

Phases of Strongly Interacting Matter

- From **Quarks** to **Nuclei** and **Neutron Stars** -



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Technische Universität München



PHYSIK
DEPARTMENT



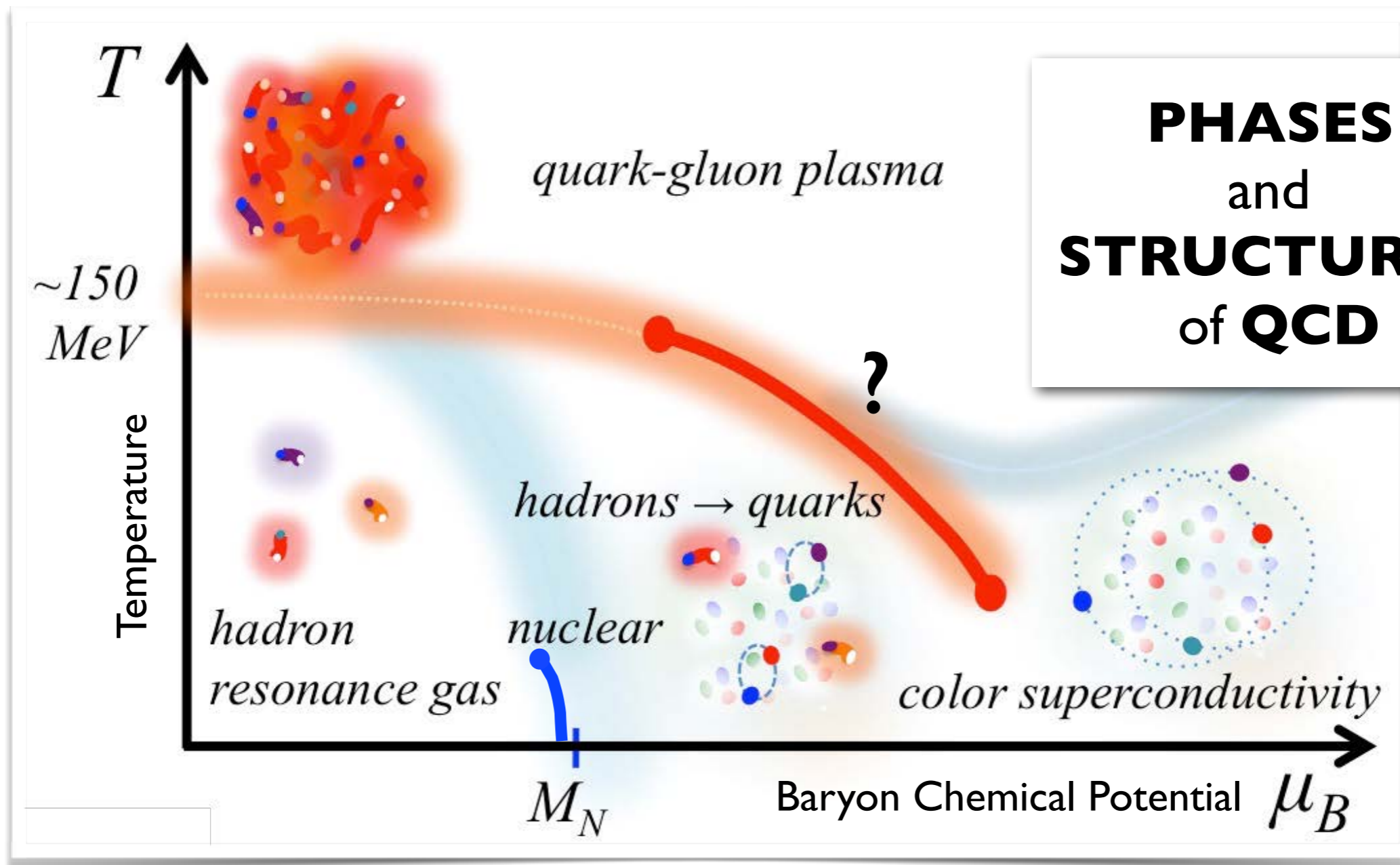
QCD symmetries and scales

- From massless quarks to massive nucleons
- Chiral symmetry and interface with nuclear physics



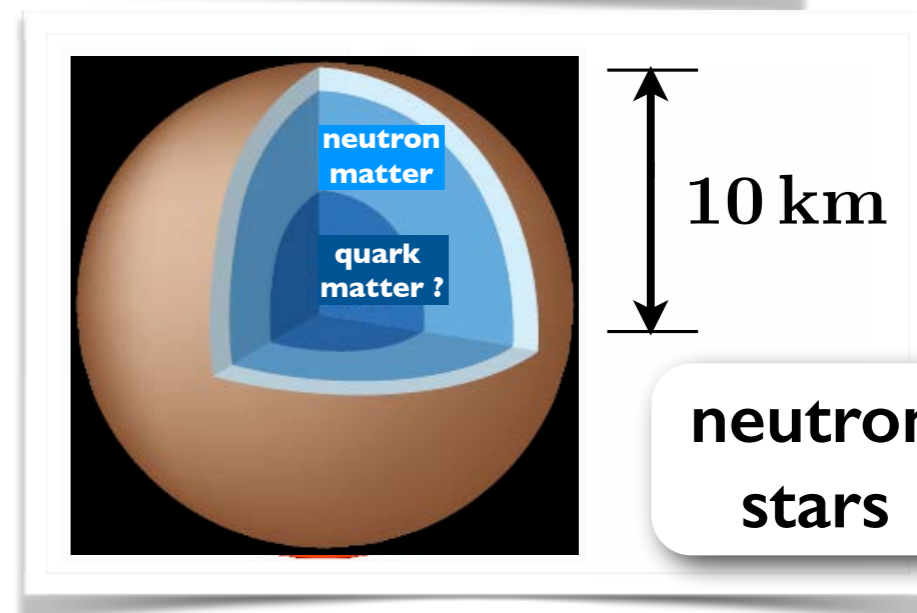
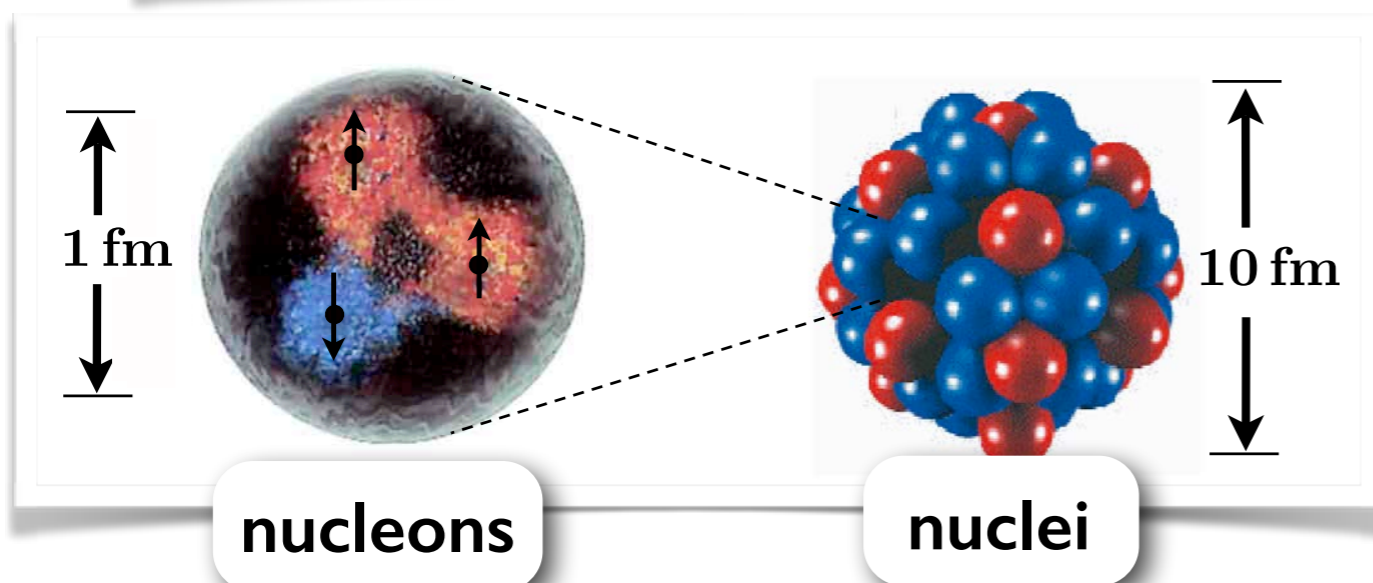
QCD phase diagram

- High temperature: confinement / deconfinement transition
- Moderate temperatures and densities: nuclear thermodynamics
- High baryon density: constraints from massive neutron stars



from:
G. Baym,
T. Hatsuda,
et al.

Rept. Prog. Phys.
81 (2018) 056902



1.

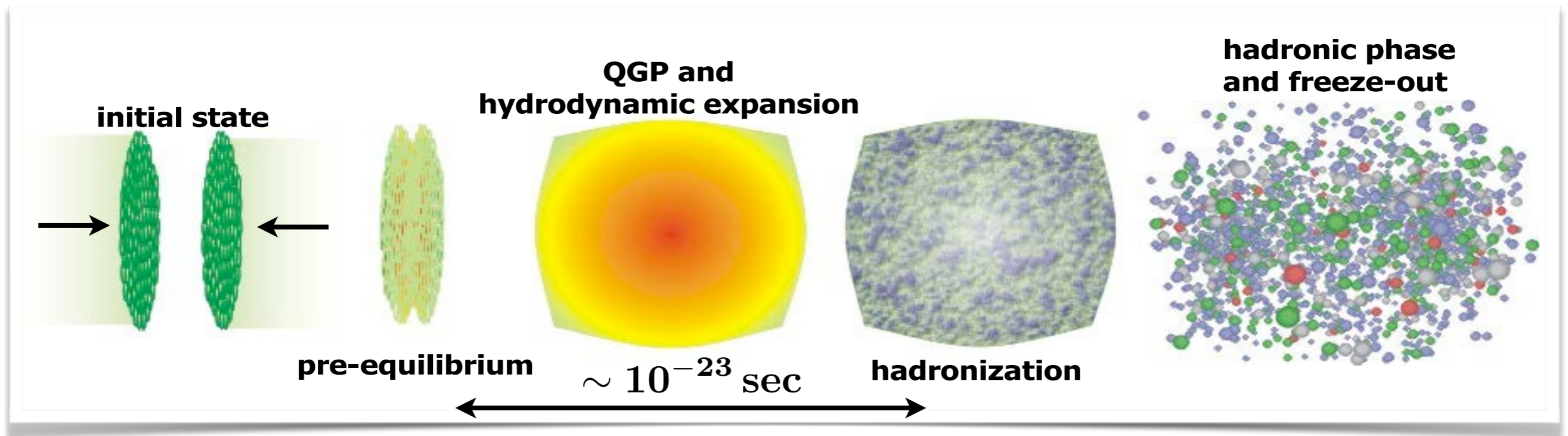
Preview :

*What do we know about the
PHASES of QCD ?*



Strategies PART I: **Heavy-Ion Physics**

- **High Energy Nuclear Collisions @ CERN/SPS, RHIC, LHC**

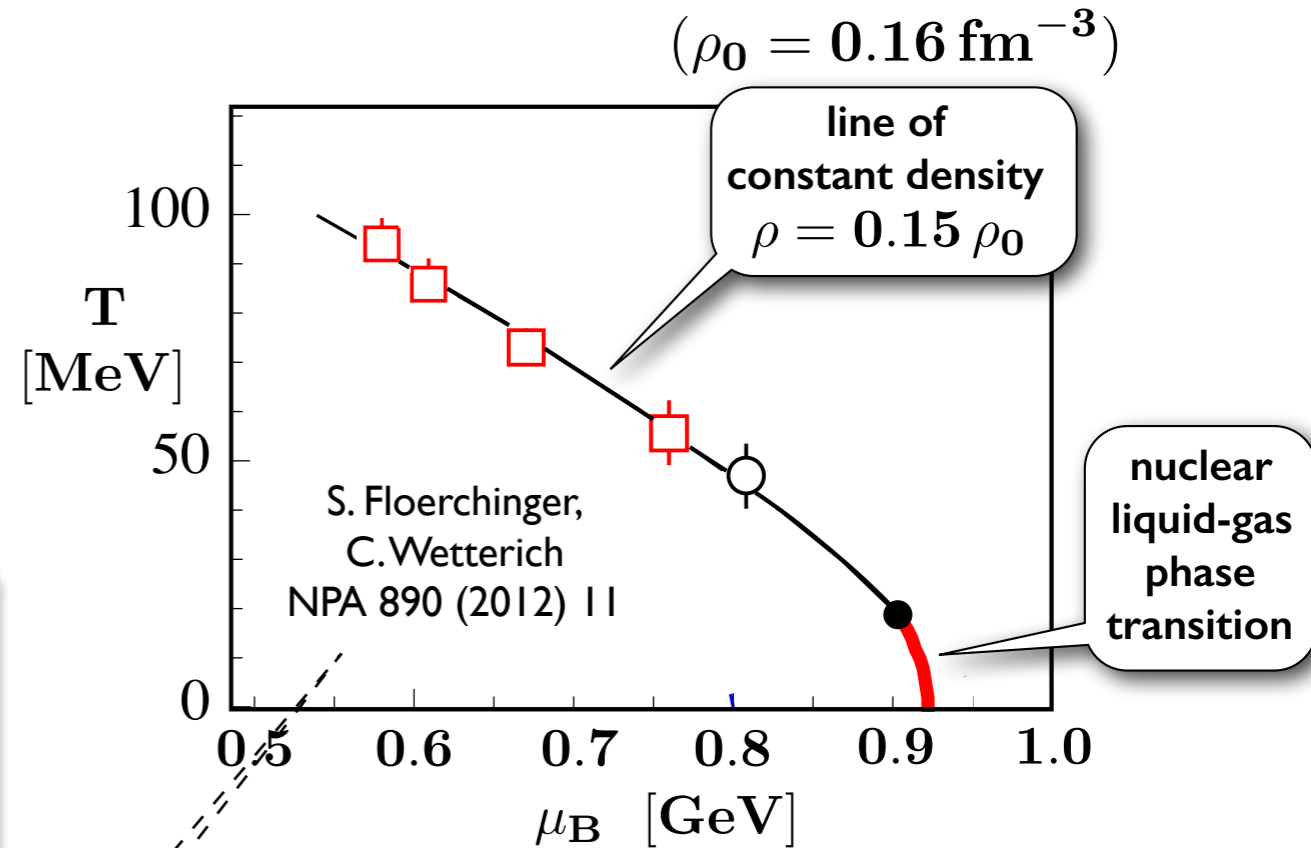
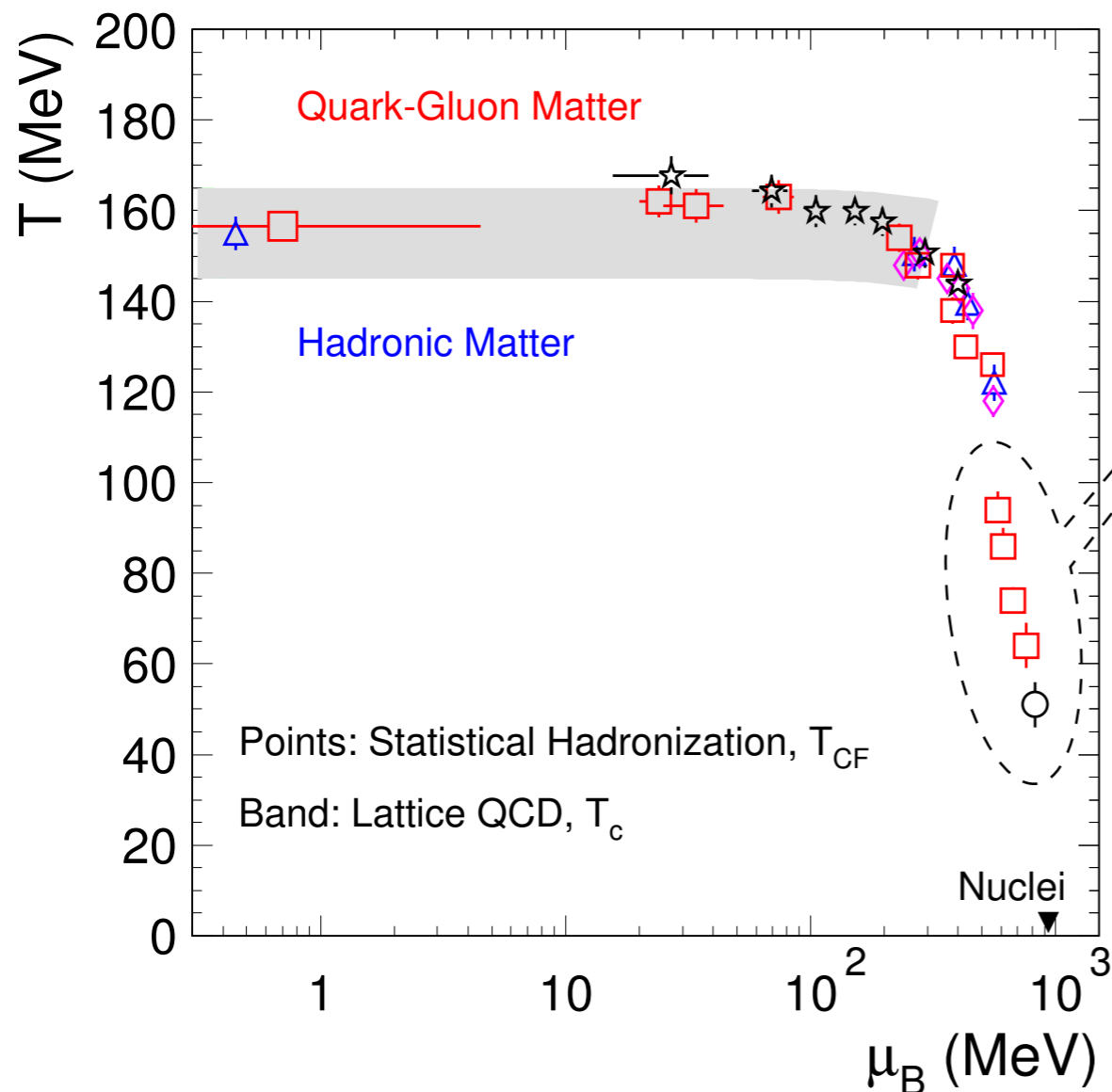


- **Analysis of RHIC and LHC data:**

- ▶ **Initial temperatures 300 - 500 MeV**
- ▶ **Fast equilibration**
- ▶ **Strongly correlated quark-gluon matter**

CHEMICAL FREEZE-OUT

A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel
Nature 561 (2018) 321



- **Freeze-out temperature**
 $T_{CF} = 156 \pm 2$ MeV
at $\mu_B \simeq 0$
- **Low-temperature freeze-out trajectory : NOT a first-order phase transition line**

Strategies PART II: **Lattice QCD**

$$\mathcal{L}_{\text{QCD}} = \bar{\psi} (i\gamma_{\mu} \mathcal{D}^{\mu} - \mathbf{m}) \psi - \frac{1}{4} \mathbf{G}_{\mu\nu} \mathbf{G}^{\mu\nu}$$

- Large-scale computer simulations on
EUCLIDEAN SPACE-TIME Lattices

- Euclidean time $\hat{=}$ inverse temperature

$$\tau = 1/T$$

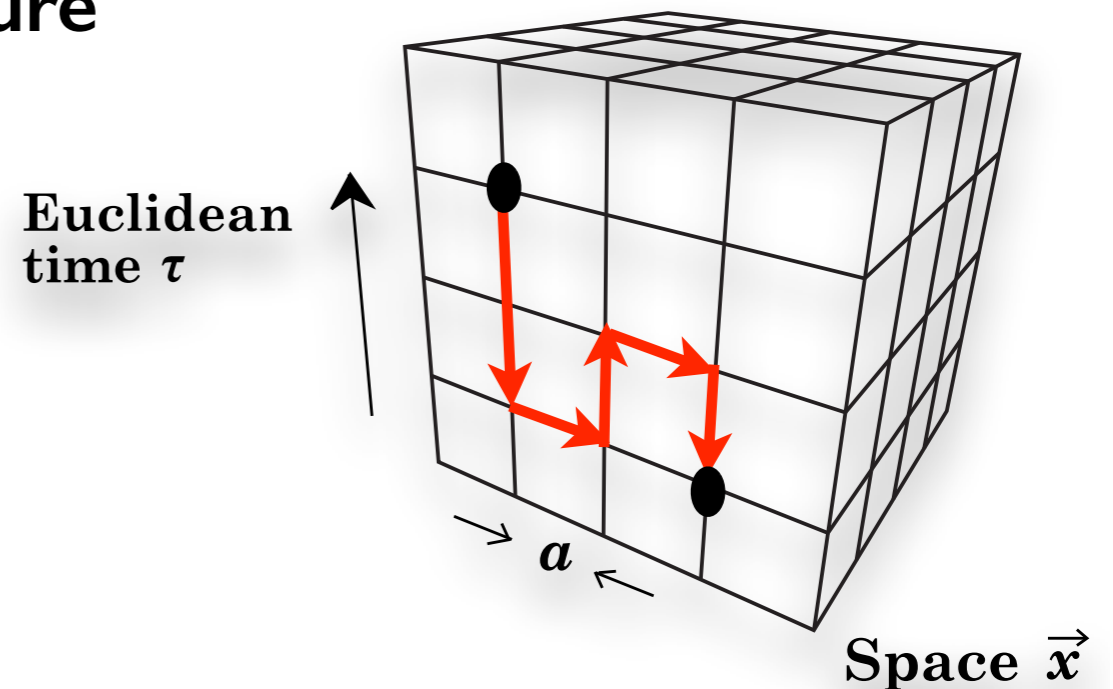
quarks on lattice sites

gluon fields on links

- **QCD THERMODYNAMICS**

Partition function

$$\mathcal{Z} = \int [d\mathcal{U} d\psi d\bar{\psi}] e^{-S_{\text{G}}(\mathcal{U}) - S_{\text{q}}(\psi, \bar{\psi}, \mathcal{U})}$$



- ▶ Non-perturbative “condensed matter physics” of QCD

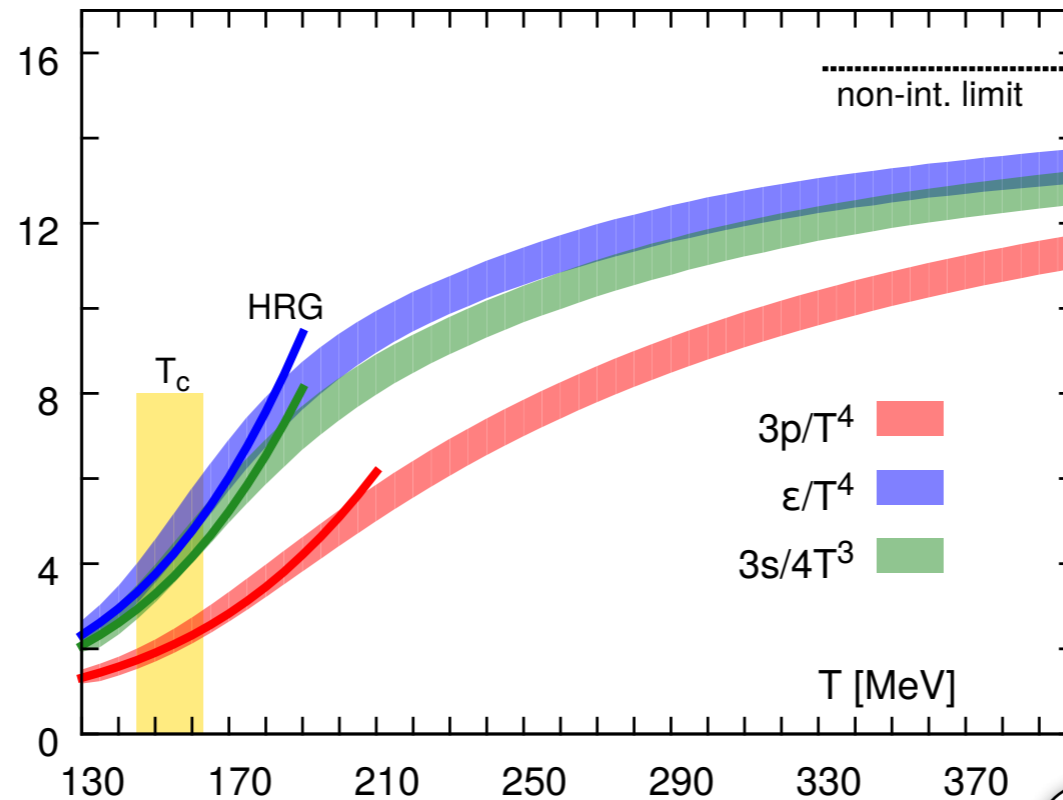


QCD THERMODYNAMICS on the LATTICE

baryon chemical potential
 $\mu_B = 0$

$$\mu_B = 0$$

crossover
 (not a phase transition)

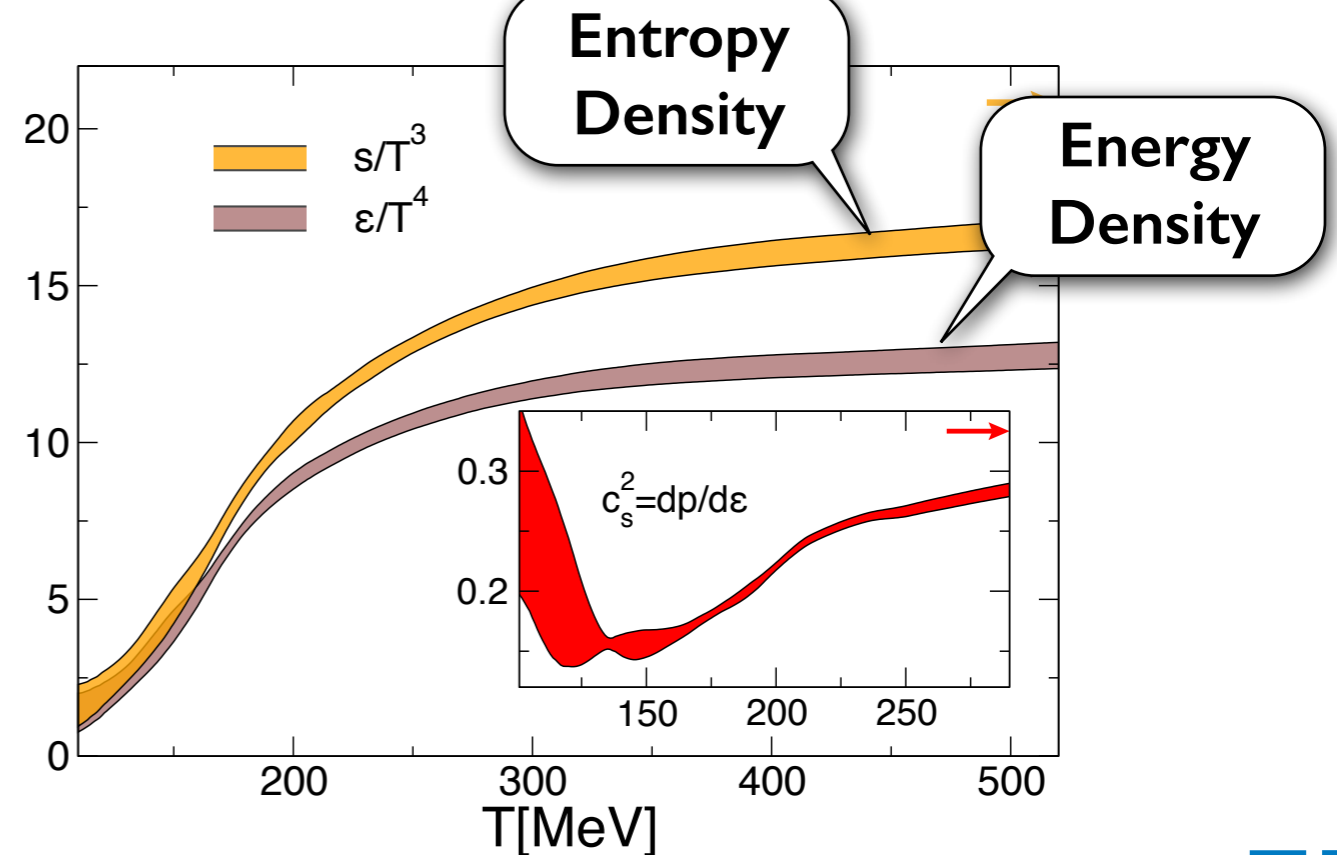
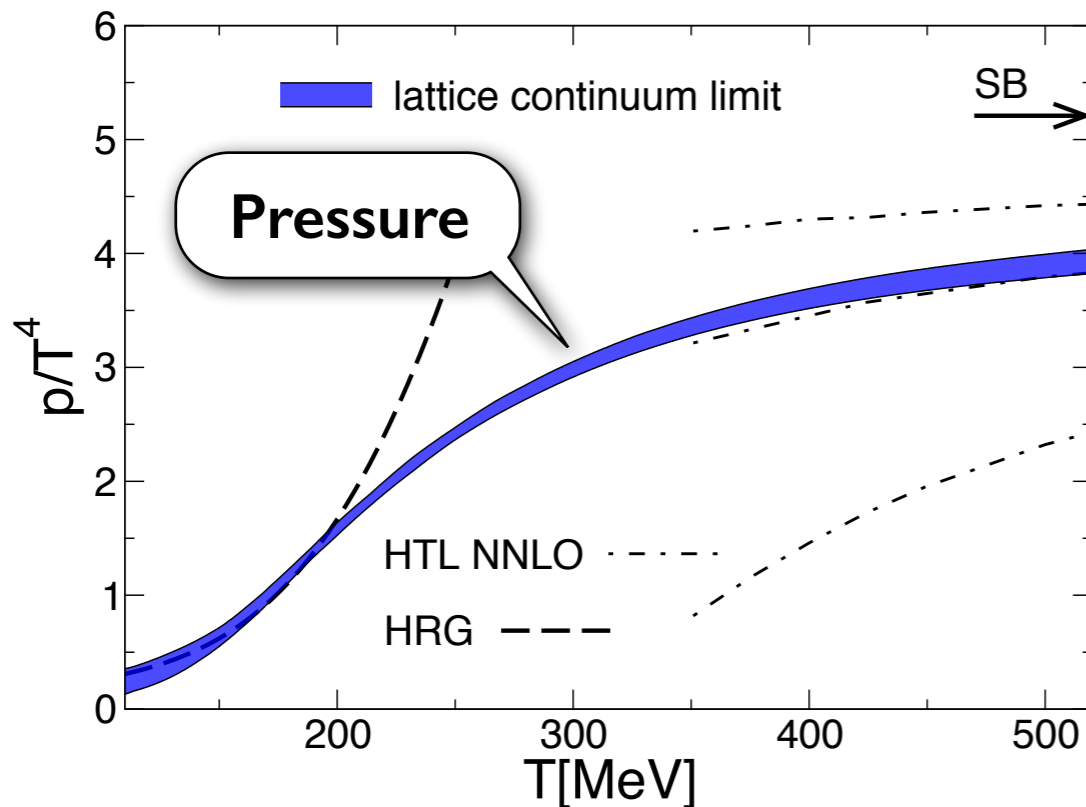


A. Bazavov et al. (HotQCD collab.)
 Phys. Rev. D90 (2014) 094503

transition temperature

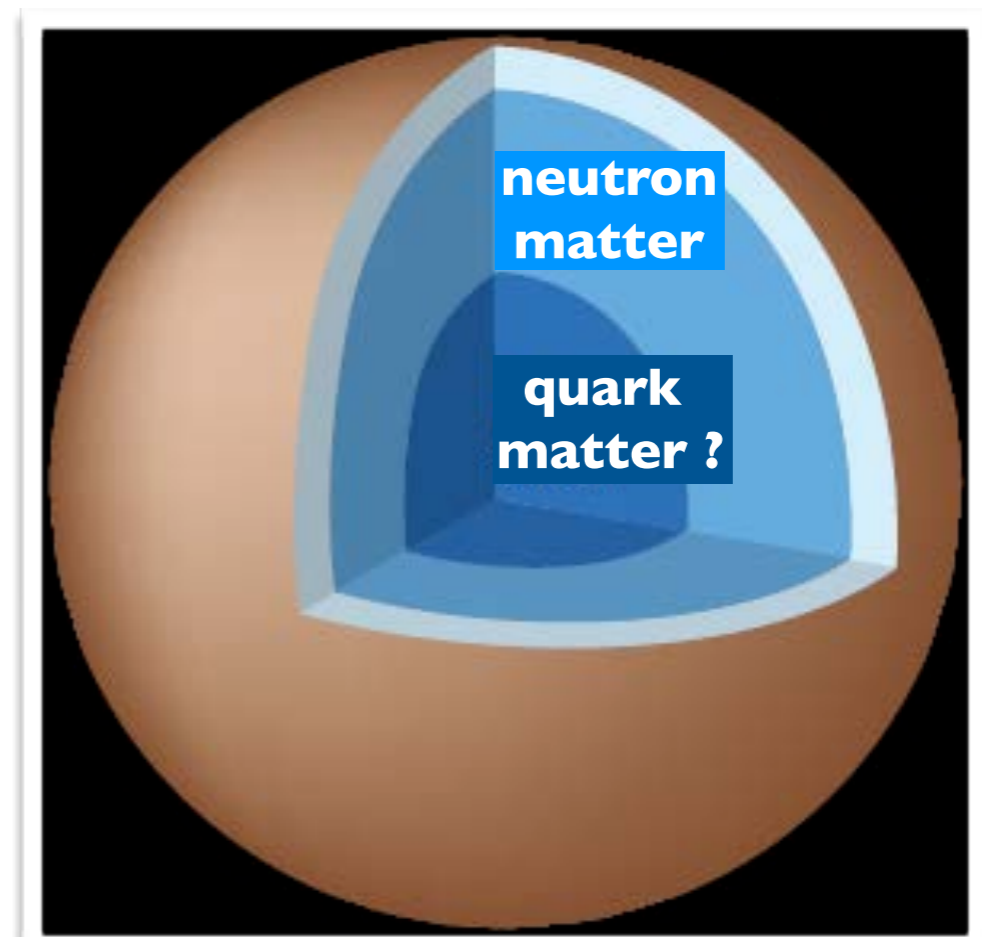
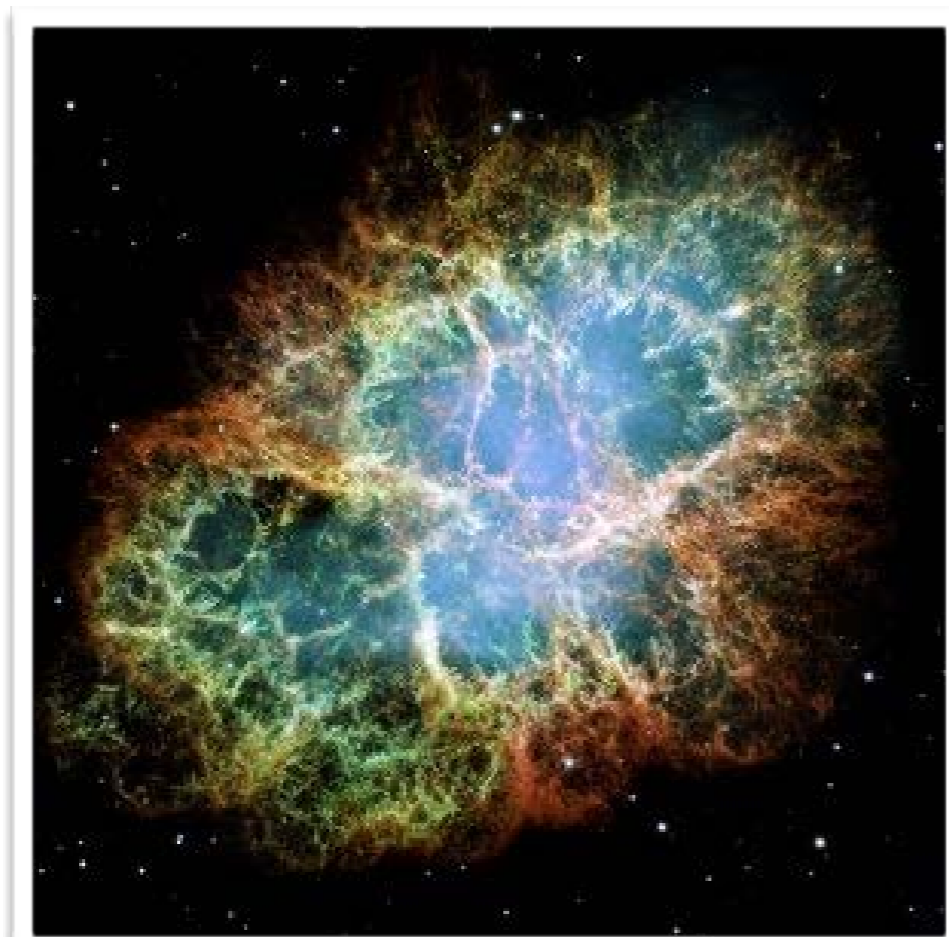
$$T_c \simeq 154 \pm 9 \text{ MeV}$$

S. Borsanyi et al.
 Phys. Lett. B 738 (2014) 187



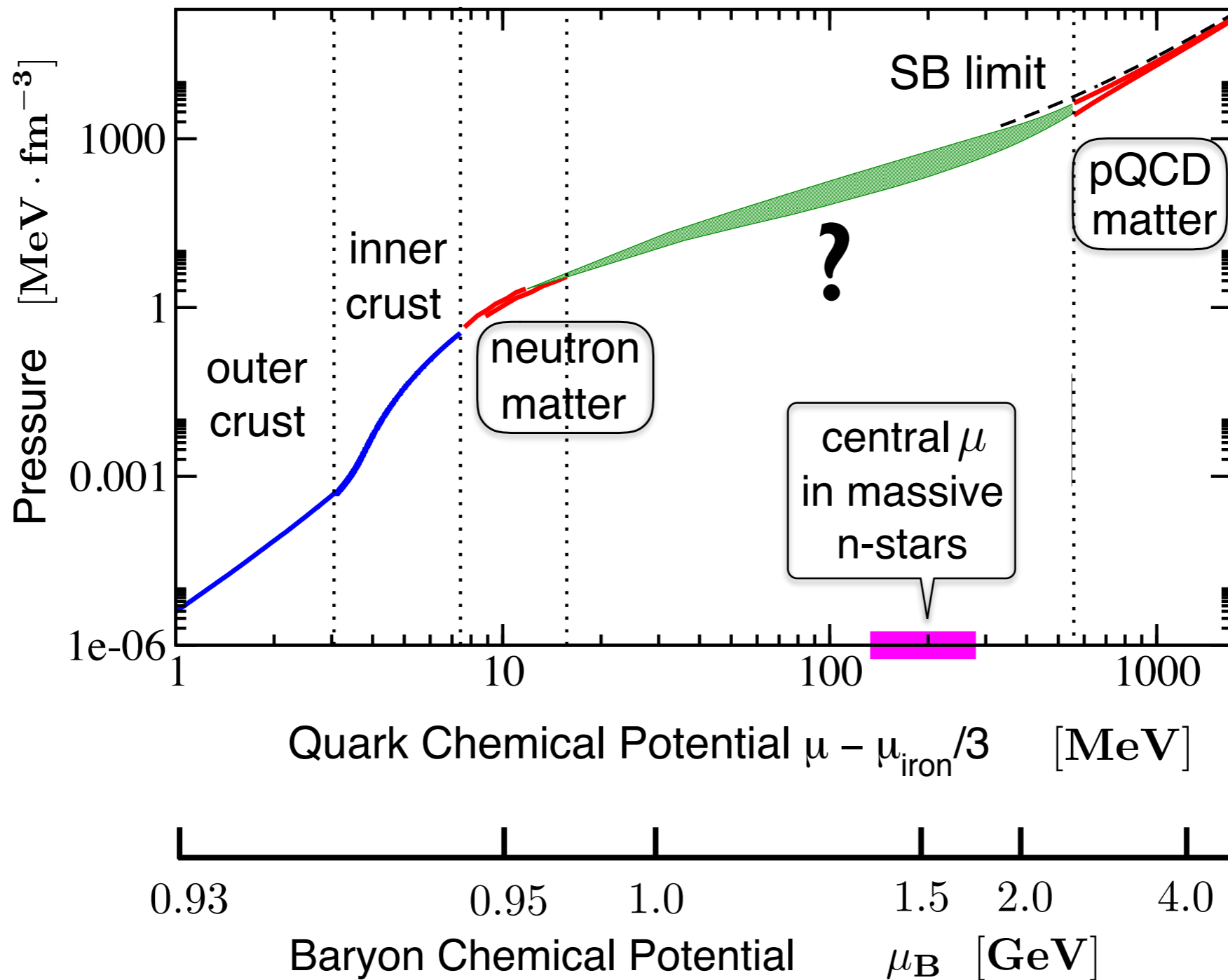
Strategies PART III: **Astrophysical Observations**

- Constraints on Equation of State of baryonic matter at **HIGH DENSITY** and **LOW TEMPERATURE**



- from **Supernovae** to **Neutron Stars**
... and **neutron star merger GW's** (LIGO & Virgo)

EQUATION of STATE NEUTRON STARS and beyond



A. Kurkela,
E.S. Fraga,
J. Schaffner-Bielich,
A. Vuorinen

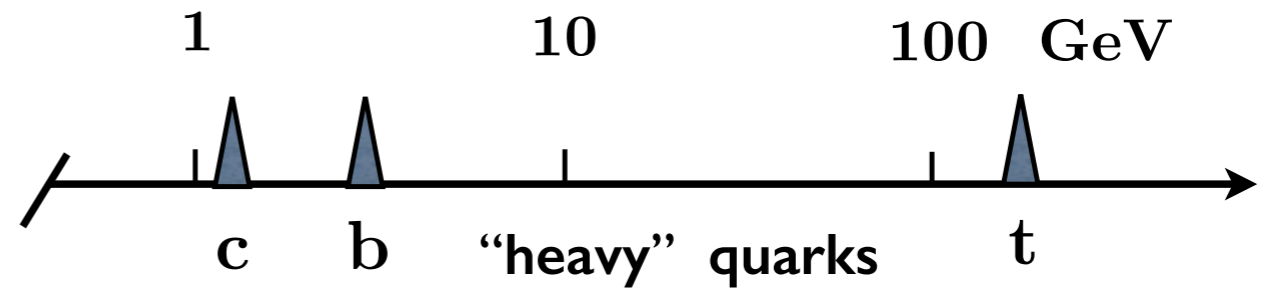
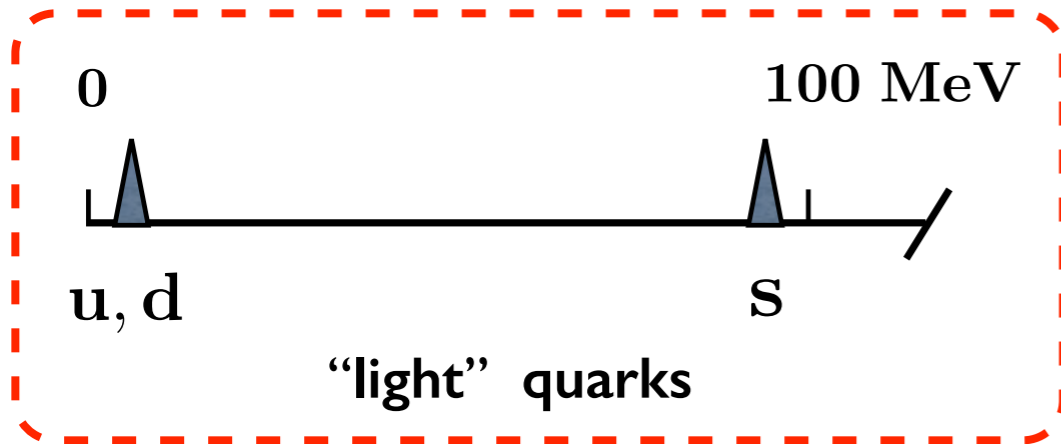
Astroph. J.
789 (2014) 127

2.

*QCD Symmetries,
Symmetry Breaking Patterns
and Scales*

Hierarchy of **QUARK MASSES** in **QCD**

- Separation of Scales -



$$m_u = 2.2 \pm 0.5 \text{ MeV}$$

$$m_d = 4.7 \pm 0.5 \text{ MeV}$$

$$m_s = 95_{-3}^{+9} \text{ MeV}$$

$$(\mu \simeq 2 \text{ GeV})$$

PDG 2018

**CHIRAL EFFECTIVE
FIELD THEORY**
of **pions & nucleons**

★ **Idealised QCD**

$$m_{u,d} \rightarrow 0$$

★ **Scale Invariance**

and

Trace Anomaly

from massless quarks to massive nucleons

★ **Chiral Symmetry**

spontaneously broken at low energy

CHIRAL SYMMETRY

★ (almost) massless u- and d-quarks :



$$\text{SU}(2)_R \times \text{SU}(2)_L$$

- Low energy : **spontaneous chiral symmetry breaking**
- **PIONS** as (almost) massless **Nambu-Goldstone bosons**

★ Symmetry breaking scale :

$$\Lambda_\chi = 4\pi f_\pi \sim 1 \text{ GeV}$$

- Pion decay constant :

$$f_\pi^{(0)} \simeq 86 \text{ MeV} \quad (\text{chiral limit})$$

$$f_\pi \simeq 92 \text{ MeV} \quad (\text{empirical})$$

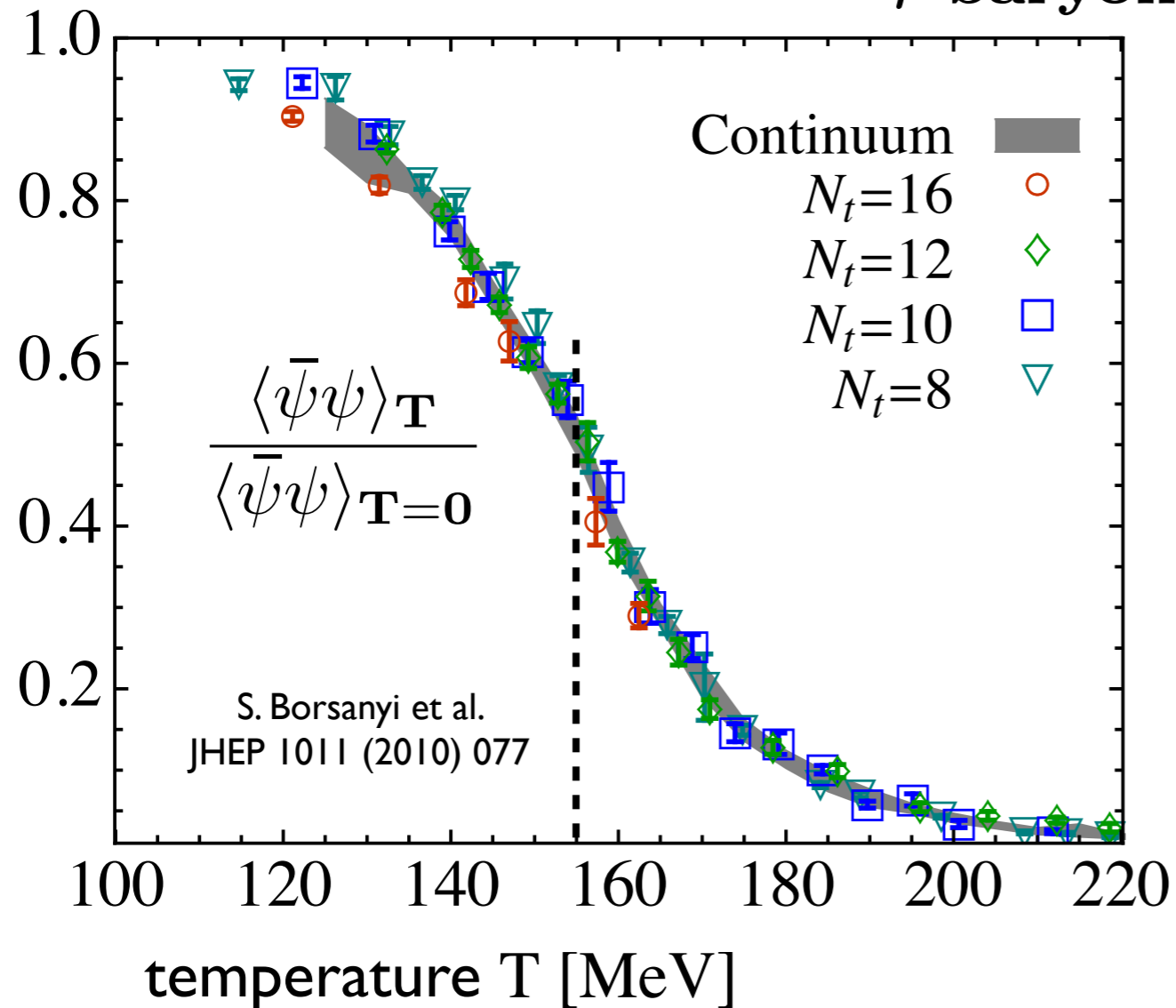
★ Order parameter f_π :

- Chiral (quark) condensate and sigma field

$$f_\pi^2 = -\frac{m_u + m_d}{2m_\pi^2} \langle \bar{q}q \rangle = \langle \sigma \rangle^2$$

LATTICE QCD THERMODYNAMICS: CHIRAL and DECONFINEMENT TRANSITIONS

$$\mu_{\text{baryon}} = 0$$



Quark Condensate

Order Parameter
of
spontaneously broken
Chiral Symmetry

**Crossover
transition temperature**

$$T_c \simeq 155 \text{ MeV}$$

CHIRAL and DECONFINEMENT
crossover transitions appear to be closely connected

SCALE INVARIANCE, TRACE ANOMALY and **MASS** of the **NUCLEON**

- ★ QCD with massless quarks : no dimensional parameter
 - Invariance under scale transformations $\mathbf{x} \rightarrow \lambda \mathbf{x}$
 - Trace of energy-momentum tensor $\Theta_{\mu\nu}$ vanishes classically ...
- ★ ... but - QCD as a QFT introduces renormalisation scale, and so :

$$\Theta_{\mu}^{\mu} \propto \text{Tr} [G_{\mu\nu} G^{\mu\nu}] \quad (\text{TRACE ANOMALY})$$

- ★ From **MASSLESS QUARKS** to **MASSIVE NUCLEONS** :

$$M_N^{(0)} = \langle N | \Theta_{\mu}^{\mu} | N \rangle = \frac{9}{4} \langle N | \frac{\alpha_s}{\pi} (\mathbf{E}^2 - \mathbf{B}^2) | N \rangle \simeq 0.89 \text{ GeV}$$

- Physical nucleon mass : $M_N = M_N^{(0)} + \sigma_N = 0.94 \text{ GeV}$
- Sigma term : $\sigma_N = \frac{1}{2} (m_u + m_d) \langle N | \bar{u}u + \bar{d}d | N \rangle$



NUCLEON MASS

- two aspects of symmetry breaking in QCD -

$$\propto \langle \mathbf{N} | \text{Tr} [G_{\mu\nu} G^{\mu\nu}] | \mathbf{N} \rangle$$

TRACE ANOMALY

Gluon dynamics

M_N

$$= g f_\pi \equiv g \langle \sigma \rangle \left(g = \frac{g_{\pi N}}{g_A} \right)$$

Spontaneously broken

CHIRAL SYMMETRY

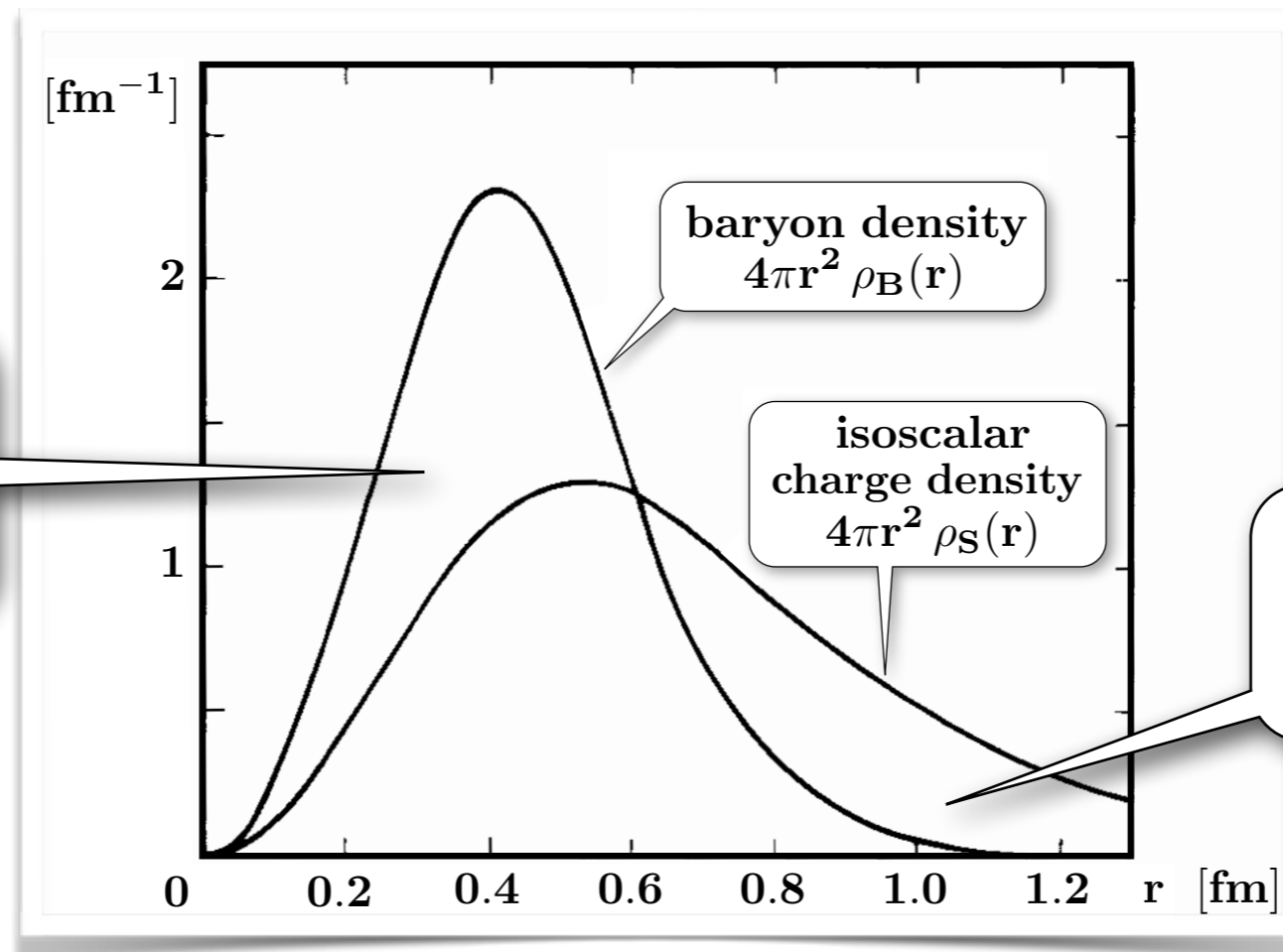
Goldberger - Treiman Relation



Reminder about **SIZES** :
CHIRAL SOLITON MODEL of the **NUCLEON**

Spontaneously broken chiral symmetry + localisation (confinement)

- **NUCLEON** : compact valence quark core + mesonic cloud



baryonic core
 $\langle r^2 \rangle_B^{1/2} \simeq 0.5 \text{ fm}$

mesonic cloud
 $\langle r^2 \rangle_{E, \text{isoscalar}}^{1/2} \simeq 0.8 \text{ fm}$

N. Kaiser,
 U.-G. Meißner, W.W.
 Nucl. Phys.
 A466 (1987) 685

- **Significant difference of scales between compact baryonic core and (multi-)pion cloud**

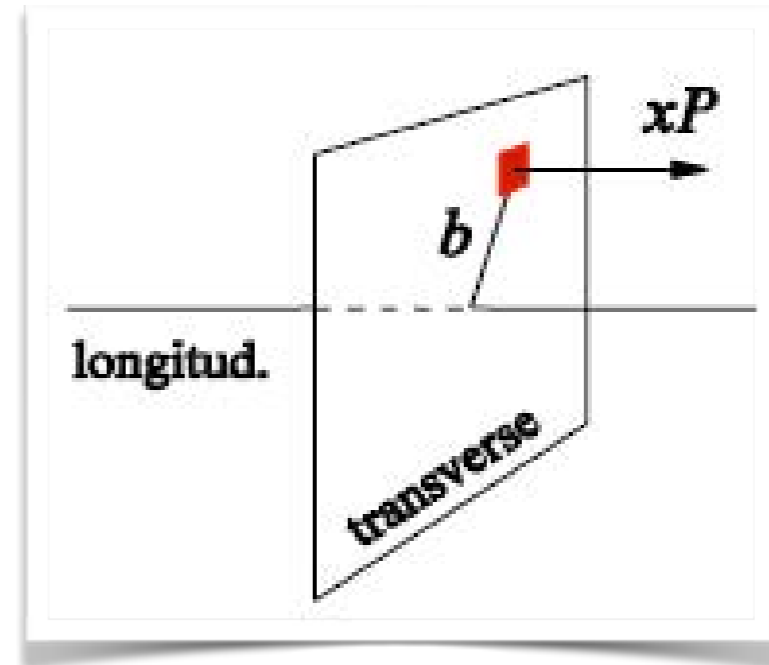
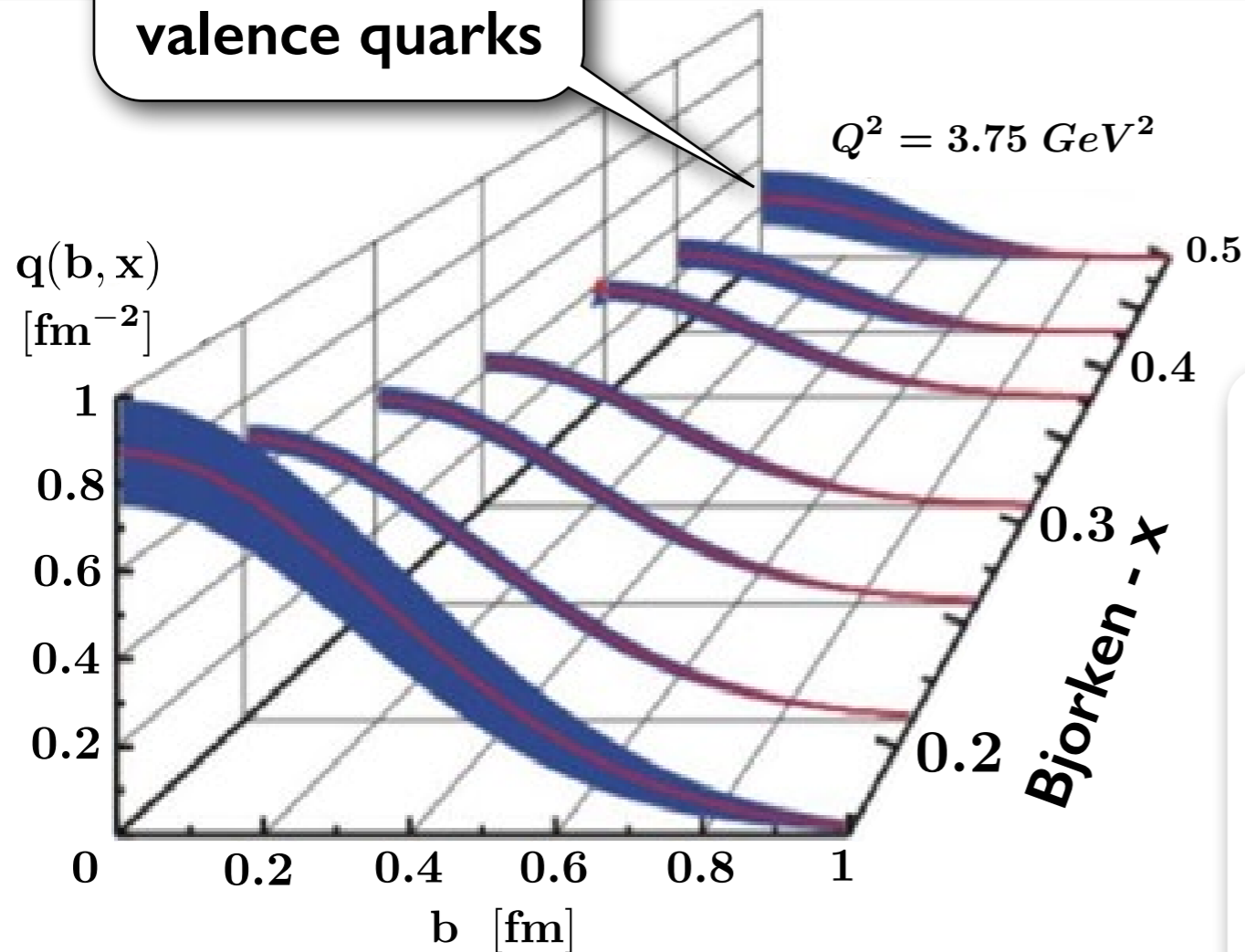


Transverse distributions of quarks in the proton

Deeply Virtual Compton Scattering @ JLab

R. Dupré, M. Guidal, M. Vanderhaeghen
Phys. Rev. D95 (2017) 011501

compact core:
valence quarks



$$\langle b^2 \rangle \simeq 0.16 \text{ fm}^2 \cdot \ln(1/x_B)$$

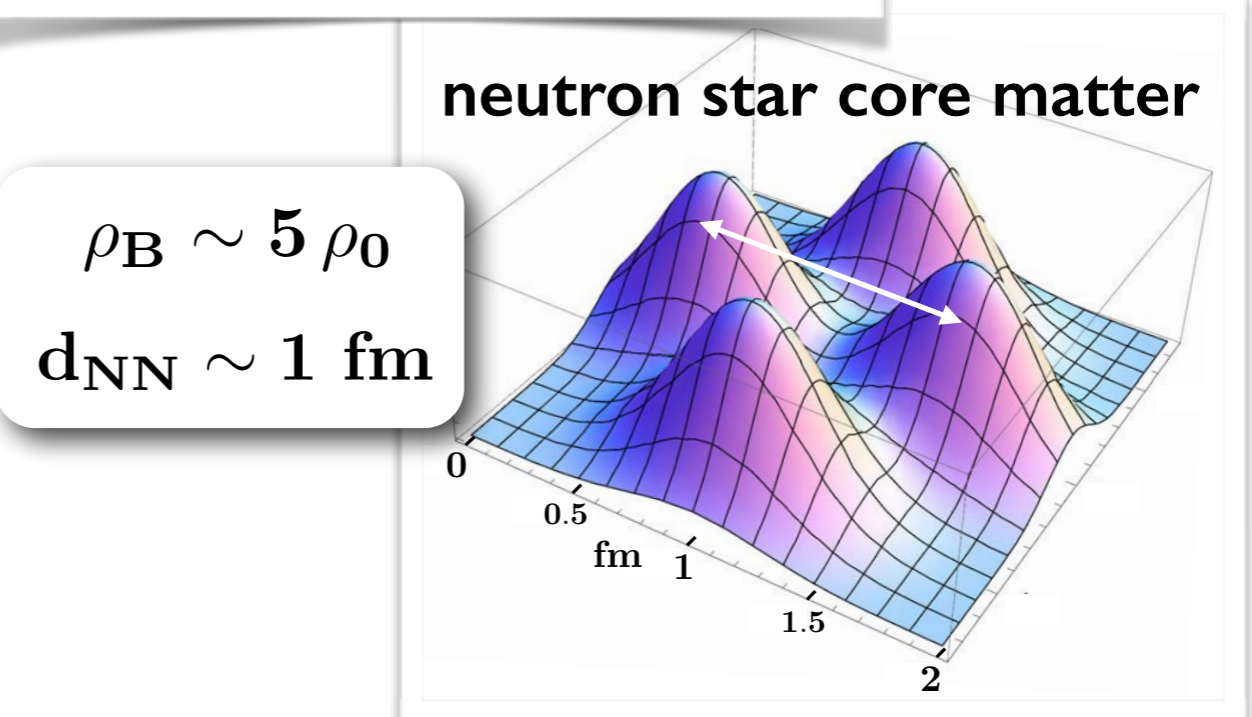
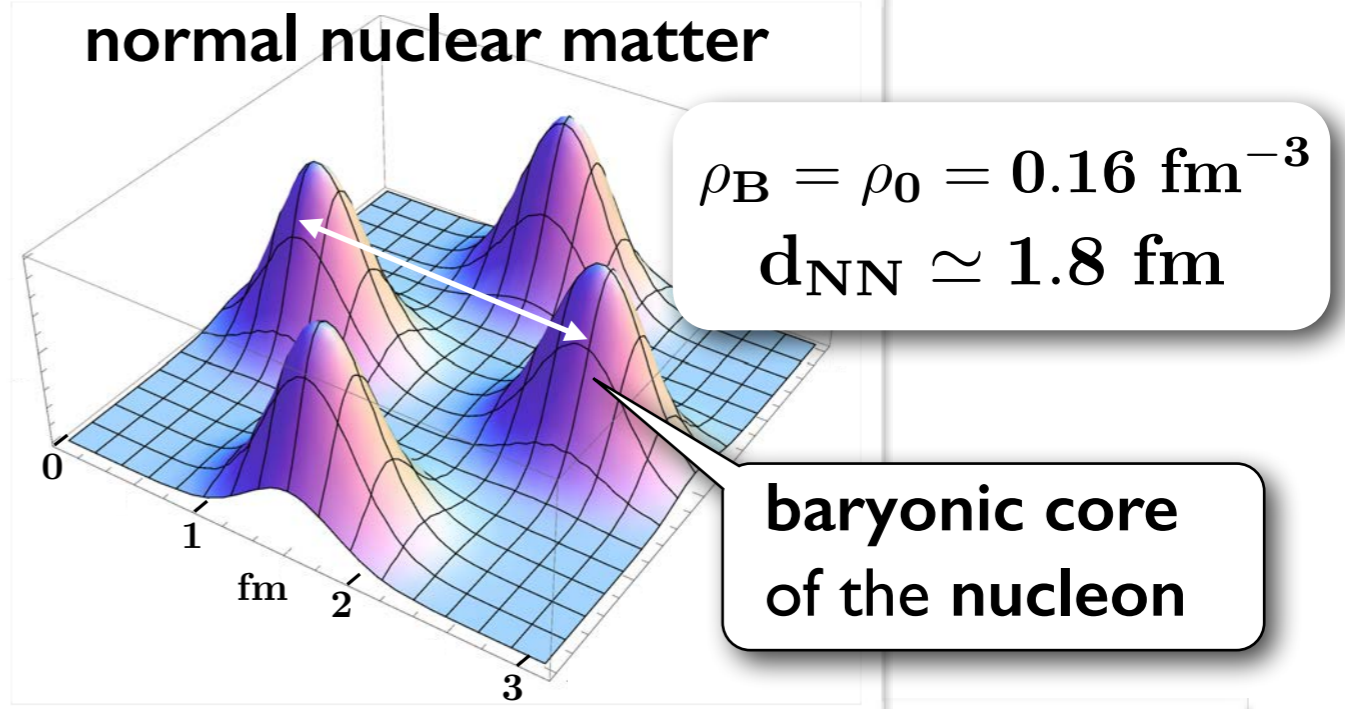
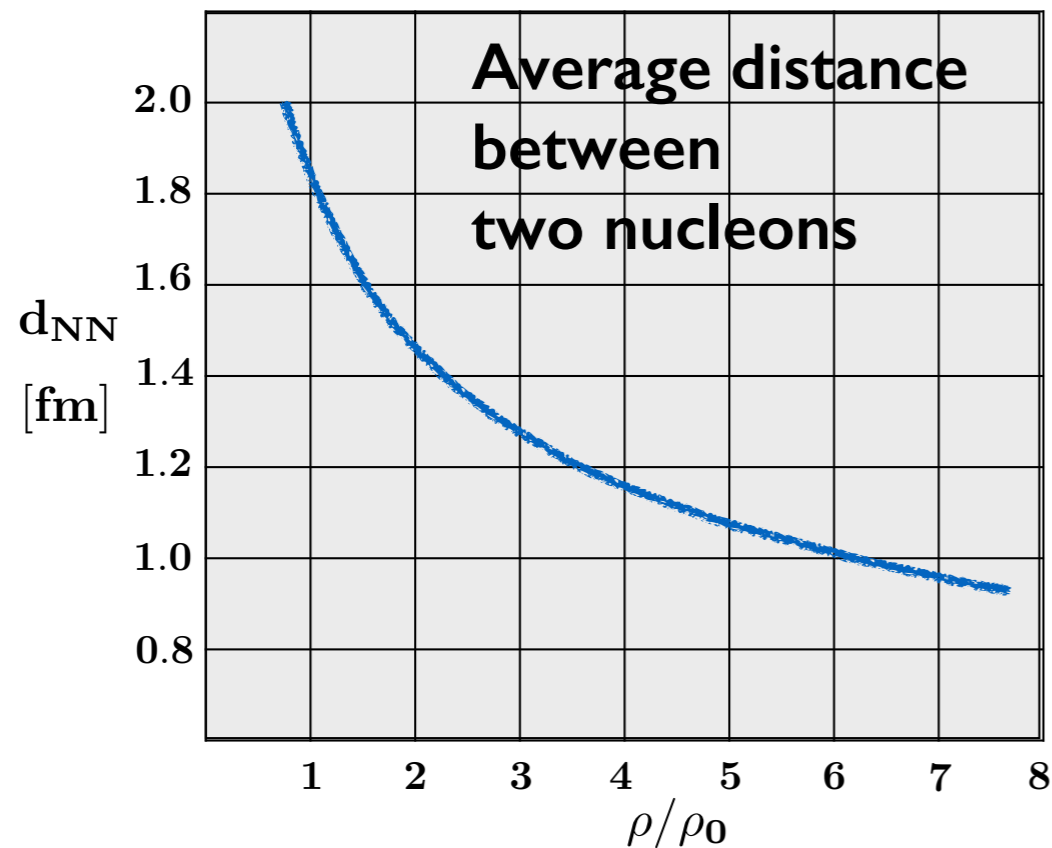
● Valence quark region:

$$\frac{1}{3} < x_B < \frac{1}{2}$$

● Core size:

$$R_{core} = \sqrt{\frac{3}{2} \langle b^2 \rangle} \sim 0.4 - 0.5 \text{ fm}$$

Densities and Distance Scales in Baryonic Matter



- (Multi-)pion fields in space between baryonic sources (ChEFT)
- Quark cores of nucleons overlap (percolate) at baryon densities $\rho_B > 5 \rho_0$

NUCLEAR FORCES from LATTICE QCD

NN Central Potential ($S = 0, l = 1$)

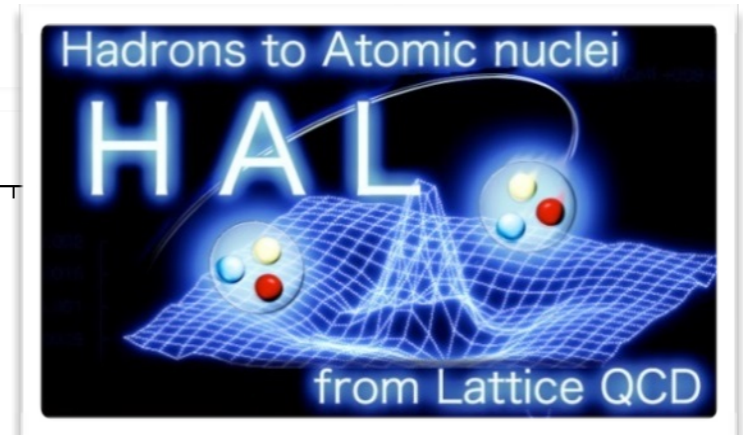
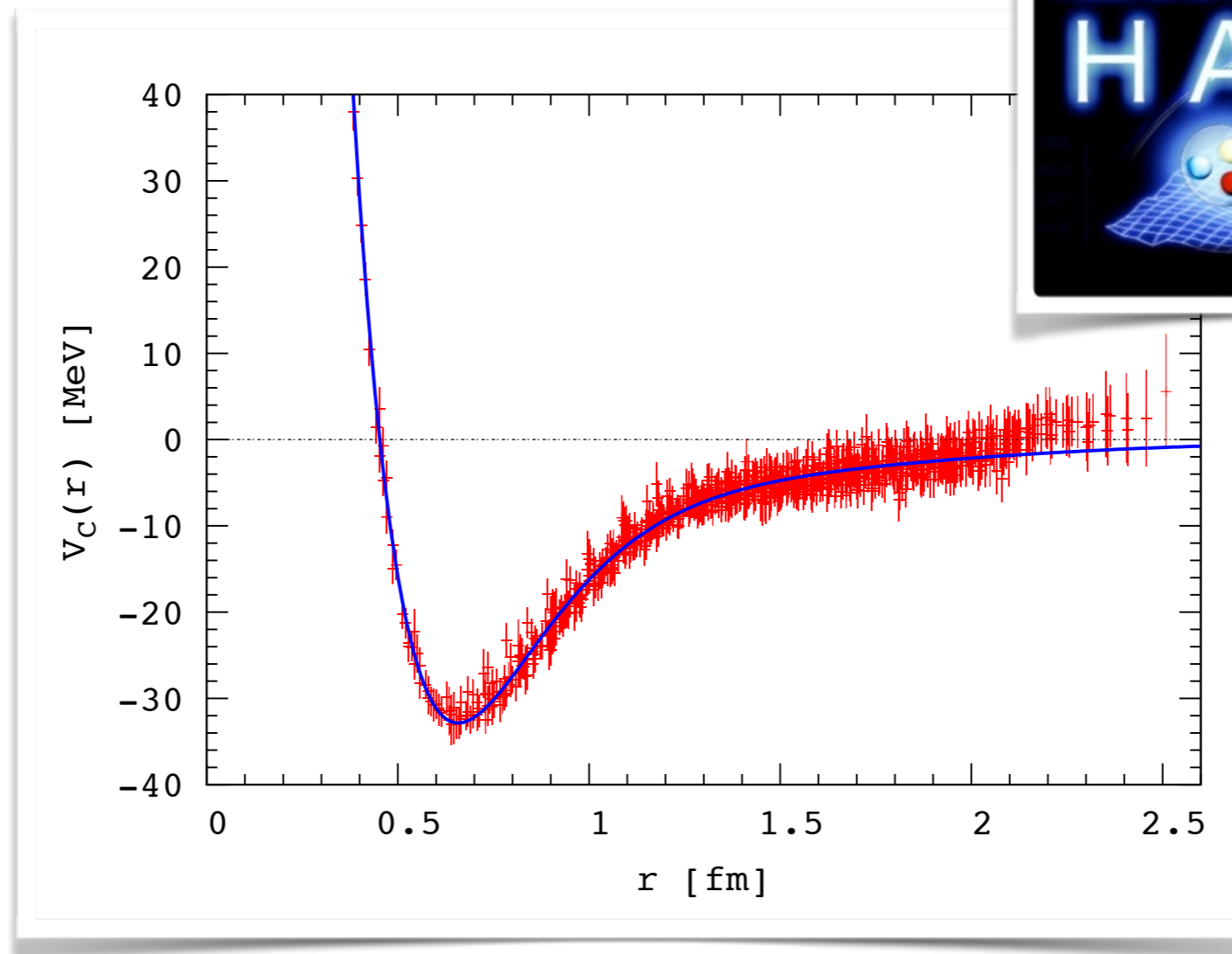
deduced from LQCD two-nucleon (6-quark) correlation function

previously:
unphysically large
u- and d-quark
masses

...but :
stable 0.5 Fermi
repulsive core

S.Aoki, T. Hatsuda, N. Ishii
Prog. Theor. Phys. 123 (2010) 89

S.Aoki
Eur. Phys. J. A49 (2013) 81



now:
towards
**physical
quark
masses**

3.

Chiral Effective Field Theory and related approaches to the Nuclear Many-Body Problem



PIONS and **NUCLEI** in the context of **LOW-ENERGY QCD**

- **CONFINEMENT** of quarks and gluons in hadrons
- Spontaneously broken **CHIRAL SYMMETRY**



LOW-ENERGY QCD

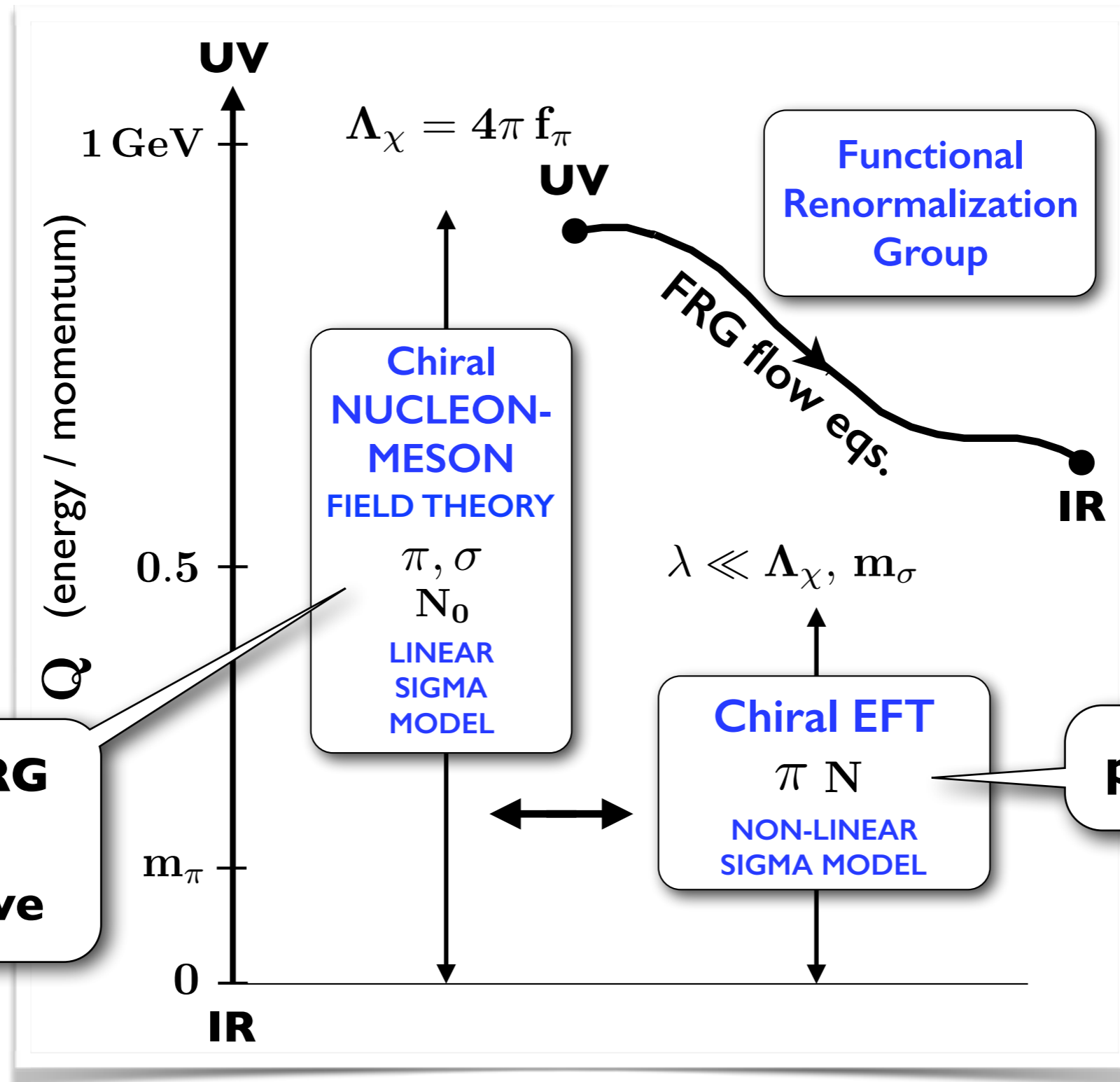
At (energy and momentum) scales $Q < 4\pi f_\pi \sim 1 \text{ GeV}$
is realised as an

Effective **F**ield **T**heory

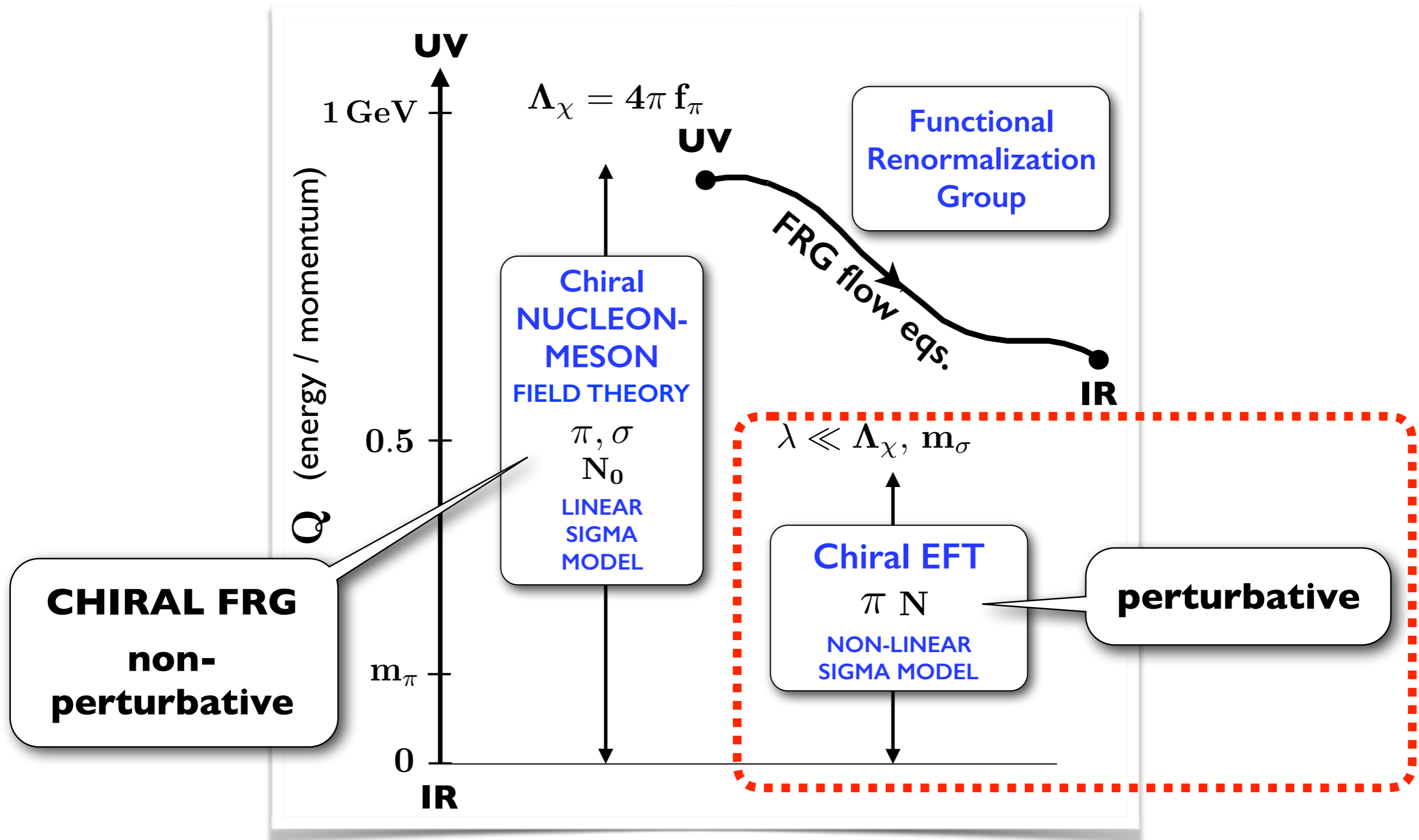
of Nambu-Goldstone Bosons (**PIONS**) coupled to
NUCLEONS as (heavy) Fermion sources



Theoretical FRAMEWORKS and METHODS



Theoretical FRAMEWORKS and METHODS



NUCLEON-NUCLEON INTERACTION

from CHIRAL EFFECTIVE FIELD THEORY

Weinberg

Bedaque & van Kolck

Bernard, Epelbaum, Kaiser, Meißner ;

	NN interaction	
LO		
NLO		
N ² LO		
N ³ LO		

...

- Systematically organized hierarchy in powers of $\frac{Q}{\Lambda}$ (Q: momentum, energy, pion mass)

3 – body forces	
N ² LO	
N ³ LO	

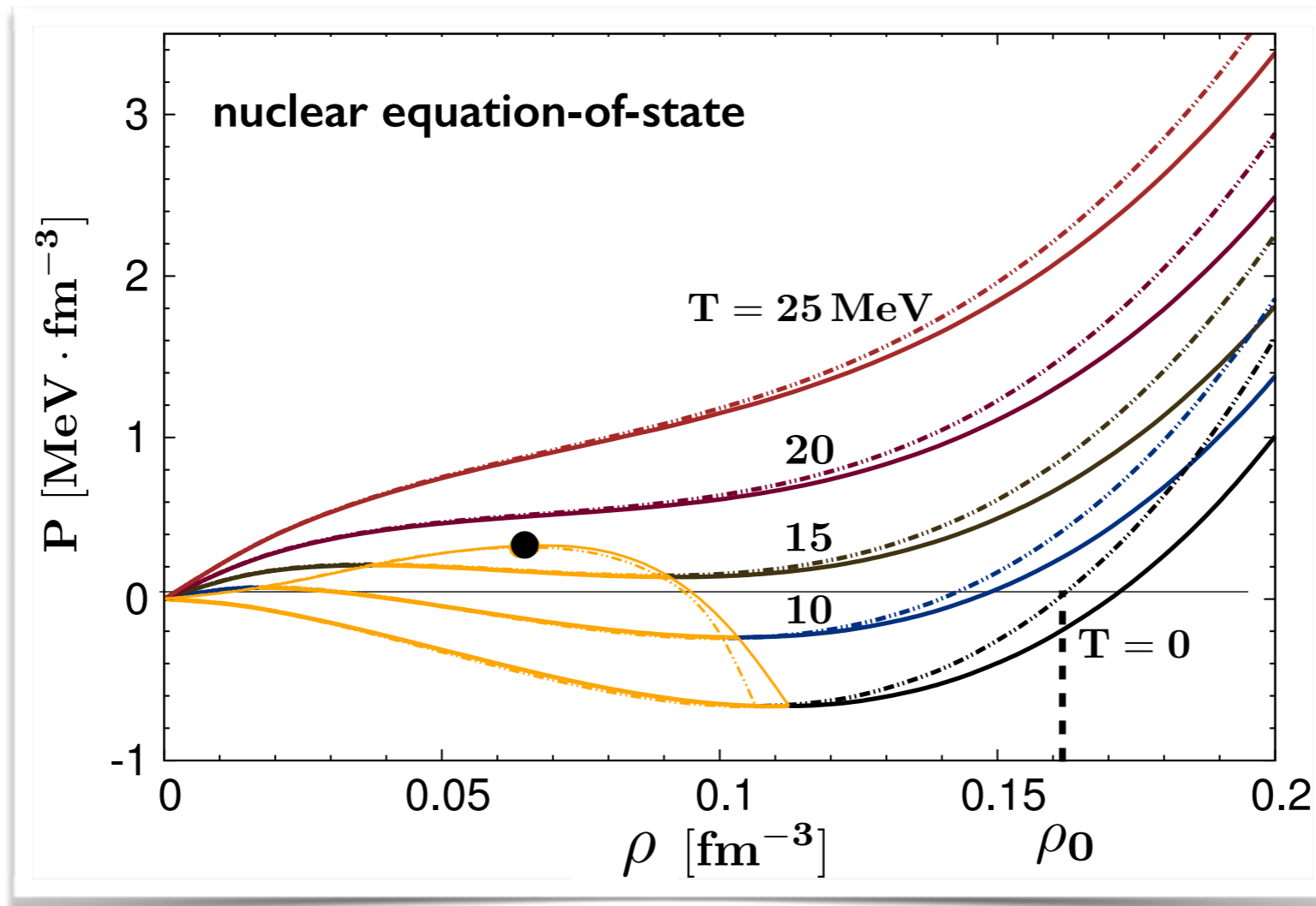
4 – body forces	
N ³ LO	

- NN interaction state-of-the-art: N⁴LO plus convergence tests at N⁵LO



NUCLEAR THERMODYNAMICS from CHIRAL EFT

- Symmetric nuclear matter : 1st order **liquid-gas phase transition**
- N3LO chiral NN interactions + N2LO 3-body forces



Critical
temperature
of
liquid-gas
first-order
transition :

$$T_c = 17.4 \text{ MeV}$$

C. Wellenhofer,
J.W. Holt,
N. Kaiser, W.W.
Phys. Rev.
C89 (2014) 064009
C92 (2015) 015801

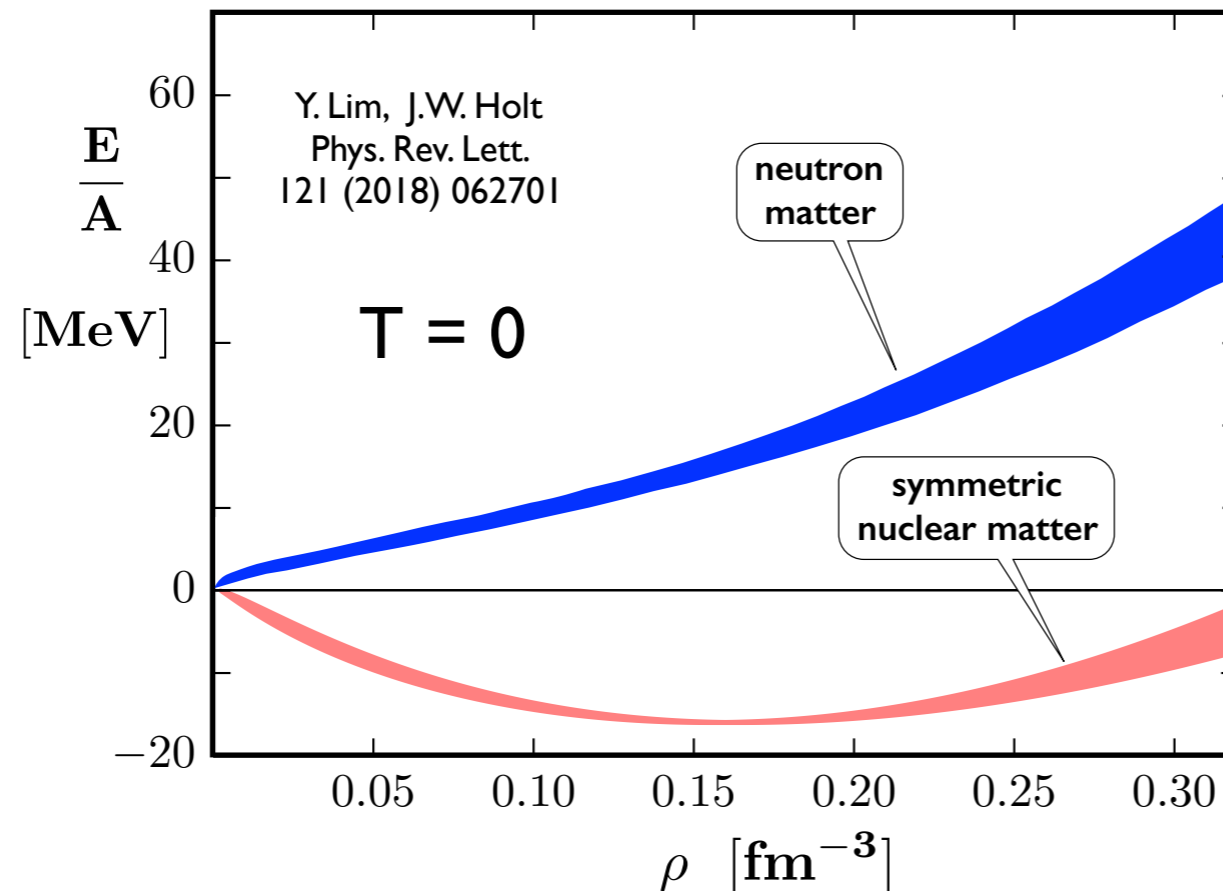
► Empirical position of liquid-gas critical point : J. B. Elliot et al. : Phys. Rev. C87 (2013) 054622

$$T_c = 17.9 \pm 0.4 \text{ MeV} \quad P_c = 0.31 \pm 0.07 \text{ MeV} \cdot \text{fm}^{-3} \quad \rho_c = 0.06 \pm 0.01 \text{ fm}^{-3}$$

NEUTRON and NUCLEAR MATTER from CHIRAL EFT

- N3LO chiral NN interactions + N2LO 3-body forces
- Many-body perturbation theory (3rd order)

J.W. Holt, N. Kaiser
Phys. Rev. C95 (2017) 034326



Perturbative
Chiral EFT :

applicable up to
baryon densities

$$\rho \sim 2 \rho_0$$

- Agreement with advanced many-body calculations
(e.g. Quantum Monte Carlo computations - S. Gandolfi et al.: EPJ A50 (2014) 10)

C.Wellenhofer, J.W. Holt, N. Kaiser, W.W.: Phys. Rev. C89 (2014) 064009, C92 (2015) 015801

- Further recent developments: N4LO F. Sammarruca et al.: arXiv:1807.06640

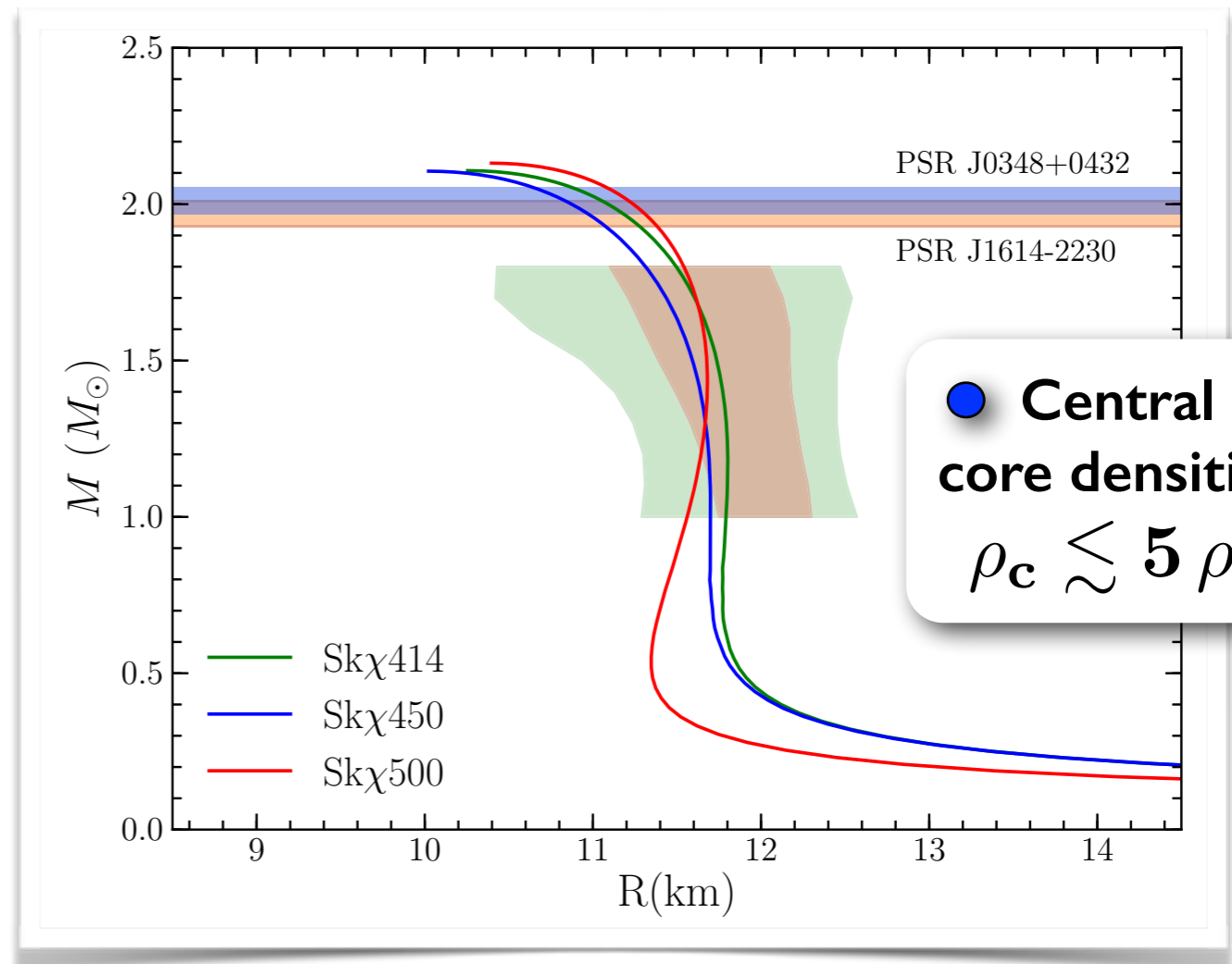
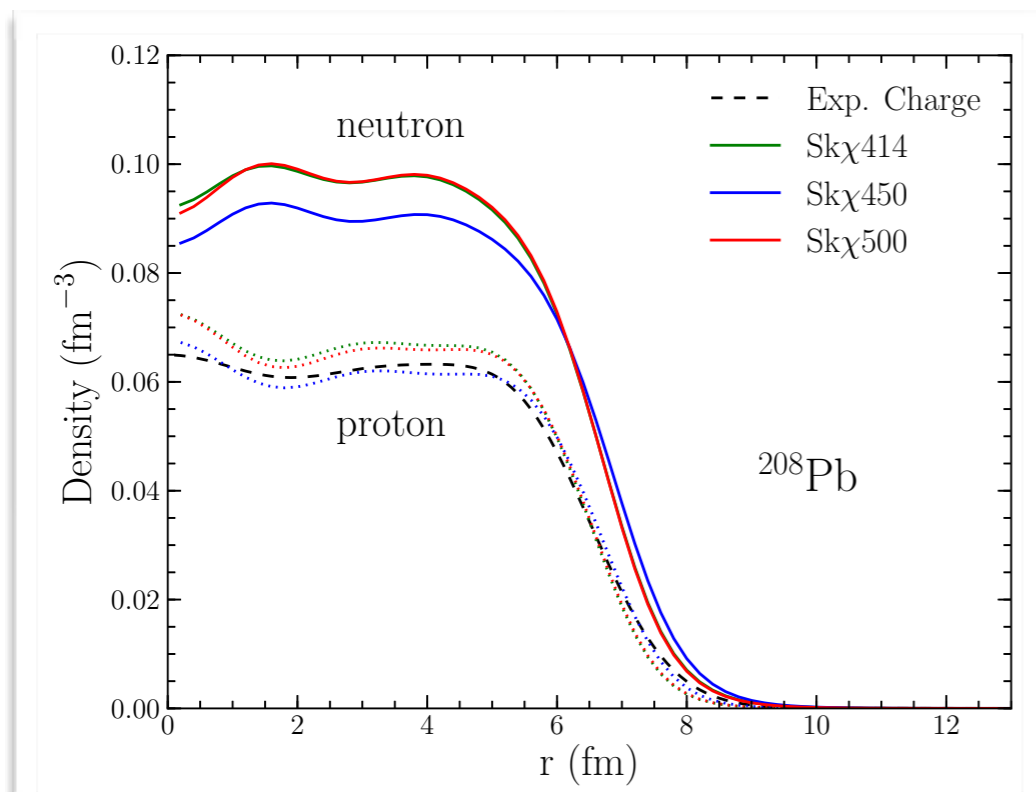
NEUTRON STAR MATTER

- Energy Density Functional (Skyrme-Hartree-Fock) deduced from Chiral Effective Field Theory

N3LO two-body interactions, N2LO three-body forces
density dependence consistent with ChEFT expansion in powers of Fermi momenta

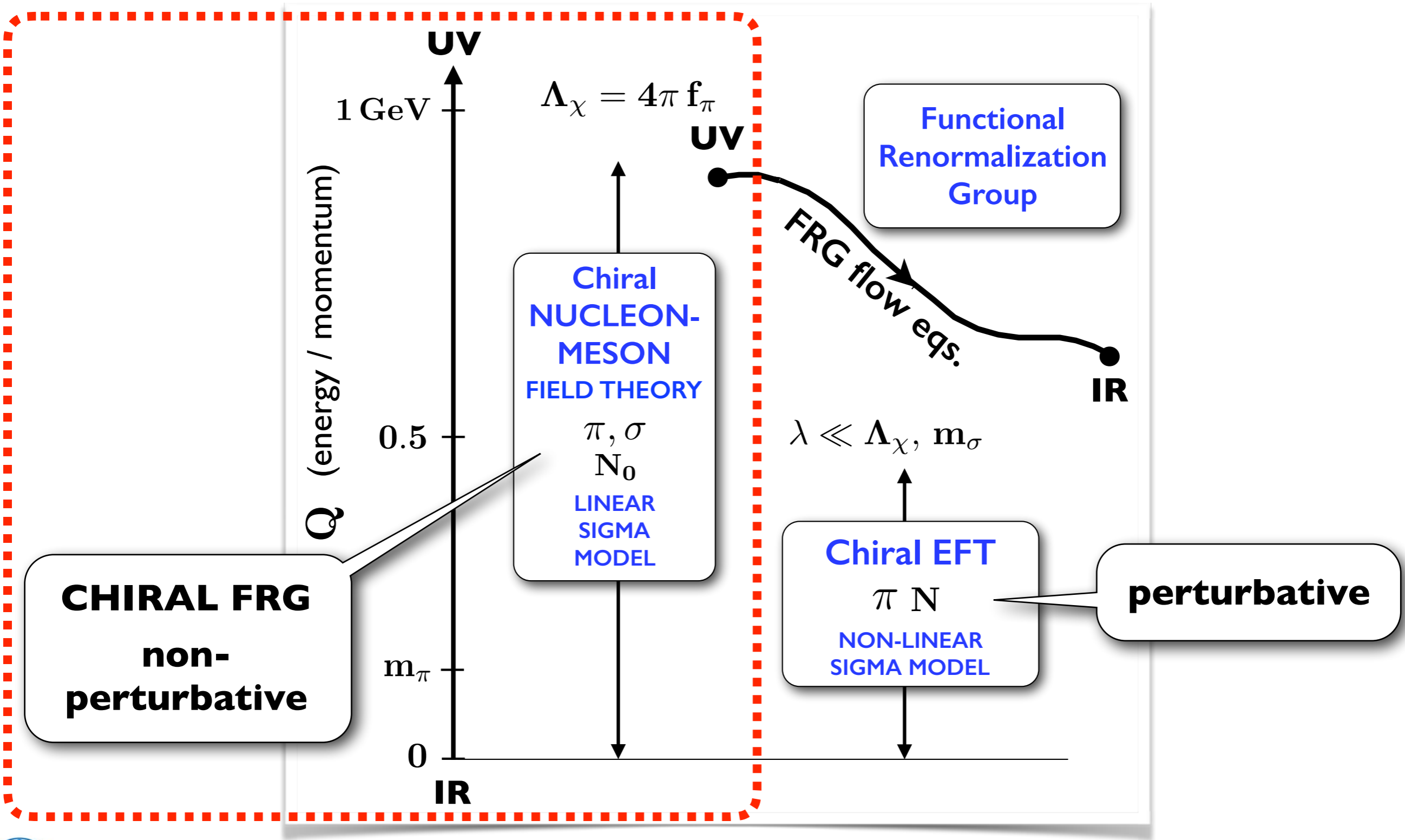
Y. Lim, J.W. Holt Phys. Rev. C95 (2017) 065805

- successfully reproduces properties of finite nuclei ...



... and neutron star crust together with $2 M_{\odot}$ constraint

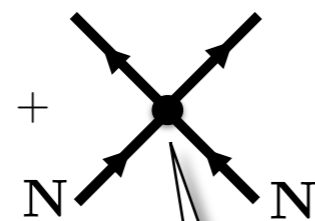
Theoretical FRAMEWORKS and METHODS



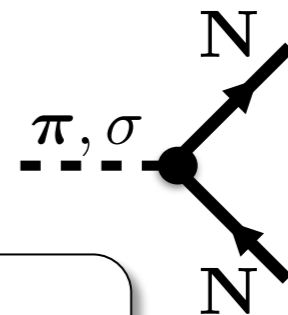
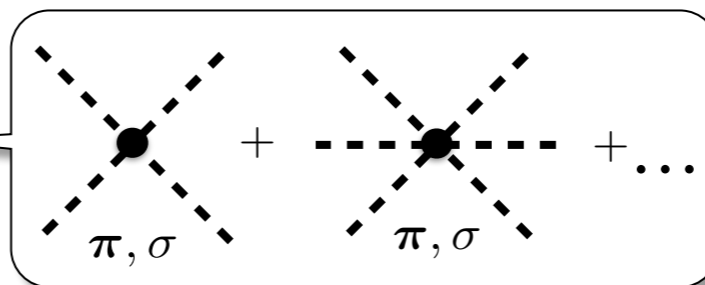
Mesons, Nucleons, Nuclear Matter and Functional Renormalization Group

- Chiral nucleon - meson Lagrangian

$$\mathcal{L} = \bar{N} i \gamma_\mu \partial^\mu N + \frac{1}{2} (\partial_\mu \sigma \partial^\mu \sigma + \partial_\mu \pi \cdot \partial^\mu \pi) + \dots$$



$-\mathcal{U}(\pi, \sigma)$



isoscalar & isovector
current-current interactions

- Nambu-Goldstone boson π and “heavy” σ
- Potential $\mathcal{U}(\sigma, \pi)$: polynomial in $\chi = \pi^2 + \sigma^2$ constructed to reproduce vacuum physics and equilibrium nuclear matter

- **Pionic fluctuations, nucleonic particle-hole excitations** and **many-body correlations** treated non-perturbatively using **FRG**

Renormalization Group strategies

k-dependent action

full propagator

Wetterich's FRG flow equations

$$k \frac{\partial \Gamma_k[\Phi]}{\partial k} = \frac{1}{2} \text{Tr} \left[k \frac{\partial R_k}{\partial k} \cdot \left(\Gamma_k^{(2)}[\Phi] + R_k \right)^{-1} \right] = \text{Diagram}$$

$$\Gamma_{k=\Lambda}[\Phi] = S$$

UV

$\Gamma_k[\Phi]$

scale regulator R_k

IR $\Gamma_{k=0}[\Phi] = \Gamma[\Phi]$

C. Wetterich:
Phys. Lett. B 301 (1993) 90

● Thermodynamics:

$$k \partial_k \bar{\Gamma}_k(T, \mu) = \left(\text{Diagram}_1 + \text{Diagram}_2 \right) \Big|_{T, \mu} - \left(\text{Diagram}_1 + \text{Diagram}_2 \right) \Big|_{T=0, \mu=\mu_c}$$

nucleons pions

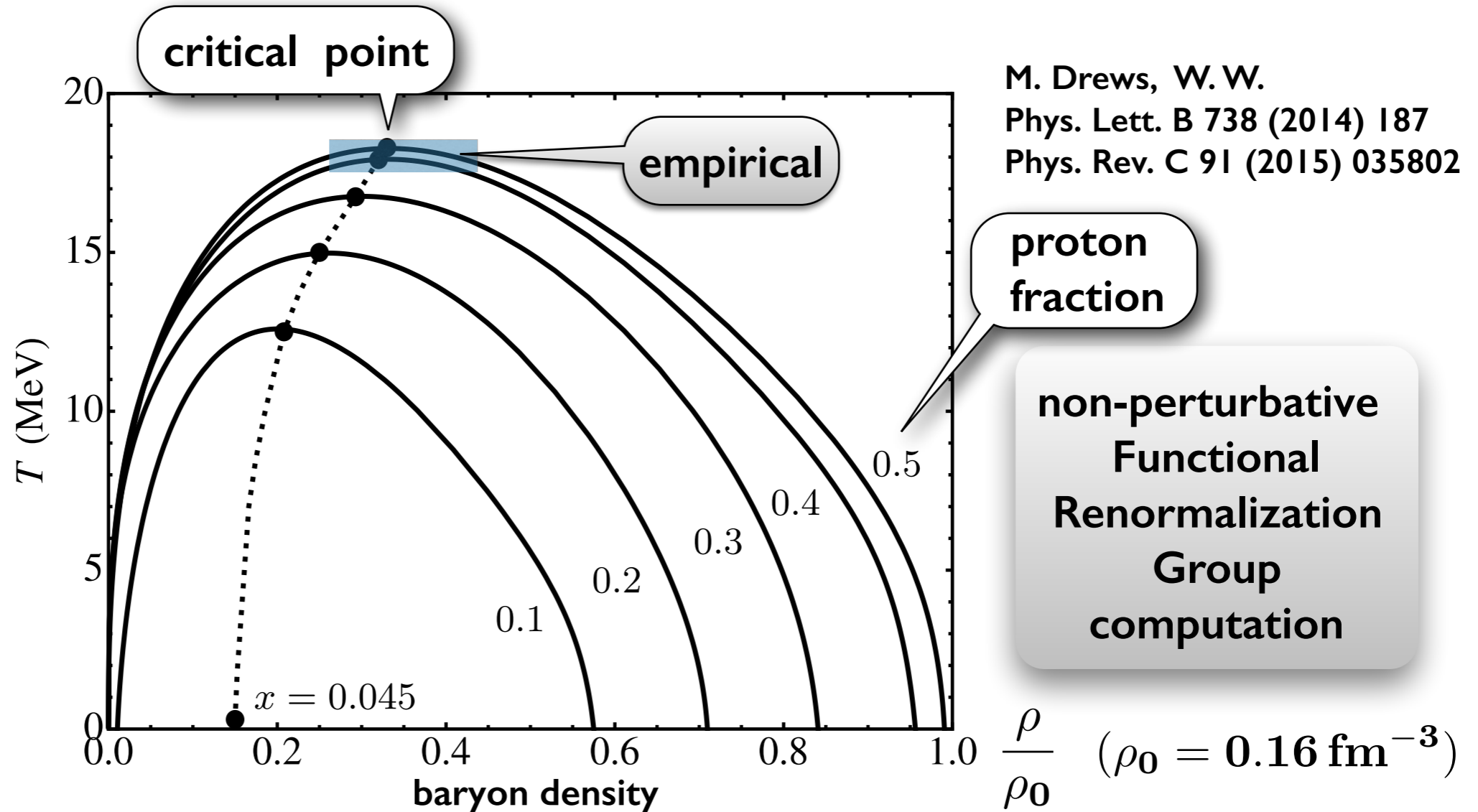
Non-perturbative treatment of :

- multi-pion exchange processes
- nucleon-hole excitations
- multi-nucleon correlations

PHASE DIAGRAM of NUCLEAR MATTER

- Trajectory of **CRITICAL POINT** of Liquid - Gas transition for asymmetric matter as function of proton fraction Z / A

M. Drews, T. Hell,
B. Klein, W. W.
Phys. Rev.
D 88 (2013)
096011



Governed by isospin dependent (two-)pion exchange dynamics

CHIRAL ORDER PARAMETER in NUCLEAR and NEUTRON MATTER

- Chiral Nucleon-Meson field theory and **F**unctional **R**enormalization **G**roup

M. Drews, W.W.

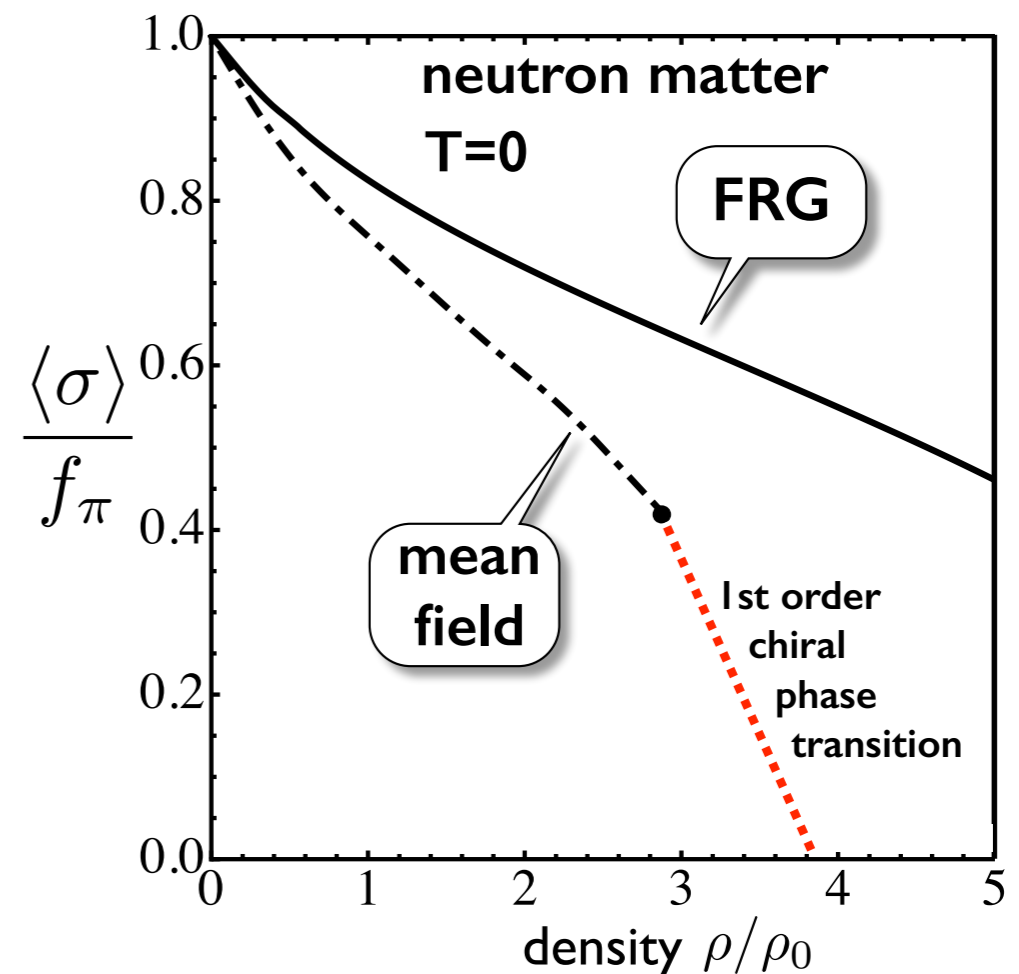
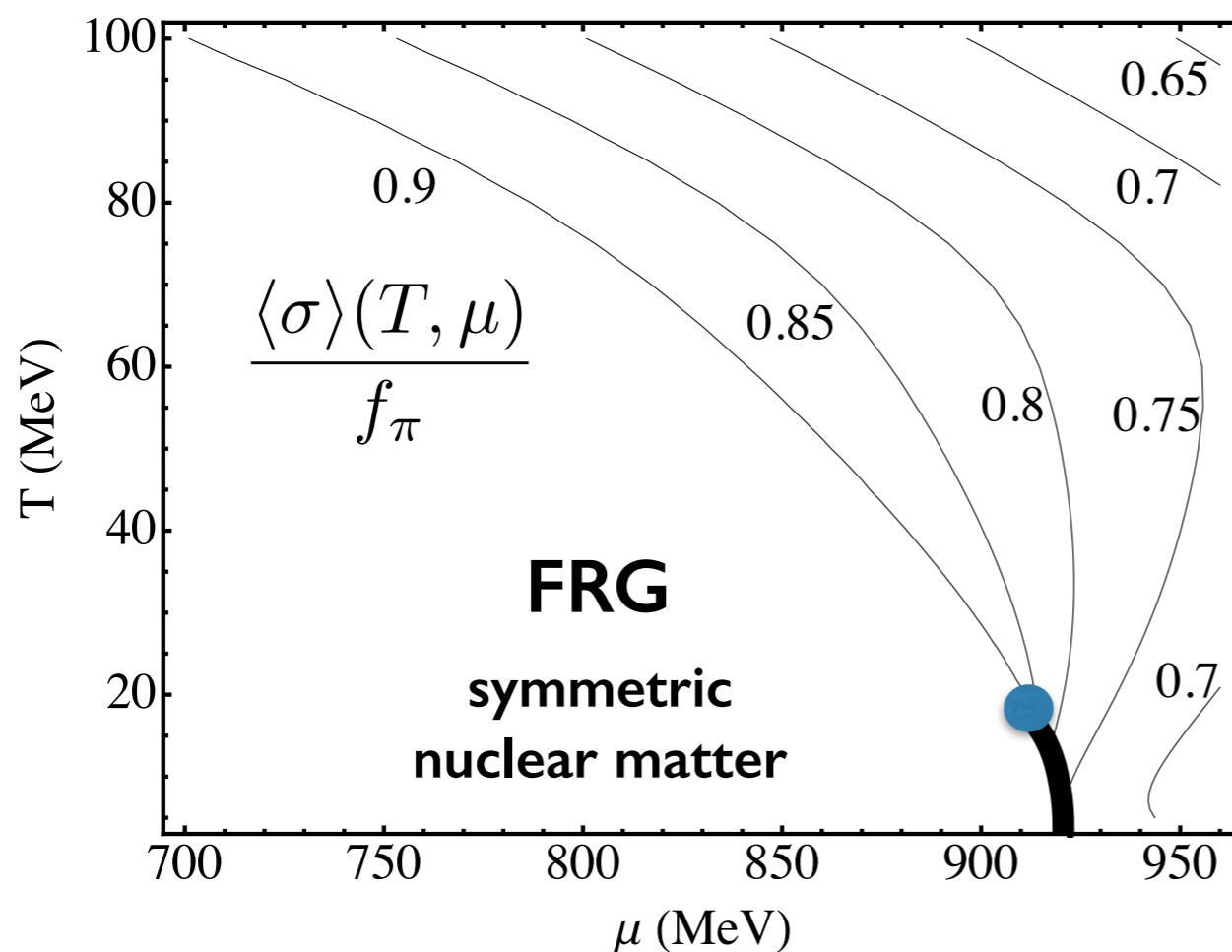
Phys. Rev. C91 (2015) 035802

Prog. Part. Nucl. Phys. 93 (2017) 69

- Chiral order parameter :

Sigma field \longleftrightarrow **in-medium pion decay constant**

$$\langle \sigma \rangle_{T,\mu} = f_{\pi}^*(T, \mu)$$



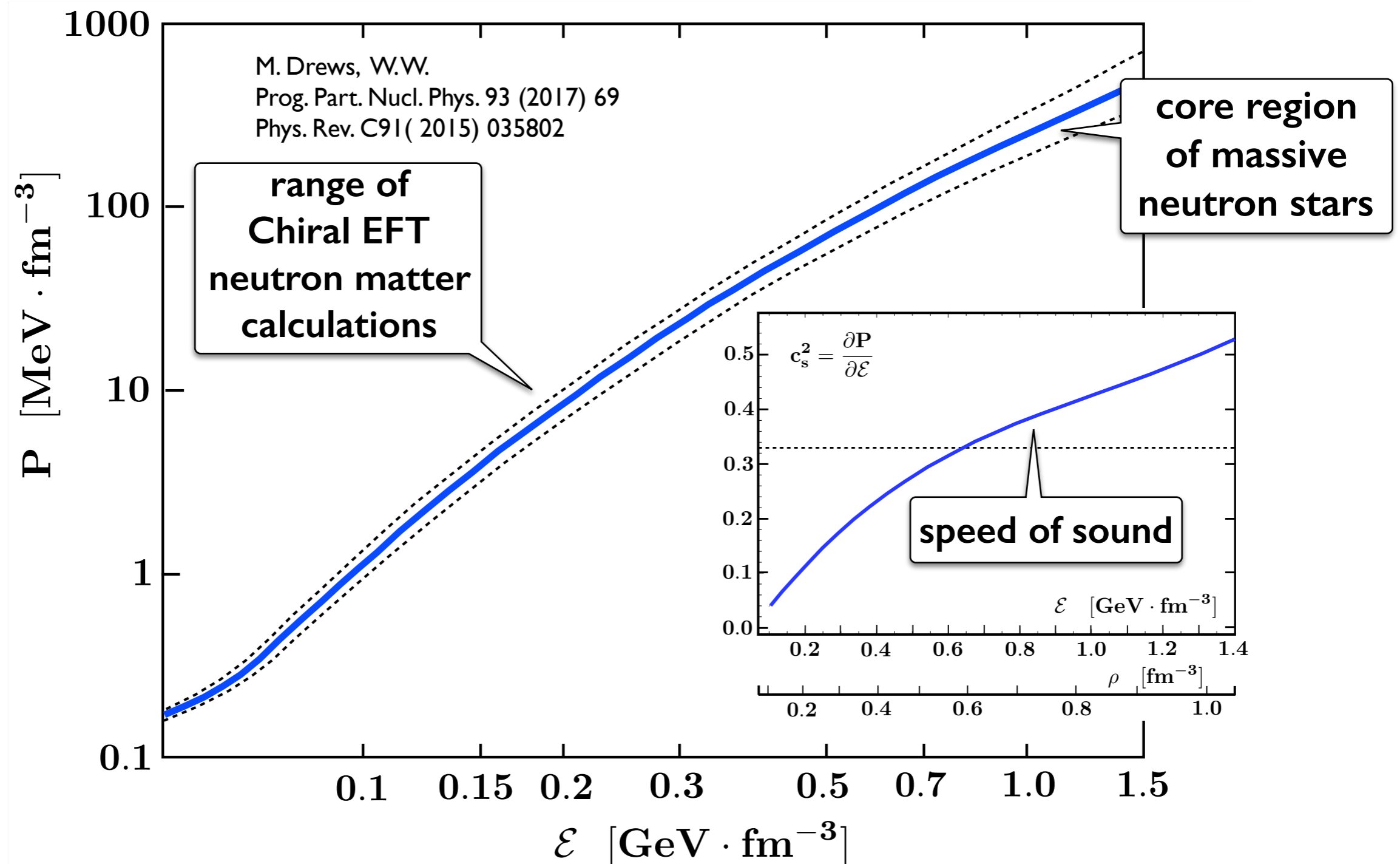
Important role of **fluctuations** (pionic and nucleon-hole) beyond mean-field appr. :

DISAPPEARANCE of first-order chiral phase transition

NEUTRON STAR MATTER Equation of State

from Chiral Nucleon-Meson Field Theory

- **FRG** calculations with inclusion of beta equilibrium

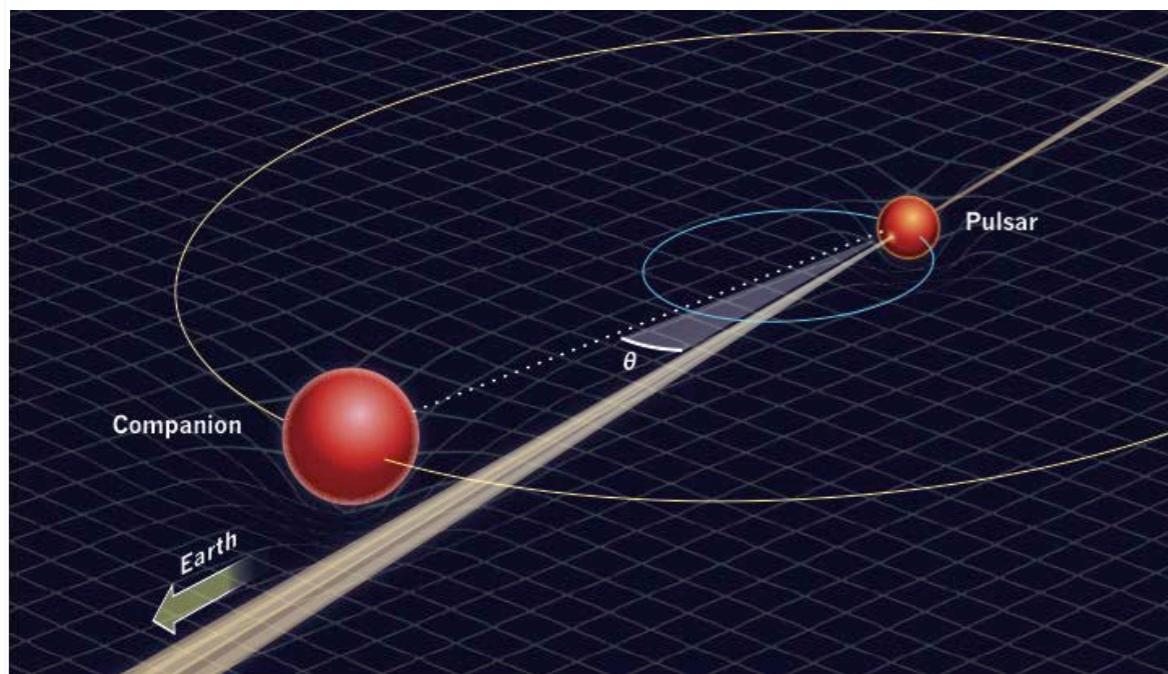
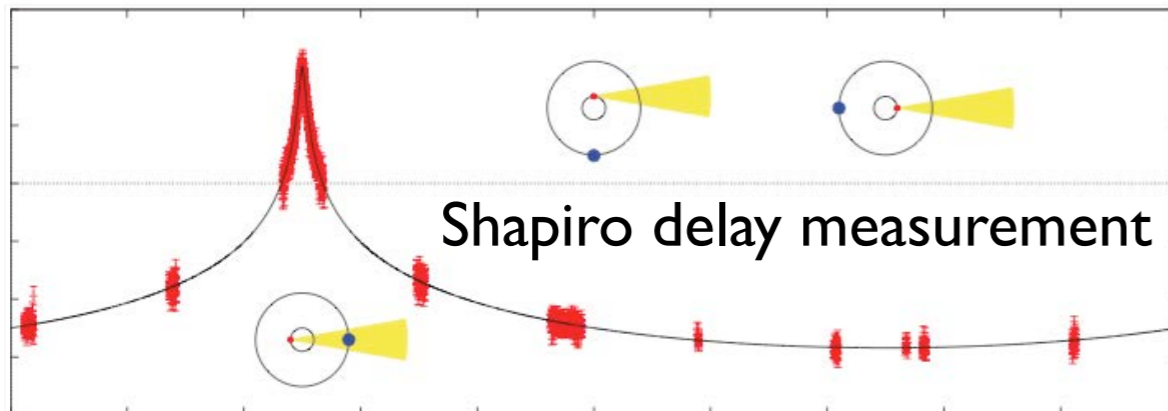


4.
Constraints from
NEUTRON STARS



MASSIVE NEUTRON STARS

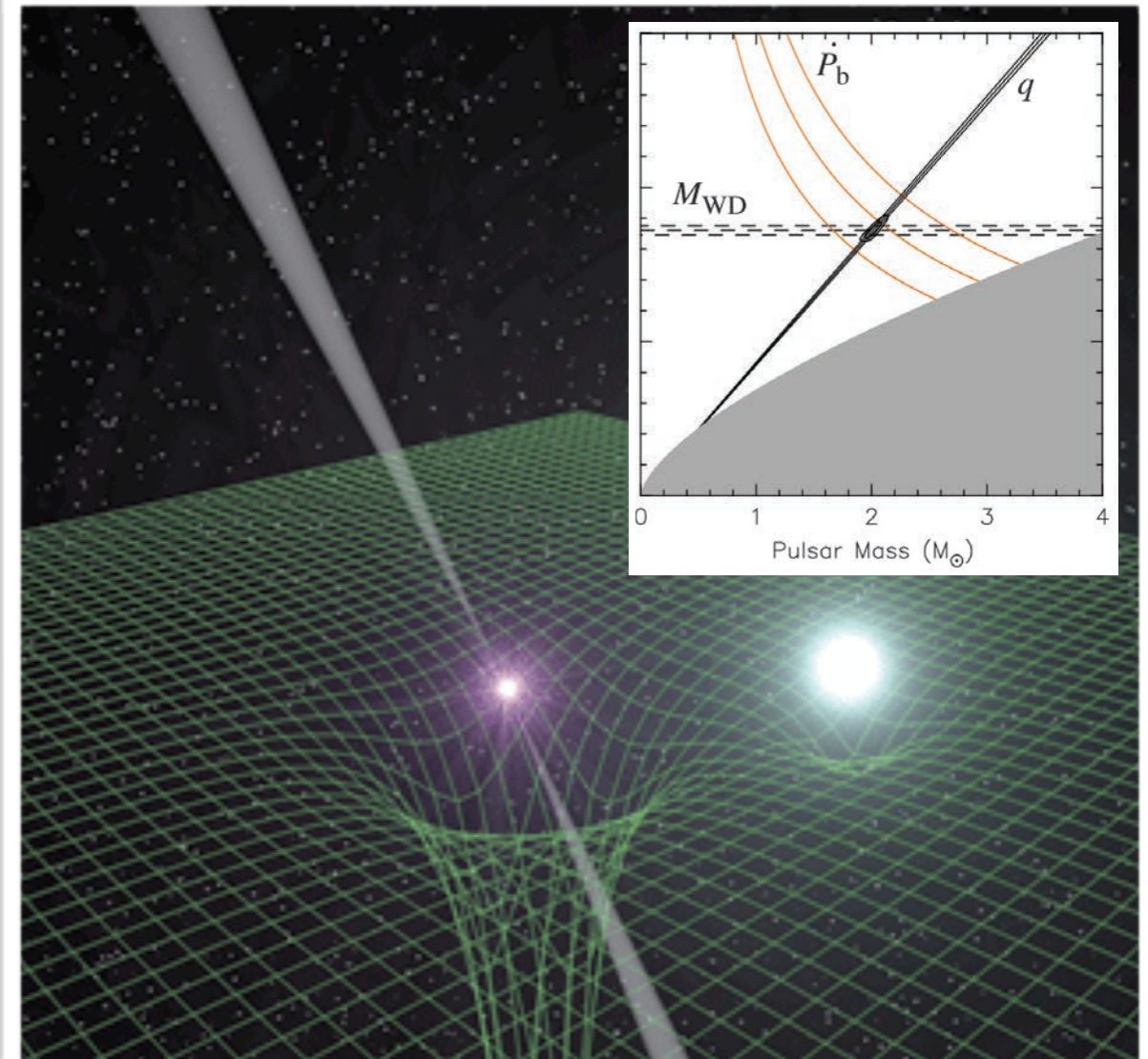
P.B. Demorest et al.
Nature 467 (2010) 1081



PSR J1614+2230

$$M = 1.97 \pm 0.04 M_{\odot}$$

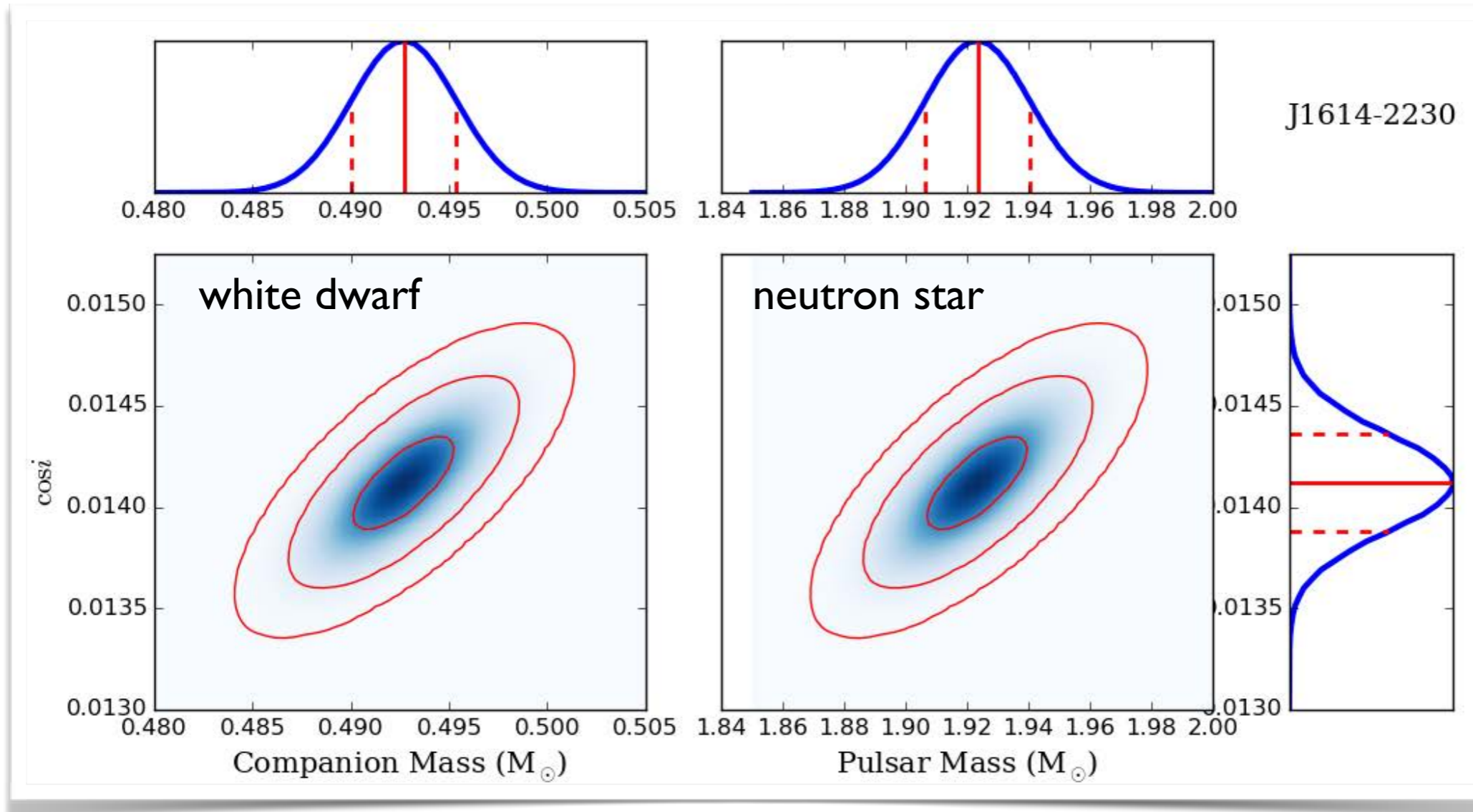
J. Antoniadis et al.
Science 340 (2013) 6131



PSR J0348+0432

$$M = 2.01 \pm 0.04 M_{\odot}$$

Updated mass determination of J1614-2230



$$M = 1.928 \pm 0.017 M_{\odot}$$

E. Fonseca et al., *Astrophys. J.* 832 (2016) 167

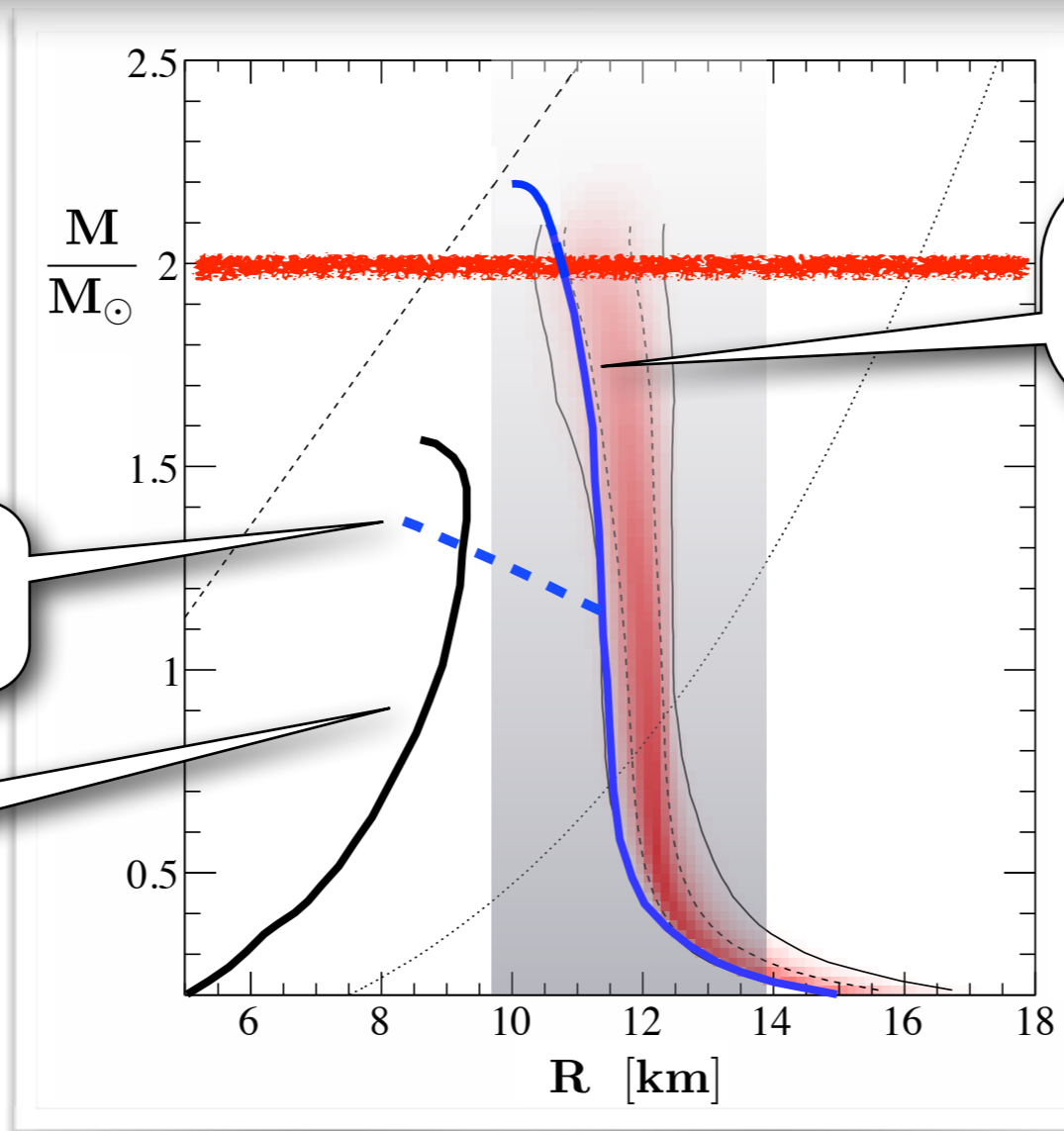
CONSTRAINTS on EQUATION of STATE

- Tolman - Oppenheimer - Volkov Equations

$$\frac{dP}{dr} = -\frac{G}{c^2} \frac{(M + 4\pi Pr^3)(\mathcal{E} + P)}{r(r - GM/c^2)}$$

$$\frac{dM}{dr} = 4\pi r^2 \frac{\mathcal{E}}{c^2}$$

Mass-Radius Relation



kaon
condensate

quark
matter

purely “nuclear” EoS

A.Akmal, V.R. Pandharipande, D.G. Ravenhall
Phys. Rev. C 58 (1998) 1804

K. Hebeler,
J. Lattimer,
Ch. Pethick,
A. Schwenk:
Phys. Rev. Lett.
105 (2010) 161102

A.W. Steiner,
J. Lattimer, E.F. Brown
Astroph. J. 722 (2010) 33

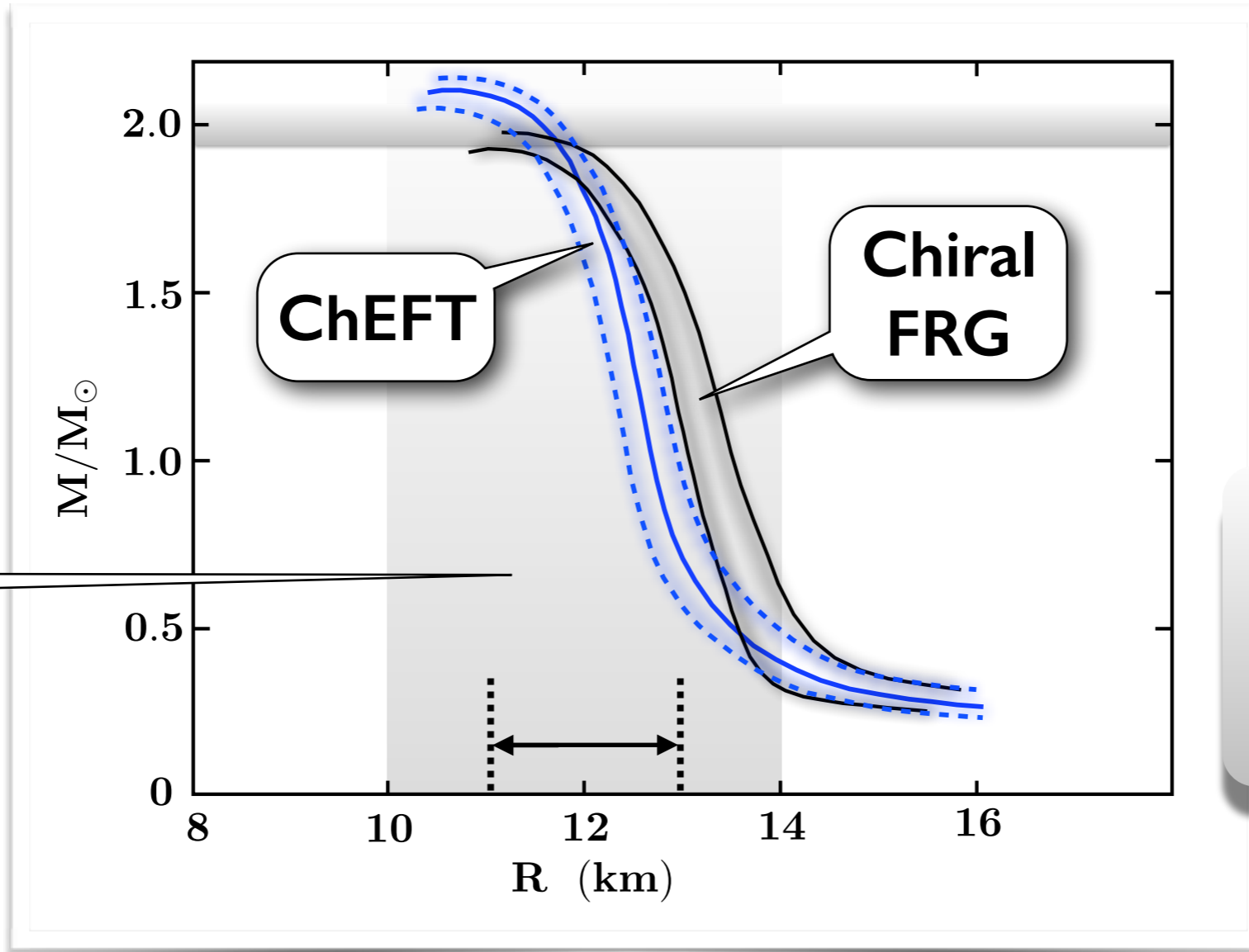
- Stiff equation of state required !

NEUTRON STAR MATTER

from **Chiral EFT** and **FRG**

- Symmetry energy range: 30 - 35 MeV

- Crust: SLy EoS



T. Hell, W.W.
Phys. Rev.
C90 (2014) 045801

M. Drews, W.W.

Phys. Rev.
C91 (2015) 035802

Prog. Part. Nucl. Phys.
93 (2017) 69

- Central core density

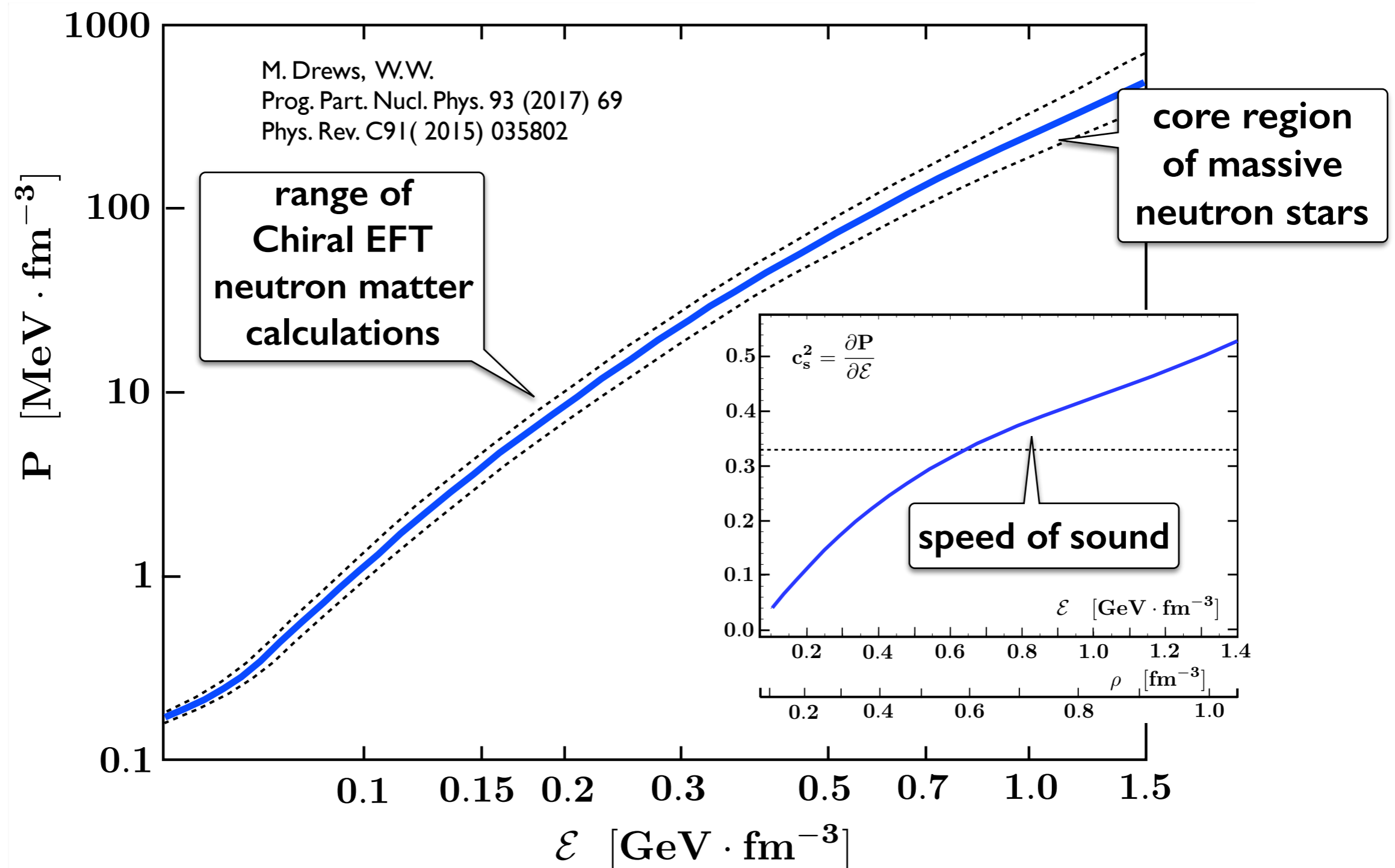
$$\rho_c \lesssim 5 \rho_0$$

- Chiral many-body dynamics using “conventional” (pion & nucleon) degrees of freedom is consistent with neutron star constraints

NEUTRON STAR MATTER

Equation of State

- Chiral **FRG** calculations with inclusion of beta equilibrium

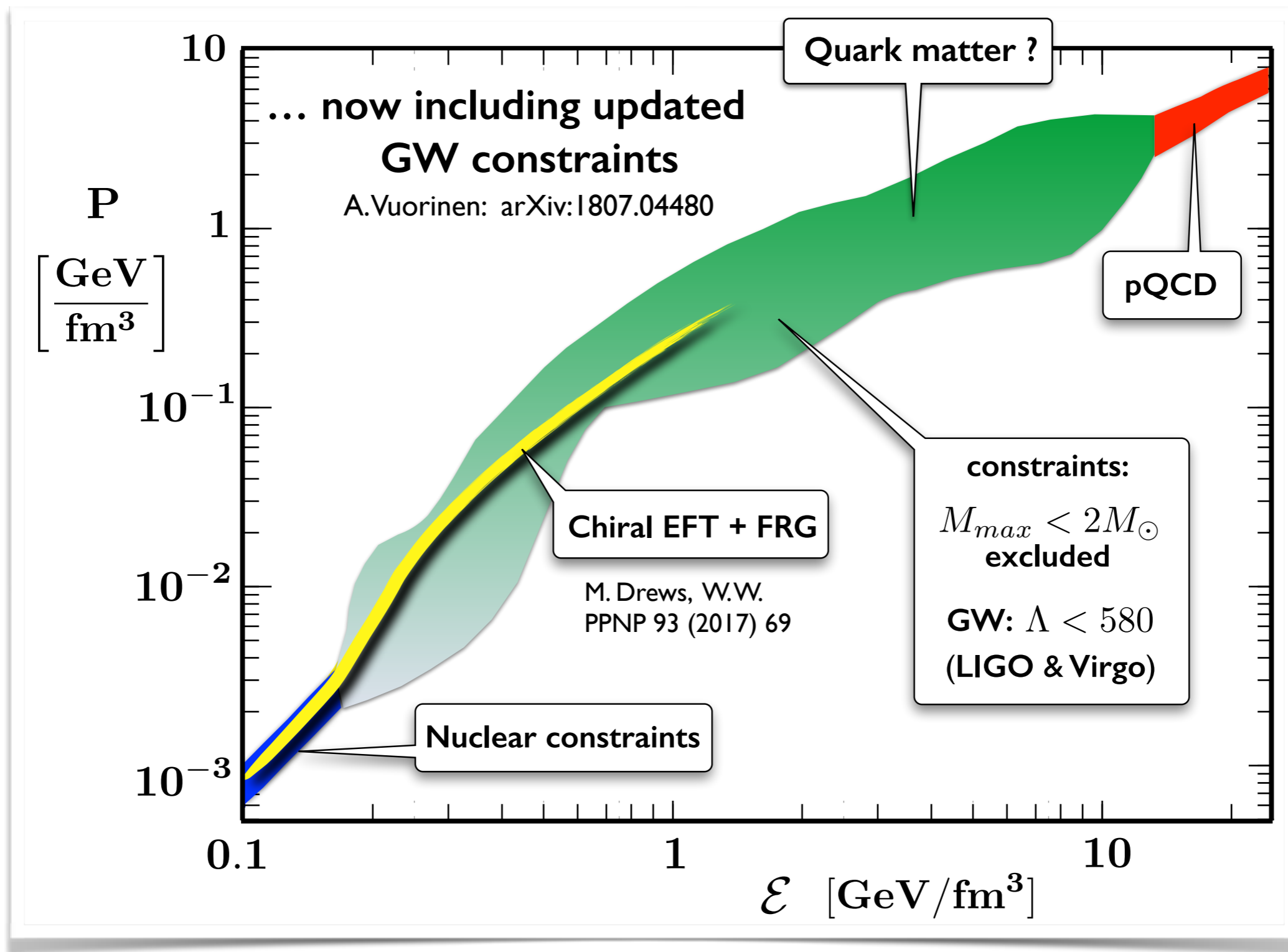


NEUTRON STAR MATTER

Equation of State

A. Kurkela et al.: Astroph. J. 789 (2014) 127

A. Annala et al.: PRL 120 (2018) 172703



SUMMARY

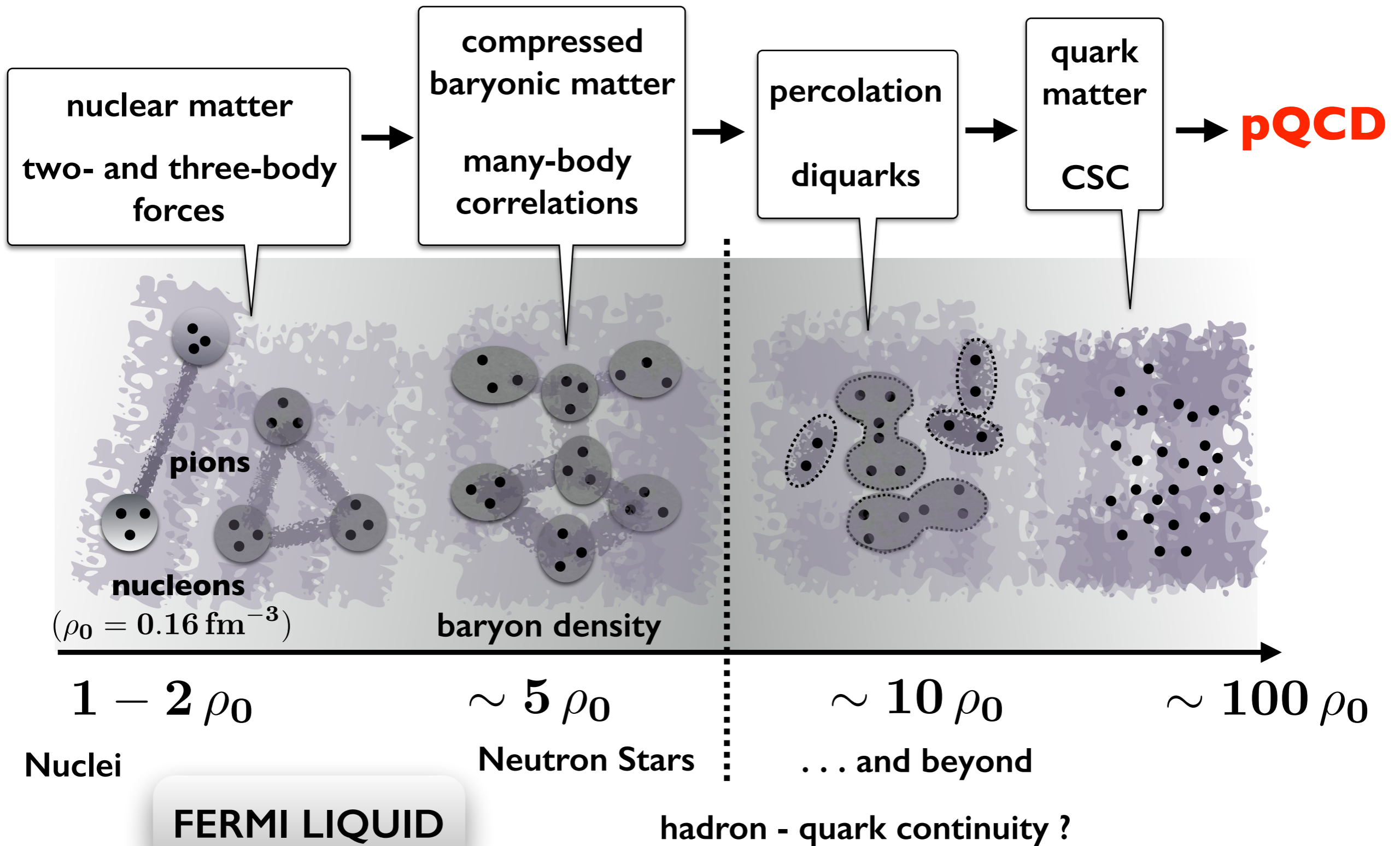
- Systematic framework at the interface of QCD (with light quarks) and physics of hadrons, nuclei and nuclear forces :

Chiral Effective Field Theory
combined with
Functional Renormalization Group

- ChEFT + many-body perturbation theory works for $\rho \lesssim 2 \rho_0$
- ChEFT + (non-perturbative) FRG may work at even higher densities
 - ▶ **No** chiral phase transition in n-matter up to at least $\rho > 5 \rho_0$
 - ▶ “Conventional” (non-exotic) EoS consistent with constraints from neutron stars ($M_{max} \simeq 2 M_{\odot}$, tidal deformability from GW)
 - ▶ Strangeness in the neutron star core ? Hyperon puzzle ?
New developments: hyperon-nuclear interactions from Chiral SU(3) Effective Field Theory



PICTORIAL SUMMARY : COLD BARYONIC MATTER



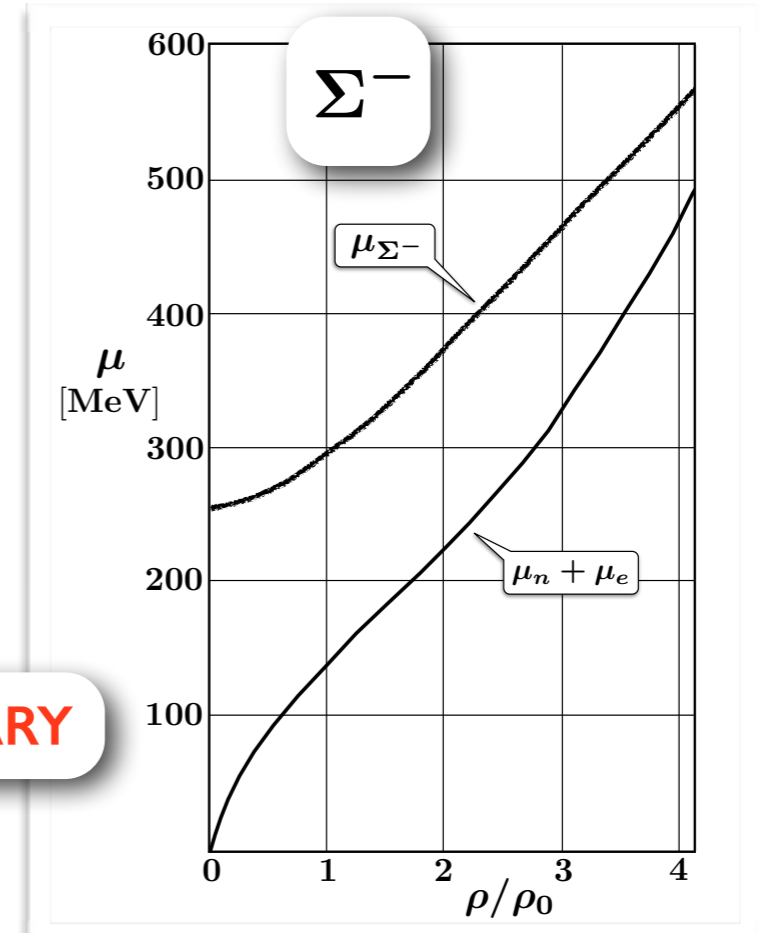
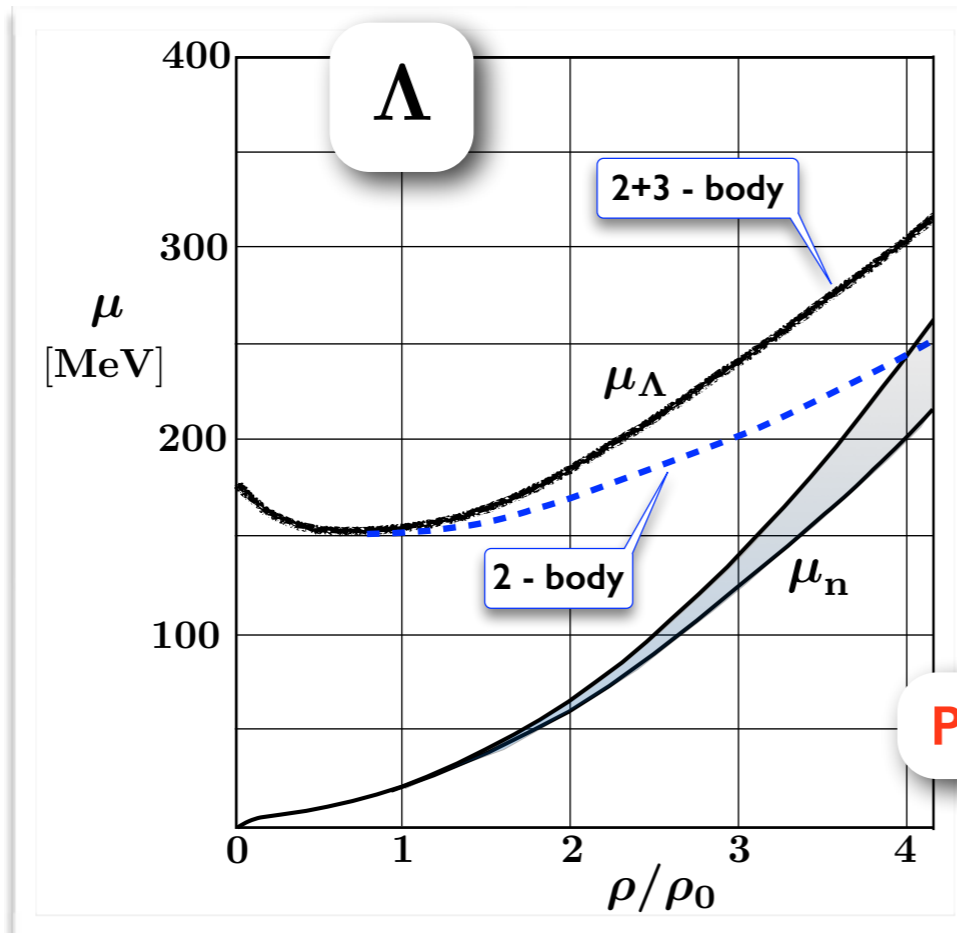
Outlook: Hyperons in Neutron Stars ?

- Onset conditions for appearance of hyperons in neutron stars :

Equalities for chemical potentials $\mu_i = \frac{\partial \mathcal{E}}{\partial \rho_i}$

$$\mu_{\Lambda} = \mu_n$$

$$\mu_{\Sigma^-} = \mu_n + \mu_e = 2\mu_n - \mu_p$$



- Extrapolations using hyperon single particle potentials in neutron matter from Chiral SU(3) EFT interactions

- Extensive and more detailed calculations in progress (D. Gerstung, N. Kaiser, W.W.)