

Nuclear systems with strangeness.

From hypernuclei to kaonic nuclei

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- Hypernuclei = nuclear systems containing nucleons + 1 or more hyperons. (M.Danzysz, J. Pniewski, Bull. Pol. Acad.Sci. 1 (1953) 42.)

BARYONS						
	Non-Strange		Hyperons			
Particle	N	Δ	Λ	Σ	Ξ	Ω
Mass	940	1232	1116	1190	1315	1672
Spin	1/2	3/2	1/2	1/2	1/2	1/2
Isospin	1/2	3/2	0	1	1/2	0
Strangeness	0	0	-1	-1	-2	-3
Quarks	uud udd	uuu uud udd ddd	uds	uus uds dds	uss dss	sss

Particle	Lifetime	Width	Decay
p	$> 10^{31}$ years	≈ 0	—
n	896 s	$7.2 \times 10^{-19} eV$	—
Δ	$5.5 \times 10^{-24} s$	120 MeV	πN
Λ	$2.6 \times 10^{-10} s$	$2.5 \mu eV$	πN
Σ^{\pm}	$0.8 \times 10^{-10} s$	$8.2 \mu eV$	πN
Σ^0	$7.4 \times 10^{-20} s$	8.9 KeV	$\gamma \Lambda$
Ξ	$1.6 \times 10^{-10} s$	$4.1 \mu eV$	$k \Lambda$
Ω	$0.8 \times 10^{-10} s$	$8.2 \mu eV$	$k \Lambda, \pi \Xi$

Why to study hypernuclei?

- Test models of baryon-baryon and meson-baryon interactions (meson exchange models, quark models, chiral models, ...)
- Test nuclear models (RMF, EDF, RPA ...)
- Test models of hadrons (SU(3) symmetry, quark models ...)
- Hypernuclear production – test reaction mechanisms
- Hypernuclear decays → study of weak interaction

Hyperon X Nucleon → no Pauli blocking →

Hyperon can penetrate deep into the nuclear interior, probe the nuclear interior, test the nuclear response

Implications for astrophysics (compact stars), HI collisions (strangeness production, medium modification of hadrons)

Λ hypernuclei

- > 30 Λ -hypernuclei:

World of matter made of u, d and s quarks

$N_u \sim N_d \sim N_s$



“Stable”

$p, n, \Lambda, \Xi^0, \Xi^-$

Higher density



Tamura

Strangeness in neutron stars ($\rho > 3 - 4 \rho_0$)

Strange hadronic matter ($A \rightarrow \infty$)

Strangeness

$\Lambda\Lambda, \Xi$ Hypernuclei

Λ, Σ Hypernuclei

N

0

-1

-2

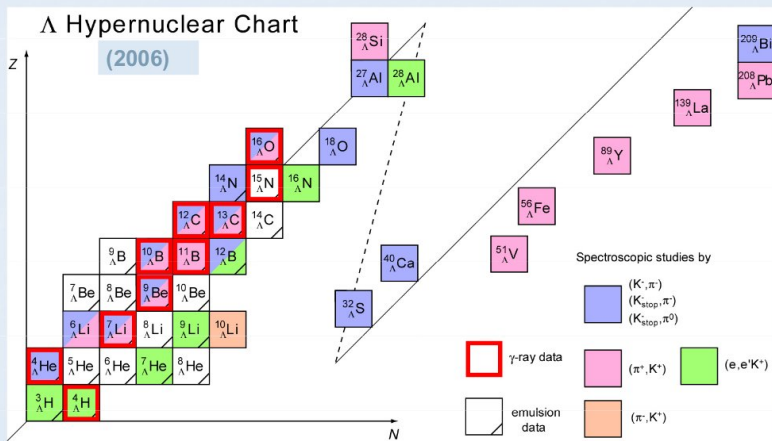
Z

Higher density

Λ hypernuclei

- > 30 Λ -hypernuclei:

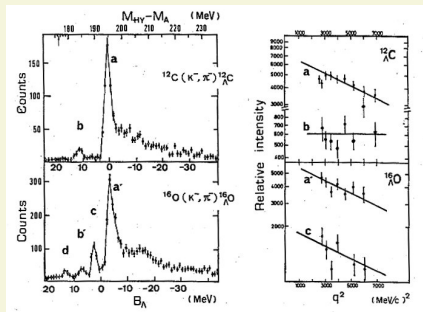
Chart of Λ Hypernuclei



Updated from: O. Hashimoto and H. Tamura, Prog. Part. Nucl. Phys. 57 (2006) 564.

Λ hypernuclei

- (K^-, π^-) reaction (emulsions, CERN, BNL, KEK, Frascati, JParc):



$$a = a' = (p_{3/2}^{-1}, p_{3/2}^\Lambda)_{J=0^+} \quad B_\Lambda(a) = 0 \text{ MeV}, B_\Lambda(a') = -3.5 \text{ MeV}$$

$$b = b' = (p_{3/2}^{-1}, s_{1/2}^\Lambda)_{J=1^-} \quad B_\Lambda(b) = 11 \text{ MeV}, B_\Lambda(b') = 7 \text{ MeV}$$

$$c = (p_{1/2}^{-1}, p_{1/2}^\Lambda)_{J=0^+} \quad B_\Lambda(c) = 2.5 \text{ MeV}$$

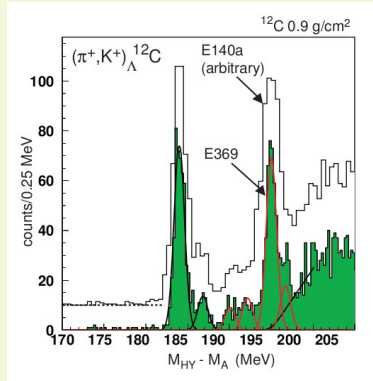
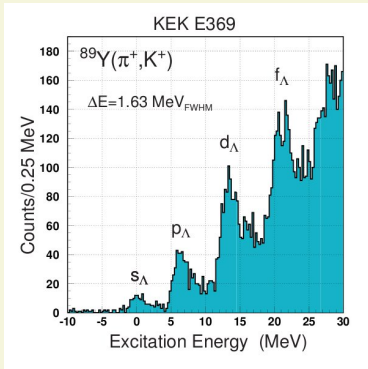
$$d = (p_{1/2}^{-1}, s_{1/2}^\Lambda)_{J=1^-} \quad B_\Lambda(d) = 13 \text{ MeV}$$

$$B_\Lambda(b') - B_\Lambda(d) = 6 \text{ MeV (n SO splitting)}, B_\Lambda(a') - B_\Lambda(c) = 6 \text{ MeV (n + } \Lambda \text{ SO splitting)}$$

$$\Rightarrow \Delta(p_{1/2}^\Lambda - p_{3/2}^\Lambda) \leq 0.3 \text{ MeV}$$

Λ hypernuclei

- (π^+, K^+) reaction (BNL, KEK):



Hotchi et al, PRC 64 (2001) 044302

- Textbook example of single-particle structure
- Λ hyperon bound by $\sim 28 \text{ MeV}$ in nuclear matter
- Negligible spin-orbit splitting

Λ hypernuclei

- RMF calculations (J.M., B.K. Jennings, PRC (1994):

(+ quark model + $Y\omega$ tensor coupling $\frac{f_{\omega Y}}{2M_Y} \bar{\Psi} \gamma \sigma^{\mu\nu} \partial_\nu V_\mu \Psi_Y$)

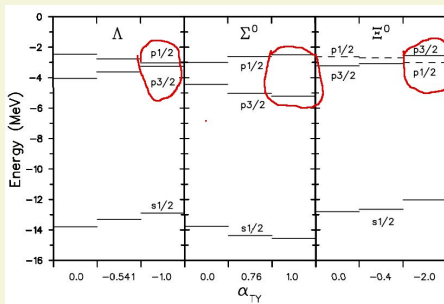
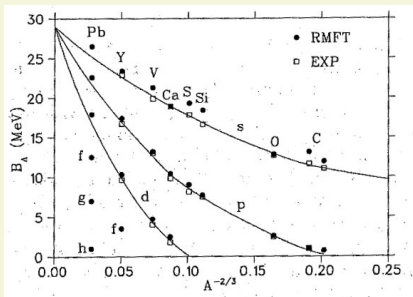
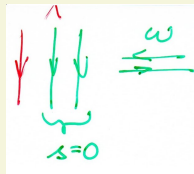
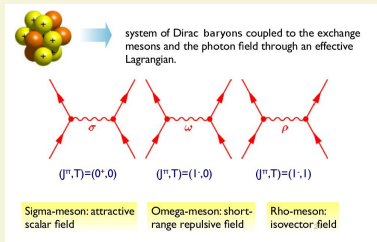


Table 2

Binding energies (in MeV) of single- Λ levels in $^{13}_{\Lambda}\text{C}$, $^{16}_{\Lambda}\text{O}$, $^{40}_{\Lambda}\text{Ca}$ and $^{89}_{\Lambda}\text{Y}$. Experimental energies [1] are shown in comparison with the results of the present calculations, using the input parameters of Table 1 and $\zeta = 0.5$ (column FKVW). Also listed are results of five different models: Quark Meson Coupling (QMC) [12,13], Fermi Hypernetted Chain (FHNC) [18], Skyrme (SK) [16], Brueckner–Hartree–Fock (BHF) [19] with the Nijmegen SC97F potential [50], and RMF models with a tensor coupling [11] (RMFI with $f_{\omega}^{\Lambda}/g_{\omega}^{\Lambda} = -1$) and density-dependent couplings [14] (RMFII).

Nucleus	$\epsilon_{s.p.}$	Expt.	FKVW	QMC	FHNC	SK	BHF	RMFI	RMFII
$^{13}_{\Lambda}\text{C}$	$1s_{1/2}$	11.38 ± 0.05	12.3	–	8.3	11.7	13.7	12.5	11.7
	$1p_{3/2}$	0.38 ± 0.1	0.1	–	–	0.9	1.4	1.1	1.1
	$1p_{1/2}$		0.0					0.8	0.0
$^{16}_{\Lambda}\text{O}$	$1s_{1/2}$	12.42 ± 0.05	12.6	16.2	12.00	13.3	15.5	12.9	12.8
	$1p_{3/2}$	1.85 ± 0.06	2.0	6.4	1.8	3.0	3.7	3.3	2.8
	$1p_{1/2}$		1.9	6.4				3.0	1.4
$^{40}_{\Lambda}\text{Ca}$	$1s_{1/2}$	20.0 ± 1.0	18.9	20.6	20.0	18.0	20.7	19.0	17.6
	$1p_{3/2}$	12.0 ± 1.0	10.1	13.9	10.6	10.1	11.5	10.7	9.1
	$1p_{1/2}$		10.1	13.9				10.5	7.8
	$1d_{5/2}$	1.0 ± 1.0	1.6	5.5	1.6	1.6	2.0	2.7	1.5
	$1d_{3/2}$		0.9	5.5				2.4	1.5
$^{89}_{\Lambda}\text{Y}$	$1s_{1/2}$	23.1 ± 0.5	23.4	24.0	23.3	21.1	24.1	23.7	23.2
	$1p_{3/2}$	16.5 ± 4.1	17.2	19.4	16.9	15.6	17.8	17.6	17.2
	$1p_{1/2}$		17.2	19.4				17.4	16.3
	$1d_{5/2}$	9.1 ± 1.3	10.2	13.4	10.1	9.1	10.4	10.7	10.3
	$1d_{3/2}$		9.8	13.4				10.5	8.9
	$1f_{7/2}$	2.3 ± 1.2	2.8	6.5	–	2.1	2.4	3.7	3.1
	$1f_{5/2}$		2.0	6.4				3.4	1.0

Λ hypernuclei

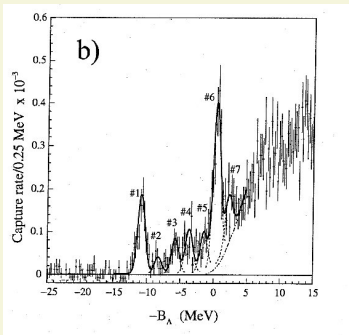
Table 4

P -shell spin-orbit splittings $\Delta \equiv \Delta\epsilon^\Lambda(p)$ for six hypernuclei (${}^{13}_\Lambda\text{C}$, ${}^{16}_\Lambda\text{O}$, ${}^{40}_\Lambda\text{Ca}$, ${}^{89}_\Lambda\text{Y}$, ${}^{139}_\Lambda\text{La}$, ${}^{208}_\Lambda\text{Pb}$). Experimental values [44], or empirical estimates [1,47,48], are shown in comparison with our theoretical predictions (FKVW), using a broad range of ζ parameters (see Eq. (12)), and other relativistic calculations with (RMFI [11]) or without (RMFII [14]) tensor coupling. All energies are given in keV. The asterisk means that a local fit has been necessary.

Nucleus	Exp. Δ [keV]	FKVW ($0.4 \leq \zeta \leq 0.66$)	RMFI [11]	RMFII [14]
${}^{13}_\Lambda\text{C}$	$152 \pm 54 \pm 36$ [44]	$-160 \leq \Delta \leq 510$	310	$\sim 1100^*$
${}^{16}_\Lambda\text{O}$	$300 \leq \Delta \leq 600$ [47] $-800 \leq \Delta \leq 200$ [1]	$-210 \leq \Delta \leq 490$	270	~ 1400
${}^{40}_\Lambda\text{Ca}$	-	$-140 \leq \Delta \leq 420$	210	~ 1400
${}^{89}_\Lambda\text{Y}$	90 [48]	$-40 \leq \Delta \leq 180$	110	~ 700
${}^{139}_\Lambda\text{La}$	-	$-20 \leq \Delta \leq 80$	50	~ 300
${}^{208}_\Lambda\text{Pb}$	-	$-20 \leq \Delta \leq 70$	50	~ 300

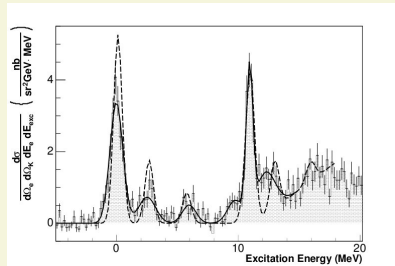
Λ hypernuclei

- $(K_{\text{stop}}^-, \pi^-)$ reaction
([FINUDA](#), PLB 622 (2005) 35):



Λ binding energy spectrum in ^{12}C

- $(e, e'K)$ reaction
([JLab](#), PRL 99 (2007) 052501):

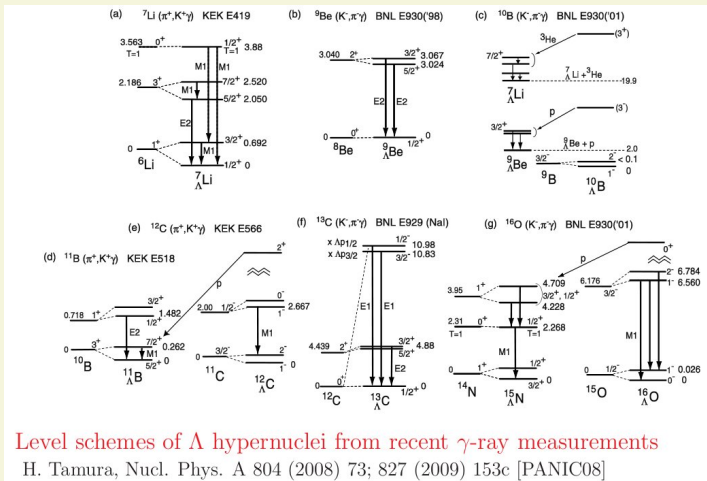


^{12}B excitation spectrum

Λ hypernuclei

- γ spectroscopy (BNL, KEK)

\Rightarrow spin dependence of the effective ΛN interaction in the nuclear p shell

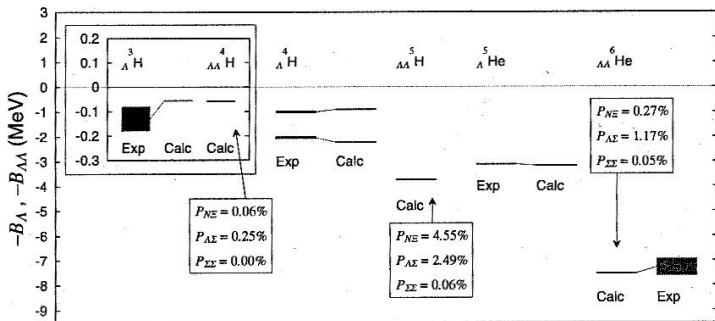


$$V_{\Lambda N} = V_0(r) + V_\sigma(r) s_N \cdot s_\Lambda + V_{LS}(r) l_{NA} \cdot (s_\Lambda + s_N) + V_{ALS}(r) l_{NA} \cdot (s_\Lambda - s_N) + V_T(r) S_{12}$$

D.J. Millener, Nucl. Phys. A 804 (2008) 84

Λ hypernuclei

- s-shell Λ hypernuclei



Nemura et al, PRL 89 (2002) 142504 (including $\Lambda N \rightarrow \Sigma N$ and $\Lambda\Lambda \rightarrow \Xi N$ mixings)
variational approach

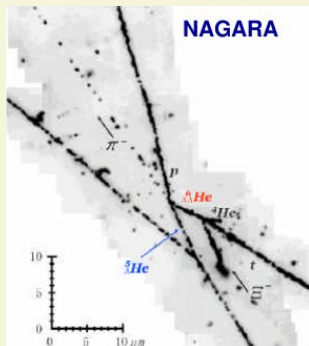
Hiyama et al, PRC 65 (2002) 011301(R) - Jacobi-coordinate Gaussian basis

Nogga et al, PRL 88 (2002) 172501 - Faddeev + Faddeev-Yakubovsky

$\Lambda\Lambda$ hypernuclei

$$B_{\Lambda\Lambda}(^A_{\Lambda\Lambda}Z) = B_{\Lambda}(^A_{\Lambda\Lambda}Z) + B_{\Lambda}(^A_{\Lambda}Z)$$
$$\Delta B_{\Lambda\Lambda}(^A_{\Lambda\Lambda}Z) = B_{\Lambda}(^A_{\Lambda\Lambda}Z) - B_{\Lambda}(^A_{\Lambda}Z)$$

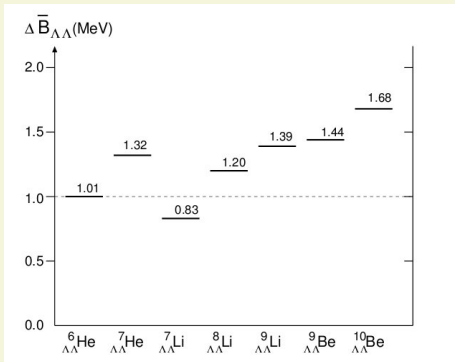
$^6_{\Lambda\Lambda}\text{He}$ (Prowse 66), $^{10}_{\Lambda\Lambda}\text{Be}$ (Danysz 63), $^{13}_{\Lambda\Lambda}\text{B}$ (KEK-E176 91) $\rightarrow \Delta B_{\Lambda\Lambda} \sim 4.3 - 4.8$ MeV



Takahashi et al, PRL 87 (2001) 212502

$$\Delta B_{\Lambda\Lambda}(^6_{\Lambda\Lambda}\text{He}) = B_{\Lambda\Lambda}(^6_{\Lambda\Lambda}\text{He}) - 2B_{\Lambda}(^5_{\Lambda}\text{He}) \approx 1 \text{ MeV}$$

$\Lambda\Lambda$ hypernuclei

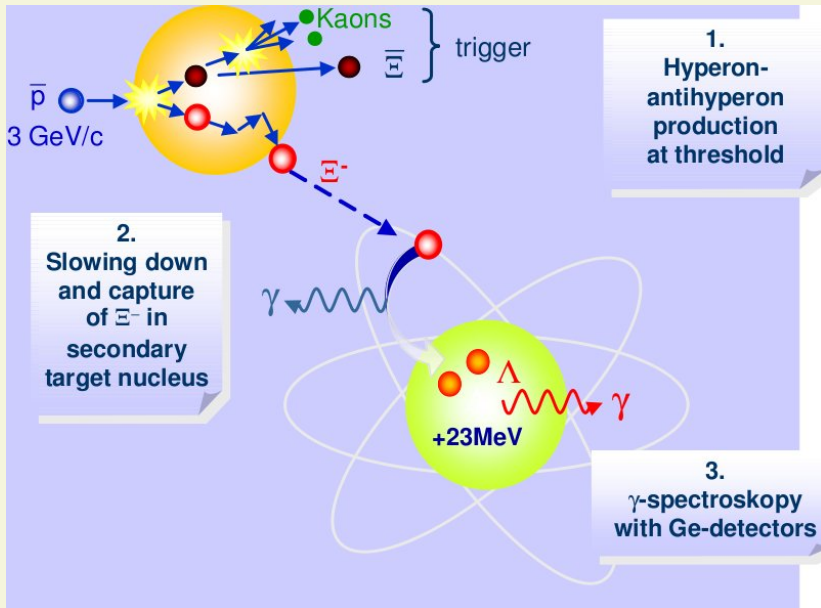


Hiyama, Kamimura, Motoba, Yamada, Yamamoto, NPA 754 (2005) 103c,

3- and 4-body cluster model calculations

Need to measure beyond ${}^6_{\Lambda\Lambda}\text{He} \rightarrow$ **PANDA**

$\Lambda\Lambda$ hypernuclei

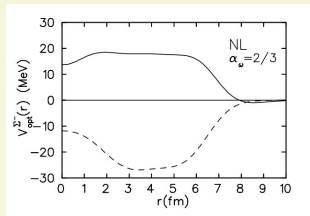
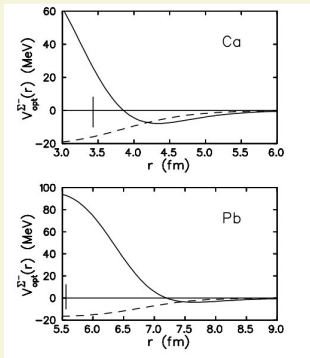


- Ξ^- conversion in 2 Λ : $\Xi^- + p \rightarrow \Lambda + \Lambda + 28.5 \text{ MeV}$
- $p(K^-, K^+)\Xi^-$
 - KEK - E176: 10^2 stopped Ξ per week
 - KEK - E373: 10^3 stopped Ξ per week
 - AGS - E885: 10^4 stopped Ξ per week
- $p + \bar{p} \rightarrow \Xi^- + \bar{\Xi}^+$
 - antiproton storage ring HESR: few times 10^5 stopped Ξ per day !
 - $\Rightarrow \gamma$ -spectroscopy feasible

- Σ -nucleus interaction:

(J.M., Friedman, Gal, Jennings, NPA 594 (1995) 311,

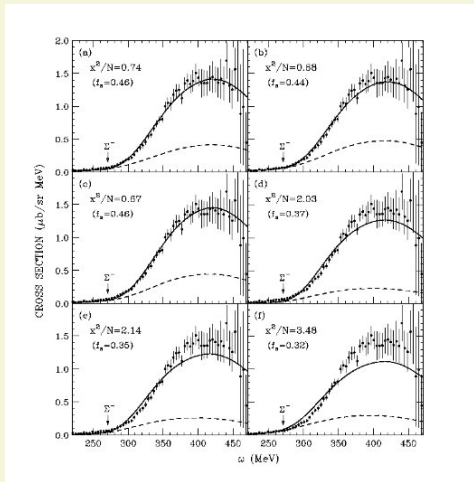
E. Friedman, A. Gal, Phys. Rept. 452 (2007) 89)



- Σ hyperons are not bound in nuclei except for ${}^4_{\Sigma}\text{He}$

- Sawafuta et al, PRL 83 (1999) 25; Noumi et al, PRL 89 (2002) 072301

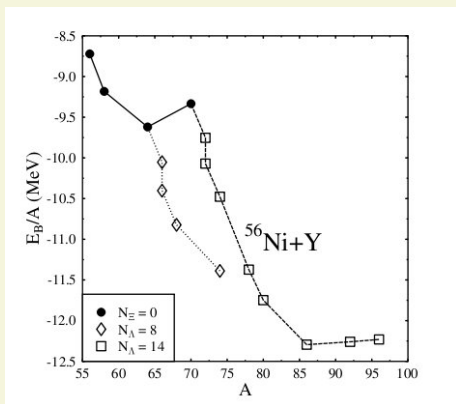
- DWIA calculations (Harada & Hirabayashi, NPA 759 (2005) 143)



$^{28}\text{Si}(\pi^-, K^+)$ spectrum from KEK-E438, using 6 Σ -nucleus potentials,
(a)-(c) with inner repulsion, (d)-(f) fully attractive

- Ξ -nucleus interaction:
- no established yet QBS
- $^{12}\text{C}(K^-, K^+)$ spectra (KEK -E224, BNL-E885) $\rightarrow V_{\Xi} \approx 14 \text{ MeV}$
- Calculations of light Ξ hypernuclei (Hiyama et al, PRC 78 (2008) 054316).
- Spectroscopic study of Ξ hypernucleus $^{12}_{\Xi}\text{B}$... (T. Nagae),
A 'Day-1' experiment E05 at J-Parc

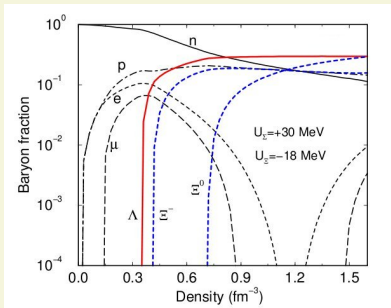
Multi-strange baryonic systems



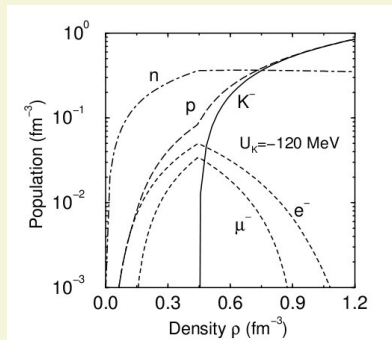
J. Schaffner, C.B. Dover, A. Gal, C. Greiner, H. Stöcker, PRL 71 (1993) 1328.

$\Xi N \rightarrow \Lambda \Lambda$ (≈ 25 MeV in free space) is Pauli blocked

- neutron star structure



Schaffner-Bielich, NPA 804 (2008) 309



Glendenning, Schaffner-Bielich,
PRC 60 (1999) 025803

- kaon condensation could occur at $\rho \gtrsim 3\rho_0$, $l^- \rightarrow K^- + \nu_l$ ($\omega_{K^-} \leq 200$ MeV)

- $\bar{K}N$ interaction

strongly attractive $\Leftarrow \exists \Lambda(1405)$ 27 MeV below K^-p threshold

- \bar{K} -nucleus interaction

strongly attractive and absorptive \Leftarrow kaonic atom level shifts and widths

? optical potential depth:

$\text{Re}V_{opt} \simeq (150-200)$ MeV \Leftarrow phenomenological models

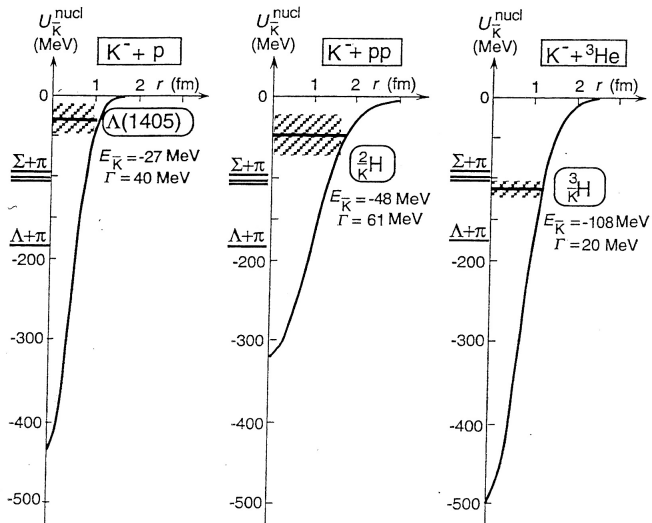
$\text{Re}V_{opt} \simeq (50-60)$ MeV \Leftarrow chiral models

$\Rightarrow \exists$ of \bar{K} -nuclear states

? sufficiently narrow to allow identification by experiment

Kaonic nuclei

T. Yamazaki, Y. Akaishi / *Physics Letters B* 535 (2002) 70–76



- K^- capture in Li and ^{12}C (FINUDA, PRL (2005)): $B = 115 \pm 6 \pm 4$ MeV, $\Gamma = 67 \pm 14 \pm 3$ MeV

vs.

- $K^- pN \rightarrow \Lambda N + FSI$ (Magas *et al.*, PRC (2006))

vs.

- K^- stopped in $^6\text{Li} \rightarrow K^- ppn$ cluster, $B = 58 \pm 6$ MeV, $\Gamma \simeq 30$ MeV
(FINUDA, PLB (2007) vs. Magas *et al.*, arXiv:0801.4504)

?

- \bar{p} annihilation on ^4He (Obelix, LEAR) $\rightarrow K^- pp$: $B \simeq 160$ MeV, $\Gamma \simeq 24$ MeV
 $\rightarrow K^- ppn$: $B = 121 \pm 15$ MeV, $\Gamma < 60$ MeV

(Bendisoli *et al.*, NPA (2007))

- $pp \rightarrow K^+ \Lambda p$ (DISTO) $\rightarrow K^- pp$: $B = 105 \pm 118$ MeV
(T. Yamazaki *et al.* EXA08, arXiv: 0810.5182 [nucl-ex])

?

- Coupled-channel calculations of a $\bar{K}NN - \pi\Sigma N$ system (Shevchenko, Gal, JM, PRL 98 (2007) 082301.)
- 3-body Faddeev equations (in AGS form):

$$\begin{aligned}U_{11} &= \quad + T_2 G_0 U_{21} + T_3 G_0 U_{31} \\U_{21} &= G_0^{-1} + T_1 G_0 U_{11} + T_3 G_0 U_{31} \\U_{31} &= G_0^{-1} + T_1 G_0 U_{11} + T_2 G_0 U_{21},\end{aligned}$$

U_{ij} describe elastic and re-arrangement processes:

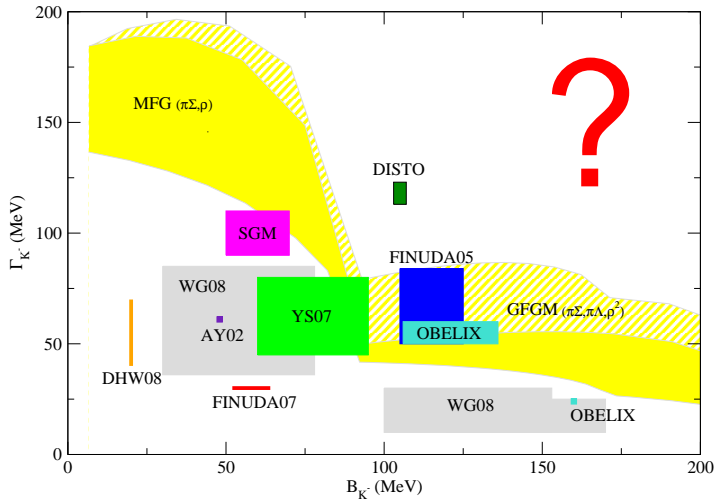
$$\begin{aligned}U_{11} &: 1 + (23) \rightarrow 1 + (23) \\U_{21} &: 1 + (23) \rightarrow 2 + (31) \\U_{31} &: 1 + (23) \rightarrow 3 + (12)\end{aligned}$$

- $\bar{K}N$ strongly coupled with $\pi\Sigma$ via $\Lambda(1405) \Rightarrow \pi\Sigma$ channel included

particle channels α :	1 : ($\bar{K}NN$)	2 : ($\pi\Sigma N$)	3 : ($\pi N\Sigma$)
$i = 1$	NN	ΣN	ΣN
$i = 2$	$\bar{K}N$	πN	$\pi\Sigma$
$i = 3$	$\bar{K}N$	$\pi\Sigma$	πN

Table: Calculated $K^- pp$ binding energies and widths (in MeV)

	single channel		coupled channel		
	AY	DHW	SGM	IS	WG
B	48	17-23	50-70	60 - 95	40-80
Γ	61	40-70	90-110	45-80	40-85



- Larger K^- -nuclear systems

Relativistic mean field model for a system of **nucleons**, **K mesons**, and **hyperons** interacting through the exchange of σ , σ^* , ω , ρ , ϕ and photon fields:

$$\mathcal{L} = \mathcal{L}_{RMF} + \mathcal{L}_K + \mathcal{L}_Y$$

where

\mathcal{L}_{RMF} = standard relativistic mean field lagrangian density

$$\mathcal{L}_K = (\mathcal{D}_\mu K)^\dagger (\mathcal{D}^\mu K) - m_K^2 K^\dagger K - g_{\sigma K} m_K \sigma K^\dagger K - g_{\sigma^* K} m_K \sigma^* K^\dagger K,$$

$$\mathcal{L}_Y = \bar{\psi}_Y [i\mathcal{D} - (m_Y - g_{\sigma Y} \sigma - g_{\sigma^* Y} \sigma^*)] \psi_Y,$$

with covariant derivative:

$$\mathcal{D}_\mu = \partial_\mu + i g_{\omega K} \omega_\mu + i g_{\rho K} \vec{I} \cdot \vec{\rho}_\mu + i g_{\phi K} \phi_\mu + i e (I_3 + \frac{1}{2} Y) A_\mu.$$

+ antikaons:

$$(-\nabla^2 - E_{K^-}^2 + m_K^2 + \Pi_{K^-})K^- = 0$$

$$\begin{aligned} \text{Re } \Pi_{K^-} = & -g_{\sigma^*K} m_K \sigma^* - g_{\sigma K} m_K \sigma - 2E_{K^-} (g_{\omega K} \omega + g_{\rho K} \rho + g_{\phi K} \phi + eA) \\ & - (g_{\omega K} \omega + g_{\rho K} \rho + g_{\phi K} \phi + eA)^2 \end{aligned}$$

$$\text{Im } \Pi_{K^-} = (0.7 f_{1\Sigma} + 0.1 f_{1\Lambda}) W_0 \rho_N(r) + 0.2 f_{2\Sigma} W_0 \rho_N^2(r) / \tilde{\rho}_0$$

f_{iY} kinematical suppression factors
(reduced phase space)

W_0 constrained by kaonic atom data

Absorption through:

- pionic conversion modes $\propto \rho_N(r)$

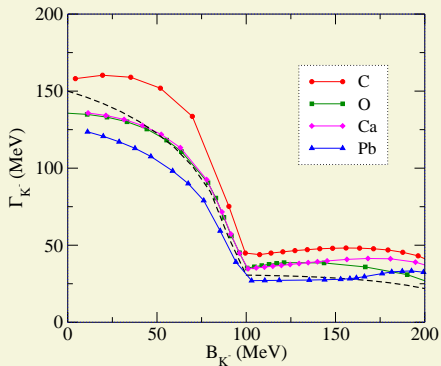
$$\bar{K}N \rightarrow \pi\Sigma + 90 \text{ MeV}, \pi\Lambda + 170 \text{ MeV} \quad (70\%, 10\%)$$

- nonmesonic modes $\propto \rho_N^2(r)$

$$\bar{K}NN \rightarrow YN + 240 \text{ MeV} \quad (20\%)$$

Γ_{K^-} width \Leftarrow phase space suppression \times density enhancement

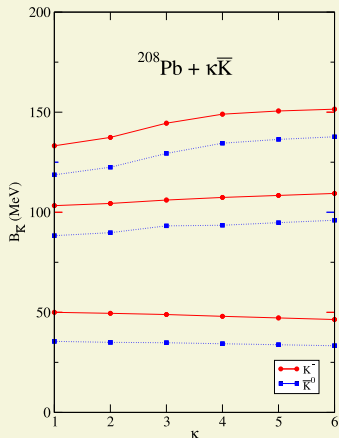
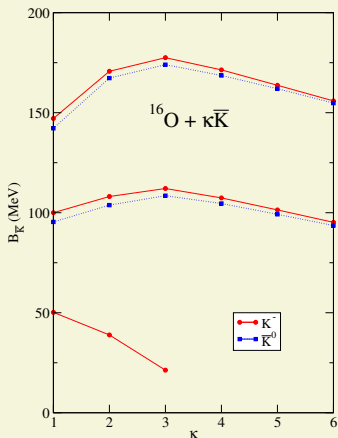
- Γ_{K^-} follows the dependence $\text{sf}(B_{K^-})$



The K^- decay widths Γ_{K^-} in $^{12}_{K^-}\text{C}$, $^{16}_{K^-}\text{O}$, $^{40}_{K^-}\text{Ca}$, and $^{208}_{K^-}\text{Pb}$ as function of the K^- binding energy B_{K^-} .

The dashed line indicates a static nuclear matter calculation.

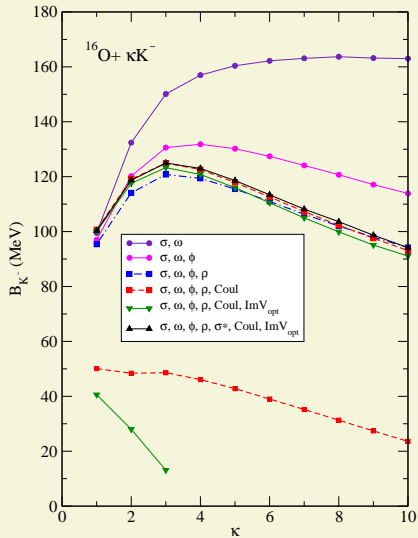
Multi- \bar{K} nuclei



The \bar{K} binding energies as functions of the number κ of antikaons.

- saturation observed **across the periodic table**
- $B_{\bar{K}} \ll m_K + m_N - m_\Lambda \gtrsim 320 \text{ MeV}$, far away from kaon condensation

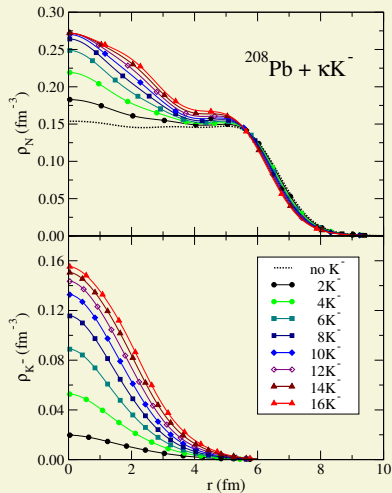
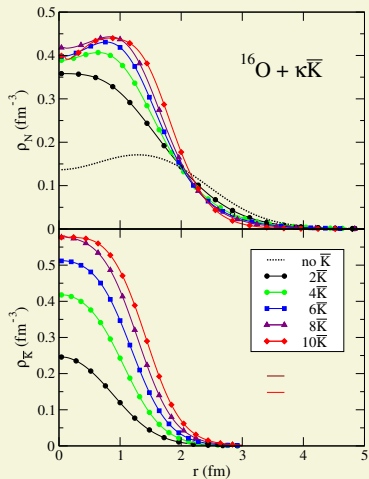
Multi- \bar{K} nuclei



The K^- binding energy as a function of the number κ of antikaons.

- saturation occurs for any boson-field composition (when ω -field present \Rightarrow repulsion)
- no saturation of $B_{\bar{K}}$ for a purely scalar interaction

Multi- \bar{K} nuclei



Nuclear (ρ_N) and \bar{K} ($\rho_{\bar{K}}$) density distributions for various numbers κ of antikaons.

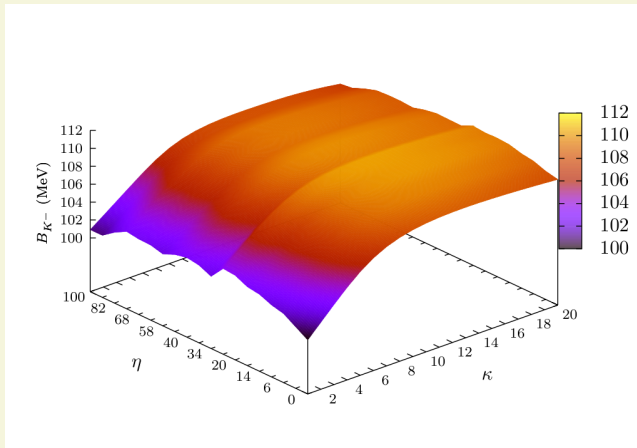
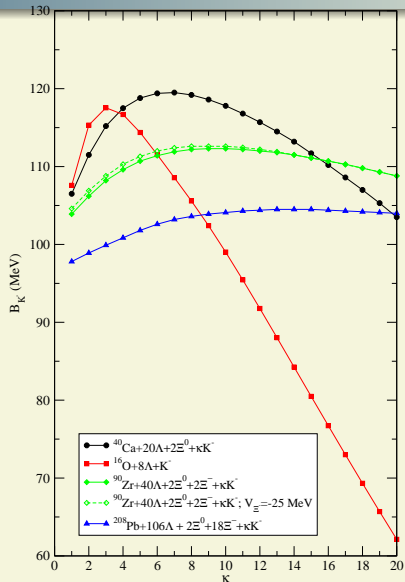


Fig. 17 The \bar{K} binding energy $B_{\bar{K}}$ in ^{208}Pb as a function of the number κ of antikaons and η of Λ hyperons.

Multi- \bar{K} hypernuclei



The \bar{K} binding energy $B_{\bar{K}}$ in $^AZ + \eta\Lambda + \mu_0\Xi^0 + \mu_-\Xi^- + \kappa K^-$ as a function of the number κ of antikaons.

- Λ hyperon bound by 28 MeV in nuclear matter, spin-orbit splitting $\rightarrow 0$
Few-body Λ (and $\Lambda\Lambda$) hypernuclei - $\Sigma N \rightarrow \Lambda N$ important
 p -shell hypernuclei - effective ΛN interaction determined
(exp. JLab, FINUDA, planned JParc, HypHI @ GSI (FAIR))
- more data on $\Lambda\Lambda$ hypernuclei needed \rightarrow PANDA
- Σ hyperons are not bound in nuclei except for ${}^4_{\Sigma}\text{He}$
- Ξ hyperons perhaps bound by ≈ 14 MeV in nuclear matter
(planned exp. JParc)
- \bar{K} nuclei \rightarrow the issue is far from being resolved
(searches for $K^- pp$ are underway in GSI and JParc)
- kaon condensation is unlikely to occur in strong-interaction self-bound strange hadronic matter