

# $\Lambda$ -p femtoscopy

Author:

**Oliver Arnold**

(oliver.arnold(at)mytum.de)

Speaker:

**Dimitar Mihaylov**



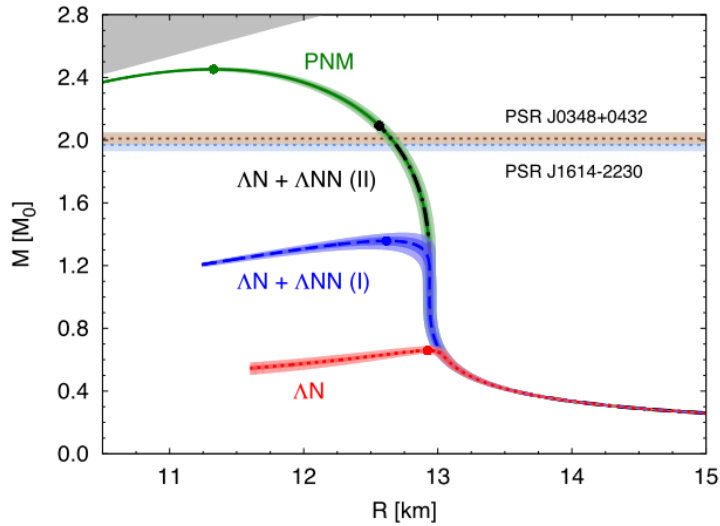
Technische Universität München

GSI, February 2017

- **Two particle correlations: Definition**
- **Proton-proton correlations**
  - ➔ Corrections and results from comparison with models
- **Lambda-proton correlations**
  - ➔ Use of proton-proton results to investigate the interaction of  $\Lambda p$  pairs
- **Summary and outlook**

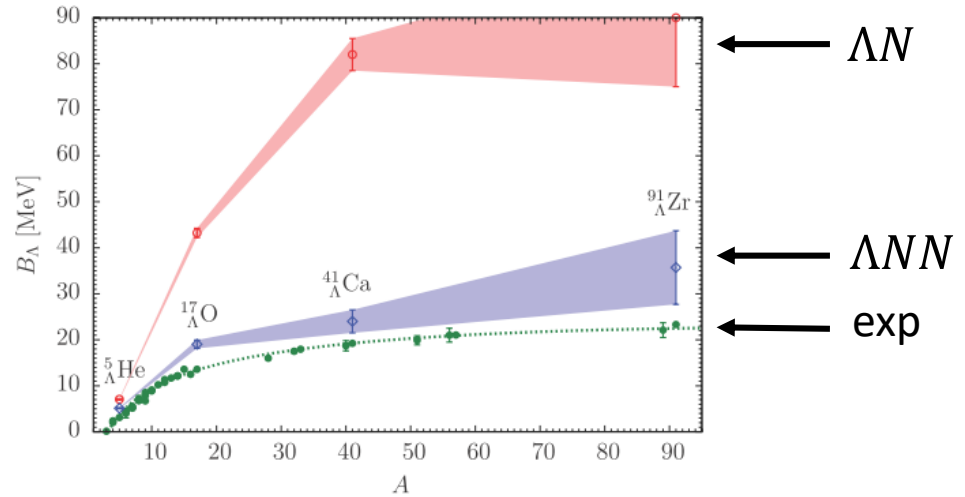
Detailed information needed to describe various systems:

## Neutron stars



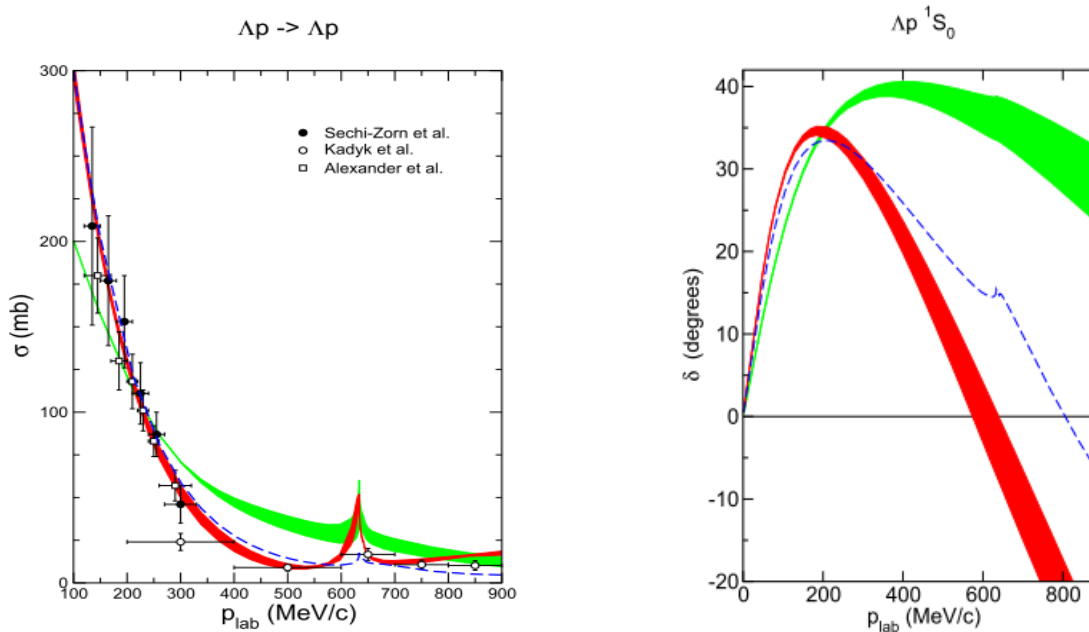
Lonardoni et al., Phys. Rev. Lett. 114, 092301

## Hypernuclei



Lonardoni et al., Phys.Rev. C87 (2013) 041303

Experimental data is quite scarce



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Theoretical correlation function:

$$C^{ab}(\mathbf{P}, \mathbf{q}) = \frac{\mathcal{P}(\vec{p}_a, \vec{p}_b)}{\mathcal{P}(\vec{p}_a)\mathcal{P}(\vec{p}_b)} = \int d^3r' S_{\mathbf{P}}(\mathbf{r}') |\phi(\mathbf{q}, \mathbf{r}')|^2$$

**Source function:**

Distribution of relative distance between the particle pairs (in CMS)

**Wave function of particle pair:**

Includes the interactions

Experimental correlation function:

$$C(k) = \frac{A(k)}{B(k)}$$

$$k = \frac{1}{2} |\mathbf{p}_1 - \mathbf{p}_2|$$

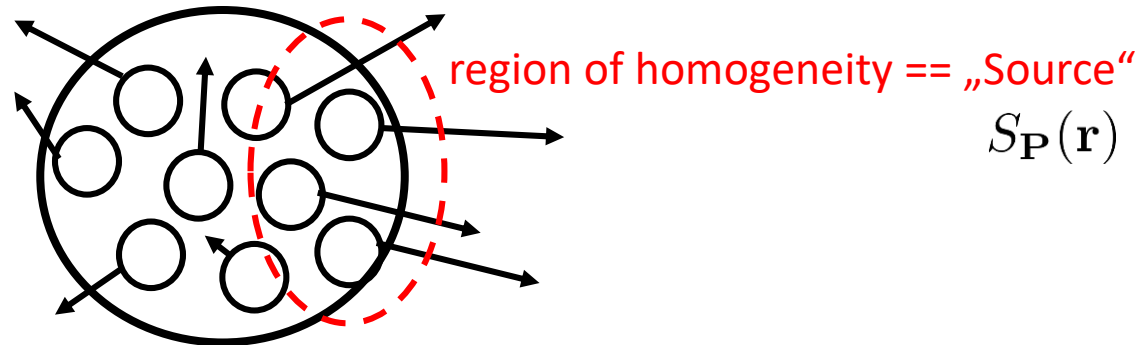
$$\mathbf{p}_1 + \mathbf{p}_2 = 0 \quad \text{Pair reference frame (PRF)}$$

- **Same:** relative momentum dist. of particles in the same event
- **Mixed:** particles from different events (not correlated)
- **Normalized to unity:**  $C(k > 100 \text{ MeV}/c) \equiv 1$

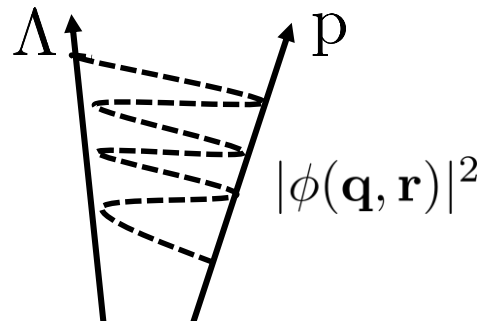
Strategy of analysis – two steps:

$$C^{ab}(\mathbf{P}, \mathbf{q}) = \frac{\mathcal{P}(\vec{p}_a, \vec{p}_b)}{\mathcal{P}(\vec{p}_a)\mathcal{P}(\vec{p}_b)} = \int d^3r' \underbrace{S_{\mathbf{P}}(\mathbf{r}')}_1 \underbrace{|\phi(\mathbf{q}, \mathbf{r}')|^2}_2$$

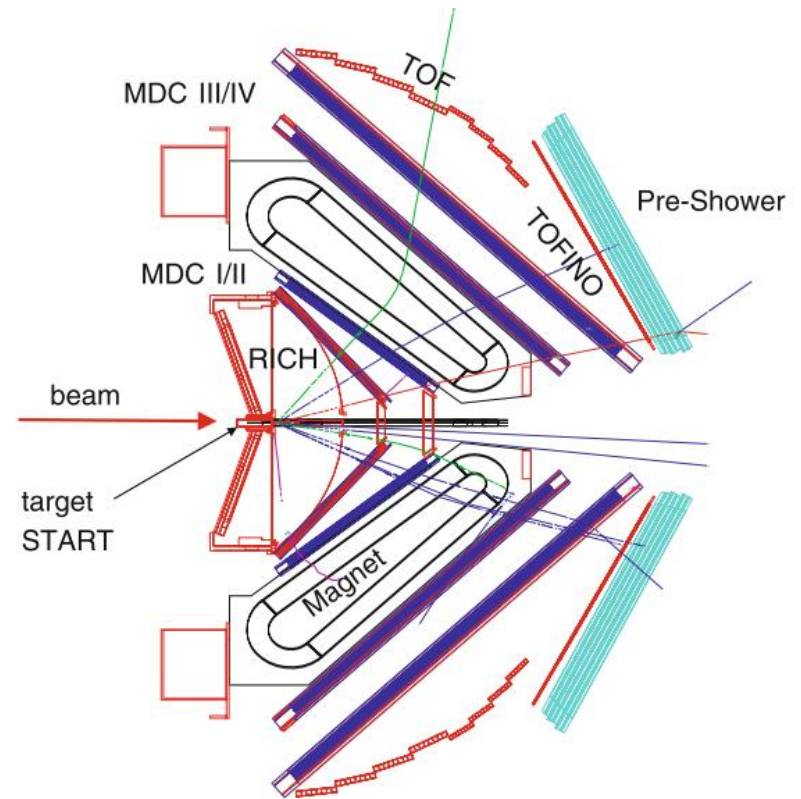
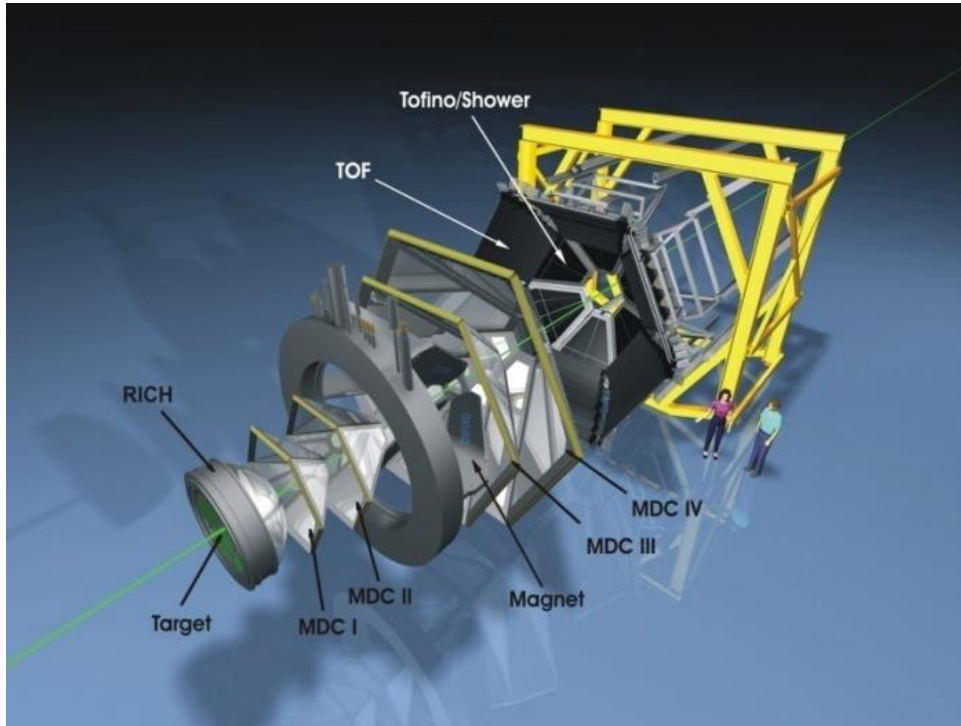
1. Understand the emission profile of the pNb system



2. Use the information of point 1 to investigate particle interactions which are not well known



## High Acceptance Di-Electron Spectrometer - HADES:

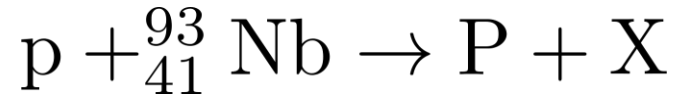


### Features of HADES:

- Large geometric acceptance  $\phi \in [0, 2\pi], \Theta \in [15^\circ, 85^\circ]$
- Momentum resolution  $\sim 2 - 6\%$


# Reaction

System under investigation:



$$P = pp, \pi^{\pm}\pi^{\pm}, \dots$$

**Beam:**

p  


$$\sim 2 \cdot 10^6 / \text{s}$$

$$T_p = 3.5 \text{ GeV}$$

$$\sqrt{s_{NN}} = 3.18 \text{ GeV}$$

**Target:**

12-fold segmented target of  ${}^{93}\text{Nb}$  discs  
 2.8% interaction probability  
 $\langle A_{part} \rangle \sim 2.7$

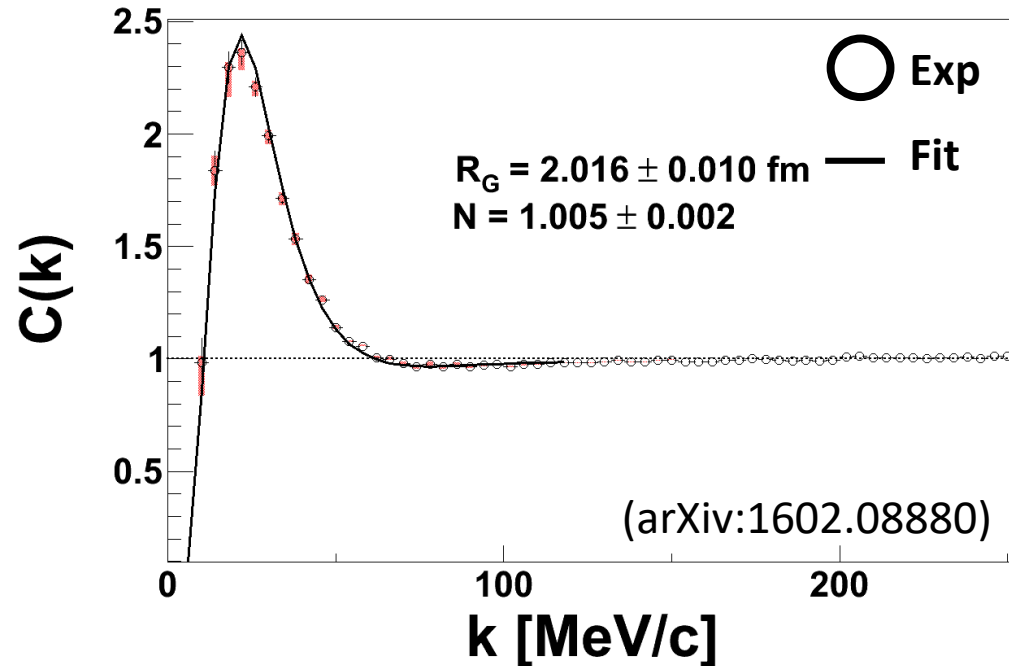
Femtoscscopy in a small system!



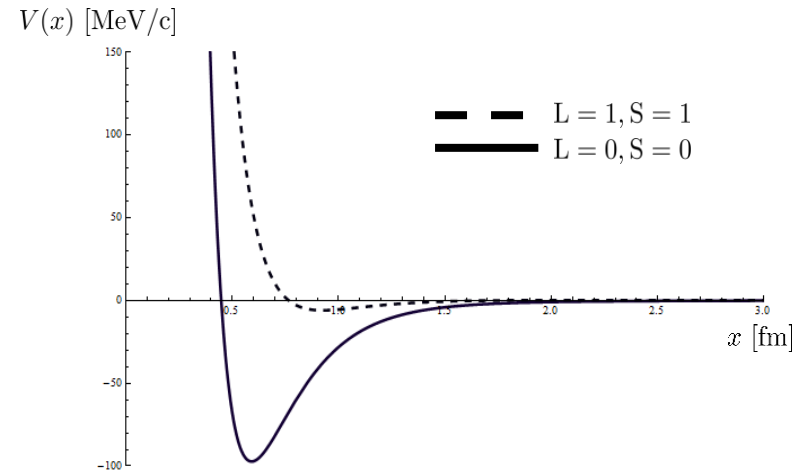
# Source Size (pp)

Information about the source: proton-proton correlation function:

Extract source size:  $C^{ab}(k) = N \int d^3r' S_{\mathbf{P}}(\mathbf{r}') |\phi(\mathbf{k}, \mathbf{r}')|^2$



Potential used for strong interaction:



B. D. Day, Phys. Rev. C 24, (1981), 1203

$$\frac{d^2 w}{d\rho^2} + \left[ 1 - \frac{2\eta}{\rho} - \frac{l(l+1)}{\rho^2} - \frac{2\mu}{k^2} V(\rho) \right] = 0 \quad S(r) \sim \exp(-r^2/4R_G^2)$$



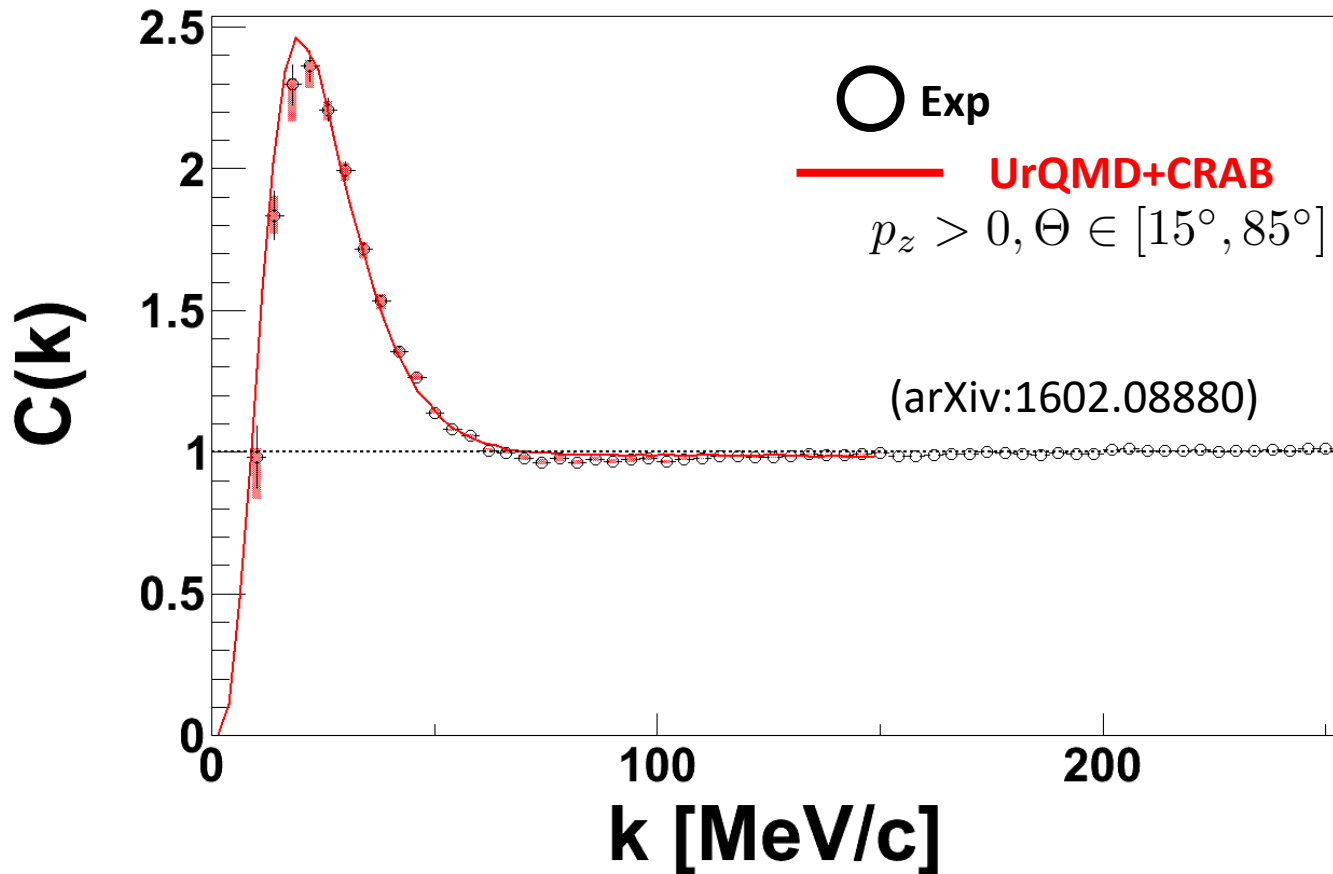
$$R_G = 2.016 \pm 0.010^{+0.109}_{-0.118} \text{ fm}$$

# Model Comparison (pp)

Source comparison to transport theory (same potential used as for the fit):

In one dimension:

Calculation of UrQMD correlation function with help of CRAB



UrQMD gives a good source description for protons

# Interaction ( $\Lambda p$ )

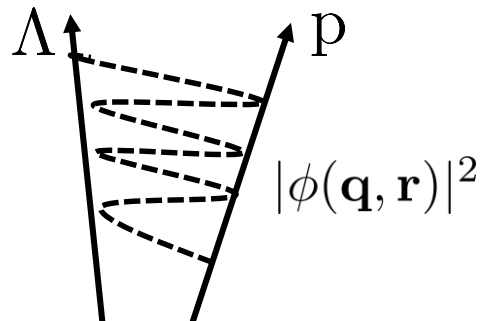
Strategy of analysis:

$$C^{ab}(\mathbf{P}, \mathbf{q}) = \frac{\mathcal{P}(\vec{p}_a, \vec{p}_b)}{\mathcal{P}(\vec{p}_a)\mathcal{P}(\vec{p}_b)} = \int d^3r' S_{\mathbf{P}}(\mathbf{r}') \underbrace{|\phi(\mathbf{q}, \mathbf{r}')|^2}_{2.}$$

1. Understand the emission profile of the pNb system

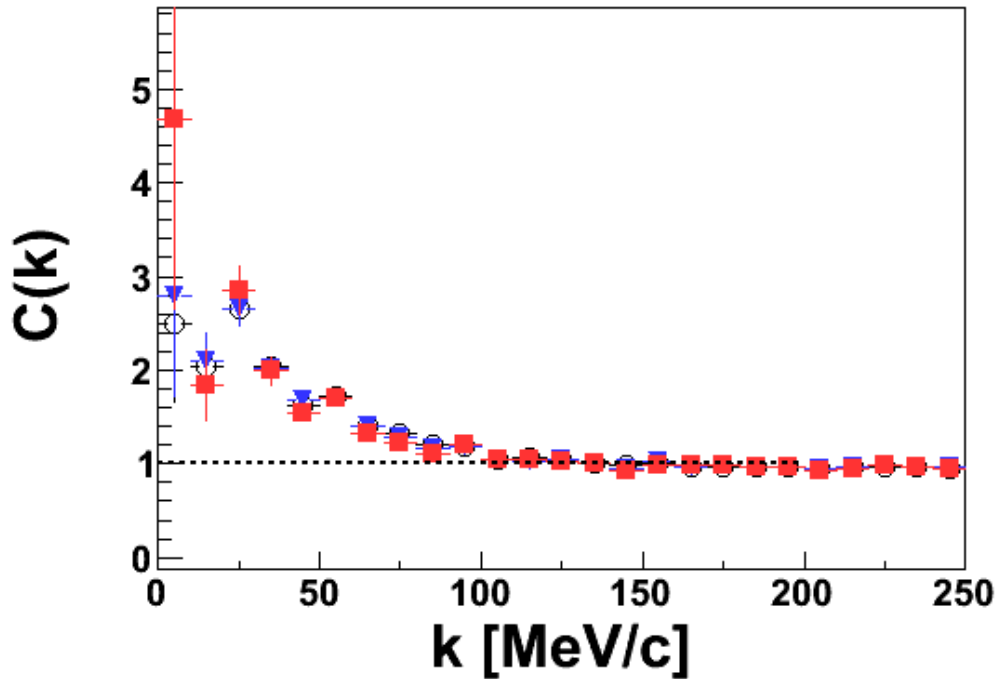


2. Use the information of point 1 to investigate particle interactions of not well known type



Apply corrections – investigate systematics:

Correlation function after application of all corrections



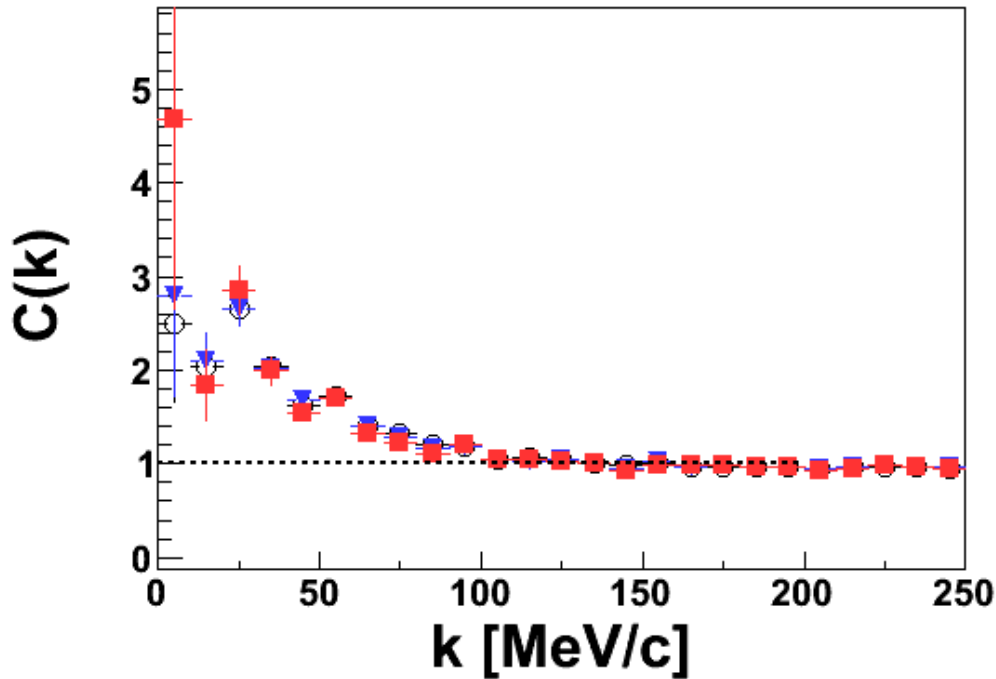
(arXiv:1602.08880)

Lednický's model:

$$C(k) = 1 + \sum_S \rho_S \left[ \frac{1}{2} \left| \frac{f^S(k)}{R_G^{\Lambda p}} \right|^2 \left( 1 - \frac{d_0^S}{2\sqrt{\pi} R_G^{\Lambda p}} \right) + 2 \frac{\mathcal{R}f^S(k)}{\sqrt{\pi} R_G^{\Lambda p}} F_1(Q R_G^{\Lambda p}) - \frac{\mathcal{I}f^S(k)}{R_G^{\Lambda p}} F_2(Q R_G^{\Lambda p}) \right]$$

Apply corrections – investigate systematics:

Correlation function after application of all corrections



(arXiv:1602.08880)

Lednický's model:

$$C(k) = 1 + \sum_S \rho_S \left[ \frac{1}{2} \left| \frac{f^S(k)}{(R_G^{\Lambda p})} \right|^2 \left( 1 - \frac{d_0^S}{2\sqrt{k} (R_G^{\Lambda p})} \right) + 2 \frac{\mathcal{R}f^S(k)}{\sqrt{k} (R_G^{\Lambda p})} F_1(Q \overline{R_G^{\Lambda p}}) - \frac{\mathcal{I}f^S(k)}{(R_G^{\Lambda p})} F_2(Q \overline{R_G^{\Lambda p}}) \right]$$

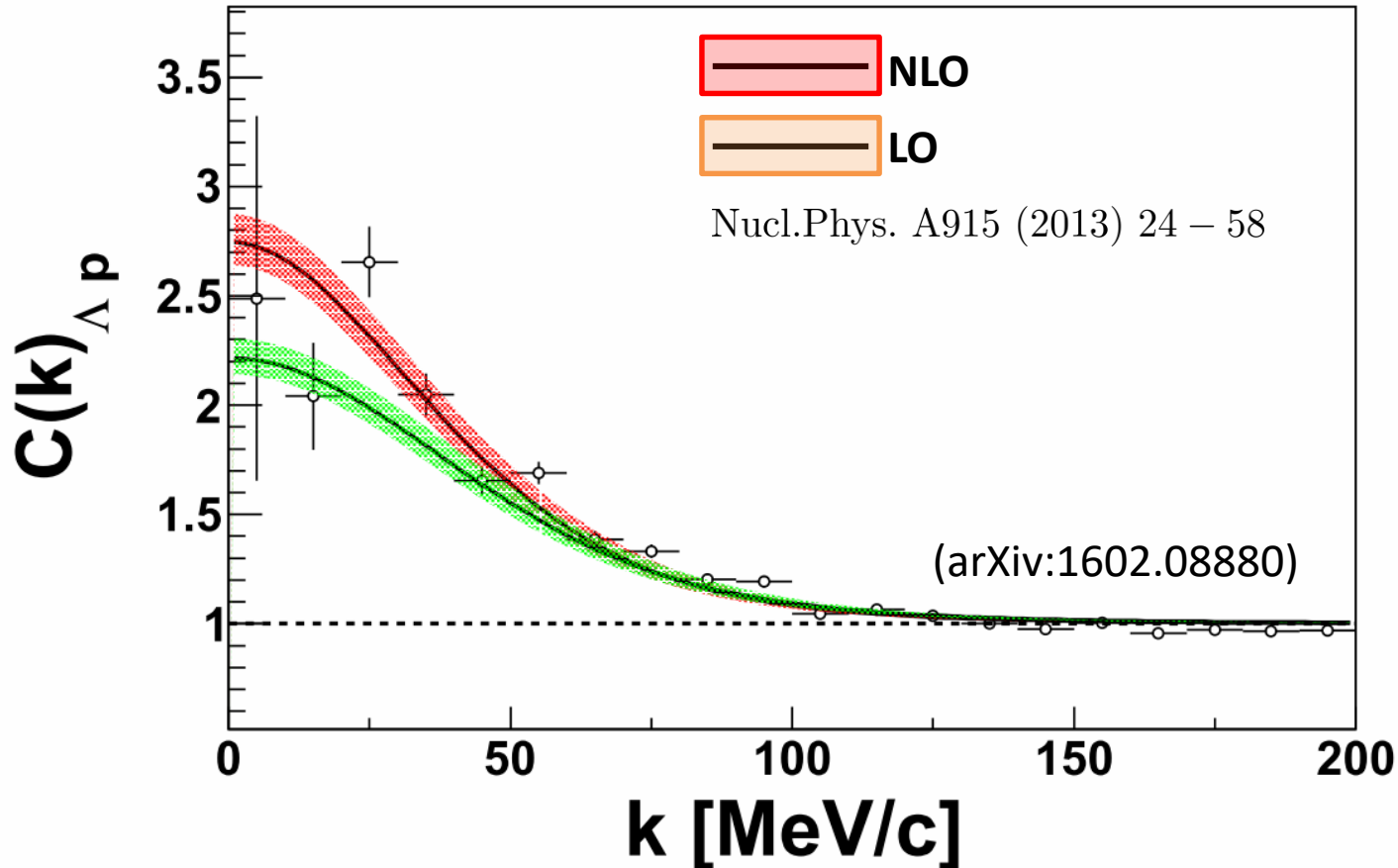
# Interaction ( $\Lambda p$ )

Comparison to models:

$$RF = \frac{R_{inv}^{pp}}{R_{inv}^{\Lambda p}} = 1.184$$

$$R_G = 2.016 \pm 0.010^{+0.109}_{-0.118} \text{ fm}$$

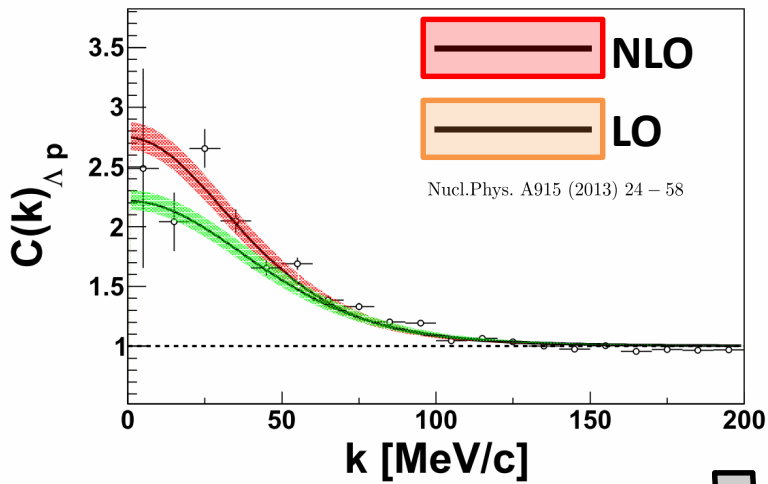
$$R_G^{\Lambda p} = R_G^{pp} / RF$$



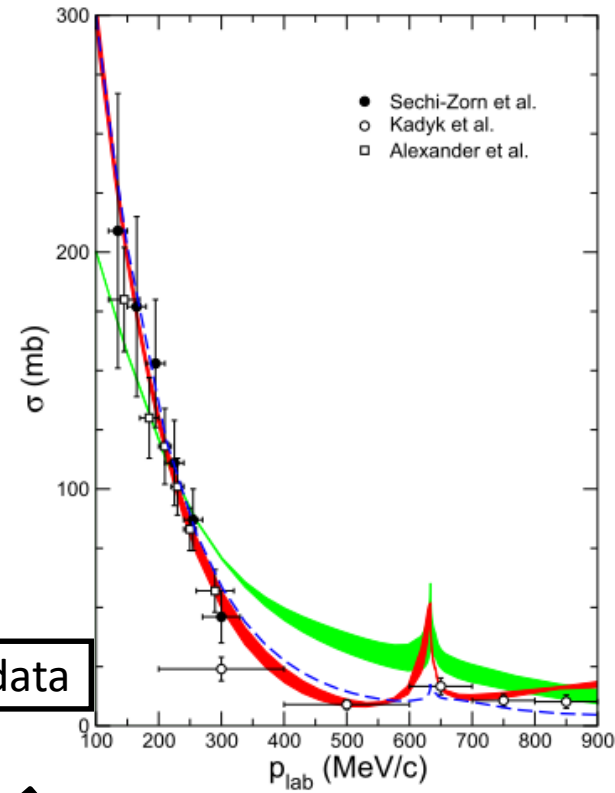
# Interaction ( $\Lambda p$ )

Comparison to models:

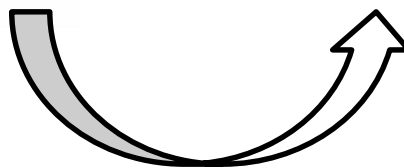
$\Lambda p \rightarrow \Lambda p$



no data



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„Closing the gap“

- Source size of emission region in pNb system determined with pp-pairs
- Knowing the source size allows to study final state interactions of not well known type

 „Closing the gap“: No scattering data at very low relative momenta

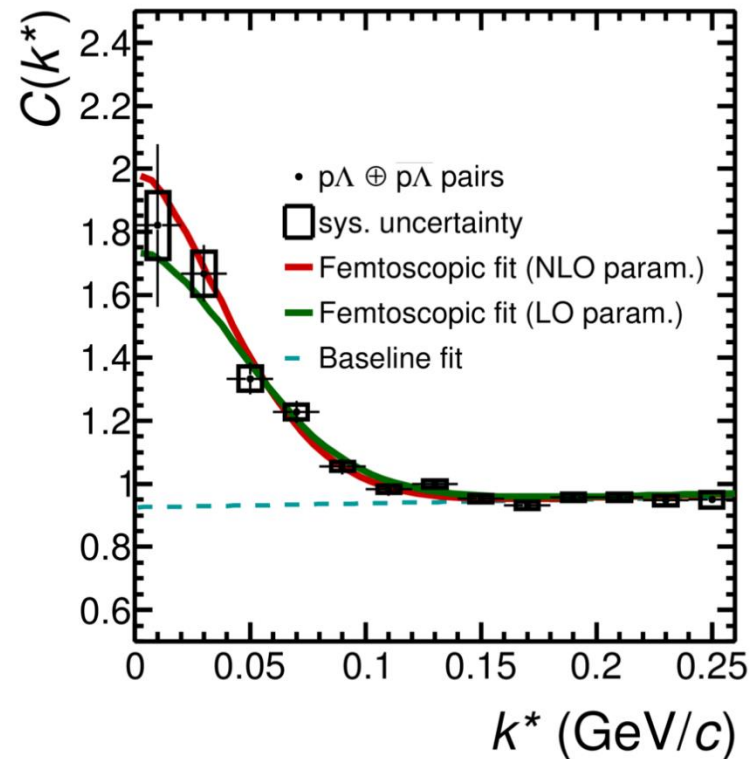
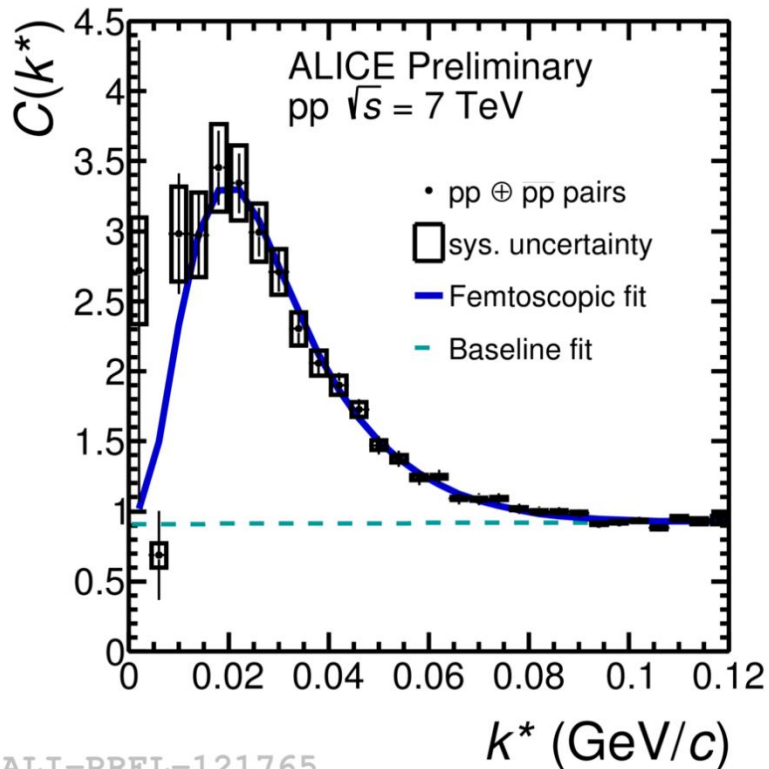
*Article for detailed information:*

**J. Adamczewski-Musch *et al.* (HADES Collaboration)  
Phys. Rev. C 94, 025201**



# Outlook

- Apply the same technique to **ALICE** data.  
Currently investigating the **pp 7 TeV** data (*Oliver Arnold*).



- Currently developing a *Correlation Analysis Tool using the Schrödinger equation* (CATS).  
(*Dimitar Mihaylov*)
- Attempt to perform multi-particle femtoscopy.  
(*Ante Bilandzic*)

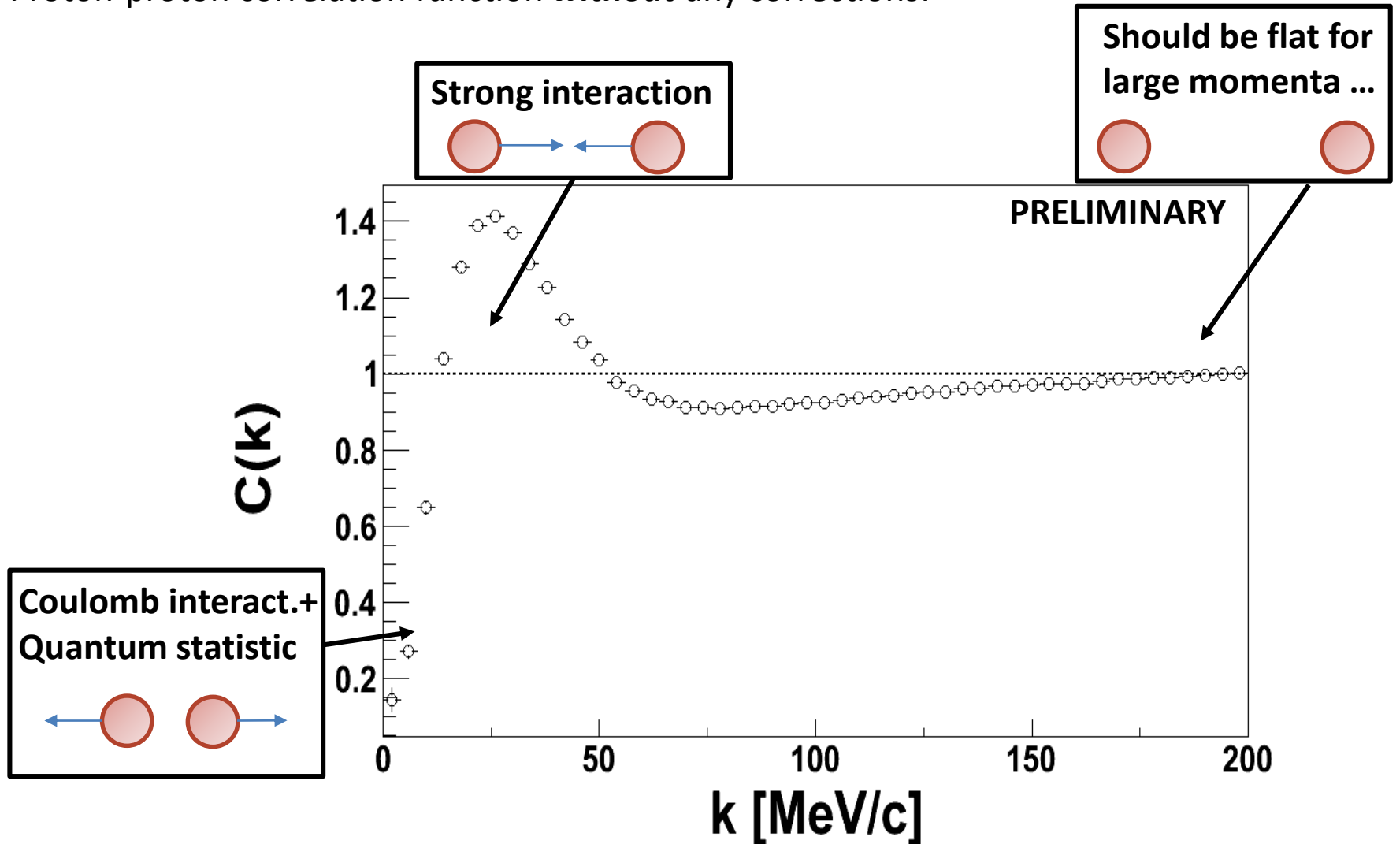
*Thank You For  
Your Attention*



Munich, Germany

# Correlation Function (pp)


Information about the source: proton-proton correlation function:  
 Proton-proton correlation function *without* any corrections:



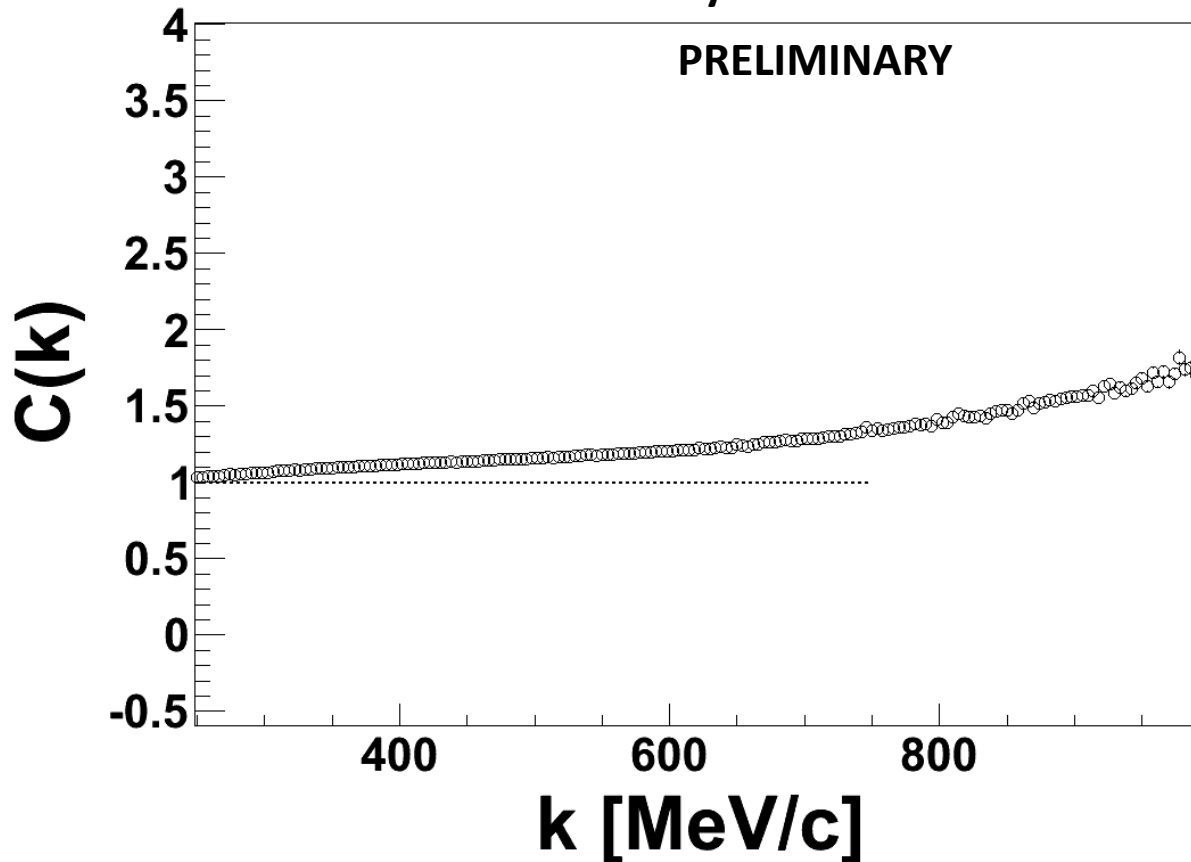
# Correlation Function (pp)

Information about the source: proton-proton correlation function:  
 Proton-proton correlation function *without* any corrections:

Should be flat for large momenta ...



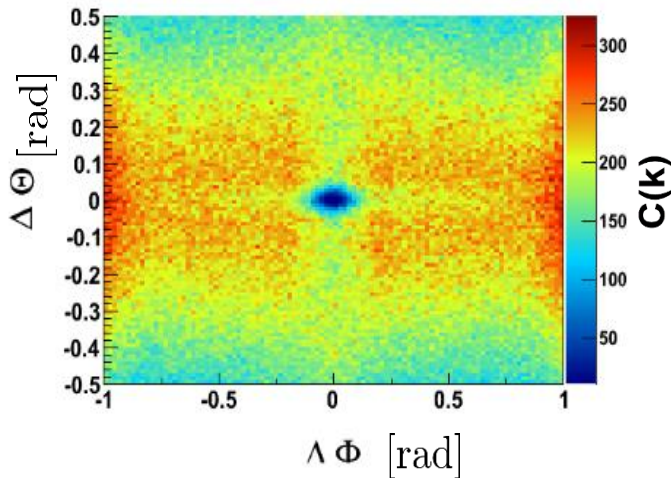
... unfortunately *not* the case



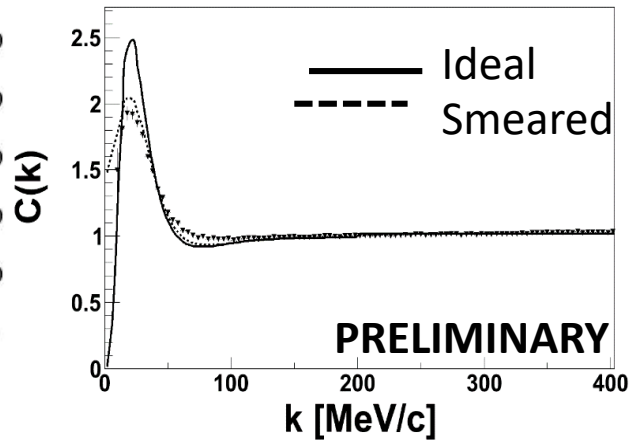
Information about the source: proton-proton correlation function:

## Corrections

Reject pairs which are too close together

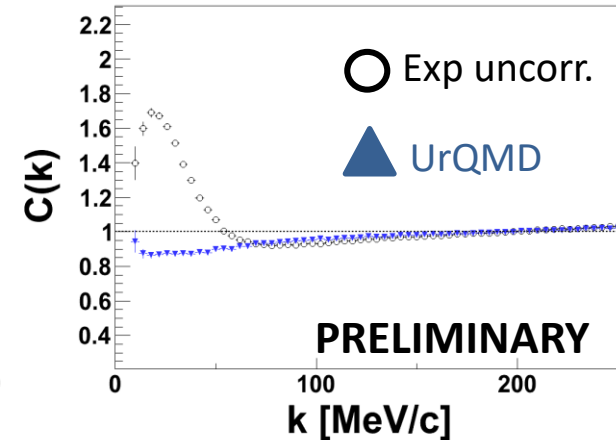


Correct for finite momentum resolution



$$\frac{C_{\text{real}}(k)}{C_{\text{measured}}(k)} = \frac{C_{\text{ideal}}(k)}{C_{\text{smeared}}(k)}$$

Correct for long range correlations



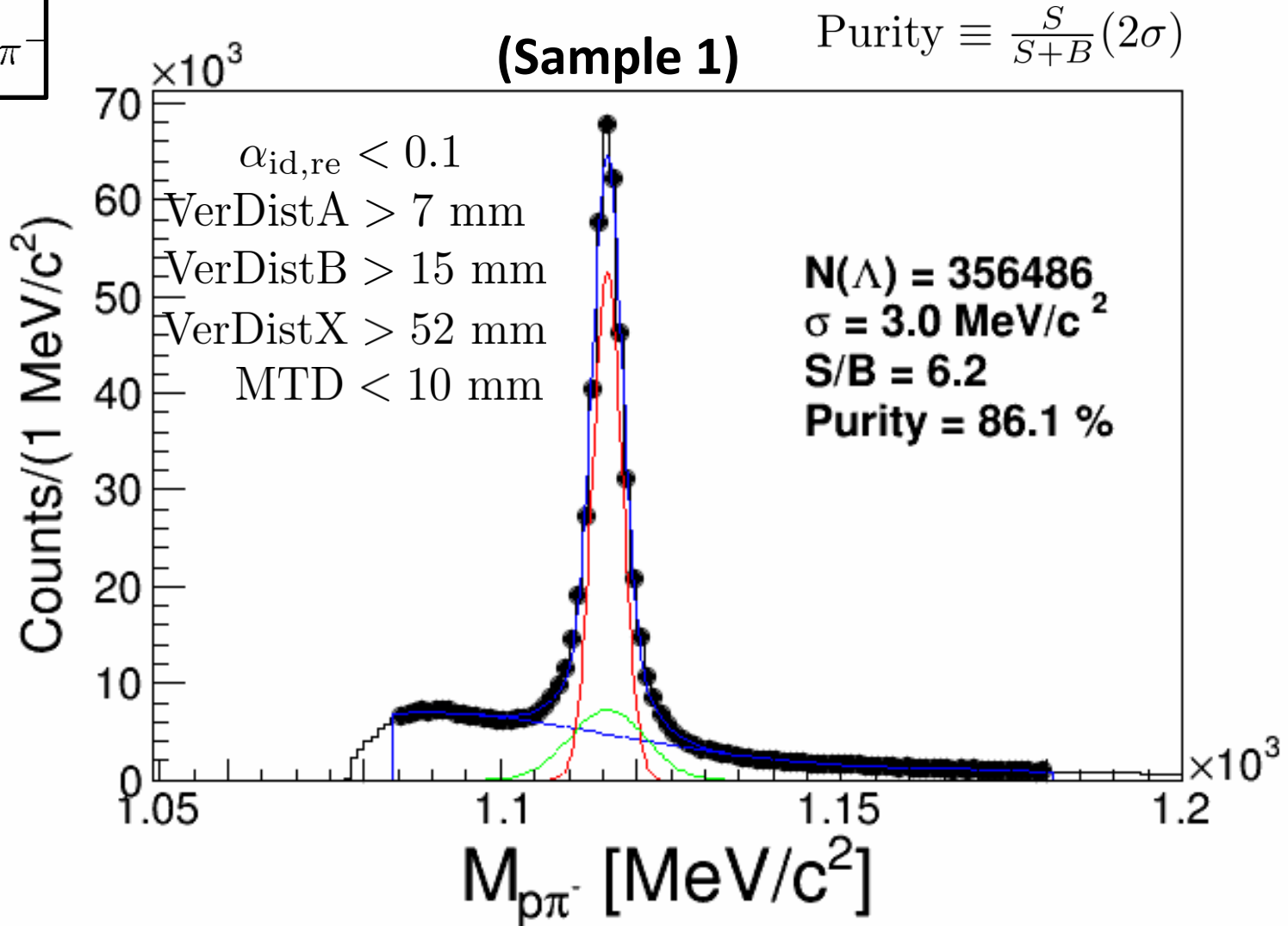
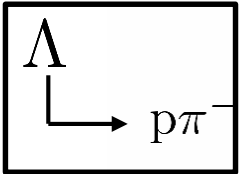
$$C(k) \equiv C_{\text{raw}}(k) / C_{\text{UrQMD}}(k)$$

$$|\Delta\phi| > 3 \times 0.039 \text{ rad}$$

$$|\Delta\Theta| > 3 \times 0.015 \text{ rad}$$

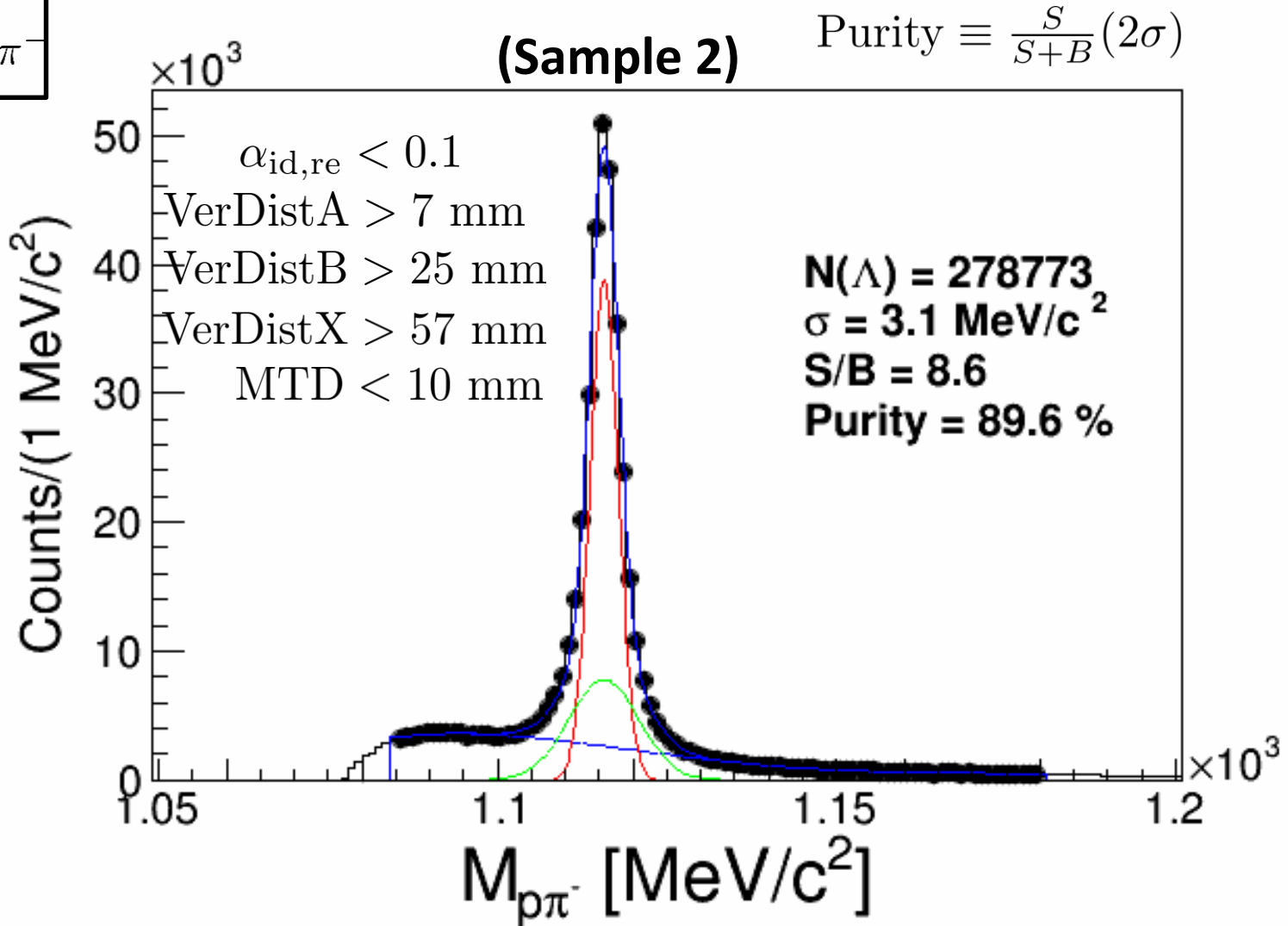
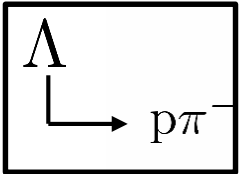
# Interaction ( $\Lambda p$ )

Select  $\Lambda'_s$  with large purity – different cut combinations to investigate systematics:



# Interaction ( $\Lambda p$ )

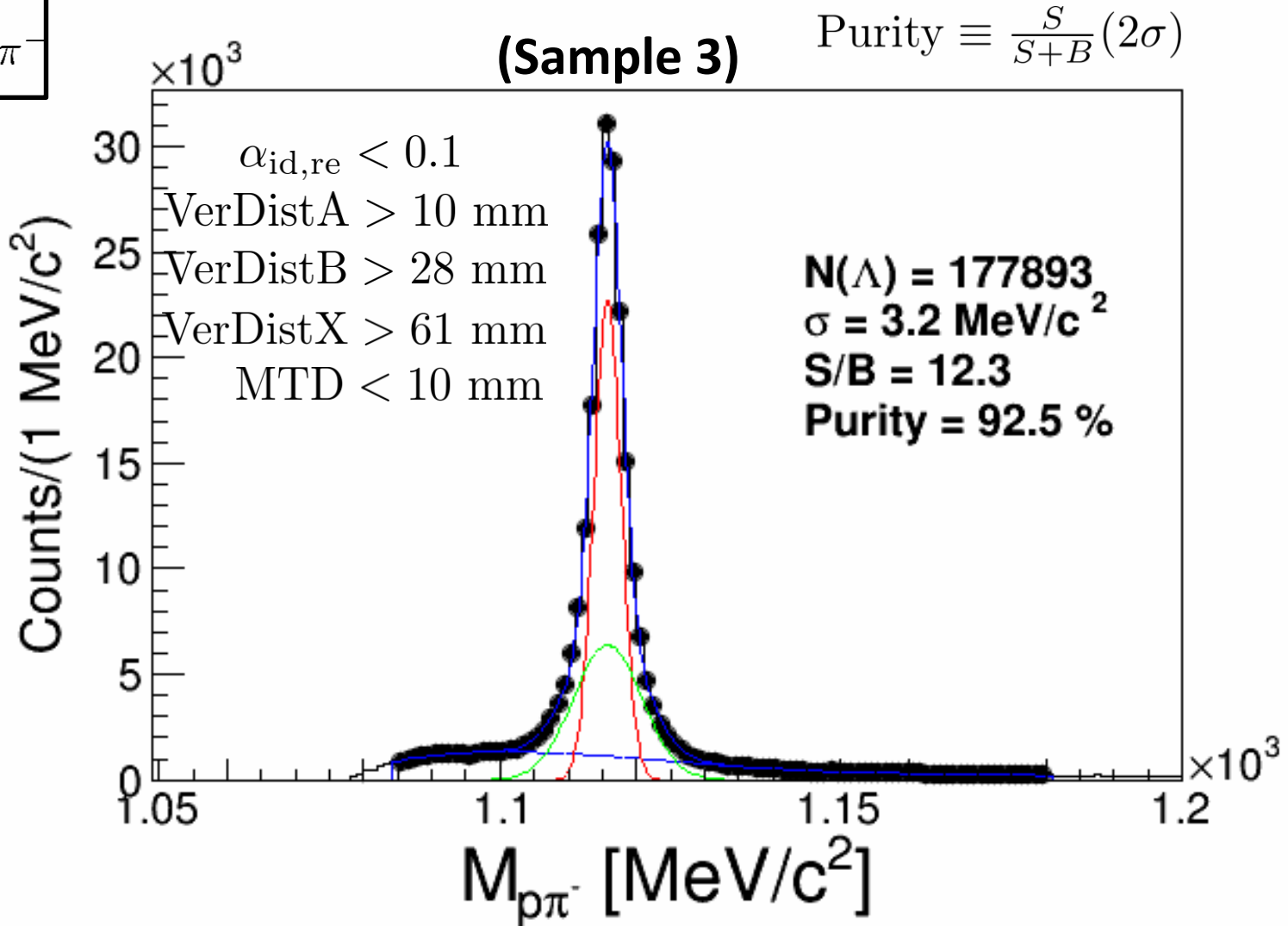
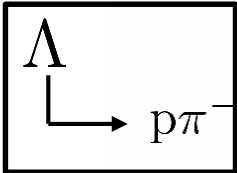
Select  $\Lambda'_s$  with large purity – different cut combinations to investigate systematics:





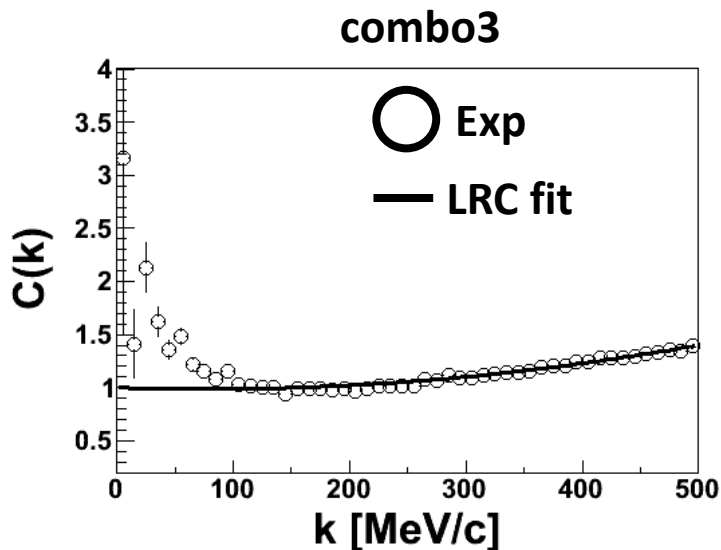
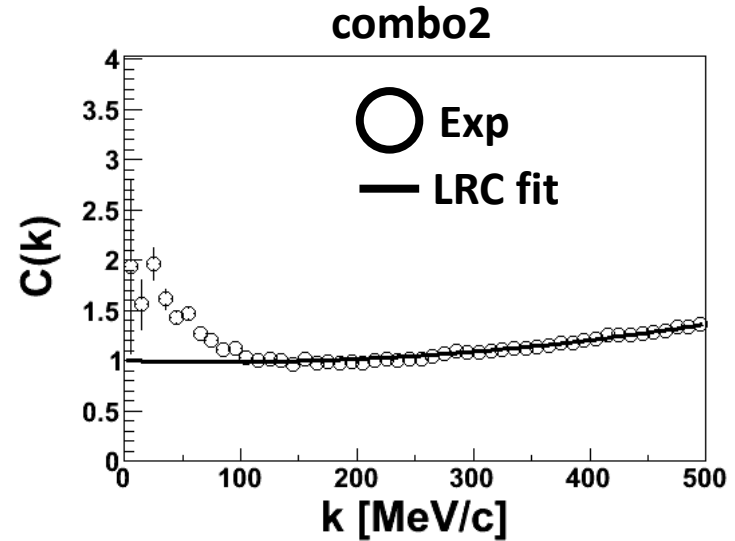
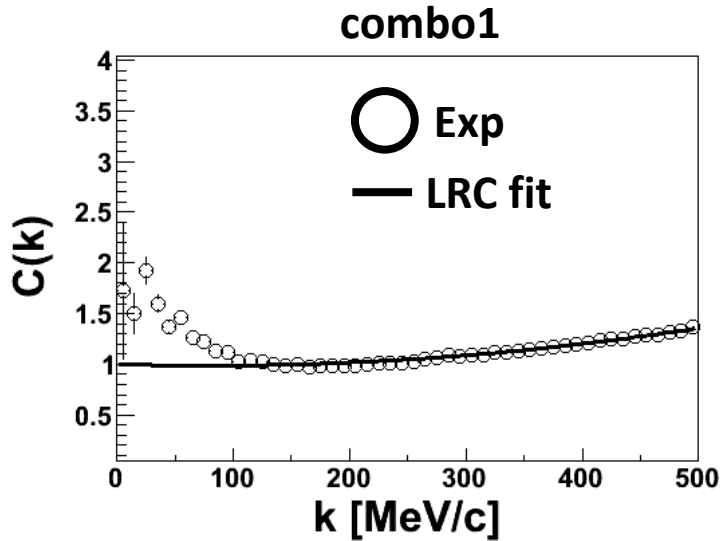
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Select  $\Lambda'_s$  with large purity – different cut combinations to investigate systematics:



# Interaction ( $\Lambda p$ )

Again corrections: Influence of long range correlations for all three cut combinations:

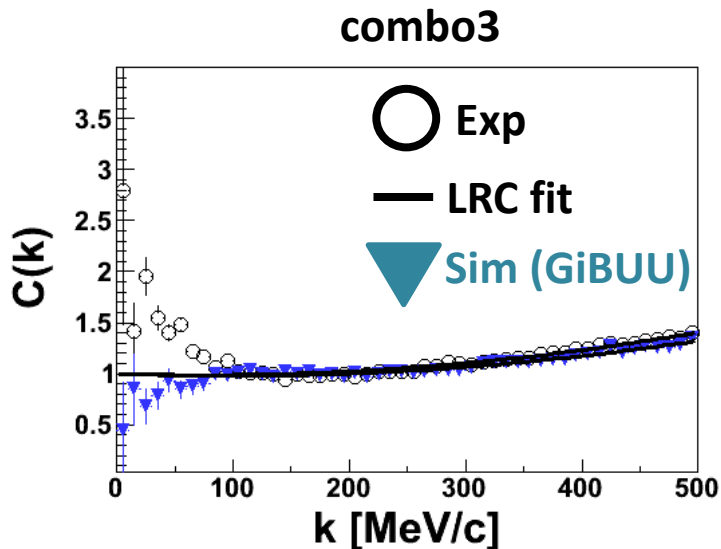
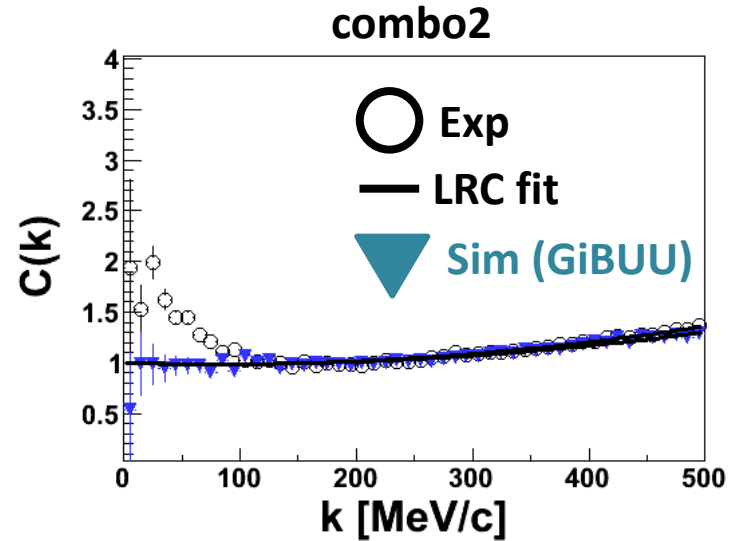
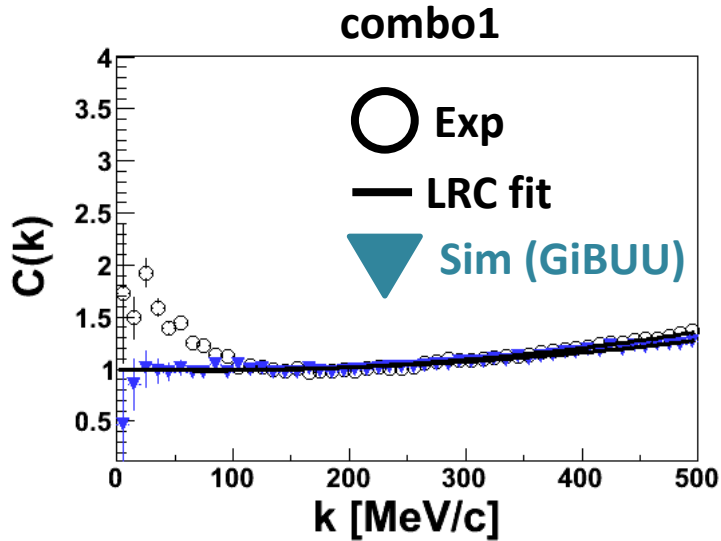


Model the long-range part with a polynomial

$$C_{\text{LRC}} = 1 + ak + bk^2 \quad k \in [250, 600] \text{ MeV/c}$$

# Interaction ( $\Lambda p$ )

Again corrections: Influence of long range correlations for all three cut combinations:



Model the long-range part with a polynomial

$$C_{\text{LRC}} = 1 + ak + bk^2 \quad k \in [250, 600] \text{ MeV/c}$$

Simulation confirms trend of the fit from the long-range part also at small relative momenta

# Interaction ( $\Lambda p$ )

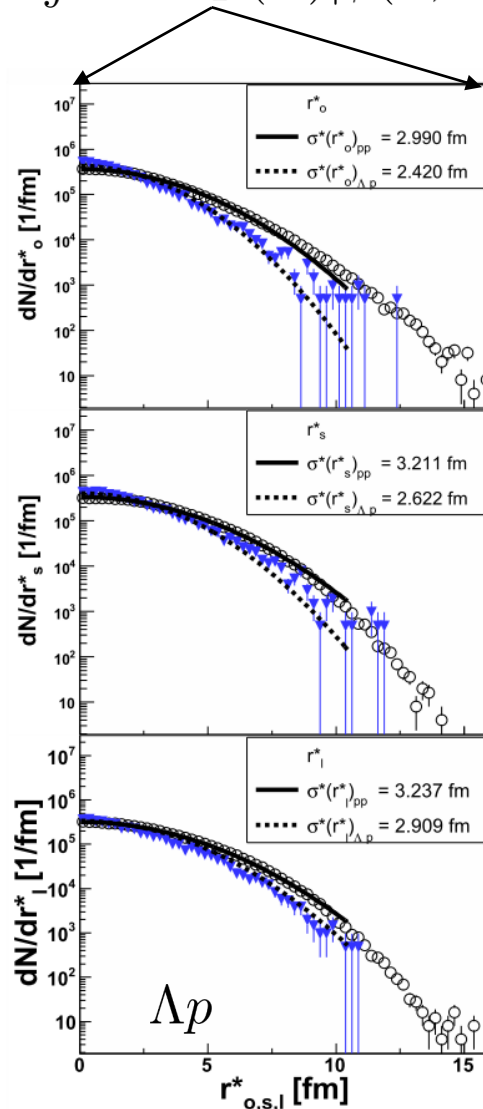
Source extraction from transport theory (UrQMD) - LCMS:

$$C^{ab}(k) = \int d^3r' S_P(\mathbf{r}') |\phi(\mathbf{k}, \mathbf{r}')|^2 \quad k < 30 \text{ MeV}/c$$

$\Lambda p$   
 $pp$

$$R_{\text{inv}} = \sqrt{\frac{R_{\text{out}}^{*2} + R_{\text{side}}^{*2} + R_{\text{long}}^{*2}}{3}}$$

$$\text{RF} = \frac{R_{\text{inv}}^{pp}}{R_{\text{inv}}^{\Lambda p}} = 1.184$$



Fit function used:

$$\sim \exp(-r^2/2\sigma^2)$$