

Hadrons with Strangeness and Charm in Dense Matter

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Uncover the Phase Diagram of Dense QCD

Neutron Star Astrophysics & Exotic Hadrons

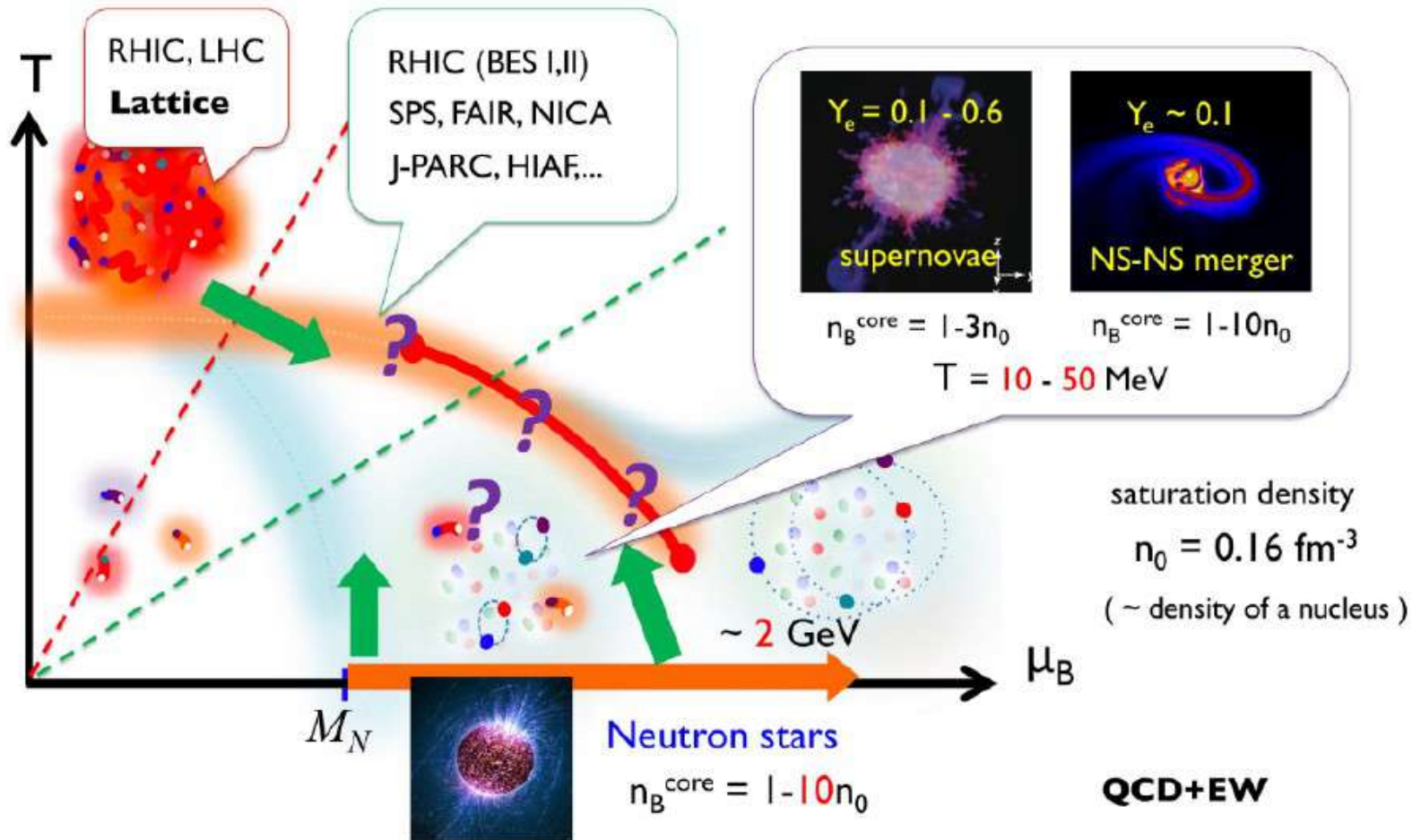


Figure from T. Kojo arXiv:1912.05326 [nucl-th]

Uncover the Phase Diagram of Dense QCD

Neutron Star Astrophysics & Strange Hadrons

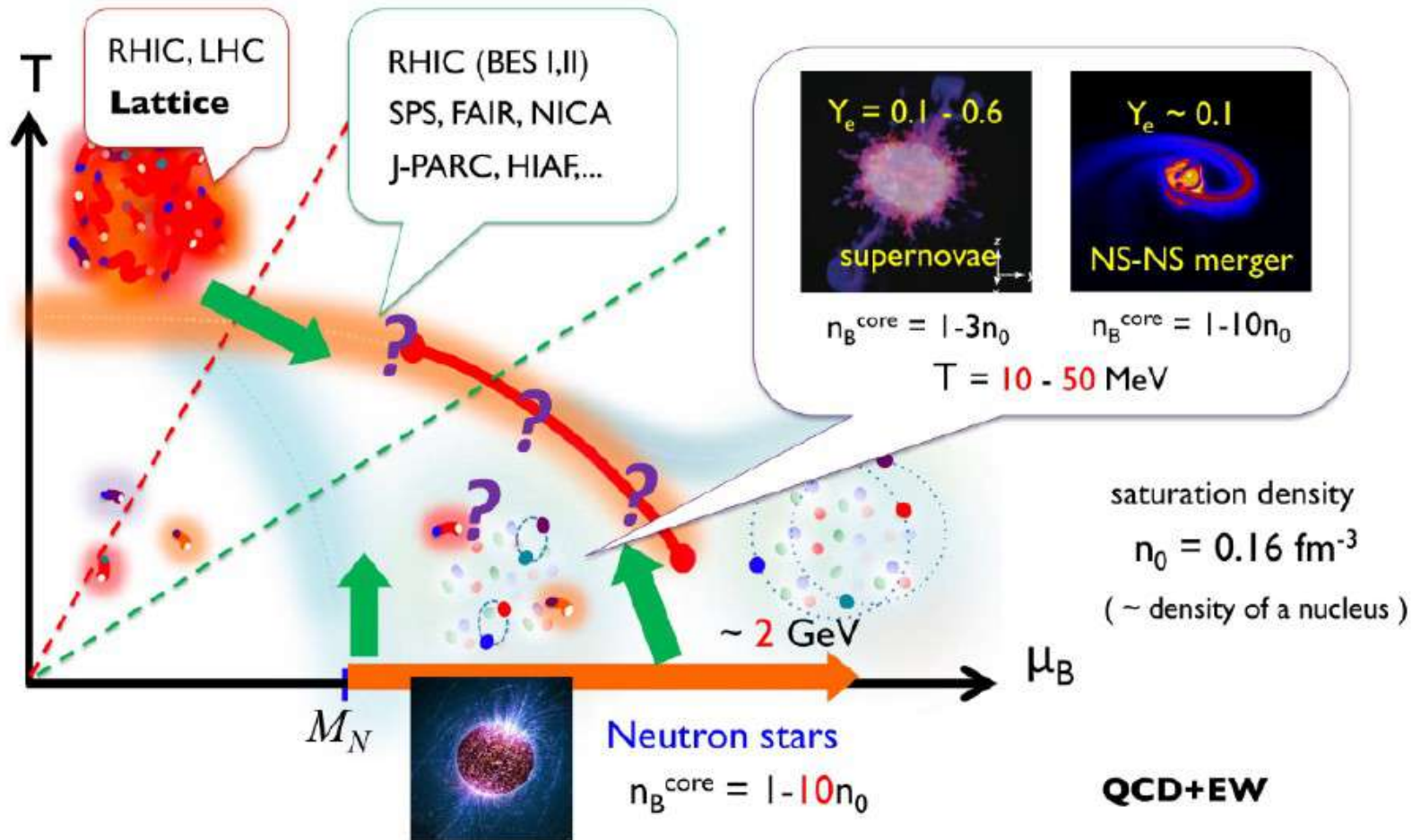


Figure from T. Kojo arXiv:1912.05326 [nucl-th]

Uncover the Phase Diagram of Dense QCD

Neutron Star Astrophysics & H(S)exaquarks

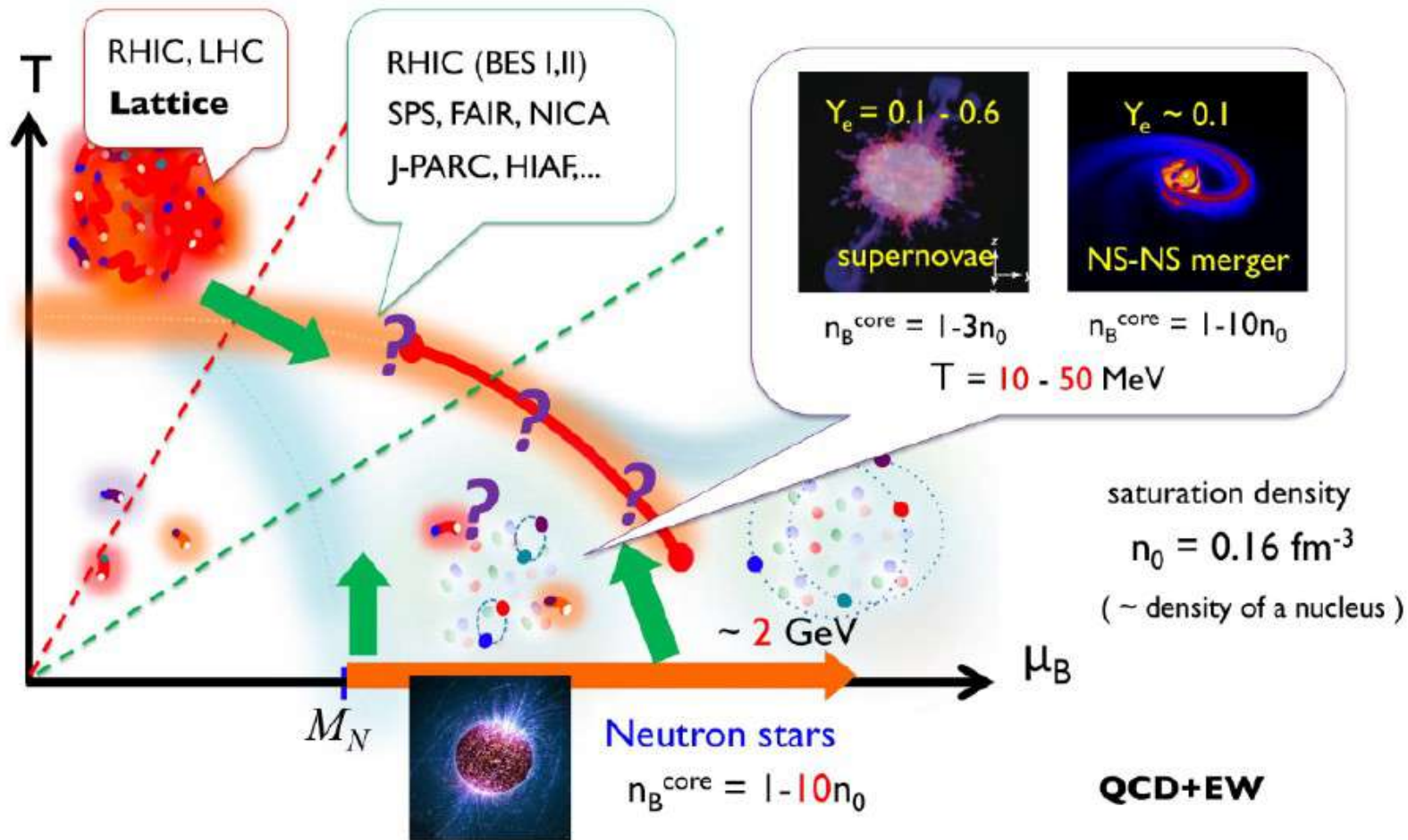


Figure from T. Kojo arXiv:1912.05326 [nucl-th]

Phase Diagram of Dense QCD and Neutron Star Astrophysics

- DD2 approach to relativistic mean field theory with density-dependent couplings
- Relativistic density functional for color superconducting quark matter with confinement
- Hyperon puzzle, sexaquark dilemma and the „Berlin Wall“ constraint for neutron stars

The Sexaquark $S(uuddss)$ & Dense QCD in Neutron Stars

The Hexaquark $d^*(2380)$ and a Charmed Hexaquark

H(S)exaquarks in pA Collisions

Conclusions

Neutron star phenomenology from TOV eqns.

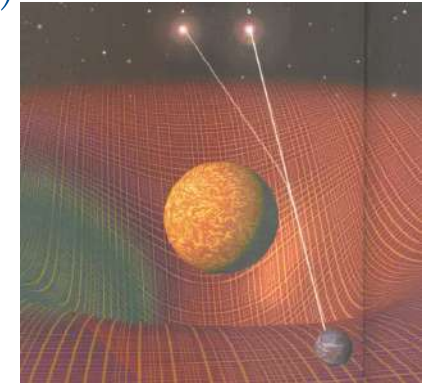
There is a 1:1 correspondence EOS \leftrightarrow M(R)

Tolman-Oppenheimer-Volkoff (TOV) equations



Einstein equations

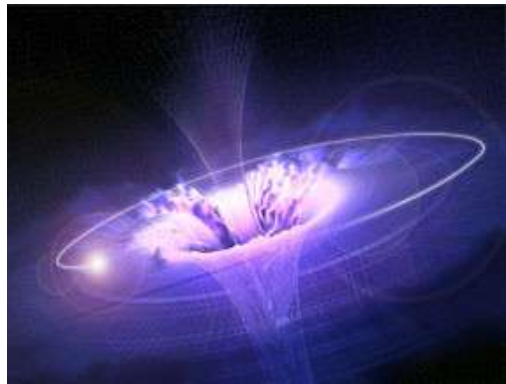
$$G_{\mu\nu} = 8\pi G T_{\mu\nu}$$



Non-rotating, spherical masses \rightarrow Schwarzschild

Metrics

$$ds^2 = -\left(1 - \frac{2M}{r}\right)dt^2 + \left(1 - \frac{2M}{r}\right)^{-1}dr^2 + r^2d\Omega^2$$



Tolman-Oppenheimer-Volkoff eqs.*) for structure and stability of spherical compact stars

$$\frac{dP(r)}{dr} = -G \frac{m(r)\epsilon(r)}{r^2} \left(1 + \frac{P(r)}{\epsilon(r)}\right) \left(1 + \frac{4\pi r^3 P(r)}{m(r)}\right) \left(1 - \frac{2Gm(r)}{r}\right)^{-1}$$

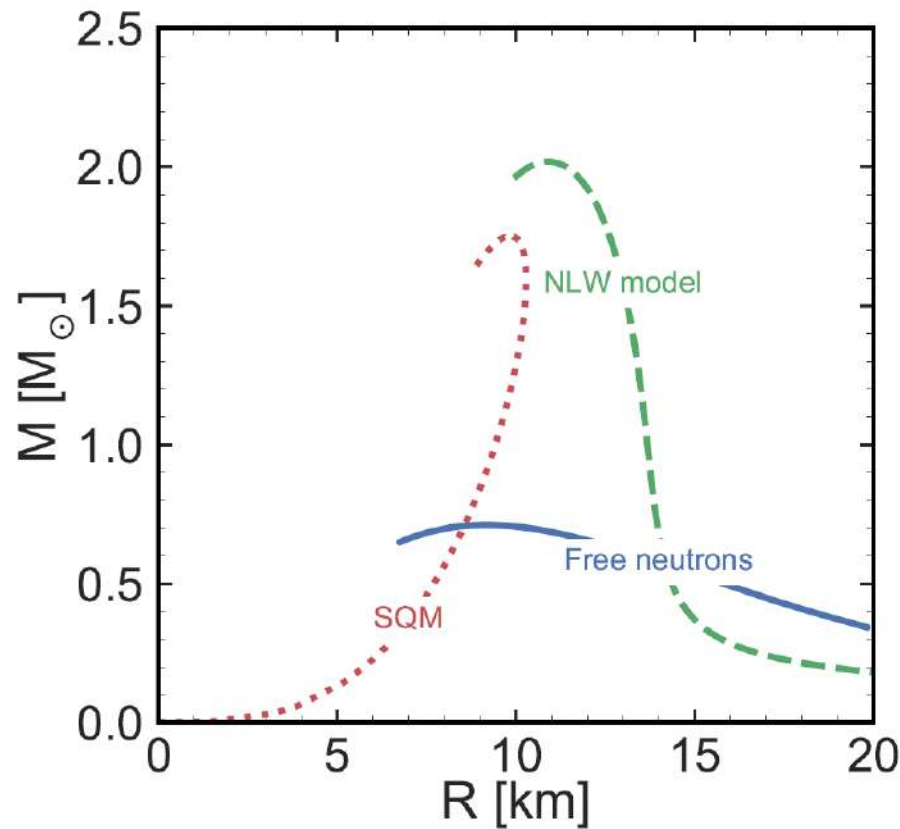
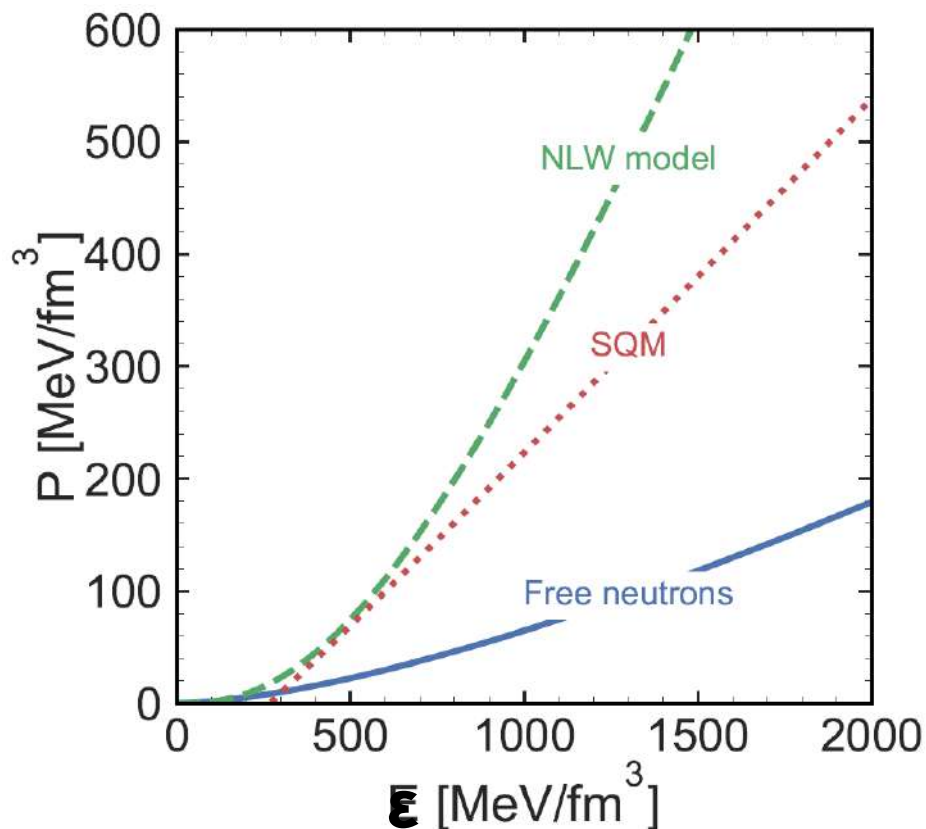
Newtonian case GR corrections from EoS and metrics

*)R.C. Tolman, Phys. Rev. 55 (1939) 364; J.R. Oppenheimer, G.M. Volkoff, ibid., 374

Neutron star phenomenology from TOV eqns.

There is a 1:1 correspondence EOS $P(\epsilon) \leftrightarrow M(R)$

Tolman-Oppenheimer-Volkoff (TOV) equations - solutions

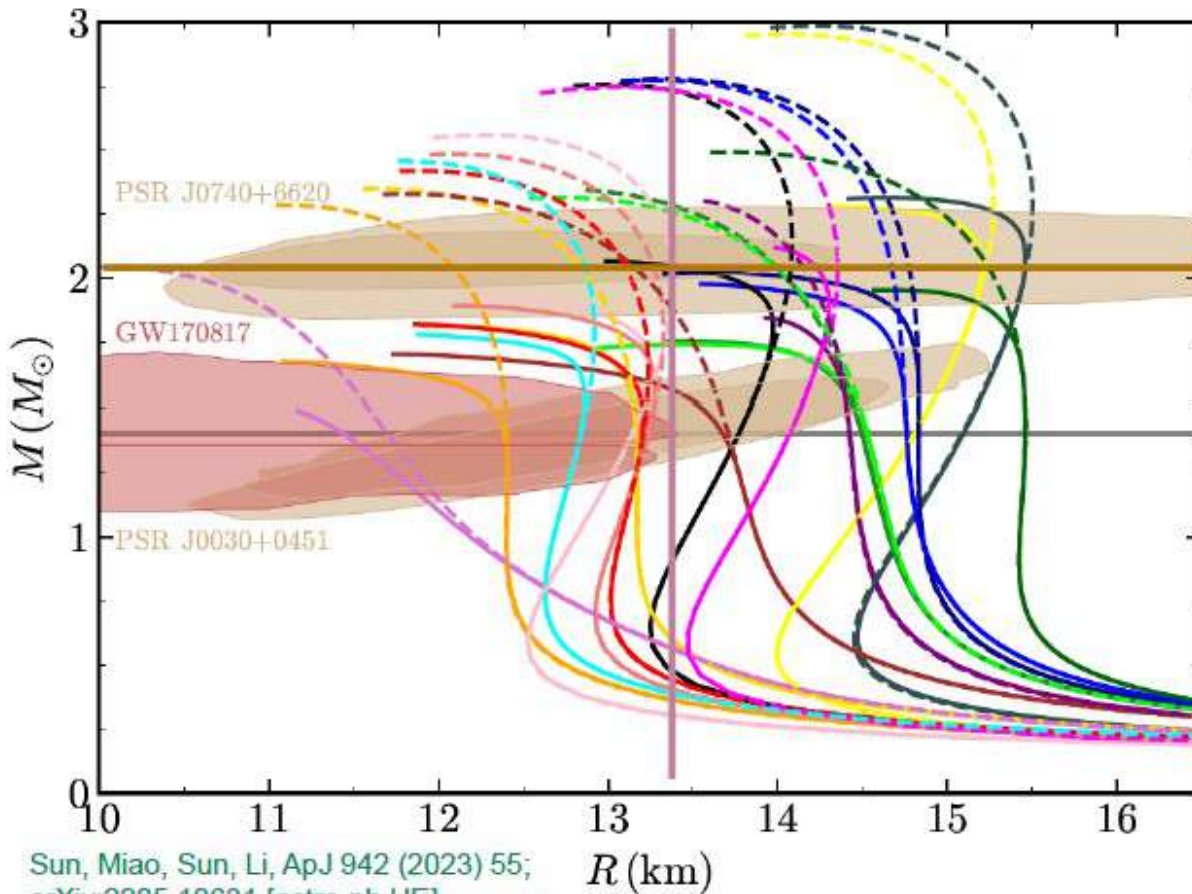


Stiffer equation of state \rightarrow larger radius and larger maximum mass

“Berlin wall” constraint for neutron stars

Realistic hadronic EOS (with strange baryons)

Tension with modern multi-messenger observations by LVC and NICER



Sun, Miao, Sun, Li, ApJ 942 (2023) 55; arXiv:2205.10631 [astro-ph.HE]

Examples for hadronic EoS without (dashed lines) and with (solid lines) strange baryons. EoS which fulfill the observational constraints should be left of the vertical line at 1.4 Msun and should cross the horizontal line for the minimal maximum mass at 2.01 Msun. There is no EoS of this sample which fulfills both constraints !!

- LHS
- RMF201
- NL3
- Hybrid
- TM2
- NLSV1
- PK1
- NL3 $\omega\rho$
- S271v6
- HC
- DD-LZ1
- DD-ME2
- DD2
- PKDD
- DD-PC1
- FKVW
- PC-PK1
- OMEG

From Tab. 2 select EoS which fulfill (w. Y) $70 < \Lambda_{1.4} < 580$ and check their M_{\max}

EoS	M_{\max}	EoS	M_{\max}
NL3 $\omega\rho$	1.974	DD2	1.935
DDLZ1	1.989	PKDD	1.781
DD-ME2	1.971	HC	1.828
OMEG	1.862		

“Berlin Wall” constraint for neutron stars?

Mass-radius diagram for purely hadronic EOS

Appearance of hyperons softens the EOS → Limitation for the maximum mass

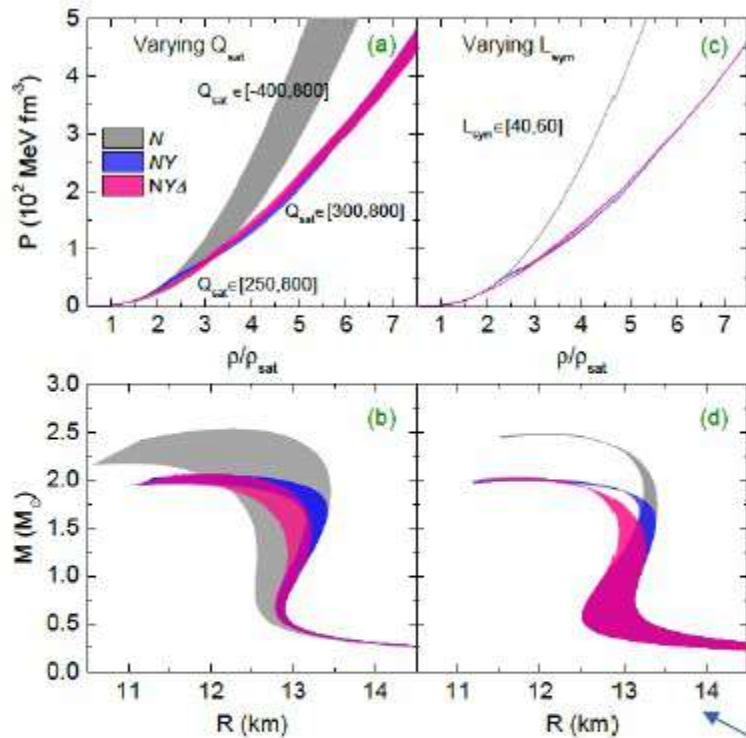


FIG. 4. EoS models and MR relations for N , NY , and $NY\Delta$ compositions of stellar matter. The bands are generated by varying the parameters Q_{sat} [MeV] (a, b) and L_{sym} [MeV] (c, d). The ranges of Q_{sat} and L_{sym} allowed by χ EFT and maximum mass constraints are indicated in the figures.

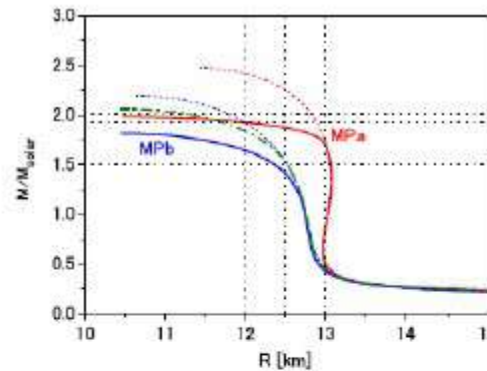


FIG. 7. Neutron-star masses as a function of the radius R . Solid (dashed) curves are with (without) hyperon (Λ and Σ^-) mixing for ESC+MPa and ESC+MPb. The dot-dashed curve for MPb is with Λ mixing only. Also see the caption of Fig. 3.

Yamamoto et al., Phys.Rev.C 96 (2017) 06580; arXiv:1708.06163 [nucl-th]

Yamamoto et al., Eur. Phys. J. A 52 (2016) 19; arXiv:1510.06099 [nucl-th]

Ji & Sedrakian, Phys. Rev. C 100 (2019) 015809; arXiv:1903.06057 [astro-ph.HE]

Examples for realistic hadronic EoS which suggest a Berlin Wall is inferior to the line $M = 2.0 M_{\text{sun}}$

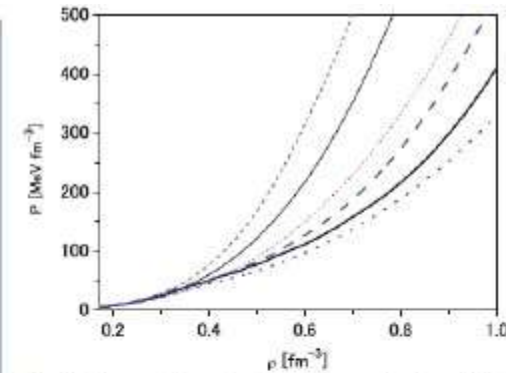


Fig. 8. Pressure P as a function of baryon density ρ . Thick (thin) curves are with (without) hyperon mixing. Solid, dashed and dotted curves are for MPa, MPa $^+$ and MPb.

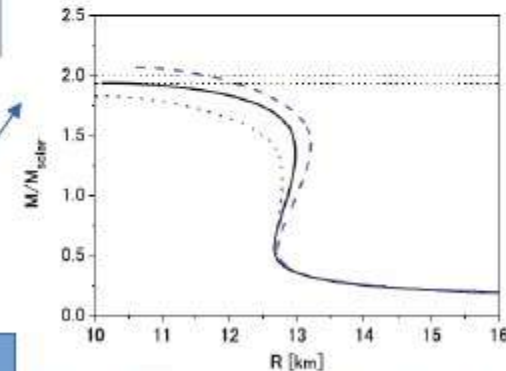
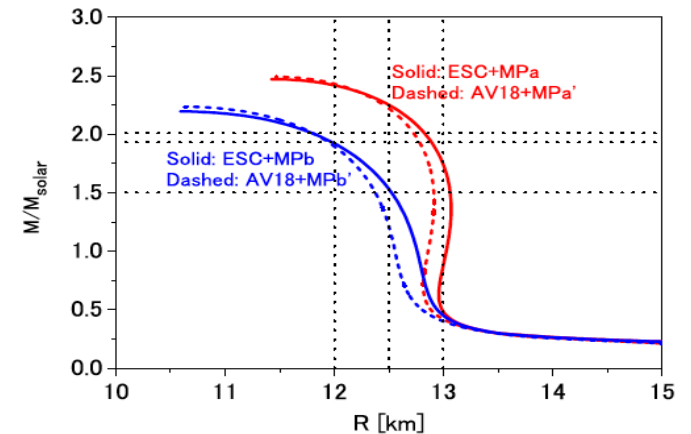
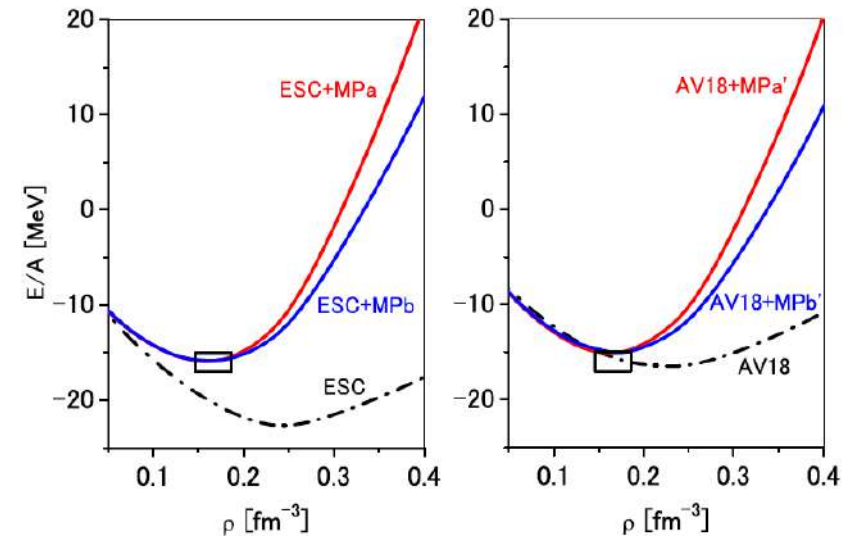
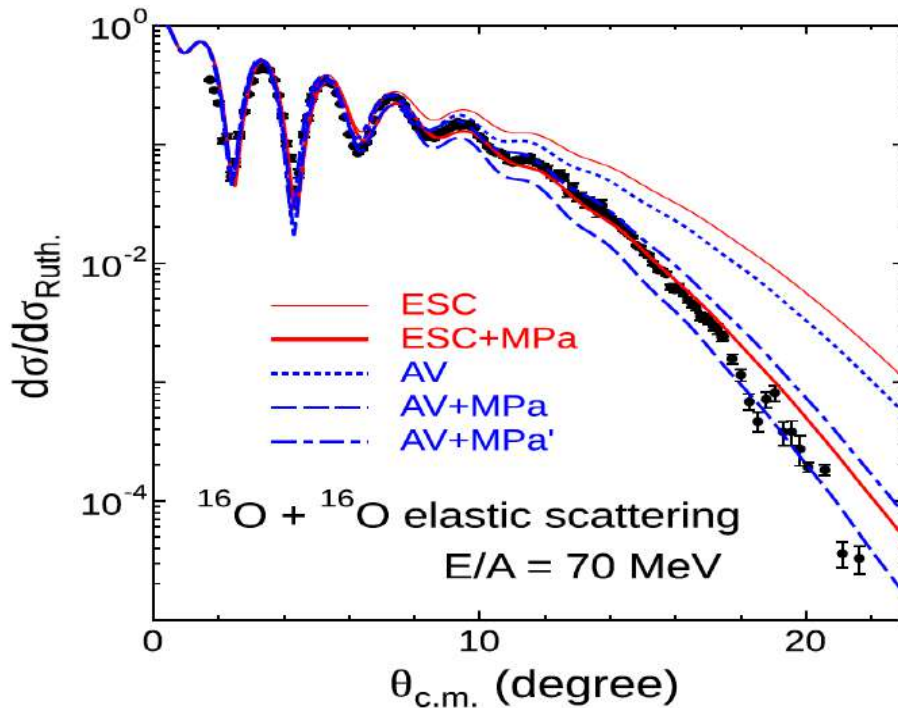


Fig. 9. Neutron-star masses as a function of the radius R . Solid, dashed and dotted curves are for MPa, MPa $^+$ and MPb. Two dotted lines show the observed mass $(1.97 \pm 0.04)M_{\odot}$ of J1614-2230.

“Berlin wall” constraint for neutron stars

Realistic hadronic EOS (with strange baryons)

Y. Yamamoto, H. Togashi, T. Tamagawa, T. Furumoto, N. Yasutake, T. Rijken, PRC 96 (2017)

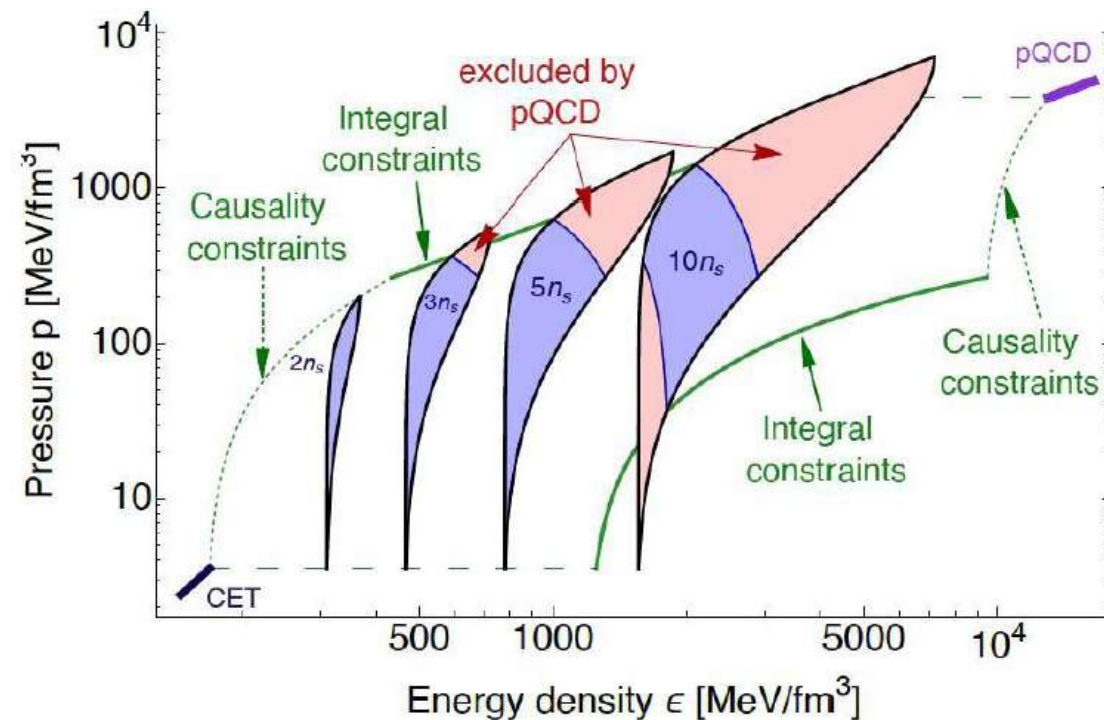


Short-range multi-pomeron exchange potential (MPP) added to AV18 potential gives significant improvement of large-angle scattering cross section (s.a.) and the Nuclear saturation properties, when compared to APR.
→ Neutron star radii $R(M < 2 M_{sun}) > 12$ km !!

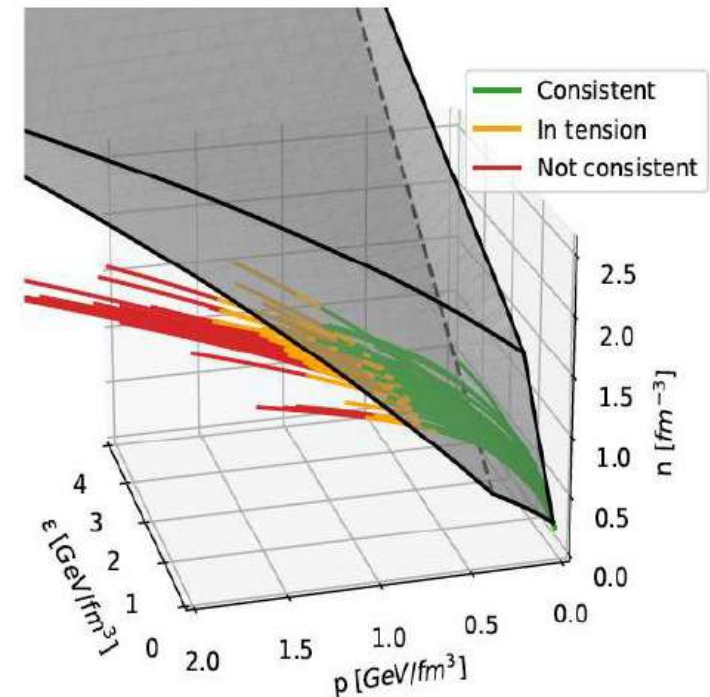
Breaking the “Berlin wall” constraint

With Bayesian analyses and hybrid EOS

Neutron star EoS constraint from pQCD



Consistency check for neutron star EoS from the ComPOSE library



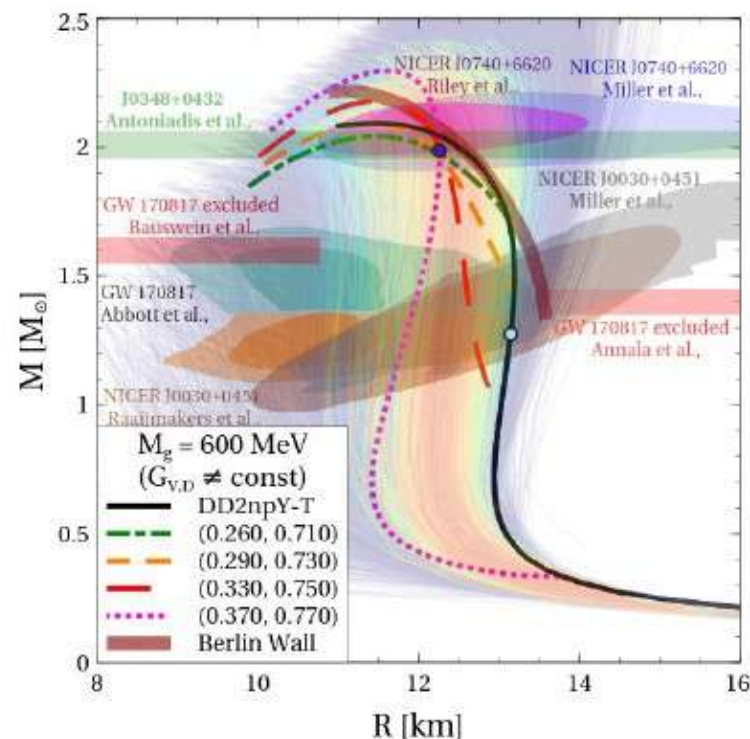
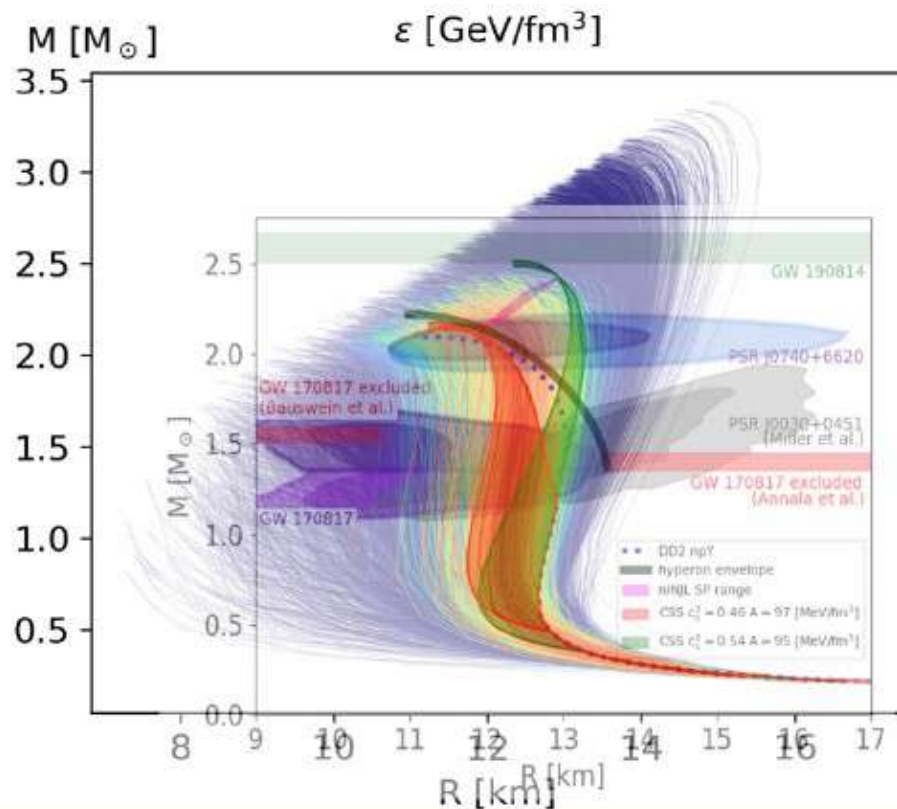
O. Komoltsev and A. Kurkela, Phys. Rev. D 128 (2022) 202701

Result: Not all EoS fulfill the consistency check with pQCD asymptotics! pQCD important for NS!

Breaking the “Berlin wall” constraint

With Bayesian analyses and hybrid EOS

M(R) curves generated by causality, thermodynamic stability and pQCD limit



The conjectured “Berlin Wall” overlaid to the Fig. 2 from Gorda, Komoltsev & Kurkela [2204.11877 [nucl-th]] and hybrid EoS with quark matter described by a CSS model (left) and a confining relativistic density functional (right).

Relativistic density functionals for QCD

String-flip model for quark matter



Röpke, Blaschke, Schulz, PRD34 (1986) 3499

$$\mathcal{Z} = \int \mathcal{D}\bar{q}\mathcal{D}q \exp \left\{ \int_0^\beta d\tau \int_V d^3x [\mathcal{L}_{\text{eff}} + \bar{q}\gamma_0\hat{\mu}q] \right\}, \quad q = \begin{pmatrix} q_u \\ q_d \end{pmatrix}, \quad \hat{\mu} = \text{diag}(\mu_u, \mu_d)$$

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{free}} - U(\bar{q}q, \bar{q}\gamma_0q), \quad \mathcal{L}_{\text{free}} = \bar{q} \left(-\gamma_0 \frac{\partial}{\partial \tau} + i\vec{\gamma} \cdot \vec{\nabla} - \hat{m} \right) q, \quad \hat{m} = \text{diag}(m_u, m_d)$$

General nonlinear functional of quark density bilinears: scalar, vector, isovector, diquark ...

Expansion around the expectation values:

$$U(\bar{q}q, \bar{q}\gamma_0q) = U(n_s, n_v) + (\bar{q}q - n_s)\Sigma_s + (\bar{q}\gamma_0q - n_v)\Sigma_v + \dots,$$

$$\langle \bar{q}q \rangle = n_s = \sum_{f=u,d} n_{s,f} = - \sum_{f=u,d} \frac{T}{V} \frac{\partial}{\partial m_f} \ln \mathcal{Z}, \quad \Sigma_s = \left. \frac{\partial U(\bar{q}q, \bar{q}\gamma_0q)}{\partial (\bar{q}q)} \right|_{\bar{q}q=n_s} = \frac{\partial U(n_s, n_v)}{\partial n_s},$$

$$\langle \bar{q}\gamma_0q \rangle = n_v = \sum_{f=u,d} n_{v,f} = \sum_{f=u,d} \frac{T}{V} \frac{\partial}{\partial \mu_f} \ln \mathcal{Z}, \quad \Sigma_v = \left. \frac{\partial U(\bar{q}q, \bar{q}\gamma_0q)}{\partial (\bar{q}\gamma_0q)} \right|_{\bar{q}\gamma_0q=n_v} = \frac{\partial U(n_s, n_v)}{\partial n_v}$$

$$\mathcal{Z} = \int \mathcal{D}\bar{q}\mathcal{D}q \exp \{ \mathcal{S}_{\text{quasi}}[\bar{q}, q] - \beta V \Theta[n_s, n_v] \}, \quad \Theta[n_s, n_v] = U(n_s, n_v) - \Sigma_s n_s - \Sigma_v n_v$$

$$\mathcal{S}_{\text{quasi}}[\bar{q}, q] = \beta \sum_n \sum_{\vec{p}} \bar{q} G^{-1}(\omega_n, \vec{p}) q, \quad G^{-1}(\omega_n, \vec{p}) = \gamma_0(-i\omega_n + \hat{\mu}^*) - \vec{\gamma} \cdot \vec{p} - \hat{m}^*$$

$$\mathcal{Z} = \int \mathcal{D}\bar{q}\mathcal{D}q \exp \{ \mathcal{S}_{\text{quasi}}[\bar{q}, q] - \beta V \Theta[n_s, n_v] \}, \quad \Theta[n_s, n_v] = U(n_s, n_v) - \Sigma_s n_s - \Sigma_v n_v$$

$$\mathcal{Z}_{\text{quasi}} = \int \mathcal{D}\bar{q}\mathcal{D}q \exp \{ \mathcal{S}_{\text{quasi}}[\bar{q}, q] \} = \det[\beta G^{-1}], \quad \ln \det A = \text{Tr} \ln A$$

$$P_{\text{quasi}} = \frac{T}{V} \ln \mathcal{Z}_{\text{quasi}} = \frac{T}{V} \text{Tr} \ln[\beta G^{-1}] \quad \text{"no sea" approximation ...}$$

$$= 2N_c \sum_{f=u,d} \int \frac{d^3p}{(2\pi)^3} \left\{ T \ln \left[1 + e^{-\beta(E_f^* - \mu_f^*)} \right] + T \ln \left[1 + e^{-\beta(E_f^* + \mu_f^*)} \right] \right\}$$

$$P_{\text{quasi}} = \sum_{f=u,d} \int \frac{dp}{\pi^2} \frac{p^4}{E_f^*} [f(E_f^* - \mu_f^*) + f(E_f^* + \mu_f^*)] \quad \begin{aligned} E_f^* &= \sqrt{p^2 + m_f^{*2}} \\ f(E) &= 1/[1 + \exp(\beta E)] \end{aligned}$$

$$P = \sum_{f=u,d} \int_0^{p_{F,f}} \frac{dp}{\pi^2} \frac{p^4}{E_f^*} - \Theta[n_s, n_v], \quad p_{F,f} = \sqrt{\mu_f^{*2} - m_f^{*2}}$$

$$\begin{aligned} \hat{m}^* &= \hat{m} + \Sigma_s \\ \hat{\mu}^* &= \hat{\mu} - \Sigma_v \end{aligned}$$

Selfconsistent densities

$$n_s = - \sum_{f=u,d} \frac{\partial P}{\partial m_f} = \frac{3}{\pi^2} \sum_{f=u,d} \int_0^{p_{F,f}} dp p^2 \frac{m_f^*}{E_f^*}, \quad n_v = \sum_{f=u,d} \frac{\partial P}{\partial \mu_f} = \frac{3}{\pi^2} \sum_{f=u,d} \int_0^{p_{F,f}} dp p^2 = \frac{p_{F,u}^3 + p_{F,d}^3}{\pi^2}.$$

Relativistic density functionals for QCD

String-flip model for quark matter

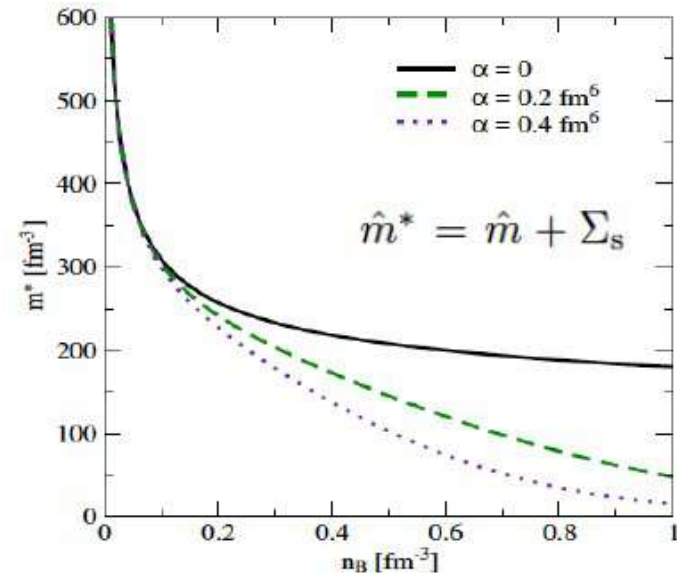
Density functional for the SFM

$$U(n_s, n_v) = D(n_v)n_s^{2/3} + an_v^2 + \frac{bn_v^4}{1 + cn_v^2},$$

Quark selfenergies

$$\Sigma_s = \frac{2}{3}D(n_v)n_s^{-1/3}, \quad \text{Quark "confinement"}$$

$$\Sigma_v = 2an_v + \frac{4bn_v^3}{1 + cn_v^2} - \frac{2bcn_v^5}{(1 + cn_v^2)^2} + \frac{\partial D(n_v)}{\partial n_v}n_s^{2/3}$$

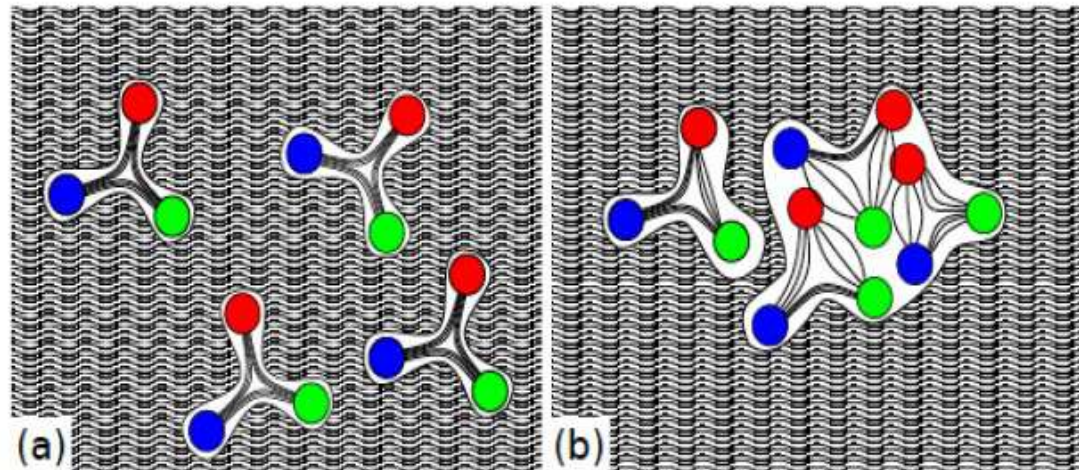


String tension & confinement due to dual Meissner effect (dual superconductor model)

$$D(n_v) = D_0\Phi(n_v)$$

Effective screening of the string tension in dense matter by a reduction of the available volume $\alpha = v|v|/2$

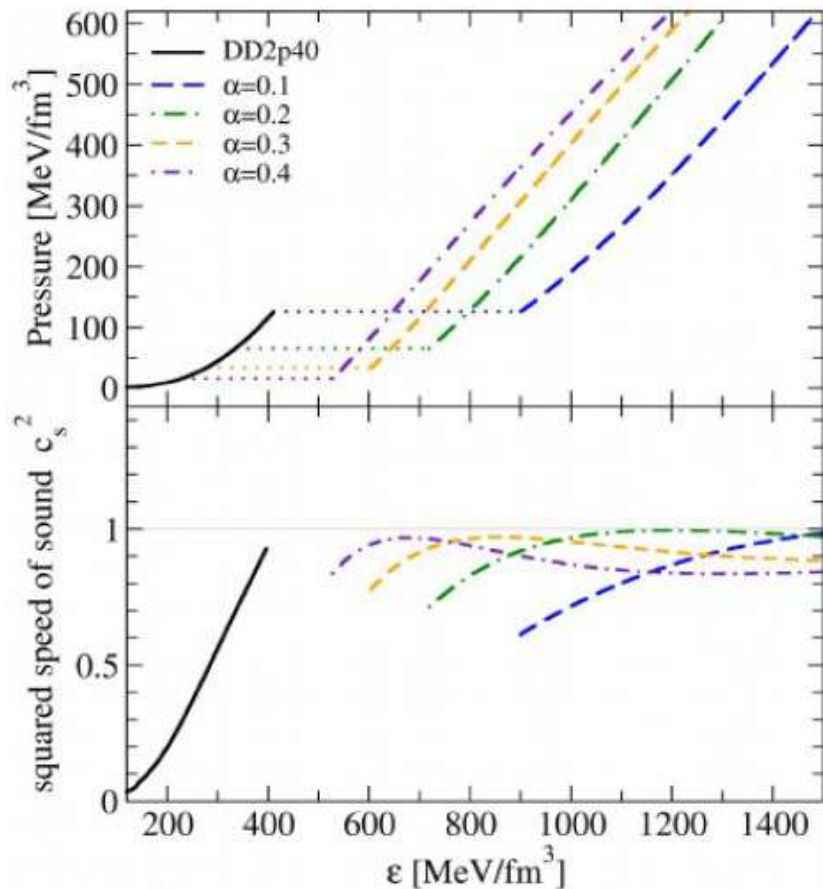
$$\Phi(n_B) = \begin{cases} 1, & \text{if } n_B < n_0 \\ e^{-\alpha(n_B - n_0)^2}, & \text{if } n_B > n_0 \end{cases}$$



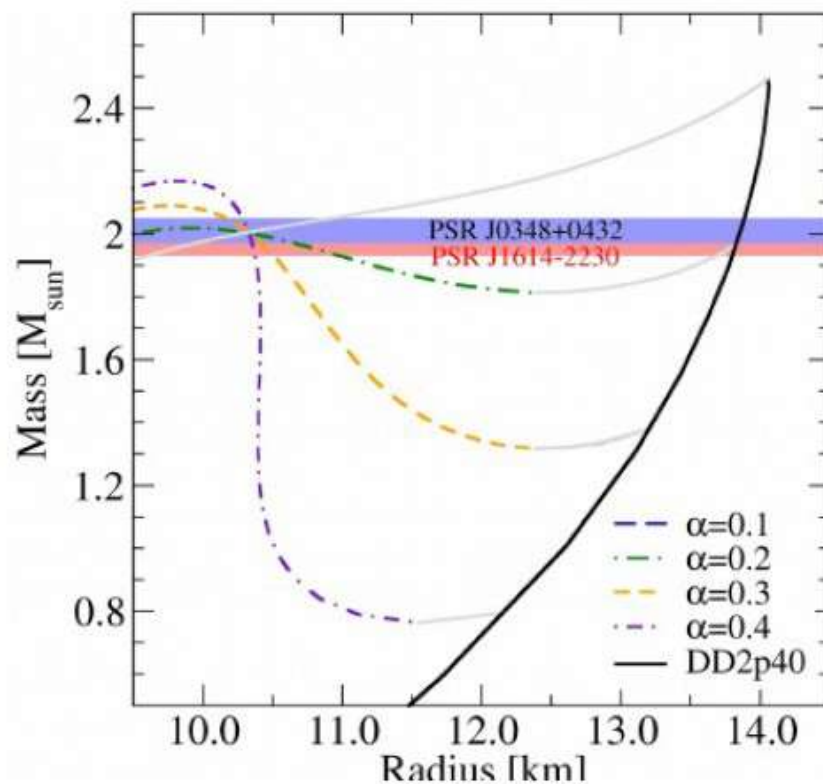
Relativistic density functionals for QCD

String-flip model for quark matter

Results for 1st order phase transition by Maxwell construction with DD2p40



third family \leftrightarrow mass twin stars

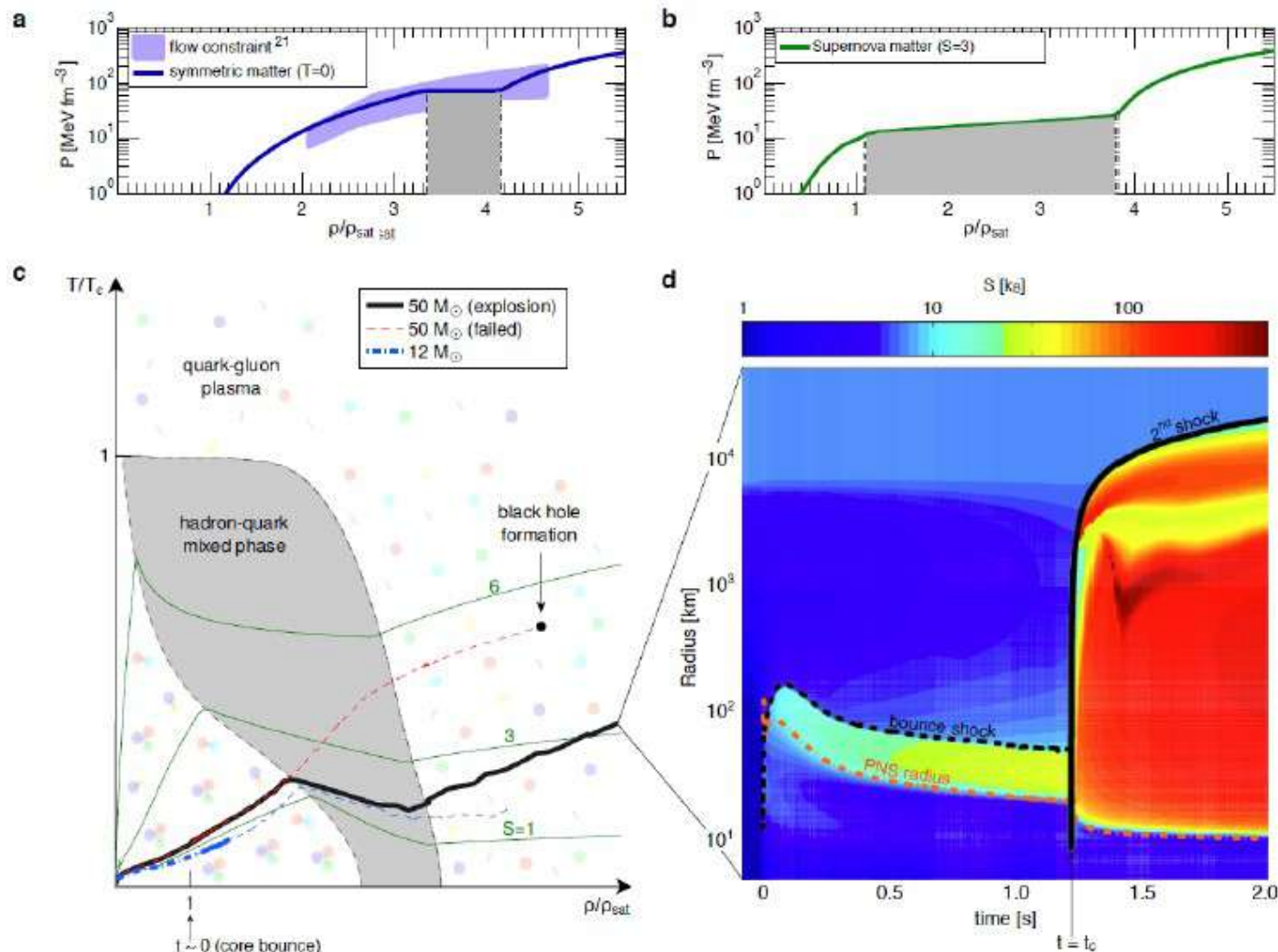


Kaltenborn, Bastian, Blaschke, arXiv:1701.04400

Phys. Rev. D 96, 056024 (2017)

Deconfinement as supernova engine

Of massive blue supergiant star explosions

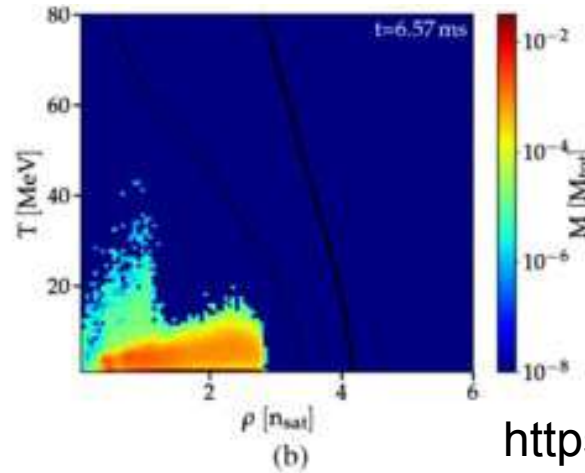
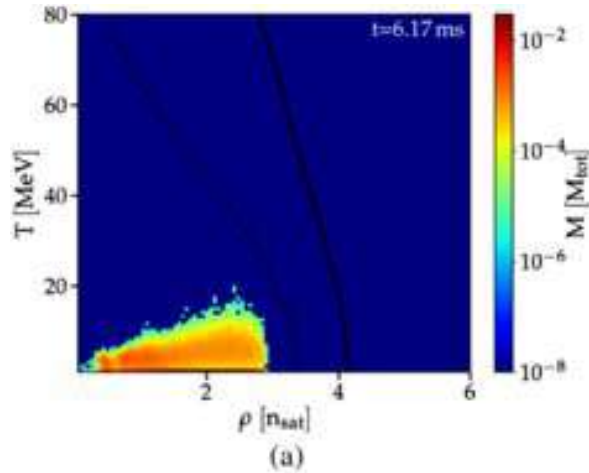


Progenitor:
 $M = 50 M_{\odot}$

T. Fischer et al., Nature Astronomy 2, 960 (2018)

Ultra-heavy Nucleus-Nucleus Collisions !

Population of the QCD phase diagram in a merger



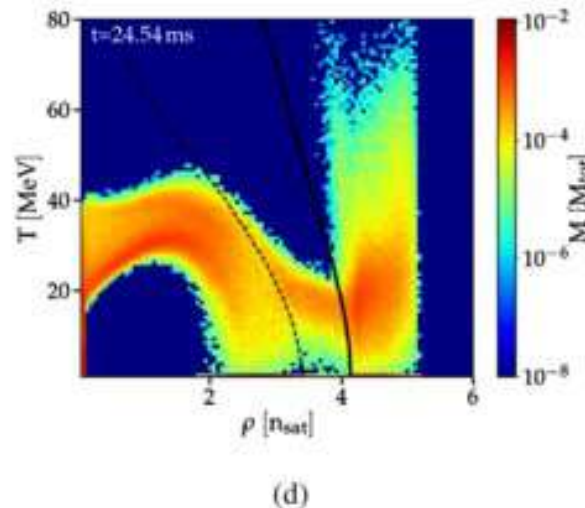
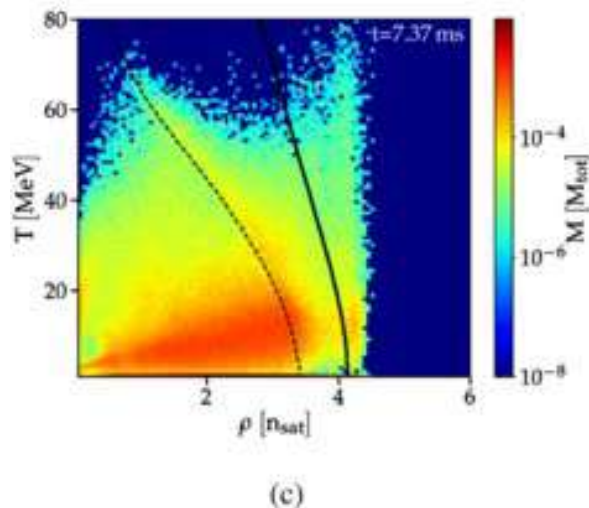
1.35 M_{sun} + 1.35 M_{sun}

EoS for supernova and merger simulations:

CompOSE

With deconfinement:

<https://compose.obspm.fr/eos/166>

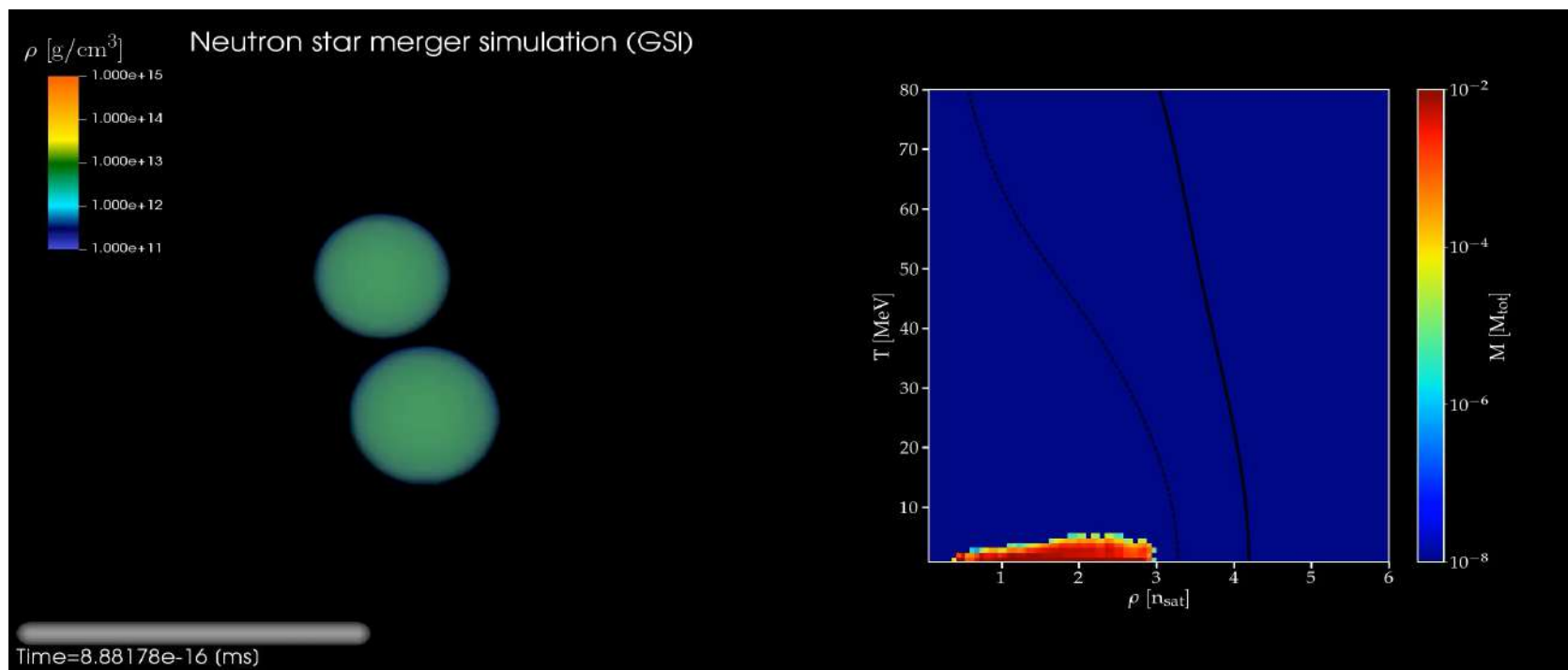


S. Blacker, A. Bauswein, et al.,
Phys. Rev. D 102 (2020) 123023

Binary neutron star merger simulation

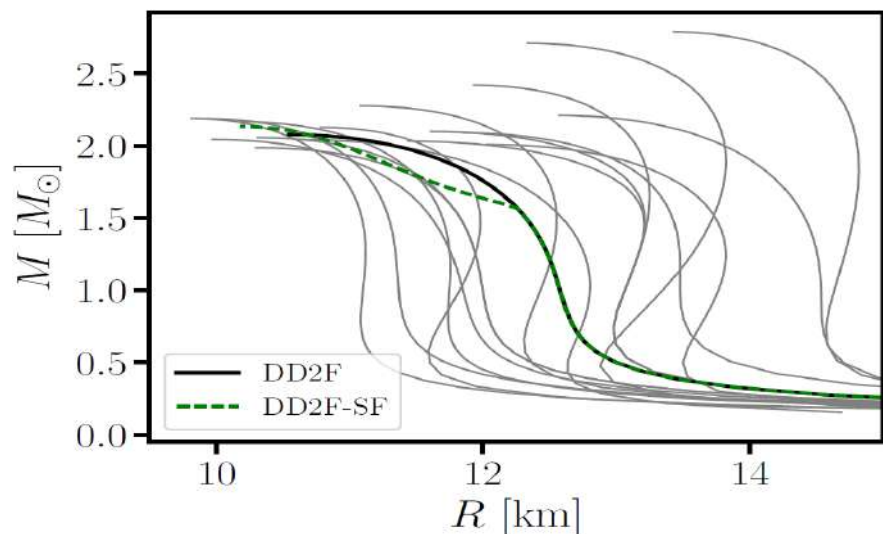
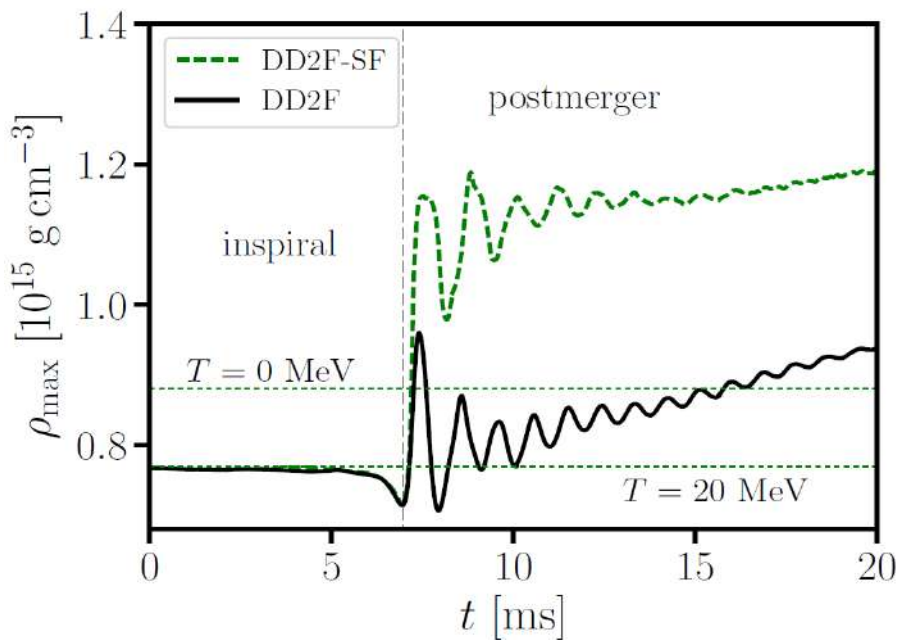
S. Blacker, A. Bauswein et al., Phys. Rev. D 102 (2020) 123023

Population of the QCD phase diagram with mixed phase; time = 6 ... 25 ms

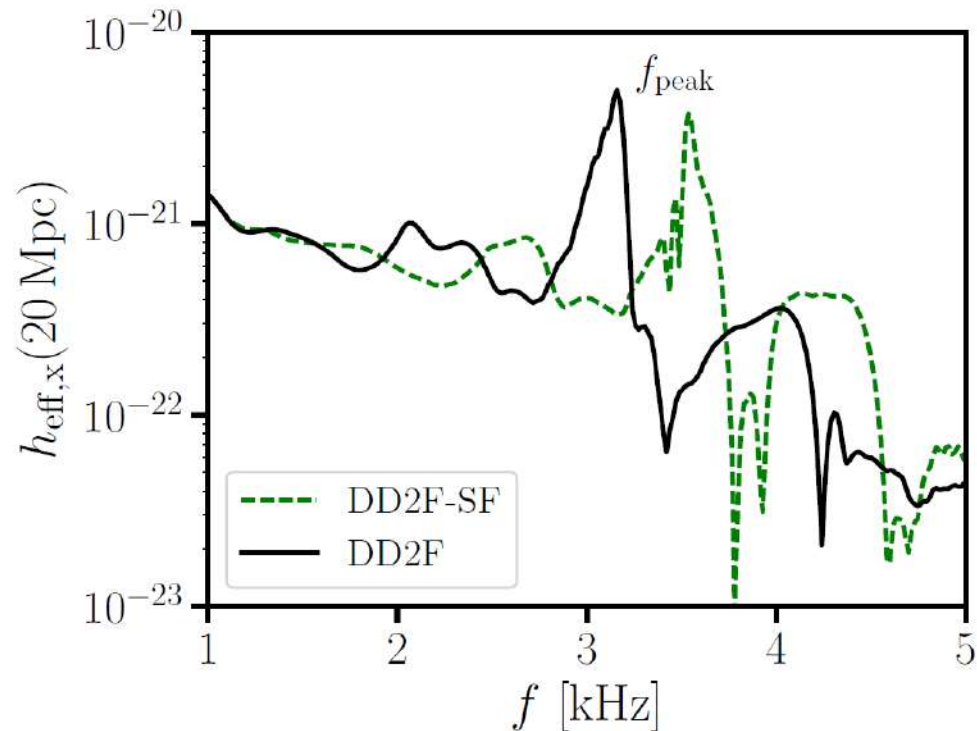


http://ift.uni.wroc.pl/~blaschke/grant_opus17.html

Ultra-heavy Nucleus-Nucleus Collisions !



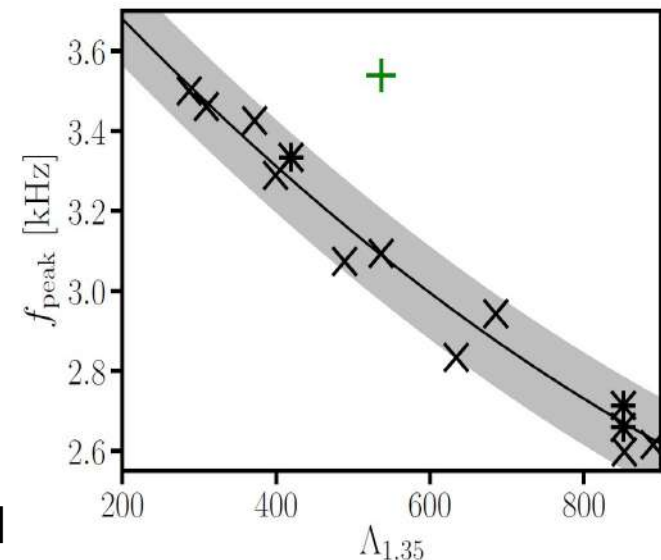
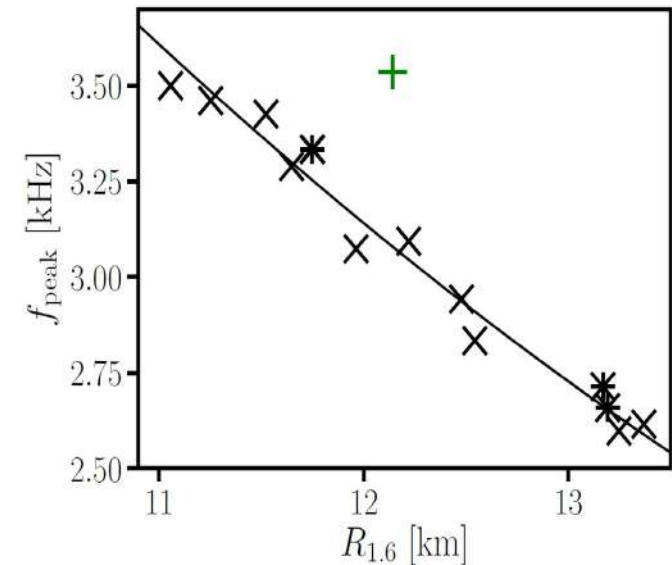
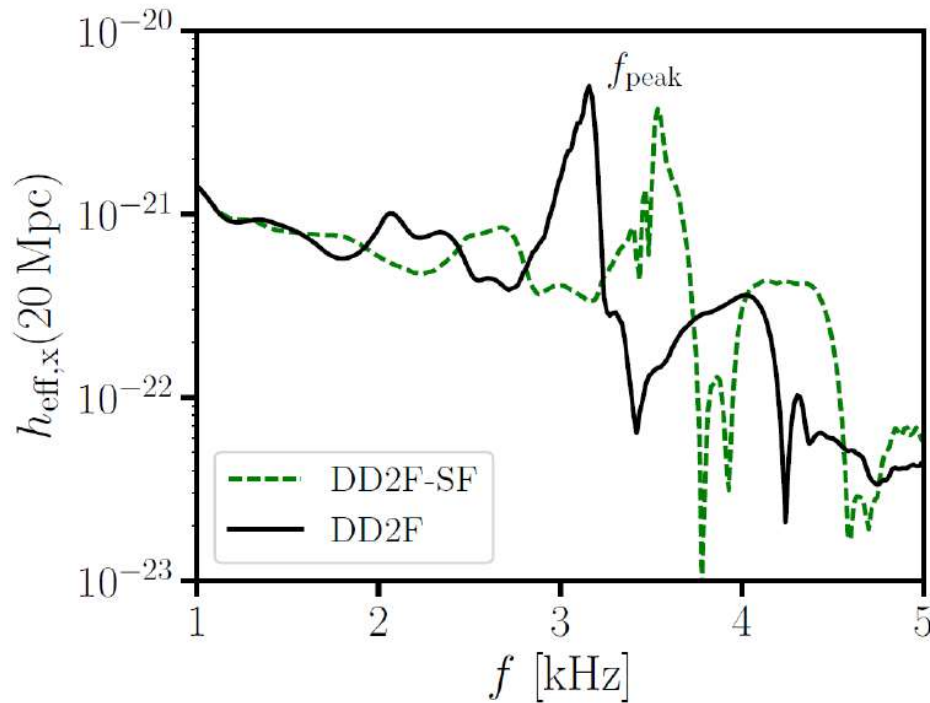
A. Bauswein et al.,
 Strong phase transition in postmerger GW,
 PRL 122 (2019) 061102; [arxiv:1809.01116]



Hybrid star formation during NS merger
 → higher densities and compact star
 → higher peak frequency of the GW

Ultra-heavy Nucleus-Nucleus Collisions !

Signal of a deconfinement transition



Strong deviation from $f_{\text{peak}} - R_{1.6}$ relation signals **strong phase transition** in NS merger!

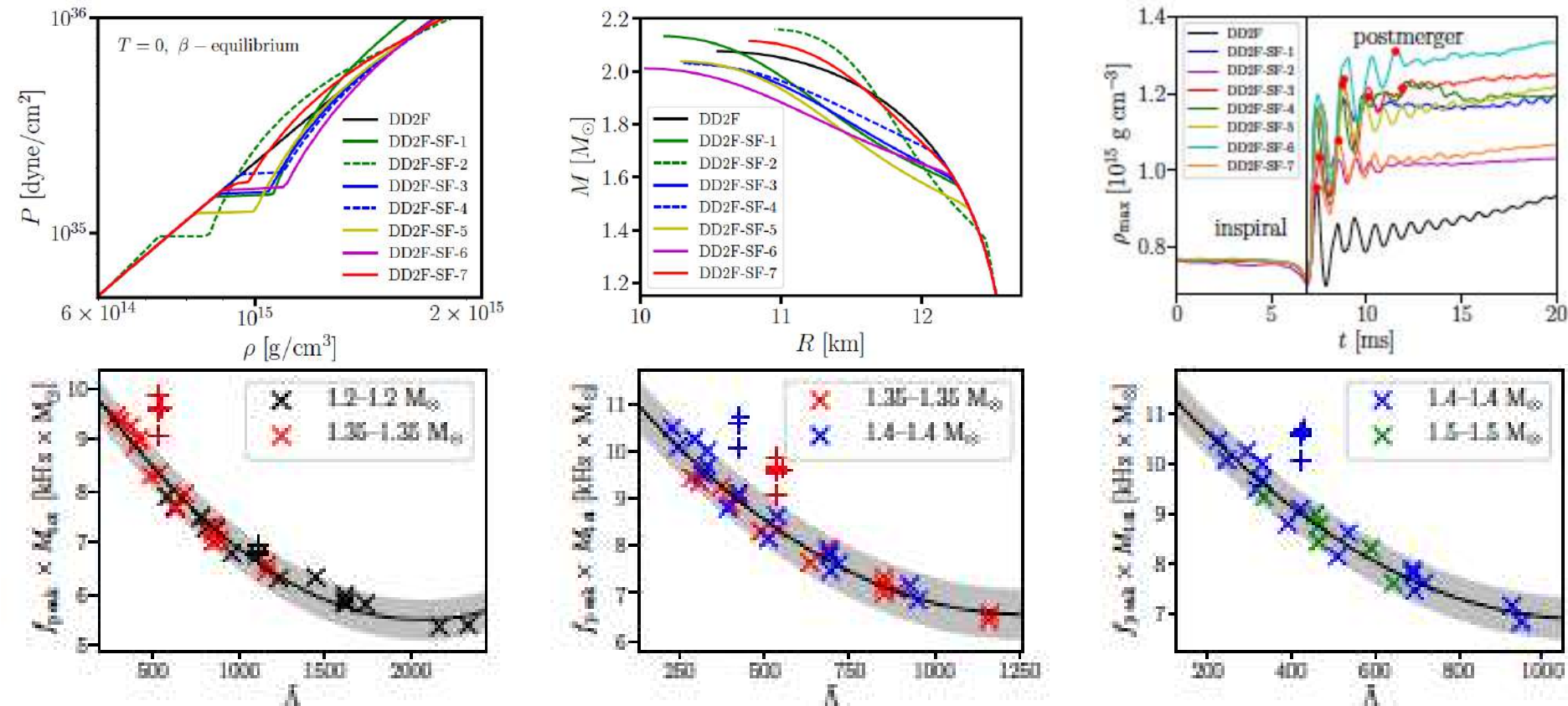
Complementarity of f_{peak} from **postmerger** with tidal deformability $\Lambda_{1.35}$ from **inspiral phase**.

A. Bauswein et al., PRL 122 (2019) 061102; [arxiv:1809.01116]

Ultra-heavy Nucleus-Nucleus Collisions !

Signal of a deconfinement transition

Strong PT in postmerger GW signal, S. Blacker et al., arxiv:2006.03789, PRD102 (2020) 123023

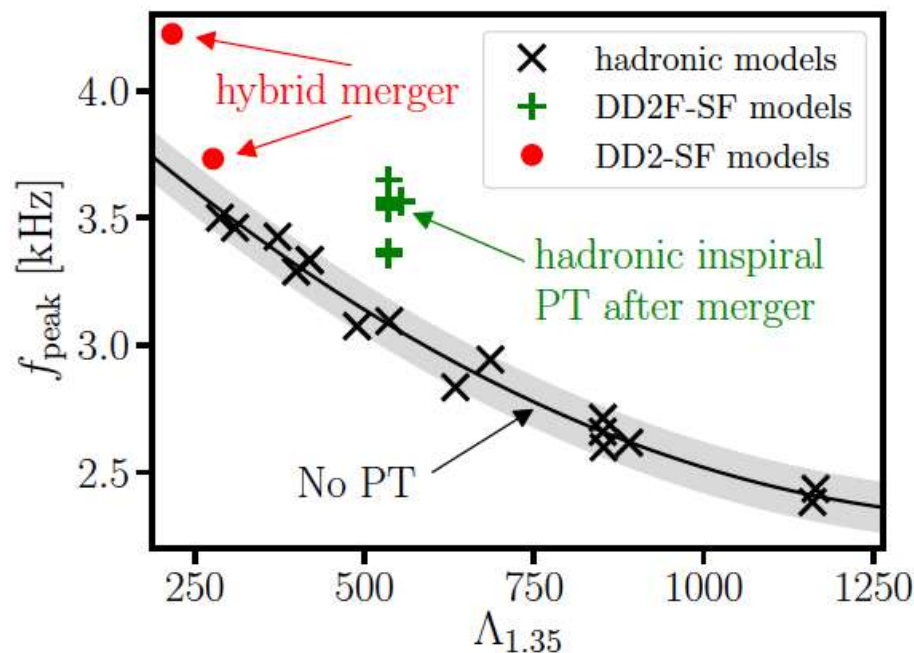
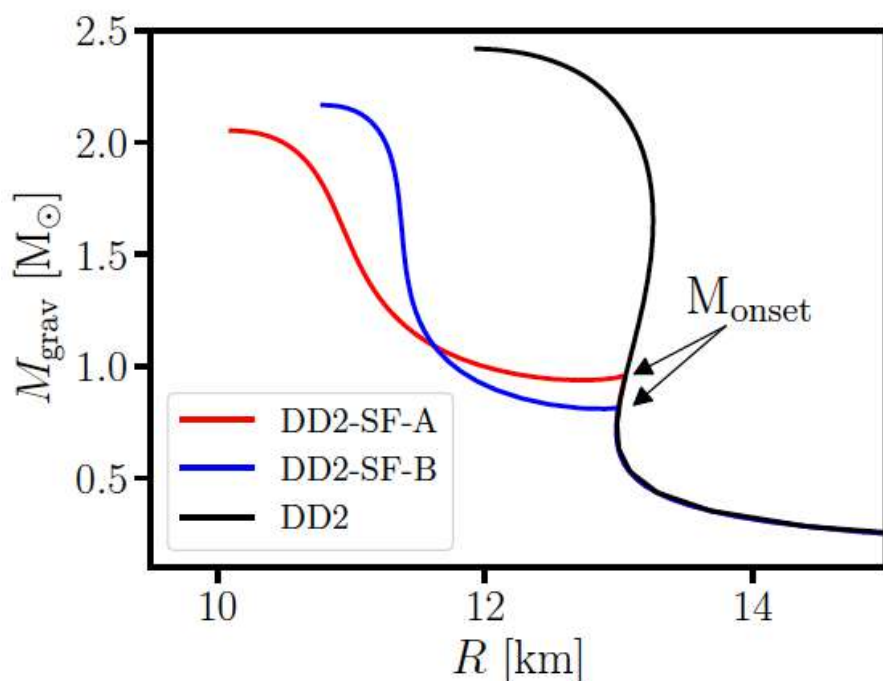


Dominant **postmerger** frequency f_{peak} vs. tidal deformability $\Lambda_{1.35}$ from **inspiral** phase:
 Results from hybrid models appear as **outliers** of the grey band (maximal deviation of purely hadronic models from a least squares fit) = signalling a **strong phase transition in NS !**

Ultra-heavy Nucleus-Nucleus Collisions !

Signal of a deconfinement transition

Merger of hybrid stars with early phase transition: Bauswein & Blacker, EPJ ST 229 (2020)

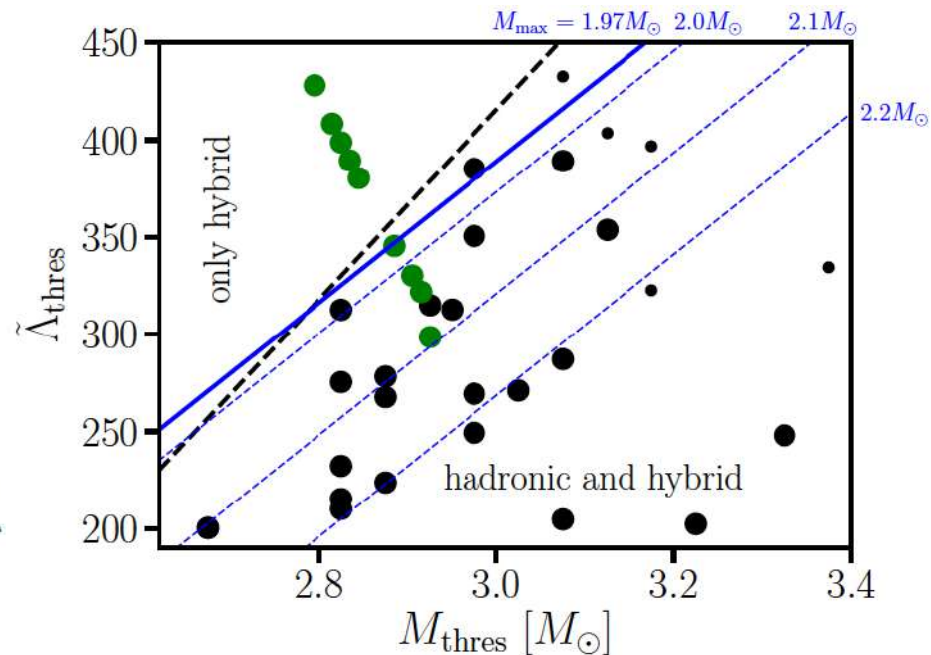
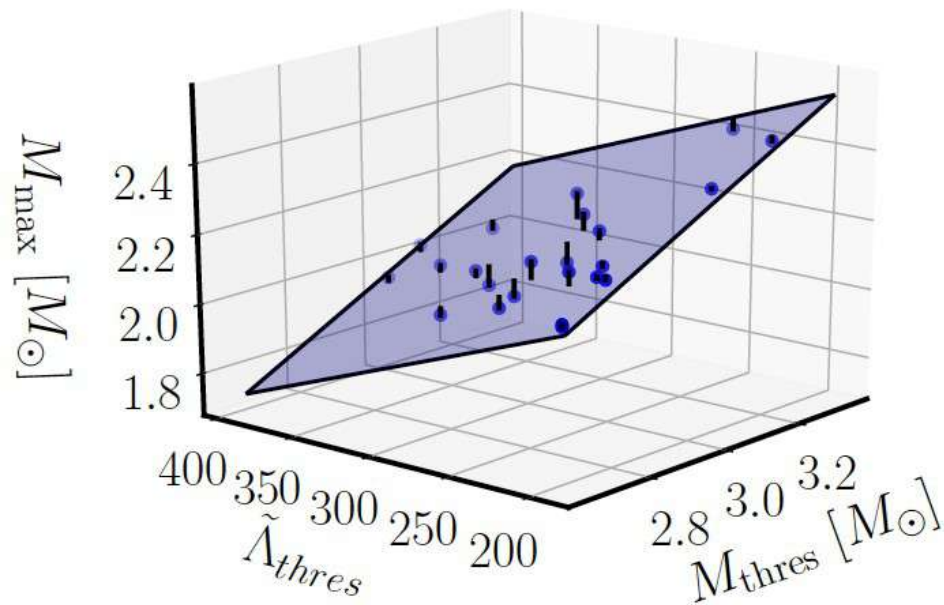


The combination of stiff hadronic EoS (DD2) and string-flip (SF) model allows for early onset of deconfinement in low-mass neutron stars and even third-family solutions (mass twins). For these cases, the event GW170817 could have been a **merger of two hybrid stars!** Also in these cases (red dots in above figure) a **significant deviation** from the grey band of Purely hadronic star mergers without a phase transition is obtained!

Ultra-heavy Nucleus-Nucleus Collisions !

EoS constraint from threshold binary mass

M_{\max} of nonrotating NS from binary mergers: A. Bauswein et al., PRL 125 (2020) 141103



$$M_{\max}(M_{\text{thres}}, \tilde{\Lambda}_{\text{thres}}) = aM_{\text{thres}} + b\tilde{\Lambda}_{\text{thres}} + c,$$

$$a = 0.632, b = -0.002 M_{\odot} \text{ and } c = 0.802 M_{\odot}$$

$$\tilde{\Lambda}_{\text{thres}} > 488(M_{\text{thres}}/M_{\odot}) - 1050$$

→ **strong evidence for a phase trans.**

Relativistic density functional for quark matter

With chiral symmetry, color SC & confinement

Lagrangian $\mathcal{L} = \bar{q}(i\cancel{\partial} - \hat{m})q - \mathcal{U} + \mathcal{L}_V + \mathcal{L}_I + \mathcal{L}_D$

- **Scalar & pseudoscalar interaction channels**

$$\mathcal{U} = G_0 \left[(1 + \alpha) \langle \bar{q}q \rangle_0^2 - (\bar{q}q)^2 - (\bar{q}i\vec{\tau}\gamma_5 q)^2 \right]^{\frac{1}{3}}$$

(motivated by String Flip Model, χ -dynamics, quark "confinement")

- **Vector-isoscalar interaction channel**

$$\mathcal{L}_V = -G_V (\bar{q}\gamma_\mu q)^2$$

(motivated by gluon exchange, stiff EoS needed to reach $2M_\odot$)

- **Vector-isovector interaction channel**

$$\mathcal{L}_I = -G_I (\bar{q}\gamma_\mu \vec{\tau} q)^2$$

(motivated by gluon exchange, isospin sensitive interaction)

- **Diquark interaction channel**

$$\mathcal{L}_D = G_D \sum_{A=2,5,7} (\bar{q}i\gamma_5 \tau_2 \lambda_A q^c) (\bar{q}^c i\gamma_5 \tau_2 \lambda_A q)$$

(motivated by Cooper theorem, color superconductivity)

What is new?

O. Ivanytskyi & D.B., Phys. Rev. D 105 (2022) 114042

Interaction
$$\mathcal{U} = D_0 [(1 + \alpha) \langle \bar{q}q \rangle_0^2 - (\bar{q}q)^2 - (\bar{q}i\vec{\tau}\gamma_5 q)^2]^\kappa$$

- Parameters**

D_0 - dimensionfull coupling, controls interaction strength

α - dimensionless constant, controls vacuum quark mass

$\langle \bar{q}q \rangle_0$ - χ -condensate in vacuum (introduced for the sake of convenience)



$$\kappa = 1/3$$



motivated by String Flip model

$$\mathcal{U}_{SFM} \propto \langle q^+ q \rangle^{2/3}$$

$$\Sigma_{SFM} = \frac{\partial \mathcal{U}_{SFM}}{\partial \langle q^+ q \rangle} \propto \langle q^+ q \rangle^{-1/3} \propto \text{separation}$$

$$\kappa = 1$$



Nambu–Jona-Lasinio model

- Dimensionality**

$$\begin{aligned} [U] &= \text{energy}^4 \\ [\bar{q}q] &= \text{energy}^3 \end{aligned} \Rightarrow [D_0]_{\kappa=1/3} = \text{energy}^2 = [\text{string tension}]$$

self energy = string tension \times separation \Rightarrow confinement

Expansion around mean fields

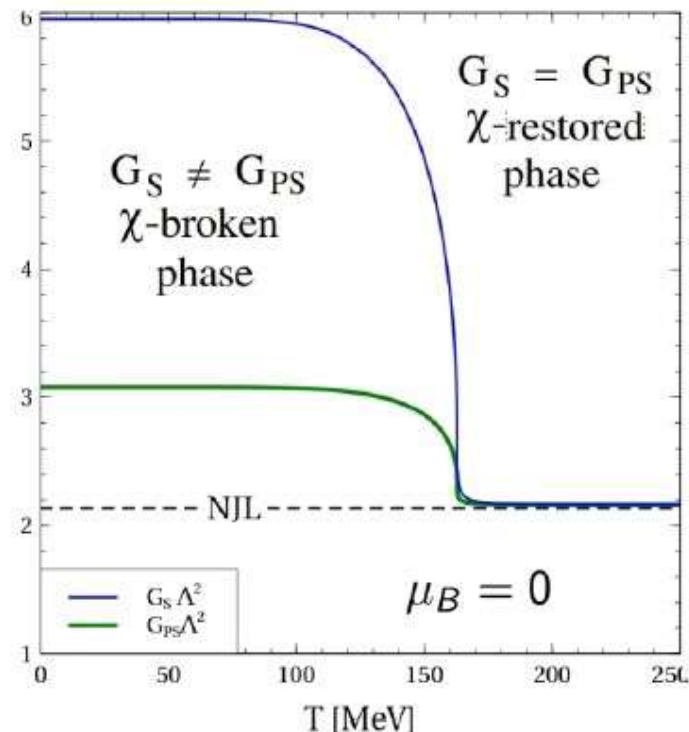
$$\mathcal{U} = \underbrace{\mathcal{U}_{MF}}_{0^{\text{th}} \text{ order}} + \underbrace{(\bar{q}q - \langle \bar{q}q \rangle) \Sigma_S}_{1^{\text{st}} \text{ order}} - \underbrace{G_S (\bar{q}q - \langle \bar{q}q \rangle)^2 - G_{PS} (\bar{q}i\vec{\tau}\gamma_5 q)^2}_{2^{\text{nd}} \text{ order}} + \dots$$

- Mean-field scalar self-energy

$$\Sigma_S = \frac{\partial \mathcal{U}_{MF}}{\partial \langle \bar{q}q \rangle}$$

- Effective medium dependent couplings

$$G_S = -\frac{1}{2} \frac{\partial^2 \mathcal{U}_{MF}}{\partial \langle \bar{q}q \rangle^2}, \quad G_{PS} = -\frac{1}{6} \frac{\partial^2 \mathcal{U}_{MF}}{\partial \langle \bar{q}i\vec{\tau}\gamma_5 q \rangle^2}$$



Comparison to Nambu—Jona-Lasinio model

$$\mathcal{L} = \bar{q}(i\not{\partial} - \underbrace{(m + \Sigma_S)}_{\text{effective mass } m^*})q + G_S(\bar{q}q)^2 + G_{PS}(\bar{q}i\vec{\tau}\gamma_5q)^2 + \dots + \mathcal{L}_V + \mathcal{L}_D$$

• Similarities:

- current-current interaction
- (pseudo)scalar, vector, diquark, ... channels

• Differences:

- high m^* at low $T, \mu \Rightarrow$ “confinement”

$$\langle \bar{q}q \rangle = \langle \bar{q}q \rangle_0 \Rightarrow m^* = m - \frac{2G_0}{3\alpha^{2/3}\langle \bar{q}q \rangle_0^{1/3}}$$

\Downarrow

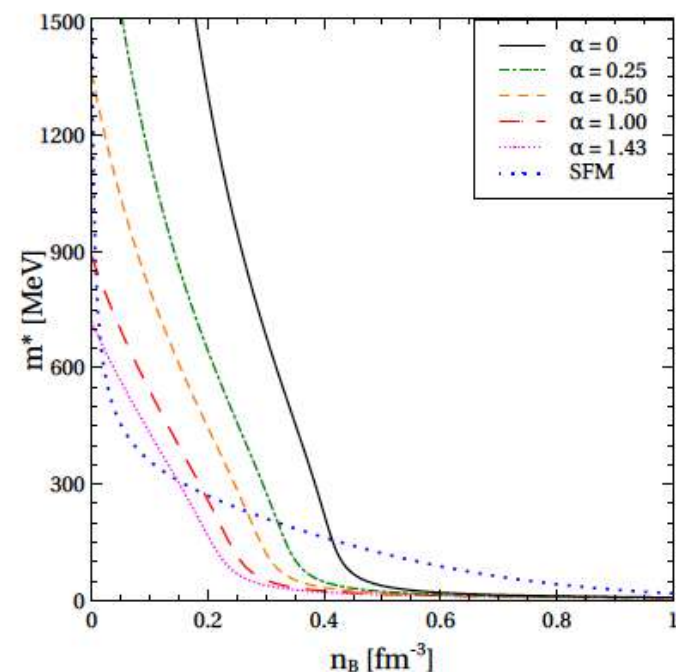
$$m^* \rightarrow \infty \text{ at } \alpha \rightarrow 0$$

- medium dependent couplings:

$$\text{low } T, \mu, \Rightarrow G_S \neq G_{PS} \Rightarrow \chi\text{-broken}$$

$$\text{high } T, \mu, \Rightarrow G_S = G_{PS} \Rightarrow \chi\text{-symmetric}$$

$T = 0$



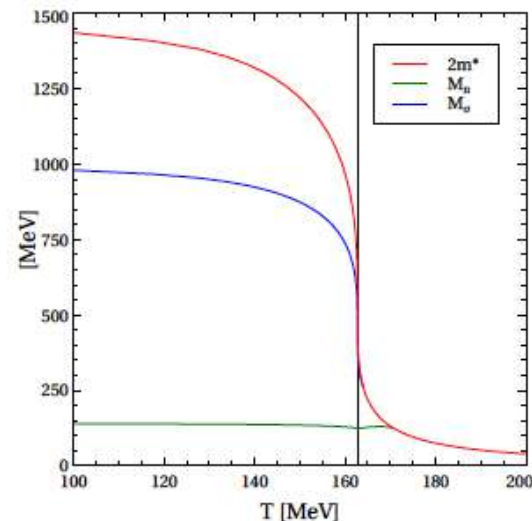
Model setup – parameter fixing with observables

- (Pseudo)scalar interaction channels
(chiral condensate & π , σ mesons)

m [MeV]	Λ [MeV]	α	$D_0\Lambda^{-2}$
4.2	573	1.43	1.39
M_π [MeV]	F_π [MeV]	M_σ [MeV]	$\langle \bar{l}l \rangle_0^{1/3}$ [MeV]
140	92	980	-267

Pseudocritical temperature

$$T_c = 163 \text{ MeV}$$



- low T: $2m_{quark} > M_\pi, M_\sigma$
(stable mesons, confined quarks)
- high T: $2m_{quark} < M_\pi, M_\sigma$
(unstable mesons, deconfined quarks)

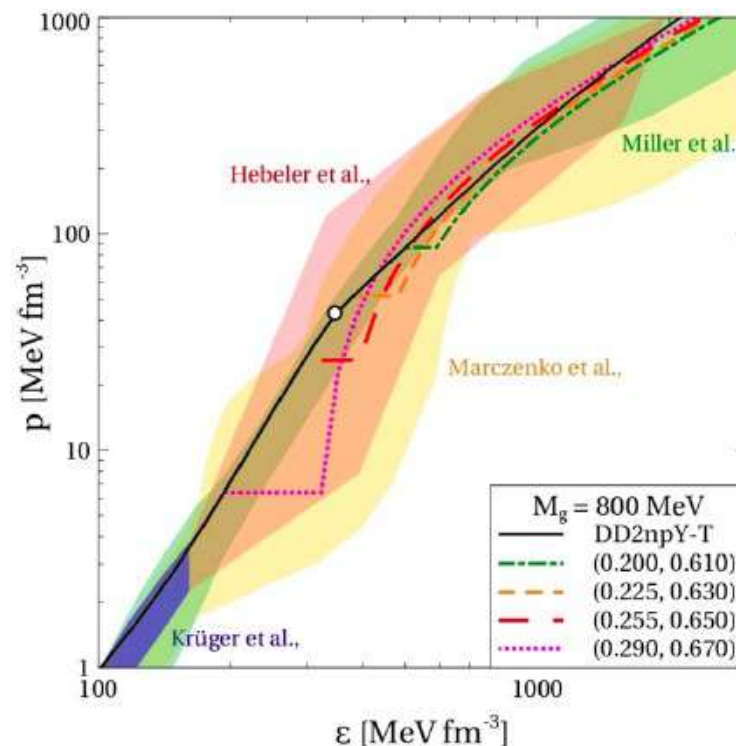
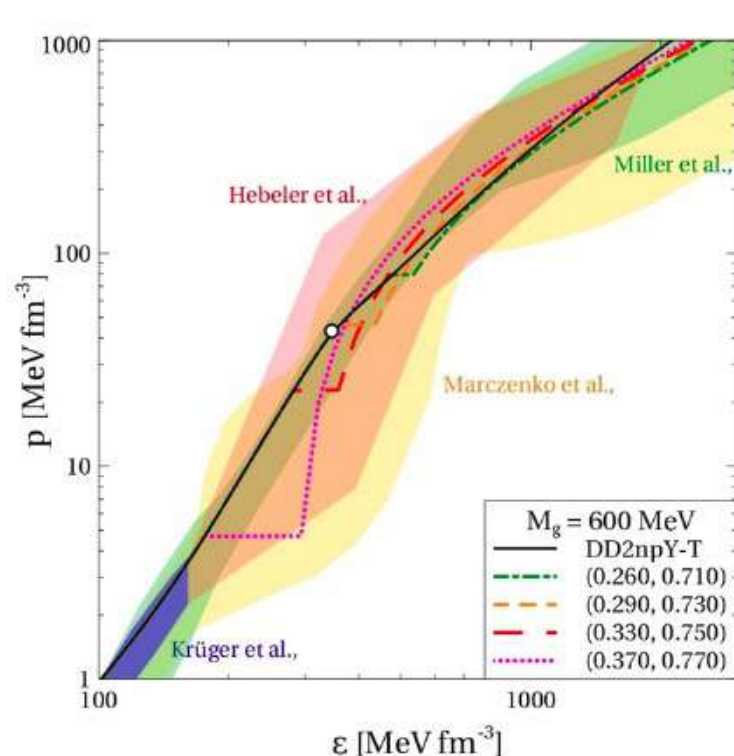
- Vector-isoscalar & vector-isovector channels (ω , ρ mesons)

$$M_\omega = 783 \text{ MeV} \Rightarrow \eta_V \equiv \frac{G_{V0}}{G_{S0}} = 0.452, \quad M_\rho = 775 \text{ MeV} \Rightarrow \eta_I \equiv \frac{G_{I0}}{G_{S0}} = 0.454$$

- Diquark pairing channel (Fierz transformation) $\eta_D \equiv \frac{G_{D0}}{G_{S0}} = 1.5\eta_V = 0.678$

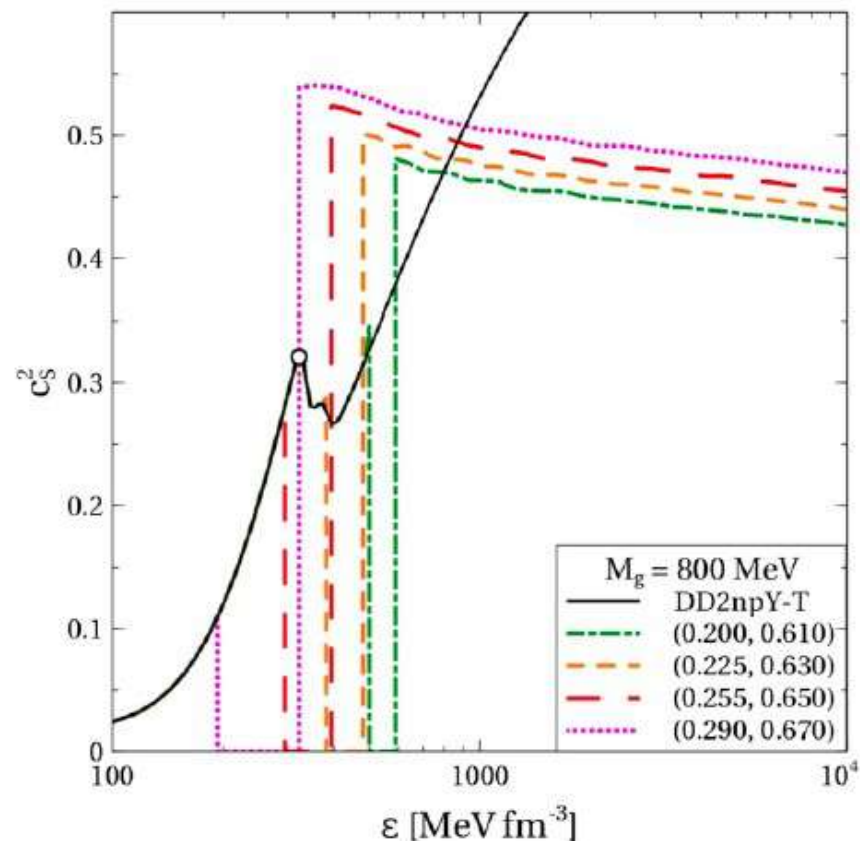
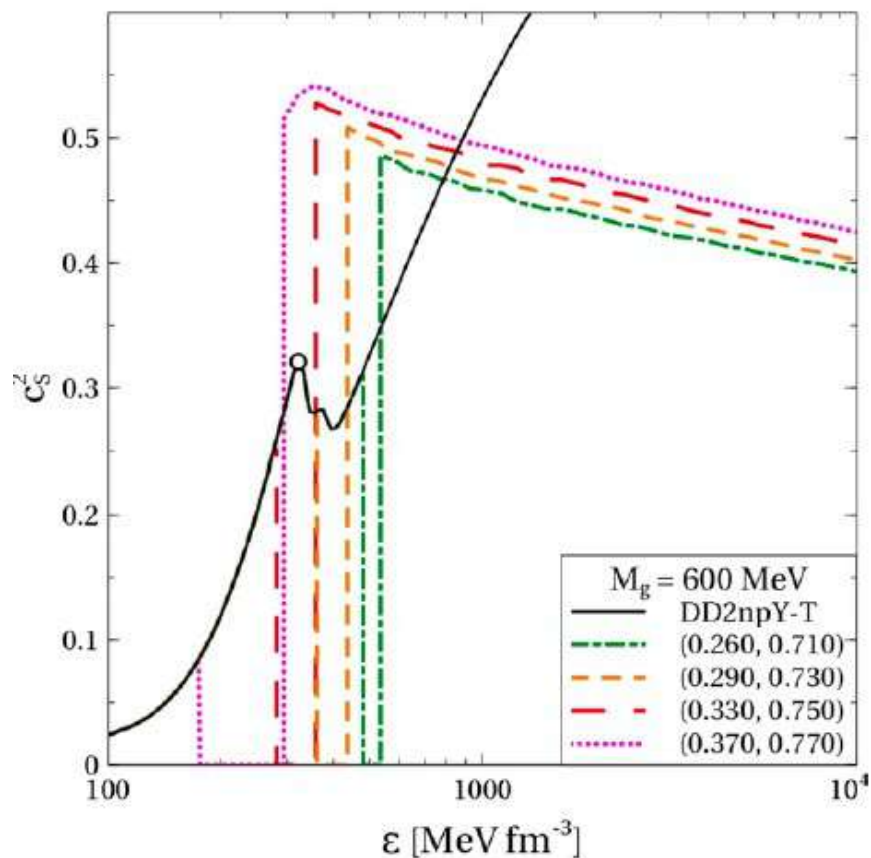
Asymptotically conformal EOS for neutron stars

- **Setup:** electric neutrality, β -equilibrium, Maxwell construction with DD2 EoS
- **Scanning over η_V and η_D at $M_{gD} = M_{gV}$**



The ω -meson value of η_V and the Fierz value of η_D prefer early deconfinement?

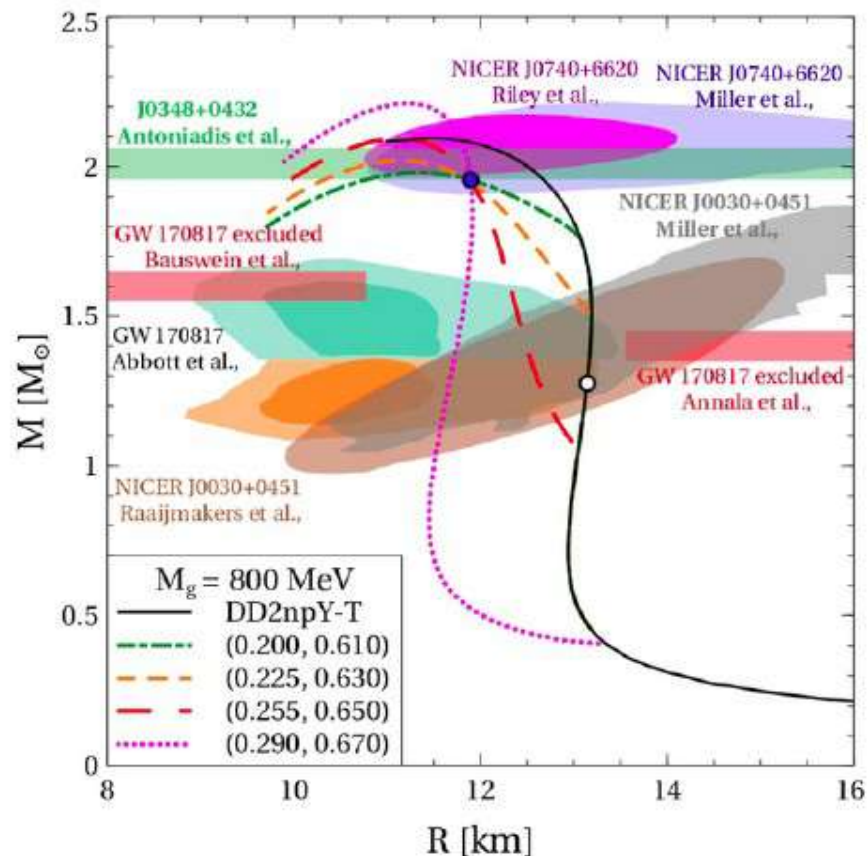
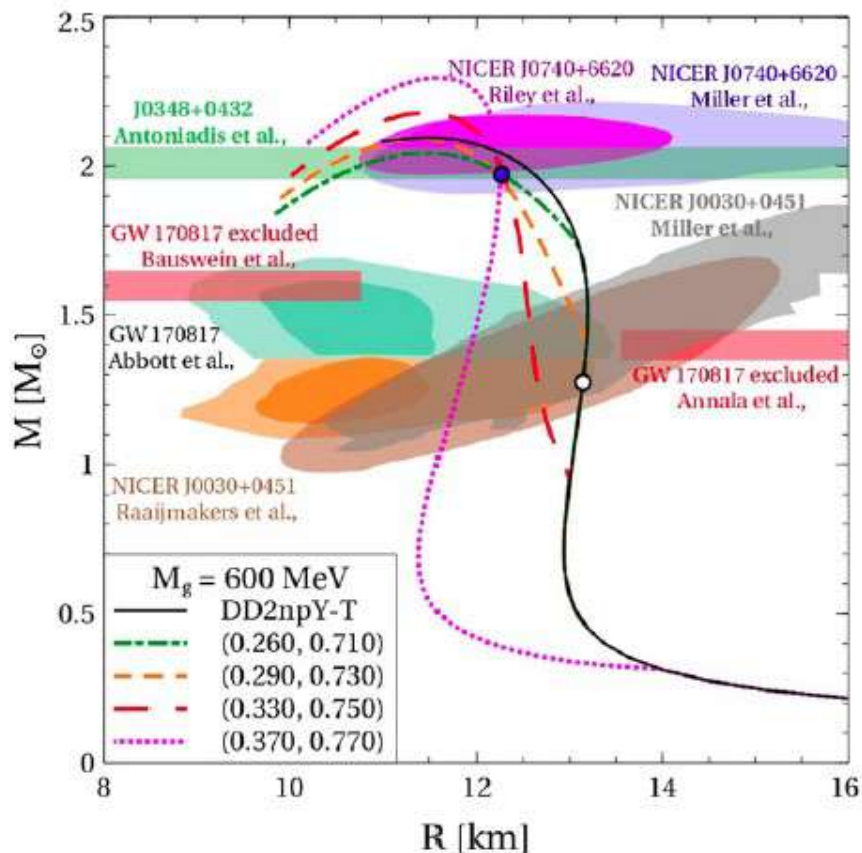
Speed of sound



O. Ivanytskyi and D.B., Particles 5 (2022) 514 - 534

Relativistic density functional for quark matter

Mass-radius diagram for hybrid neutron stars



Observational data prefer early deconfinement?

Relativistic density functional for quark matter

Special point (SP) in the mass-radius diagram for hybrid neutron stars

- Quark EoS

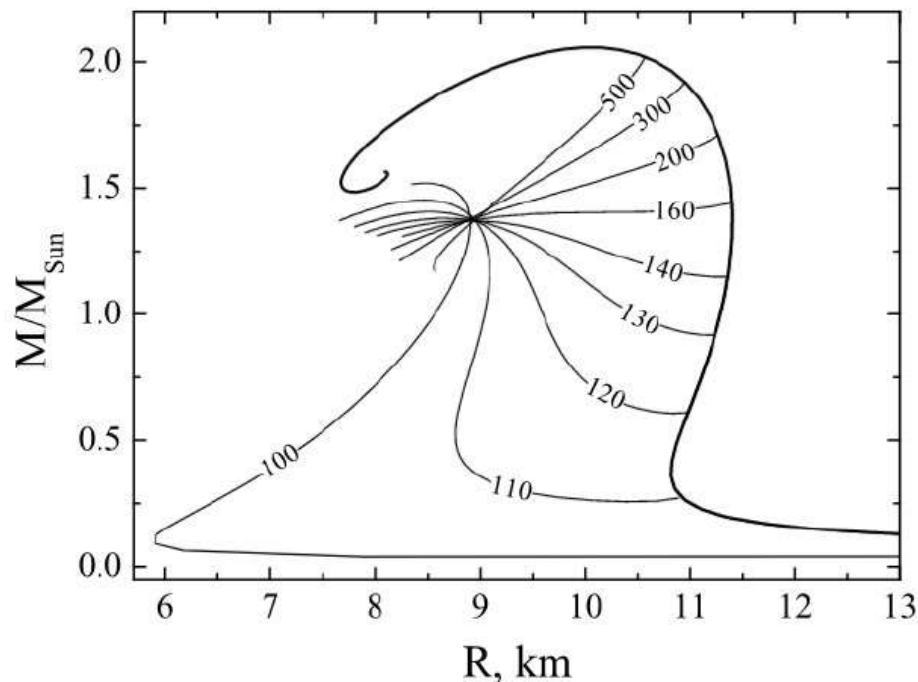
$$p = \frac{\varepsilon}{3} - \frac{4B}{3}$$

B - bag constant

- Variation of B



family of hybrid quark-hadron EoS



- **Special point** - narrow range of intersection of M-R curves

A. V. Yudin et al., Astron. Lett. 40, 201 (2014)

Relativistic density functional for quark matter

SP in M-R diagram for hybrid neutron stars

- Weak sensitivity to hadron EoS

M. Cierniak and D. Blaschke, *Eur. Phys. J. ST* 229, 3663 (2020)

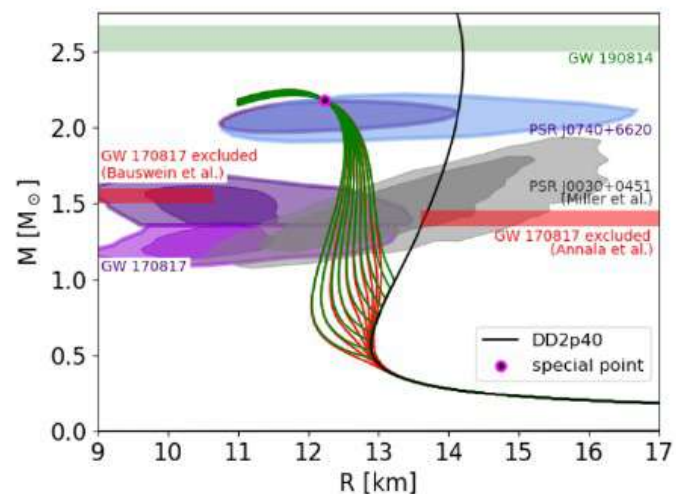
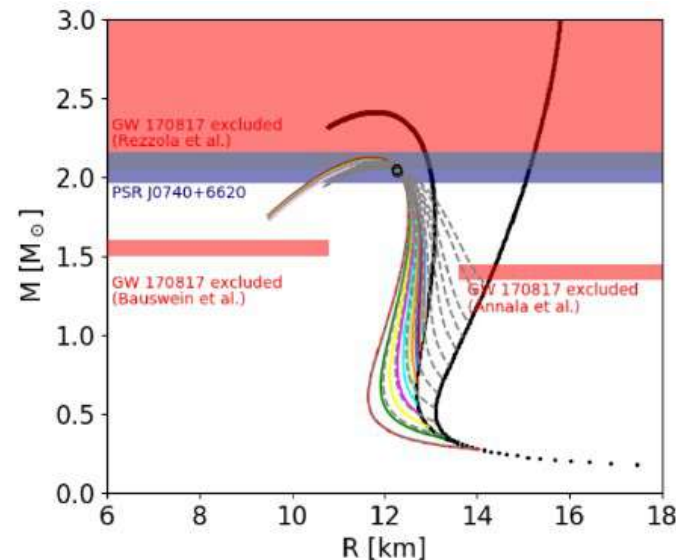
- Weak sensitivity to details of quark-to-hadron transition

M. Cierniak and D. Blaschke, *Astron. Nachr.* 342, 819-825 (2021)

- Sensitivity to quark EoS only



SP can be used in order to test quark EoS



Relativistic density functional for quark matter

SP in M-R diagram for hybrid neutron stars

- Variation of η_D at fixed η_V

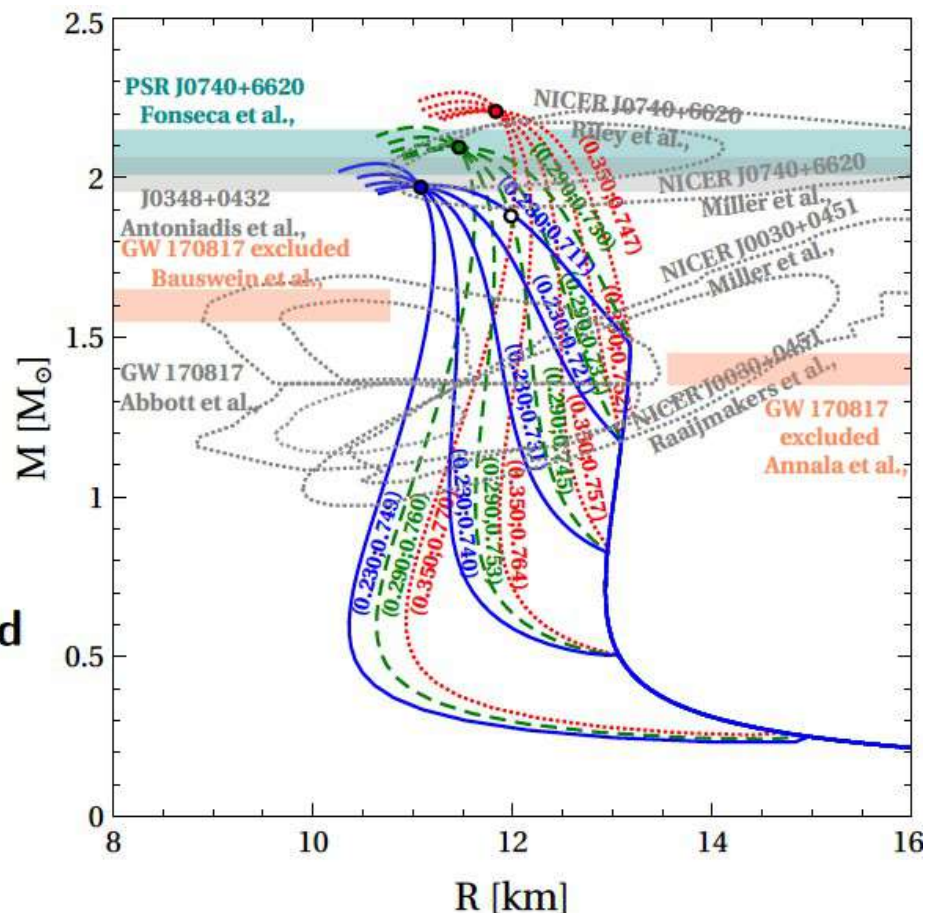


Special point

- SPs are equidistant
- M_{\max} and M_{onset} are anticorrelated

M_{\max} – observationally constrained

M_{onset} – controlled by η_V, η_D



Is it possible to constrain η_V and η_D ?

Relativistic density functional for quark matter

SP in M-R diagram for hybrid neutron stars

- No vacuum color-superconductivity

$$\eta_D < 0.78$$

O. Ivanytskyi, D. Blaschke, PRD (2022)

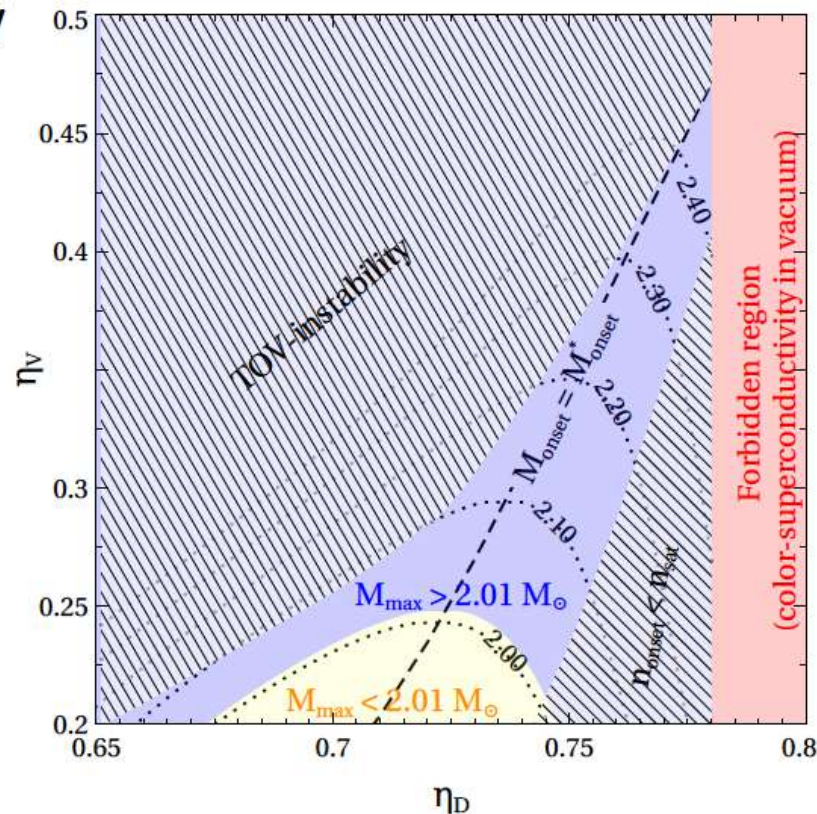
- $M_{\max} = 2.08^{+0.07}_{-0.07} M_{\odot}$

E. Fonseca et al., Astrophys. J. Lett. 915, L12 (2021)

- Not too early deconfinement

$$n_{\text{onset}} > n_{\text{saturation}}$$

- Stability of the quark branch

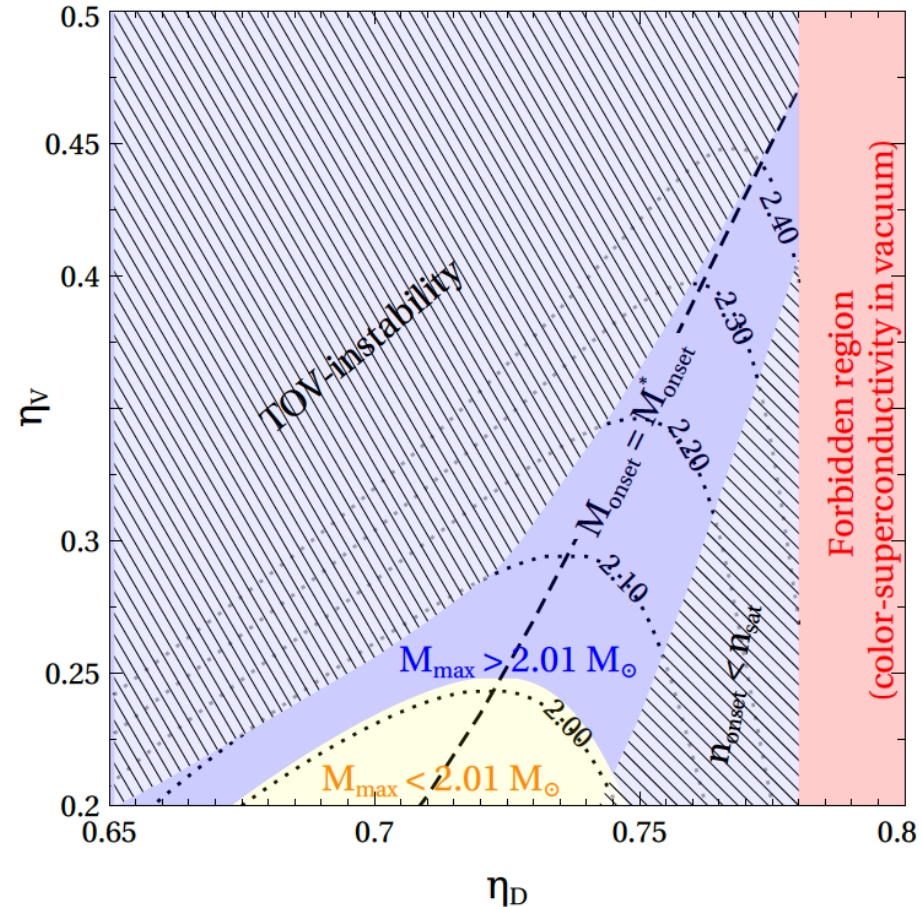
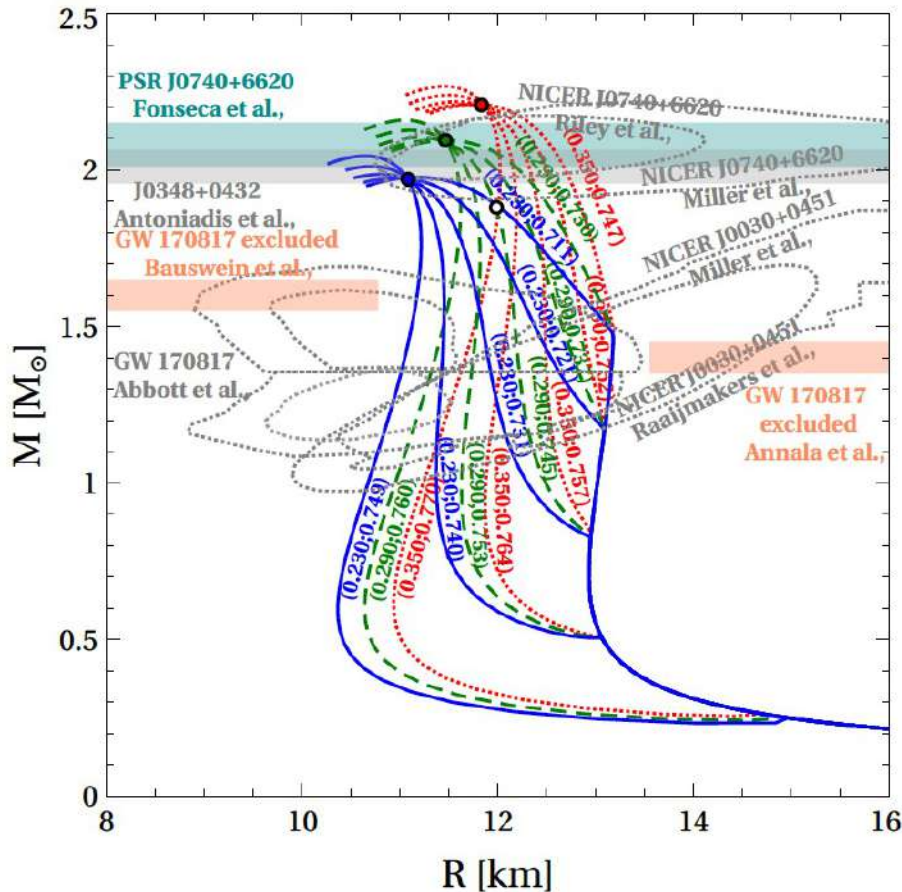


$$M_{\omega} = 783 \text{ MeV} \Rightarrow \eta_V = 0.452$$

Are the couplings constrained to the small region suggesting $M_{\text{onset}} < 0.5 M_{\odot}$ and $M_{\max} > 2.4 M_{\odot}$?

Relativistic density functional for quark matter

Mass-radius diagram for hybrid neutron stars



$$M_{\max} = M_{\text{SP}} + \delta |M_{\text{onset}}^* - M_{\text{onset}}|^{\kappa} \quad M_{\text{SP}} = k_{M_{\text{SP}}} \eta_V + b_{M_{\text{SP}}}; \quad \delta = k_{\delta} \eta_V + b_{\delta}; \quad M_{\text{onset}}^* = 1.254 M_{\odot}$$

C. Gärtlein et al., Phys. Rev. D 108 (2023) 114028; arXiv:2301.10765v2

Relativistic density functional for quark matter

Phase diagram with two-zone interpolation

- **Normal quark matter**

$$2 \text{ spin} \times 2 \text{ flavor} \times 3 \text{ color} = 12$$

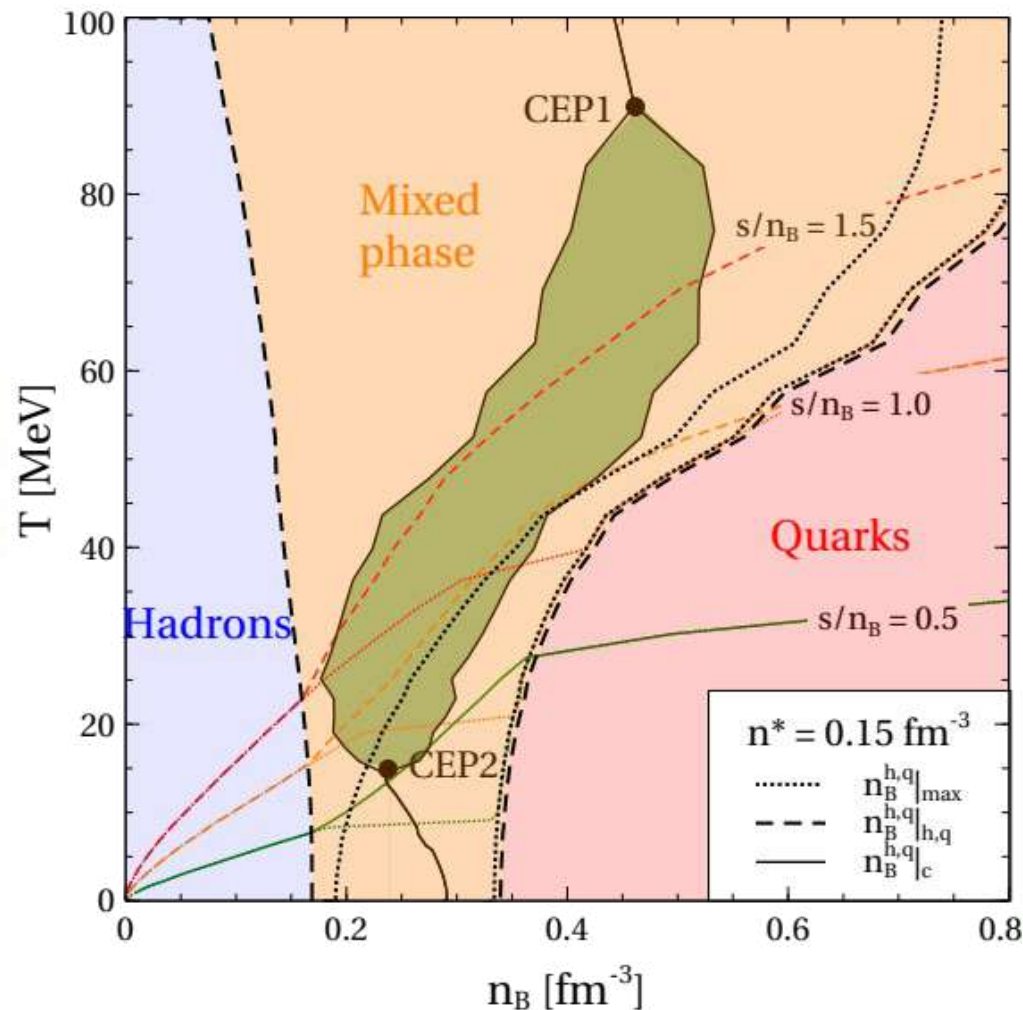
- **2SC quark matter**

$$2 \text{ spin} \times 2 \text{ flavor} \times 1 \text{ color} + 1 = 5$$

Quark pairing reduces number of quark states



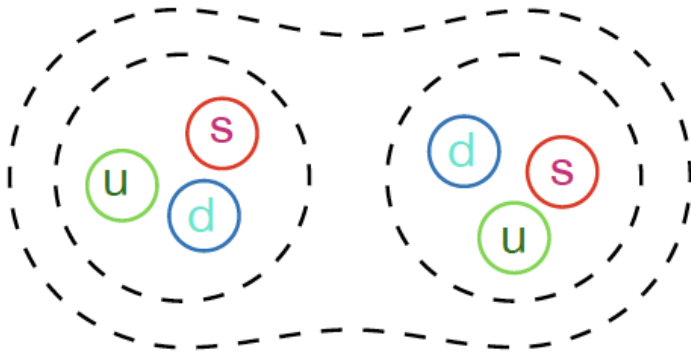
requires higher T along adiabat



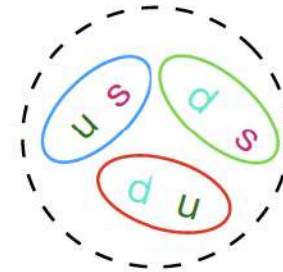
→ EOS tables are prepared for simulation of supernovae and NS mergers

The case for a light sexaquark $S(uuddss)$

A compact, stable 3-diquark state as dark matter particle



H-dibaryon $\sim \Lambda\Lambda$ molecule
 $M_H \sim 2M_\Lambda$



Light, compact sexaquark ~ 3 diquark state
 $M_S \sim 1800 \dots 2054 \text{ MeV} < M_\Lambda + M_p + M_e$

G. Farrar and N. Wintergerst, JHEP 12 (2023) 099

Wave function of a spatially symmetric, six-quark color-flavor-spin-singlet state

Only 1/5 di-baryon molecule ($\Lambda\Lambda$, $N\Xi$, $\Sigma\Sigma$), but 4/5 color octet baryons

F. Buccella, PoS (CORFU2019) 024

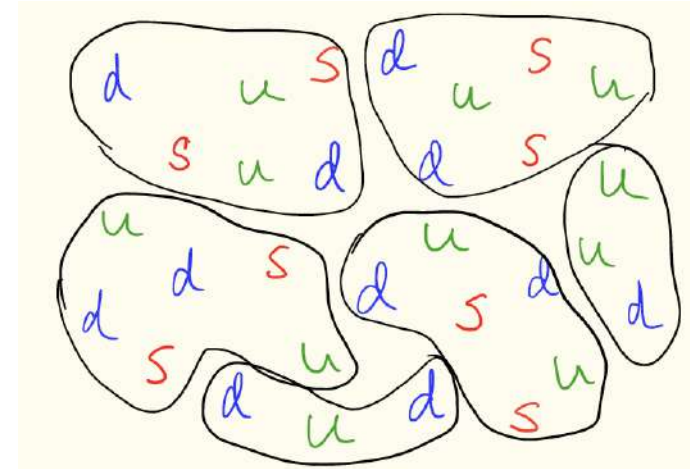
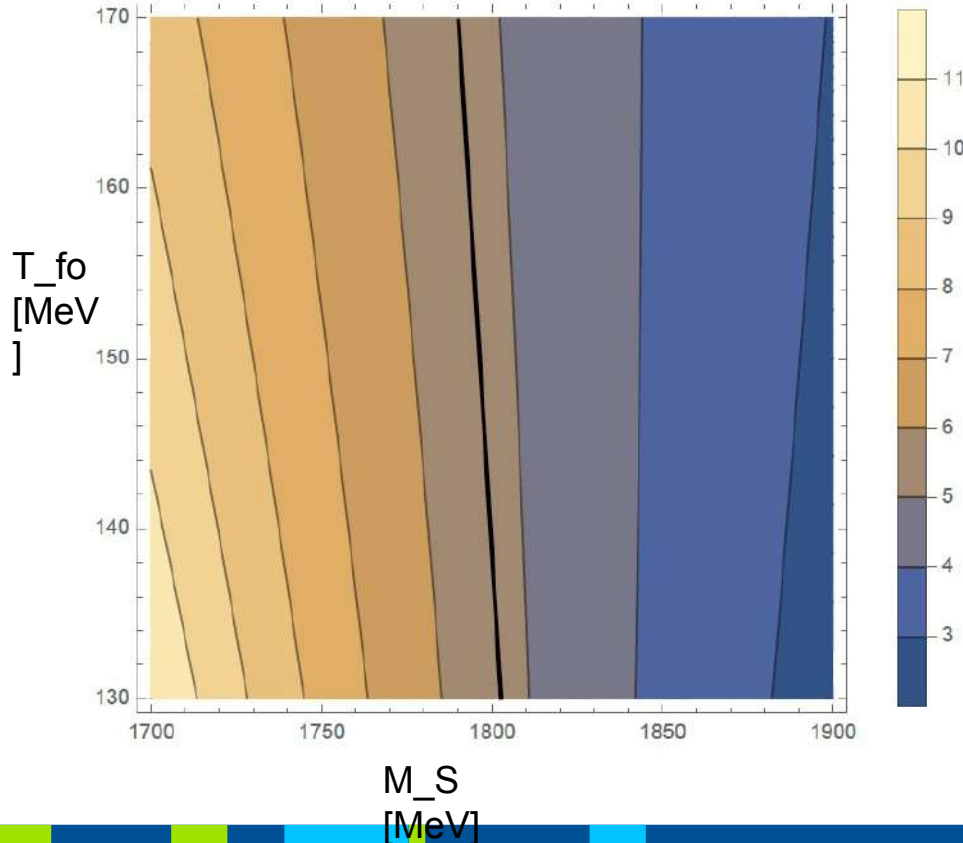
Three-diquark state including chromomagnetic & -electric interactions

$M_S = 1883 \text{ MeV}$

The case for a light sexaquark $S(uuddss)$

A compact, stable 3-diquark state as dark matter particle

Within a thermal statistical model for S abundances at the hadronisation transition ($T_{fo} = T_c = 156.5$ MeV) one obtains the Dark matter fraction depending on M_S



$$\Omega_{DM}/\Omega_b = 5.3 \pm 0.1$$

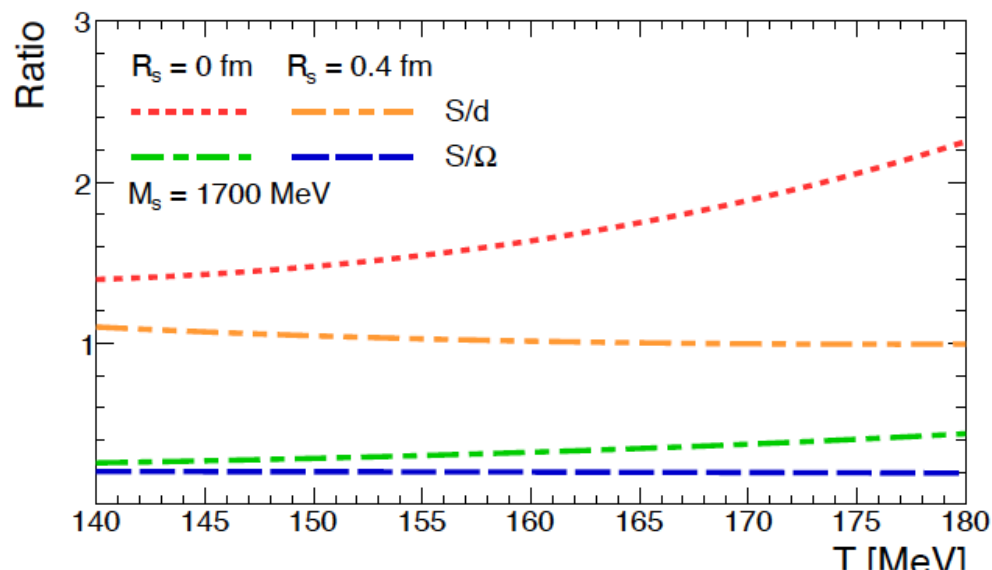
and

$$T_{fo} = 156.5 \text{ MeV}$$

requires

$$M_S \sim 1800 \text{ MeV}$$

Light sexaquark production at LHC

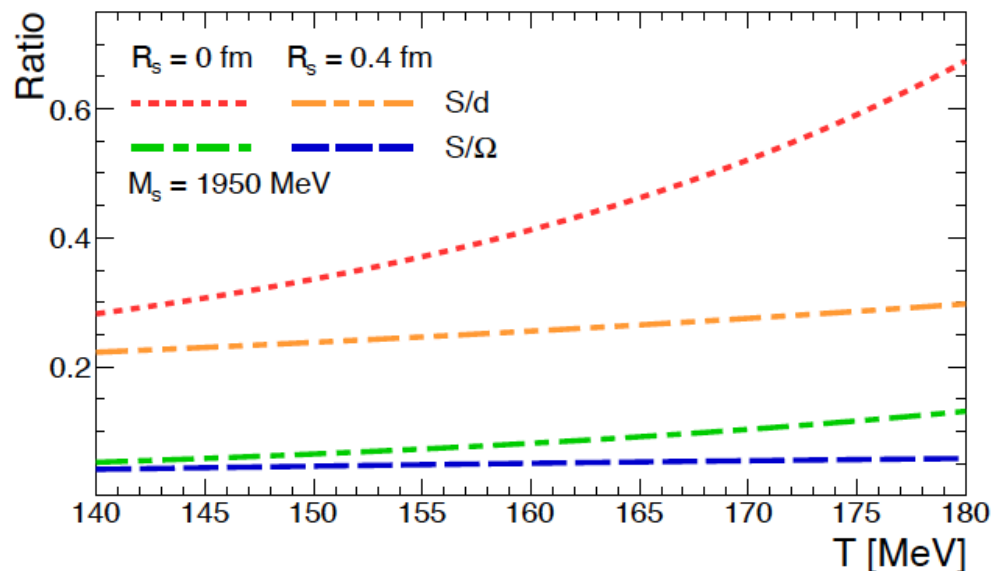


Estimates within a thermal statistical model for

$M_S = 1700$ MeV

And

$M_S = 1950$ MeV



D. Blaschke et al.

(S. Kabana, K. Bugaev, O. Vitiuk, G. Farrar, ...),

Int. J. Mod. Phys. A 36 (2020) 25

Light sexaquark in antiprotonic atoms

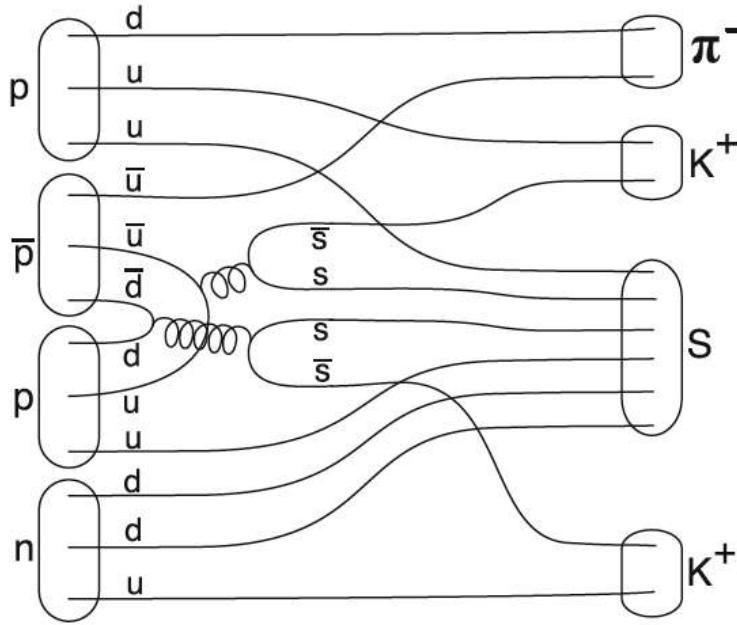
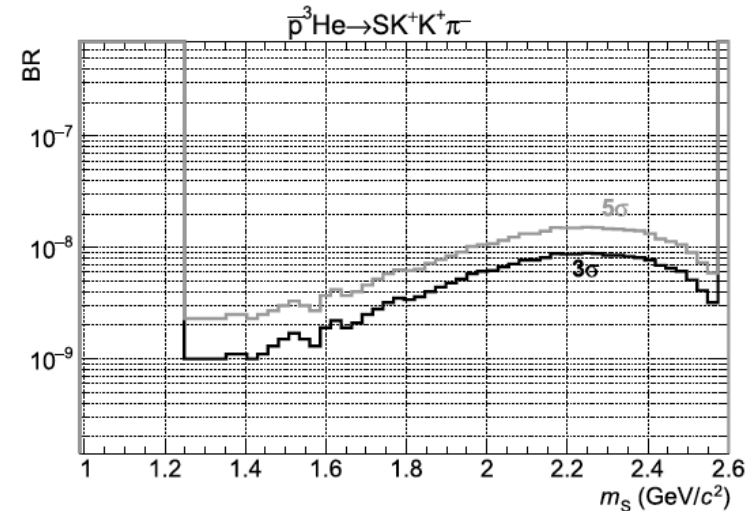
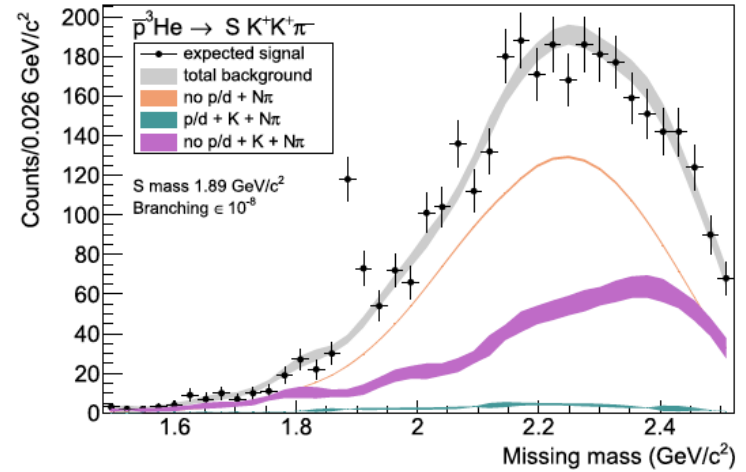
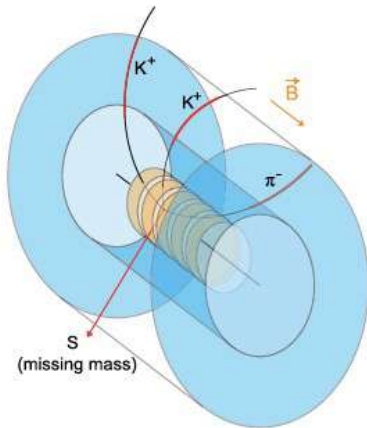


Fig. 1 Quark rearrangement and annihilation graph for the formation of a $uuddss$ sexaquark state in \bar{p} - ${}^3\text{He}$ annihilations. S denotes the putative $S(uuddss)$ sexaquark state



M. Doser, G. Farrar and G. Kornakov,
Eur. Phys. J. C 83 (2023) 1149

Light sexaquark – Dilemma for Neutron Stars ?

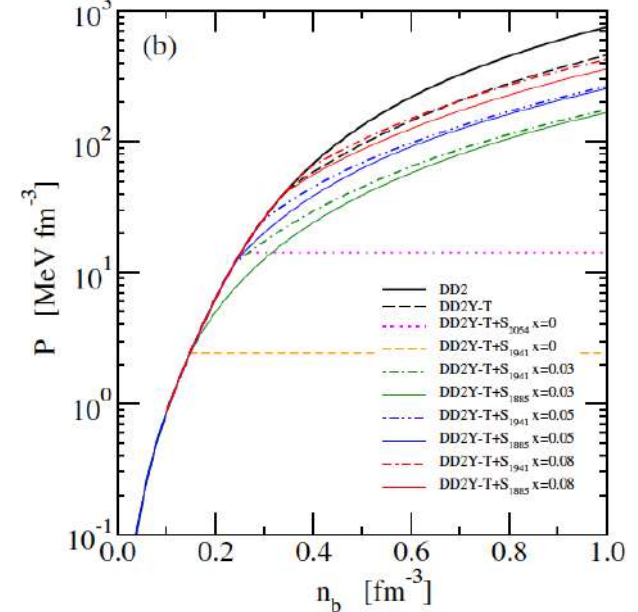
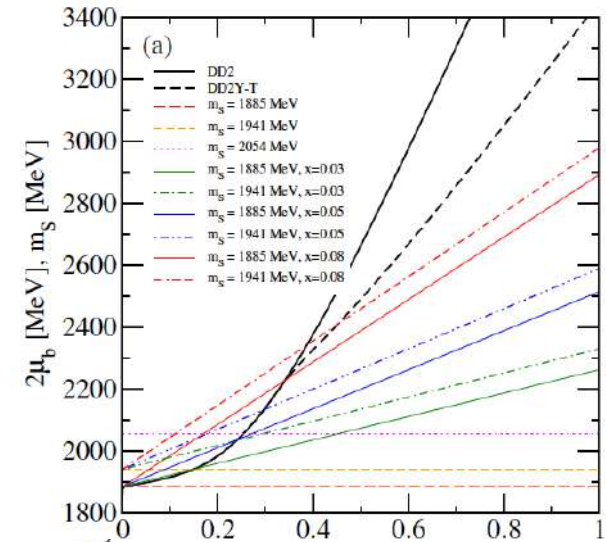
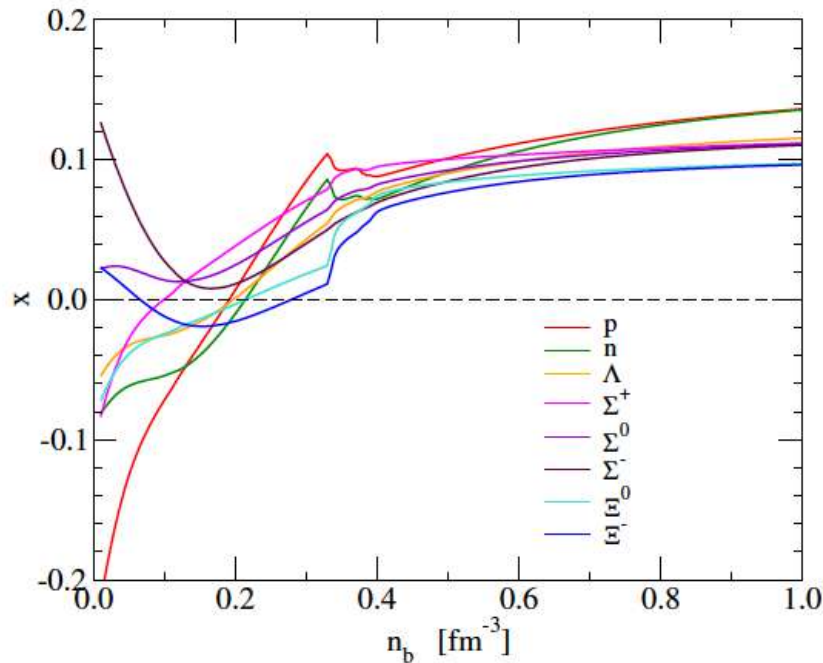
Problem: Sexaquark Bose-Einstein condensation

1. Solution: density-dependent mass

$$m_S^*(n_b, x_S) = m_S \left(1 + x_S \frac{n_b}{n_0} \right)$$

$$x_i = \frac{n_0}{m_i} \frac{dU_i}{dn_b}$$

For all baryons i from
Density-dependent
(optical) potential U_i

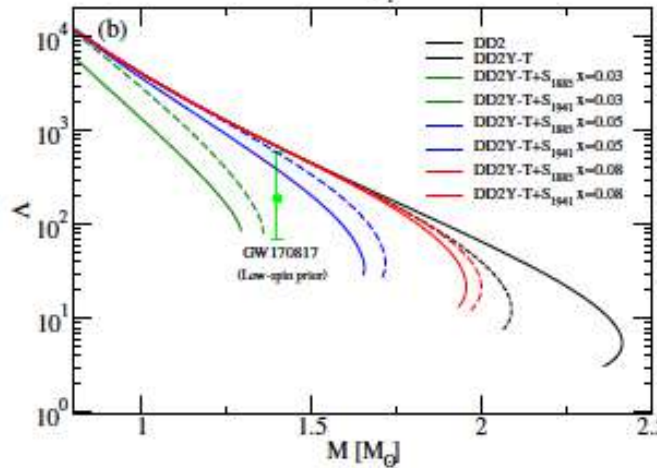
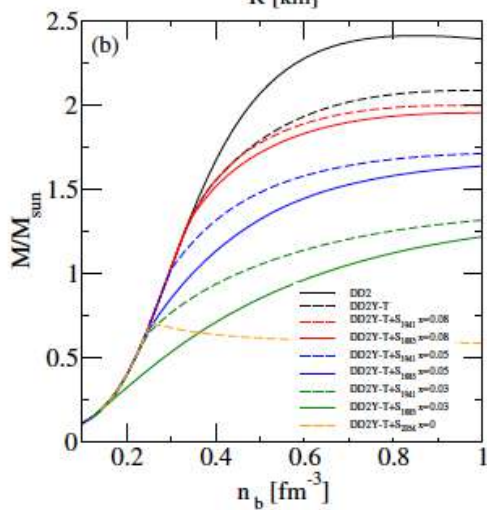
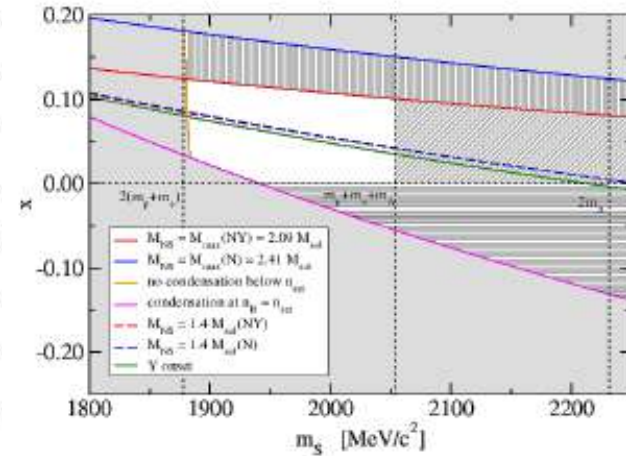
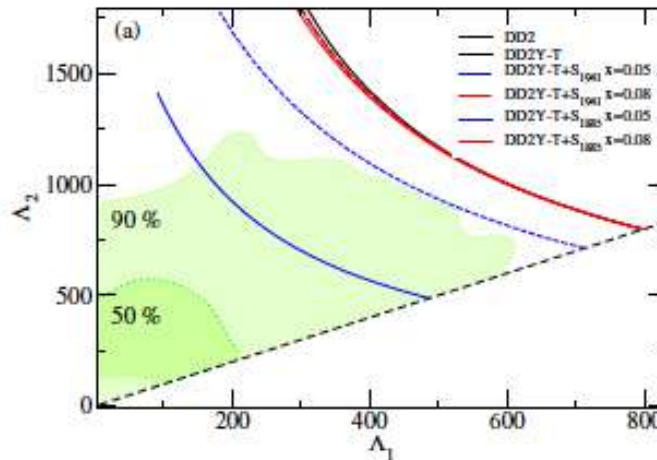
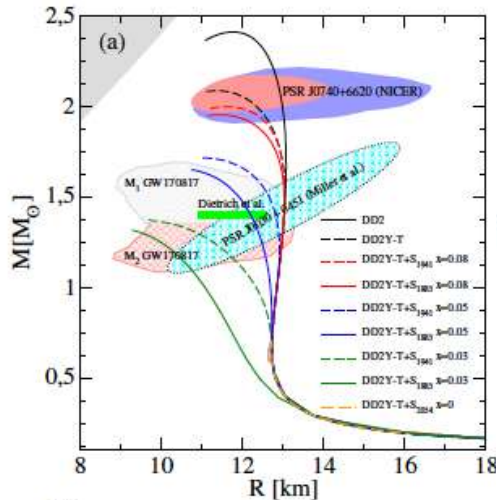


M. ShahrbaF et al., PRD 105, 103005

Light sexaquark – Dilemma for Neutron Stars ?

Problem: Sexaquark Bose-Einstein condensation

1. Solution: density-dependent mass $\rightarrow M_{\text{max}} \leftrightarrow$ Tidal deformab. Λ



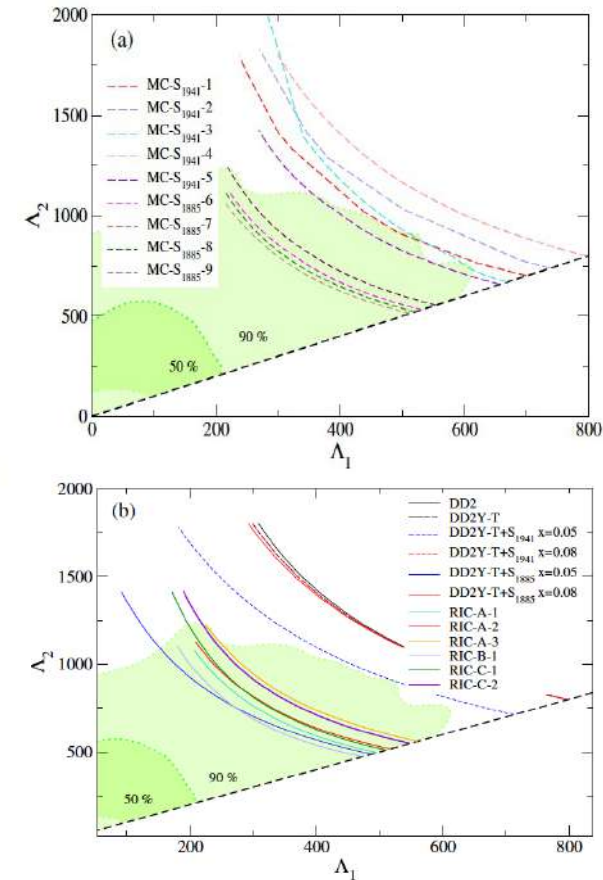
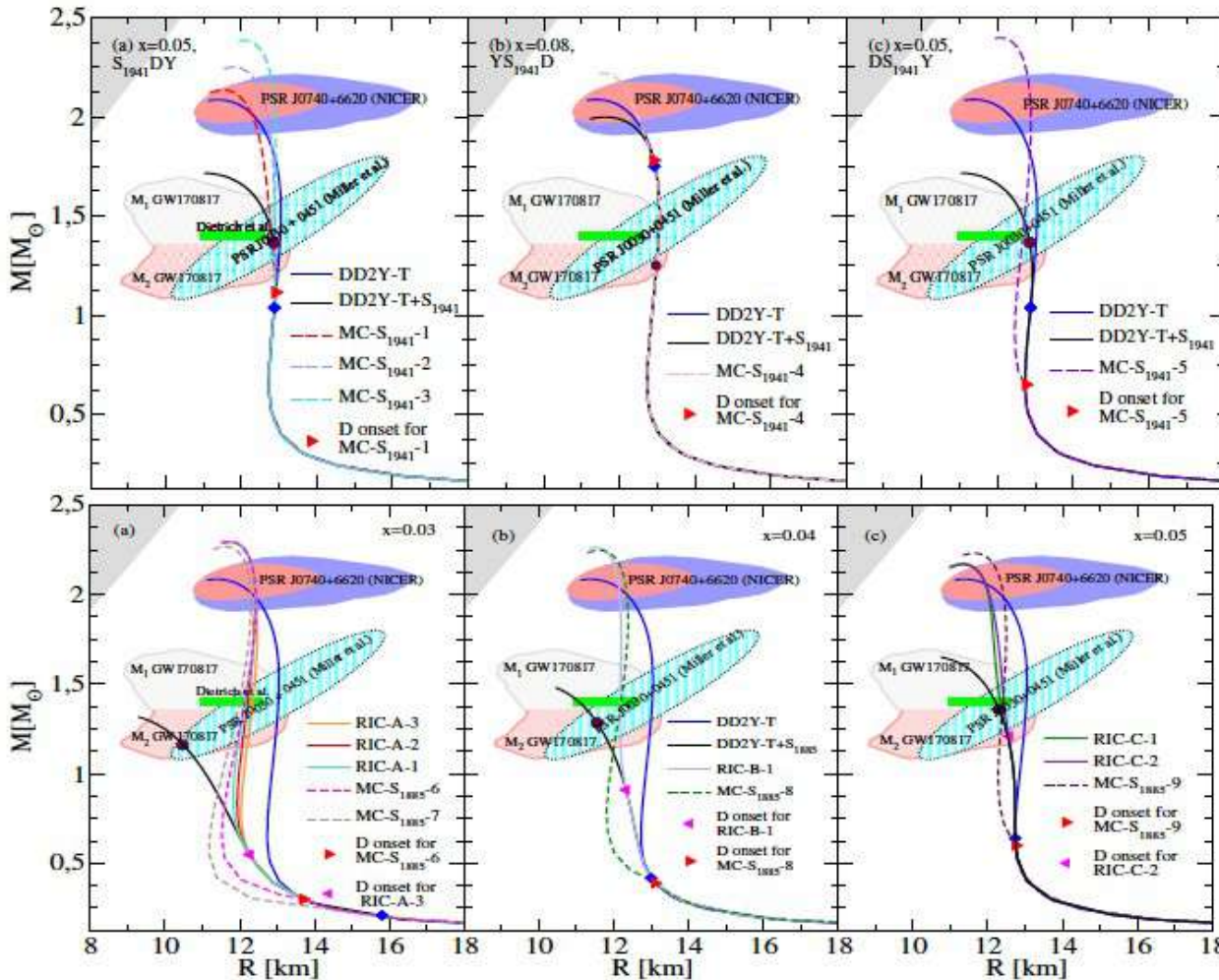
Constraint on M_S vs. slope x_s

M. ShahrbaF et al., PRD 105, 103005

Light sexaquark – Dilemma for Neutron Stars ?

Problem: Sexaquark Bose-Einstein condensation

1. Solution: density-dependent mass and quark deconfinement !!

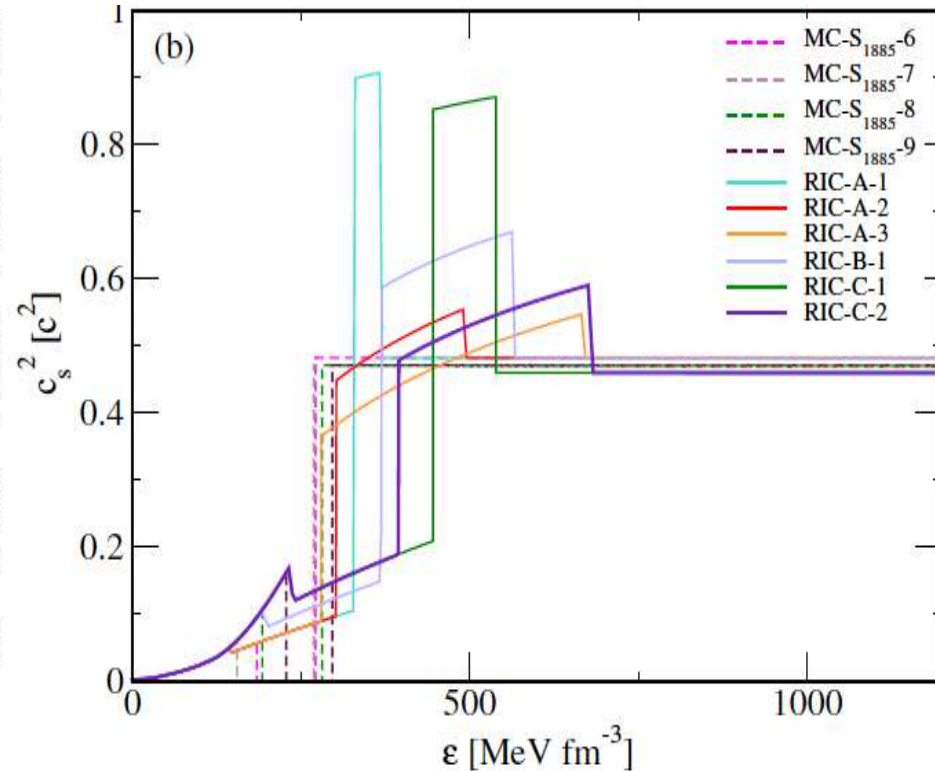
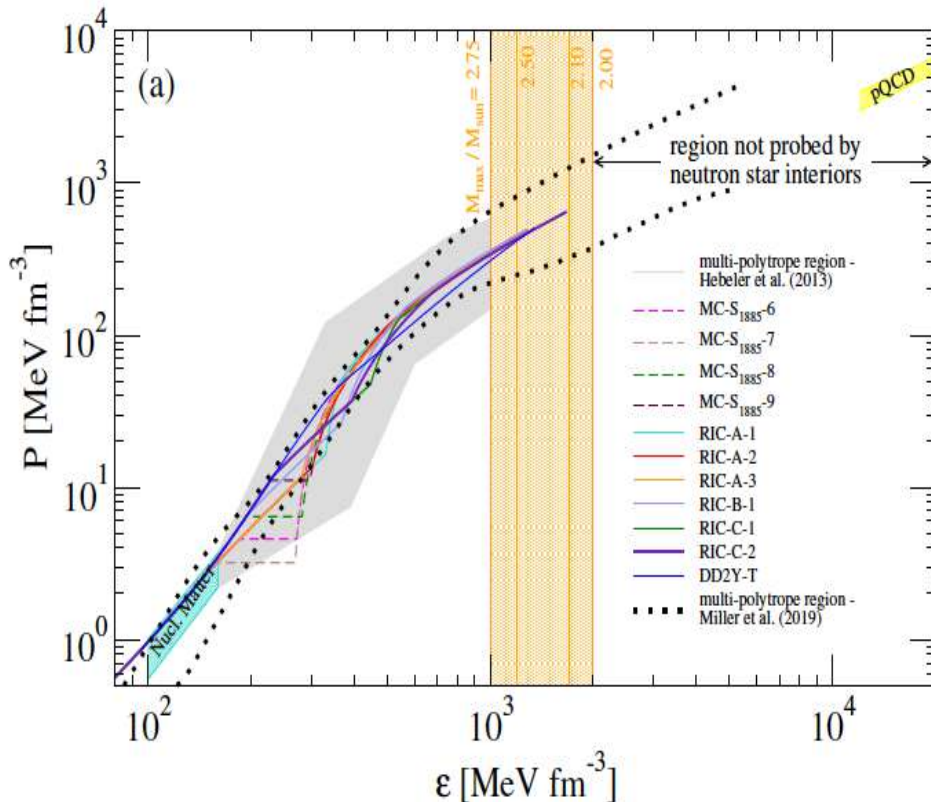


M. Shahrabaf et al.,
PRD105(2021)103005

Light sexaquark – Dilemma for Neutron Stars ?

Problem: Sexaquark Bose-Einstein condensation

1. Solution: density-dependent mass and quark deconfinement !!

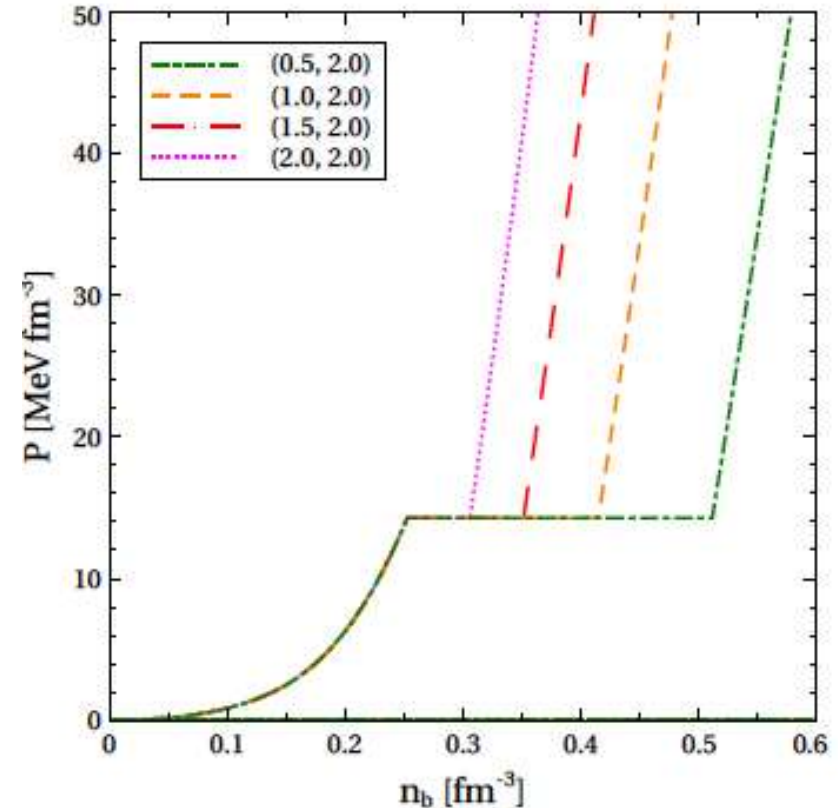
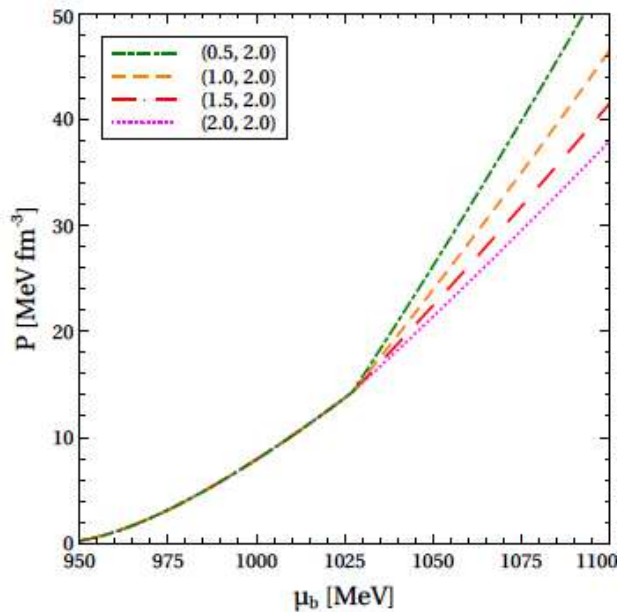
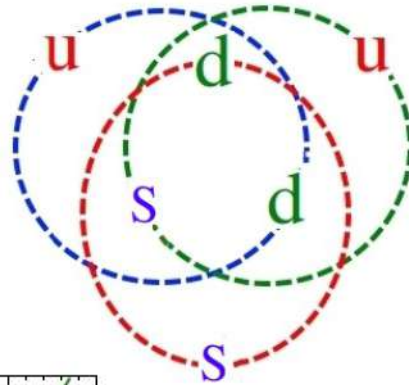
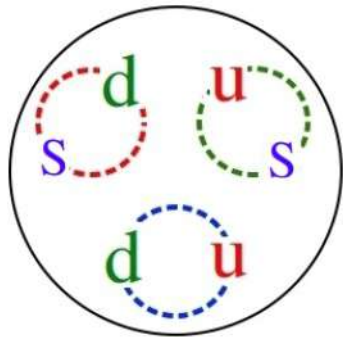


M. ShahrbaF et al., PRD 105, 103005

Light sexaquark – Dilemma for Neutron Stars ?

Problem: Sexaquark Bose-Einstein condensation

2. Solution: BEC of S triggers early deconfinement to CFL quark matter

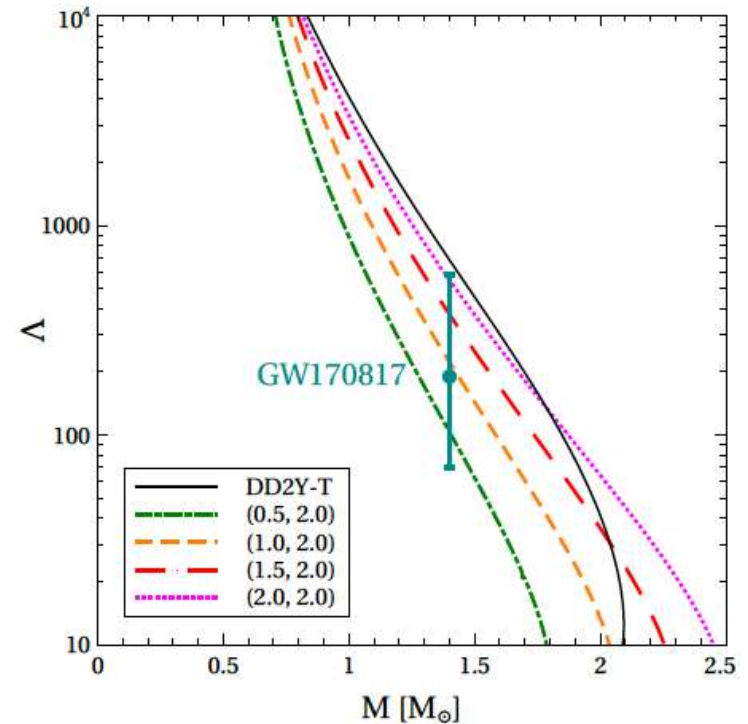
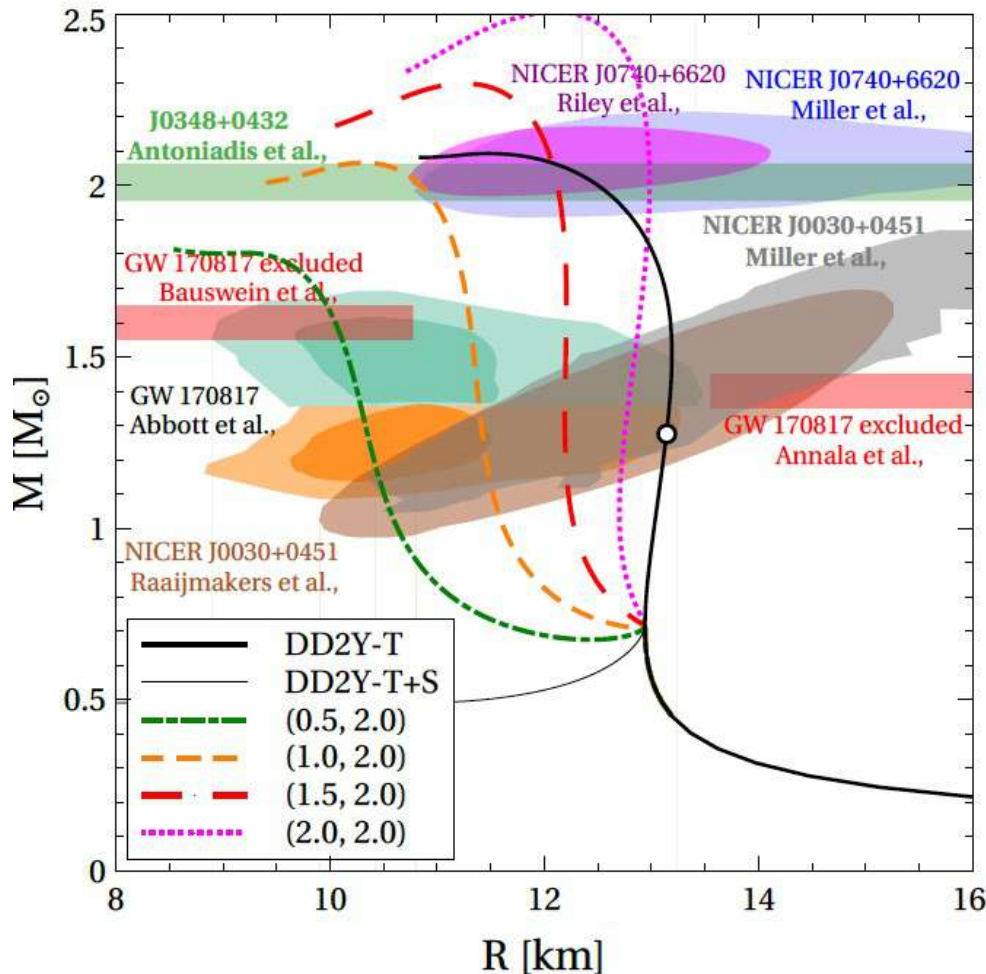


D. Blaschke et al., arXiv:2202.05061

Light sexaquark – Dilemma for Neutron Stars ?

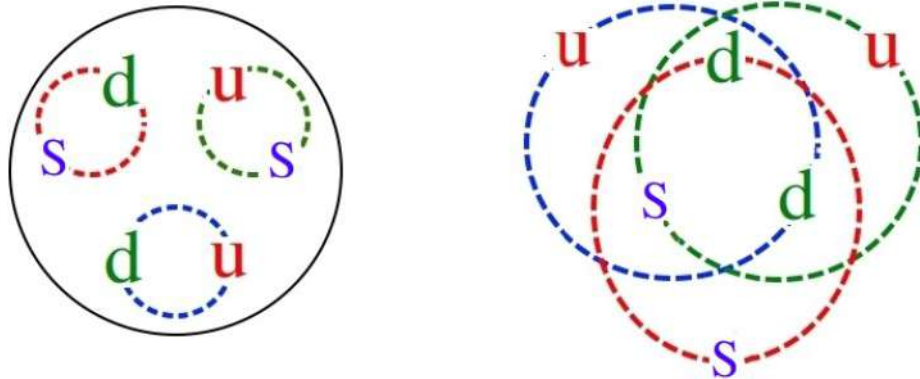
Problem: Sexaquark Bose-Einstein condensation

2. Solution: BEC of S triggers early deconfinement to CFL quark matter



All observational constraints are simultaneously fulfilled,
 → early onset of deconfinement!
 D. Blaschke et al., arXiv:2202.05061

Light sexaquark in NS: BEC-BSC crossover ?

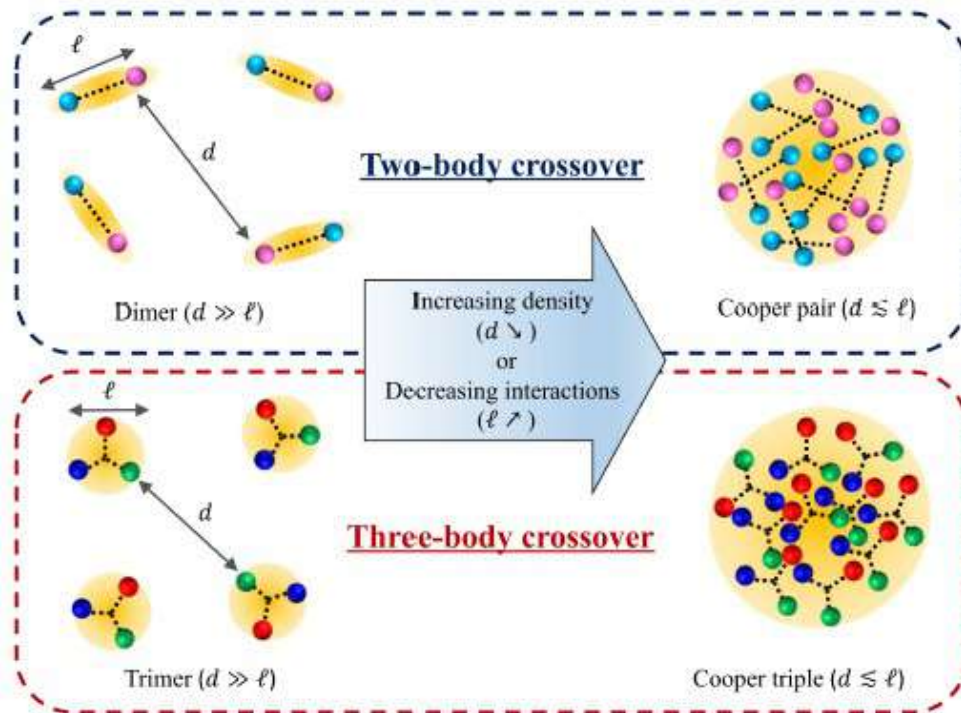


BEC → BCS crossover:
diquark Cooper triples !
(Efimov states?)

D. Blaschke et al., arXiv:2202.05061

H. Tajima et al., Symmetry 15, 333

„Density-induced hadron-quark crossover via the formation of Cooper triples“

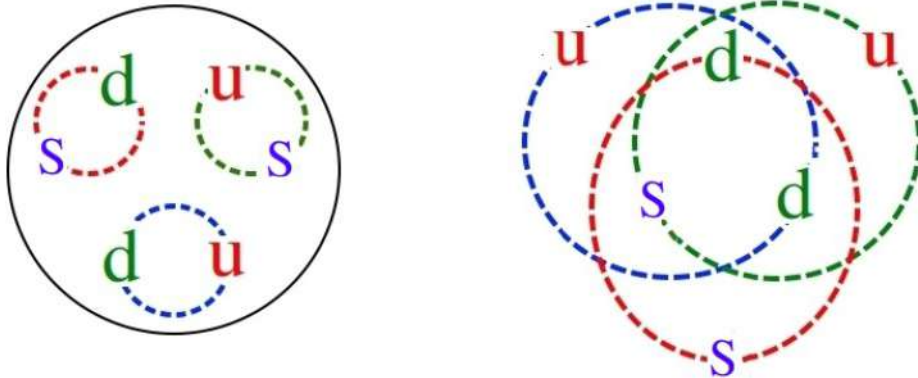


$$T_3(\Omega) = \frac{V_3}{1 - V_3 \Xi(\Omega)}$$

$$\Xi(\Omega) = \sum_{k,q} \frac{(1 - f_k)(1 - f_q)(1 - f_{k+q}) + f_k f_q f_{k+q}}{\Omega_+ + 3\mu - \epsilon_k - \epsilon_q - \epsilon_{k+q}}$$

$$f_k = \frac{1}{\exp\left(\frac{\epsilon_k - \mu}{T}\right) + 1}$$

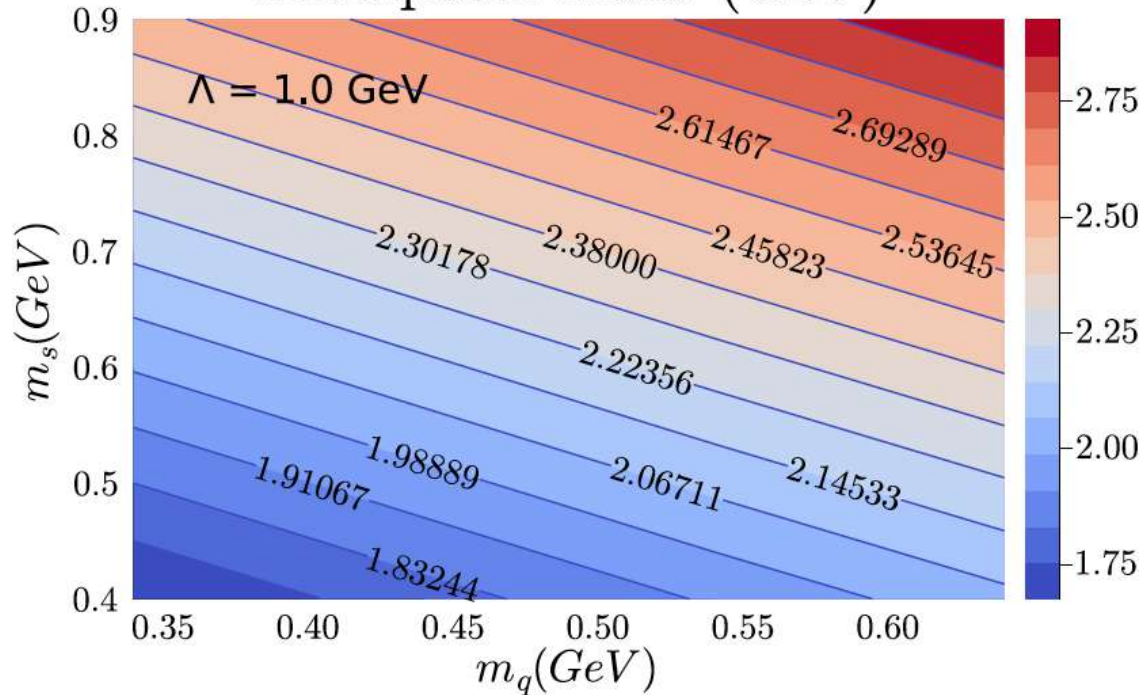
Light sexaquark in NS: BEC-BSC crossover ?



BEC → BCS crossover:
diquark Cooper triples !
(Efimov states?)

D. Blaschke et al., arXiv:2202.05061

Sexaquark Mass (GeV)



B. Mahato et al.,

„Density-induced hadron-quark crossover via the formation of diquark Cooper triples“

Replacement:

triplet quarks

→ antitriplet diquarks

$$T_3(\Omega) = \frac{V_3}{1 - V_3 E(\Omega)}$$

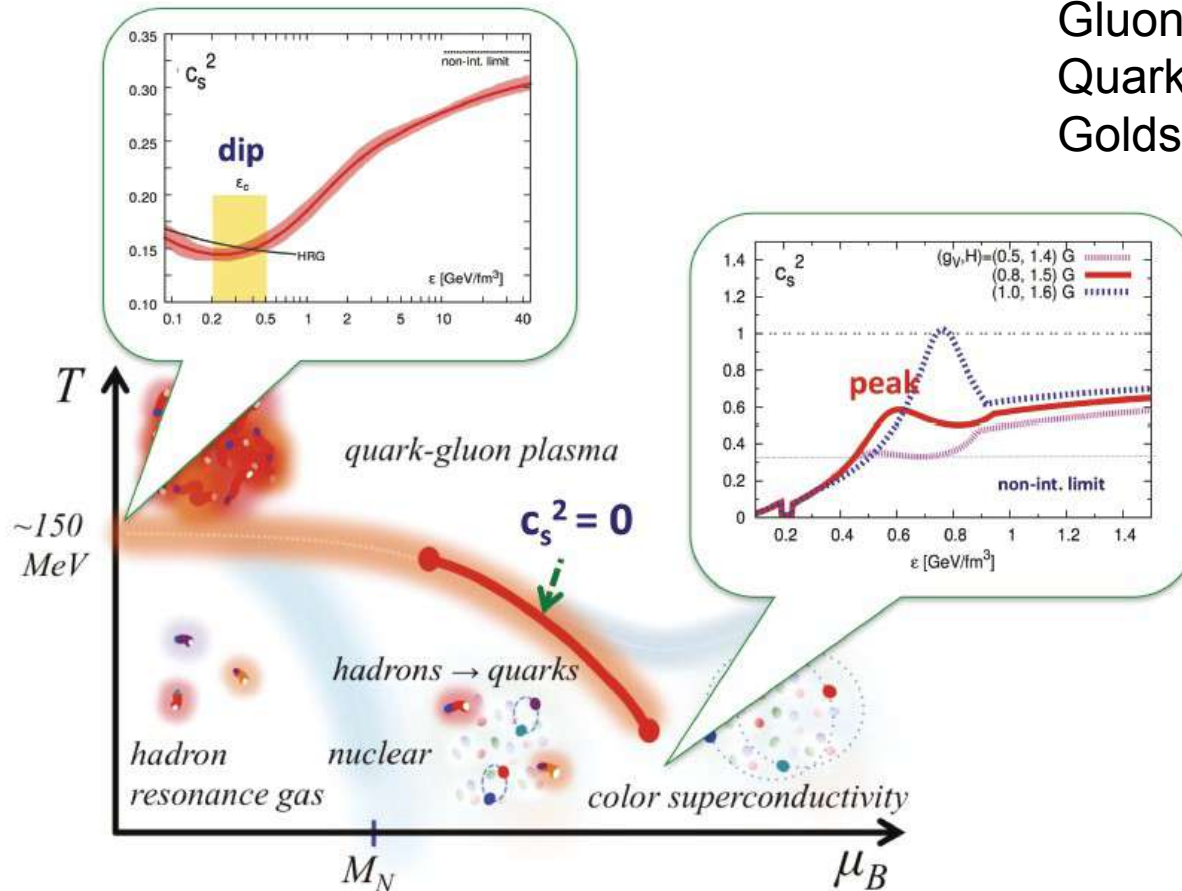
QCD Phase Diagram

Landscape of our investigations

Gluons \leftrightarrow Vector mesons

Quarks \leftrightarrow Baryons

Goldstones \leftrightarrow Pseudoscalar mesons



**Quark-Hadron
Duality?**

**Mutual influence of
Order parameters for
ChiSB and CSC**

From: T. Kojo,
“QCD equations of state in
quark-hadron continuity”,
Universe 4 (2018) 42

T. Schaefer & F. Wilczek, Phys. Rev. Lett. 82 (1999) 3956

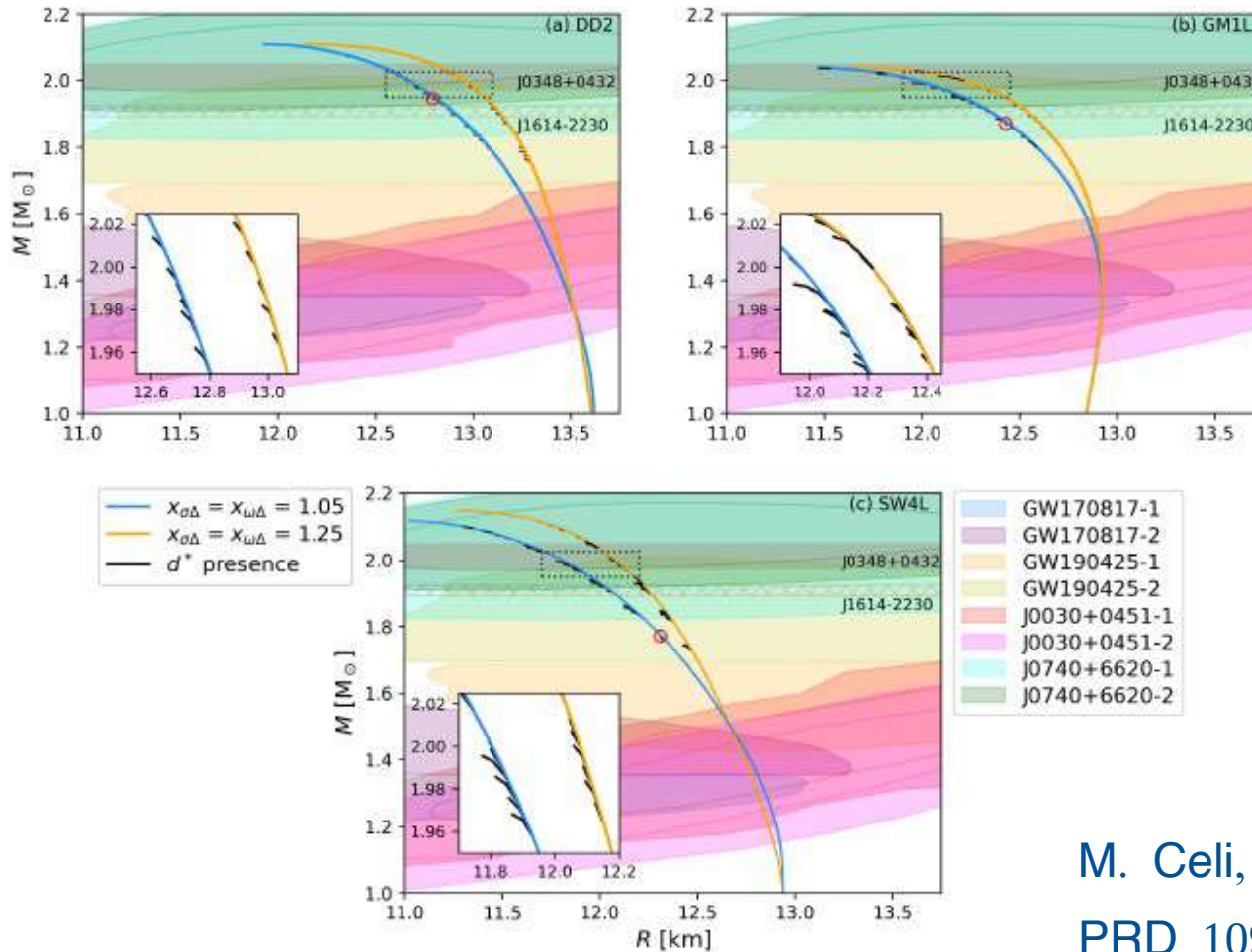
C. Wetterich, Phys. Lett. B 462 (1999) 164

T. Hatsuda, M. Tachibana, T. Yamamoto & G. Baym, Phys. Rev. Lett. 97 (2006) 122001

Hexaquark $d^*(2380)$ – Another Dilemma for NS?

Problem: Hexaquark Bose-Einstein condensation

1. Solution: Onset of BEC only at high NS masses



M. Celi, M. Bashkanov et al.,
PRD 109 (2024) 023004

Hexaquark $d^*(2380)$ – Another Dilemma for NS?



Problem: Hexaquark Bose-Einstein condensation

2. Solution: d^* hexaquark BEC triggers crossover to 2SC quark matter in NS

Interesting scenario ... not yet realised!

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Charmed Hexaquark $H(ucsddd)$ – Another Dilemma for NS?

No!

Since $d^*(2380)$ surely exists and $H(ucsddd)$ has to be heavier, its appearance in neutron stars is circumvented by either S or d^*

Group photo in the Oratorium Marianum Hall CPOD 2016 Conference, University of Wroclaw

