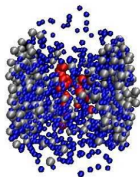


# Hadron production from PHSD in heavy-ion reactions from 1 to 160 A GeV

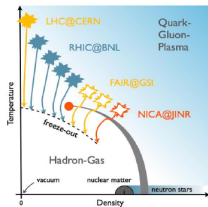
Alessia Palmese

in collaboration with W. Cassing, P. Moreau, E.L. Bratkovskaya  
Institut für Theoretische Physik, Gießen

The 3<sup>rd</sup> Strangeness Workshop, Warsaw, 22 April 2016

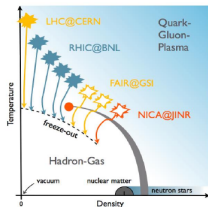


**Beam Energy scan** is pointing at lower energies to explore systems with higher baryon density.

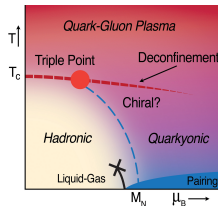


# Motivation

**Beam Energy scan** is pointing at lower energies to explore systems with higher baryon density.

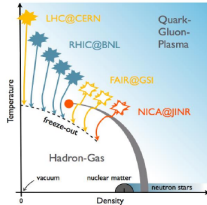


Can we find a manifestation of the **Chiral Symmetry restoration** in Heavy-Ion Collisions (HIC) observables?

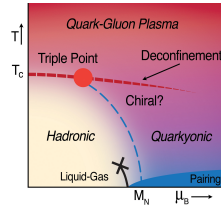


# Motivation

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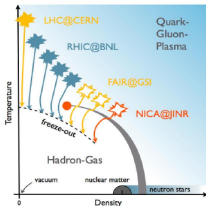


There are many open questions related to the **strangeness production** in HIC!

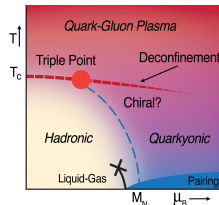


# Motivation

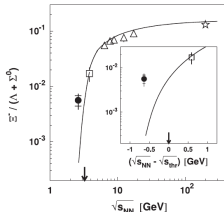
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High multiplicities of  $\Xi^-$ .

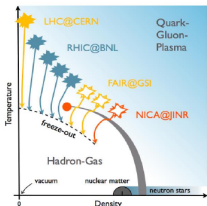


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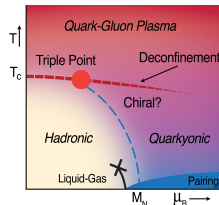
(G. Agakishiev et al., HADES Collaboration, Phys. Rev. Lett. 103, 132301, 2009.)

# Motivation

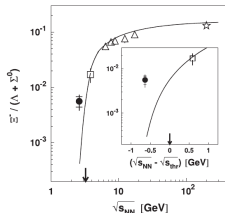
Beam Energy scan is pointing at lower energies to explore systems with higher baryon density.



Can we find a manifestation of the **Chiral Symmetry restoration** in Heavy-Ion Collisions (HIC) observables?



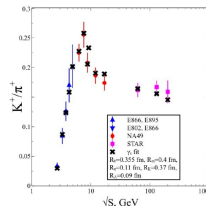
High multiplicities of  $\Xi^-$ .



(G. Agakishiev et al., HADES Collaboration, Phys. Rev. Lett. 103, 132301, 2009.)

There are many open questions related to the **strangeness production** in HIC!

"Horn" feature of  $K^+/\pi^+$ .

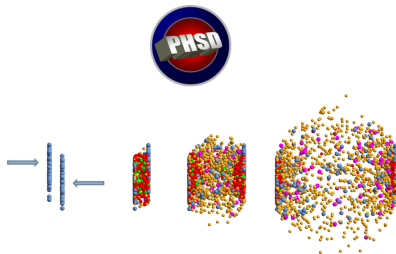


(K. A. Bugaev et al., arXiv:1511.06698v1, 2015.)

- 1** Parton Hadron String Dynamics (PHSD)
  - Dynamical Quasi-Particle Model (DQPM)
  - Stages of a heavy-ion collision
- 2** Low energy strangeness production in PHSD
  - Low energy production channels
  - Results on the  $\Xi$  yield
- 3** Chiral Symmetry restoration
  - String dynamics
  - Chiral Symmetry restoration in PHSD
  - Results
- 4** Conclusions

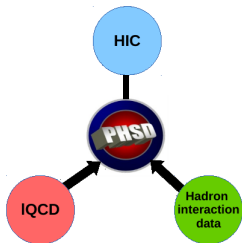
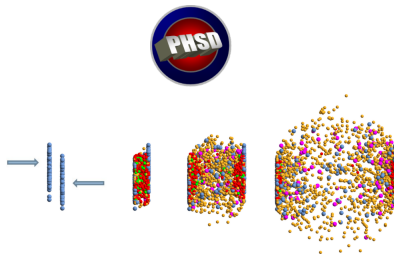
# Parton Hadron String Dynamics (PHSD)

- Dynamical many-body transport approach.
- Consistently describes the full time evolution in HIC.
- Explicit parton-parton interactions, explicit phase transition from hadronic to partonic degrees of freedom.



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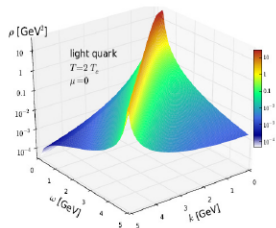
- Model applicable out of equilibrium and in agreement with the lattice results in equilibrium as well as with the nuclear physics input.
- Transport theory: off-shell transport equations in phase-space representation based on Kadanoff-Baym equations for the partonic and hadronic phase.

W.Cassing, E.Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215; W.Cassing, EPJ ST 168 (2009) 3.

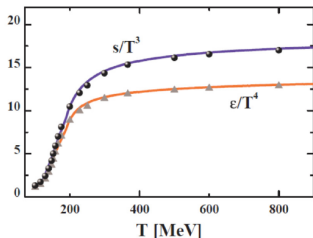
# Dynamical Quasi-Particle Model (DQPM)

The QGP phase is described in terms of interacting quasi-particles with Lorentzian spectral functions:

$$\rho_i(\omega, T) = \frac{4\omega\Gamma_i(T)}{(\omega^2 - \mathbf{p}^2 - M_i^2(T))^2 + 4\omega^2\Gamma_i^2(T)}, \quad (i = q, \bar{q}, g)$$

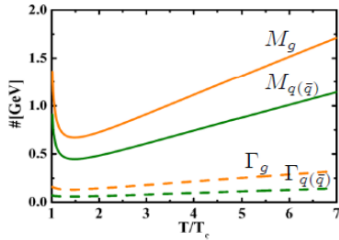


Properties of quasi-particles are fitted to the lattice QCD results:



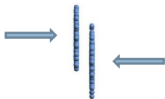
Peshier, Cassing, PRL 94 (2005) 172301; Cassing, NPA 791 (2007) 365; NPA 793 (2007) .

Masses and widths of partons depend on the temperature of the medium:

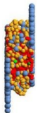


# Stages of a heavy-ion collision in PHSD

Initial A+A  
collision



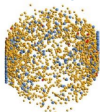
Partonic  
phase



Hadronization

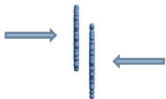


Hadronic phase

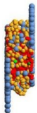


# Stages of a heavy-ion collision in PHSD

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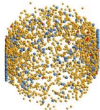
Partonic  
phase



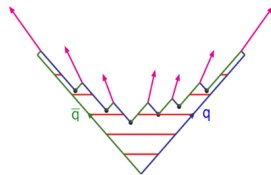
Hadronization



Hadronic phase

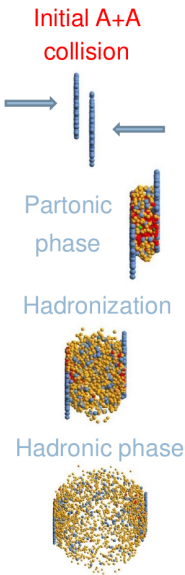


- **String formation** in primary NN Collisions.
- **String decays** to pre-hadrons (baryons and mesons).

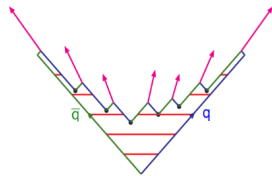




# Stages of a heavy-ion collision in PHSD



- **String formation** in primary NN Collisions.
- **String decays** to pre-hadrons (baryons and mesons).
- Formation of a **QGP state** if  $\epsilon > \epsilon_C \approx 0.5 \text{ GeV fm}^{-3}$ .
- Dissolution of newly produced secondary hadrons into **massive colored quarks/antiquarks** and **mean-field energy**  $U_q$ :

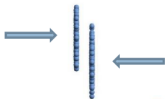


- **DQPM** defines the properties (masses and widths) of partons and mean-field potential at a given local energy density  $\epsilon$ :

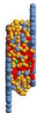
$$m_q(\epsilon) \quad \Gamma_q(\epsilon) \quad U_q(\epsilon).$$

# Stages of a heavy-ion collision in PHSD

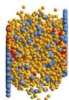
Initial A+A  
collision



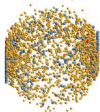
Partonic  
phase



Hadronization

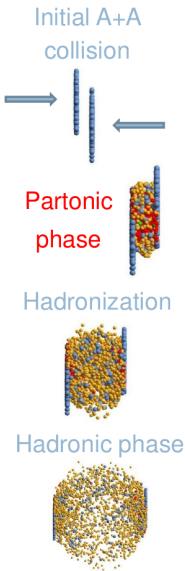


Hadronic phase



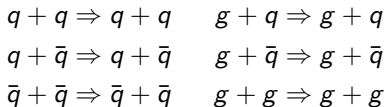
- Propagation of partons, considered as dynamical quasi-particles, in a self-generated mean-field potential from the DQPM.
- EoS of partonic phase: crossover from Lattice QCD fitted by DQPM.

# Stages of a heavy-ion collision in PHSD

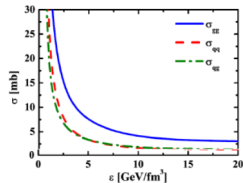
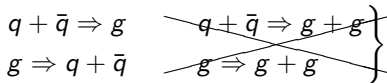


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- EoS of partonic phase: crossover from Lattice QCD fitted by DQPM.

- (Quasi-)elastic collisions:

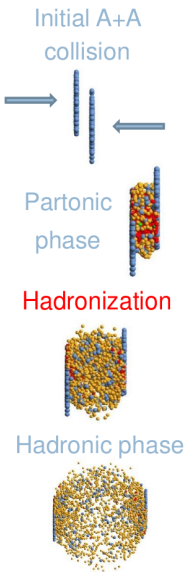


- Inelastic collisions:

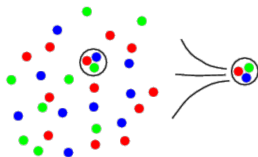


Suppressed due to the large gluon mass.

# Stages of a heavy-ion collision in PHSD



- Massive and off-shell (anti-)quarks hadronize to colorless off-shell mesons and baryons:



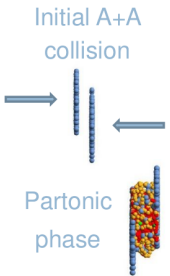
$$g \Rightarrow q + \bar{q}$$

$$q + \bar{q} \Rightarrow \text{meson ('string')}$$

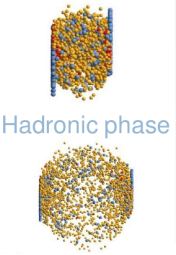
$$q + q + q \Rightarrow \text{baryon ('string')}$$

- Local covariant off-shell transition rate.
- Strict 4-momentum and quantum number conservation.

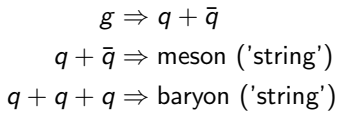
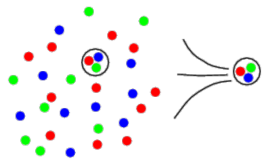
# Stages of a heavy-ion collision in PHSD



Hadronization

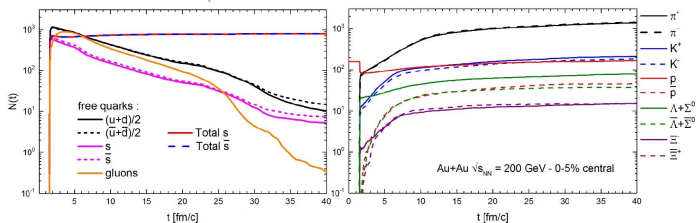


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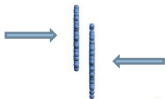
- Local covariant off-shell transition rate.
- Strict 4-momentum and quantum number conservation.

Central Au+Au – Top RHIC

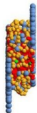


# Stages of a heavy-ion collision in PHSD

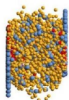
Initial A+A  
collision



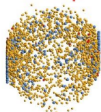
Partonic  
phase



Hadronization



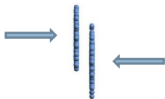
Hadronic phase



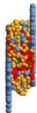
- Hadron-string interactions – **off-shell HSD**.
- Elastic and inelastic collisions between baryons ( $B$ ), mesons ( $m$ ) and resonances ( $R$ ).

# Stages of a heavy-ion collision in PHSD

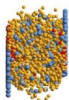
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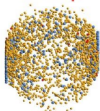
Partonic  
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Hadronization

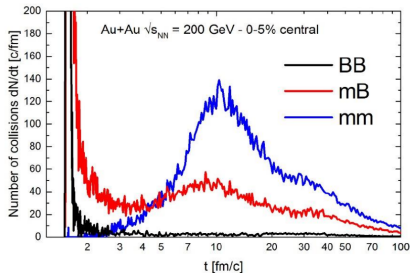


Hadronic phase



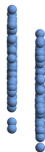
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Distribution of hadron collisions as a function of time:








# Stages of a heavy-ion collision in PHSD

$t = 0.1 \text{ fm}/c$



**Au + Au  $\sqrt{s_{NN}} = 200 \text{ GeV}$**   
 **$b = 2.2 \text{ fm}$  – Section view**

-  Baryons (394)
-  Antibaryons ( 0)
-  Mesons ( 0)
-  Quarks ( 0)
-  Gluons ( 0)

P. Moreau








# Stages of a heavy-ion collision in PHSD

$t = 1.63549 \text{ fm}/c$



$\text{Au} + \text{Au} \sqrt{s_{\text{NN}}} = 200 \text{ GeV}$   
 $b = 2.2 \text{ fm}$  – Section view

-  Baryons (394)
-  Antibaryons ( 0)
-  Mesons (1598)
-  Quarks (4383)
-  Gluons (344)


P. Moreau

# Stages of a heavy-ion collision in PHSD

$t = 2.06543 \text{ fm}/c$



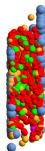
**Au + Au  $\sqrt{s_{NN}} = 200 \text{ GeV}$**   
 **$b = 2.2 \text{ fm}$  – Section view**

-  Baryons (396)
-  Antibaryons ( 2)
-  Mesons (1136)
-  Quarks (5066)
-  Gluons (516)

P. Moreau

# Stages of a heavy-ion collision in PHSD

$t = 3.20258 \text{ fm}/c$



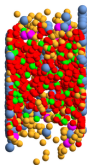
**Au + Au  $\sqrt{s_{NN}} = 200 \text{ GeV}$**   
**b = 2.2 fm – Section view**

-  Baryons (413)
-  Antibaryons ( 13)
-  Mesons (1080)
-  Quarks (4708)
-  Gluons (761)



P. Moreau

# Stages of a heavy-ion collision in PHSD

$t = 5.56921 \text{ fm}/c$



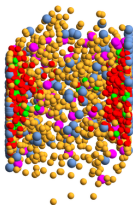
**Au + Au  $\sqrt{s_{NN}} = 200 \text{ GeV}$**   
**b = 2.2 fm – Section view**

-  Baryons (472)
-  Antibaryons ( 70)
-  Mesons (1724)
-  Quarks (3843)
-  Gluons (652)




P. Moreau

# Stages of a heavy-ion collision in PHSD

$t = 8.06922 \text{ fm}/c$



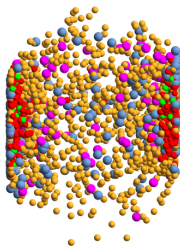
**Au + Au  $\sqrt{s_{NN}} = 200 \text{ GeV}$**   
**b = 2.2 fm – Section view**

-  Baryons (559)
-  Antibaryons (139)
-  Mesons (2686)
-  Quarks (2628)
-  Gluons (442)

P. Moreau



# Stages of a heavy-ion collision in PHSD

$t = 10.5692 \text{ fm/c}$



**Au + Au  $\sqrt{s_{NN}} = 200 \text{ GeV}$**

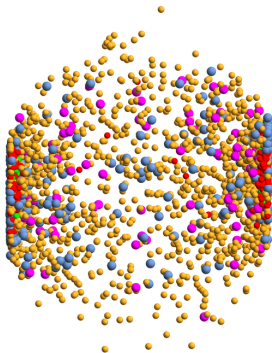
**b = 2.2 fm – Section view**

-  Baryons (604)
-  Antibaryons (187)
-  Mesons (3169)
-  Quarks (2076)
-  Gluons (319)

P. Moreau




# Stages of a heavy-ion collision in PHSD

$t = 15.5692 \text{ fm}/c$



**Au + Au  $\sqrt{s_{NN}} = 200 \text{ GeV}$**

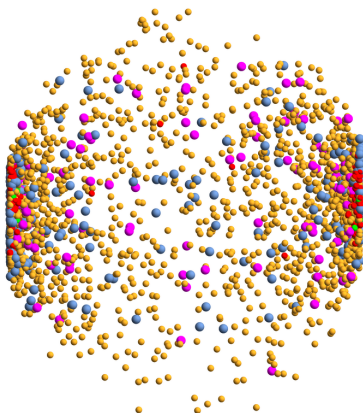
**b = 2.2 fm – Section view**

-  Baryons (662)
-  Antibaryons (229)
-  Mesons (3661)
-  Quarks (1499)
-  Gluons (175)





P. Moreau

# Stages of a heavy-ion collision in PHSD

$t = 20.5692 \text{ fm}/c$



**Au + Au  $\sqrt{s_{NN}} = 200 \text{ GeV}$**   
**b = 2.2 fm – Section view**

-  Baryons (692)
-  Antibaryons (266)
-  Mesons (4022)
-  Quarks (1184)
-  Gluons ( 90)

P. Moreau



# Low energy production channels in PHSD

## List of **Baryon-Baryon channels** in PHSD

$$NN \Leftrightarrow NN$$

$$NN \Leftrightarrow N\Delta$$

$$NN \Leftrightarrow NN^*$$

$$NN^* \Leftrightarrow NN'^*$$

$$N\Delta \Leftrightarrow NN^*$$

$$\Delta\Delta \Leftrightarrow NN^*$$

$$NN \Leftrightarrow NN\pi$$

( $N^* = N(1440), N(1535)$ )

for  $\sqrt{s} > \sqrt{s_{thre}} = 2.65 \text{ GeV} \Rightarrow$  String Fragmentation  
( $NN \rightarrow NYK, NN \rightarrow \Delta YK, N\Delta \rightarrow NYK, \Delta\Delta \rightarrow NYK$ ).

# Low energy production channels in PHSD

## List of **Baryon-Baryon** channels in PHSD

$$NN \Leftrightarrow NN$$

$$NN \Leftrightarrow N\Delta$$

$$NN \Leftrightarrow NN^*$$

$$NN^* \Leftrightarrow NN'^*$$

$$N\Delta \Leftrightarrow NN^*$$

$$\Delta\Delta \Leftrightarrow NN^*$$

$$NN \Leftrightarrow NN\pi$$

$(N^* = N(1440), N(1535))$

for  $\sqrt{s} > \sqrt{s_{thre}} = 2.65 \text{ GeV} \Rightarrow$  String Fragmentation  
( $NN \rightarrow NYK$ ,  $NN \rightarrow \Delta YK$ ,  $N\Delta \rightarrow NYK$ ,  $\Delta\Delta \rightarrow NYK$ ).

**Strangeness** is always produced in pairs  $s\bar{s}$ .

In  $p + p$  collisions there is a strict energy threshold:

$$\sqrt{s_{th1}} = m_p + m_K + m_{\Lambda(\Sigma)} = 2.55(2.62) \text{ GeV} \quad \sqrt{s_{th2}} = m_p + 2 * m_K + m_{\Xi} = 3.24 \text{ GeV}$$

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### Hyperon ( $Y = \Lambda, \Sigma$ ) production

$$\pi + N \Leftrightarrow K + Y$$

$$N + N \Leftrightarrow N + K + Y$$

$$N + \bar{K} \Leftrightarrow Y + \pi$$



### Cascade $\Xi$ production

$$Y + \bar{K} \Leftrightarrow \Xi + \pi$$

$$Y + Y \Leftrightarrow \Xi + N$$



### Cascade $\Omega$ production

$$\Xi + \bar{K} \Leftrightarrow \Omega + \pi$$

$$\Xi + \Xi \Leftrightarrow \Omega + Y$$

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Focus on the  $\Xi$  production from **strangeness exchange reactions**.

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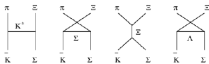
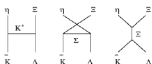
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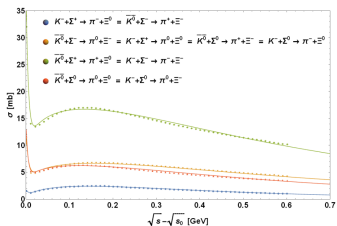
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← Born diagrams for  $\Xi$  production from strangeness m-B exchange reactions.



by Pierre Moreau

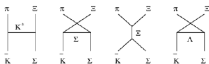
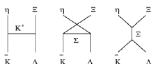
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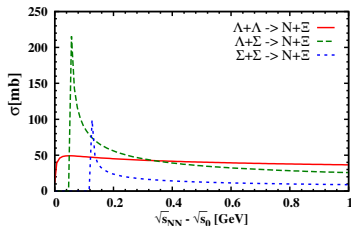
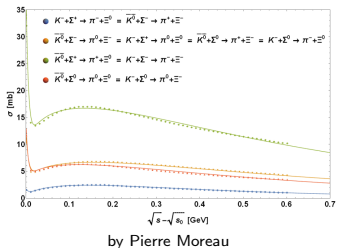
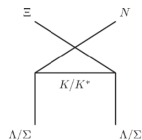
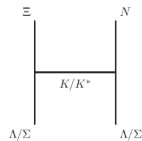
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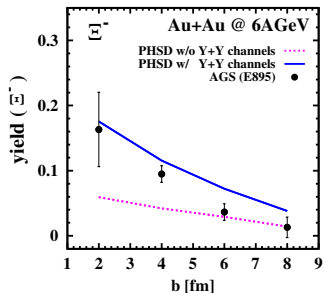
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Born diagrams for  $\Xi$  production from strangeness B-B exchange reactions. →

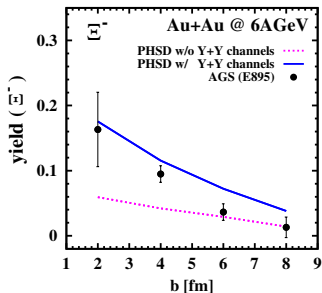




# Results on the $\Xi^-$ yield



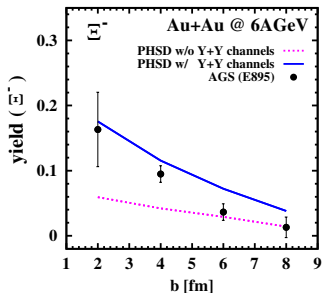
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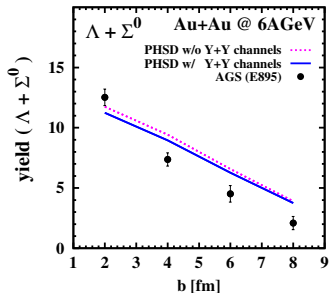
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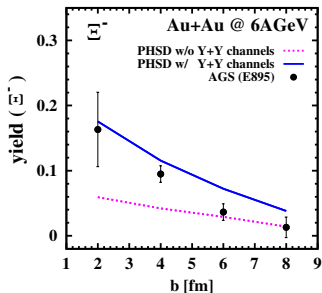


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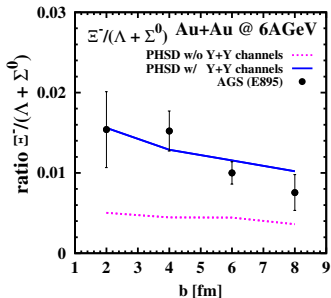
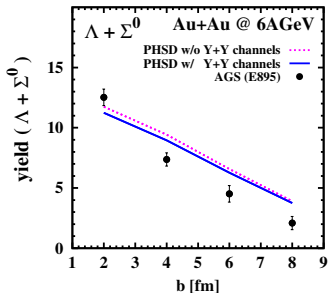


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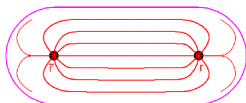


# String dynamics

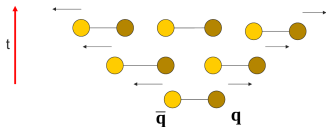
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A color flux connects the rapidly receding string-ends.

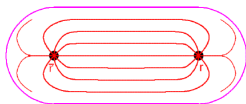


Production of virtual  $q\bar{q}$  or  $qq\bar{q}\bar{q}$  pairs which break the color field tube.

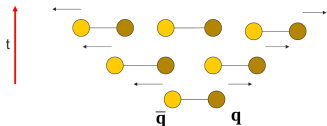


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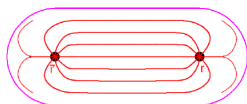
with  $\kappa \approx 0.176 \text{ GeV}^2$  and  $m_{u,d,s}$  as constituent masses.



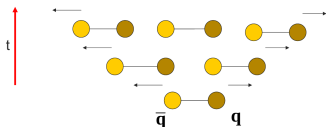
The relative production factors in PHSD/HSD are:

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$$f(x, m_T) \approx \frac{1}{x} (1 - x^a) \exp(-bm_T^2/x).$$



- In presence of a hot and dense hadronic medium, the degrees of freedom undergo modifications of their properties, e.g. the **mass**:

$$m_{q,s}^* = m_{q,s}^0 + (m_{q,s}^v - m_{q,s}^0) \left| \frac{\langle \bar{q}q \rangle}{\langle \bar{q}q \rangle_v} \right|,$$

where  $m_s^0 \approx 100 \text{ MeV}$  and  $m_q^0 \approx 7 \text{ MeV}$  for the bare quark masses and  $m_s^v \approx 500 \text{ MeV}$  and  $m_q^v \approx 350 \text{ MeV}$  for the vacuum quark masses.

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An estimate for  $\langle \bar{q}q \rangle$  is given by

Friman et al., Eur. Phys. J. A **3**, 165, 1998:

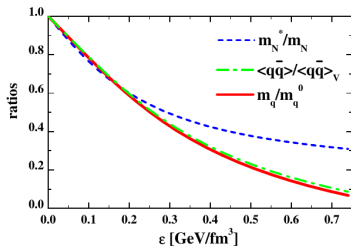
$$\frac{\langle \bar{q}q \rangle}{\langle \bar{q}q \rangle_V} = 1 - \frac{\Sigma_\pi}{f_\pi^2 m_\pi^2} \rho_S - \sum_h \frac{\sigma_h \rho_S^h}{f_\pi^2 m_\pi^2},$$

with  $\Sigma_\pi \approx 45 \text{ MeV}$ ,  $\sigma_h$  as the  $\sigma$ -commutator of the meson  $h$ ,  $\langle \bar{q}q \rangle_V \approx -3.2 \text{ fm}^{-3}$  (from the Gell-Mann-Oakes-Renner relation) and  $\rho_S$  as scalar density which can be obtained within the non-linear  $\sigma - \omega$  model.

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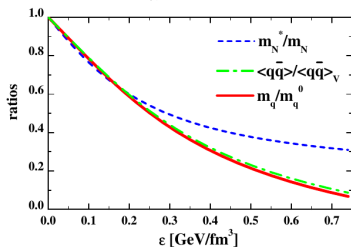
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In the **Schwinger formula** effective quark masses  $m_{q,s}^*$  have to be considered.

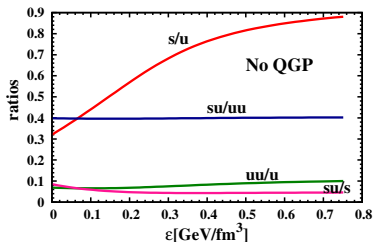


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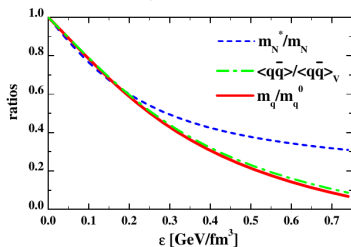


The **ratio s/u** increases with decreasing  $\langle q\bar{q} \rangle$  and increasing  $\epsilon$ .

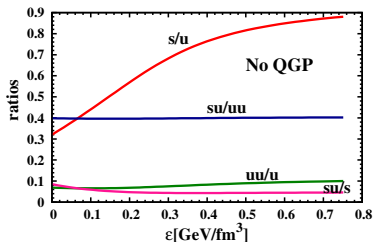


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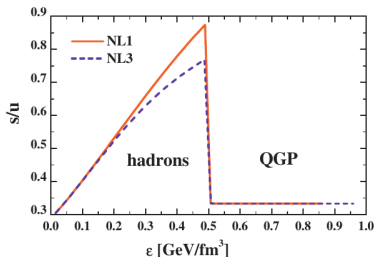
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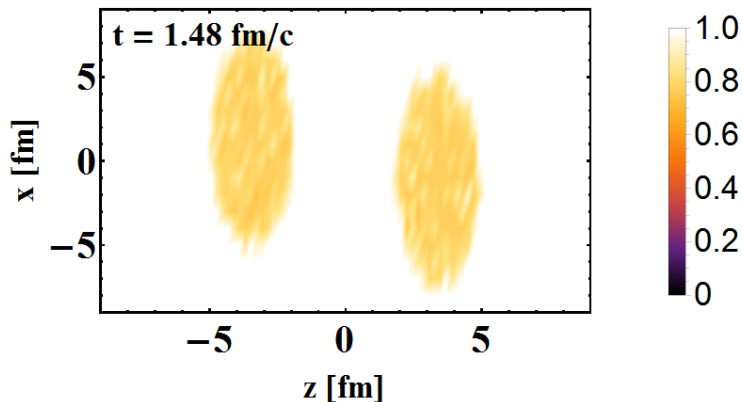


- **"Horn"** feature in the energy dependence of the  $s/u$  ratio!
- In the **QGP phase**, the string decay does not occur anymore and the  $s/u$  ratio drops.
- Some dependence on the nuclear EoS: **NL1 vs NL3**.



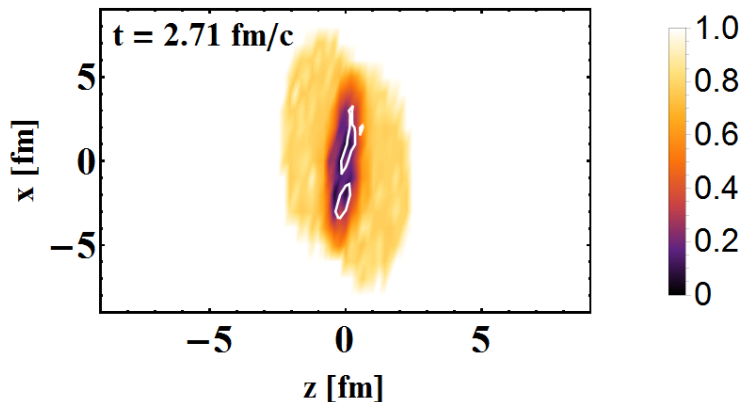
# Chiral Symmetry restoration: Results

Time evolution of the ratio  $\frac{\langle q\bar{q} \rangle}{\langle q\bar{q} \rangle_V}$   
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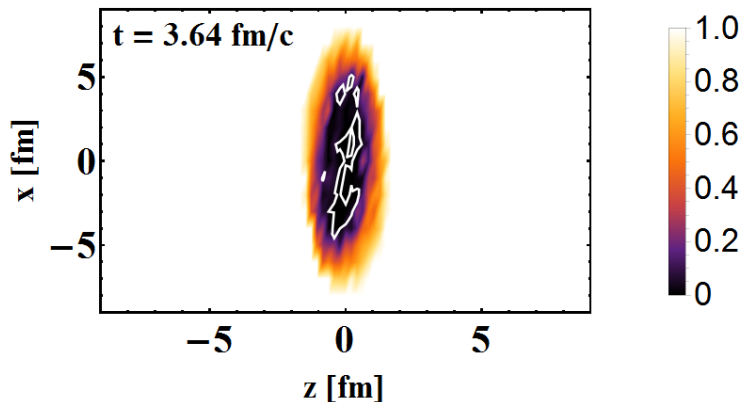
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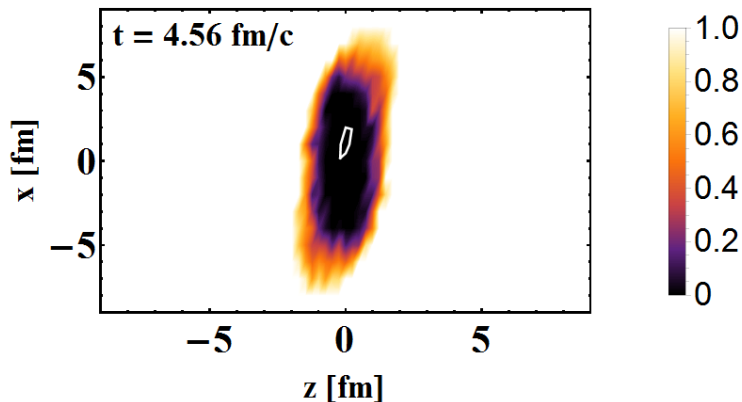
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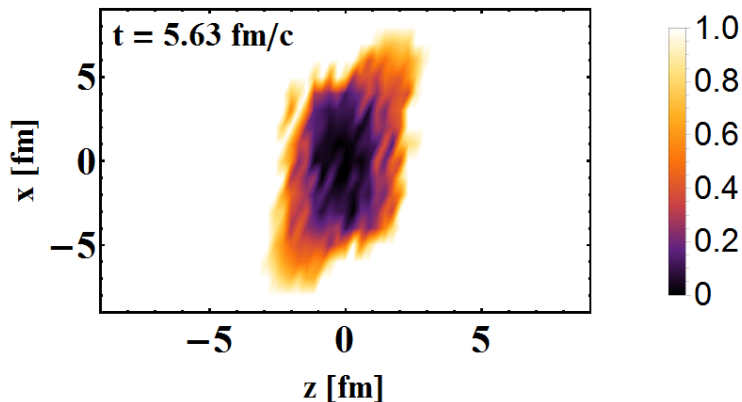
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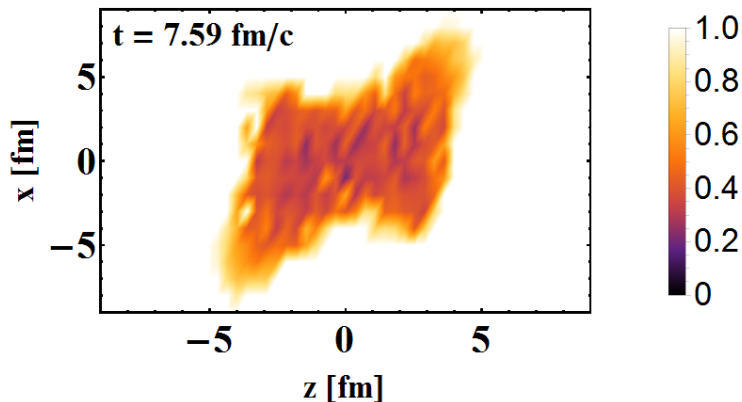
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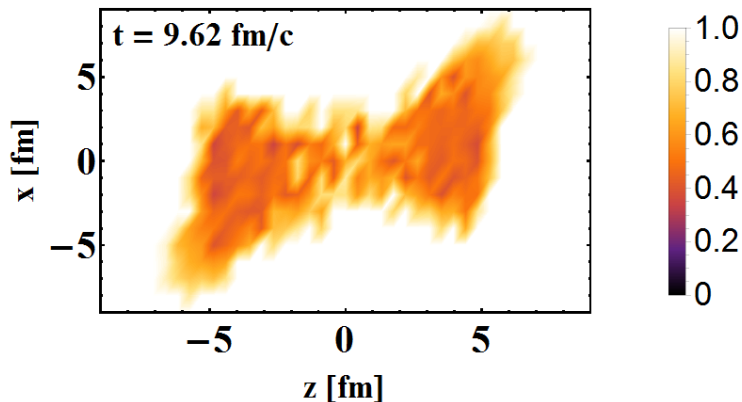
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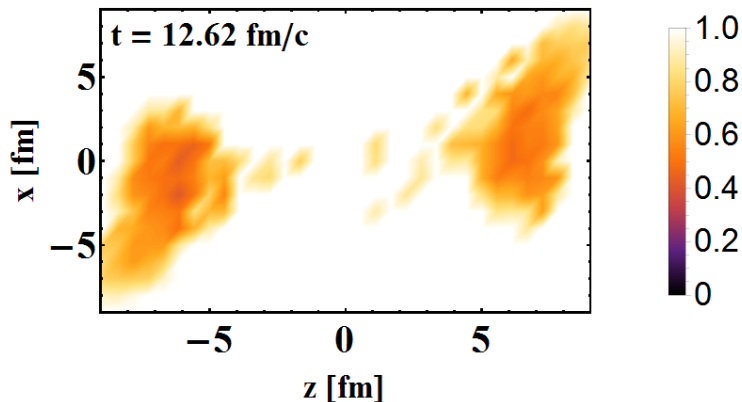
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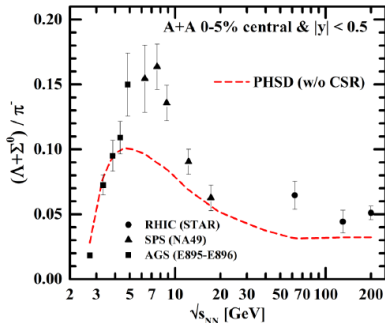
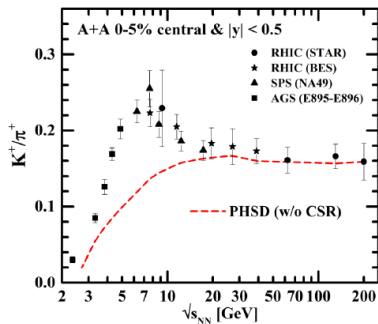
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# Chiral Symmetry restoration: Results

The scalar quark condensate  $\langle q\bar{q} \rangle$  is not a direct observable.

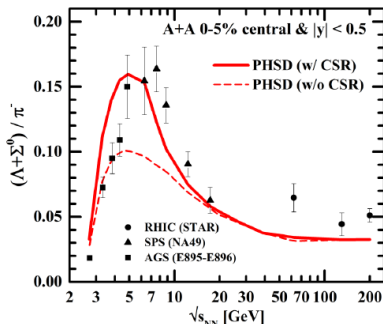
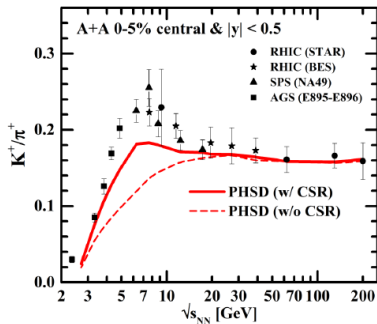
→ Can we find a manifestation of the Chiral Symmetry restoration indirectly in hadronic observables?



W. Cassing, A. P., P. Moreau, E.L. Bratkovskaya, Phys. Rev. C93 (2016) 014902.

# Chiral Symmetry restoration: Results

The strangeness enhancement at AGS/SPS energies (FAIR/NICA energies) is observed to be related to the partial restoration of Chiral Symmetry in the hadronic phase.

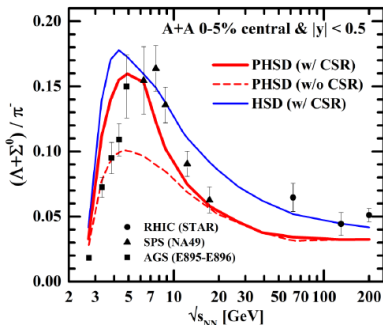
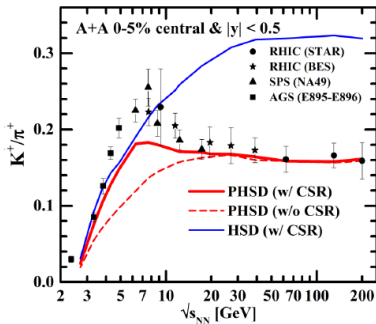


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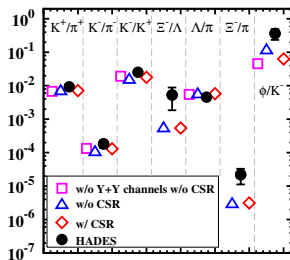
We observe a rise in the ratio  $K^+/\pi^+$  at low  $\sqrt{s_{NN}}$  related to Chiral Symmetry Restoration (CSR) and then a drop due to the appearance of a deconfined partonic medium. → A "horn"-structure emerges.



W. Cassing, A. P., P. Moreau, E.L. Bratkovskaya, Phys. Rev. C93 (2016) 014902.

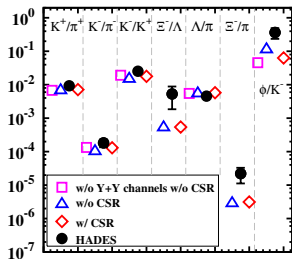
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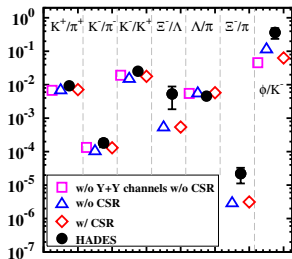
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Still open question about the  $\phi$ -yield.

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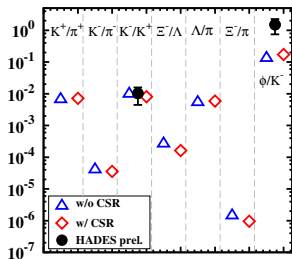


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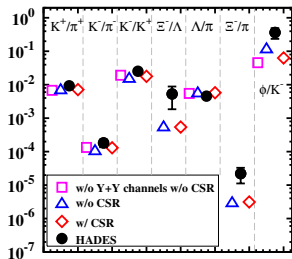
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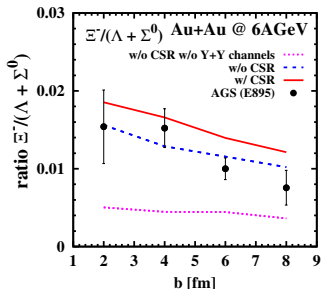
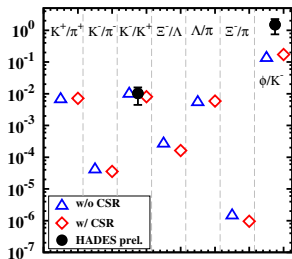


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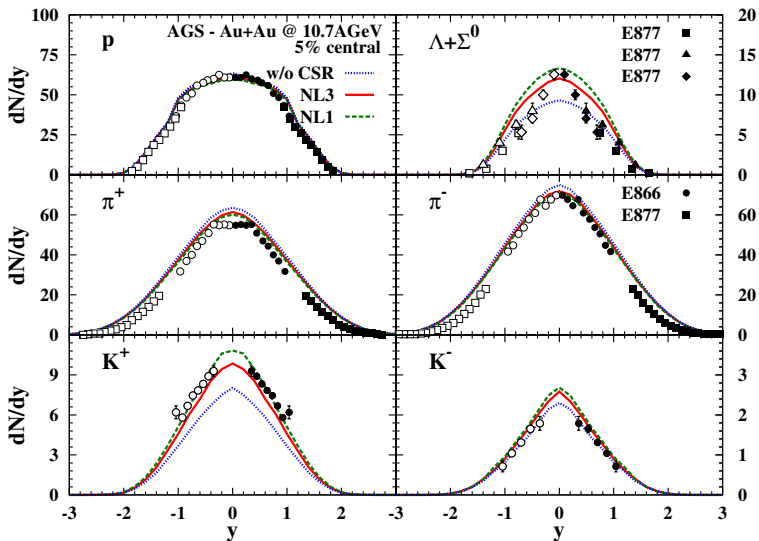
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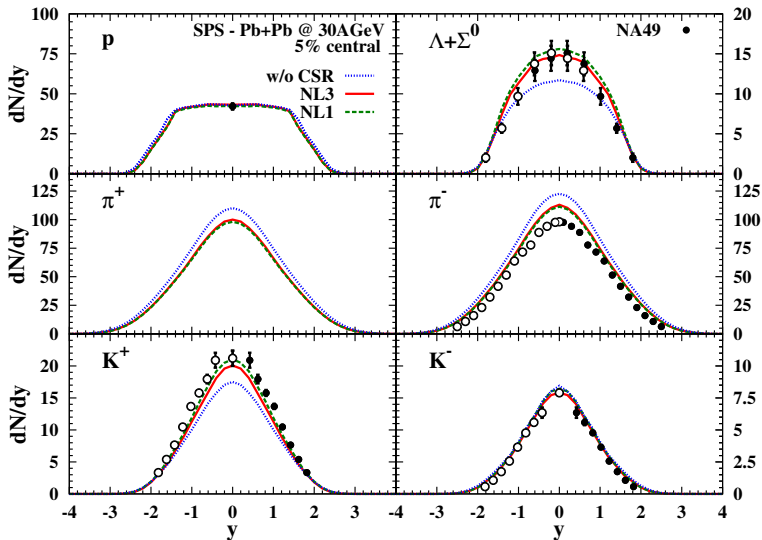
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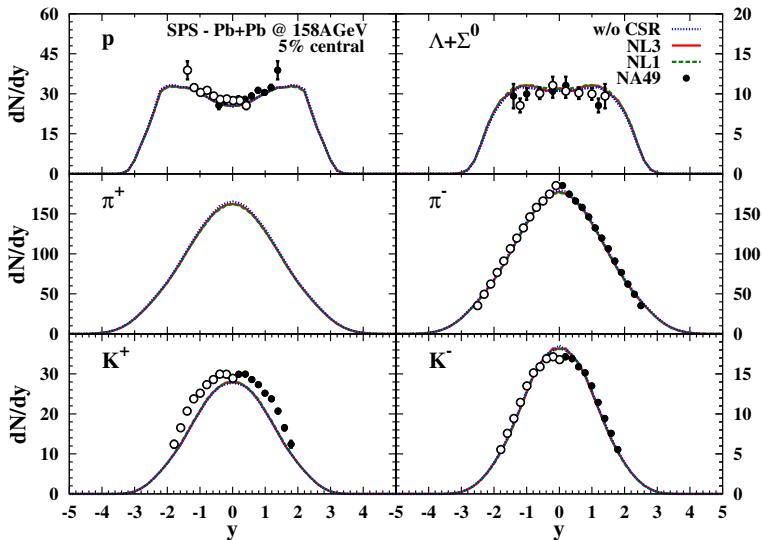
Au+Au @ 10.7 AGeV in comparison to data at AGS



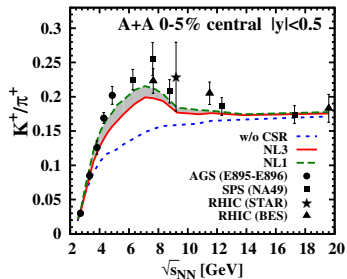
## Pb+Pb @ 30A GeV in comparison to data at SPS

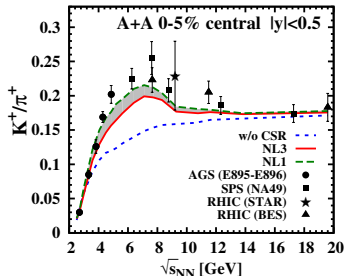


Pb+Pb @ 158A GeV in comparison to data at SPS

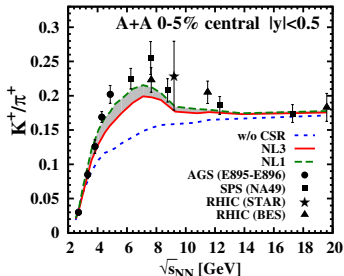




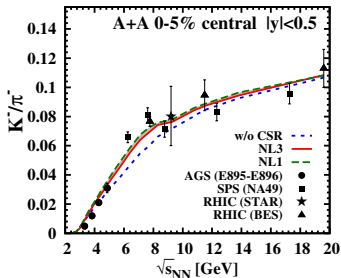


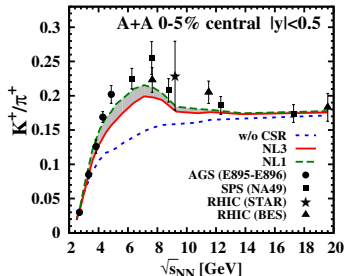


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- NL1 parameter set for the EoS shows a sharper peak in the  $K^+/\pi^+$  ratio in good agreement with the data.

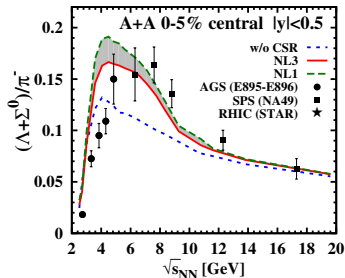
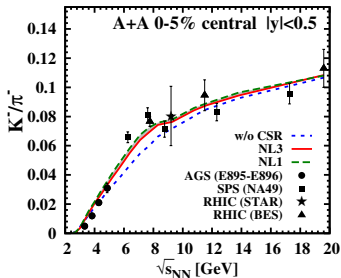


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# Conclusions

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  - First microscopic explanation of the "Horn": a rise in the ratio  $K^+/\pi^+$  associated to the chiral symmetry restoration and then a drop due to the appearance of the deconfined partonic medium.
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Thank you for your attention!

# BACK-UP SLIDES

# Chiral Symmetry restoration: Basic Principles

- The QCD Lagrangian for massless quarks is chirally symmetric, namely invariant under a transformation of the symmetry group  $SU(2)_L \times SU(2)_R$ . The associated transformation for the quark field is:

$$\varphi \rightarrow \varphi' = e^{-i\frac{\tau_a}{2}\Theta_a P_L} e^{-i\frac{\tau_b}{2}\Theta_b P_R} \varphi, \quad \text{with } P_{L,R} = \frac{1}{2}(1 \mp \gamma_5).$$

- This transformation can be rewritten in terms of transformation  $\Lambda_V \times \Lambda_A$  of the group  $SU(2)_V \times SU(2)_A$ :

$$e^{-i\frac{\tau_a}{2}\Theta_a P_L} e^{-i\frac{\tau_b}{2}\Theta_b P_R} \varphi \rightarrow e^{-i\frac{\vec{\tau}}{2}\vec{\Theta}_V} e^{-i\gamma_5 \frac{\vec{\tau}}{2}\vec{\Theta}_A} \varphi.$$

If the Chiral Symmetry holds, the vector and axial currents are equal.

- In case of massive quarks, the Chiral Symmetry is explicitly broken:

$$\Lambda_A : m(\bar{\varphi}\varphi) \rightarrow m(\bar{\varphi}\varphi) - 2im\vec{\Theta} \cdot \left(\bar{\varphi} \frac{\vec{\tau}}{2} \gamma_5 \varphi\right).$$

For energies larger than the particle masses,  $\Lambda_A$  may be treated as approximate symmetry.

- The chiral condensate is adopted as order parameter of the transition between the chiral non-symmetric and the chiral symmetric phase:

$$\langle \bar{\varphi}\varphi \rangle = -\frac{T}{V} \frac{\partial}{\partial m_q} \log Z = \begin{cases} \neq 0 & \text{for } T < T_{ch} \text{ (chiral non-symmetric phase)} \\ = 0 & \text{for } T \geq T_{ch} \text{ (chiral symmetric phase).} \end{cases}$$

# Chiral Symmetry restoration in PHSD

- In presence of hot and dense medium, the hadrons undergo modifications of their properties, e.g. the mass!

$$m_N^*(x) = m_N^V - g_s \sigma(x),$$

where the scalar field  $\sigma(x)$  mediates the scalar interaction with the surrounding medium through the coupling  $g_s$ .

- The value of  $\sigma(x)$  is determined locally by the non-linear gap equation:

$$m_\sigma^2 \sigma(x) + B\sigma^2(x) + C\sigma^3(x) = g_s \rho_S = g_s d \int \frac{d^3 p}{(2\pi)^3} \frac{m_N^*(x)}{\sqrt{p^2 + m_N^{*2}}} f_N(x, \mathbf{p})$$

- Within the non-linear  $\sigma - \pi$  model for nuclear matter, the parameters  $g_s, m_\sigma, B, C$  can be fixed in order to reproduce the values of the main nuclear matter quantities at saturation, i.e. saturation density, binding energy per nucleon, compression modulus and the effective nucleon mass.  
(Actually there are different sets for the values of the parameters, due to the large experimental uncertainties on their values.)

# Chiral Symmetry restoration in PHSD

An estimate for the quark scalar condensate is given by Friman et al., Eur. Phys. J. A **3**, 165, 1998:

$$\frac{\langle \bar{q}q \rangle}{\langle \bar{q}q \rangle_V} = 1 - \frac{\Sigma_\pi}{f_\pi^2 m_\pi^2} \rho_S - \sum_h \frac{\sigma_h \rho_S^h}{f_\pi^2 m_\pi^2},$$

with  $\Sigma_\pi \approx 45 \text{ MeV}$  (reduced in case of hyperons according to the light quark content),  $\sigma_h$  as the  $\sigma$ -commutator of the meson  $h$  ( $= m_\pi/2$  for mesons made of light quarks,  $= m_\pi/4$  for mesons composed of (anti-)strange quarks).

- The vacuum scalar condensate  $\langle q\bar{q} \rangle_V$  is fixed by the Gell-Mann-Oakes-Renner relation:

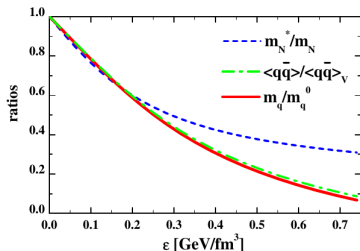
$$f_\pi^2 m_\pi^2 = -\frac{1}{2}(m_u^0 + m_d^0) \langle \bar{q}q \rangle_V \quad \rightarrow \quad \langle \bar{q}q \rangle_V \approx -3.2 \text{ fm}^{-3}$$

for the bare quark masses  $m_u^0 = m_d^0 \approx 7 \text{ MeV}$ .

- The nucleon scalar density  $\rho_S$  is obtained after solving the gap equation for the field  $\sigma(x)$ .

# Chiral Symmetry restoration in PHSD

In Schwinger-like formula effective masses have to be considered:

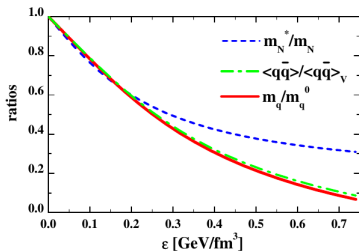


$$m_{q,s}^* = m_{q,s}^0 + (m_{q,s}^V - m_{q,s}^0) \left| \frac{\langle \bar{q}q \rangle}{\langle \bar{q}q \rangle_V} \right|,$$

using  $m_s^0 \approx 100 \text{ MeV}$  and  $m_q^0 \approx 7 \text{ MeV}$  for the bare quark masses.

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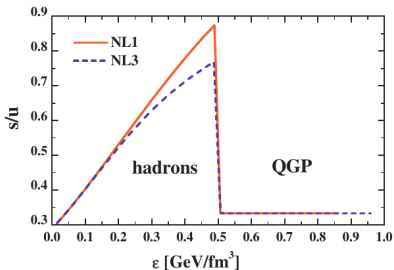
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As long as the string tension remains approximately constant, the ratio  $s/u$  increases with decreasing  $\langle q\bar{q} \rangle$ .



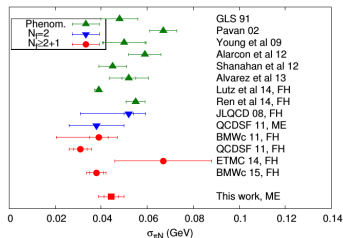
Within the deconfined phase the ratio  $s/u$  is fixed to  $\sim 1/3$  by comparison to the strangeness production at RHIC and LHC energies observed experimentally.



# Chiral Symmetry restoration: EOS

Dependence on the Hadronic EOS.

$$\Sigma_{\pi N} = 45 \text{ MeV}$$



Yi-Bo Yang et al., arXiv 1511.09089



Modifications on the value of  $\Sigma_{\pi N}$  have no effect on the ratio  $K^+/\pi^+$ .

NL1 vs NL3

	NL1	NL3
$g_s$	6.91	9.50
$g_v$	7.54	10.95
$B$ (1/fm)	-40.6	1.589
$C$	384.4	34.23
$m_s$ (1/fm)	2.79	2.79
$m_v$ (1/fm)	3.97	3.97
$K$ (MeV)	380	380
$m^*/m$	0.83	0.70

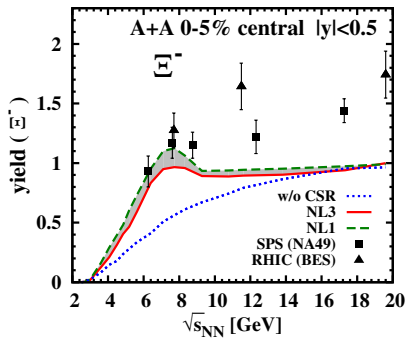
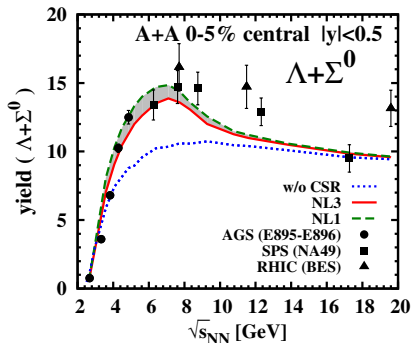
A. Lang et al., Z. Phys. A 340, 287 (1991).



There is some sensitivity related to the hadronic EoS in our results.

# Chiral Symmetry restoration: Results

Excitation function of the hyperons  $\Lambda$  and  $\Xi^-$ .



# Many body theory

## Kadanoff Baym Gleichungen (exact)

$$[\mathbb{B}\partial_t - h(t)] G(t, t') = \delta(t - t') + \int_c d\bar{t} \Sigma[G](t, \bar{t}) G(\bar{t}, t')$$

$$[-\mathbb{B}\partial_{t'} - h(t')] G(t, t') = \delta(t - t') + \int_c d\bar{t} G(t, \bar{t}) \Sigma[G](\bar{t}, t')$$



## Limiting to two-particle correlations

$$\left\{ i\hbar \frac{\partial}{\partial \tau} - [F(\mathbf{p}) + \Delta(\mathbf{p}) + i\Gamma(\mathbf{p})] \right\} g^<(\mathbf{p}, t, \tau) = I(\mathbf{p}, t)$$

W. Cassing , S. Juchem, NPA 665 (2000) 377;  
672 (2000) 417; 677 (2000) 4451

## Off-shell (generalized) transport theory

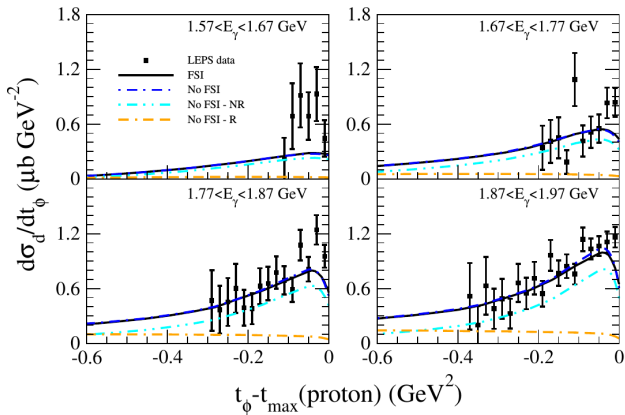
Only one-particle distributions=diagonal Green's Functions,  
no correlations, weakly interacting or dilute systems

$$\frac{\partial}{\partial t} f(\mathbf{p}, t) = I(\mathbf{p}, t)$$

Boltzmann (BUU oder Vlasov-Boltzmann)



# Phi production



A. Kiswandhi et al., arXiv:1604.01555, 2016.