

# Partial Wave Analysis of Strangeness Production at GeV Energies

Laura Fabbietti, Steffen Maurus

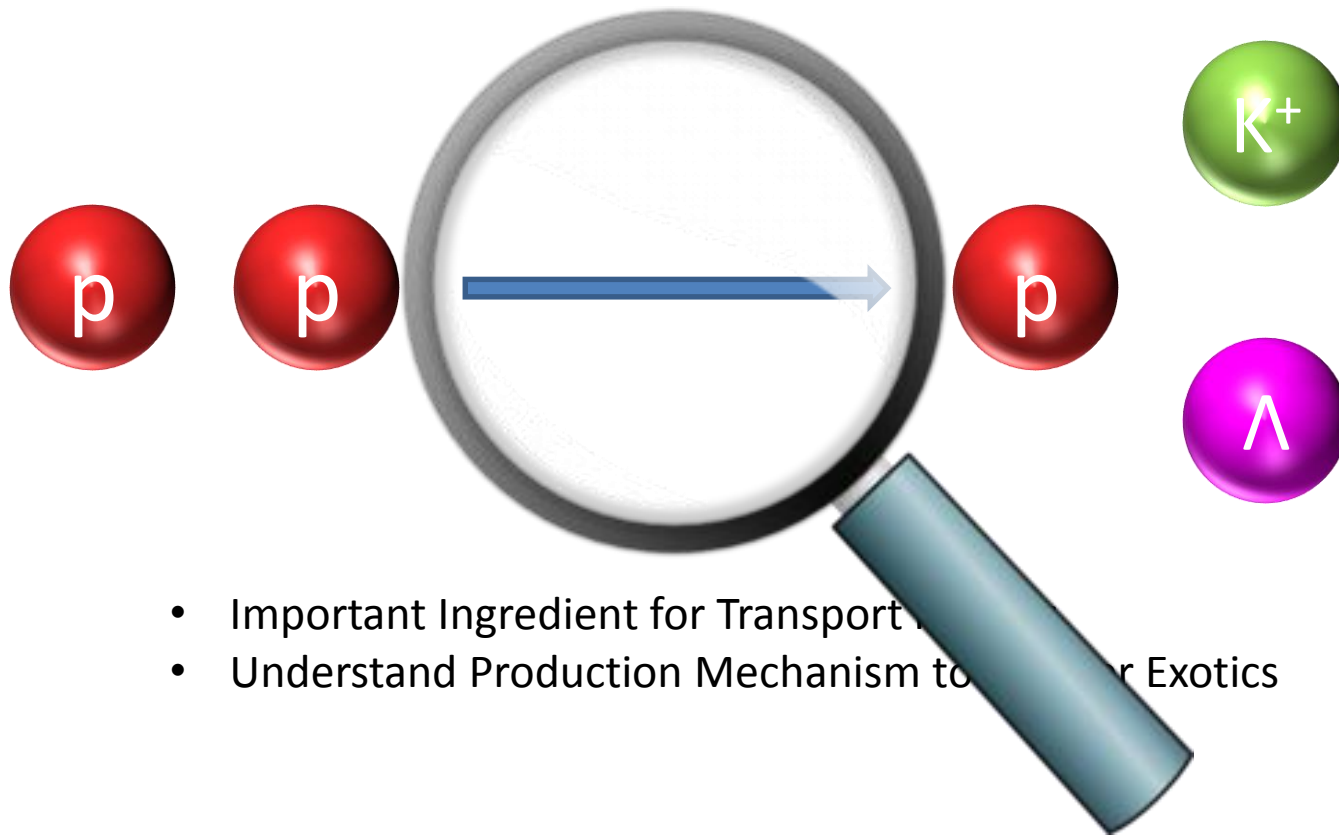
Robert Münzer, Shuna Lu,

Technische Universität München

Excellence Cluster – Origin of the Universe

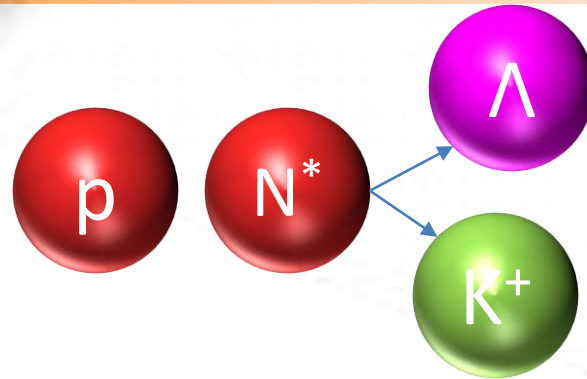


# Strangeness Production



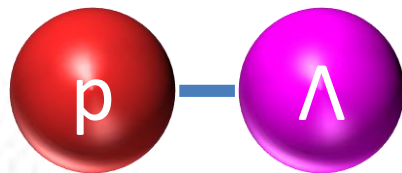
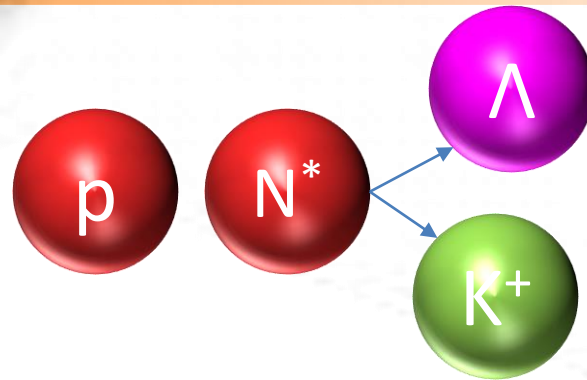
- Important Ingredient for Transport
- Understand Production Mechanism to ... Exotics

# Strangeness Production

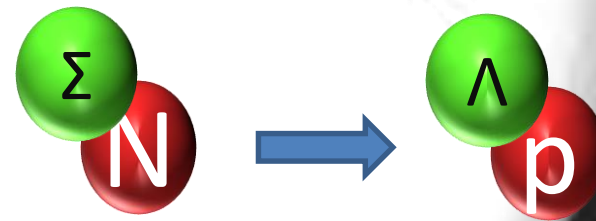


Resonance	$J^P$	Mass ( $GeV/c^2$ )	$\Gamma$ ( $MeV/c^2$ )
N*(1650)	$1/2^-$	1.655	0.150
N*(1710)	$1/2^+$	1.710	0.100
N*(1720)	$3/2^+$	1.720	0.250
N*(1875)	$3/2^-$	1.875	0.220
N*(1880)	$1/2^+$	1.870	0.235
N*(1895)	$1/2^-$	2.090	0.090
N*(1900)	$3/2^+$	1.900	0.0250

# Strangeness Production



Final State Interaction  
Aka: scattering length and  
effective range



Conversion Processes  
(Cusp Effect)

# Partial Wave Analysis

## Bonn-Gatchina PWA Framework

A. Sarantsev et.al., Eur.Phys J A 25 2005

### Cross-section Decomposition

$$d\sigma = \frac{(2\pi)^4 |A|^2}{4|k|\sqrt{s}} d\phi(P, q_1, q_2, q_3), \quad P = k_1 + k_2$$

$A$  : reaction amplitude  $A = \sum_{\alpha} A_{tr}^{\alpha}(s) \cdot Q^{in} \cdot A_{2b}(\alpha) \cdot Q^{out}$

$Q^{in}, Q^{out}$  : spin-momentum operator of initial and final state

$A_{2b}$  : resonant: Breit-Wigner (for  $N^*$  and Cusp)

non-resonant: Effective range approximation, dependent on scattering parameters

$A_{tr}^{\alpha}(s) = (a_1^{\alpha} + a_3^{\alpha}\sqrt{s})e^{ia_2^{\alpha}}$  :  $a_1^{\alpha}$  constant amplitude

$a_2^{\alpha}$  phase

$a_3^{\alpha}$  energy dependent amplitude

$d\phi(P, q_1, q_2, q_3)$ : invariant three-particle phase space

# Multi-PWA

# Data Sets

Experiment	$E_B$ [GeV]	$pK^+\Lambda$ Statistics	Status
COSY-TOF	1.96	~160k	In Preparation (not used in the analysis)
DISTO	2.15	121 k	Available
COSY-TOF	2.16	43 k	Available
COSY-TOF	2.16	~90k	In Preparation (not used in the analysis)
DISTO	2.5	304 k	Available
DISTO	2.85	424 k	Available
FOPI	3.1	0.9 k	Single PWA
HADES	3.5	21 k	Single PWA

HADES PLB 742 (2015) 242-248.

# COSY-TOF Spectrometer

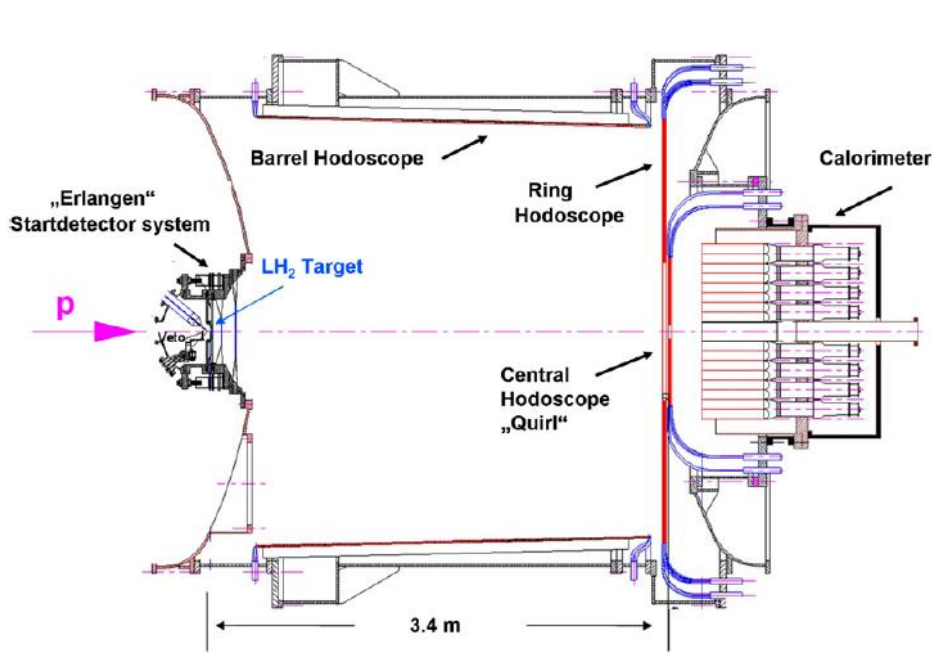


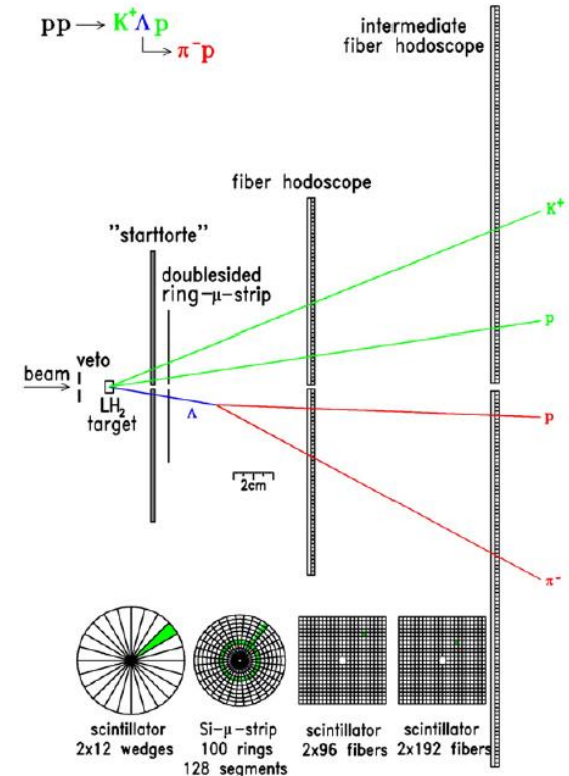
Fig. 1. Schematic view of the COSY-TOF detector.

Acceptance:  $1^\circ$ - $60^\circ$  (polar),  $2\pi$  (azimuthal)

Sec. Vertex:  $\sigma_{x,y} < 1\text{mm}$ ,  $\sigma_z < 3\text{mm}$

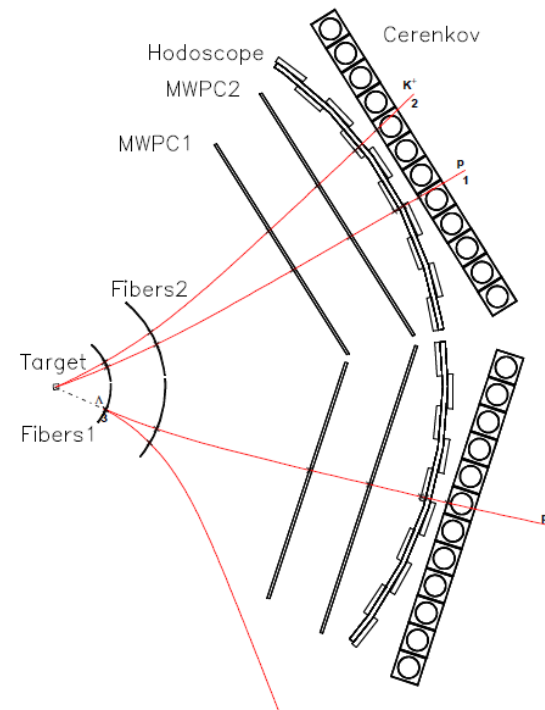
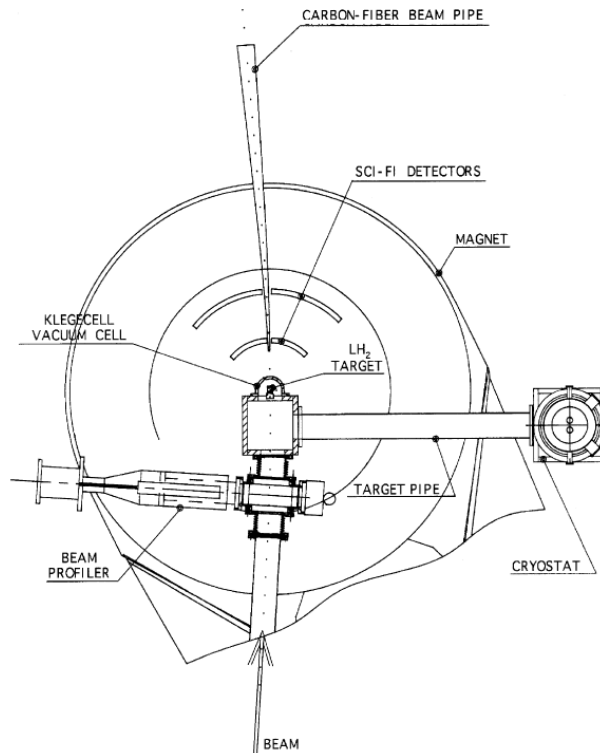
$$\sigma_{TOF} = 300\text{ps}$$

$$\sigma_{MM(pK)} = 16\text{ MeV}/c^2$$





# DISTO Spectrometer



Acceptance:  $23^\circ$ - $43^\circ$  (polar),  $2\pi$  (azimuthal)

$$\sigma_p = 5\%$$

$$\sigma_{MM(pK)} = 30 \text{ MeV}/c^2$$

# Combined Analysis

1. Solution for HADES+FOPI+DISTO25
  - Start values for the global fit
  - Energy Range wide enough for energy dependence
  - High energy for higher N\*-Resonances
2. Include Stepwise further data sample
  - Cosy216 / DISTO21 / DISTO28

# Parameter Scan

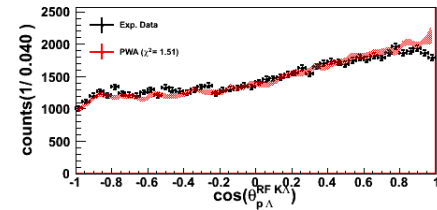
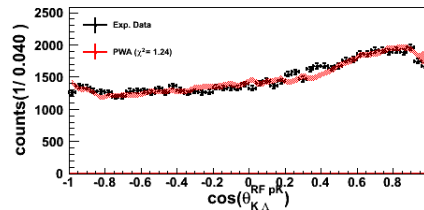
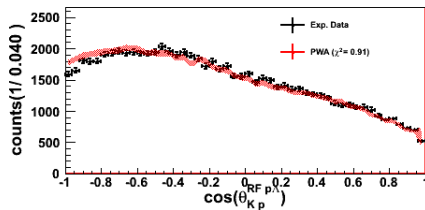
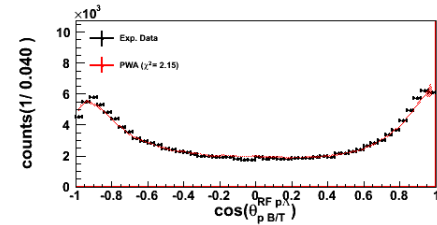
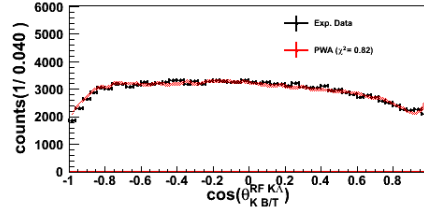
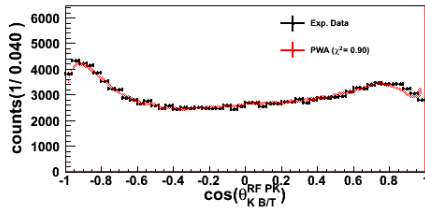
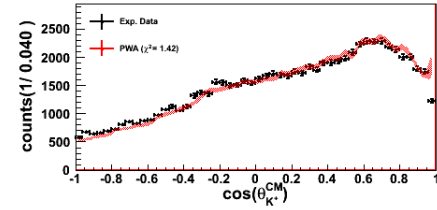
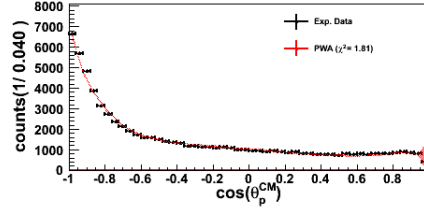
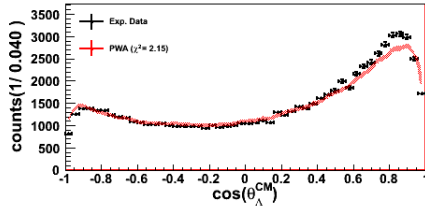
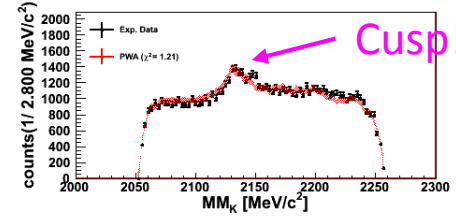
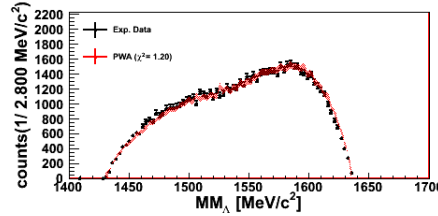
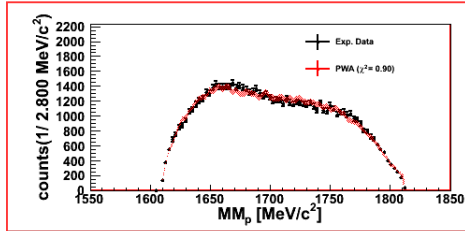
Initial pp states up to F wave

Include different N\* Resonances

Solution	A	B	C	D	E
Loglike	-67142	-67018	-66878	-66504	-66405
$\frac{\chi^2}{ndf}$ ( $ndf = 4547$ )	9,50	9,98	9,98	10,01	10,34
N*(1650)	+	+	+	+	+
N*(1710)	+	+	+	+	+
N*(1720)	+	+	+	+	-
N*(1875)	+	+	-	-	+
N*(1880)	+	+	+	+	+
N*(1895)	+	+	+	+	+
N*(1900)	-	+	+	-	+
Cusp Wave $\Sigma N (0^+, 1^+)$	+	+	+	+	+

# DISTO@2.14 GeV

Preliminary



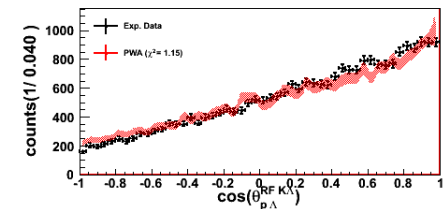
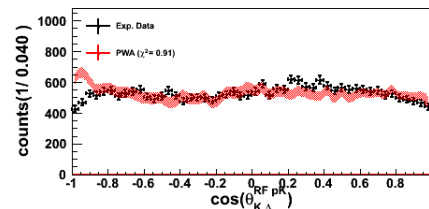
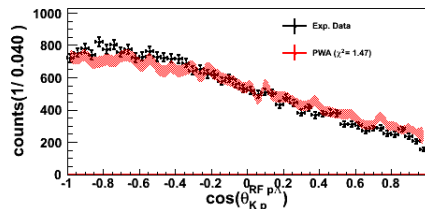
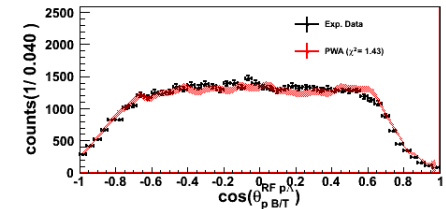
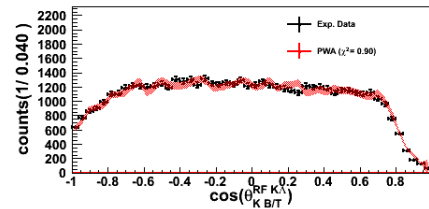
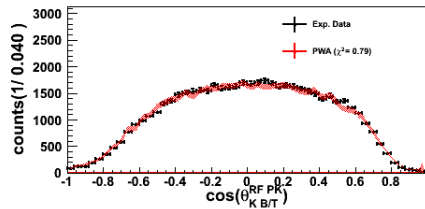
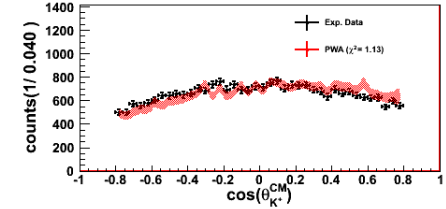
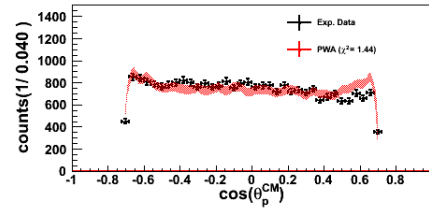
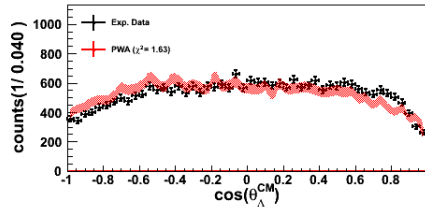
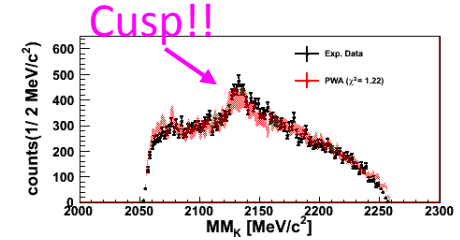
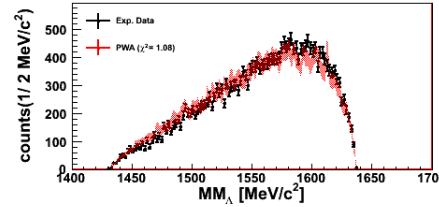
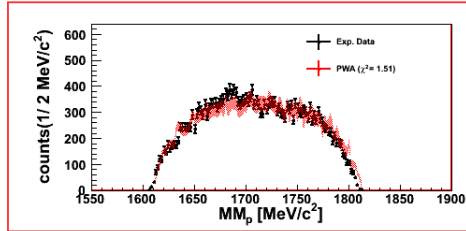
$\chi^2 / \text{nfd}$  (ndf=428)

PWA

1.52

# COSY-TOF@2.16 GeV

Preliminary

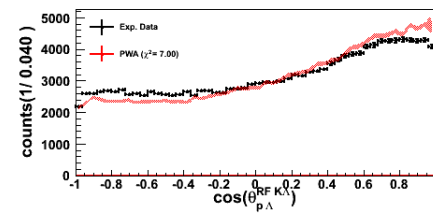
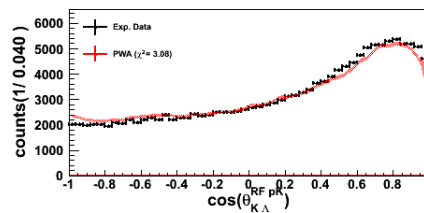
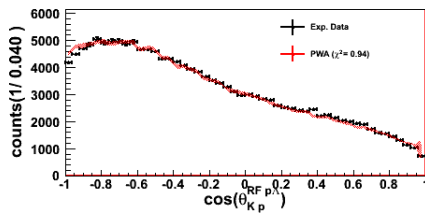
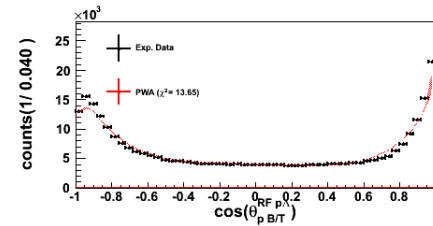
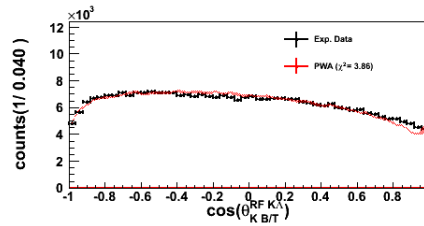
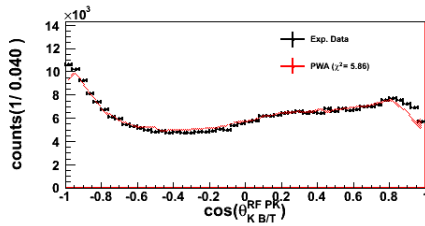
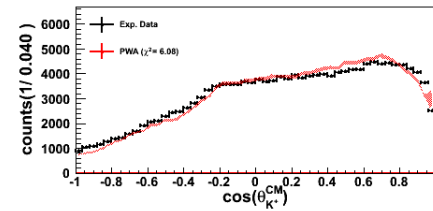
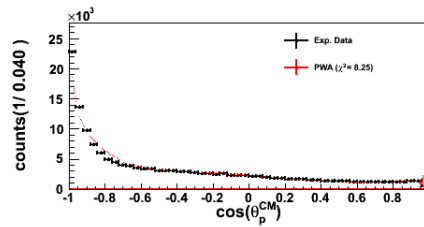
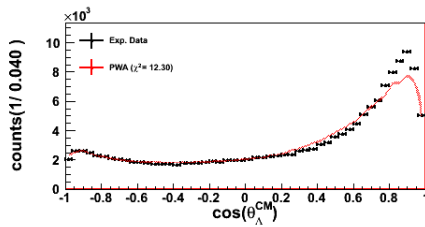
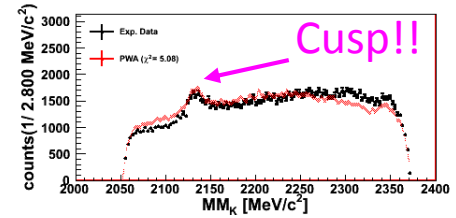
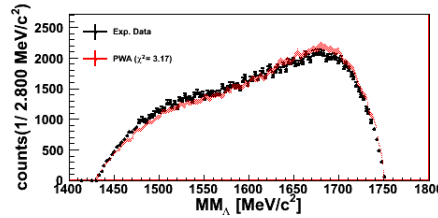
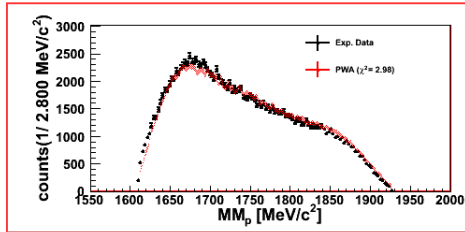


	$\chi^2 / \text{ndf}$ (ndf=428)
PWA	0.44



# DISTO@2.5 GeV

Preliminary



$\chi^2 / \text{ndf}$  (ndf=428)

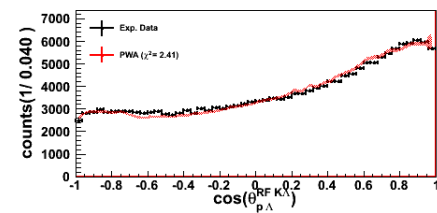
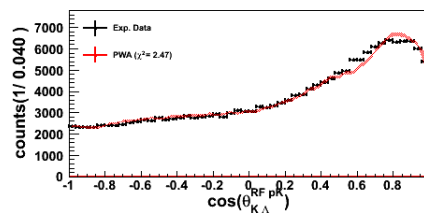
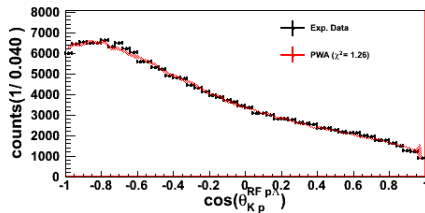
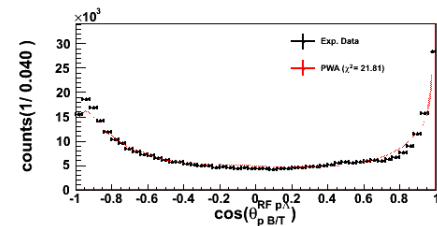
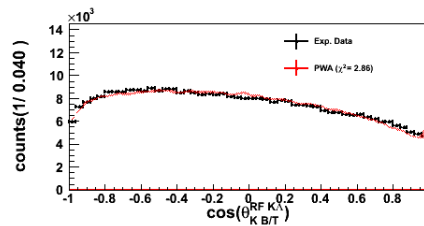
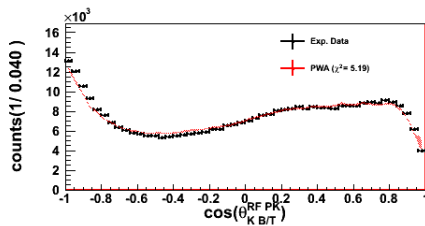
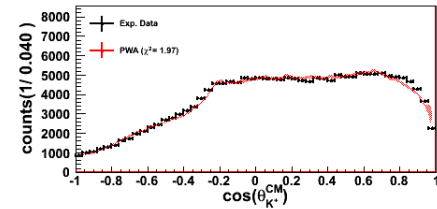
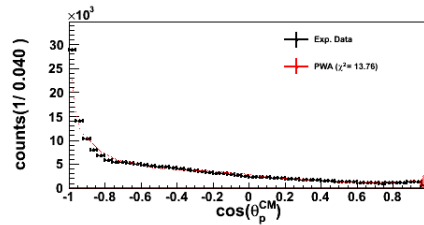
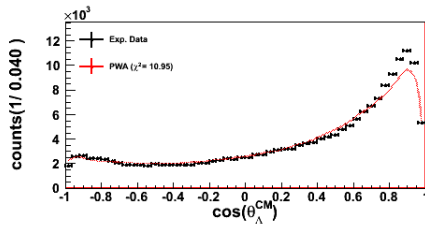
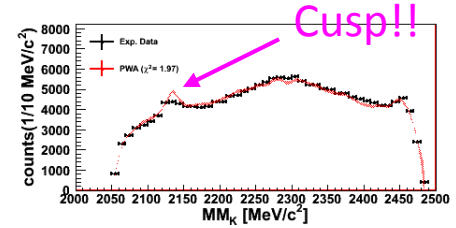
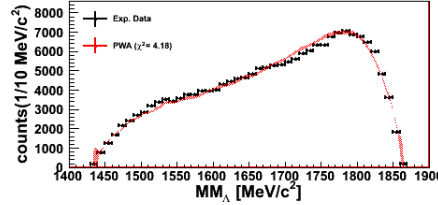
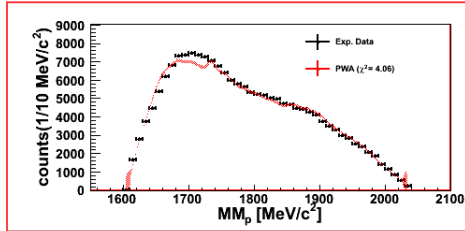
PWA

2.56



# DISTO@2.85 GeV

Preliminary

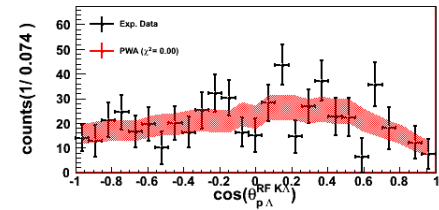
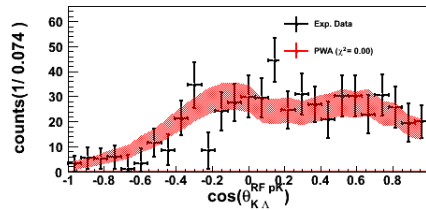
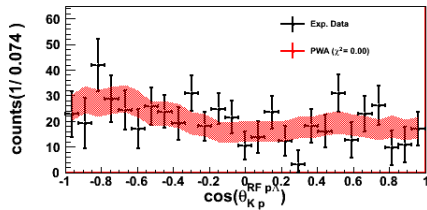
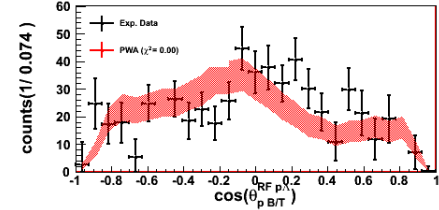
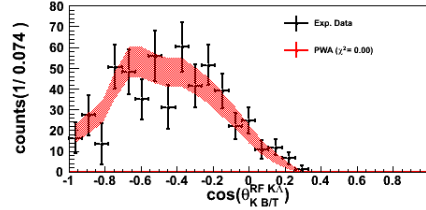
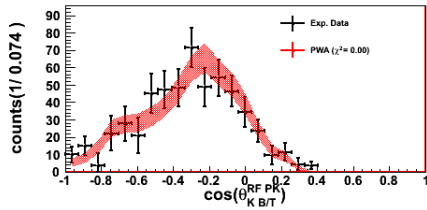
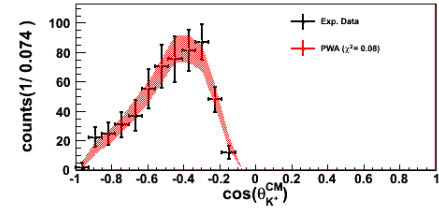
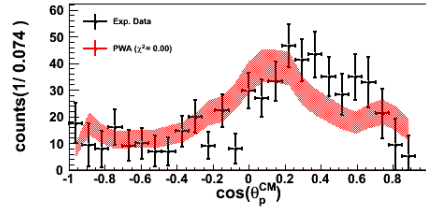
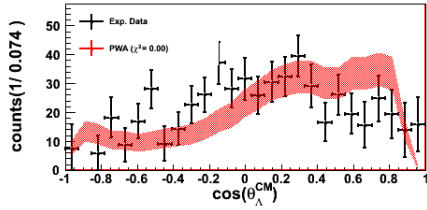
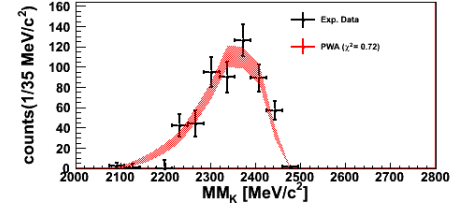
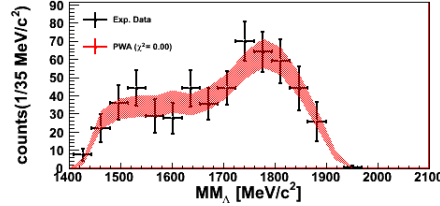
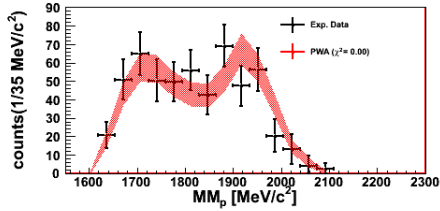


$\chi^2 / \text{ndf}$  (ndf=428)

PWA

3.55

# FOPI



$\chi^2 / \text{ndf}$  (ndf=428)

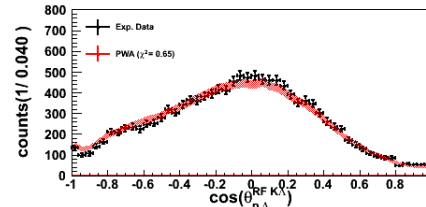
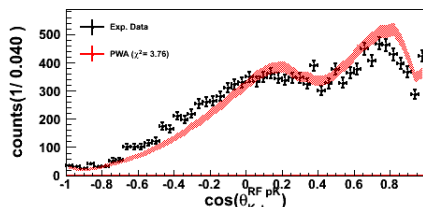
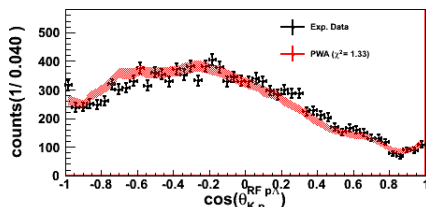
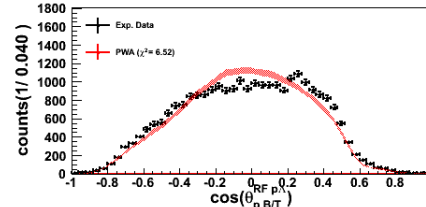
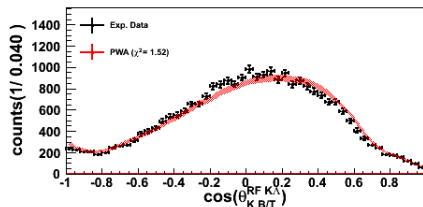
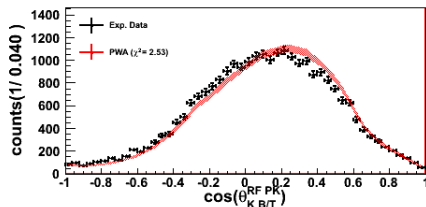
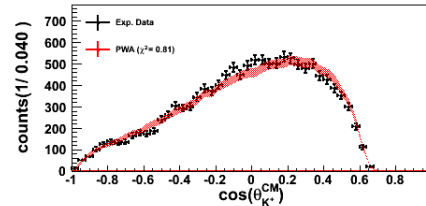
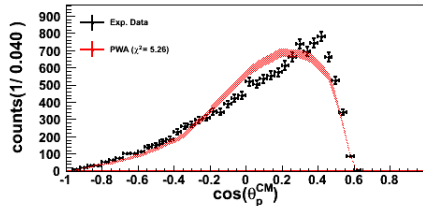
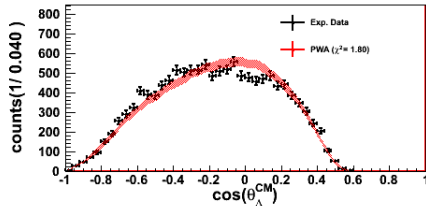
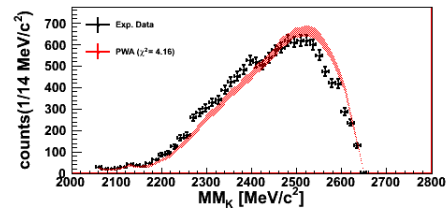
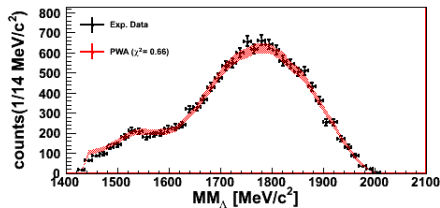
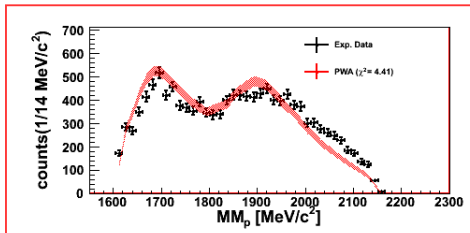
PWA

0.91



# HADES

Preliminary



$\chi^2 / \text{ndf}$  (ndf=428)

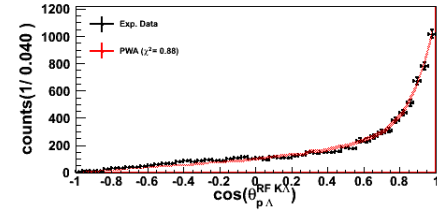
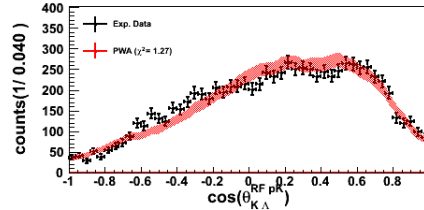
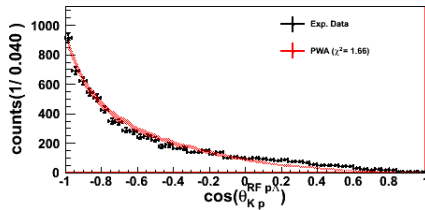
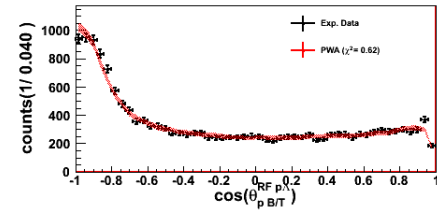
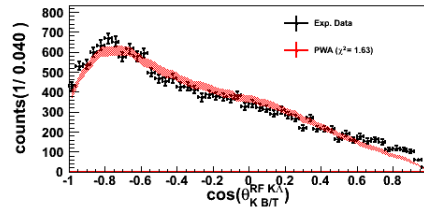
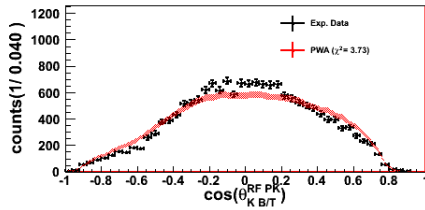
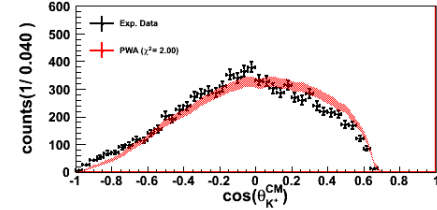
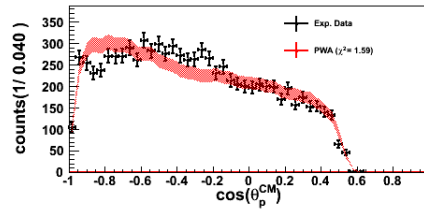
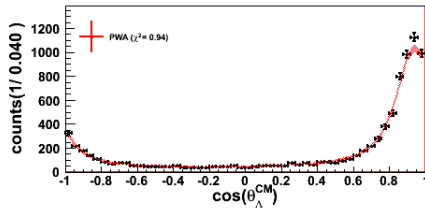
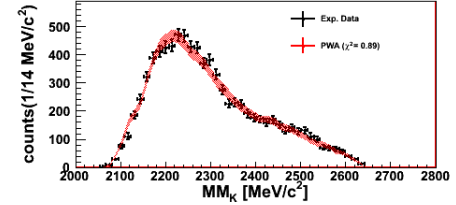
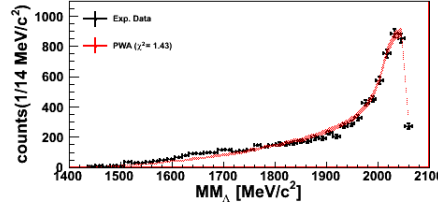
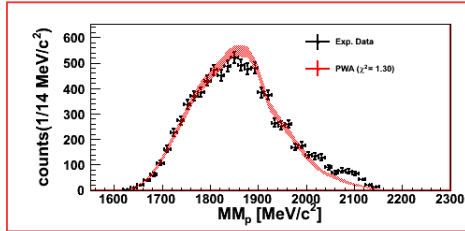
PWA

2.14



# HADES - WALL

Preliminary



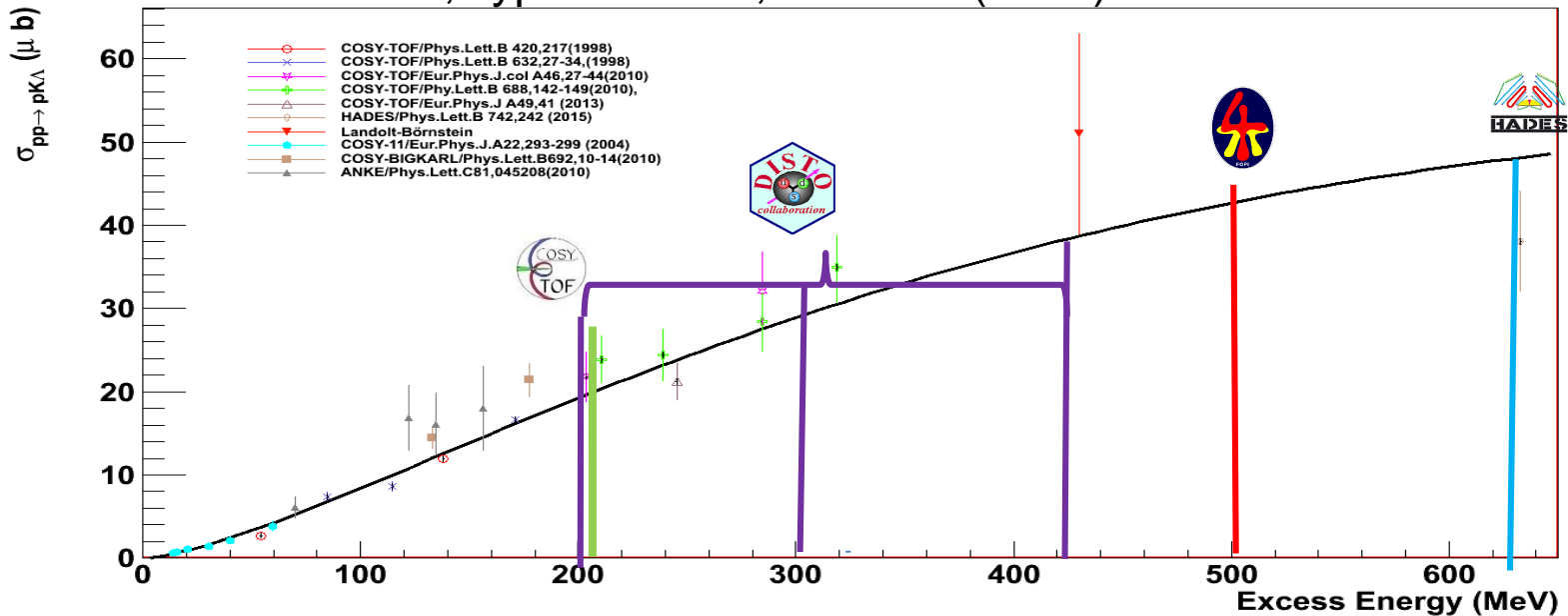
$\chi^2 / \text{ndf}$  (ndf=428)

PWA

1.86

# Total Cross Section

R.Muenzer et al., Hyperfine 233, 159-166 (2016)



Value:

$$\sigma_{pK\Lambda} = C_1 \left( 1 - \frac{s_0}{(\sqrt{s_0} + \epsilon)^2} \right)^{C_2} \left( \frac{s_0}{(\sqrt{s_0} + \epsilon)^2} \right)^{C_3}$$

$$C_1 = 4.03 \pm 0.57 \cdot 10^2$$

$$C_2 = 1.49 \pm 0.04$$

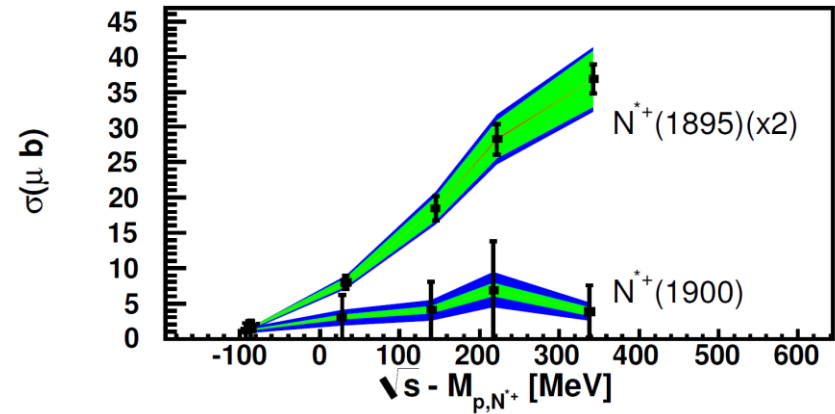
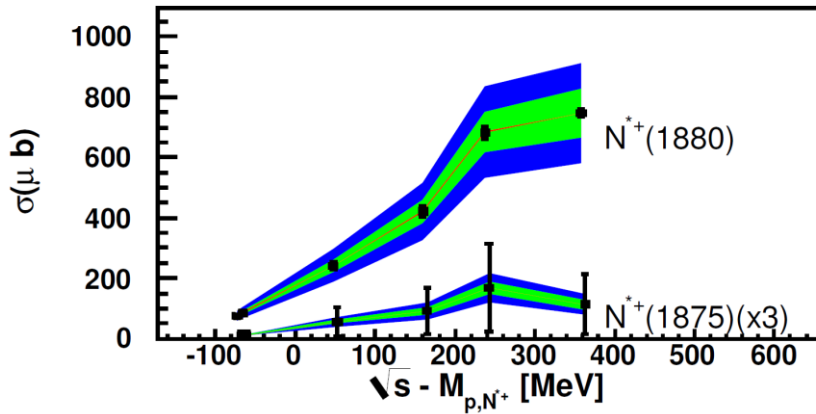
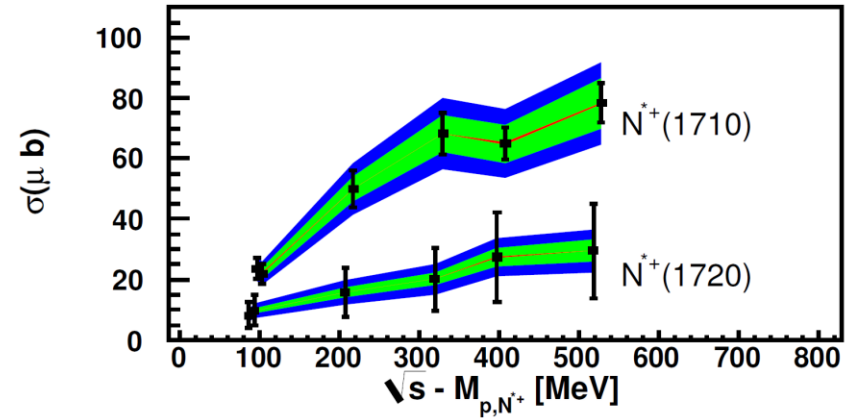
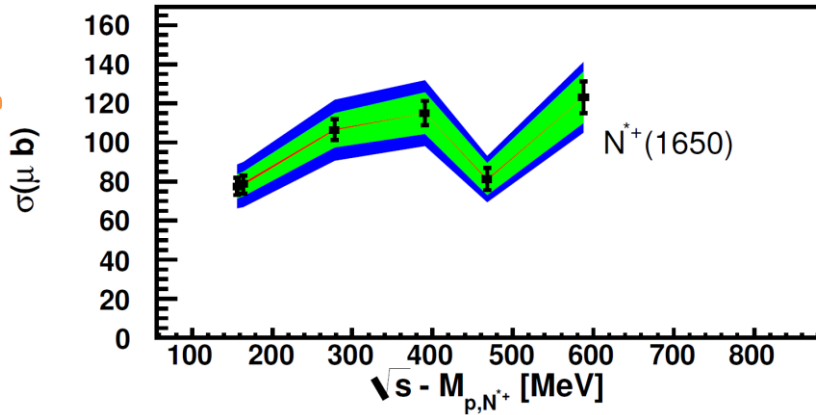
$$C_3 = 1.43 \pm 0.39$$

# Branching Ratio

	Mass [GeV/c <sup>2</sup> ]	Width [GeV/c <sup>2</sup> ]	$\Gamma_{\Lambda K}/\Gamma_{All}$ %
N(1650)S <sub>11</sub>	1.655	0.150	3-11
N(1710)P <sub>11</sub>	1.710	0.200	5-25
N(1720)D <sub>13</sub>	1.720	0.250	1-15
N(1875)D <sub>13</sub>	1.875	0.220	4±2
N(1880)P <sub>11</sub>	1.870	0.235	2±1
N(1895)S <sub>11</sub>	1.895	0.090	18±5
N(1900)P <sub>13</sub>	1.900	0.250	0-10

# Cross Section

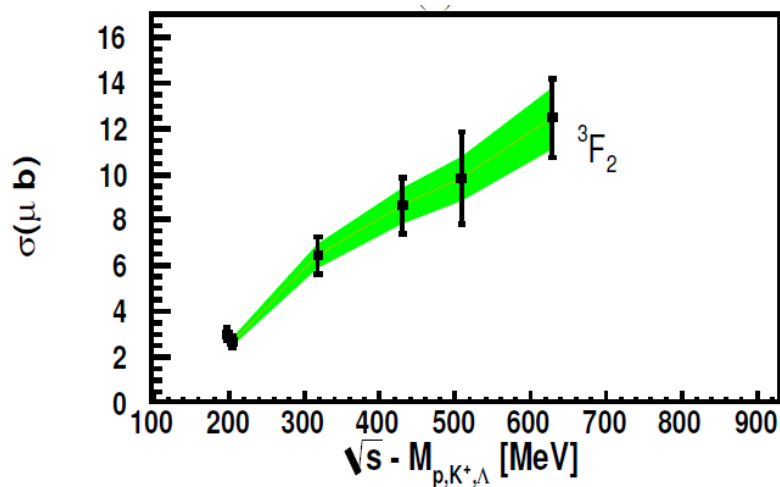
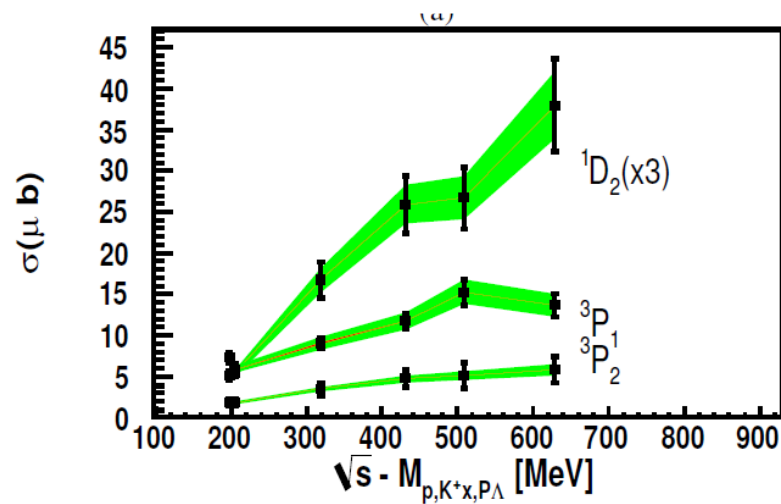
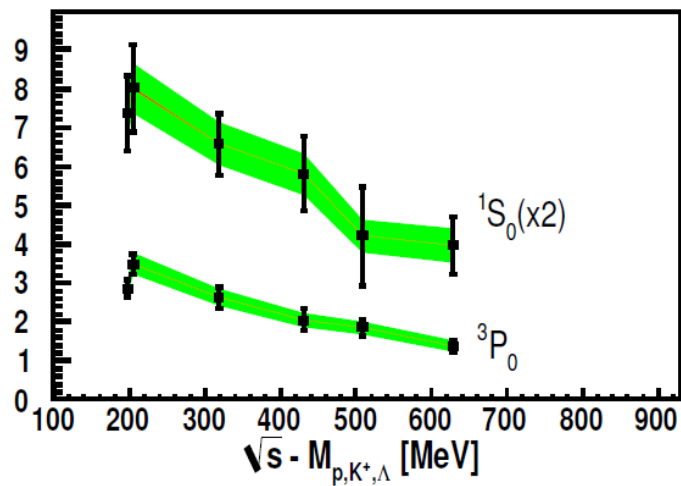
Preliminary



Non Resonant-Resonant: 20%-80%

# Initial State

Preliminary



# Final State Interaction in PWA

$$A_{2b}^{\beta} = \frac{\sqrt{s_i}}{1 + \frac{1}{2} r^{\beta} q^2 a_{p\Lambda}^{\beta} + i q a_{p\Lambda}^{\beta} q^{2L} / F(q, r^{\beta}, L)}$$

$a_{p\Lambda}^{\beta}$  Scattering Length For  $l=0$

$r^{\beta}$  Effective Range of System

$$\alpha_s = -1.43 \pm 0.36 \pm 0.09 \text{ fm} \quad \alpha_t = -1.88 \pm 0.38 \pm 0.10 \text{ fm}$$

$$r_s = 1.31 \pm 0.24 \pm 0.16 \text{ fm} \quad r_t = 1.04 \pm 0.78 \pm 0.15 \text{ fm}$$

Source	$^1S_0 a_{\Lambda-p}$ [fm]	$^1S_0 r_{\Lambda-p}$ [fm]	$^3S_1 a_{\Lambda-p}$ [fm]	$^3S_1 r_{\Lambda-p}$ [fm]	$\langle a_{\Lambda-p} \rangle$ [fm]
This work	$-1.43 \pm 0.36 \pm 0.09$	$1.31 \pm 0.24 \pm 0.16$	$-1.88 \pm 0.38 \pm 0.10$	$1.04 \pm 0.78 \pm 0.15$	
NLO <sup>2</sup> [15]	-2.91	2.78	-1.54	2.72	-1.88 <sup>3</sup>
LO <sup>2</sup> [15]	-1.91	1.40	-1.23	2.13	-1.4 <sup>3</sup>
[16]	$-1.8_{-4.2}^{+2.3}$	-	$-1.6_{-0.8}^{+1.1}$	-	-
[17]	-	-	-	-	$-1.25 \pm 0.08 \pm 0.03$
[18]	-	-	$-1.31_{-0.49}^{+0.32} \pm 0.3 \pm 0.16$	-	$-1.233 \pm 0.014 \pm 0.3 \pm 0.12$

[15] Haidenbauer et al. Nuclear Physics A, 915, 24-58 (2013)

[16] G. Alexander et al., Phys. Rev. 173, 1452 (1968).

[17] M. Roeder et al., Eur. Phys. J. A 49, 157 (2013)

[18] Hauenstein 2014

# Data Sets for Cusp Analysis

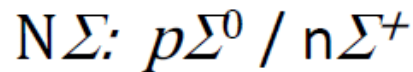
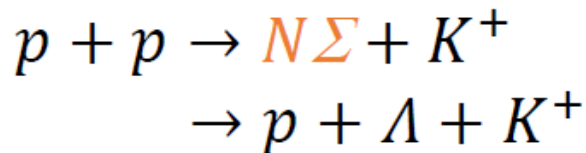
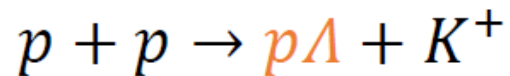
Experiment	$E_B$ [GeV]	$pK^+\Lambda$ Statistics	Status
COSY-TOF	1.96	$\sim 160k$	In Preparation (not used in the analysis)
DISTO	2.15	121 k	Available
COSY-TOF	2.16	43 k	Available
COSY-TOF	2.16	$\sim 90k$	In Preparation (not used in the analysis)
DISTO	2.5	304 k	Available
DISTO	2.85	424 k	Available
FOPI	3.1	0.9 k	Single PWA
HADES	3.5	21 k	Single PWA



# Cusp Effect

Effect close to the  $\Sigma N$  threshold

*Coupled Channel Interaction*

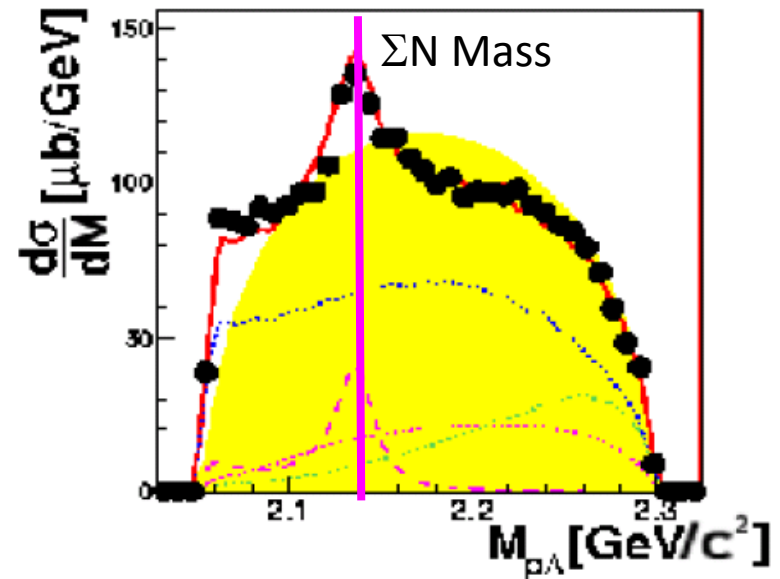


The  $\Sigma$  and  $N$  are expected to be in a relative *s-wave state*.

spin-parity of the  $N\Sigma$  system is either  $J^P = 0^+$  or  $1^+$ .

## ● Cosy-TOF Analysis:

S.Abd El-Samad, Eur.Phys.J A49(2013)



Solid line: Full MC simulation

Shaded areas: phase-space distributions

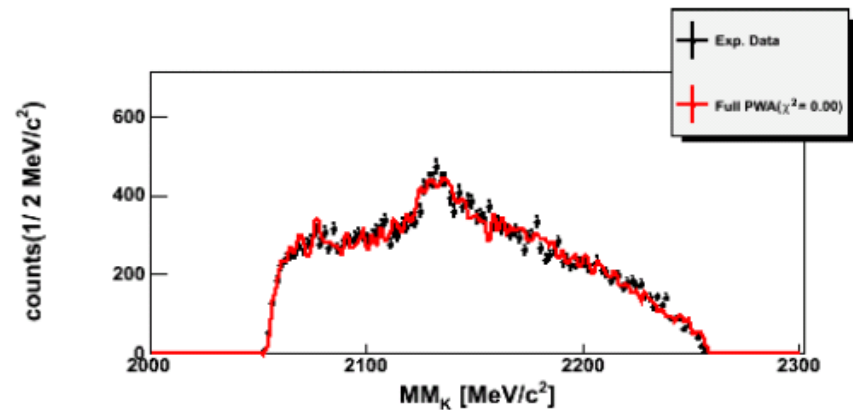
# BG-PWA + Breit-Wigner approach

The Relativistic Breit-Wigner distribution:

$$\frac{d\sigma_{p\Lambda}}{dm_{p\Lambda}} \approx \frac{1}{m_R^2 - m_{p\Lambda}^2 - i\Gamma m_{p\Lambda}}$$

$m_R$	Mass of resonance
$\Gamma$	Width of resonance
$m_{p\Lambda}$	Invariant mass of $p\Lambda$

- COSY-TOF 2.16GeV
- Invariant Mass  $m_R$ : 2:13 GeV/c<sup>2</sup>
- Width  $\Gamma$ : 0.02 GeV/c<sup>2</sup>



Data from: M. Roeder et al., Eur. Phys. J. A 49, 157 (2013)

# BG-PWA + Flatté approach

The Flatté parameterization:

$$\frac{d\sigma_{p\Lambda}}{dm_{p\Lambda}} \approx \frac{C * m_R * \sqrt{\Gamma_{p\Lambda}\Gamma_o}}{|m_R^2 - m_{p\Lambda}^2 - im_{p\Lambda}(\Gamma_{p\Lambda} + \Gamma_{p\Sigma})|^2}$$

$m_R$  Mass of resonance

$\Gamma$  Width of resonance

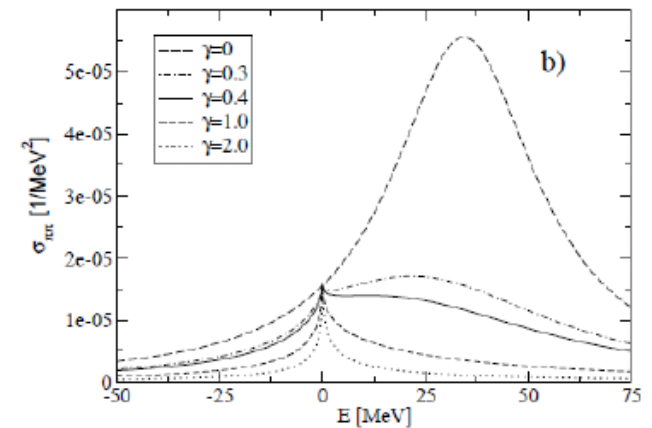
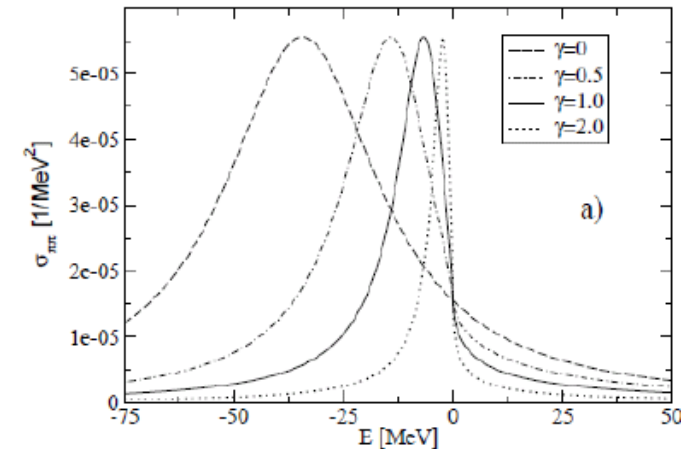
$m_{p\Lambda}$  Invariant mass of  $p\Lambda$

$$\Gamma_{p\Lambda} = g_{p\Lambda} * q_{p\Lambda} \quad \Gamma_{p\Sigma} = g_{p\Sigma} * q_{p\Sigma}$$

$g_{p\Lambda}, g_{p\Sigma}$  Coupling constant squared

$q_{p\Lambda}, q_{p\Sigma}$  c.m. momentum

$$q_{p\Sigma} = i * \frac{\sqrt{((m_\Sigma + m_p)^2 - m_{p\Sigma}^2) * (m_{p\Sigma}^2 - (m_p - m_\Sigma)^2)}}{2m_{p\Sigma}}$$

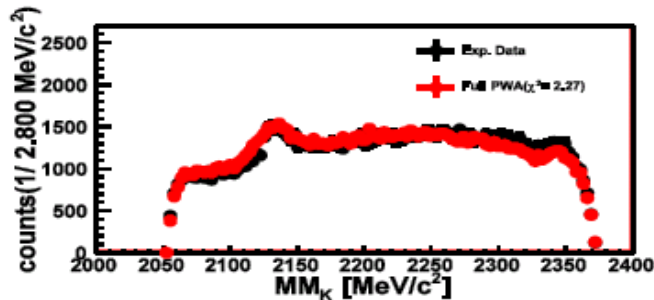


# BG-PWA + Flatté approach

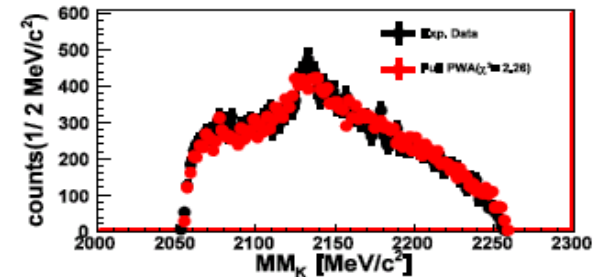
## Combined data analysis

Preliminary

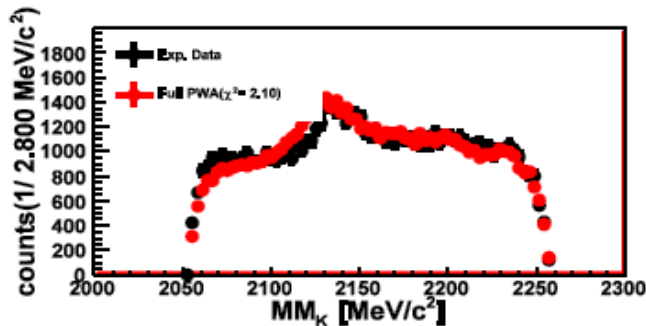
● DISTO 2.5GEV



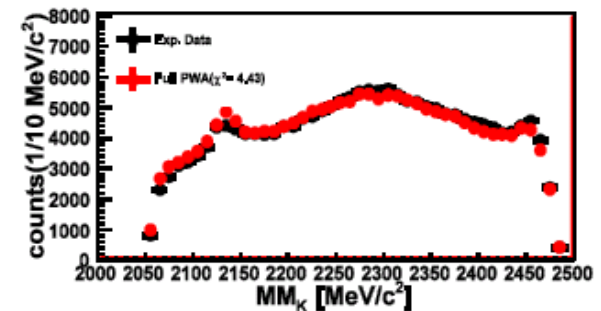
● COSY-TOF 2.16GEV



● DISTO 2.14GEV



● DISTO 2.85GEV



- Final coupling constants:  $g_{N\Sigma} = 1.55 \pm 0.08 \times 10^{-2}$ ,  $g_{p\Lambda} = 0.30 \pm 0.03 \times 10^{-2}$
- Threshold mass value from the fit:  $m_R = 2.13 \pm 0.006 \text{ GeV}/c^2$

# Summary and Outlook

- Combined Analysis for COSY & DISTO & HADES & FOPI completed for N\*
- Systematical Analysis performed
- Excitation Function for N\* and pKL extracted
- Scattering Length p- $\Lambda$  separate for Singlet and Triplet
- Cusp Wave: preliminary studies on 4 data set
  
- Paper 1) is being Finalized at the Moment ( N\*)
- Estimation of the global upper limit for ppK-
- Global analysis including the cusp with Flatte'