

# Neutrino oscillations: the state of the subject

Federico Sánchez

Institut de Física d'Altes Energies

Barcelona Institute of Science and Technology

ONLY THOSE WHO SEE THE INVISIBLE  
CAN DO THE IMPOSSIBLE

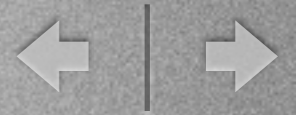
MAMALLAPURAM SPECIAL GRADE TOWN PANCHAYAT



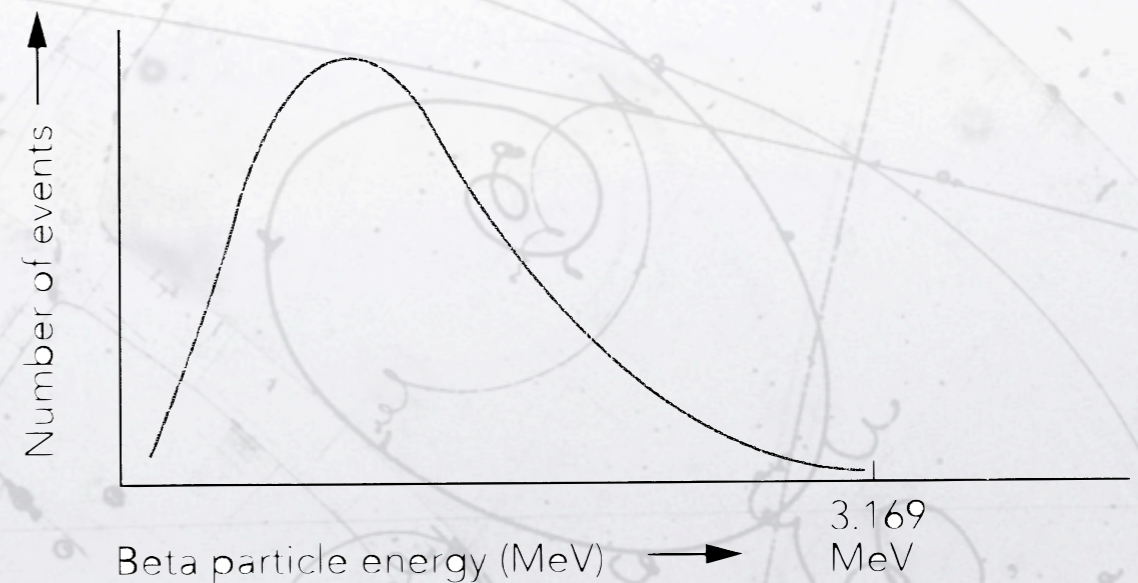
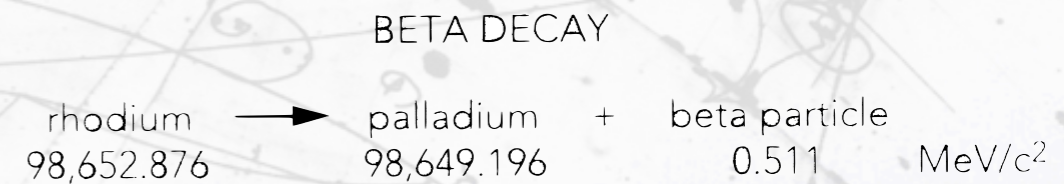
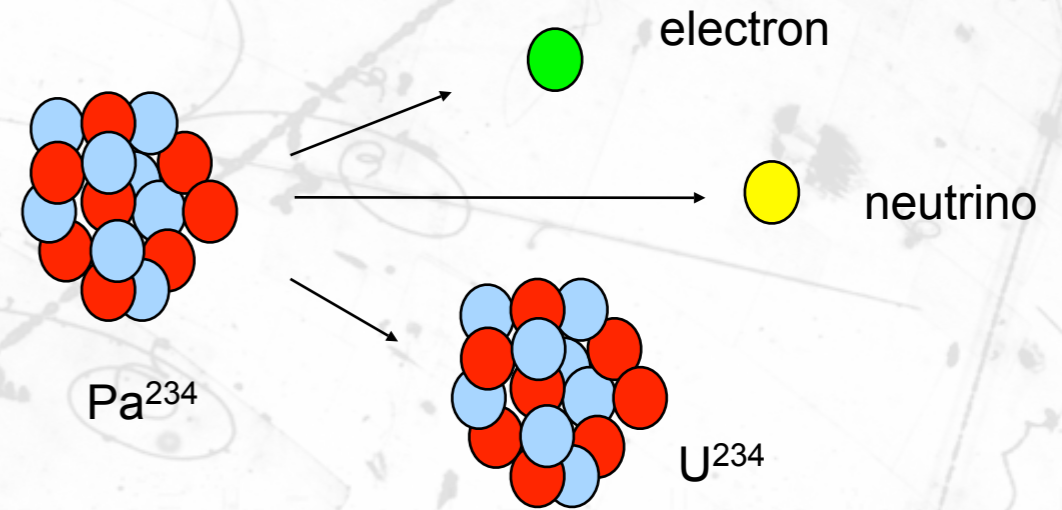
- Neutrinos: discovery and early ideas.
- Oscillation phenomenology:
  - Solar neutrinos + Kamland
  - Atmospheric neutrinos + Long Base line experiments.
  - $\theta_{13}$  & CP violation.
- Closing remarks



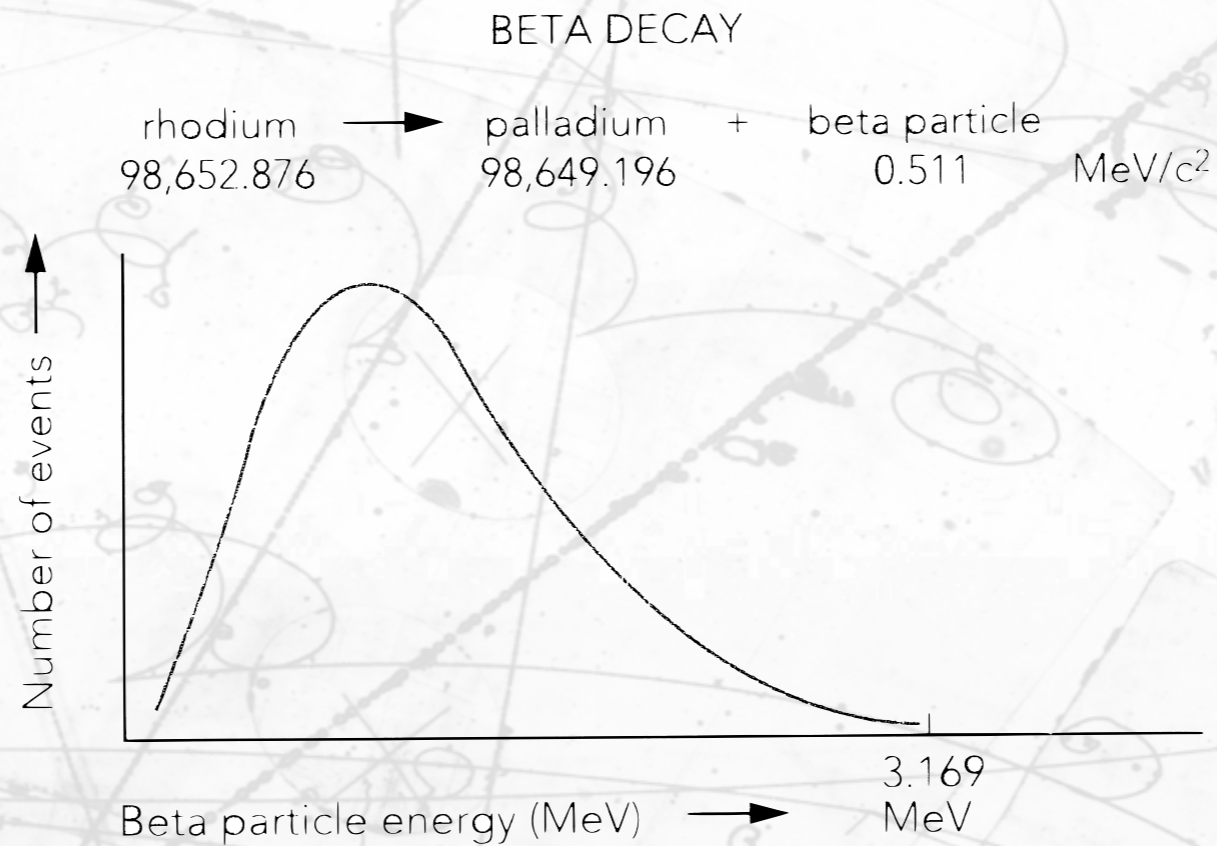
# Neutrinos



- Neutrinos were proposed in 1931 by Pauli in a desperate attempt to understand the  $\beta$  spectrum.
- The particle (first called neutron) had the following properties:
  - Neutral
  - weakly interacting
  - low mass ( $\ll m_e$ )
  - Spin 1/2







In the 30's, it was already known that  $m_\nu < 100 \text{ MeV}$

- Mass of the neutrino can be measured by the end point of the  $\beta$  decay spectrum:

$$m_\nu = M_{Rhodium} - M_{Palladium} - E_{e^-}^{max}$$

The  $m_\nu$  precision is limited by the resolution of masses and electron energy.

Nowadays we still use the same technique in Katrine



# Neutrino discovery

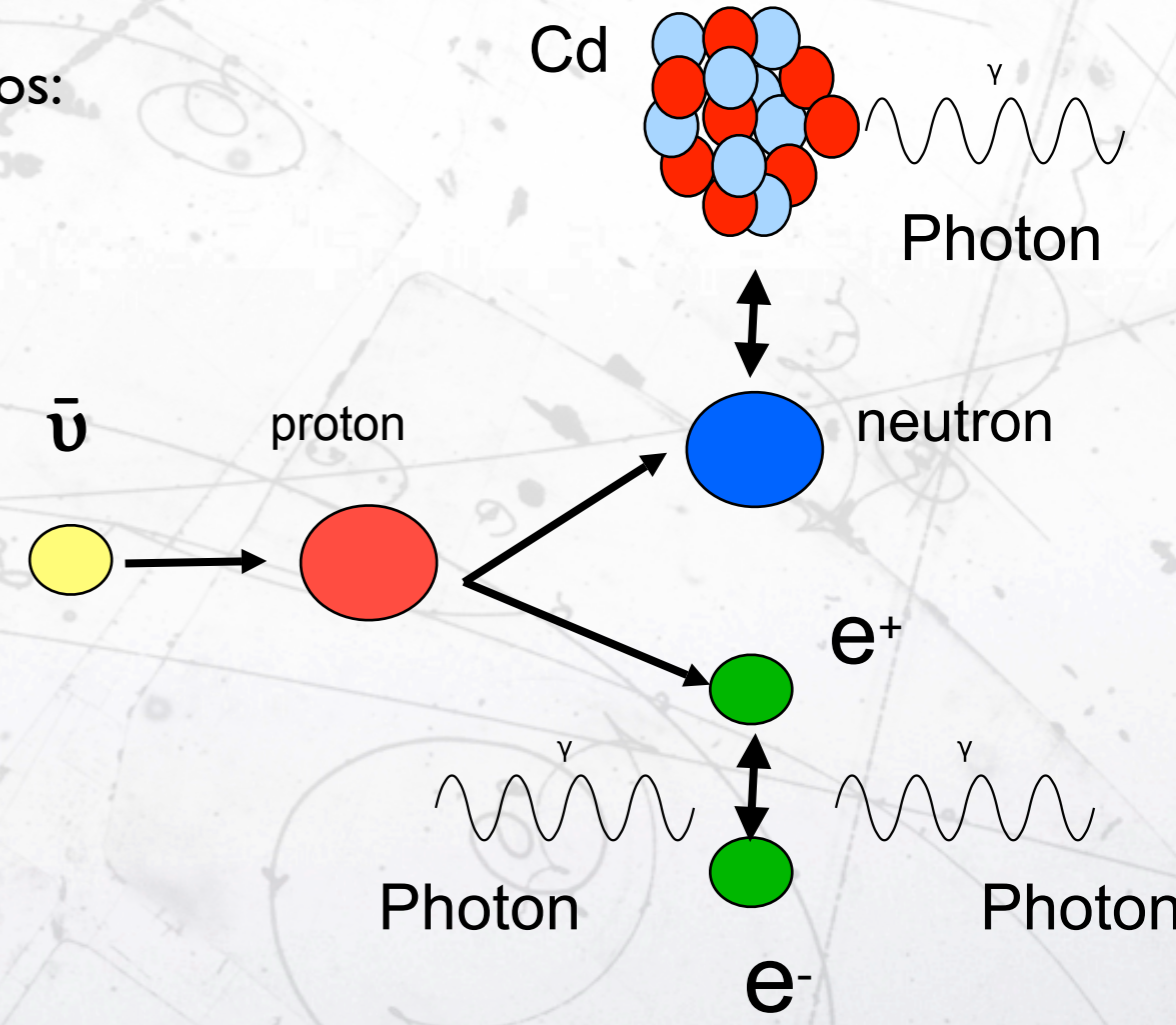
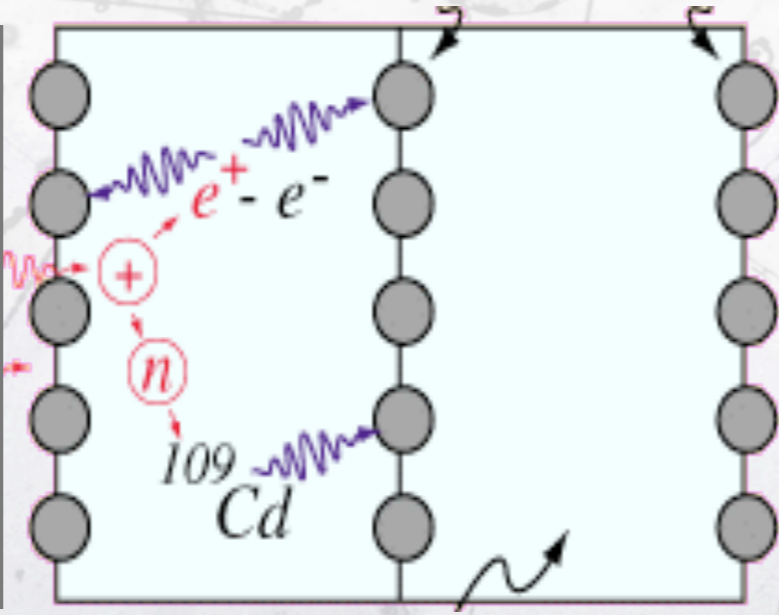


- The first neutrino detection was done by Reines & Cowan in 1956.
- Neutrinos from the Savannah River (USA) experimental nuclear power plant: very intense source of neutrinos!
- A retarded coincidence signal was used to detect neutrinos:
  - Prompt positron (measures neutrino energy)
  - electron-positron annihilation
  - neutron absorption in Cd.



$10^{13}$   
ν/cm<sup>2</sup>/s

Soil absorber





# How many neutrinos ?



	I	II	III
mass →	3 MeV	1.24 GeV	172.5 GeV
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
name →	<b>u</b> up	<b>c</b> charm	<b>t</b> top
Quarks	6 MeV	95 MeV	4.2 GeV
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom
Leptones	<2 eV	<0.19 MeV	<18.2 MeV
	0	0	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino
	0.511 MeV	106 MeV	1.78 GeV
	-1	-1	-1
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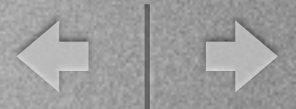
- Elementary particles are grouped in 3 generations.
- Each generation is like the previous but with larger masses.

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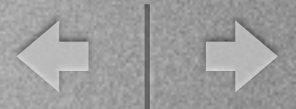
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# How many neutrinos ?



- Elementary particles are grouped in 3 generations.
- Each generation is like the previous but with larger masses.
- Ordinary matter is made of the lightest generation (protons, neutrons and electrons).
- There is one neutrino associated to each family: **3 neutrinos!**

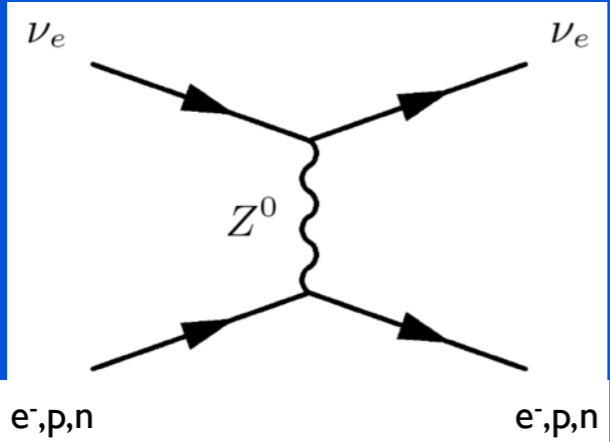
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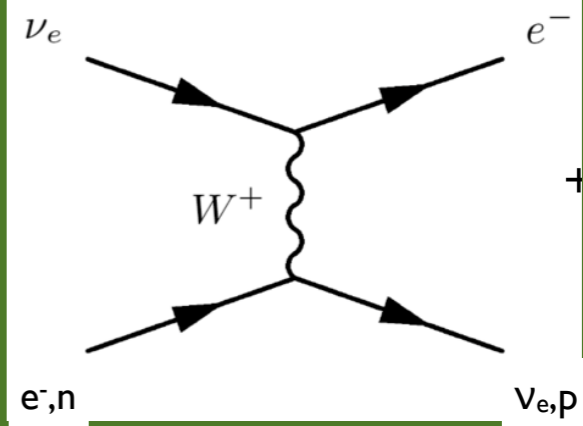
## Neutrinos suffer only weak interactions

### Neutral Current



Neutrinos in the final state.  
It does not distinguish neutrino flavour

### Charged Current



Massive lepton in the final state.  
It does distinguish neutrino flavour

Neutrinos has no electric charge. Neutrinos has to (weakly) interact to be detected.

At distances of around  $3 \times 10^{-17}$  m, the weak interaction is 10,000 times weaker than the electromagnetic



- Neutrinos suffer only weak interactions.
- Weak interactions couple only to left-handed chiral ( $\sim$ helicity in the massless limit) particles.
- The usual Dirac Lagrangian term for the mass is given by:

$$\mathcal{L}_D = -m_D \bar{\nu}_L \nu_R + h.c.$$

- This implies that, if the neutrino has mass there should be both right handed and left handed neutrinos.
- Right handed neutrinos are “sterile”:
  - this was the main argument to believe that the neutrinos were massless.

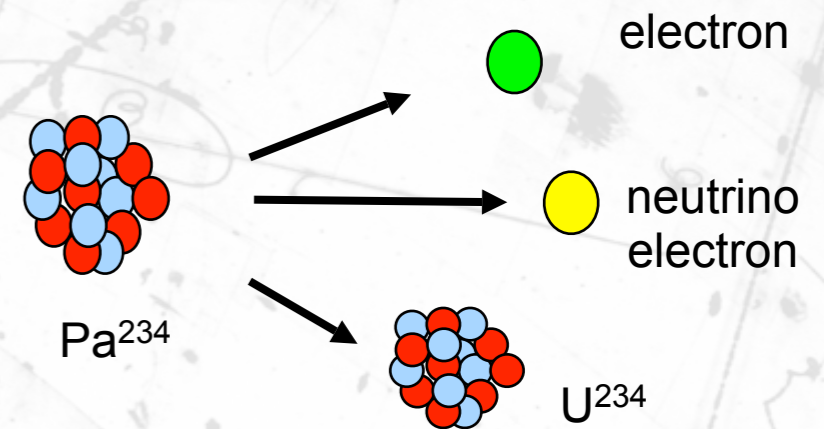
There are models where neutrino = antineutrinos avoiding the “sterile” component.



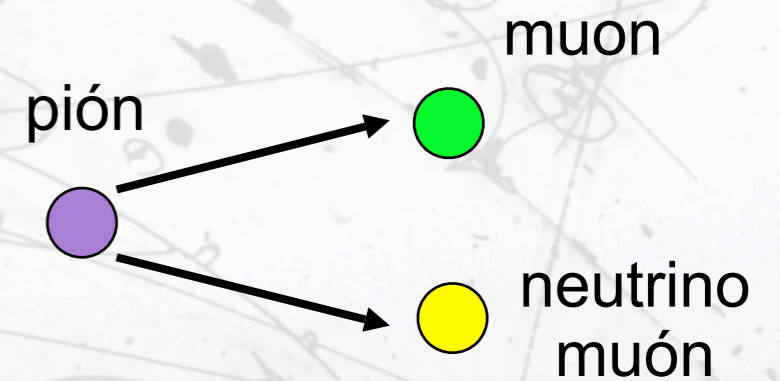
Neutrino flavour depends on the way it interacts

- When a neutrino interacts (**produced or disappeared**) it is associated to :
  - electron, muon ( $\mu$ ) or tau ( $\tau$ )
- Depending on the associated particle (leptón) neutrinos are classified as:
  - neutrino electron ( $\nu_e$ )
  - neutrino muon ( $\nu_\mu$ )
  - neutrino tau ( $\nu_\tau$ )

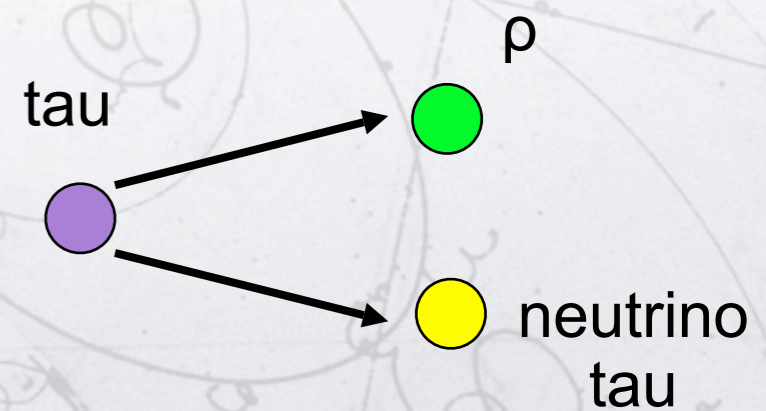
Neutrino electron



Neutrino muon

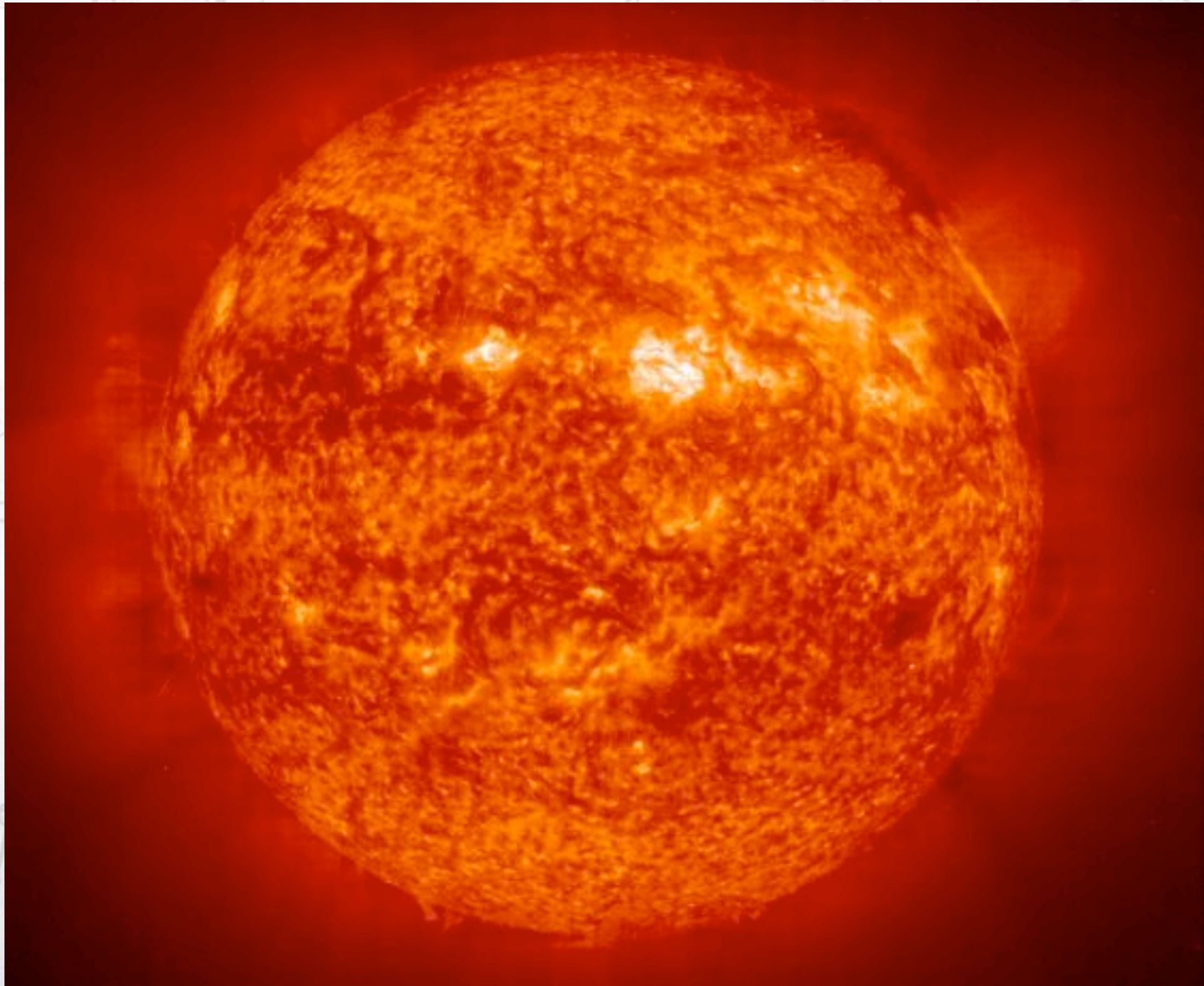


Neutrino tau



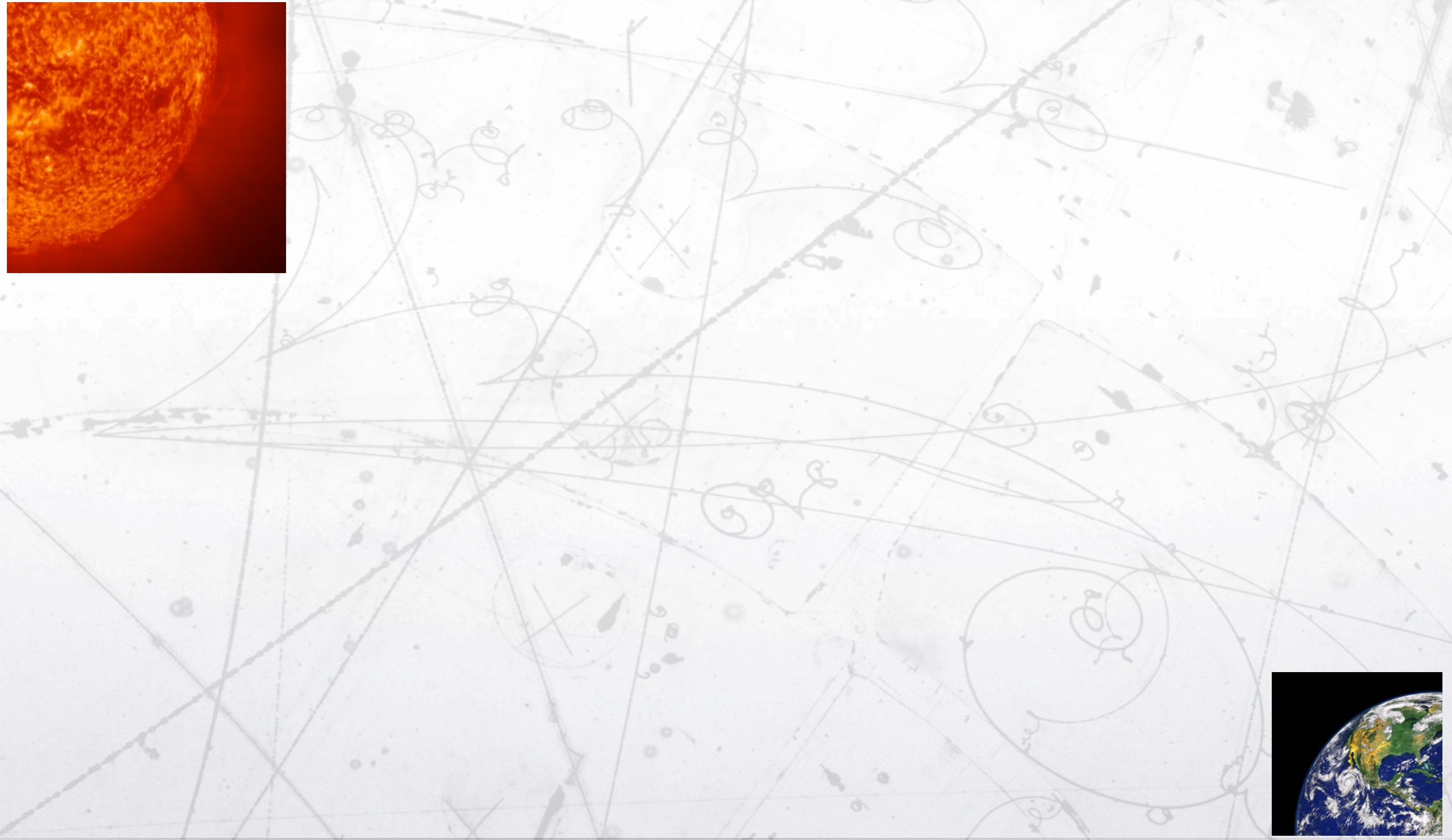
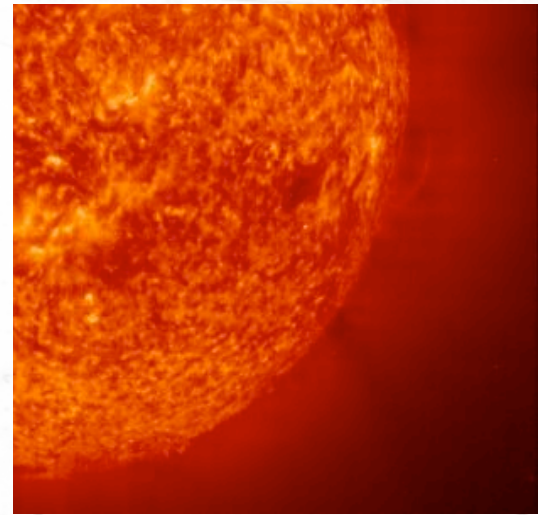


# The sun



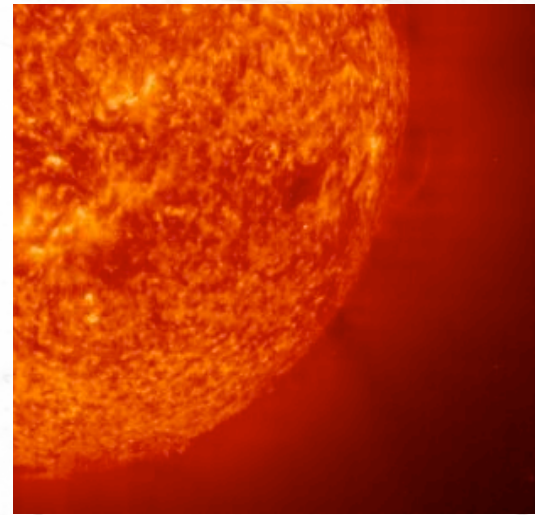


# Solar neutrinos

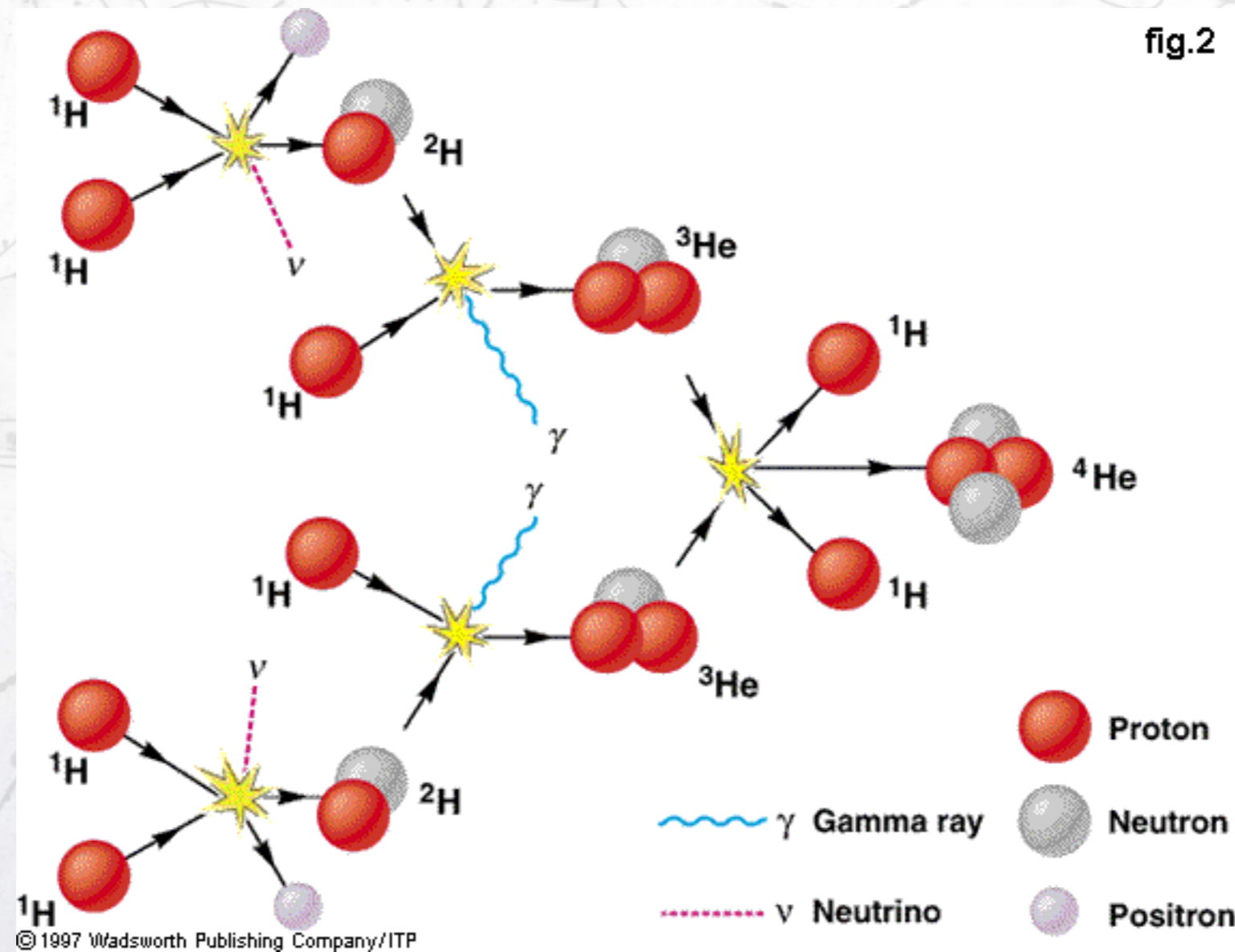




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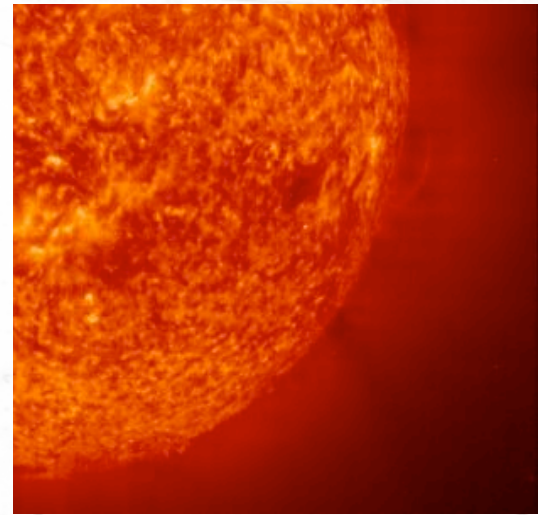


- 4 protons fuse producing a Helium 2 positrones and 2 neutrinos.





# Solar neutrinos

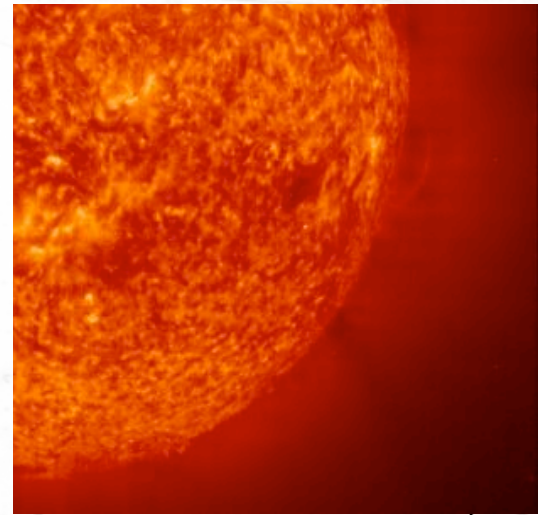


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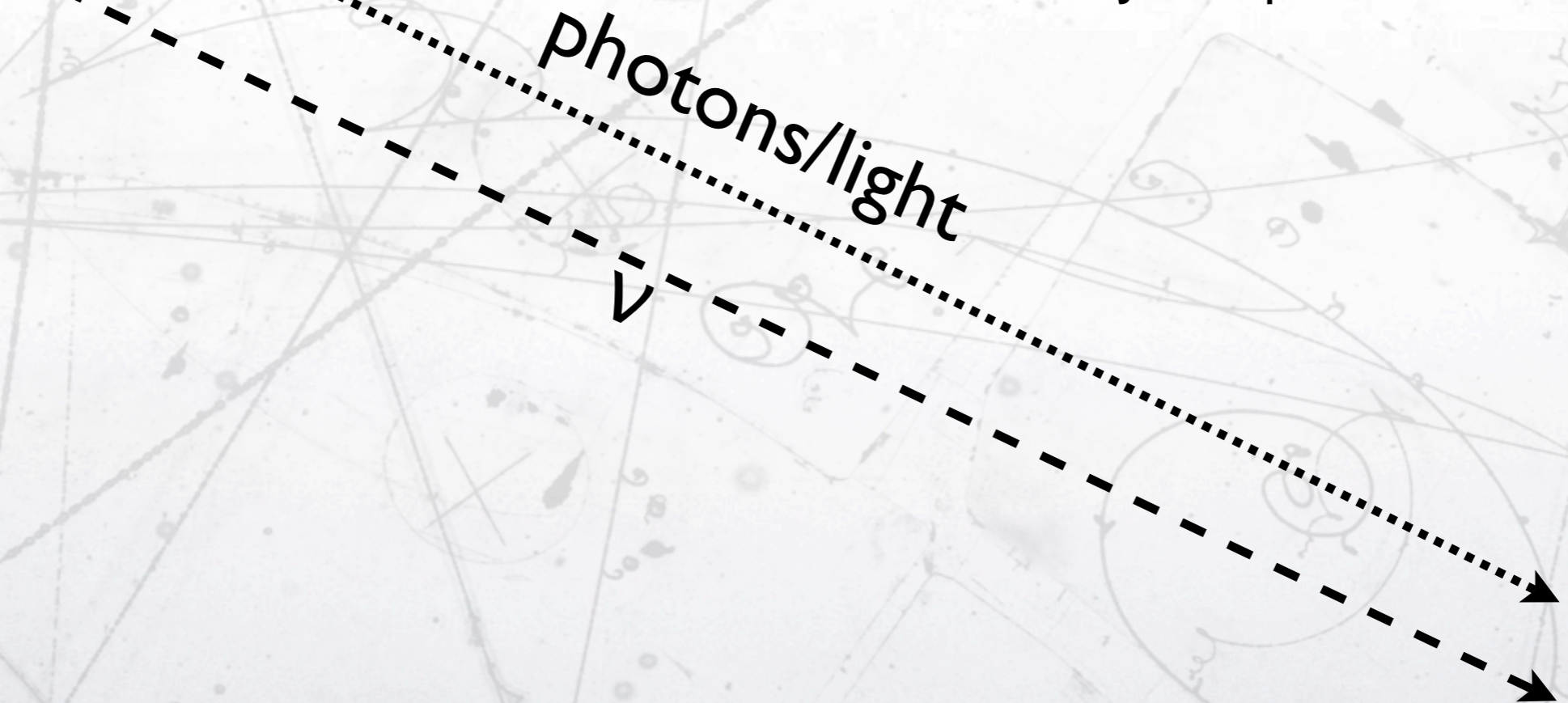


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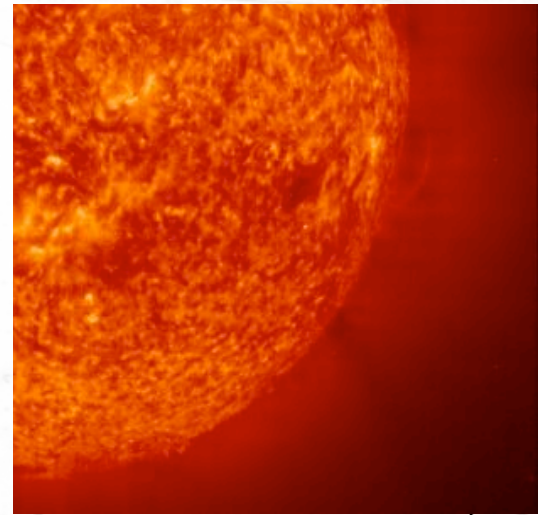
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- The sun produces  $2.06 \times 10^{12}$  Joules per neutrino.



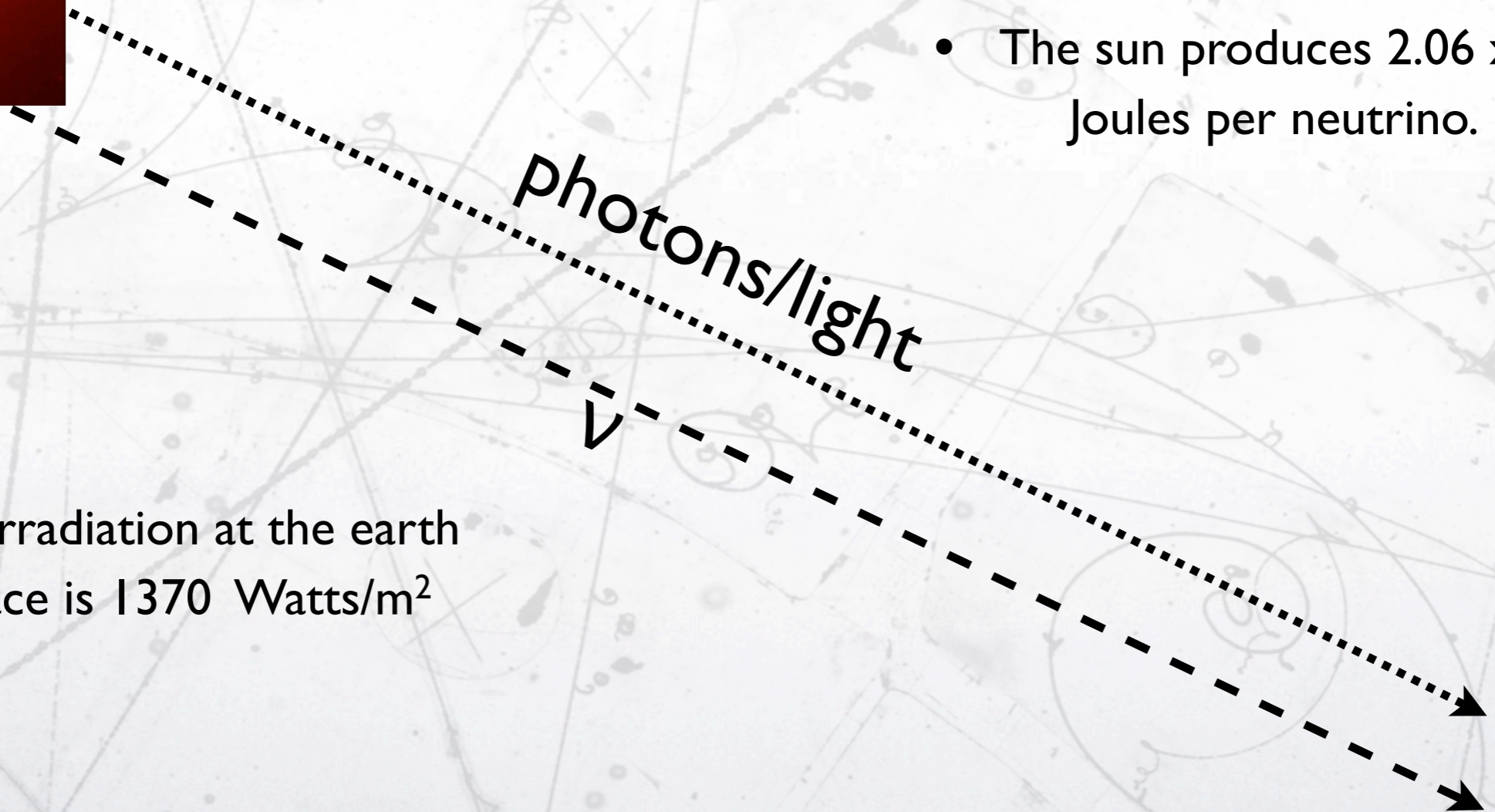


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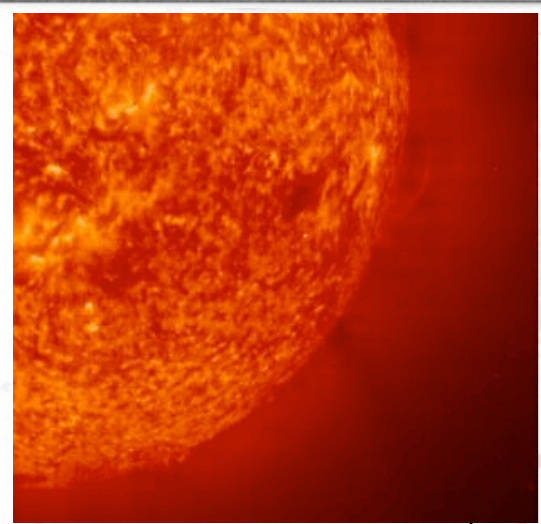


- The solar irradiation at the earth superface is 1370 Watts/m<sup>2</sup>



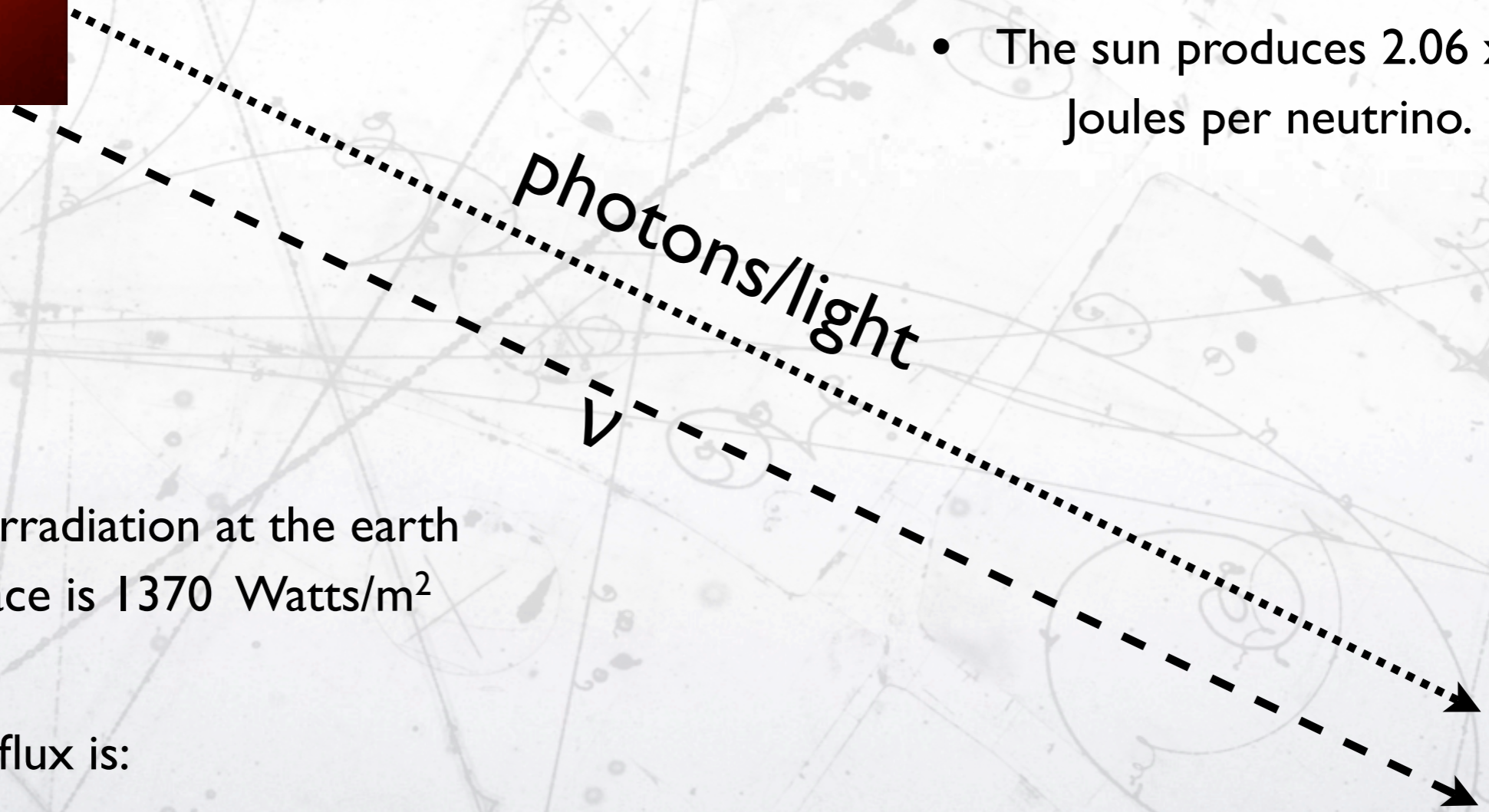


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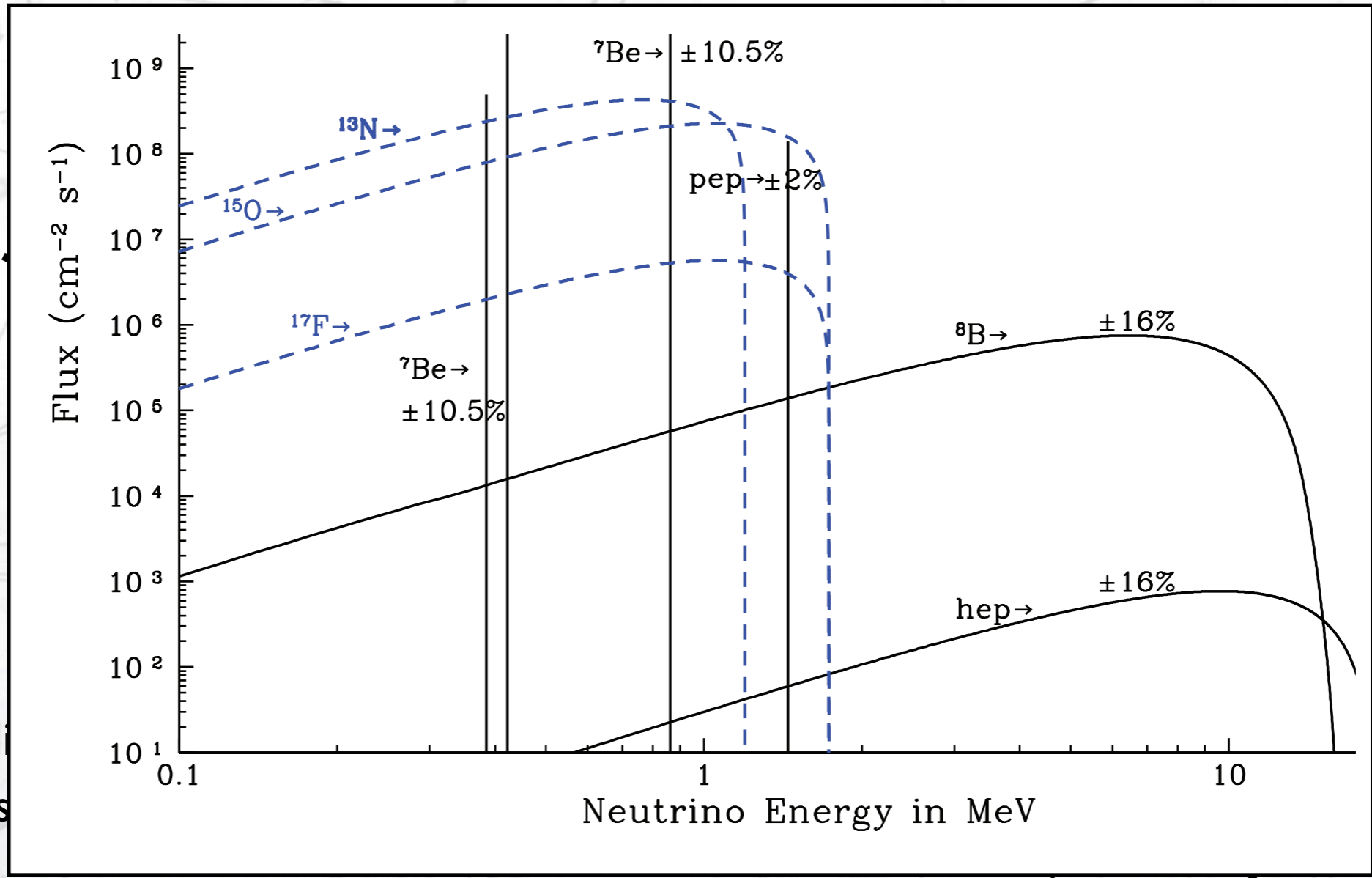
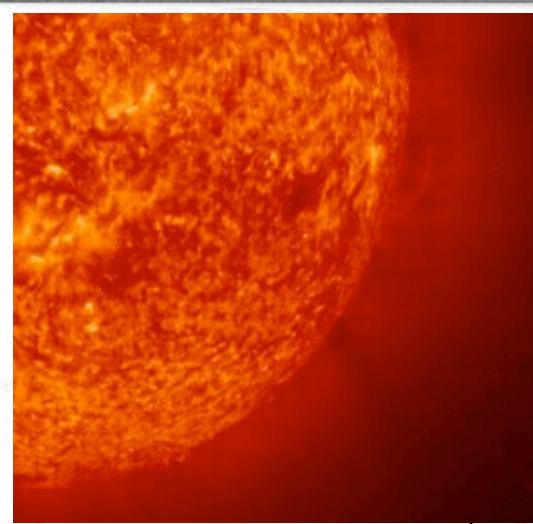


- The solar irradiation at the earth superface is 1370 Watts/m<sup>2</sup>
- Neutrino flux is:
  - $1370 / (2.06 \times 10^{-12}) / \text{m}^2 / \text{sec} = 6.65 \times 10^{10} / \text{cm}^2 / \text{sec}.$





# Solar neutrinos



- The solar irradiance at the Earth's surface is  $1370 \text{ W/m}^2$

- Neutrino flux is:

- $$1370 / (2.06 \times 10^{-12}) / \text{m}^2/\text{sec} = 6.65 \times 10^{10} / \text{cm}^2/\text{sec}.$$

The spectrum is known with 10% error

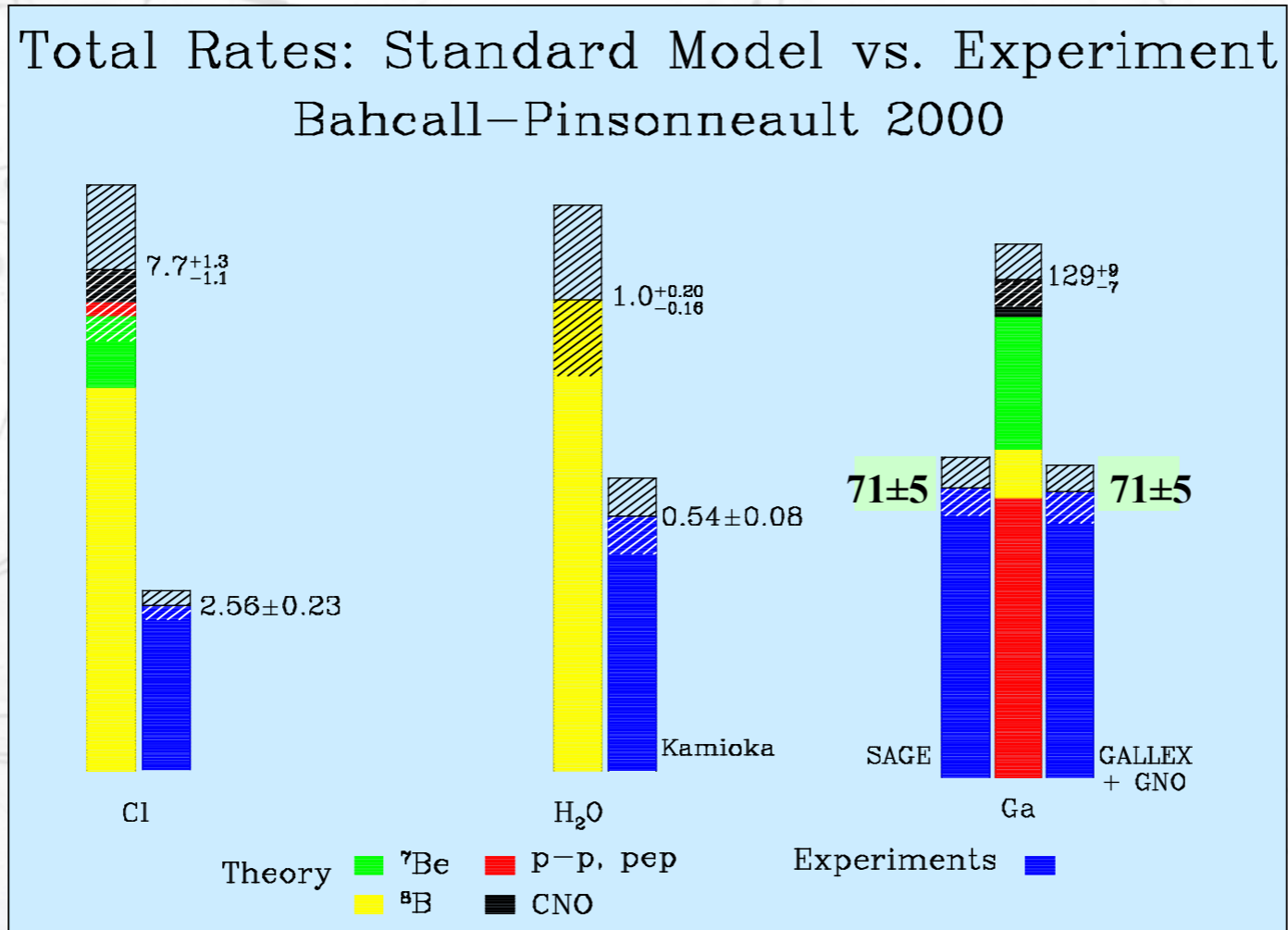




- The first experiments were based on radiochemical detection:
  - Chlorine:  $\nu_e {}^{37}\text{Cl} \rightarrow {}^{37}\text{Ar} e^-$  ( $E_\nu > 0.8$  MeV)
  - SAGE/Gallex/GNO:  $\nu_e {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} e^-$  ( $E_\nu > 0.2$  MeV)
- Later the water Cherenkov detector Kamiokande was added to the list with a threshold of  $\sim 6$  MeV.
  - Water Cherenkov added the possibility of online event recording and the determination of neutrino direction:
    - Reduced background, Day/Night and seasonal effects...



The experiments



- All of them detected neutrinos, but at a different rate than expected: solar model?, detector efficiencies?, neutrino deficit through oscillations?,...
- This disagreement was called for years “the solar neutrino problem”.



## The paradigm

- **Pontecorvo:** "Unfortunately, the weight of the various thermonuclear reactions in the sun, and the central temperature of the sun are insufficiently well known in order to allow a useful comparison of expected and observed solar neutrinos..."
- **Georgi & Luke:** "Most likely, the solar neutrino problem has nothing to do with particle physics. It is a great triumph that astrophysicists are able to predict the number of  $^8\text{B}$  neutrinos to within a factor of 2 or 3..."
- **Yang:** "I did not believe in neutrino oscillations even after Davis' painstaking work and Bahcall's careful analysis. The oscillations were, I believed, uncalled for."
- **Drell:** "... the success of the Standard Model was too dear to give up."

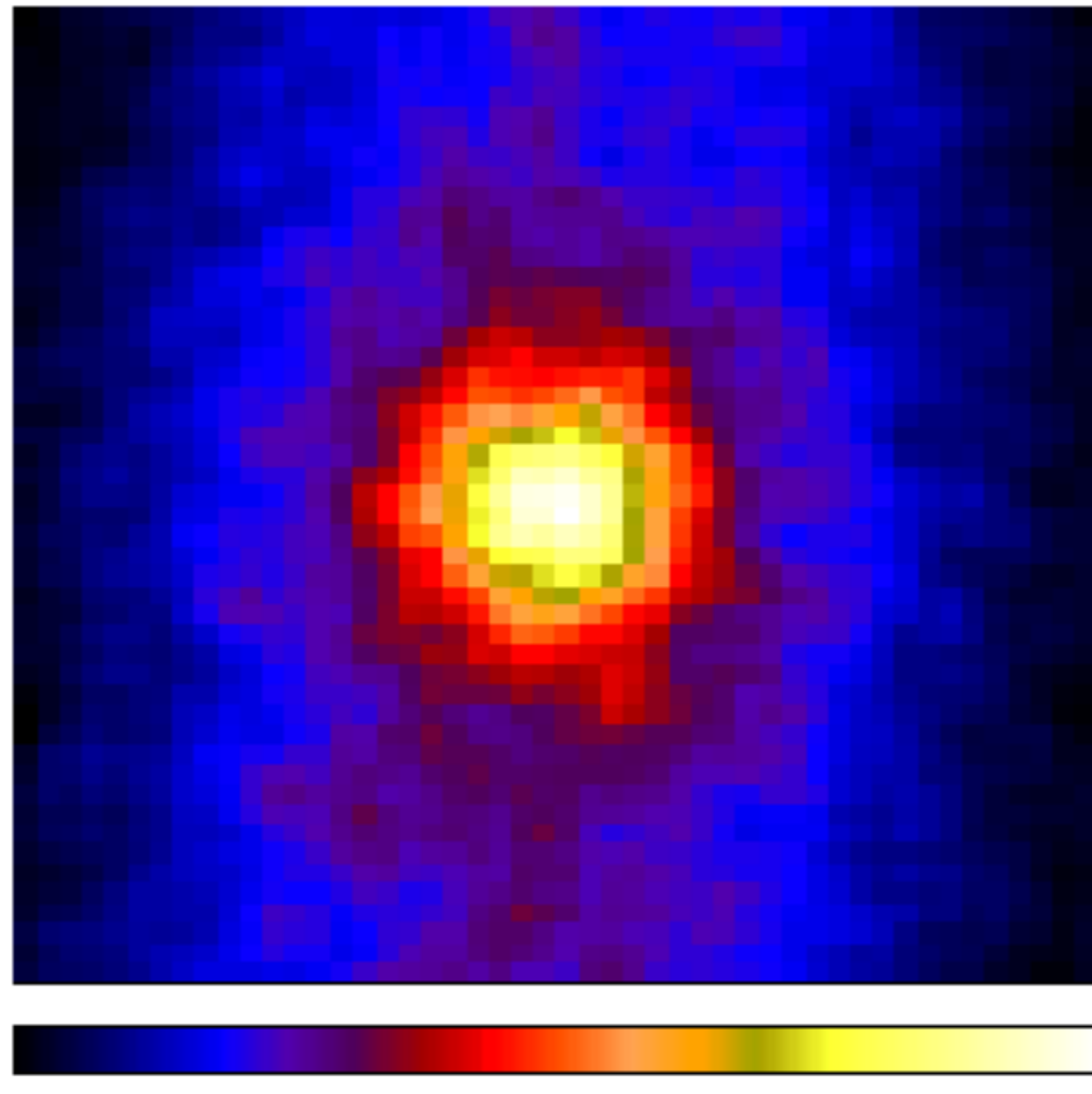




# $\nu$ from the sun ?



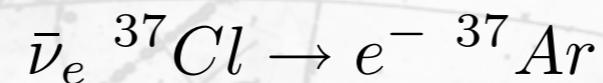
Picture of the sun taken with neutrinos by Super-Kamiokande.





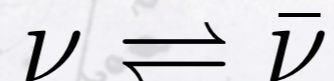
## Early ideas

- Bruno Pontecorvo proposed, back in 1957, that the lepton sector might show oscillation phenomena similar to that of the  $K^0$  meson. Neutrinos were neutral particles, and the lepton-hadron analogy was assumed.
- At that time Davis was doing experiments with anti-neutrinos from a reactor looking for the reaction:



As many other times the hints finally vanished.

- And observed some events !!!!!
- At that time only one neutrino especie was known and then the only option was to have oscillations (also similar to  $K^0$  system) was:



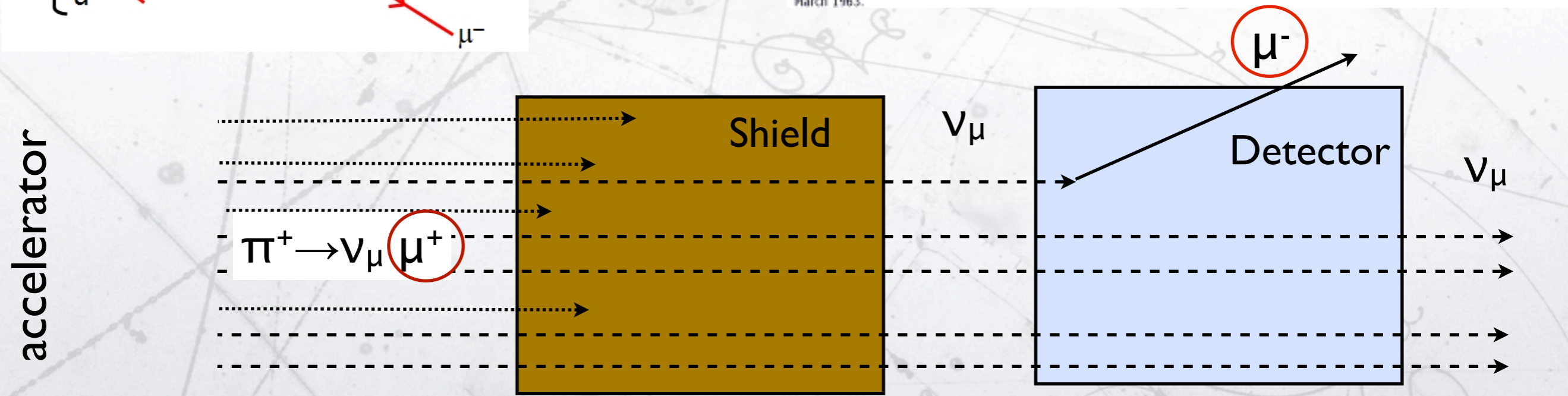
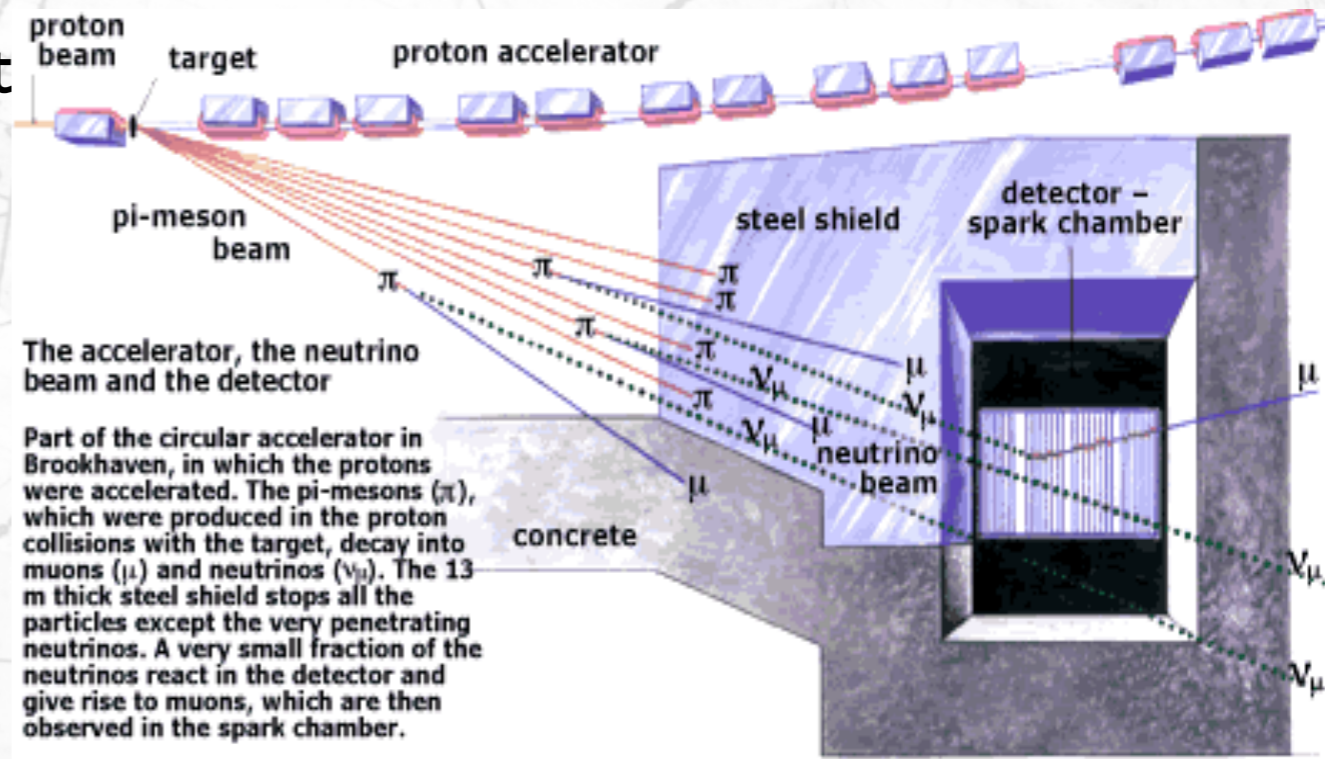
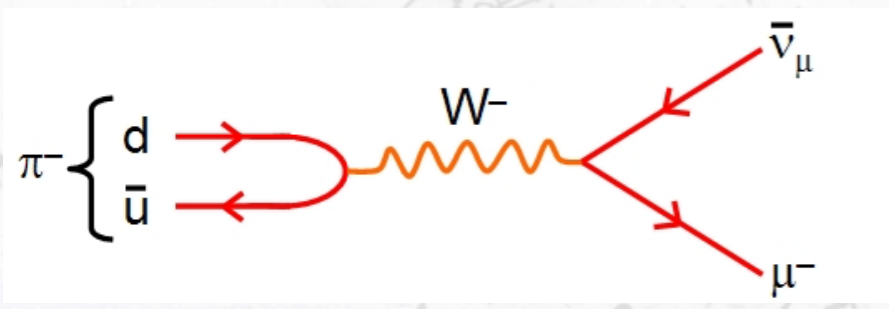
This is the valid reaction:  $\bar{\nu}_e \ ^{37}\text{Cl} \rightarrow e^+ \ ^{37}\text{S}$



# Muon neutrino discovery



- Muon neutrino was discovered in 1962 at Brookhaven using the new technology to accelerate protons to high energies.
- This is the same technology use today in neutrino experiments!



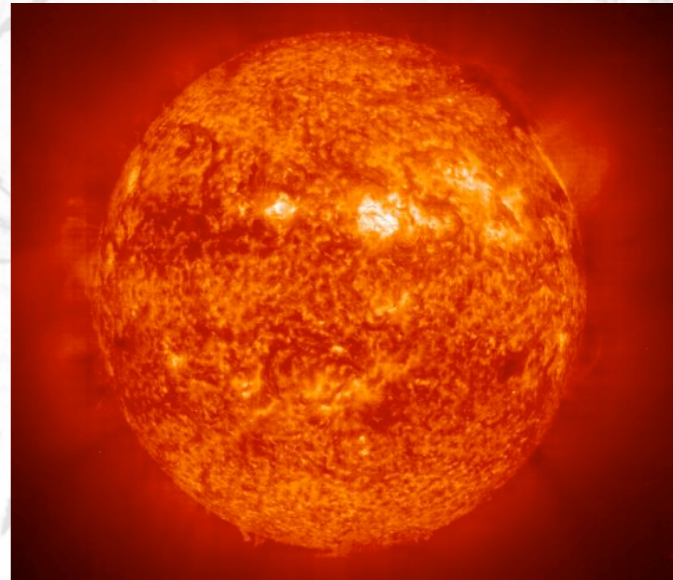


- After the  $\nu_\mu$  discovery at Brookhaven, Bruno Pontecorvo proposed the alternative model based on  $\nu_\mu \rightleftharpoons \nu_e$  oscillations.
- The model “only” required:
  - that neutrinos were massive.
  - mass eigenstates are different from flavour eigenstate.
- But, neutrinos were thought to be massless:
  - this was a mainly to avoid the need for “sterile” right handed neutrinos needed to form the Dirac mass term.

Theoretical prejudices!

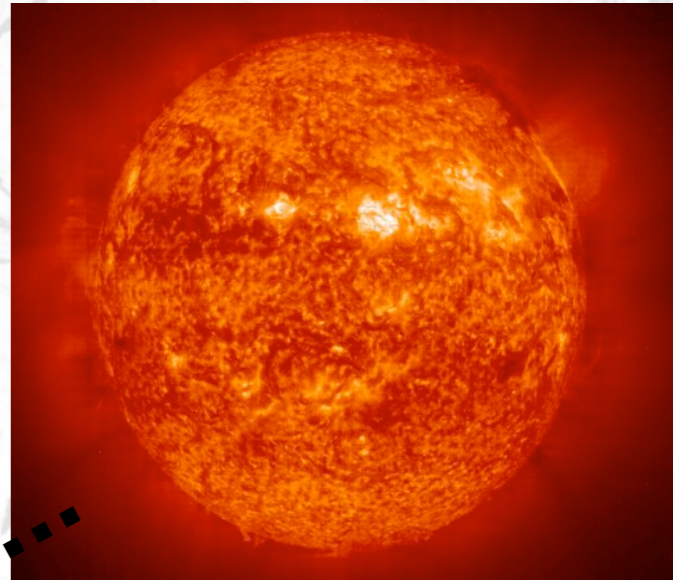


# Solar neutrinos & oscillations



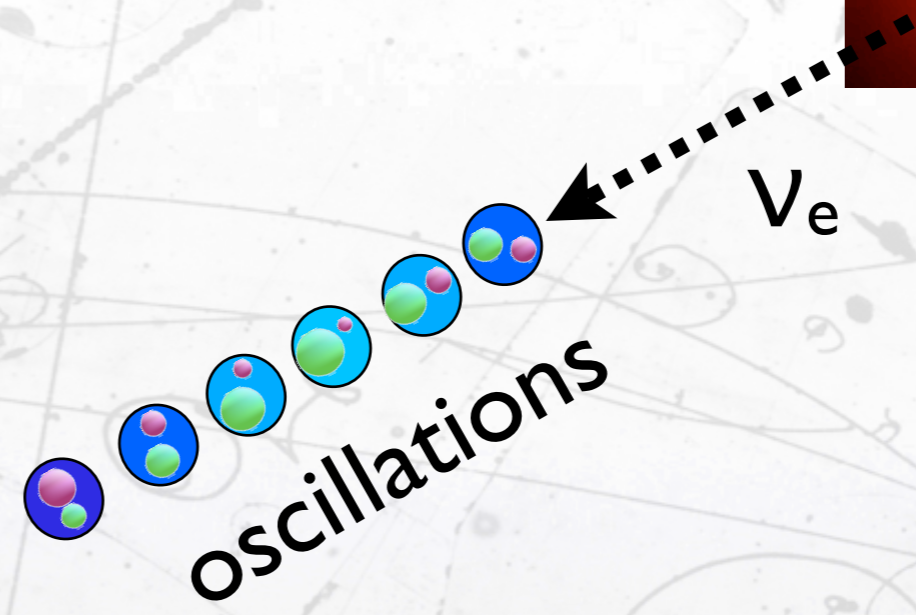
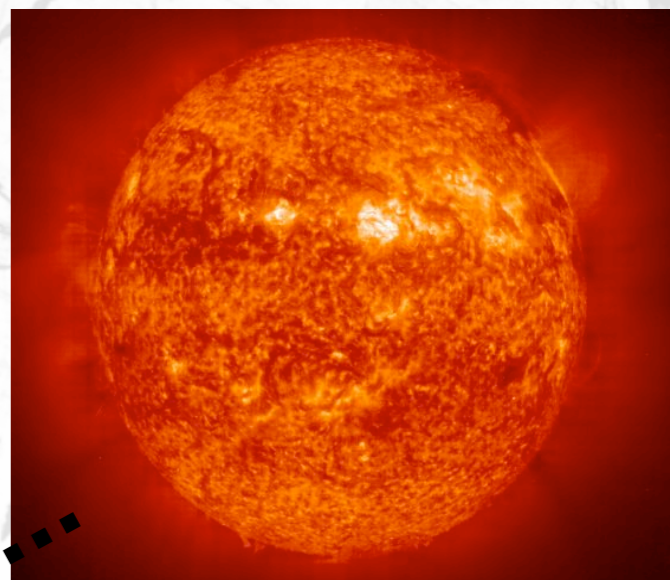


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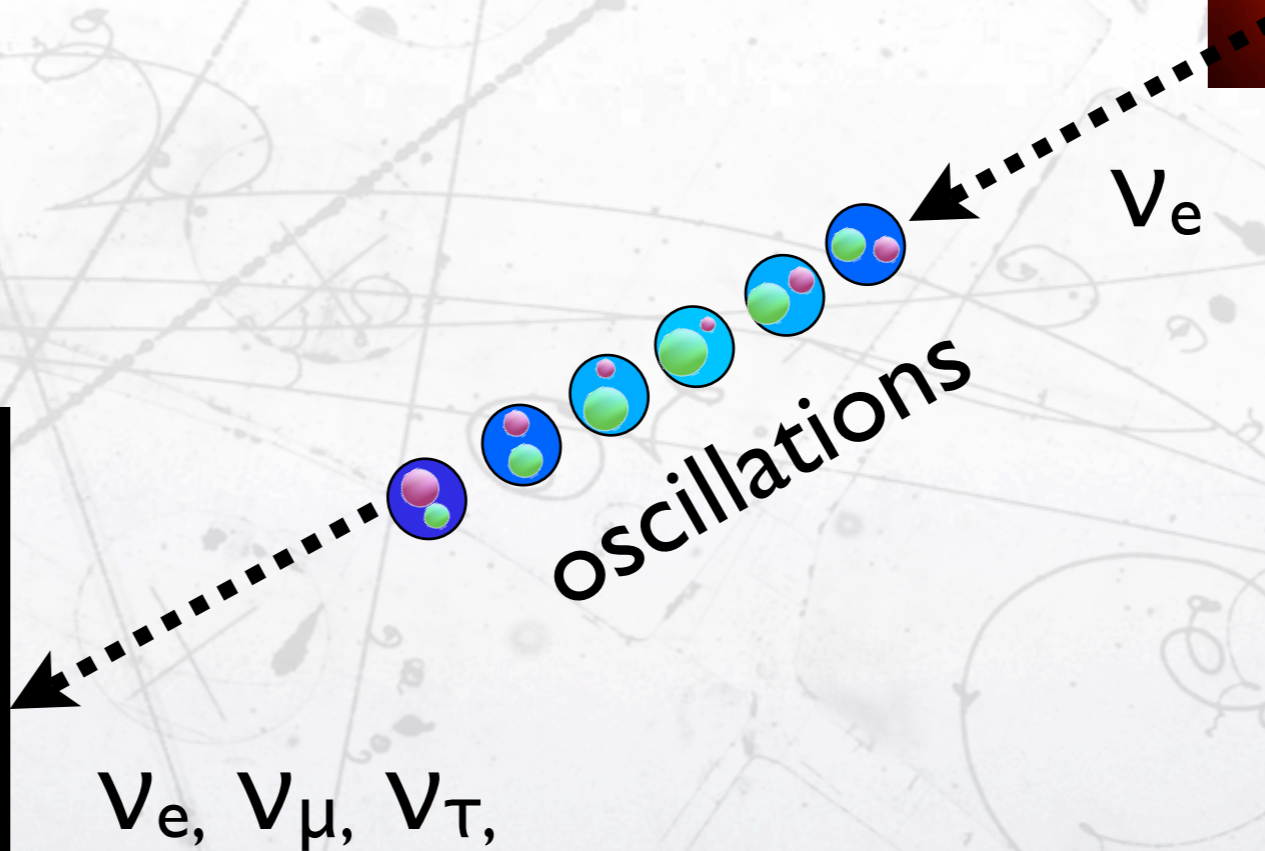
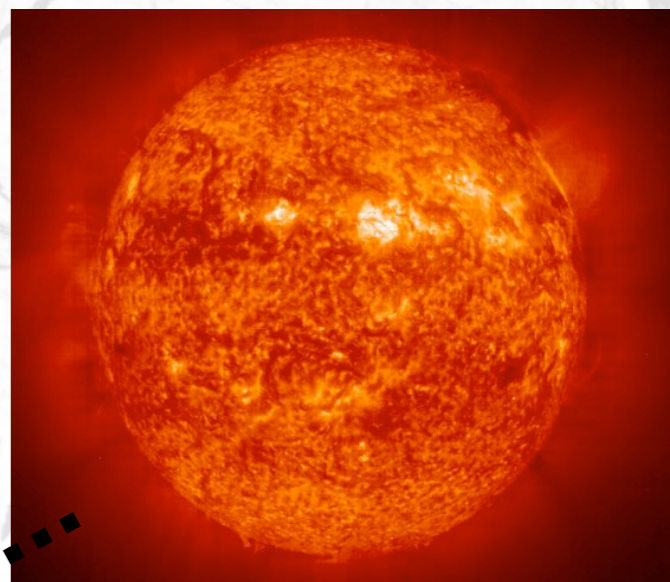


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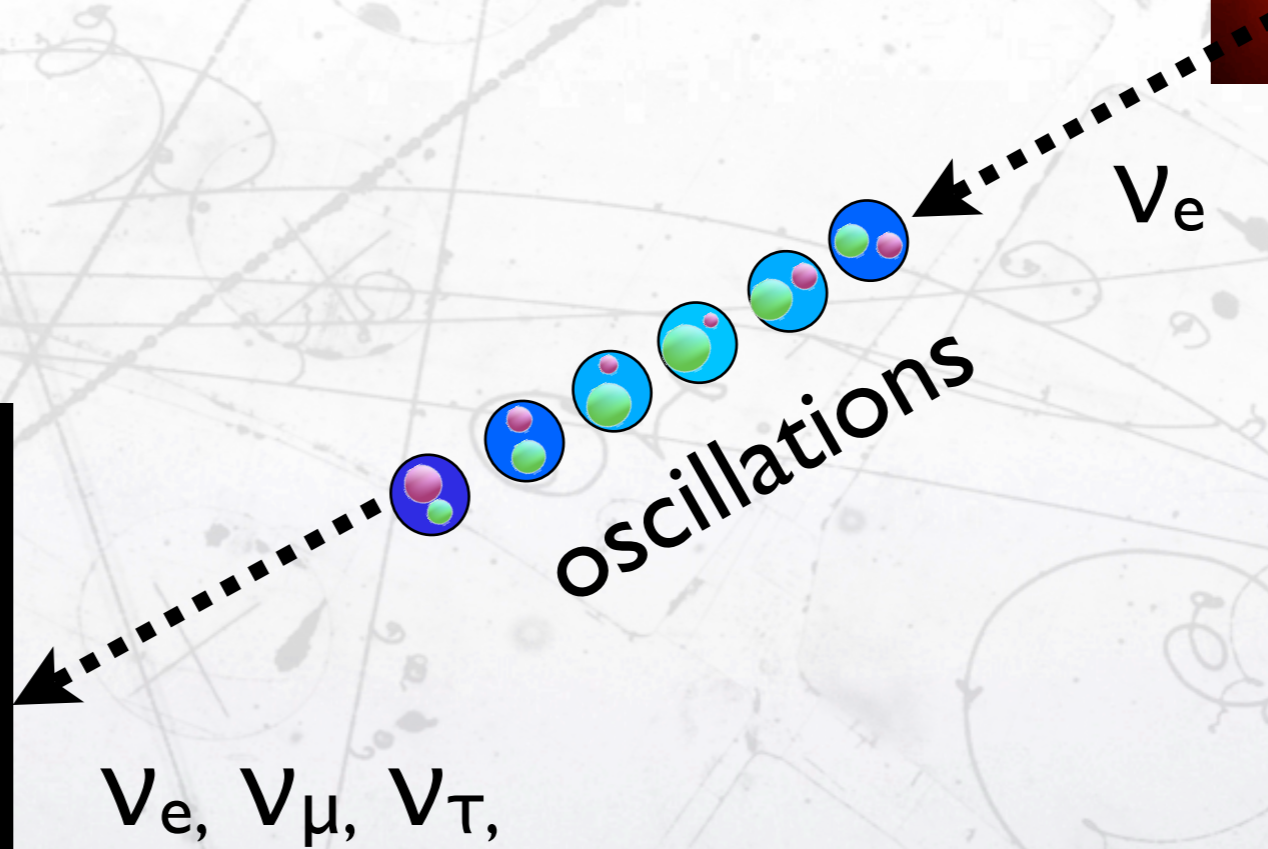
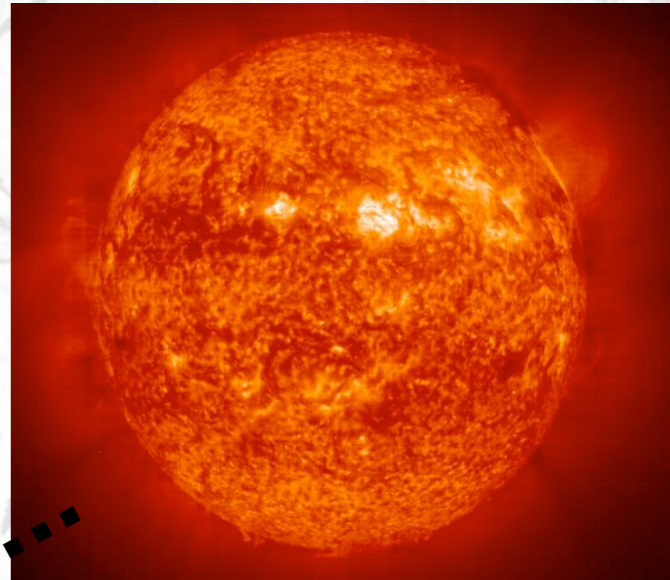




The oscillations do not change the number of neutrinos:

$$N_{\nu_e} + (N_{\nu_\mu} + N_{\nu_\tau}) = N^{\text{sol}}_{\nu_e}$$

But, not all of them are electron neutrinos.



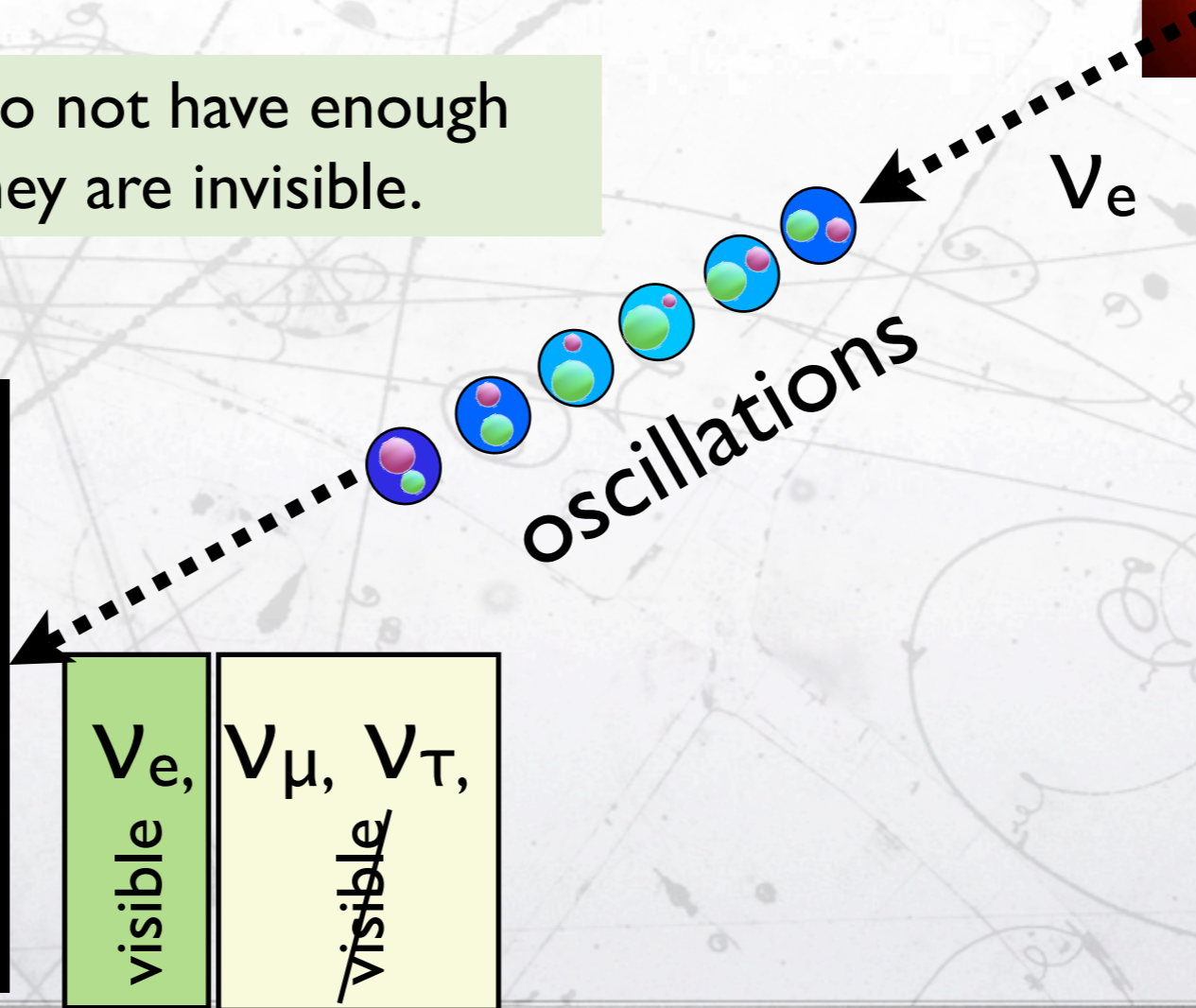
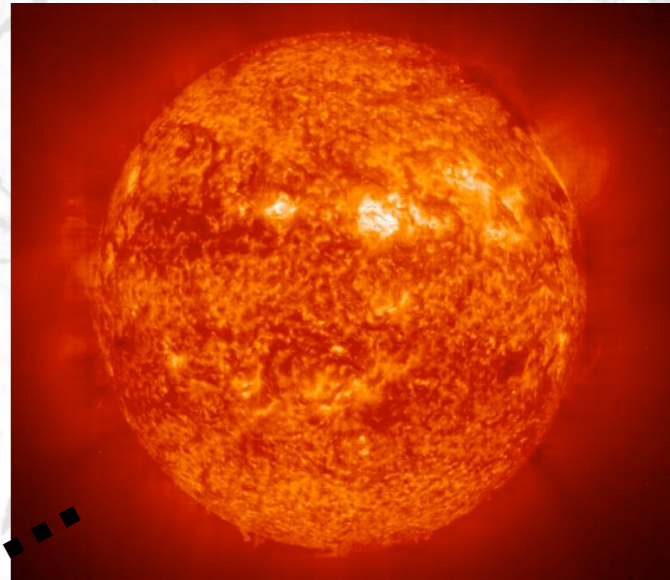


The oscillations do not change the number of neutrinos:

$$N_{\nu_e} + (N_{\nu_\mu} + N_{\nu_\tau}) = N^{\text{sol}}_{\nu_e}$$

But, not all of them are electron neutrinos.

Muon and tau neutrinos do not have enough mass to be detected → they are invisible.



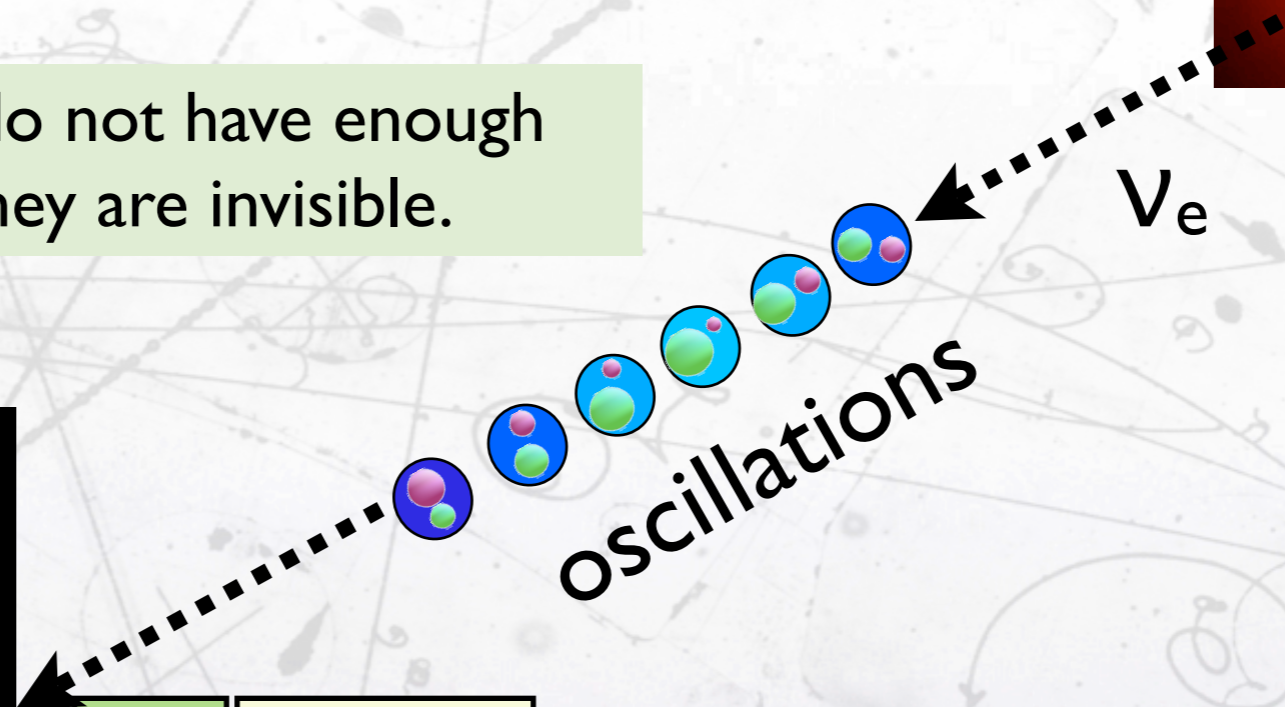
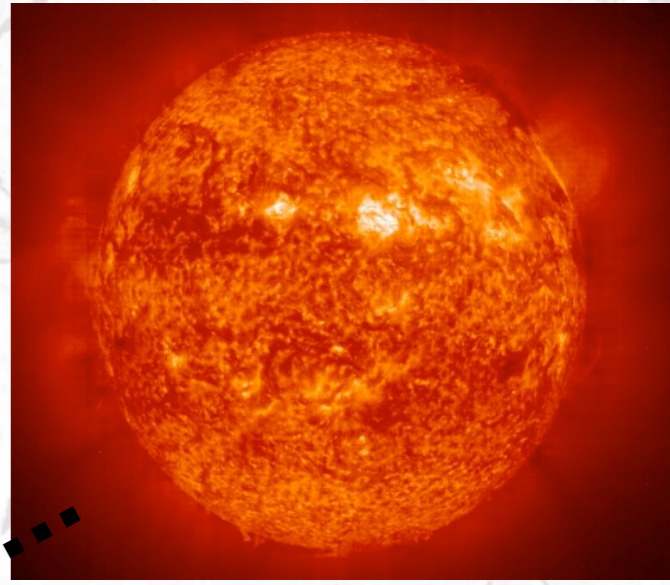
$\nu_e$ , visible	$\nu_\mu, \nu_\tau$ , <del>visible</del>
----------------------	---



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$\nu_e$ , visible	$\nu_\mu, \nu_\tau$ , <del>visible</del>
----------------------	---

At earth we see only the remaining fraction of neutrinos that are still electron type.



## The theory

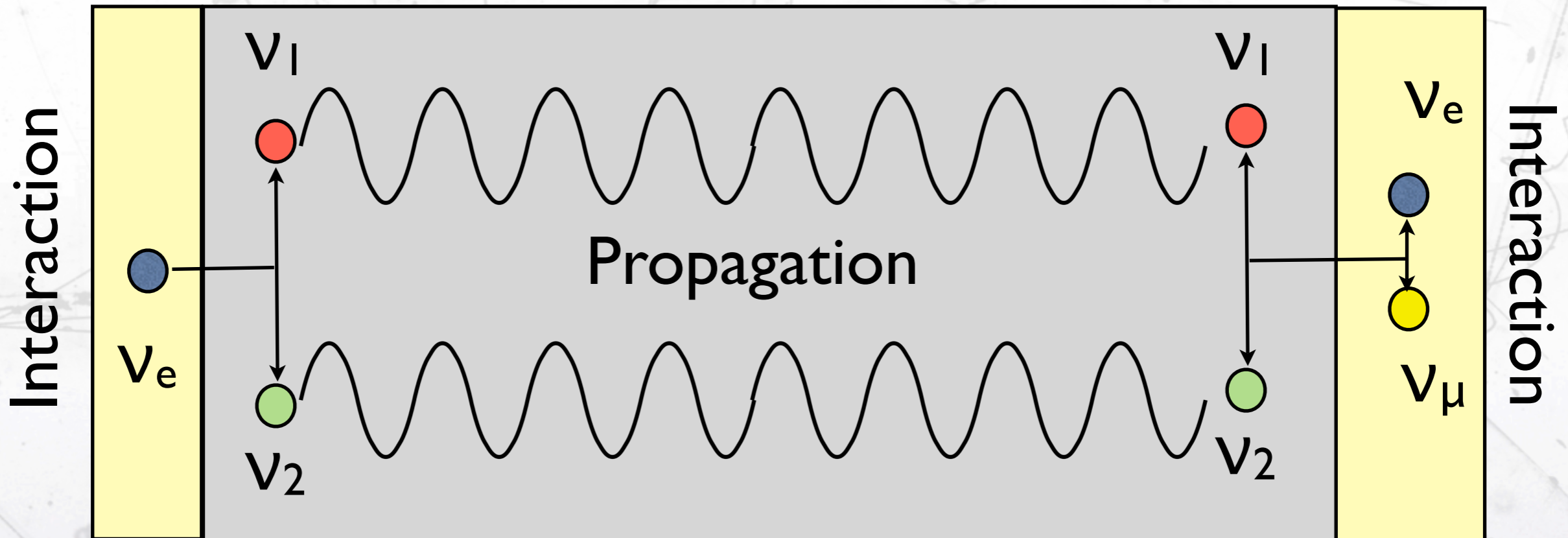
- The first phenomenological neutrino oscillation model was elaborated by Gribov and Pontecorvo in 1969.
- The model assumed that:
  - neutrinos have mass, albeit a very small one.
  - neutrinos interact as  $\nu_e$  or  $\nu_\mu$  (neutrino flavour).
  - the eigenstates of flavour and mass(Lorentz) are not the same. They can be related via a linear combination or rotation between the two bases.

$$\begin{aligned}
 |\nu_e\rangle &= \cos\theta|\nu_1\rangle + \sin\theta|\nu_2\rangle \\
 |\nu_\mu\rangle &= -\sin\theta|\nu_1\rangle + \cos\theta|\nu_2\rangle
 \end{aligned}$$



The theory

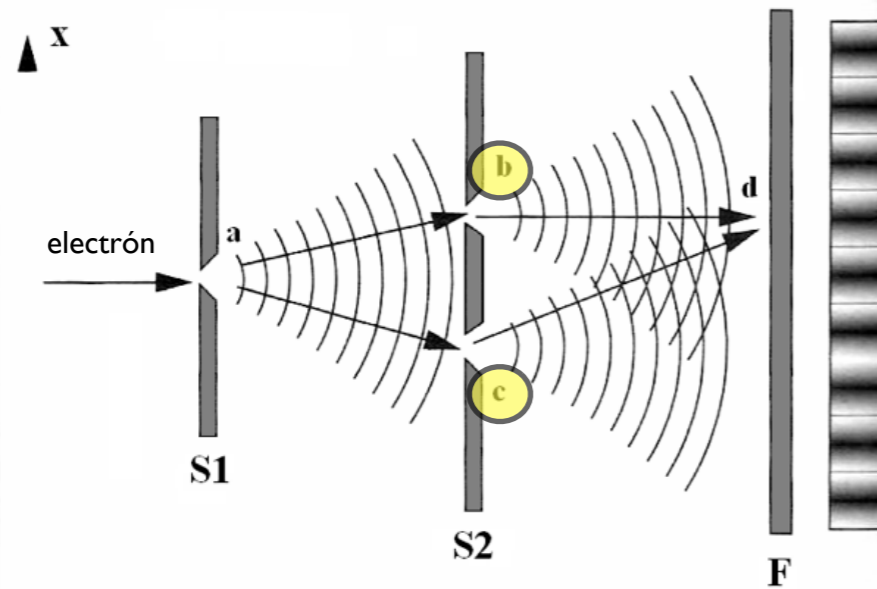
- Neutrinos are produced always as a flavour neutrino but they propagate in vacuum as mass eigenstates.



- If neutrinos 1 & 2 propagate at different speeds (mass) and they keep the coherence at the interaction point the proportions are changed and it might appear other neutrino flavour.



Neutrino oscillations is similar to the double slit experiment.



Each slit is equivalent to a mass state in the neutrino case. It is a different path to go from emission to detection.

Particles go from source to detector through both slits.

Neutrinos fly through both mass states at the same time.

Every slit gives a different path length → interference

Every mass state gives a different path length (phase) → interference



## The theory

- When we produce electron neutrino:

$$|\nu_e\rangle = \cos\theta|\nu_1\rangle + \sin\theta|\nu_2\rangle$$

- Neutrinos are transported in vacuum following the Schrödinger equation in vacuum:

$$i\hbar\frac{\partial\nu}{\partial t} = H\nu = E\nu = \sqrt{m_\nu^2 + p^2}\nu$$

- $m_\nu \ll p$ :

$$i\hbar\frac{\partial\nu}{\partial t} = \left(p + \frac{m_\nu^2}{2p}\right)\nu$$

$$\nu(t) = e^{i\left(p + \frac{m_\nu^2}{2p\hbar}\right)t}\nu(0)$$



- If we produce a  $\nu_e$ , after some time the state is:

$$|\nu_e; t\rangle = \cos\theta e^{i(p + \frac{m_1^2}{2p})\frac{t}{\hbar}} |\nu_1; 0\rangle + \sin\theta e^{i(p + \frac{m_2^2}{2p})\frac{t}{\hbar}} |\nu_2; 0\rangle = e^{i(p + \frac{m_1^2}{2p})\frac{t}{\hbar}} (\cos\theta |\nu_1; 0\rangle + \sin\theta e^{i\frac{m_2^2 - m_1^2}{2p}\frac{t}{\hbar}} |\nu_2; 0\rangle)$$

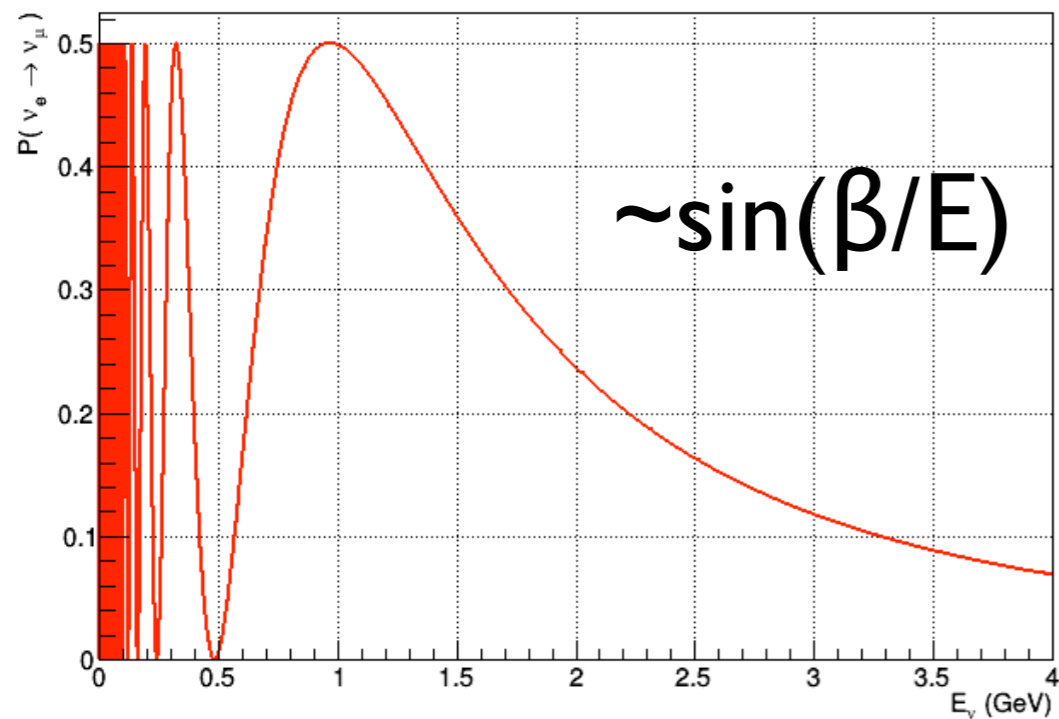
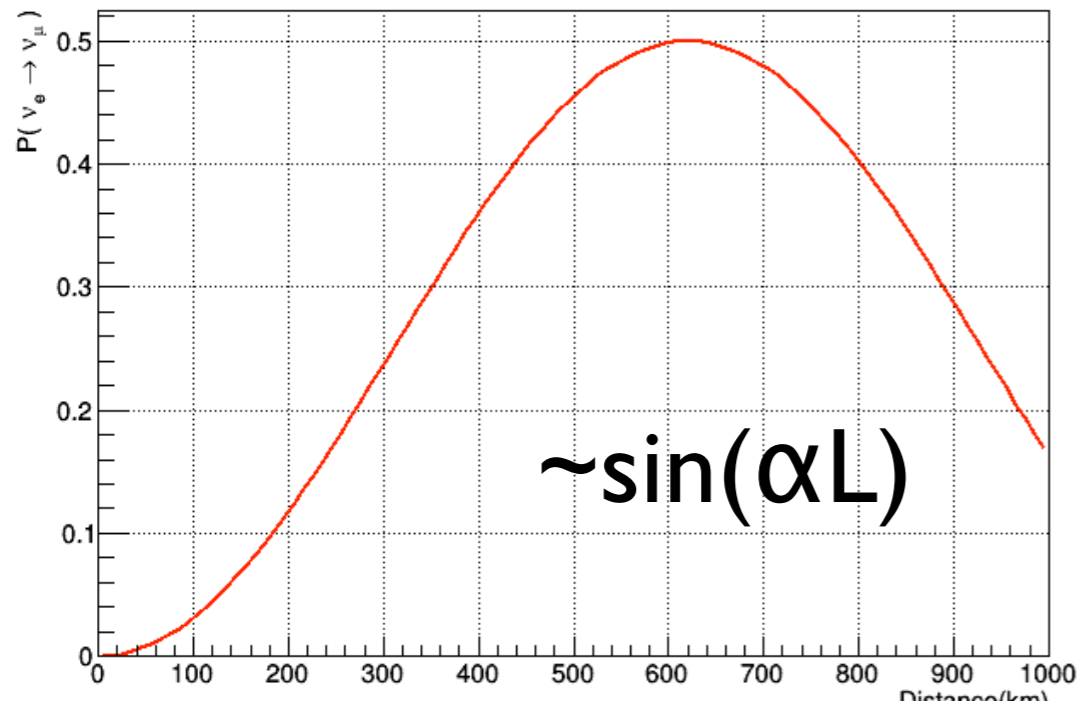
- The probability of getting a  $\nu_\mu$  at the interaction is then:

$$\begin{aligned} |\langle \nu_\mu | \nu_e; t \rangle|^2 &= |-\cos\theta \sin\theta \langle \nu_1 | \nu_1; 0 \rangle + \sin\theta \cos\theta e^{i\frac{m_2^2 - m_1^2}{2p}\frac{t}{\hbar}} \langle \nu_2 | \nu_2; 0 \rangle|^2 \\ &= \sin^2\frac{\theta}{2} \sin^2\frac{m_2^2 - m_1^2}{4p}\frac{t}{\hbar} = \sin^2\frac{\theta}{2} \sin^2 1.267 \frac{\Delta m^2 L}{E} \frac{\text{GeV}}{\text{eV}^2 \text{km}} \end{aligned}$$

- Flavour-lepton number is not conserved!. Opens the possibility for flavour violation in lepton decay & production.



# Neutrino Oscillation



$$\theta = \pi/2$$

$$\Delta m^2 = 2. \times 10^{-3} \text{ eV}^2$$

$$| \langle \nu_\mu | \nu_e; t \rangle |^2 = \sin^2 \frac{\theta}{2} \sin^2 1.267 \frac{\Delta m^2 L}{E} \frac{\text{GeV}}{\text{eV}^2 \text{ km}}$$

Oscillations are seen as  
change of  $\nu$  flavour  
composition as function of:

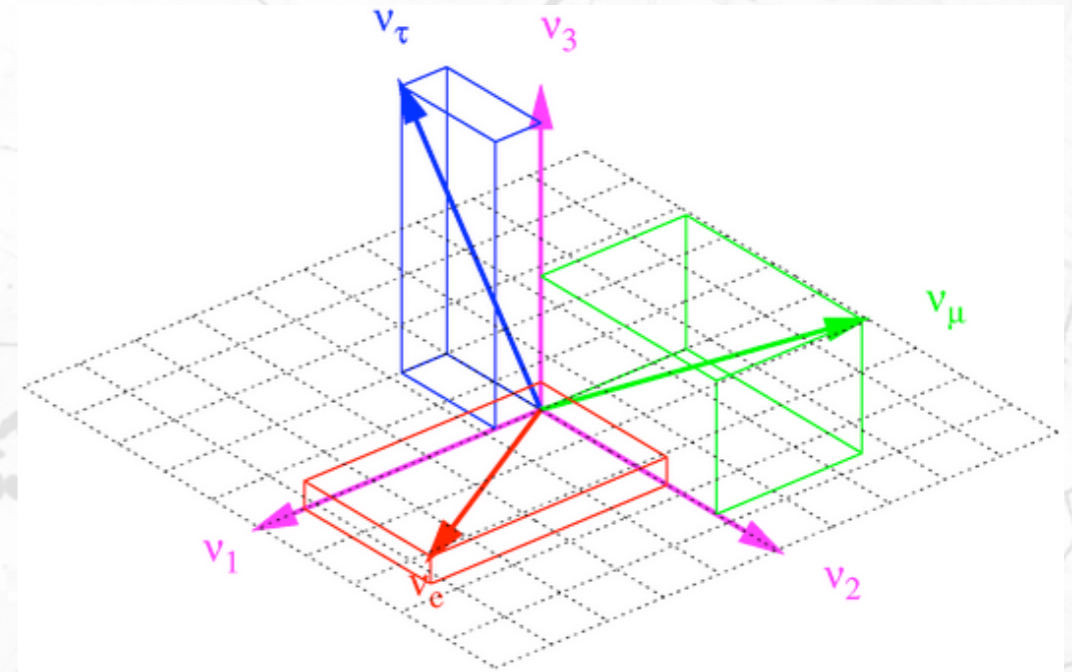
**Energy**  
**Distance**





The theory

$$\begin{pmatrix} \nu_e & \nu_\mu & \nu_\tau \end{pmatrix} = U_{PNMS} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



$$U_{PNMS} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & \sin \theta_{13} e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -\sin \theta_{13} e^{i\delta_{CP}} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{21} & \sin \theta_{21} & -\sin \theta_{21} \\ 0 & \cos \theta_{21} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- With 3 $\nu$ , there are 3 angles and 1 imaginary phase:
- The phase allows for CP violation similar to the quark sector.
- There are also 2 values of  $\Delta m^2$ , traditionally  $\Delta m^2_{12}$  &  $\Delta m^2_{31}$ .

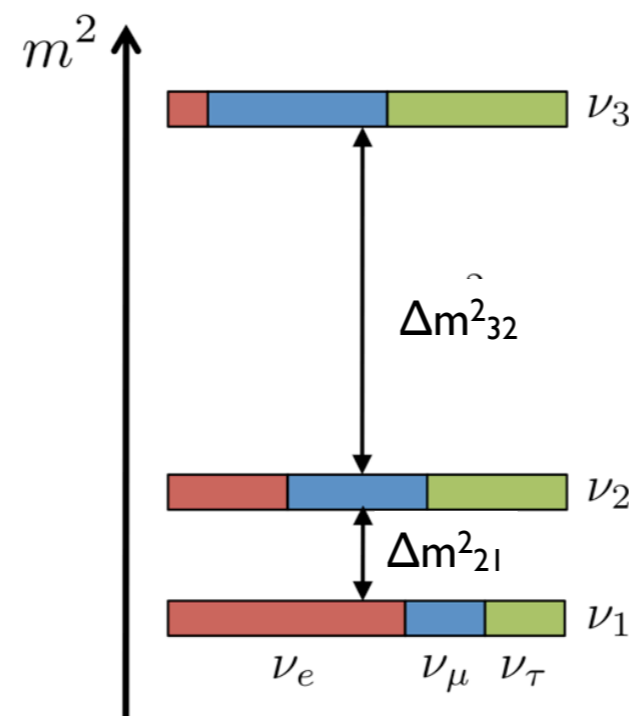


- $\nu$  oscillation is an interference phenomenon:
- We can't measure the absolute neutrino mass, only differences.
- $\nu$  mass levels do not need to follow the ones of the "heavy" leptons.

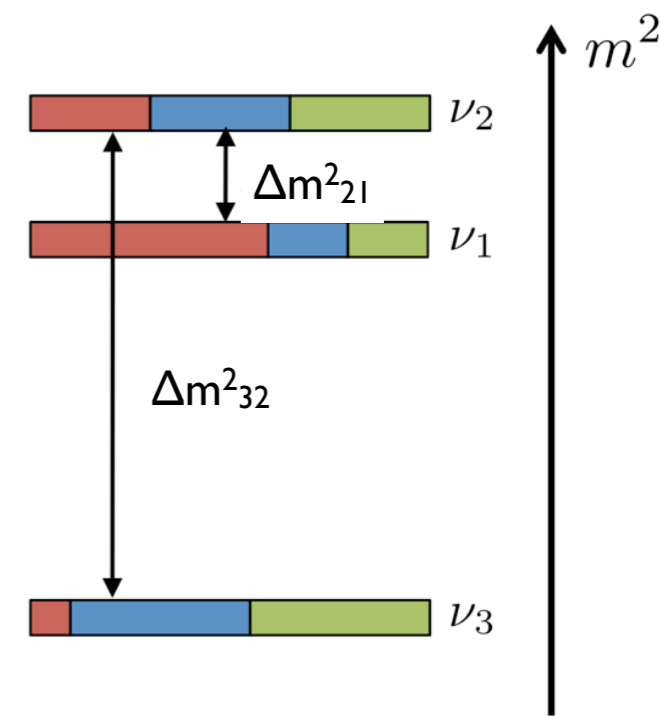
### Definition

$\nu_1$  is the largest component of  $\nu_e$   
 $\nu_2$  is the largest component of  $\nu_\mu$   
 $\nu_3$  is the largest component of  $\nu_\tau$

normal hierarchy (NH)

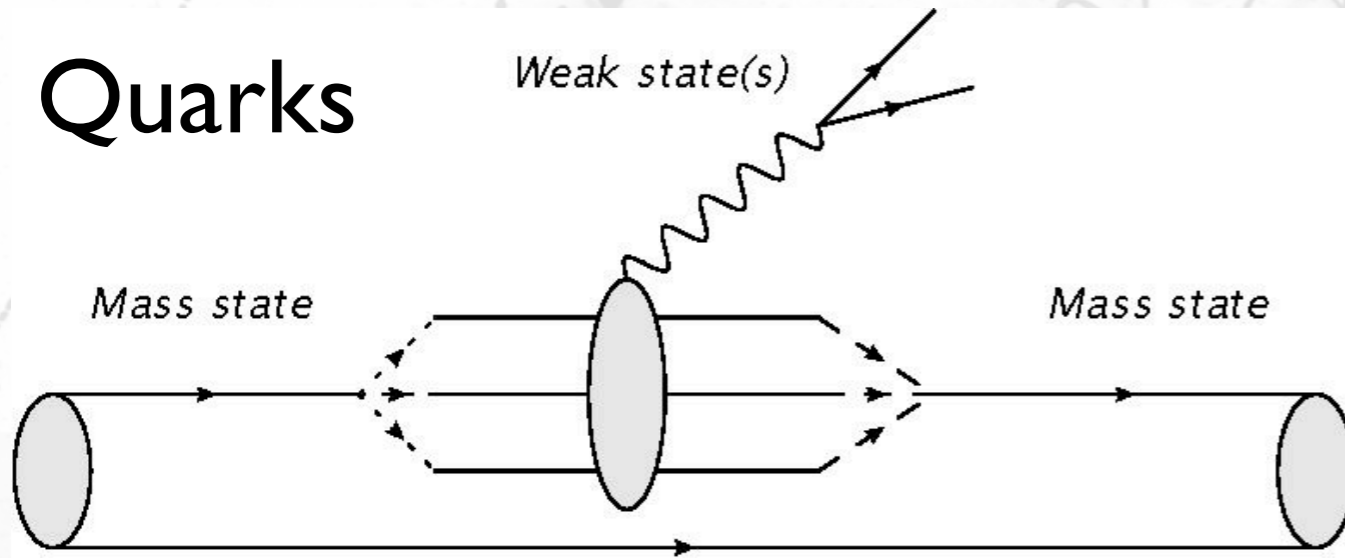


inverted hierarchy (IH)

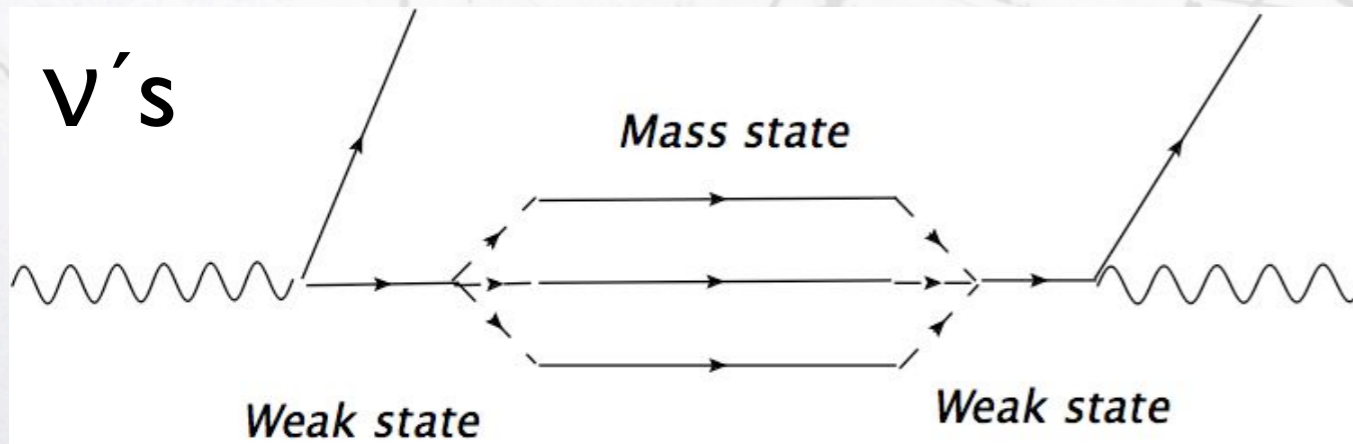




## Quarks



## $\nu$ 's



## Quark and neutrino mixing are the same phenomena!

- Quarks & neutrinos exist in matter and vacuum as mass states.
- In quark mixing, the quark is at the mass state at the initial and final state.
- In neutrino oscillations, the mass state are intermediate states, initial and final are flavour states.
- There are cases where the neutrino behaves “as the quarks do”: i.e. lepton flavour violation in decays.

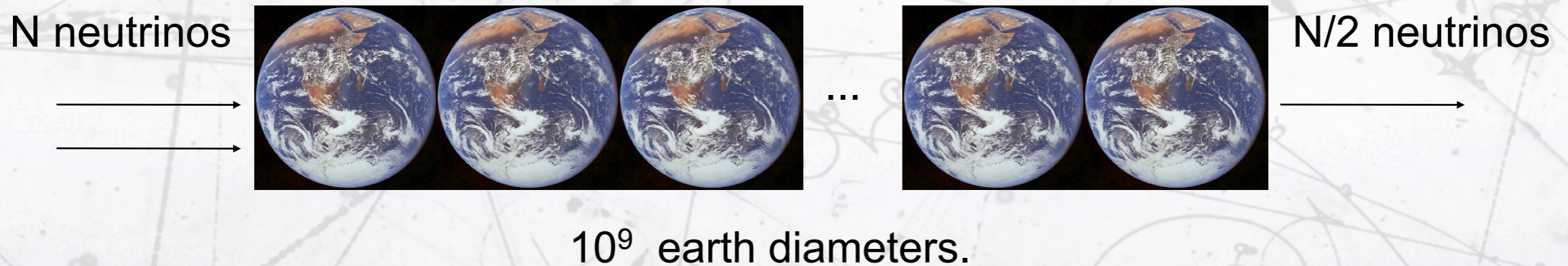


## Back to experiments

- How to unveil the “solar neutrino” problem?
  - It was not statistics or systematics, repeating experiments won't help.
  - measure the total neutrino flux (3 flavours) from the Sun (SNO).
  - produce a neutrino flux that is calculable. (Kamland).
- In parallel, search in the  $\nu_\mu$  sector for equivalent phenomena (atmospheric neutrinos & SuperKamikande).



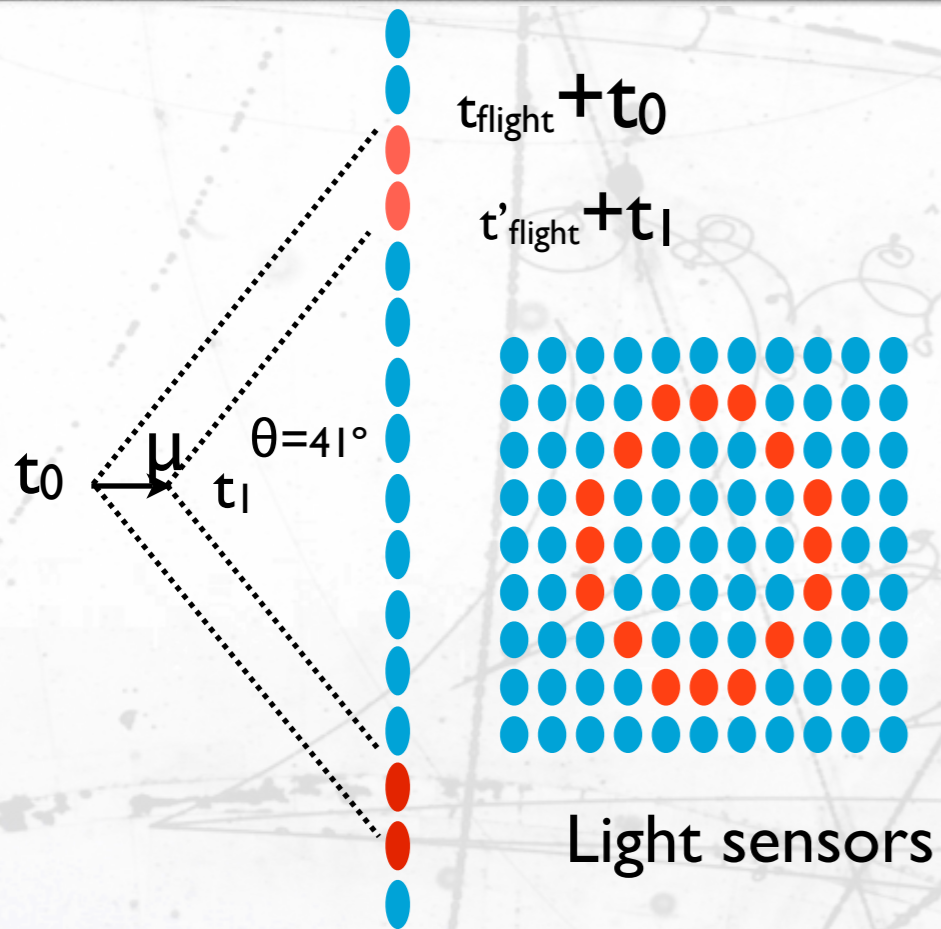
- Neutrinos have a very low probability (weak force) to interact with matter.
- neutrinos of 1 GeV can cross  $10^9$  earth diameters without interaction.



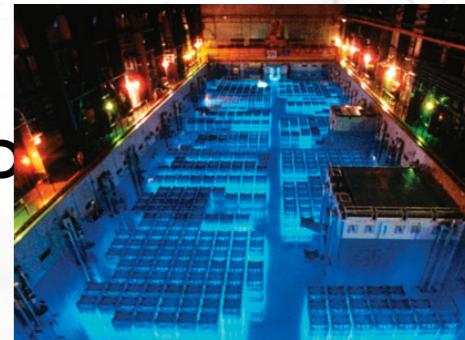
- We need very large neutrino fluxes ( $\sim 10^{20}$ ) and detectors (hundreds of Tons) to detect a handful of neutrinos.



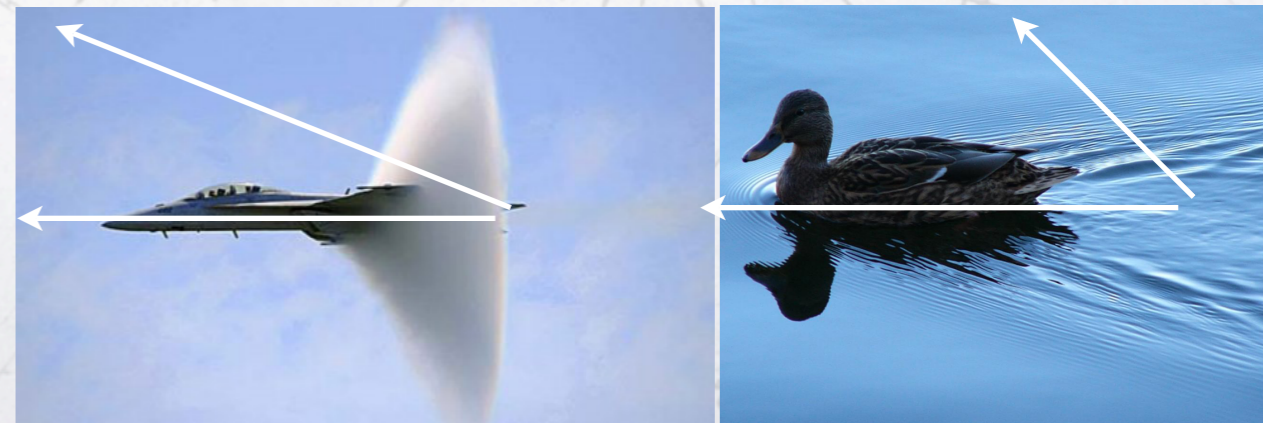
# Cerenkov & big detectors



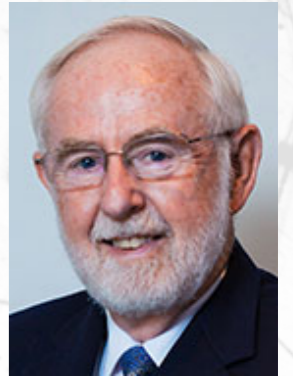
- When charged particles travels in a material faster than the speed of light in this material emits ultraviolet and blue light.
- This light forms a shock wave, so it remembers the particle direction.
- In water the light is emitted in a 45° cone around the particle direction.



- Shock waves are visible in other areas of physics.







# SNO

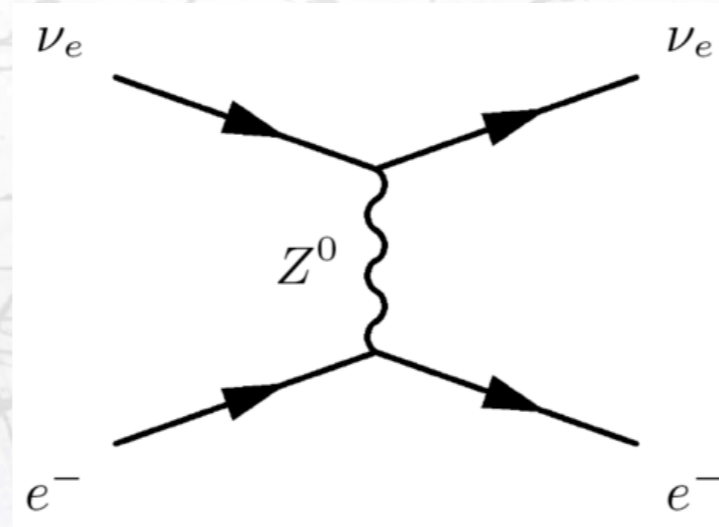
## The solution to the solar neutrino problem

$$\Theta_{12} \text{ \& \ } \Delta m^2_{12}$$



## SNO experimental concept.

- SNO tried to measure the total flux of solar neutrinos.
- Neutral currents do not produce heavy leptons, only neutrinos. There is no energy limit in the reaction:

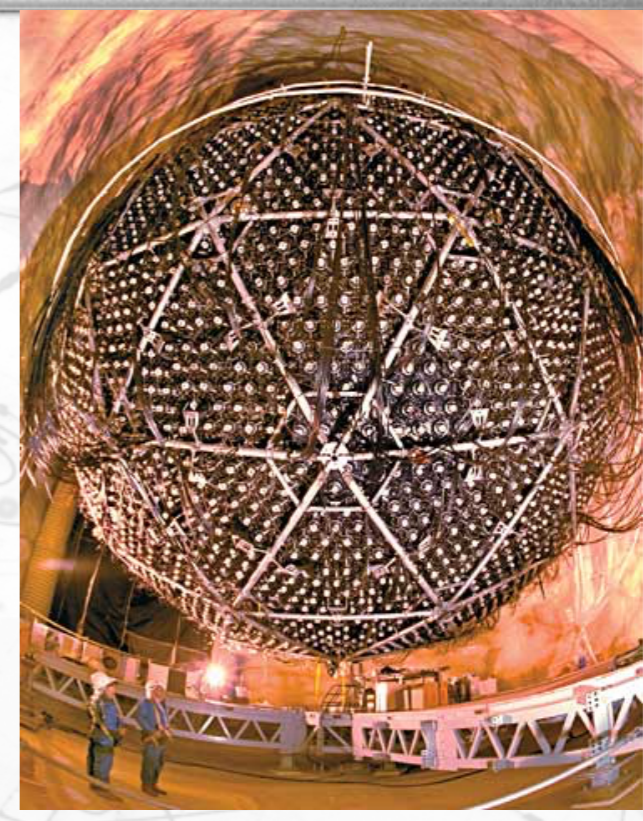
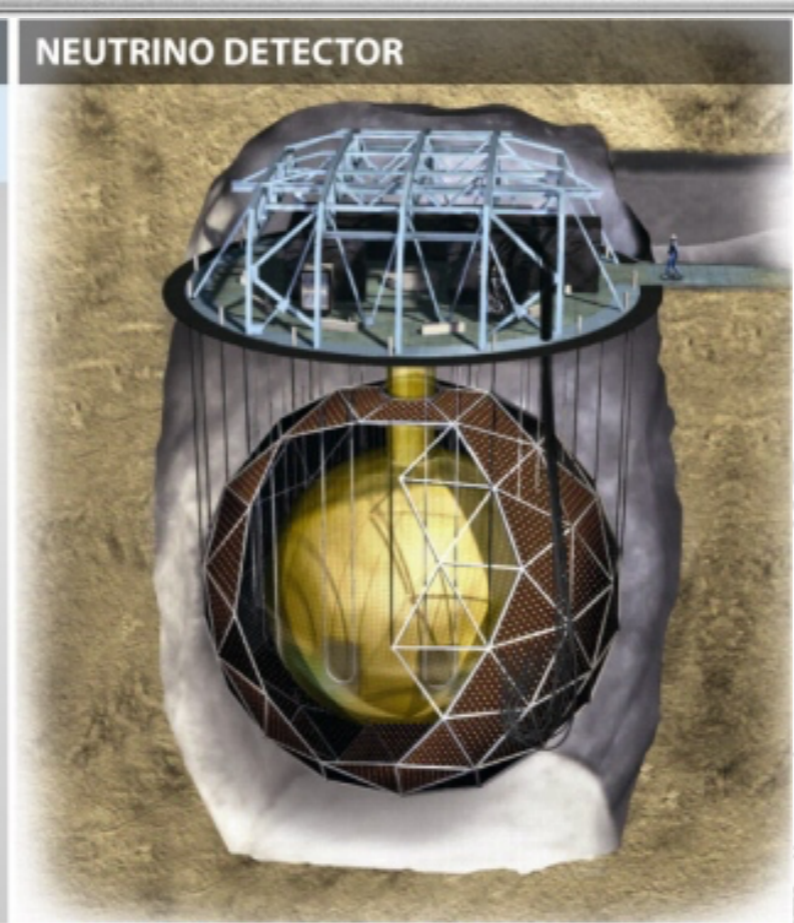
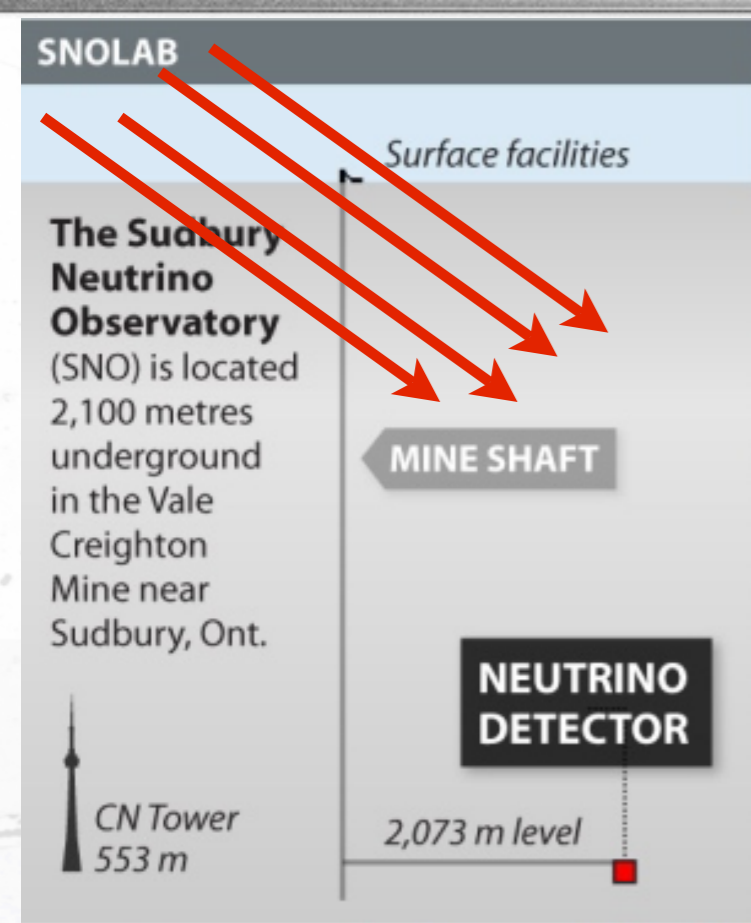


90.2 GeV	80.4 GeV
0	$\pm 1$
<b>Z<sup>0</sup></b>	<b>W<sup>±</sup></b>
Weak force	Weak force

- Neutral currents do not distinguish the flavour of the neutrino, but the integrated flux:

$$N_{\nu}^{neutral\ current} \approx N_{\nu_e} + N_{\nu_{\mu}} + N_{\nu_{\tau}} = N_{\nu_e}^{sun}$$





Filled with heavy water.  
In heavy water the hydrogen is replaced by deuterium: 1 proton and 1 neutron.

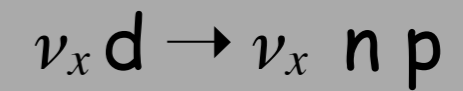
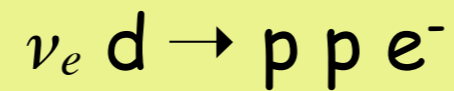
Deuterium is a neutron moderator.  
Canadian strategic reserve.

Cerenkov light detection





- SNO made 3 measurements each with a different neutrino interaction reaction



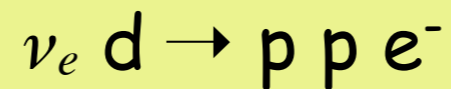
~5 events/day



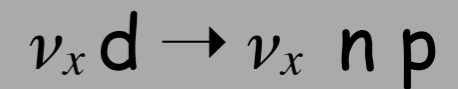
- SNO made 3 measurements each with a different neutrino interaction reaction



*Electron neutrinos bring 9 times more events.*



*It is only sensitive to electron neutrinos.*



*The three neutrinos give the same signature.*

**~5 events/day**

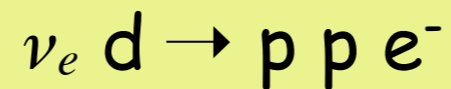


- SNO made 3 measurements each with a different neutrino interaction reaction



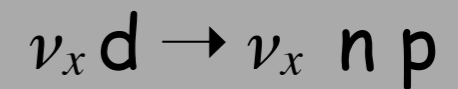
*Electron neutrinos bring 9 times more events.*

$$N_{meas.} = 9 N_{electron} + N_{\mu} + N_{\tau}$$



*It is only sensitive to electron neutrinos.*

$$N_{meas.} = N_{electron}$$



*The three neutrinos give the same signature.*

$$N_{meas} = N_{electron} + N_{\mu} + N_{\tau}$$

**~5 events/day**



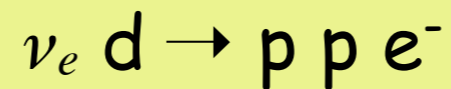
- SNO made 3 measurements each with a different neutrino interaction reaction



*Electron neutrinos bring 9 times more events.*

$$N_{meas.} = 9 N_{electron} + N_{\mu} + N_{\tau}$$

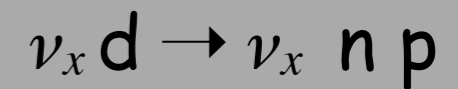
*Signal: 1 electron pointing back to the sun.*



*It is only sensitive to electron neutrinos.*

$$N_{meas.} = N_{electron}$$

*Signal: 1 electron not pointing to the sun.*



*The three neutrinos give the same signature.*

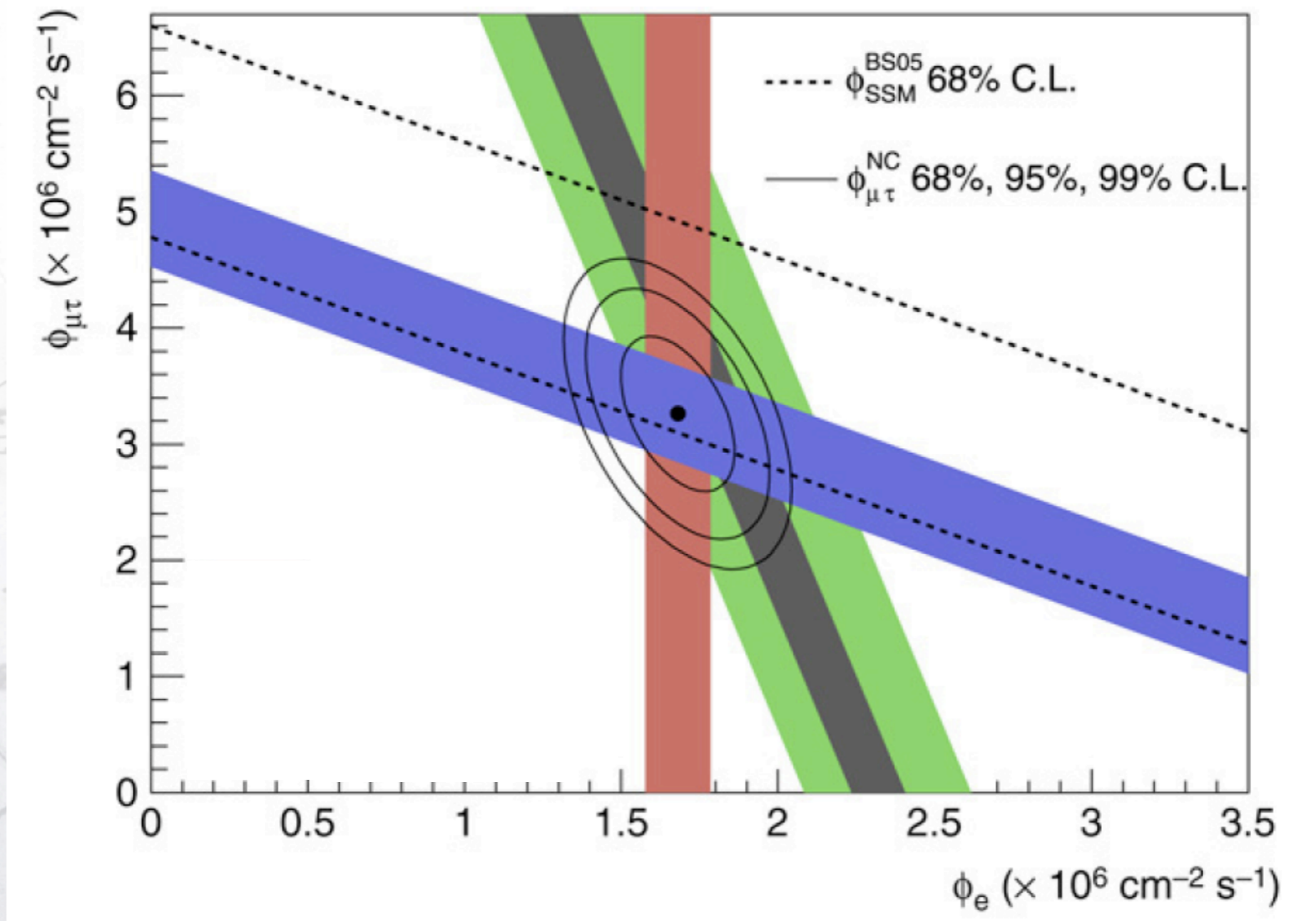
$$N_{meas} = N_{electron} + N_{\mu} + N_{\tau}$$

*Signal: 1 neutron*

**~5 events/day**

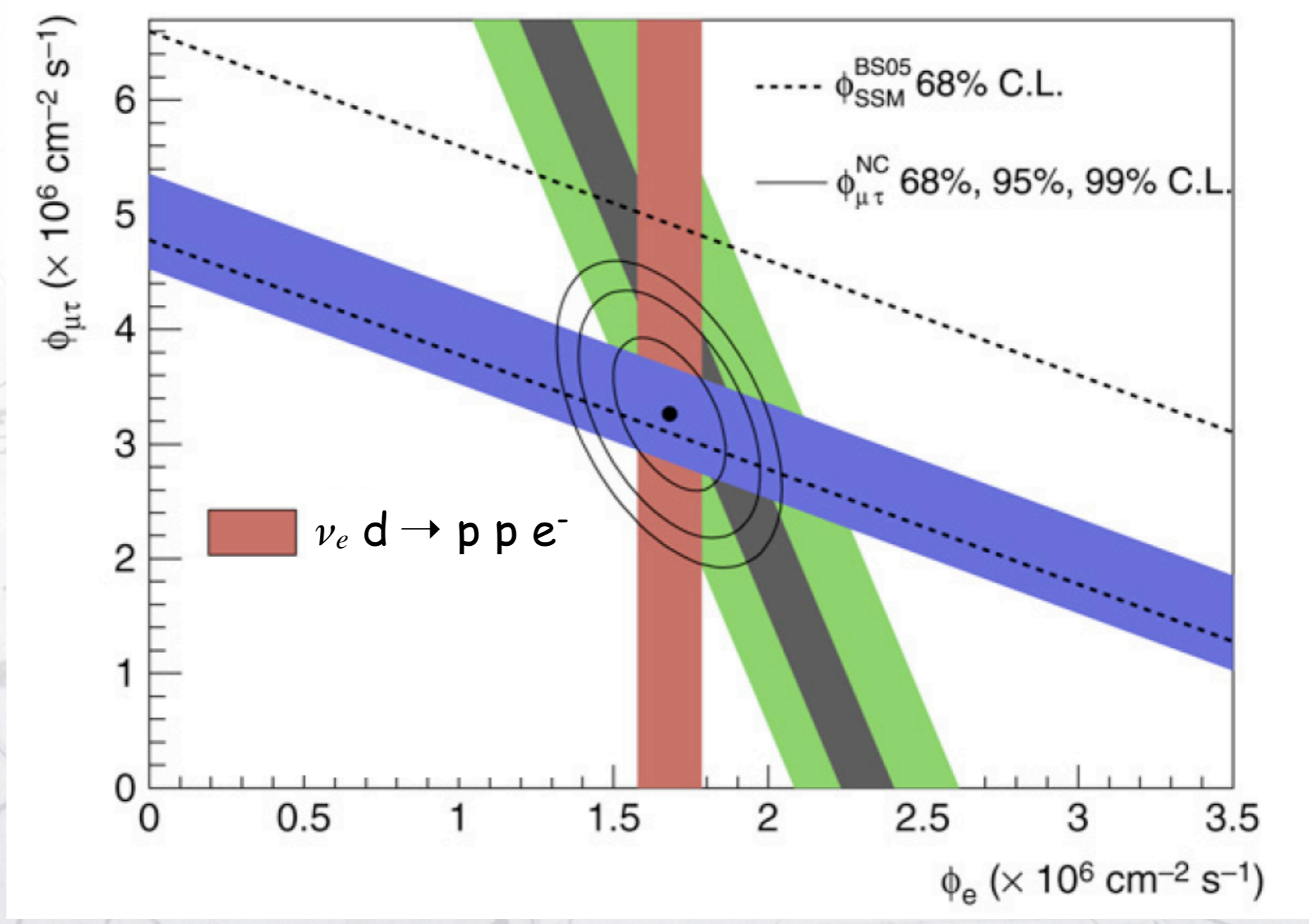


# SNO



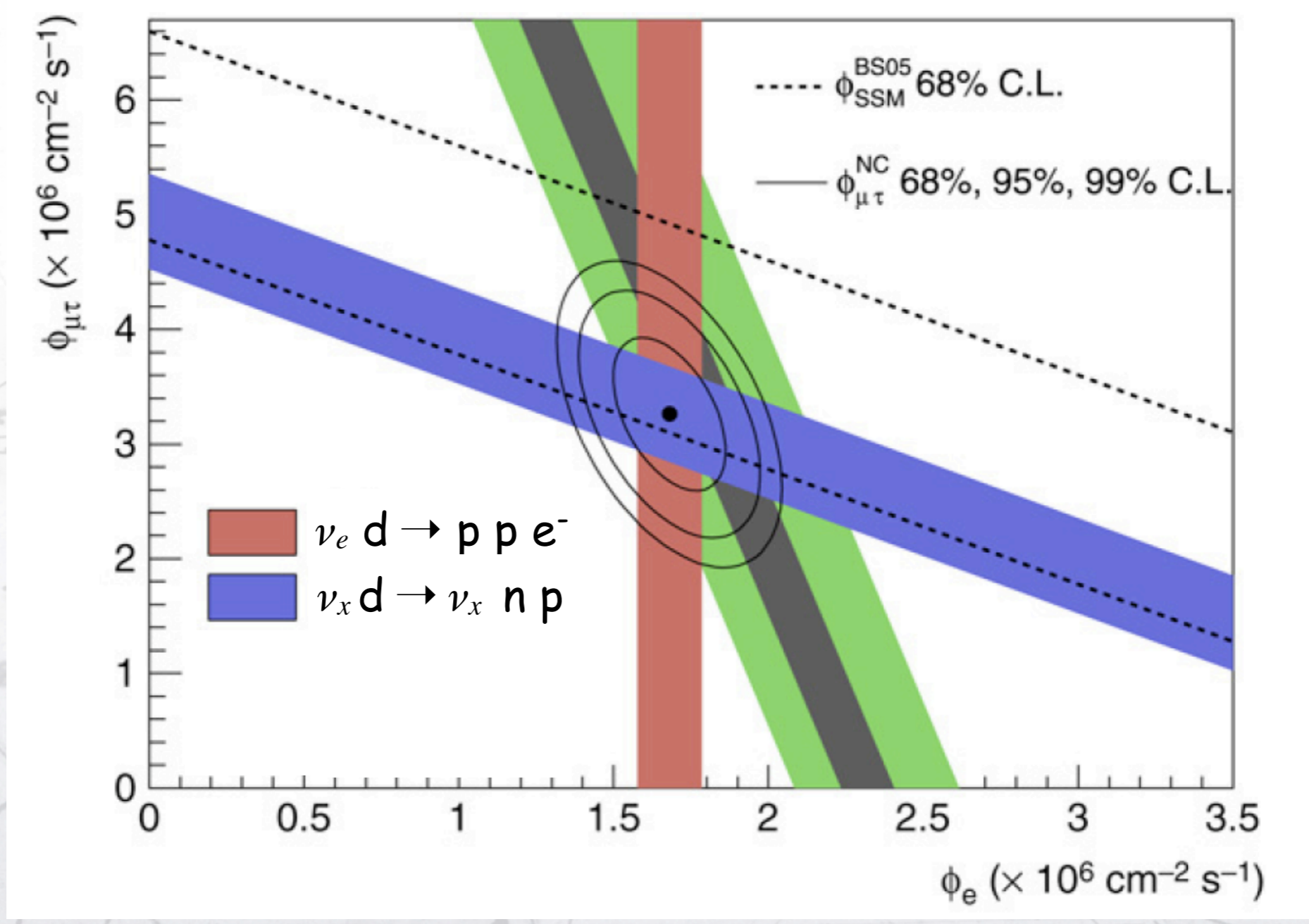


# SNO



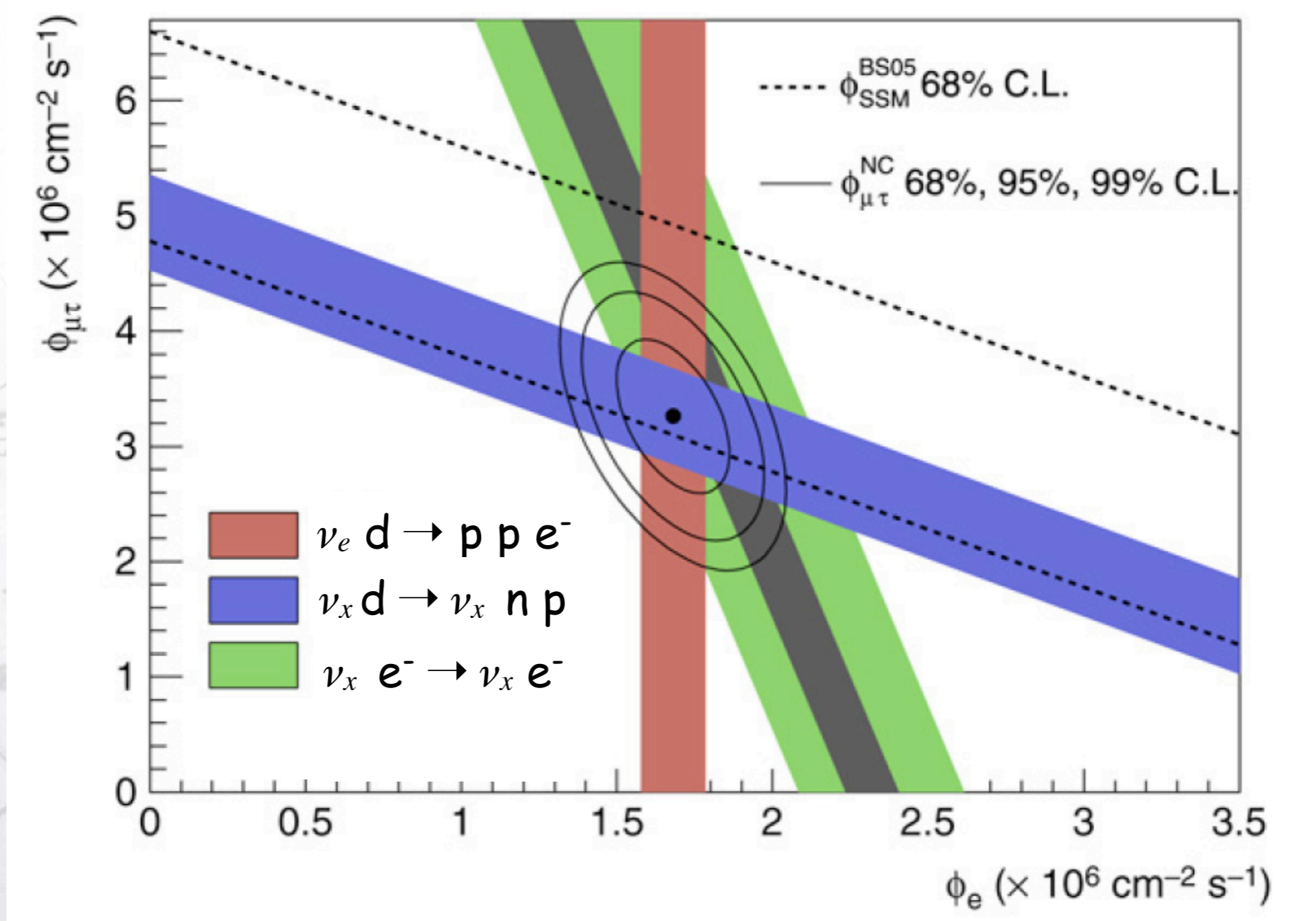


# SNO



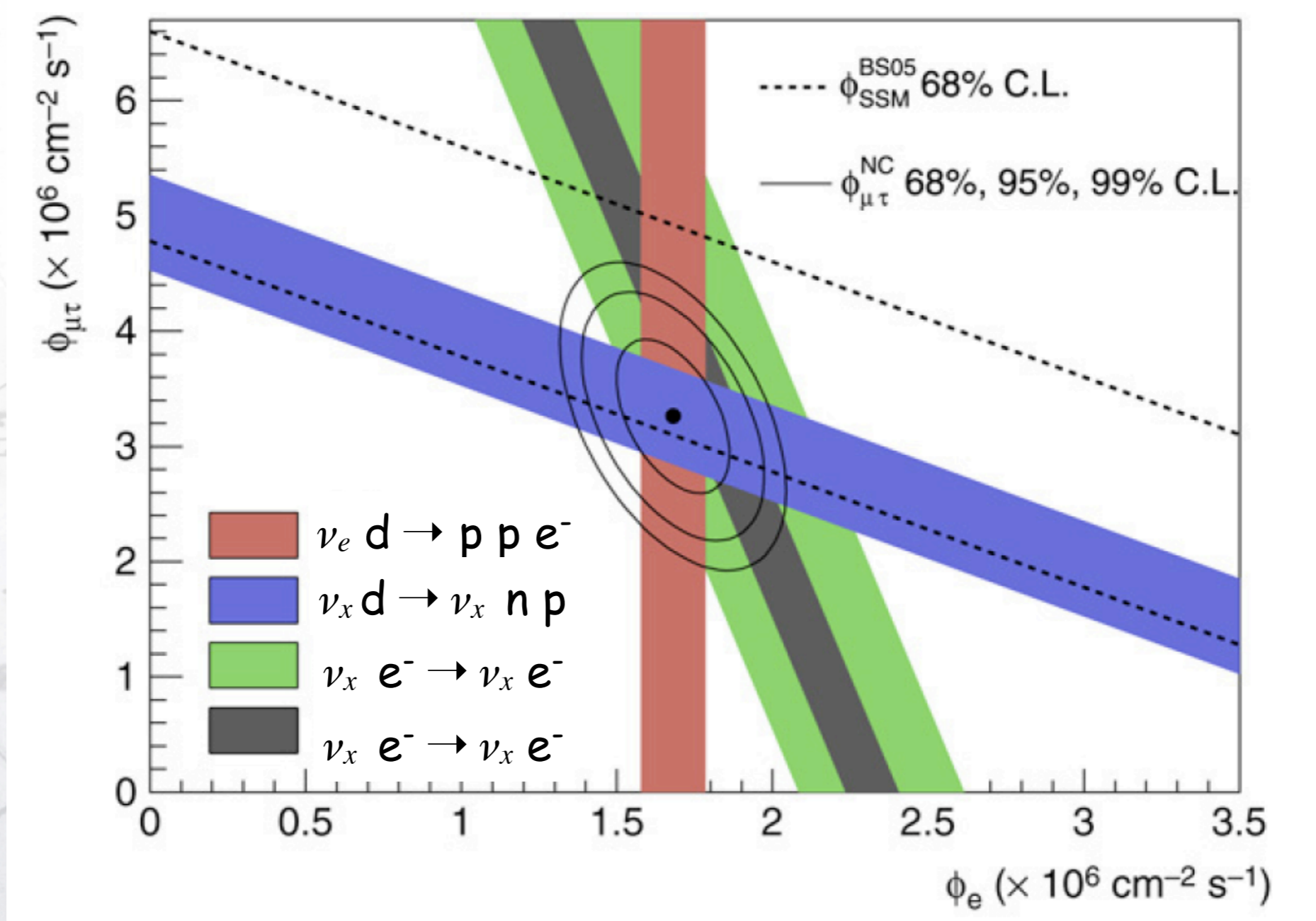


# SNO



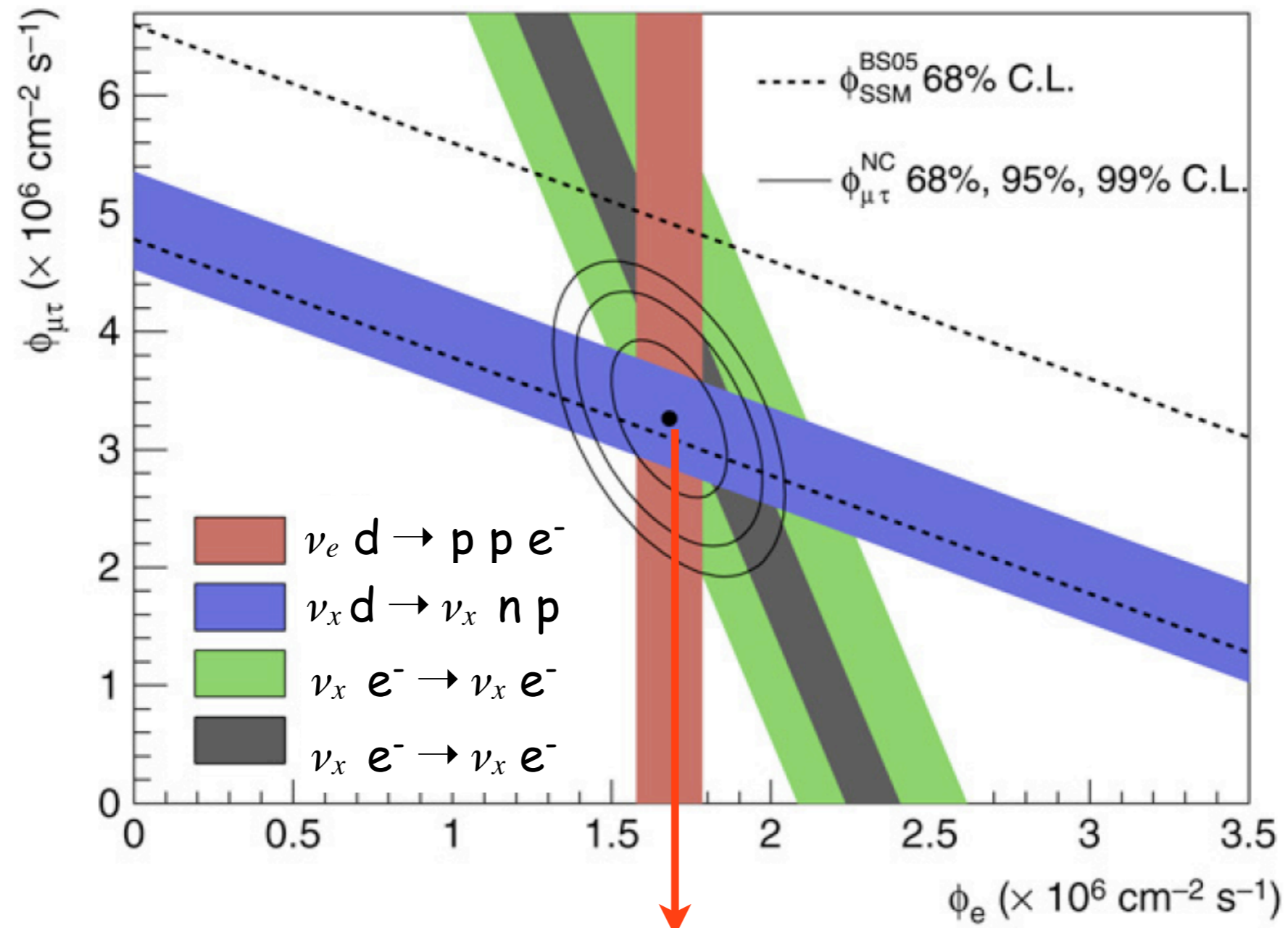


# SNO





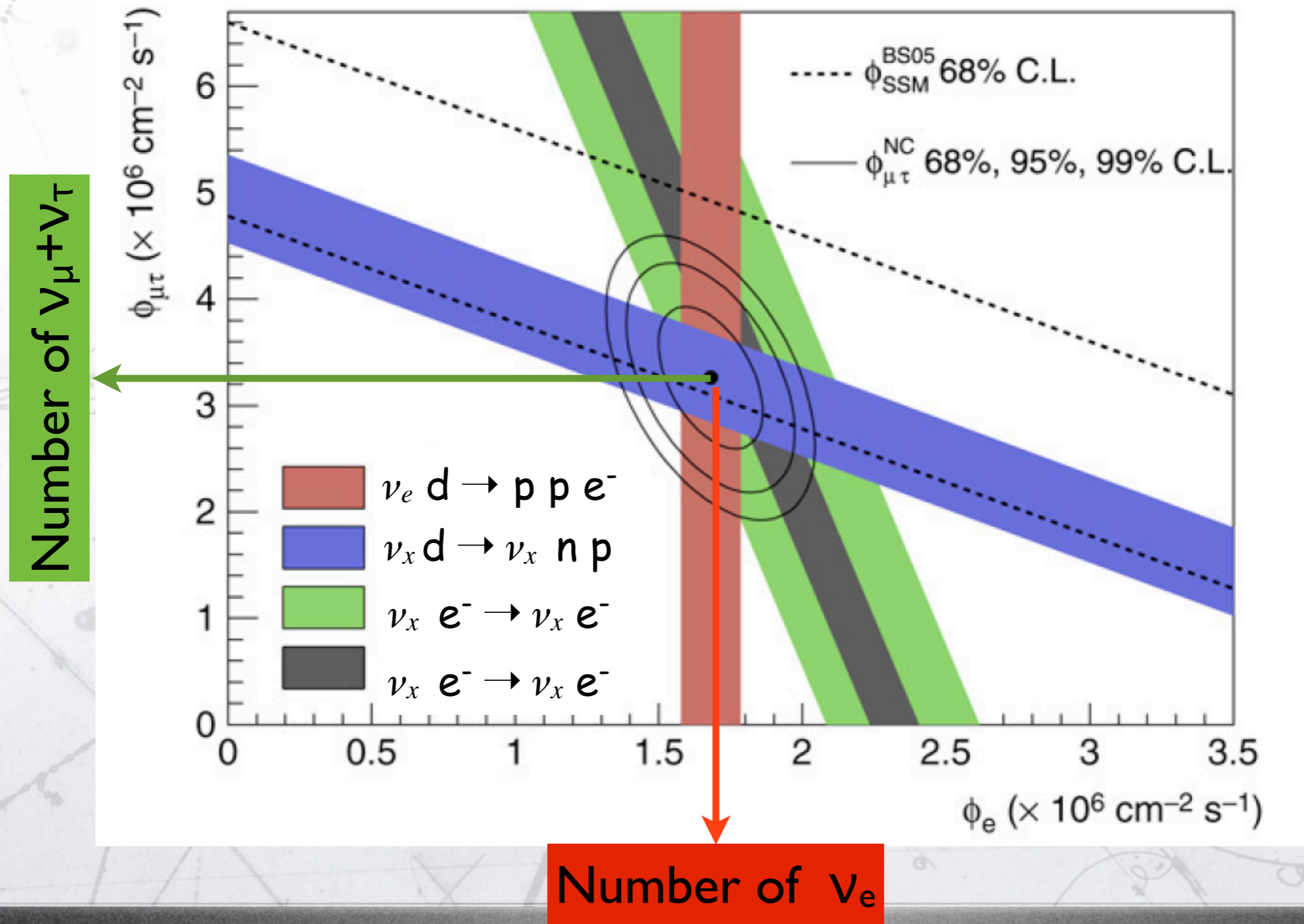
# SNO



Number of  $\nu_e$

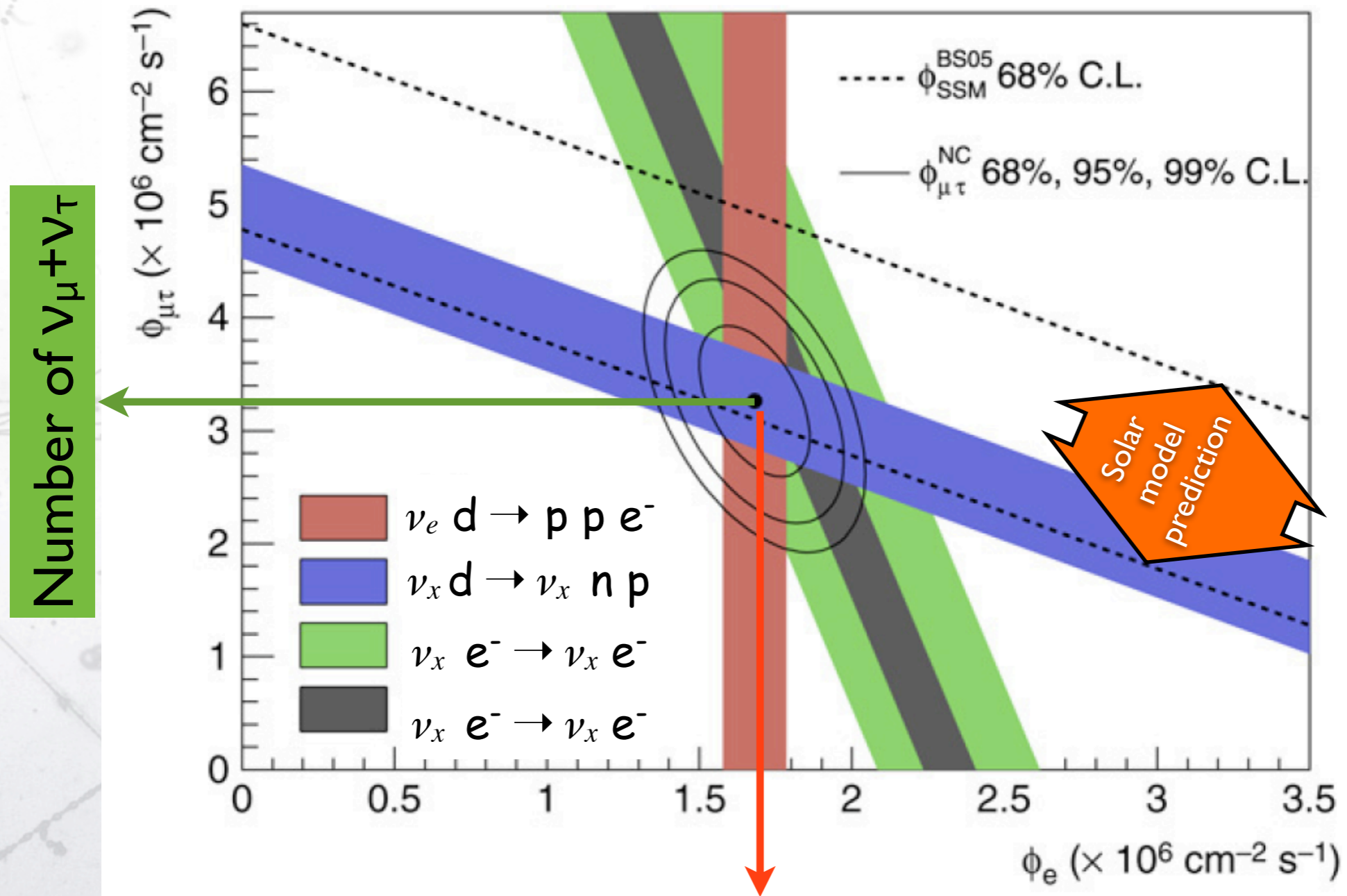


# SNO





# SNO

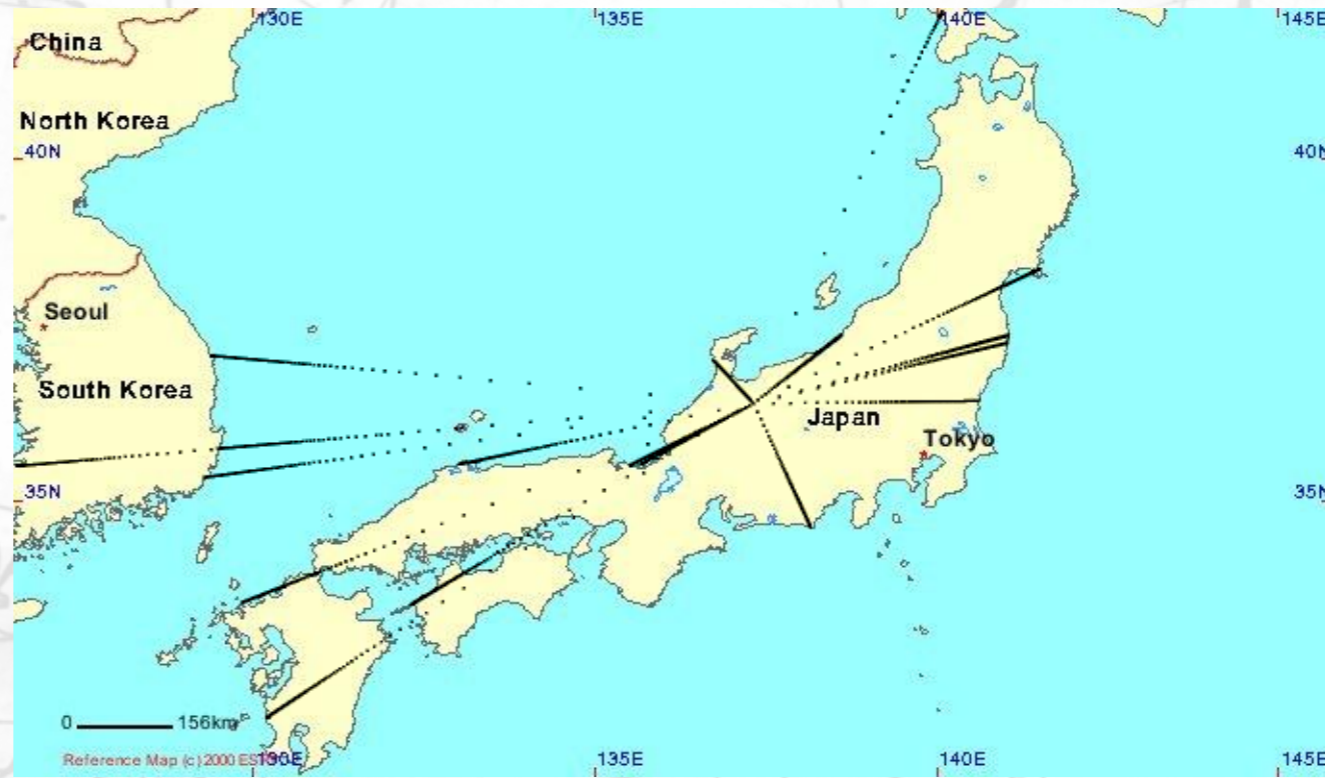
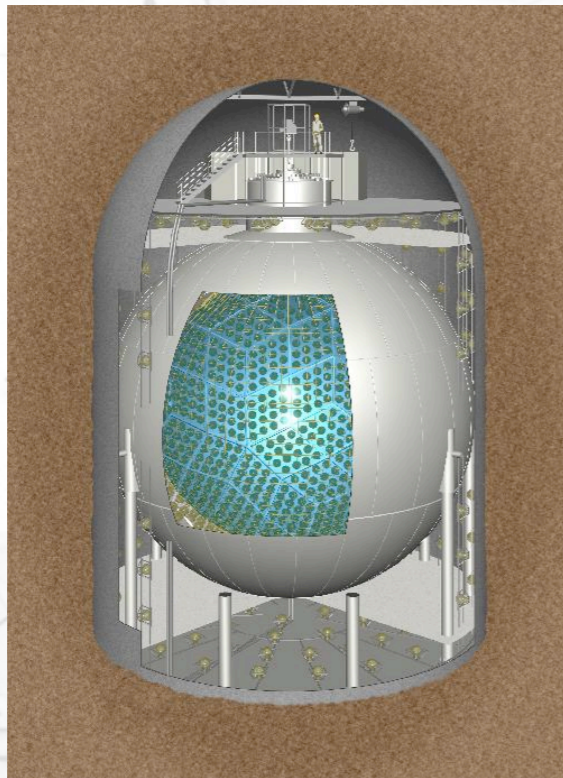


Number of  $\nu_{\mu} + \nu_{\tau}$

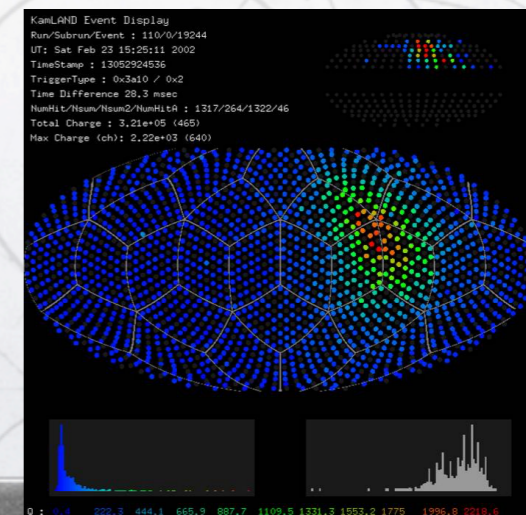
Number of  $\nu_e$



The experiments

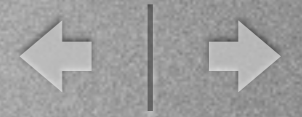


- Search for  $\bar{\nu}_e$  oscillations from nuclear reactors.
- Average distance:  $\sim 180\text{km}$ .
- Average Energy:  $\sim 4\text{ MeV}$ .
- Sensitive to  $\Delta m^2 \sim 10^{-4}\text{ eV}^2$
- Liquid scintillator detector.





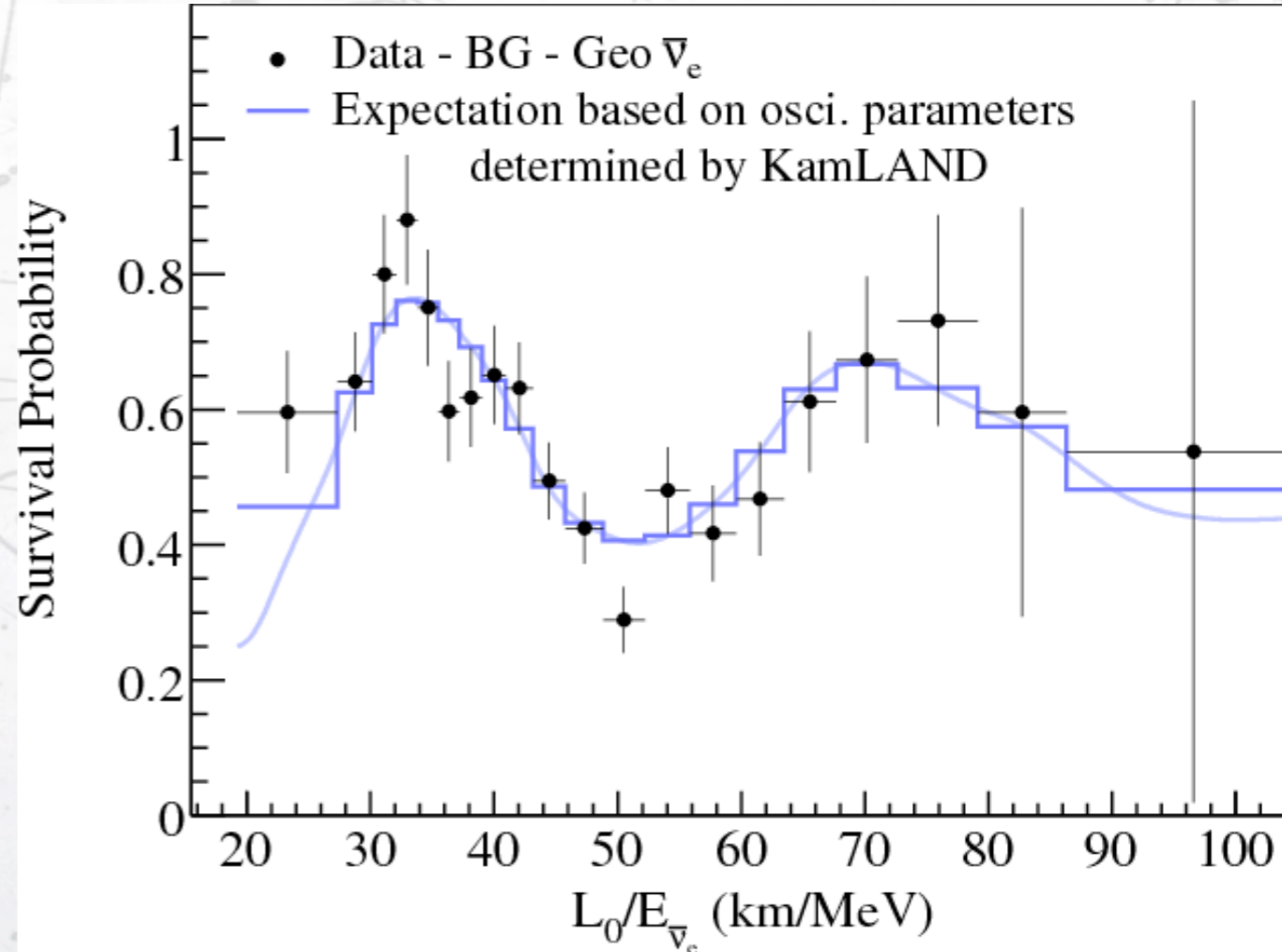
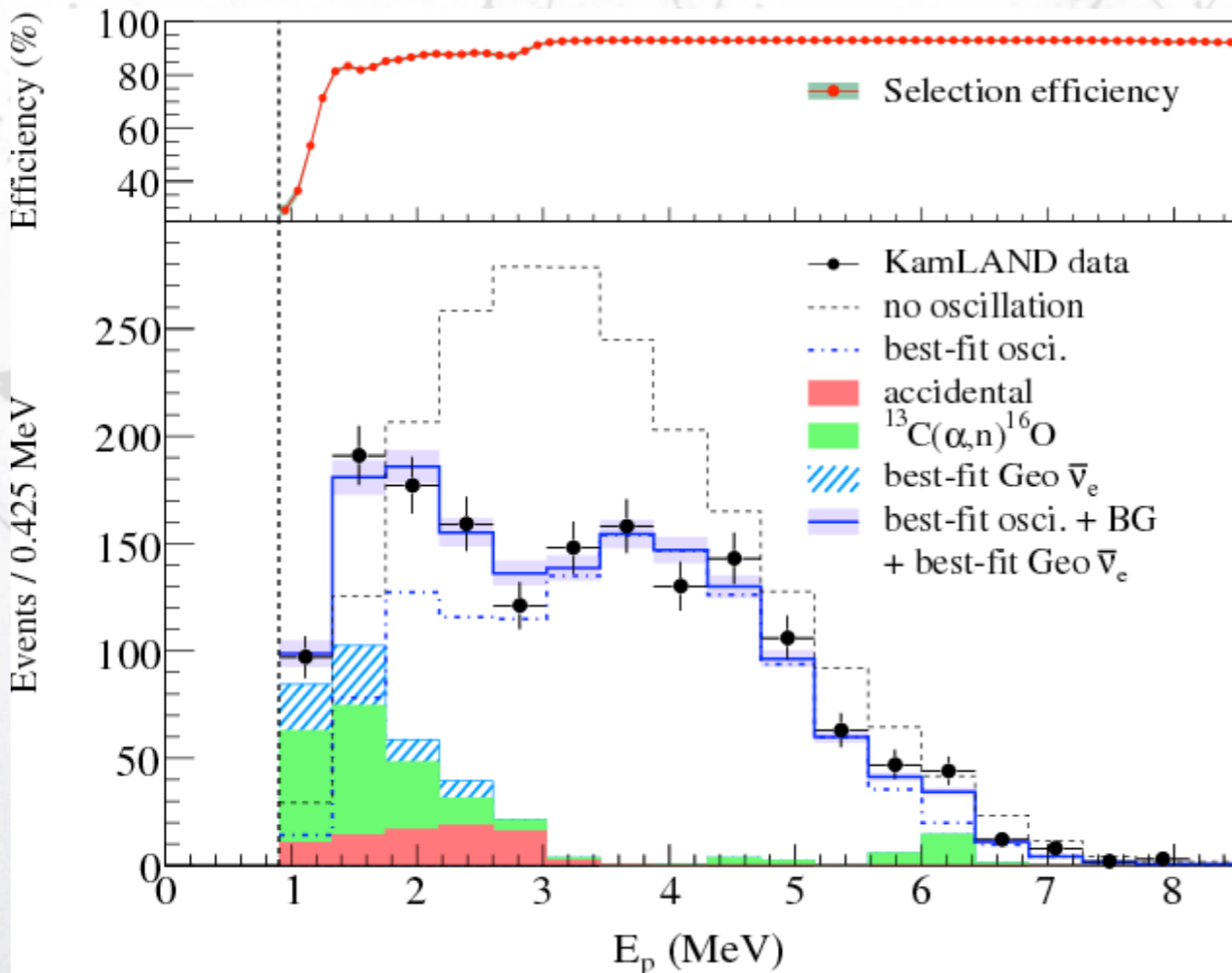
# Kamland



$\nu_e \rightarrow \nu_\tau \nu_\mu$  not enough energy to see  $\tau$  or  $\mu$

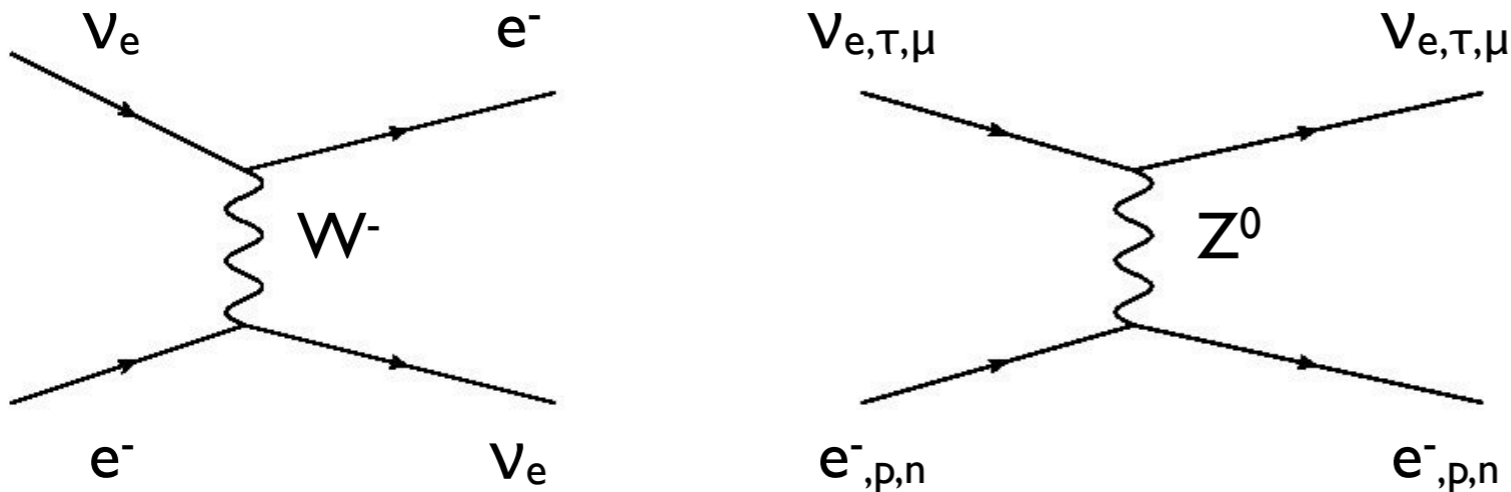
$\sim \sin(\beta/E)$

$\sim \sin(\alpha L/E)$





- Neutrinos in matter react differently depending on the flavour:

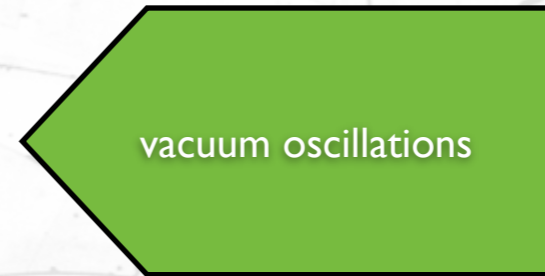
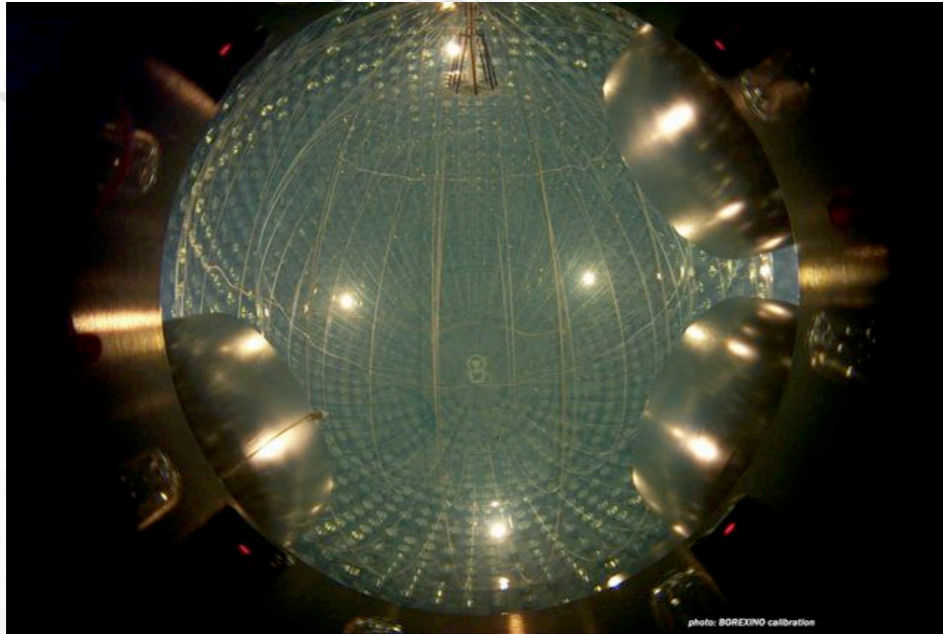


Coherent scattering, only phase is change!

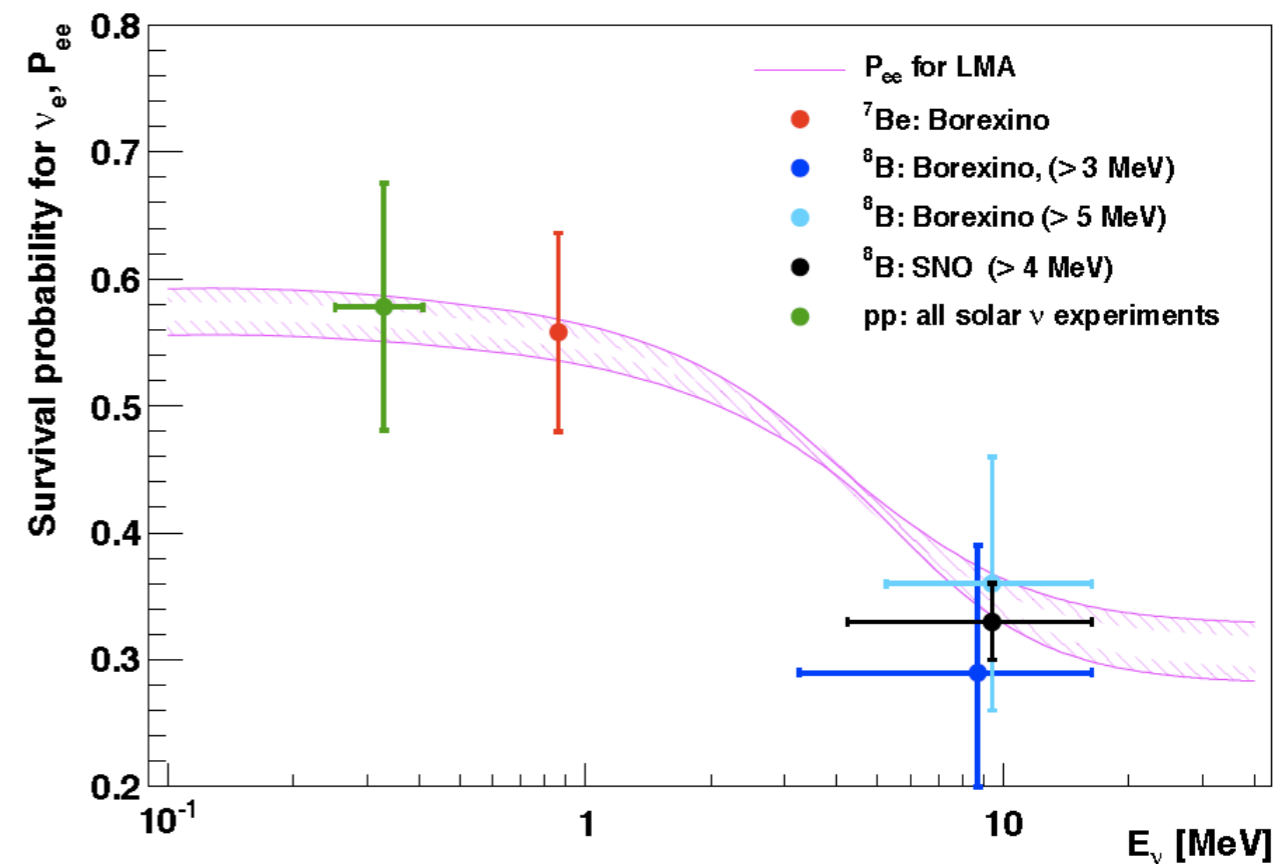
- Electron neutrinos behave differently in matter than the tau and muon neutrinos.
  - This is like having a different effective mass (“index of refraction”)
- This is more relevant for higher neutrino energies and high electron density (THE SUN!!!).
- The effect is a “modified” oscillation pattern (matter effects).
- Neutrinos are emitted from the sun in the state with largest mass ( $\nu_2$ )



- Liquid scintillator detector.



- Borexino, low energy solar neutrino experiment, was able to check the matter effects.
- The matter resonant effect depends on the neutrino energy.
- So, we should expect a transition when this happens.







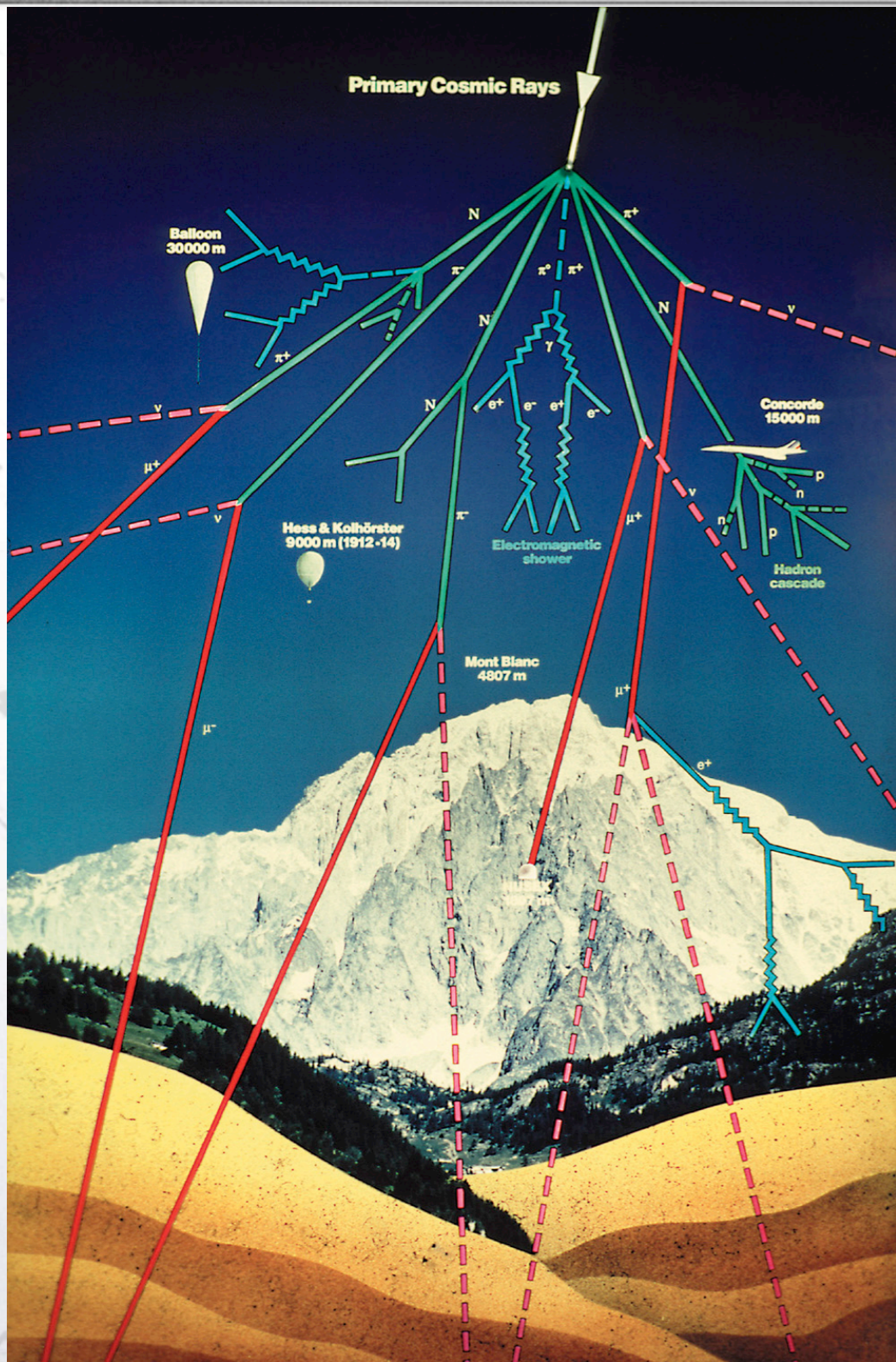
# SuperKamiokande & the universality of neutrino oscillations.

$$\Theta_{23} \quad \& \quad \Delta m^2_{23}$$



- Up to now we have been looking at  $\nu_e$  disappearance:
  - Is the  $\nu_e$  oscillating to  $\nu_\mu$  or  $\nu_\tau$ ?
  - What about the  $\nu_\mu$  and  $\nu_\tau$ ?
- Some trivialities:
  - Solar neutrinos ( $\sim$ MeV) do not have energy to produce  $\mu$  (106MeV) or  $\tau$ (1777MeV). So, we can't distinguish them. Only NC are possible (SNO).
  - We need another “abundant” source of higher energy neutrinos:
    - the atmosphere!!.





## Atmospheric neutrinos

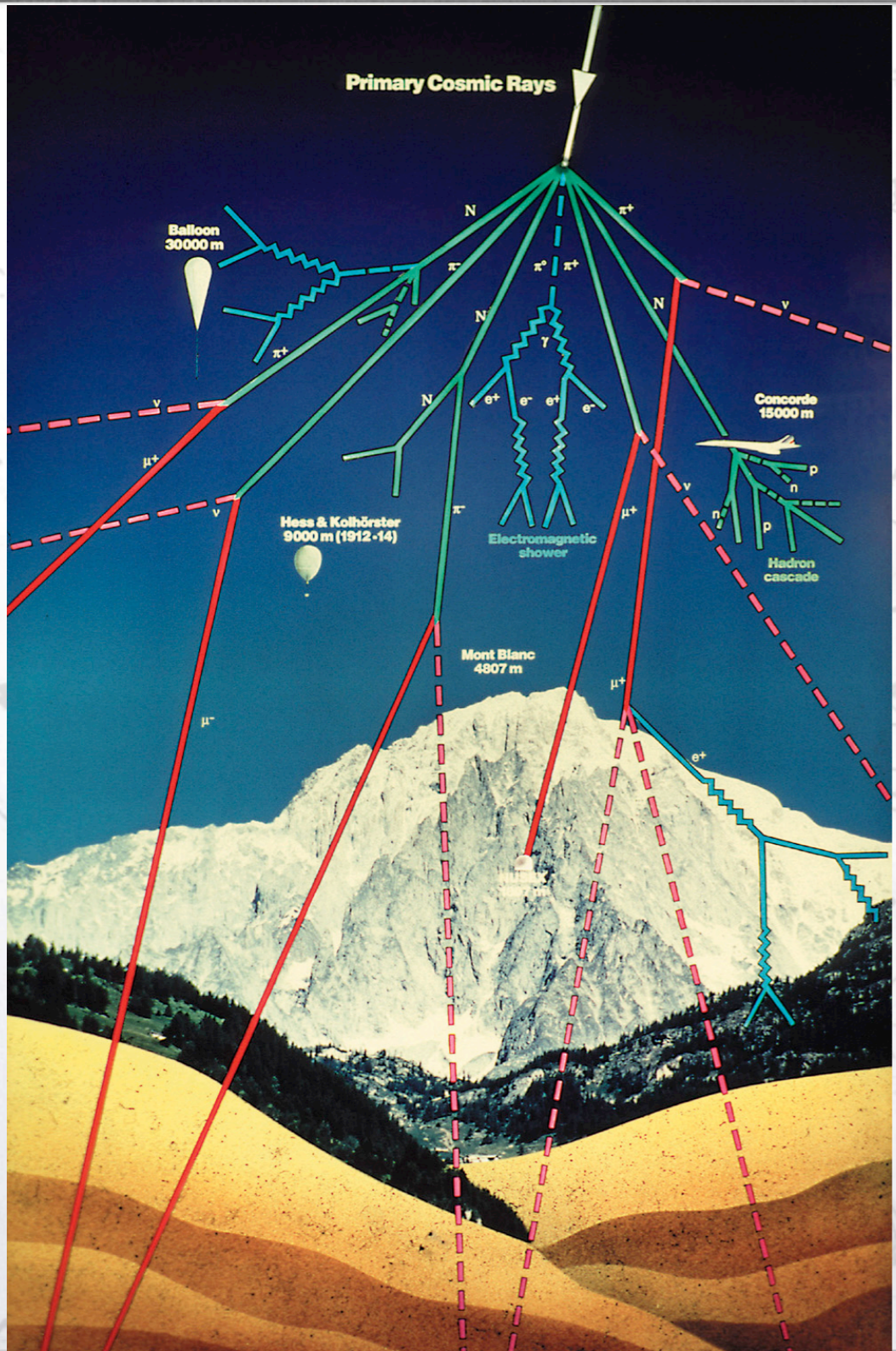
Extraterrestrial high energy protons collide with the atmosphere and produce a “shower” of particles.

Many of the particles are pions that decay into muons and muon neutrinos.  $I \nu_{\mu}$

Muons decay into electrons, muon neutrinos and electron neutrinos.  $I \nu_{\mu} + I \nu_e$

In atmospheric showers,  $\sim 2$  muon neutrinos are produced per electron neutrino.

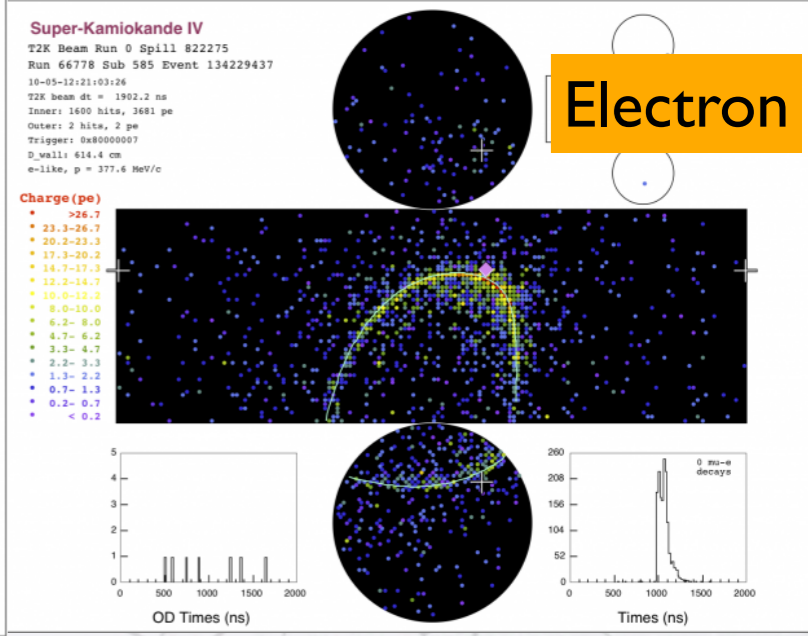
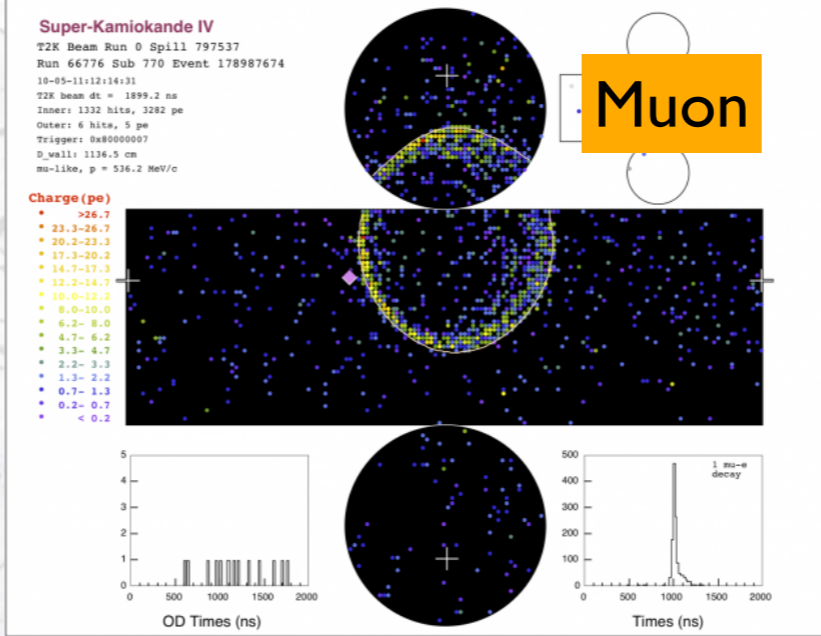




## Atmospheric neutrinos

SK uses the  $\sim 2 \nu_{\mu}/\nu_e$  ratio

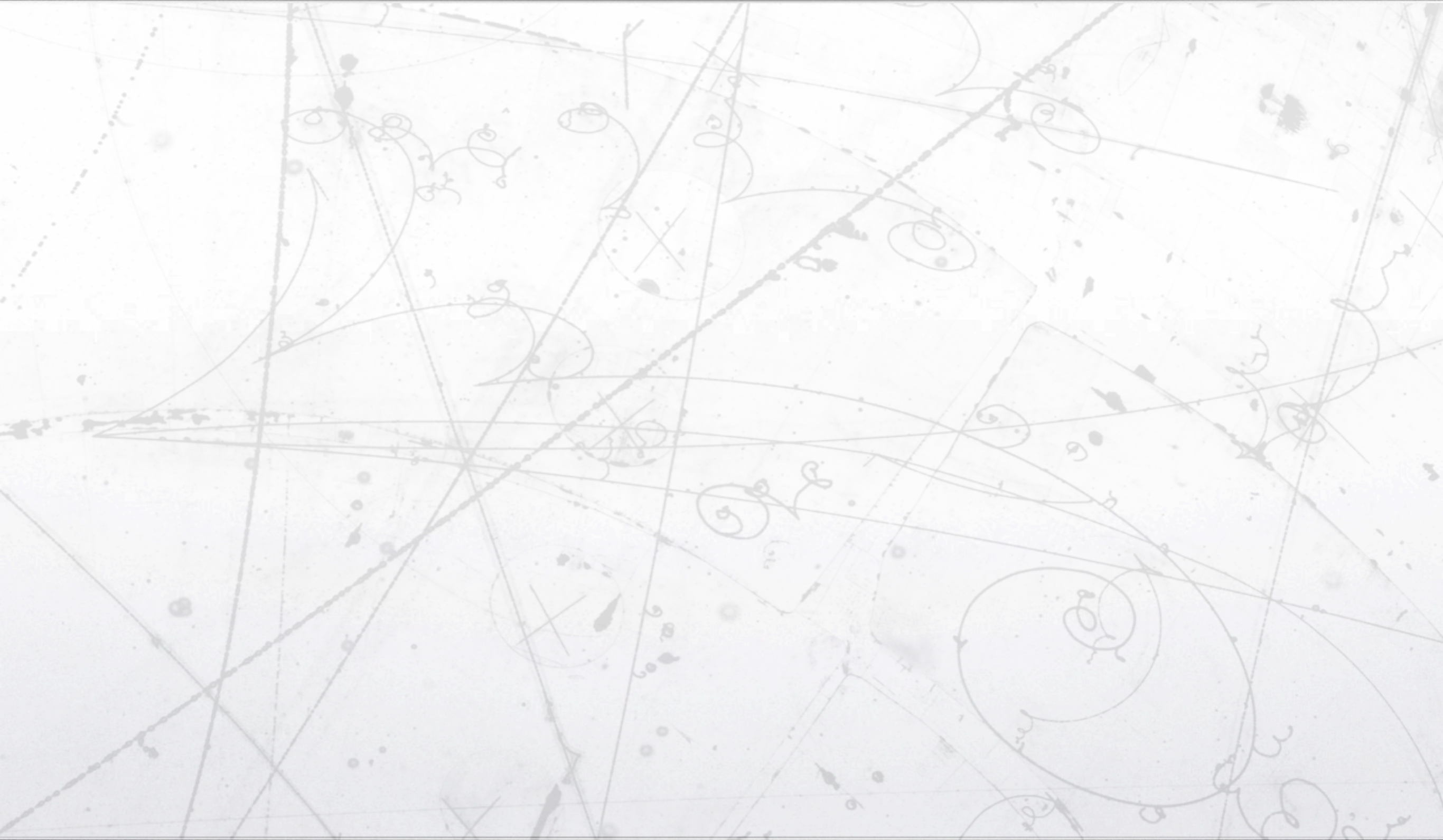
Super-Kamiokande distinguish between electrons and muons.



Super-Kamiokande also detect the direction of the lepton. (directionality of Cerenkov light)



# SuperKamiokande

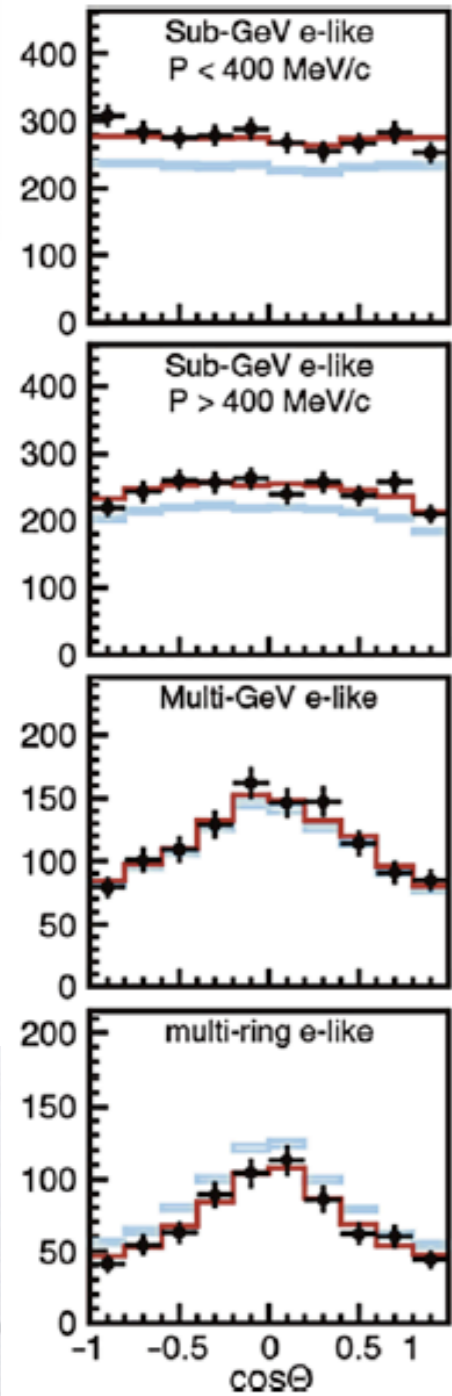




## I. Electron sample is similar to expected

$\nu_e$

Number of events



Higher Energy

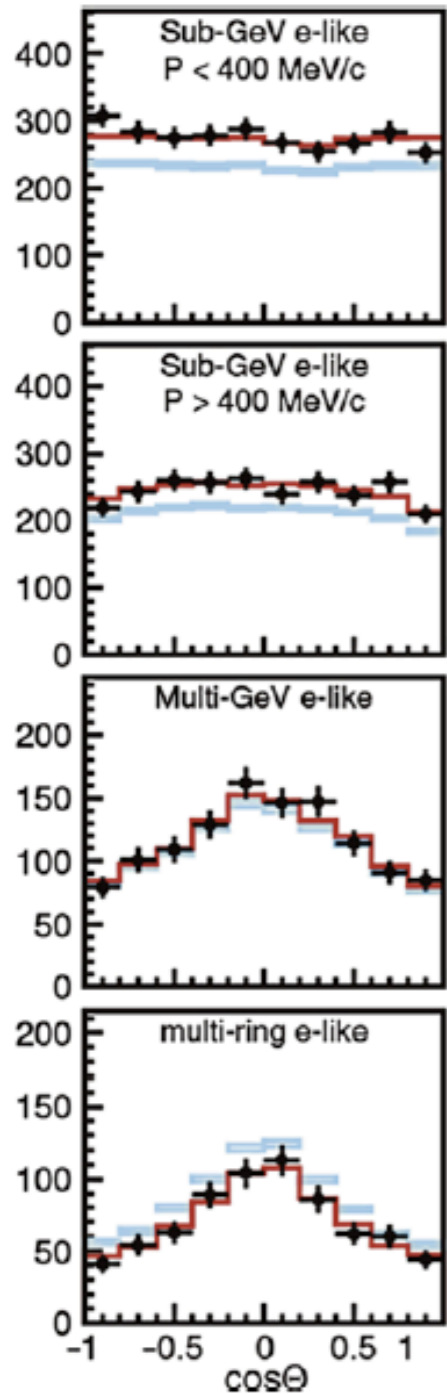


# SuperKamiookande



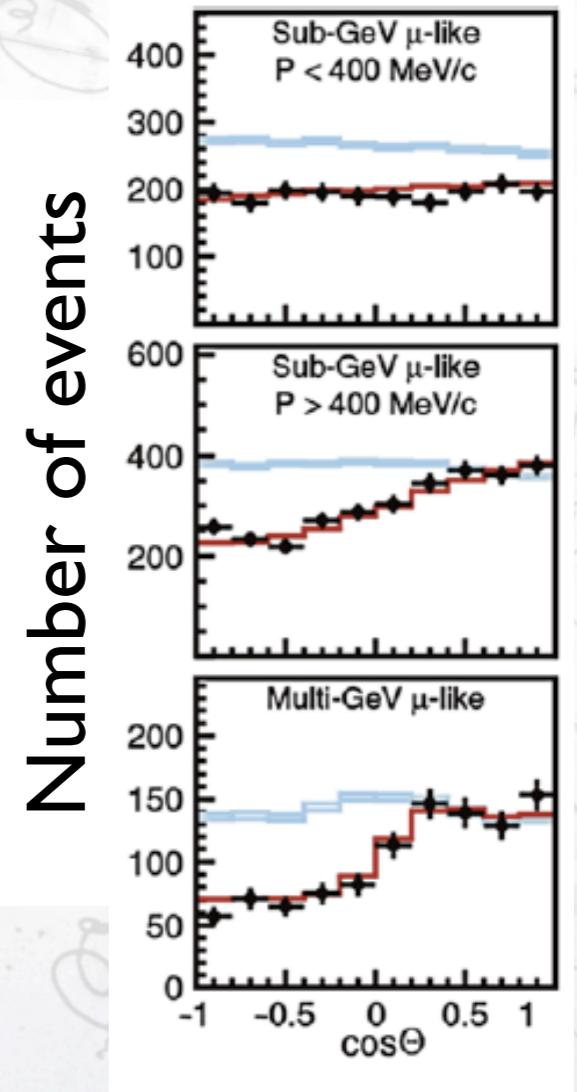
1. Electron sample is similar to expected
2. There is a deficit of muon neutrinos crossing the earth.

$\nu_e$



Higher Energy

$\nu_\mu$



Higher energy





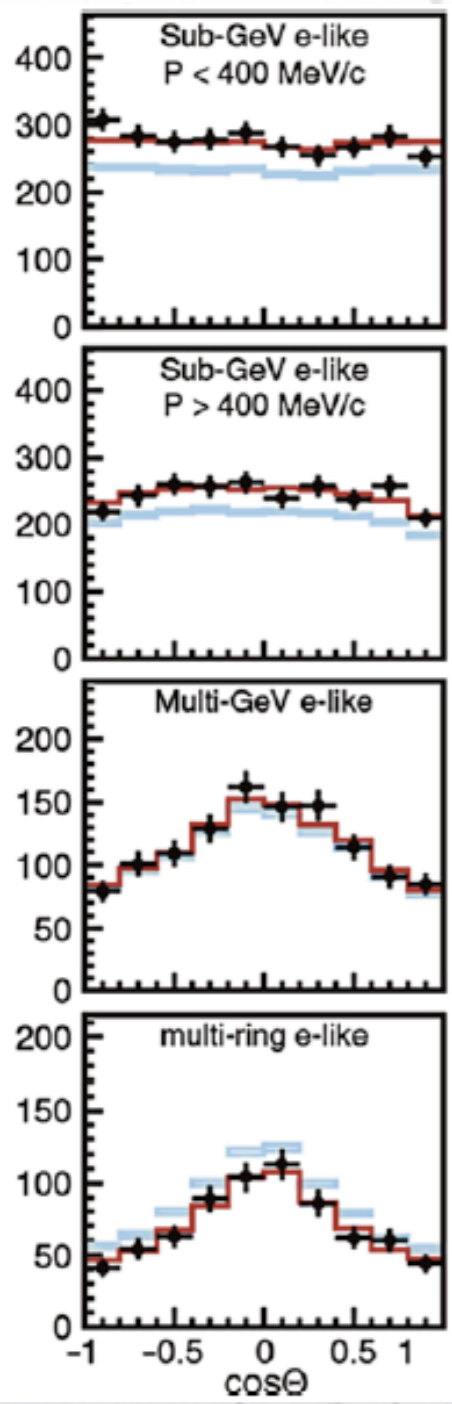
# SuperKamiookande



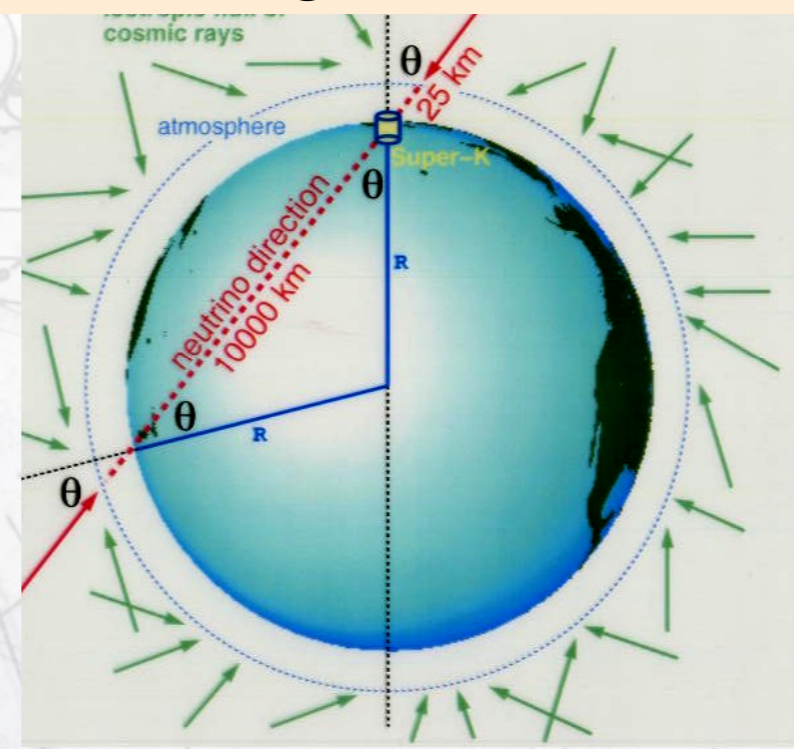
1. Electron sample is similar to expected
2. There is a deficit of muon neutrinos crossing the earth.
3. The angle provides the  $\nu$  travel, and mixing, distance.

$\nu_e$

Number of events

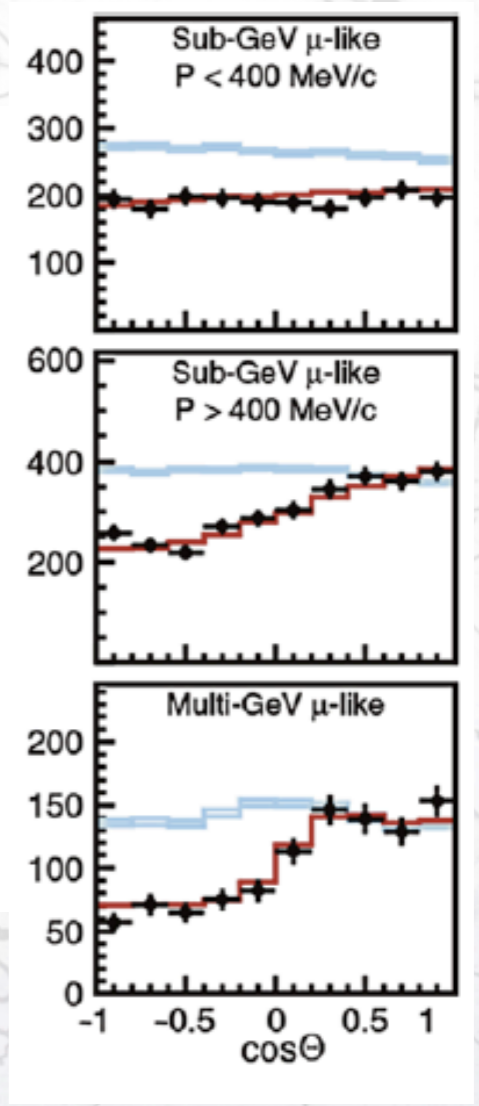


Higher Energy



$\nu_\mu$

Number of events



Higher energy



# SuperKamiookande



1. Electron sample is similar to expected
2. There is a deficit of muon neutrinos crossing the earth.
3. The angle provides the  $\nu$  travel, and mixing, distance.

$\nu_e$

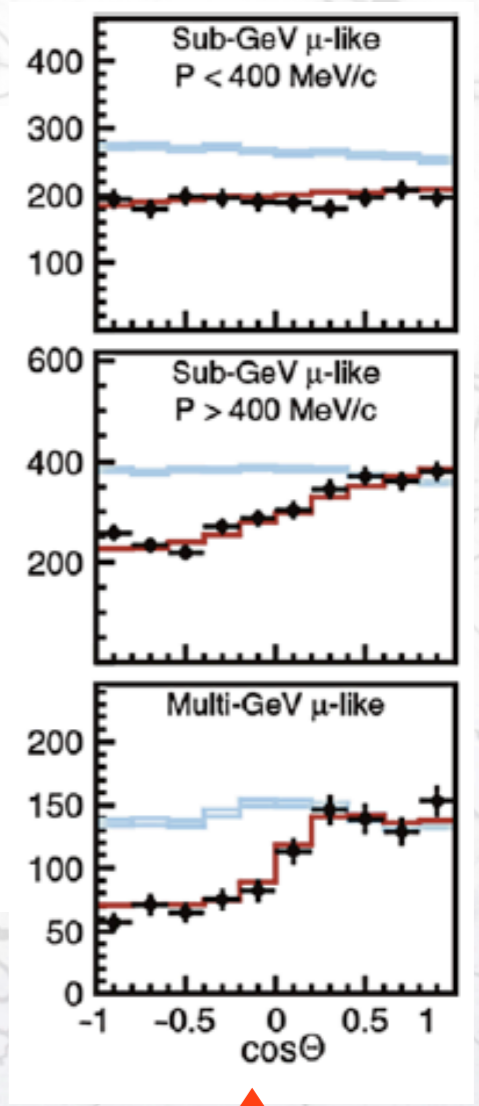
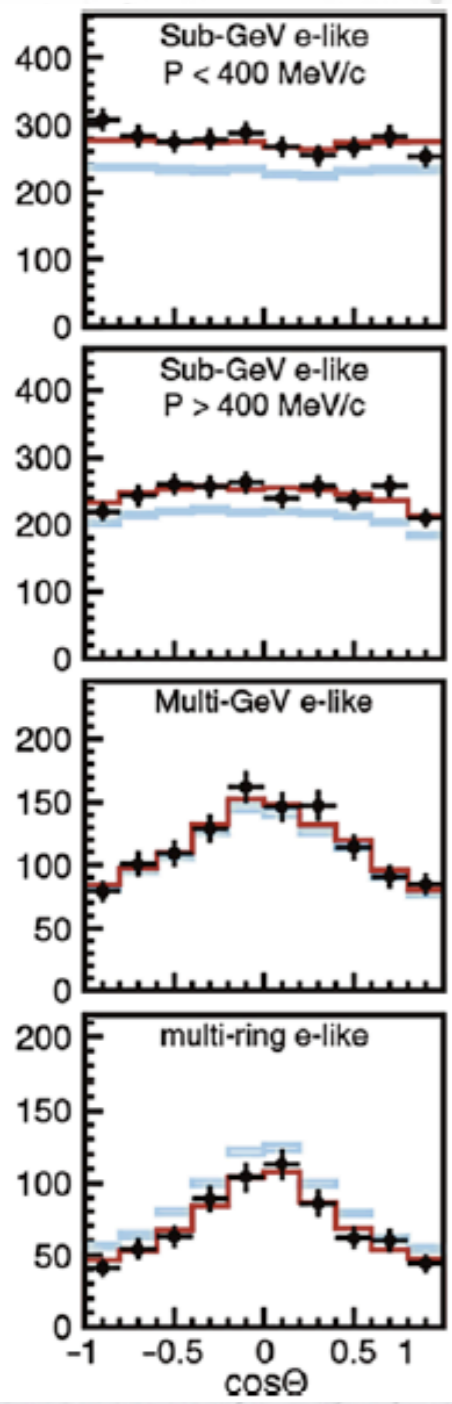
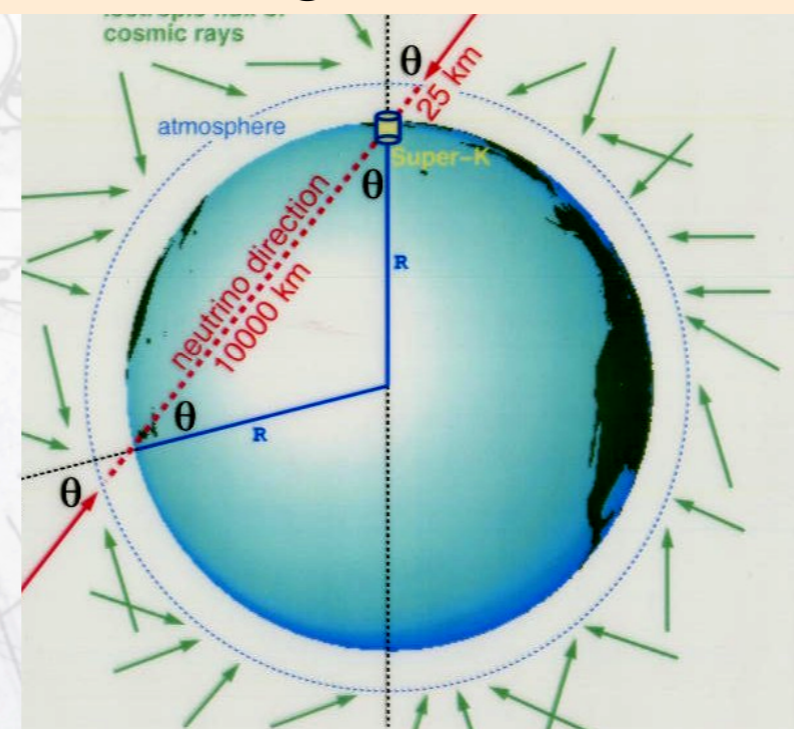
$\nu_\mu$

Number of events

Number of events

Higher Energy

Higher energy

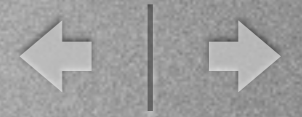


Hypothesis:  
electron neutrinos did not oscillate.  
Muon neutrinos oscillate to tau neutrinos.



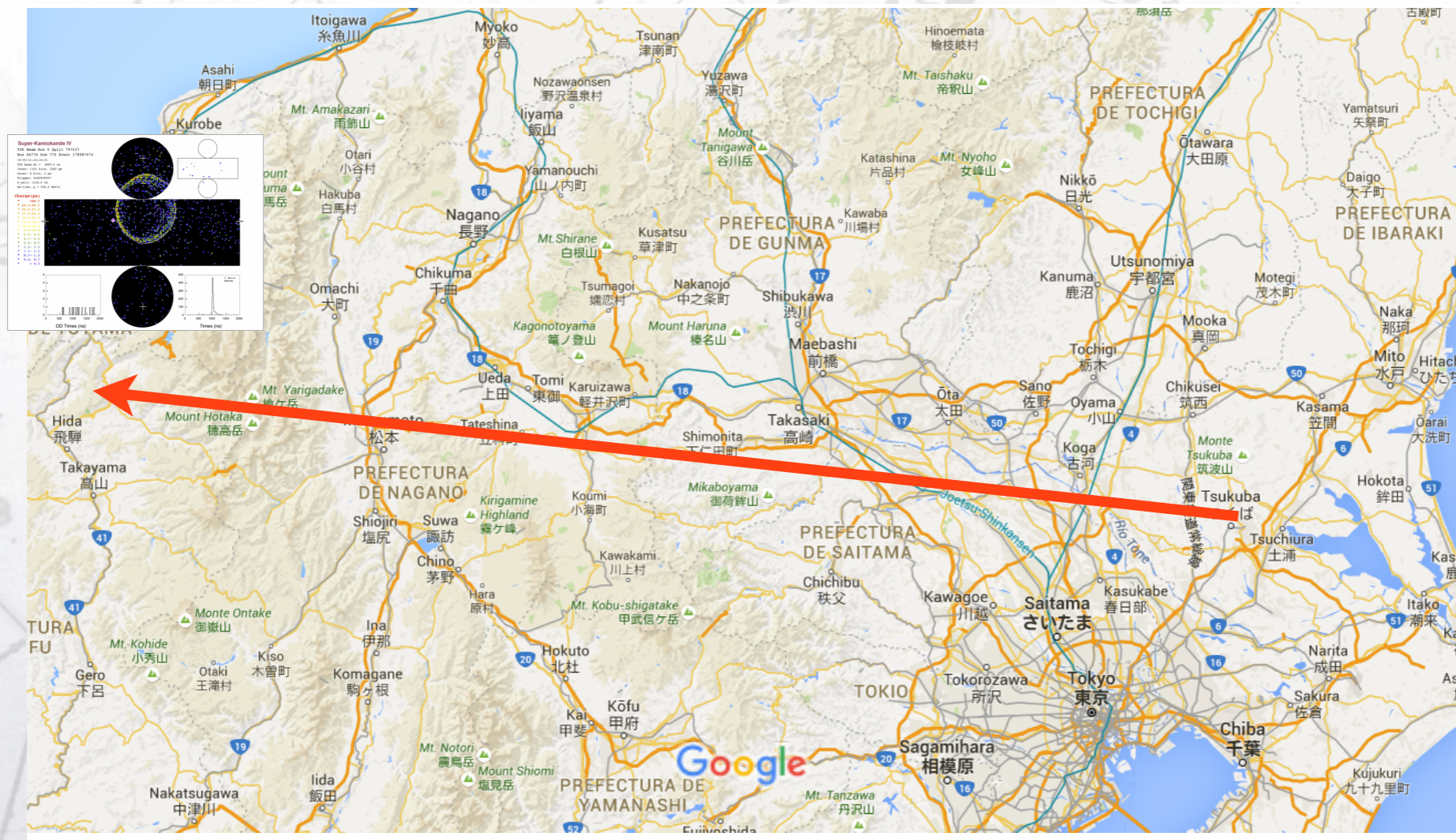


# K2K: the confirmation



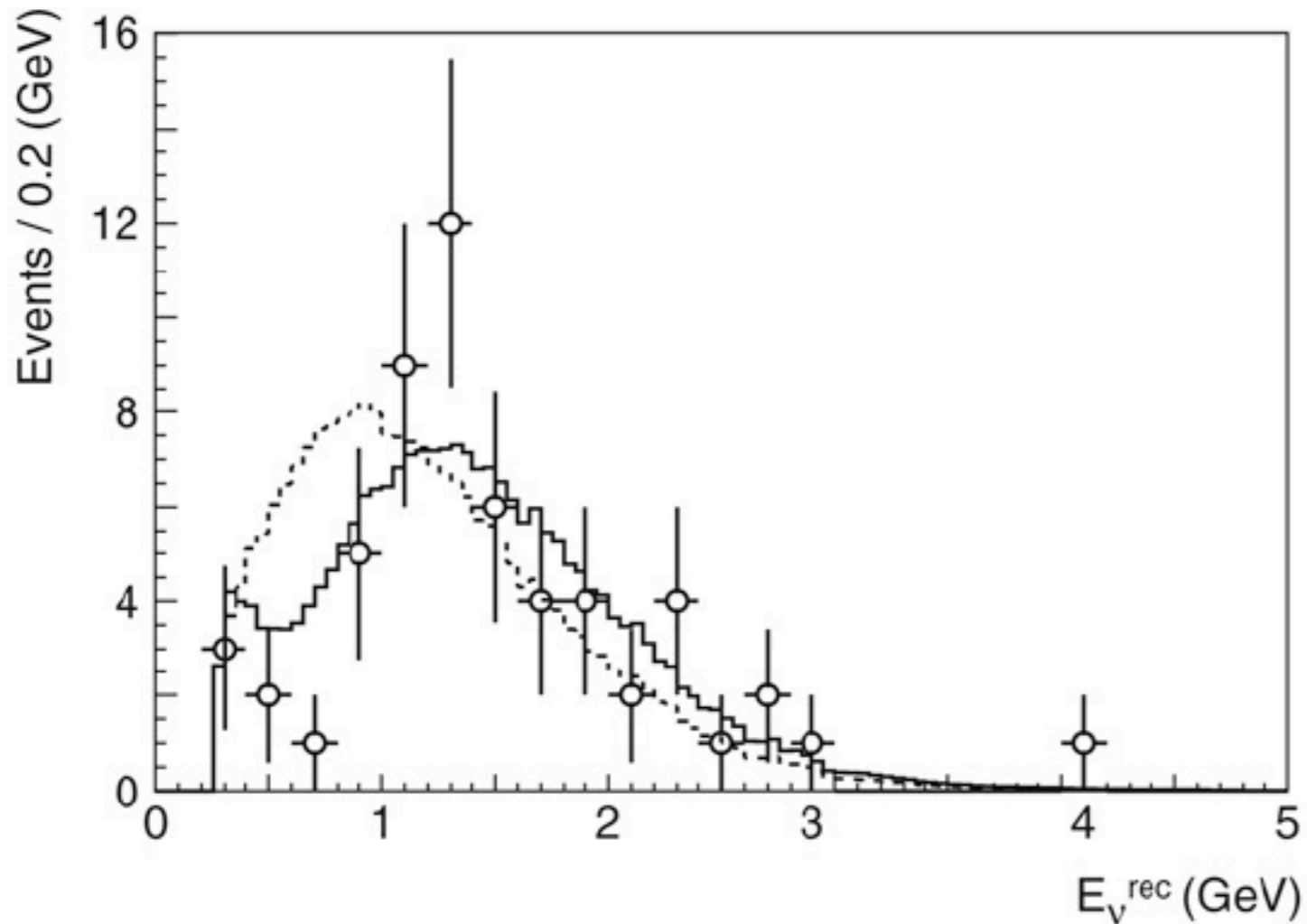
The experiments

- Artificial neutrinos of  $\sim 1.6$  GeV are produced in the east coast of Japan.
- Neutrino flux and spectrum is measured at a near detector to reduce uncertainties (“a priori” large)
- Neutrinos were detected at 250 km at Superkamiokande.





The experiments



- 1<sup>st</sup> long base line experiment: prove of principle and technology.
- Deficit and spectrum distortion compatible with SK results.
- man-made beam confirming oscillations.

Minos came later to improve these results!



- The observed oscillations are:

- $\nu_e \rightarrow \nu_{\mu,\tau}$  (SOLAR)  $\theta_{12}$

- $\nu_{\mu} \rightarrow \nu_{\tau}$  (ATMOSPHERIC)  $\theta_{32}$

- To observe  $\nu_{\mu} \rightarrow \nu_e$  from solar parameters ( $\theta_{12}, \Delta m^2_{12}$ )

- the energy should be similar to solar neutrinos or the distance should be very large.

$$\frac{\Delta m^2_{23}}{\Delta m^2_{12}} \approx 30.$$

- We need energies 30x smaller ( $\sim 30\text{MeV}$  where  $\nu_{\mu}$  production & detection is difficult) or distances 30x larger (tough, we can't make earth 30 times larger!) than standard atmospheric experiments.

Solar & atmospheric appear to us like two decoupled oscillations

Selecting E and/or distance we can chose one or the other



# The most recent results: $\theta_{13}$ angle





- There are two possibilities:

- $\nu_\mu \longrightarrow \nu_e$  with atmospheric  $\Delta m^2$  (long base line: T2K, Nova)

$$P_{\nu_\mu, \nu_e} \approx \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 \frac{\Delta m_{31}^2 L}{4E}$$

$$\pm \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^3 \frac{\Delta m_{31}^2 L}{4E}$$

$$- \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \cos \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \frac{\Delta m_{31}^2 L}{4E} \sin \frac{2\Delta m_{31}^2 L}{4E}$$

$$+ \left(\frac{\Delta m_{12}^2}{\Delta m_{31}^2}\right)^2 \cos^2 \theta_{23} \sin^2 \theta_{12} \sin^2 \frac{\Delta m_{31}^2 L}{4E}$$

- Sensitive to violation of Charge Parity symmetry.

- $\nu_e \longrightarrow \nu_e$  with “atmospheric”  $\Delta m^2$

$$P_{\nu_e, \nu_e} \approx 1 - \sin^2 2\theta_{13} \sin^2 \frac{\Delta m_{31}^2 L}{4E}$$

- Insensitive to CP phase.

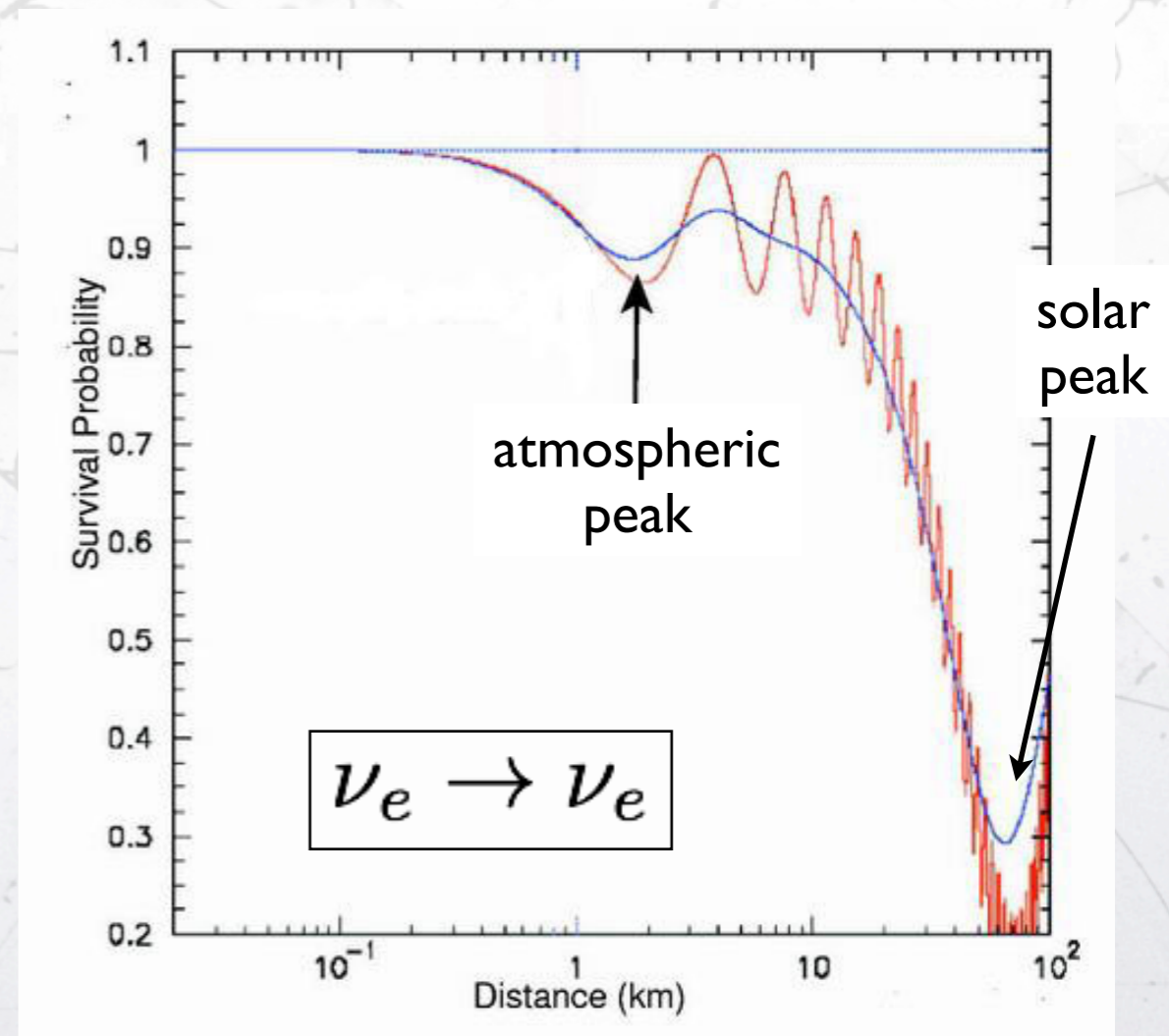
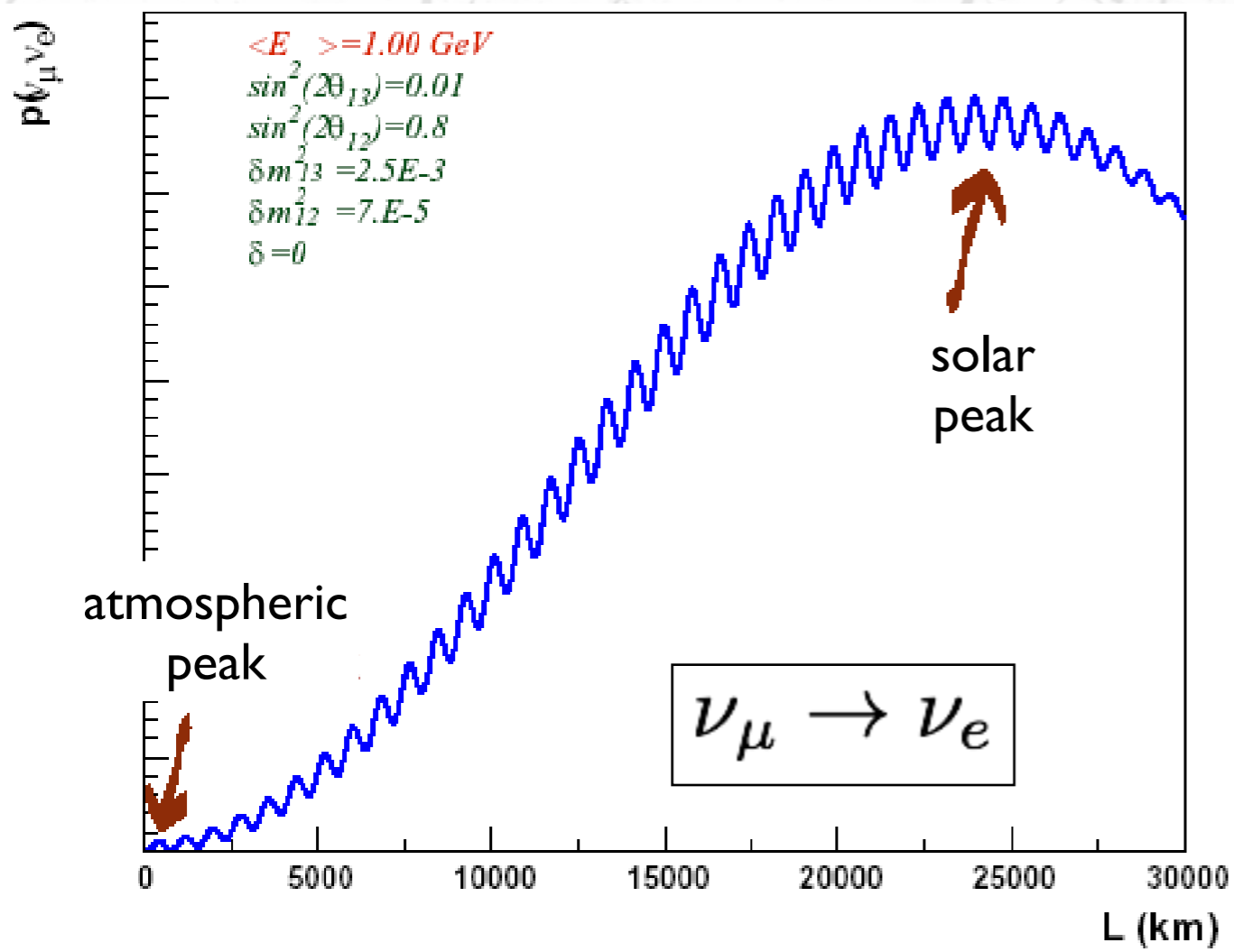


# Measuring $\theta_{13}$



Look for  $\nu_e$  appearance from  $\nu_\mu$  at atmospheric neutrino oscillations distances.

Look for  $\nu_e$  disappearance (like solar oscillations) at atmospheric neutrino oscillations distances.

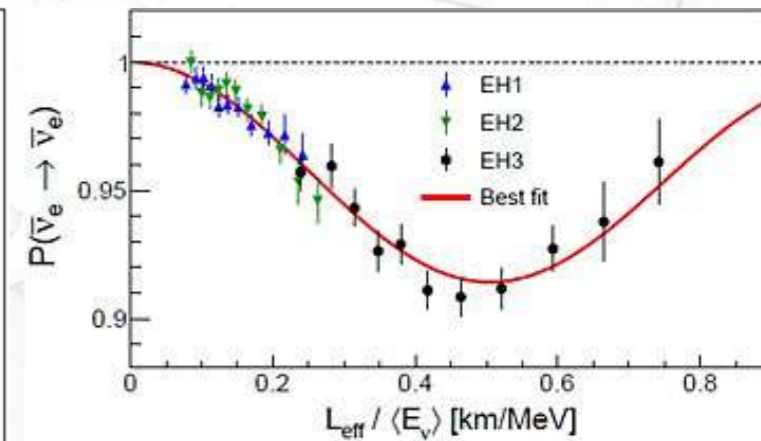
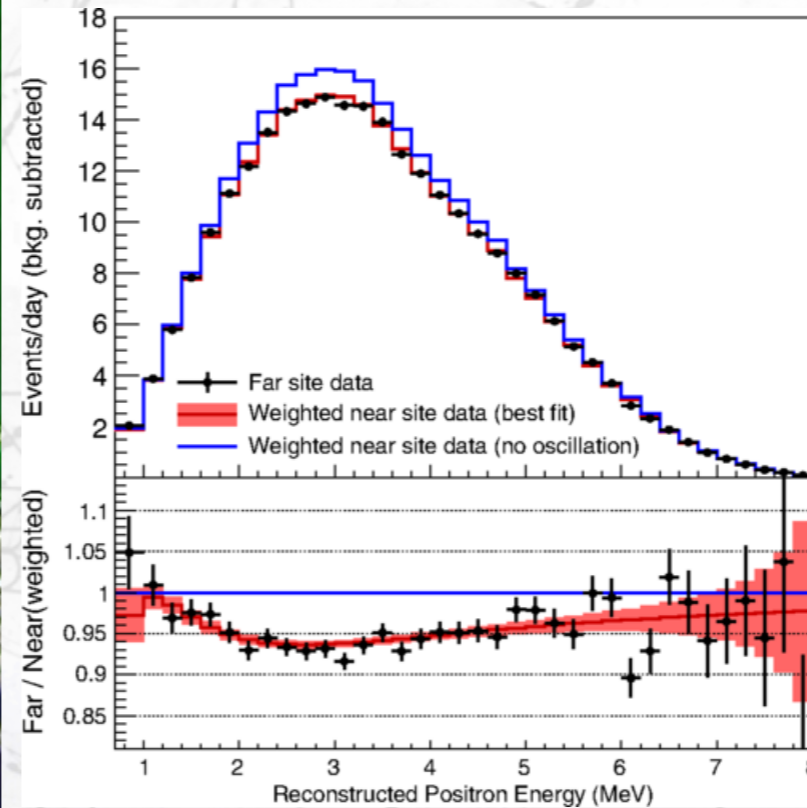




# Daya Bay



- Electron anti-neutrinos from a powerful nuclear power plant.
- Several sites & detectors (near and far)



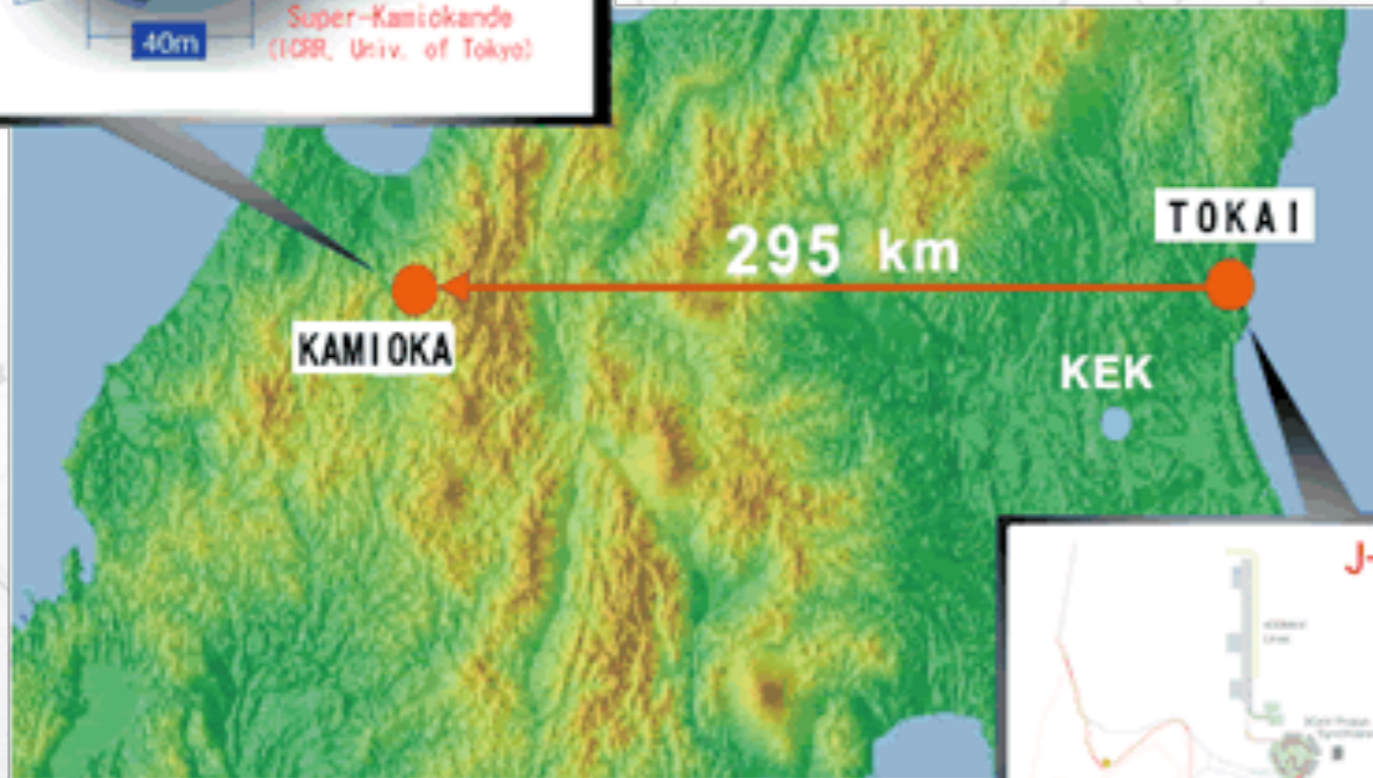
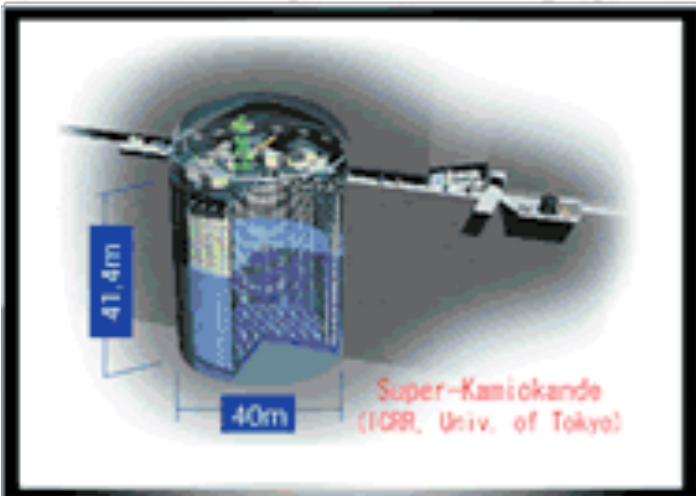
$$\sin^2 2\theta_{13} = 0.084 \pm 0.005$$

The most precise mixing angle measured so far.

Detection technique (inverse  $\beta$  decay) similar to the original Davis experiment.

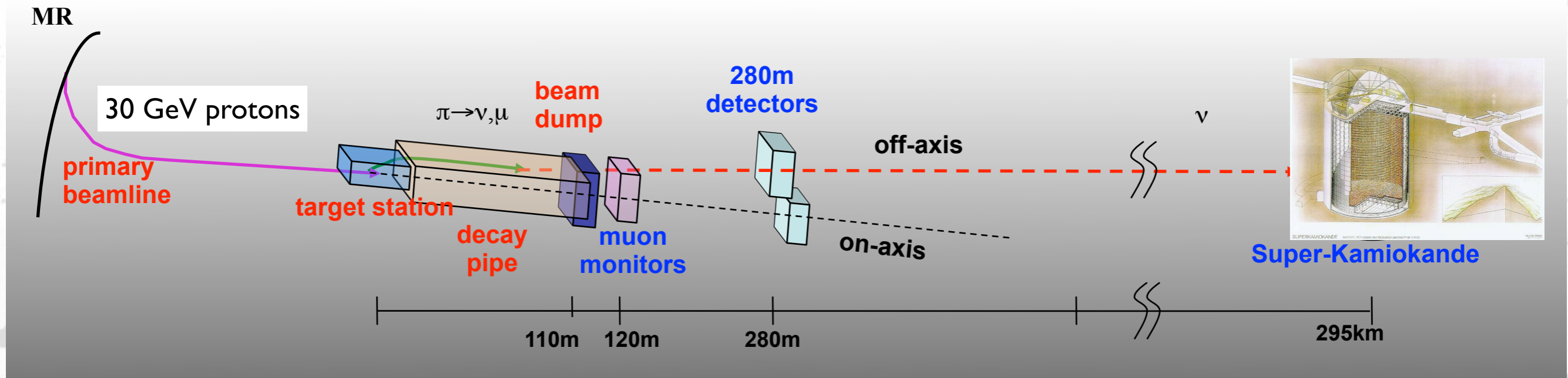






- High intensity  $\nu_{\mu}$  beam is produced at high intensity (400 kW) JPARC accelerator complex in Tokai.
- Neutrino flux measured at the near detector site prior to oscillations.
- Neutrinos are detected at the Super-Kamiokande detector at the west coast.

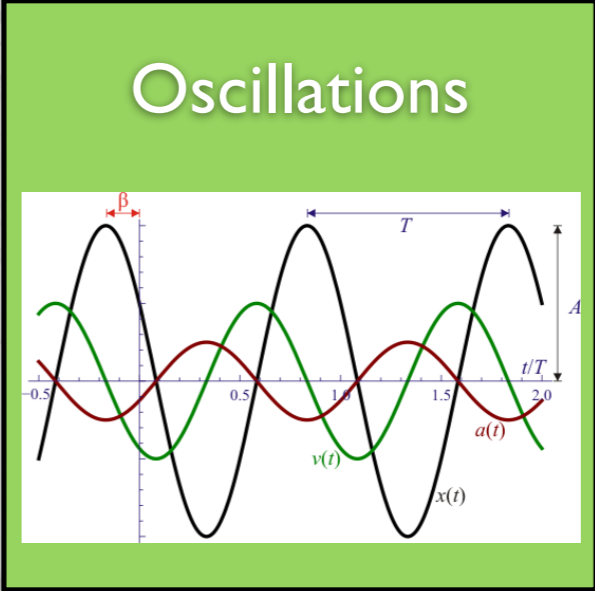




Neutrinos are produced in an accelerator:

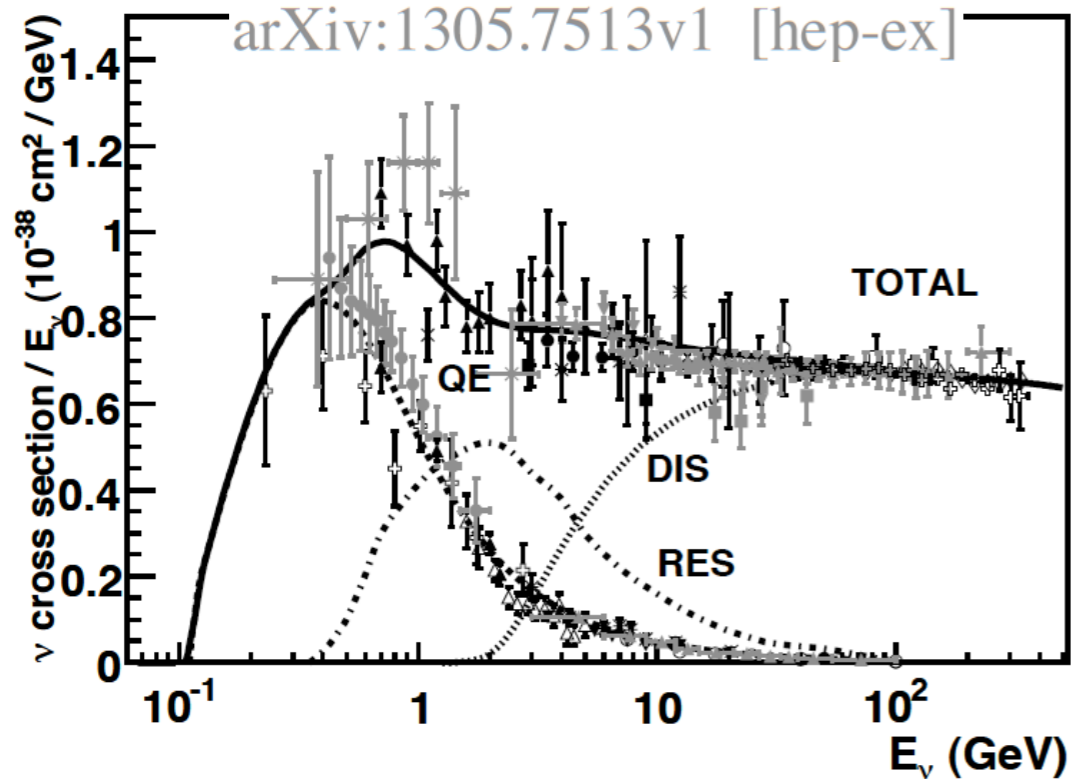
1. Protons produce pions that decay into muon neutrinos.
2. Pions are focused with a magnetic horn.

The flux is measured to reduce errors.



Measurement of oscillated flux.





Neutrino spectrum is always broad (we do not know how to make it mono-energetic)

We rely on the interaction to reconstruct the neutrino energy.

$E_\nu > 100 \text{ MeV}$  the  $\nu$ -Nucleus cross-section dominates.

Modelling of  $\nu$ -Nucleus is not trivial.

Charge current	
CC-QuasiElastic	$\nu_\mu n \rightarrow \mu^- p$
CC-Resonance	$\nu_\mu N \rightarrow \mu^- \pi^{+,0} N$
CC-Deep Inelastic	$\nu_\mu N \rightarrow \mu^- X$



# Cross-sections!



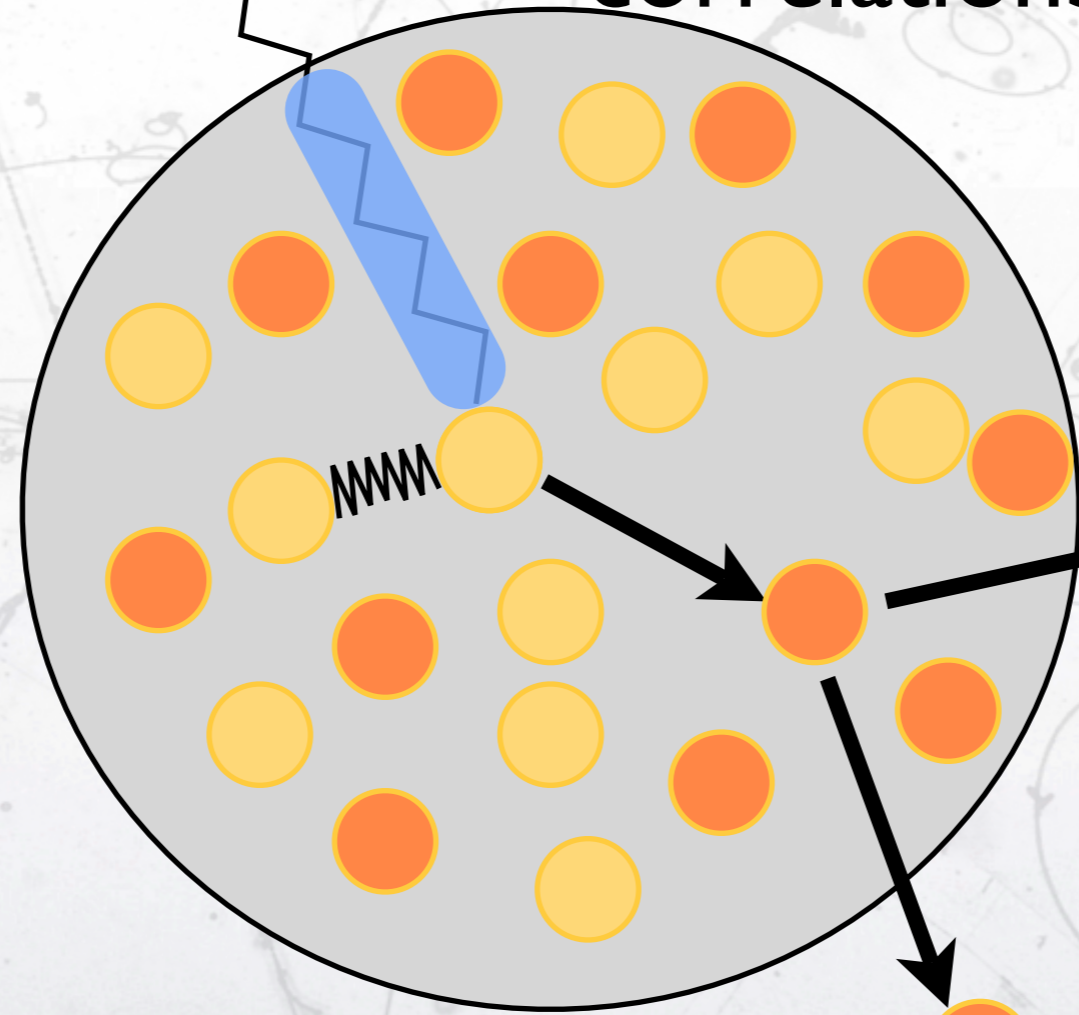
$v_l$

$|\pm$

Long range correlations

Fermi motion & Pauli blocking

Short range correlations



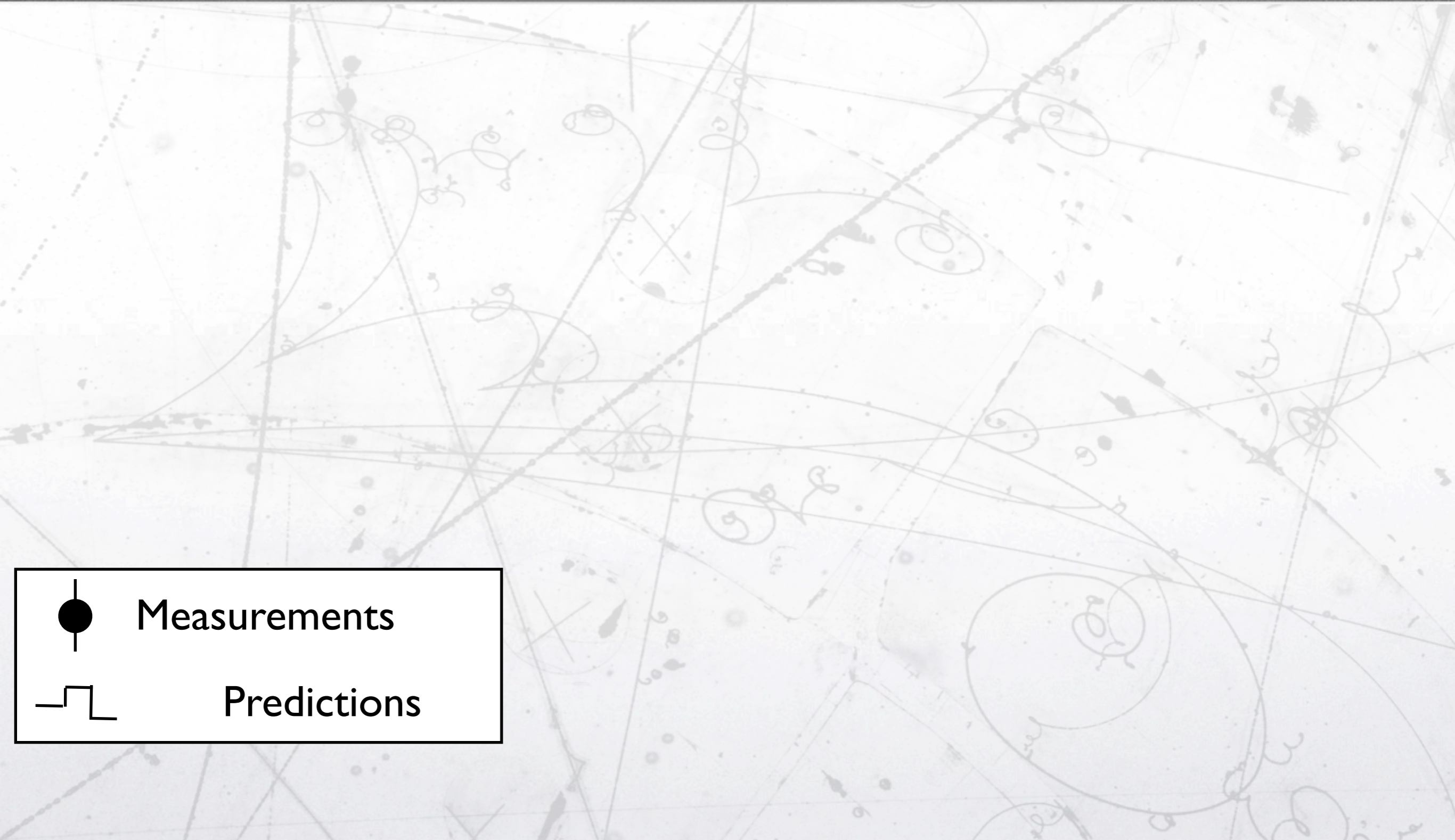
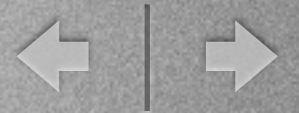
FSI

Nuclear physics!





# T2K measurement

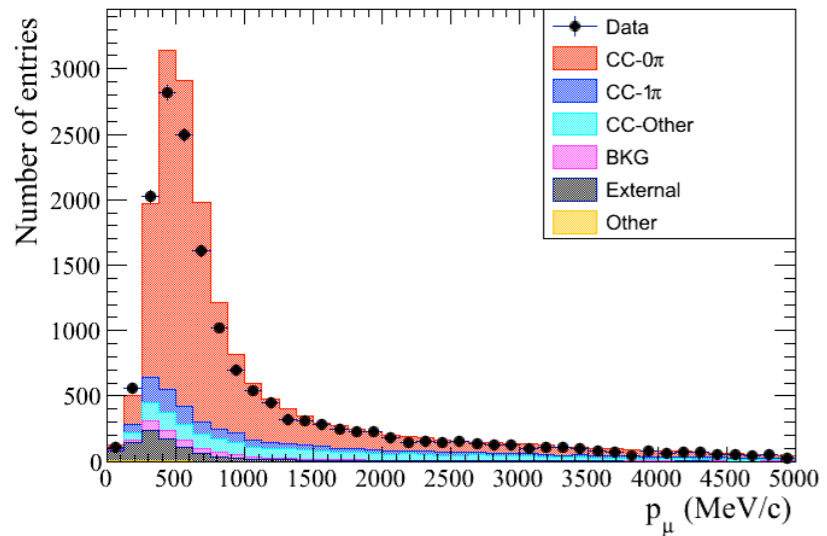


● Measurements  
▬ Predictions





## Measurement at the near detector

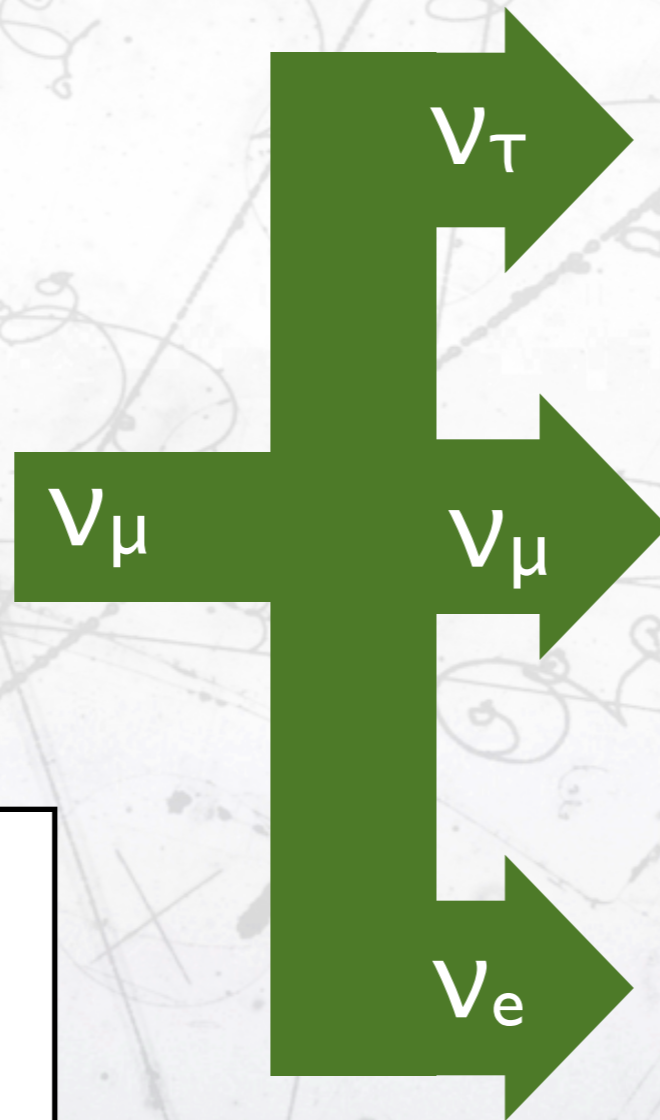
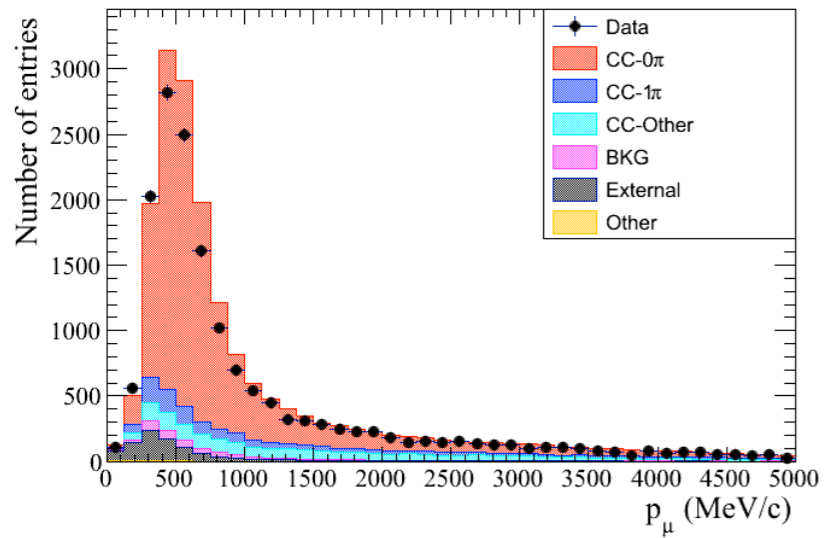




**Measurements**



**Predictions**



## Measurement at the near detector



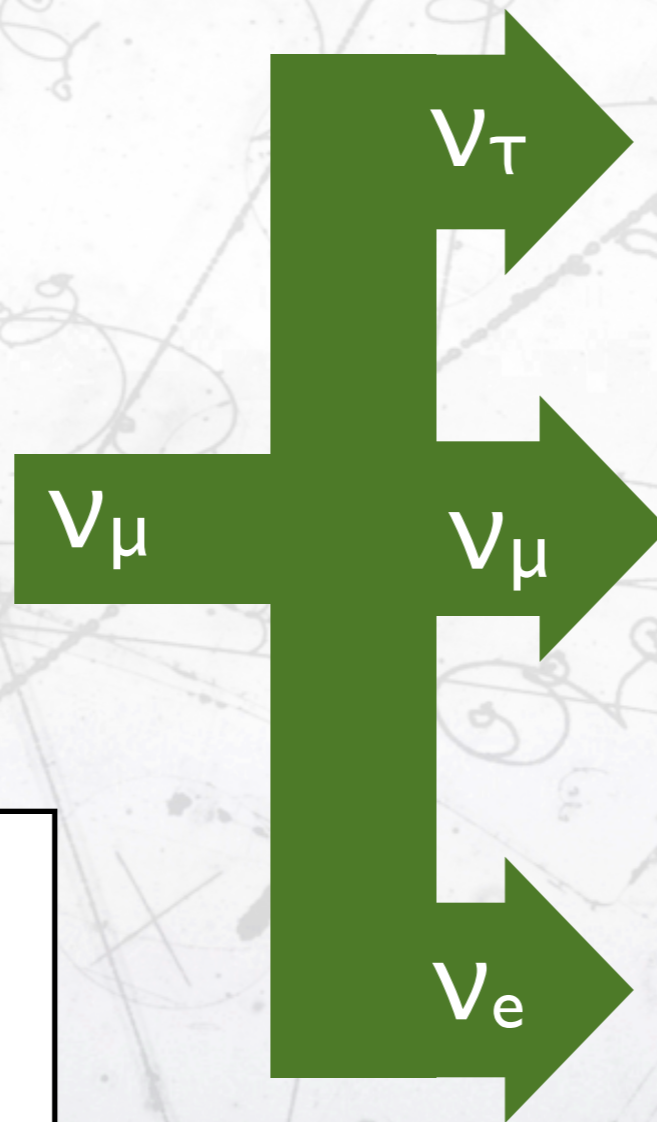
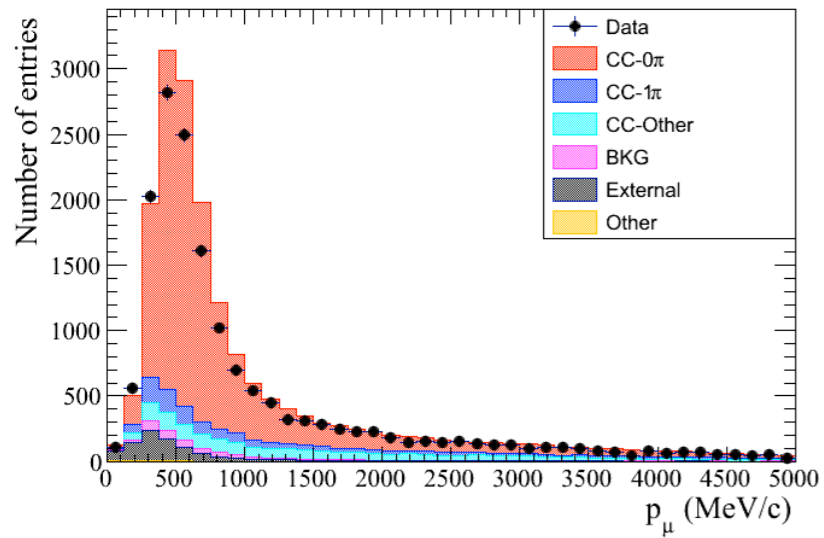

**Measurements**



**Predictions**




## Measurement at the near detector

## Super-Kamiokande



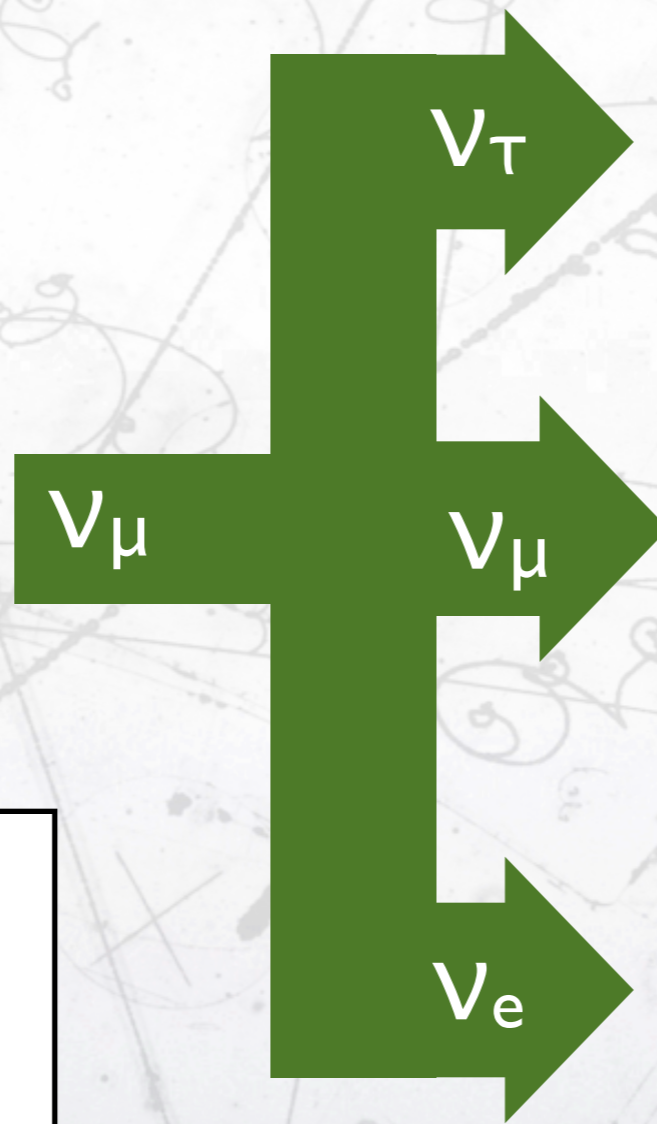
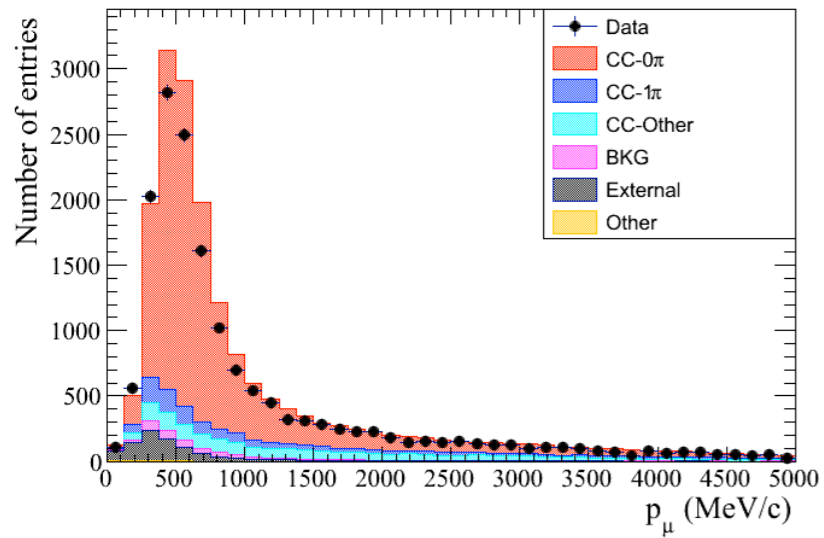

**Measurements**


**Predictions**



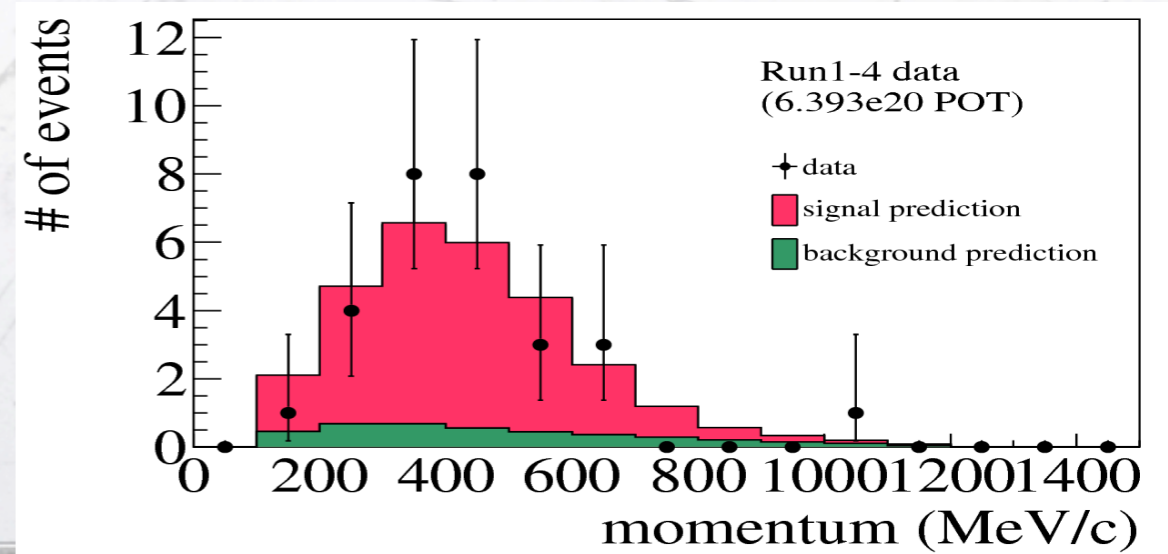
## Measurement at the near detector

## Super-Kamiokande



**Measurements**

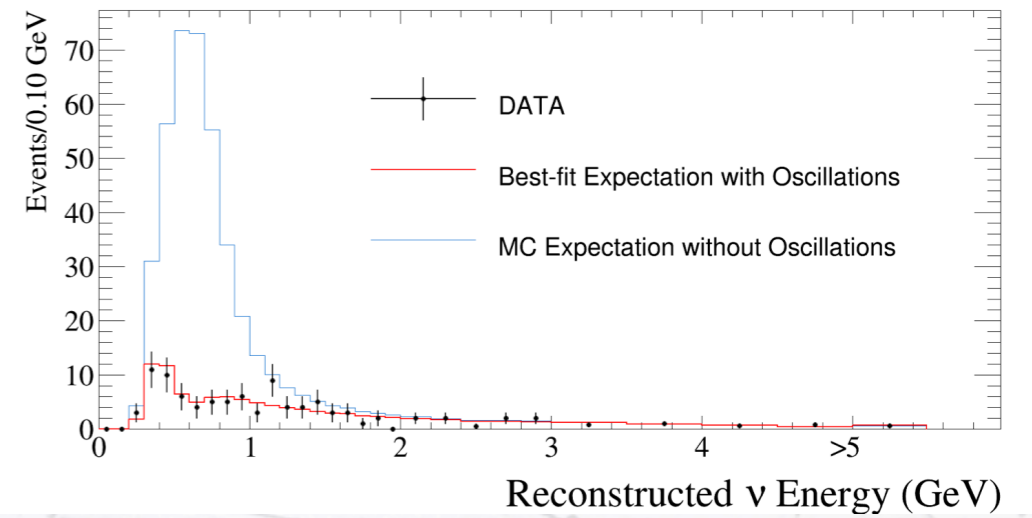
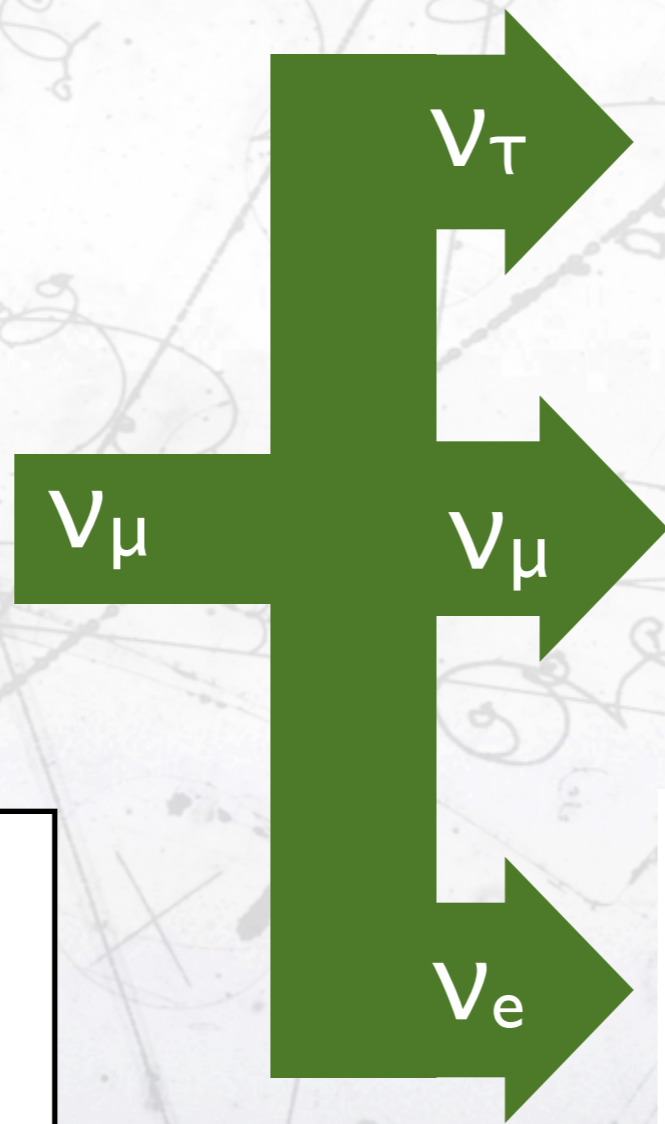
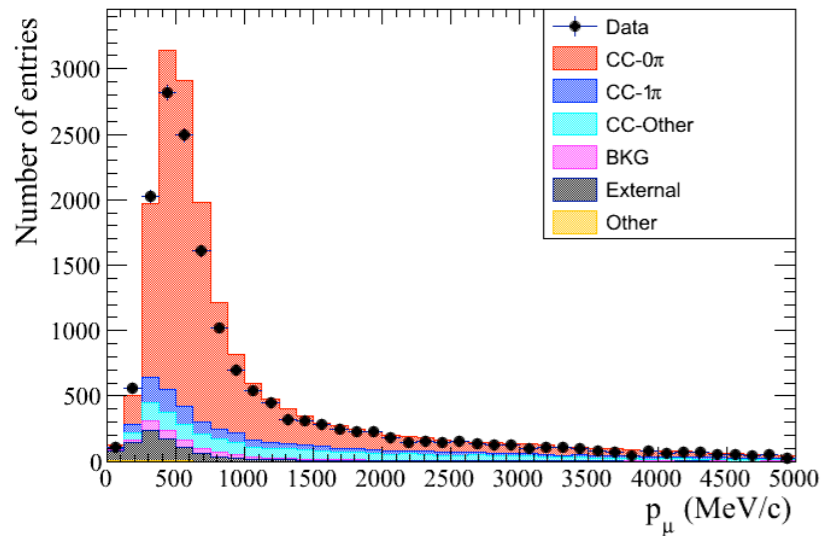
**Predictions**





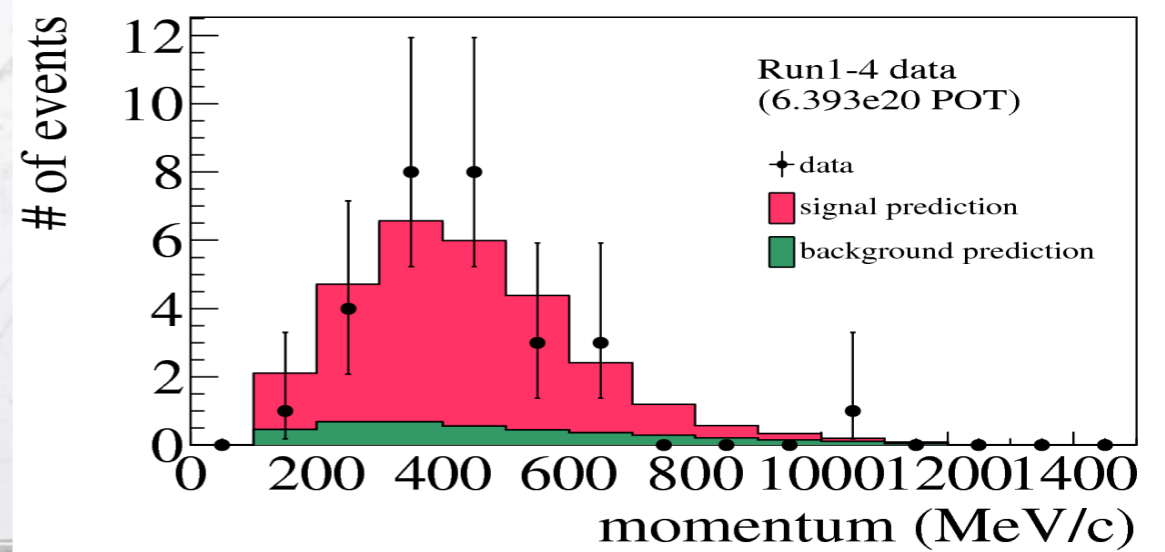
## Measurement at the near detector

## Super-Kamiokande



**Measurements**

**Predictions**

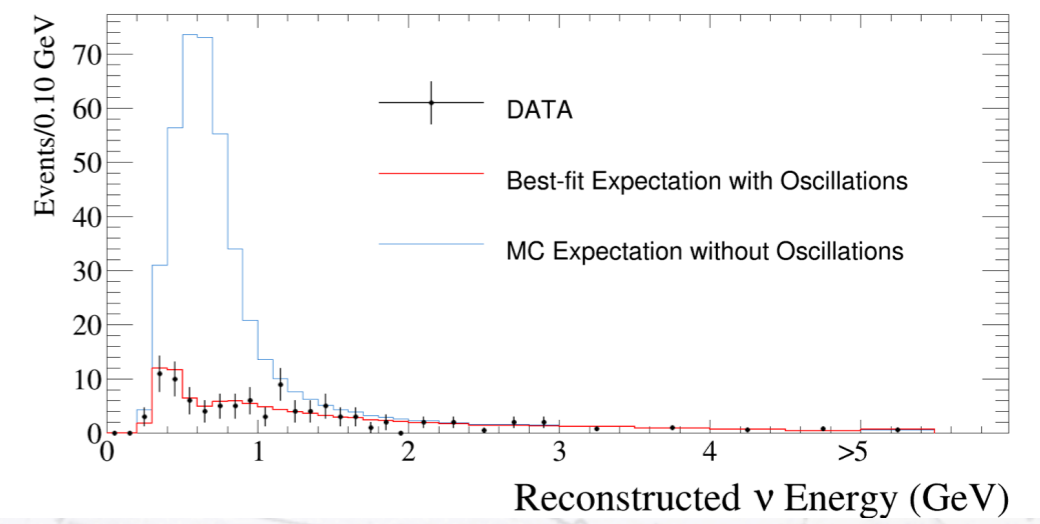
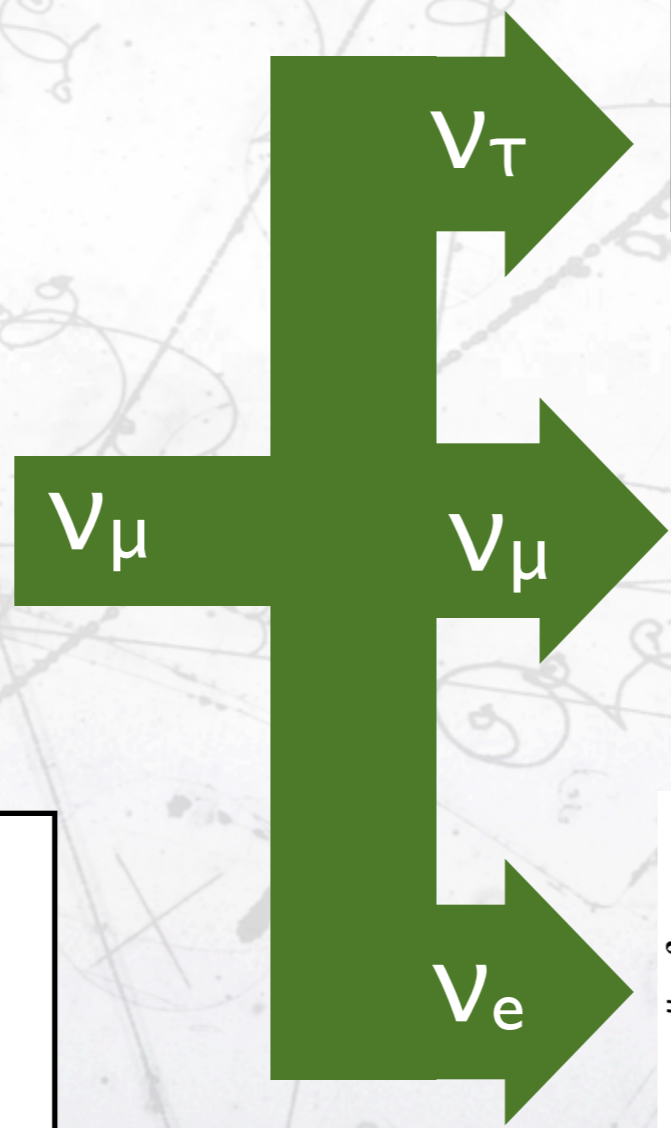
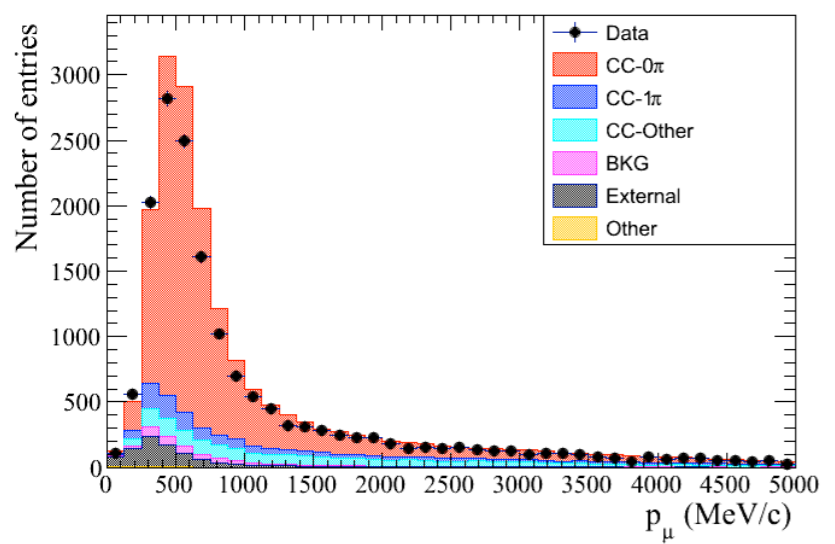






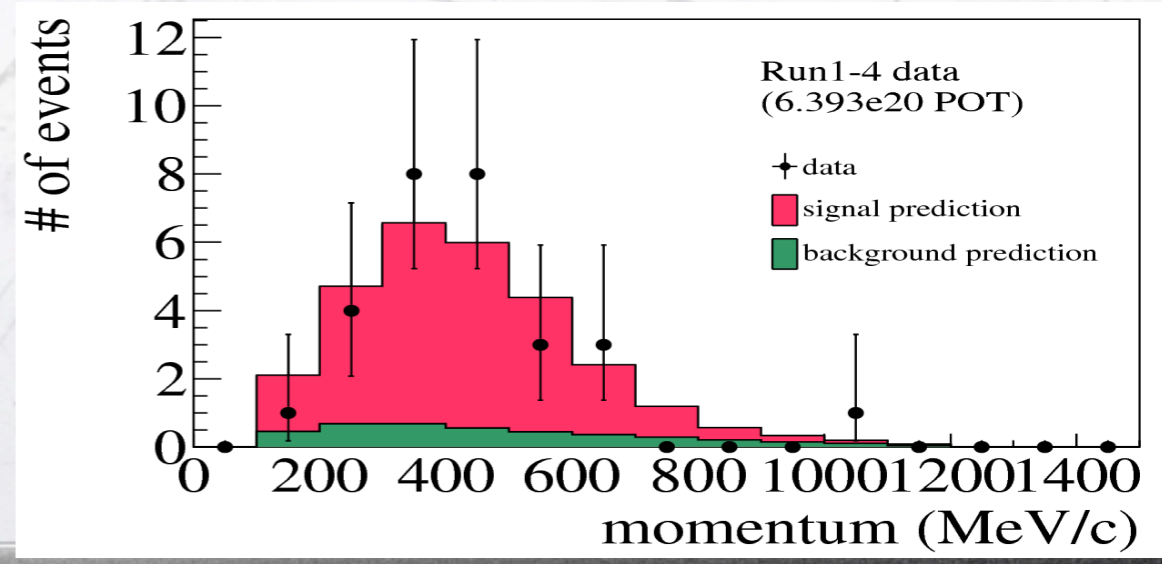
## Measurement at the near detector

## Super-Kamiokande

Invisible @ T2K  
Not enough energy.



 **Measurements**  
 **Predictions**

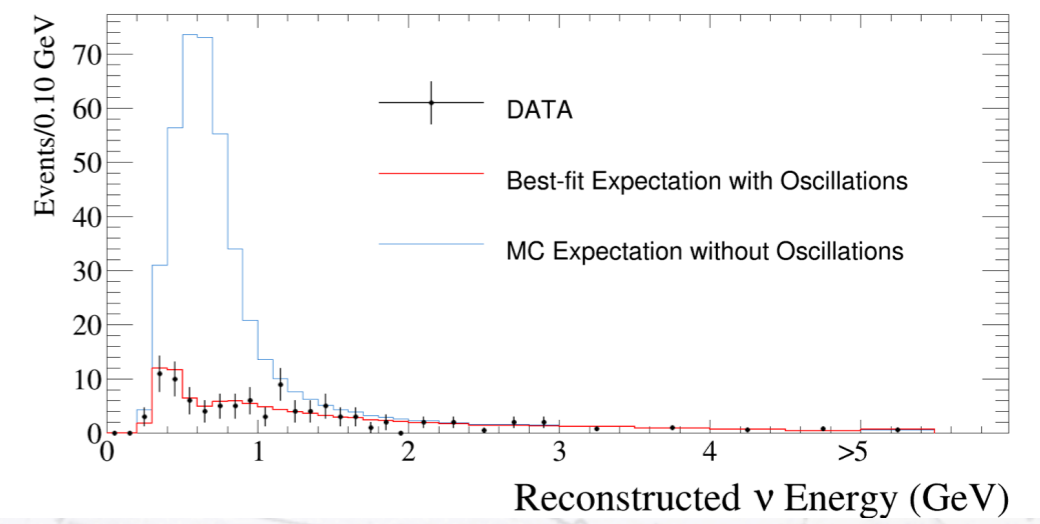
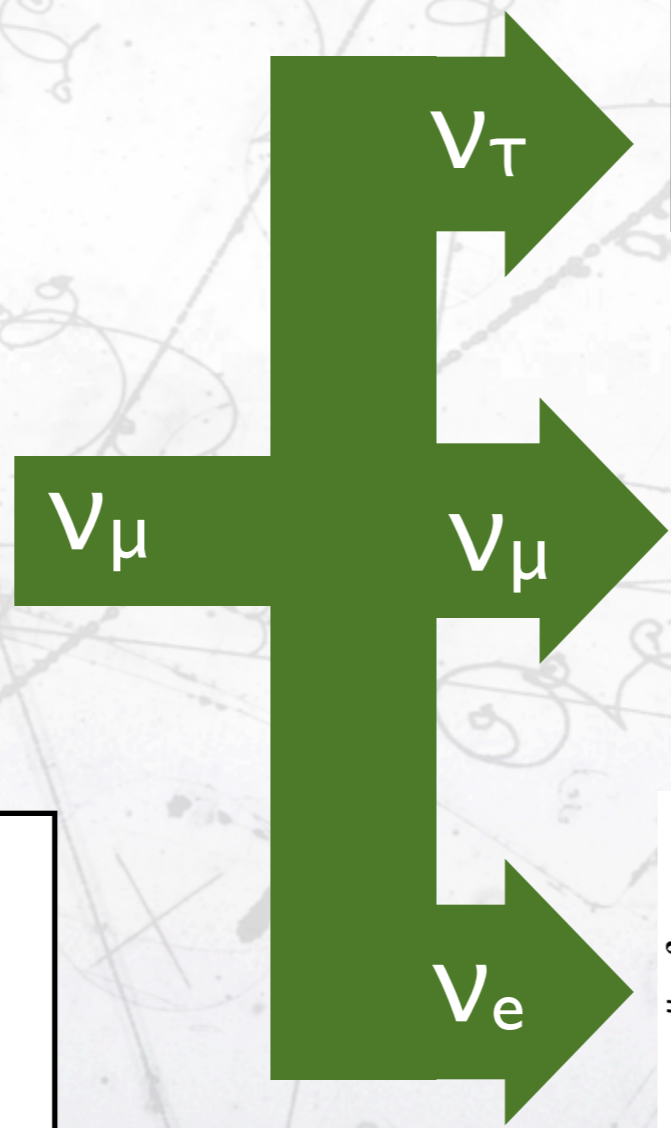
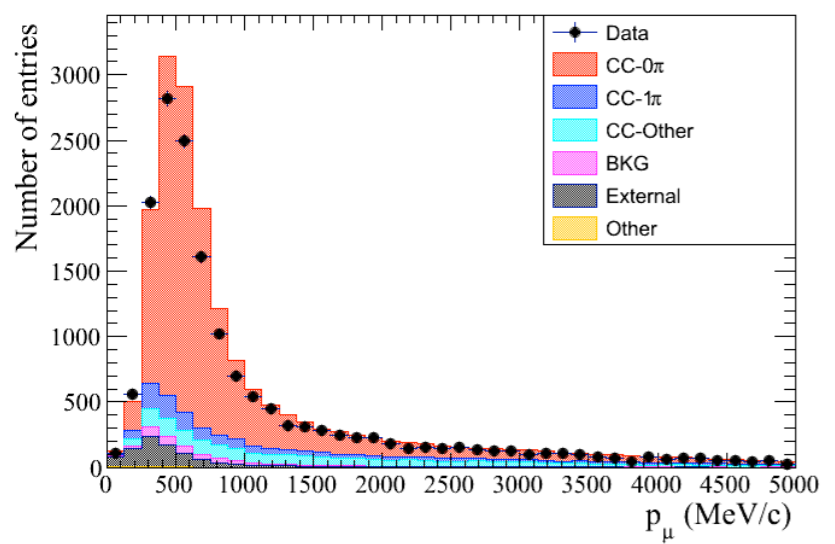






## Measurement at the near detector

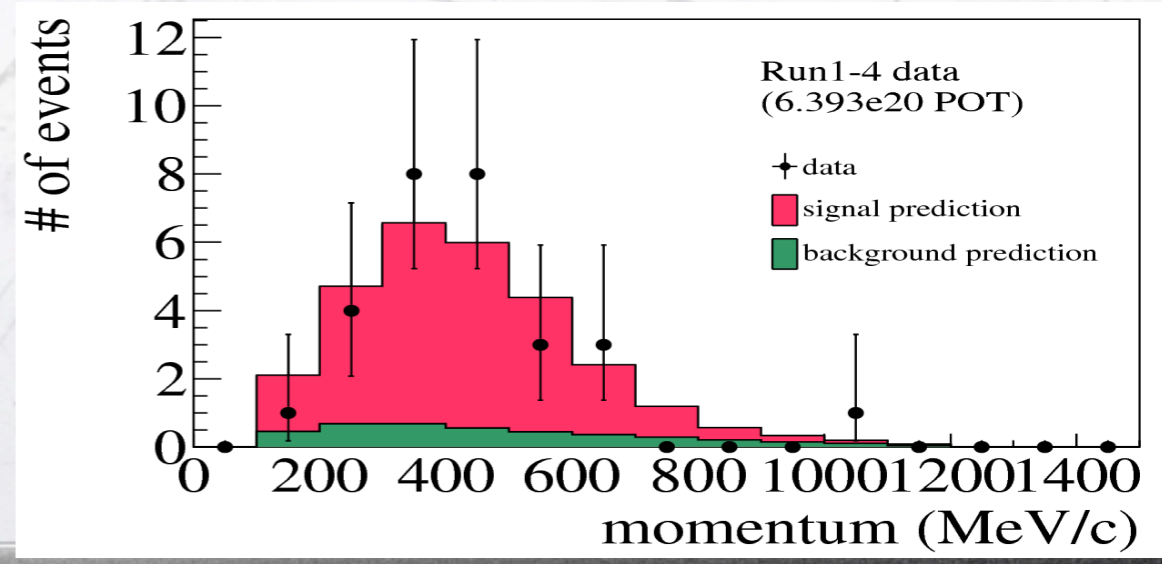
## Super-Kamiokande

Invisible @ T2K   
Not enough energy.



 Measurements

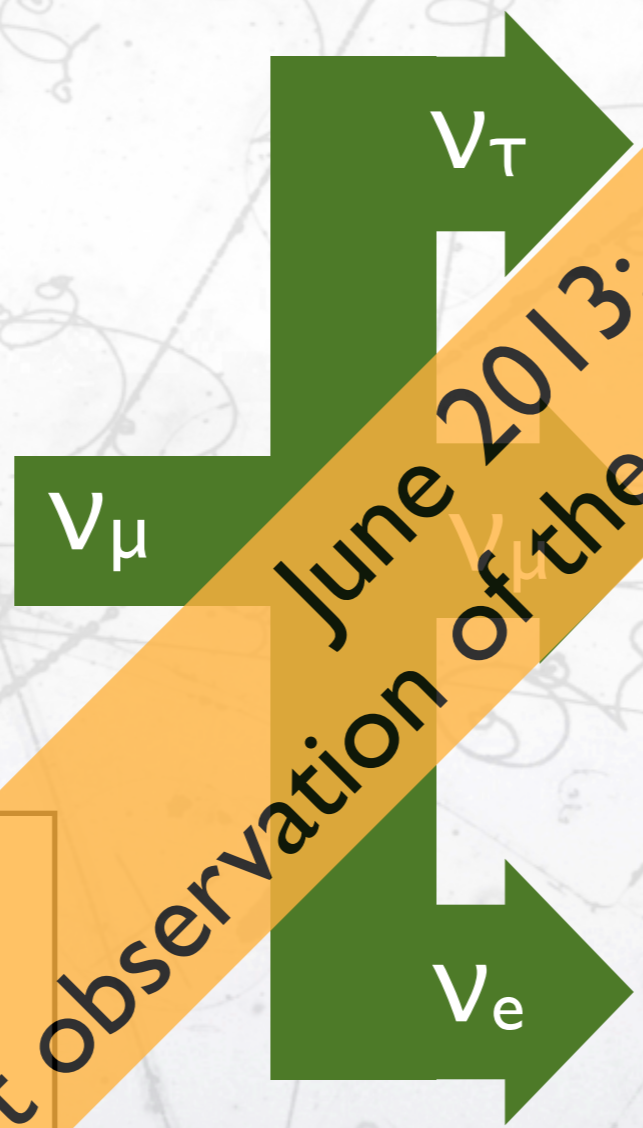
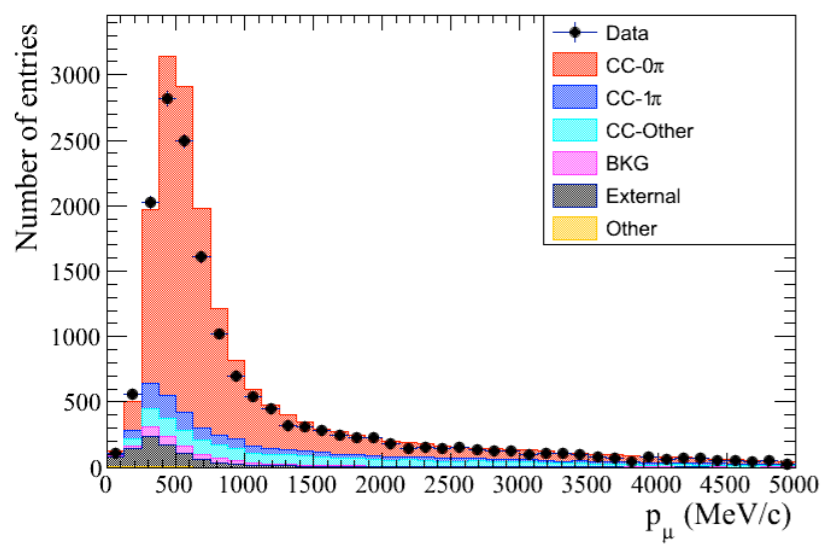
 Predictions



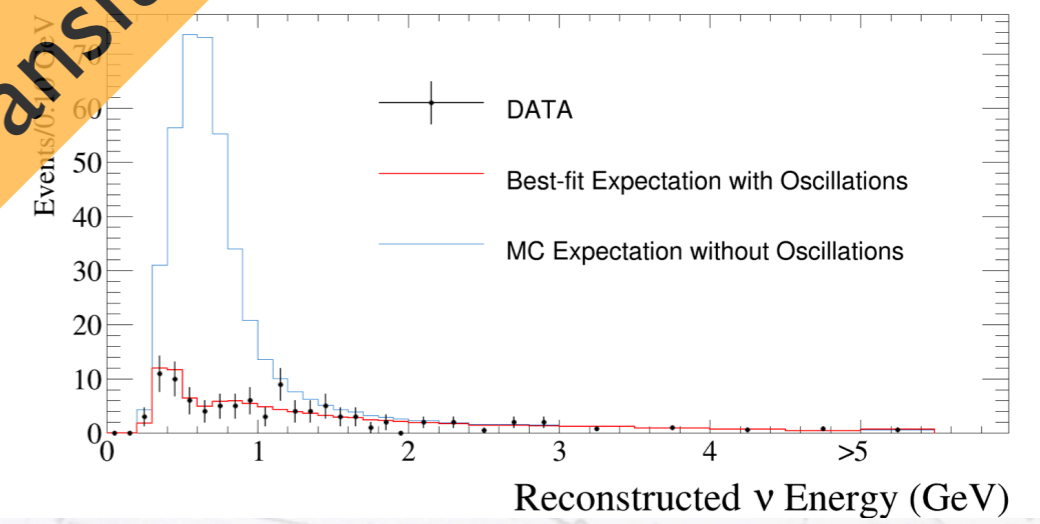


## Measurement at the near detector

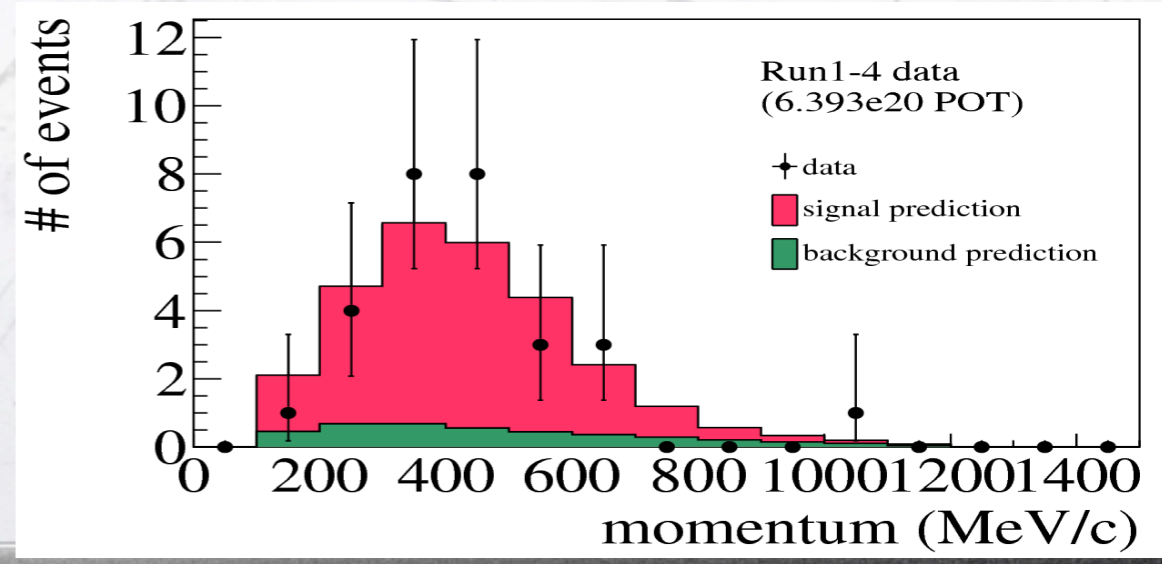
## Super-Kamiokande



Invisible @ T2K  
Not enough energy. 😞



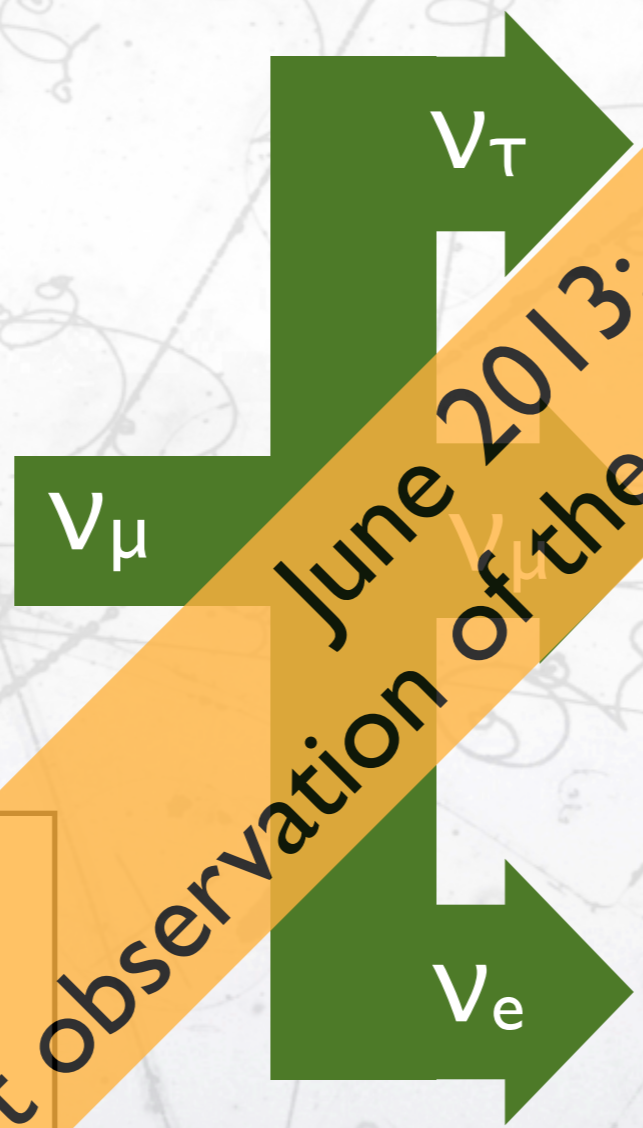
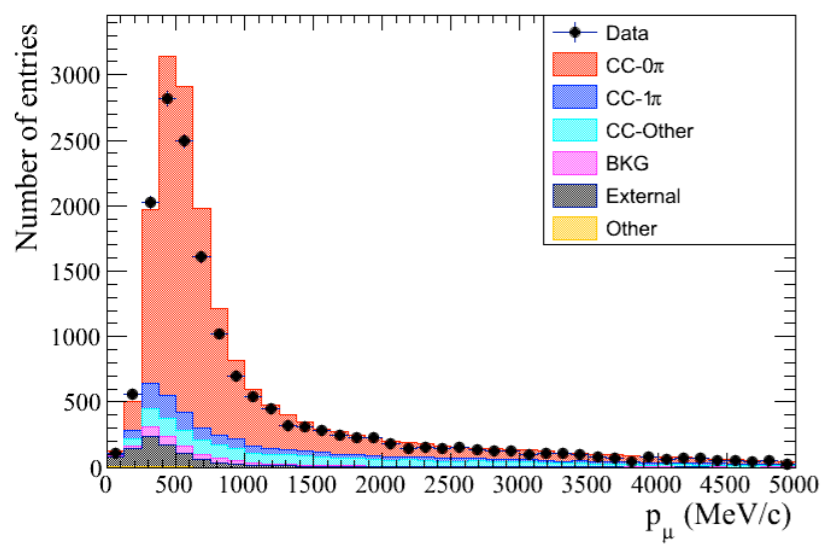
Measurements  
 Predictions



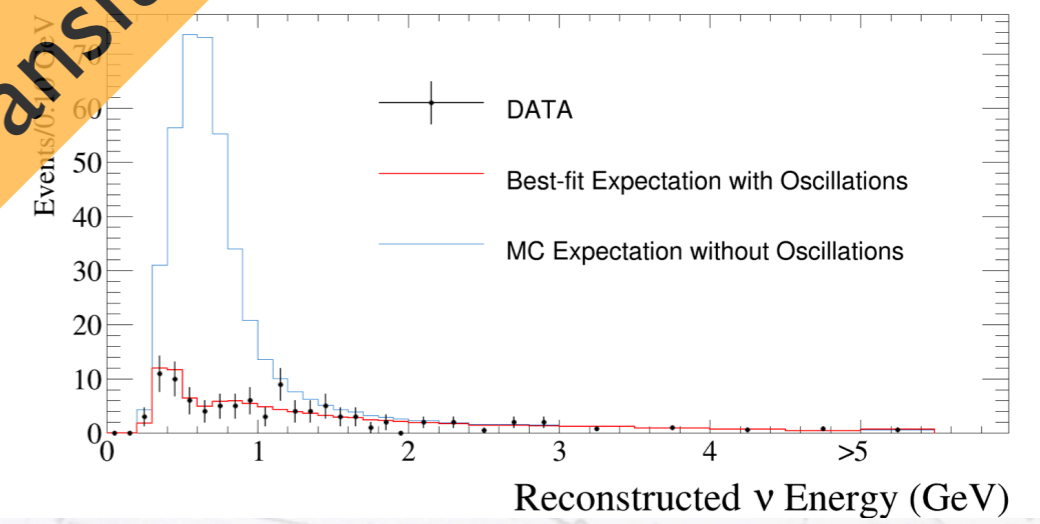




## Measurement at the near detector

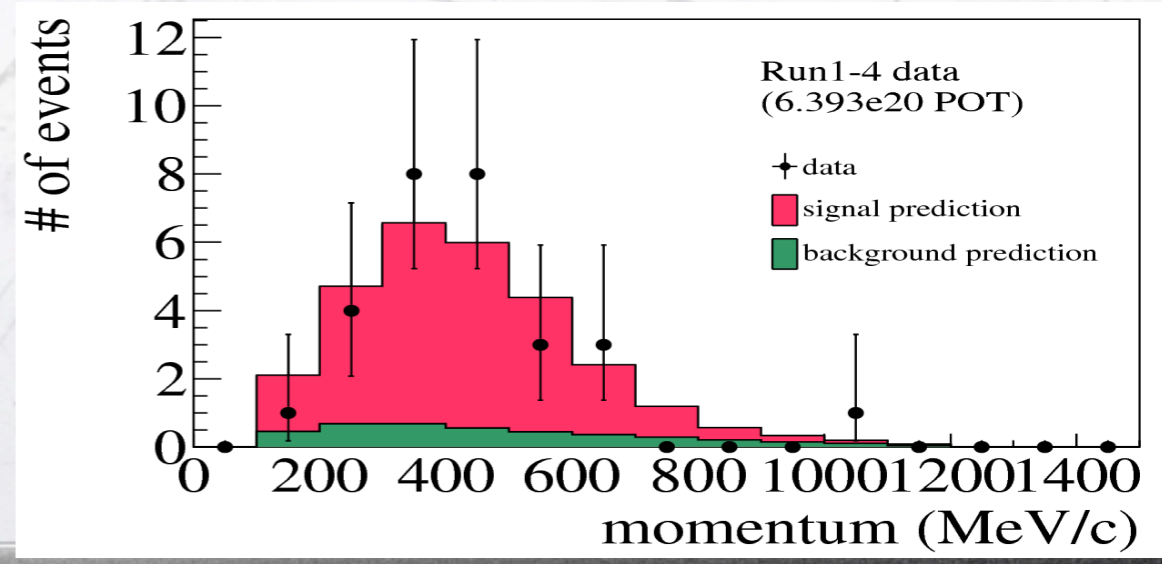
## Super-Kamiokande



Invisible @ T2K  
Not enough energy. 🙄



 Measurements  
 Predictions



Results confirmed by Nova Collab.



To measure CP we need  $\theta_{13} \neq 0$ . 🙌

## Direct CP violation determination

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \neq P(\nu_\mu \rightarrow \nu_e)$$

- ✓ Model independent.
- ✗ Inefficient to produce and detect anti-neutrinos.

## Indirect CP violation determination

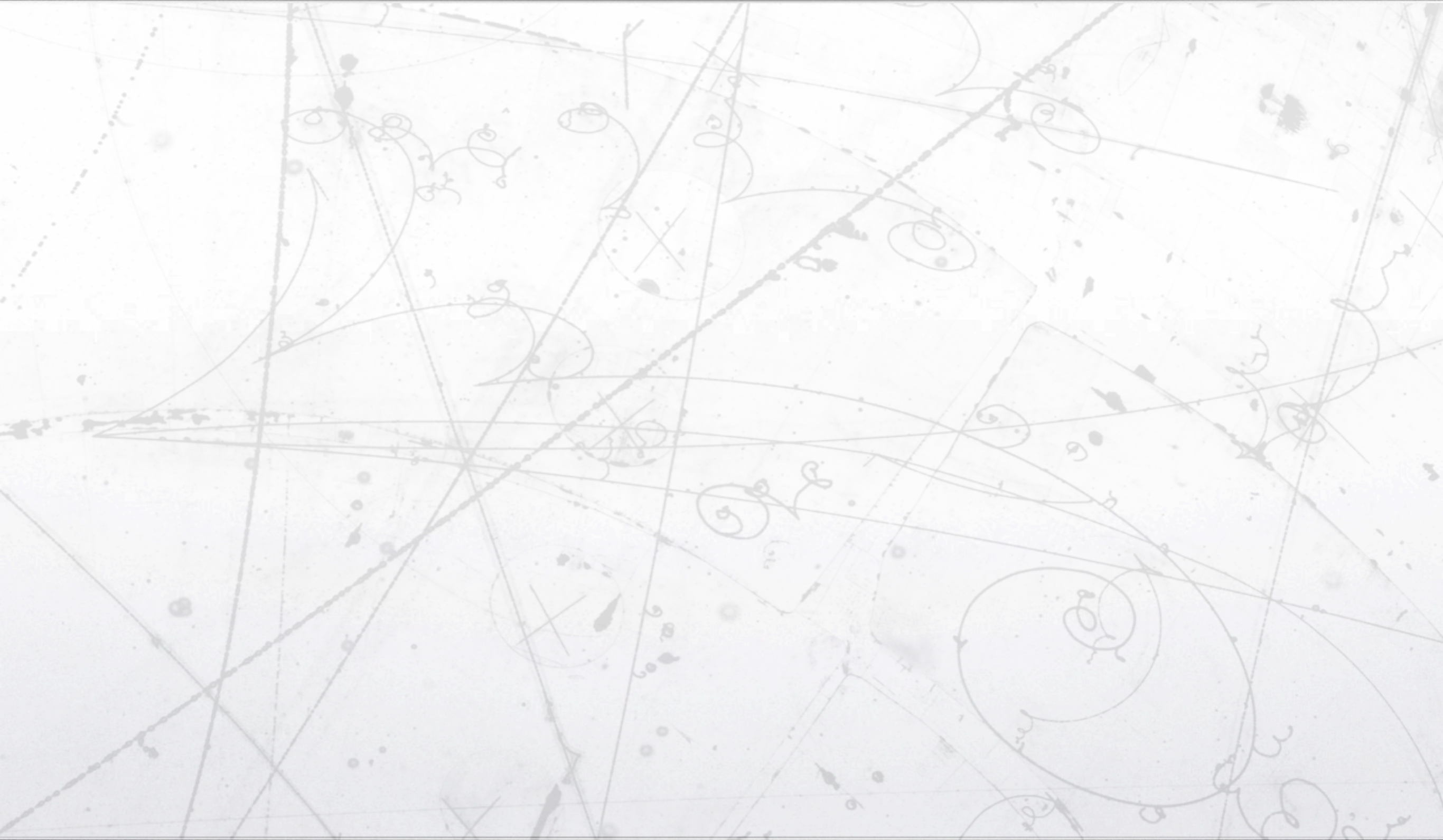
Compare  $P(\nu_\mu \rightarrow \nu_e)$  with  $P(\nu_e \rightarrow \nu_e)$

- ✗ Model dependent
- ✓  $\#\nu_\mu/\text{€} \gg \#\bar{\nu}_\mu/\text{€}$

Matter effects also alter the results differently for neutrinos and antineutrinos (matter is made of matter!) and for the sign of  $\Delta m^2$  (is  $m_3 > m_1$  ? hierarchy)

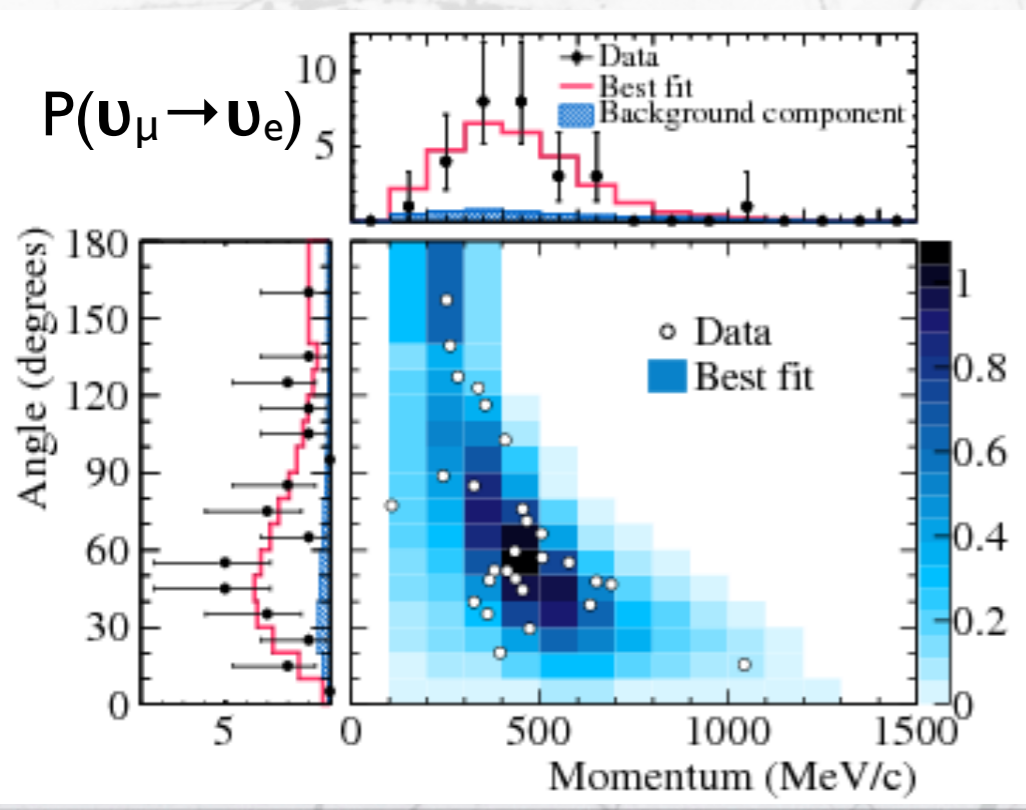
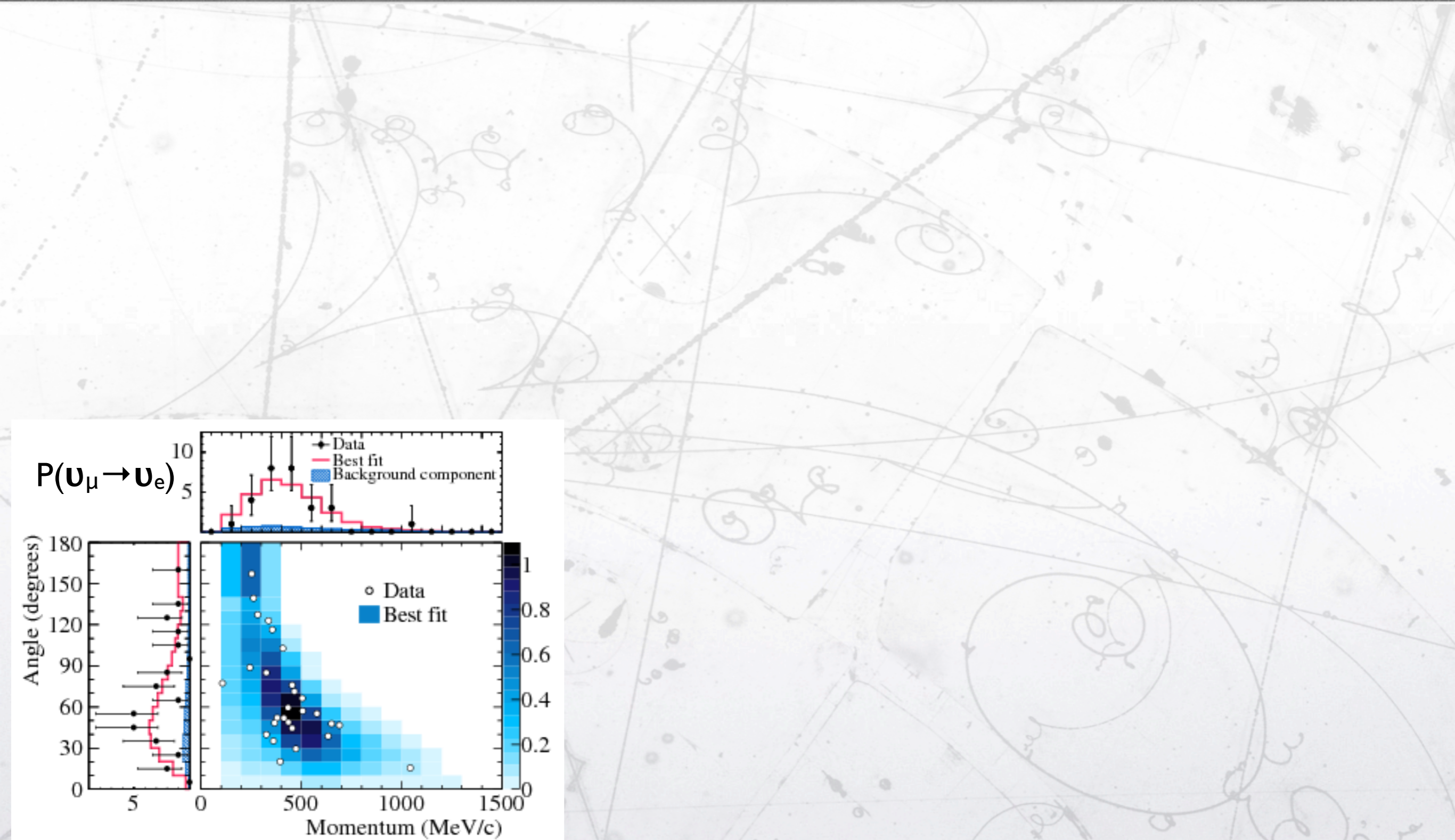


# CP violation



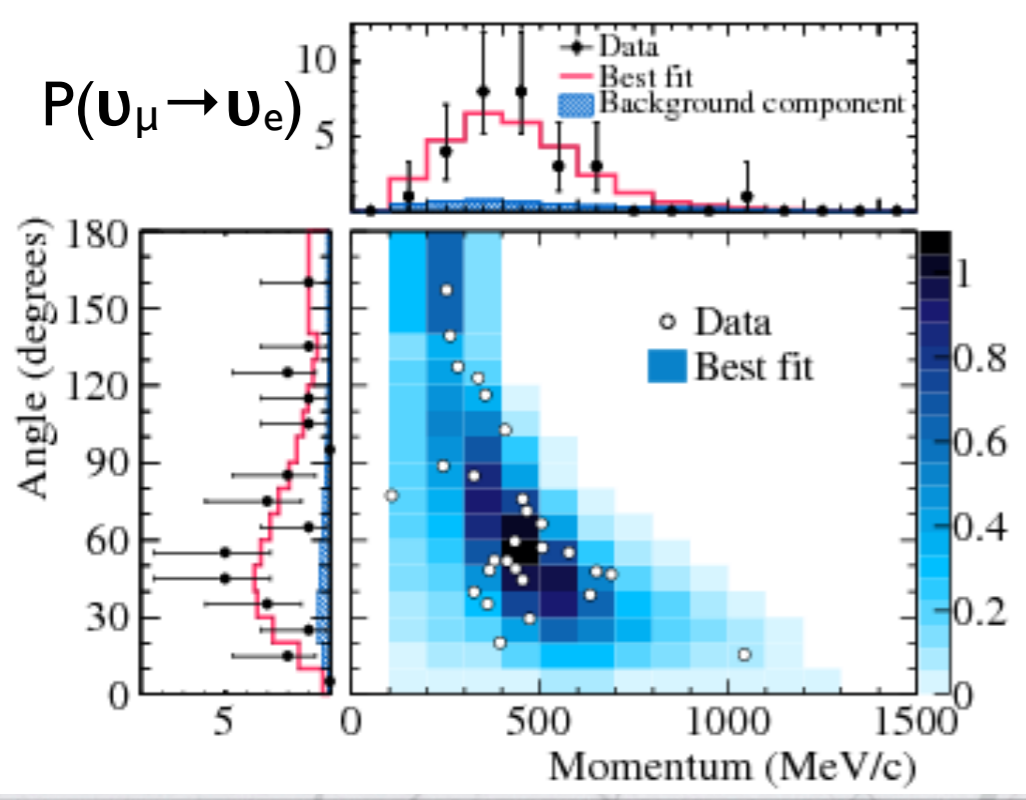
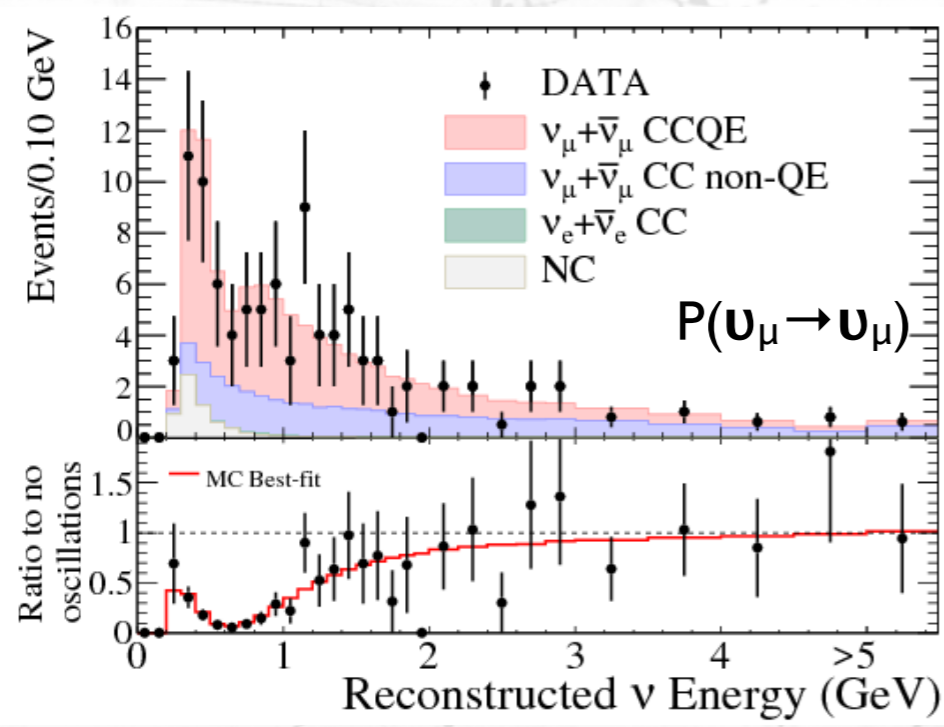


# CP violation



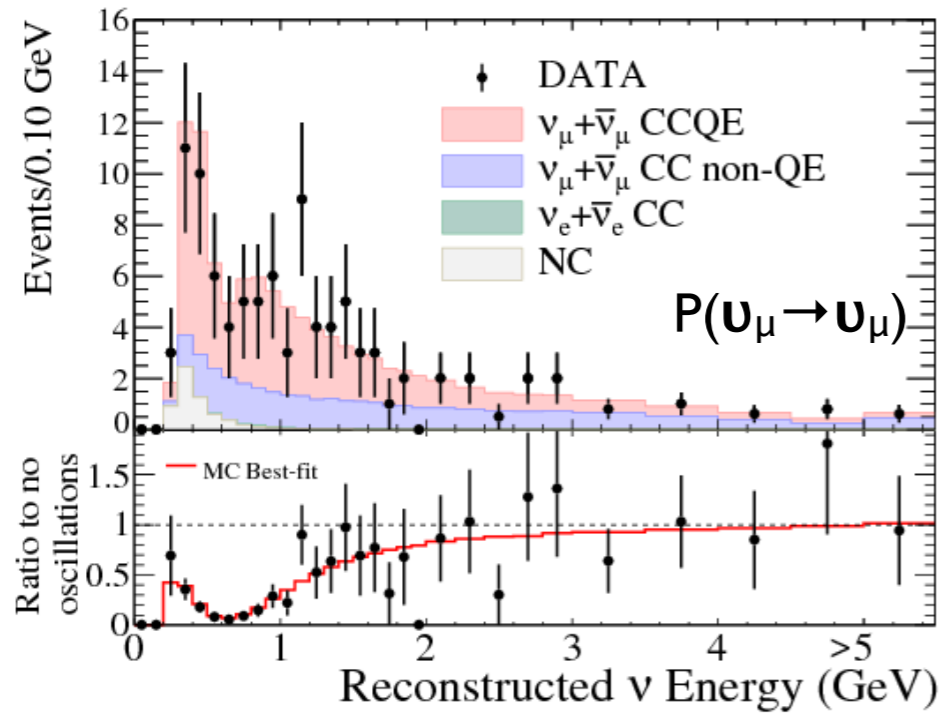


# CP violation

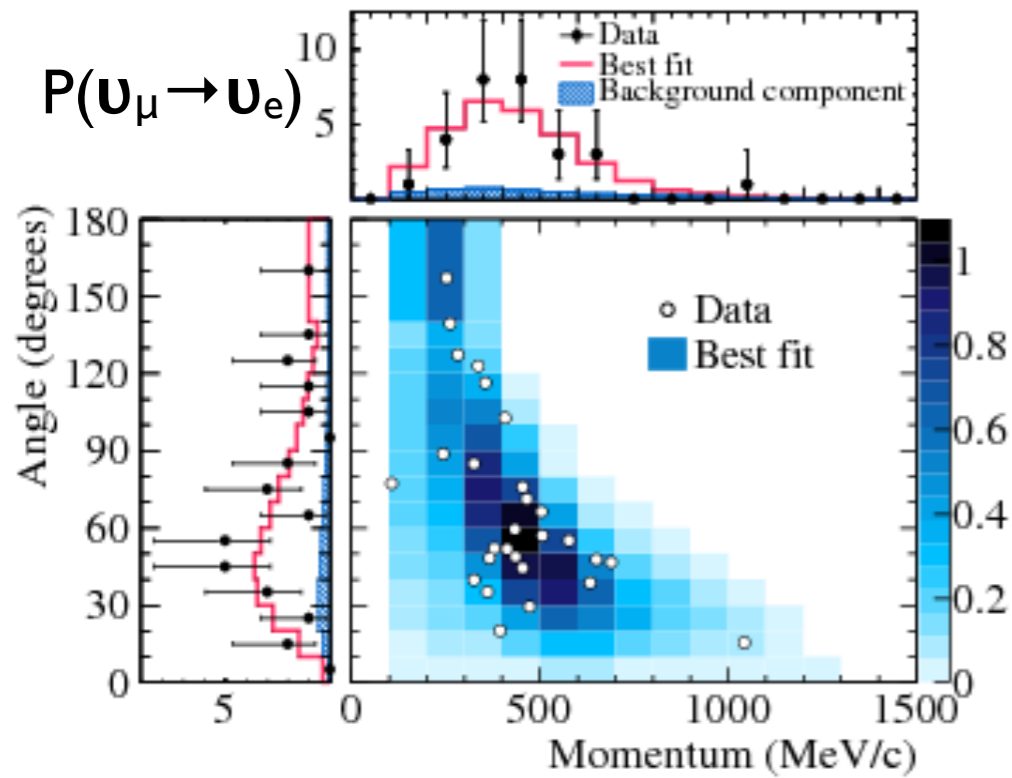




# CP violation

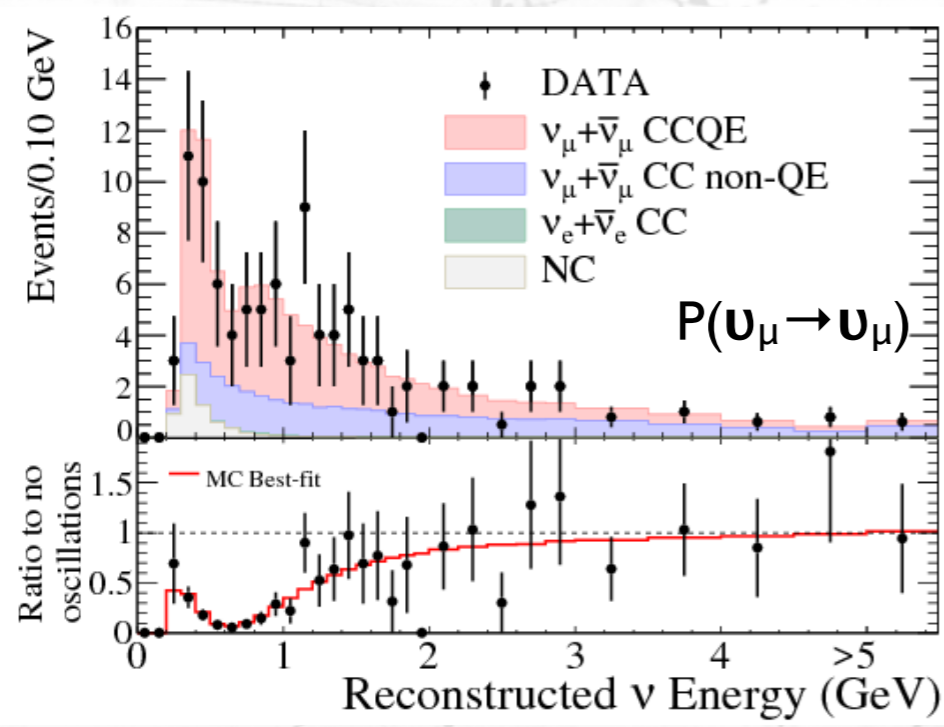


atmospheric  
 $\Theta_{23}$



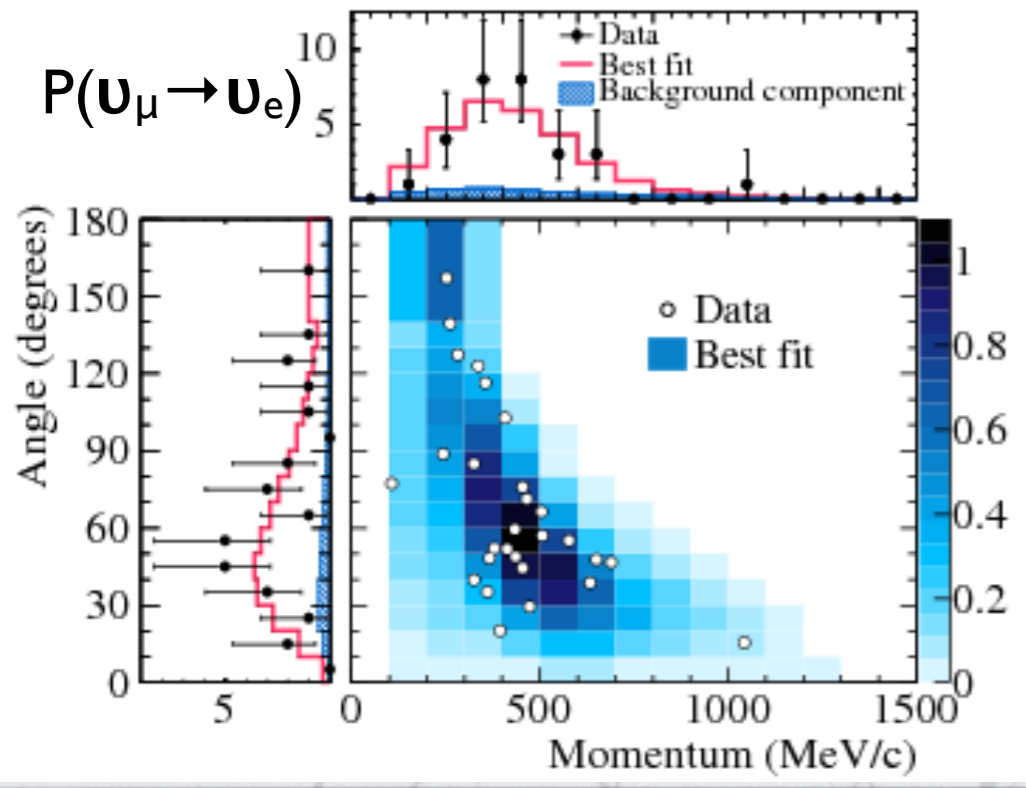


# CP violation



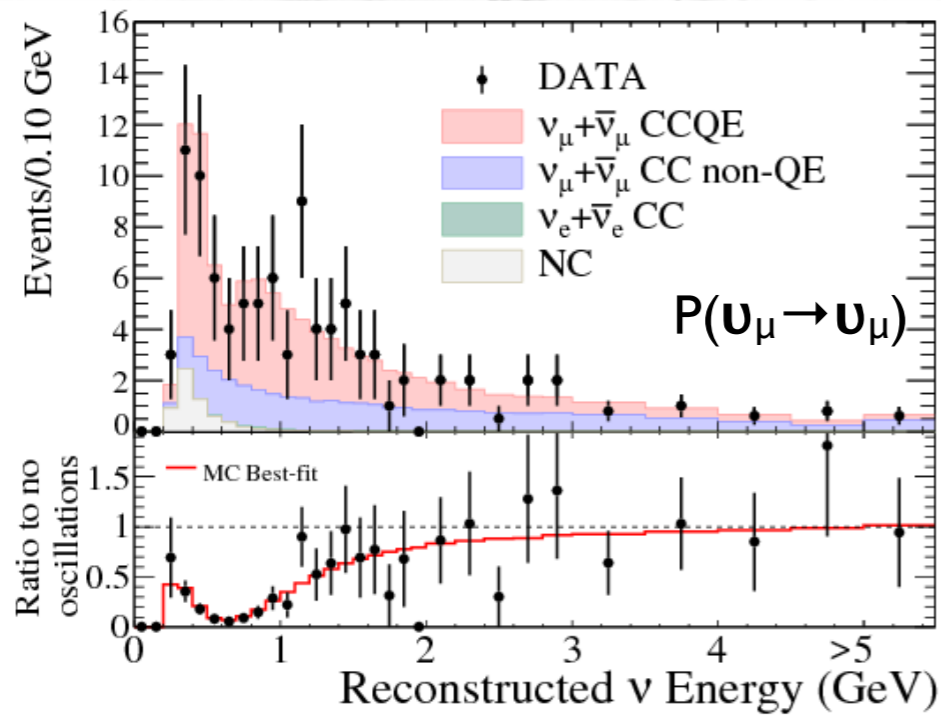
atmospheric  
 $\Theta_{23}$

Solar  
 $\Theta_{12}$



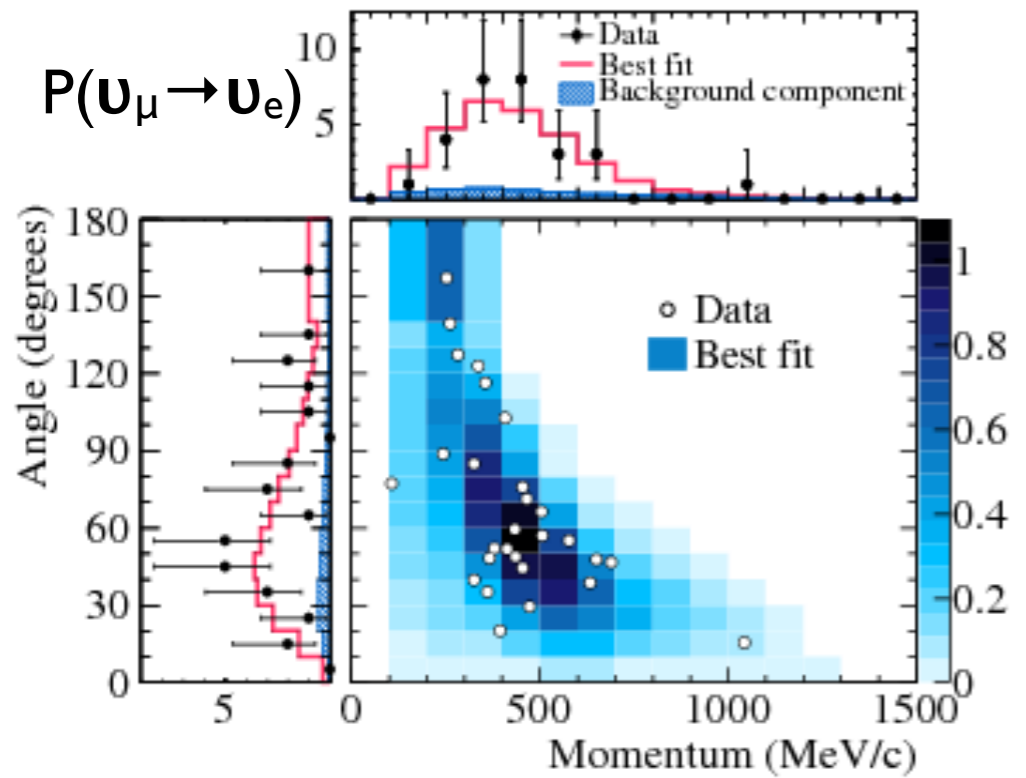


# CP violation



atmospheric  
 $\Theta_{23}$

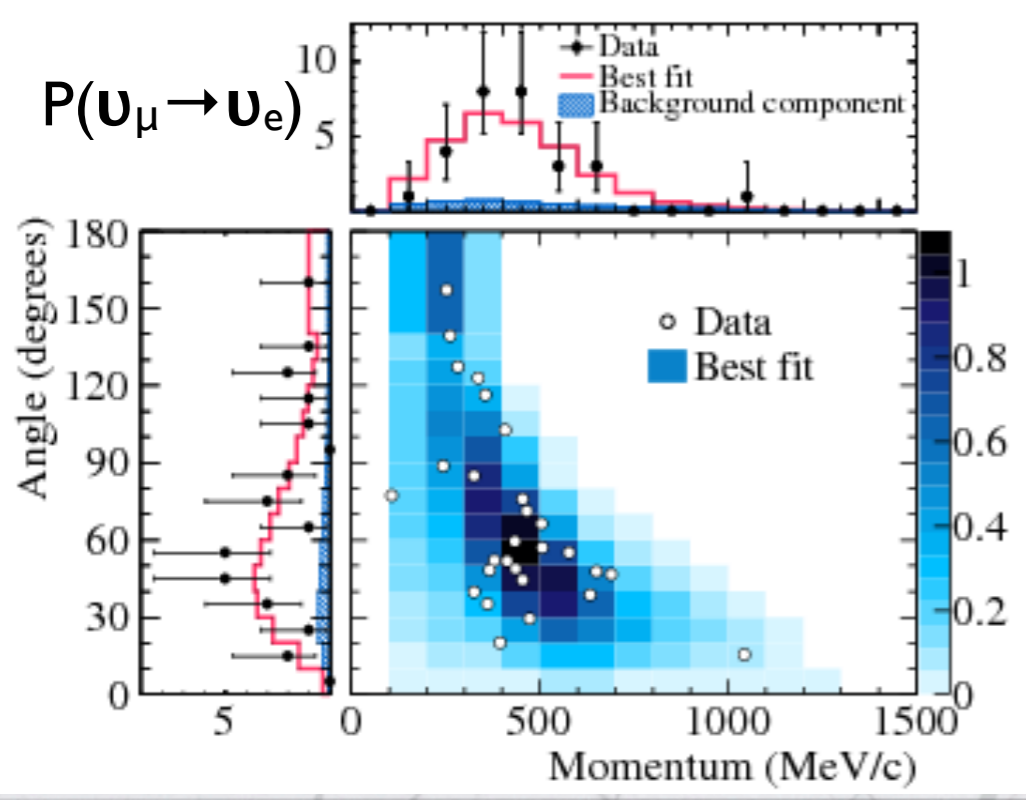
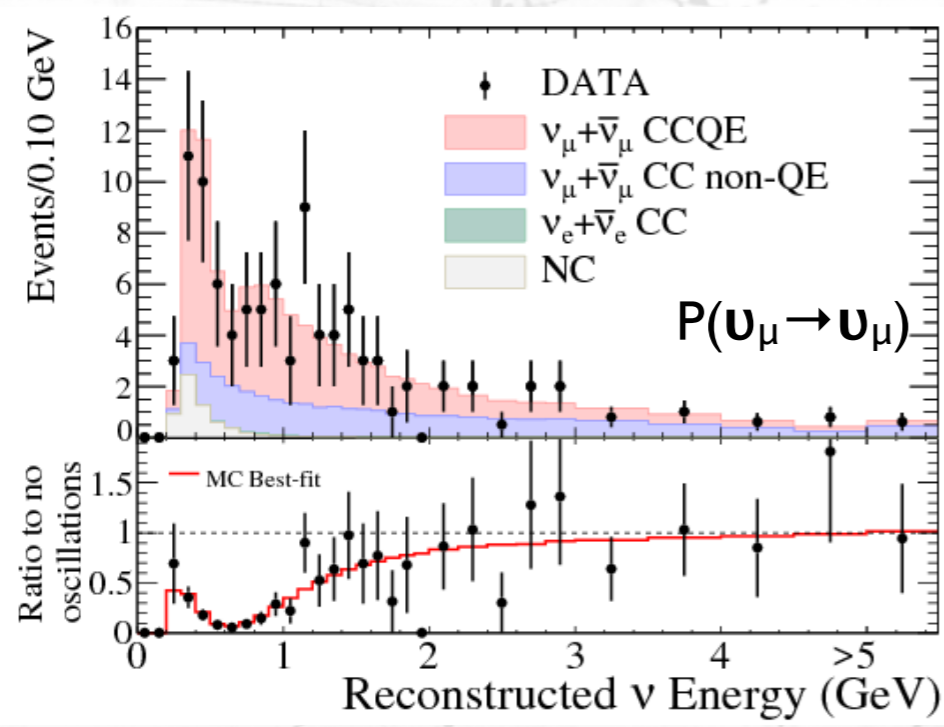
Solar  
 $\Theta_{12}$



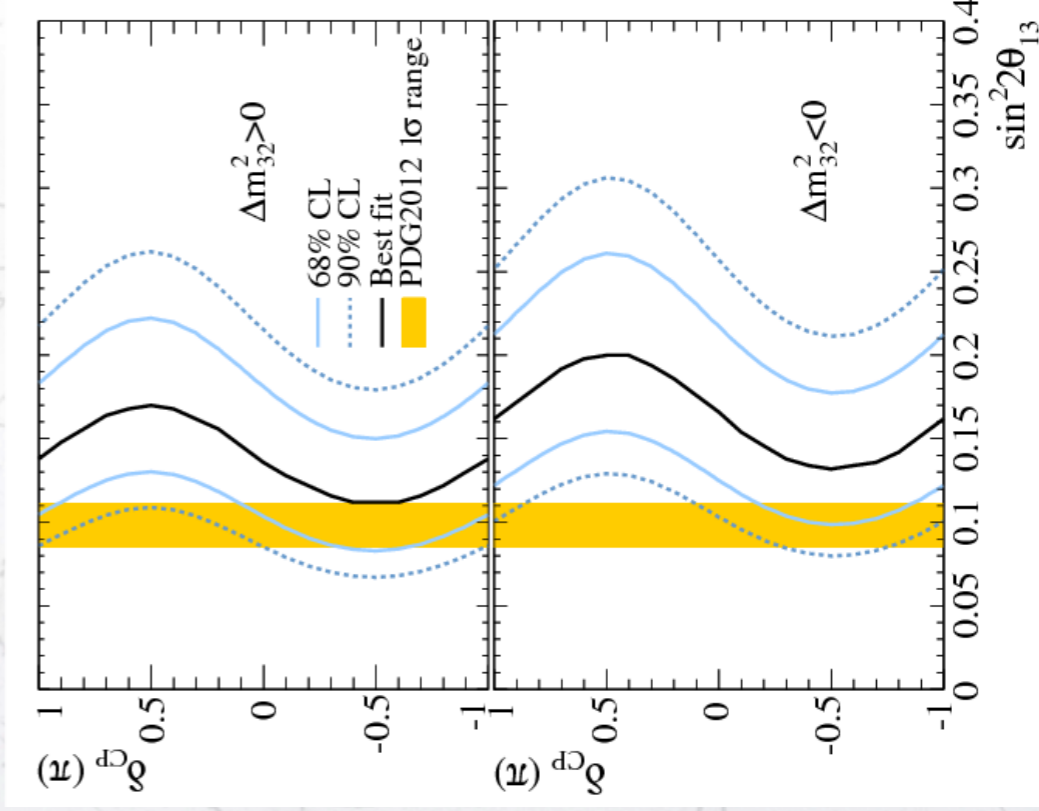
$$P_{\nu_\mu, \nu_e} \approx \begin{aligned} & \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\ & \pm \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^3 \frac{\Delta m_{31}^2 L}{4E} \\ & - \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \cos \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \frac{\Delta m_{31}^2 L}{4E} \\ & + \left( \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \right)^2 \cos^2 \theta_{23} \sin^2 \theta_{12} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \end{aligned}$$



# CP violation

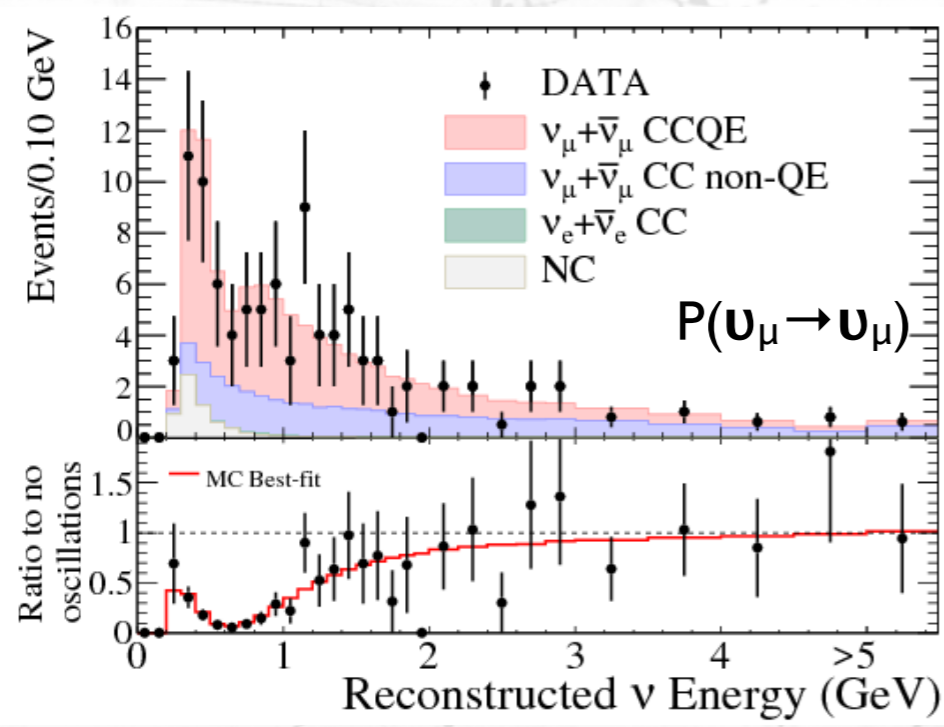


$$P_{\nu_\mu, \nu_e} \approx \begin{matrix} \pm & - & + \\ \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 \frac{\Delta m_{31}^2 L}{4E} & \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^3 \frac{\Delta m_{31}^2 L}{4E} & \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \cos \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \frac{\Delta m_{31}^2 L}{4E} \\ \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^3 \frac{\Delta m_{31}^2 L}{4E} & \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \cos \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \frac{\Delta m_{31}^2 L}{4E} & \left( \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \right)^2 \cos^2 \theta_{23} \sin^2 \theta_{12} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \end{matrix}$$





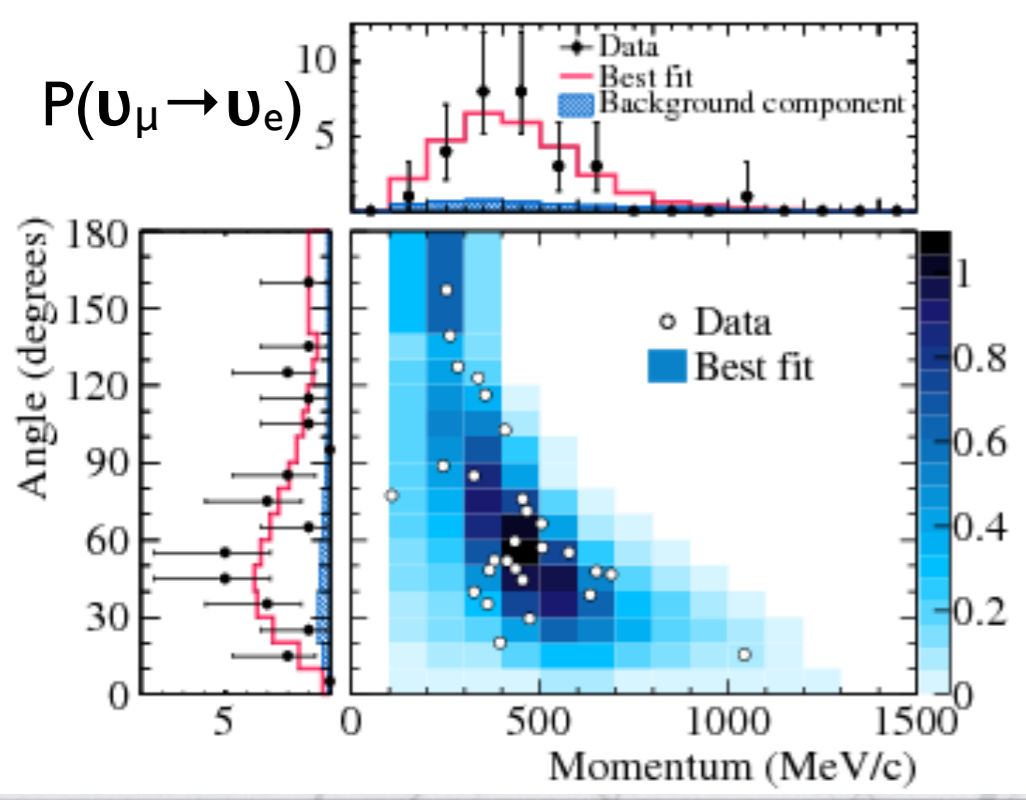
# CP violation



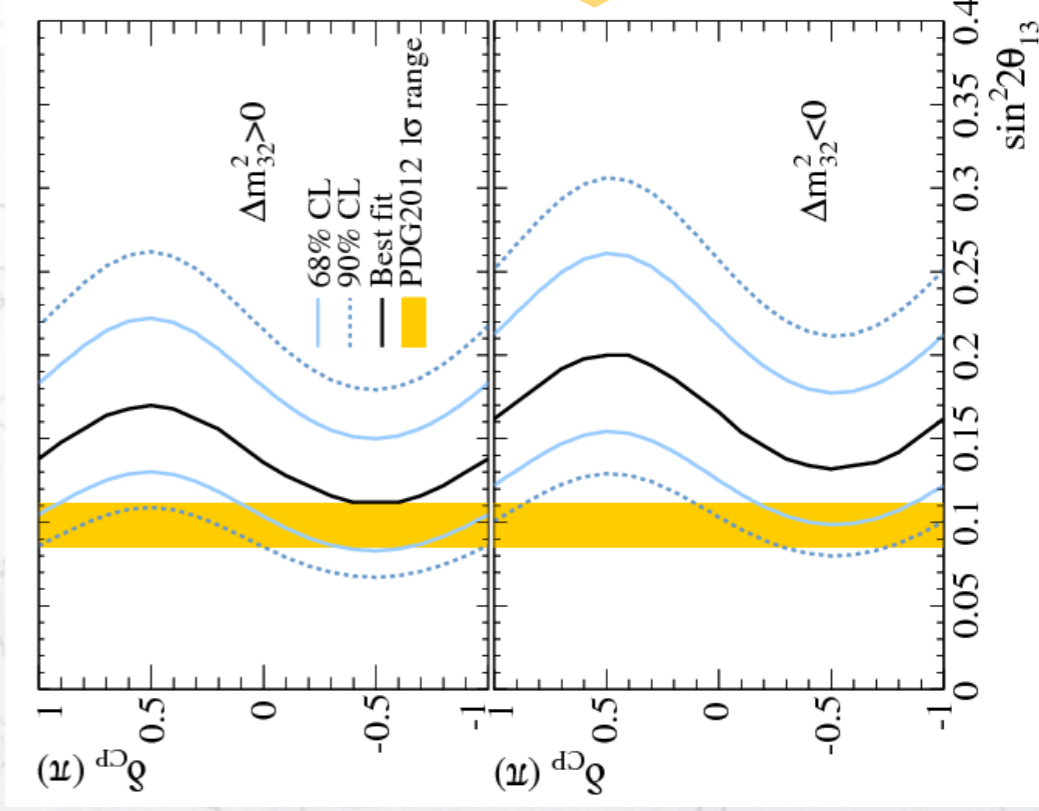
atmospheric  
 $\Theta_{23}$

Solar  
 $\Theta_{12}$

$P(\nu_e \rightarrow \nu_e)$   
 $\Theta_{13}$

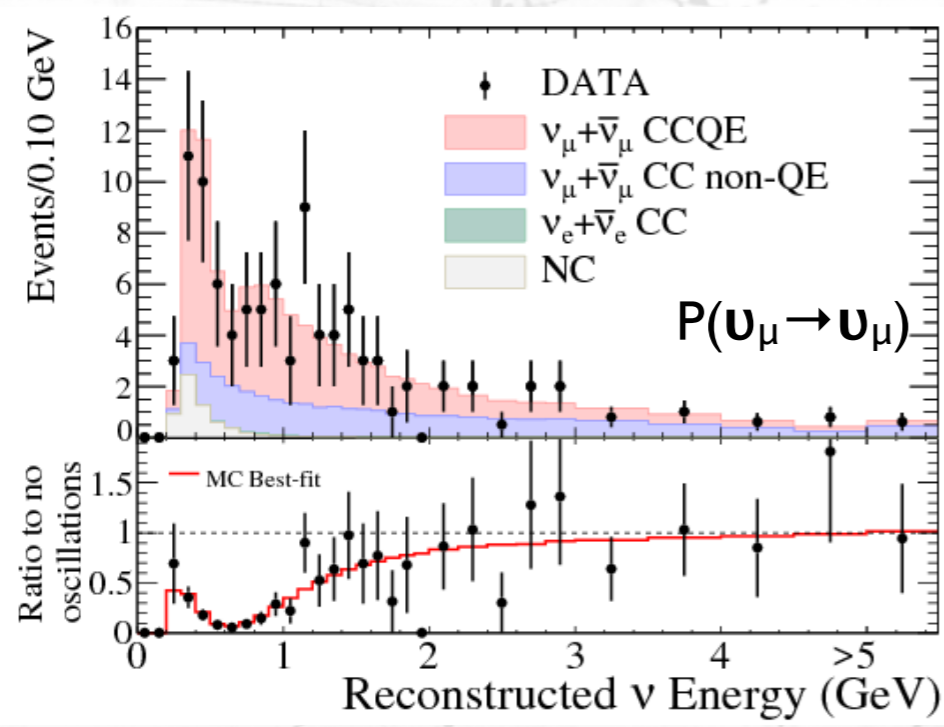


$$P_{\nu_\mu, \nu_e} \approx \begin{matrix} \pm & - & + \\ \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 \frac{\Delta m_{31}^2 L}{4E} & \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^3 \frac{\Delta m_{31}^2 L}{4E} & \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \cos \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \frac{\Delta m_{31}^2 L}{4E} \\ \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^3 \frac{\Delta m_{31}^2 L}{4E} & \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \cos \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \frac{\Delta m_{31}^2 L}{4E} & \left( \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \right)^2 \cos^2 \theta_{23} \sin^2 \theta_{12} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \end{matrix}$$





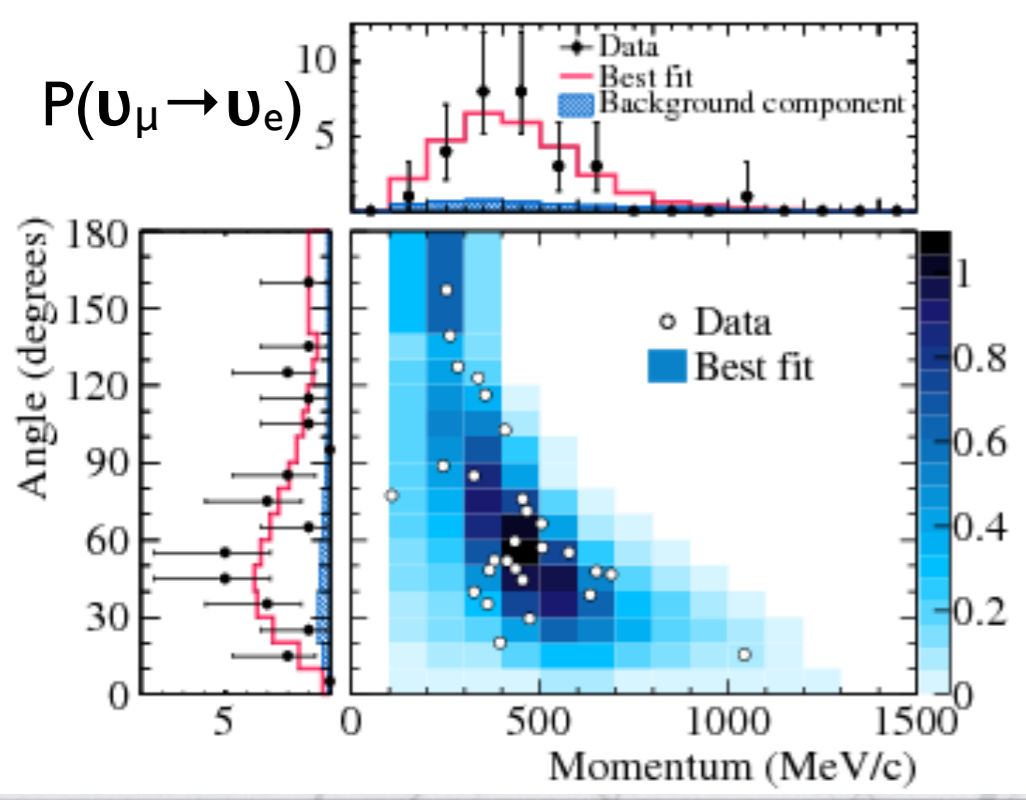
# CP violation



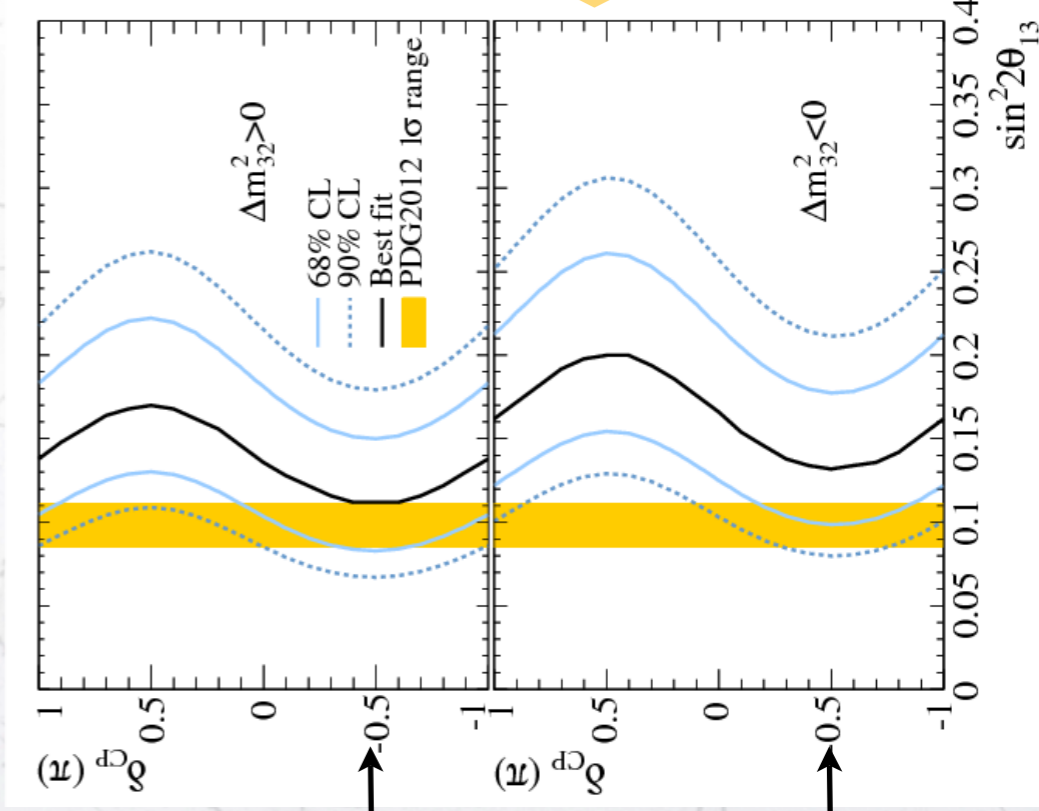
atmospheric  
 $\Theta_{23}$

Solar  
 $\Theta_{12}$

$P(\nu_e \rightarrow \nu_e)$   
 $\Theta_{13}$



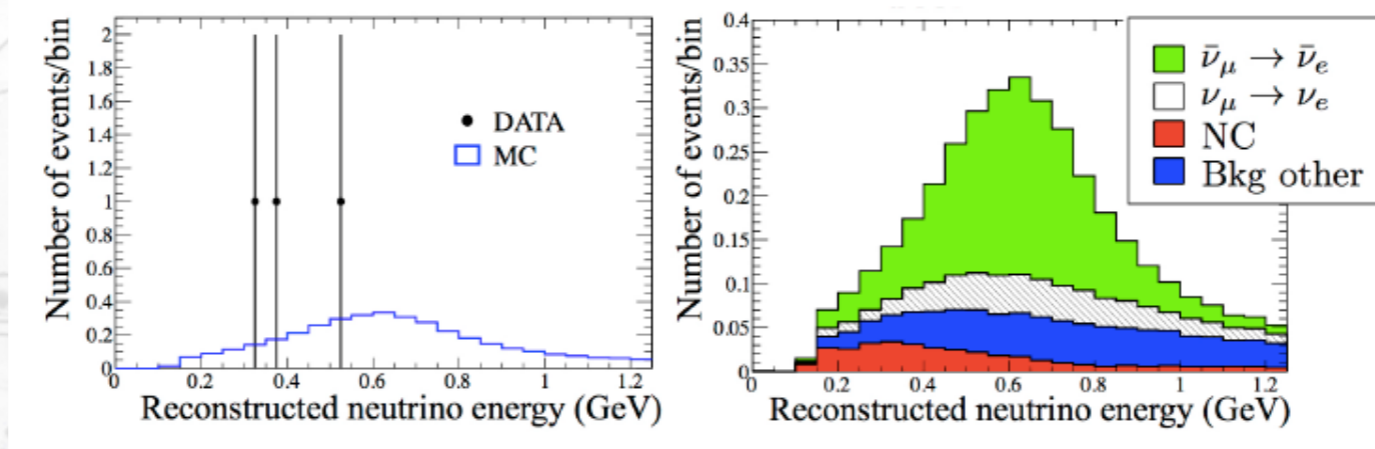
$$P_{\nu_\mu \nu_e} \approx \pm \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \mp \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \frac{\Delta m_{31}^2 L}{4E} \pm \left( \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \right)^2 \cos^2 \theta_{23} \sin^2 \theta_{12} \sin^2 \frac{\Delta m_{31}^2 L}{4E}$$



Preferred solution is not 0!



- T2K has been looking for anti-neutrino electrons in an anti-neutrino muon beam since 2014.
- Statistics ( 3 events ) is very low! (T2K got ~15 neutrinos for the same number of protons on target).



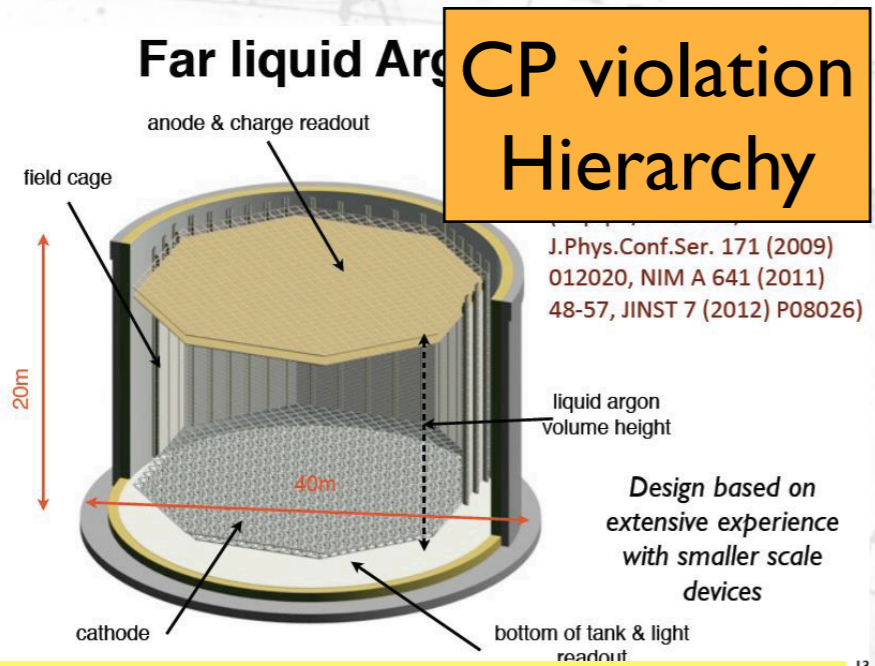
- Statistics is the key !
  - Next generation of experiments aimed at larger neutrino fluxes (x2 or 3) and/or larger detector masses (factors 2 to 10)
  - HyperKamiokande, Dune, etc...



# The future

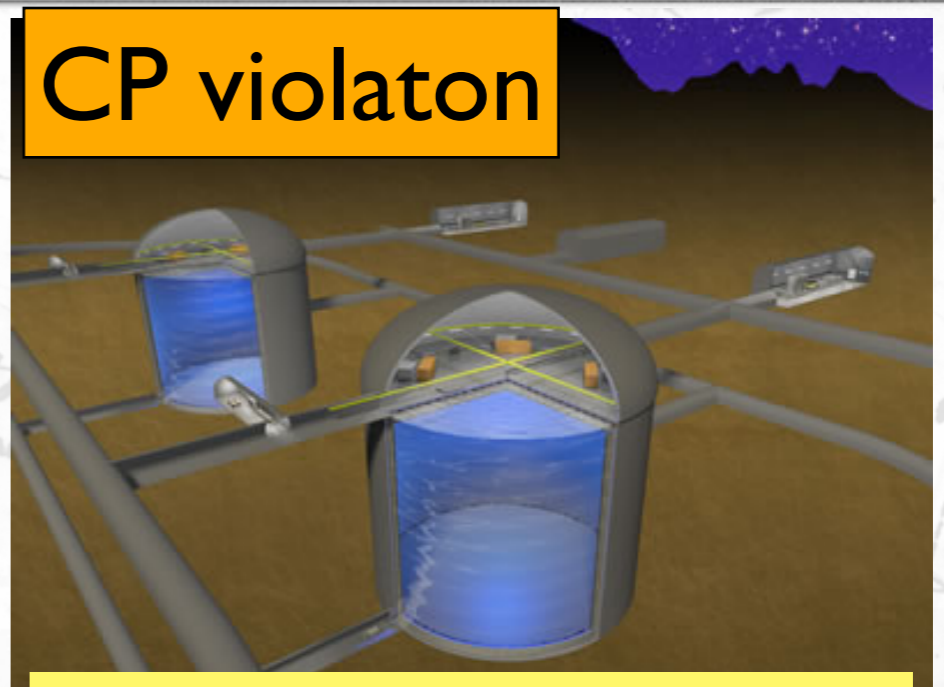


DUNE



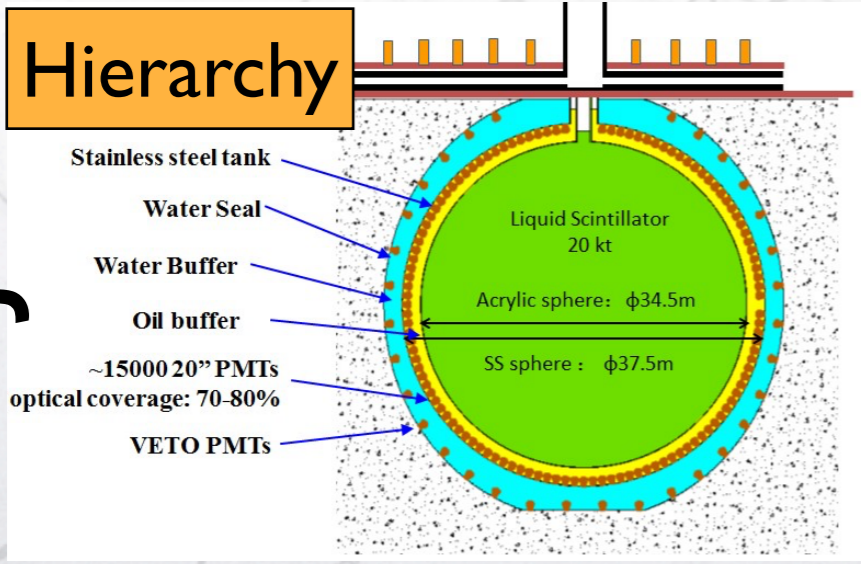
40 Ktons of Liquid Argon TPC in 4 tanks!

HyperKamiokande



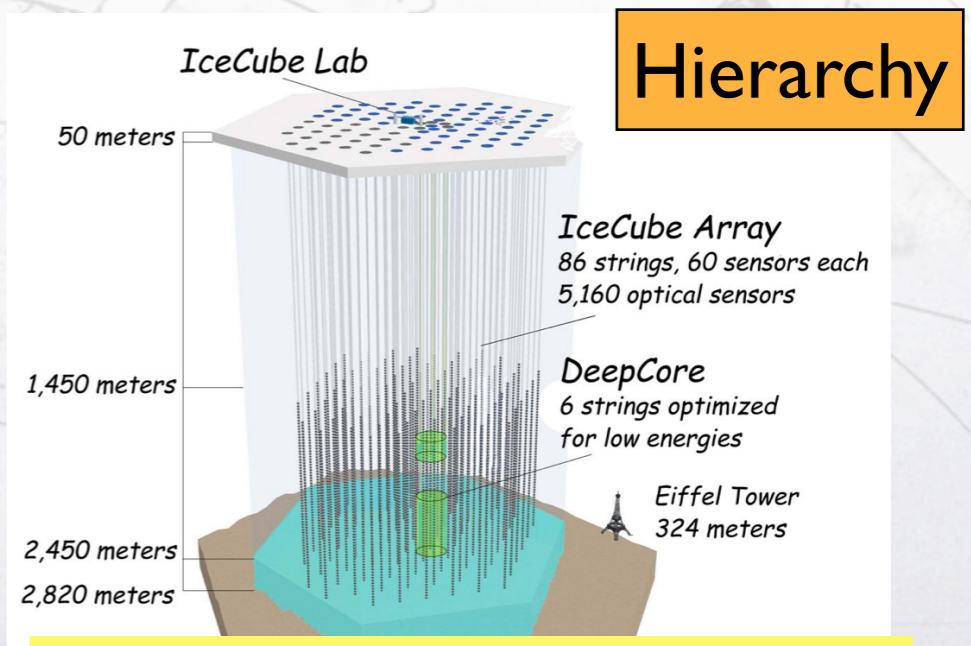
500 Ktons of pure water Cerenkov detector in 2 tanks!

Juno



20 Ktons of liquid scintillator

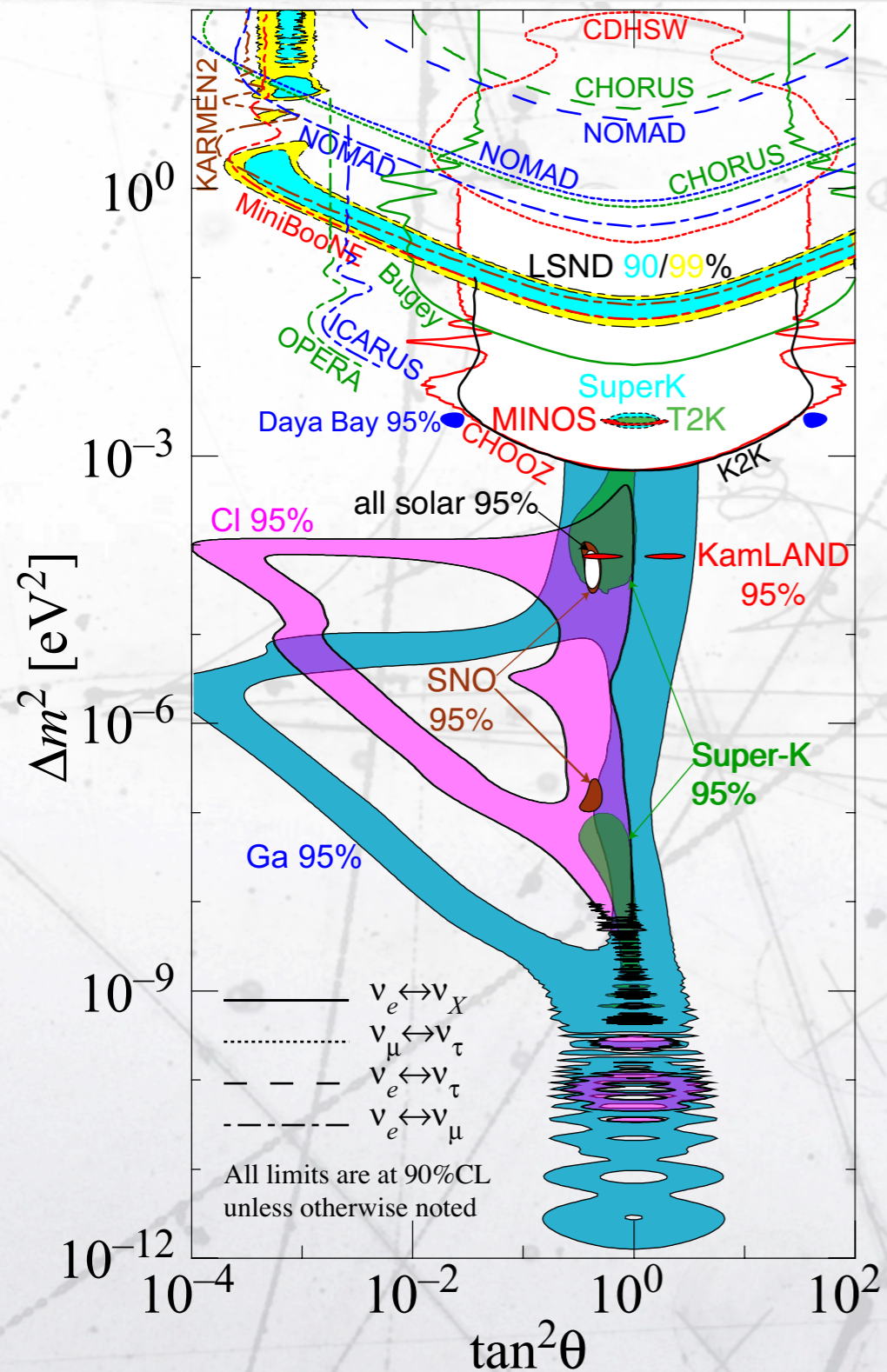
IceCube/Pingu



1 km<sup>3</sup> of ice



# As conclusions



- Fast development in the last 20 years:
- mixing parameters (for  $\bar{\nu}$  &  $\nu$ )
- over  $\sim 13$  orders of magnitude.
- mass differences and hierarchies (for  $\bar{\nu}$  &  $\nu$ ):
- over  $\sim 6$  orders of magnitude.
- solar and atmospheric models tested at several experiments with natural and artificial sources.

Parameter	best-fit ( $\pm 1\sigma$ )	$3\sigma$
$\Delta m_{21}^2$ [ $10^{-5}$ eV <sup>2</sup> ]	$7.54^{+0.26}_{-0.22}$	6.99 – 8.18
$ \Delta m^2 $ [ $10^{-3}$ eV <sup>2</sup> ]	$2.43 \pm 0.06$ ( $2.38 \pm 0.06$ )	2.23 – 2.61 (2.19 – 2.56)
$\sin^2 \theta_{12}$	$0.308 \pm 0.017$	0.259 – 0.359
$\sin^2 \theta_{23}, \Delta m^2 > 0$	$0.437^{+0.033}_{-0.023}$	0.374 – 0.628
$\sin^2 \theta_{23}, \Delta m^2 < 0$	$0.455^{+0.039}_{-0.031}$	0.380 – 0.641
$\sin^2 \theta_{13}, \Delta m^2 > 0$	$0.0234^{+0.0020}_{-0.0019}$	0.0176 – 0.0295
$\sin^2 \theta_{13}, \Delta m^2 < 0$	$0.0240^{+0.0019}_{-0.0022}$	0.0178 – 0.0298
$\delta/\pi$ ( $2\sigma$ range quoted)	$1.39^{+0.38}_{-0.27}$ ( $1.31^{+0.29}_{-0.33}$ )	(0.00 – 0.16) $\oplus$ (0.86 – 2.00) (0.00 – 0.02) $\oplus$ (0.70 – 2.00))



- But, we still miss few more measurements:
  - Precision, precision, precision !!!!
    - How close is  $\theta_{23}$  to  $\pi/2$  ? (sort of magic number  $\rightarrow$  theoretical implications)
  - Hierarchy (  $m_3 > m_1$  ? )
  - CP violation ?
- What is the absolute mass of the neutrinos ?
- And, a theory capable to describe massive neutrinos inside the Standard Model in a coherent way:
  - Why are the masses so low?
  - Right handed neutrinos are “sterile” but they are needed to provide mass to the neutrino in the Dirac model. (Is this correct?)
  - What is the relation between quark and neutrino mixing ?



**NEUTRINOS, they are very small.  
They have no charge and have no mass  
And do not interact at all  
The earth is just a silly ball  
To them, through which they simply pass,  
Like dustmaids down a drafty hall  
Or photons through a sheet of glass.  
They snub the most exquisite gas,  
Ignore the most substantial wall,  
Cold shoulder steel and sounding brass,  
Insult the stallion in his stall,  
And scorning barriers of class,  
Infiltrate you and me! Like tall  
and painless guillotines, they fall  
Down through our heads into the grass.  
At night, they enter at Nepal  
and pierce the lover and his lass  
From underneath the bed-you call  
It wonderful; I call it crass.**

*- Telephone Poles and Other Poems, John Updike, Knopf, 1960*



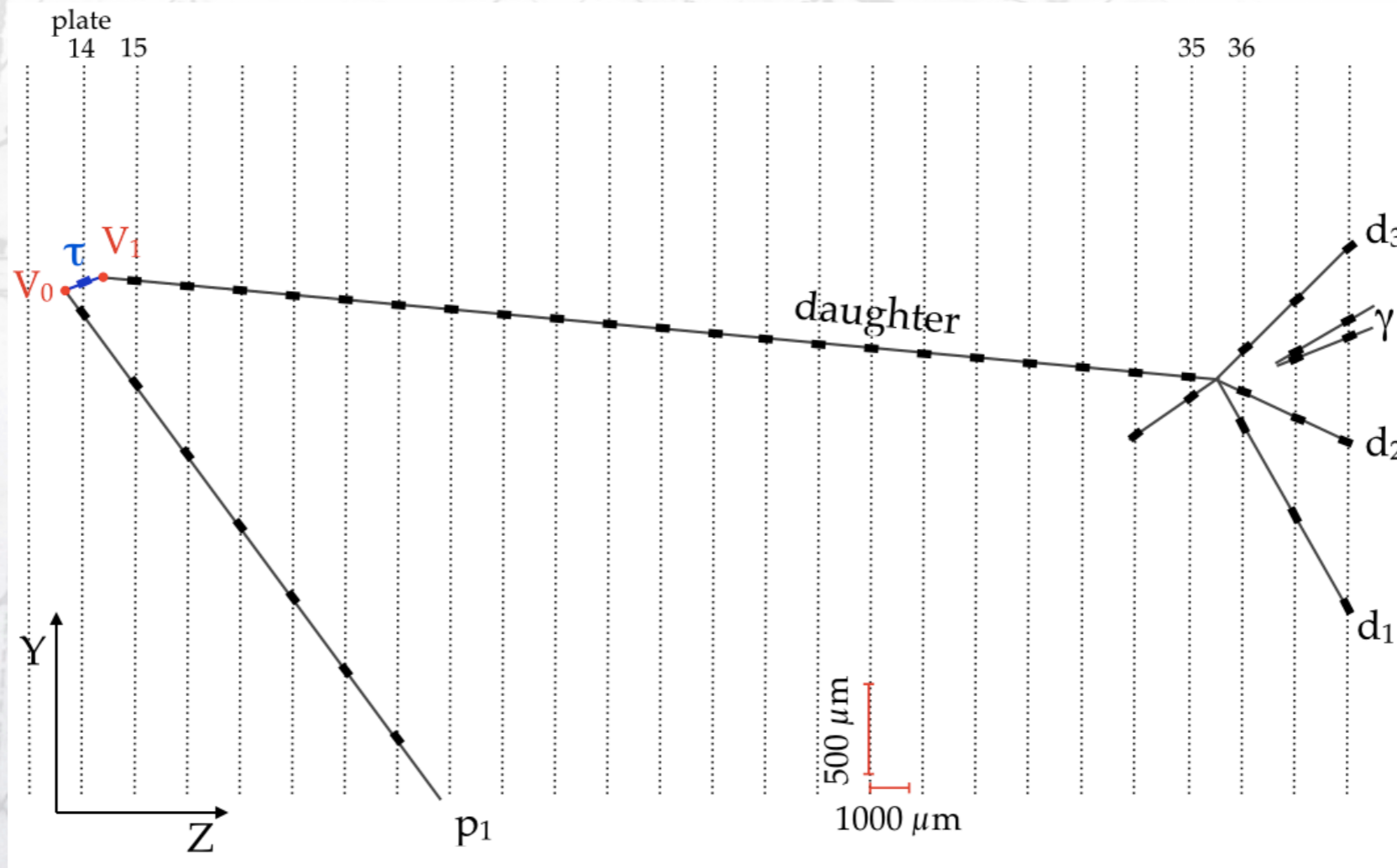
# Support slides



# Tau neutrinos



- Transition:  $\nu_\mu \rightarrow \nu_\tau$  detected at the CNGS/OPERA experiment.
- 5 events with kink detected in the detector emulsion.





## The theory

- Neutrinos can have two types of interaction with matter:
  - Incoherent inelastic:  $\sigma \sim 10^{-43} (E/\text{MeV})^2$
  - Coherent. The medium is unchanged and the scattered and un-scattered waves interfere enhancing the effect.
    - It introduces a phase in the propagation, that can be invisible... **except for the fact that matter is made of electrons.**

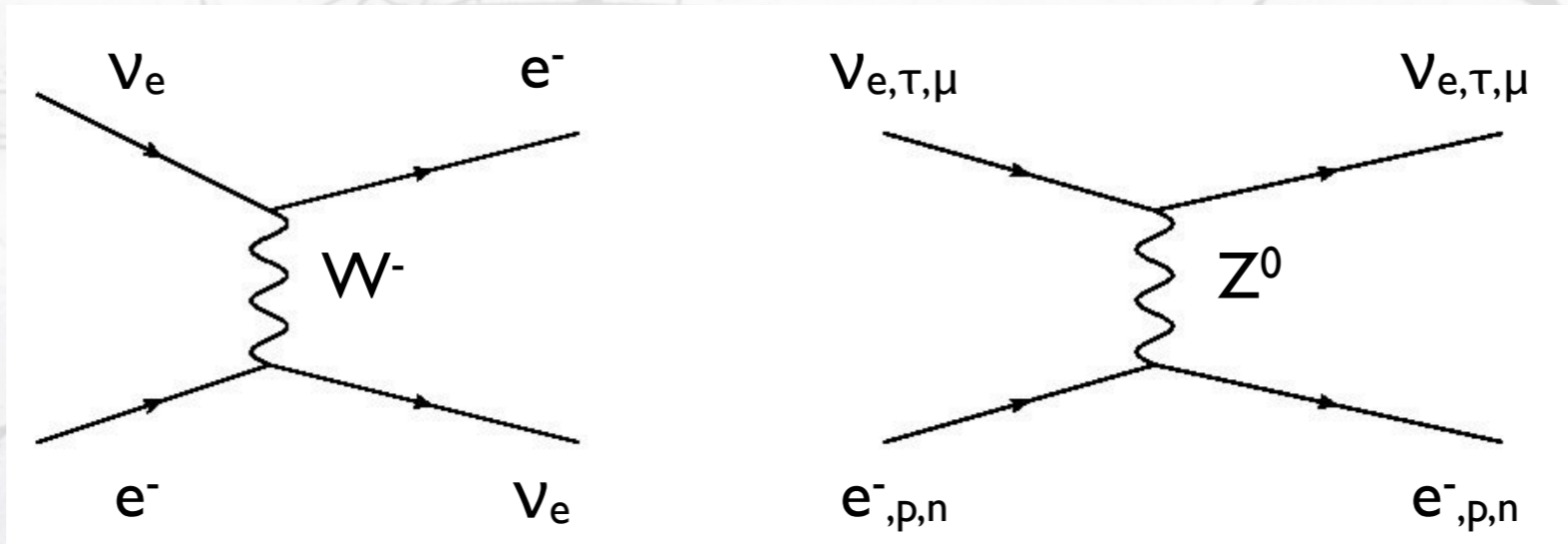


The theory

- The Schrödinger equation of  $\nu$  in matter:

$$i\hbar \frac{\partial \nu_i}{\partial t} = \left( \frac{m_i^2}{2E} + V_C^i \right) \nu_i$$

- $V_C$  introduces the coherent interaction (phase) depending on the neutrinos flavour:



- The NC phase is common and factorizes. The CC remains:

$$V_C = \text{diag}(\pm \sqrt{2} G_F n_e, 0, 0)$$



## The theory

- The mass effect can be interpreted as a change in the mass eigenstate and eigenvalue. It changes interference pattern & effective mixing angle. Both depend on the neutrino energy and local electron density.

$$\mu_{1,2}^2(x) = \frac{m_1^2 + m_2^2}{2} + E_\nu(V_\alpha + V_\beta) \mp \frac{1}{2} \sqrt{[\Delta m^2 \cos 2\theta - A]^2 + [\Delta m^2 \sin 2\theta]^2}$$

$$\tan 2\theta_m = \frac{\Delta m^2 \sin 2\theta}{\Delta m^2 \cos 2\theta - A}$$

$$A = 2E_\nu(V_\alpha - V_\beta)$$

- As we have seen,  $V_\alpha = \pm \sqrt{2} G_F n_e$ ,  $V_\beta = 0$
- When crossing  $A \sim \Delta m^2 \cos(2\theta)$ , the  $\tan(2\theta_m)$  changes sign  $\rightarrow$  The proportions of 1 & 2 invert for  $\alpha$  &  $\beta$  states (“level crossing”).



- The first experiments to determine the mass of neutrinos were proposed in 1933 by Perrin and Fermi. The idea was to investigate the endpoint of the  $\beta$  spectrum.
- This is still the method used for direct search in Katrin!!!!
- At that time, upper limits of 100 eV were achieved.
- After the parity violation in  $\beta$ -decays were discovered, the two-component neutrino theory (Landau, Lee and Yang and Salam, 1957) was the first theoretical idea about neutrino masses.
- The idea was simple, two neutrinos (Left-Right), one of them is “sterile” (do not interact) so it is not “needed”.



- If we consider that the neutrino field has two components (L,R) the Dirac equations can be written as:

$$i\gamma^\alpha \partial_\alpha \nu_L(x) - m_\nu \nu_R(x) = 0$$

$$i\gamma^\alpha \partial_\alpha \nu_R(x) - m_\nu \nu_L(x) = 0$$

- Taking into account the boundaries and the fact that only one field was needed (L or R) to describe the weak interactions, it was accepted that  $m_\nu = 0$ .
- The “other” helicity was a “sterile”: no mass & no interaction.
- The neutrino helicity was measured in 1958 in a spectacular experiment by M. Goldhaber: neutrinos were left-handed.



- From this point of view the parity violation in weak interactions was due to the fact that the neutrino mass was zero and only one neutrino helicity existed.
- This idea was changed after the Feynman, Gell-Mann, Marshak and Sudarshan proposed the V-A theory in 1958. The two component theory was not needed because the interaction was governed by the propagator and not the neutrino helicity.
- But, the simplicity of the  $m_\nu = 0$  theory prevailed for years... and it was “assumed” that neutrinos were massless.



- If neutrinos have mass, then the right-handed neutrino “has to exist”. After 60 years, we go back to the problem that there is a type of neutrino (Right helicity) that is sterile (does not interact).
- Theory proposed an alternative: **Majorana mass**. In this case the neutrino is the same as its antiparticle, so the right handed neutrino is just the anti-particle.
- This is only possible for neutrinos because it is the only neutral fundamental lepton in the SM.
- We can write the mass term (Lorentz invariant) in two ways (or both):

**Dirac**  $\mathcal{L}_D = -m_D \bar{\nu}_L \nu_R + h.c.$

**Majorana**  $\mathcal{L}_M = -m_M \bar{\nu}_R^c \nu_R + h.c.$



- Majorana mass implies two new properties:
  - The neutrino is equal to its antiparticle.
  - There is no right handed, it is just the anti-particle.
- Turning the argument around!. We need an additional symmetry to forbid the Majorana term in the Lagrangian. Whatever we discover will be very relevant to the SM.
- How to detect them:
  - We can boost back a neutrino and find an antineutrino.
  - We can look for a process where the neutrino-antineutrino cancels in a loop or propagator: neutrino-less double beta decay, or any  $\Delta L=2$  process.



- Consider that we have both Majorana ( $m^M$ ) and Dirac ( $m^D$ ) mass terms.

$$\mathcal{L} = -\frac{1}{2} (\bar{\nu}_L \bar{\nu}_R^c) \begin{pmatrix} m_L^M & m^D \\ m^D & m_R^M \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \nu_R \end{pmatrix} + h.c.$$

- When we diagonalize the matrix we obtain the following eigenvalues:

$$\lambda_{\pm} = \frac{1}{2}(m_L^M + m_R^M) \pm \frac{1}{2} \sqrt{(m_L^M + m_R^M)^2 - 4(m_L^M m_R^M - m^D m^D)}$$

- If we assume  $(m_L^M m_R^M - m^D m^D) \ll (m_L^M + m_R^M)^2$ , then:

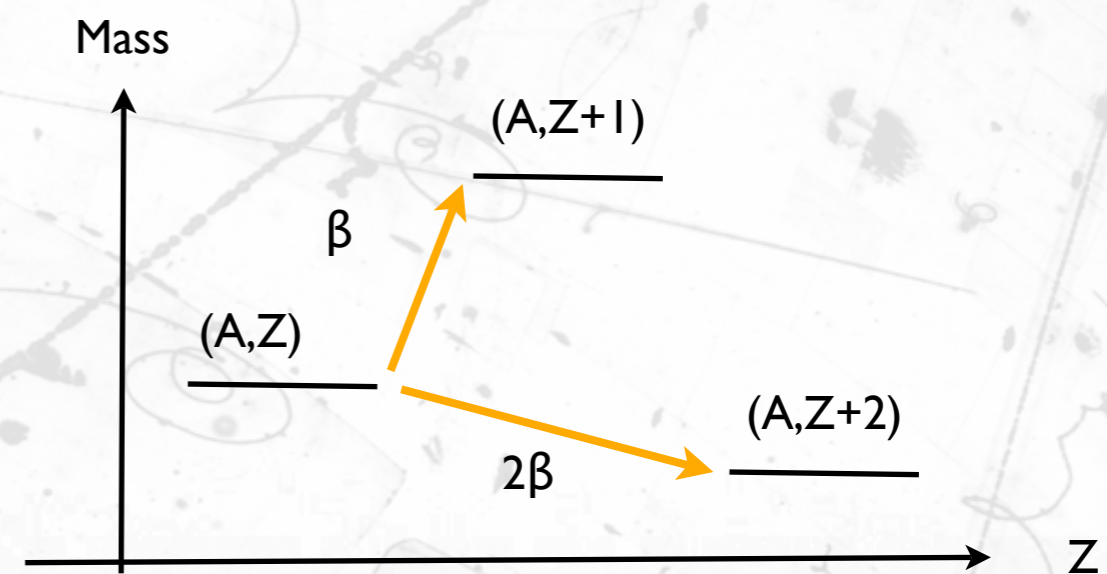
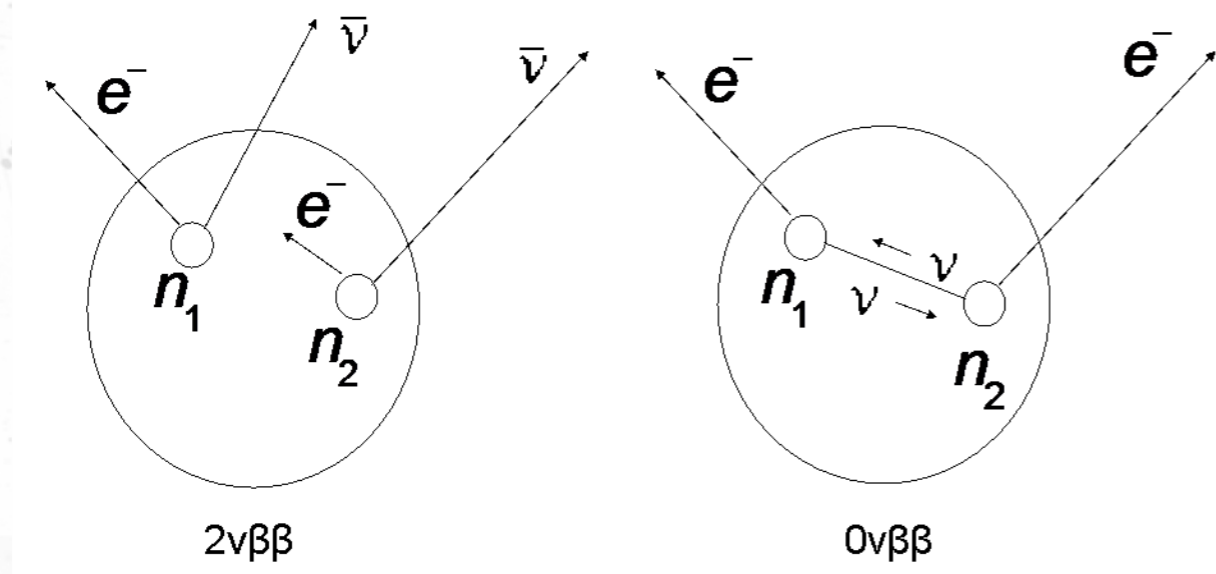
$$\lambda_+ = m_L^M + m_R^M$$

$$\lambda_- = \frac{(m_L^M m_R^M - m^D m^D)}{m_L^M + m_R^M}$$

- And,  $\lambda_+ \gg \lambda_-$ . Tuning the values of  $m_R^M$  we can generate the  $\lambda_-$  as small as needed since  $m_R^M$  is basically a free parameter.



# $0\nu 2\beta$ process

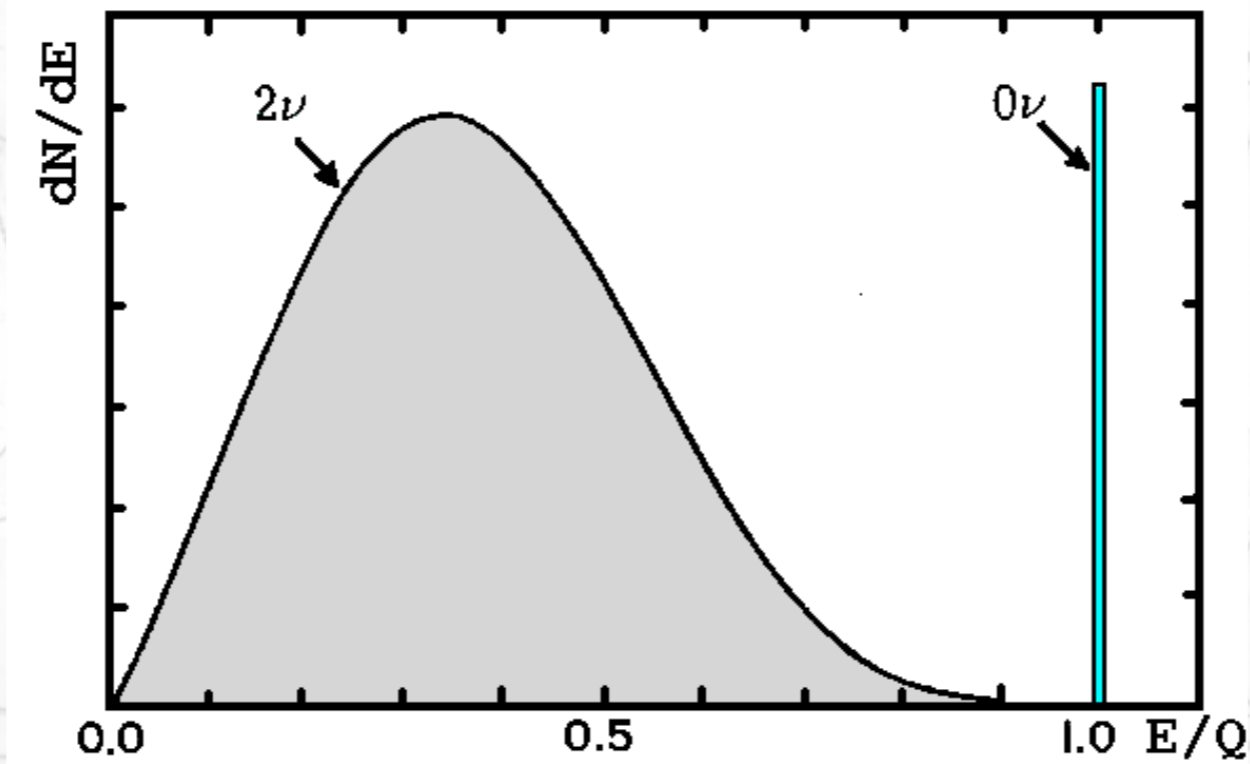


- The  $2\nu 2\beta$  has been measured for several isotopes.
- The  $0\nu 2\beta$  has been search in many of them (“almost”) without success.
- Experimentally is complex, both processes are rare:  $T_{1/2} \gg 10^{20} \text{ s}$
- The rate of  $0\nu 2\beta$  is proportional to a  $\nu$  effective mass: kind of  $\nu$  mass scale.





# $0\nu 2\beta$ process

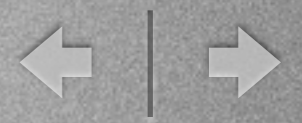


- The  $0\nu 2\beta$  is characterized by a monochromatic  $2e$  emission.
- The experiments are mainly low background underground high resolution calorimeters ( $\Delta E/E \sim 0.2\%$ )
- New experiments try to get the advantage of the 2 electrons to reduce non  $2\beta$  background from natural radioactivity: NEMO, NEXT,...

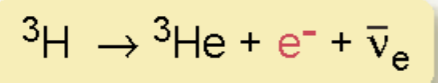




# Katrin

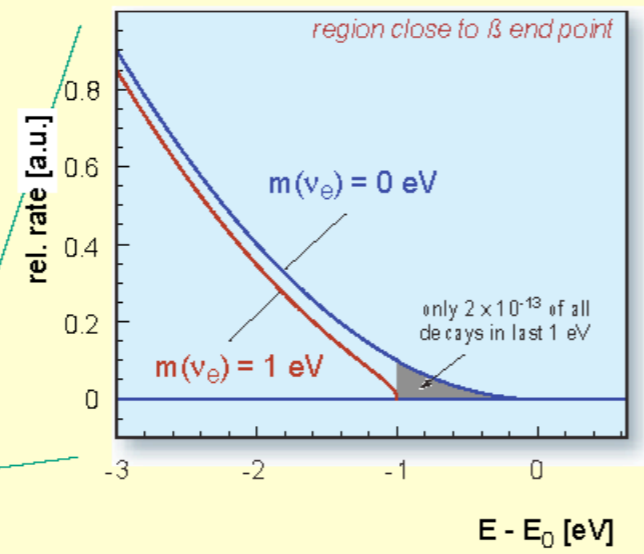
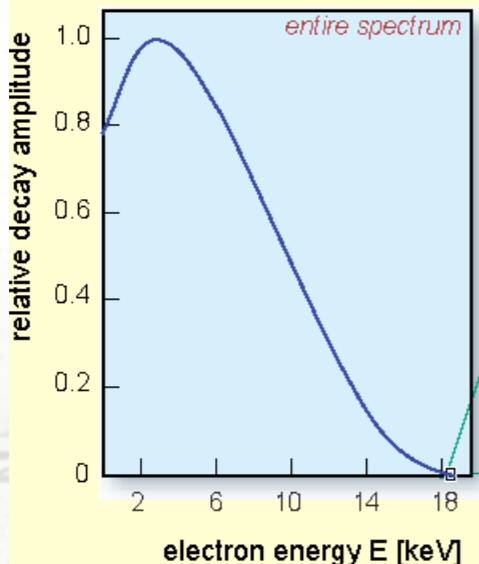


## tritium $\beta$ -decay and the neutrino rest mass



half life :  $t_{1/2} = 12.32 \text{ a}$   
 $\beta$  end point energy :  $E_0 = 18.57 \text{ keV}$

superallowed



- Absolute neutrino mass experiment:
  - ${}^3\text{H}$   $\beta$ -decay end point.
  - MAC-E filter threshold spectrometer.
  - High resolution:  $\sim 0.2 \text{ eV}$

