

Charge-changing and total interaction cross section measurements

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Nuclear Size and Interaction Cross Sections

Reaction Cross Section

Interaction Cross Section

$$\sigma_{\text{tot}} = \sigma_{\text{R}} + \sigma_{\text{el}}$$

$$\sigma_{\text{I}} = \sigma_{\text{R}} - \sigma_{\text{inel}}$$

σ_{I} σ_{R}



Nuclear Size

Glauber Calculation

$$\sigma_{\text{R}} = \int db \left[1 - \exp \left(- \int d^2r \sum_{i,j} \sigma_{\text{NN}}(E) \rho_i(r) \rho_j(r) \right) \right]$$

σ_{R} can be uniquely calculated by 3 quantities

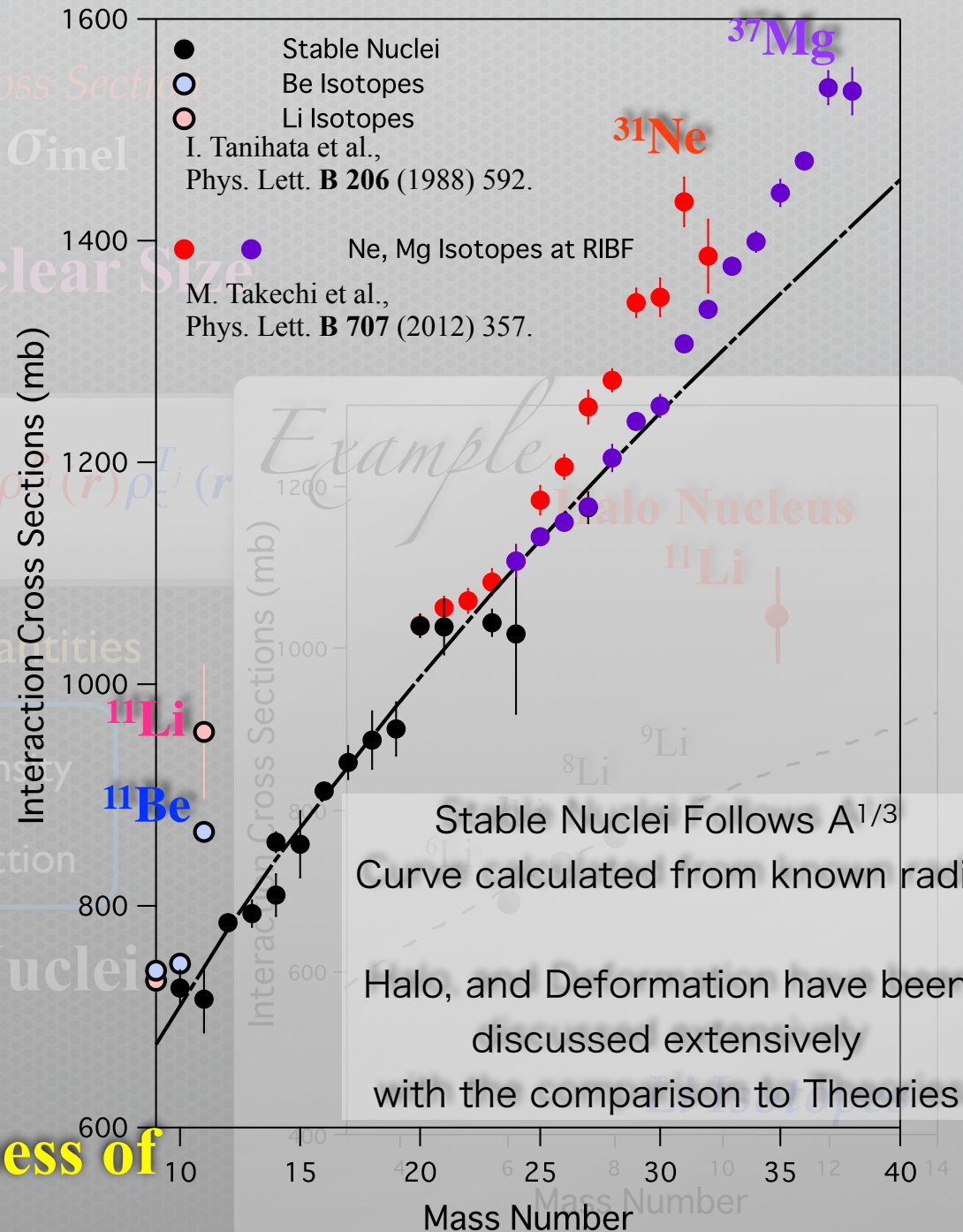
ρ^{P} Projectile Density

ρ^{T} Target Density

σ_{NN} Nucleon- Nucleon Total Cross Section

Nuclear Size of unknown Nuclei
→ Halo features

Next : Neutron Skin Thickness of Nuclei $A > 40$



Neutron Skin and Nuclear Matter EOS

K. Oyamatsu and K. Iida
PRC **81**, 054302 (2010)

$$w(n, \delta) \approx w_0 + \frac{K_0}{18n_0^2}(n - n_0)^2 + \delta^2 \left[S_0 + \frac{L}{3n_0}(n - n_0) \right]$$

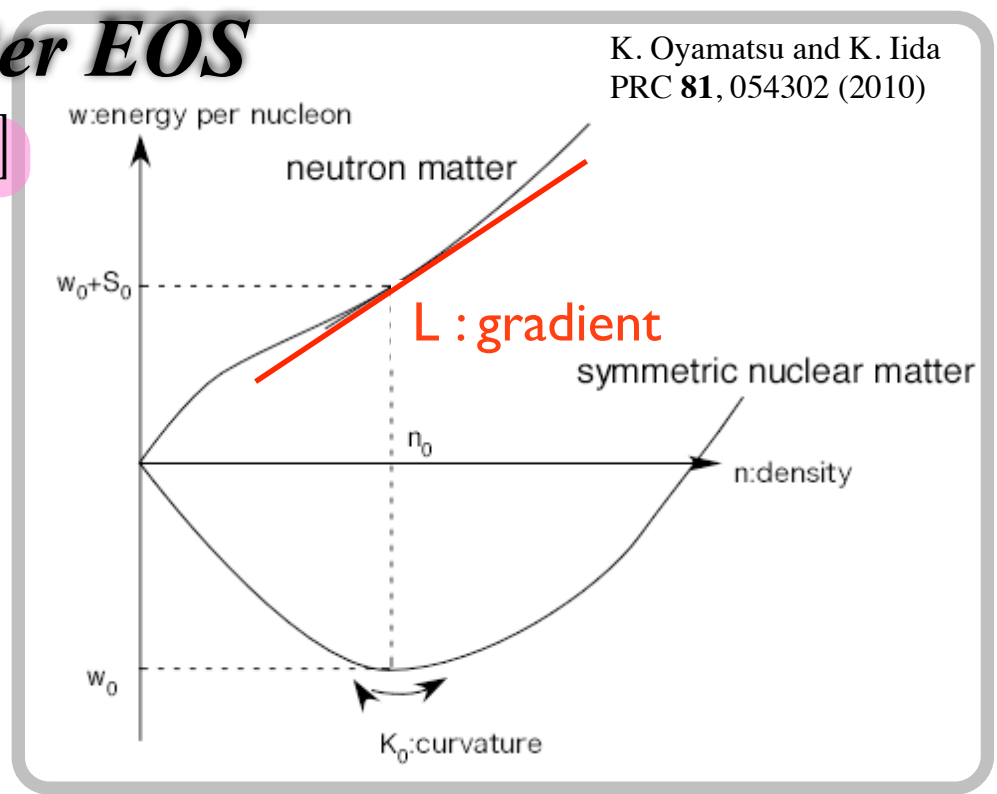
n_0 : saturation density, w_0 : saturation energy
 K_0 : incompressibility, S_0 : symmetry energy at $n = n_0$

$$\delta = (N - Z)/A$$

L : Density derivative coefficient of symmetry energy

First Key Parameter : **L**

How to know **L**?

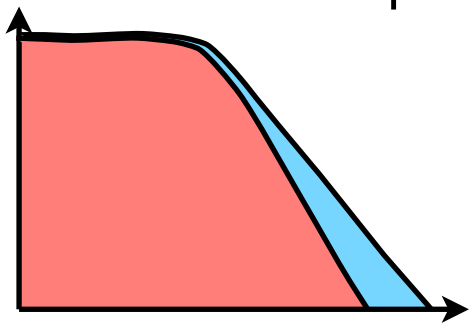


One Simple correlation between L and Neutron Skin

M. Centelles et al., PRL 102, 122502 (2009)

EOS around $N=Z$ $w(n, \delta) \approx w_0 + \frac{K_0}{18n_0^2}(n - n_0)^2 + \delta^2 \left[S_0 + \frac{L}{3n_0}(n - n_0) \right]$

Droplet Model $E_B = a_V A - a_S A^{2/3} - a_C \frac{Z^2}{A^{1/3}} - a_A \frac{(A - 2Z)^2}{A} - \delta(A, Z)$



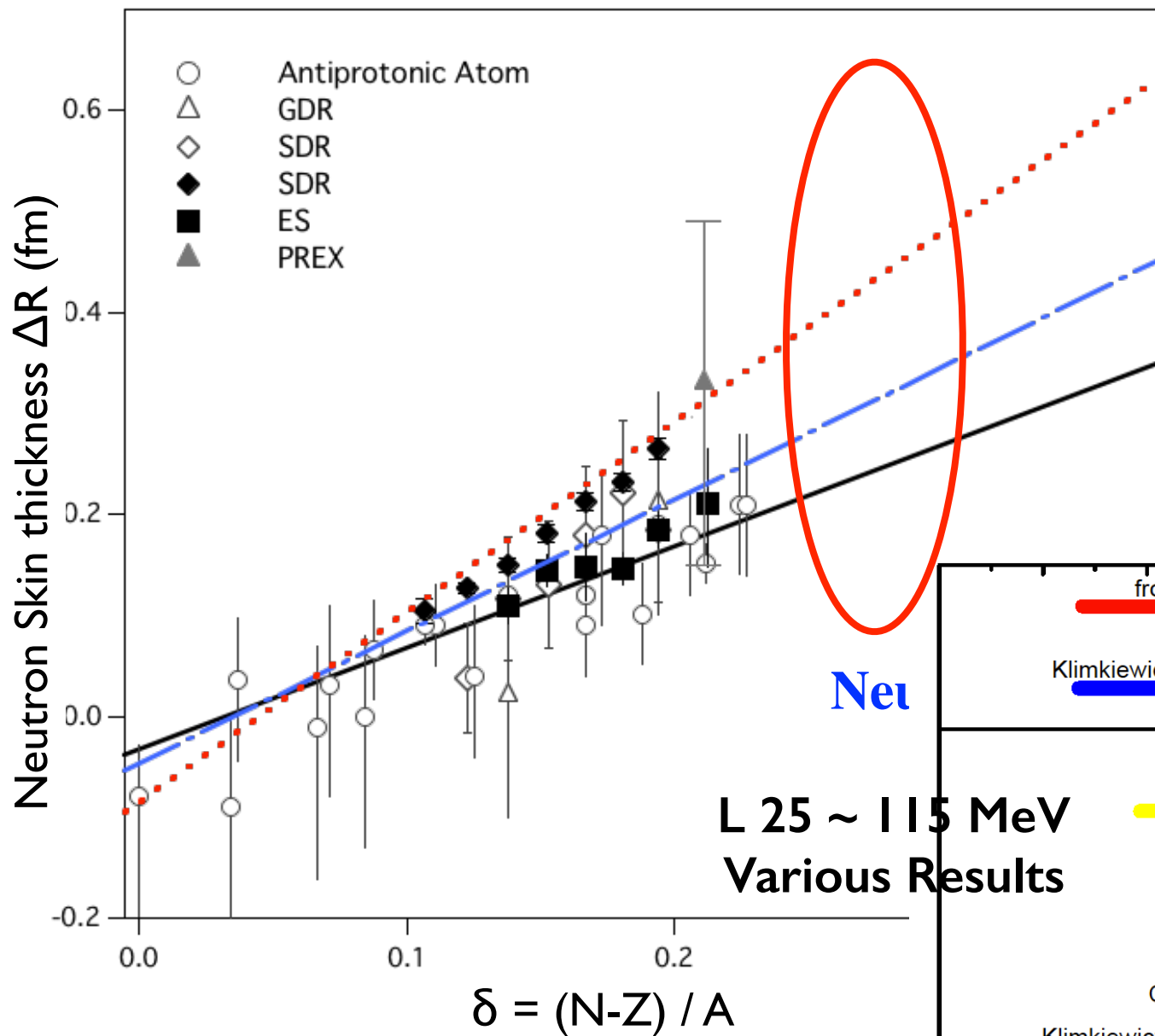
When the density of nuclear matter is around nuclear surface density $\sim 0.1 \text{ fm}^{-3}$
Symmetry term $a_A \approx$ symmetry term of EOS

Neutron skin thickness $\Delta R \sim L \times \delta + \text{correction term}$

$\delta = (N - Z)/A, A > 40$

Measurement of δ dependence of $\Delta R \rightarrow$ **L**

Existing data for Neutron Skin Thickness



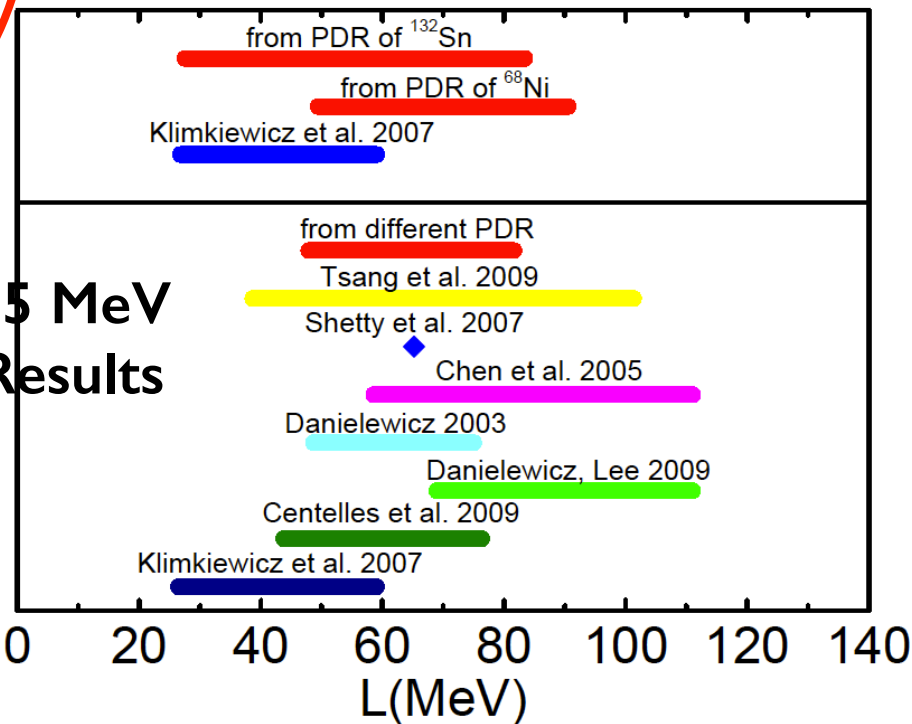
Prediction from NL3 interaction
Neutron Star $R_{1.4M_{\odot}}$ 15km
 $M_{\max} = 2.8 M_{\odot}$

FSUGold interaction
Neutron Star $R_{1.4M_{\odot}}$ 13km
 $M_{\max} = 1.7 M_{\odot}$

M. Centelles et al.,
Analysis of L using
Antiprotonic Atom Data
from $A = 40 \sim 238$

Nei

L 25 ~ 115 MeV
Various Results



Anti Protonic Atom : A. Trzcinska et al., Phys. Rev. Lett. **87** 082501 (2001).

GDR : A. Krasznahorkay et al., Nucl. Phys. A 567 521 (1994).

SDR : A. Krasznahorkay et al., Phys. Rev. Lett. 82, 3216 (1999).

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ES : S. Terashima et al.

ES : J. Zenihiro et al.

Skin thickness for Neutron-rich Nuclei

Ying Cao, H. Sagawa, G. Col'oro
Nuclear Structure in China 2012 (2012) 33

How to determine Neutron Skin Thickness for Exotic Nuclei?

Neutron Skin $\Delta R =$ Neutron Radius R_n - Proton Radius R_p

σ_I (Interaction cross section) \rightarrow Matter Radius

$\sigma_I \longleftrightarrow R_m$

$$\sigma_R = \int db \left[1 - \exp \left(- \int d^2r \sum_{i,j} \sigma_{NN}(E) \rho_z^{P_i}(r) \rho_z^{T_j}(r-b) \right) \right]$$

To know Neutron Skin Thickness, R_p is necessary!

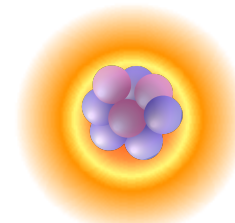
Stable Nuclei :

Electron Scattering Experiment
X-ray Measurements Muonic Atom

Unstable Nuclei :

Isotope shift Measurements

Proton Radii
Sensitive to the
Coulomb Potential of
Protons

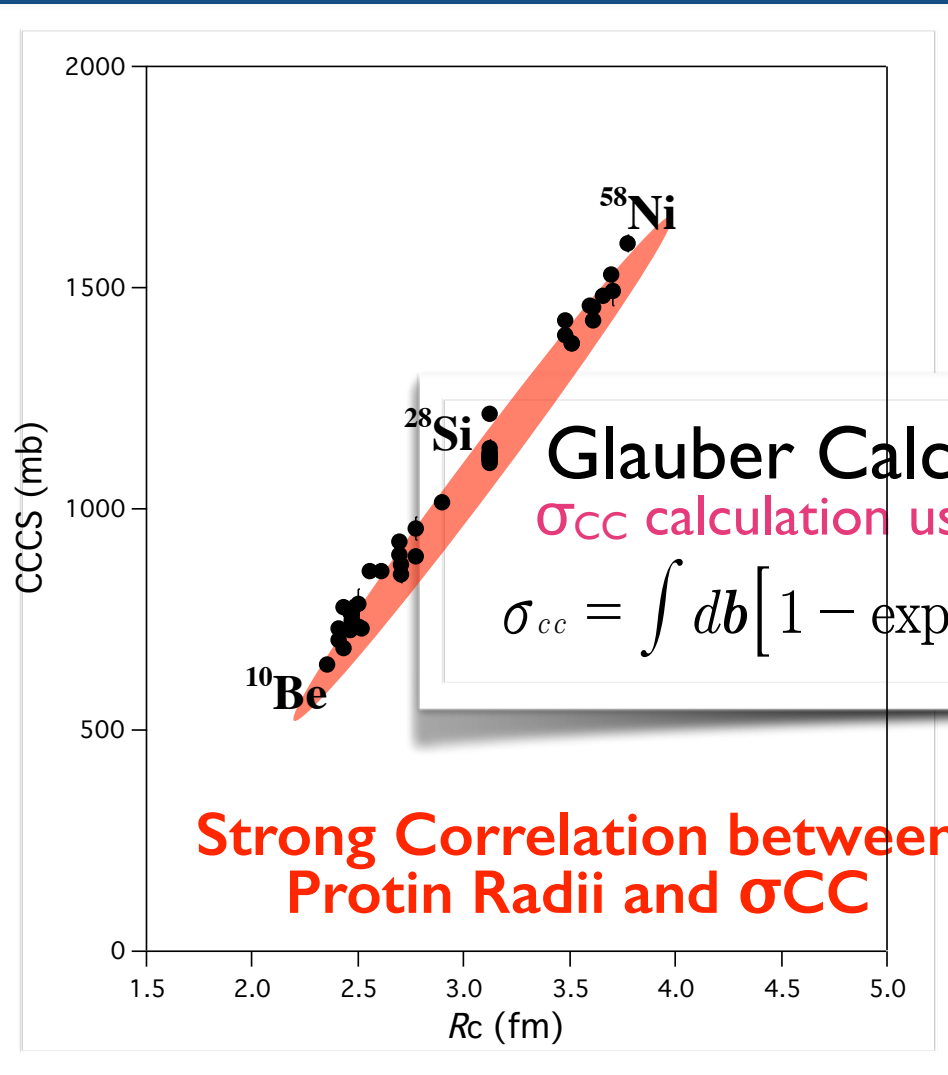


New Method :
Charge Changing Cross Section

$\sigma_{CC} \longleftrightarrow R_p$

Proton Distribution Radius R_p and σ_{cc}

R_p (Electron Scattering Data) VS σ_{cc}



$\sigma_{cc} \rightarrow$ Proton Radius ?

Glauber Calculation for σ_{cc}

σ_{cc} calculation using charge distribution of nucleus

$$\sigma_{cc} = \int db \left[1 - \exp \left\{ - \left(\sigma_{pp} \int \rho_{proton}^{Projectile} \rho_{proton}^{Target} + \sigma_{np} \int \rho_{proton}^{Projectile} \rho_{neutron}^{Target} \right) \right\} \right]$$

$\sigma_{CC} \longleftrightarrow R_p$
?

Determination of skin thickness

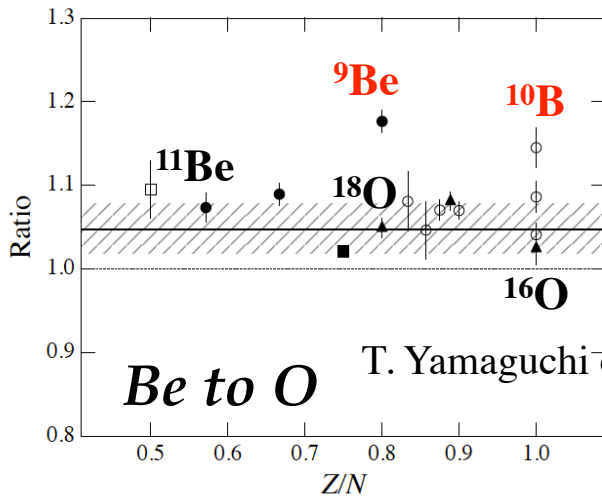
Charge radii from CC cross sections

Glauber Calculation for σ_{CC}

σ_{CC} calculation using charge distribution of nucleus

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Determination of charge radius for ^{16}C from σ_{CC} (HIMAC)

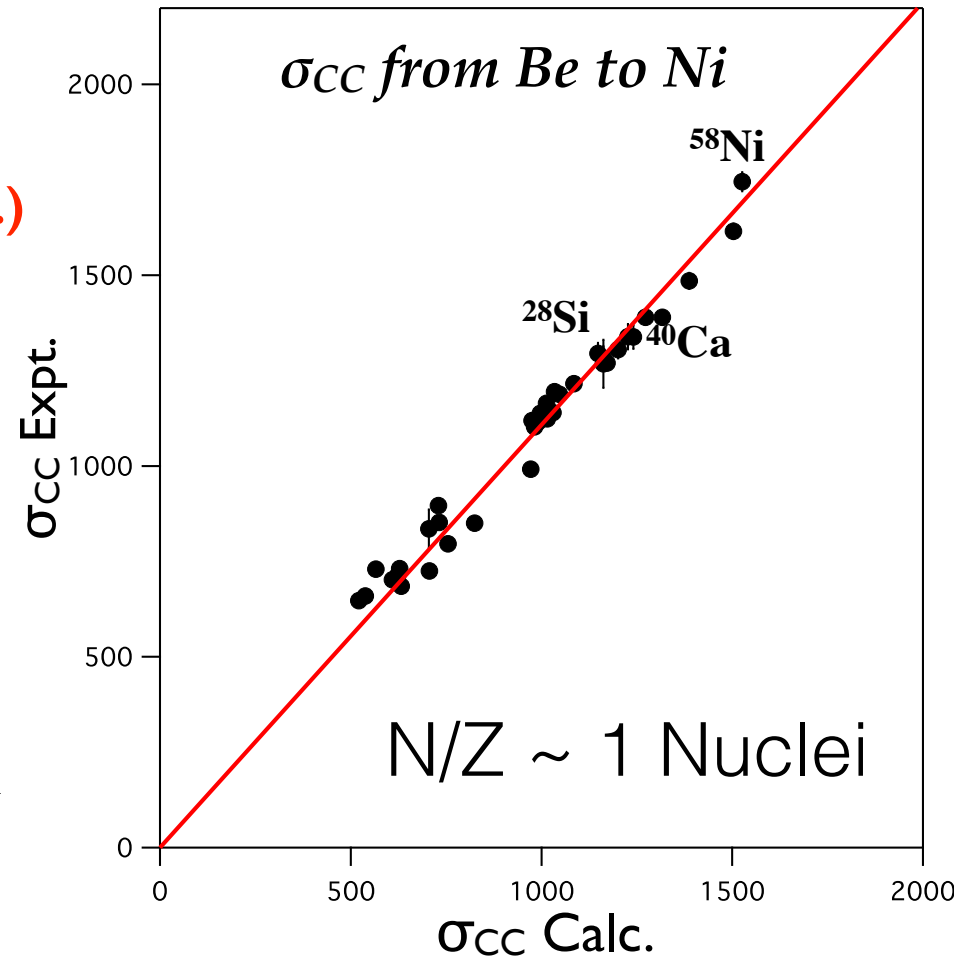


Calibration of $\sigma_{CC}(\text{Expt.}) / \sigma_{CC}(\text{Calc.})$ for light nuclei in wide range of Z/N (Charge Radii known) $^9\text{Be}, ^{10}\text{B}$, Borromean

Determination of charge radius for $^{12-19}\text{C}$ from σ_{CC} (GSI) ~ 1 GeV/u

R. Kanungo et al., PRL 117, (2016) 102501

How about unstable, heavier nuclei $A > 40$?



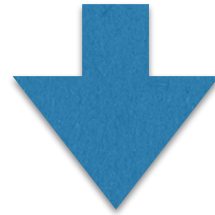
$\sigma_{CC}(\text{Expt.}) / \sigma_{CC}(\text{Calc.}) \sim \text{Constant}$

σ_{CC} Measurements

σ_{CC} Measurements for ^{40-48, 50}Ca, ⁵⁸⁻⁶⁴Ni, ³⁸⁻⁴⁷K, ⁶²⁻⁸⁰Cu

*Charge Radii are known
(Isotope-shift Measurements)*

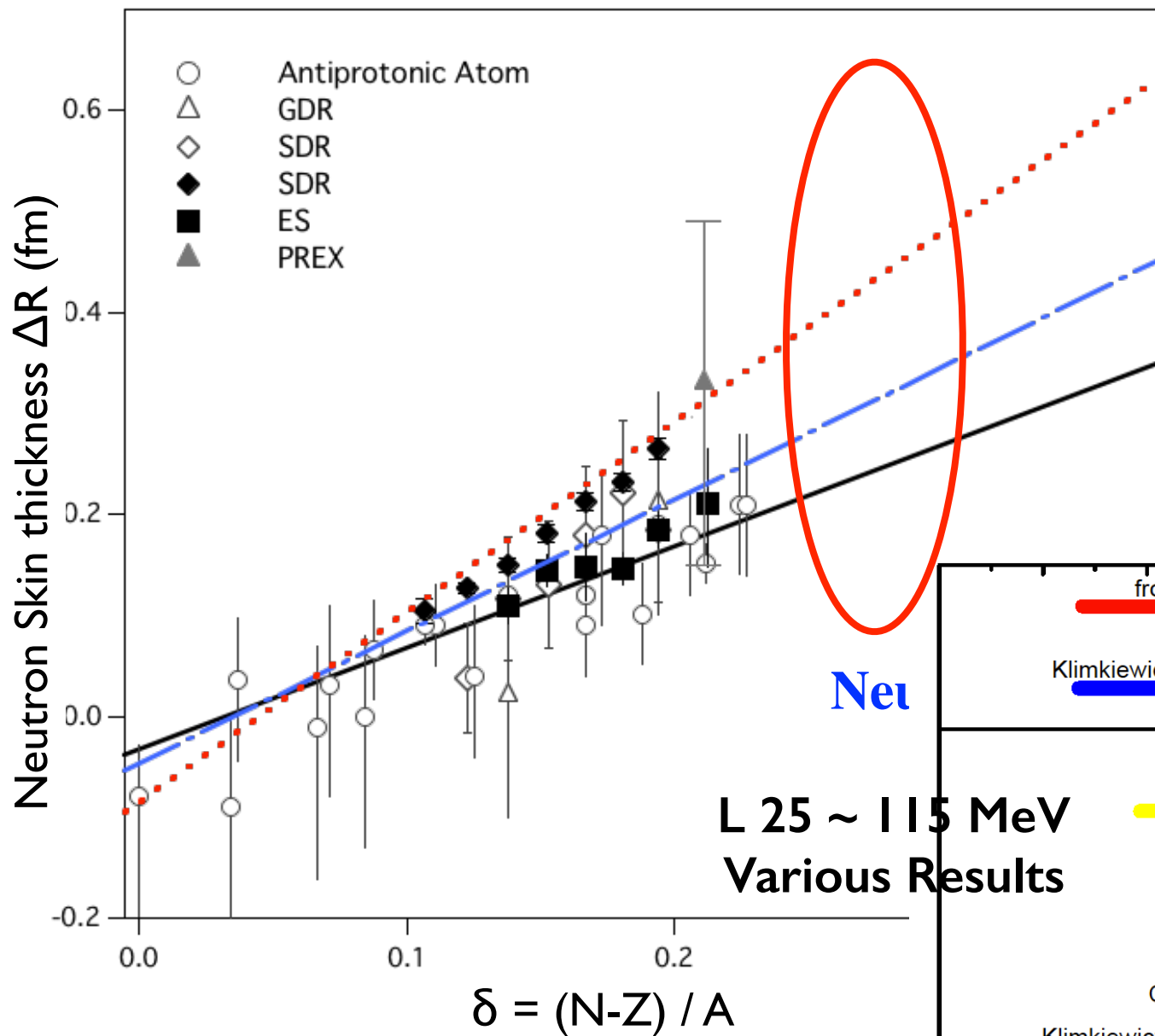
Study of $\sigma_{CC}(\text{Expt.}) / \sigma_{CC}(\text{Calc.})$ for $A > 40$ nuclei in wide Z/N range



And

σ_I and σ_{CC} Measurements for ⁵⁸⁻⁷⁸Ni

Existing data for Neutron Skin Thickness



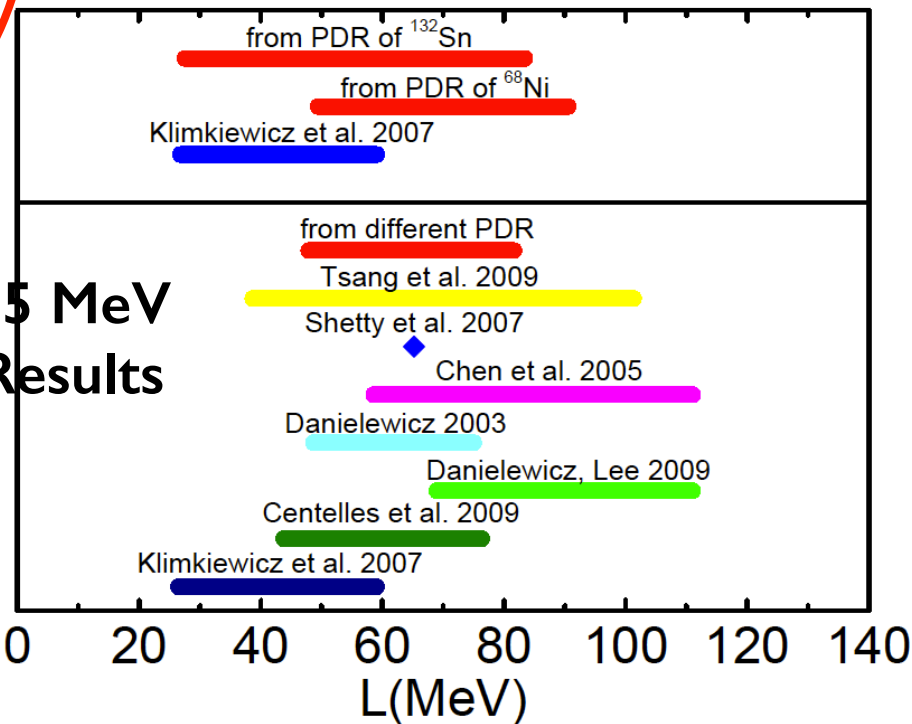
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Skin thickness for Neutron-rich Nuclei

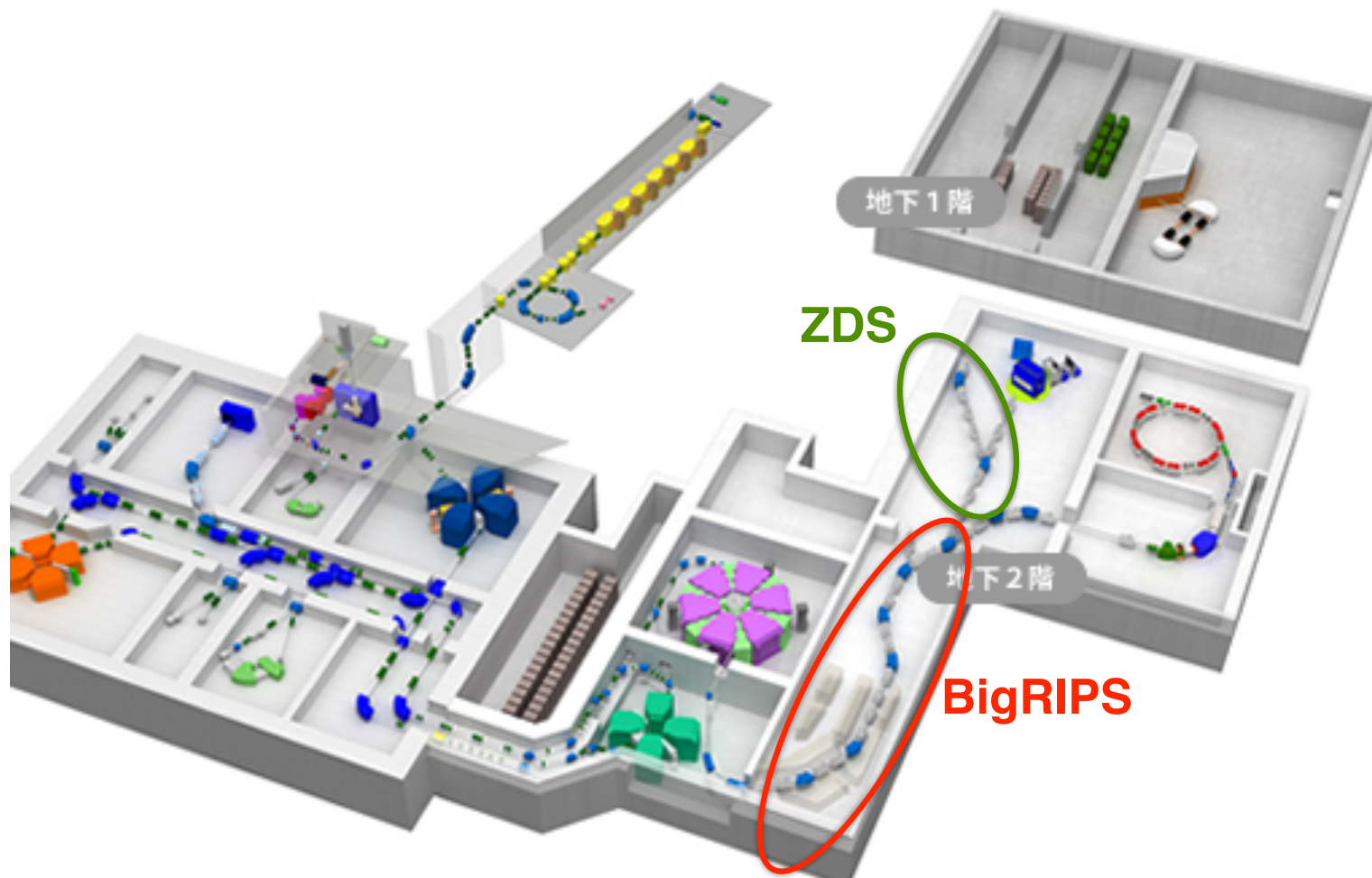
Ying Cao, H. Sagawa, G. Col'oro
Nuclear Structure in China 2012 (2012) 33

Experiment at RIBF



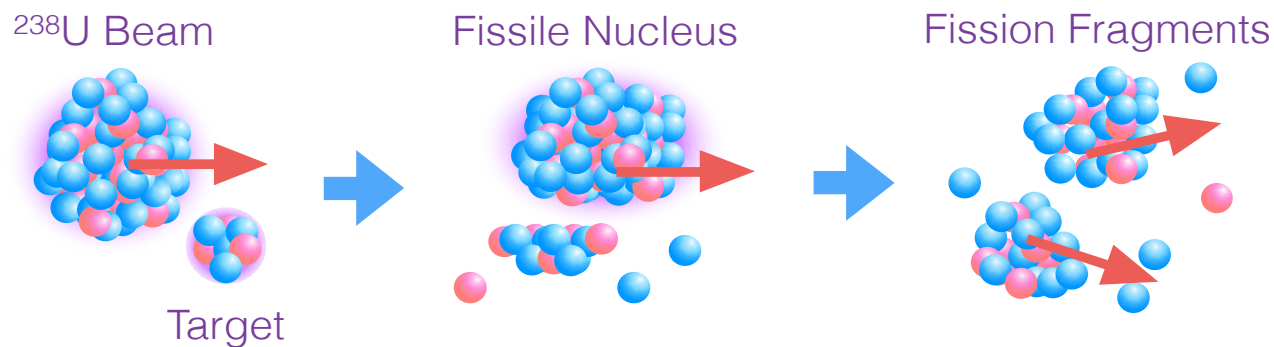
RIBF ZDS F11, two MUSICs from GSI

Experiment at RIBF

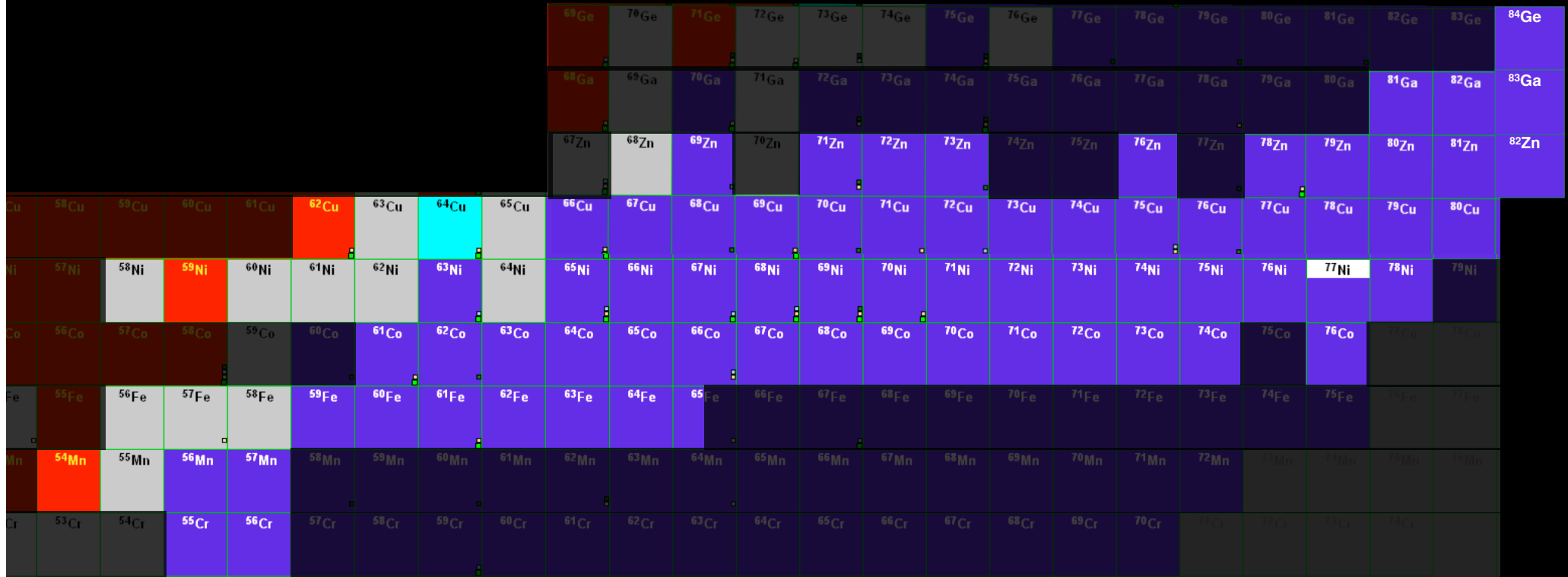


^{238}U Beam
345 MeV/u 30 pA

Abrasion Fission
on Be Target



Produced Beam around Ni Region ²³⁸U on Be Abrasion Fission



⁸⁴Ge

⁸¹⁻⁸³Ga

⁶⁸⁻⁸²Zn

⁶²⁻⁸⁰Cu

⁵⁸⁻⁷⁸Ni

⁶¹⁻⁷⁶Co

⁵⁶⁻⁶⁵Fe

⁵⁴⁻⁵⁷Mn

⁵⁵⁻⁵⁶Cr

Produced Beam around Ca Region

⁴⁰⁻⁵⁰Ca

⁴¹⁻⁴⁸K

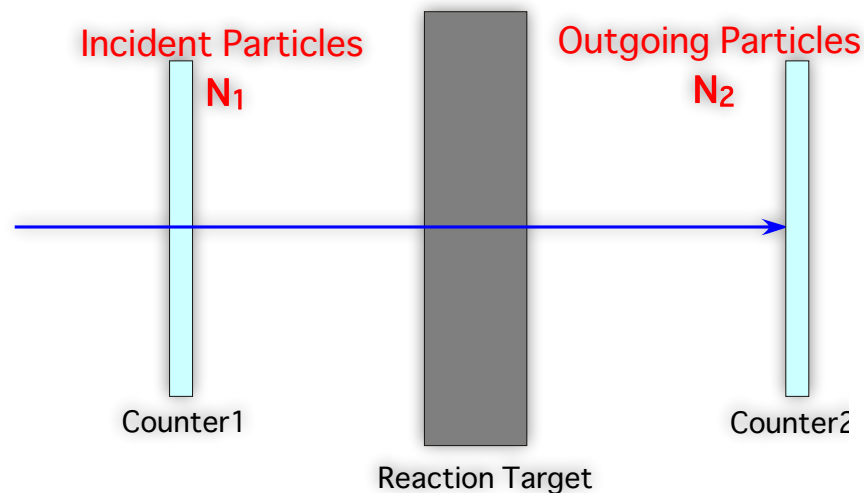
³⁹⁻⁴⁶Sc etc. ...

σ_{CC} Measurements for $^{40-48}\text{Ca}$, $^{58-64}\text{Ni}$, $^{38-47}\text{K}$, $^{62-80}\text{Cu}$

*Charge Radii are known
(Isotope-shift Measurements)*

σ_I and σ_{CC} Measurements for $^{58-78}\text{Ni}$ and nuclides nearby

Measurements : Transmission Method



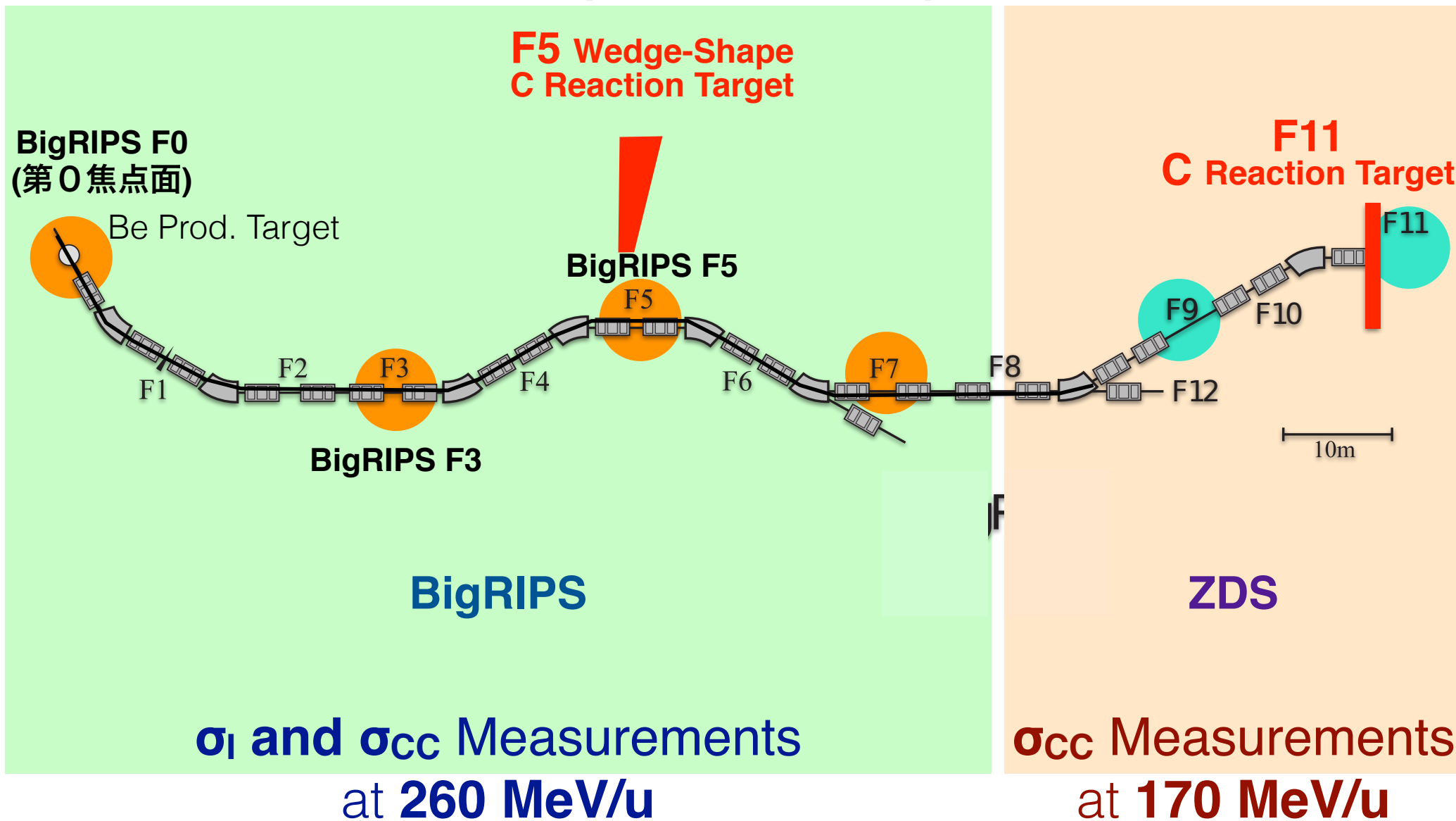
$$\sigma_{I \text{ or } CC} = -\frac{1}{t} \ln\left(\frac{N_2}{N_1}\right)$$

N_1 : Incident particle

σ_I N_2 : Without changing Z and A

σ_{CC} N_2 : Without changing Z

Experimental Setup



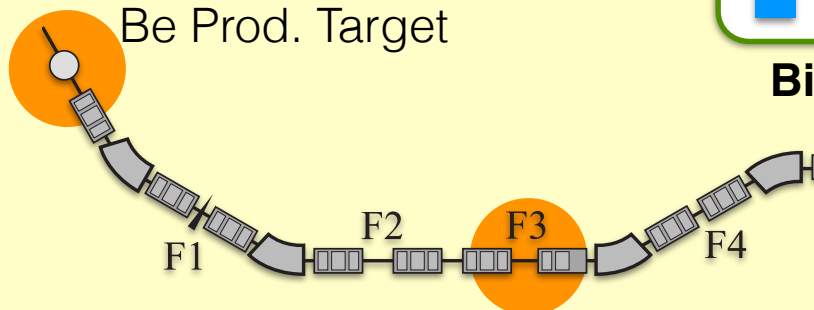
σ_{CC} at two different energies and σ_I measured simultaneously

F5 Target Measurement

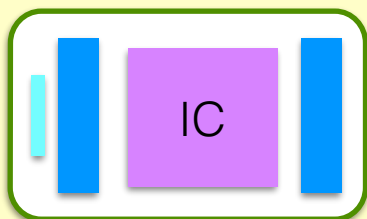
BigRIPS F0 - F5

BigRIPS F0
(第0焦点面)

Be Prod. Target



BigRIPS F3



σ_I and σ_{CC} Measurements
at 260 MeV/u

Reaction
Target

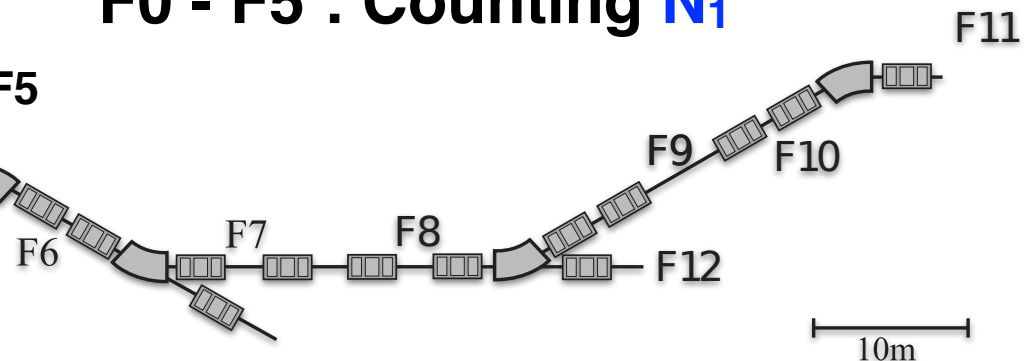
PPAC F5PL



BigRIPS F5



F0 - F5 : Counting N_1



$$\sigma_{I \text{ or } CC} = -\frac{1}{t} \ln \left(\frac{N_2}{N_1} \right)$$

N_1 : Incident particle

Identification : $\Delta E - B\rho - TOF$ Method

Magnetic Rigidity ($B\rho$) : F5 PPAC

Energy Loss : Ion Chamber at F3 (F3IC)

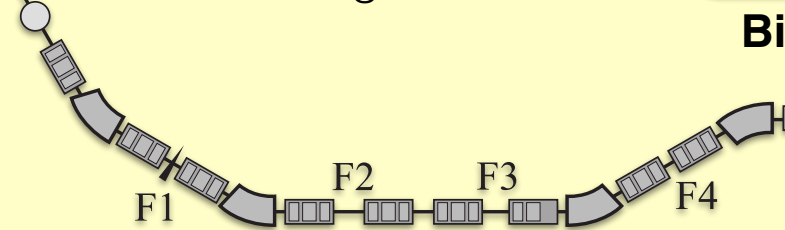
Time of Flight of F3 - F5 : F3PL, F5PL

F5 Target Measurement

BigRIPS F0 - F5

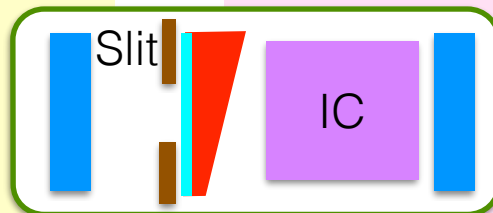
BigRIPS F0
(第0焦点面)

Be Prod. Target

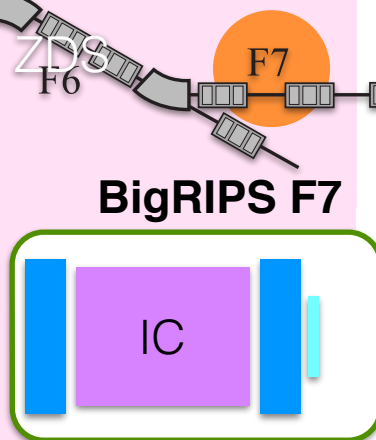
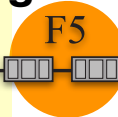


σ_I and σ_{CC} Measurements
at 260 MeV/u

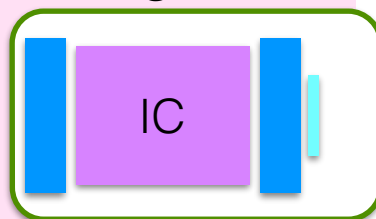
Reaction Target
PPAC F5PL PPAC



BigRIPS F5



BigRIPS F7



PPAC PPAC F7P

F5 - F7 : Counting N_2

BigRIPS F5 - F7

$$\sigma_{I \text{ or } CC} = -\frac{1}{t} \ln\left(\frac{N_2}{N_1}\right)$$

σ_I N_2 : Without changing Z and A

σ_{CC} N_2 : Without changing Z

Identification : $\Delta E - B\rho - TOF$ Method

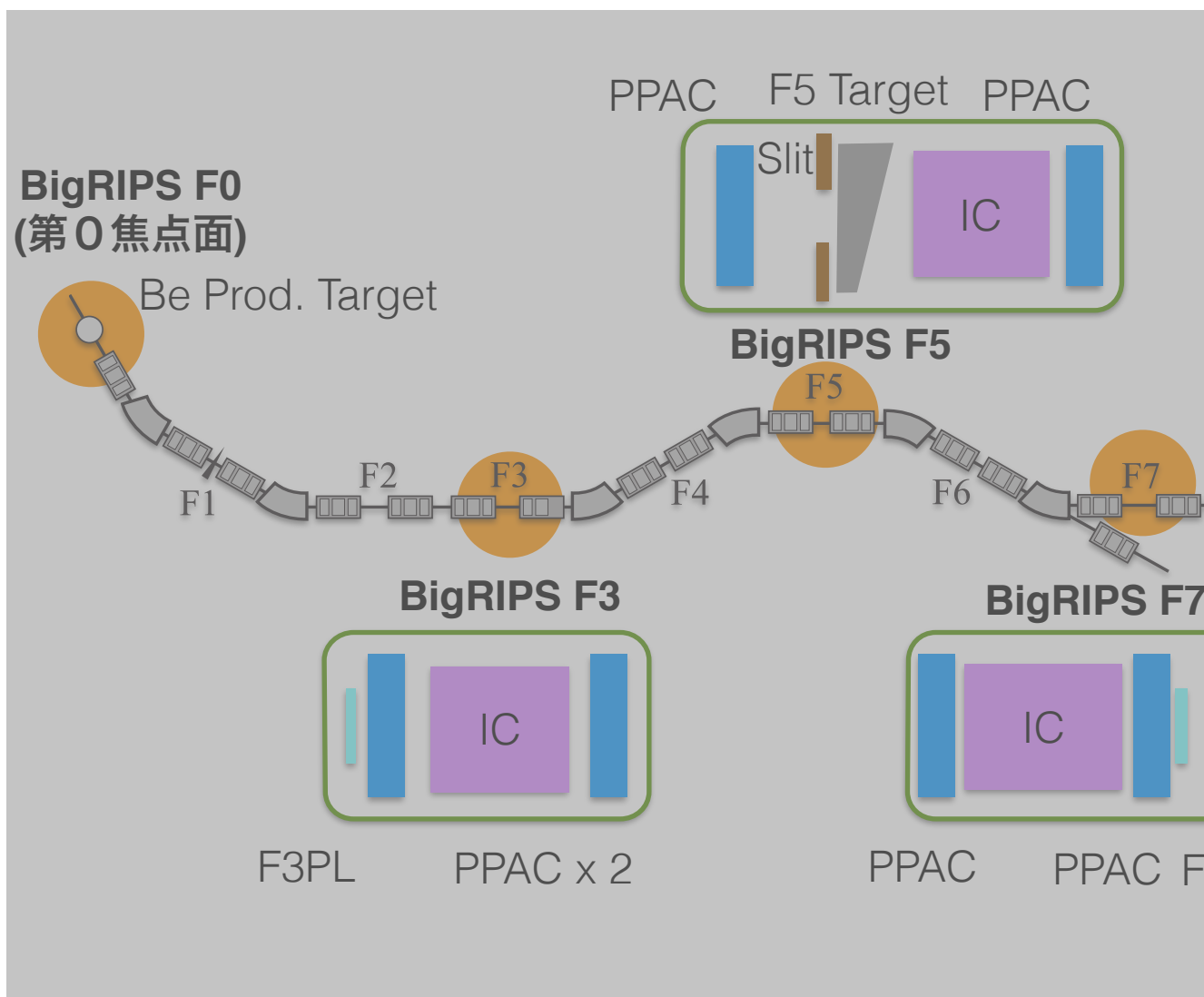
Magnetic Rigidity ($B\rho$) : F5 PPAC

Energy Loss : Ion Chamber at F5 and F7 (F5IC, F7IC)

Time of Flight of F5 - F7 : F5PL, F7PL

10m

F11 Target Measurement



$$\sigma_{cc} = -\frac{1}{t} \ln\left(\frac{N_2}{N_1}\right)$$

N_1 : Incident particle

N_2 : Without changing Z

σ_{cc} Measurements
at **170 MeV/u**

F11 Target Measurement

F7 - F11 : Counting N_1

Identification : $\Delta E - B\rho - TOF$ Method

$B\rho$: F9 PPAC

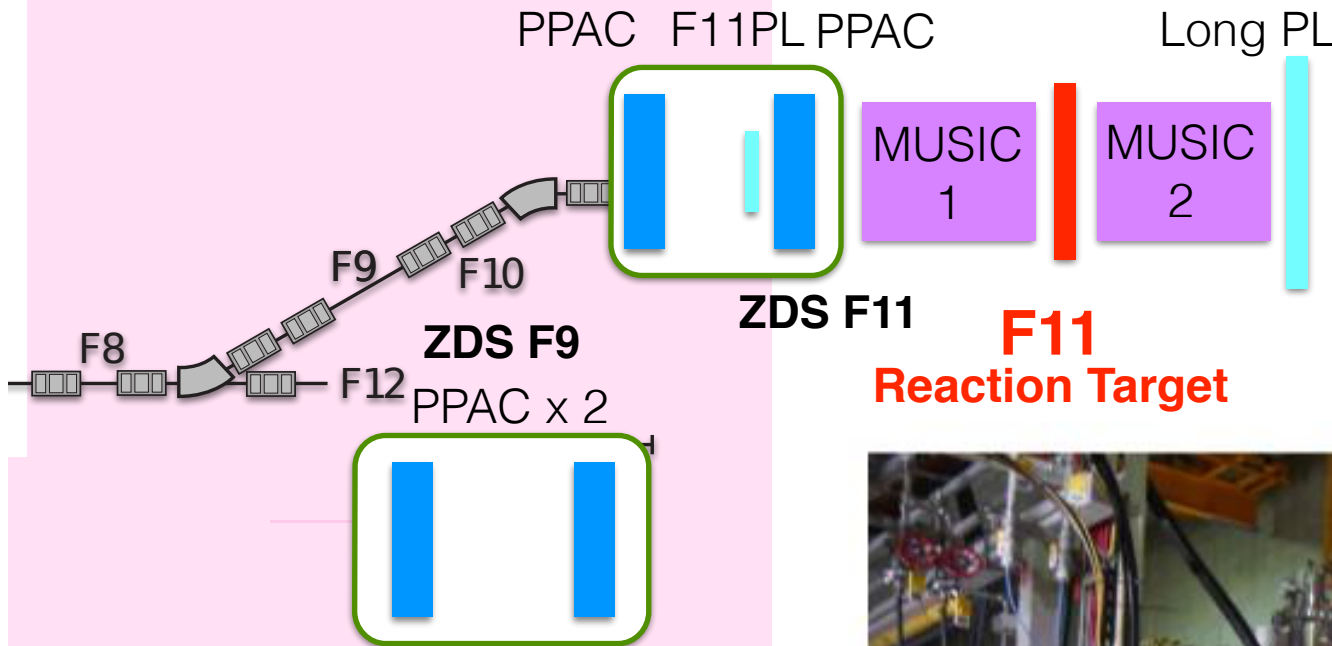
ΔE : MUSIC 1

TOF F7PL, F11PL

$$\sigma_{cc} = -\frac{1}{t} \ln\left(\frac{N_2}{N_1}\right)$$

N_1 : Incident particle

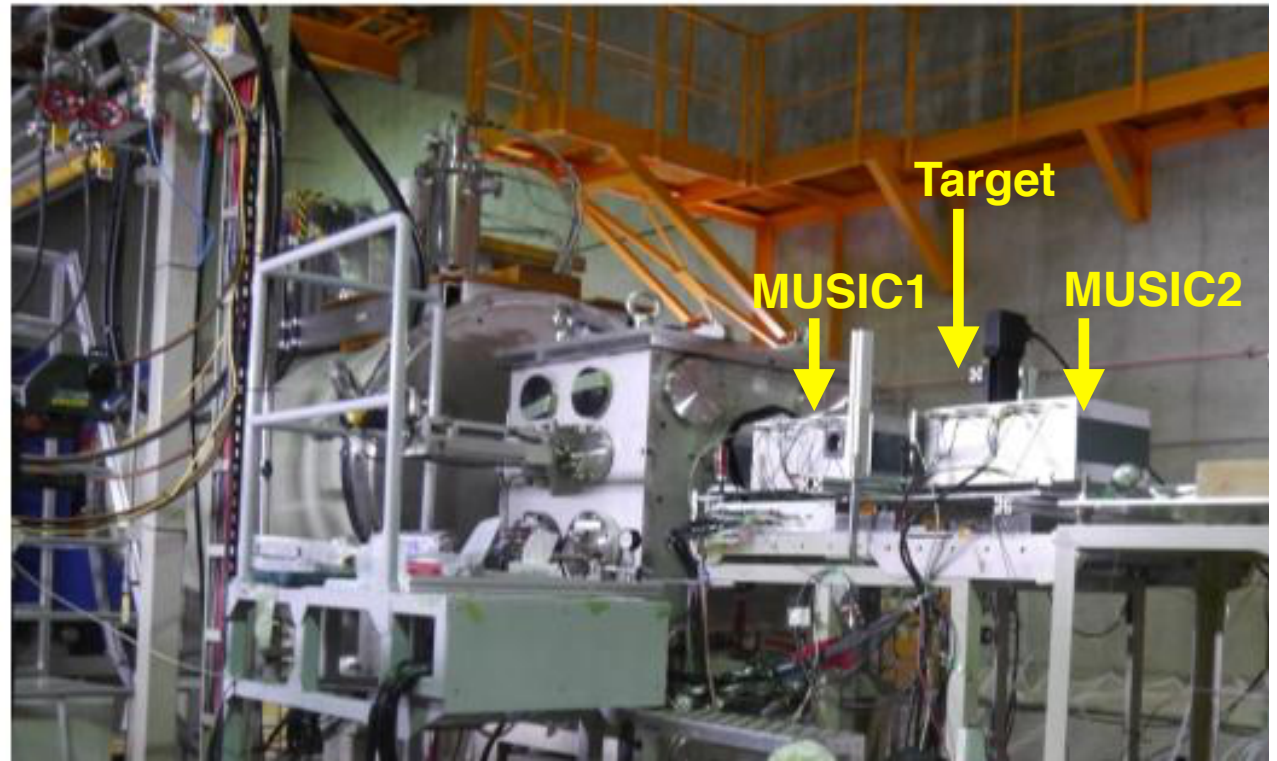
N_2 : Without changing Z



MUSIC2 : Counting N_2

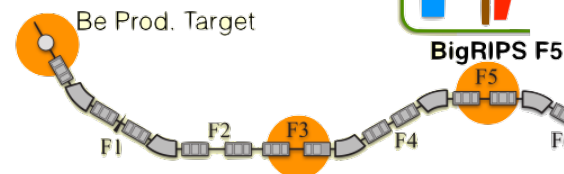
F11
Reaction Target

σ_{cc} Measurements
at **170 MeV/u**



BigRIPS F0 - F5

BigRIPS F0
(第0焦点面)

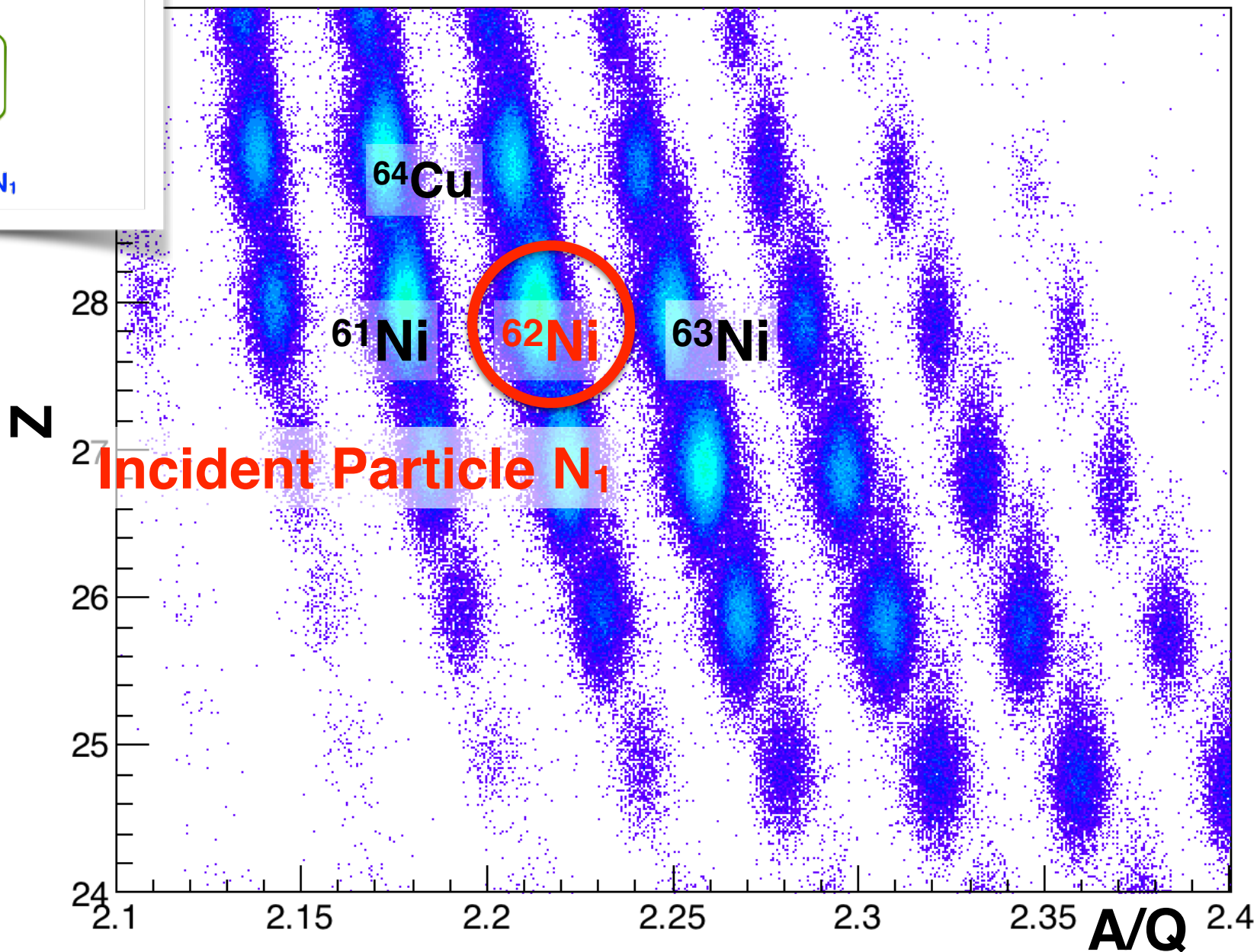


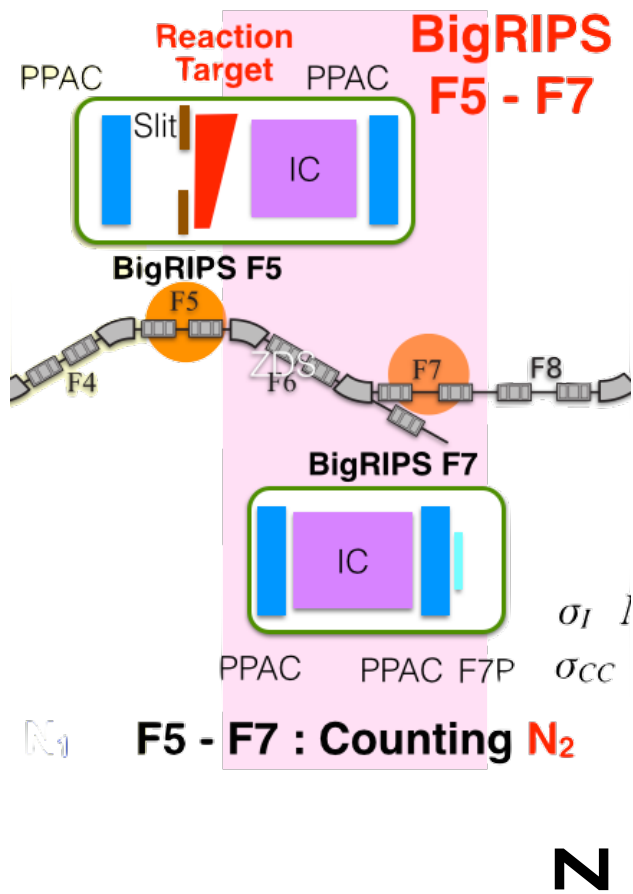
BigRIPS F3



F0 - F5 : Counting N_1

Particle Identification Incident Beam on **F5 Target**





Particle Identification after the Reaction Target

