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# Intrinsic Charm in the Proton

Felix Hekhorn

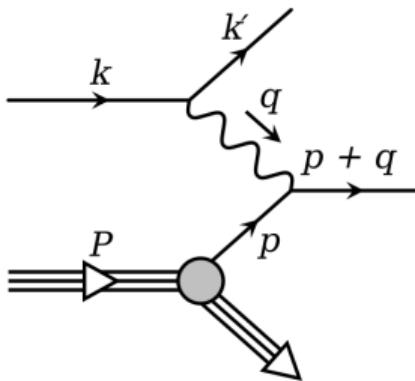
Physics opportunities with proton beams at  
SIS100, February 2024

# Overview

1. Fitting PDFs as e.g. in NNPDF4.0 [[EPJC82.428](#)]
2. Evidence for intrinsic charm quarks in the proton [[Nature608.483](#)]
3. The intrinsic charm quark valence distribution of the proton  
[[2311.00743](#)]
4. Summary

Fitting PDFs as e.g. in NNPDF4.0 [EPJC82.428]

# Parton Distribution Functions

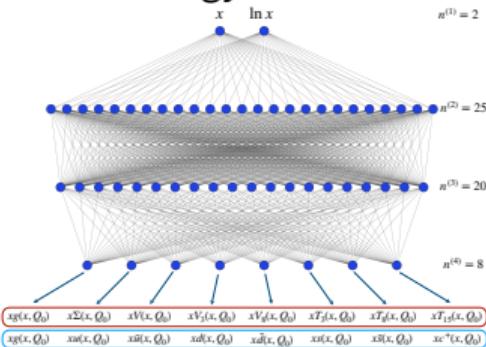


Parton Distribution Functions (PDF)  $\mathbf{f}(x, \mu_F^2)$

- ▶ universal functions to describe high-energy QCD scattering
- ▶ describe the fundamental constituents of the proton: quarks, gluons
- ▶  $\mu_F$ -dependence: DGLAP equations!
- ▶  $x$ -dependence: fit!

# How to fit a PDF? Use Machine Learning!

## Methodology:



taken from [EPJC82.428]

## Theory:

$$s^2 \frac{d^2 \sigma_{\text{SM}, g}^{(1), H, fin}}{dt_1 du_1} = \alpha \alpha_s g_{g, Q}^{N_1} g_{V, Q}^{N_2} K_{gV} N_C C_F \left[ -\frac{2}{u_1} P_{g, gV}^H(x_1) \right. \\ \left\{ B_{e,\text{QED}}^{(1)}(x_1 k_1) \left( \ln \left( \frac{s_1^2}{m^2(s_1 + m^2)} \right) - \ln(\mu_F^2/m^2) \right) - 2B_{e,\text{QED}}^{(1)}(x_1 k_1) \right\} \\ + C_A \frac{s_1}{2\pi(s_1 + m^2)} \left( \int d\Omega_{k_1} R_{e,OK} \right)^{\text{finite}} \\ \left. + 2C_F \frac{s_1}{2\pi(s_1 + m^2)} \int d\Omega_{k_1} R_{e,\text{QED}} \right]. \quad (5.36)$$

taken from [1910.01536]

## Experiment:

$p_T$ [GeV]	Dimuon cross section (pb)	Dielectron cross section (pb)	Dilepton cross section (pb)
0 - 1.0	8.8945 <small>±0.00005</small>	9.0042 <small>±0.00006</small>	9.2821 <small>±0.00010</small>
1.0 - 2.0	23.05 <small>±0.00010</small>	23.482 <small>±0.00007</small>	22.786 <small>±0.00008</small>
2.0 - 3.0	31.799 <small>±0.00007</small>	32.848 <small>±0.00007</small>	32.042 <small>±0.00007</small>
3.0 - 4.0	35.663 <small>±0.00007</small>	37.025 <small>±0.00008</small>	36.225 <small>±0.00008</small>
4.0 - 5.0	36.435 <small>±0.00008</small>	37.570 <small>±0.00008</small>	36.882 <small>±0.00008</small>
5.0 - 6.0	35.091 <small>±0.00008</small>	36.201 <small>±0.00008</small>	35.579 <small>±0.00008</small>
6.0 - 7.0	33.127 <small>±0.00008</small>	34.275 <small>±0.00009</small>	33.547 <small>±0.00009</small>
7.0 - 8.0	30.967 <small>±0.00010</small>	32.2 <small>±0.00009</small>	31.324 <small>±0.00009</small>
8.0 - 9.0	29.702 <small>±0.00009</small>	29.834 <small>±0.00009</small>	29.089 <small>±0.00009</small>
9.0 - 10.0	26.687 <small>±0.00009</small>	27.309 <small>±0.00009</small>	26.933 <small>±0.00009</small>

taken from [JHEP12.061]

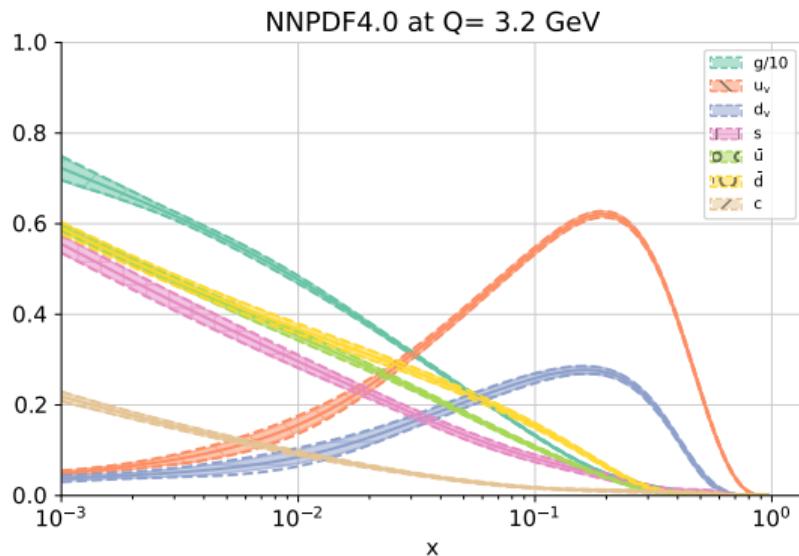
## Strategy:

repeat until converged:

guess candidate PDF  $f(Q_0^2) \rightarrow$  compute theory predictions  $T \rightarrow$  compare to data  $D$

# NNPDF4.0 [EPJC82.428]

- ▶  $\sim 4500$  data points from  $\sim 90$  datasets
- ▶ use NNLO pQCD predictions
- ▶ fit 8 independent functions in NN:  
 $g, u, \bar{u}, d, \bar{d}, s, \bar{s}, c^+ = c + \bar{c}$
- ▶ fitting scale  
 $Q_0 = 1.65 \text{ GeV} > m_c = 1.51 \text{ GeV}$
- ▶ uncertainties via MC replicas
- ▶ typical uncertainties in data region:  
singlet  $\sim 1\%$ , non-singlet  $\sim 2 - 3\%$
- ▶ checks: closure tests [EPJC82.330] +  
future tests [APhysPolB.52.243]



Evidence for intrinsic charm quarks in the  
proton [Nature608.483]

# What is intrinsic charm?

- ▶ NNPDF4.0 determines the total charm distribution  $c^+ = c + \bar{c}$
- ▶ **fitted charm** is an arbitrary mixture of

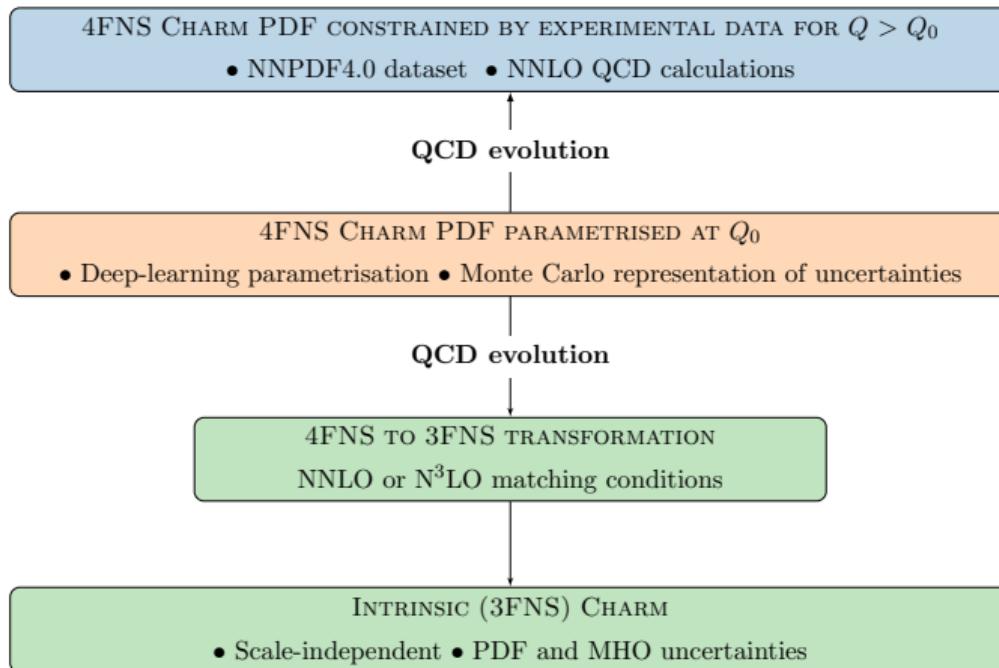
**perturbative charm**

**non-perturbative charm**

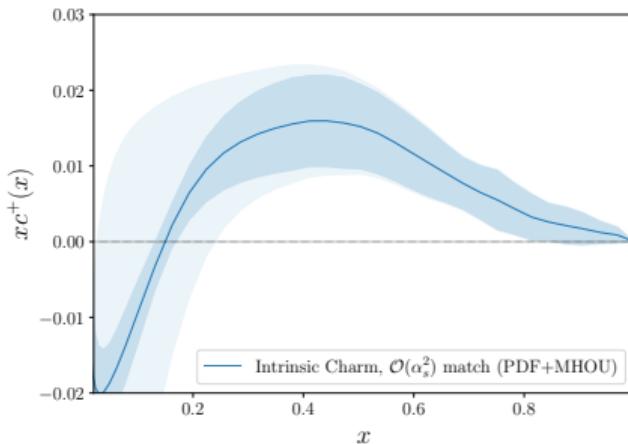
- |  |   |
|--|---|
| <ul style="list-style-type: none"><li>▶ fully perturbative, i.e., predictable at all scales</li><li>▶ generated by perturbative radiation</li><li>▶ always present above heavy quark threshold</li></ul> | <ul style="list-style-type: none"><li>▶ <b>intrinsic charm</b></li><li>▶ part of the static proton wave functions</li><li>▶ present at all scales</li></ul> |
|--|---|

some use a model for intrinsic charm (e.g. [BHP5]), but we don't!

# Strategy

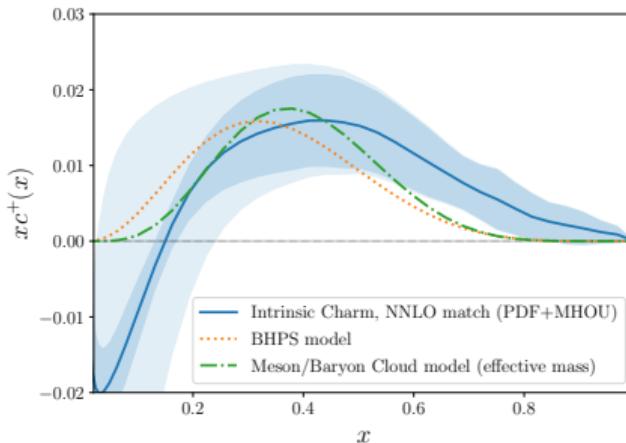


# Discovery of intrinsic charm



- ▶ we find a peak for intrinsic charm
- ▶ for  $x \leq 0.2$  the perturbative uncertainties are quite large
- ▶ the carried momentum fraction is within 1%

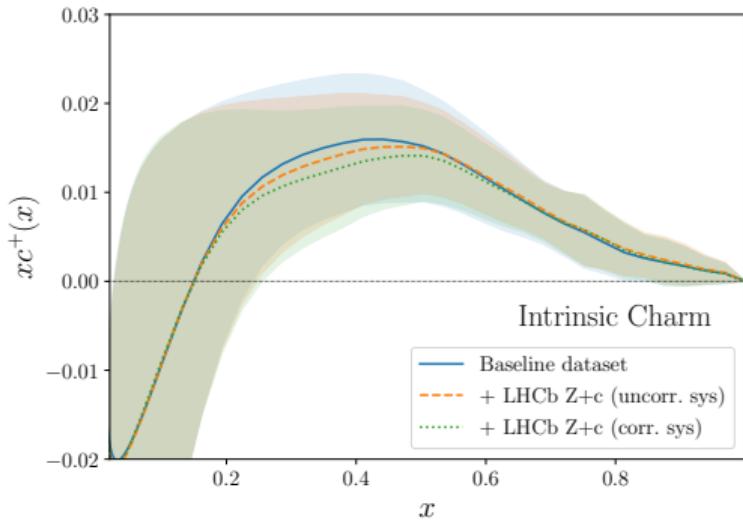
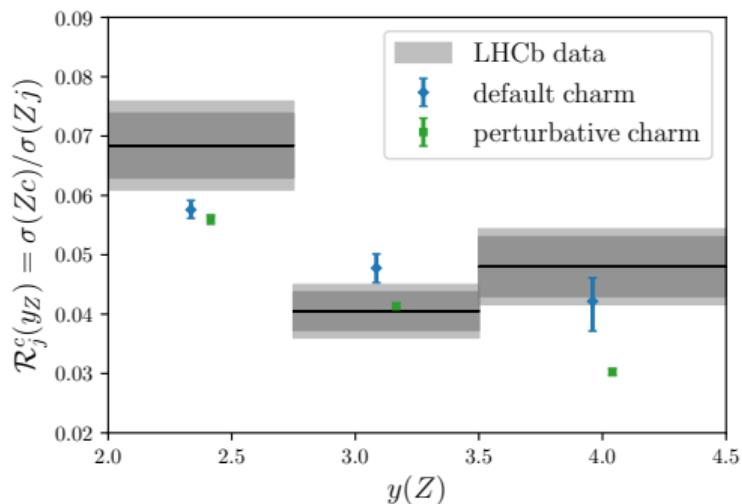
# Data driven intrinsic charm vs. models



[BHPS] or [Meson/Baryon Cloud Model]

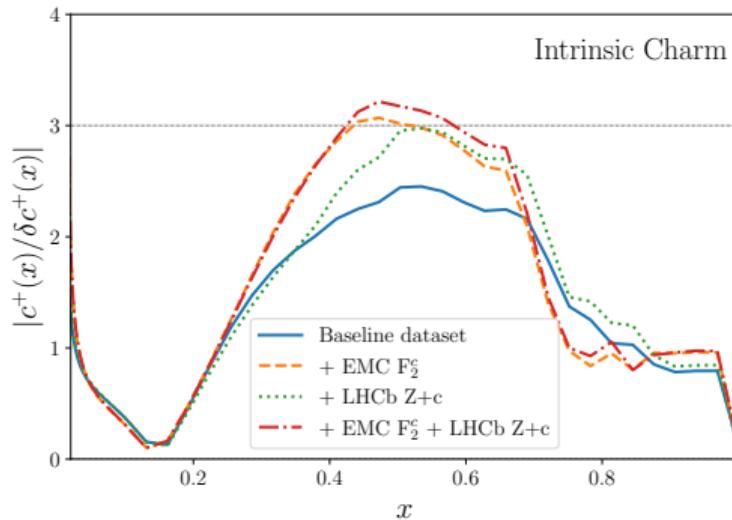
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# Z+charm @ LHCb [PRL128.082001]



- ▶ assuming intrinsic charm predicts better recent measurement
- ▶ reweighting is consistent

# Significance

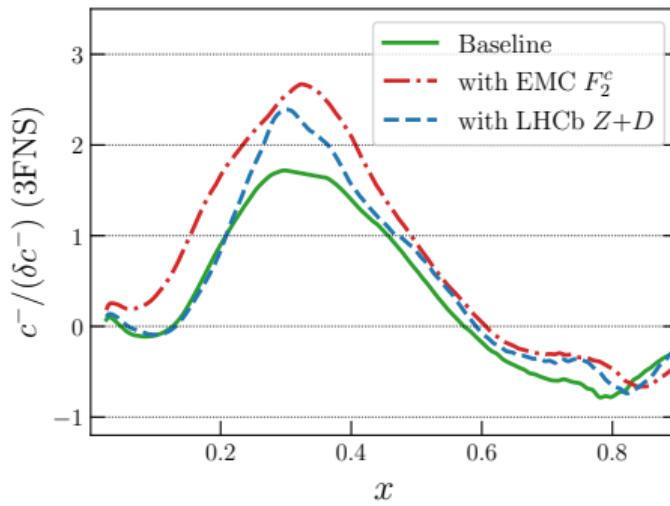
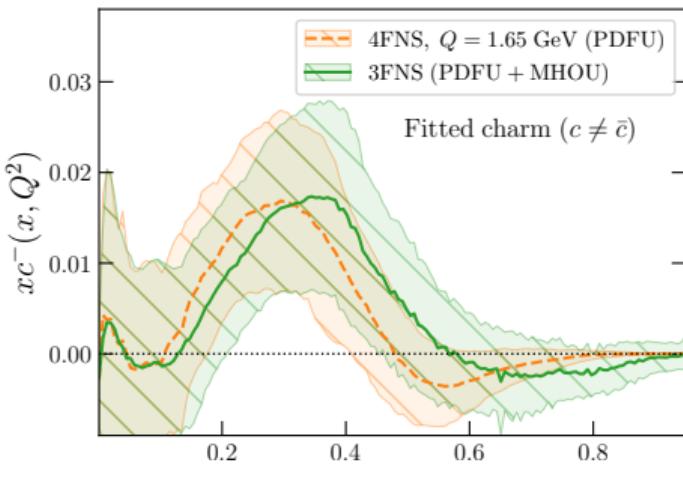


- ▶ we find a  $3\sigma$  evidence of intrinsic charm
- ▶ result is stable with mass variation, dataset variation

The intrinsic charm quark valence  
distribution of the proton [2311.00743]

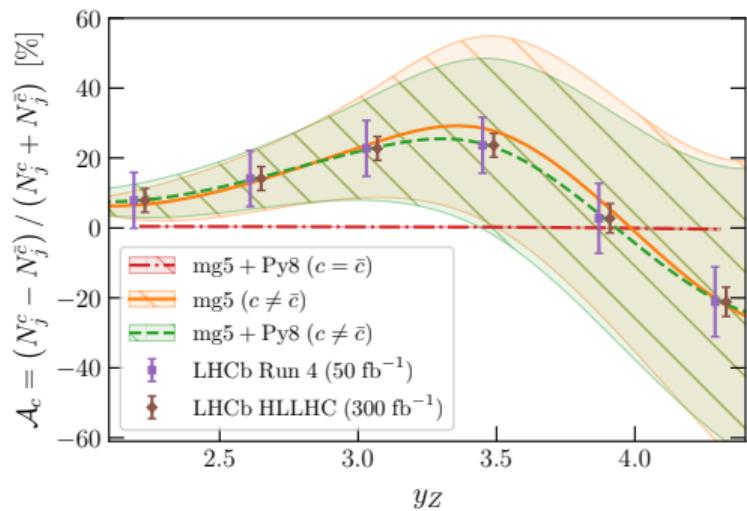
# Fitting the valence charm distribution

- ▶ fit in addition valence charm distribution  $c^- = c - \bar{c}$
- ▶ perturbative charm comes from pair production
- ▶  $\Rightarrow$  asymmetric charm must be intrinsic



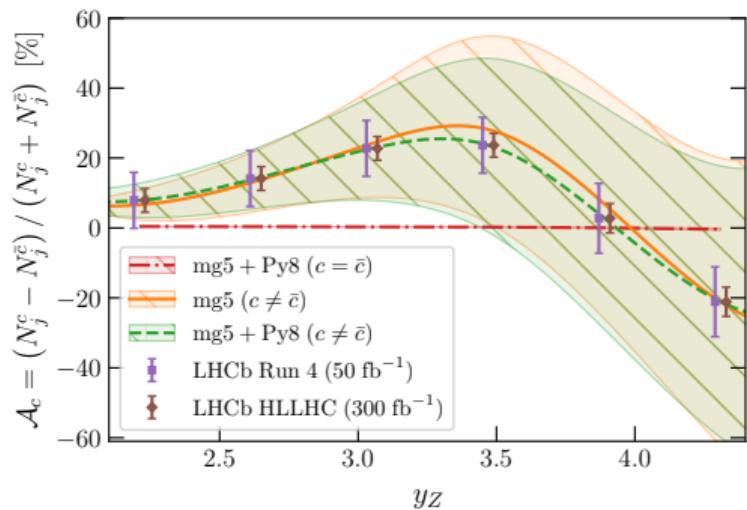
# Measuring the valence charm distribution

Charm asymmetries in Z+c @ LHCb

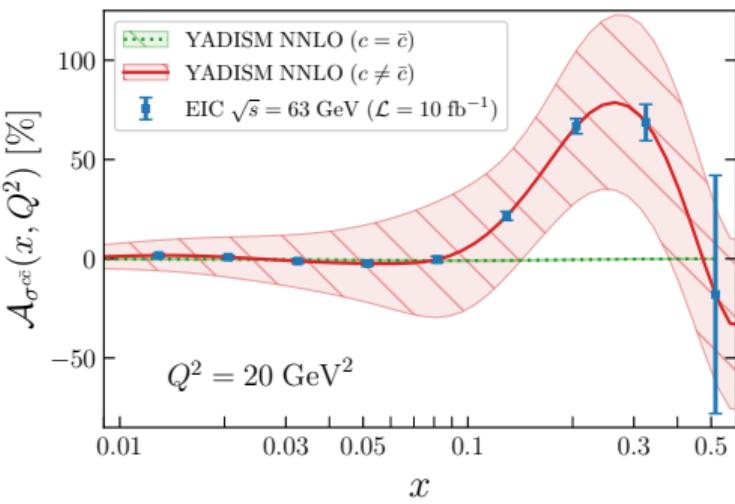


# Measuring the valence charm distribution

Charm asymmetries in Z+c @ LHCb



Charm-tagged DIS at the EIC



# Summary

# Summary

- ▶ we fit charm to experimental data
- ▶ we remove perturbative charm component
- ▶ intrinsic charm is non-zero with  $3\sigma$  significance
- ▶ more data  $\rightarrow c^+$  with  $5\sigma$  significance
  
- ▶ finding a valence charm distribution signals intrinsic charm
- ▶ with current data we can not give a clear answer
- ▶ we need experimental measurements sensitive to valence charm

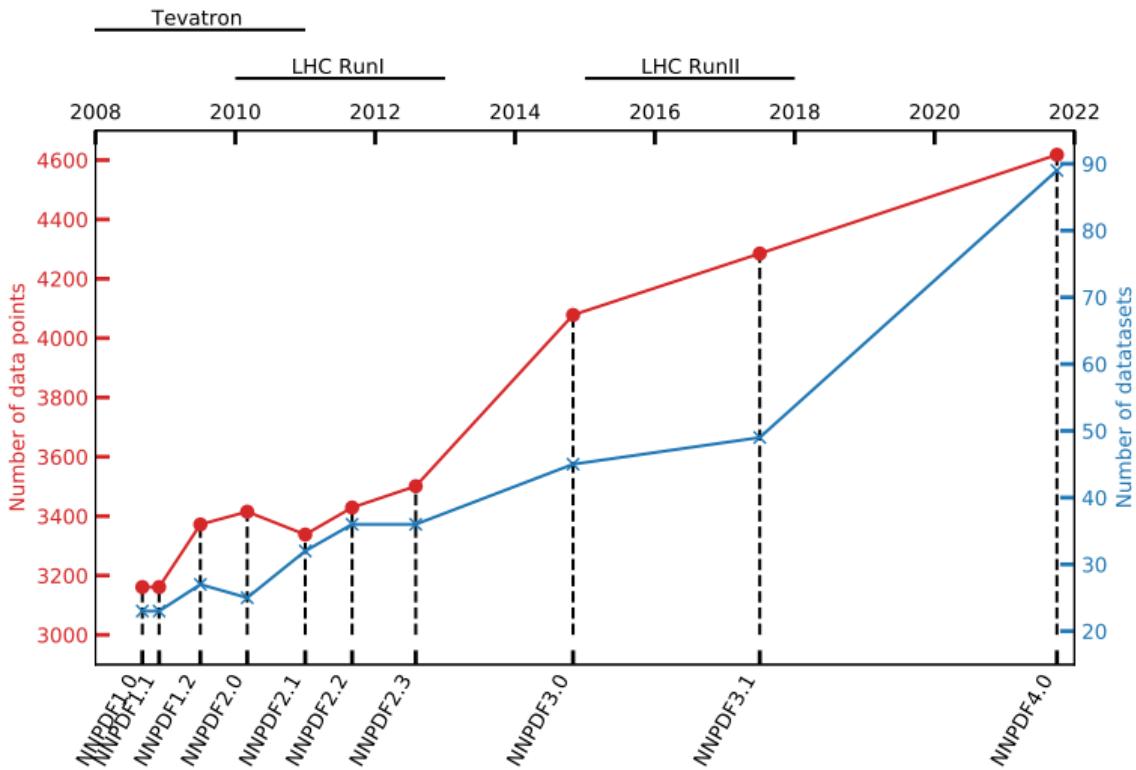
# Summary

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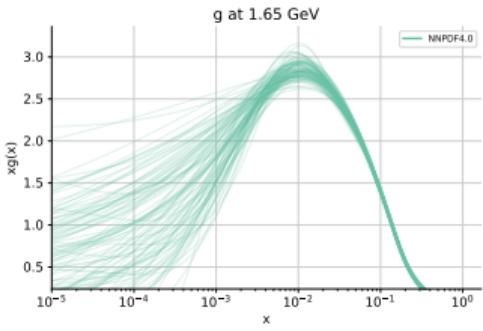
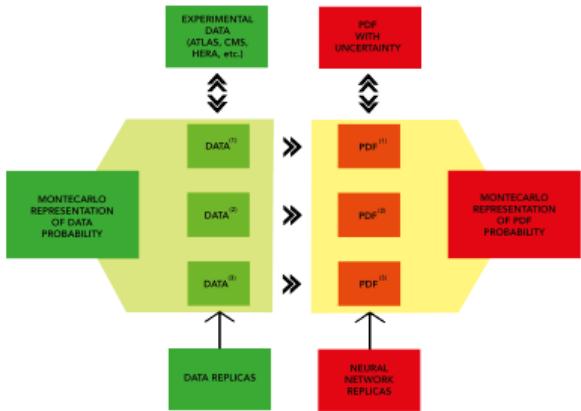
Danke! Thanks! Kiitos!

# Backup slides

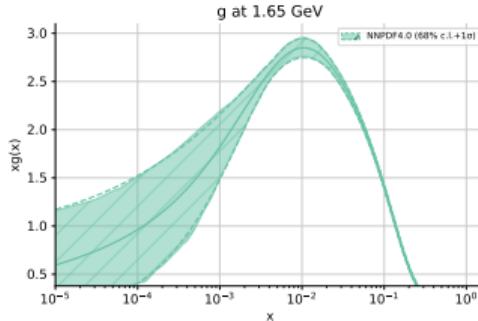
# Data: History



# Methodology: Replicas

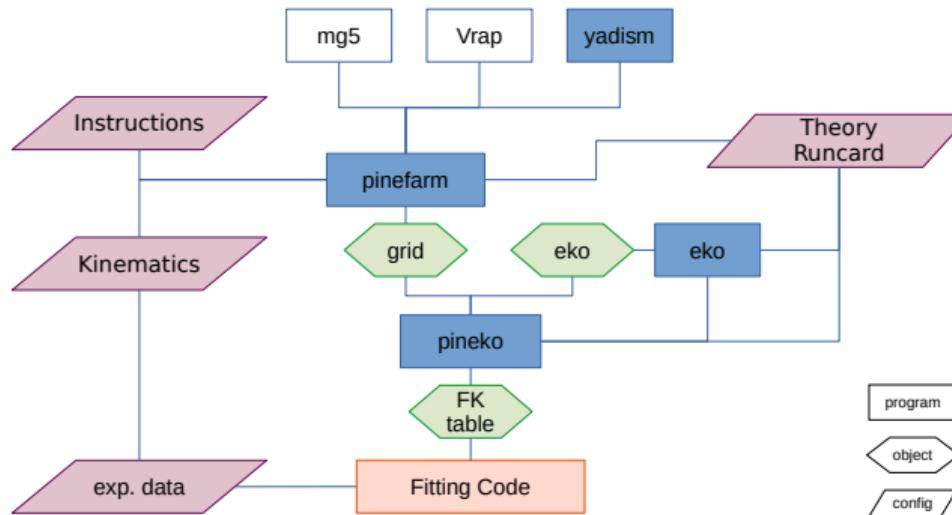


- ▶ Data is given by central values and covariance matrix
- ▶ generate Monte Carlo data replicas which as an ensemble represent the experiment
- ▶ fit one PDF replica to each data replica
- ▶ ⇒ ensemble of PDF replica



# New Theory Prediction Pipeline Pineline [2302.12124]

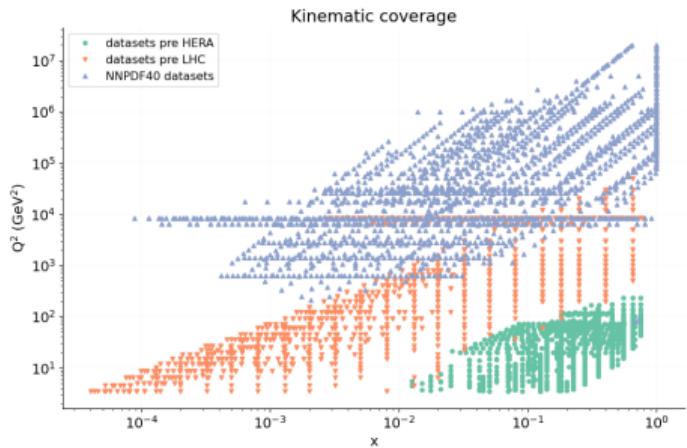
Produce FastKernel (FK) tables!



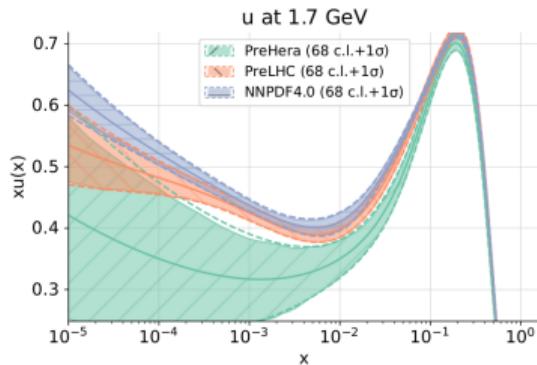
The workhorse in the background: PineAPPL

# Checks: Future Tests [Acta Phys.Polon.B52.243]

Go to the past and look into the (back then) future!

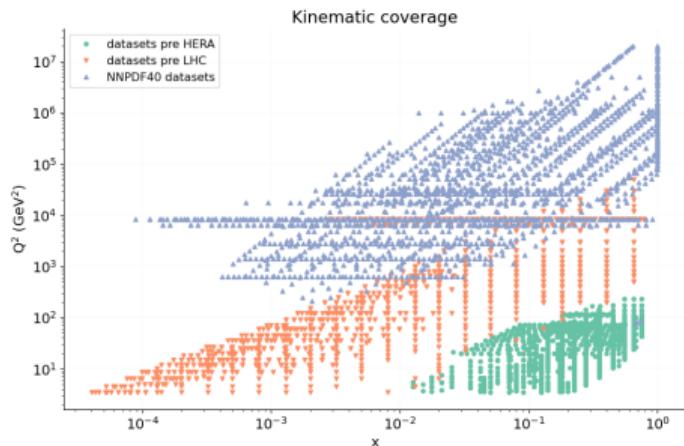


(dataset)	$\chi^2/N$ (only exp. covmat)		
	NNPDF4.0	pre-LHC	pre-Hera
pre-HERA	1.09	1.01	0.90
pre-LHC	1.21	1.20	23.1
NNPDF4.0	1.29	3.30	23.1

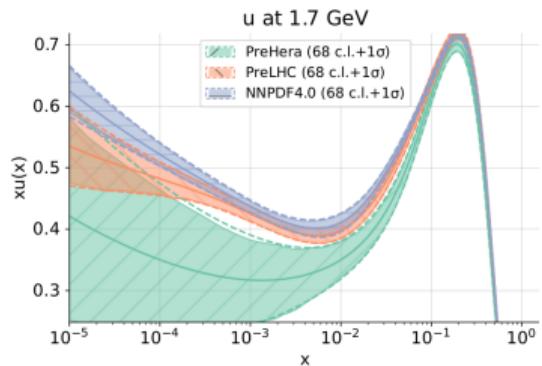


# Checks: Future Tests [Acta Phys.Polon.B52.243]

Go to the past and look into the (back then) future!



(dataset)	$\chi^2/N$ (exp. and PDF covmat)	NNPDF4.0	pre-LHC	pre-Hera
pre-HERA				0.86
pre-LHC			1.17	1.22
NNPDF4.0	1.12	1.30	1.38	



- ▶ without data PDF errors have to be big
- ▶ with PDF errors the total uncertainty increases, and accommodates for difference between predictions and new data

# Checks: Closure Tests [EPJC82.330]

Fake a universe with known input assumptions

1. Assume a “true” underlying PDF (e.g. a single PDF replica)
2. Produce fake data distributed accordingly
3. Perform a fit to this fake data

Observe statistical estimators (e.g. bias and variance)

→ Is the truth within one sigma in 68% of cases?

---

$$\sqrt{\text{bias}/\text{variance}} \quad \xi_{1\sigma}^{(\text{data})}$$

---

$$1.03 \pm 0.05 \quad 0.68 \pm 0.02$$

# QCD Evolution

For (forward) evolution across a matching scale  $\mu_h^2$ :

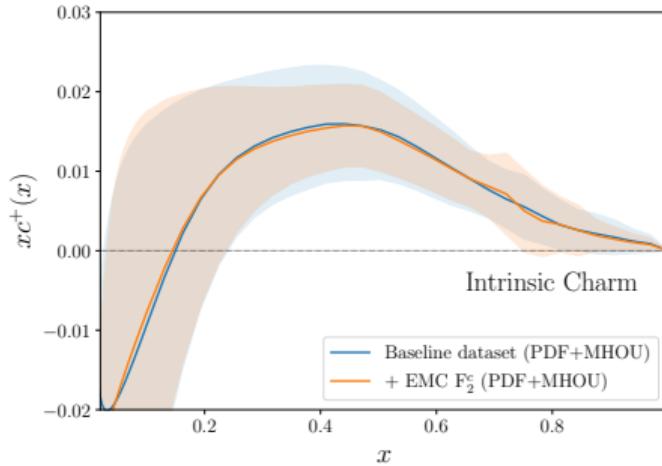
$$\tilde{\mathbf{f}}^{(n_f+1)}(\mu_{F,1}^2) = \tilde{\mathbf{E}}^{(n_f+1)}(\mu_{F,1}^2 \leftarrow \mu_h^2) \mathbf{R}^{(n_f)} \tilde{\mathbf{A}}^{(n_f)}(\mu_h^2) \tilde{\mathbf{E}}^{(n_f)}(\mu_h^2 \leftarrow \mu_{F,0}^2) \tilde{\mathbf{f}}^{(n_f)}(\mu_{F,0}^2) \quad (1)$$

with  $\mathbf{R}^{(n_f)}$  a flavor rotation matrix and  $\tilde{\mathbf{A}}^{(n_f)}(\mu_h^2)$  the operator matrix elements (partially known up to N<sup>3</sup>LO)

for backward evolution:

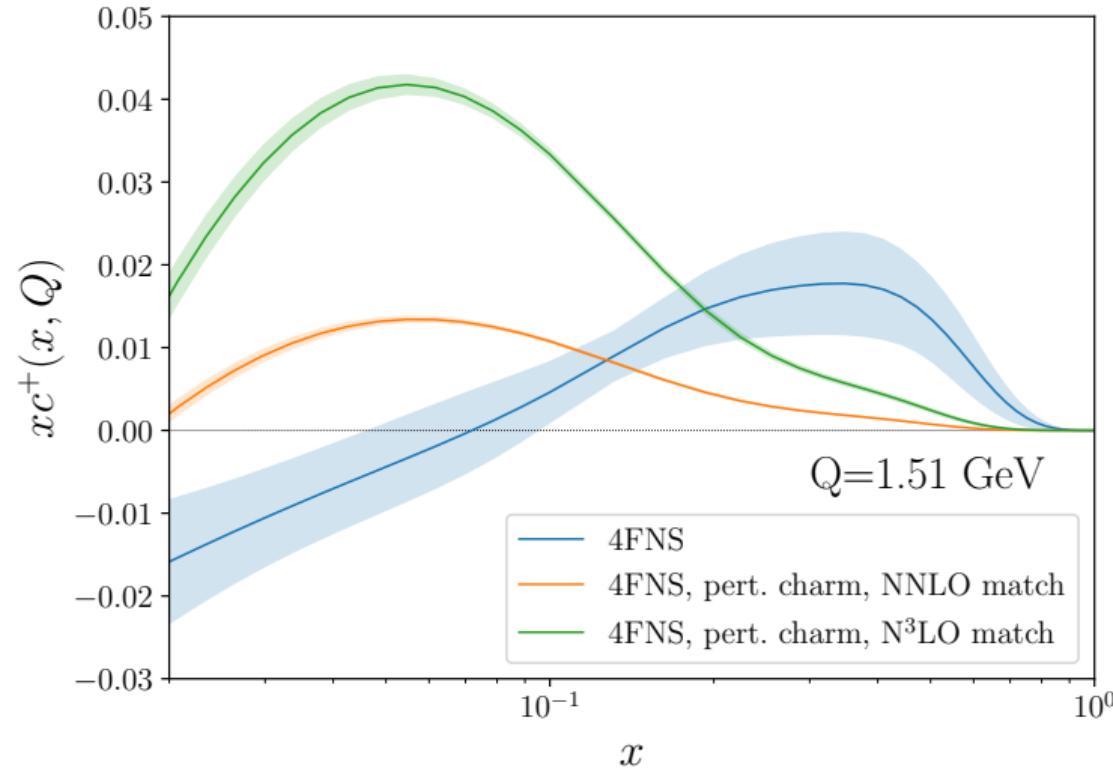
- ▶ invert  $\tilde{\mathbf{E}}^{(n_f)}$ : simple (invert RGE flow) ✓
- ▶ invert  $\mathbf{R}^{(n_f)}$ : simple (static matrix) ✓
- ▶ invert  $\tilde{\mathbf{A}}^{(n_f)}$ : expanded or exact

# EMC [NPB461.181]

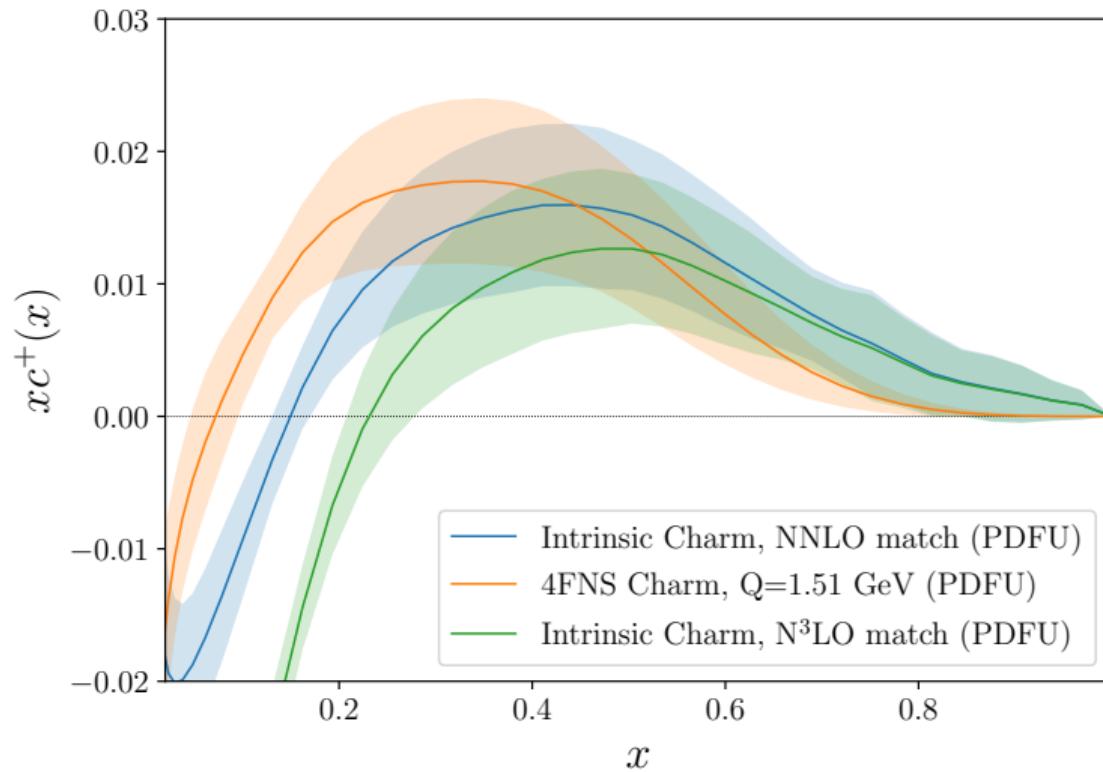


- ▶ direct measurement of  $F_2^c$
- ▶ evidence for intrinsic charm claimed, but experiment disputed
- ▶ adding EMC data is consistent

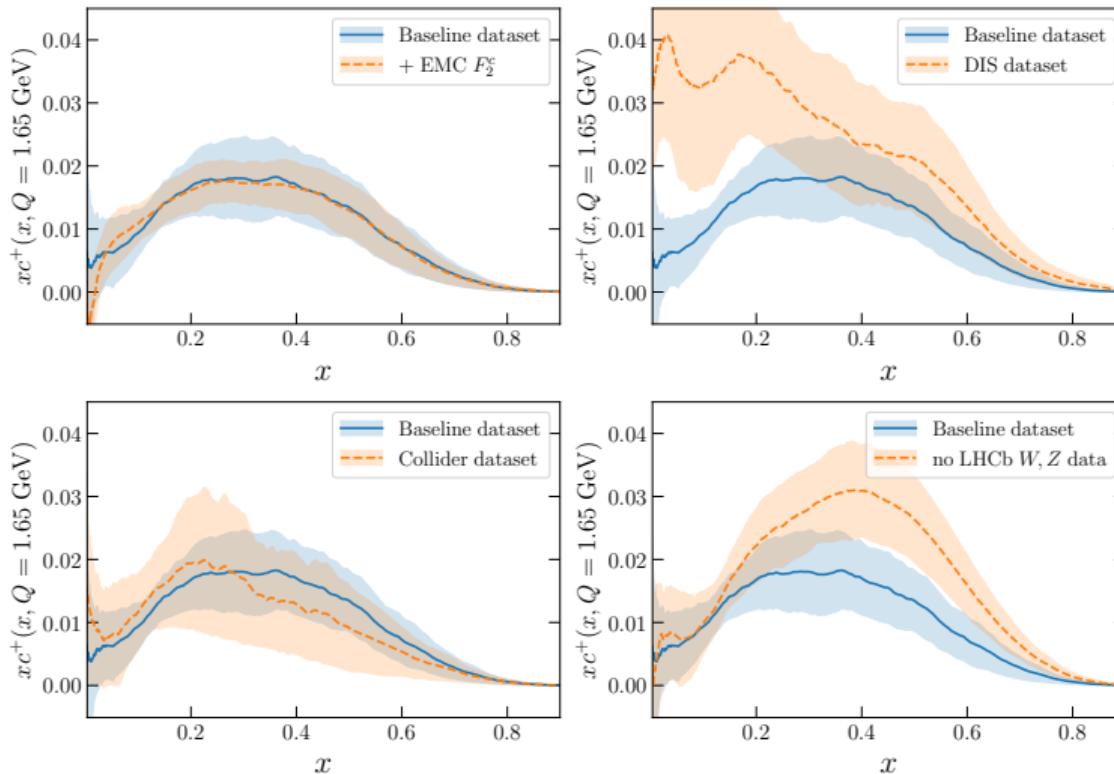
# IC vs. PC



# IC - uncertainties splitted



# IC - dataset variation



# IC - mass dependency

