

Short-Range Correlations and Nuclear Universality

Or Hen – MIT



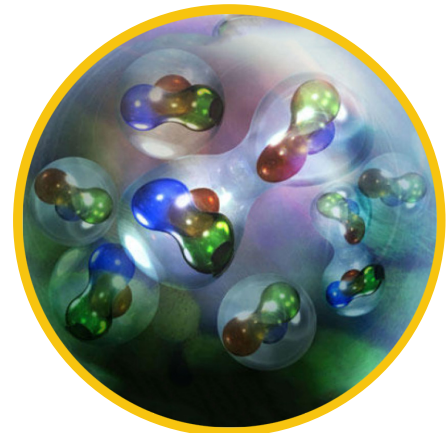
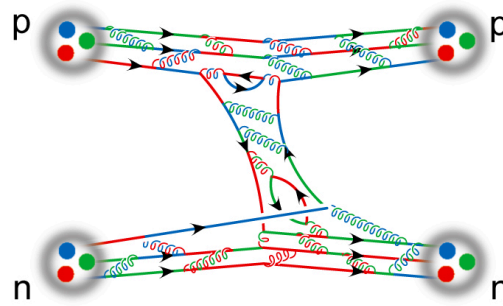
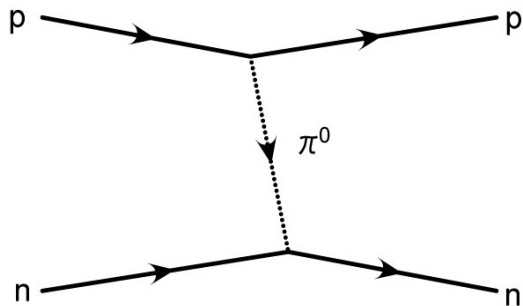
Nuclear Many-Body Challenge

Many-body Schrödinger Equation

$$\sum_i \left\{ -\frac{\hbar^2}{2m_i} \nabla_i^2 \Psi(\vec{r}_1, \dots, \vec{r}_N, t) \right\} + U(\vec{r}_1, \dots, \vec{r}_N) \Psi(\vec{r}_1, \dots, \vec{r}_N, t) = i\hbar \frac{\partial}{\partial t} \Psi(\vec{r}_1, \dots, \vec{r}_N, t)$$

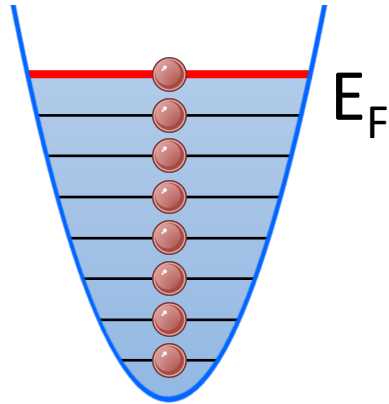
Main Challenges:

1. No 'fundamental' Interaction.
2. Complex phenomenological parametrizations (e.g. over 18 operators)

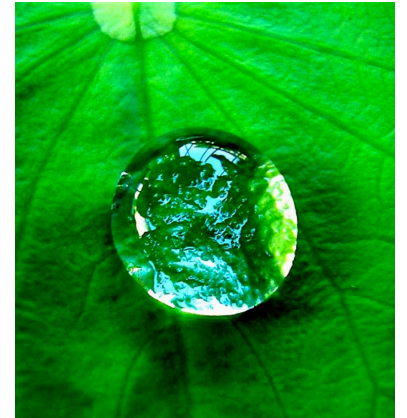


Solution: Effective Theories

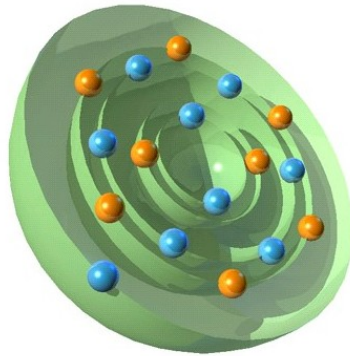
Fermi
Gas
Model



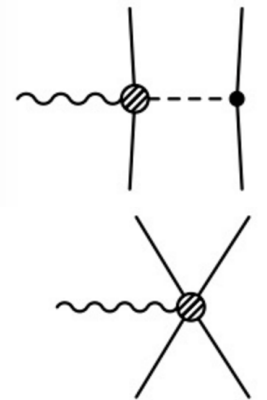
Liquid
Drop
Model



Shell
Model

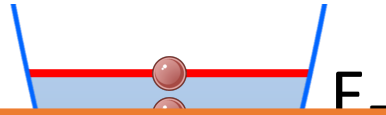


Chiral
Perturbation
Theory



Solution: Effective Theories

Fermi



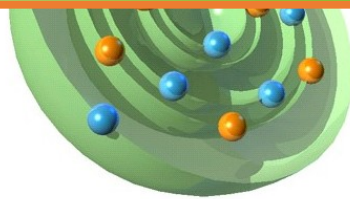
Liquid



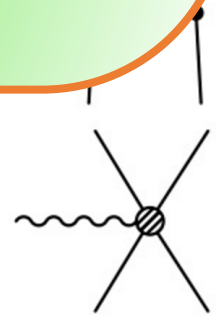
Common idea:

Scale separation of *long* and *short* range dynamics

Model

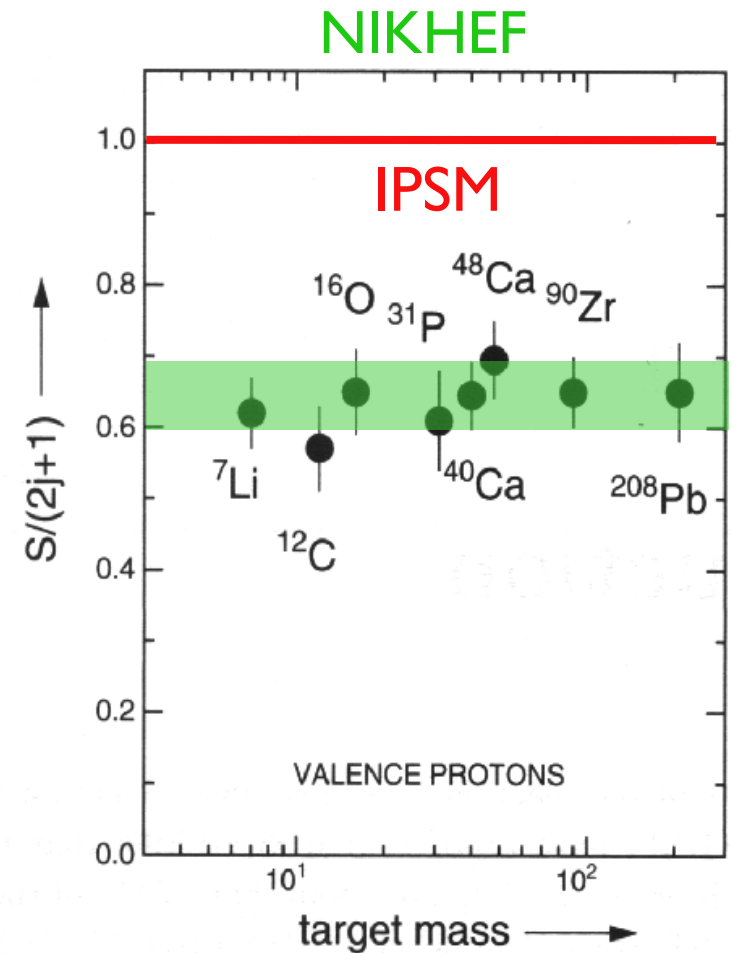


Perturbation Theory



Universality of long-range dynamics

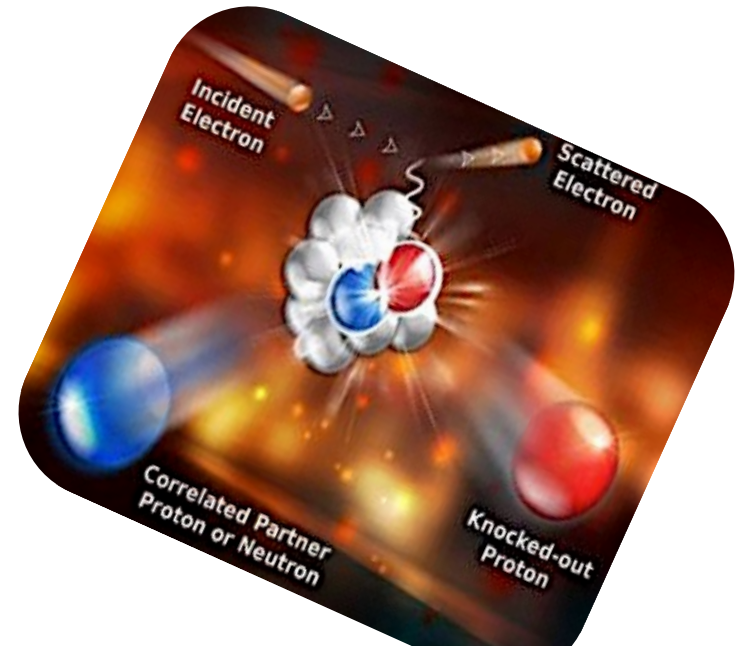
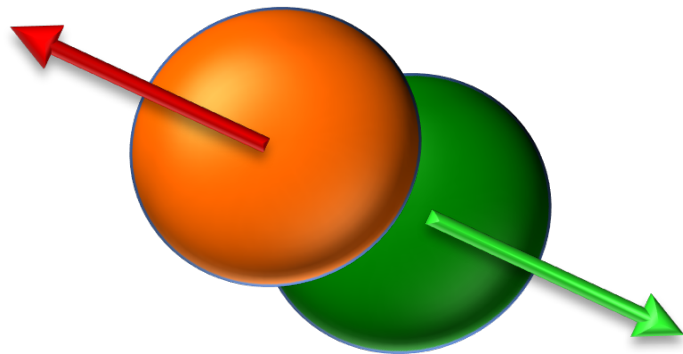
- Long-range (low-momentum) structure of nuclei studied for many years.
- Mean-field models give good description of this part of the ground state.
- Two big questions:
 - How important are of the short-range dynamics?
 - Is there an effective, *universal*, way to include them?



What Are SRC?

SRC are pairs of nucleon that are close together in the nucleus (wave functions overlap)

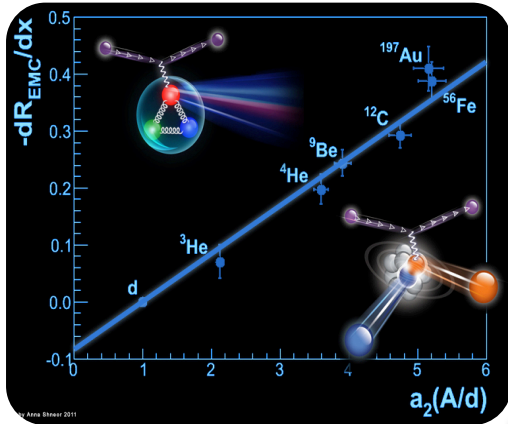
=> Momentum space: pairs with high relative momentum and low c.m. momentum compared to the Fermi momentum (k_F)



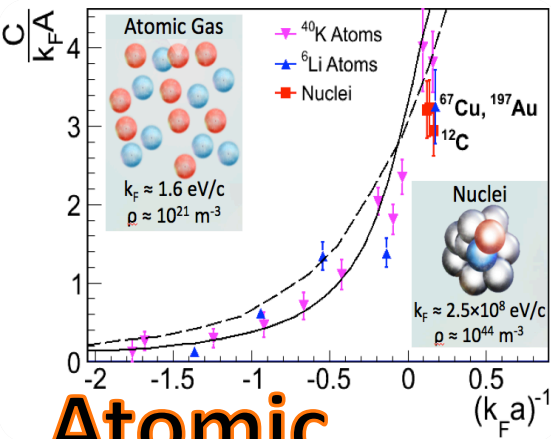
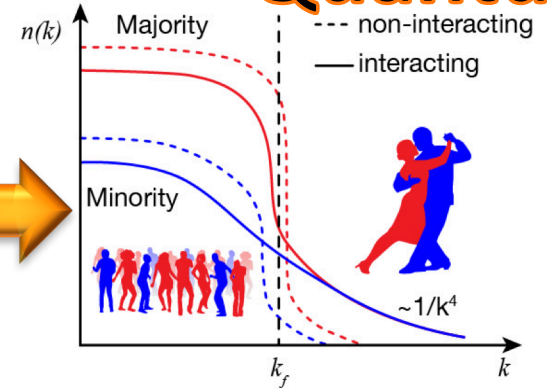
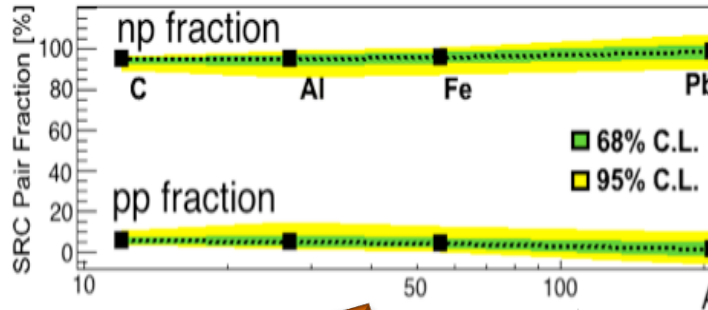
Why SRC?

Nuclear

Quantum

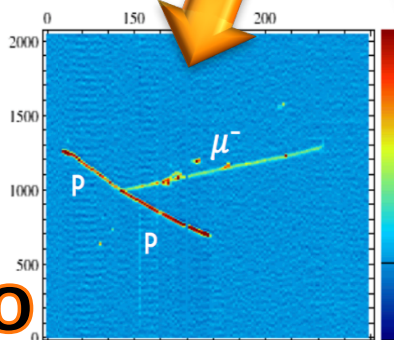
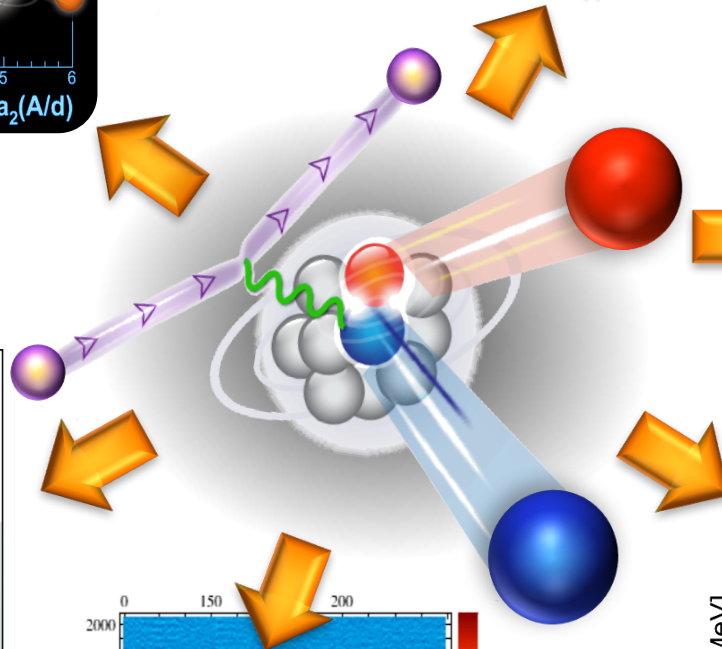


Particle

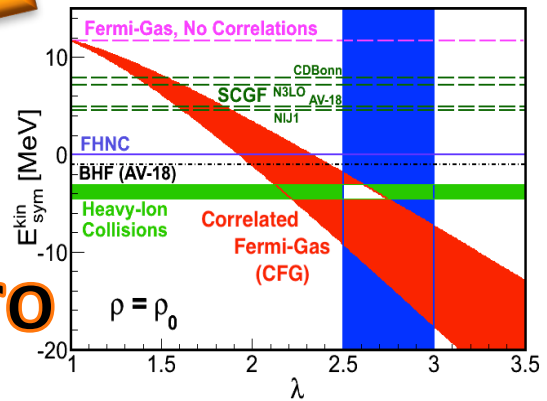


Atomic

Neutrino

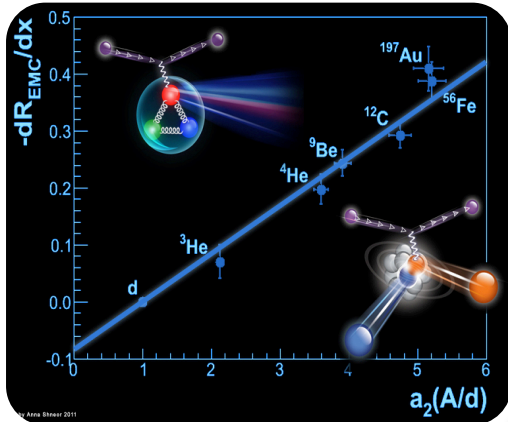


Astro

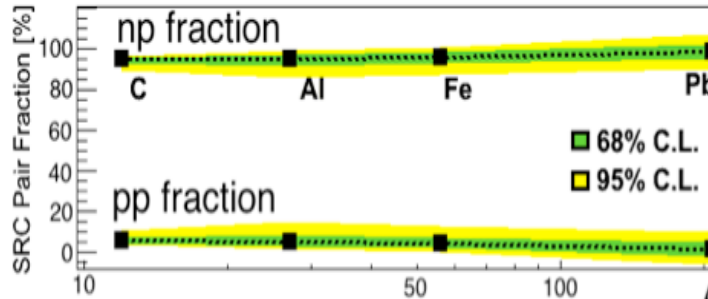


Why SRC?

Particle



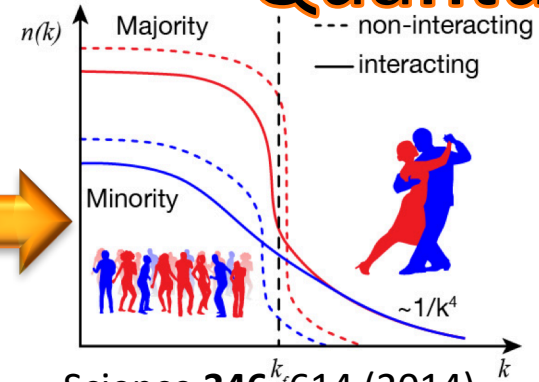
PRL **106**, 052301 (2011),
 PRD **84**, 117501(2011),
 PRC **85**, 047301(2012),
 IJMPE **22**, 1330017 (2013),
 arXiv 1607.03065 (2016).



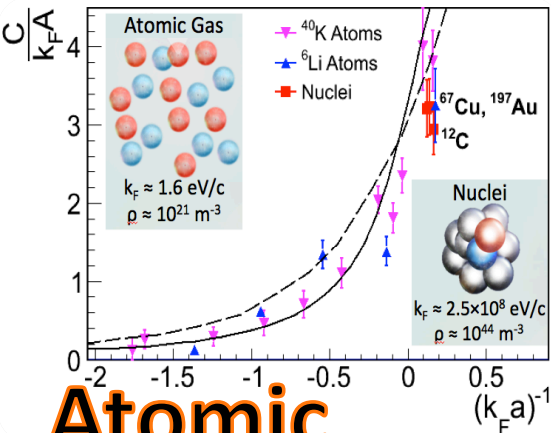
Nuclear

Science **320**, 1476 (2008),
 PRL **108**, 092502 (2012),
 PLB **772**, **63** (2013),
 PRL **113**, 022501 (2014),
 PRC **92**, 024604 (2015).

Quantum



Science **346**, 614 (2014).

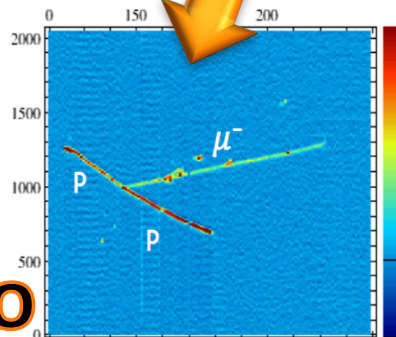


Atomic

PRC **92**, 045205 (2015).

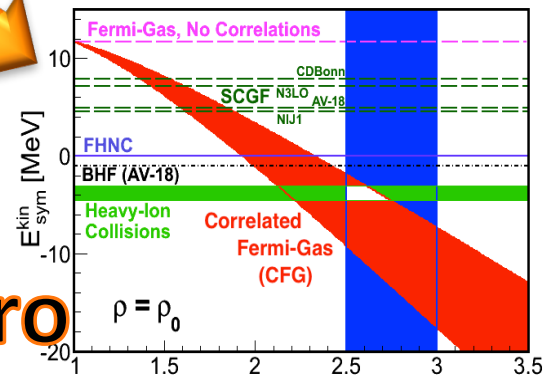
Neutrino

PRD **90**, 012008 (2014); PRC **94**, 045501 (2016)



Astro

PRC **91**, 025803 (2015), PRC **93**, 044610 (2016),
 PRC **91**, 044601 (2015), PRC **93**, 014619 (2016),
 PRC **92**, 011601 (2015), PLB **759**, 79 (2016),
 arXiv: 1608.00487 (2016); 1606.08045 (2016) ⁸



Why SRC?

**You can't do nuclei without
correlations!**

Today:

What? (do we know)

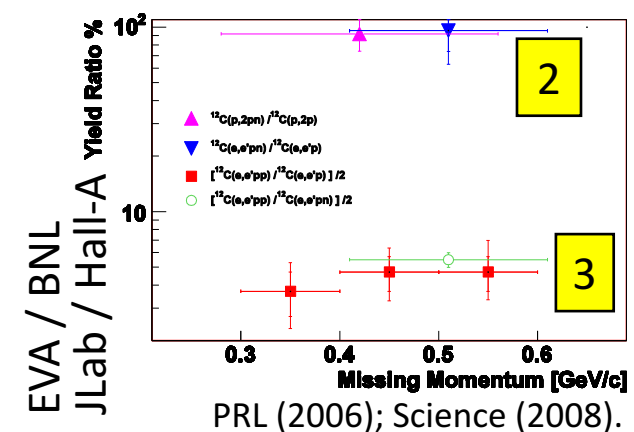
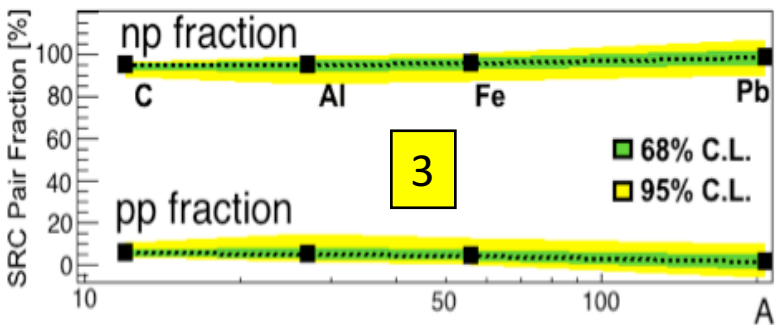
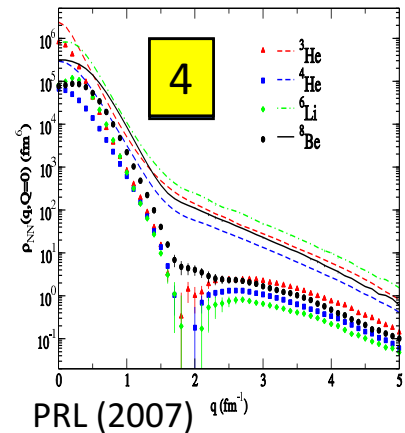
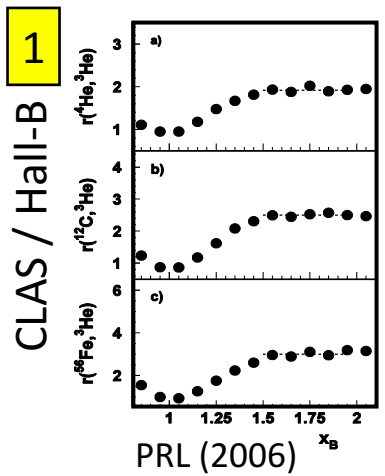
How? (do we know it)

Where? (do we go from here)

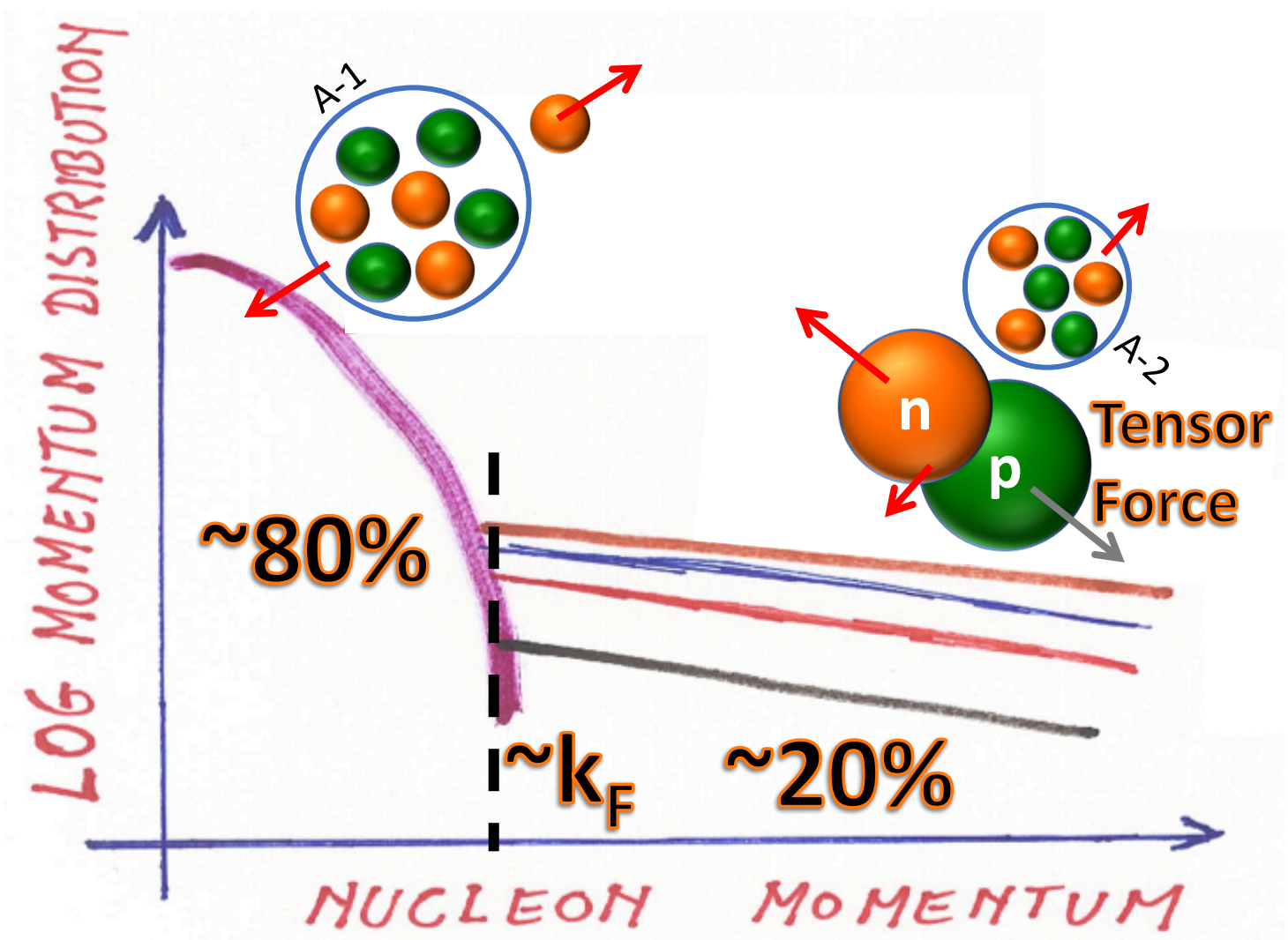
**You can't do nuclei without
correlations!**

What? (do we know about SRC)

- 1 Account for ~ 25% of nucleons in nuclei.
- 2 Dominate the momentum distribution for $k \geq 300$ MeV/c.
- 3 Probability for np-SRC is ~18 times larger than pp-SRC. Also true for heavy asymmetric nuclei.
- 4 Dominant NN force in the 2N-SRC is tensor force. High momentum tail (300-600 MeV/c) dominated by L=0,2 S=1 np-SRC pairs.

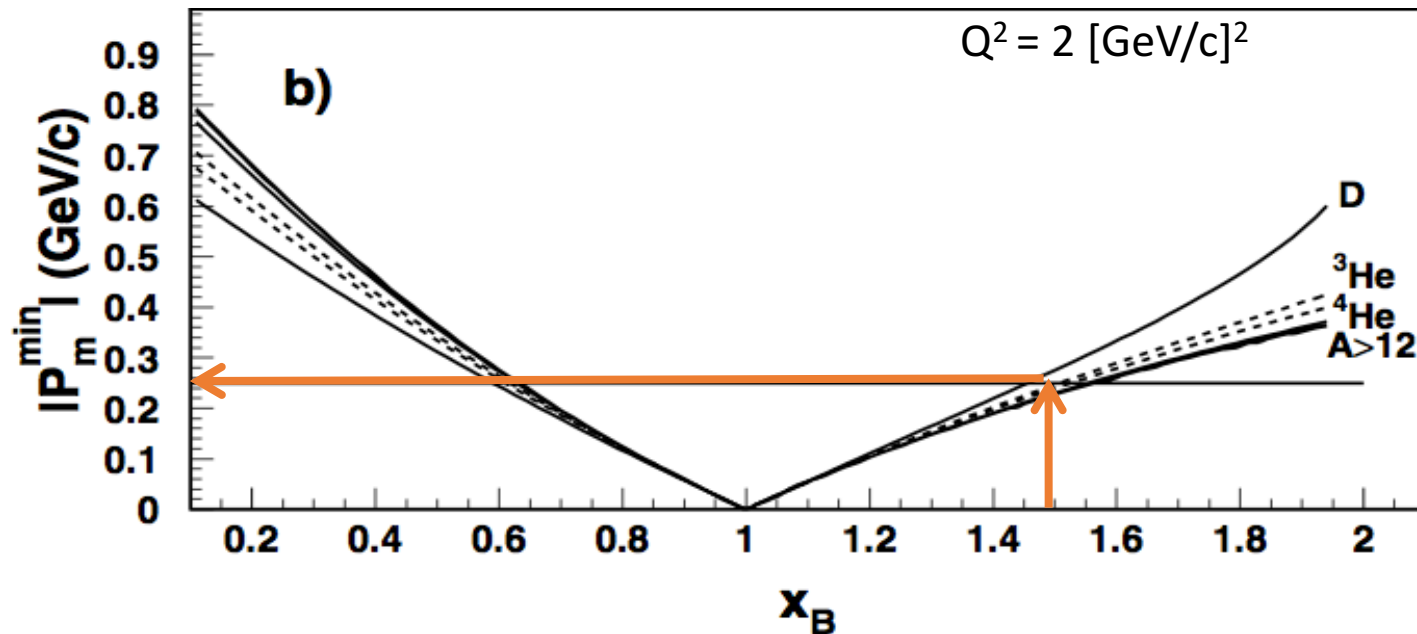


What? (do we know about SRC)



How? (do we get 25%)

(e,e') cross section at different kinematics is sensitive to different 'parts' of the nuclear momentum distribution.

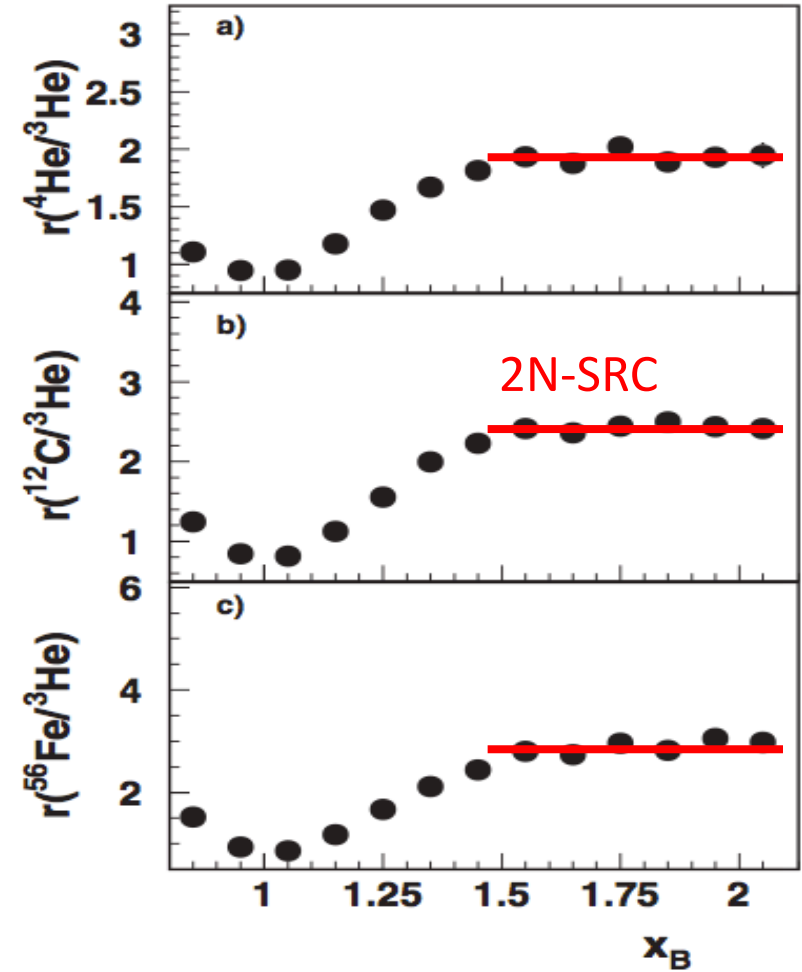


$$(q + p_A - p_{A-1})^2 = p_f^2 = m_N^2$$

How? (do we get 25%)

- A/d (e, e') cross section ratios sensitive to $n_A(k)/n_d(k)$
- Observed scaling in for $x_B \geq 1.5$.

$$\Rightarrow n_A(k > k_F) = a_2(A) \times n_d(k)$$



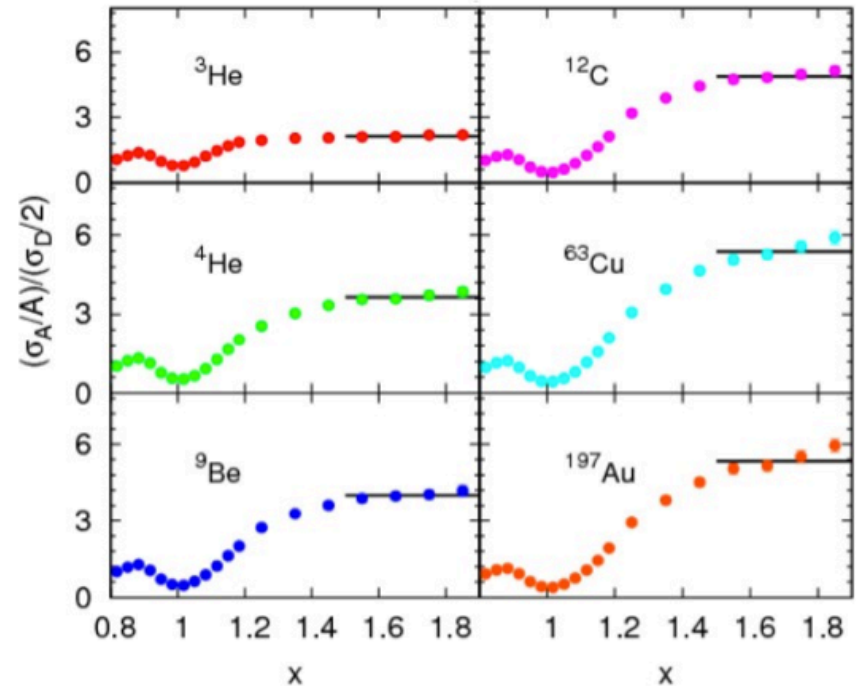
K. Egiyan et al., PRL **96**, 082501(2006).

L. Frankfurt et al., Phys. Rev. C **48**, 2451 (1993).

K. Egiyan et al., Phys. Rev. C **68**, 014313 (2003). N. Fomin et al., Phys. Rev. Lett. **108**, 092502 (2012).

How? (do we get 25%)

- A/d (e, e') cross section ratios sensitive to $n_A(k)/n_d(k)$
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N. Fomin et al., PRL **108**, 092502 (2012)

$$\Rightarrow n_A(k > k_F) = a_2(A) \times n_d(k)$$

A	$a_2(A/D)$	A	$a_2(A/D)$
^3He	2.1 ± 0.1	^{12}C	4.7 ± 0.2
^4He	3.6 ± 0.1	^{63}Cu	5.2 ± 0.2
^9Be	3.9 ± 0.1	^{197}Au	5.1 ± 0.2

O. Hen et al., PRC **85**, 047301 (2012)

L. Frankfurt et al., Phys. Rev. C **48**, 2451 (1993).
 K. Egiyan et al., Phys. Rev. C **68**, 014313 (2003).

K. Egiyan et al., PRL **96**, 082501 (2006)

How? (do we get 25%)

Nuclei have a high-momentum tail!

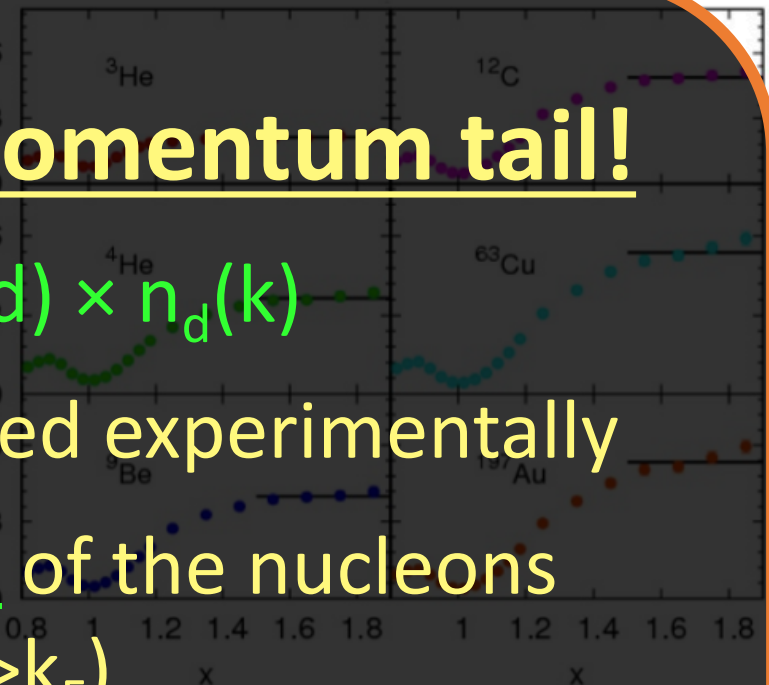
A/d (e, e') cross section ratios sensitive to

1. It scales: $n_A(k > k_F) = a_2(A/d) \times n_d(k)$

2. Scale factor, a_2 , determined experimentally

Observed scaling in for $x_B \geq 1.5$.

3. In $A \geq 12$ nuclei, 20 – 25% of the nucleons have high-momentum ($k > k_F$).



N. Fomin et al., PRL **108**, 092502 (2012)

$$\Rightarrow n_A(k > k_F) = a_2(A) \times n_d(k)$$

A	$a_2(A/D)$	A	$a_2(A/D)$
³ He	2.1 ± 0.1	¹² C	4.7 ± 0.2
⁴ He	3.6 ± 0.1	⁶³ Cu	5.2 ± 0.2
⁹ Be	3.3 ± 0.1	¹⁹⁷ Au	5.1 ± 0.2

O. Hen et al., PRC **85**, 047301 (2012)

L. Frankfurt et al., Phys. Rev. C **48**, 2451 (1993).
 K. Egiyan et al., Phys. Rev. C **68**, 014313 (2003).

K. Egiyan et al., PRL **96**, 082501 (2006)

How? (do we get 25%)

Nuclei have a high-momentum tail!

ratios sensitive to

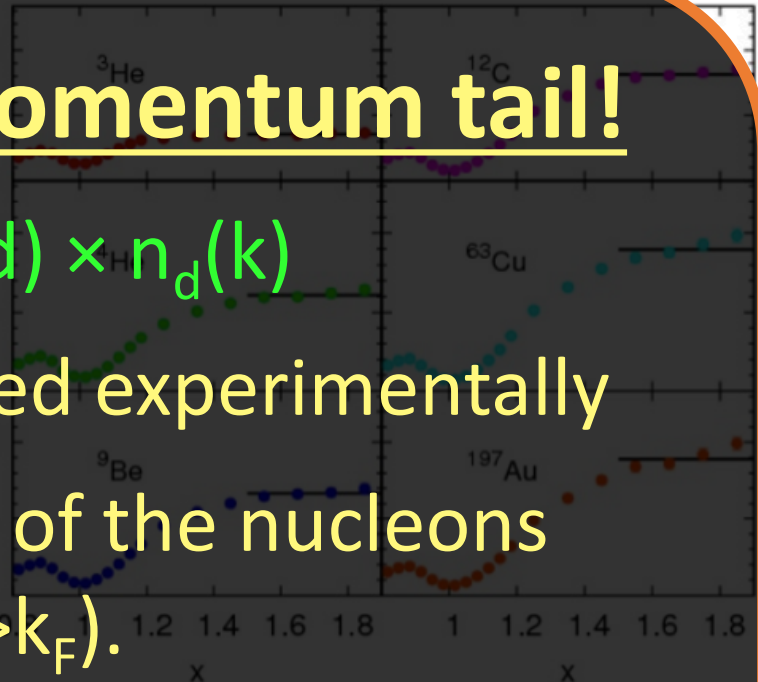
1. It scales: $n_A(k > k_F) = a_2(A/d) \times n_d(k)$

2. Scale factor, a_2 , determined experimentally

3. In $A \geq 12$ nuclei, 20–25% of the nucleons ≥ 1.5 have high-momentum ($k > k_F$).

Do ALL high-momentum nucleons come in

$\Rightarrow n_A(k > k_F) = a_2(A) \times n_d(k)$
pairs? What kind of pairs?



N. Fomin et al., PRL **108**, 092502 (2012)

A	$a_2(A/D)$	A	$a_2(A/D)$
³ He	1.0 ± 0.1	¹² C	4.7 ± 0.2
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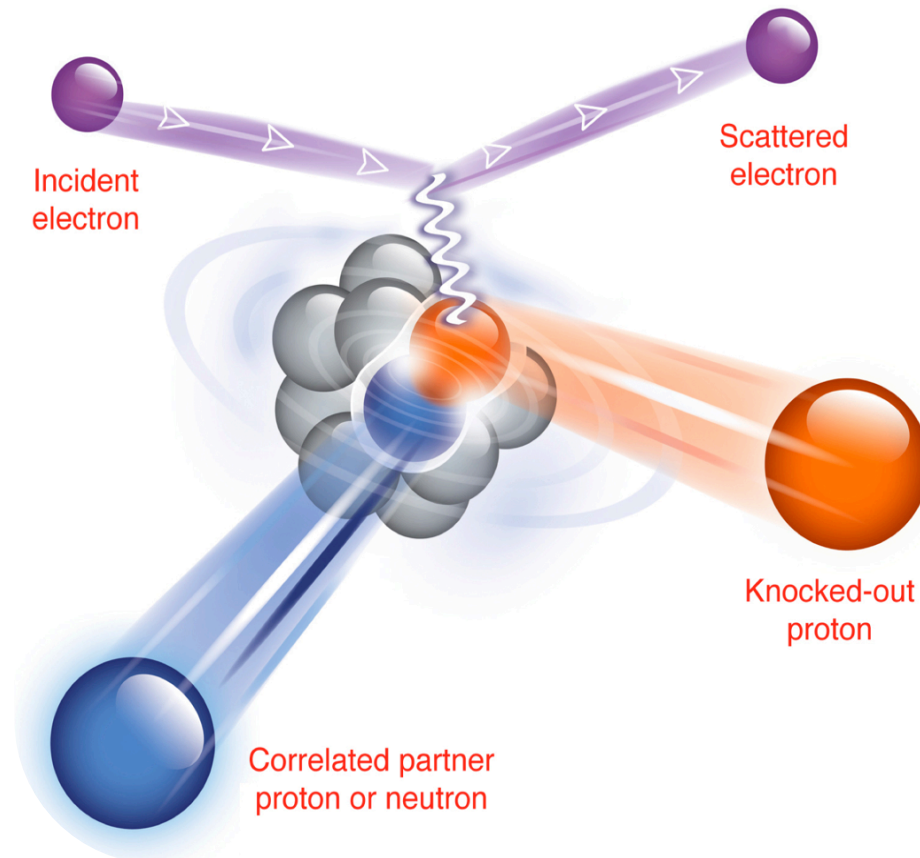
O. Hen et al., PRC **85**, 047301 (2012)

How? (do we get np dominance)

Breakup the pair =>

Detect both nucleons =>

Reconstruct 'initial' state

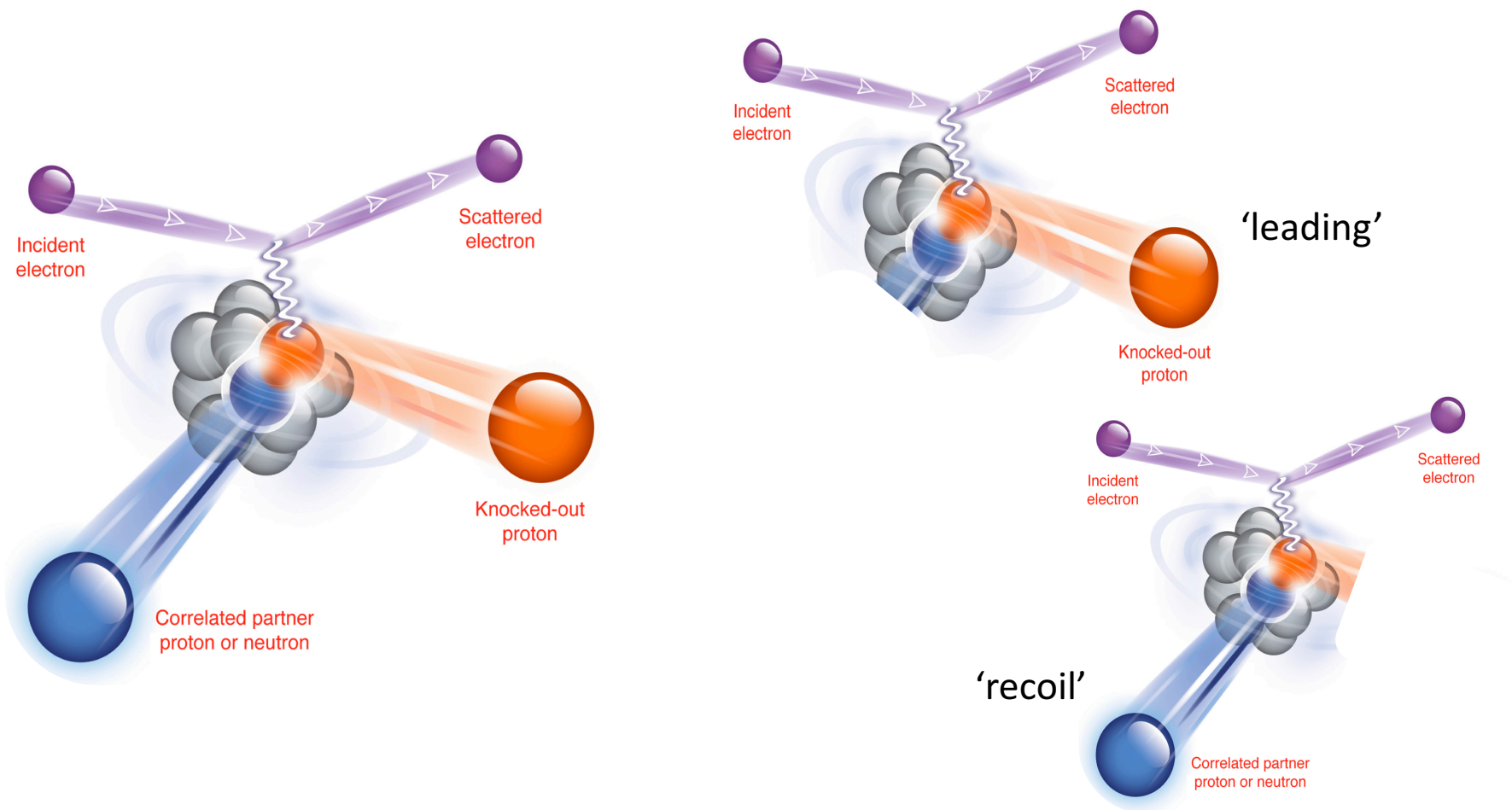


How? (do we get np dominance)

Breakup the pair =>

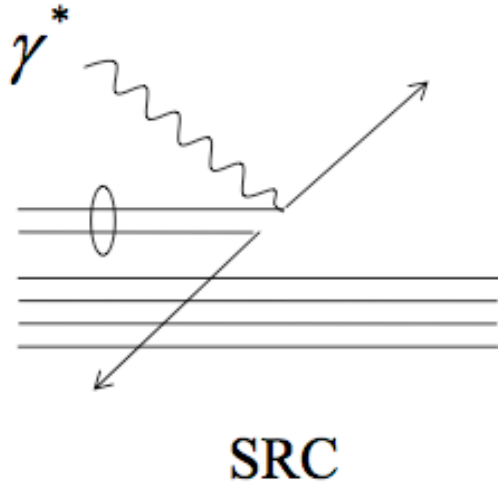
Detect both nucleons =>

Reconstruct 'initial' state

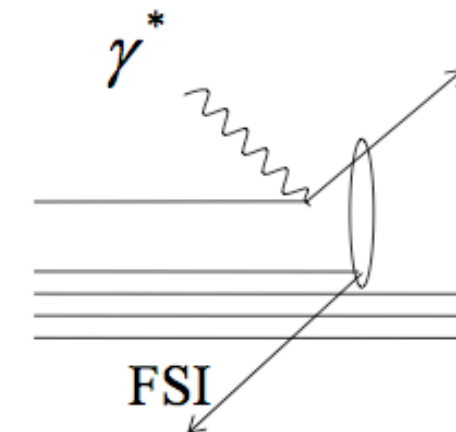
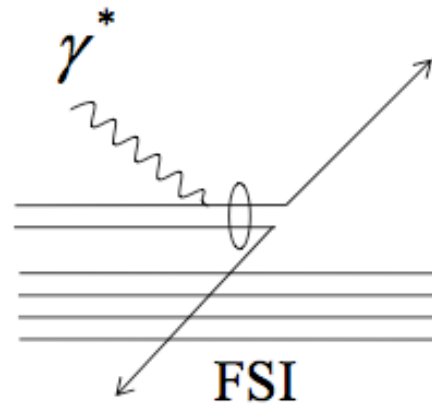
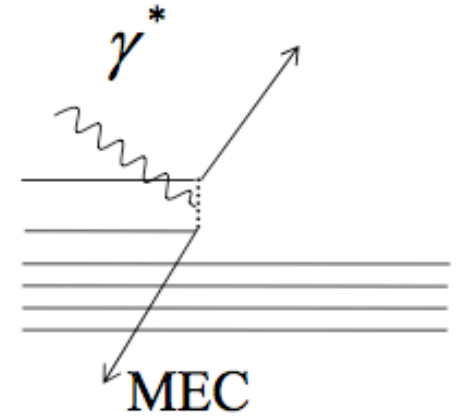
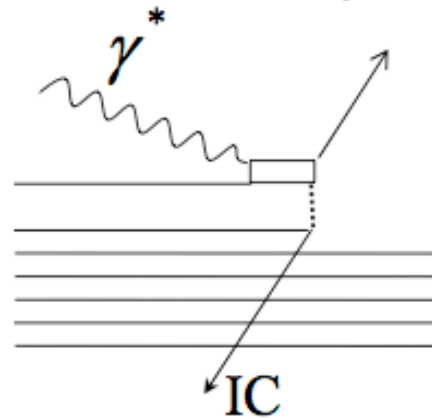


Issue: Reaction Mechanisms

What we want:



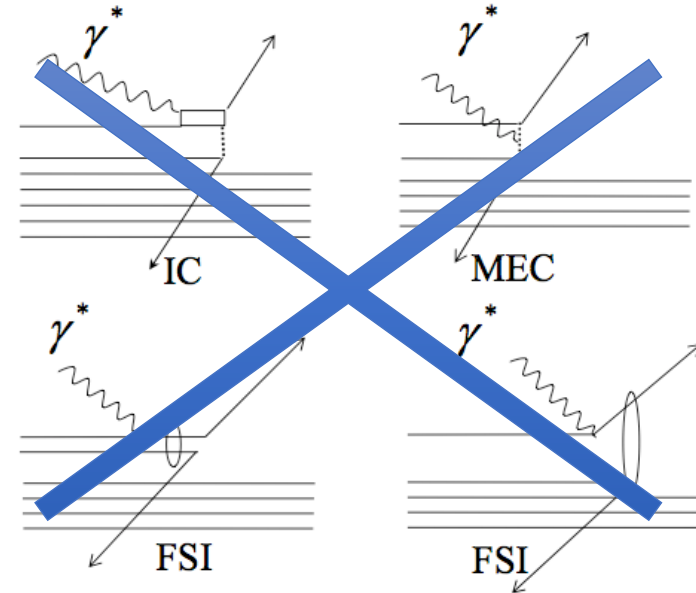
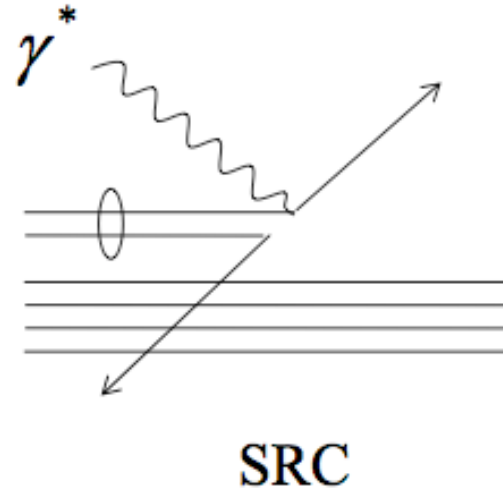
What we (might) get:



Solution: Hard Knockout Reactions!

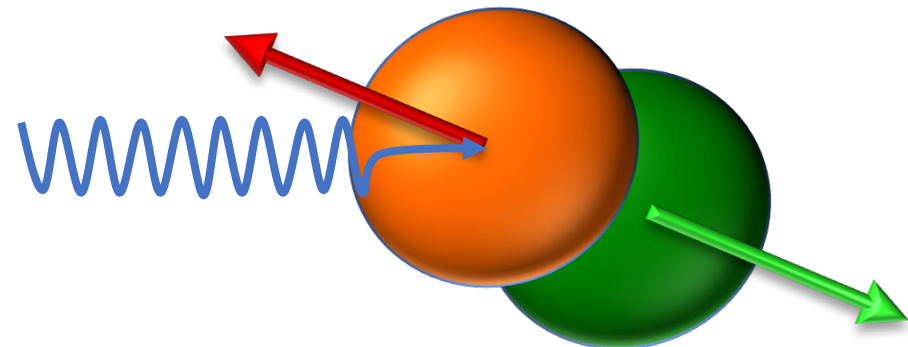
Trick: choose 'good' kinematics!

- $x_B > 1.2$
- $Q^2 \sim 2 \text{ (GeV/c}^2\text{)}$
- **Anti-Parallel Kinematics**

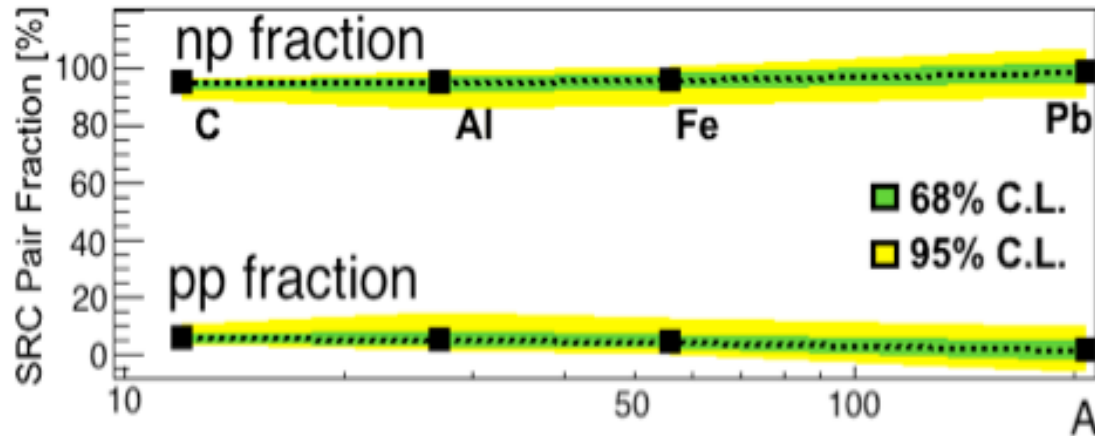
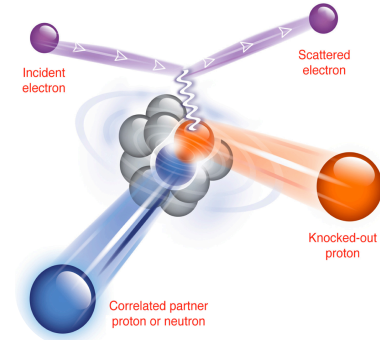


A word on FSI:

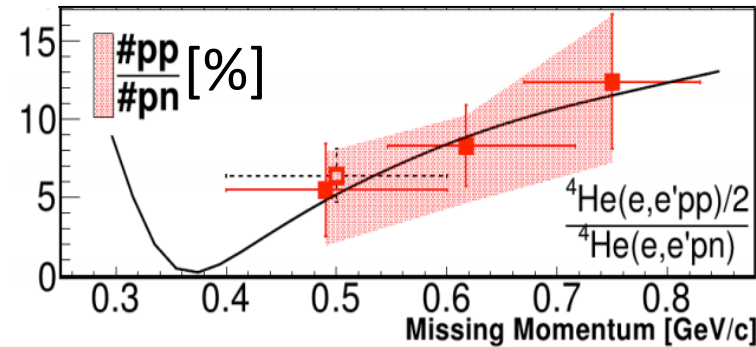
- Large- Q^2 ($\propto |t, u, s|$) allow using the Eikonal approximation for FSI calculations.
- Combines with $x_B > 1$ ensures FSI are confined to within the nucleons of the pair.



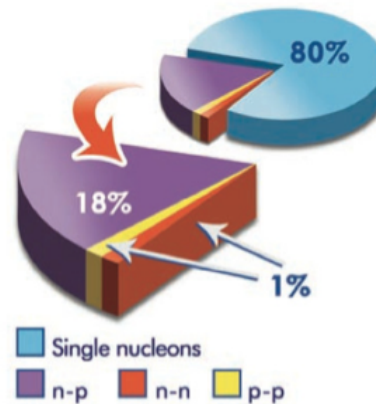
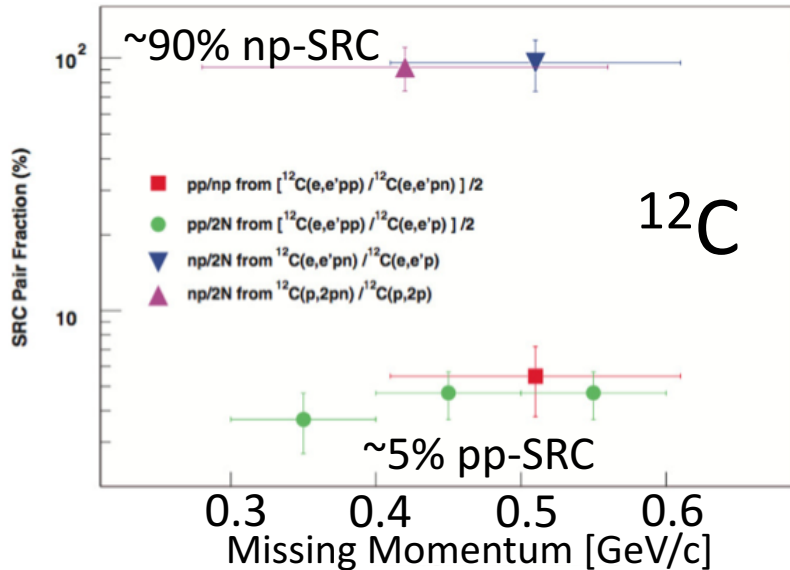
How? (do we get np dominance)



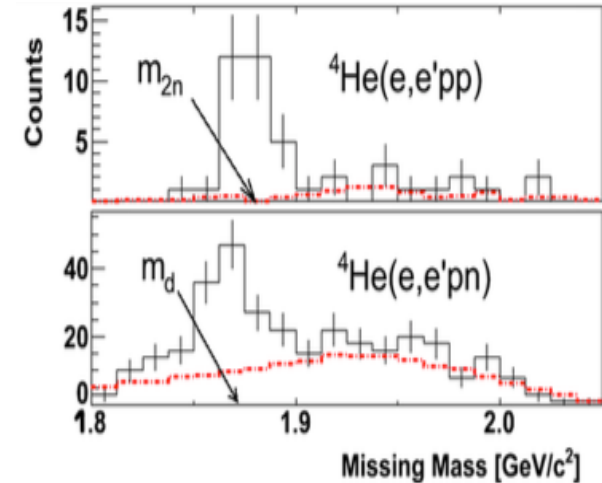
O. Hen et al., Science 364 (2014) 614



R. Subedi et al., Science 320 (2008) 1476



I. Korover et al., PRL 113 (2014) 022501



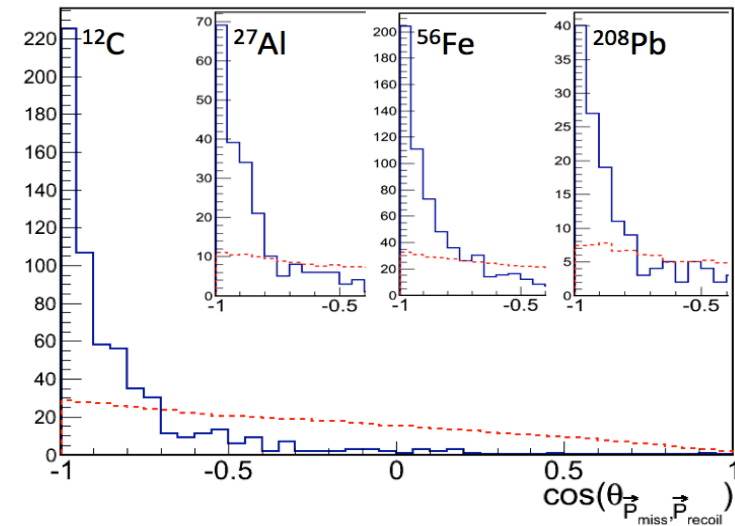
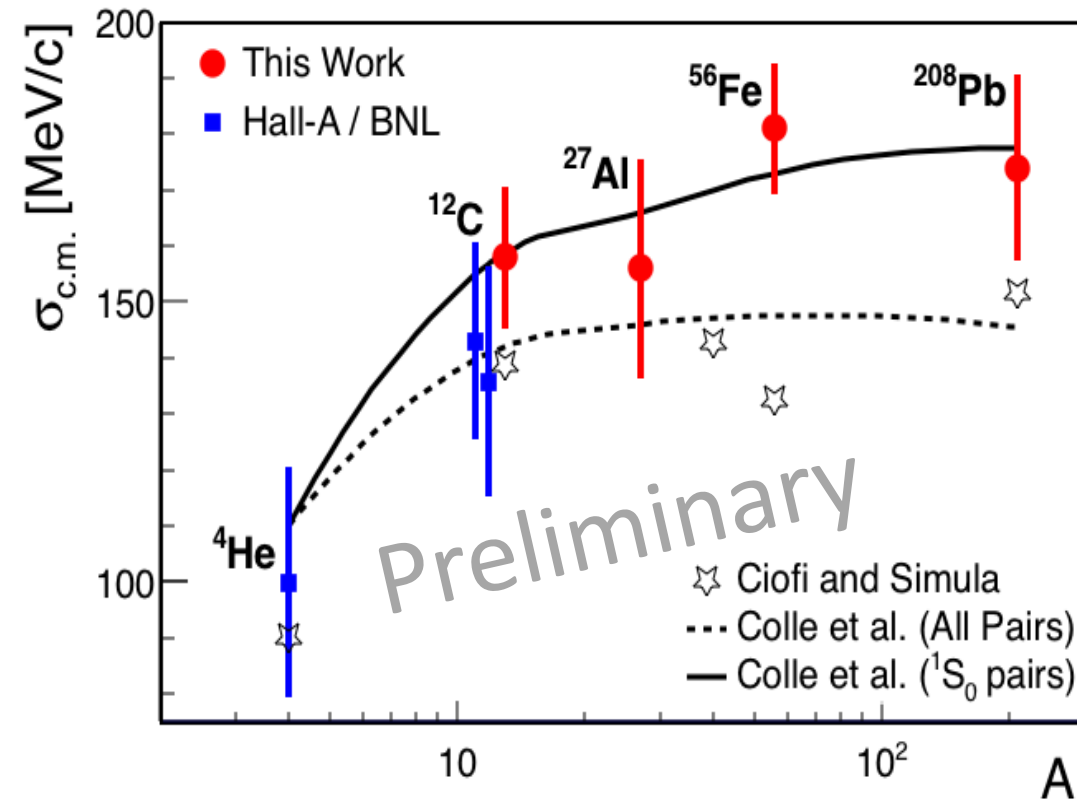
A. Tang et al., PRL (2003);

E. Piasezky et al., PRL (2006);

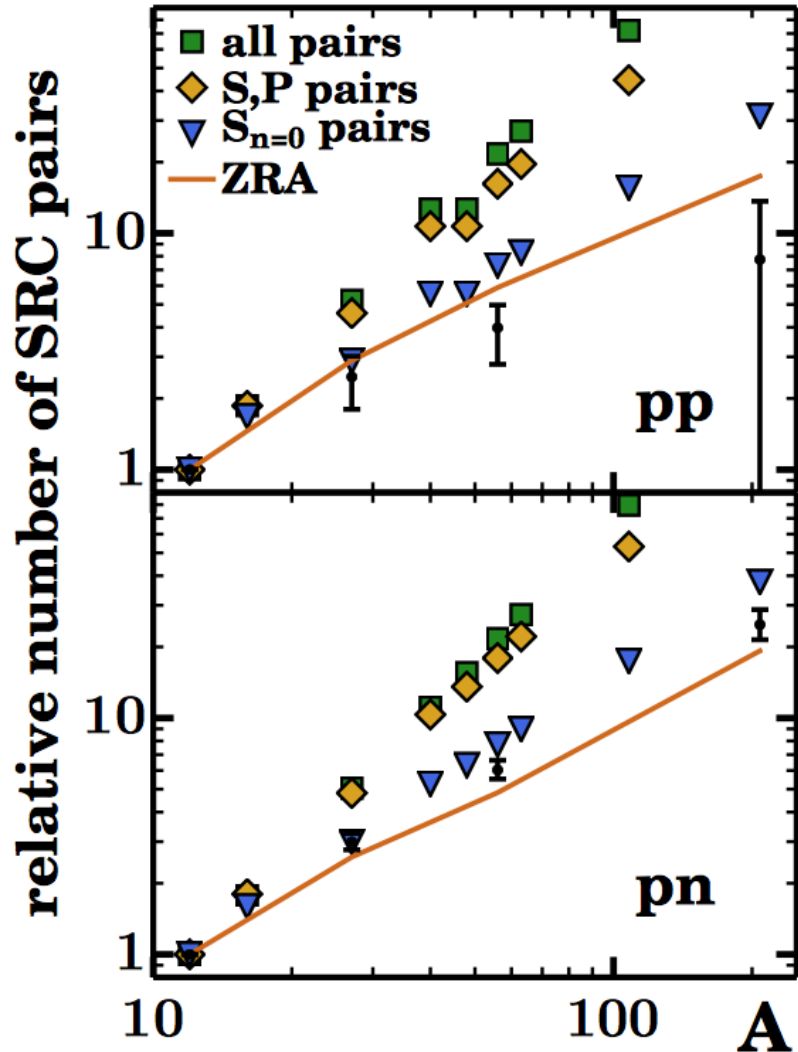
R. Shneor et al., PRL (2007)

How? (do we know its properties)

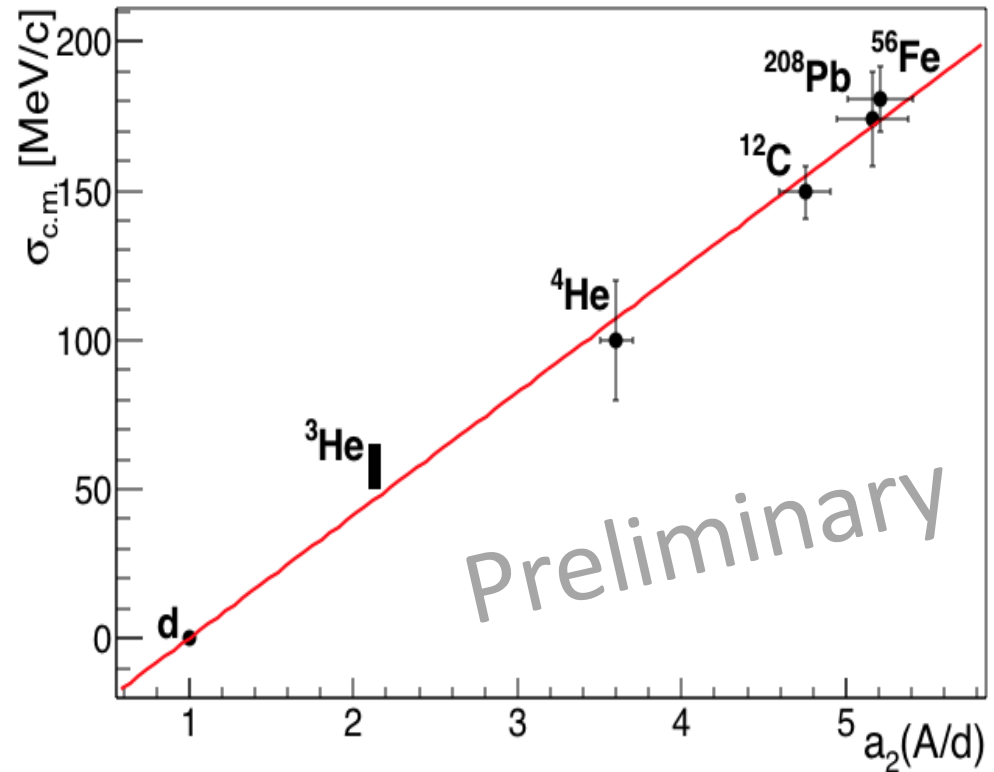
“... *high relative momentum* and *low c.m. momentum* compared to the Fermi momentum (k_F)”



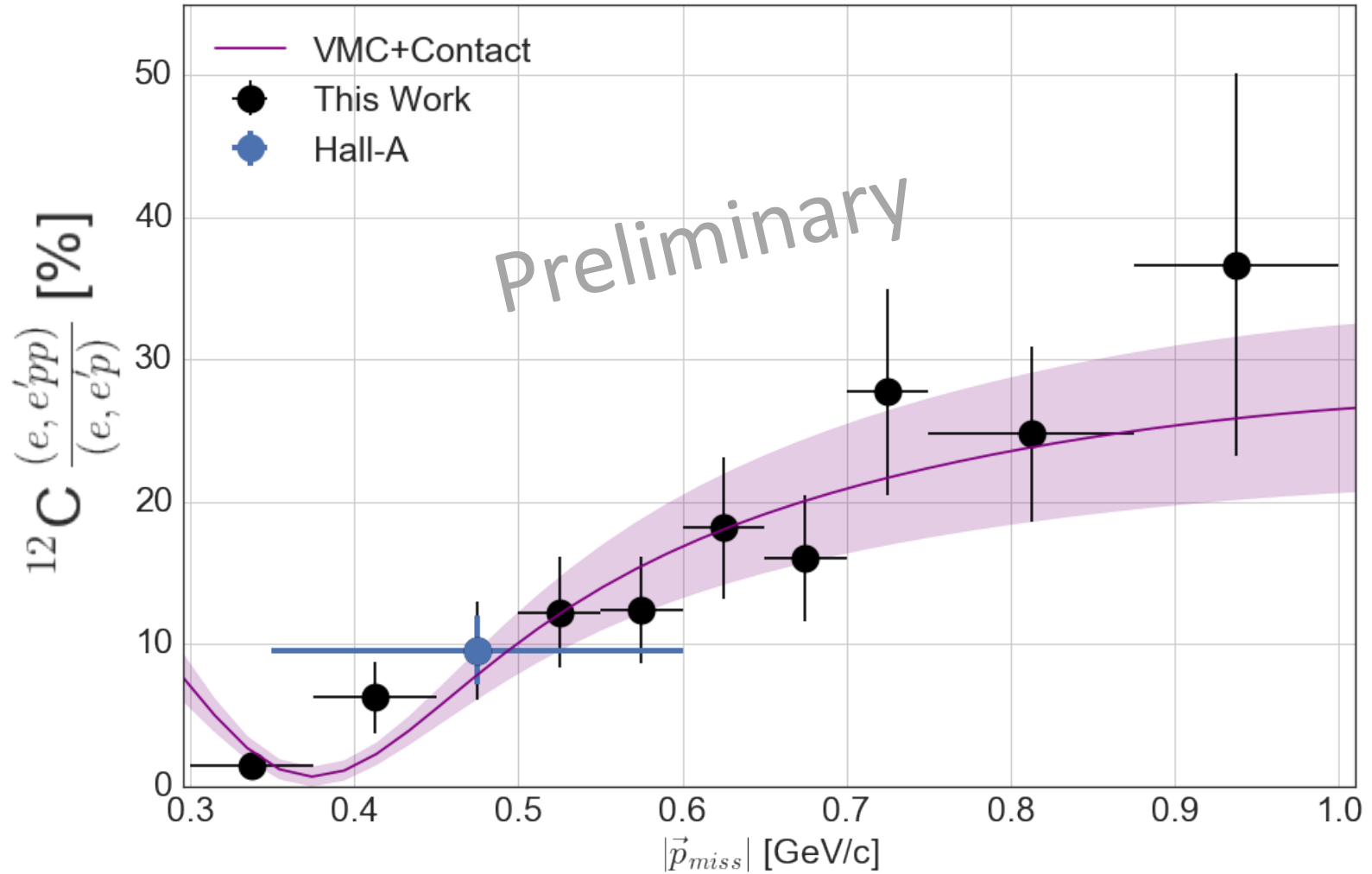
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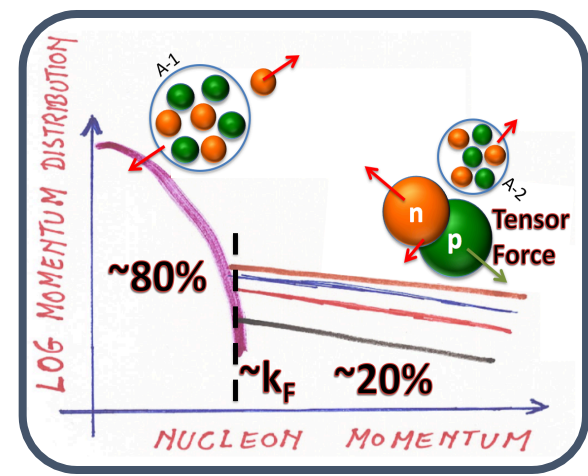
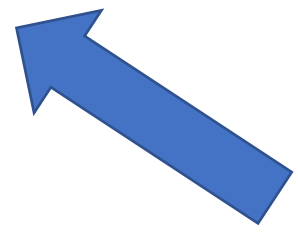
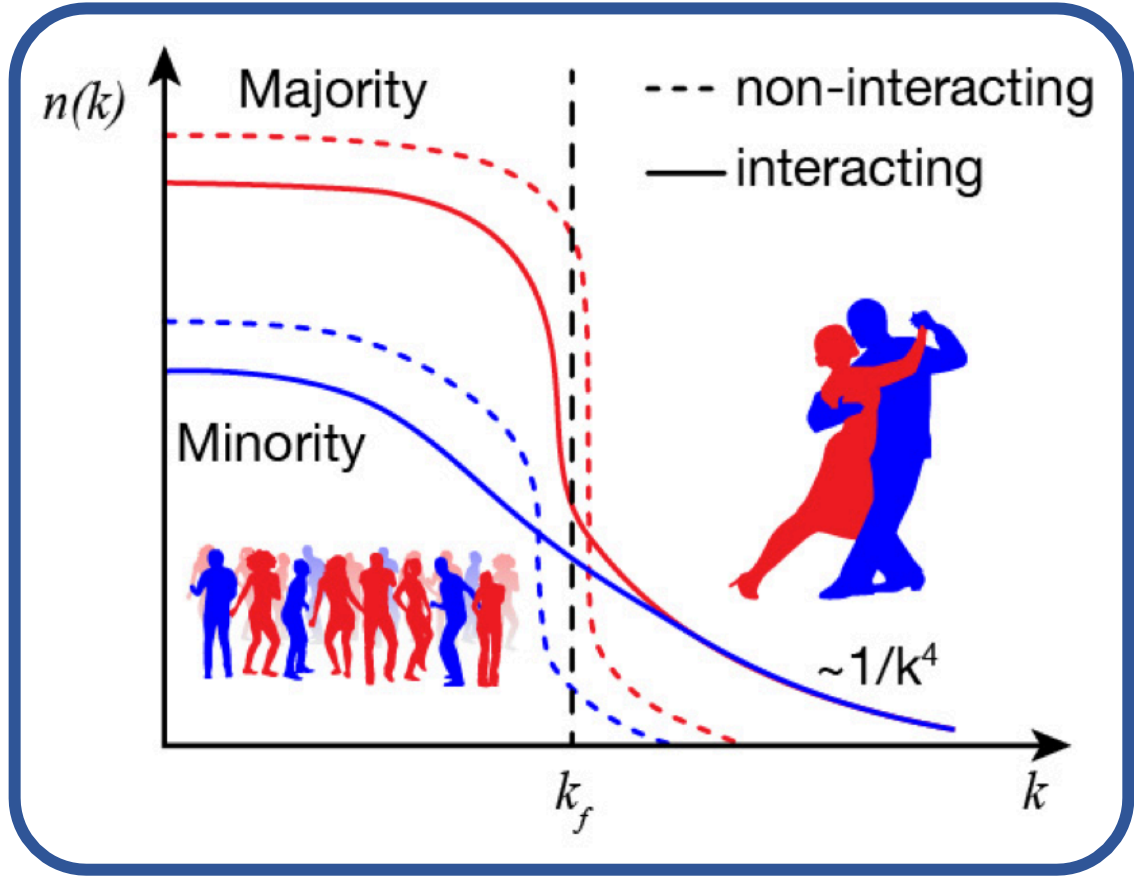
C. Colle et al., PRC (2015)



How? (do we probe the repulsive core)

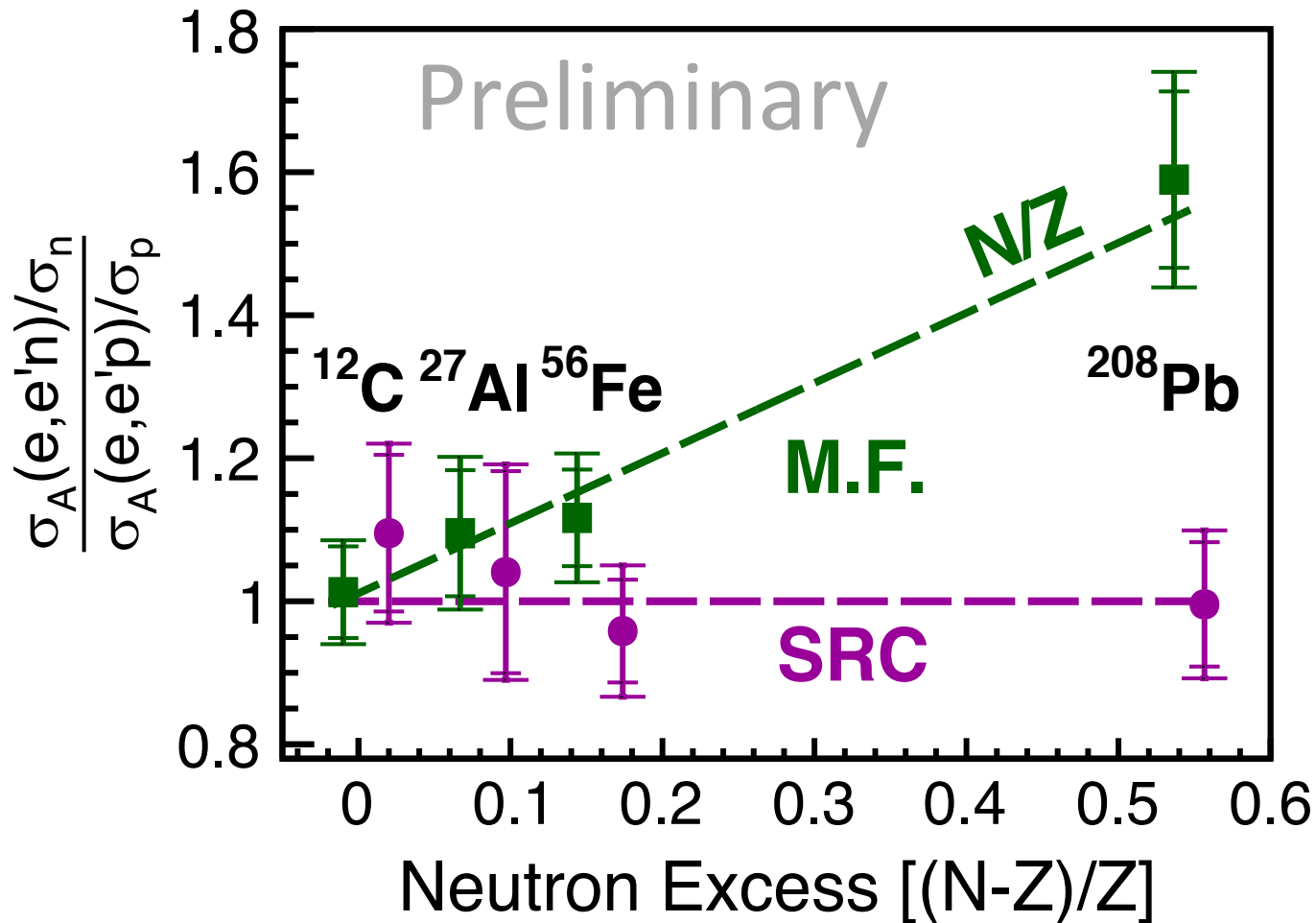


How? (do we study asymmetry dependence)



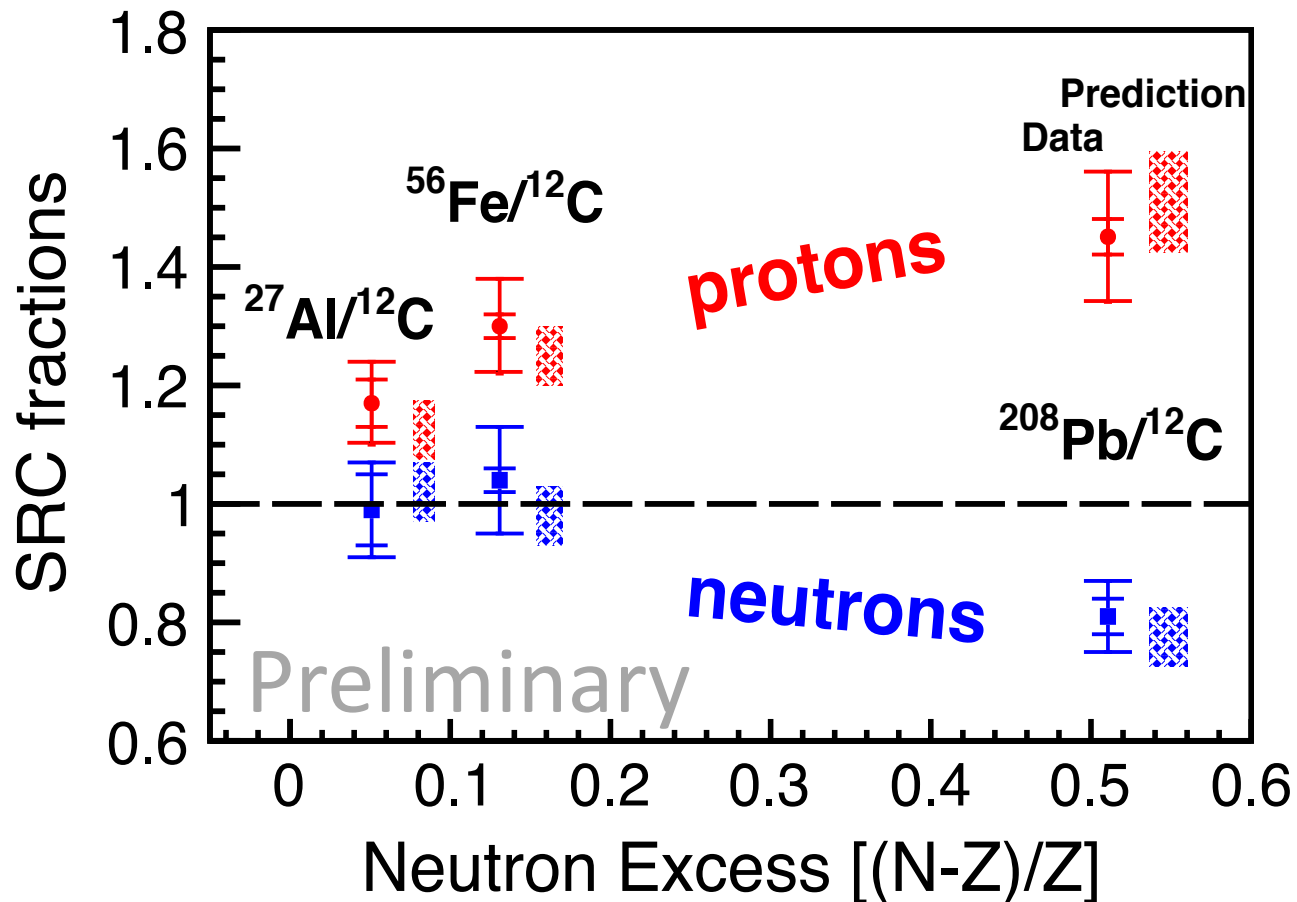
How? (do we study asymmetry dependence)

Same number of high-momentum protons and neutrons, even in neutron rich nuclei!



How? (do we study asymmetry dependence)

Protons are more correlated in neutrons rich nuclei!



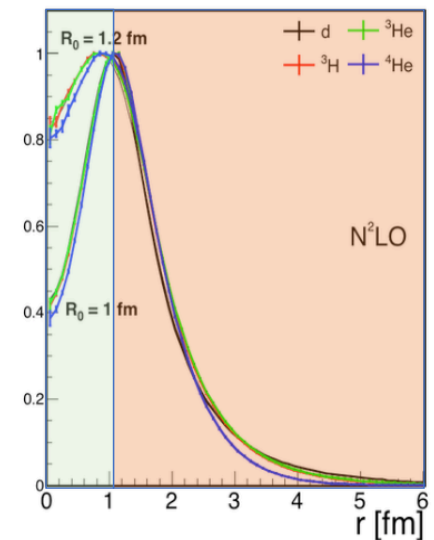
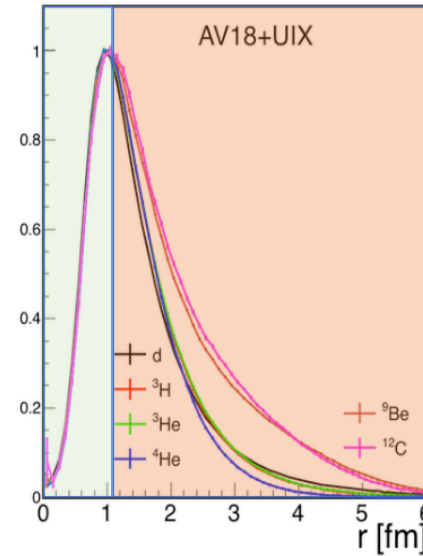
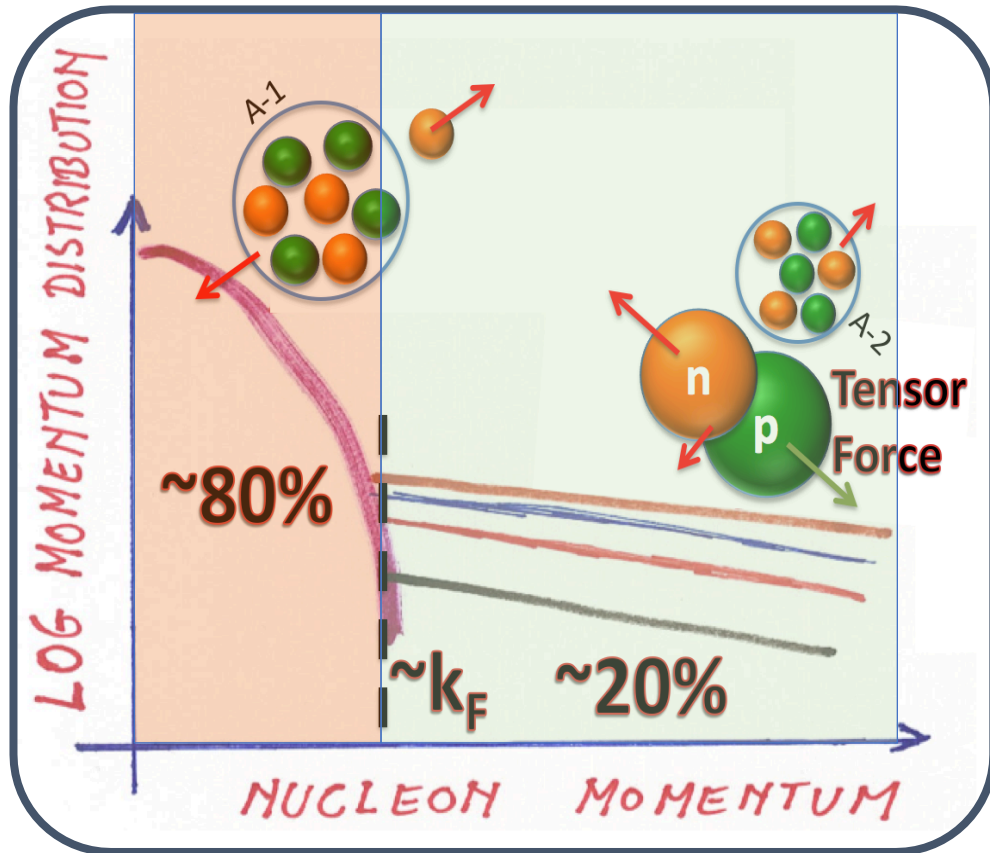
New Era in SRC Research!

Consistent set of (e,e') , $(e,e'p)$, $(e,e'pN)$ and $(p,2pn)$ measurements, on a variety of nuclei, allow quantifying SRCs with unprecedented accuracy!

1. SRC Exist in Nuclei (!) and account for:
 - $\sim 20\%$ of the nucleons in nuclei.
 - $\sim 100\%$ of the high- p ($k > k_F$) nucleons in nuclei.
2. Have large relative momentum and low c.m. momentum.
3. Predominantly due to np-SRC.
4. Universal for $A = 4 - 208$ nuclei.
5. np-SRC create a larger fraction of high-momentum protons in neutron rich nuclei!
6. **Tensor force** dominance at short distance.

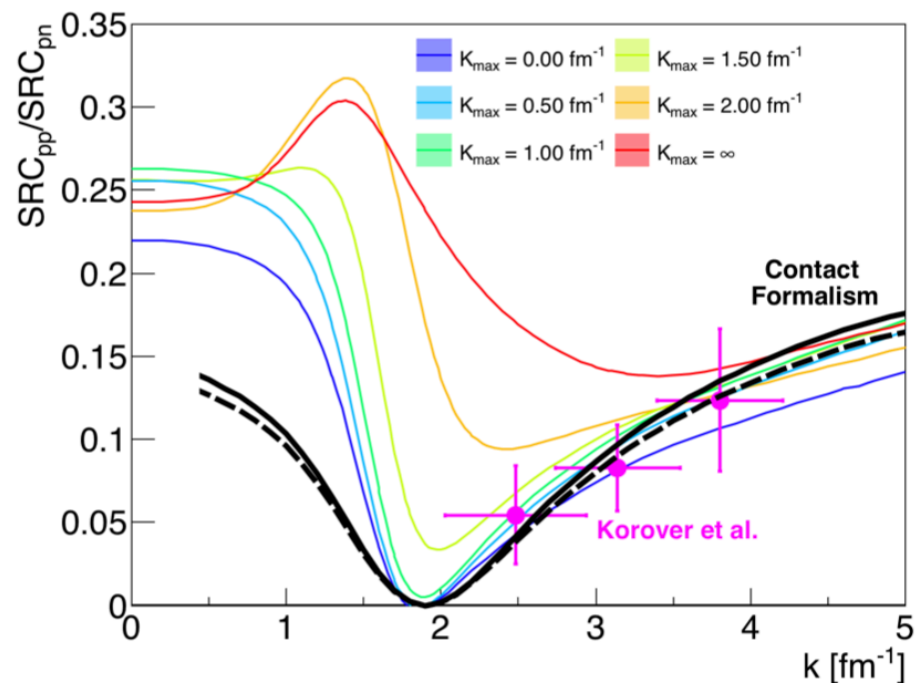
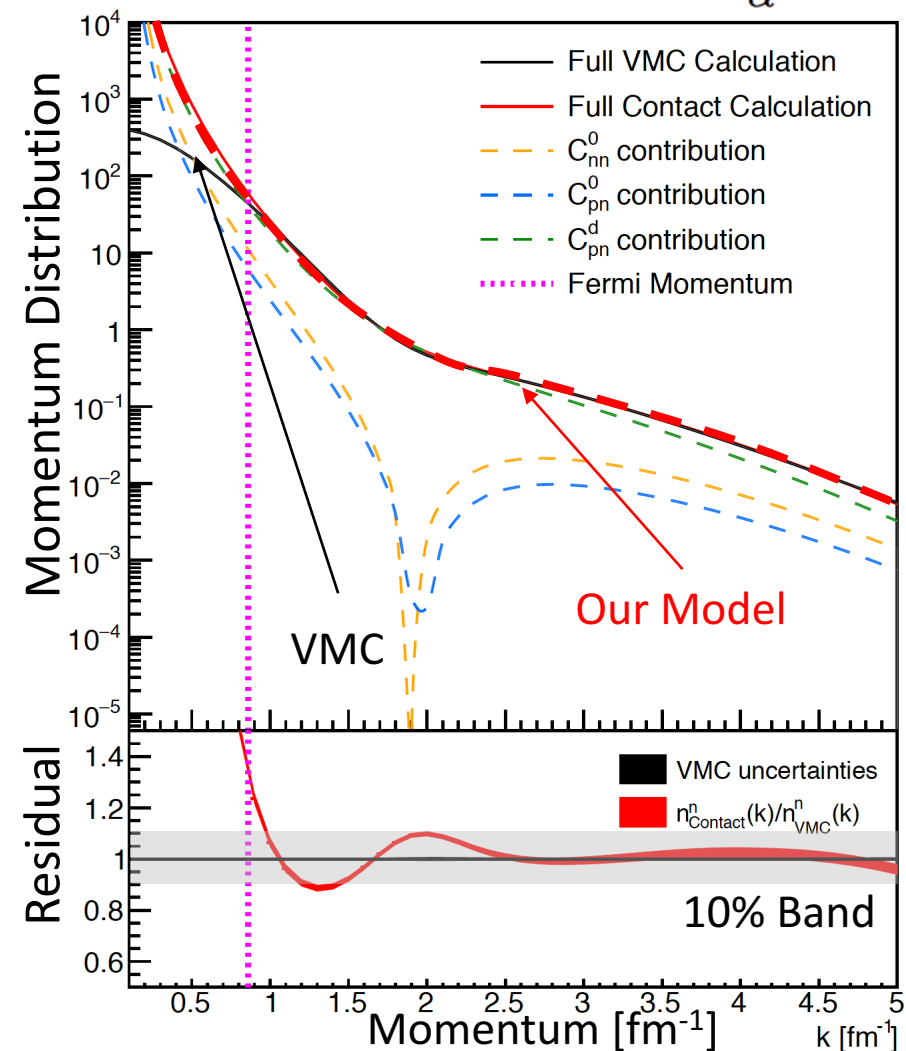
Universal Nuclear Structure?

Can we formulate a universal description of the SRC phase (in both coordinate and momentum space) WITHOUT relying on many-body calculations? (YES)



Universal Nuclear Structure!

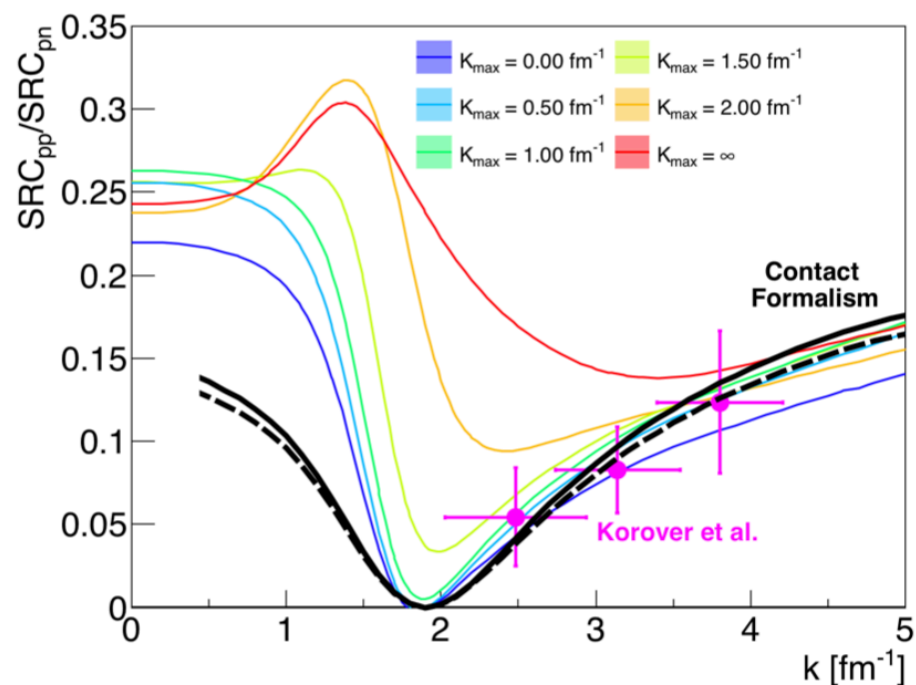
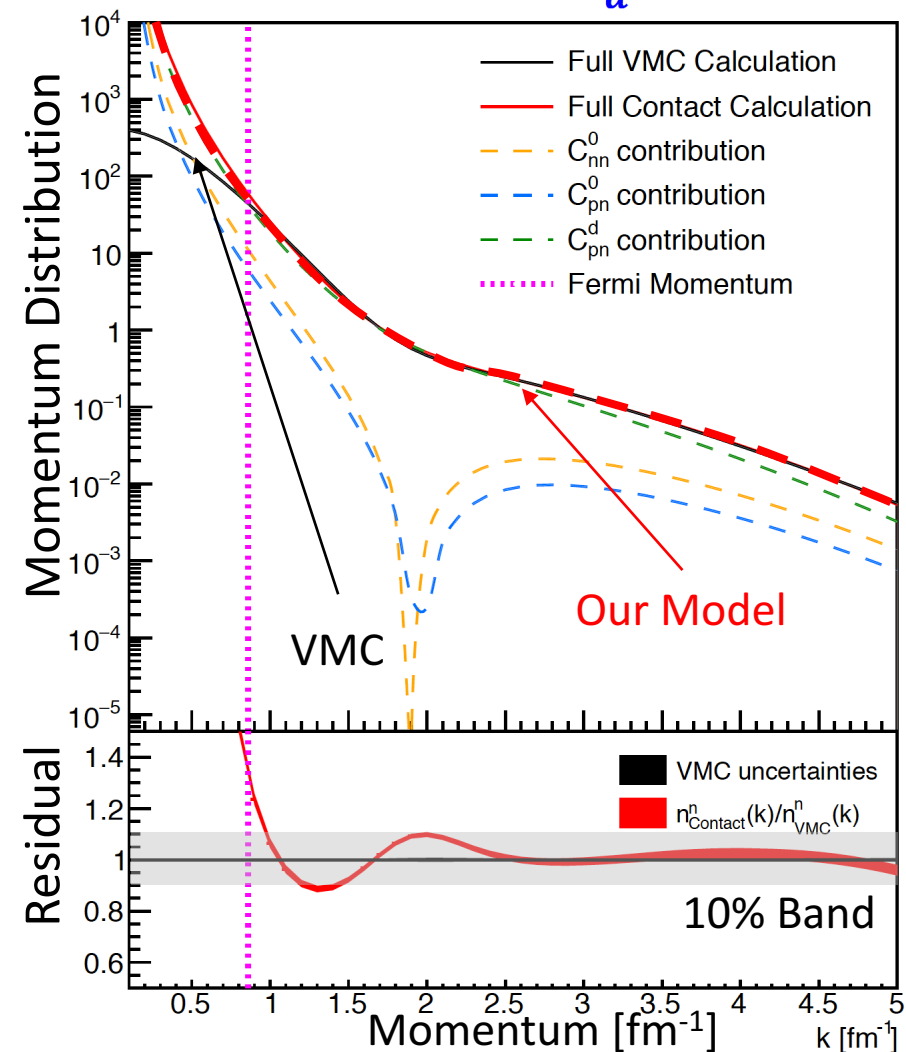
$$\Psi \xrightarrow{r_{ij} \rightarrow 0} \sum_{\alpha} \varphi_{\alpha}(\mathbf{r}_{ij}) A_{ij}^{\alpha}(\mathbf{R}_{ij}, \{\mathbf{r}\}_{k \neq ij})$$



Nuclear contacts can also be extracted from experiment!

Universal Nuclear Structure!

$$n_p(k) = \sum_{\alpha} |\tilde{\varphi}_{pp}^{\alpha}(k)|^2 2C_{pp}^{\alpha} + \sum_{\alpha} |\tilde{\varphi}_{pn}^{\alpha}(k)|^2 C_{pn}^{\alpha}$$



Nuclear contacts can also be extracted from experiment!

Short Range Correlations and the EMC Effect in Effective Field Theory

Jiunn-Wei Chen,^{1,2,*} William Detmold,^{2,†} Joel E. Lynn,^{3,4,‡} and Achim Schwenk^{3,4,5,§}

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²*Center for Theoretical Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA*

³*Institut für Kernphysik, Technische Universität Darmstadt, 64289 Darmstadt, Germany*

⁴*ExtreMe Matter Institute EMMI, GSI Helmholtzzentrum für Schwerionenforschung GmbH, 64291 Darmstadt, Germany*

⁵*Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, 69117 Heidelberg, Germany*

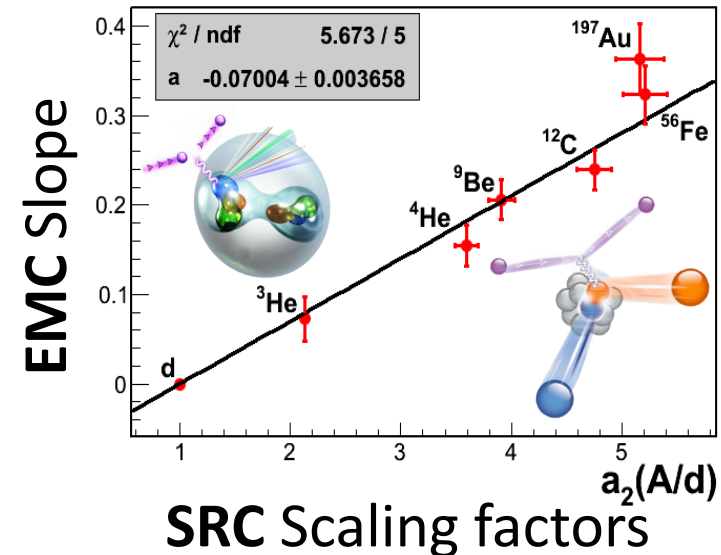
arXiv: 1607.03065 (2016)

EFT description of bound nucleon structure:

$$F_2^A(x, Q^2)/A = F_2^N(x, Q^2) + g_2(A, \Lambda) f_2(x, Q^2, \Lambda).$$

$$g_2(A, \Lambda) = \frac{1}{A} \langle A | \underbrace{(N^\dagger N)^2}_{\text{SRC contact}} | A \rangle_\Lambda$$

$$a_2(A, x > 1) = \frac{g_2(A, \Lambda)}{\text{[SRC Scaling Factor]} g_2(2, \Lambda)}$$



RMP Review

Nucleon-Nucleon Correlations and the Quarks Within

Or Hen

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MA 02139*

Gerald A. Miller

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University of Washington, Seattle,
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Eli Piassetzky

*School of Physics and Astronomy,
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Israel*

Lawrence B. Weinstein

*Department of Physics,
Old Dominion University, Norfolk,
VA 23529*

(Dated: November 2, 2016)

- conventional (non-quark) nuclear physics cannot account for the EMC effect
- models need to include nucleon modification to account for the EMC effect. These models can modify the structure of either:
 - mean field nucleons, or
 - nucleons belonging to SRC pairs.
- there is a phenomenological connection between the strength of the EMC effect and the probability that a nucleon belongs to a two-nucleon SRC pair ($a_2(A)$), see Fig. 33.
- the influence of SRC pairs can account for the EMC-SRC correlation because both effects are driven by high virtuality nucleons with $p^2 \neq M^2$,
- the connection between the EMC effect and the coefficients $a_2(A)$ has been derived using two completely different theories, so that this connection is no accident
- nuclei must contain a small percentage of baryons that are not nucleons. Such baryons exist in the short-ranged correlations and are the source of the EMC effect.

Where? (do we go from here)

- **Probe universality and Factorization breakdown.**
- SRC formation process.
- Proton dynamics in neutron rich nuclei
- Nuclear Interaction at *very* short distances – NN repulsive core
- Direct observation (discovery) of 3N-SRC
- Non-nucleonic degree of freedom in SRCs

SRC Studies Hit a Statistic Wall

experiment	pp pairs	np pairs	nn pairs
EVA/BNL	-	18	-
E01-015/JLab	263	179	-
E07-006/JLab	50	223	-
CLAS/JLab	1533	-	-
Total	<2000	<450	0

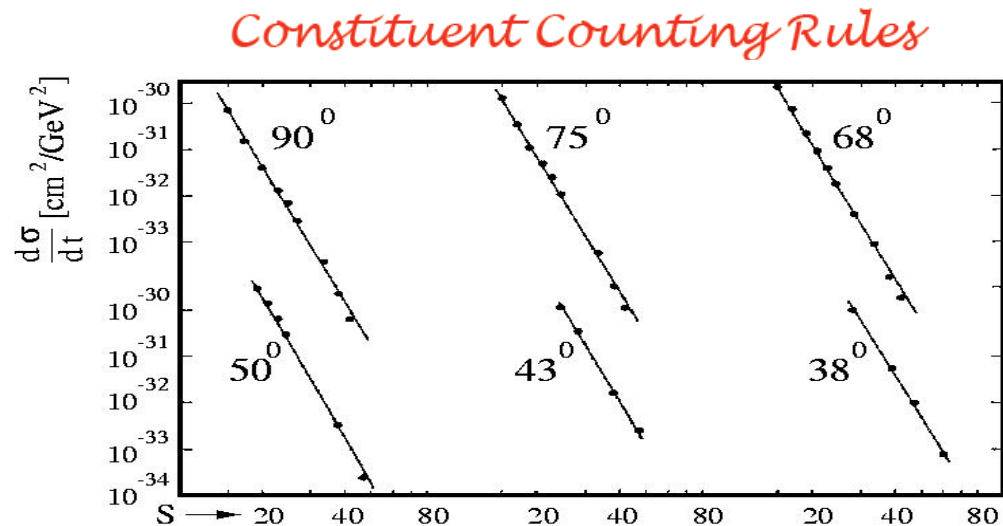
=> Need 1-2 orders of magnitude improvement to address next generation BIG questions

Proton beam advantage:

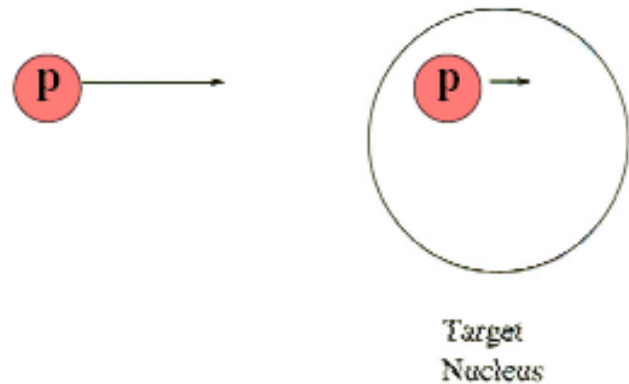
Selective Attention!

pp \rightarrow pp elastic scattering
near 90⁰ c.m.:

$$\frac{d\sigma}{dt} \propto s^{-10}$$



Incident proton prefers to
interact with forward going
high momentum nuclear
protons



Proton beam advantage:

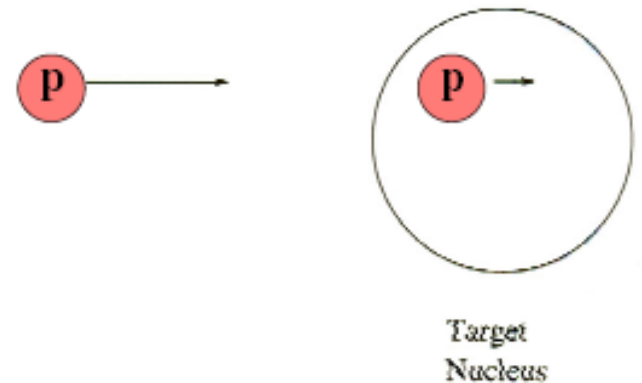
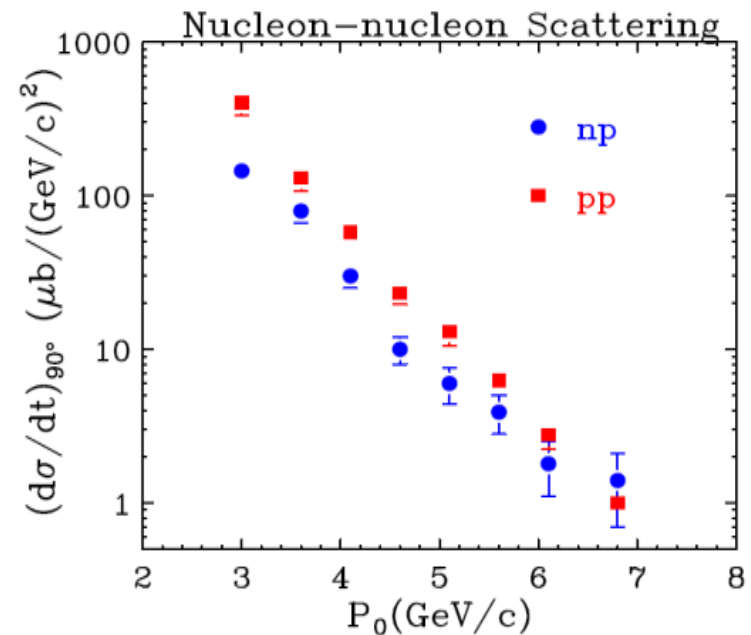
Selective Attention!

pp \rightarrow pp elastic scattering
near 90° c.m:

$$\frac{d\sigma}{dt} \propto s^{-10}$$

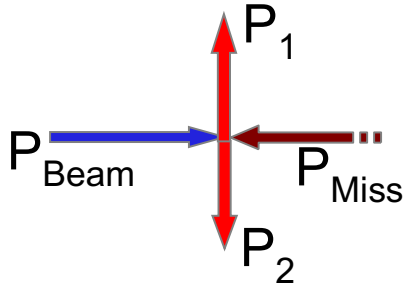
Lower energy increase the cross-section and the sensitivity to SRC via S weighting. But... **need to keep a hard process ($s, t, u > 2 \text{ GeV}^2$).**

3.5 – 5 GeV beams are ideal!

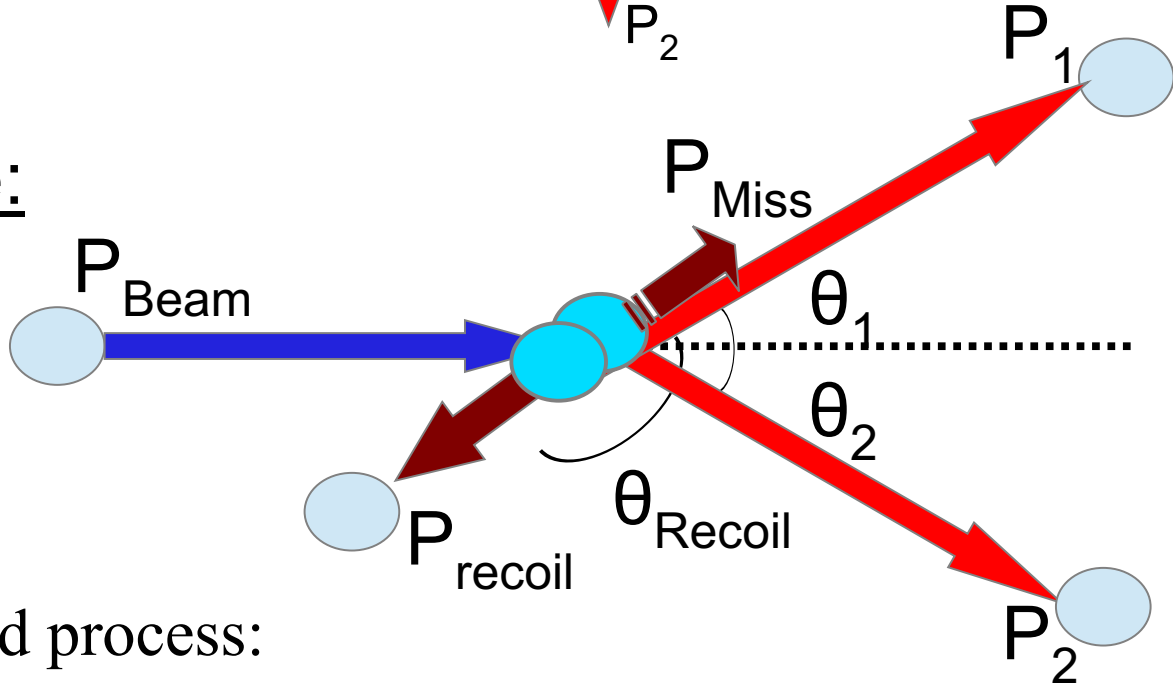


SRC Kinematics: 2N-SRC

C.M. Frame ($90^\circ \pm 10^\circ$ scattering):



Lab Frame:



• SRC dominance:

$$|P_{\text{recoil}}| \geq 250 \text{ MeV} / c$$

• Hard process:

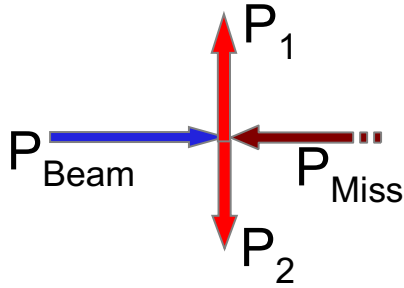
$$-t = -(pb - p1)^2 > 2(\text{GeV} / c)^2$$

$$-u = -(pb - p2)^2 > 2(\text{GeV} / c)^2$$

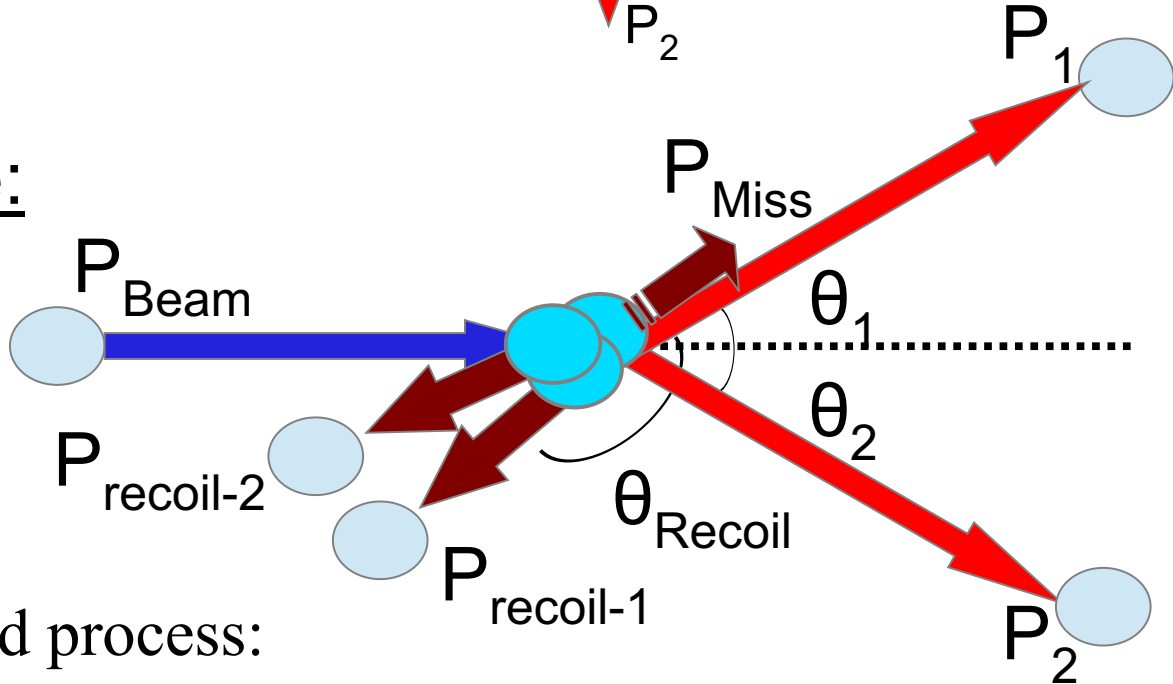
$$s = (p1 + p2)^2 > 2(\text{GeV} / c)^2$$

SRC Kinematics: 3N-SRC

C.M. Frame ($90^\circ \pm 10^\circ$ scattering):



Lab Frame:



• SRC dominance:

$$|p_{\text{recoil}}| \geq 250 \text{ MeV} / c$$

• Hard process:

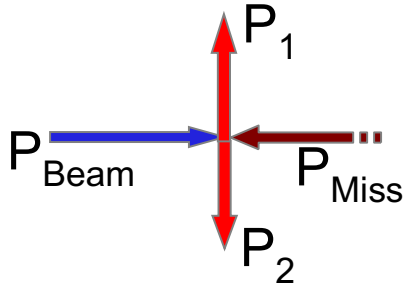
$$-t = -(pb - p1)^2 > 2(\text{GeV} / c)^2$$

$$-u = -(pb - p2)^2 > 2(\text{GeV} / c)^2$$

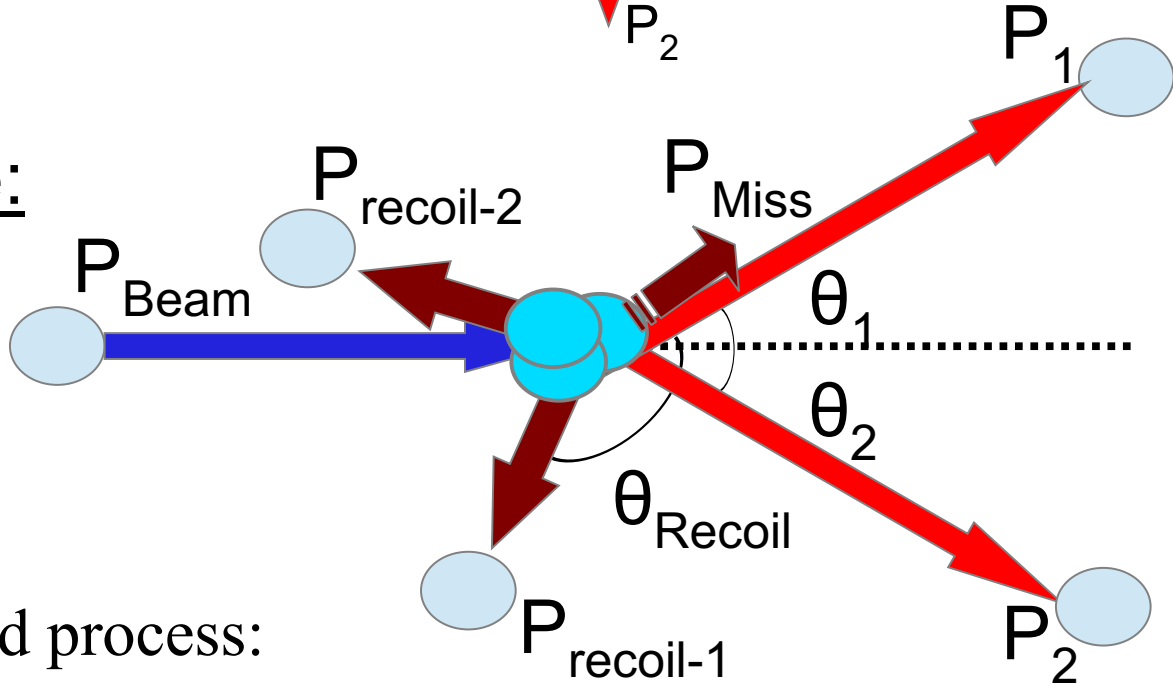
$$s = (p1 + p2)^2 > 2(\text{GeV} / c)^2$$

SRC Kinematics: 3N-SRC

C.M. Frame ($90^\circ \pm 10^\circ$ scattering):



Lab Frame:



• SRC dominance:

$$|P_{\text{recoil}}| \geq 250 \text{ MeV} / c$$

• Hard process:

$$-t = -(pb - p1)^2 > 2(\text{GeV} / c)^2$$

$$-u = -(pb - p2)^2 > 2(\text{GeV} / c)^2$$

$$s = (p1 + p2)^2 > 2(\text{GeV} / c)^2$$

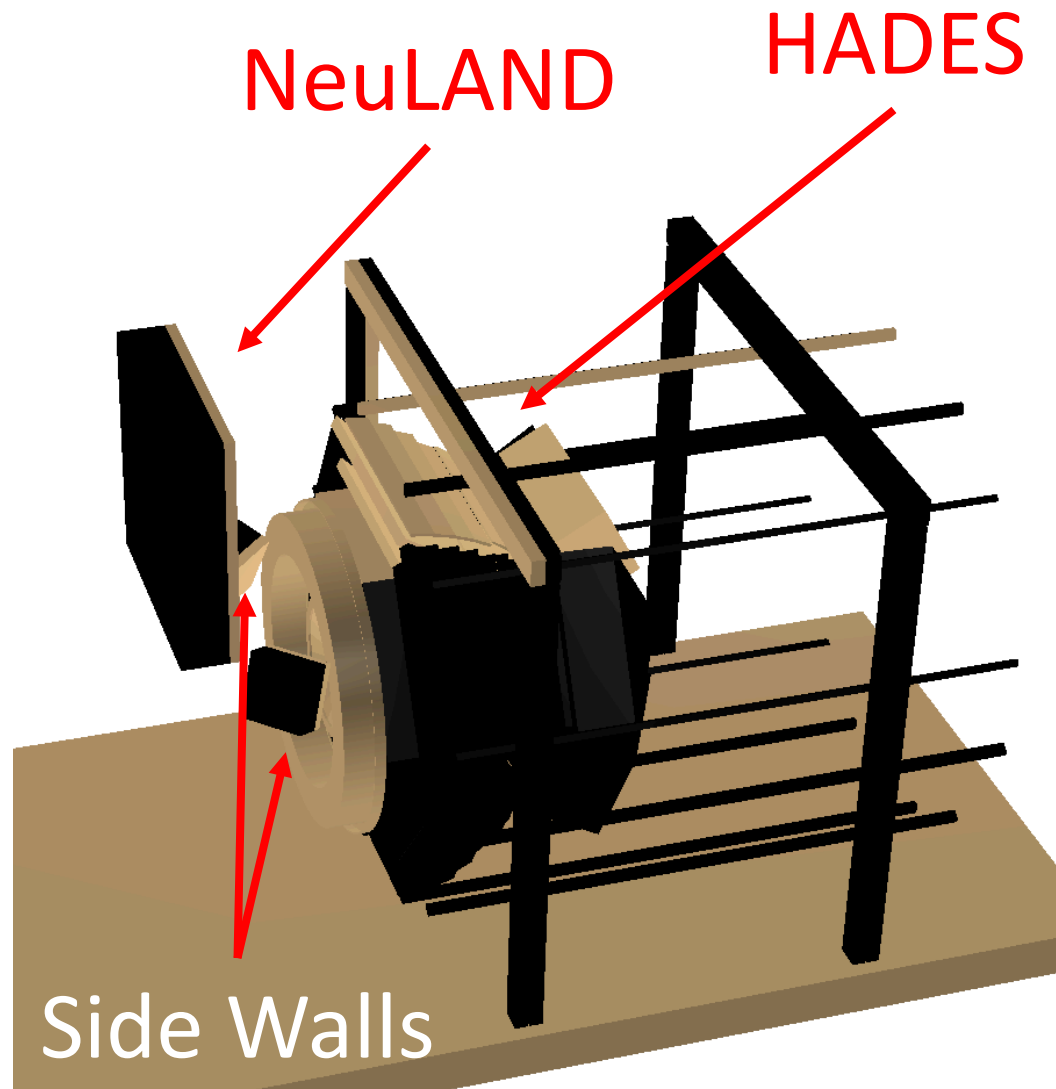
HADES + NeuLAND

Central Wall (NeuLAND)

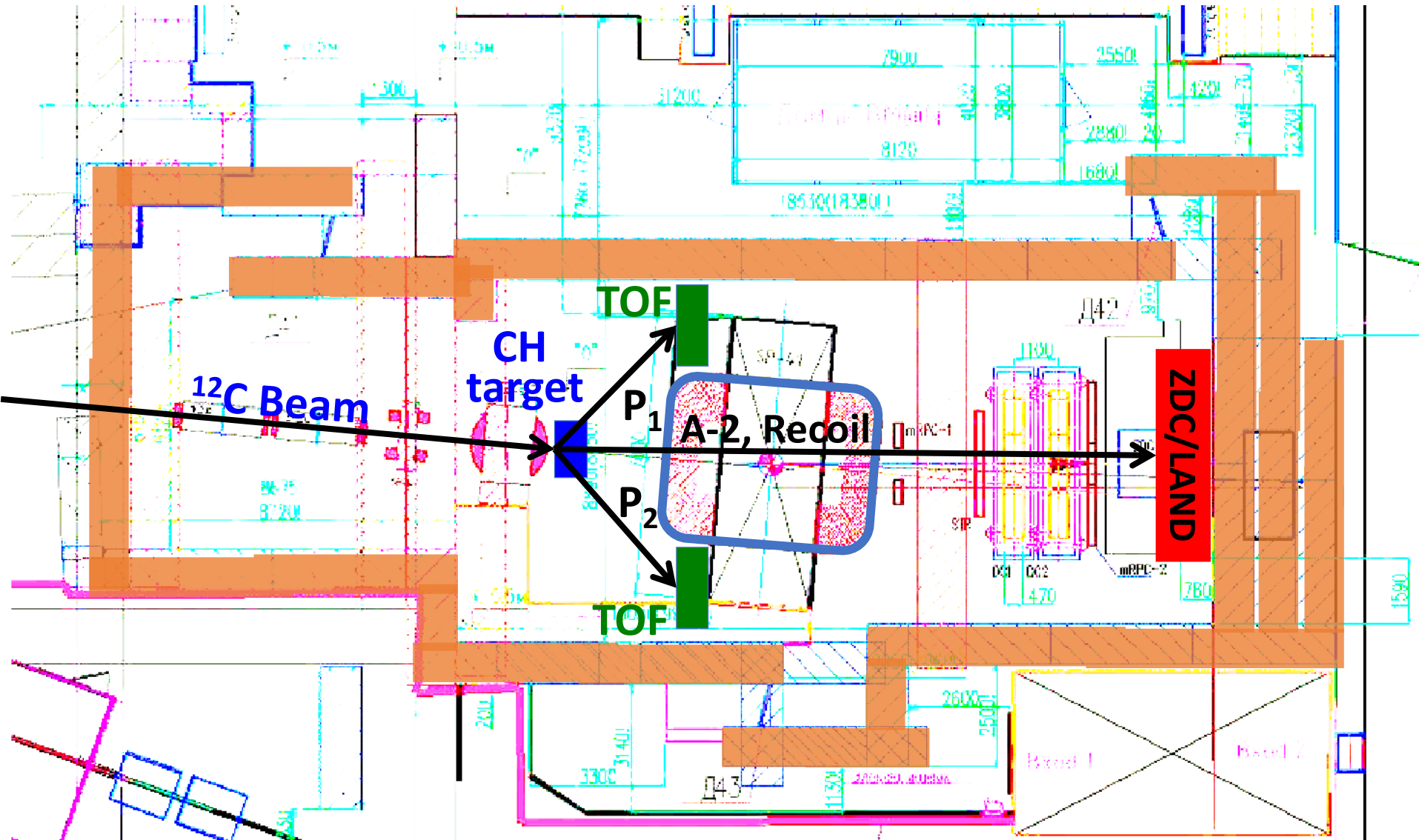
- 250x250x60 cm³
- 6 planes 10 cm thick
- 2 cm veto plane

Side Walls:

- 70x70x40 cm³
- 4 planes 10 cm thick
- 2 cm veto plane

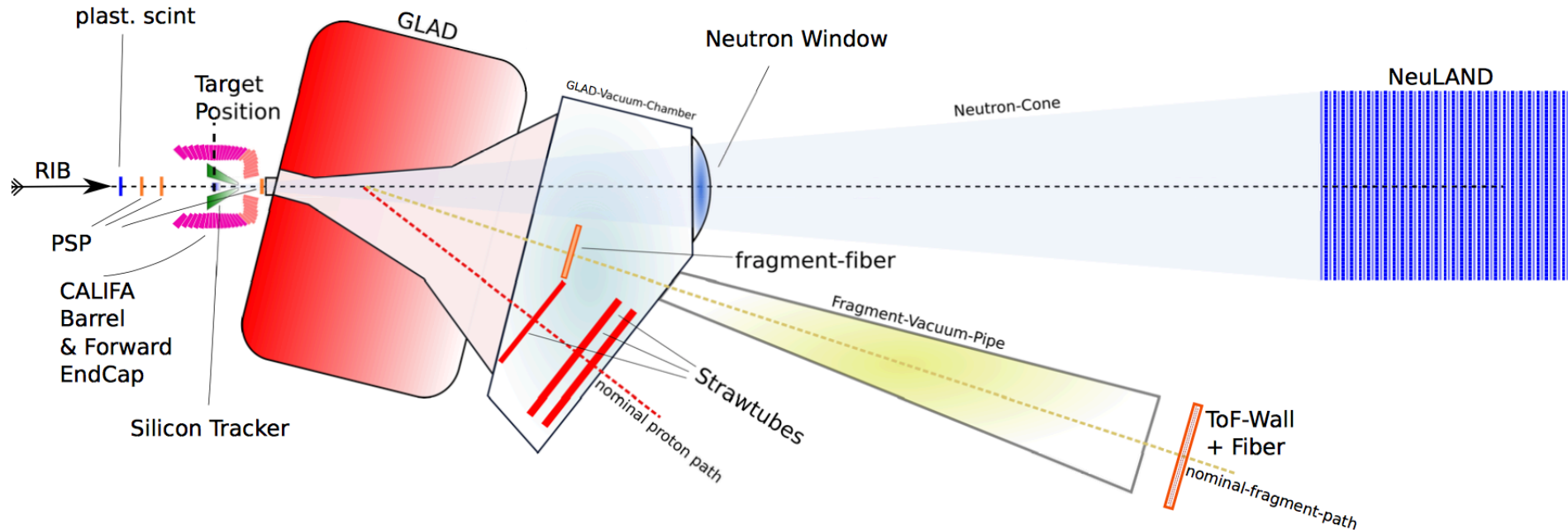


Inverse Kinematics @ DUBNA (Nov. 2017!?!)



Inverse Kinematics @ GSI

R3B Phase 1



GLAD: 0 – 40 degree, +/-80 mrad, 5 Tm bending power

Relative momentum resolution: 10^{-3}

Neutrons: +/- 80 mrad at 15 m distance



The Correlations group



- MIT (Or Hen):



Barak Schmookler



Reynier Torres



Efrain Segarra



Afroditi Papadopoulou



Axel Schmidt



George Laskaris



Maria Patsyuk



Taofeng Wang

- TAU (Eli Piassetzky):



Erez Cohen



Meytal Duer



Igor Korover



Adi Ashkenazy

- ODU (Larry Weinstein):



Mariana Khachatryan



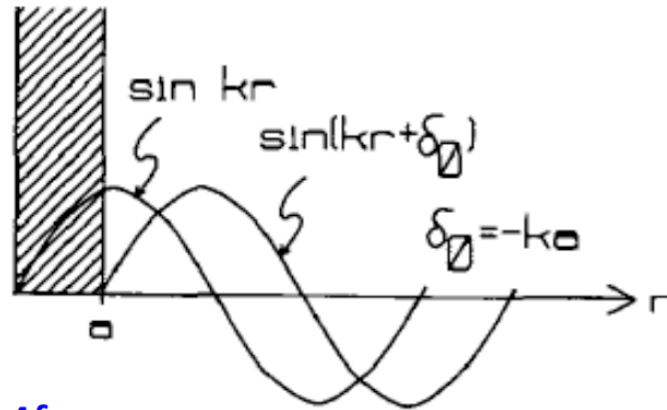
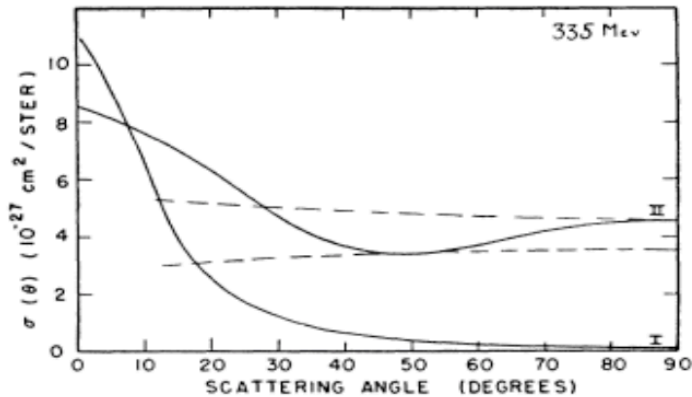
Florian Hauenstein

- Theory Collaborators (lots!)

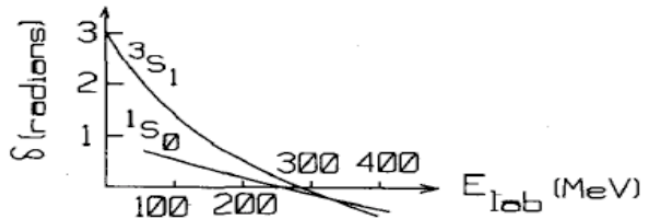
Repulsive Core

- Nuclear Forces at Short Distances: **NN repulsive core**

Jastrow 1951 assumed the existence of the hard core to explain the angular distribution of pp cross section at 340 MeV ($r_0=0.6\text{fm}$)

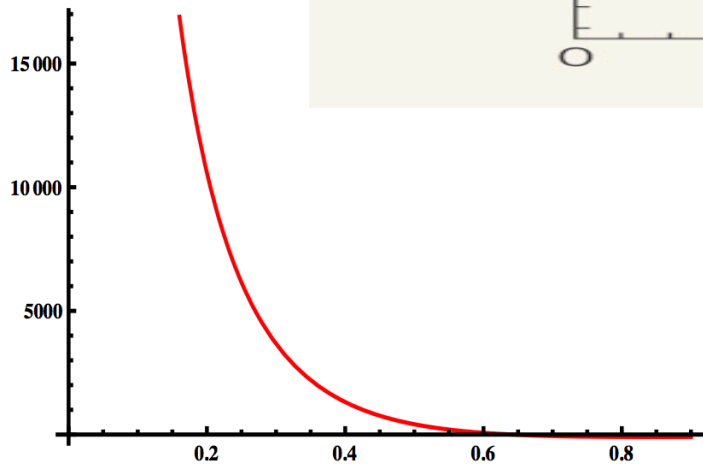
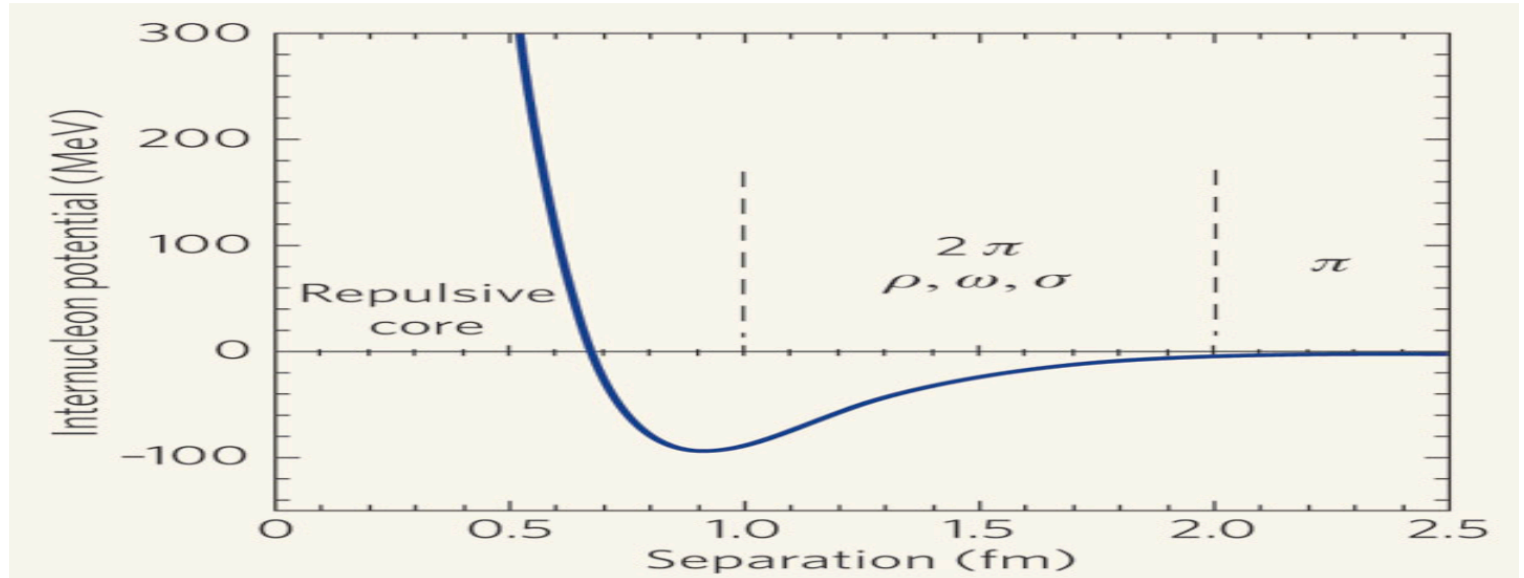


$r_0 = 0.4\text{fm}$

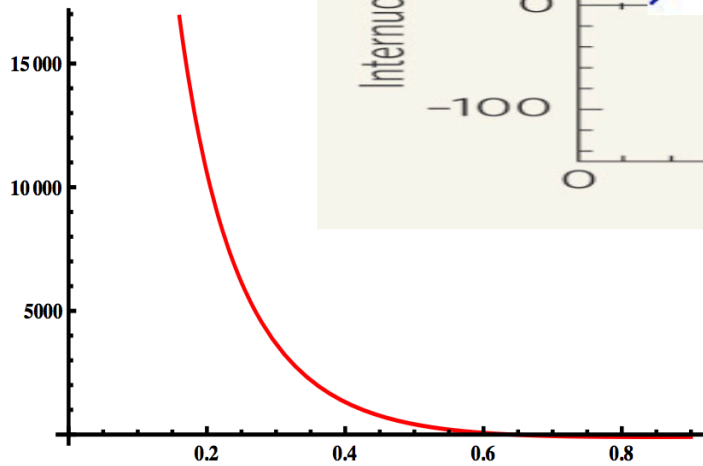
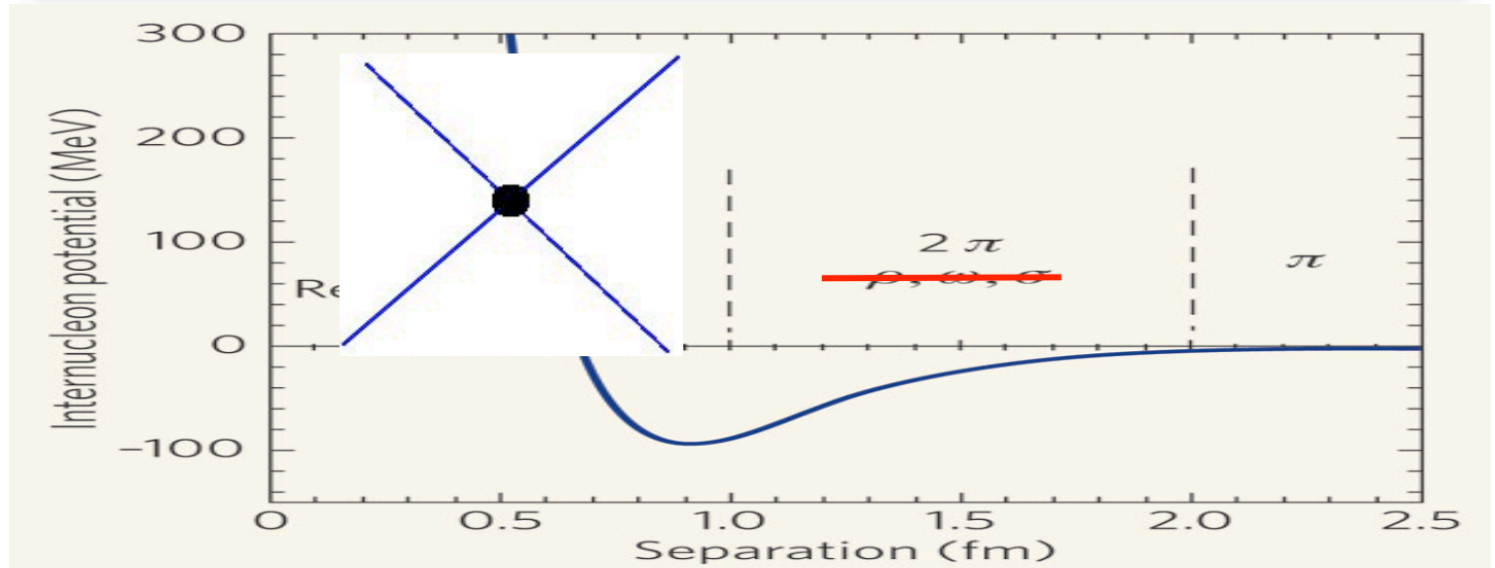
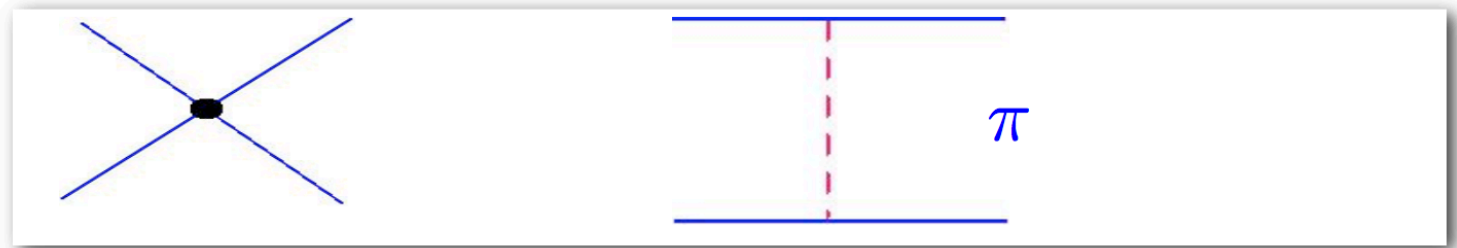


Stability Theorem: Nuclei will Collapse without Repulsive interaction 1950s Weisskopf, Blatt

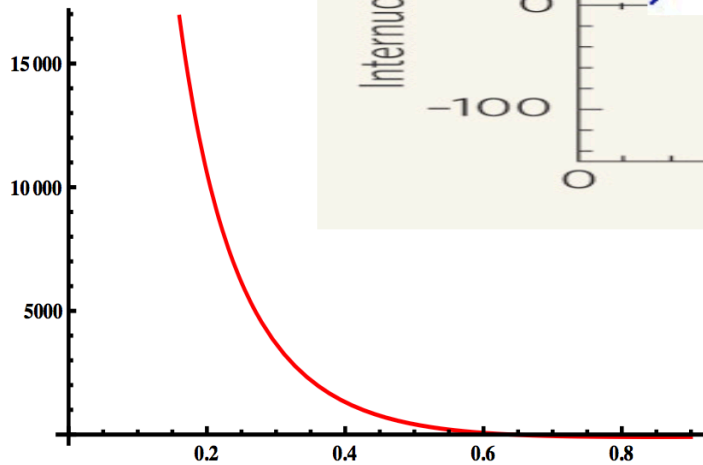
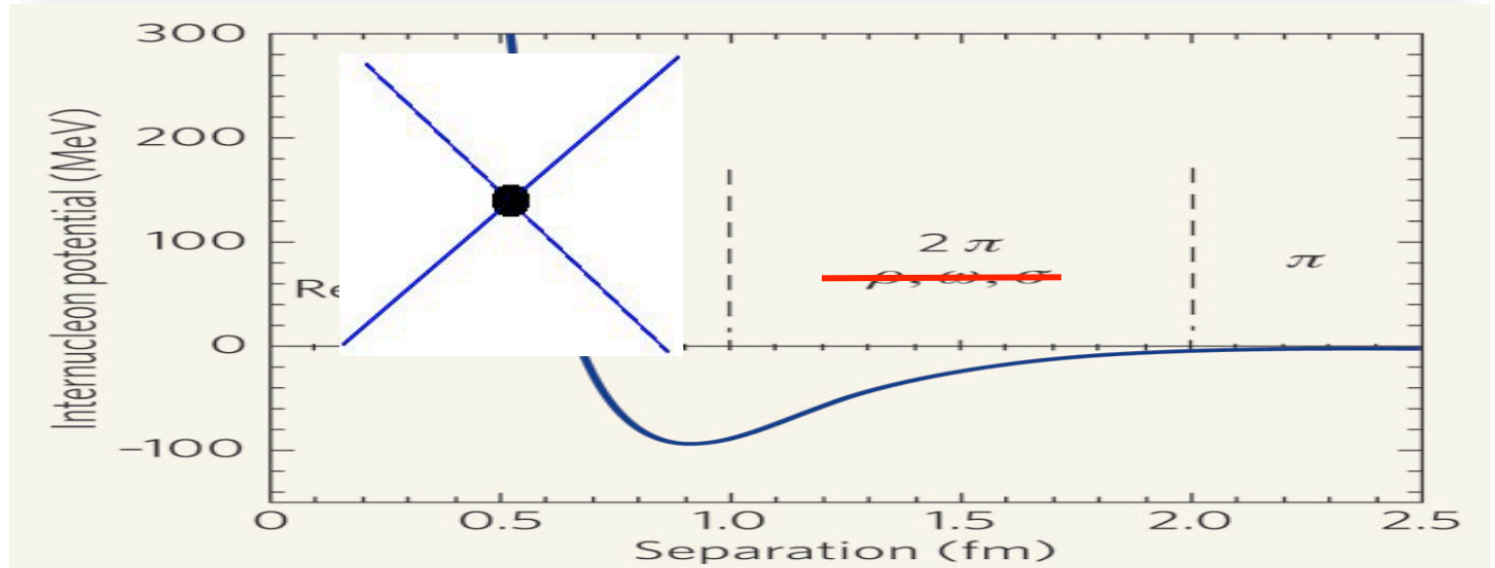
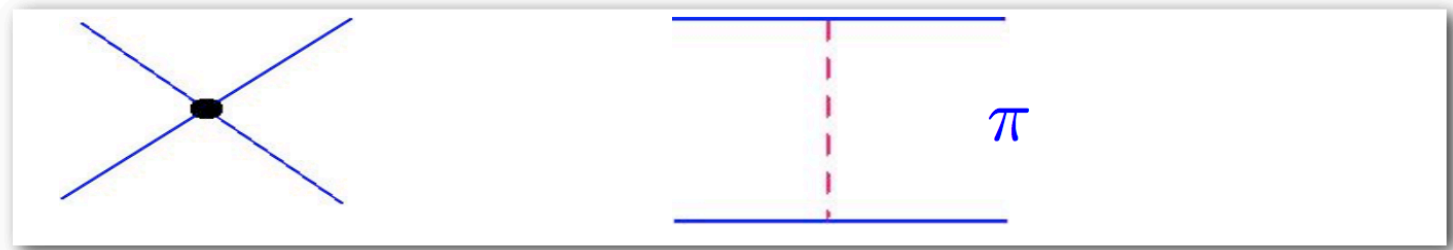
Repulsive Core



Repulsive Core



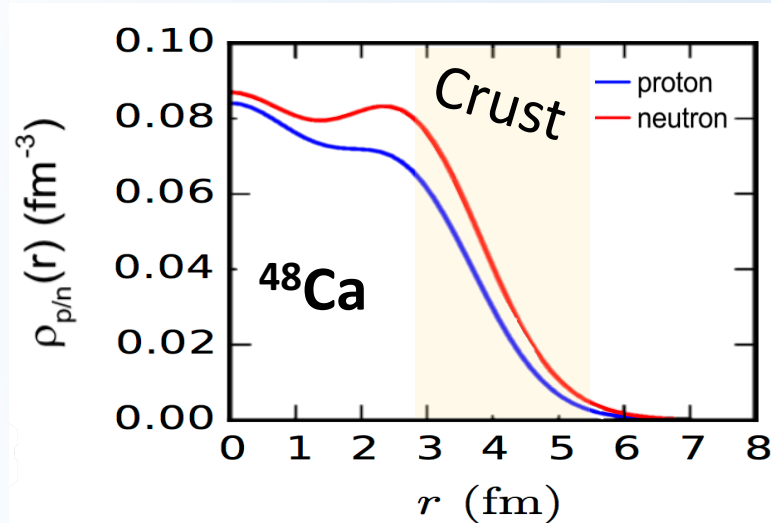
Repulsive Core



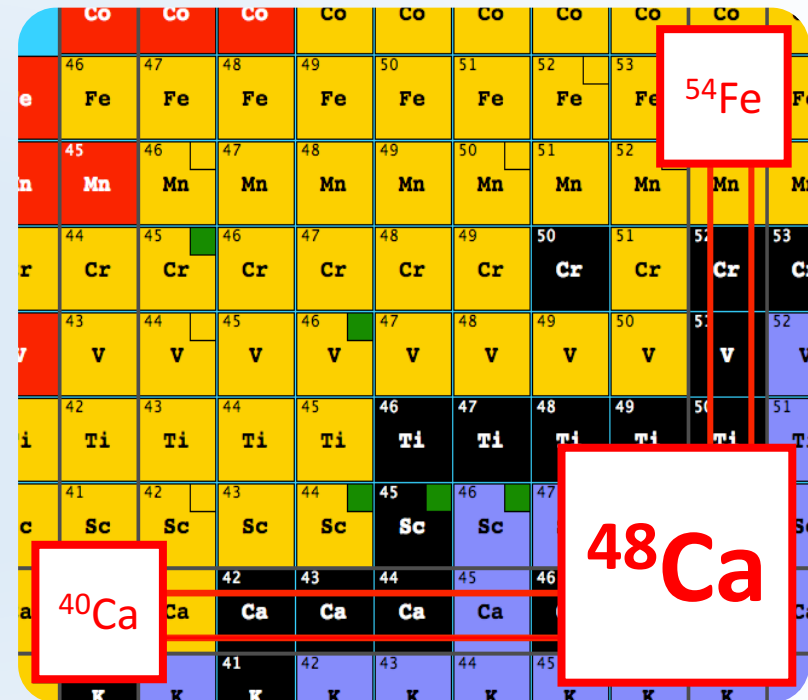
“Repulsive core has to be large to support neutron stars > 1 solar mass”

Protons Dynamics in Neutron Rich Nuclei

Focused Study of SRC dynamics in ^{48}Ca by comparing to the CaFe triplet.



G. Hagen et al., Nature Physics 12, 186 (2016)



+ 6 Protons

- 8 Neutrons

3N-SRC (Terra Incognita!)

