

# Novel beam injection optimization

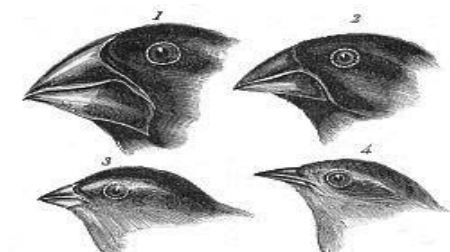
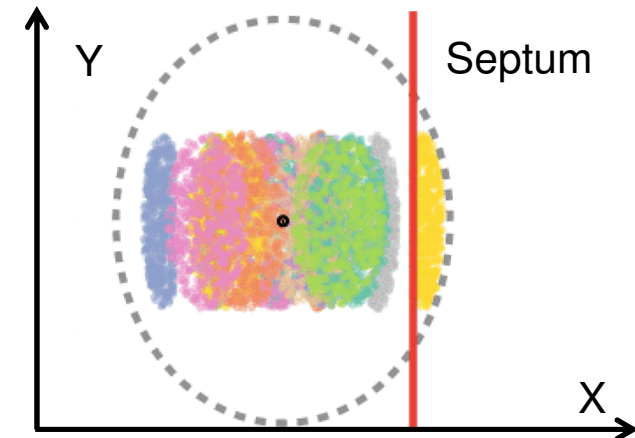
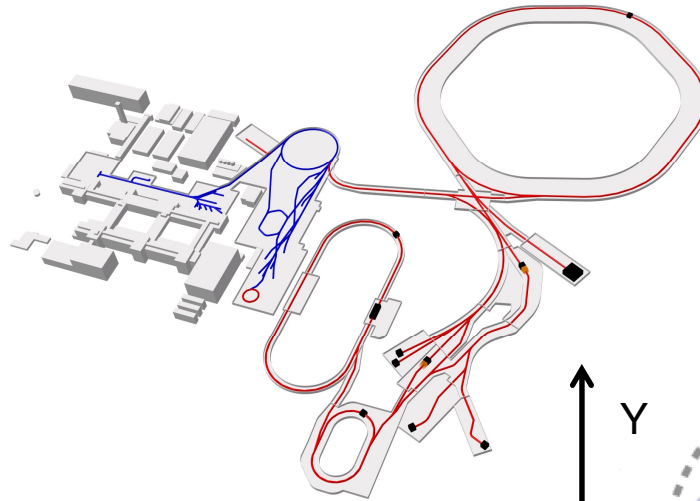
Dr. Sabrina Appel, Accelerator Physics Department, GSI, Darmstadt

- **Multi-Turn Injection**

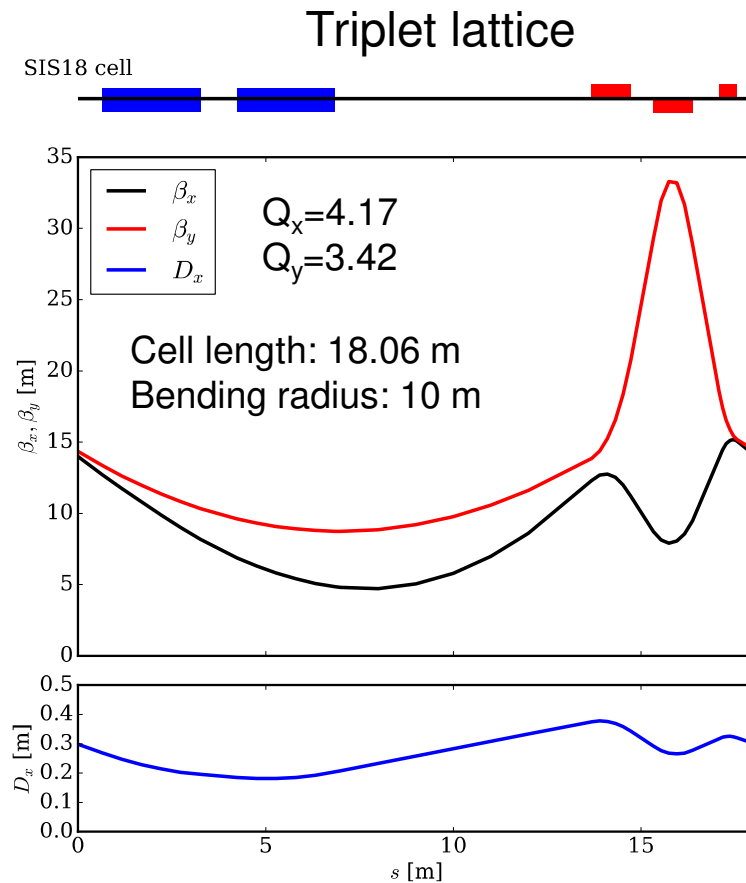
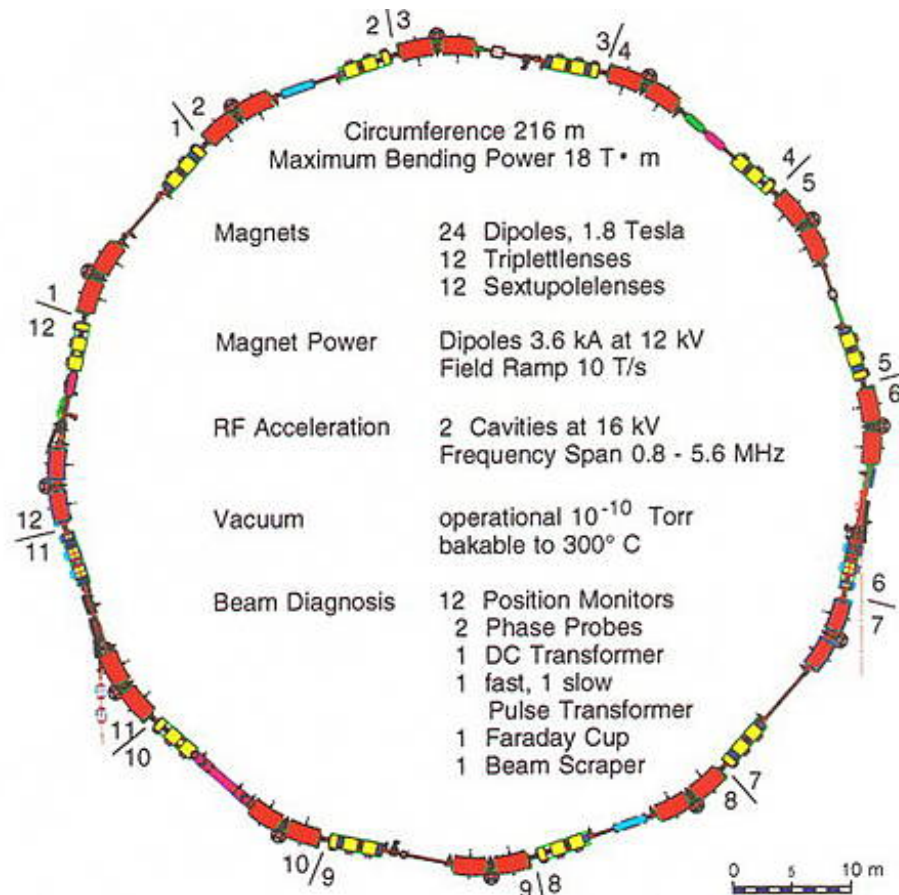
- SIS18
- Intensity limitation

- **Optimization**

- Algorithms
  - Genetic Algorithms
  - Particle swarm algorithms
- Technical solution
  - EMTEX
  - Skew quadrupoles

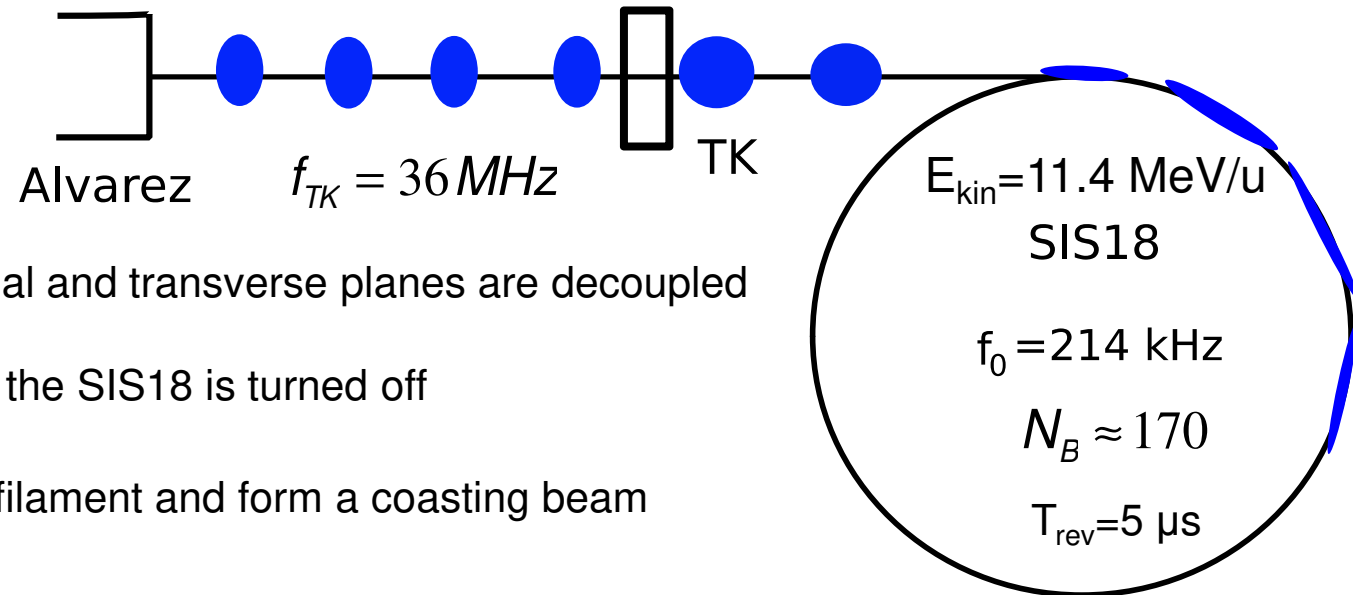






On the ramp a dynamic change-over from triplet to doublet focusing is foreseen  
 Doublet focusing → less quad strength → easier beam extraction and chromaticity correction

# Overview injection into SIS18



We assume that the longitudinal and transverse planes are decoupled

During MTI injection the RF in the SIS18 is turned off

The micro-bunches debunch, filament and form a coasting beam within a few turns

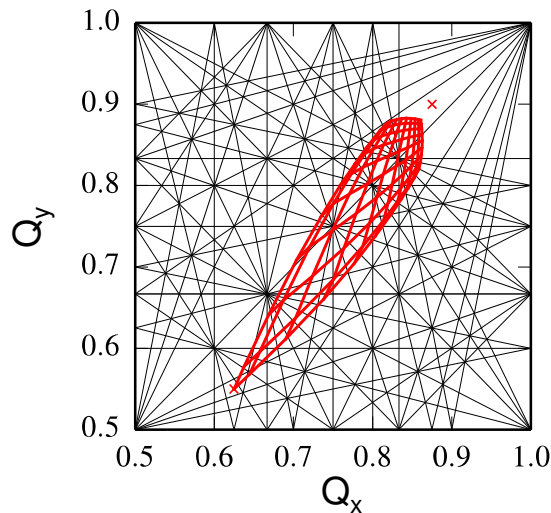
Final full momentum spread after injection should be within the rf bucket area

$$\Delta p / p \leq 10^{-3} \quad (\text{equivalent parabolic distribution})$$

Transverse beam size (4 rms physical emittance) should be within the machine acceptance

$$\epsilon_x = 150 \text{ mm mrad} \quad \epsilon_y = 50 \text{ mm mrad} \quad (\text{equivalent K-V distribution})$$

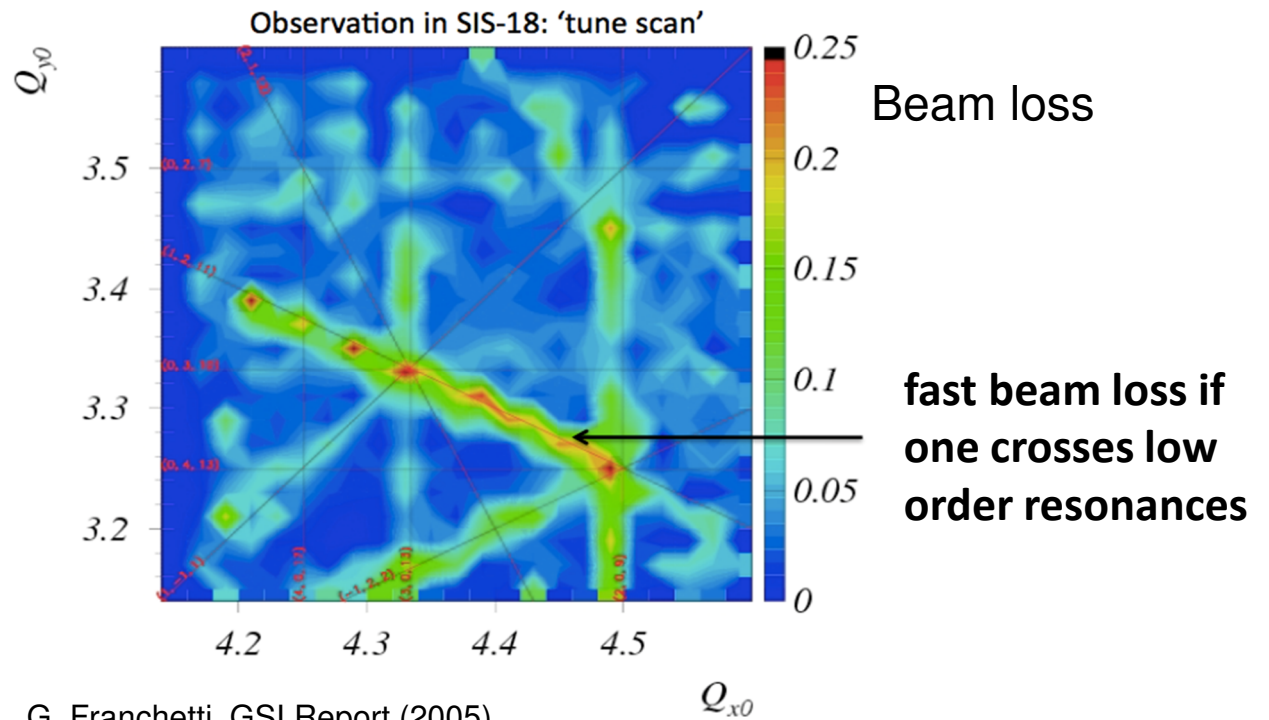
# Intensity limit: Space charge



The (incoherent) transverse space charge force is the main intensity limiting effect in the FAIR synchrotrons

Tune shift: 
$$\Delta Q_y^{sc} \propto -\frac{q^2}{m} \frac{N}{B_f} \frac{4}{\epsilon \beta_0^2 \gamma_0^3}$$

Intensity limit: 
$$|\Delta Q^{sc}| \lesssim 0.1 - 0.5$$



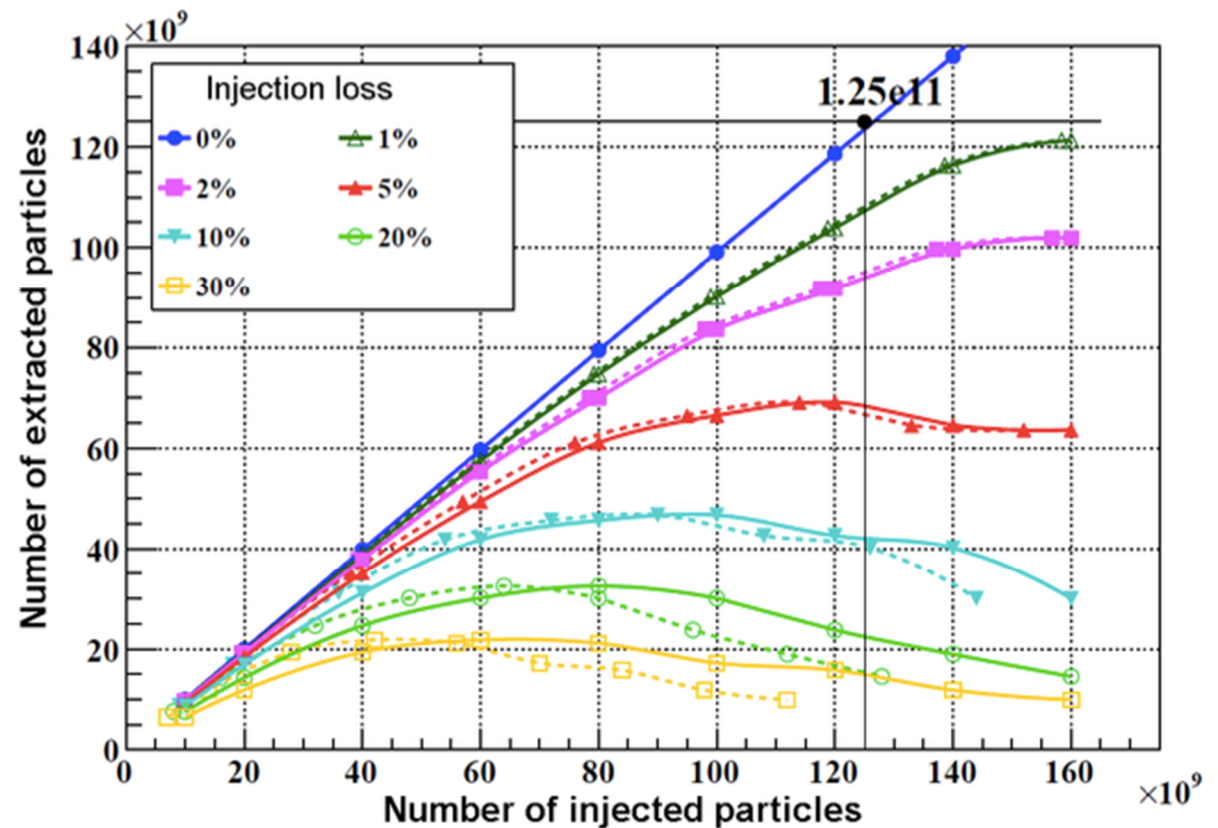
G. Franchetti, GSI Report (2005)

# Intensity limit: Dynamic vacuum

For intermediate charge state ions, the loss-induced vacuum degradation is another important key intensity-limiting factor.

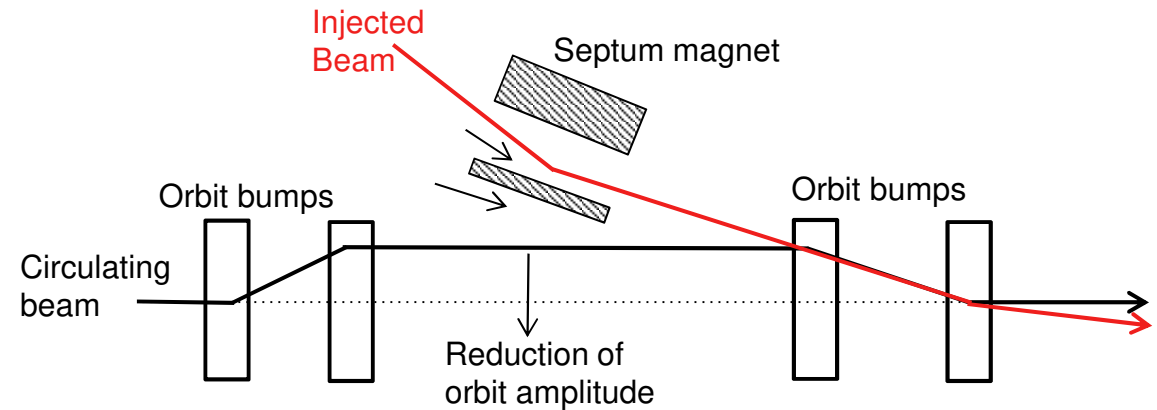
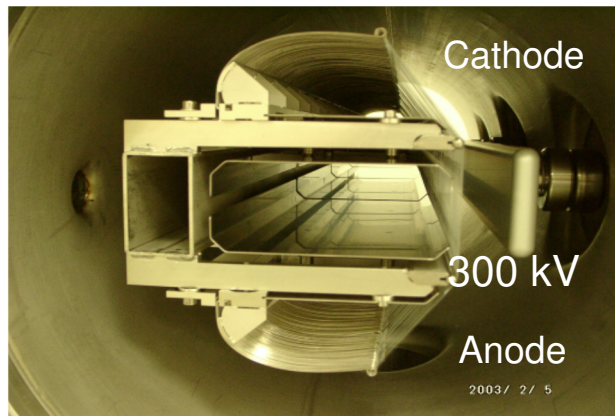
Results of STRAHLSIM simulations for the desired SIS18 booster operation with different (uncontrolled) initial beam loss.

P. Spiller {SIS18} upgrade: Status, Present and Expected Performance Low Charge State Heavy Ion Beams. MAC, (2013)



# Multi-turn injection (MTI) into SIS18

SIS18 electrostatic injection septum

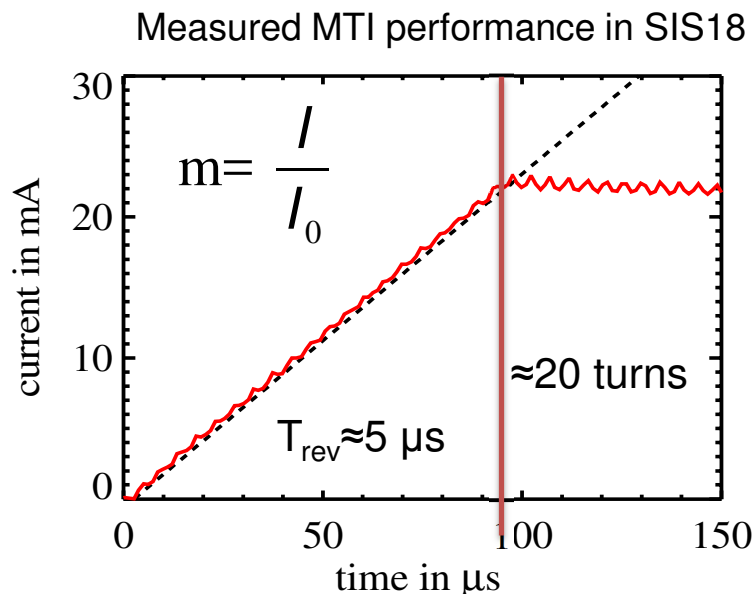


SIS18 **flexibility** in providing a broad range of ions allow only **Liouvillian injection** schemes

MTI has to respect Liouville's theorem:  
Injected beams only in free space

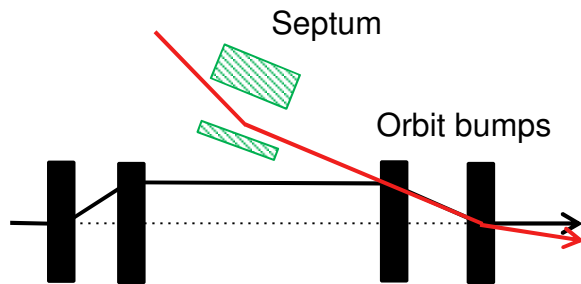
The beam from linac is injected until machine acceptance is reached and maximize intensity

**Loss** at septum and acceptance should be as **low** as possible due to loss induced dynamic vacuum





# Overview injection into SIS18

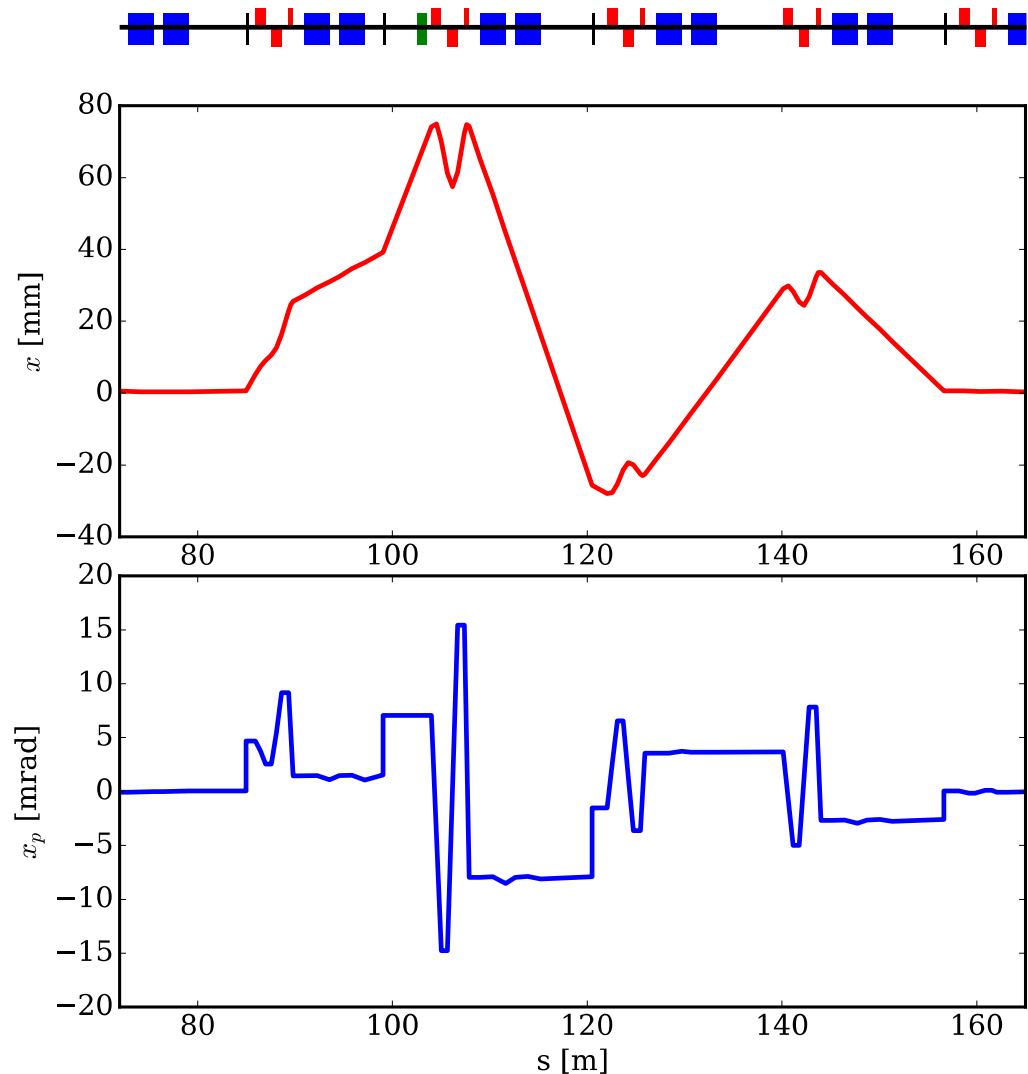


No distortion outside injection region

Degrees of freedom position and angle of closed orbit at septum

An analytical solution is known  
See: C.J. Gardner, Booster  
technical note no. 197, 1991

SEC11-SEC03



MTI has to respect Liouville's theorem:  
Injected beams only in free space

Loss of ions at the septum due to the betatron oscillation

Loss minimization at septum

$$Q_x \neq \text{integer}$$

Injected beam into upright ellipses

$$\frac{\alpha_0}{\beta_0} = -x'/x$$

Mismatch of lattice function to  
adapt to ring curvature

$$\frac{\beta_0}{\beta_i} = \left(\frac{\epsilon}{\epsilon_i}\right)^{\frac{1}{3}}$$

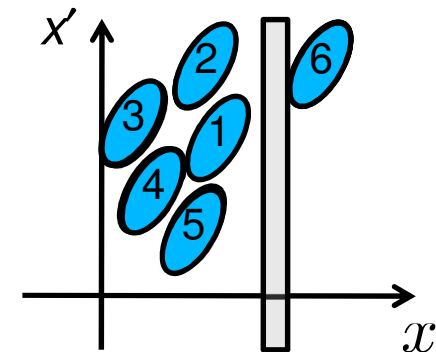
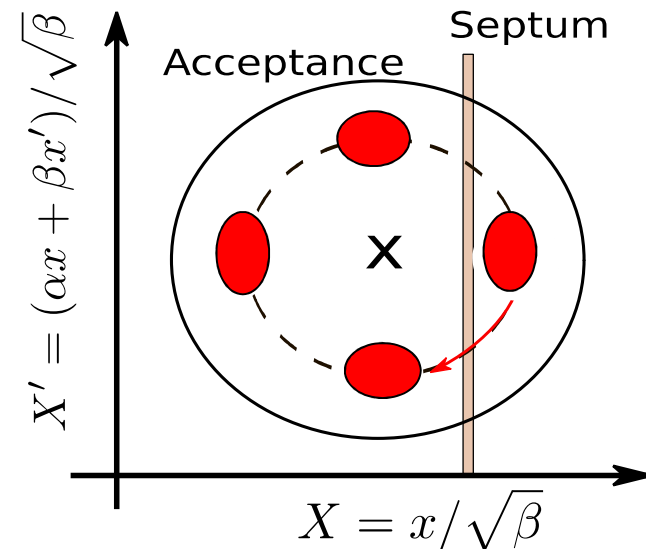
Linear orbit bump reduction

$$\Delta x = \frac{1}{4}(2a + d_c)$$

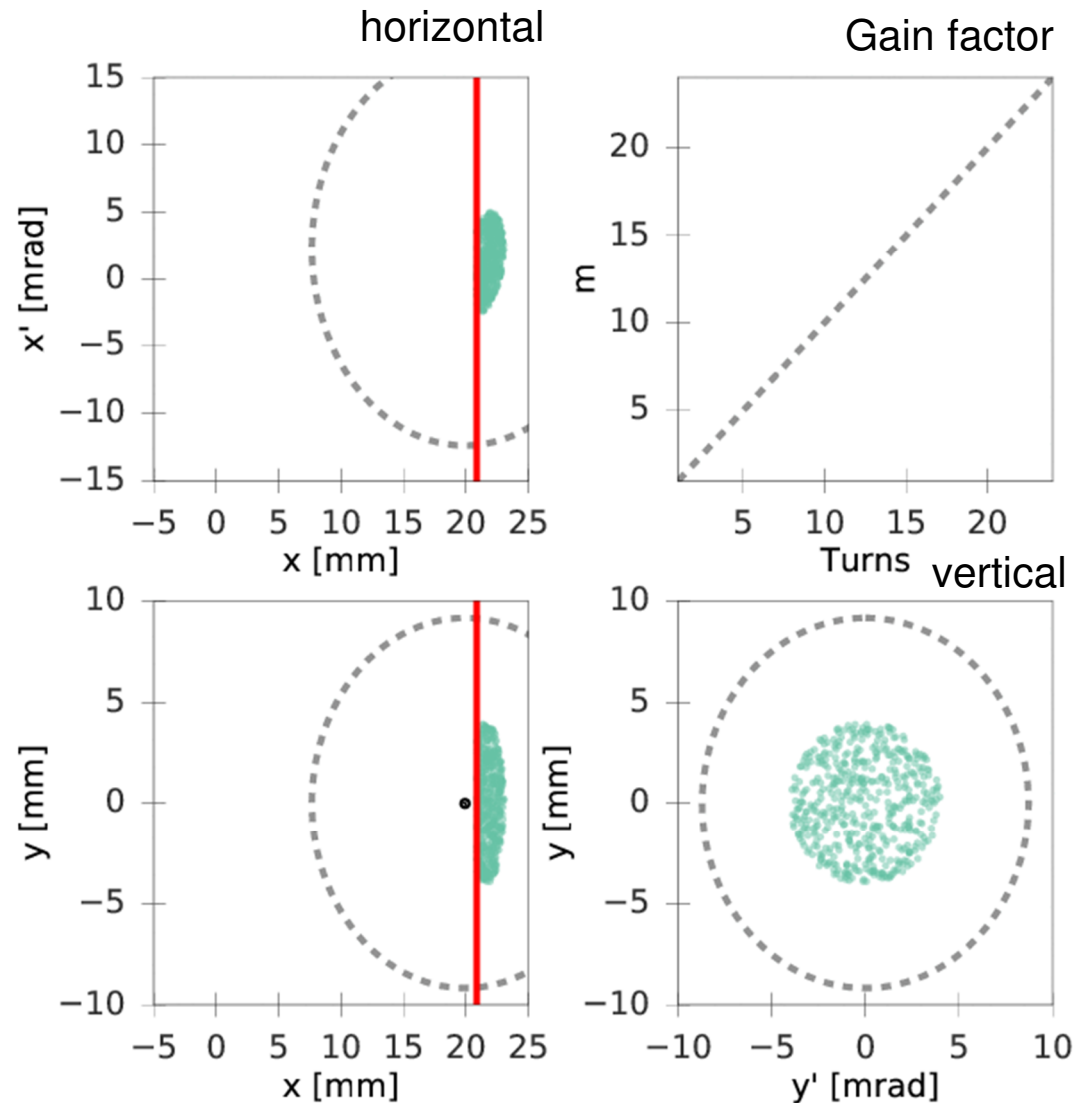
Imagined best optimum injection  
scheme has the smallest dilation and  
the lowest loss at the septum.

→ Contradicting

Betatron oscillation and  
orbit bump reduction  
→ free phase space



# Multi-turn injection into SIS: Movie



----- Acceptance

— Septum

Normalized coordinates

15 turns injection  
with 15% loss

## Multi-objectives:

- stacked current (maximize)
- beam loss (minimize)
- emittance

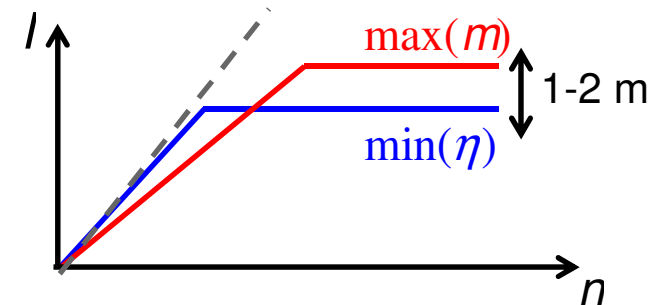
$$I = mI_0$$

$$\eta = \frac{I_{\text{loss}}}{nI_0}$$

$$\epsilon_x$$

output

$$m = (1 - \eta)n$$



## Constraints:

- Position of septum  $x_s$
- Machine acceptance  $A$
- Closed orbit (bumper kick)  $\phi_i(Q_x)$

Model in  
simulation code

## Parameters:

- Position of incoming beam at septum
- Initial bump amplitude and its decreasing
- Injected turns
- Horizontal tune
- Horizontal emittance
- Skew strengths

$$x_c, x'_c, M$$

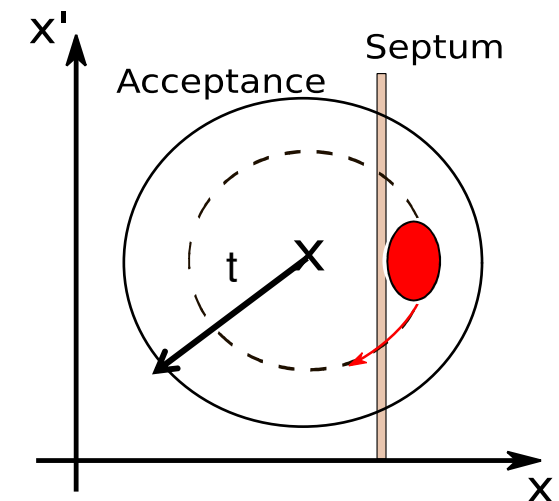
$$x_0, x'_0, \tau$$

$$n$$

$$Q_x$$

$$\epsilon_x$$

$$k$$



# Multi-turn injection into SIS: Optimization problem

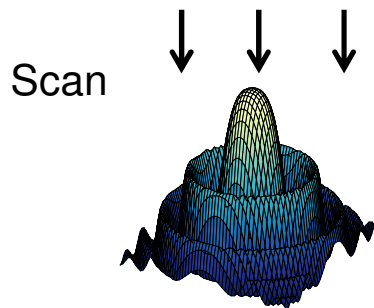
The analytical description characterizes:  
Incoming beam position and this mismatch

Loss minimization at septum: tune  
Linear orbit bump reduction: tune + size

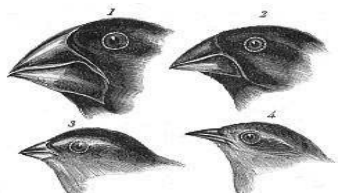


Unfortunately the MTI model is underrepresented:  
A few variables can be chosen freely from a value range

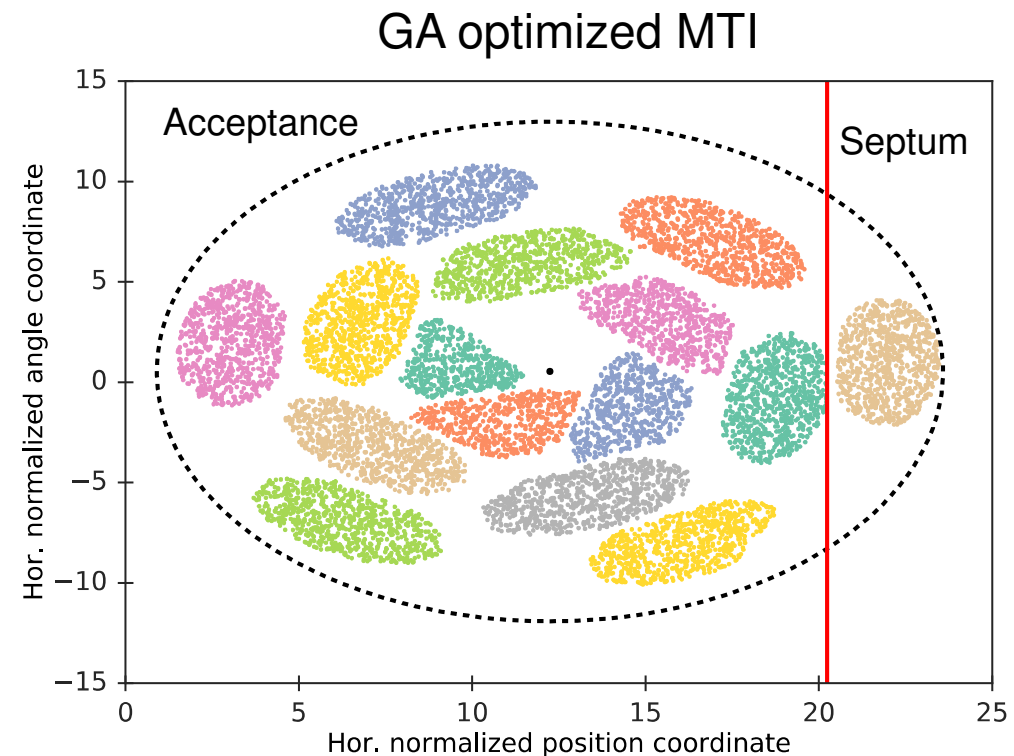
Discover by trial and error optimum  
settings or perform parameter scans



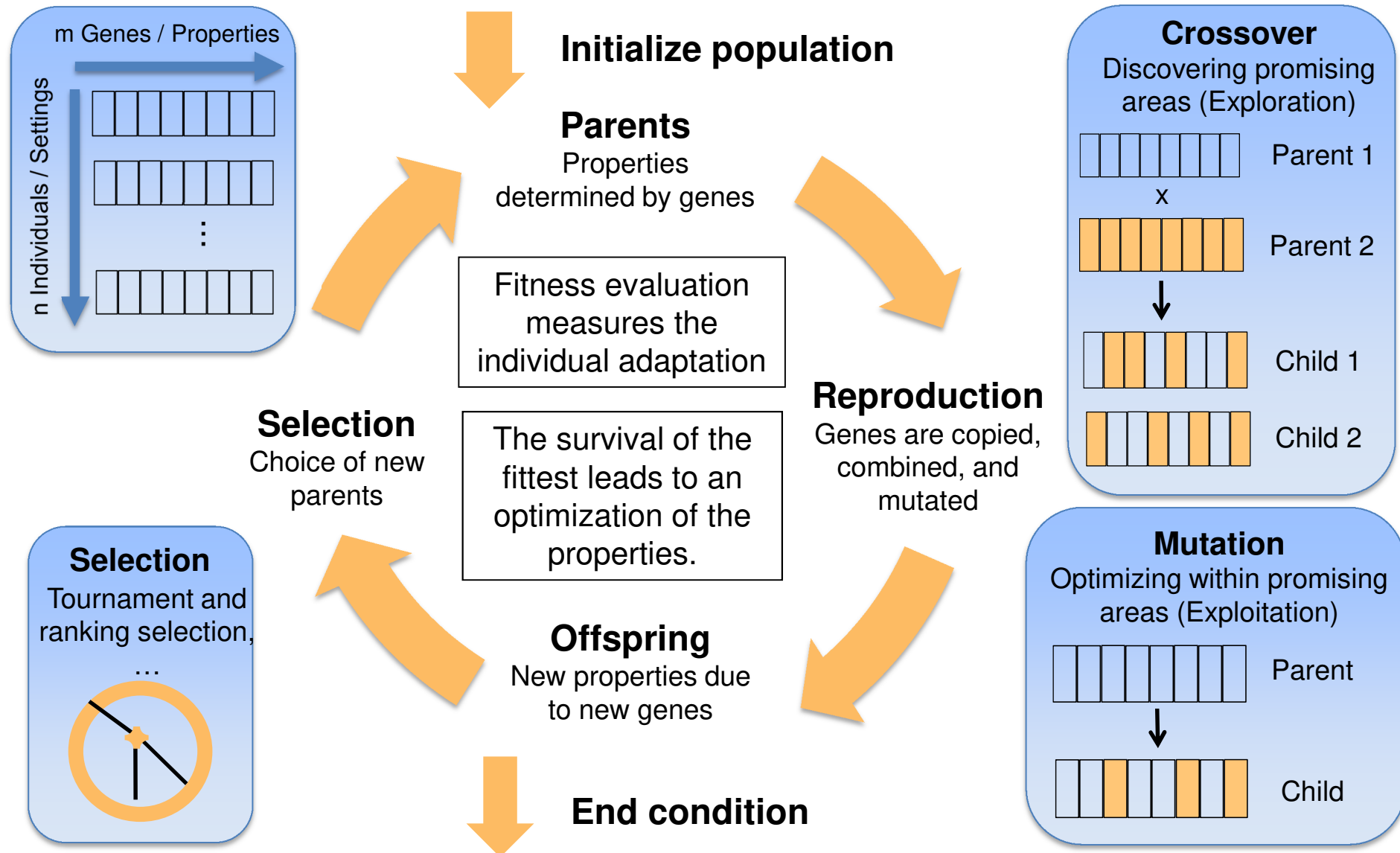
New approach is the use of genetic  
algorithms (GA) and particle swarm (PA)



Darwin Finches  
J. Gould,  
Voyage of the  
Beagle







Inspiration from the “graceful but unpredictable choreography of a bird flock”

## Position

$$x_i(t + 1) = x_i(t) + v_i(t + 1)$$

## Velocity update

$$v_i(t + 1) = wv_i(t) + r_1C_1(P_i^l - x_i) + r_2C_2(P^g - x_i)$$

$x_i$  Each individual particle position refers to a point in the variable space

$w$  Inertia weight reflects effect of particle current motion

$P_i^l$  Personal best; analogous to “nostalgia”

$C_1$  Cognitive parameter is contribution of particle personal experience

$P^g$  Global best is the best position ever for entire swarm

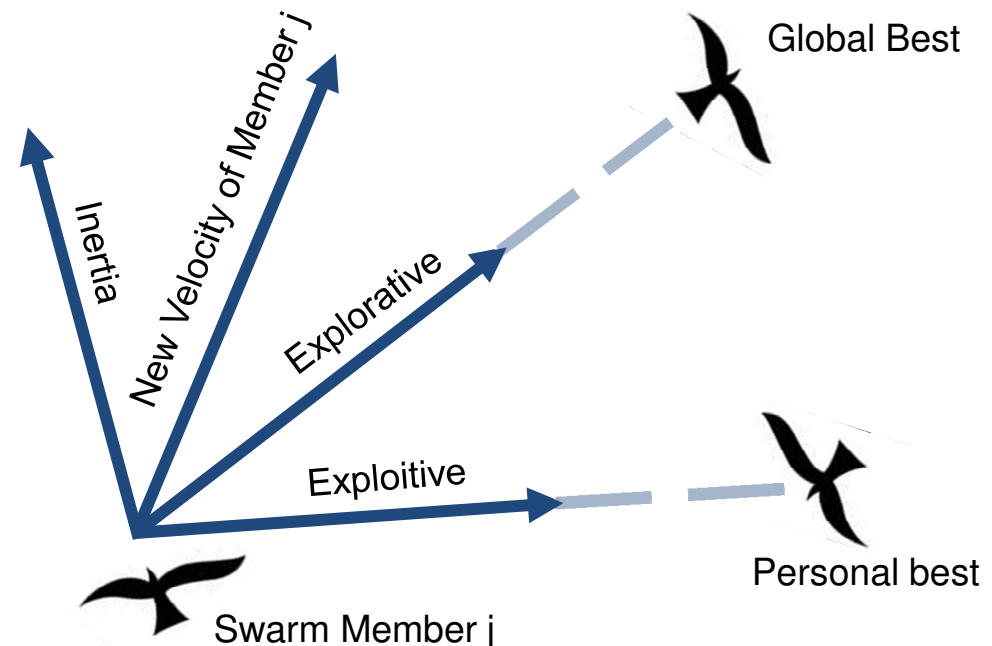
$C_2$  Social parameter reflects publicized knowledge or social norms

$r_1, r_2$  Stochastic elements of the algorithm

Inertia

Local search

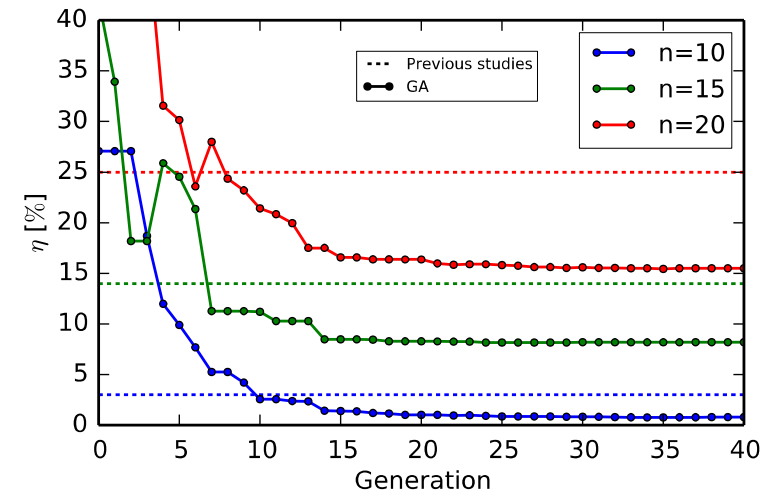
Global search



## Optimization of loss

Genetic algorithms can improve MTI

Especially for **longer** injection GA discovers a much **better** solution

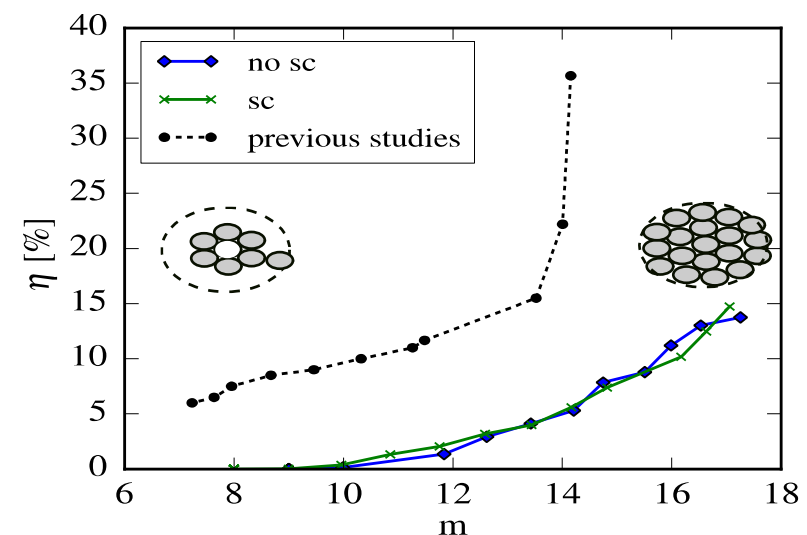


## Optimization of loss and gain factor

Dependence of gain factor on loss

Loss-free injection could be found

**Space charge** results in a **similar PA front**, but with different injection settings

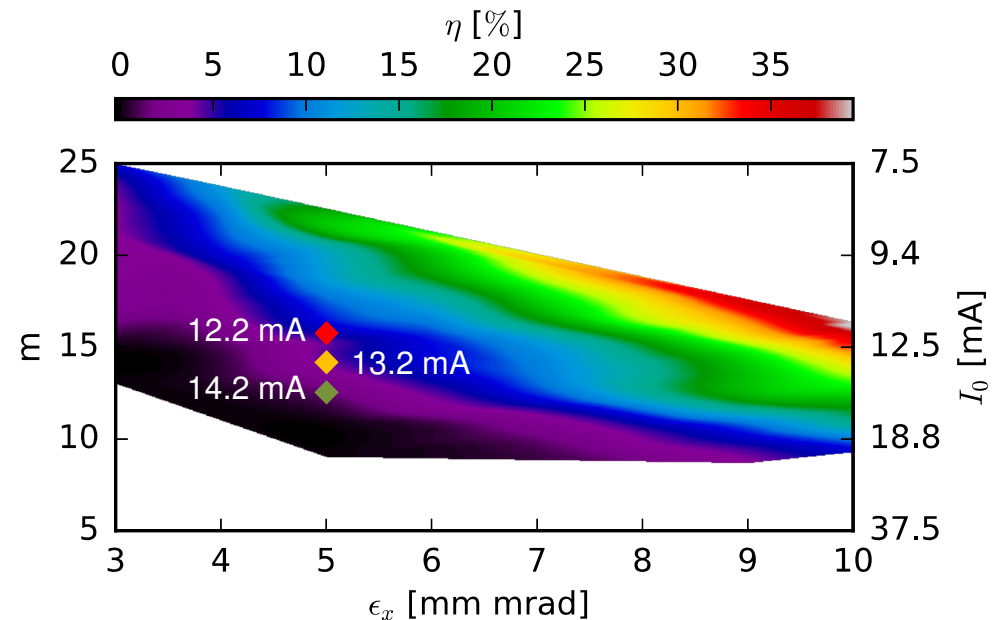


## Optimization of loss, gain factor and beam emittance (injector)

Dependence of interface parameter

$$B = \frac{I}{\varepsilon} \quad m(\eta) = \frac{N}{I} q f_0$$

allows to define a frame, in which the required beam parameter can be  
**matched at best for a high performance**



This crucial information gives more flexibility for the injector upgrade layout.

New Alvarez DTL provide requirement beam brilliance (including errors)

S. Appel et al: Nucl. Instrum. Methods A 852 (2017), pp. 73-79

A. Rubin, Beam dynamics design of the new FAIR post-stripper linac,  
GSI Accelerator Seminar, 14.05.17

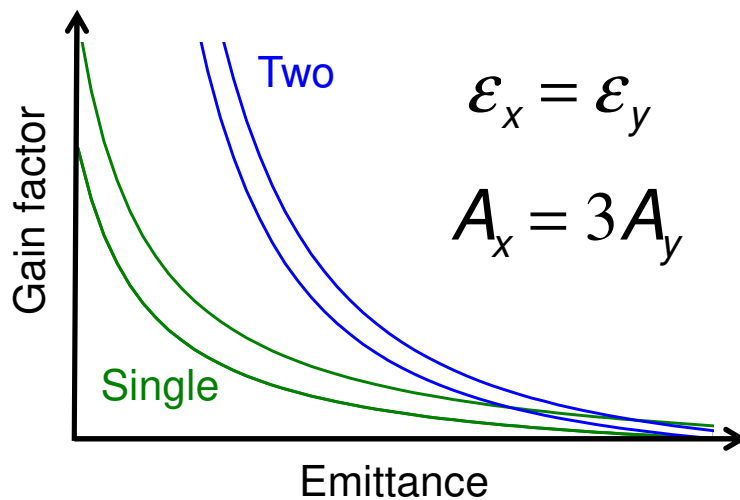
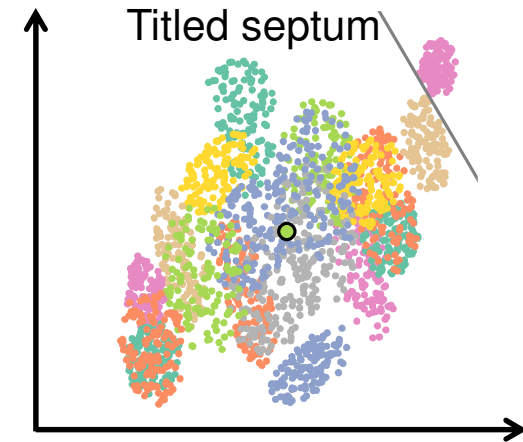
# Multi-turn injection

Smaller beam emittance increase MTI performance

Available acceptance limited MTI performance

Besides the horizontal phase space, the vertical one can also be exploited, which can lead to higher gain factors

➤ Titled septum or skew quadrupoles



Single plane:  $m = \frac{A}{d\epsilon} \quad d \approx 1.5 - 2$

Two plane:  $m = \frac{A_x A_y}{d\epsilon_x \epsilon_y} \quad d \approx 8 - 10$

G.H. Rees in Handbook of accelerator physics and engineering



# Multi-turn injection (Two plane)

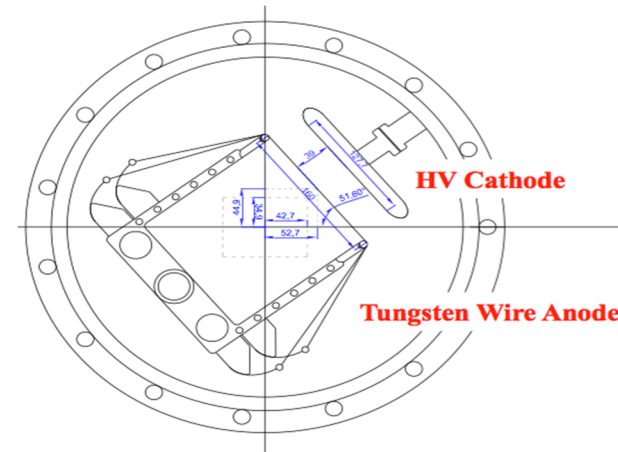
## Titled septum

Need **new technical development**

Titled septum and magnets in transfer line

Coordinate rotation system

Four additional bumpers (vertical)



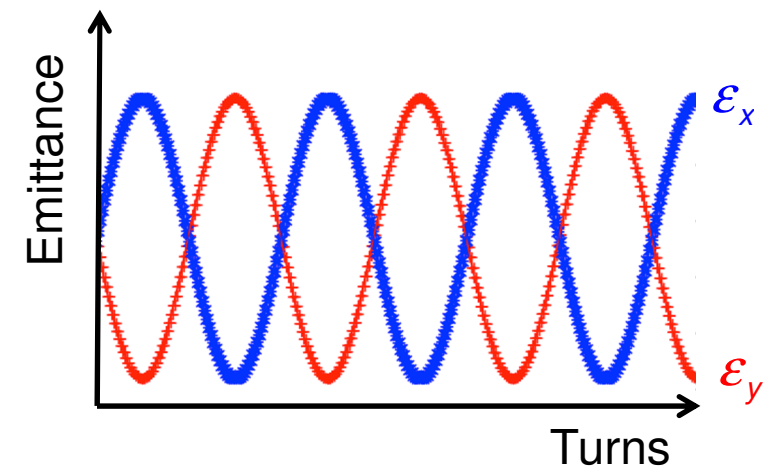
BRing of  
HIARF  
project

## Skew quadrupoles

Using **installed** skew quadrupoles

Linear coupling of hor. and ver. phase space

Skew strength should be swift off after injection

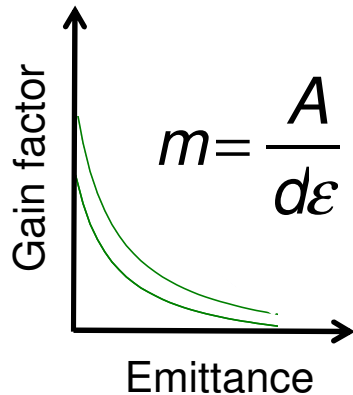


Which gain factors can be reached for a given beam emittance and loss for SIS18?

For conventional, skew and titled septum injection?

# Injector brilliance depending

## Emittance Transfer EXperiment (EMTEX)



One consequence of single-plane MTI is that the **required** horizontal injection **emittance** is very **demanding**; to the **other plane not**.

**Re-partitioning** of the injected beam emittances: round-to-flat transformation would **increase** the injection efficiency

Repartition with constant emittance product:  
Effective solenoid exit fringe field + skewed quadrupole triplet

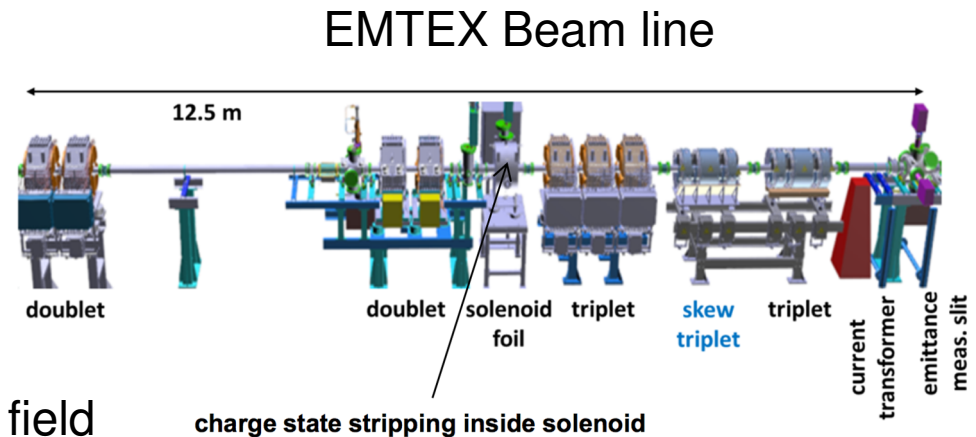
Twiss-parameters are preserved

Beam flatness amount is controlled by solenoid field

The effective solenoid exit fringe field is created by changing the ion charge state

L. Groening: Phys. Rev. ST Accel. Beams 14 064201 (2011)  
C. Xiao et al: Phys. Rev. ST Accel. Beams 16 044201 (2013)

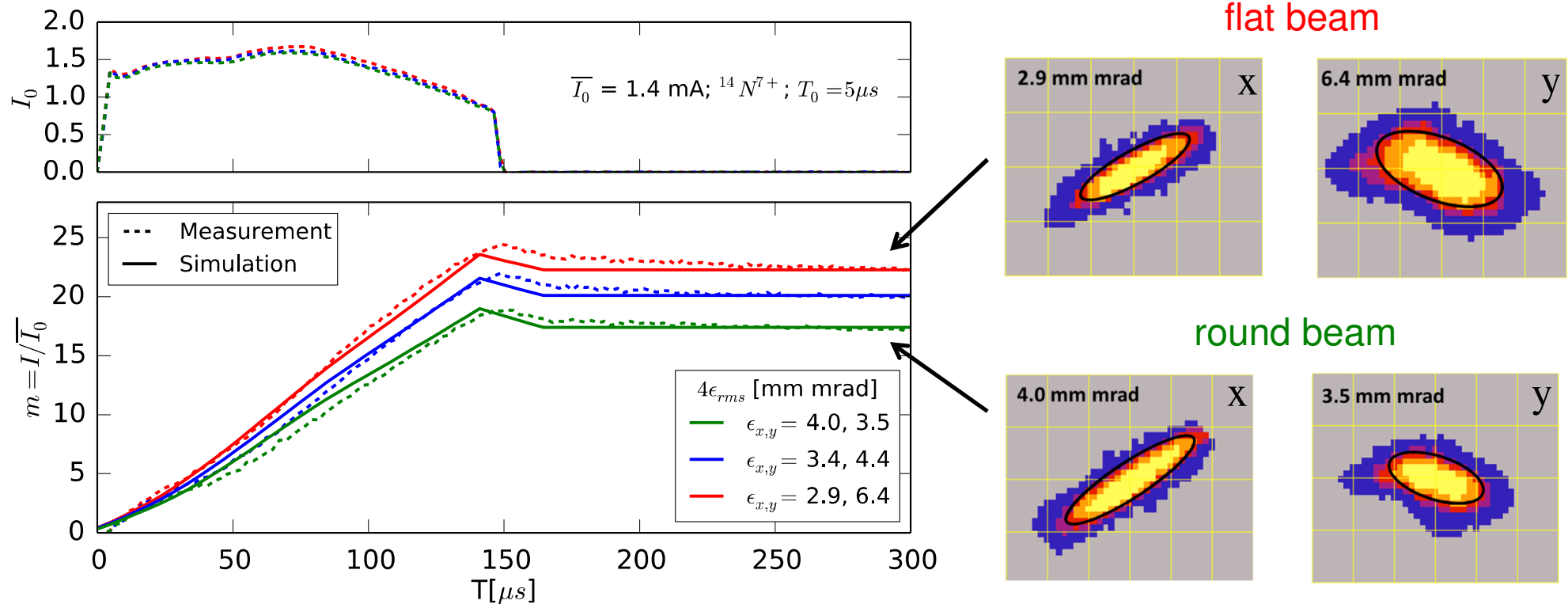
L. Groening et al: Phys. Rev. Lett. 113 264802 (2014)  
S. Appel et al: Nucl. Instrum. Methods A 866 (2017), pp. 36-39



# Injector brilliance depending

## EMittance Transfer EXperiment (EMTEX)

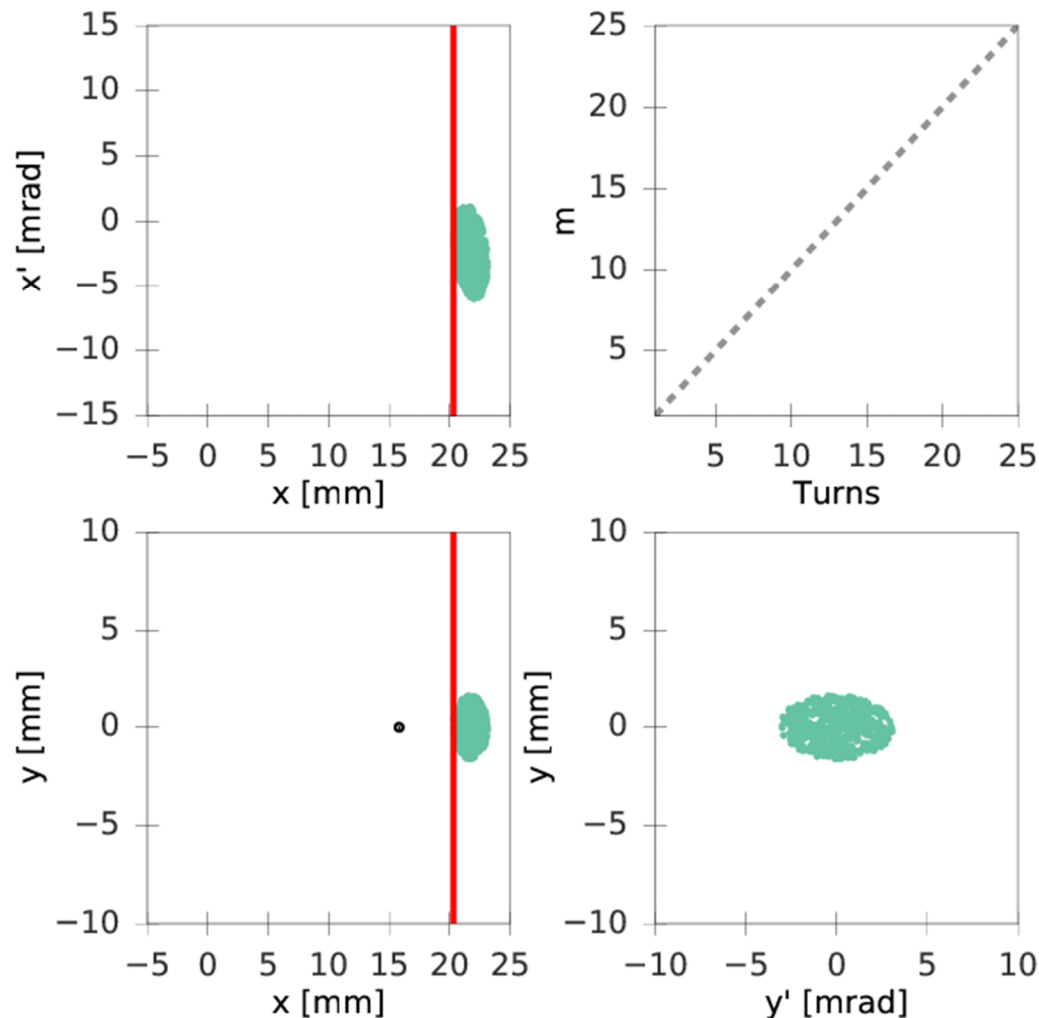
MTI performance has been measured as a function of the amount of beam flatness



**Excellent** agreement between simulation and measured injection performance was achieved thanks to fast adjustment of the beam flatness without changing other beam parameters.

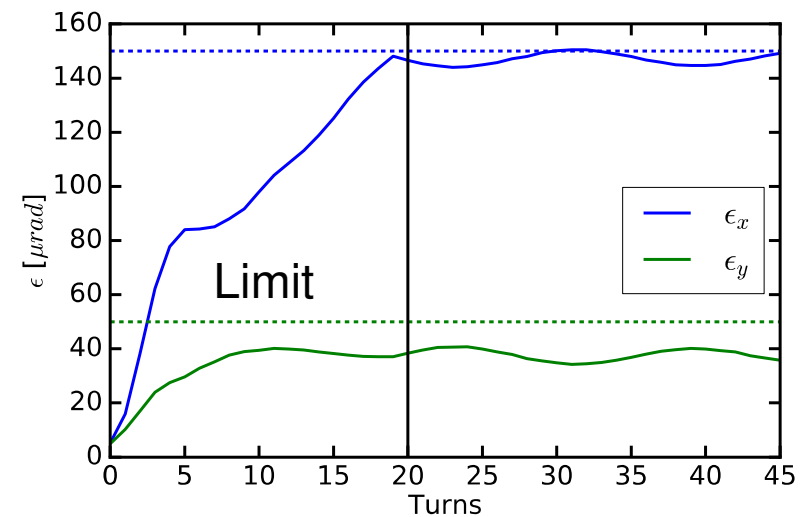
# Multi-turn injection with skew quadrupoles

With linear coupling the injection loss could reduce from **15% to 1-5%** for  $n = 20$



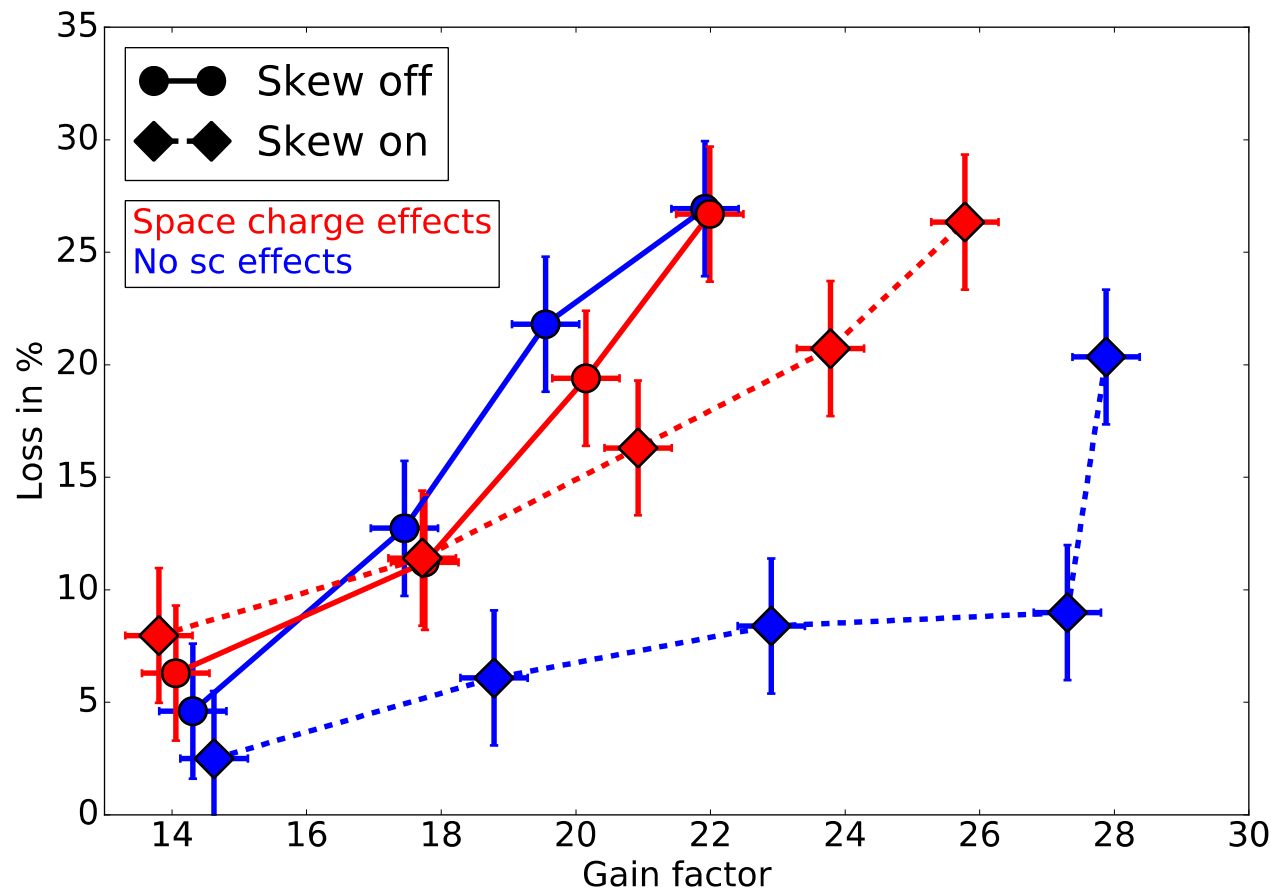
Coupling parameters:  $Q_x: 4.17, Q_y: 3.22,$   
 $k: 0.0141/m, \delta: -0.05$

## Emittance development



# Multi-turn injection with skew quadrupoles

The injection performance can **increase** with linear coupling  
Unfortunately, space charge effects **lower** the beneficial effect





## Evolutionary Optimization

- ✓ MTI setting for a loss-free or low-loss injection were identified
- ✓ Range of optimum brilliances for all ions species can be defined (shown for  $U^{28+}$ )
- Online optimization of MTI (GA, PSA or derivative-free algorithm)

## EMTEX

- ✓ Injection optimization through generation of flat ion beams
- Application for intense beams (e.g.  $U^{28+}$ )

## Two plane MTI

- Skew
  - ✓ The injection performance can increase with linear coupling
    - Unfortunately, space charge effects lower the beneficial effect
- Corner septum

**Thank you for your attention**