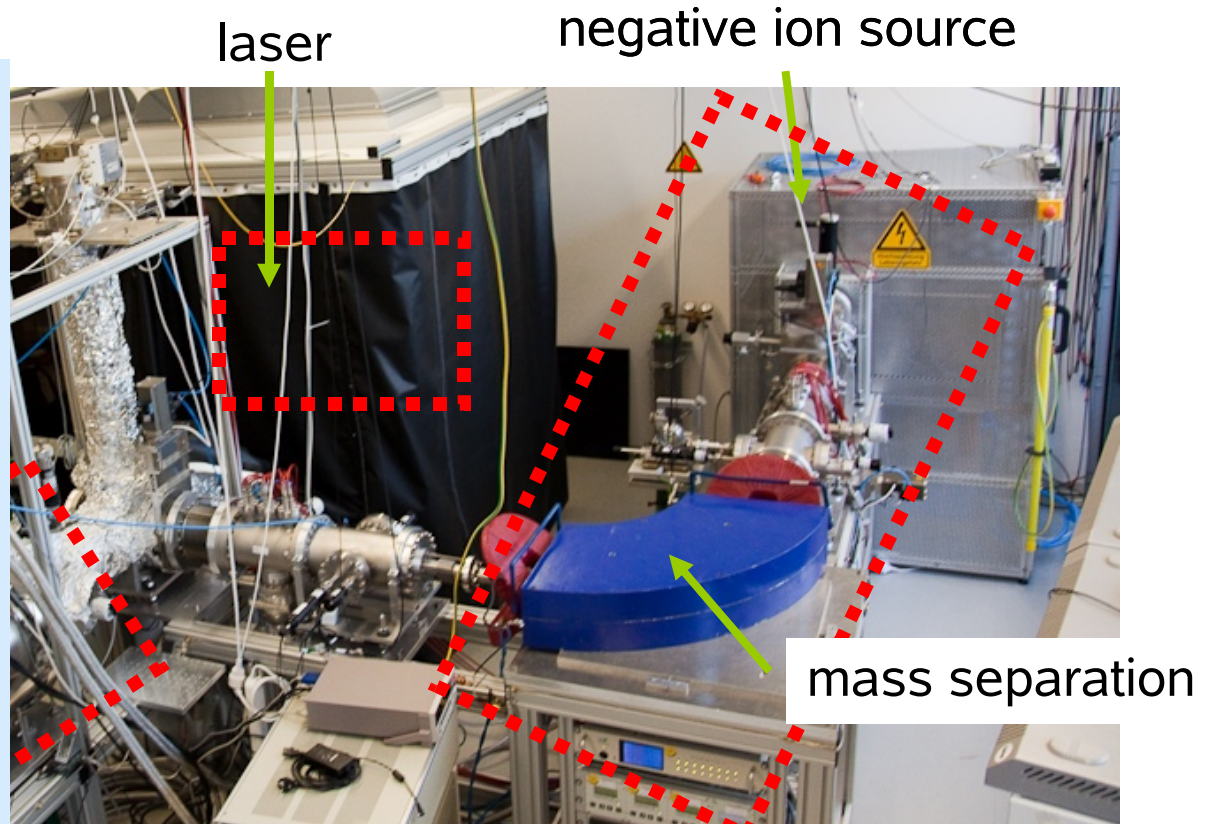
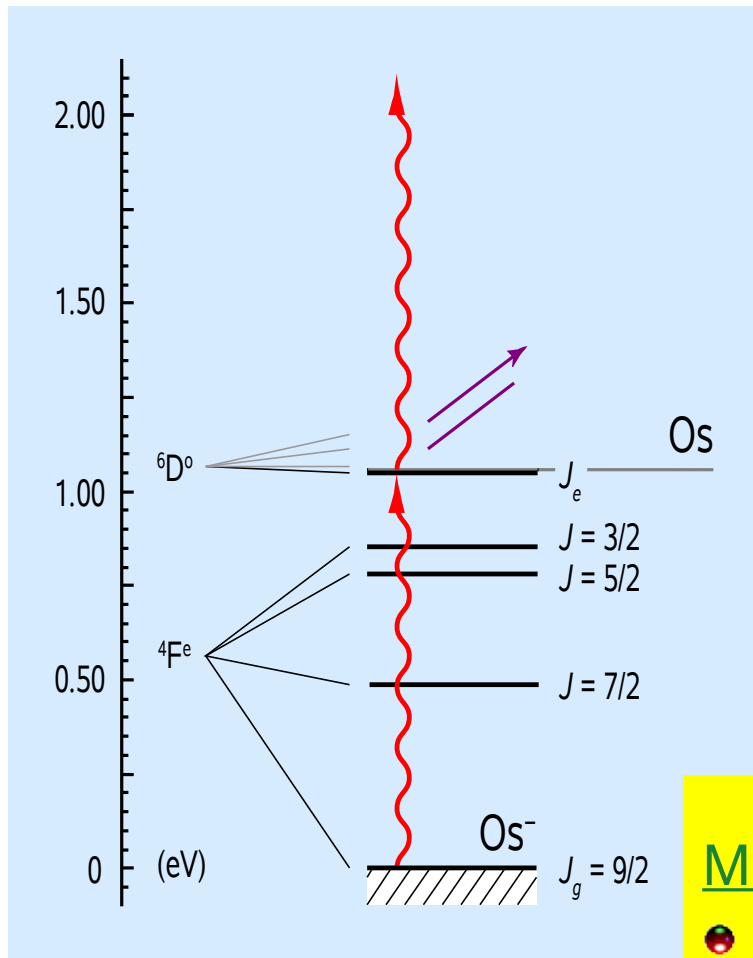


Processes during the collision:

- excitation into higher shells
- ionization (δ -electrons)
- MO radiation
- characteristic x-rays

Laser spectroscopy of Os-

@ MPI-K in Heidelberg (A. Kellerbauer *et al.*)



Measurement principle:

- Laser frequency is scanned around transition frequency
- Excited state is detached by electric field

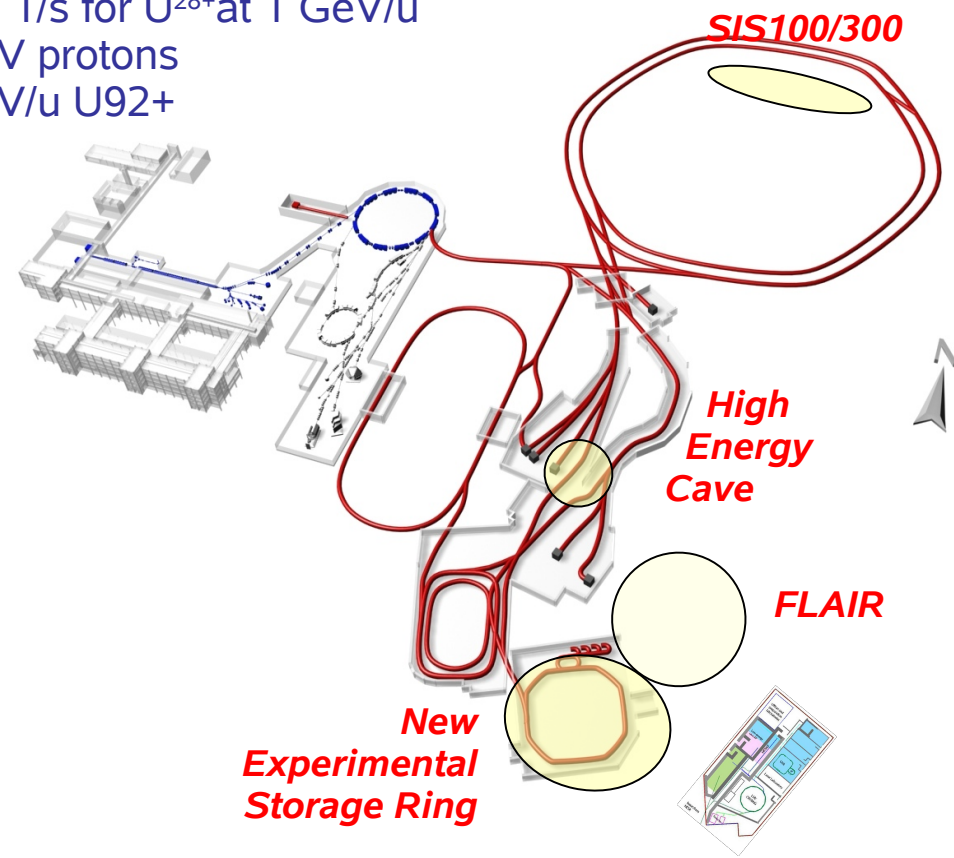
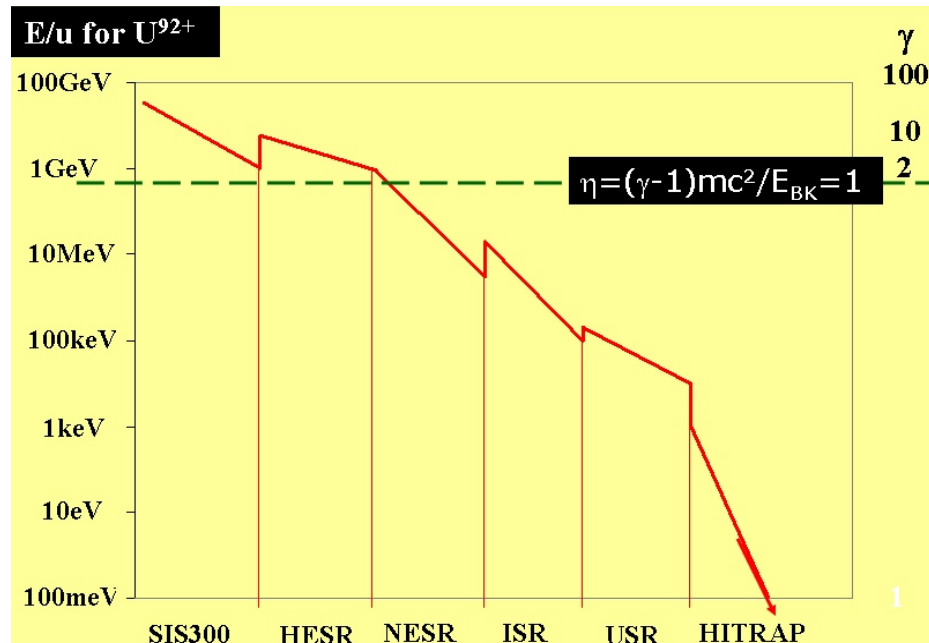
Neutrals detected on forward MCP

SPARC-Collaboration @ FAIR

1×10^{12} 1/s for U^{28+} at 1 GeV/u
 90 GeV protons
 34 GeV/u U^{92+}

Stored and Cooled

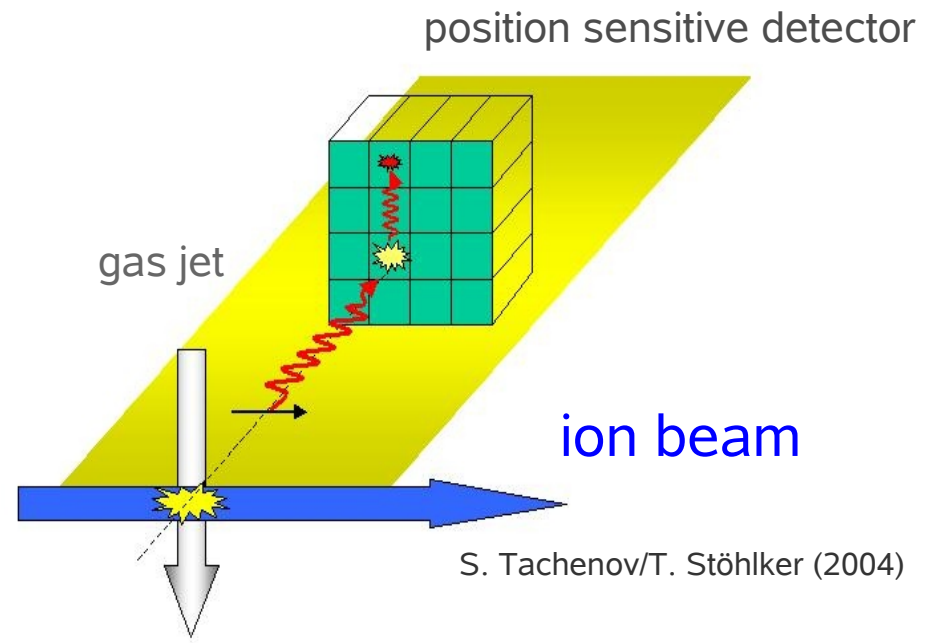
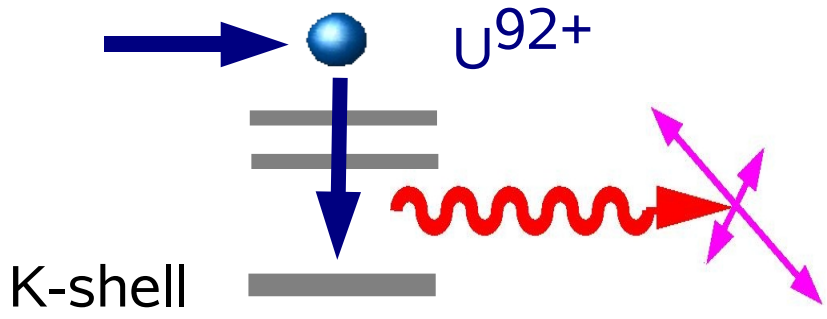
- Highly-Charged Ions and Exotic Nuclei
from Rest to Relativistic Energies
- Intense Beams of Radioactive Isotopes
- Virtual Photon Sources at X- and γ -Ray Energies
- XUV Energies via Lorentz Boost of optical wavelengths



... with Novel Instrumentation

- Ultracold Electron-Beam Target
- High Resolution X-Ray and Electron Spectrometers
- In-Ring Recoil Momentum Microscope
- Highly Intense Laser Beams
- Traps

Polarization of the K-shell REC photons



S. Tachenov/T. Stöhlker (2004)

● Compton effect: Klein-Nishina formula

$$\frac{d\sigma}{d\Omega} \propto \frac{\hbar\omega}{\hbar\omega'} + \frac{\hbar\omega'}{\hbar\omega} - 2 \sin^2 \theta \cos^2 \phi$$

polarization dependence

