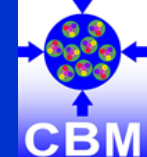


Strangeness Production



(with focus on FAIR energy range)

Outline

Part I

History

Quarkmodel

Strange hadrons

Strange particle yields in heavy ion collisions

Strangeness enhancement

The „horn“

Thermal Model description

Thermalization times

Connection to phase transition

Equation-of-state from subthreshold kaon production

Part II

In medium modification of hadrons

Connection to chiral symmetry of QCD

Predictions of transport model (PHSD)

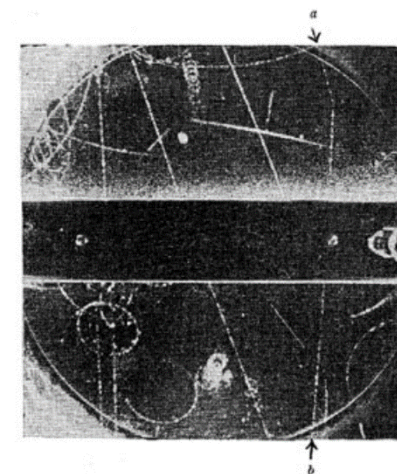
Flow of kaons

Hypernuclei

Λ (1405)

Deeply bound kaonic states

~ 1950 many V particles (~100):



kaon discovery

G.D. Rochester; C.C. Butler (1947).

Nature. **160** (4077): 855–857

1953 Murray Gell – Mann, Abraham Pais, Kazuhiko Nishijima introduce „strangeness“

Description of „discovery“ process:

M. Gell-Mann. STRANGENESS. *Journal de Physique Colloques*, 1982, 43 (C8), pp.C8-395-C8-408. <10.1051/jphyscol:1982825>. <jpa-00222385>

<https://hal.archives-ouvertes.fr/jpa-00222385>

usually appears as a paradox. but a paradox is after all just one way of having your path blocked ; in art the blocking is manifested differently. Having filled your mind with the problem and the difficulty you may then find that in an odd moment while driving or shaving or while asleep and dreaming (as in the case of Kekulé and the benzene ring) or through a slip of the tongue as in this case one may suddenly find the path unblocked. Perhaps the solution comes, in the language of the psychoanalyst (a language that is not very popular in scientific circles today), from the preconscious mind, the portion of our mind that is just out of awareness.

Gell-Mann–Nishijima formula

$$Q = I_3 + \frac{1}{2}(B + S) = I_3 + \frac{1}{2} Y$$

Q – electric charge

I – Isospin

B – Baryon number

S – Strangeness

Y – Hypercharge

Key argument: Is reaction $n + n \rightarrow \Lambda + \Lambda$ possible ?

Conserved quantities in strong interactions:

Baryon number B, Strangeness S, Isospin I, I_3

$$S = - (n(\text{s-quarks}) - n(\text{anti_s-quarks}))$$

Ansatz: mass of strange quark (~ 150 MeV) small on nucleon scale (1 GeV).
u,d,s approximately degenerate.

u,d,s – symmetry can be expressed by unitary matrix containing 9 complex numbers (with 18 real parameter):

$$\begin{pmatrix} u' \\ d' \\ s' \end{pmatrix} = \hat{U} \begin{pmatrix} u \\ d \\ s \end{pmatrix} = \begin{pmatrix} U_{11} & U_{12} & U_{13} \\ U_{21} & U_{22} & U_{23} \\ U_{31} & U_{32} & U_{33} \end{pmatrix} \begin{pmatrix} u \\ d \\ s \end{pmatrix}$$

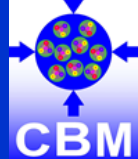
9 parameters are fixed from unitarity. $\hat{U}^\dagger \hat{U} = 1$

1 matrix is just the multiplication with complex phase.

The 8 remaining parameters have $\det U=1$ and form the SU(3) symmetry group.

Generators are 8 Hermitian matrices: $\vec{T} = \frac{1}{2} \vec{\lambda}$, $\hat{U} = e^{i\vec{\alpha} \cdot \vec{T}}$

Gell – Mann Matrices λ_i



Flavor SU(3): Quark states

$$u = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \quad d = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \quad s = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

$$u \leftrightarrow d \quad \lambda_1 = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_2 = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$u \leftrightarrow s \quad \lambda_4 = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} \quad \lambda_5 = \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix}$$

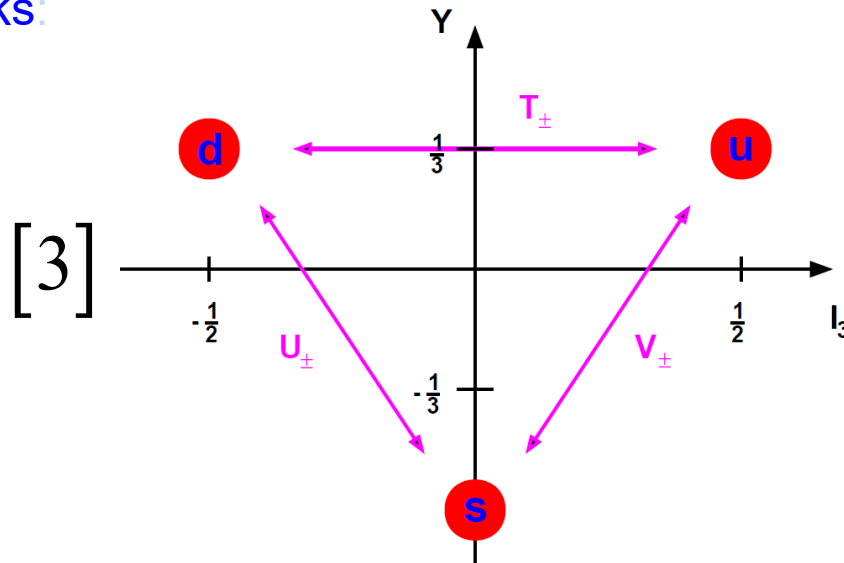
$$d \leftrightarrow s \quad \lambda_6 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \quad \lambda_7 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix}$$

$$\lambda_8 = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}$$

SU(3)_F – fundamental representations



Quarks:



Hypercharge Y:

$$Y = B + S$$

Baryon number B

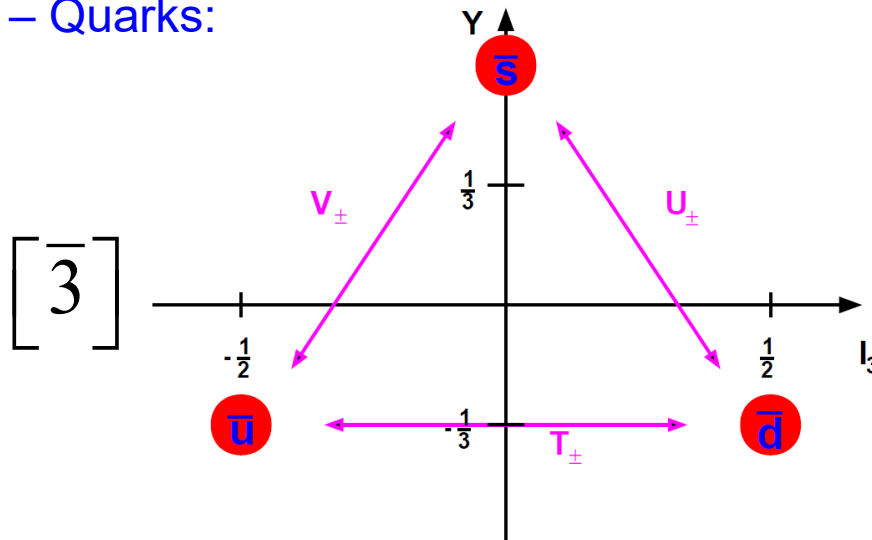
Strangness number S

Charge Q:

$$Q = I_3 + Y/2$$

3. component of isospin I_3

Anti – Quarks:



Ladder operators:

$$T_+ d = u, \quad T_- d = u$$

$$V_+ s = u, \quad V_- u = s$$

$$U_+ s = d, \quad U_- d = s$$

$$T_+ \bar{u} = -\bar{d}, \quad T_- \bar{d} = -\bar{u}$$

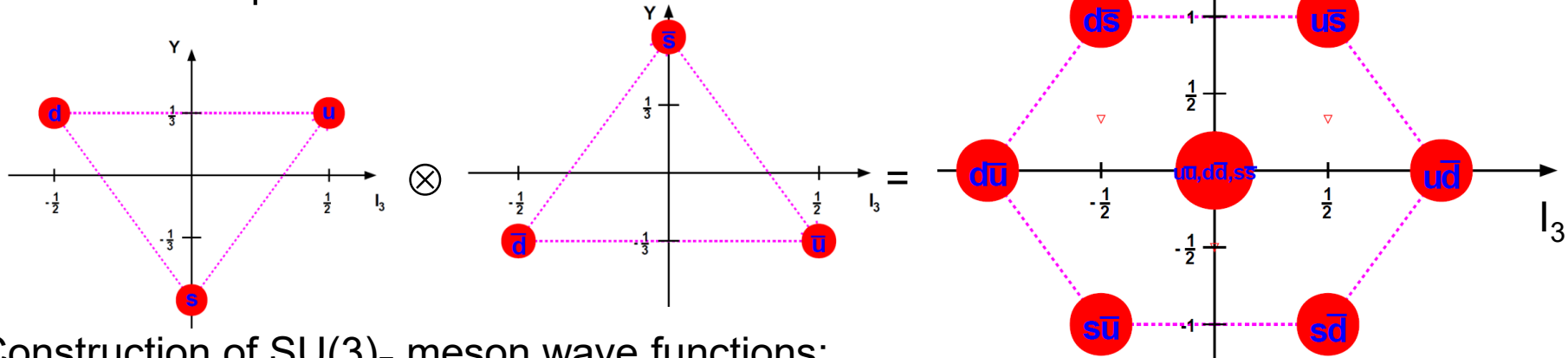
$$V_+ \bar{u} = -\bar{s}, \quad V_- \bar{s} = -\bar{u}$$

$$U_+ \bar{d} = -\bar{s}, \quad U_- \bar{s} = -\bar{d}$$

Light $SU(3)_F$ – (uds) – mesons



Quark – Anti-quark states:



Construction of $SU(3)_F$ meson wave functions:

add conjugate (antiparticle) triplet to each point of fundamental (particle) triplet

$$[3] \otimes [\bar{3}] = [8] \oplus [1]$$

triplet

antitriplet

octet

singlet

3 states with $(Y, I_3) = (0, 0)$:

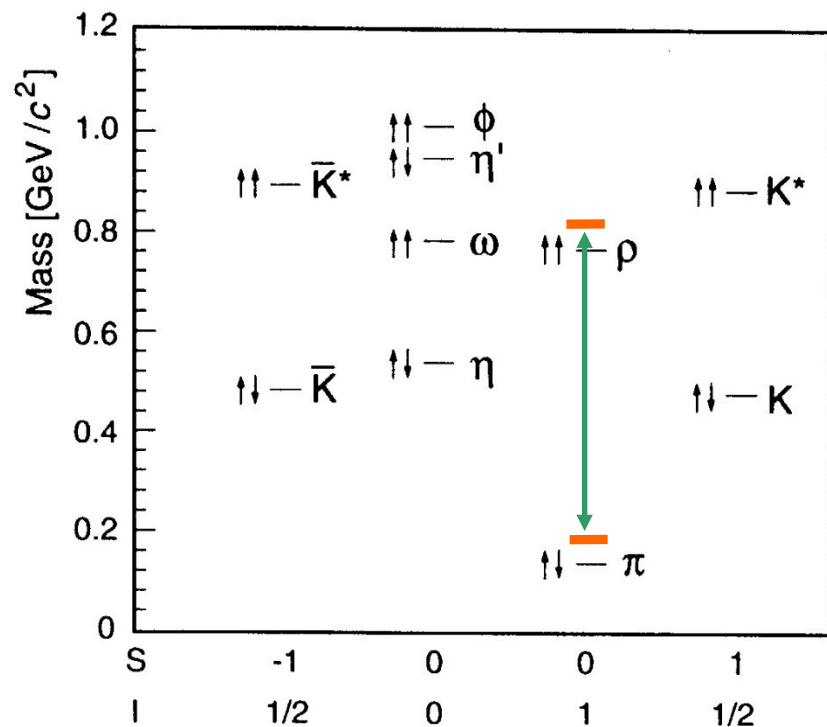
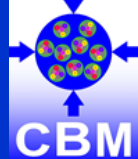
1) fully symmetric state:

2) neutral pion:

3) orthogonal state:

$$\begin{aligned} \{1 | 0, 0\rangle\} &= \frac{1}{\sqrt{3}} (|u\bar{u}\rangle + |d\bar{d}\rangle + |s\bar{s}\rangle) = |\eta'\rangle \\ \{8 | 1, 0\rangle\} &= \frac{1}{\sqrt{2}} (|u\bar{u}\rangle - |d\bar{d}\rangle) = |\pi^0\rangle \\ \{8 | 0, 0\rangle\} &= \frac{1}{\sqrt{6}} (|u\bar{u}\rangle + |d\bar{d}\rangle - 2|s\bar{s}\rangle) = |\eta\rangle \end{aligned}$$

The light meson mass spectrum



$J = 1$

Mass difference ~ 600 MeV

$J = 0$

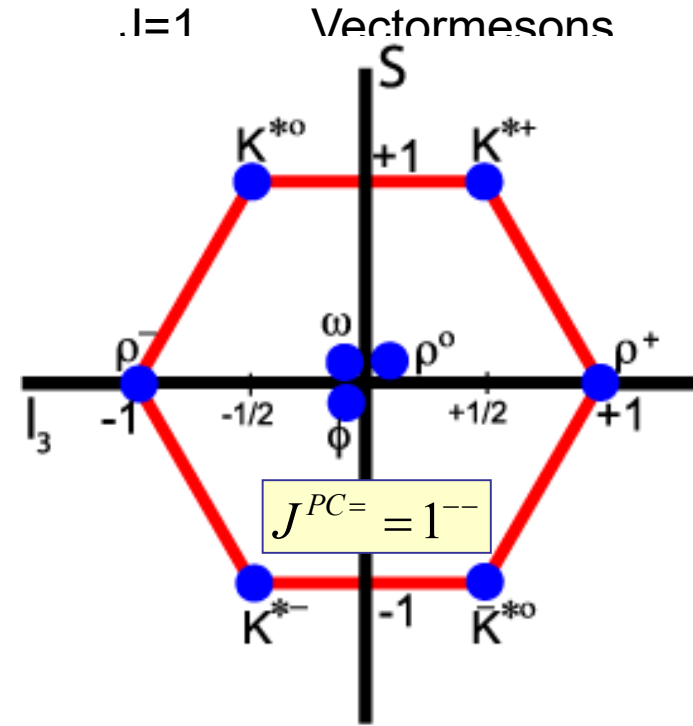
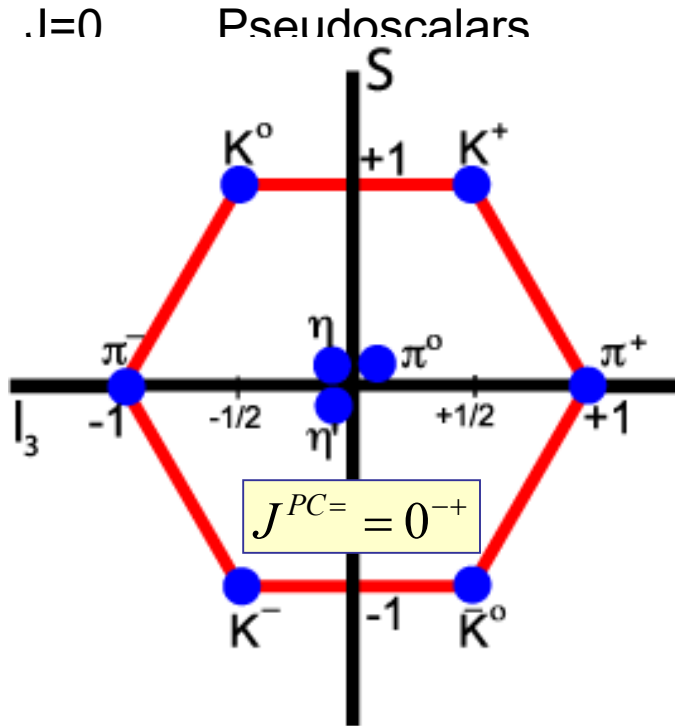
Mass splitting between pseudoscalar and vector mesons suggests color magnetic interaction:

$$\Delta M_J \propto \frac{\vec{\sigma}_q}{m_q} \cdot \frac{\vec{\sigma}_{\bar{q}}}{m_{\bar{q}}}$$

Light $SU(3)_F - (uds)$ – mesons



2 nonets exist due to spin with the same flavour wave functions:



Parity:

$$P = P(q)P(\bar{q})(-)^L = -(-)^L$$

Charge conjugation for neutral states:
(allowed Eigenvalues)

$$C = \underbrace{(-)}_{\text{interchange of fermions}} (-)^{S+1} (-)^L = (-)^{L+S}$$

Parity and C-parity are conserved in e.m. and strong interactions.

Quark model states

- For $q\bar{q}$ meson systems, let L to be the orbital angular momentum. The meson spin J is given by $|L-S| < J < |L+S|$, where $S=0$ (antiparallel quark spin) or $S=1$ (parallel quark spin)
- The parity P and charge parity C of the meson system can be expressed as:

$$P = (-1)^{L+1}$$

$$C = (-1)^{L+S}$$

S	0	1	0	1	1	1	0	...
L	0	0	1	1	1	1	2	...
J	0	1	1	0	1	2	2	...
J^{PC}	0⁻⁺	1⁻⁻	1⁺⁻	0⁺⁺	1⁺⁺	2⁺⁺	2⁻⁺	...
^{2S+1}L_J	¹S₀	³S₁	¹P₁	³P₀	³P₁	³P₂	¹D₂	...

Not all combinations of quantum numbers are possible in quark model

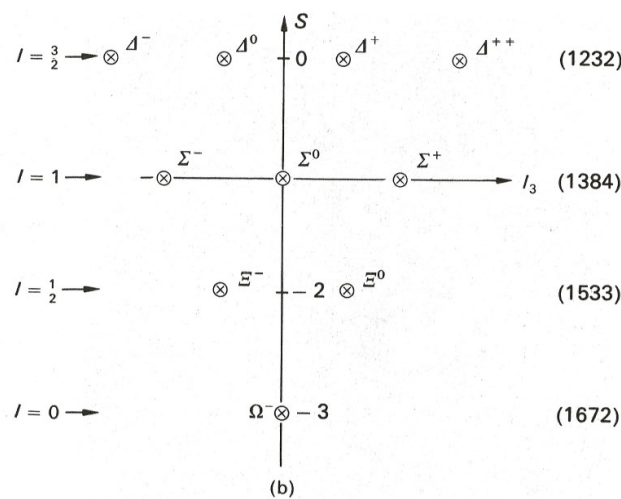
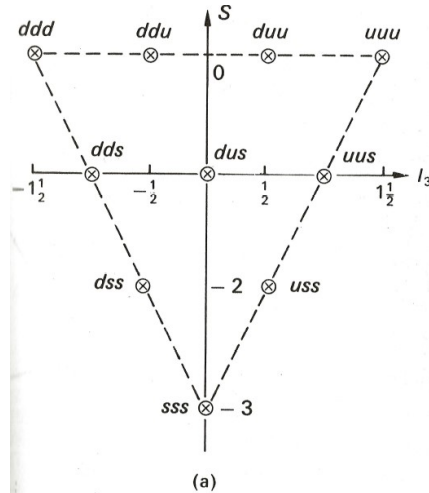
⇒ Exotic J^{PC} : 0^{--} , 0^{+-} , 1^{-+} , 2^{+-} , ...

Exotic mesons can have these J^{PC} due to additional degrees of freedom.

The $SU(3)_F$ – baryon multiplets



Baryon decuplet: $J=3/2$



Mass (MeV)

(Figs.: Perkins)

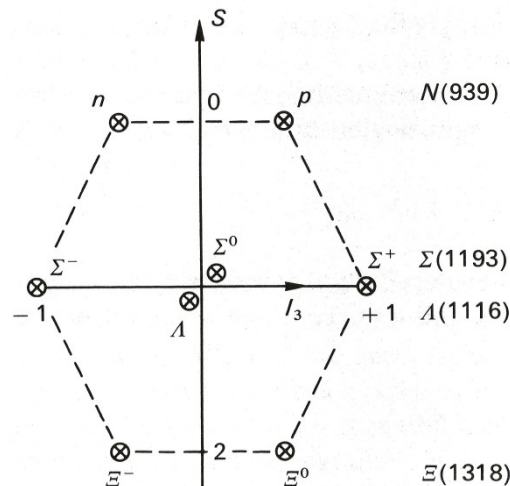
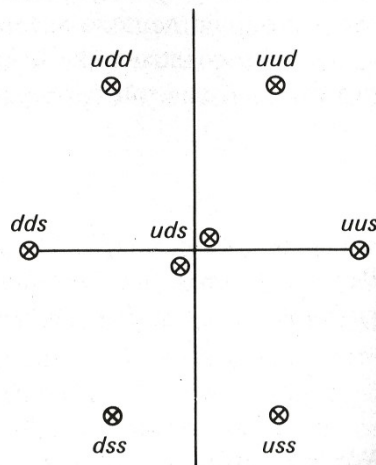
ΔM (MeV)

152

149

139

Baryon octet: $J=1/2$



Historically:

Gell-Mann – Okubo mass formula

$$M = M_0 + M_1 Y + M_2 \left(I(I+1) - \frac{Y^2}{4} \right)$$

Ω^- - discovery

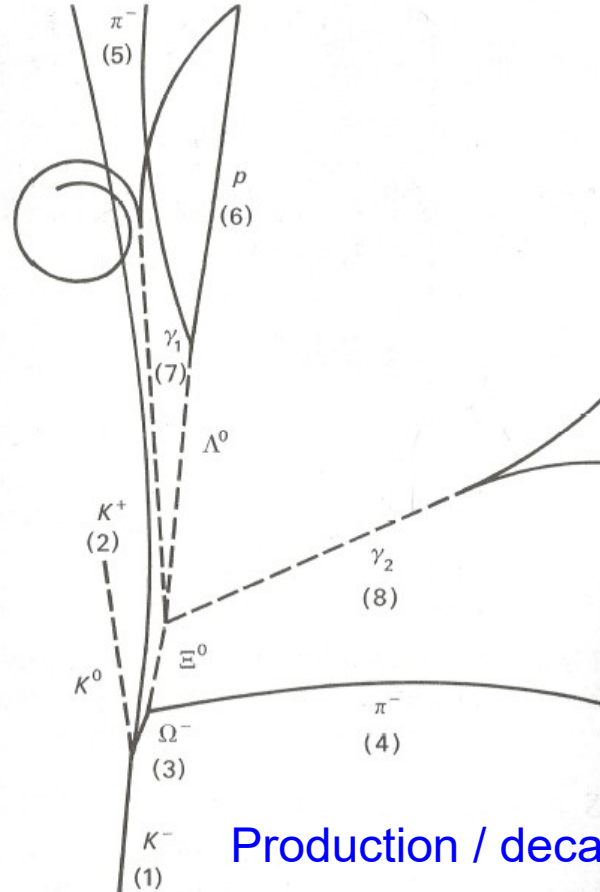


V. Barnes et al., PRL 12, 204 (1964)

Details:

K^- - beam, 5GeV, AGS @ BNL

100.000 bubble chamber pictures



Production / decay chain:

$$K^- + p \rightarrow \Omega^- + K^0 + K^+$$

$$\Omega^- \rightarrow \Xi^0 + \pi^-$$

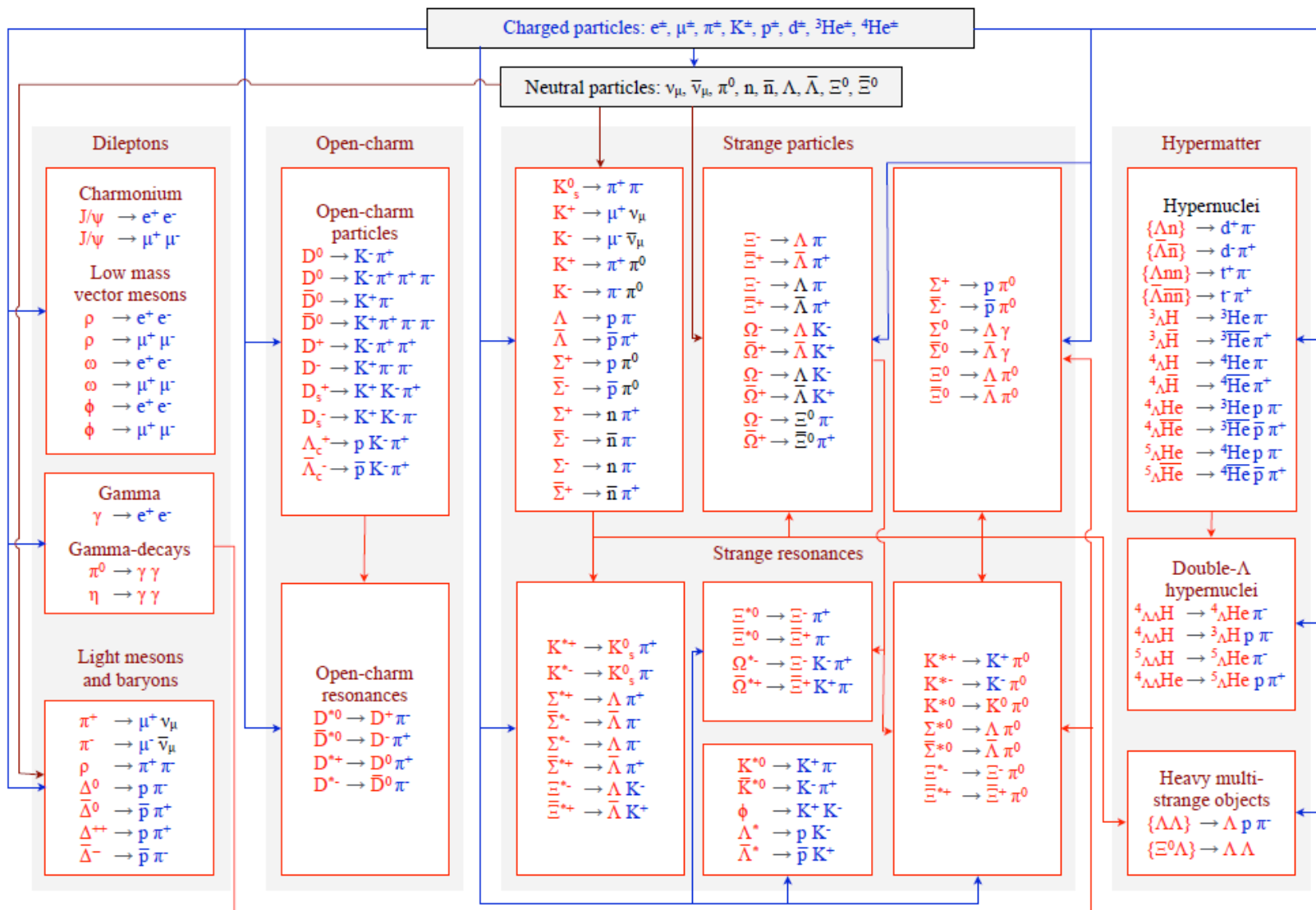
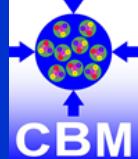
$$\Xi^0 \rightarrow \Lambda^0 + \pi^0$$

$$\Lambda^0 \rightarrow p + \pi^-$$

$$\pi^0 \rightarrow \gamma + \gamma$$

Groundstate strange hadrons decay by weak interaction
=> long lifetimes

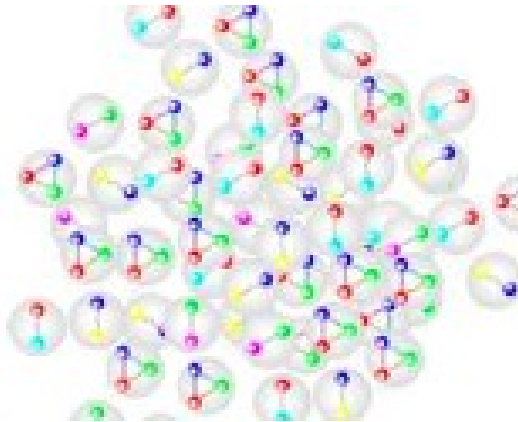
KF Particle Finder



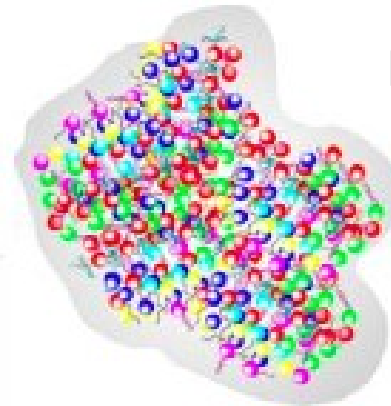
Strangeness as probe for QCD matter



hadronic



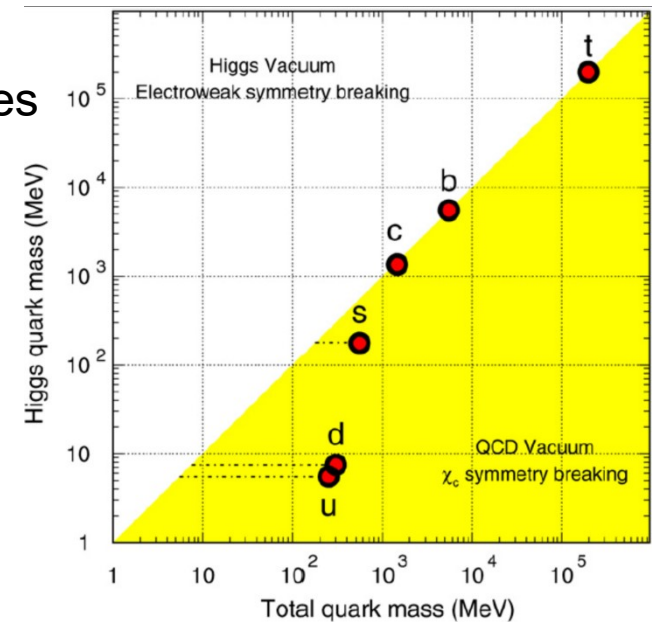
partonic



No strangeness in initial state

Strange hadrons offer a wide variety of mass scales
probing different energy scales

Strange quarks probe chiral symmetry



Quark masses



Static picture of hadrons
constituent quark masses

Ansatz:

$$M_{hadron} = \sum_q m_q + \Delta M_J$$

J – spin of hadron
(spin – spin interaction of quarks)

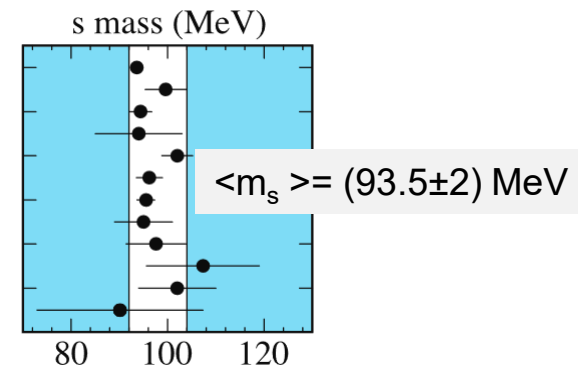
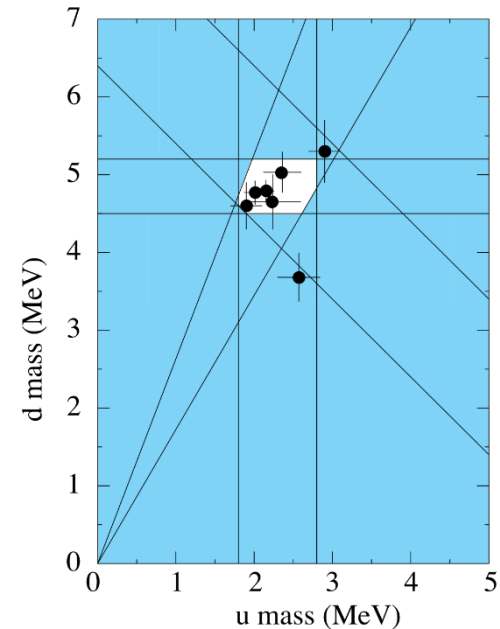
Result:

$$m_{u,d} \approx 310 \text{ MeV} / c^2$$

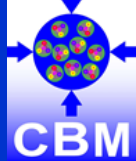
$$m_s \approx 483 \text{ MeV} / c^2$$

dynamic picture
current quark masses

<http://pdg.lbl.gov/2017/reviews/rpp2016-rev-quark-masses.pdf>



Experiments with Strangeness Measurements



GSi-SIS

FOPI, KAOS, HADES

BNL-AGS

E866, E877, E891, E895, ...

CERN-SPS (Pb beam)

WA97, NA44, NA45, NA50
NA49, NA57, NA61

BNL-RHIC

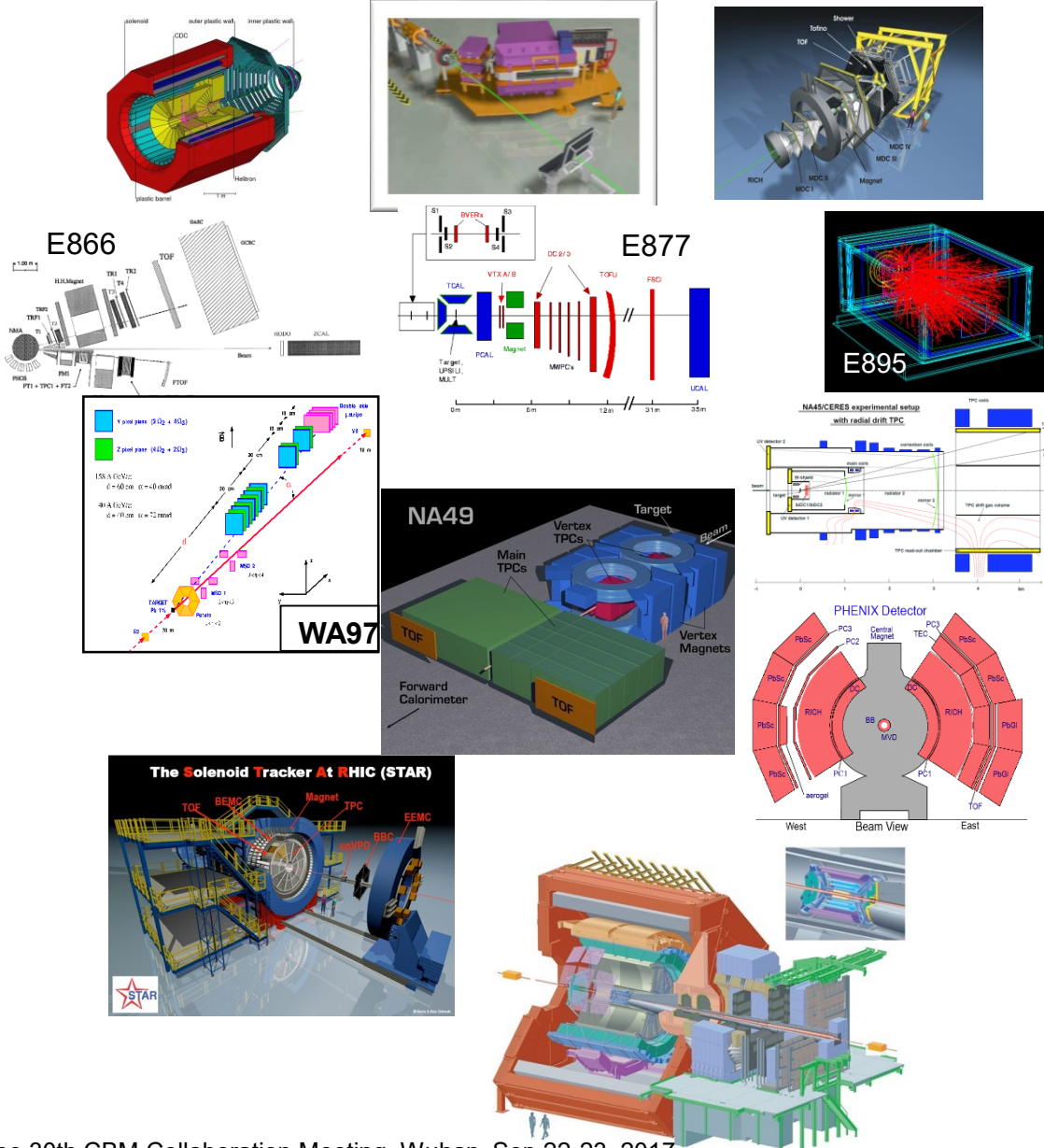
STAR, PHENIX, BRAHMS

CERN-LHC

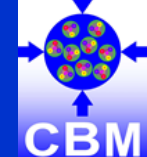
ALICE

New low energy programs

CBM@FAIR, NICA

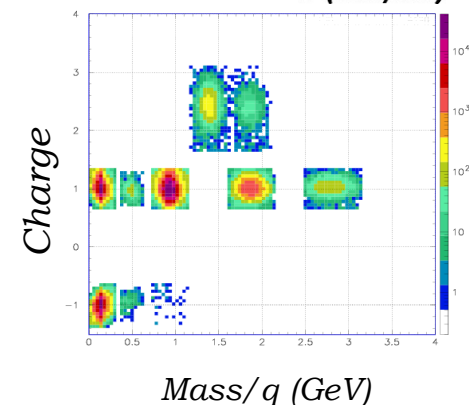
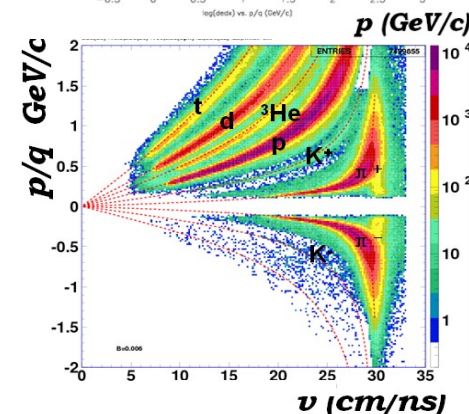
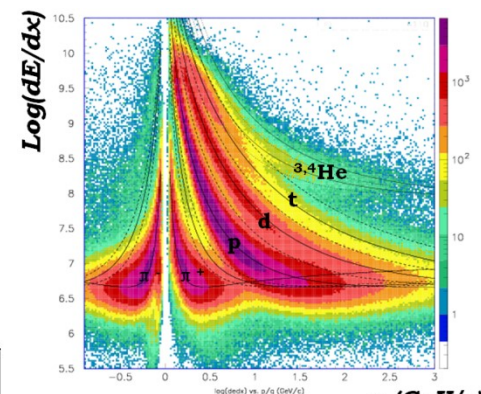
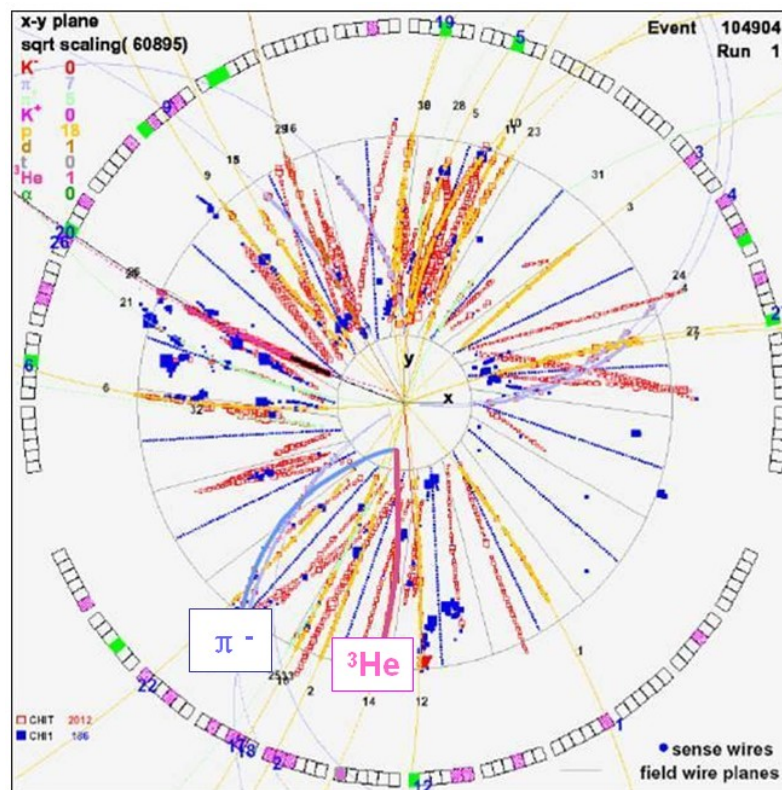


Strange particle reconstruction



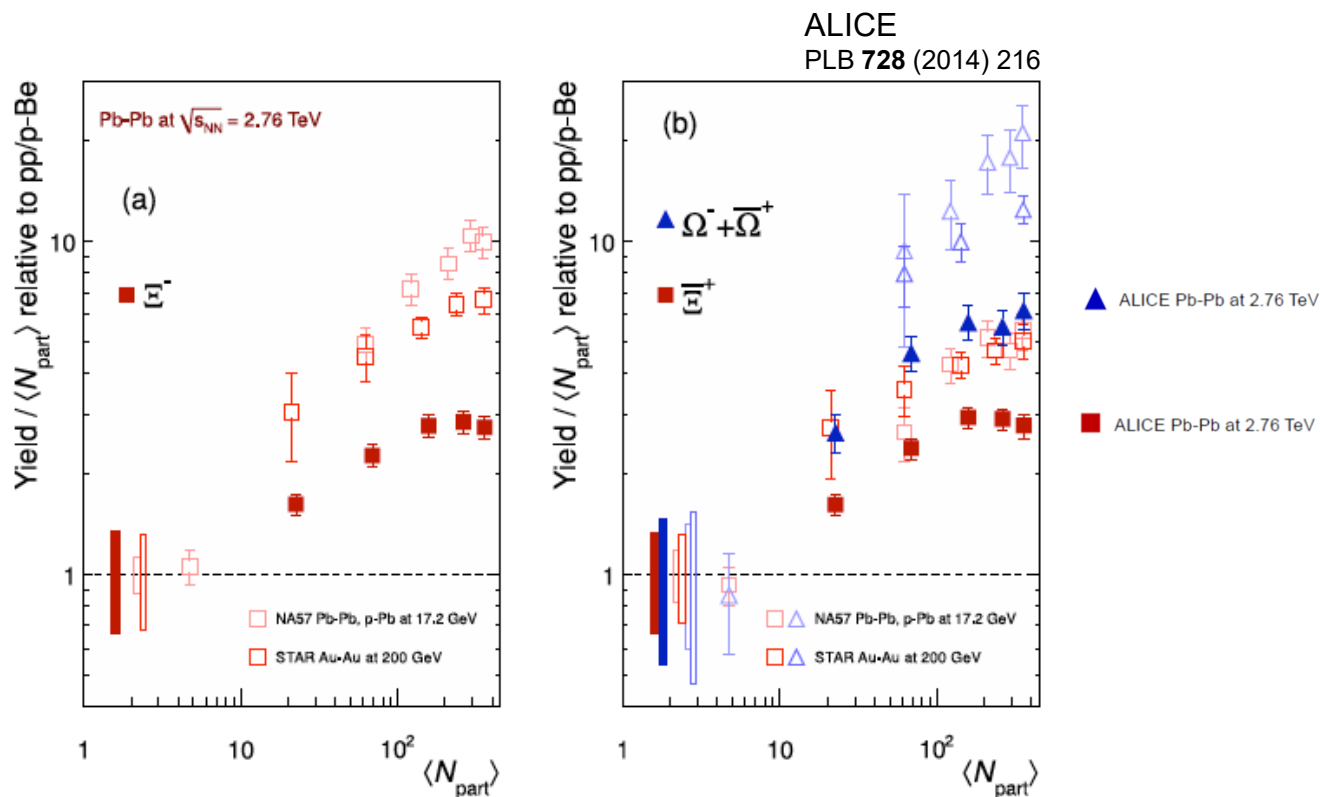
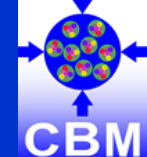
Particle identification,
coverage of phase space,
spectral shapes,
extrapolation to uncovered regions,
...

$$\Lambda t \rightarrow {}^3\text{He} + \pi^-$$



FOPI @ SIS18 of GSI
Ni+Ni @ 1.91 AGeV
S325e (2008), ~ 60 M events

Strangeness production



$$\text{Enhancement factor: } E = \frac{2}{N_{part}} \left[\frac{dN}{dy} (Pb + Pb) \Big|_{y=0} / \frac{dN}{dy} (p + p) \Big|_{y=0} \right]$$

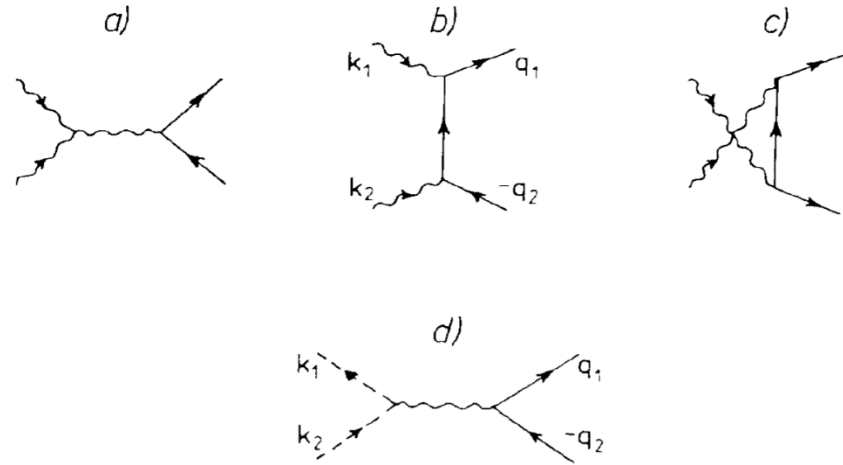
Enhancement factor for Ω :	SPS	20
(in central collisions)	RHIC	12
	LHC	6

Strangeness enhancement as QGP signature

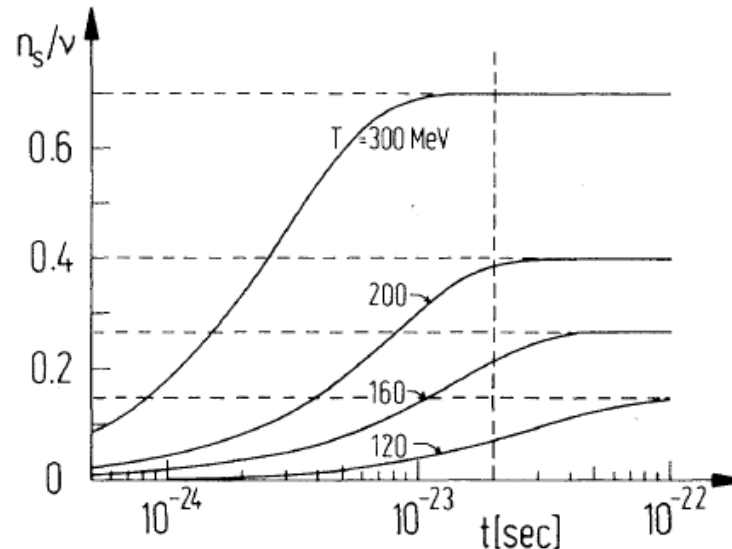


P. Koch, B. Müller, J. Rafelski, Phys. Rep. 142 (1986) 167

Elementary production processes:



Strangeness fraction



Relaxation of s-Quarks
in a QGP within few fm/c
 $\approx$ lifetime of the fireball

Expectation:

More strangeness production in A+A relative to p+p if QGP was formed

Statistical Hadronization Model (Thermal model)



P. Braun-Munzinger et al., arXiv:nucl-th/0304013

Chemical thermal model:

assume a common 'surface' at which all particles decouple (inelastic collisions stop)

Grand canonical formulation (i.e. energy and particle exchange with heat bath)

Partition function:

$$Z^{GC}(T, V, \mu_Q) = \text{Tr} \left[e^{-\beta \left(H - \sum_i \mu_{Q_i} Q_i \right)} \right]$$

Q_i = conserved quantum numbers (baryon number, strangeness, isospin, charm,...)

$\beta = 1/T$, T = Temperature

H = Hamiltonian of non-interacting hadron gas

Decomposition into individual hadronic species:

$$\ln Z^{GC}(T, V, \mu) = \sum_i \ln Z_i^{GC}(T, V, \mu)$$

Thermal model for particle production



P. Braun-Munzinger et al., arXiv:nucl-th/0304013

Chemical equilibrium concept.

Density of particle species i :

$$n_i(\mu, T) = \frac{N_i}{V} = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int \frac{p^2 dp}{e^{\frac{E_i - \mu_i}{T}} \pm 1}$$
$$\mu_i = \mu_B B_i + \mu_S S_i + \mu_{I_3} I_{3,i}$$

“+” for fermions, “-” for bosons

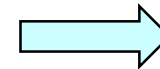
g_i – spin degeneracy factor

Chemical potentials μ_i are constrained by conservation of quantum numbers:

baryon number: $V \sum_i n_i B_i = Z + N \rightarrow V$

strangeness: $V \sum_i n_i S_i = 0 \rightarrow \mu_S$

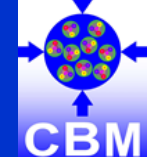
charge: $V \sum_i n_i I_{3,i} = \frac{Z - N}{2} \rightarrow \mu_{I_{3,i}}$



3 equations,
5 unknowns

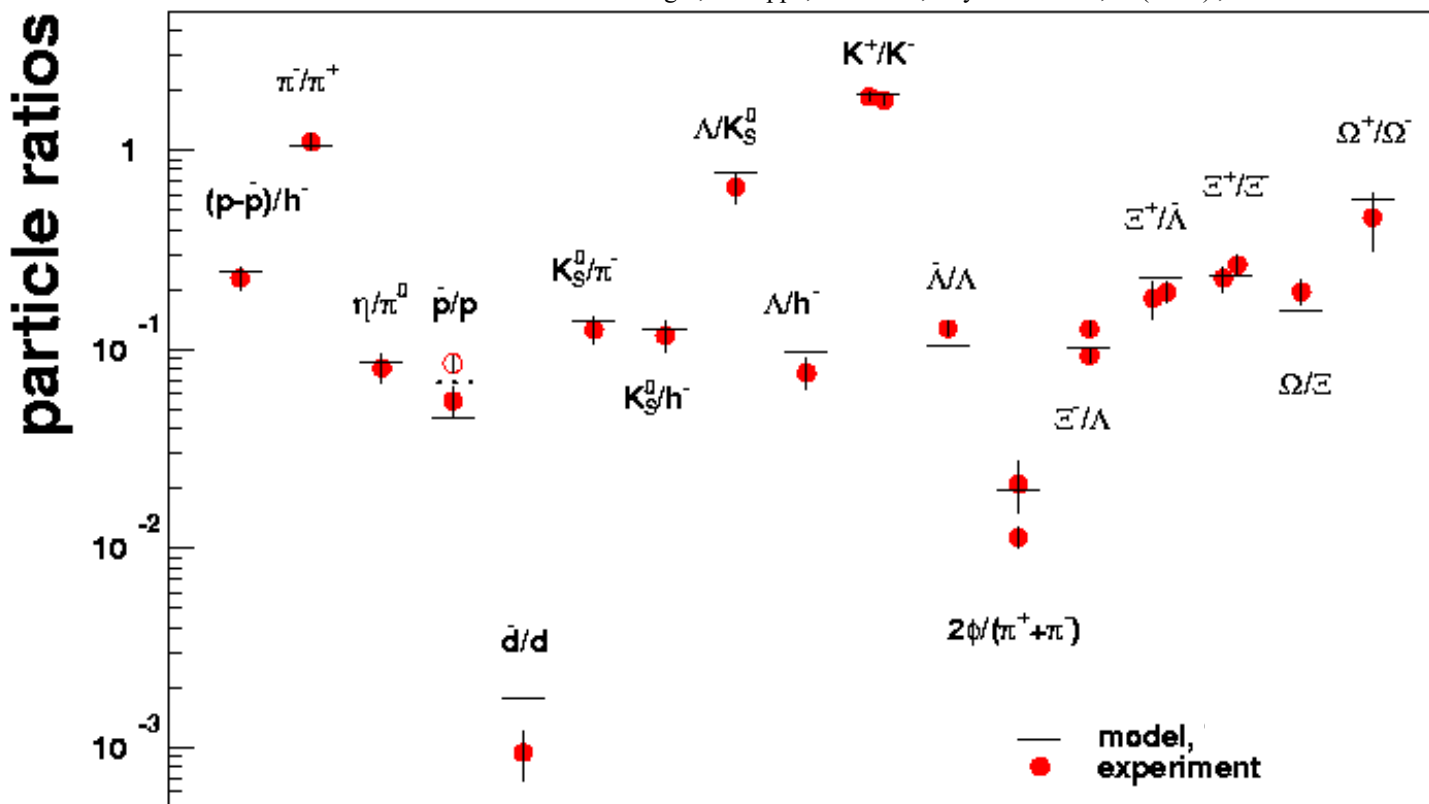
↓
2 free parameter

Chemical equilibrium



Example: SPS data, $E_{\text{beam}}=158 \text{ AGeV}$, Pb+Pb

P. Braun-Munzinger, I. Heppe, J. Stachel, Phys.Lett.B465, 15(1999), *nucl-th/9903010*



Model parameter:

$$T = 168 \pm 2.4 \text{ MeV}$$

$$\mu_B = 266 \pm 5 \text{ MeV}$$

Note: volume is not needed for
description of particle ratios.

$$\mu_S = 71.1 \text{ MeV}$$

$$\mu_{I_3} = -5. \text{ MeV}$$



4 January 1996

PHYSICS LETTERS B

Physics Letters B 365 (1996) 1–6

Thermal and hadrochemical equilibration in nucleus-nucleus collisions at the SPS

P. Braun-Munzinger, J. Stachel, J.P. Wessels, N. Xu¹

Department of Physics, State University of New York at Stony Brook, Stony Brook, NY 11794 – 3800, USA

Interpretation in bag model:

1. order phase transition: latent heat

densities

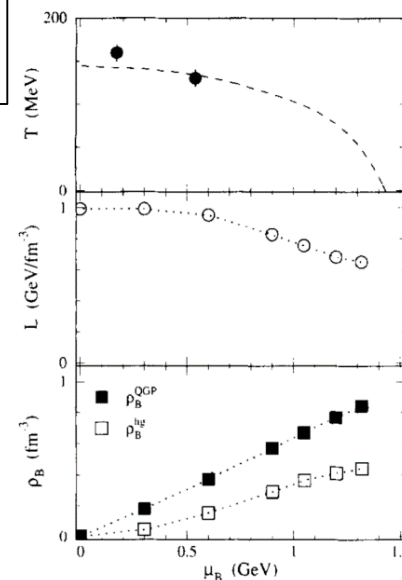
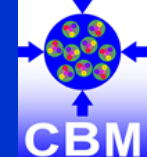


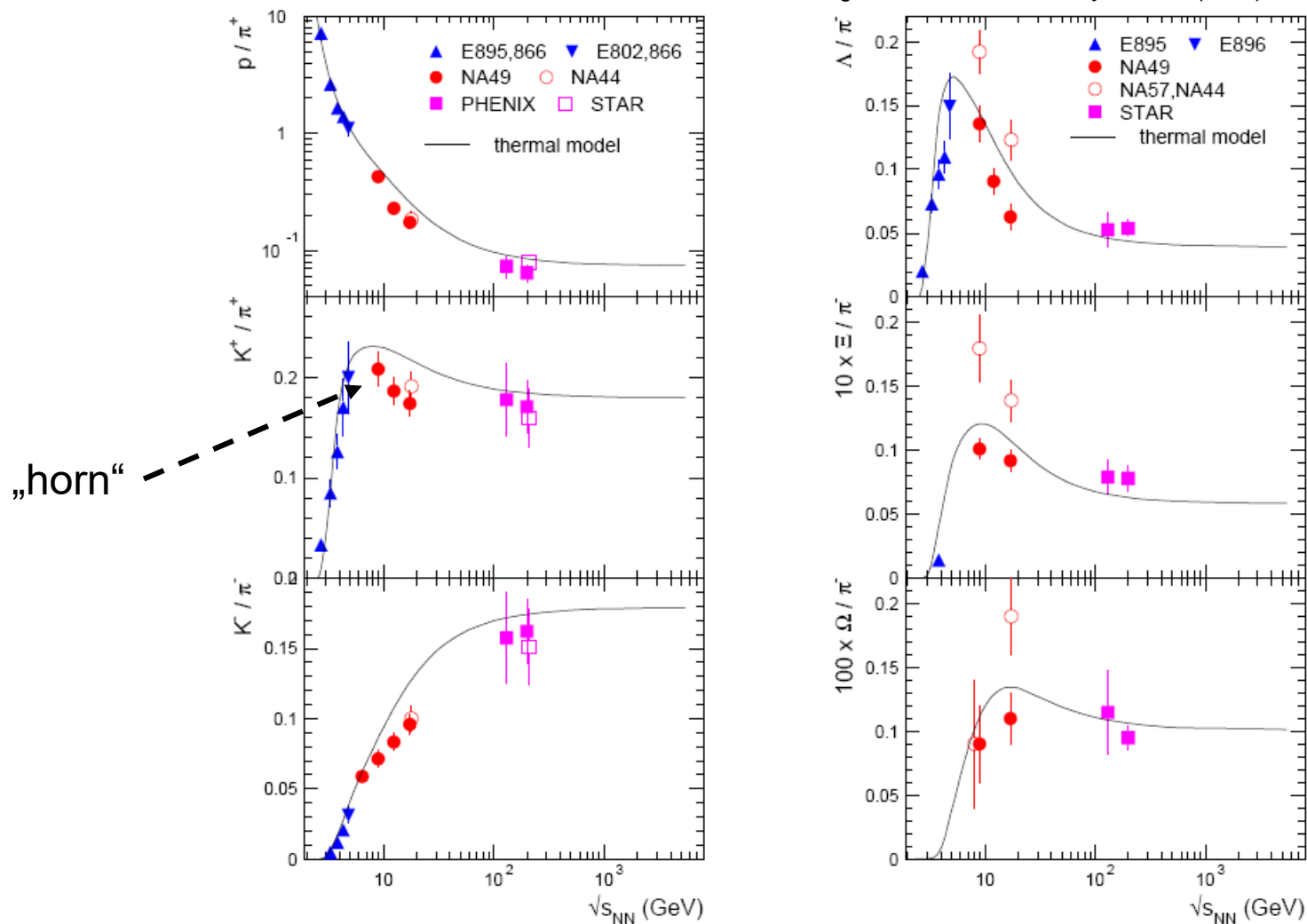
Fig. 3. Phase boundary between a hadron gas and a quark-gluon plasma (top) as function of temperature and baryon chemical potential together with the freeze-out points for Si(S) + Au(W,Pb) collisions at AGS [11] and SPS (present paper) energies. Latent heat of the phase transition (middle) and baryon density in the hadron and quark-gluon phase at the phase boundary (bottom).

Strange particles are crucial to constrain fit parameters

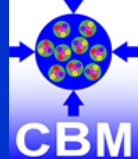
Excitation function of particle ratios



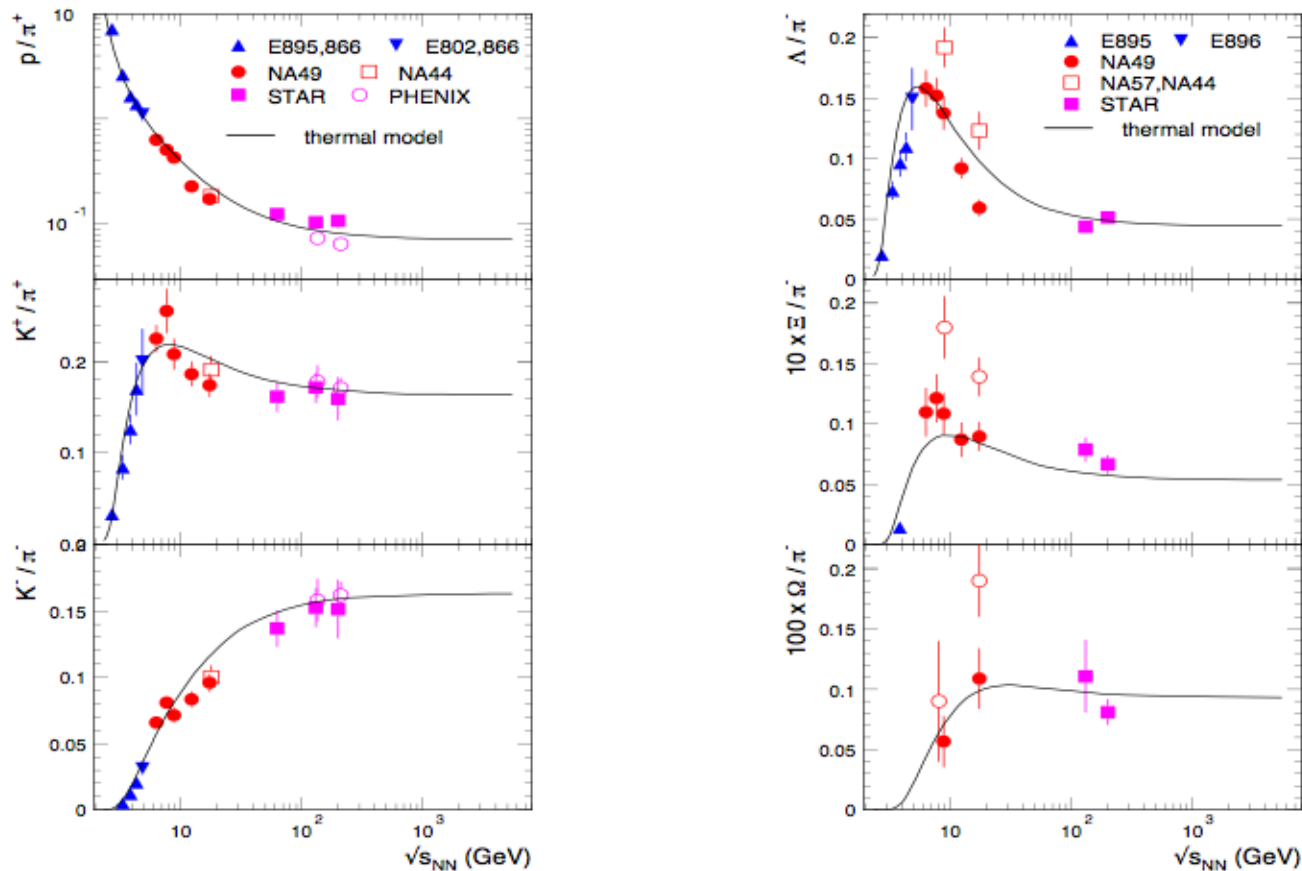
A. Andronic, P. Braun-Munzinger, J. Stachel, *Nucl. Phys. A* 772 (2006) 167



Particle ratios revisited



A. Andronic, P. Braun-Munzinger, J. Stachel, Phys. Lett. B 673 (2009) 142



Thermal model with extended resonance mass spectrum

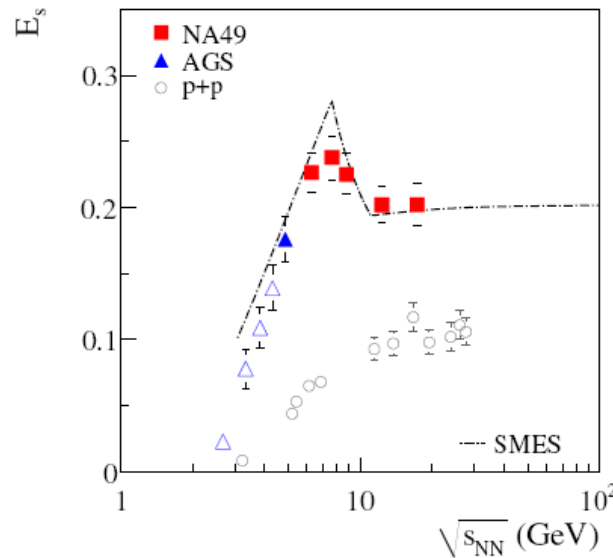
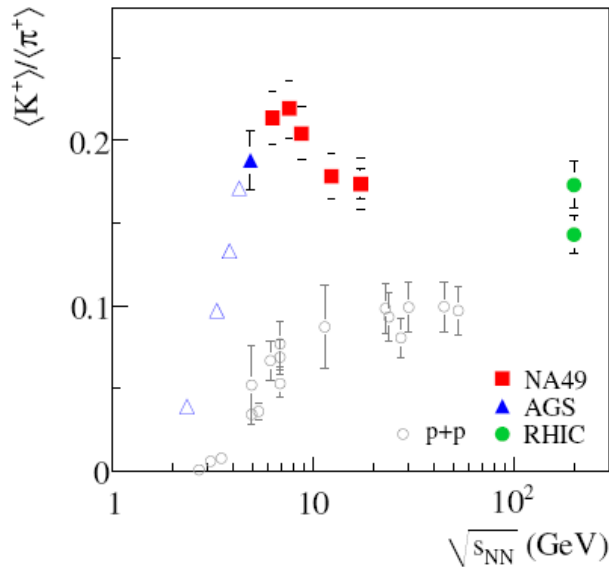
- high lying resonances ($M > 2$ GeV)
 - sigma meson ($M = 600$ MeV)
- gross features very well.

Statistical Model for Early Stage (SMES)



Gadzicki Acta Phys Pol, B, 35,187(2004);
Gorenstein JPG,28,1623(2002)

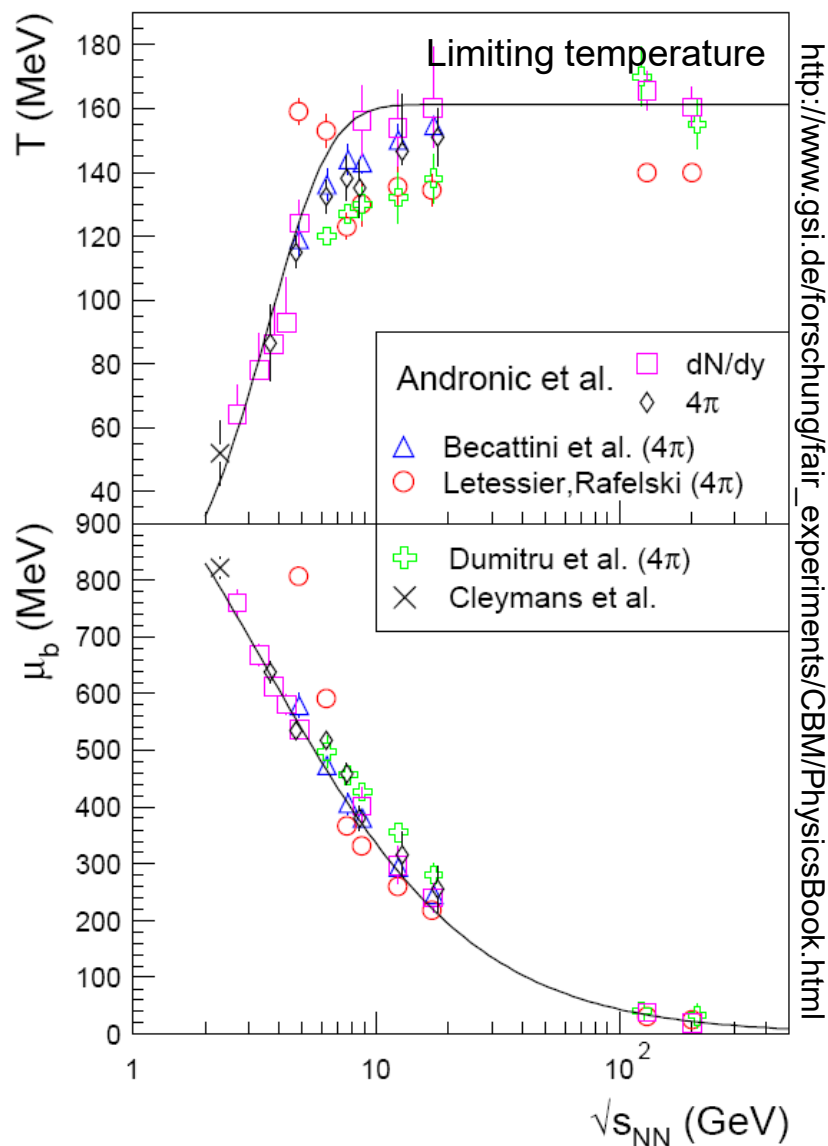
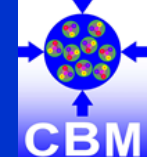
E_s =Ratio of strangeness
to entropy



Large entropy
production beyond
threshold energy

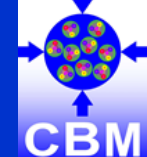
In the SMES the role of strangeness is different. This is because statistical production of particles is postulated and therefore also strange particles are assumed to be produced in equilibrium. Consequently possible secondary processes do not modify its value. At $T = T_c$ the strangeness density is lower in the QGP than in confined matter. Thus, a suppression of strangeness production is expected to occur when crossing the transition energy range from below. The low level of strangeness production in N+N interactions as compared to the higher strangeness yield per participant nucleon in central A+A collisions (called strangeness enhancement) can be understood as mostly due to the effect of strict strangeness conservation (canonical suppression) imposed on the strange and anti-strange degrees of freedom [32]. This constraint has an important effect for small statistical systems such as the confined matter in the early stage of N+N collisions.

Excitation function of particle production

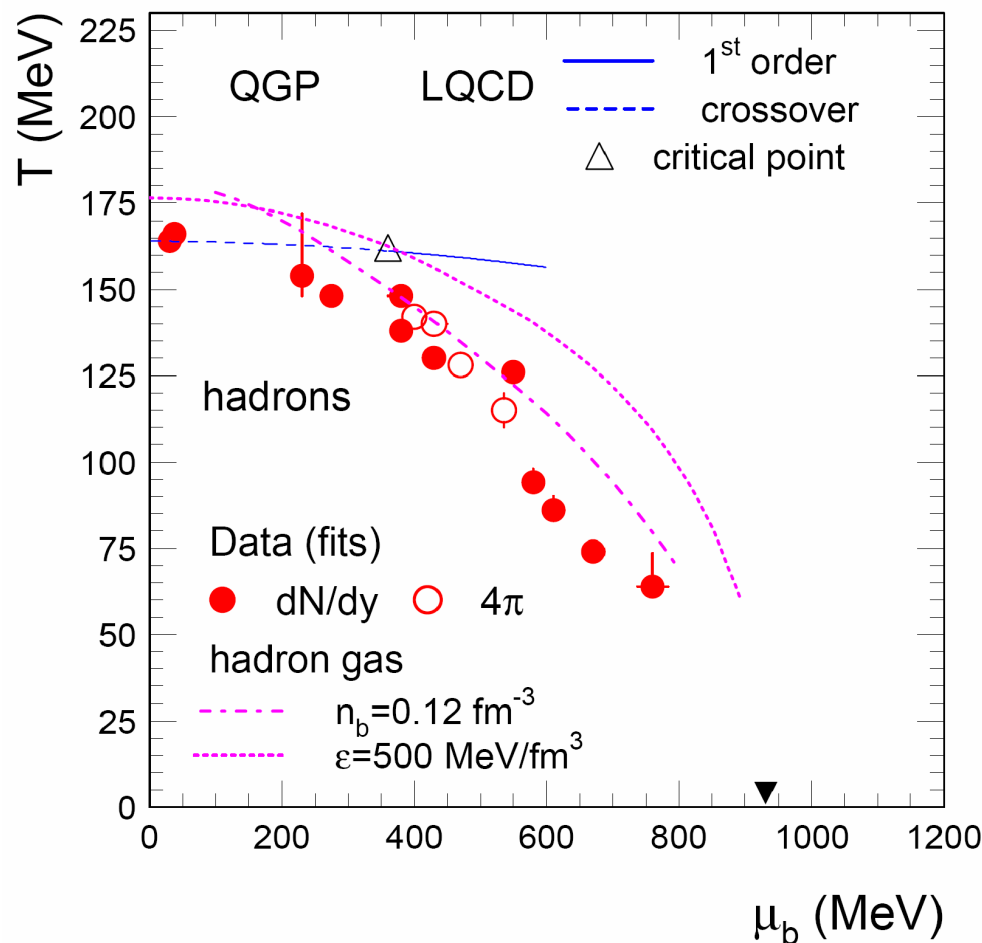


- Fit works at all energies from SIS to LHC
- T and μ_b evolve monotonically with $\sqrt{s_{NN}}$
- T saturates at $\sqrt{s_{NN}} = 10$ GeV: $T_{lim} = 160$ MeV

Phase diagram with freeze-out data



A. Andronic et al., Phys. Lett. B 673 (2009).



Fit results

- depend on input data ($4\pi - dN / dy$)
- point to low density of hadron gas
- have substantial errors at large μ_b

Equilibration times in hadronic matter



Naïve estimate:

3 collisions needed for equilibration (result from kinetic theory)

hadronic cross section: $\sigma = 40 \text{ mb} = 4 \text{ fm}^2$

strangeness production cross section: $\sigma = 400 \text{ } \mu\text{b} = 4 \cdot 10^{-2} \text{ fm}^2$

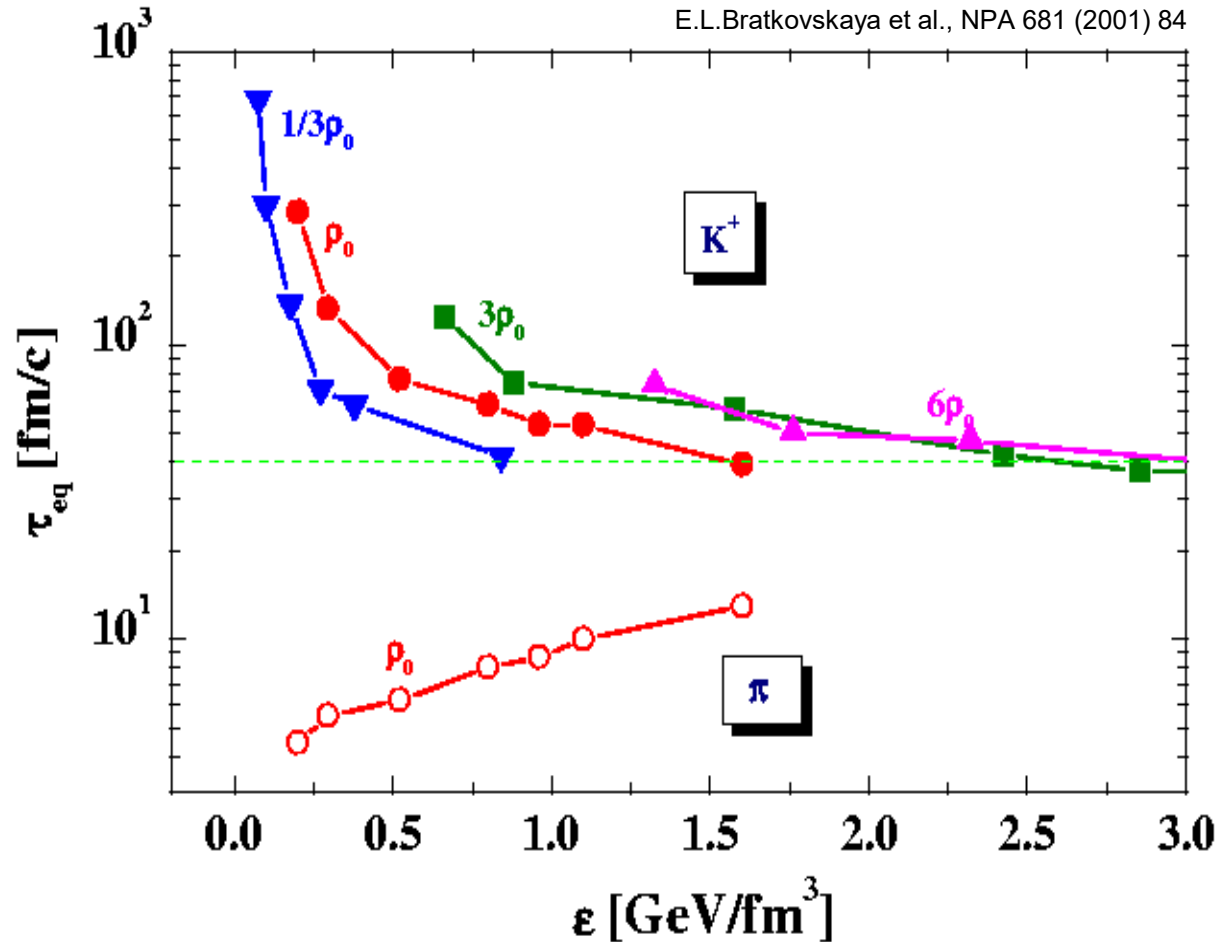
mean free path $\lambda = \frac{1}{n\sigma} = \frac{1}{0.17 \text{ fm}^{-3} \cdot 4 \text{ fm}^2} = 1.5 \text{ fm}$

time between collisions $\tau = \lambda / c = 1.5 \text{ fm} / c$

minimal equilibration time $\tau_{eq}^{pion} = 4.5 \text{ fm} / c$

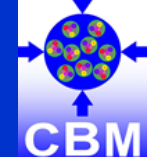
$\tau_{eq}^{strangeness} = 450 \text{ fm} / c$

Equilibration times in hadronic matter



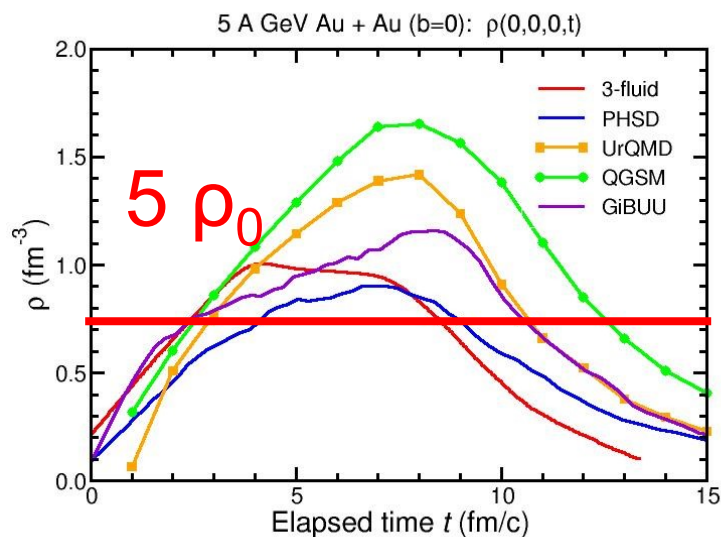
Even the lightest strange particle (K^+) needs at least 40 fm/c to equilibrate.

Baryon densities in central Au+Au collisions

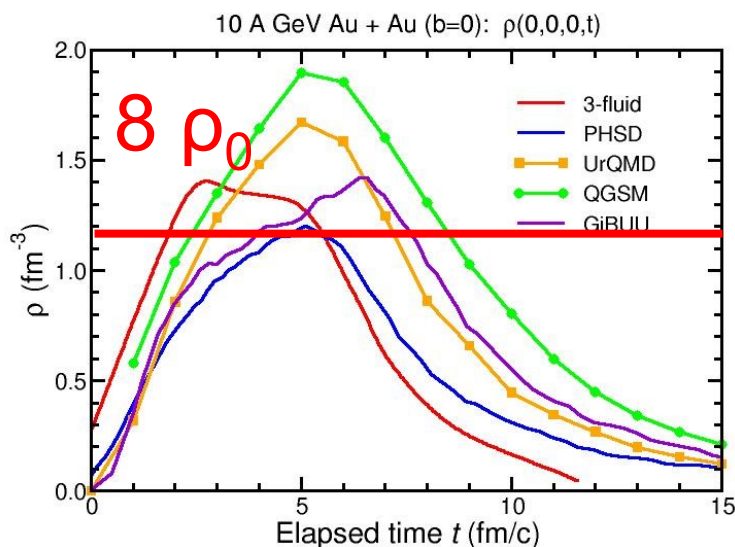


I.C. Arsene et al., Phys. Rev. C 75, 24902 (2007)

5 A GeV



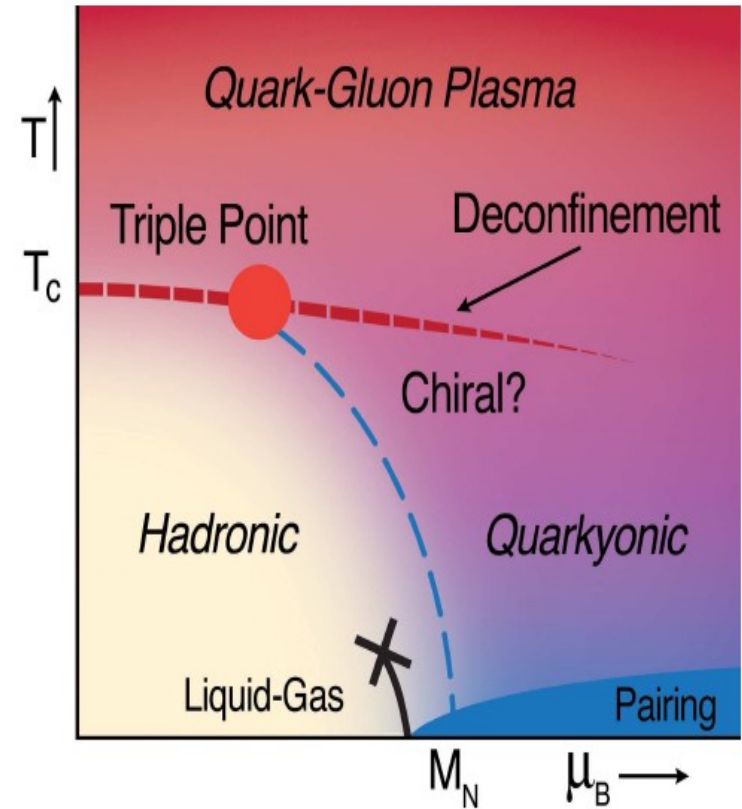
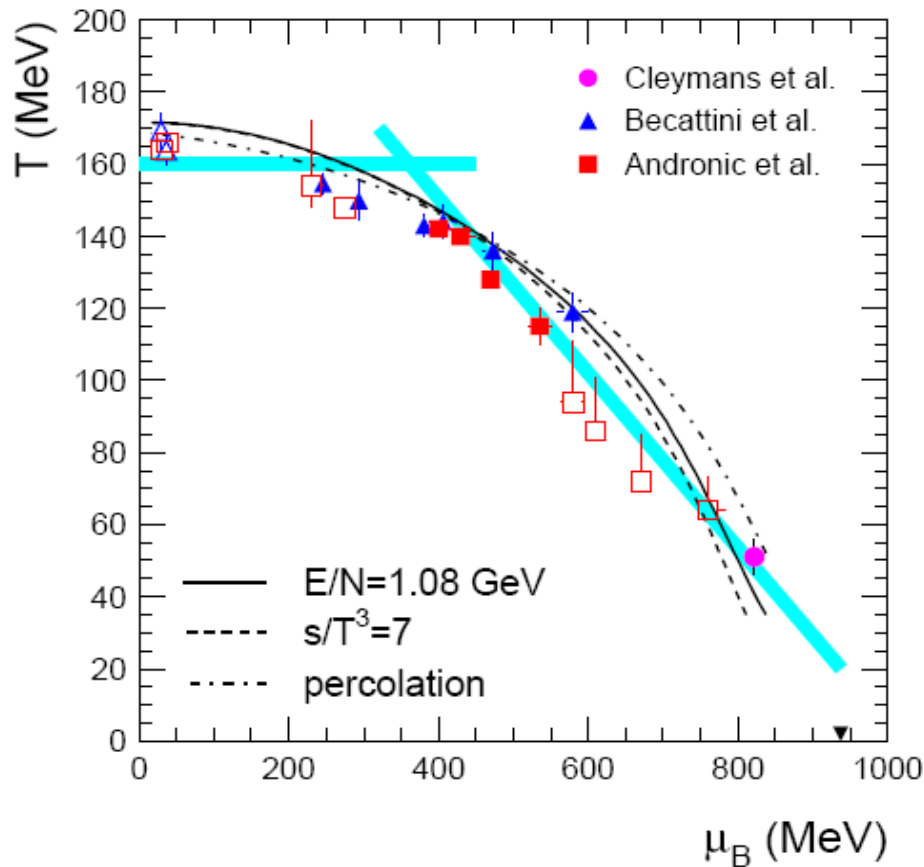
10 A GeV



Chemical Freeze-out phase diagram

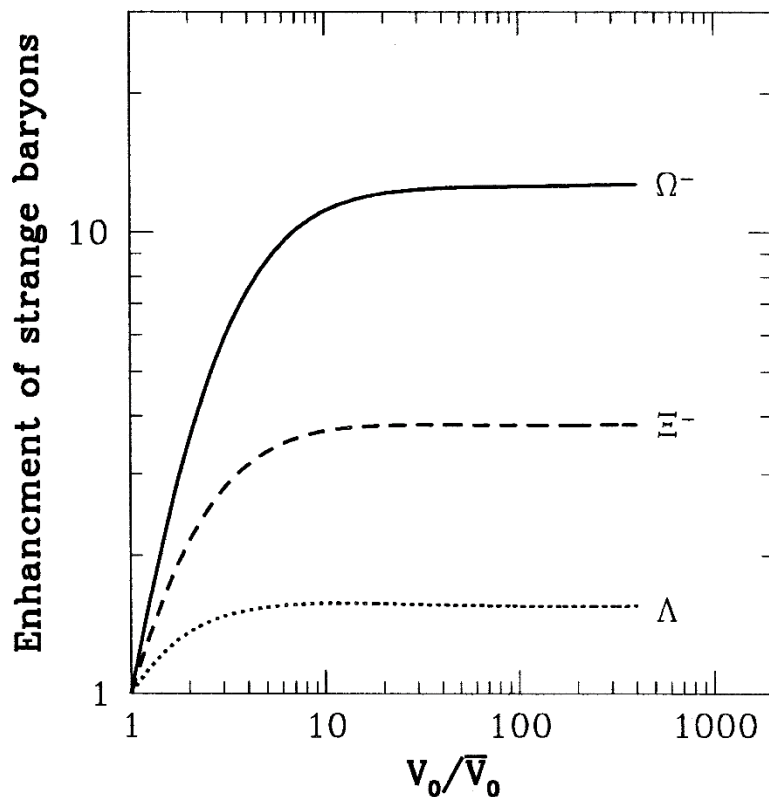


A. Andronic et al., arXiv:0911.4806



Speculation about the existence of a 1.order phase transition because of apparent thermal equilibrium.

S. Hamieh, K. Redlich und A. Tounsi,
Phys. Lett. B 486 (2000) 61



Small systems:
local conservation of strangeness
(needs canonical ensemble:
N, V fixed, energy can vary)

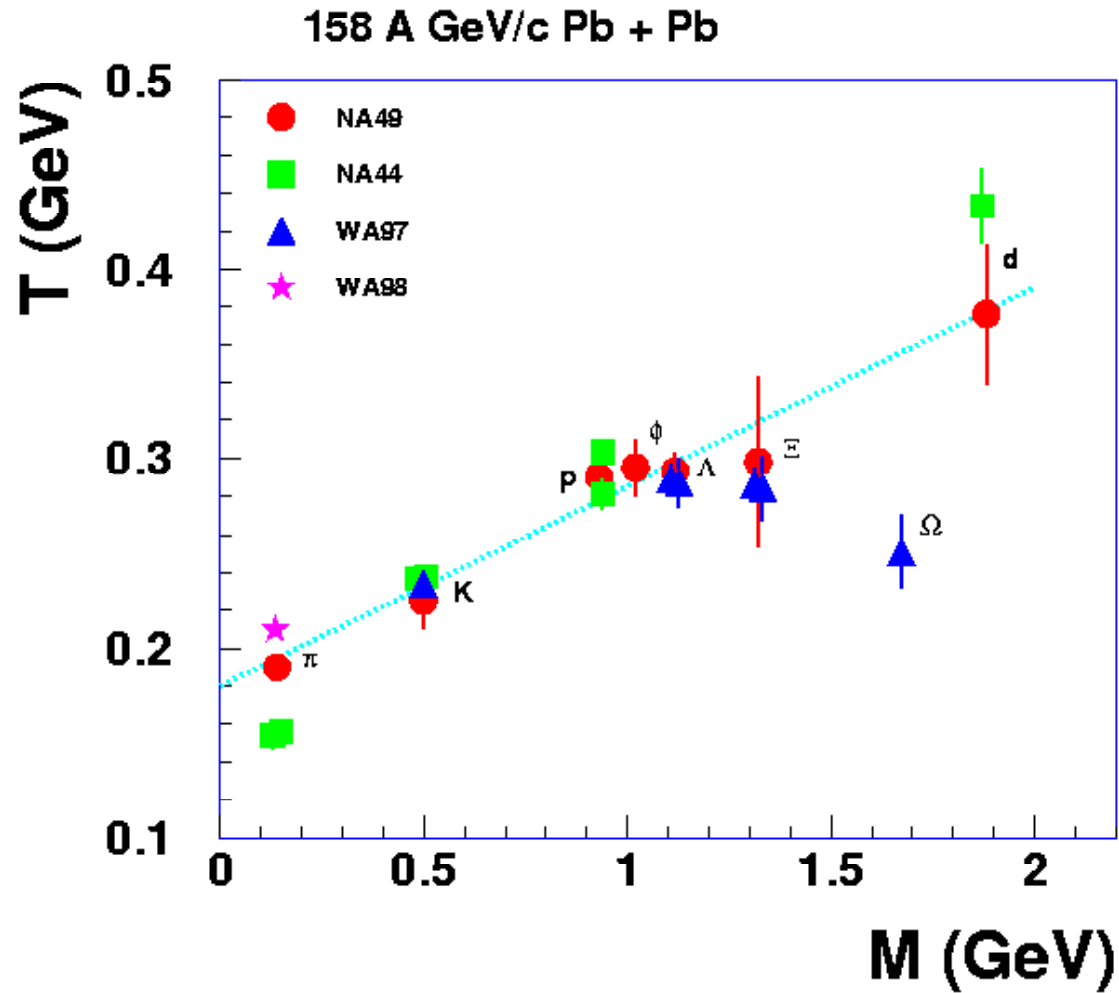
Result:
Particle numbers of strange particle in
canonical (C) and grand canonical (GC)
approach are related:

$$n_{|S|}^C = n_{|S|}^{GC} \cdot F(n_{|S|}^{GC} \cdot V)$$

F is a ratio of modified Bessel functions,
V is correlation volume

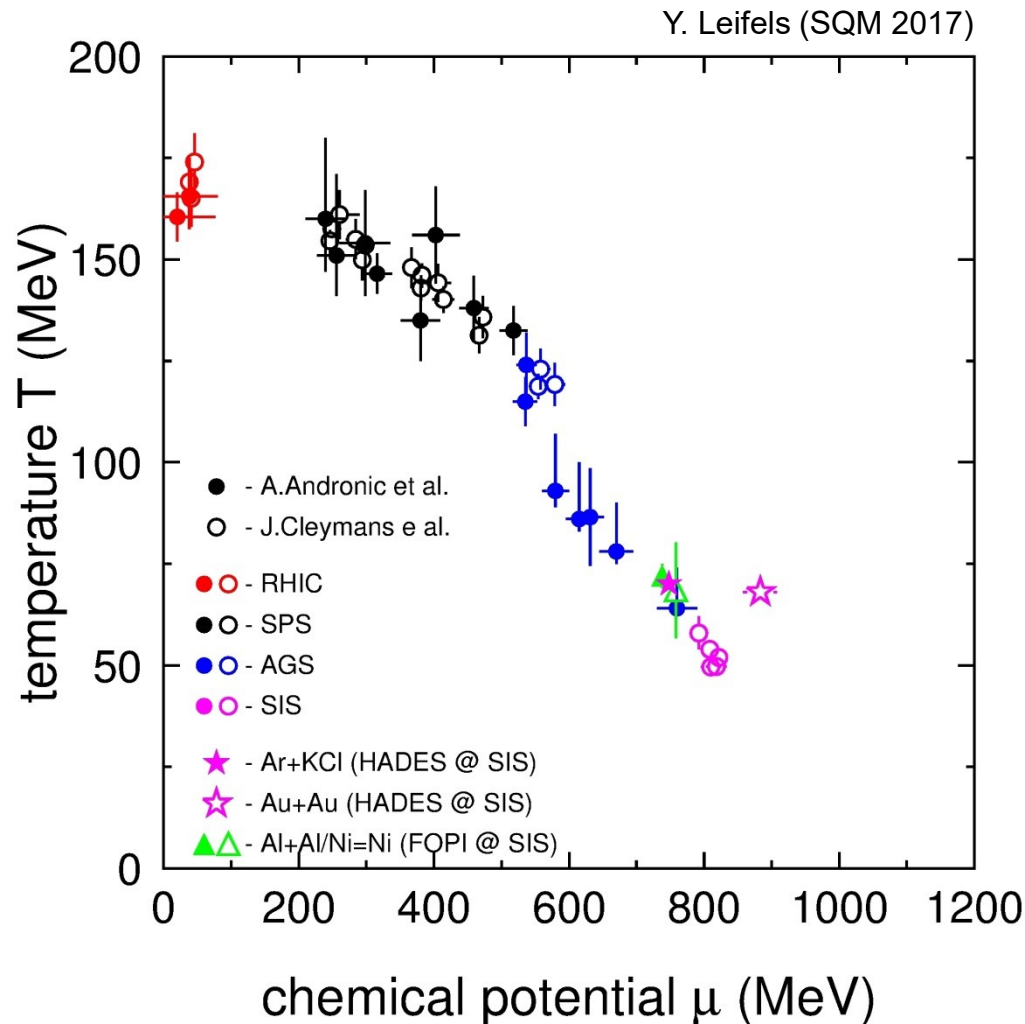
Conclusion: strangeness is in equilibrium over the whole energy range !?
Needs consistency checks!

Transverse expansion



Slopes are proportional to mass except for multiple strange particles.

Collection of SHM freeze-out data



High energies:
grandcanonical ensemble

Lower energies / small systems:
canonical ensemble,
strangeness suppression factor

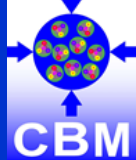
Equilibrium achieved in small systems?

Equilibrium as signature for phase transition?

Freeze-out line at large baryon densities
as phase boundary to quarkyonic matter ?

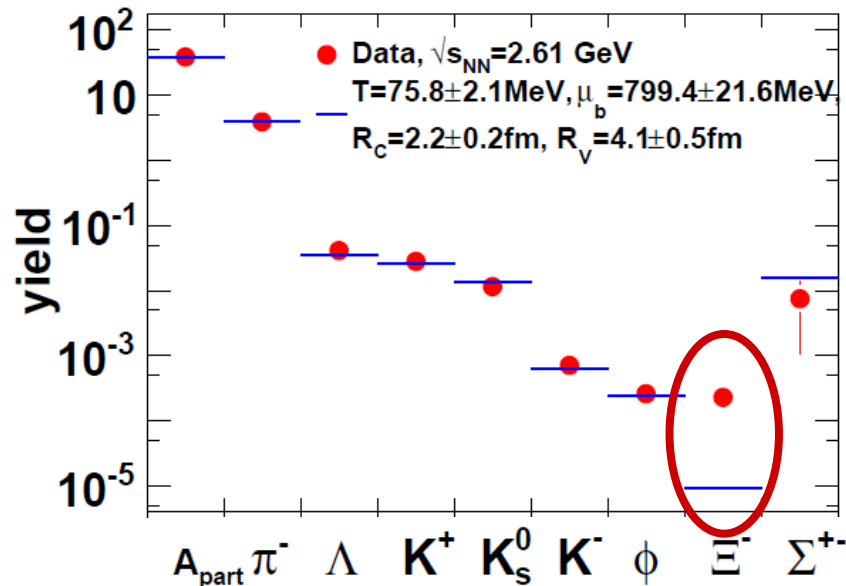
FOPI analysis: K. Piasecki et al., Phys.Rev. C94 (2016)
Thermus V2.3,
Wheaton & Cleymans Comp. Phys. Comm. 180 (2009)

HADES: Sub-threshold Ξ^- - production

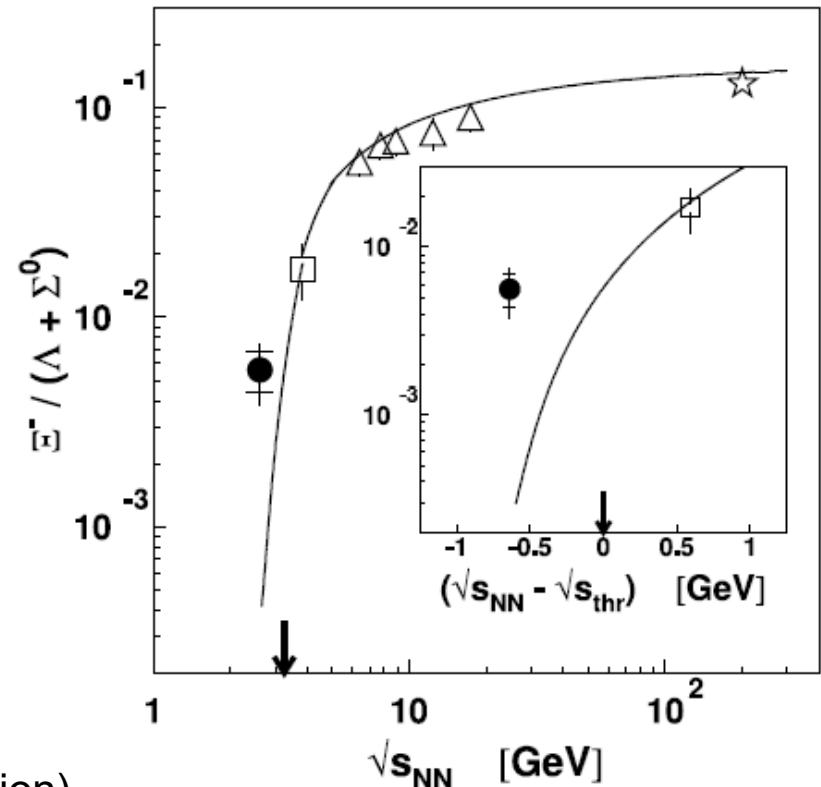


Ar+KCl reactions at 1.76A GeV

- Ξ^- yield by appr. factor 25 higher than thermal yield



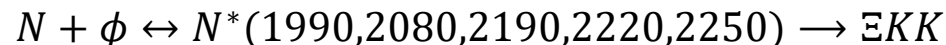
G. Agakishiev et al. (HADES), PRL103, 132301, (2009)



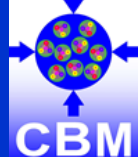
Enhancement factor: ∞ (deep subthreshold production)

Note: yield can be reproduced by microscopic models (e.g. UrQMD)

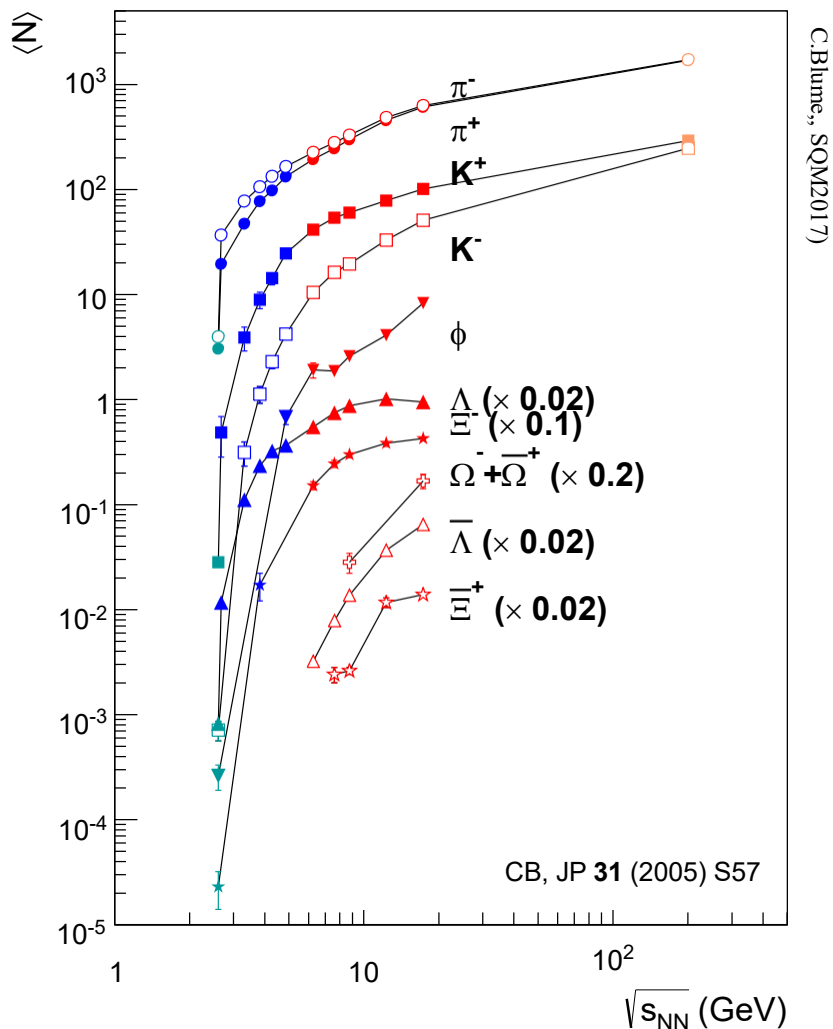
tuning branching ratios of heavy resonances (Steinheimer, Bleicher, arXiv: 1503.07305) :



Final state particle abundance

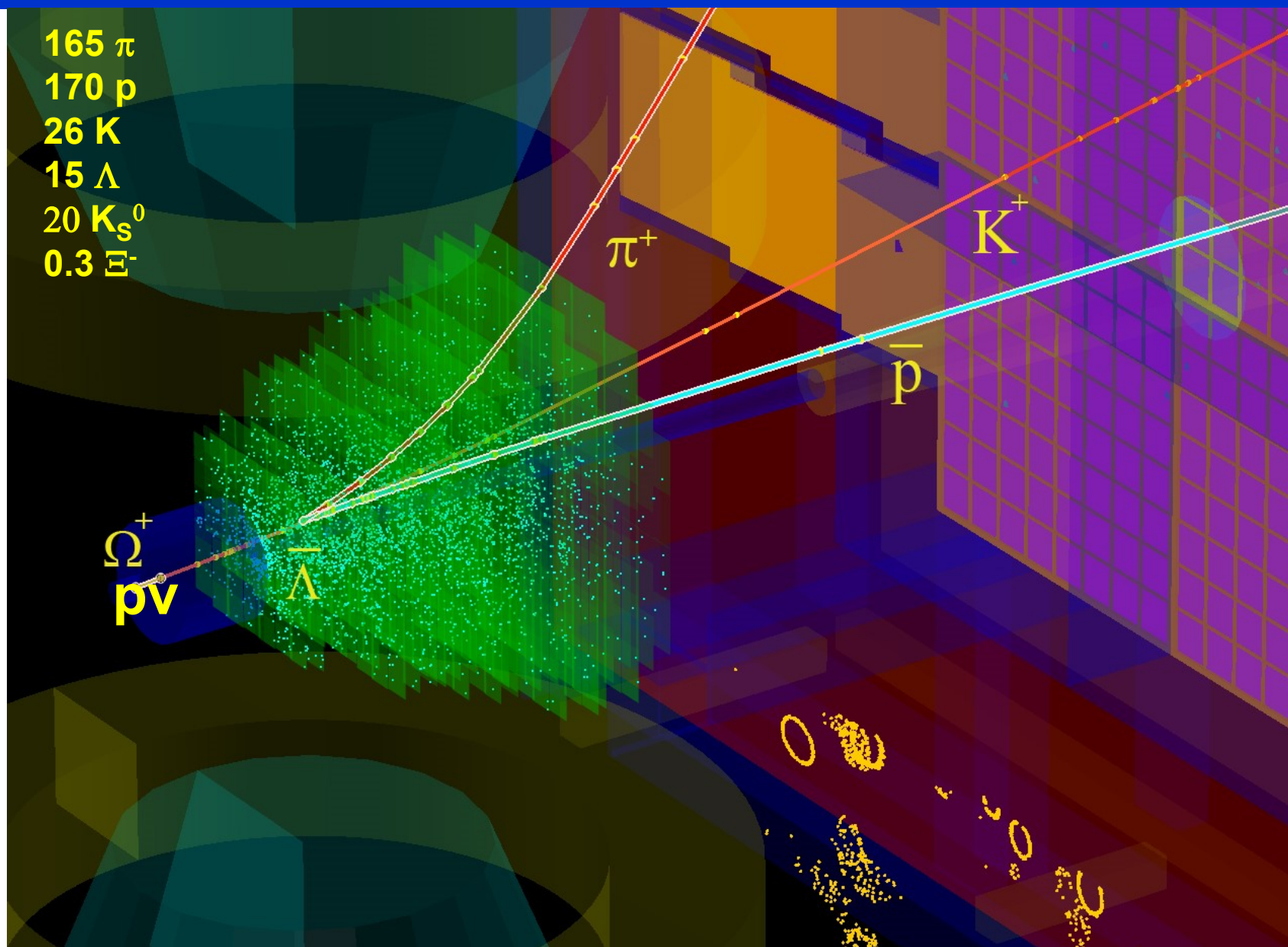


Particle yields from central Au + Au collisions

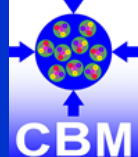


Strange and charmed particle production thresholds in pp - collisions

reaction	$\sqrt{s}$ (GeV)	T_{lab} (GeV)
$pp \rightarrow K^+ \Lambda p$	2.548	1.6
$pp \rightarrow K^+ K^- pp$	2.864	2.5
$pp \rightarrow K^+ K^+ \Xi^- p$	3.247	3.7
$pp \rightarrow K^+ K^+ K^+ \Omega^- n$	4.092	7.0
$pp \rightarrow \Lambda \bar{\Lambda} pp$	4.108	7.1
$pp \rightarrow \Xi^- \bar{\Xi}^+ pp$	4.520	9.0
$pp \rightarrow \Omega^- \bar{\Omega}^+ pp$	5.222	12.7
$pp \rightarrow J/\Psi pp$	4.973	12.2



Matter effects on strangeness production



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Subthreshold Kaon Production as a Probe of the Nuclear Equation of State

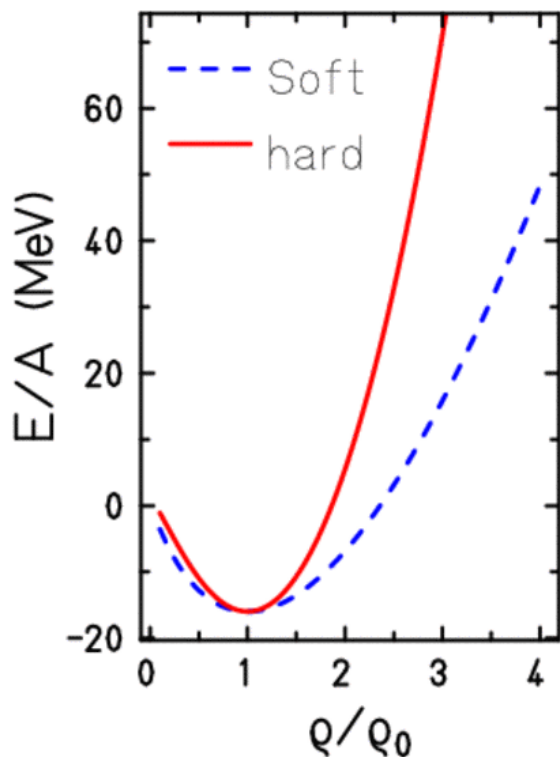
J. Aichelin and Che Ming Ko^(a)

Joint Institute for Heavy Ion Research, Holifield Heavy Ion Research Facility, Oak Ridge, Tennessee 37831

(Received 11 June 1985; revised manuscript received 23 September 1985)

The production of kaons at subthreshold energies from heavy-ion collisions is sensitive to the nuclear equation of state. In the Boltzmann-Uehling-Uhlenbeck model, the number of produced kaons from central collisions between heavy nuclei at incident energies around 700 MeV/nucleon can vary by a factor of ~ 3 , depending on the equation of state.

equation of state



Transport model (IQMD)

Softer EOS

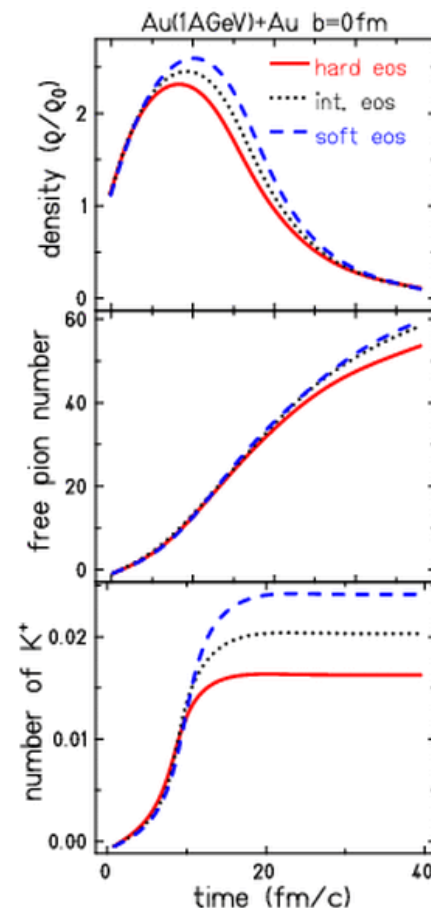
- ⇒ larger densities
- ⇒ stronger resonance population
- ⇒ more $N\Delta$ collisions
- ⇒ more collisions above production threshold:

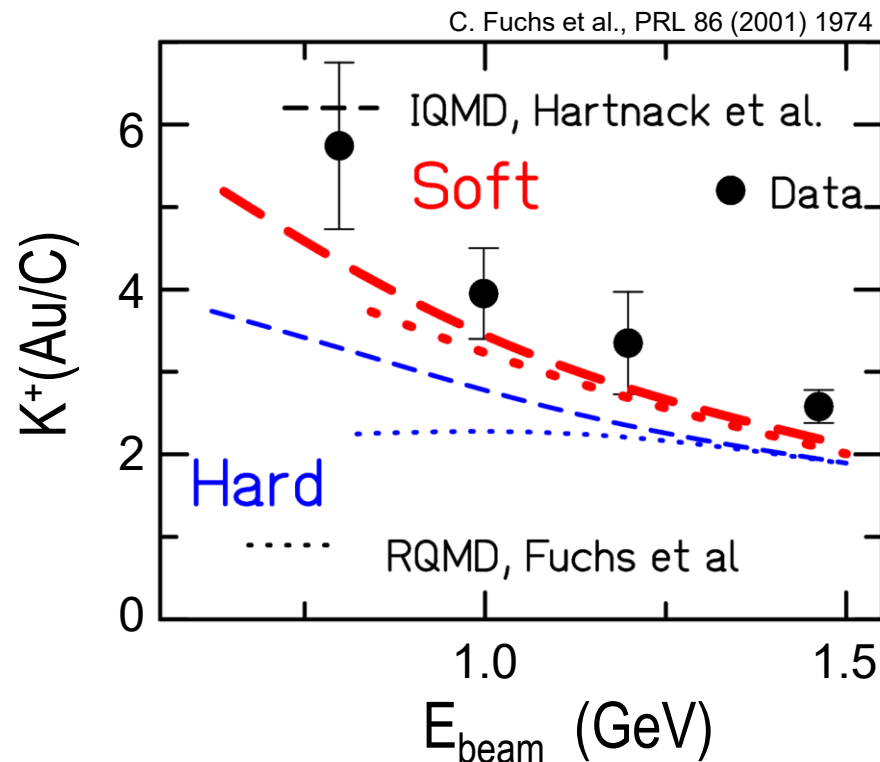
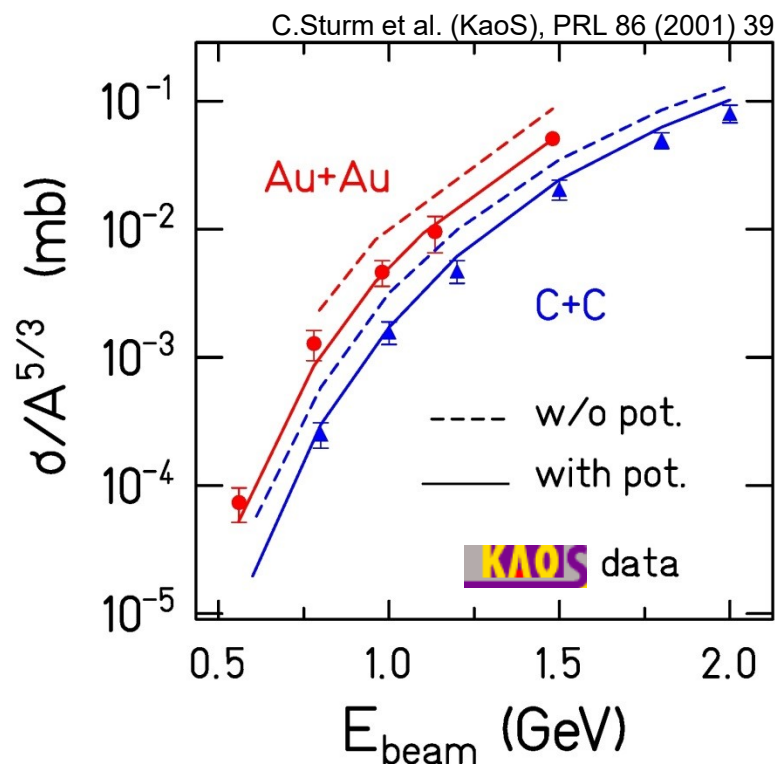
$N\Delta \rightarrow NK\Lambda$

$\Delta\Delta \rightarrow NK\Lambda$

(associated production)

C. Hartnack (IQMD)





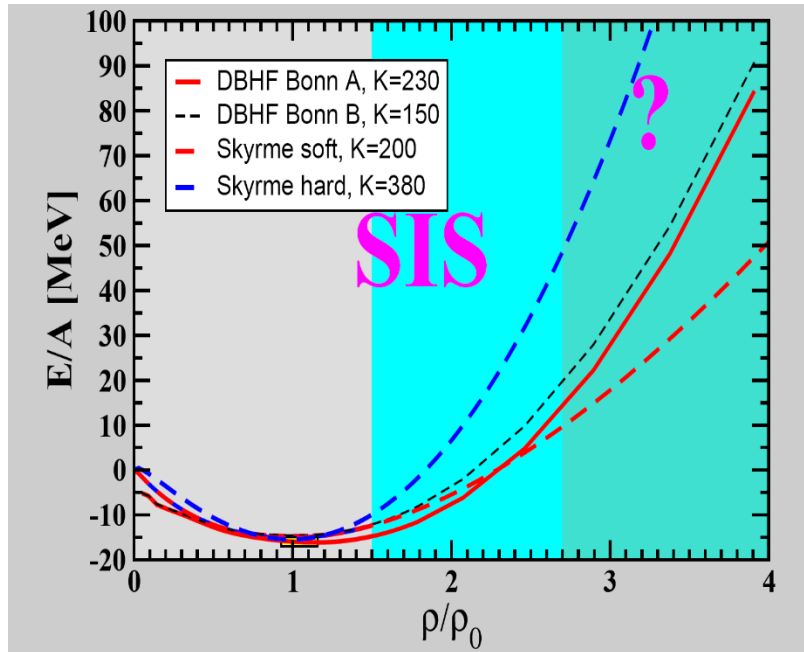
Sub-threshold kaon production

- multi-step processes, using resonances/pions as intermediate energy storage
 - strongly dependent on density
- sensitive to the stiffness of the nuclear matter equation of state
- EOS is soft up to densities $\rho \leq 2.5 \rho_0$

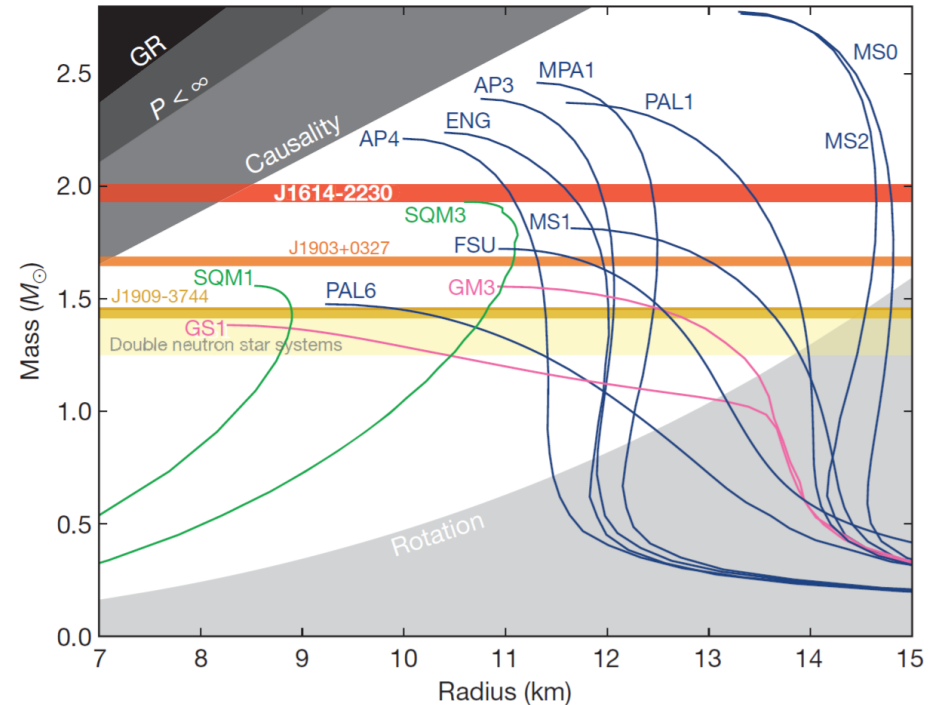
Astrophysical constraints on the EOS



C. Fuchs,
Prog. Part. Nucl. Phys. 56 (2006) 1



P.B. Demorest (2010)
doi:10.1038/nature09466



Soft EOS (Skyrme, $K = 200$ MeV) is not repulsive enough to allow for a neutron star with 2 solar masses.

Stiffening must occur in the range of densities up to $4 \rho_0$.