



Mesons: Searching for new properties and rare species

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New Precision Experiments with COMPASS at CERN

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Brief Overview



- Polarizabilities
 - Analogies with atoms
 - Pion polarisability
- Radiative excitations
- Spectroscopy in strong interaction
 - Introduction
 - Identification method (PWA)
 - Result summary and a new meson
- New insights into production/decay dynamics
- Conclusions

- Hadron: colour neutral system of quarks

- Baryon (qqq)
- Meson (q \bar{q})



- At small energy scales

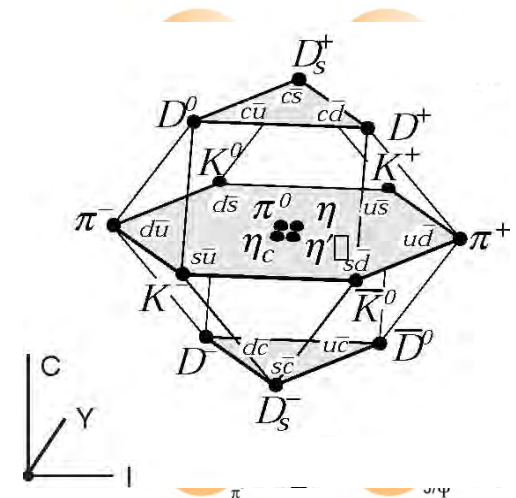
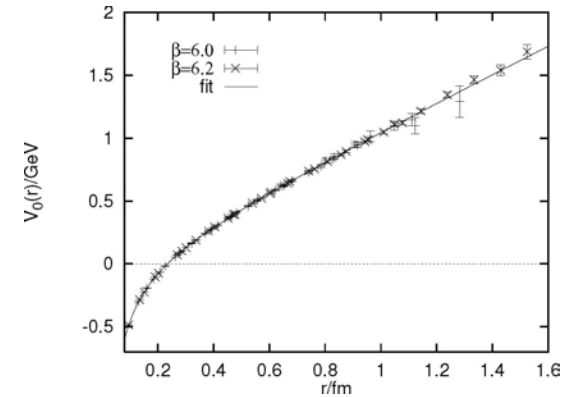
- QCD not analytically solvable
- Effective degrees of freedom: constituent quarks
Coupling quarks with gluon field (99% of p-mass)
 $m_u = m_d = 310 \text{ MeV}/c^2$; $m_s = 485 \text{ MeV}/c^2$
Use effective potential

- Use symmetries flavour, spin, colour
build ‚Periodic table‘ of hadrons
- Classify into multiplets

Hadron masses are sum of quark masses

- Use hyperfine-interaction (spin-spin interaction) mass spectrum surprisingly well described

- effective $q\bar{q}$ potential



Spin-Parity selection rules for bound $q\bar{q}'$ system

- Quark spins couple to total **intrinsic spin S**
 $S = 0$ (singlet) or $S=1$ (triplet)
- Relative **orbital angular momentum L** couples with total **spin S** to J

Meson spin: $\vec{J} = \vec{L} + \vec{S}$

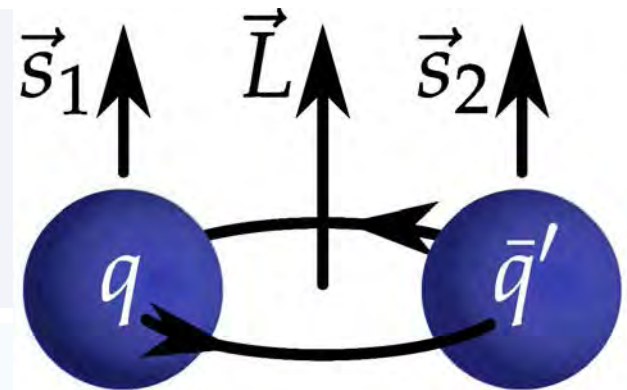
- Isospin: $I = 1$ for u,d quarks, $I=0$ for other quarks

$$I_z(\text{u}) = 1/2$$

$$I_z(\text{d}) = -1/2$$

light Mesons: $I = 0$ or 1

other Mesons: $I = 0$ or $1/2$



- Parity:

$$P = (-1)^{L+1}$$

- Charge conjugation:

$$C = (-1)^{L+S}$$

- G-parity:

$$G = C \cdot e^{i\pi I_z} = (-1)^{I+L+S}$$

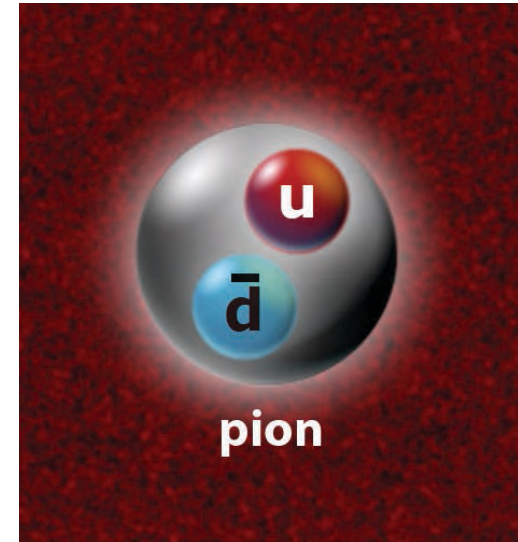


Constituent Quark Model II Mesonen



- **Allowed** J^{PC} combinations:
 - $L = 0 \rightarrow$ pseudo-scalar 0^{-+} , Vector 1^{--}
 - $L = 1 \rightarrow$ scalar 0^{++} , axial-vector 1^{+-} , 1^{++} and tensor 2^{++}
- **Forbidden** J^{PC} combinations: 0^{-} , 0^{+-} , 1^{-+} , 2^{+-} , 3^{+-}
- Same quantum numbers mix

- Pion is **lightest composite** system
- Properties:
 - $M_{\pi^+} = 139.57 \text{ MeV}/c^2$
 - $M_{\pi^0} = 134.97 \text{ MeV}/c^2$
 - Spin $S = 0$
 - *Lifetime* $\tau = 2.603 \cdot 10^{-8} \text{ s}$
 - *Flightpath* $\Delta x = 10.6 \text{ km (at } p = 190 \text{ GeV}/c)$
 - $\sqrt{\langle r^2 \rangle} = 0.672 \pm 0.008 \text{ fm} = (0.672 \pm 0.008) \cdot 10^{-15} \text{ m}$



Question: what is it's **macroscopic structure** ?

Refractive index n

- Macroscopically: dielectric constant $\tilde{\epsilon} = \epsilon_1 + i\epsilon_2 = n + iK$

- Microscopically:

– Light wave polarizes atoms \rightarrow induced dipole moment: $\vec{P} = \alpha \cdot \vec{E}$

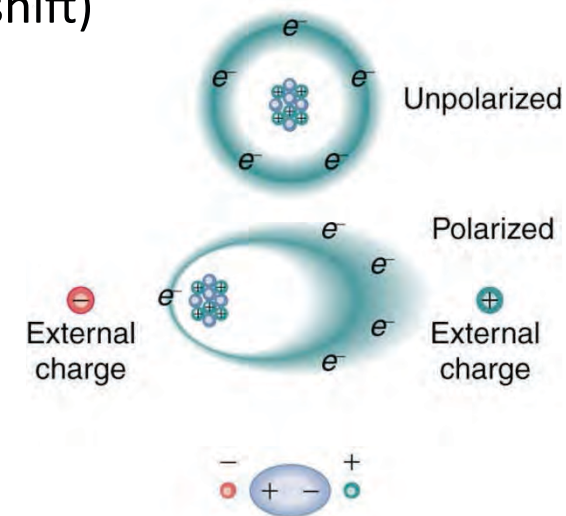
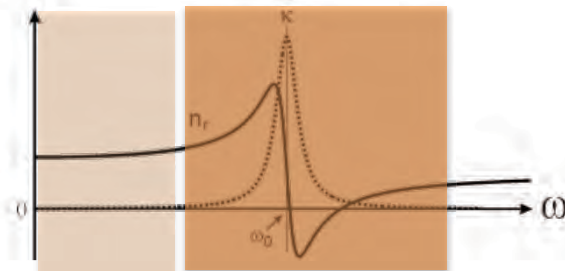
α : electric polarisability

– Relaxation \rightarrow dipole radiation (delayed – phase shift)

superimposing incoming field $\rightarrow c_{matter} = \frac{c_{Vac}}{n}$

$$\alpha(\omega) = \frac{n(\omega) - 1}{2\pi} \text{\AA}^3 \approx \frac{9}{2} a_{Bohr}^3 \quad \alpha_{He} = 9.3 \text{\AA}^3$$

– Strength is frequency dependent (dispersion)



- „stable“ object with smallest „Bohr“ radius
- Polarizability

- strong interaction $\Delta E(\pi \rightarrow \rho) \approx 600 \text{ MeV}$
- electromagnetic $\Delta E(H_{1S} \rightarrow H_{2S}) \approx 10 \text{ eV}$

Indicator for
stiffness of system

- Difference in stiffness: $\frac{\alpha_{em}}{\alpha_{strong}} = \frac{1/137}{0.7} \approx 0.01$

$$\frac{\alpha_{\pi}}{\langle r_{\pi}^{em} \rangle^3} (\pi) \approx \frac{1}{100} \frac{\alpha_{atom}}{a_{Bohr}^3} (atom) \cdot (q_{eff}^{\pi})^2 \ll \frac{\alpha_{atom}}{a_{Bohr}^3} (atom) \quad \langle r_{\pi}^{em} \rangle^2 \approx 0.45 \pm 0.01 \text{ fm}^2$$

- Theory: $\chi_{PT} : \alpha_{\pi} = 2.85 \pm 0.5 \cdot 10^{-4} \text{ fm}^3$
Others : $\alpha_{\pi} = 4 - 10 \cdot 10^{-4} \text{ fm}^3$



How to measure α ?



- Atomic physics: deflection of an atom in a laser field

$$\vec{F} = \alpha \cdot \vec{E} \cdot \nabla E$$

- Need strong fields and strong gradients (laser cavity)

$$E = 10^6 \text{ V / cm} \quad \nabla E = 10^{11} \text{ V/cm}^2$$

- Particle physics: scatter high energy π from photon source

- Photon source: high Z nucleus

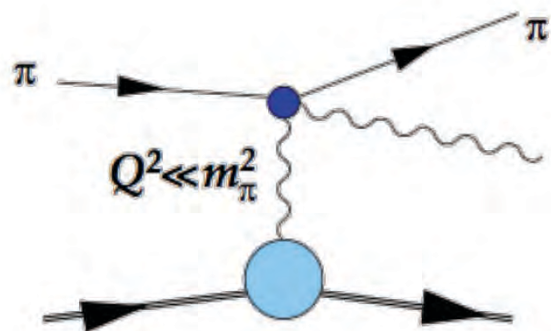
- High gradients: relativistic amplification

$$E = 10^5 \text{ V / fm}$$

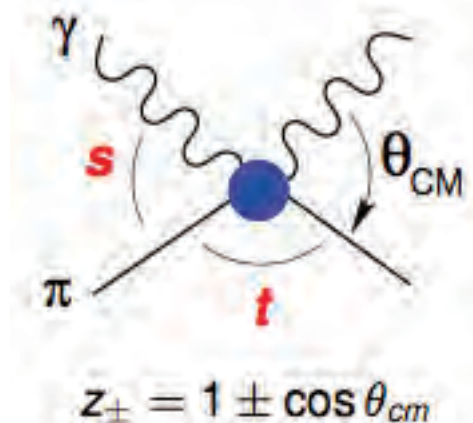
- Charged particle is deflected in field (Born term)



- Use Compton scattering
 - π instable: inverse kinematics
 - μ as point like reference



190 GeV/c beam particles



$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{cm}} = \underbrace{\frac{\alpha^2 (s^2 z_+^2 + m_\pi^4 z_-^2)}{s (sz_+ + m_\pi^2 z_-)^2}}_{\text{Compton}} = \underbrace{\frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2 (sz_+ + m_\pi^2 z_-)}}_{\text{Extended object}} \cdot \mathcal{P}$$

Compton

Extended object

$$\mathcal{P} = z_-^2 (\alpha_\pi - \beta_\pi) + \dots$$

elasticity:

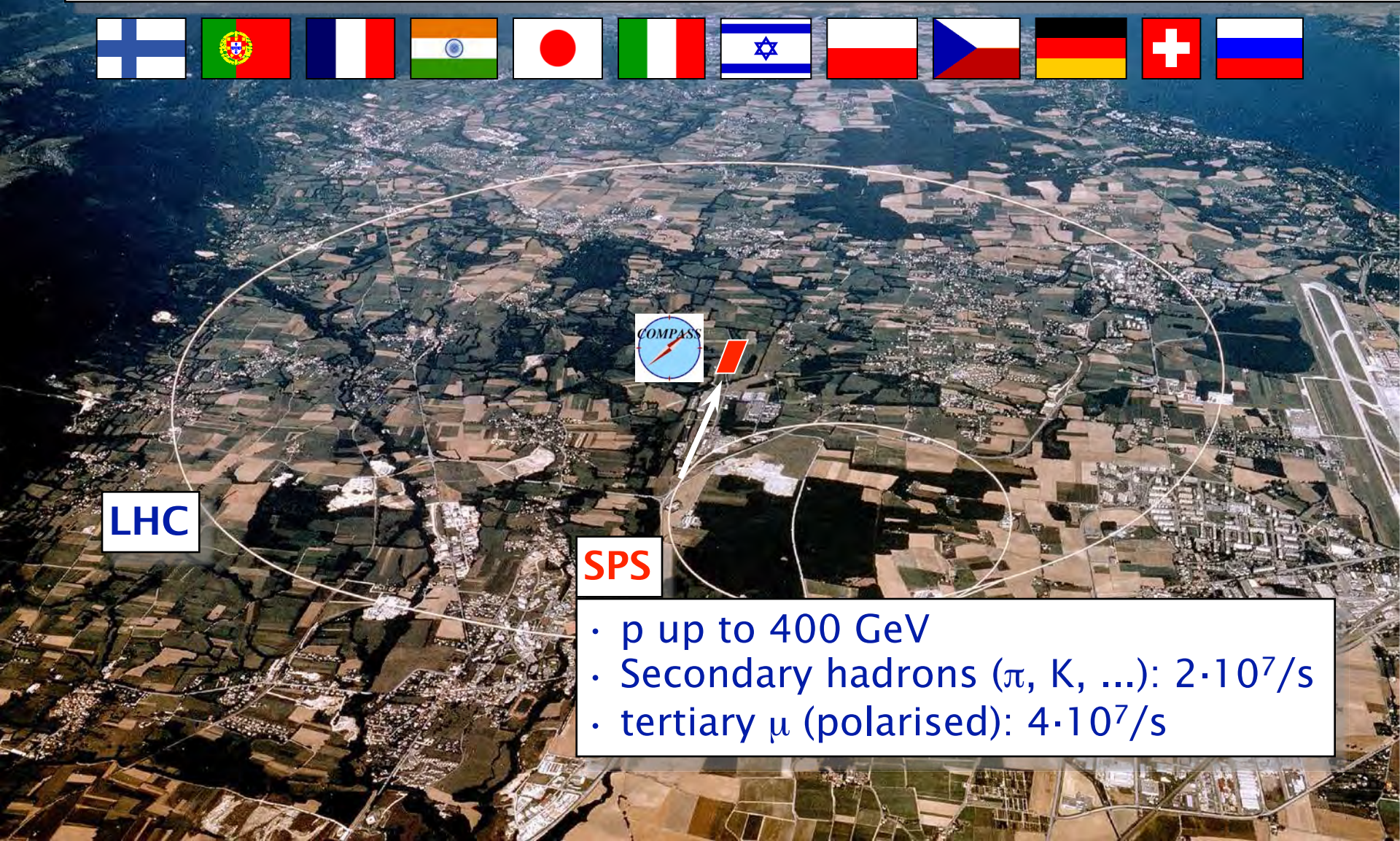
$$s = p_\gamma^2 + p_\pi^2 < (2m_\pi)^2$$



COMPASS am CERN



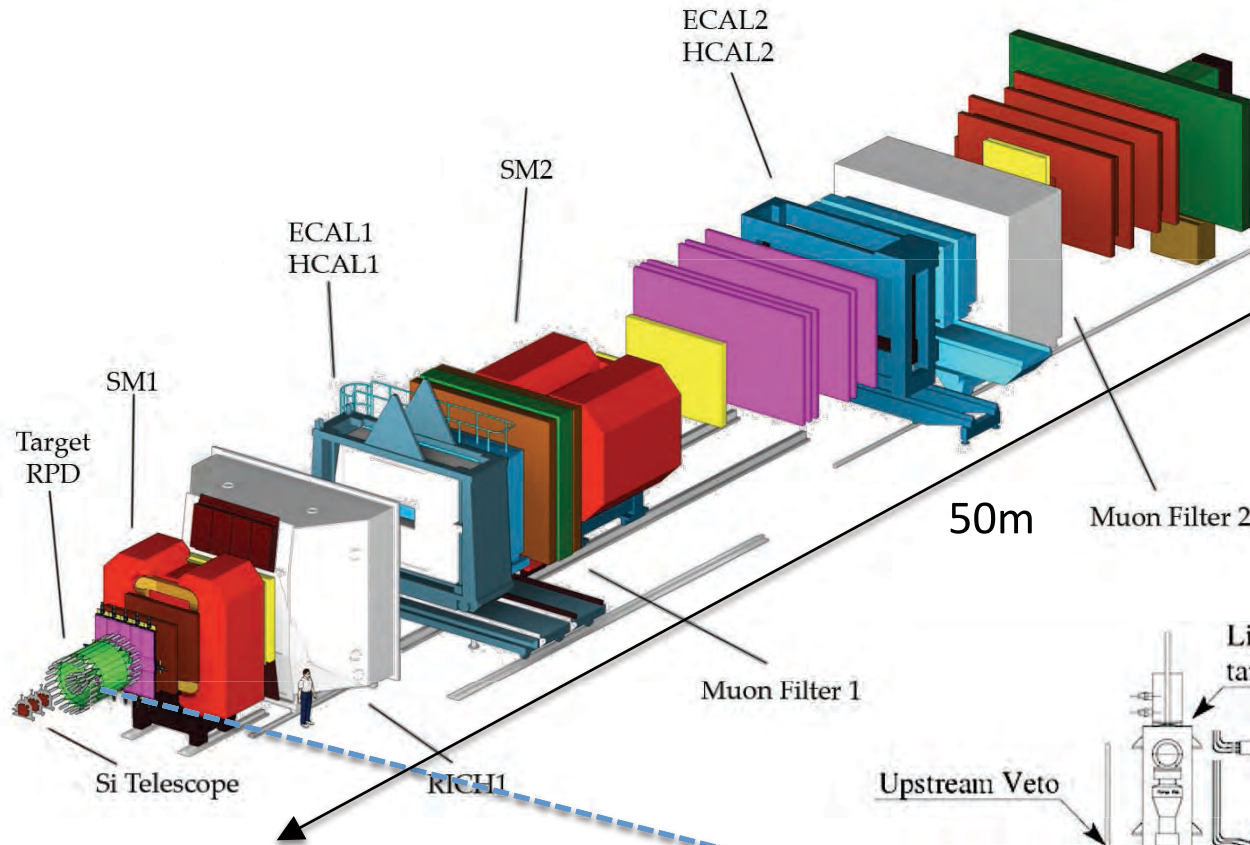
COmmon Muon and Proton Apparatus for Structure and Spectroscopy



LHC

SPS

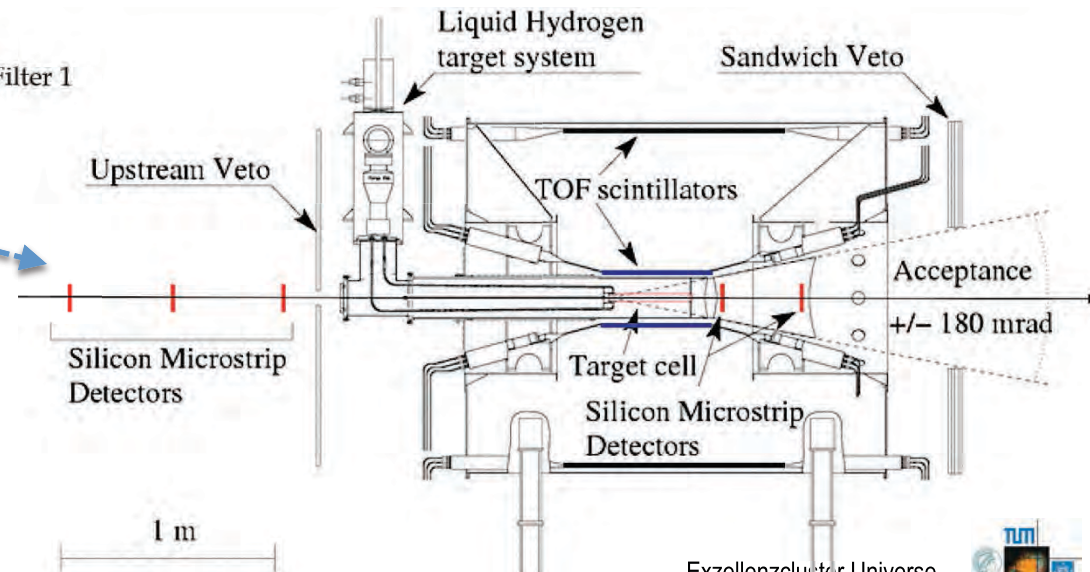
- p up to 400 GeV
- Secondary hadrons (π , K, ...): $2 \cdot 10^7/s$
- tertiary μ (polarised): $4 \cdot 10^7/s$



CERN SPS

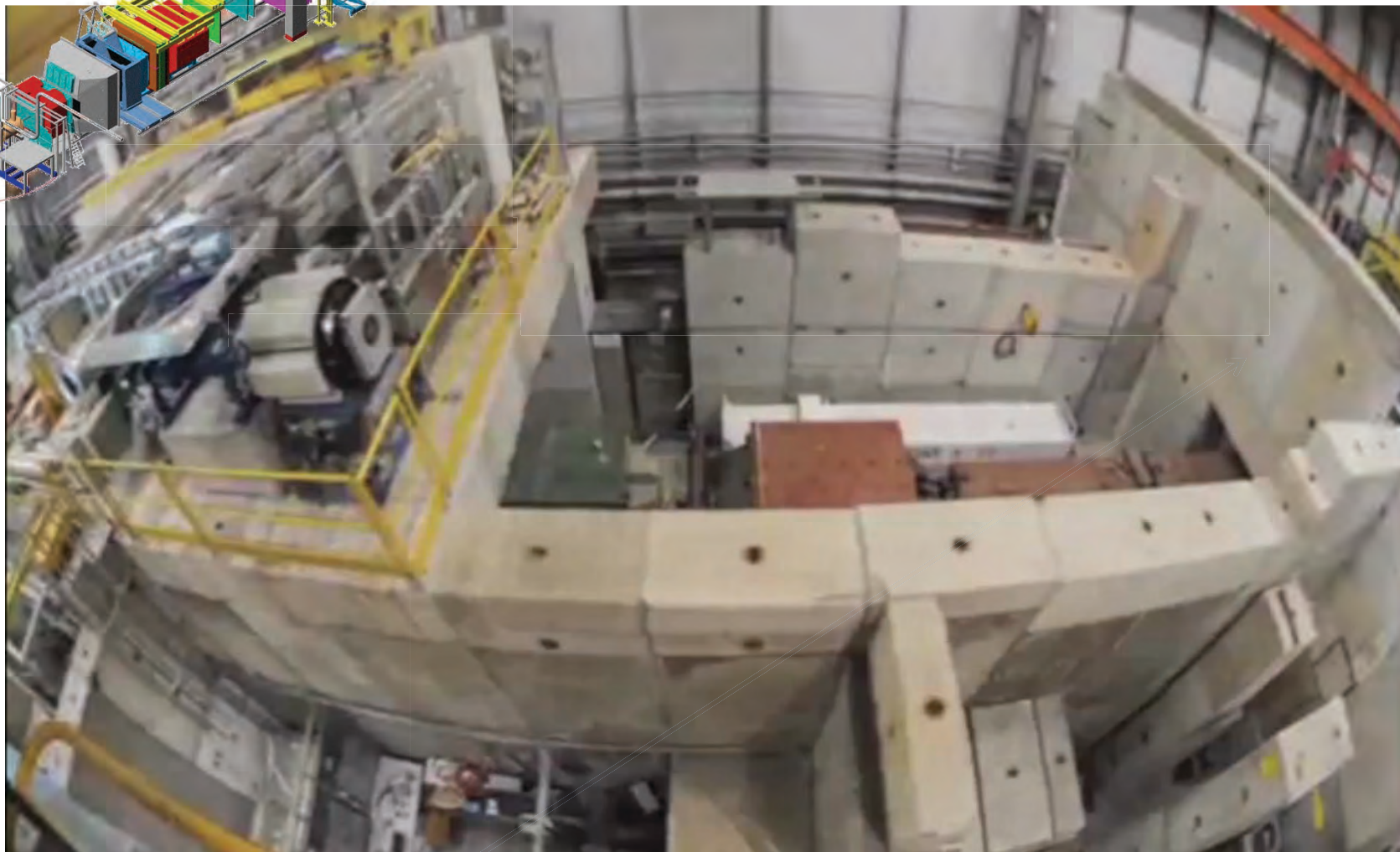
Hadron beam:

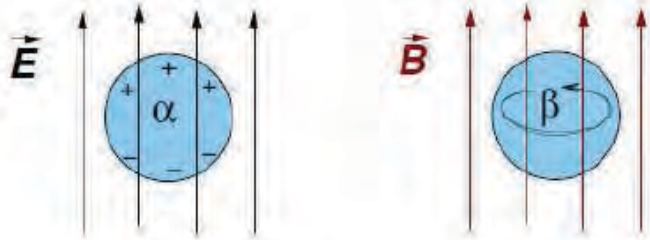
- 190 GeV/c π , K, ρ
- $5 \cdot 10^7$ particles/SPS-spill
- 60 days data taking 2008
- **Trigger:** RPD hit, beam veto





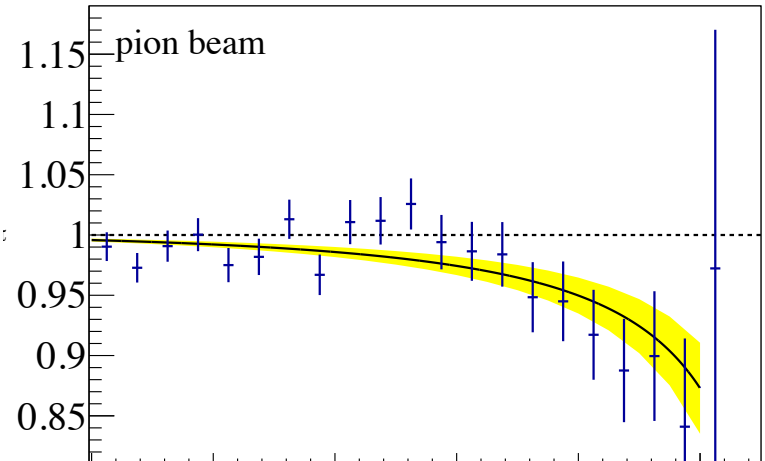
The COMPASS Experiment



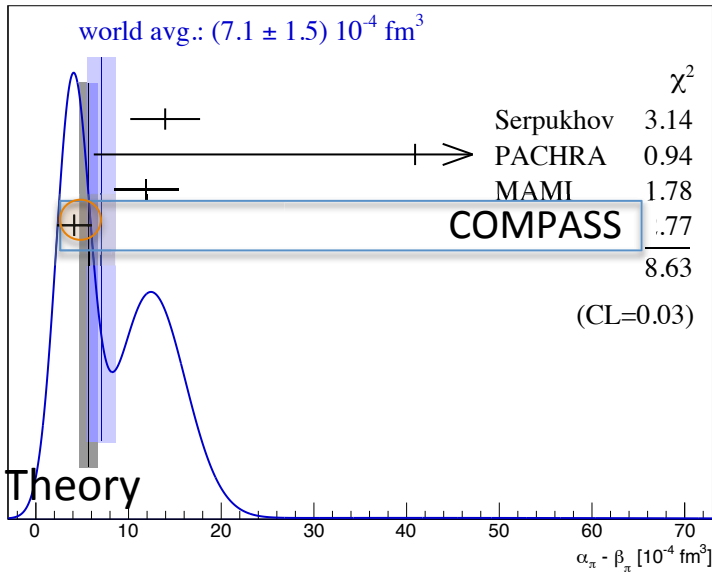
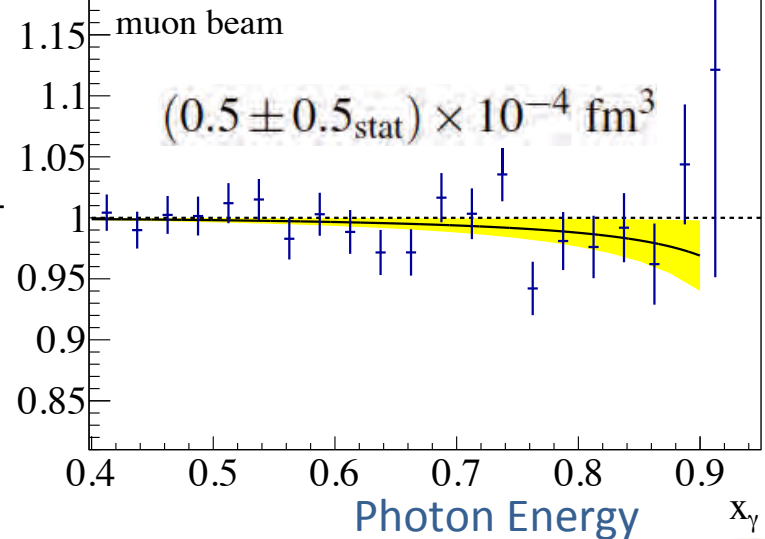


$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3$$

$$R_\pi = \frac{\sigma_{\text{meas}}}{\sigma_{\text{point}}}$$

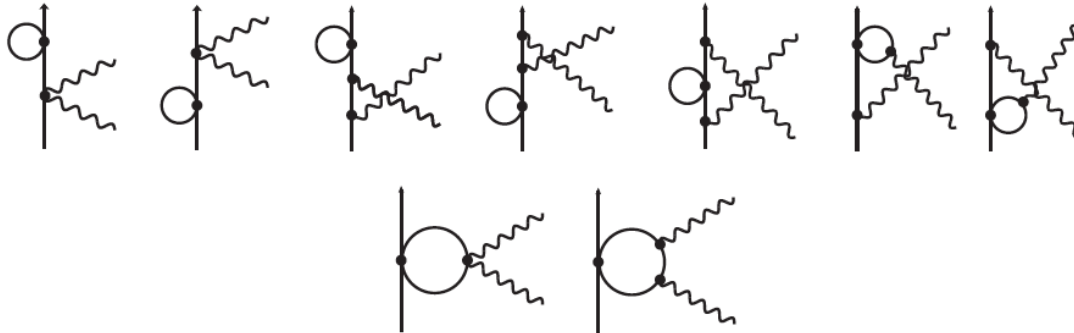


$$R_\mu = \frac{\sigma_{\text{meas}}}{\sigma_{\text{point}}}$$



π polarizability: χ PT confirmed
 Long standing puzzle solved !

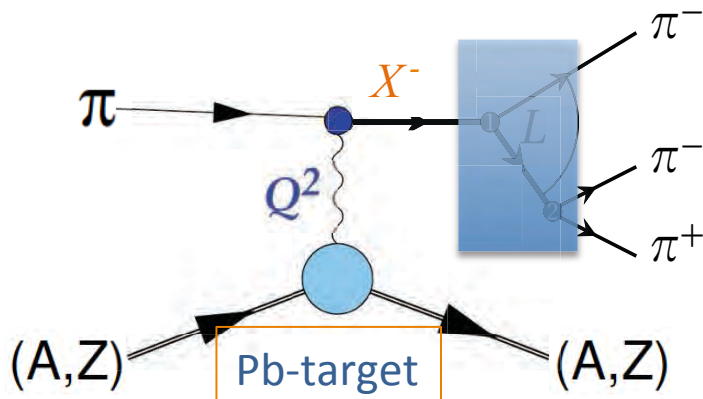
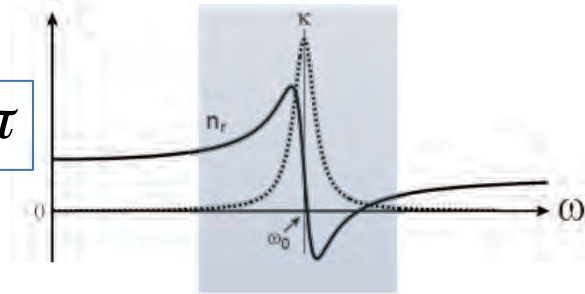
- Pion is GoldstoneBoson of spontaneous chiral symmetry breaking
- Massless excitation of ground state
- Long wavelength description of QCD
 - Polarisability is basic interaction with electromagnetic field



- Photon scattering of pion cloud of pion
- Correct results (2-loop calculation) gives VERY Strong support for SSB scenario

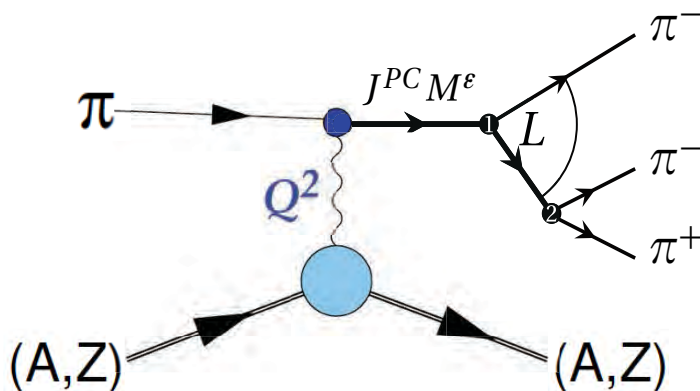
- So far: excitations far below resonance region (elastic scattering)
- Higher energies: photon-scattering **inelastic**
 - Atoms: **electronic excitations**
 - Hadrons: **resonance production**
- Various **multipole excitations** possible
 - Determine **angular distribution** in de-excitation process
- For Primakoff reactions: wide range of photon energies
 - Analysis of final state determines reaction type and excitation energy
 - Coupling $\alpha_{em} \ll \alpha_{strong} \rightarrow$ **resonance** will decay via strong interaction (PWA)

$$\delta\varphi_{out-in} = \pi$$



$$A(\pi\gamma) \ll A(\pi\pi\pi)$$

- Study resonances with **electromagnetic probe**
 - similar to **photo-production** of Δ^+ off **protons**
 - **radiative transitions** of **charmonia**
- Competition by **strong interaction** (with same final state)
 - **Photon:** $S = 1$ and $H = \pm 1$
Helicity conservation \rightarrow Spin alignment of resonance X^-
 - **Diffraction:** need angular momentum for **Spin alignment**
Suppressed in forward production



Identify **photo**-production via spin alignment

$M = 1$ at low $t' < 10^{-3} \text{ GeV}^2/c^2$

$$\sigma_{\text{Photo}} \approx e^{-b_{\text{photo}} t'}$$

$$\sigma_{\text{diffract}} \approx t'^M \cdot e^{-b_{\text{diff}} t'} \quad b_{\text{photo}} \gg b_{\text{diffract}}$$

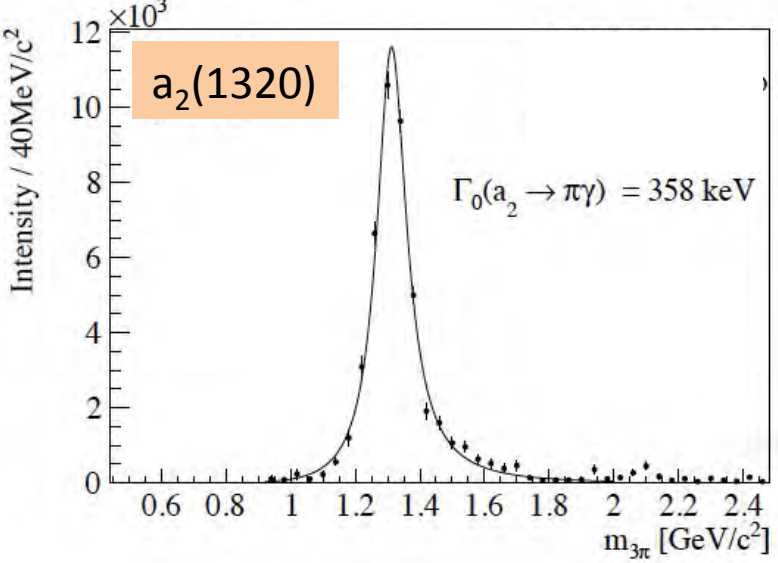
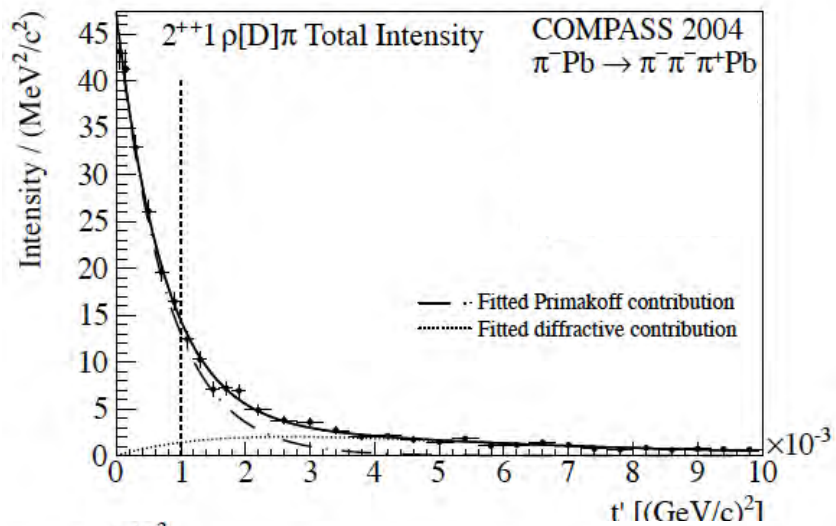
$\rightarrow M = 1$ is suppressed in diffraction



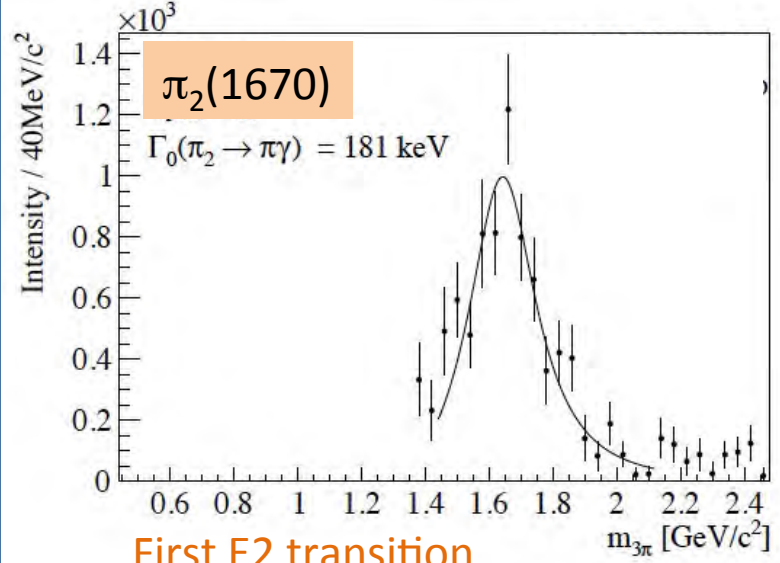
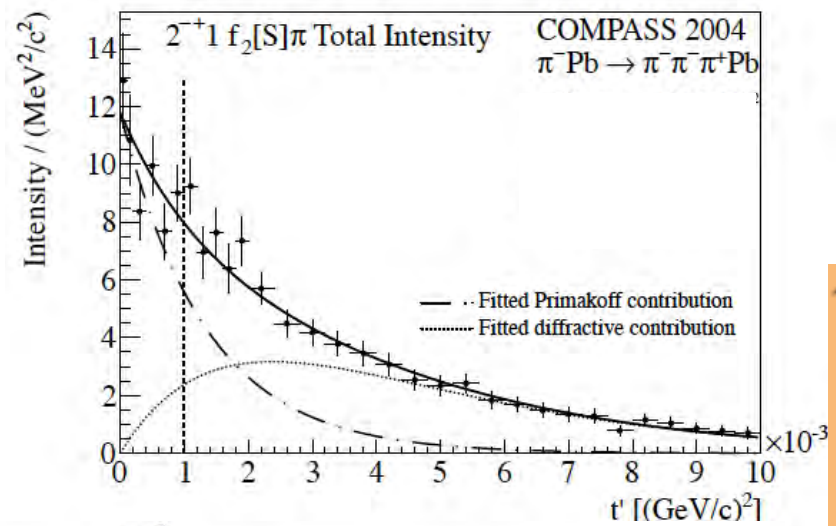
EM-Transitions for Mesons



$\Gamma_0(a_2(1320) \rightarrow \pi\gamma)$



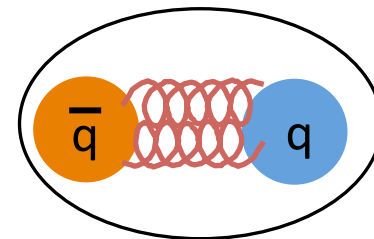
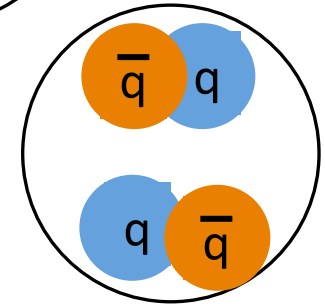
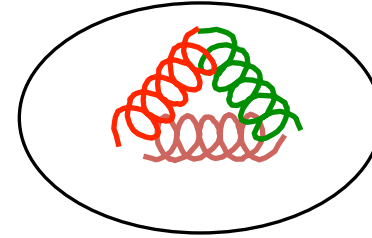
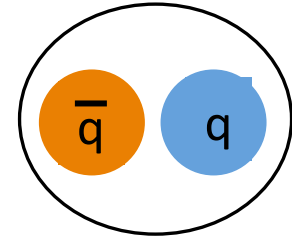
M2 transition



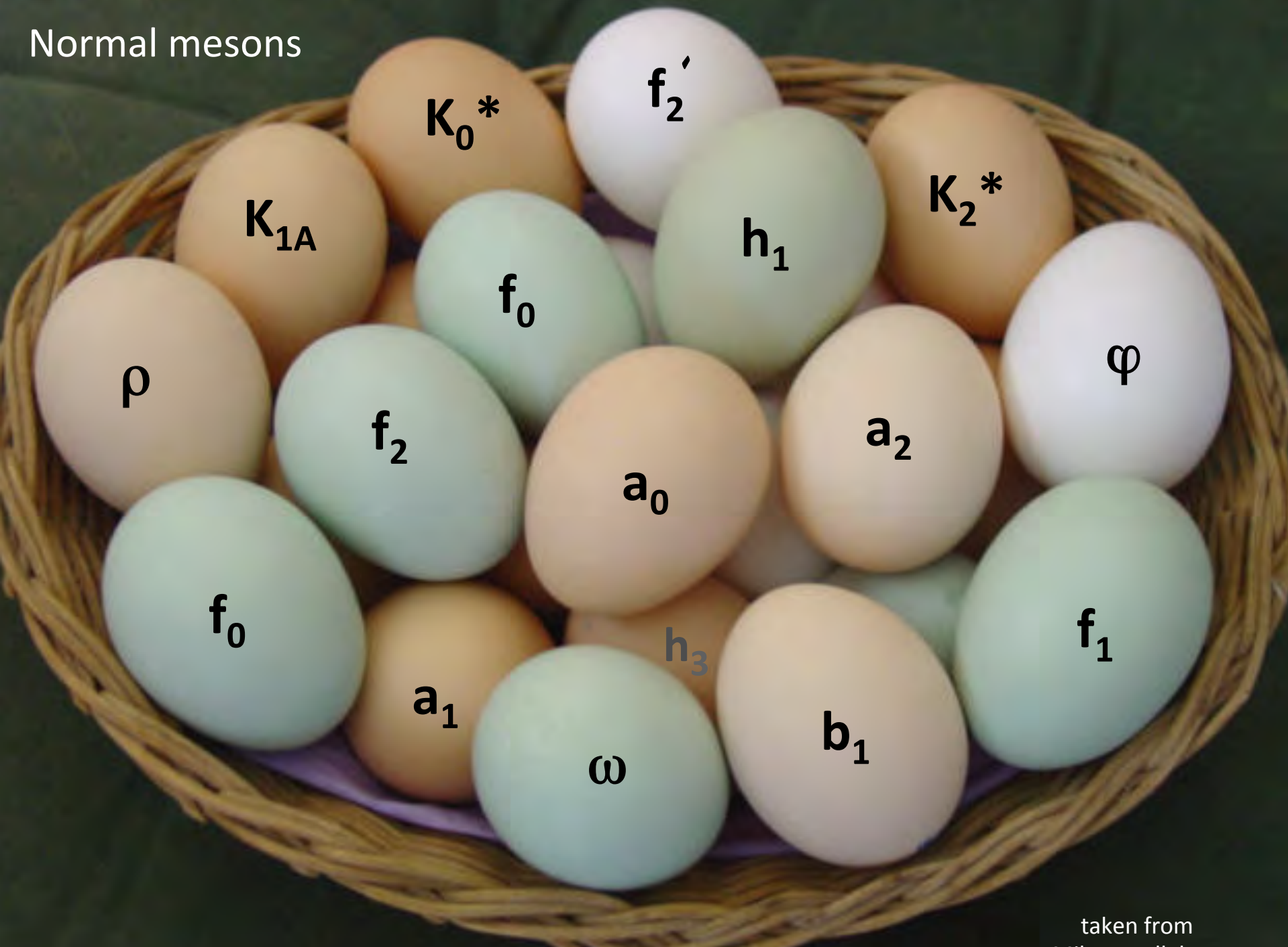
First E2 transition
observed for mesons

$\Gamma(\pi_2 \rightarrow \pi\gamma)$

- **Quark model mesons** (u, d, s quarks)
- **Glueballs** (gluons and **no valence quarks**)
- **Multiquarks** (quark-antiquark pairs)
- **Hybrids** (quarks and gluonic excitation, which contribute to static properties)



Normal mesons



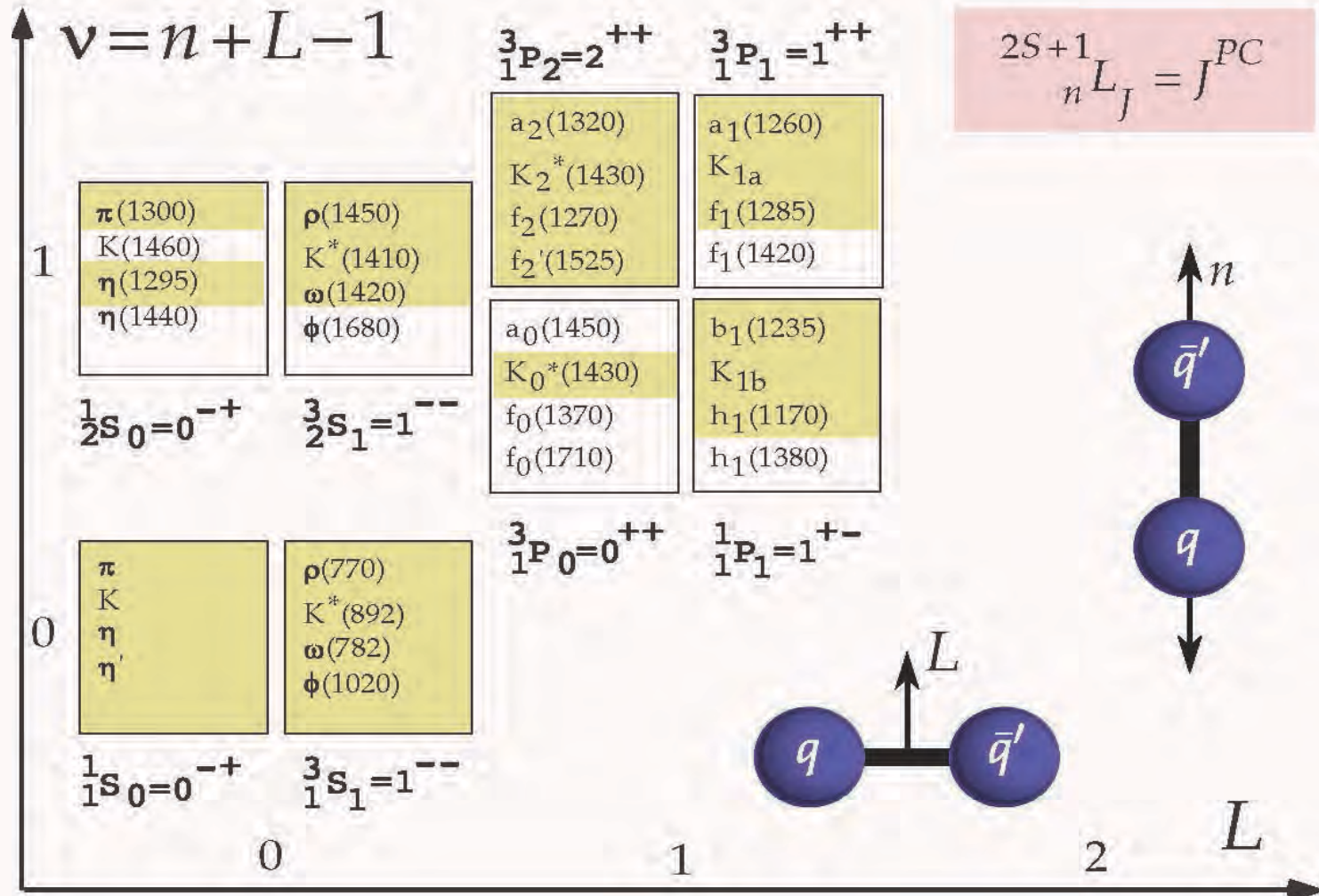
More Surprising States?



taken from
Mike pendle

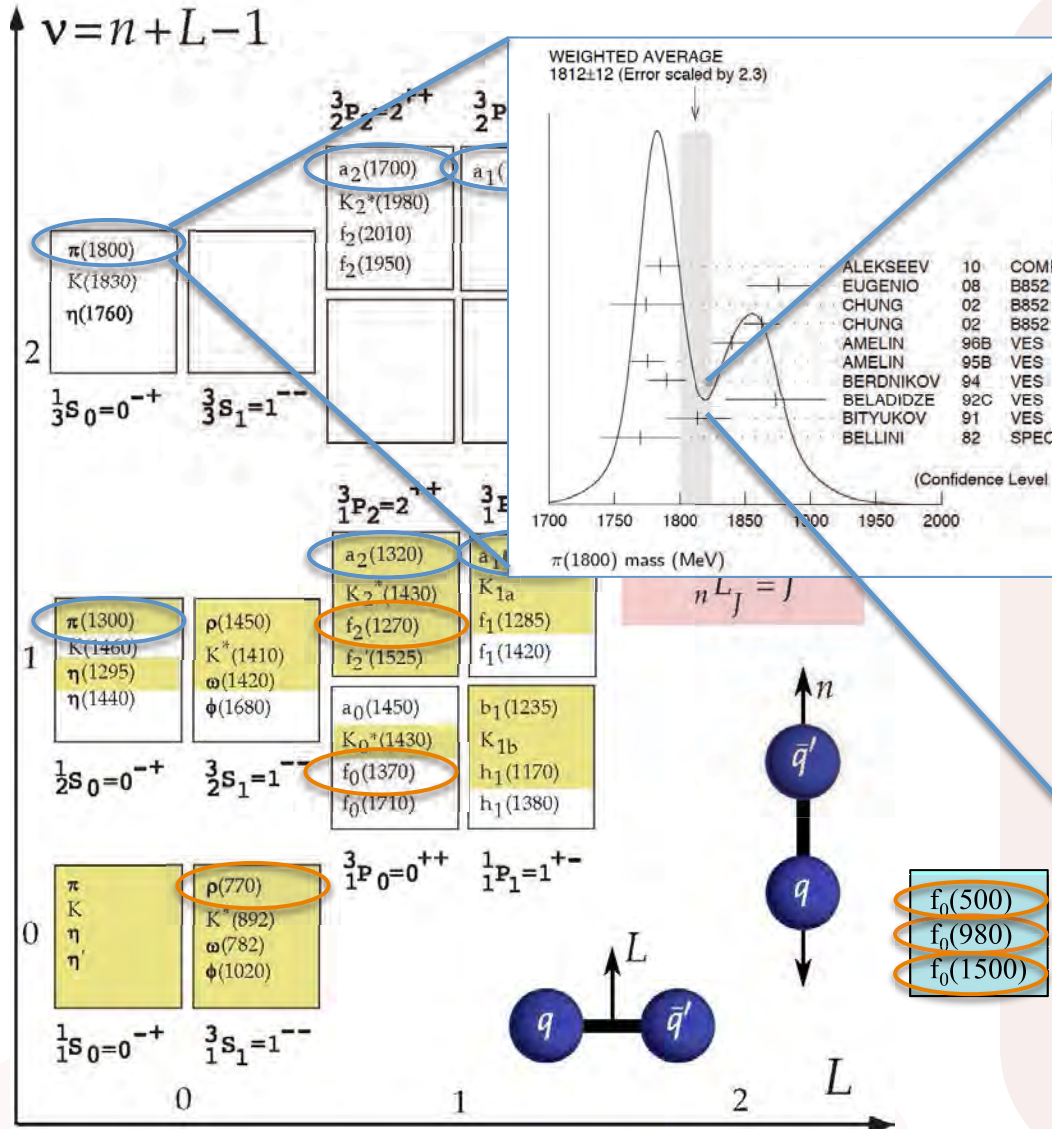
Constituent Quarks and Mesons

Spectrum of light mesons:





Constituent Quarks and Mesons



$\pi_2(1880)$ MASS

VALUE (MeV)	EVTS
1895 ± 16 OUR AVERAGE	
1929 ± 24 ± 18	4k
1876 ± 11 ± 67	145k
2003 ± 88 ± 148	69k
1880 ± 20	

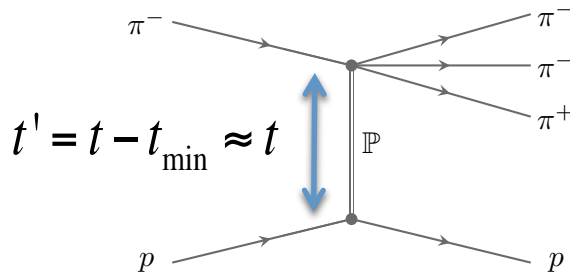
$\pi_2(1880)$ WIDTH

VALUE (MeV)	EVTS
235 ± 34 OUR AVERAGE	
323 ± 87 ± 43	4k
146 ± 17 ± 62	145k
306 ± 132 ± 121	69k
255 ± 45	

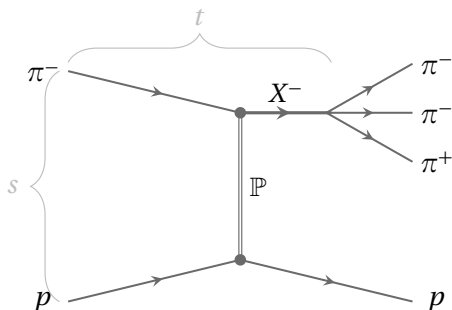
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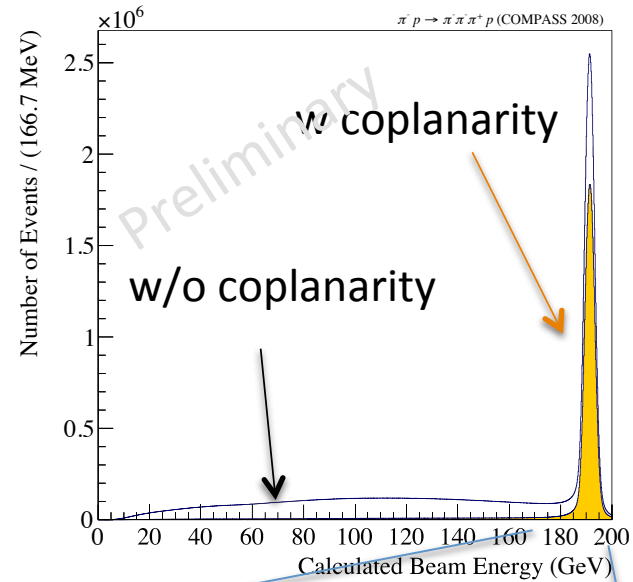
generic process



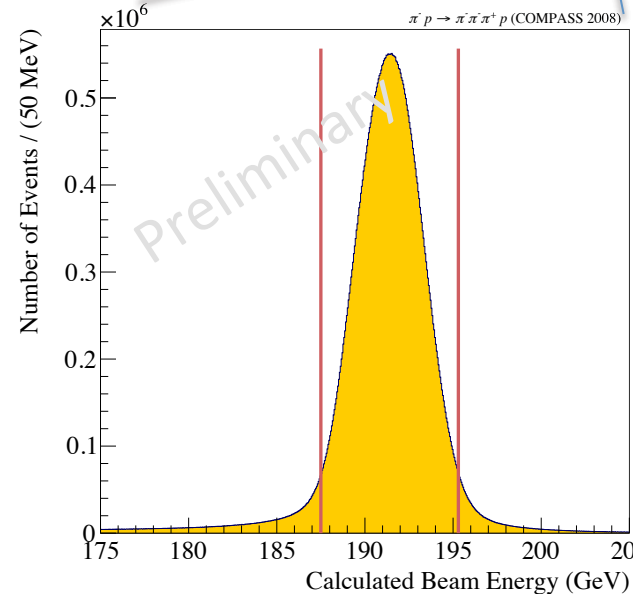
what we are after

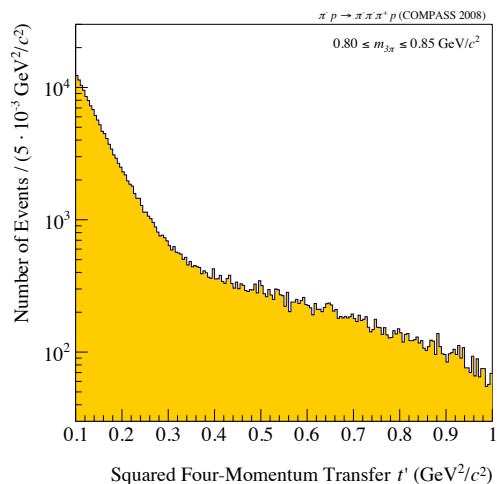
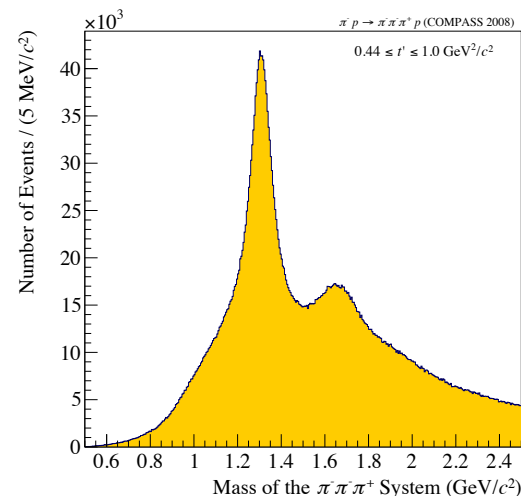
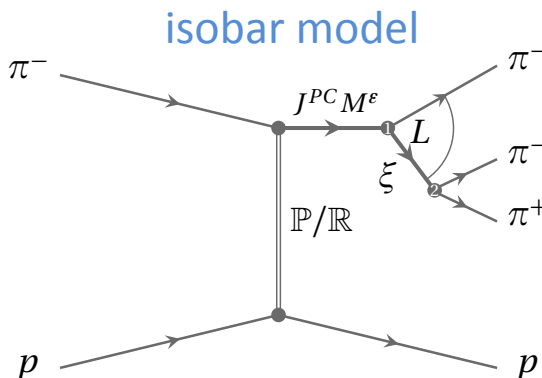
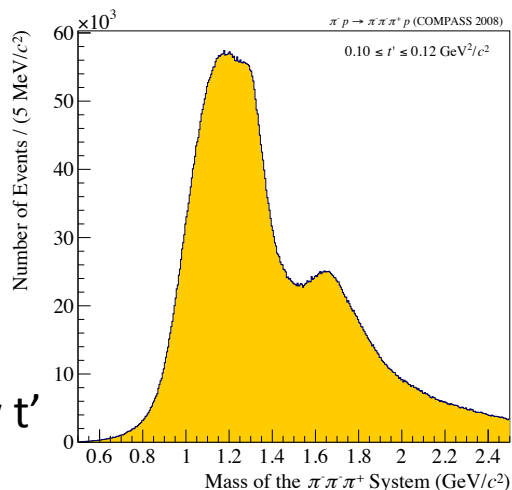


exclusive reaction

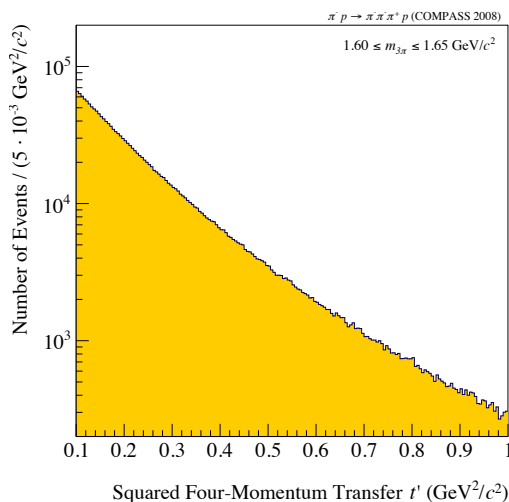


zoom

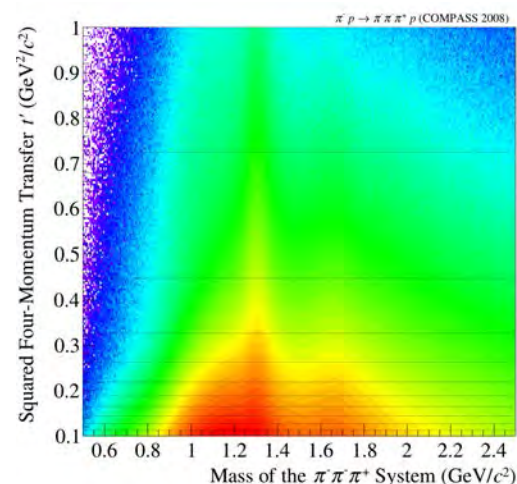




$0.8 < m_{3\pi} < 0.85$



$1.6 < m_{3\pi} < 1.65$

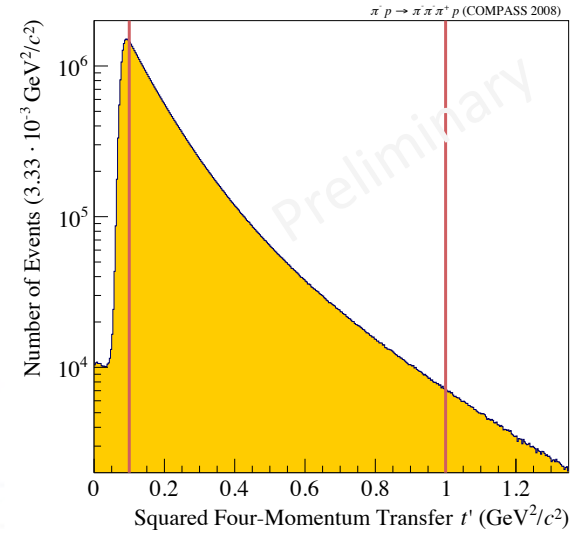
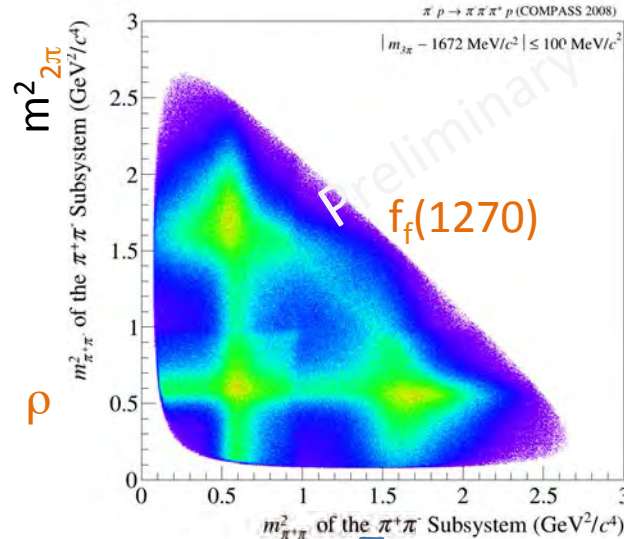
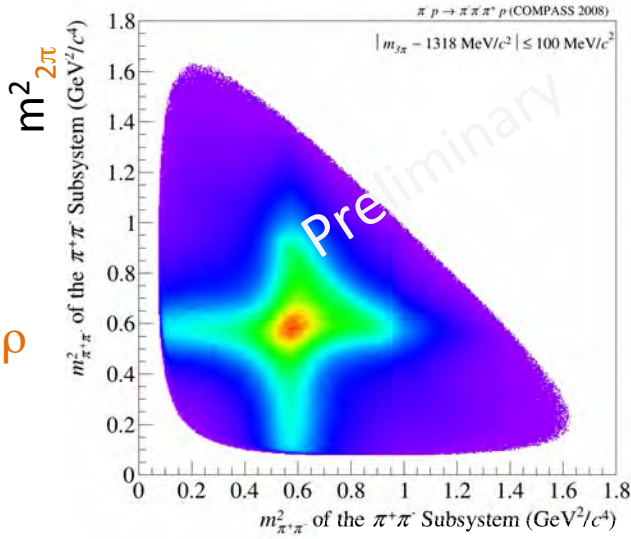


grid of t' used

$\Delta m: 20 \text{ MeV}/c^2$
 Exzellenzcluster Universe

First Impressions

Motivation for Isobar Model

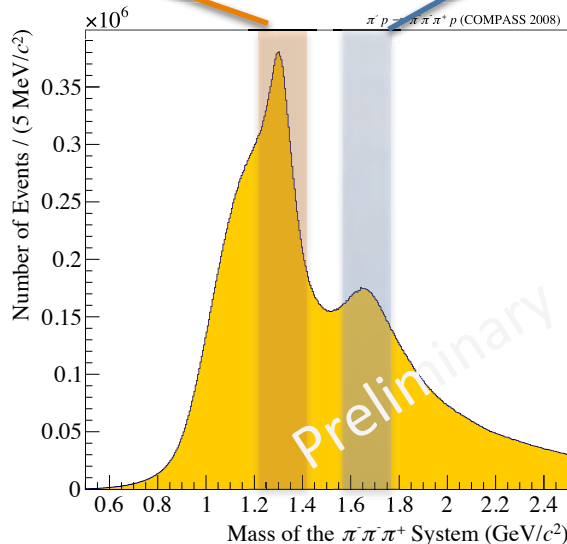


$m^2_{2\pi}$

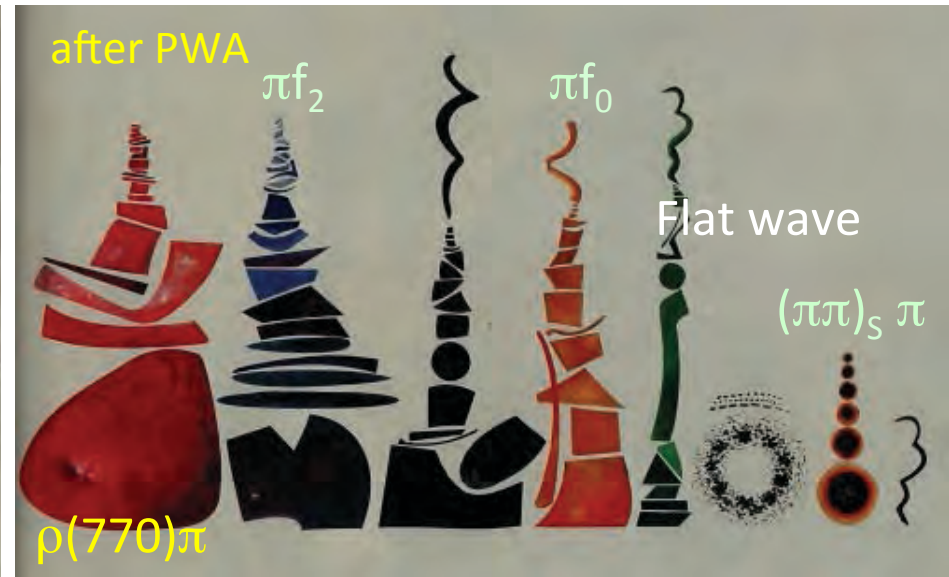
$m^2_{2\pi}$

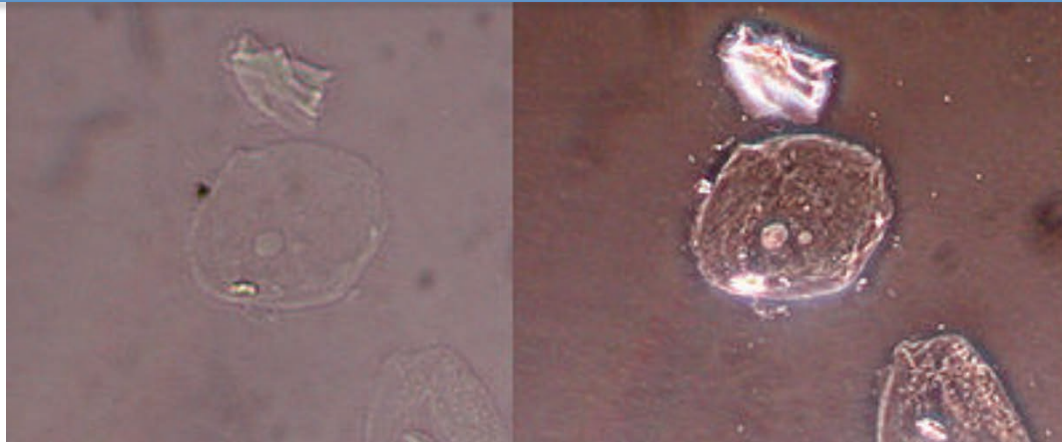
$t'_{3\pi}$

used in analysis



inspired by M. Pennington



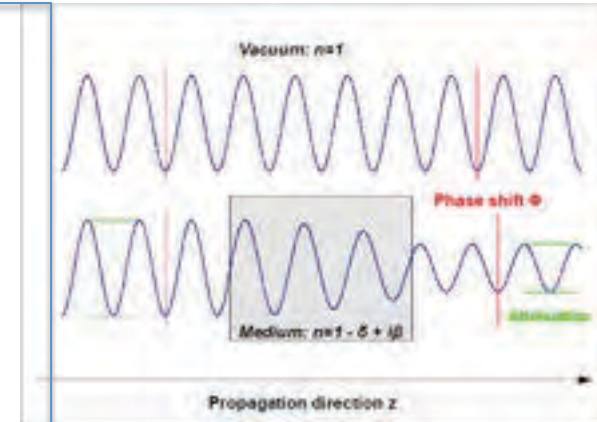


Bright field microscopy maps distribution of imaginary part of refractive index

Peak hunting

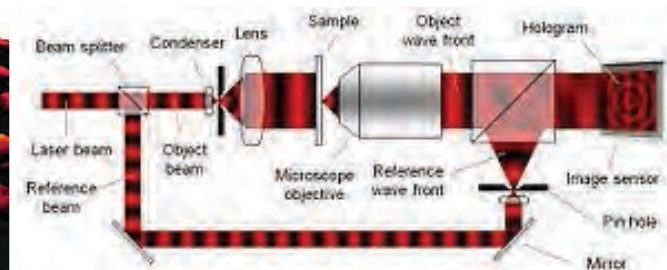
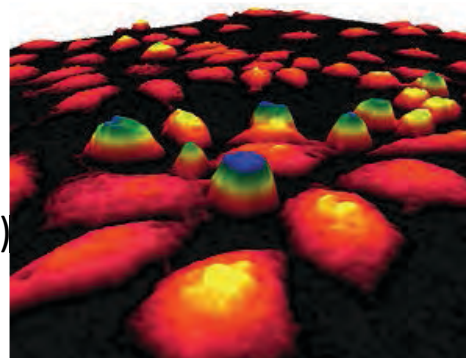
Phase contrast microscopy maps distribution of complex refractive index modulation using interference effects

Dalitz plot analysis



Holographic Phase imaging maps interference pattern with reference beam
3D image of object (quantitative)

Low statistics PWA

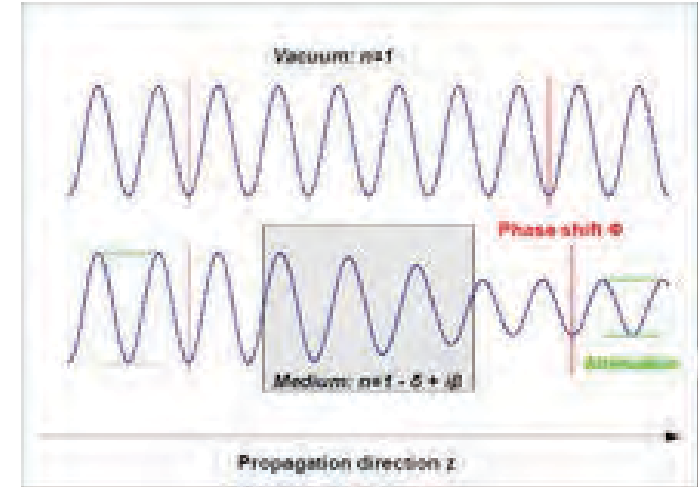




Absorption



Phase contrast



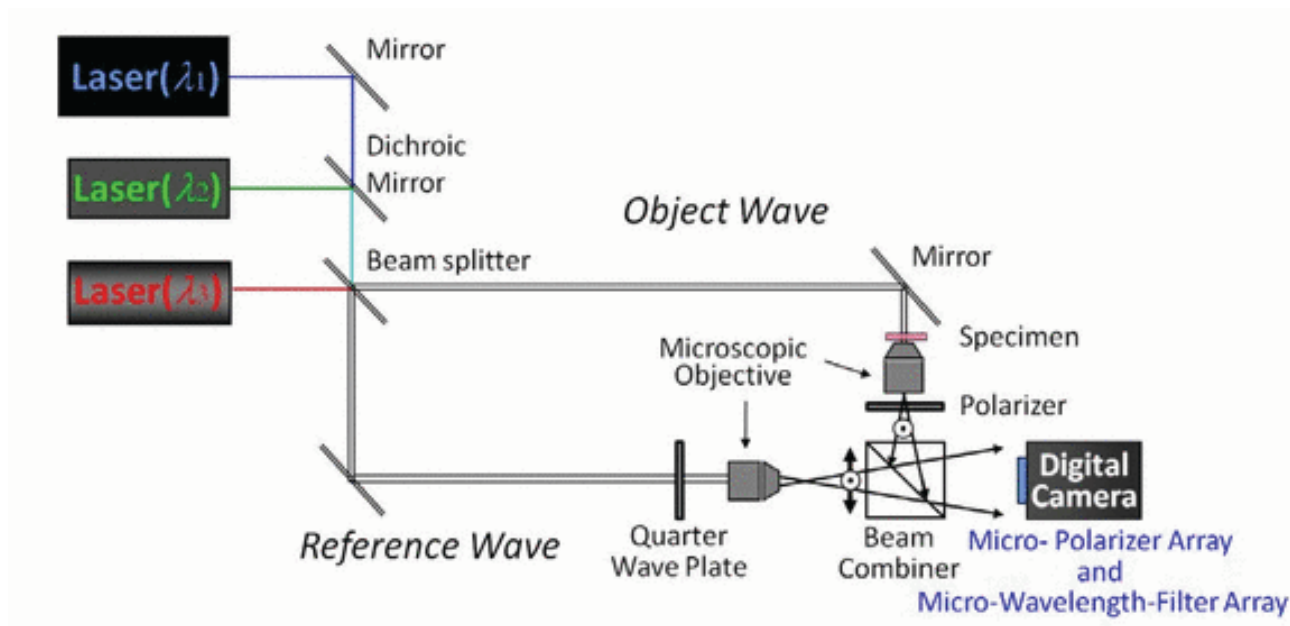
$$n=1-\delta+i\beta$$

X-rays

Optical methods:

If you have enough lasers.. you can add color to your phase shift holography

- solves sign of **phase shift ambiguities**
- useful for **recording dynamic processes**



Compass: Combine results at different t'

What is PWA ?

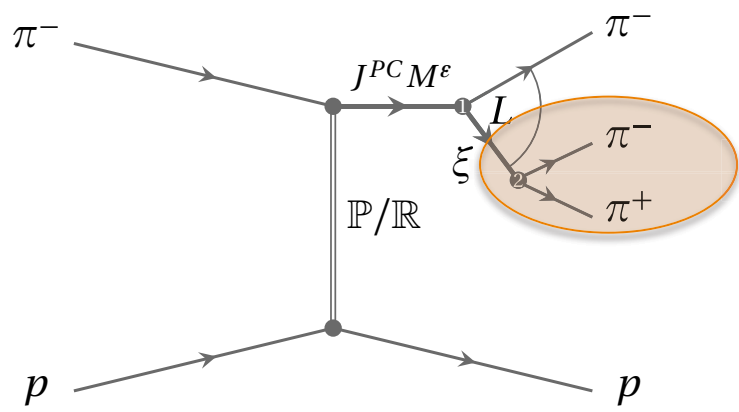
Describe population in 5-dimensional phase space in $\pi\pi\pi$ by model

- Define a set of quantum numbers J^{PC}
 - Define a set of possible decay channels for each J^{PC}
($X^- \rightarrow \text{isobar} + \pi$; $\text{isobar} \rightarrow \pi\pi$) : wave (88 waves used)
 - each such “wave” has a pre-determined population in phase space
 - each wave may have alignment of J described by quantum number M
 - For each bin of 20 MeV/c² mass of $\pi\pi\pi$: determine which coherent combination of waves fits distribution best
 - Obtain spin-density matrix
- step 2
- Describe spin density matrix (submatrix) by model containing resonances and non-resonant contributions connecting all mass bins
 - Determine resonance parameters

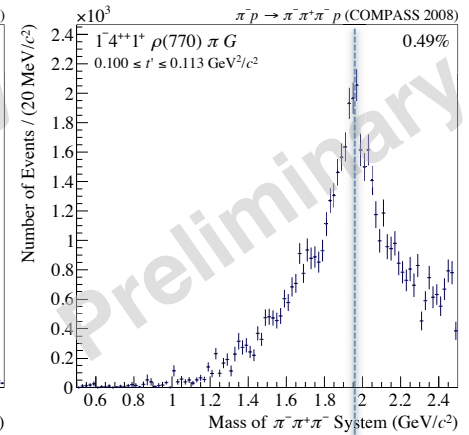
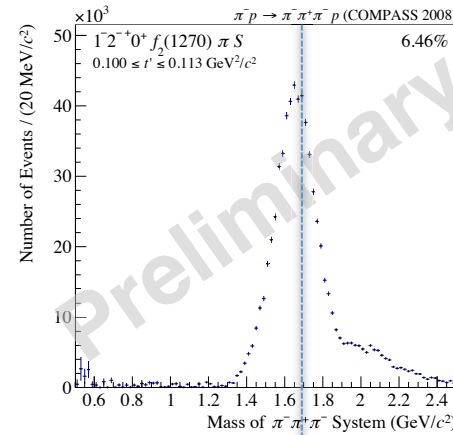
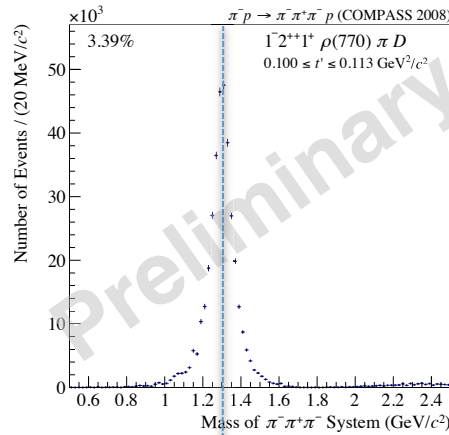
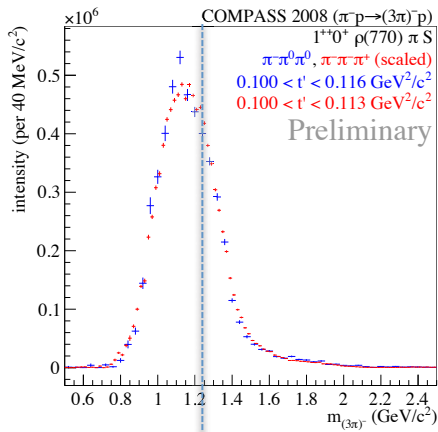
experts only

Particle	J^{PC}	Mass [MeV/c ²]	Width [MeV/c ²]
$f_0(500)$	0^{++}	400 to 550	400 to 700
$f_0(980)$	0^{++}	990 ± 20	40 to 100
$f_2(1270)$	2^{++}	1275.1 ± 1.2	$185.1^{+2.9}_{-2.4}$
$f_0(1370)$	0^{++}	1200 to 1500	200 to 500
$f_0(1500)$	0^{++}	1505 ± 6	109 ± 7
$\rho(770)$	1^{--}	775.49 ± 0.34	149.1 ± 0.8
$\rho_3(1690)$	3^{--}	1688.8 ± 2.1	161 ± 10

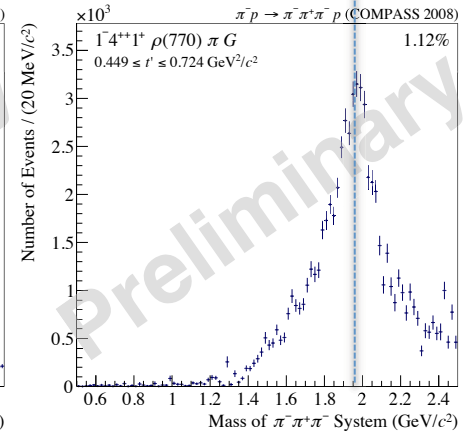
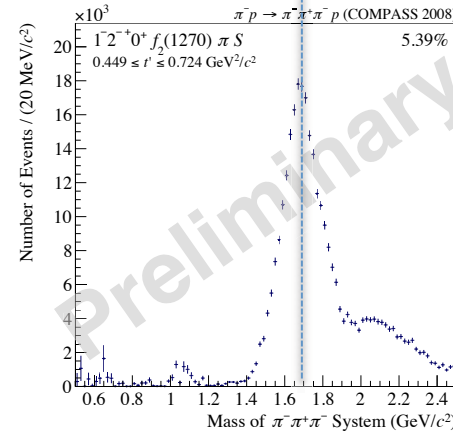
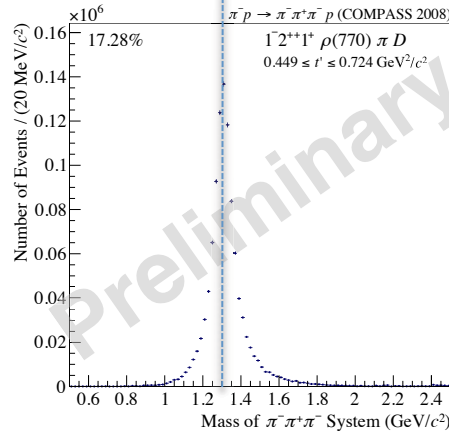
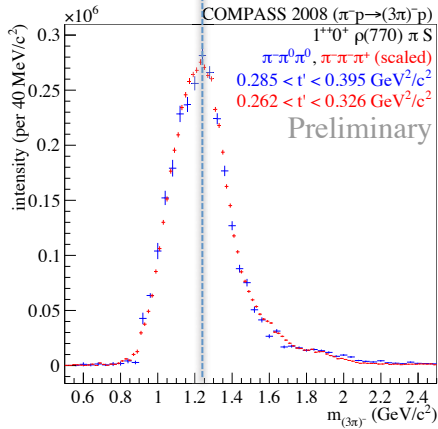
$[\pi\pi]_S$



low t



high t



$1^{++}0^+ \rho \pi S$

$2^{++}1^+ \rho \pi D$

$2^{-+}0^+ f_2 \pi S$

$4^{++}1^+ \rho \pi G$

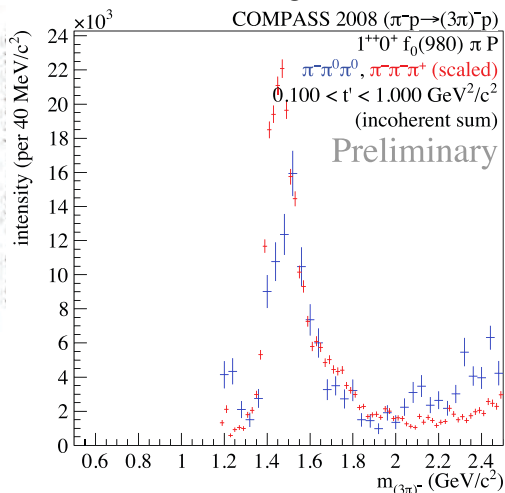
More exotic families



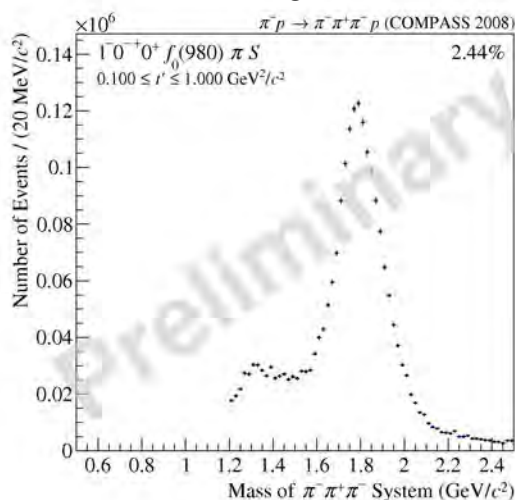


Waves involving $f_0(980)$

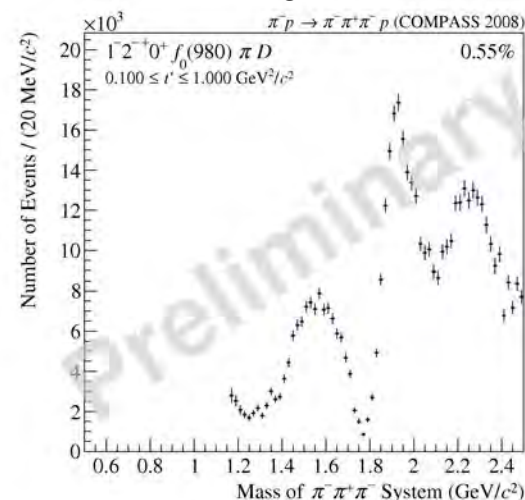
$1^{++}0^+ f_0(980) \pi P$



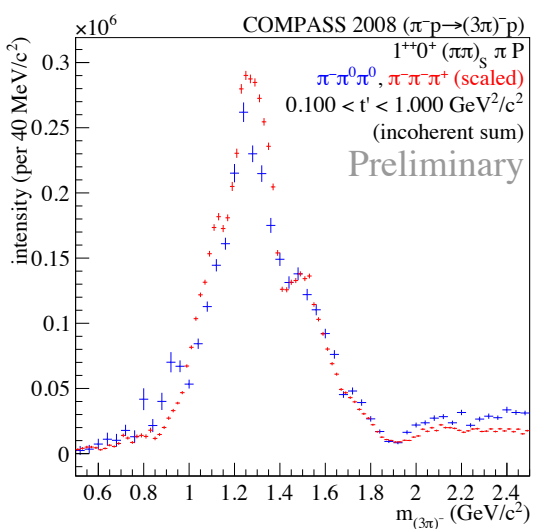
$0^{-+}0^+ f_0(980) \pi S$



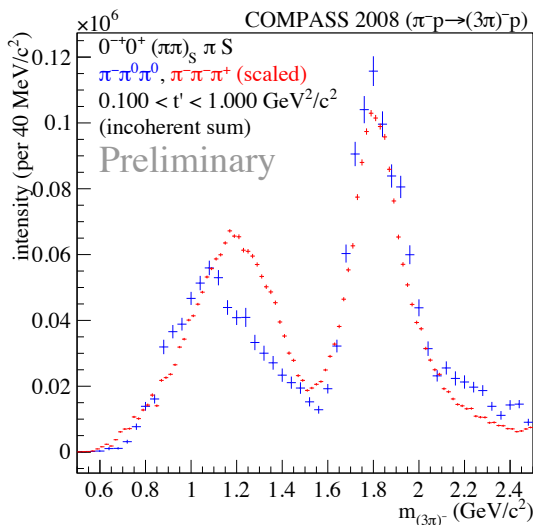
$2^{-+}0^+ f_0(980) \pi D$



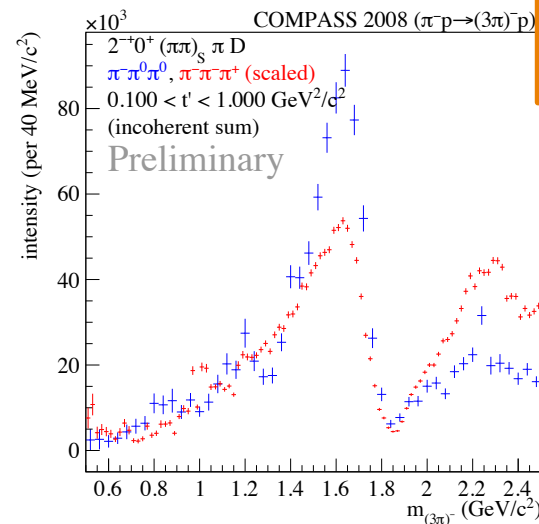
$\pi^- \pi^+ \pi^-$ and $\pi^- \pi^0 \pi^0$



$1^{++}0^+ [\pi\pi]_S \pi P$



$0^{-+}0^+ [\pi\pi]_S \pi S$

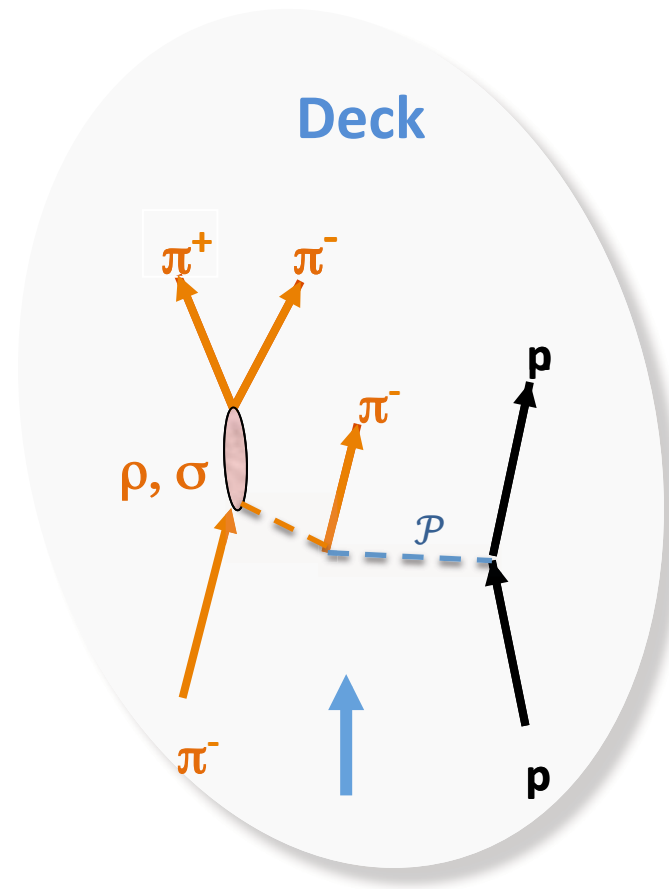
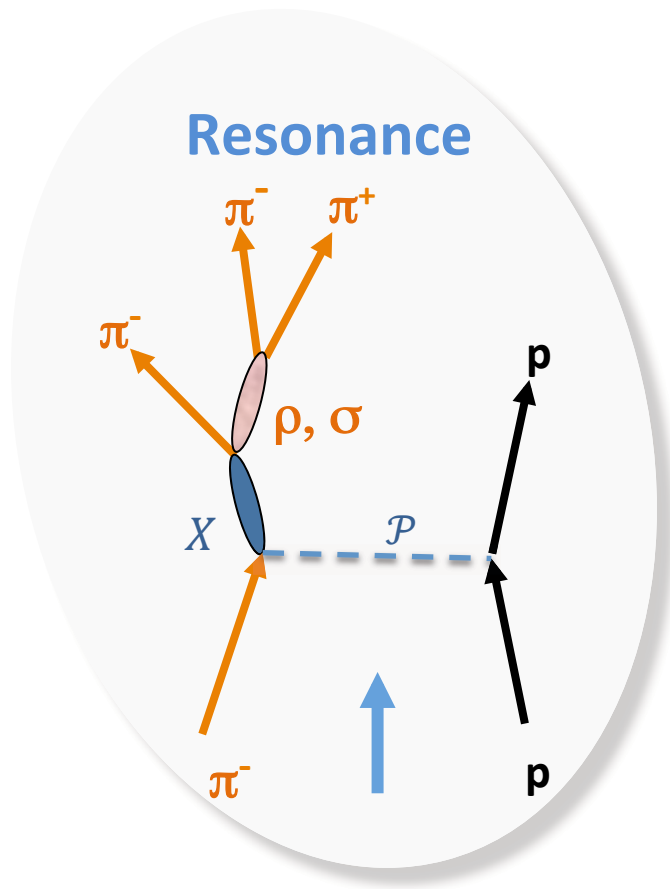


$2^{-+}0^+ [\pi\pi]_S \pi D$

experts only

Describe the results obtained independently in different mass bins by a model

- select physics contributions
- fit to **spin density matrix** (not only to simple mass spectra)



Two types of contributions

Use only lowest $M = 0, 1$ waves (so far)

experts only

This work: 6 waves

Model:

$1^{++} \quad 0^+ \rho \pi S$

$2^{++} \quad 1^+ \rho \pi D$

$4^{++} \quad 1^+ \rho \pi G$

$2^{-+} \quad 0^+ f_2 \pi S$

$1^{++} \quad 0^+ f_0(980) \pi P$

$0^{-+} \quad 0^+ f_0(980) \pi S$

$J^{PC} M^{\epsilon} [isobar] \pi L$

2 resonances : $a_1(1260)$ and a_1' + non resonant term

2 resonances : $a_2(1320)$ and a_2' + non resonant term

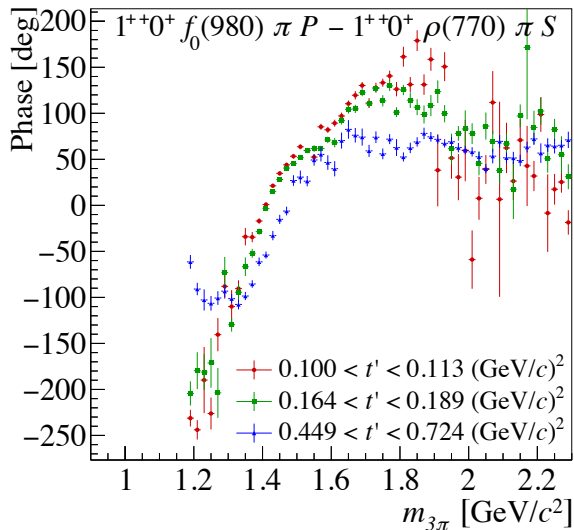
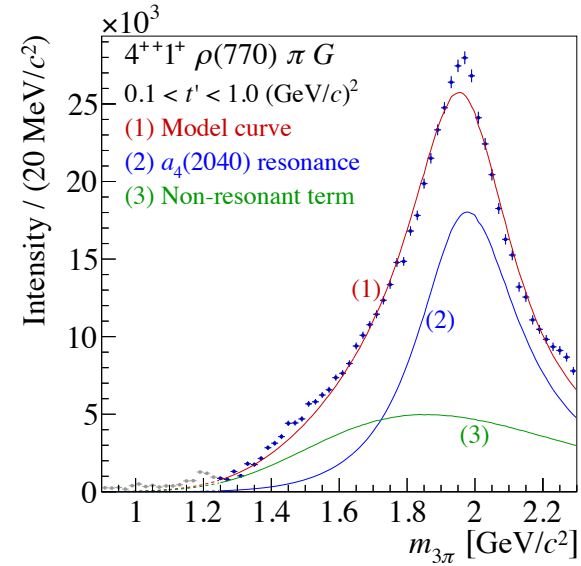
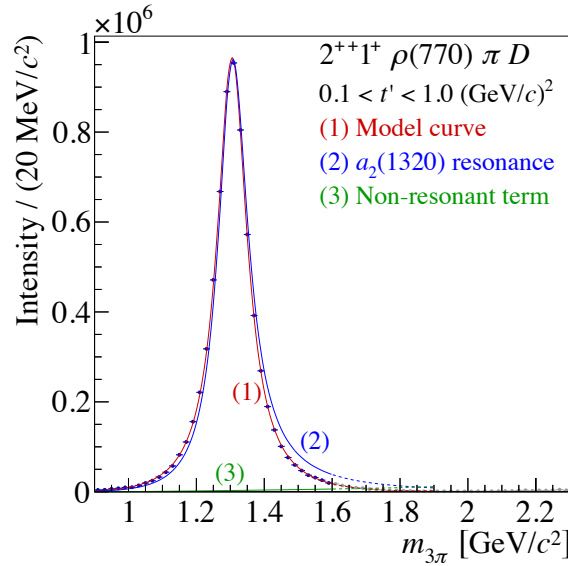
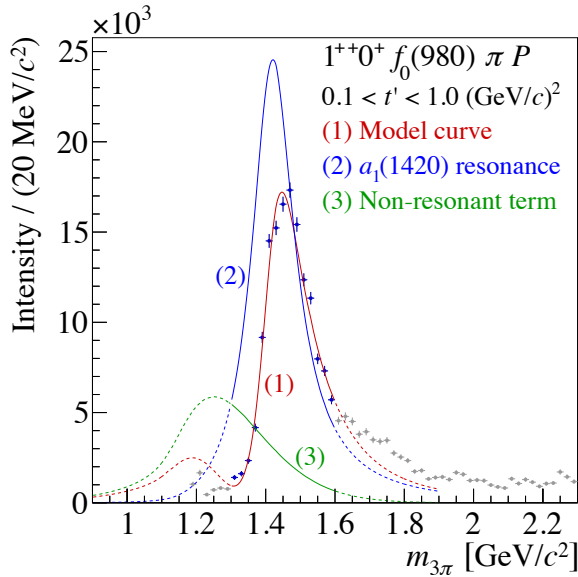
1 resonance : $a_4(2040)$ + non resonant term

2 resonances : $\pi_2(1670)$ and π_2' + non resonant term

1 resonance : $a_1(1420)$ + non resonant term

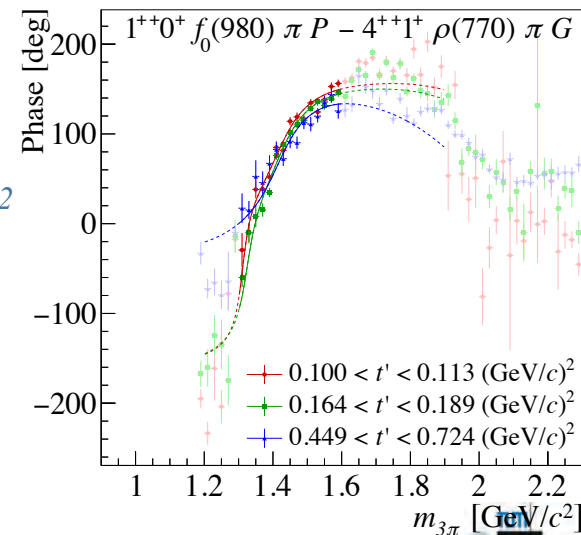
1 resonance : $\pi(1800)$ + non resonant term

- 231 mass distributions with 23100 data points
- 352 free parameters



Observation:

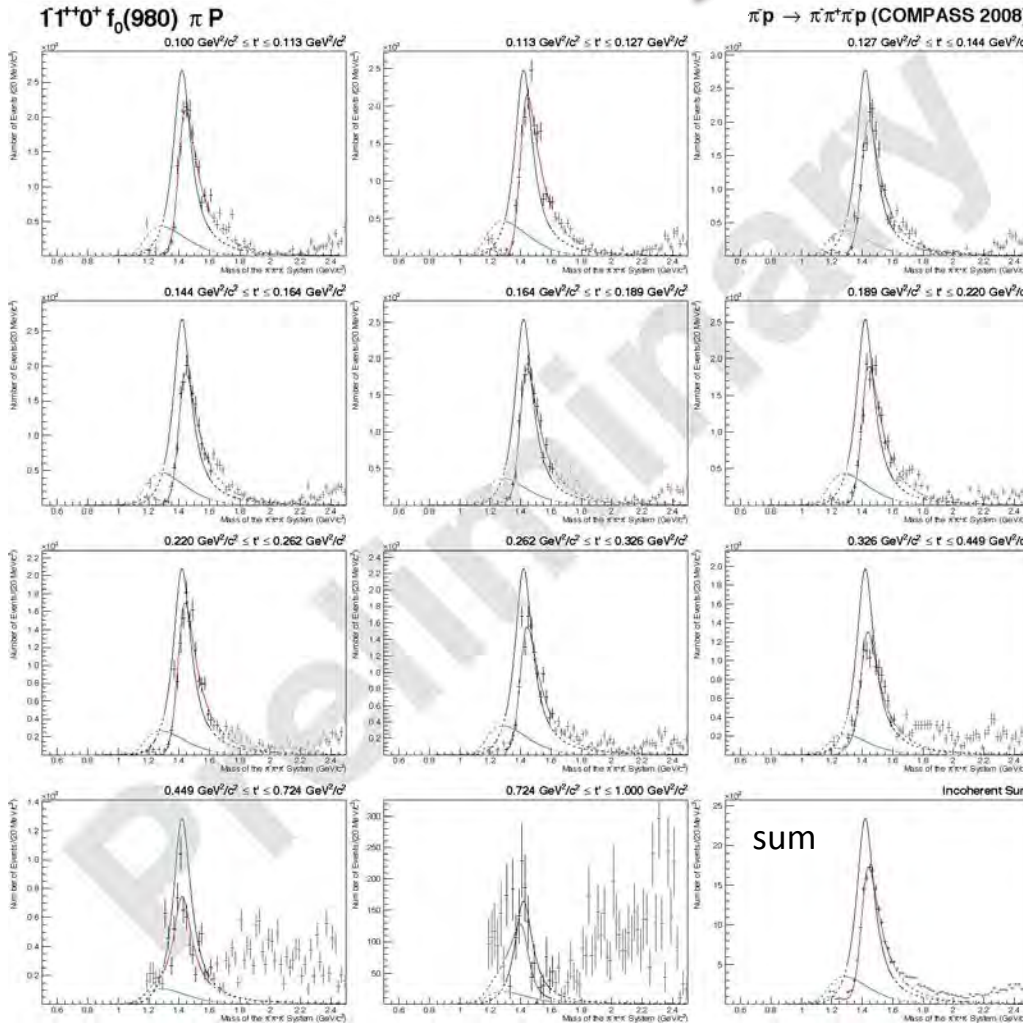
- Decay only : $[f_0(980)] \pi P$
- Mass : $1413 \pm 15 \pm 13 \text{ MeV/c}^2$
- Width: $157 \pm 8 \pm 23 \text{ MeV/c}^2$



Mass dependent fits $a_1(1420)$

Fit in 11 t -bins

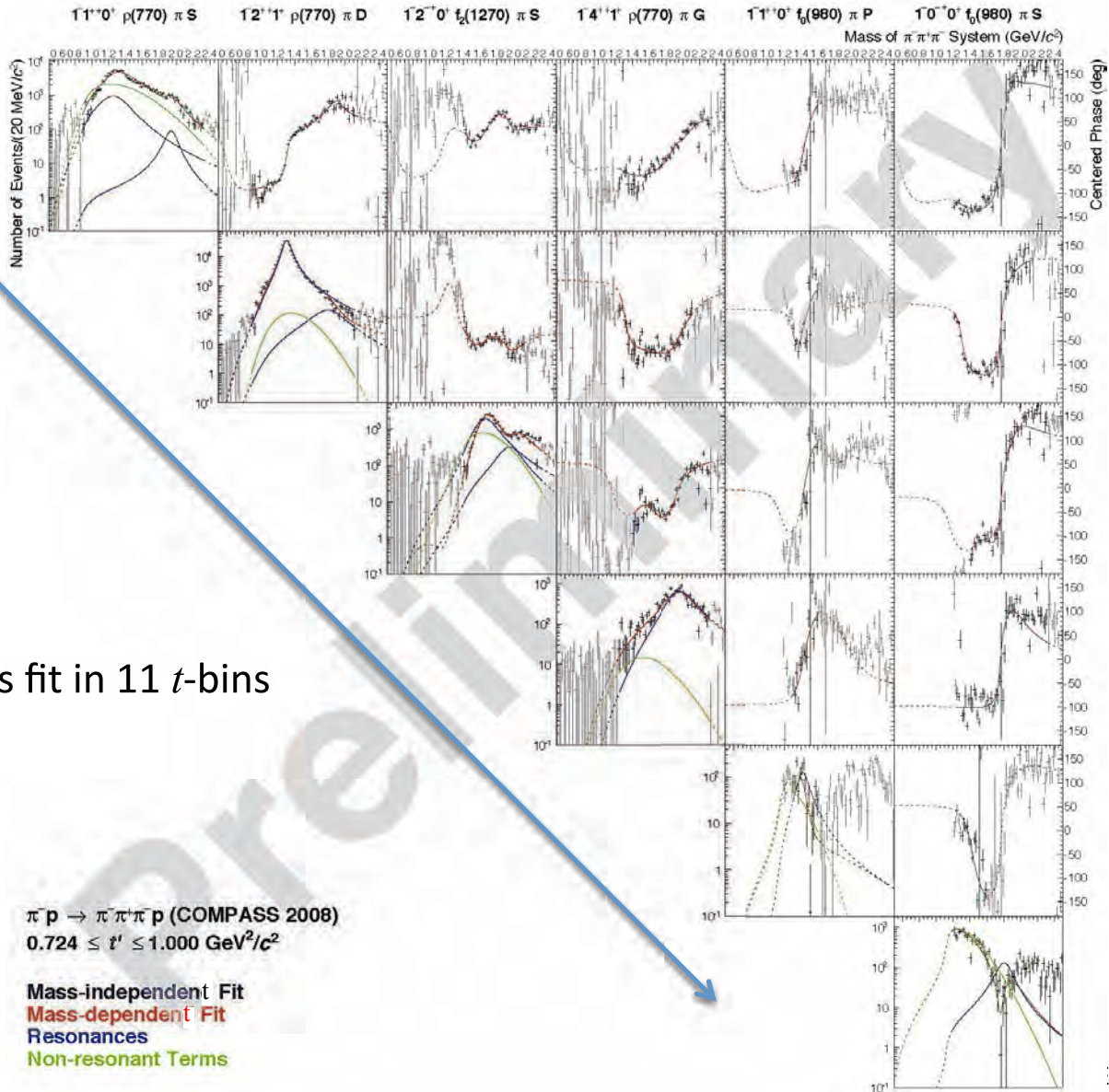
t



$1^{++}0^+ f_0(980) \pi P$

t

NEW



Reference waves

Interferometry

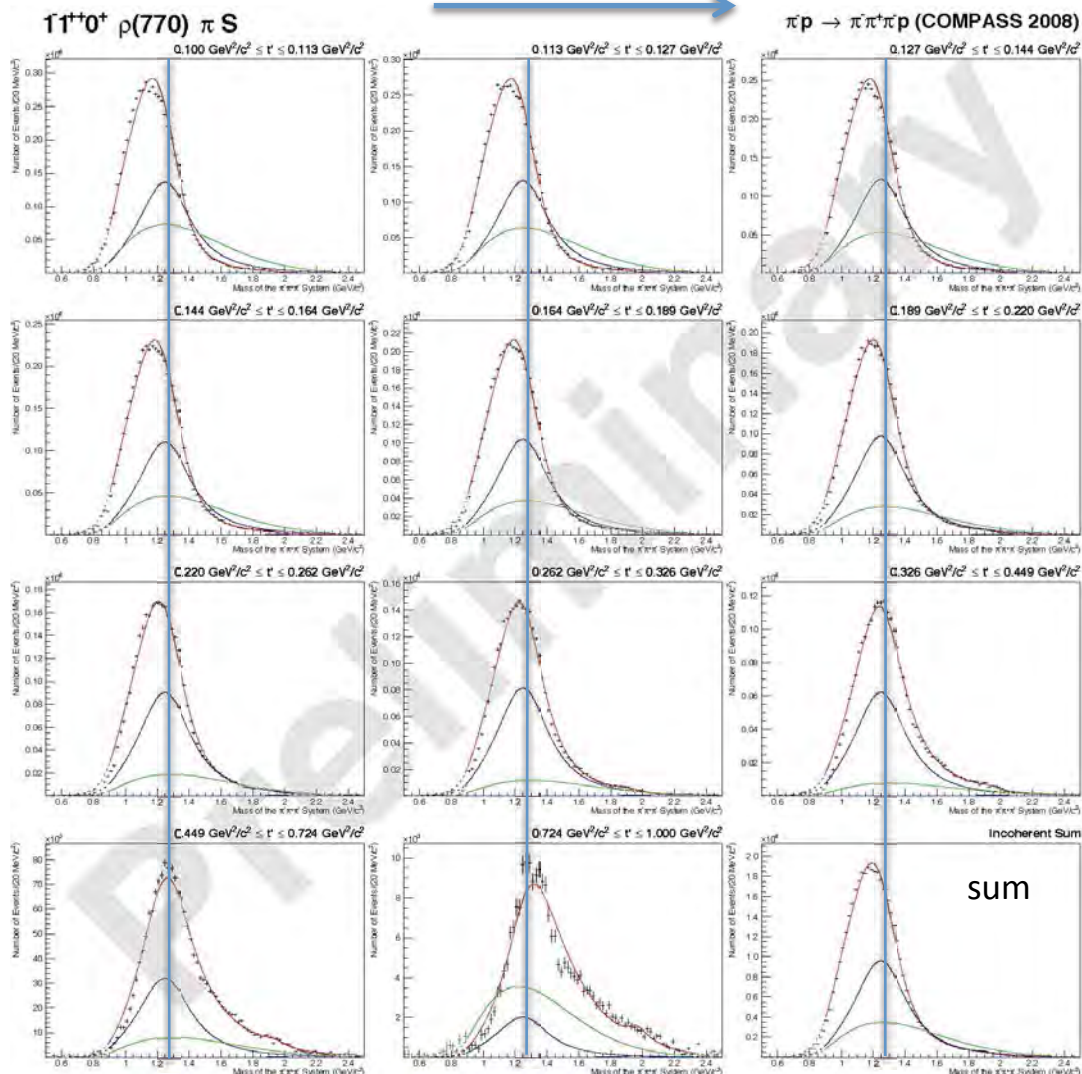
simultaneous fit in 11 t -bins

$\pi^- p \rightarrow \pi^+ \pi^- \pi^+ p$ (COMPASS 2008)
 $0.724 \leq t' \leq 1.000 \text{ GeV}^2/c^2$

Mass-independent Fit
 Mass-dependent Fit
 Resonances
 Non-resonant Terms

Fit in 11 t-bins

t



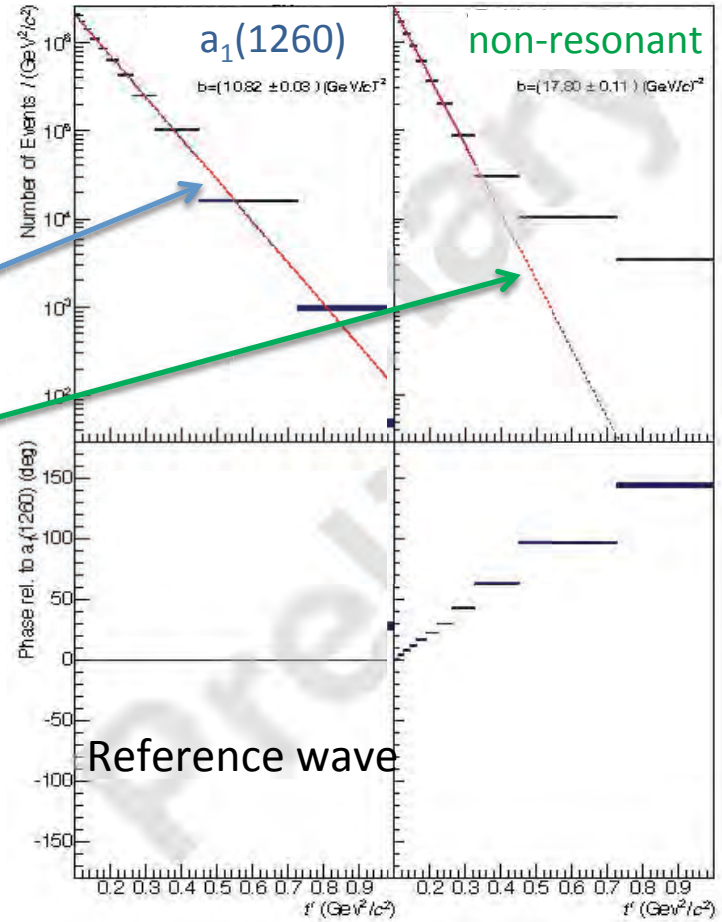
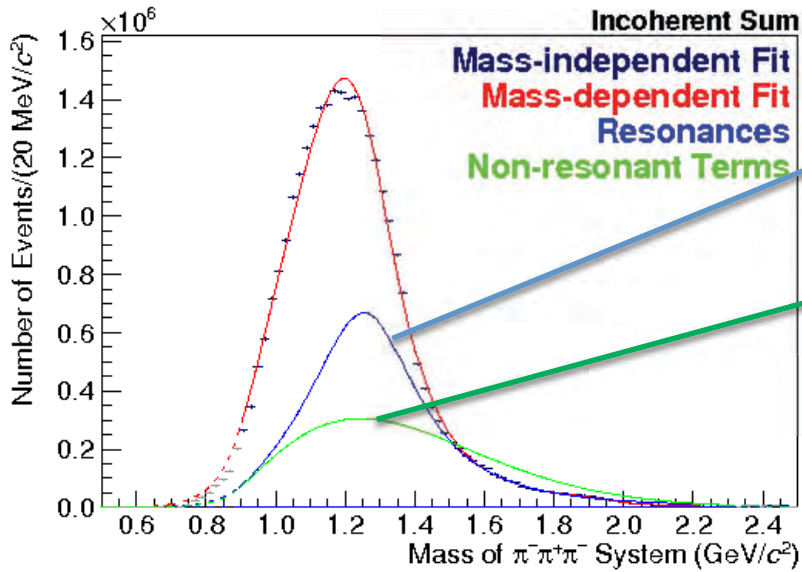
Strongly t-dependent
spectral shape around
 $a_1(1260)$

$1^{++}0^+ \rho \pi S$

$J^PC M^\epsilon [isobar] \pi L$

t

$\pi\pi\pi$ COMPASS 2008



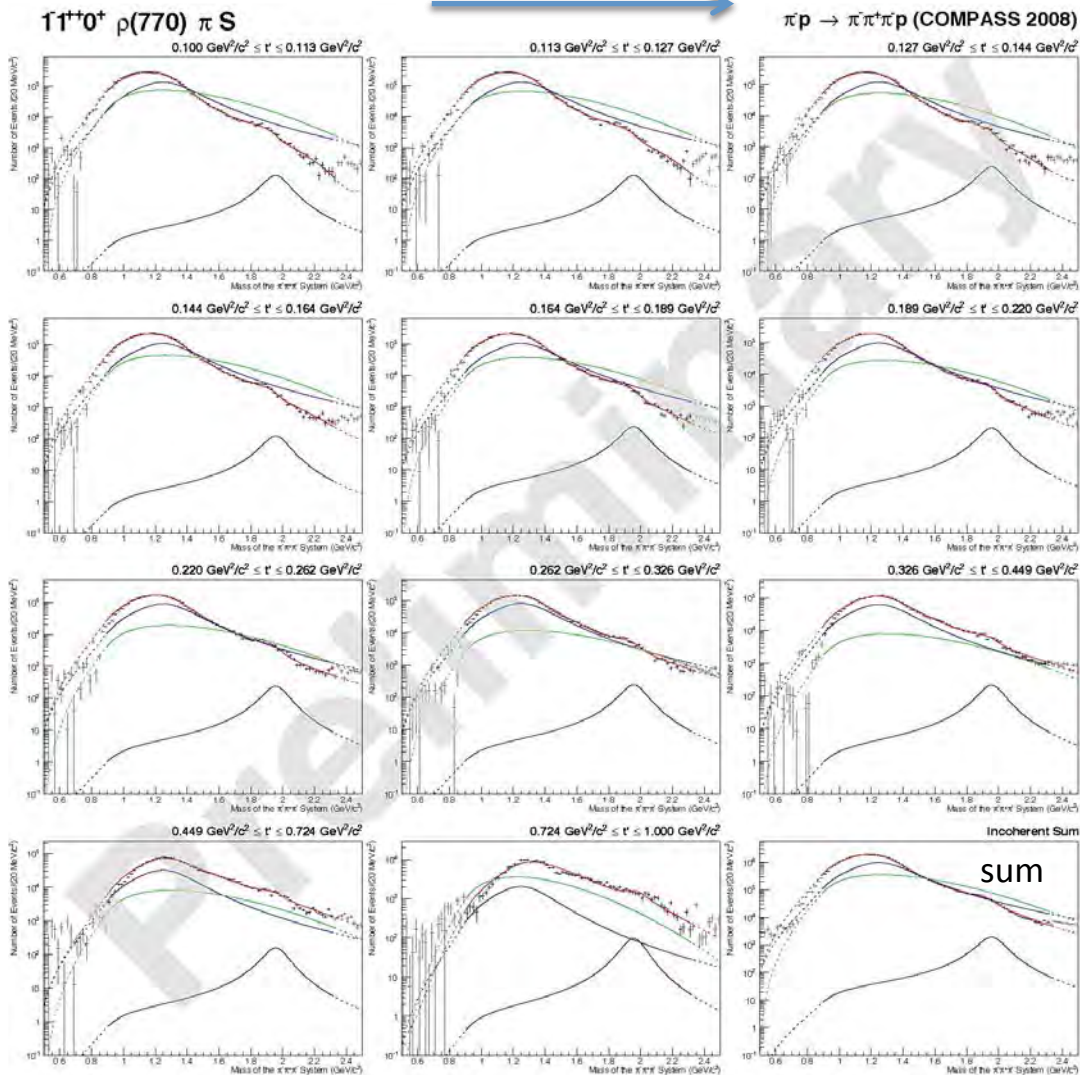
$$1^{++}0^+ \rho\pi S$$

$$J^{PC}M^{\epsilon}[\text{isobar}]\pi L$$

t

Fit in 11 t-bins

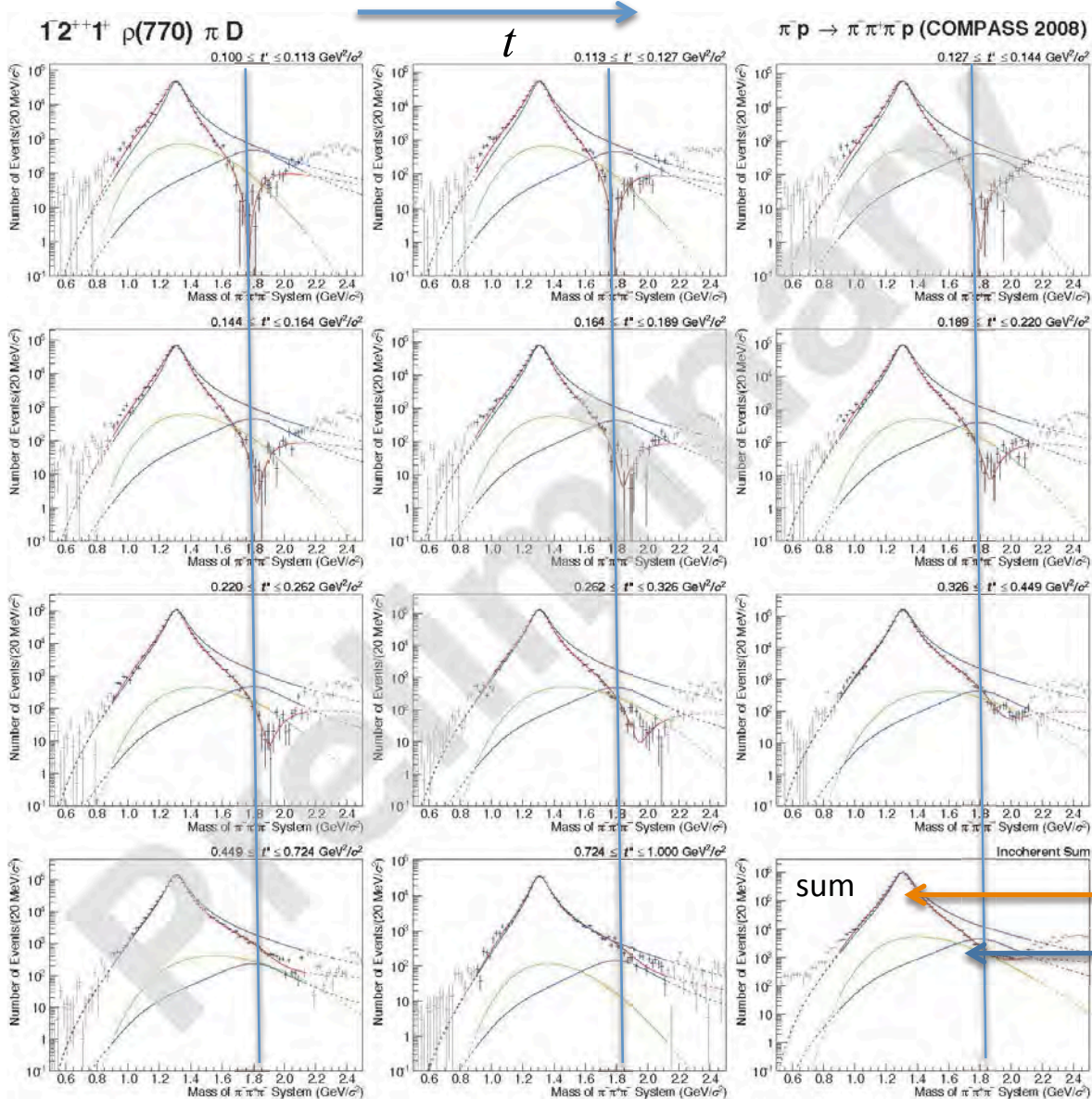
t



Second high-mass a_1' resonance visible

$1^{++}0^+ \rho \pi S$

t



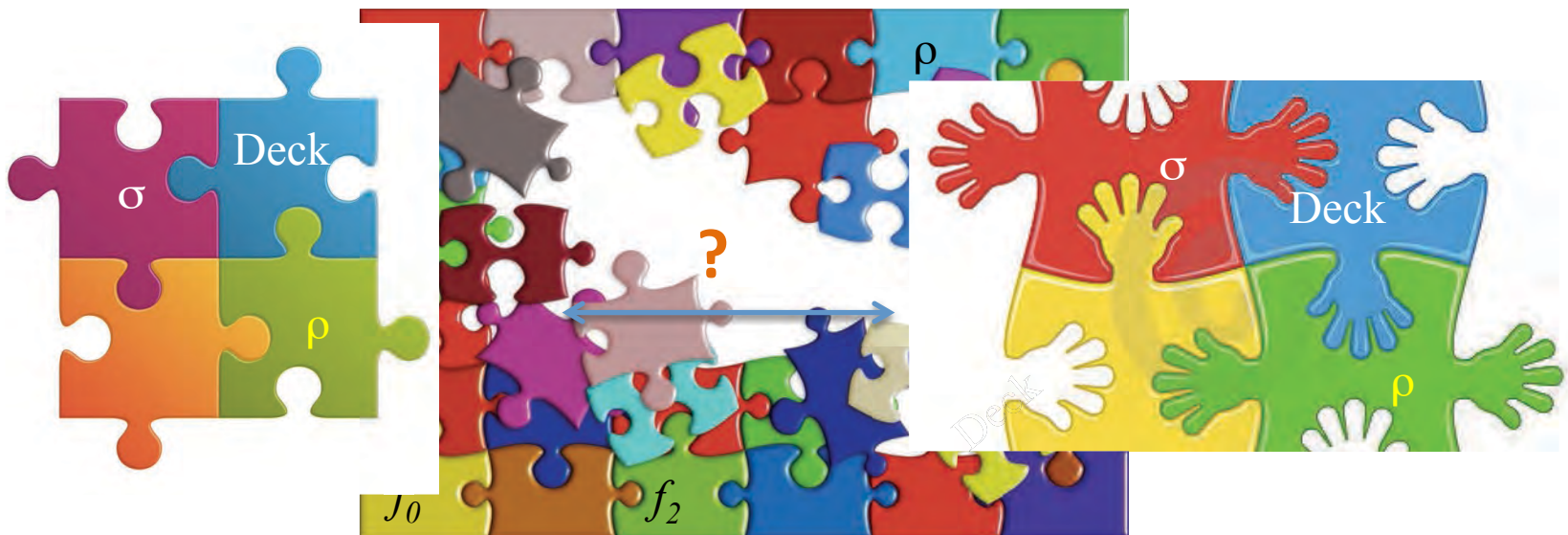
Strongly t -dependent interference effects
high-mass a_2'

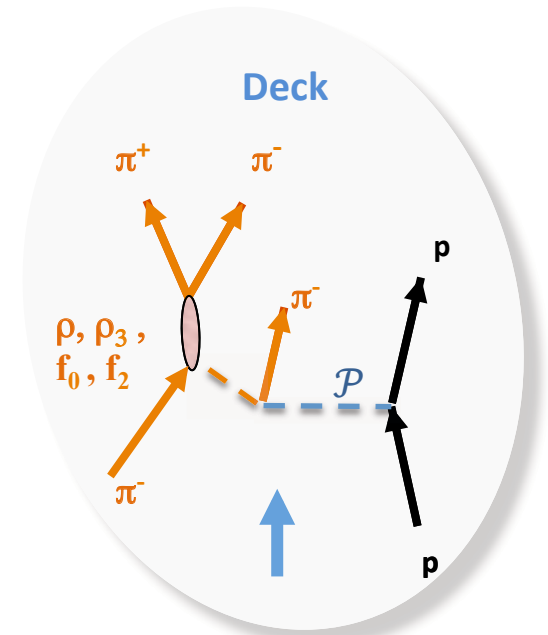
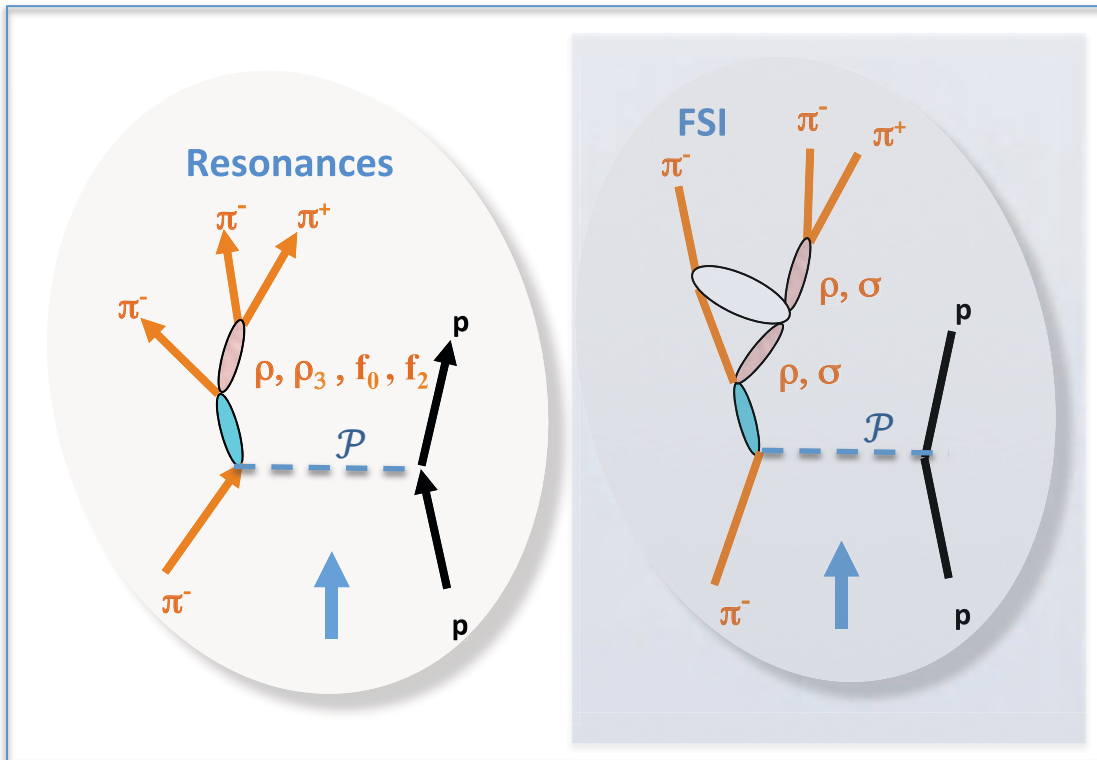
t

$a_2(1320)$
 a_2'

Particle	J^{PC}	Mass Range [MeV/c ²]	Width Range [MeV/c ²]	PDG Values	
				m [MeV/c ²]	Γ [MeV/c ²]
“Established” states				PDG	
$a_1(1260)$	1^{++}	1260–1290	360–420	1230 ± 40	250–600
$a_2(1320)$	2^{++}	1312–1315	108–115	$1318.3^{+0.5}_{-0.6}$	107 ± 5
$a_4(2040)$	4^{++}	1928–1959	360–400	1996^{+10}_{-9}	255^{+28}_{-24}
States not in PDG summary table					
$a_1(1930)$	1^{++}	1920–2000	155–255	1930^{+30}_{-70}	155 ± 45
$a_2(1950)$	2^{++}	1740–1890	300–555	1950^{+30}_{-70}	180^{+30}_{-70}
truly new states					
$a_1(1420)$	1^{++}	1412–1422	130–150		

- We have solved a puzzle – but were the building blocks correct ?

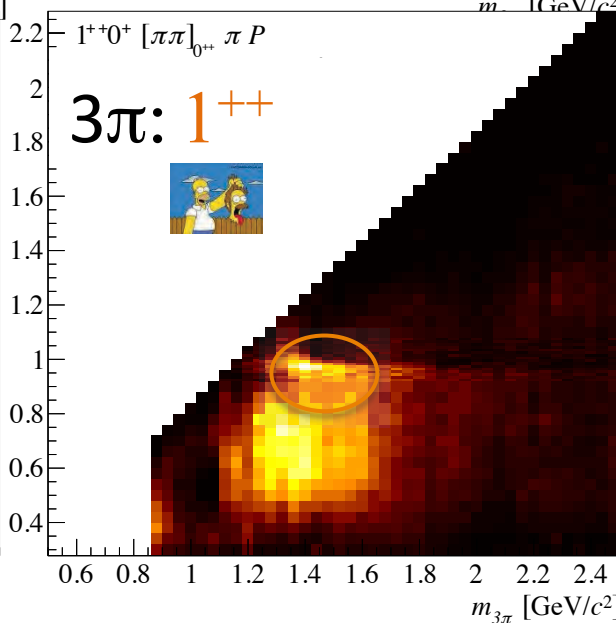
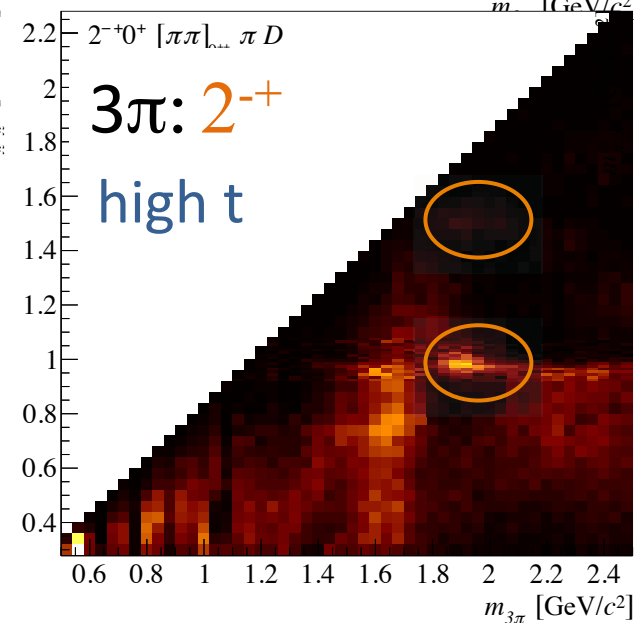
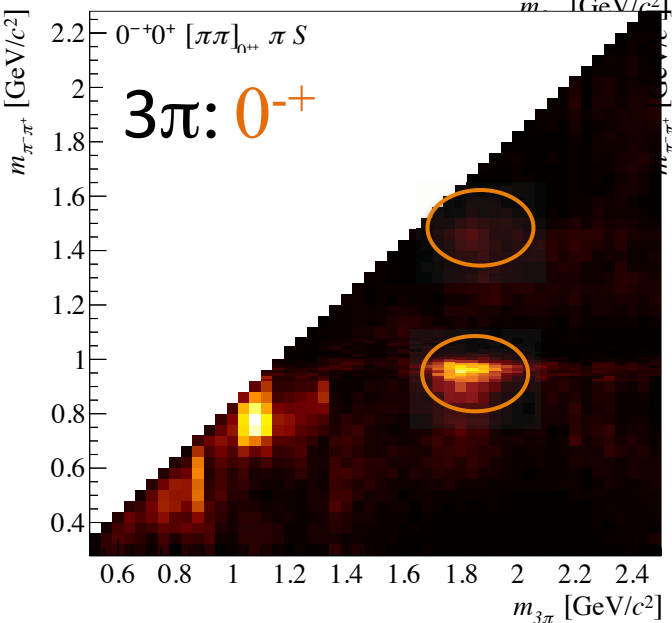
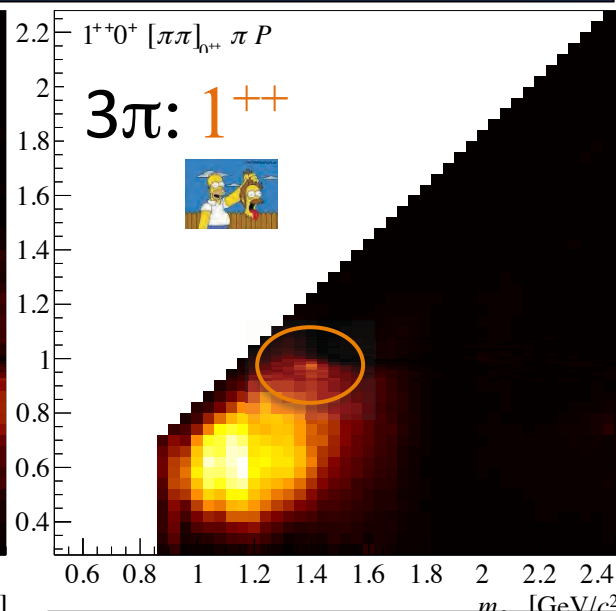
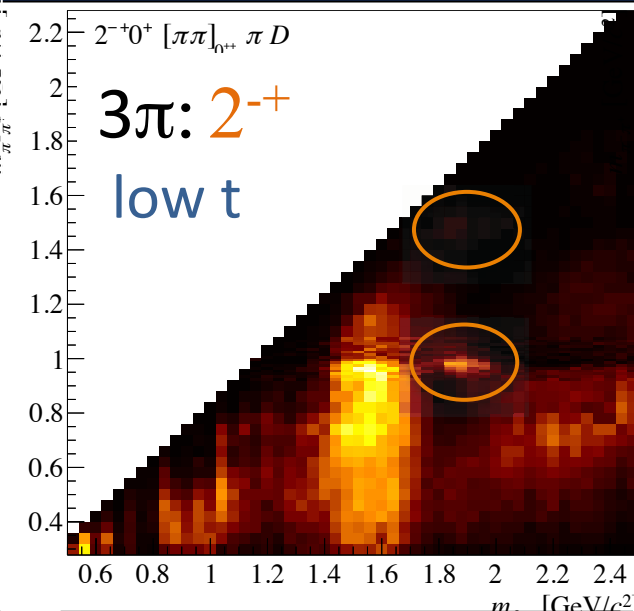
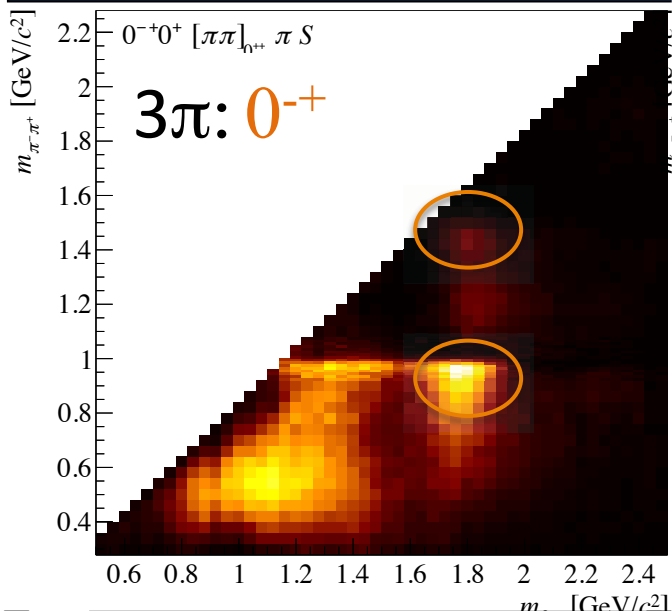




- Select J^{PC} via PWA
- For each J^{PC} and mass-bin in 3π :
 - determine composition and shapes of 2π isobars
 - complex couplings
 - non-resonant contributions (via t -dependence)



Correlation: $m_{2\pi}(0^{++})$ vs $m_{3\pi}(J^{PC})$





Conclusion - Pion



- **First** precise measurement of π polarizability
 - Pion much stiffer than atom (strong interaction)
 - Excellent **agreement with theory** (χ PT)
 - Future: separate magnetic and electric polarizabilities
- New path to radiative meson excitations

- Establish **new** “2D” fit method to perform PWA in $m_{3\pi}$ and t

- Find **new iso-vector** state $a_1(1420)$

- $M_{a_1(1420)} = 1412-1422 \text{ MeV}/c^2$, $\Gamma_{a_1(1420)} = 130-150 \text{ MeV}/c^2$

- (exclusive) decay into $f_0(980)\pi$ in relative P-wave



- **Nature of $a_1(1420)$?**

Isospin partner of $f_1(1420)$ (considered to be exotic) ?

Dynamically generated through $a_1(1260) \leftrightarrow KK^* \leftrightarrow f_0(980)\pi$ channel ?

Interference of $a_1(1260)$ with non resonant amplitudes ?



Conclusion



- Developed **new method** to establish shape of isobar-spectrum
 - **first application**: $[\pi\pi]_S^*$:
 - Shows **strong dependence** on $m_{3\pi}$ and on J^{PC} of mother wave
 - Reveals information on **scalar isobars** (measure **phases** in decays)

Open Path to **Dalitz-plot analysis** using PWA
from PWA identified states

Needs **high statistics !!**