

# Study of antiproton-proton annihilation reaction and experimental contribution to hadron polarimetry



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angular distribution of pion,

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Introduction

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Comparison of figure of merit for np zero  
exchange and charge exchange reactions

Polarized protons and neutrons: measure  
analyzing powers up to 4.2 GeV/c  
on C, CH, CH<sub>2</sub> targets

Preliminary Results

Summary

# PART I

$$\bar{p}p \rightarrow \pi^- \pi^+$$

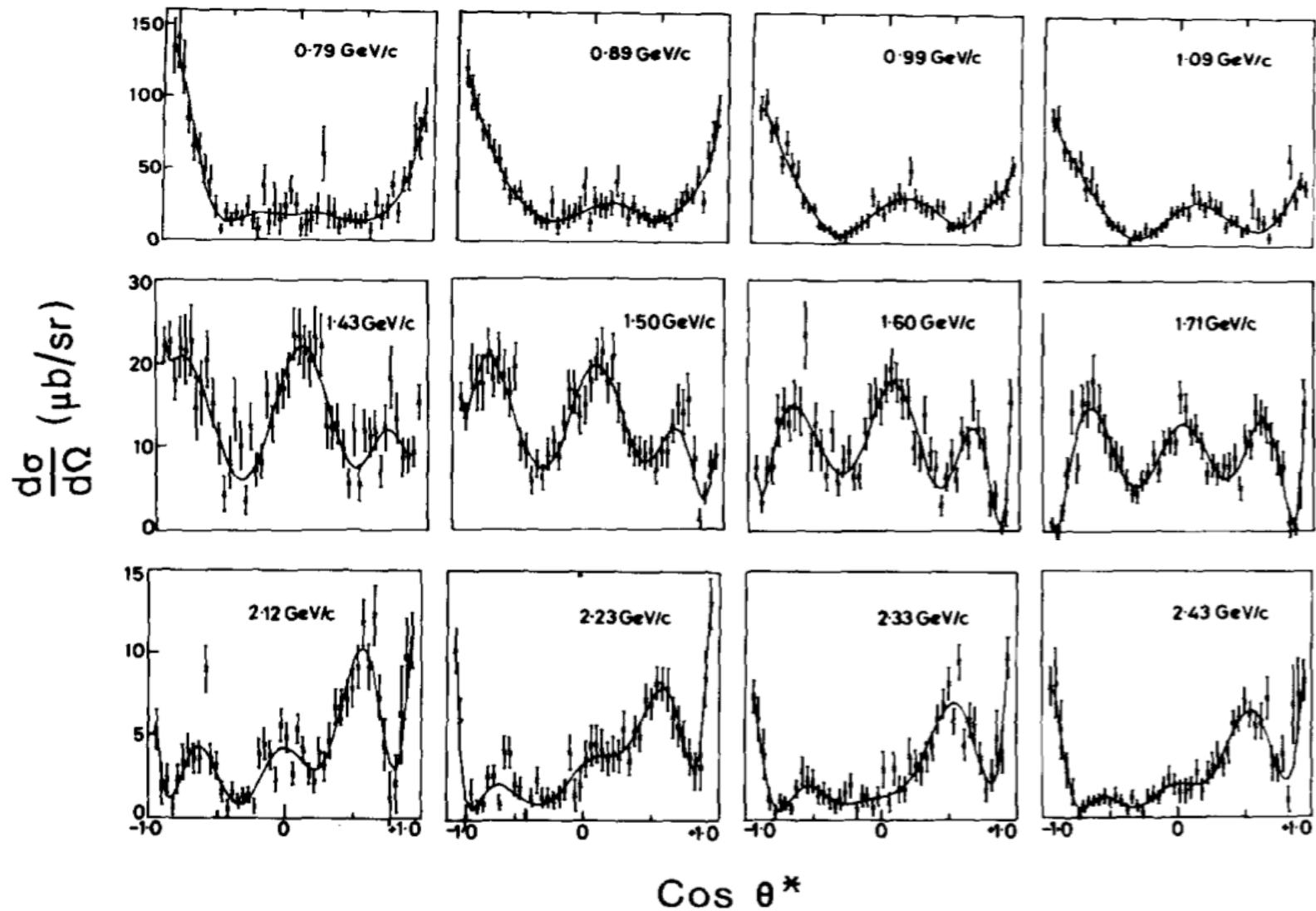
## Motivation

- ▶ The reaction  $\bar{p}p \rightarrow e^+ e^-$  allows to measure electromagnetic proton form factors.
- ▶ Important simulation work is under way.
- ▶ The reaction  $\bar{p}p \rightarrow \pi^+ \pi^-$  is the main background :
  - ▶ has a large cross section,
  - ▶ contains information on the quark content of the proton
  - ▶ allow to test different QCD models

It is necessary to fully understand the process  $\bar{p}p \rightarrow \pi^+ \pi^-$ .

# Evolution of oscillatory behavior : Sum of resonances

Plab (0.79 – 2.43 GeV/c )



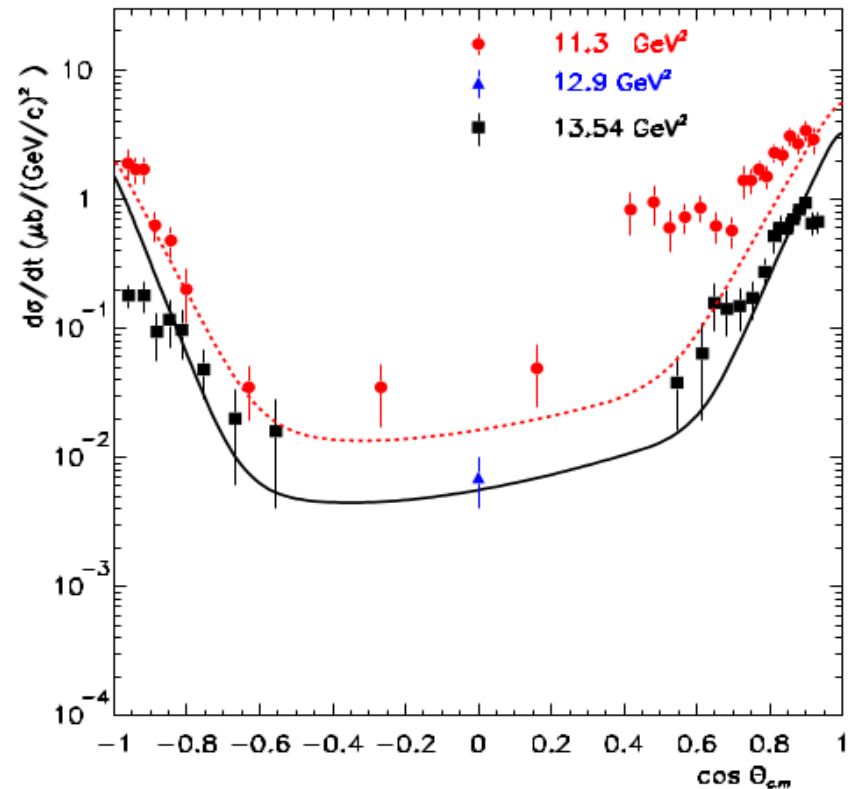
# Earlier recent work

Comparison with the model from ref: EPJ A 46 (2010) , 291-298

- With Regge factor

- well work for the backward region. can be improved in the forward and central regions.

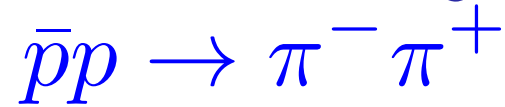
- the parameters in the Regge factors are not well followed the mass and angular momentum.



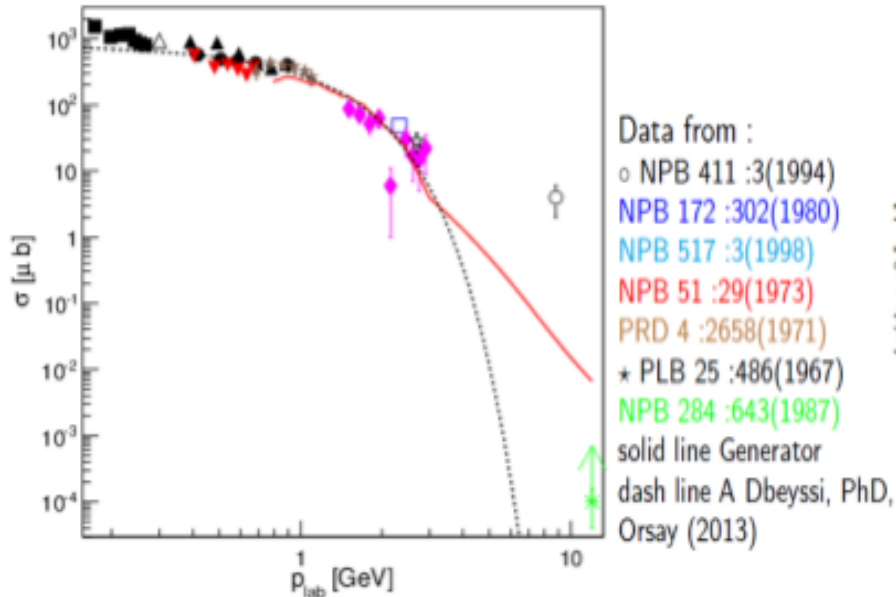
# PART I

## Motivation

Few experimental data at the PANDA energies to constrain the model

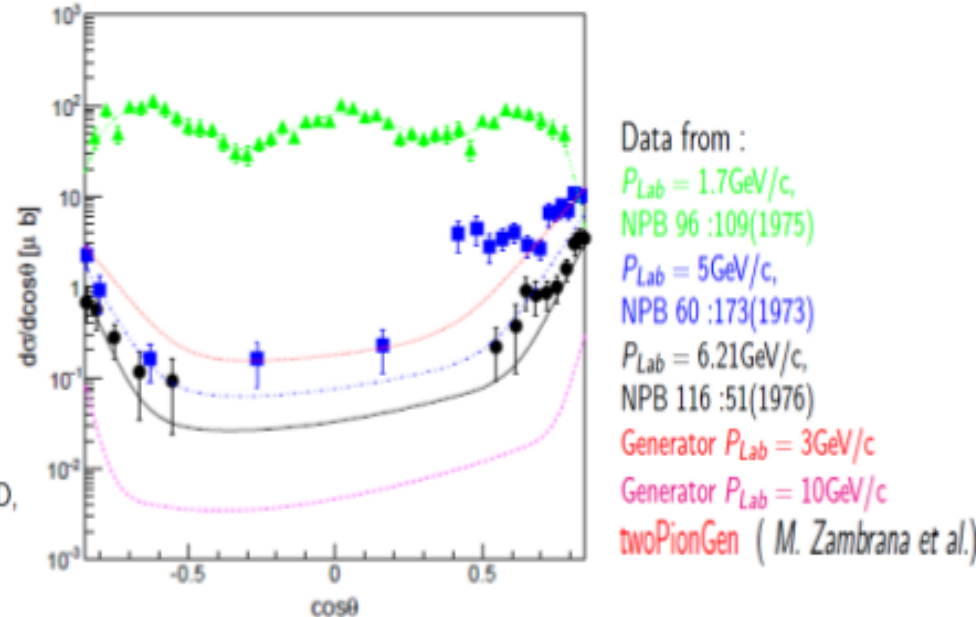


### 1. Total cross section



Extrapolation of existing models to Panda range is risky

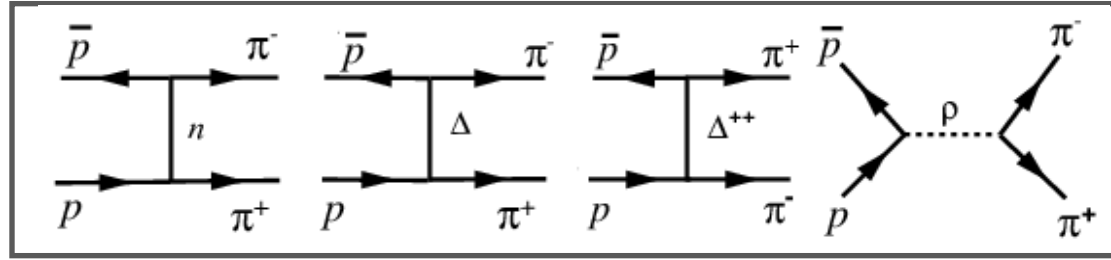
### 2. Differential cross section



Few and incomplete angular distributions data of annihilation(6 sets of  $\pi^+\pi^-$  in panda energy region)

# Effective Lagrangian Model

$$\frac{d\sigma}{d\Omega} = \frac{1}{2^8 \pi^2} \frac{1}{s} \frac{\beta_\pi}{\beta_p} \overline{|\mathcal{M}|^2}$$



$$\mathcal{M} = \mathcal{M}_n + \mathcal{M}_{\Delta^0} + \mathcal{M}_{\Delta^{++}} + \mathcal{M}_\rho.$$

$$F_{N,\Delta}(x) = \frac{\mathcal{N}_{N,\Delta} \cdot M_0^4}{\left[ (x - \Lambda_{N,\Delta}^2) \log \frac{(x - \Lambda_{N,\Delta}^2)}{\Lambda_{QCD}^2} \right]^2},$$

→ logarithmic form factors

→ no Regge factors

- Regge factors not well extrapolation to time like region
- Regge factors give none physic parameters

$$x = s, t, u$$

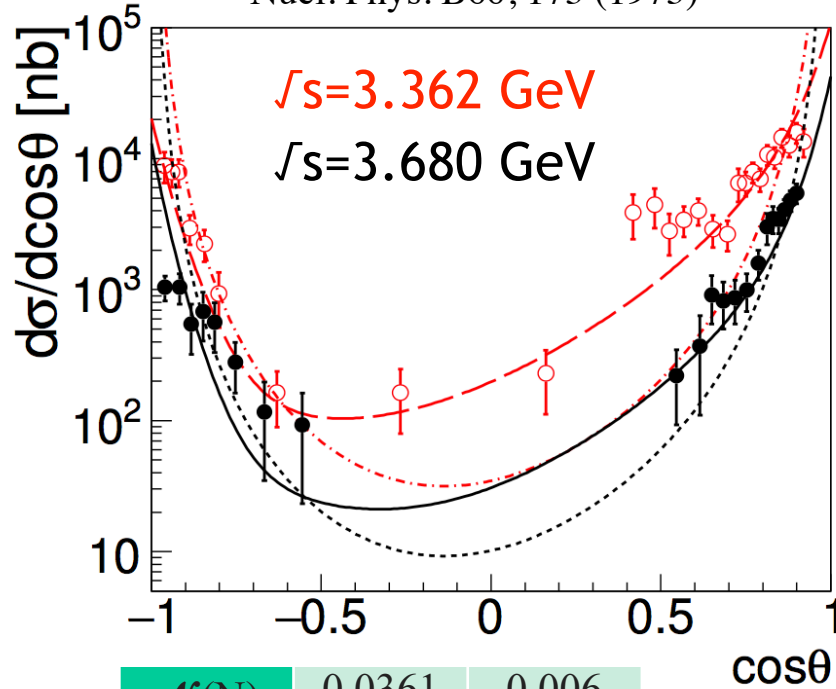
$M_0 = 3.86$  GeV is a scale parameter

$\Lambda_{QCD} = 0.3$  GeV is the QCD scale parameter

# Results and Comparison

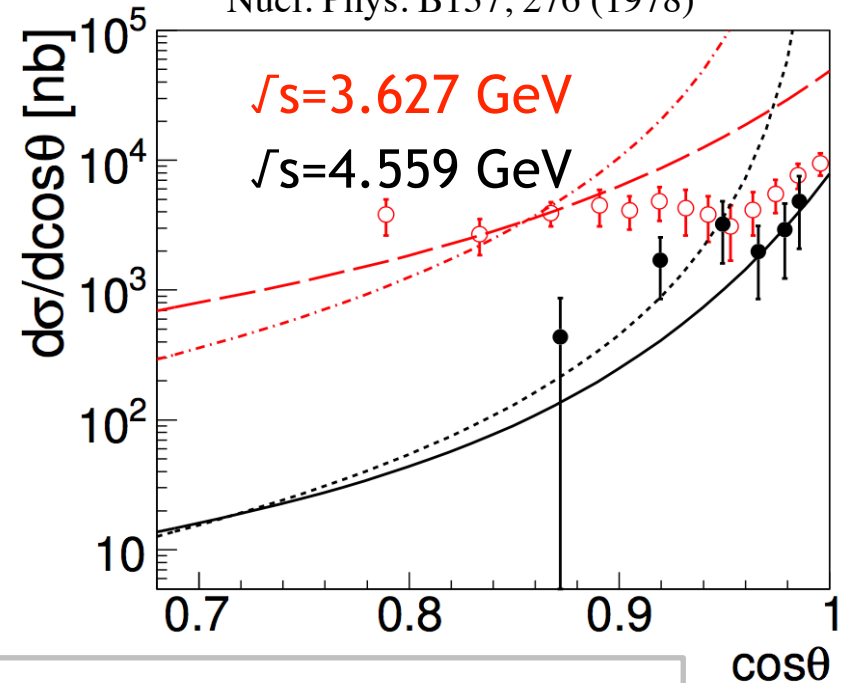
Nucl. Phys. B116, 51 (1976)

Nucl. Phys. B60, 173 (1973)



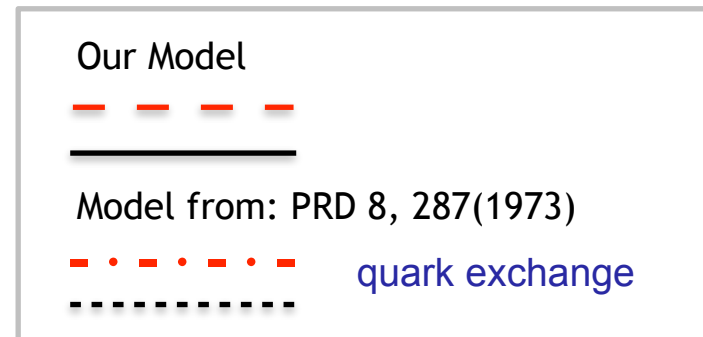
Phys. Rev. Lett. 39, 378 (1977)

Nucl. Phys. B137, 276 (1978)



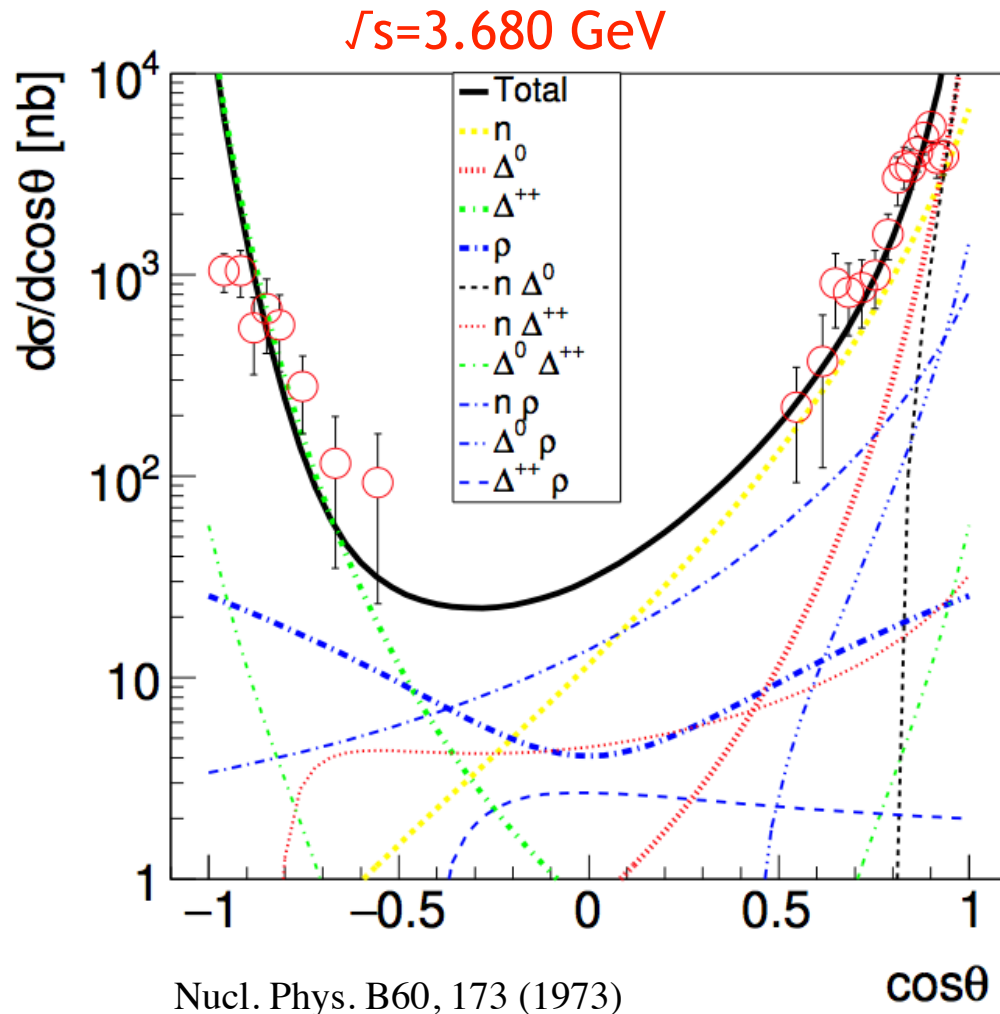
$\mathcal{N}(N)$	0,0361	0,006
$\mathcal{N}(\Delta)$	0,041	0,003
$\Lambda(N)$	2,25	0,09
$\Lambda(\Delta)$	1,05	0,04

$$\chi^2/ndf = 1.99$$





# Components of our model



Forward mainly from  
n and  $\Delta^0$

Backward mainly from  
 $\Delta^{++}$

s-channel from  $\rho$  and  
interferences

# Crossing symmetry

$$\bar{p}(p_1) + p(p_2) \rightarrow \pi^-(k_1) + \pi^+(k_2)$$

$$\pi^-(-k_2) + p(p_2) \rightarrow \pi^-(k_1) + p(-p_1), \quad p_1 \rightarrow -k_2$$

$$s_s = (-k_2 + p_2)^2 \rightarrow t_a \quad \sigma^a = \frac{1}{2} \frac{|\vec{k}_s|^2}{|\vec{p}_a|^2} \sigma^s = f \sigma^s$$

$$t_s = (-k_2 - k_1)^2 \rightarrow s_a$$

$$u_s = (-k_2 + p_1)^2 \rightarrow u_a \quad \text{when } t \text{ is small,}$$

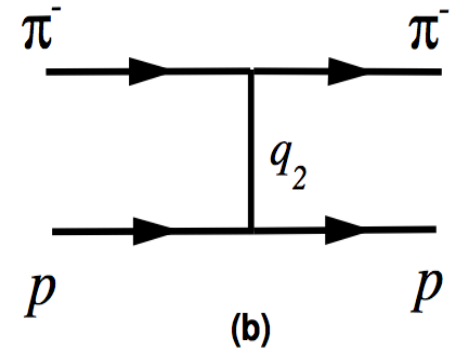
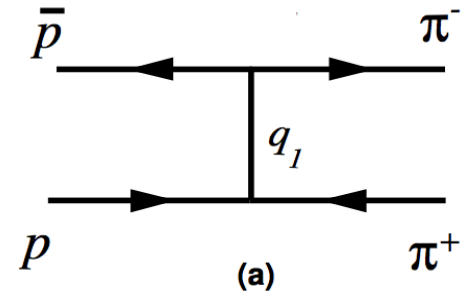
$$\sigma^a = \frac{1}{4} \frac{|\mathcal{M}_{(a)}|^2}{64\pi^2 s} \frac{|\vec{k}_a|}{|\vec{p}_a|}$$

$$\sigma^s \simeq \text{const} \cdot s^{-2}$$

$$\sigma^s(s) = \sigma^s(s_1) \cdot \frac{s^{-2}}{s_1^{-2}}$$

$$\sigma^s = \frac{1}{2} \frac{|\mathcal{M}_{(s)}|^2}{64\pi^2 s} \frac{|\vec{k}_s|}{|\vec{p}_s|}$$

$$\sigma^a(s) = f \sigma^s(s_1) \cdot \frac{s^{-2}}{s_1^{-2}}$$

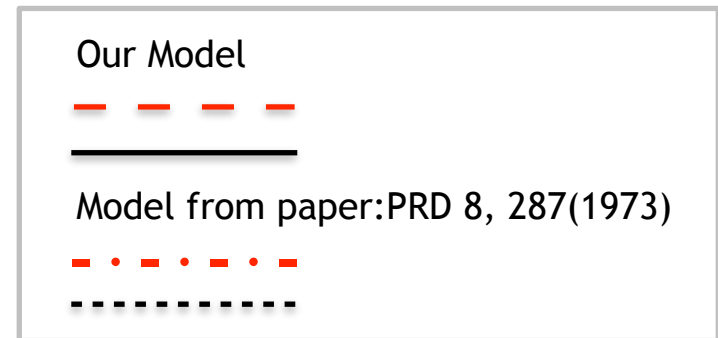
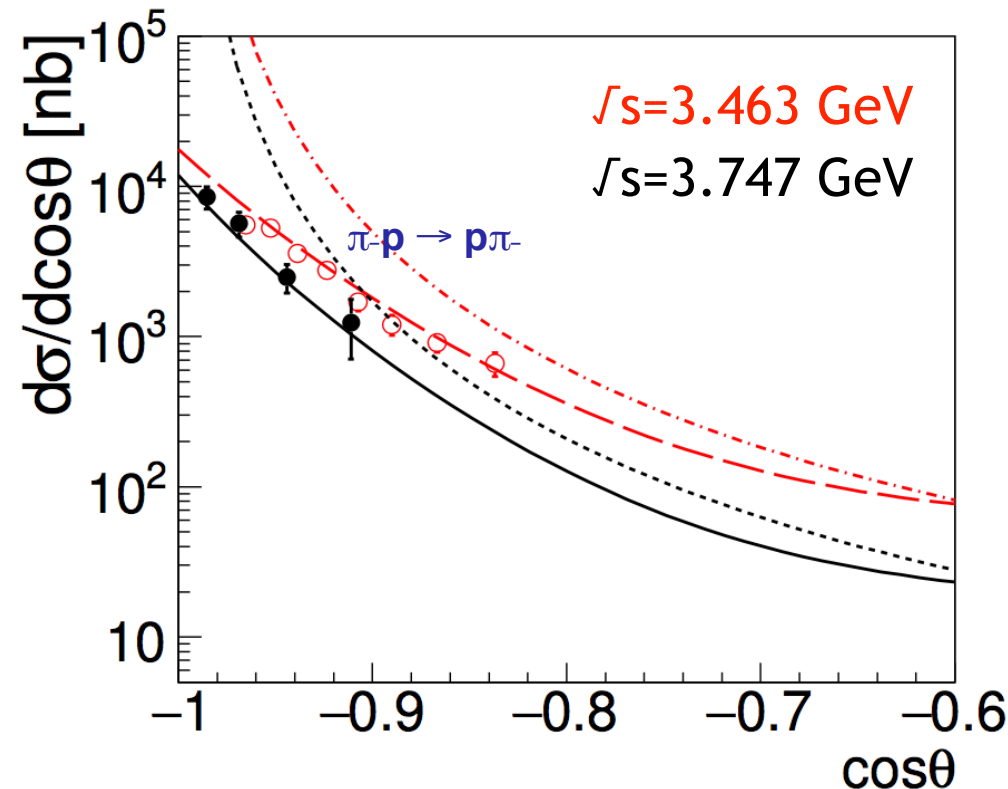


# Crossing symmetry of the model

Phys. Rev. 181, 1794 (1969)

Nucl. Phys. B 25, 385(1971)

- using crossing symmetry from  $p\pi^-$  elastic to get more experiment data in the backward region



# Quark counting rules:

## Hadron-hadron collision at high energies (CMS)

2 experimental rules in the reaction

limited T momenta with s increasing (L can be infinite)

average number of particles produced grows slowly when s increases



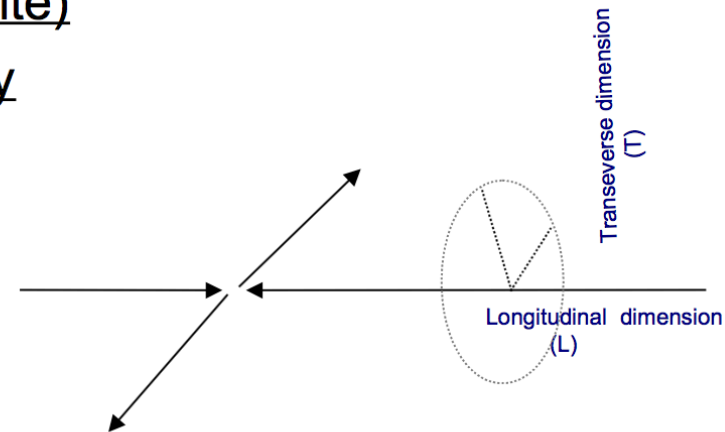
kinematics is defined by dimensions T and L

- Strong dynamical difference between T-L
- Essential constants purely related to T



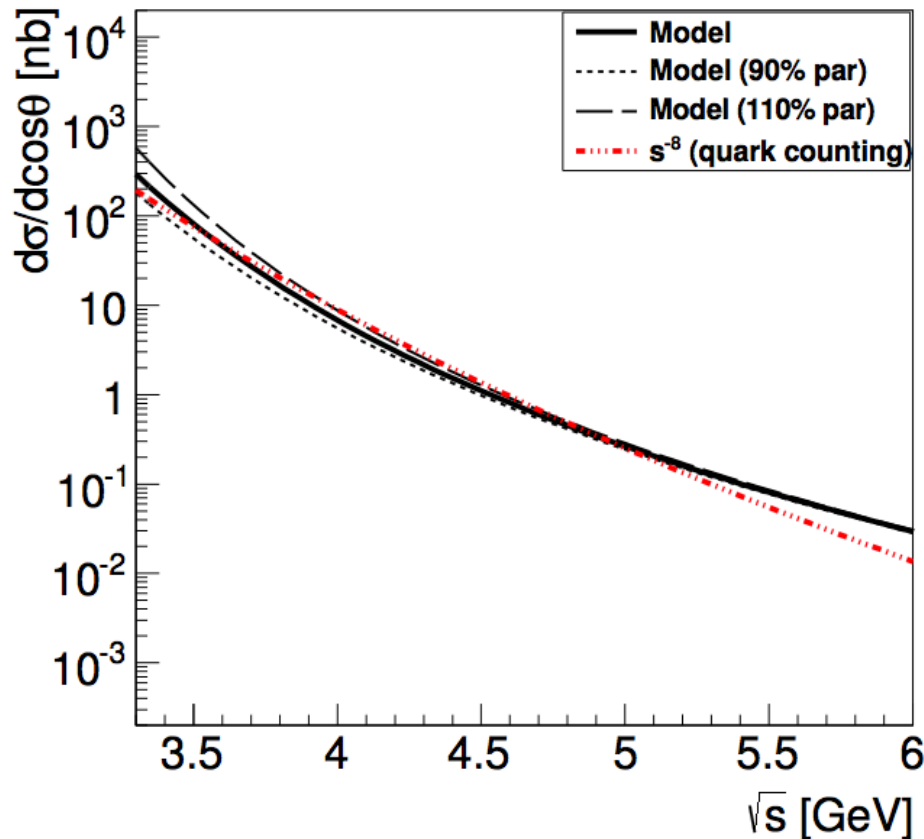
Asymptotically, the average number of particles (multiplicity), and the average transverse momentum are constant as function of s.

LETTERE AL NUOVO CIMENTO (1973) 5 14  
V. A. Matveev et al.  
Automodelity in Strong Interactions.



# S-dependence $\bar{p}p \rightarrow \pi^- \pi^+$

Compare to quark counting rules at 90 degree



PRL (1973) 31. 18.

S. J. Brodsky, G. R. Farrar

Scaling Laws at Large Transverse Momentum

LETTERE AL NUOVO CIMENTO (1973) 5 14

V. A. Matveev et al.

Automodelity in Strong Interactions.

$$d\sigma/dt \sim s^{2-n} f(t/s)$$

$$d\sigma/dt \sim s^{-8} f(t/s)$$

# Results and Comparison

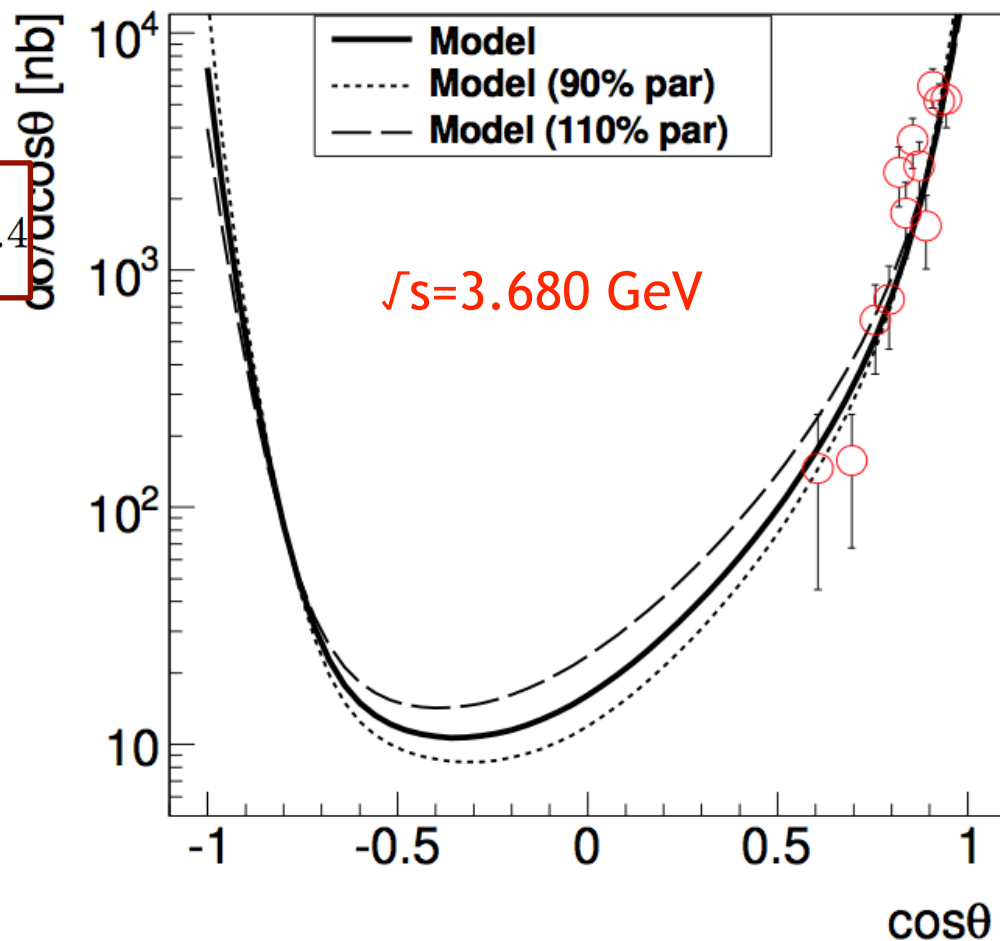
$$\bar{p}p \rightarrow K^- K^+$$

*V. Anisovich, Phys. Lett. B 364, 195 (1995).*

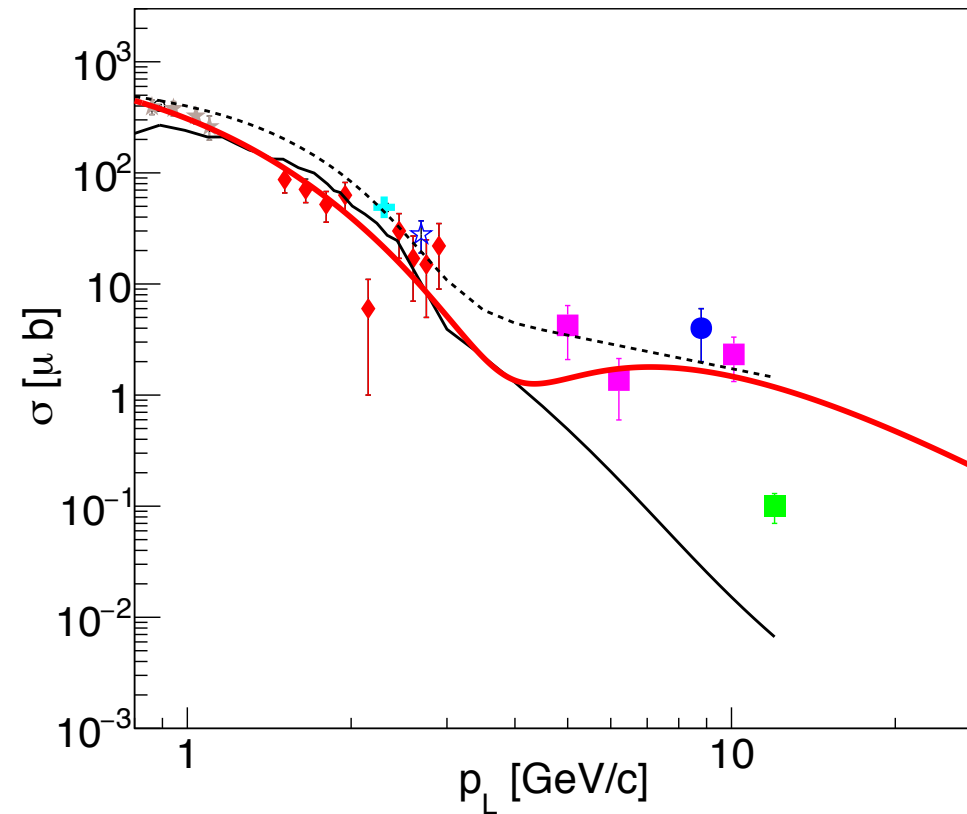
- Prediction through SU3 symmetry with no change of parameters.

$$\sigma(\pi^- \pi^+) : \sigma(K^- K^+) = 1 : \frac{4\lambda}{3}, \text{ where } \lambda = 0.4$$

- Evaluate the total cross section, from the integrated cross section  $\sigma(\bar{p}p \rightarrow K^+ K^-) = 2.1 \pm 0.8 \text{ mb}$ .



# Total cross section



- Black dashed line modified from A Dbeyssi PhD

$$\sigma = a \cdot e^{-(b \cdot p_{lab} + c \cdot p_{lab}^2 + d)} + \frac{e}{p_{lab}}$$

Added term

- Red solid line - our model
- Black solid line - Mainz generator  
pink points from the integration of limited angular distribution.

# From pion to eta through SU(3)

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Pion and eta mesons are pseudoscalar mesons.

The decay to  $\eta\eta$  can be described from  $\pi^0\pi^0$  using the well-known decomposition of singlet and octet states, where the mixing angle is  $\Theta \approx 45^\circ$

$$\eta \approx (u\bar{u} + d\bar{d})/\sqrt{2} + s\bar{s}$$
$$(u\bar{u} + d\bar{d})\sqrt{2} \leftarrow |q\bar{q}\rangle = \cos\Theta|\eta\rangle + \sin\Theta|\eta'\rangle$$
$$|s\bar{s}\rangle = -\sin\Theta|\eta\rangle + \cos\Theta|\eta'\rangle$$

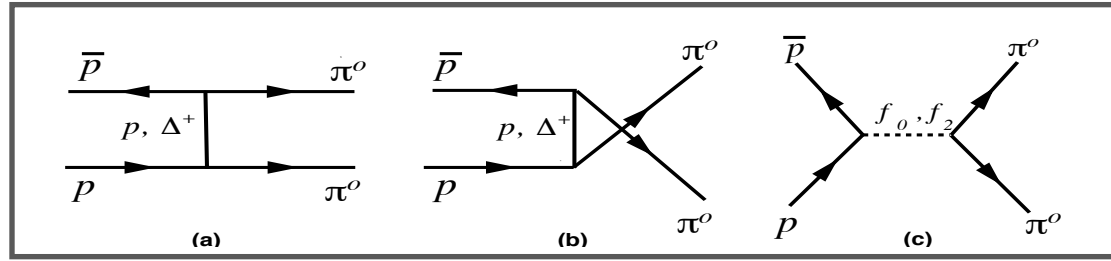
$$f(\eta\eta) = f(\pi^0 + \pi^0) \cos^2\Theta$$

$$f(\pi^0\eta) = f(\pi^0 + \pi^0) \cos\Theta$$



# $\pi^0\pi^0$ production

$$\frac{d\sigma}{d\Omega} = \frac{1}{2^8\pi^2} \frac{1}{s} \frac{\beta_\pi}{\beta_p} |\mathcal{M}|^2$$



$$F_{N,\Delta}(x) = \frac{\mathcal{N}_{N,\Delta} \cdot M_0^4}{\left[ (x - \Lambda_{N,\Delta}^2) \log \frac{(x - \Lambda_{N,\Delta}^2)}{\Lambda_{QCD}^2} \right]^2},$$



$$\begin{aligned} \mathcal{N}(s)_{p,\Delta} &\rightarrow \mathcal{N}(s)_{p,\Delta} - e^{\frac{p_{p,\Delta}^{\mathcal{N}}(s)}{\sqrt{s}}} \\ \Lambda(s)_{p,\Delta} &\rightarrow \Lambda(s)_{p,\Delta} - e^{\frac{p_{p,\Delta}^{\Lambda}(s)}{\sqrt{s}}} \end{aligned}$$

$M_0 = 3.86$  GeV is a scale parameter

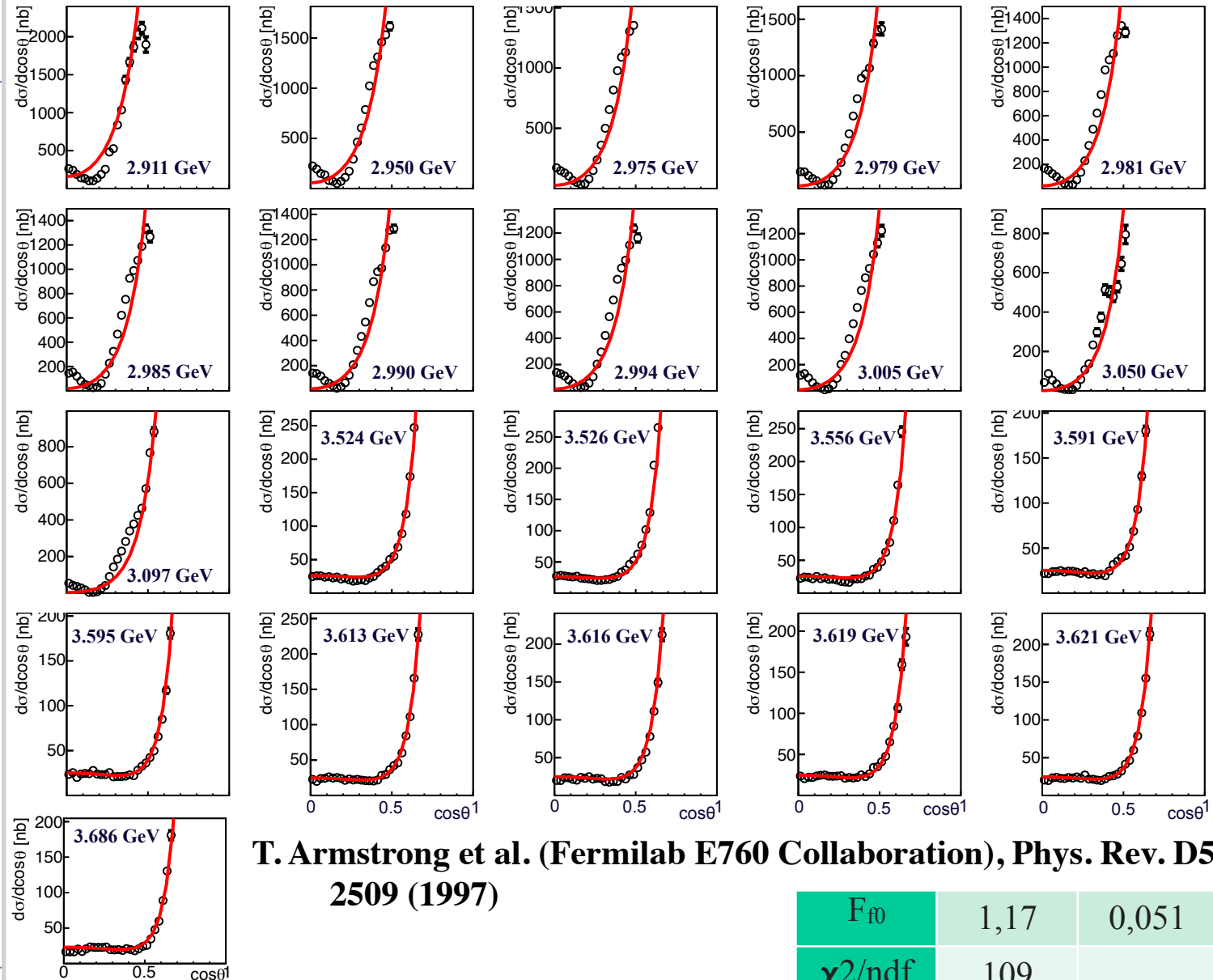
$\Lambda_{QCD} = 0.3$  GeV is the QCD scale parameter

## Form factor for s-channel

$$FF_f(s) = \frac{F_f^2}{F_f^2 + M_f^2 - s}$$

$p^{\mathcal{N}}(N)$	-3,013	0,210
$p^{\mathcal{N}}(\Delta)$	-5,959	0,205
$p^{\Lambda}(N)$	4,047	0,019
$p^{\Lambda}(\Delta)$	3,141	0,002

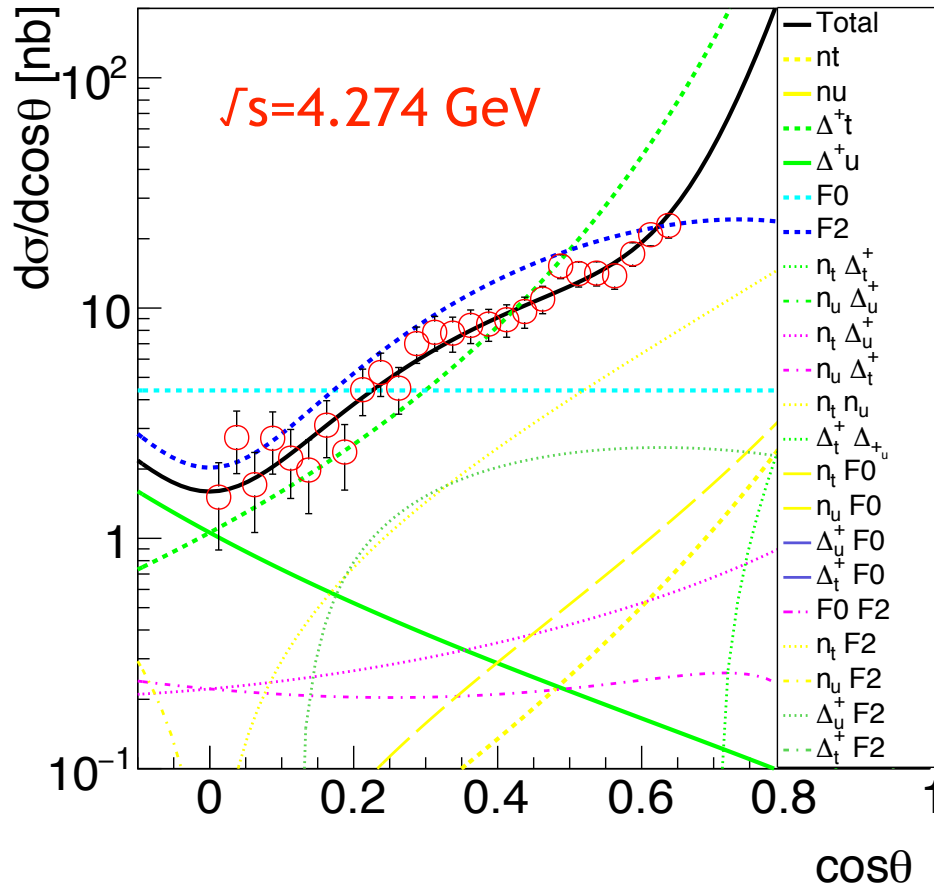
# Results of $\pi^0\pi^0$



**T. Armstrong et al. (Fermilab E760 Collaboration), Phys. Rev. D56, 2509 (1997)**

$F_{f0}$	1,17	0,051
$\chi^2/ndf$	109	

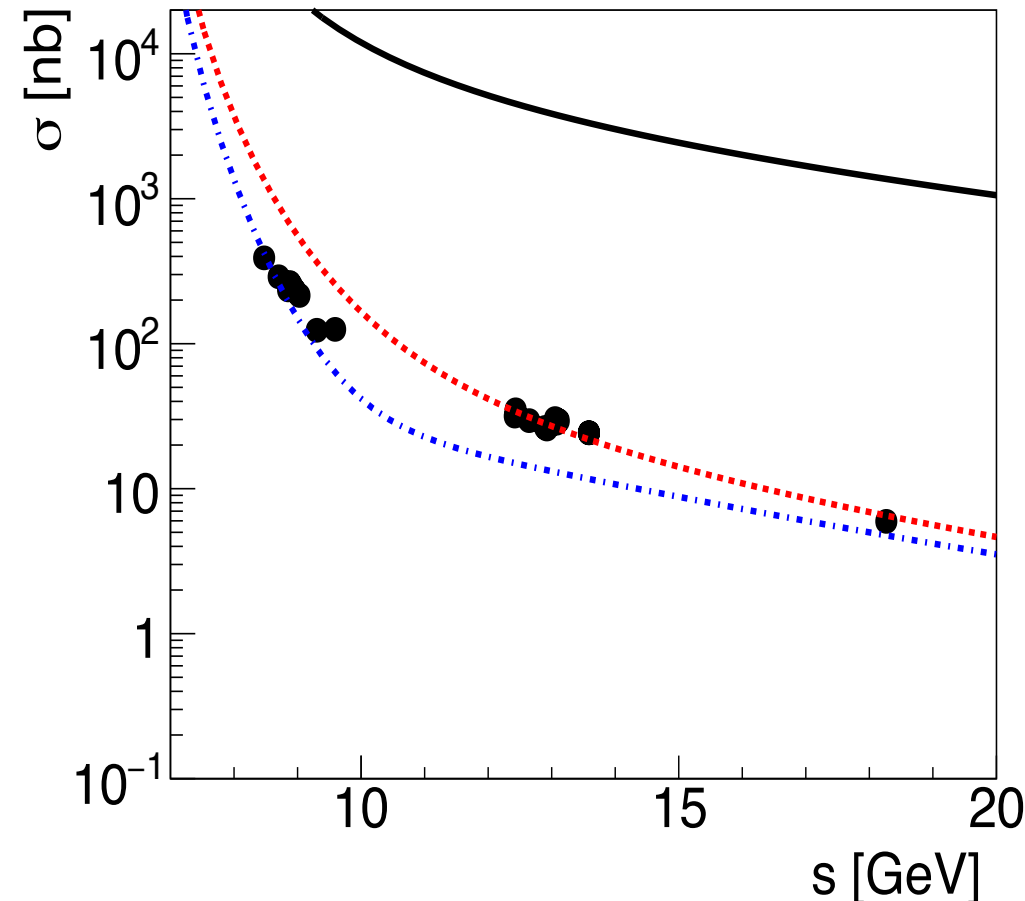
# Components for $\pi^0\pi^0$



$F_{f0}$	0,870	0,014
$F_{f2}$	0,187	0,001
$\chi^2/ndf$	0,787	

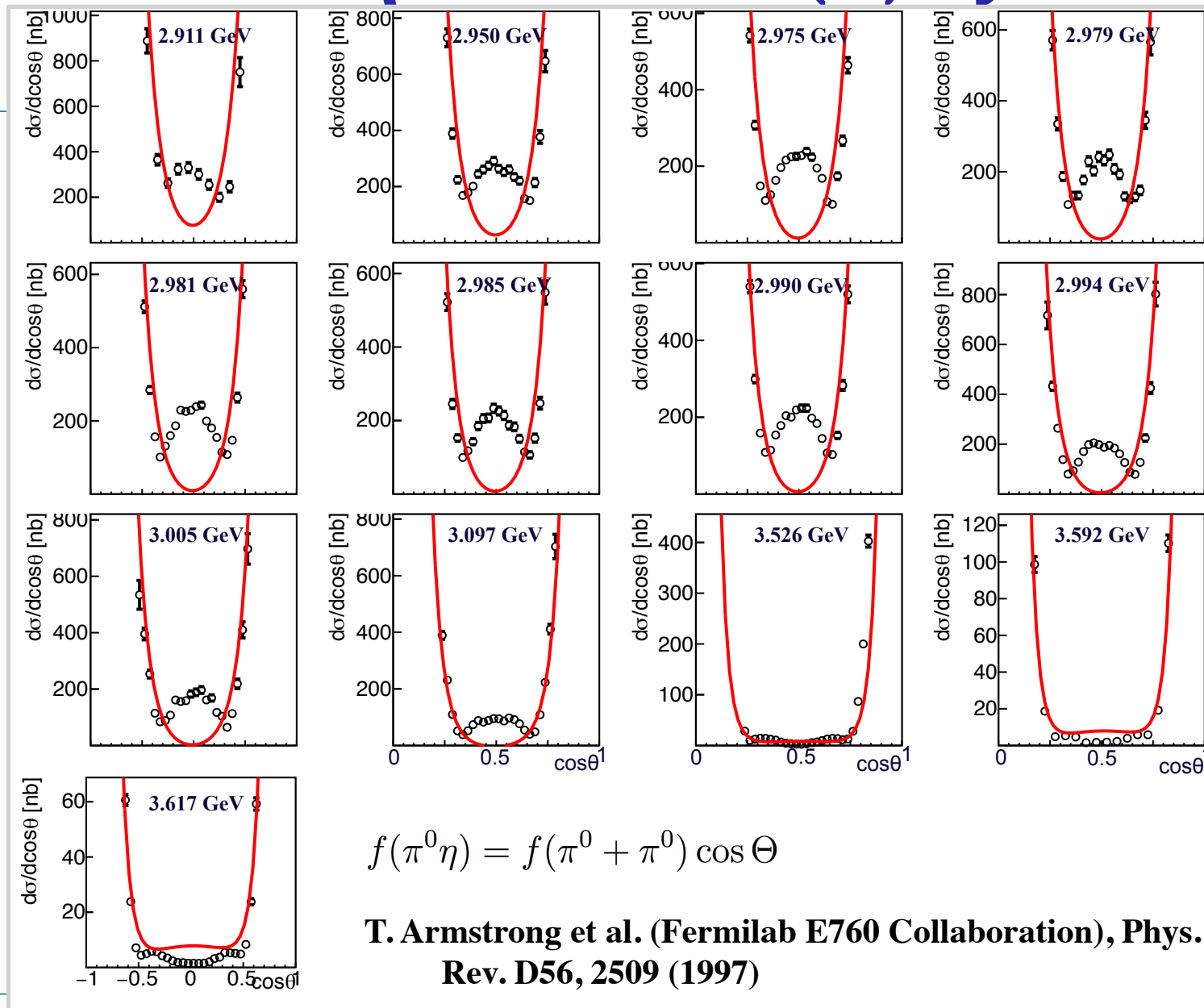
- Black solid line - our model
- Blue dashed line -  $f_0$ .
- The bump is produced by the J=2 meson  $f_2$ .

# Integrated cross section of $\pi^0\pi^0$

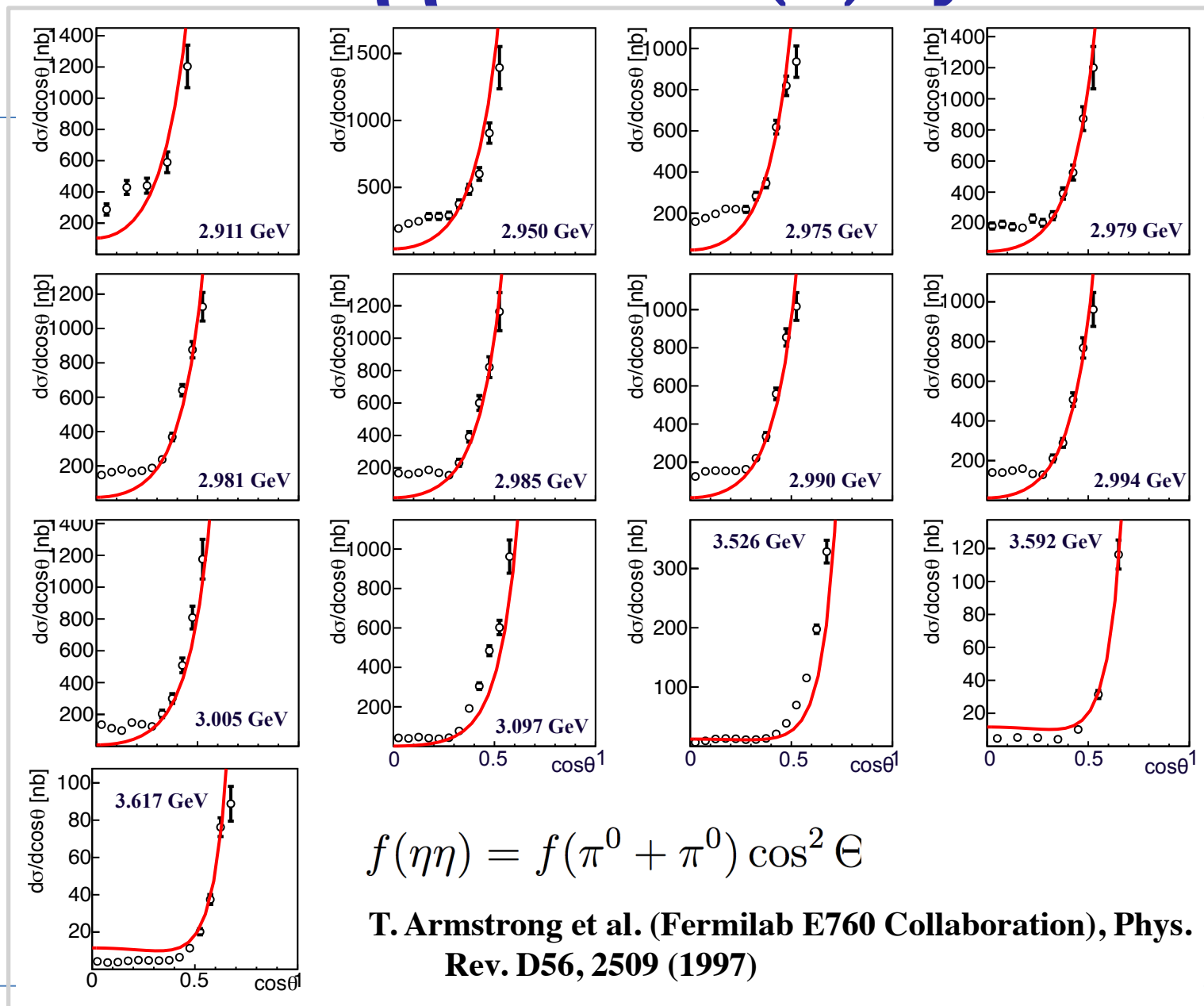


- black line - full angular range
- Red line - integrated within the region  $0 < \cos\theta < 0.66$
- Blue line - integrated within the region  $0 < \cos\theta < 0.48$

# Results of $\eta\pi^0$ with SU(3) symmetry



# Results of $\eta\eta$ with SU(3) symmetry



$$f(\eta\eta) = f(\pi^0 + \pi^0) \cos^2 \Theta$$

**T. Armstrong et al. (Fermilab E760 Collaboration), Phys. Rev. D56, 2509 (1997)**

# Summary Part I

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A promising model based on effective Lagrangian has been built to describe 2 meson production in  $p\bar{p}$  annihilation

- We reproduced existing charged and neutral pion data.
- We reproduced  $\pi^+p$ ,  $\pi^-p$  using crossing symmetry
- Charged kaon channel obtained from SU3 symmetry:  $K^+K^-$ . Neutral production  $\eta\eta, \eta\pi^0$  obtained through SU(3) symmetry from  $\pi^0\pi^0$ .
- very good results on angular distributions and the expected s-dependence have been obtained

**therefore we can trust the extrapolation of our model in the PANDA energy range.**

# PART II

## Analyzing powers

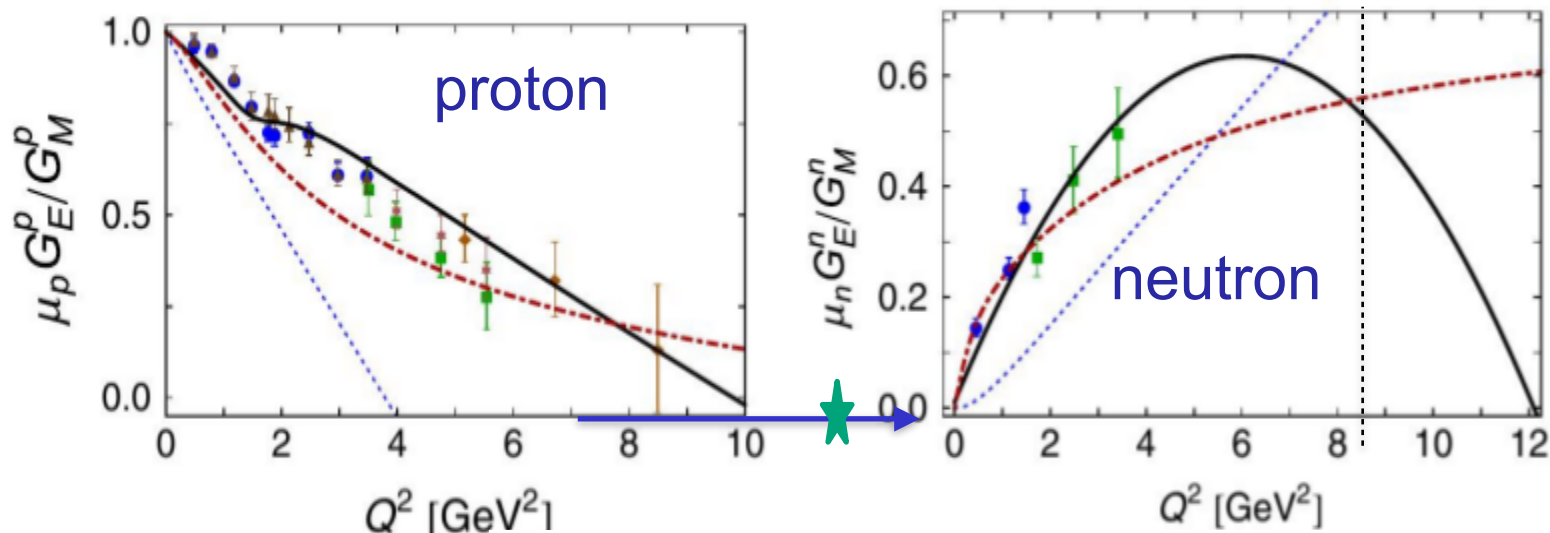
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- **Measuring analyzing powers (ALPOM2) is the first step to conceive and optimize a polarimeter to measure proton (neutron) polarization .**
- **Polarization experiments are needed for the extraction of electromagnetic form factors (FFs) using polarized eN elastic experiments (Jlab).**



# Motivation

JLab proposals (PAC 43) :Proton and neutron FFs with **Akhiezer-Rekalo recoil polarization method** at  $Q^2$  at **12.4 GeV<sup>2</sup>** and **8.4 GeV<sup>2</sup>**.



(black line)

J. Segovia *et al.*, *Few-Body Syst.* 55 (2014), 1185

(red dash)

J.J. Kelly, *Phys. Rev. C*70(2004), 068202.

(blue dotted)

D.J. Wilson *et al.*, *Phys. Rev. C*85(2012),025205.

M.K. Jones *et al.* *Phys. Rev. Lett.* 84(2000), 1398.

O. Gayou *et al.*, *Phys. Rev. Lett.* 88(2002), 092301.

V. Punjabi *et al.*, *Phys. Rev. C*71(2005), 055202.

**Points from JLab data**

D.J. Wilson *et al.*, *Phys. Rev. C*85(2012),025205.

A.J.R. Puckett *et al.*, *Phys. Rev. Lett.* 104(2010), 242301.

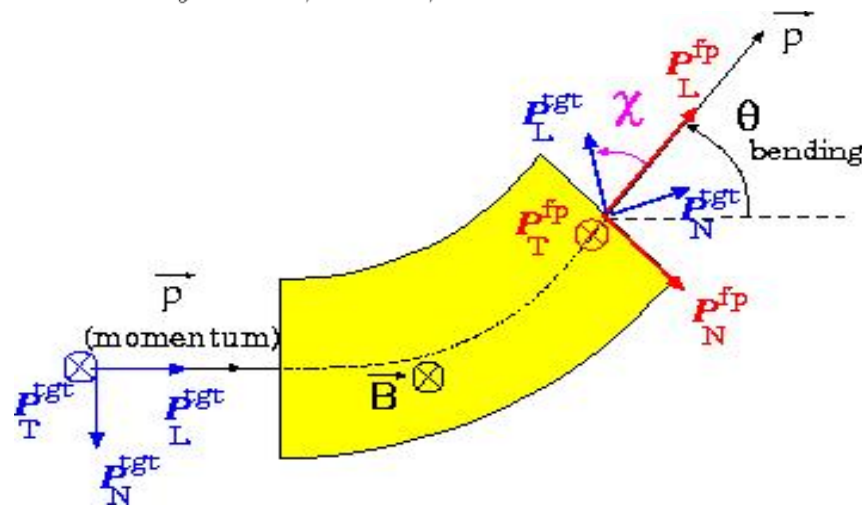
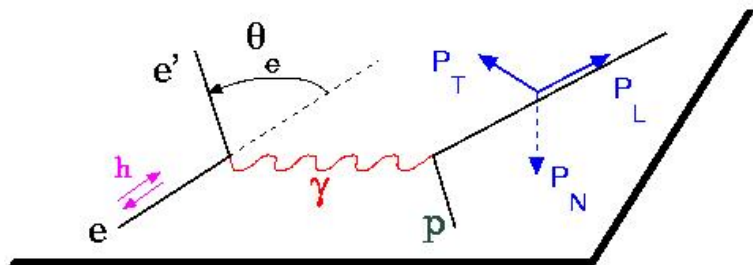
# Motivation

## Optimising nucleon polarimetry for high transfer momenta

### Akhiezer-Rekalo recoil polarization method

A.I. Akhiezer and Mikhail.P. Rekalo. Polarization phenomena in electron scattering by protons in the high energy region. *Sov.Phys.Dokl.*, 13:572, 1968.

#### Elastic $ep$ reaction ( $1-\gamma$ exchange)



$$\frac{P_{t=x}}{P_{l=z}} = -2 \cot(\theta_e/2) \frac{M_p}{\epsilon_1 + \epsilon_2} \frac{G_E}{G_M}$$

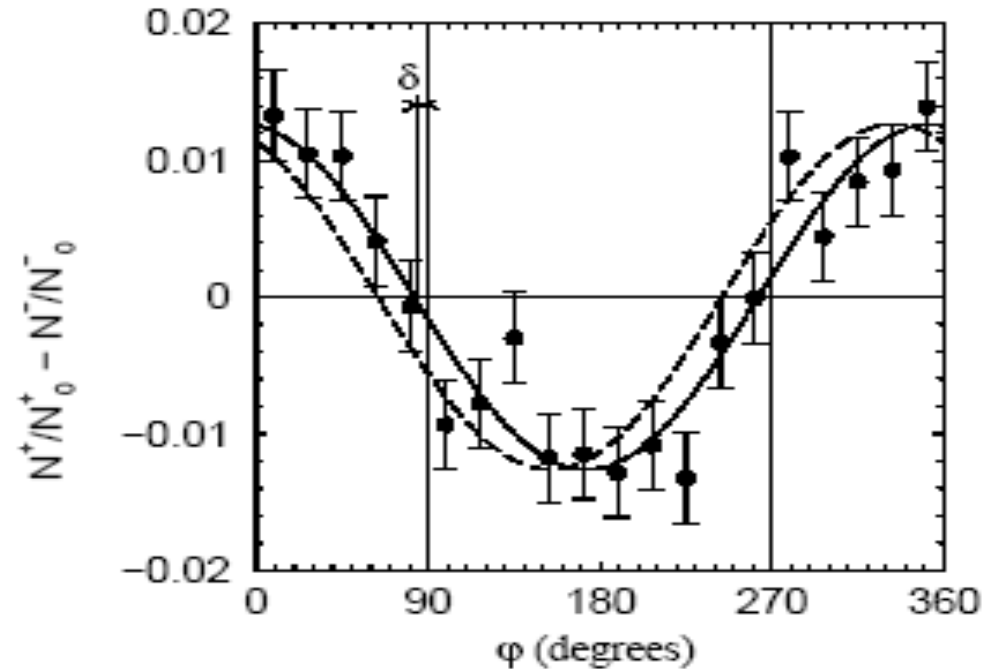
**The simultaneous measurement of  $P_t$  and  $P_l$  reduces systematic errors to achieve more precise ratio of FFs**

# Principle of polarimetry

Azimuthal distribution of protons  
after scattering in the analyzer

$$Q^2 = 5.6 \text{ GeV}/c^2$$

Asymmetry very small,  
experiment very difficult



M.K. Jones *et al.* Phys. Rev. Lett. 84(2000), 1398.

O. Gayou *et al.*, Phys. Rev. Lett. 88(2002), 092301.

V. Punjabi *et al.*, Phys. Rev. C71(2005), 055202.

A.J.R. Puckett *et al.*, Phys. Rev. Lett. 104(2010), 242301.

# Principle of polarimetry

Working principle: measurement of the azimuthal asymmetry in a scattering

Vector polarization: (Proton) inclusive scattering on light targets:

$p+C(CH_2) \rightarrow \text{one charged particle} + X$

(Neutron)

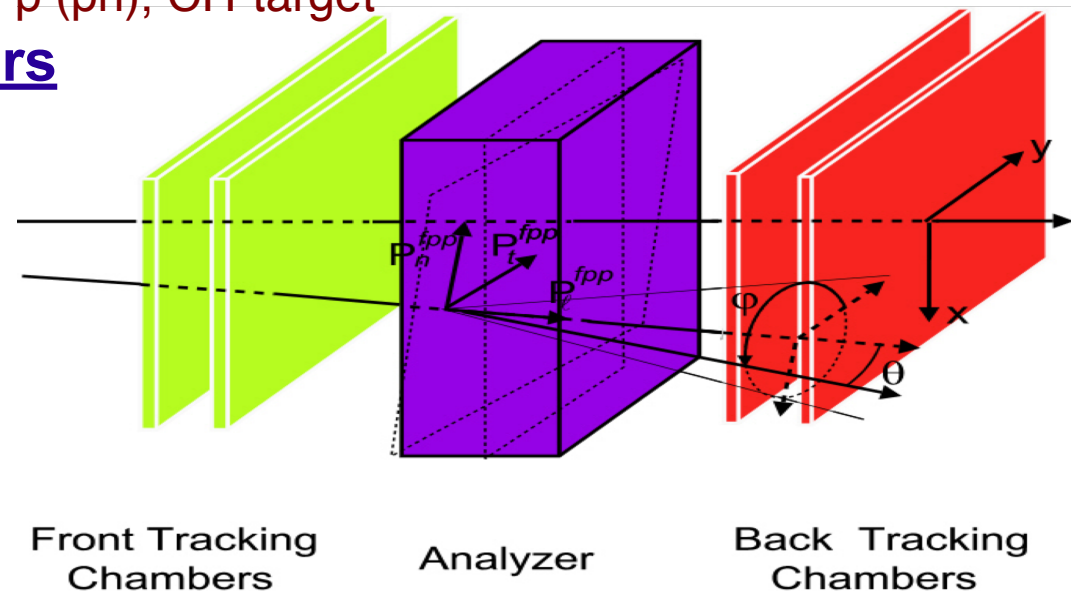
$n p \rightarrow n p$  (pn), CH-target

• Calibration: analyzing powers

$$N^{\pm}(\theta, \phi) = N_0(\theta)(1 \pm P_y A_y(\theta) \cos \phi),$$

$$R(\theta, \phi) = \frac{N^+(\theta, \phi) - N^-(\theta, \phi)}{N^+(\theta, \phi) + N^-(\theta, \phi)} = a_1(\theta) \cos \phi$$

$$A_y(\theta) = \frac{a_1(\theta)}{P_y}, \quad \Delta A_y \simeq \frac{1}{P_y} \sqrt{\frac{1}{N_{Incident}}}$$



# ALPOM II

Upgrade ALPOM (<http://lhe.jinr.ru/alpom/>)

Pp up to 7.5 GeV/c

Pn up to 5.3 GeV/c

Measurement of the inclusive  $\bar{p}CH_2$  analyzing power at high energies (ALPOM-project)

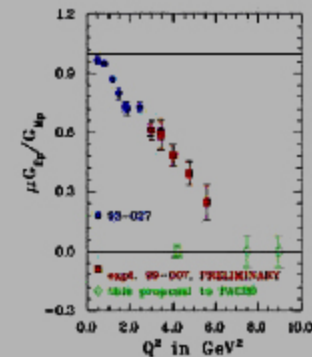
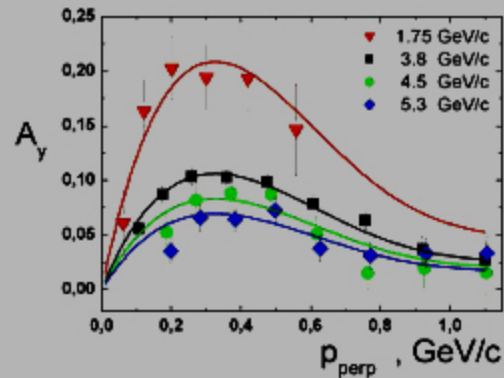


Figure 16: The  $\mu G_{Ep}/G_{Mp}$  results of experiments 93-027, 99-007 (PRELIMINARY) and proposed 00-111.

The main goal of the project is to obtain the analyzing power for  $pCH_2 \rightarrow pX$  reaction at large momenta for  $G_{Ep}/G_{Mp}$  experiment at JLAB. Also these data are necessary to develop the proton focal-plane polarimetry at hadronic facilities.

# *Neutron analyzing power measurement: which reaction is better?*

## Comparison of figure of merit

*np* → *np* elastic scattering  
(zero exchange)

*np* → *pn*  
(charge exchange)

$$\mathcal{F}^2 = \int_{\theta} \epsilon(\theta) A_y^2(\theta) d\theta$$

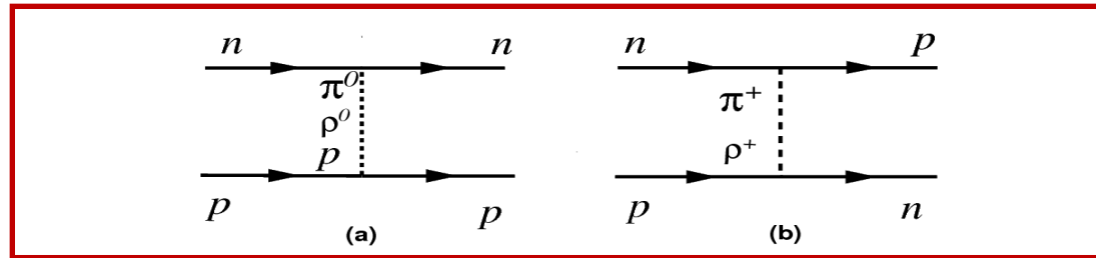
$$\epsilon(\theta) = \frac{N_{useful}(\theta)}{N_{incident}(\theta)}$$

$$\Delta P = \sqrt{\frac{2}{N_{inc} \mathcal{F}^2}}$$

# Pole model for $np \rightarrow np$ ( $pn$ )

## Neutron

➤ Differential cross section



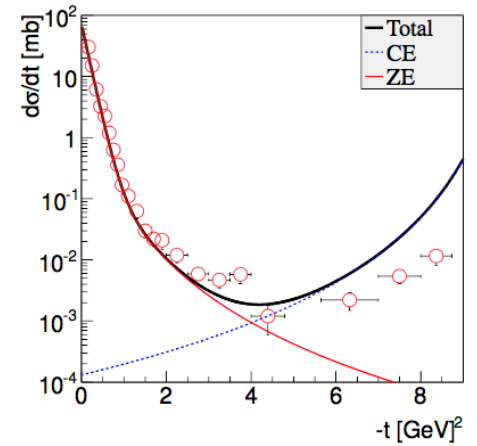
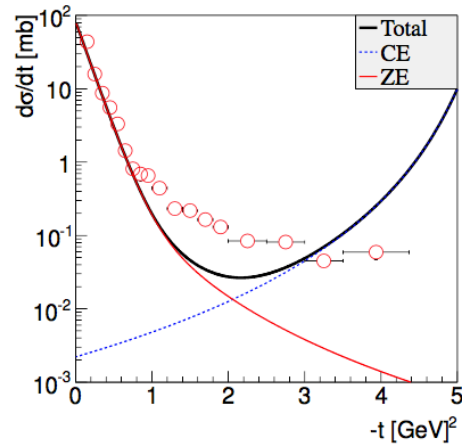
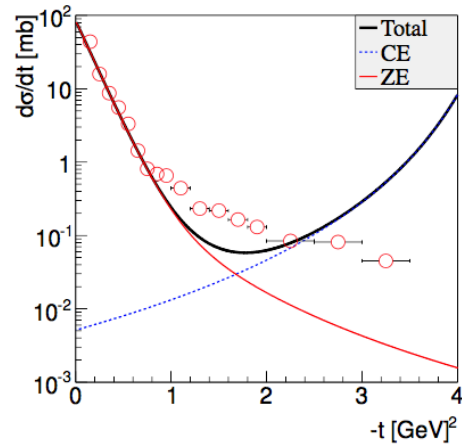
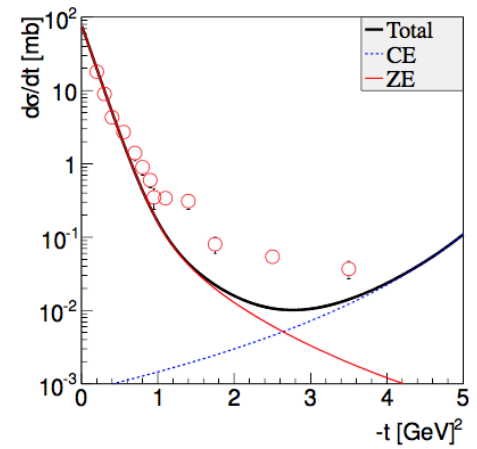
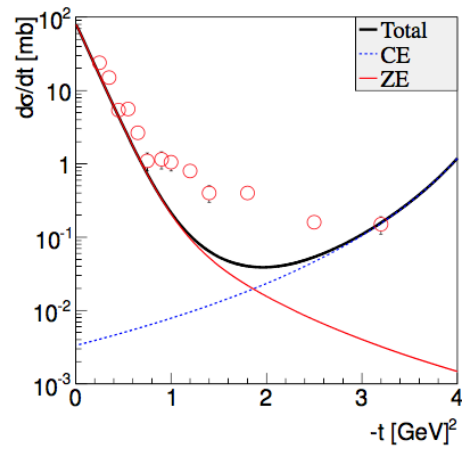
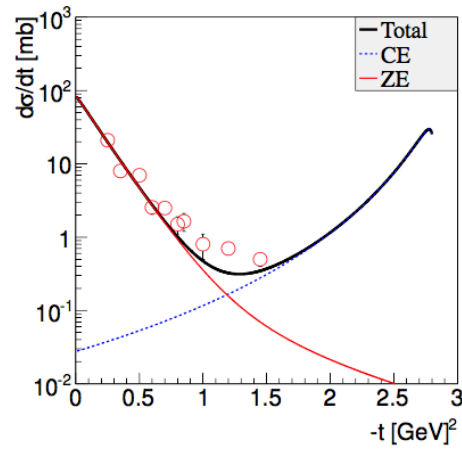
$$\frac{d\sigma}{dt} = \frac{1}{64\pi s q^2} (|T_\pi(u) + T_\rho(u)|^2 + \frac{1}{4} |T_\pi(t) + T_\rho(t)|^2 + |T_P(t)|^2)$$

$$|T_{CE}(u)|^2 = \left( F_u \frac{u A_\pi}{u - m_\pi^2} F_u \right)^2 + \left| F_u \frac{u A_\rho e^{i\varphi}}{u - m_\rho^2} F_u \right|^2 + 2 \left( F_u \frac{u A_\pi}{u - m_\pi^2} F_u \right) \left( F_u \frac{u A_\rho e^{-i\varphi}}{u - m_\rho^2} F_u \right)$$

$$|T_{ZE}(t)|^2 = \frac{1}{4} \left[ \left( F_t \frac{t A_\pi}{t - m_\pi^2} F_t \right)^2 + \left| F_t \frac{t A_\rho e^{i\varphi}}{t - m_\rho^2} F_t \right|^2 + 2 \left( F_t \frac{t A_\pi}{t - m_\pi^2} F_t \right) \left( F_t \frac{t A_\rho e^{-i\varphi}}{t - m_\rho^2} F_t \right) \right] + (A_P e^{-b|t|})^2$$

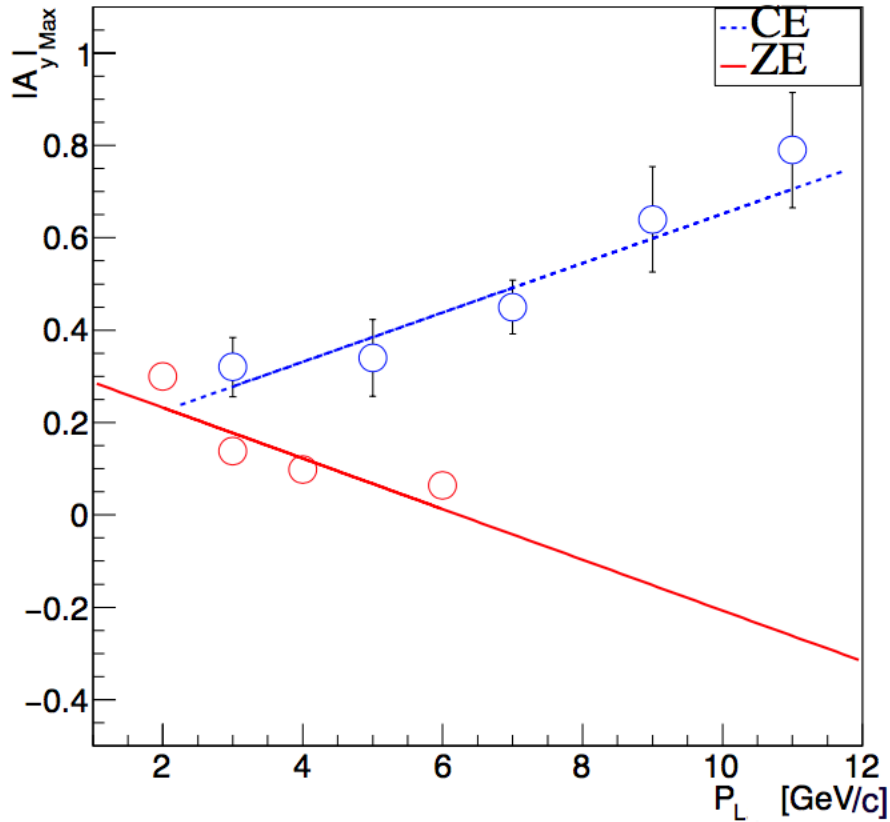
Yu.A. Troyan, M.Kh. Anikina, A.V. Belyaev, A.P. Ierusalimov, and A.Yu. Troyan. Elastic  $np \rightarrow np$  ( $pn$ ) scattering at intermediate energies. *Physics of Particles and Nuclei Letters*, 11(2):101–108, 2014.

# Differential cross section





# Maximum analyzing powers

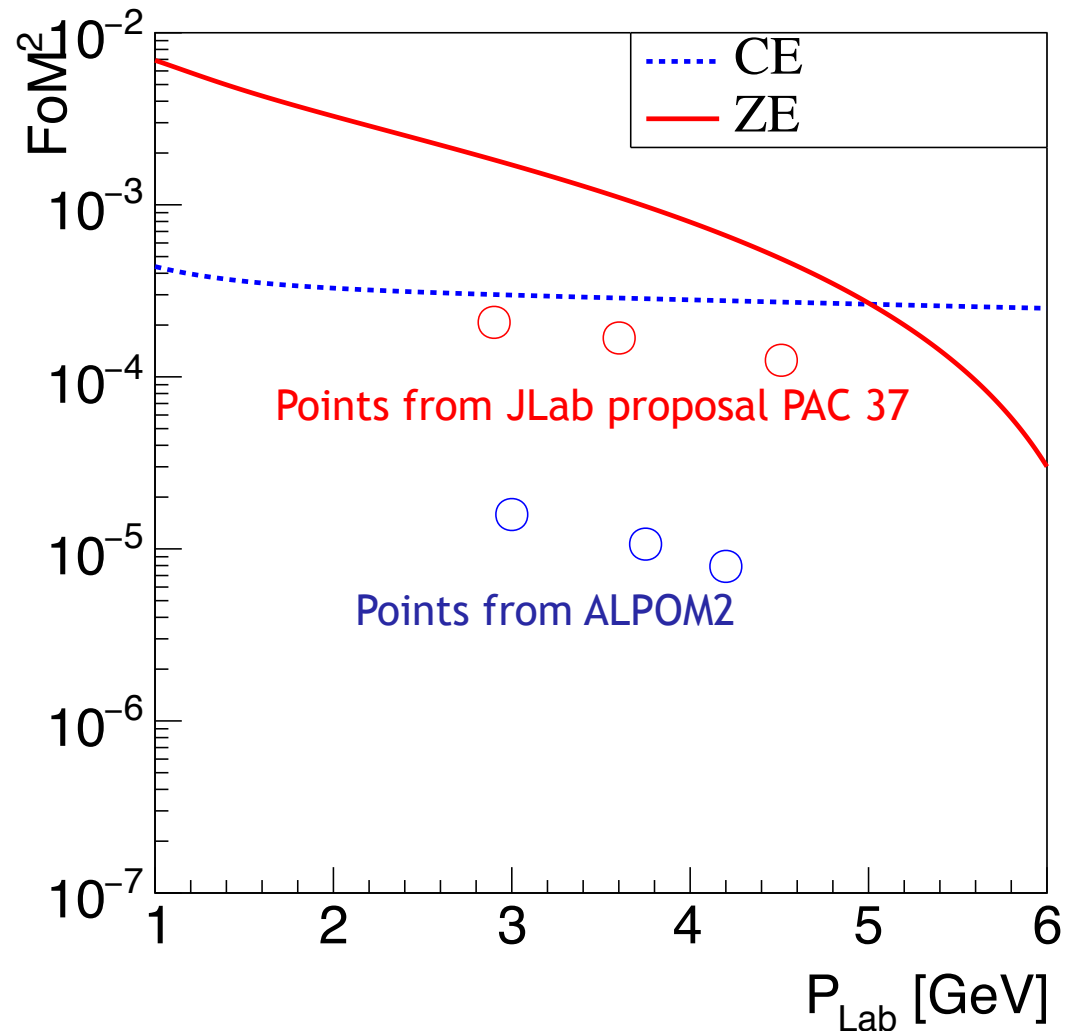


*$np \rightarrow np$  elastic scattering  
(zero exchange)*

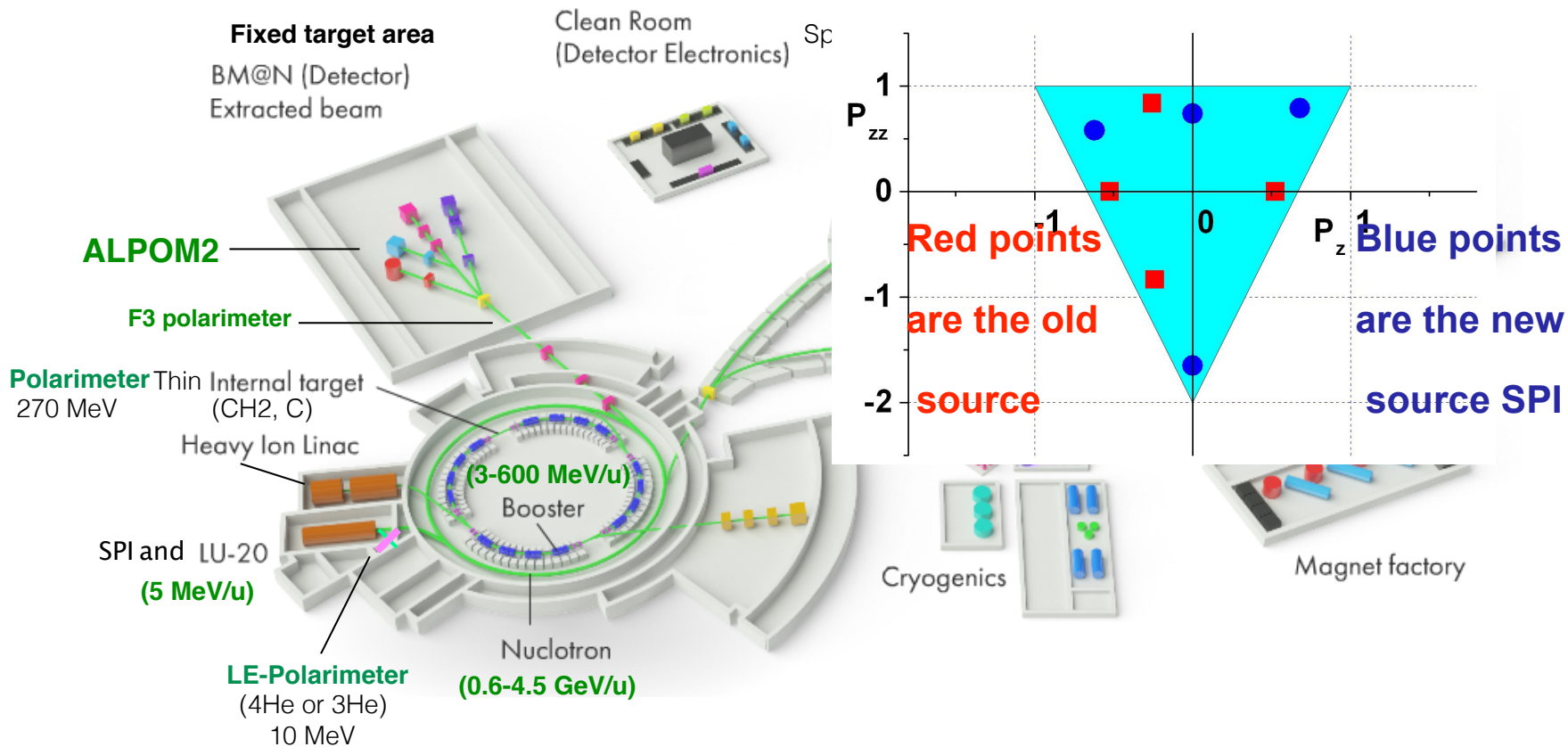
*$np \rightarrow pn$   
(charge exchange)*

# Figure of merit (100% efficiency)

From 1 to 5 GeV/c, ZE has larger Figure of merit due to its larger total cross section. After 5 GeV, as cross section becomes really small, figure of merit is dominated by analyzing power, then CE becomes bigger.



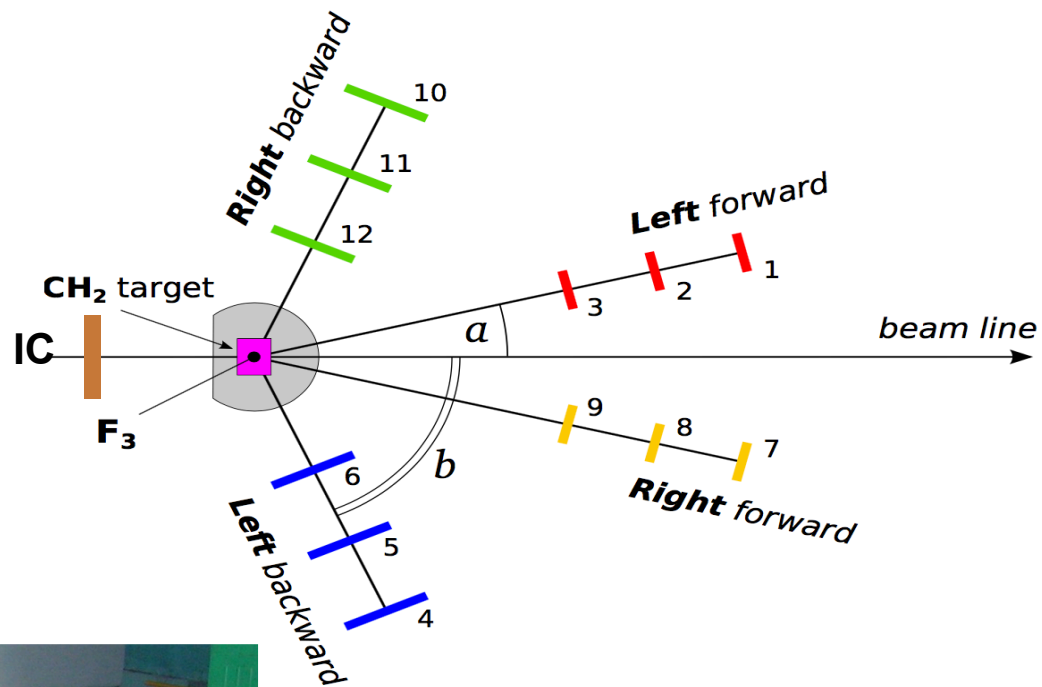
# ALPOM2 @Nuclotron



**Polarized neutrons and protons are obtained from the Nuclotron deuteron beam with momentum up to 13 GeV/c that undergoes a breakup reaction through a 8 cm thick Be target, installed about 100 m upstream of the polarimeter.**

# Beam polarization measurement

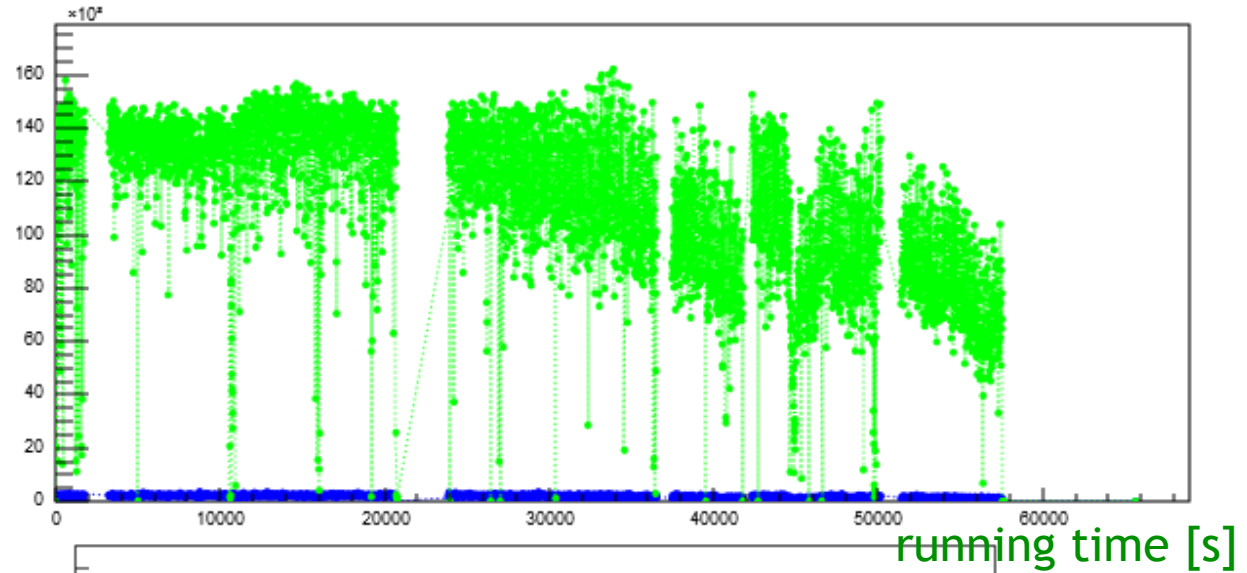
## F3 Polarimeter



by Shindin Roman

# Online Beam monitor

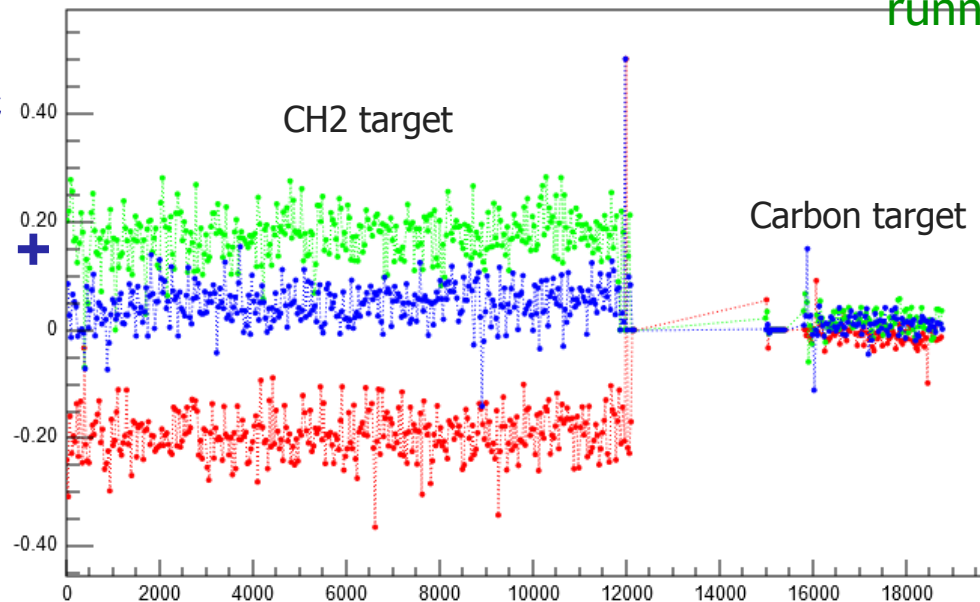
Beam stability



When  $P=3.75$  GeV/c

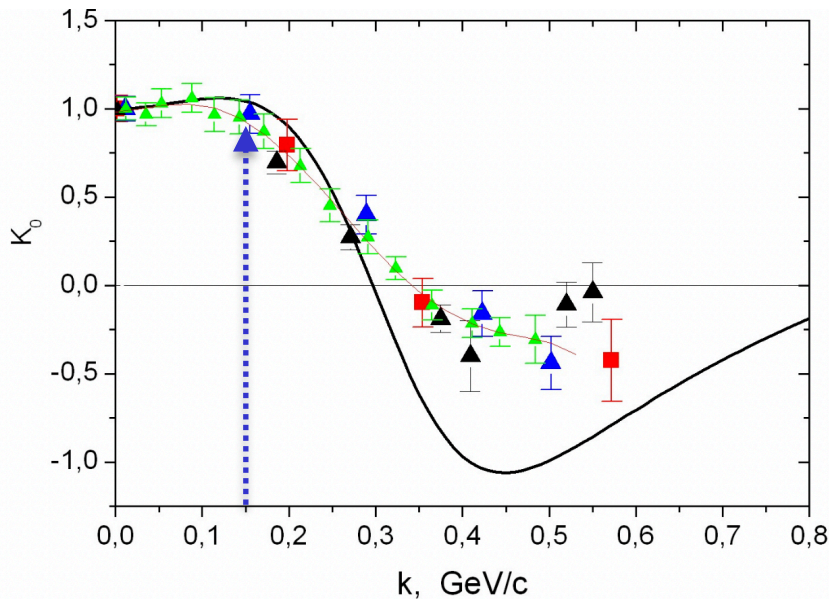
$A_y = 0.2 \pm 8\%$  pol +

$$\begin{aligned} P^+ &= 0.593 \pm 0.005 \pm 0.047, \\ P^- &= -0.302 \pm 0.006 \pm 0.024. \end{aligned}$$

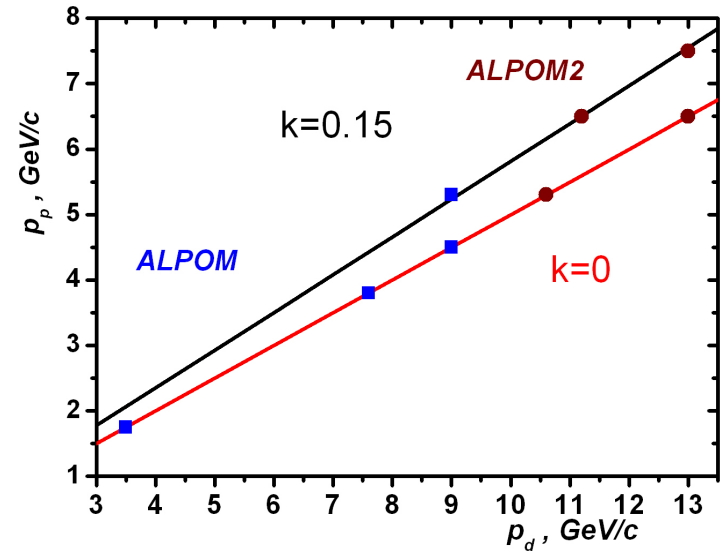


# Beam production from deuteron breakup

## Polarization transfer coefficient



## Momentum transfer



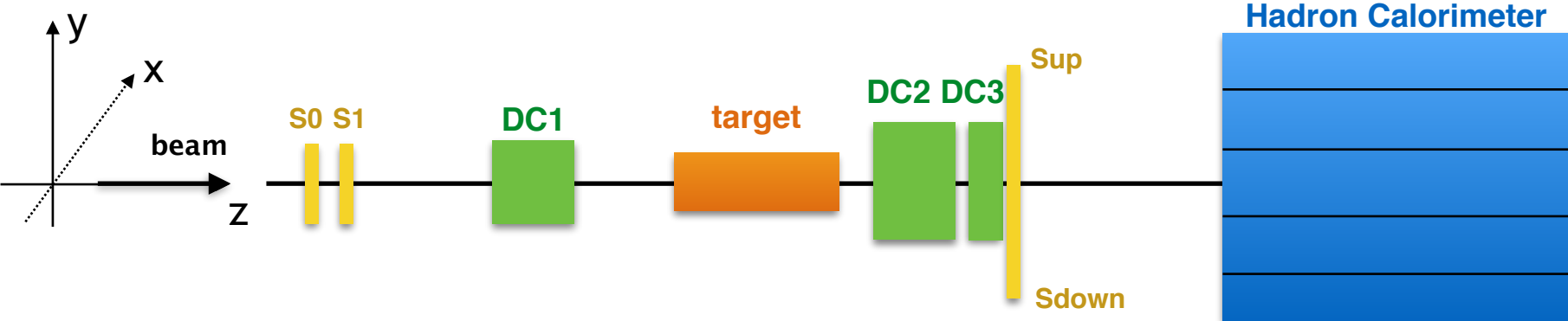
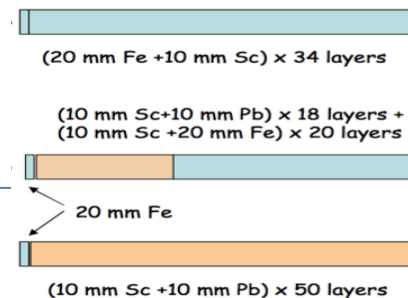
$$\kappa = \sqrt{\frac{m^2}{4\alpha(1-\alpha)} - m^2},$$

$$\alpha = \frac{E_p + p_{||}}{E_d + p_d},$$

**Ep proton energy**  
**p|| longitudinal momentum**

It is known from previous measurement that the polarization is totally transferred to the proton and neutron from the breakup, even for momenta larger than half of the deuteron momentum.

# ALPOM2 setup



Trigger for neutron beam:

active target, Sup, Sdown, and IC.

Trigger for proton beam:

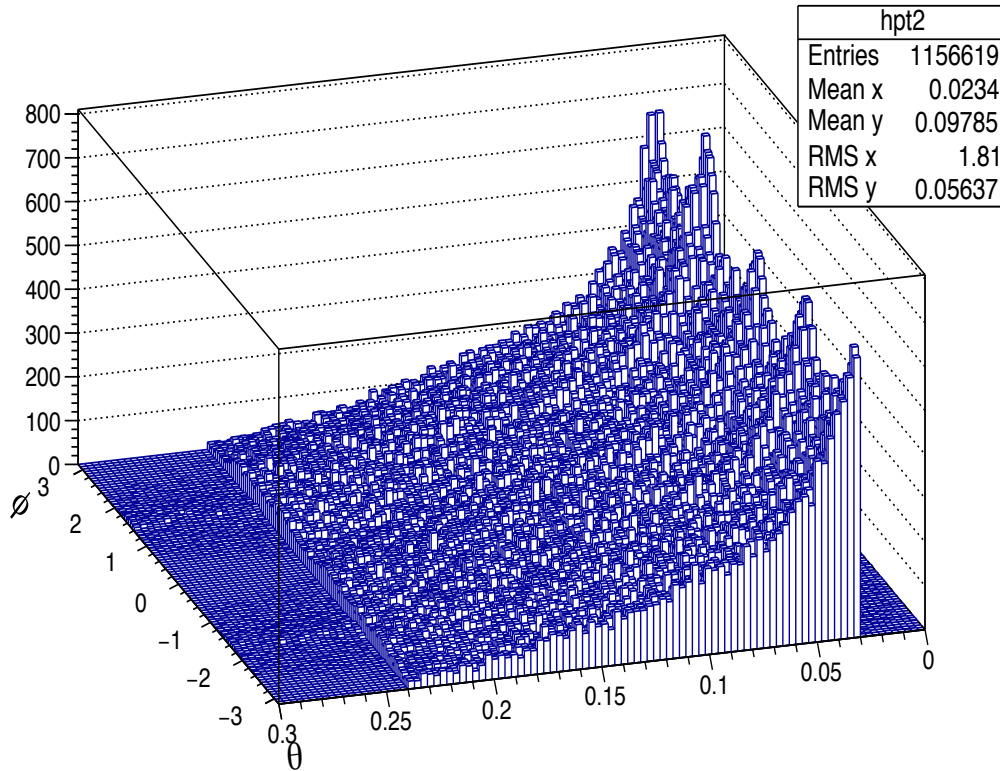
S0, S1, Sup, Sdown.

**Active target CH**  
**(CH<sub>2</sub>, Cu)**  
**For neutron**  
**(proton) A<sub>y</sub>**  
**measurement**

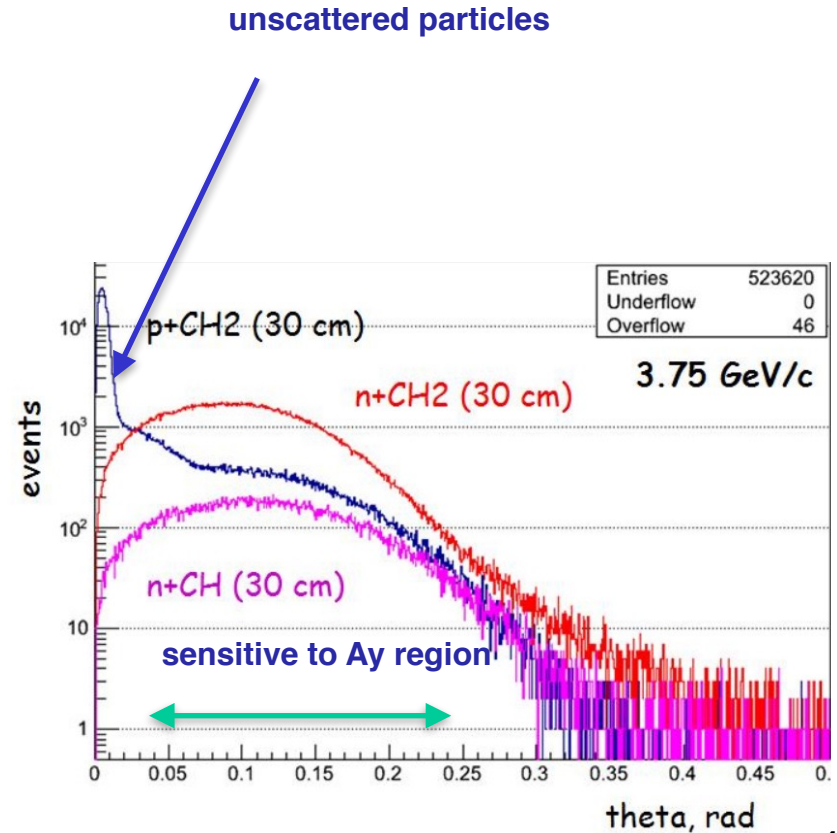
**Hadron calorimeter with**  
**the scintillator uses**  
**moduli of different size**  
**and composition at**  
**different distance around**  
**the beam axis**

# Particle distribution ( $\theta$ , $\varphi$ )

Pol=2 ThetaPhi spectrum

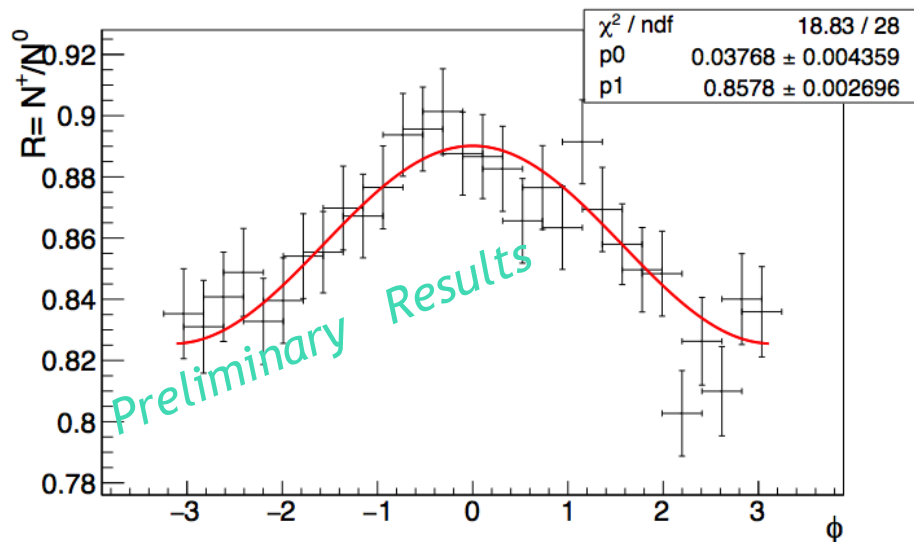


So cut off the region  
 $\theta < 0.03$  and  $\theta > 0.24$ .

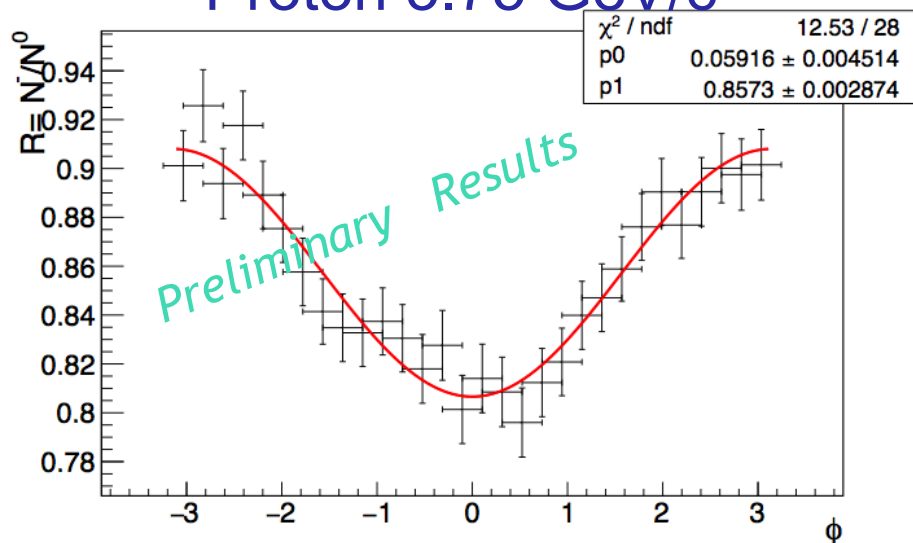




# Extraction of Analyzing power



Proton 3.75 GeV/c



$$\frac{N^+}{N_0} = \frac{N_0^+}{N_0} (1 + |P^+| A \cos \phi),$$

$$\frac{N^-}{N_0} = \frac{N_0^-}{N_0} (1 - |P^-| A \cos \phi),$$

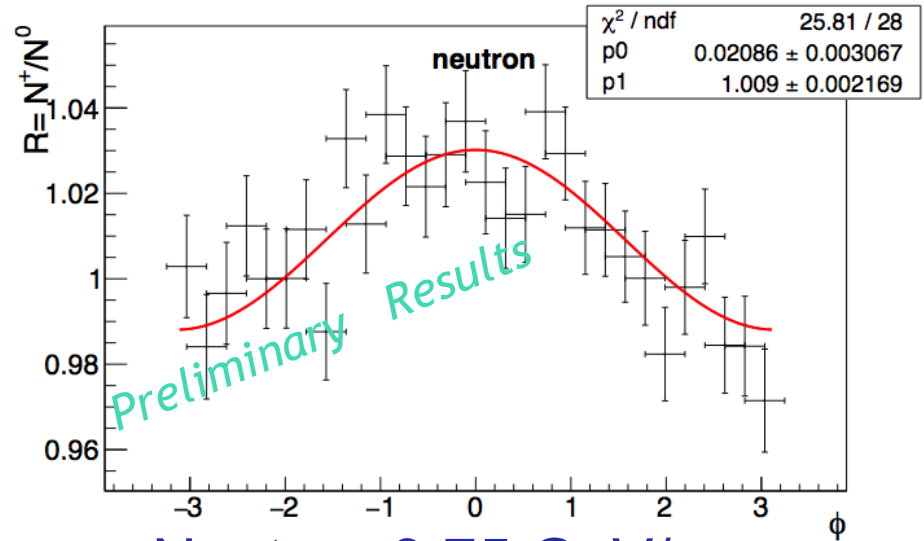
$$\Delta R = \frac{\sqrt{N^\pm \cdot (N^\pm / N_0 + 1)}}{N^\pm}.$$

# Extraction of Analyzing power

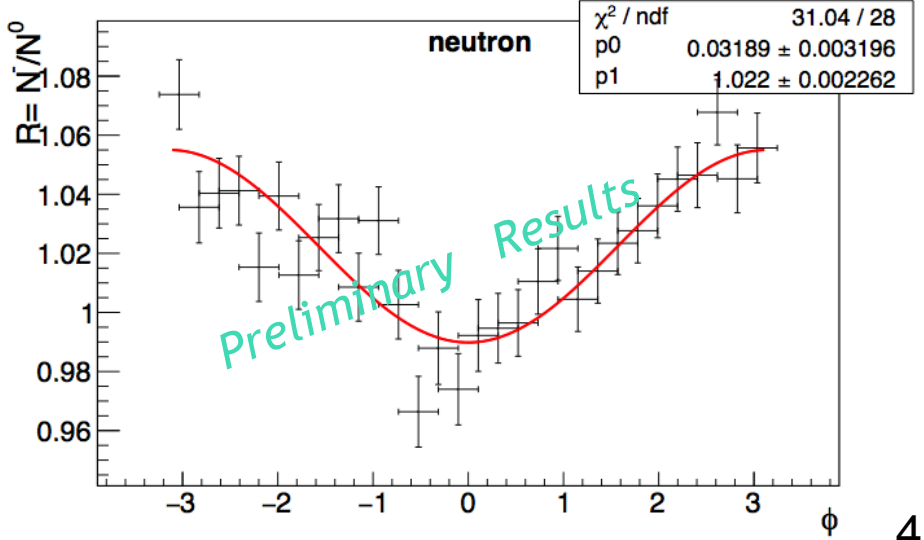
$$\frac{N^+}{N_0} = \frac{N_0^+}{N_0} (1 + |P^+| A \cos \phi),$$

$$\frac{N^-}{N_0} = \frac{N_0^-}{N_0} (1 - |P^-| A \cos \phi),$$

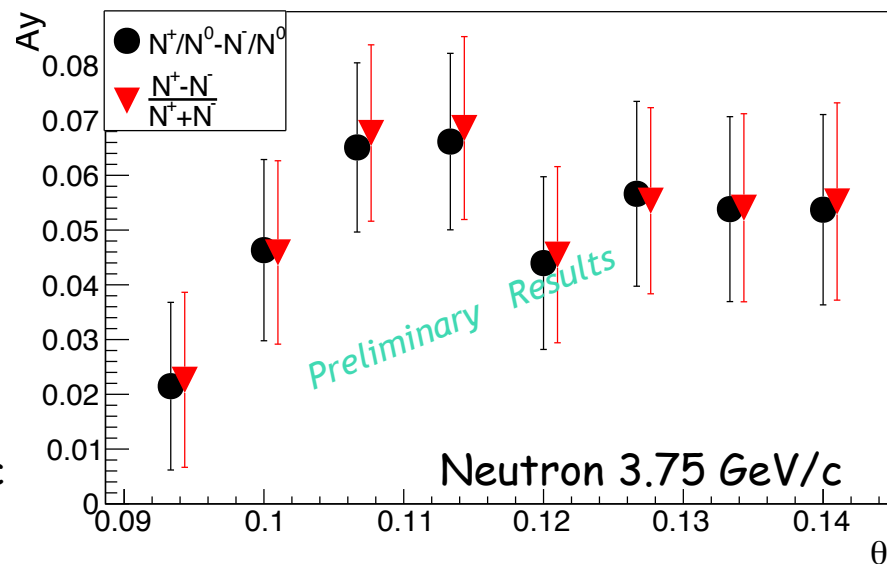
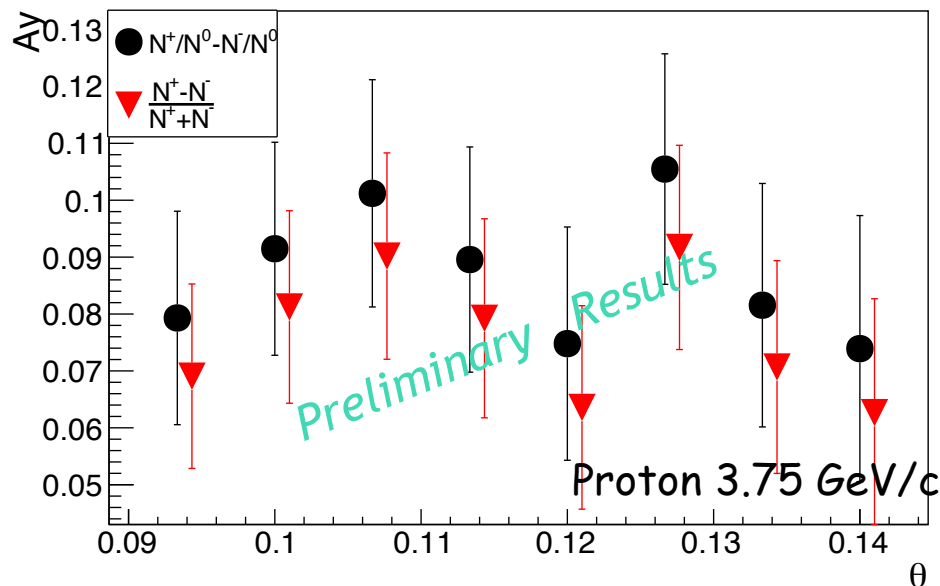
$$\Delta R = \frac{\sqrt{N^\pm \cdot (N^\pm/N_0 + 1)}}{N^\pm}.$$



Neutron 3.75 GeV/c



# Analyzing power



$$R_1 = \frac{a - b}{c} = \frac{N^+ - N^-}{N_0} = A \cos \phi (|P^+| + |P^-|) \quad R_2 = \frac{a - b}{a + b} = \frac{N^+ - N^-}{N^+ + N^-} = \frac{A \cos \phi (|P^+| + |P^-|)}{2 + A \cos \phi (|P^+| - |P^-|)}$$

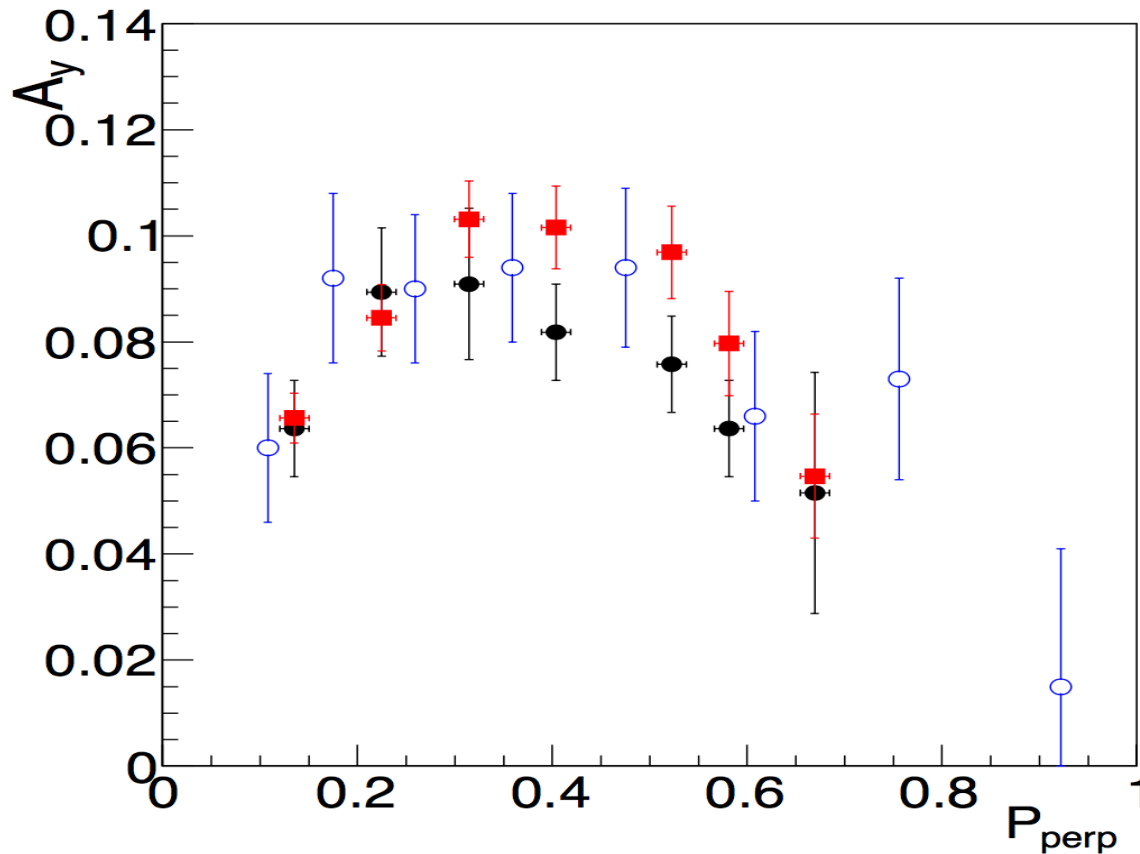
$$\Delta R_1 = \sqrt{\left(\frac{\partial R_1}{\partial a}\right)^2 \cdot \Delta a^2 + \left(\frac{\partial R_1}{\partial b}\right)^2 \cdot \Delta b^2 + \left(\frac{\partial R_1}{\partial c}\right)^2 \cdot \Delta c^2}$$

$$= \sqrt{\frac{a+b}{c^2} + \frac{(-a+b)^2}{c^3}}$$

$$\Delta R_2 = \sqrt{\left(\frac{\partial R_2}{\partial a}\right)^2 \cdot \Delta a^2 + \left(\frac{\partial R_2}{\partial b}\right)^2 \cdot \Delta b^2}$$

$$= \sqrt{\frac{4ab}{a+b}} \cdot \frac{1}{a+b}$$

# Comparison of analyzing powers from ALPOM2 and ALPOM



- The full symbols from ALPOM2
- The empty symbols from ALPOM

# Summary Part II

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- We have done the measurement of proton and neutron analyzing power at 3.0, 3.75, and 4.2 GeV/c

Proton: more precise results have been achieved

Neutron: the analyzing power on C, CH has been measured for the first time.

Next:

Measurement for higher momenta up to 7.5 GeV/c proton and 5.3 GeV/c neutron has required in the proposal will be performed soon.

**Thank you!**

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