

# Measuring Correlations in Isospin Asymmetric Nuclei

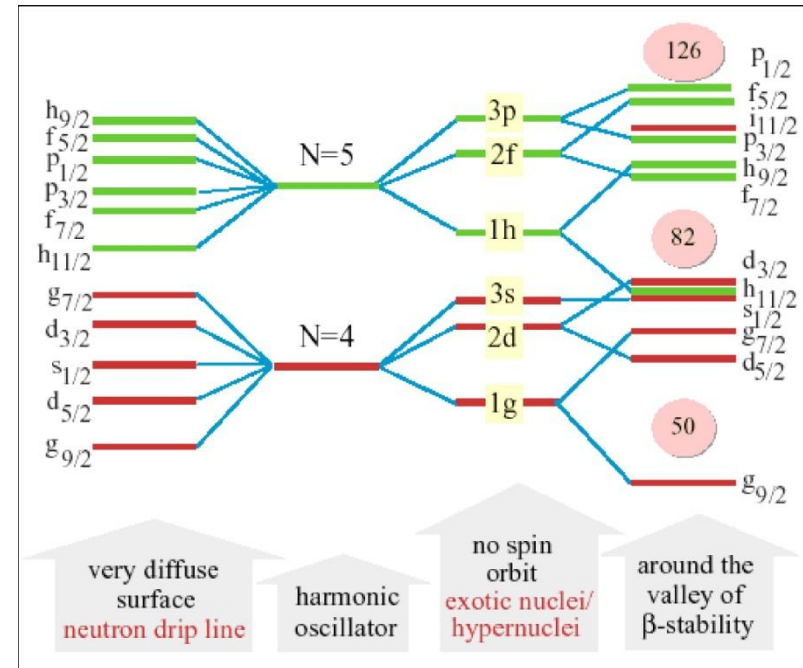
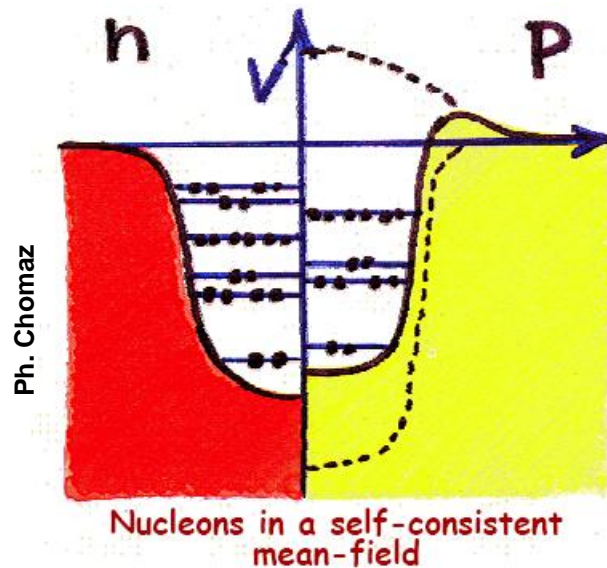
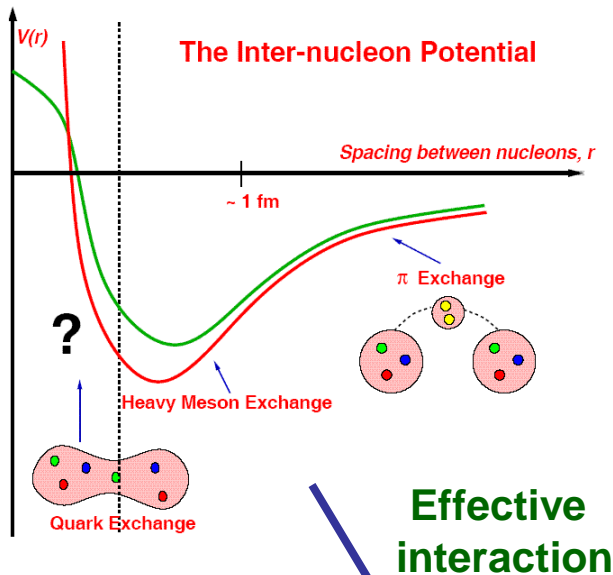
## Why and How ?

Roy Lemmon  
STFC Daresbury Laboratory  
United Kingdom

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EMMI Programme  
The Extreme Matter Physics of Nuclei: From Universal Properties to Neutron-Rich Extremes  
GSI, Darmstadt, Germany, 16 April – 11 May, 2012

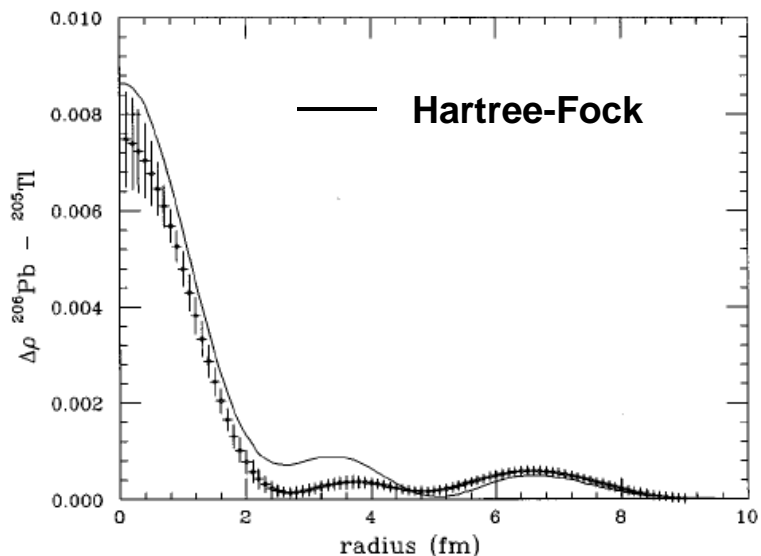
# Mean Field Model of Nuclei



- fermion system at low energies
- suppression of collisions by Pauli exclusion
- independent particle motion
- shell structure
- mean field approximation

# Validity of Mean Field Concept of Nuclei

J. Cavedon et al., Phys. Rev. Lett. 49 (1982) 978.

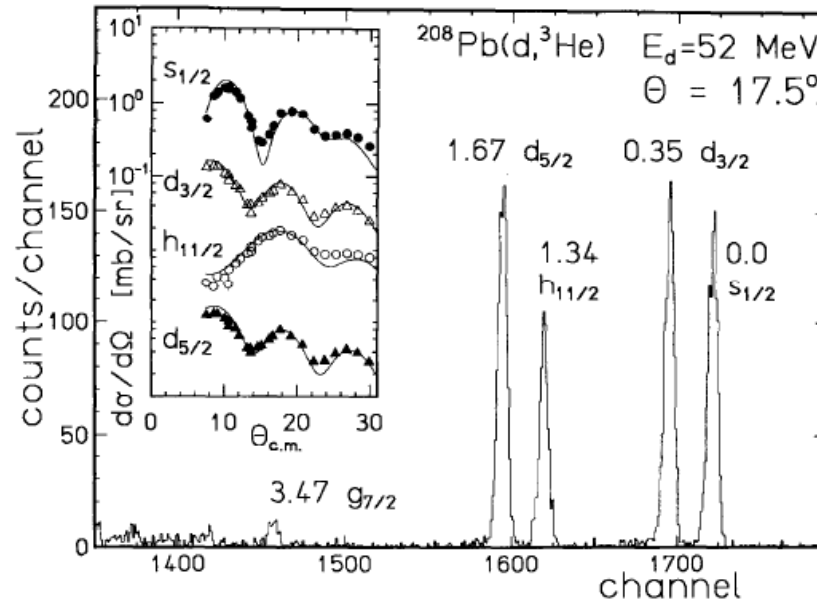


## Electron Scattering

Charge density difference between  $^{206}\text{Pb}$  and  $^{205}\text{Tl}$   
 $^{206}\text{Pb}$  and  $^{205}\text{Tl}$  differ in IPM by one  $3s_{1/2}$  proton

## Transfer Reactions

Only four strong transitions in  $^{208}\text{Pb}(d, ^3\text{He})$   
 Pickup from  $3s_{1/2}$ ,  $2d_{3/2}$ ,  $1h_{11/2}$  and  $1d_{5/2}$



P. Grabmayr et al., Nucl. Phys. A 494 (1989) 244.

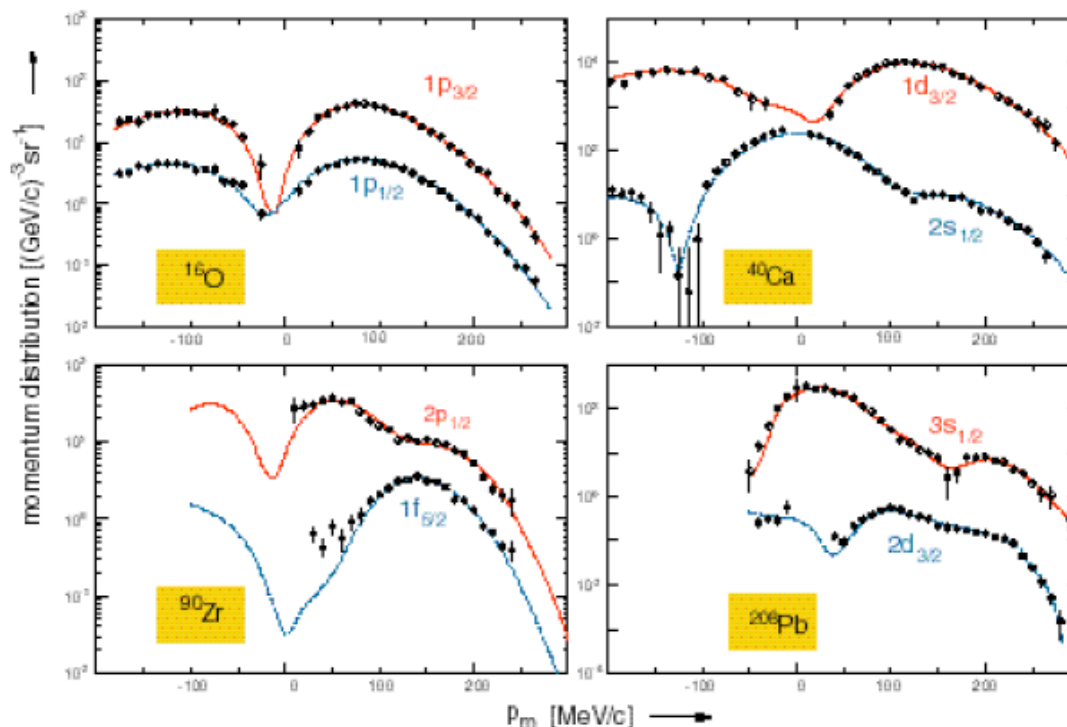
# Breakdown of Mean Field Concept

## Introduction Some early (e,e'p) results

### Spectroscopic strength with the reaction (e,e'p)

- seventies : pioneering experiments Frascati, Tokyo, Saclay
- eighties : high res. NIKHEF (e,e'p) program for nuclei A=2-209
  - spectral function at low ( $E_m$ ,  $p_m$ )
  - Momentum distributions of **valence orbits**
- nineties –present : NIKHEF/Mainz/Bates also 2N knockout
- present : JLAB towards higher  $Q^2$ , larger  $p_m$ ,  $E_m$

## NIKHEF RESULTS

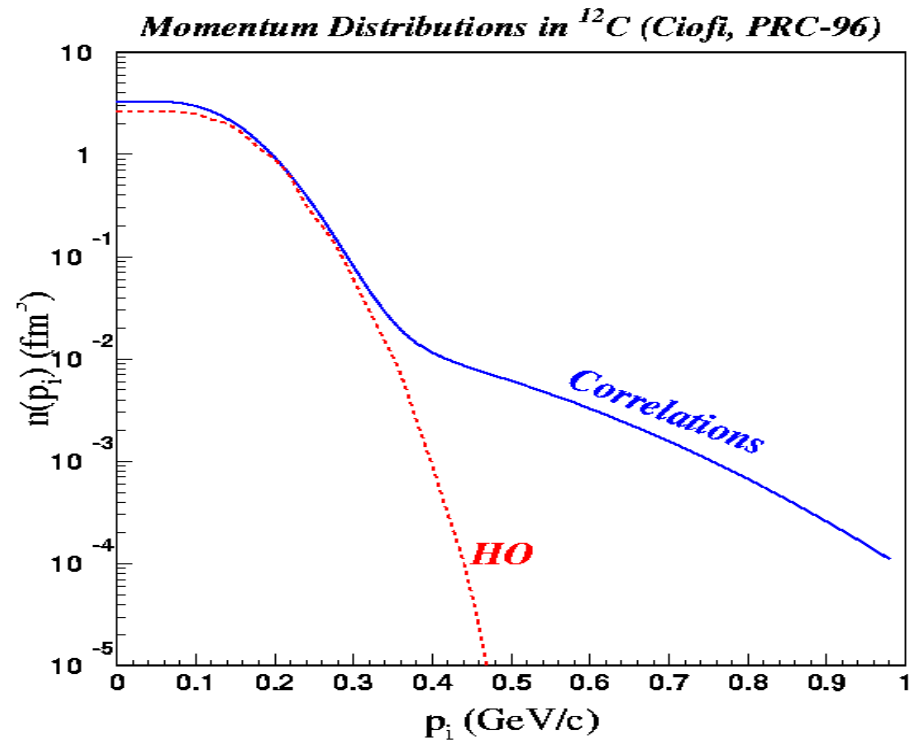
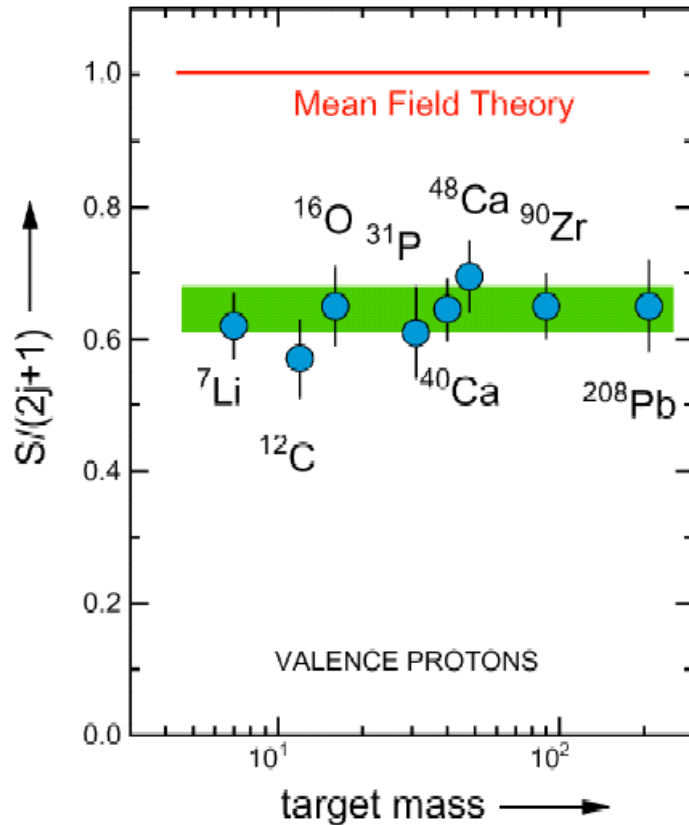


Results for **valence** orbits  
in closed-shell nuclei:

Curves scaled by about  
**0.65**  
wrt. mean field theory !!

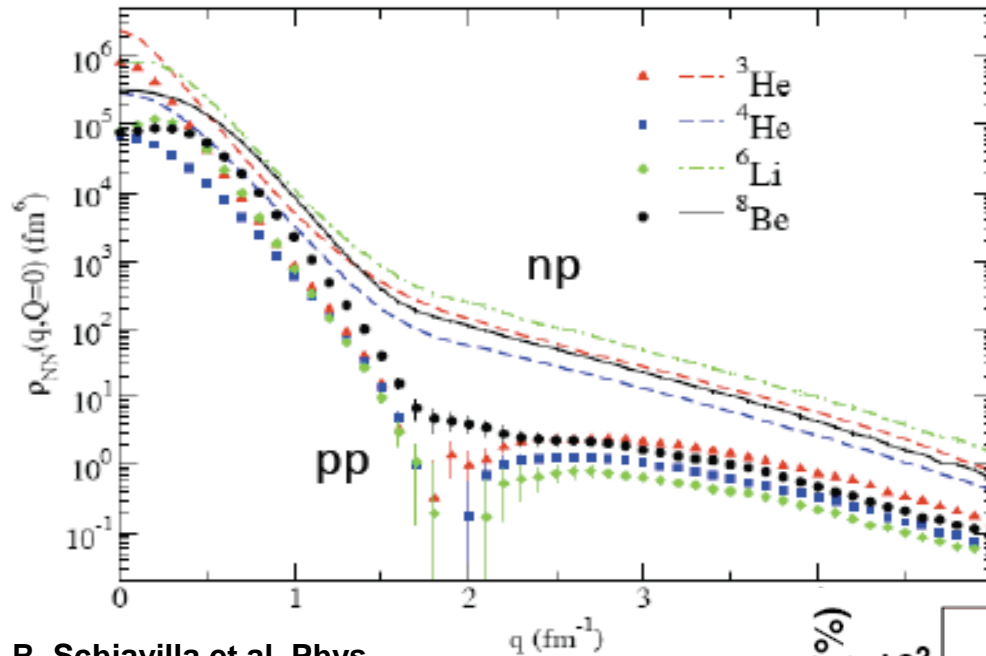
Explanation : Effect of  
**long-range**  
**and**  
**short-range**  
**correlations**

# Correlations in (Near-) Symmetric Nuclei



Reduction in spectroscopic strength relative to mean field  
 -> Long-range, tensor and short-range correlations

# Measurement of High-Momentum Nucleon Pairs

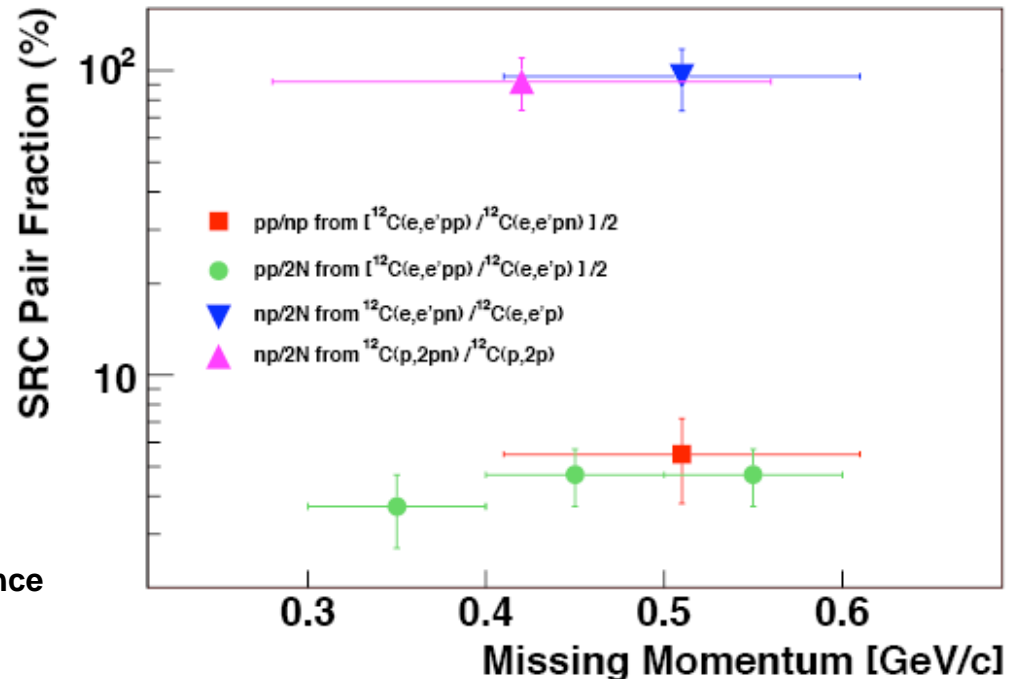


R. Schiavilla et al., Phys. Rev. Lett. 98 (2007) 132501.

- 20x more pn than pp/nn
- Tensor correlations

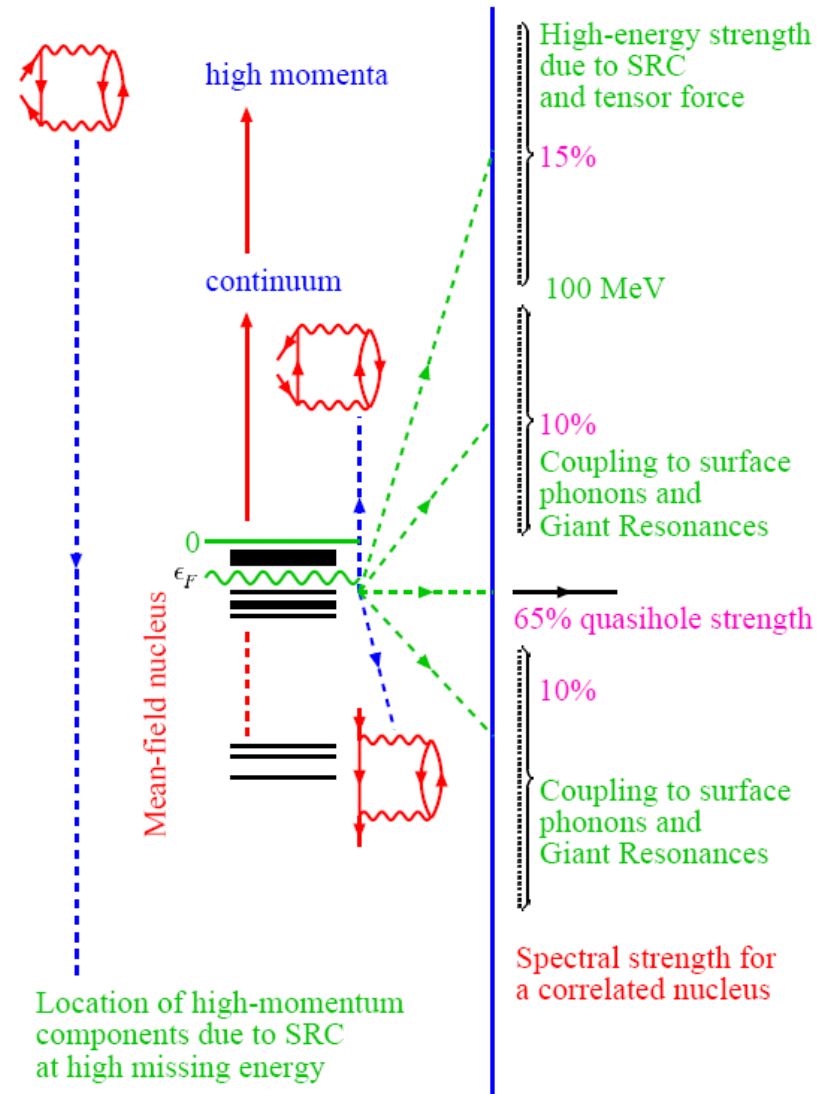
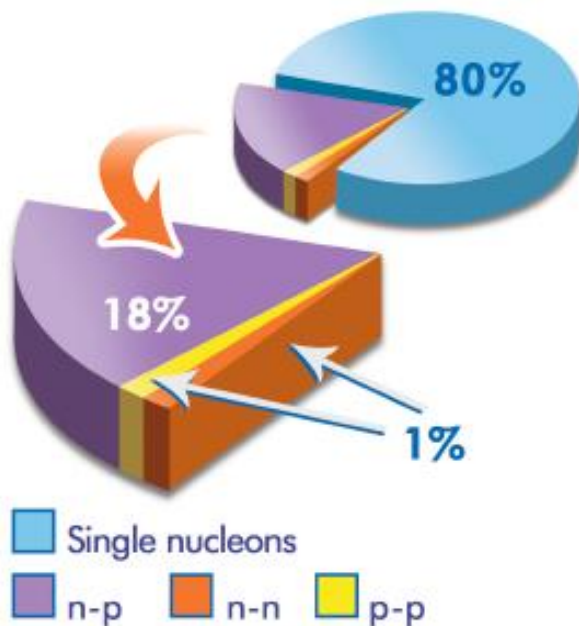
From (e,e'pN) and (p,2pN) data on **symmetric** nuclei (JLab, BNL, NIKHEF, Mainz ...):

R. Subedi et al., Science 320 (2008) 1476.



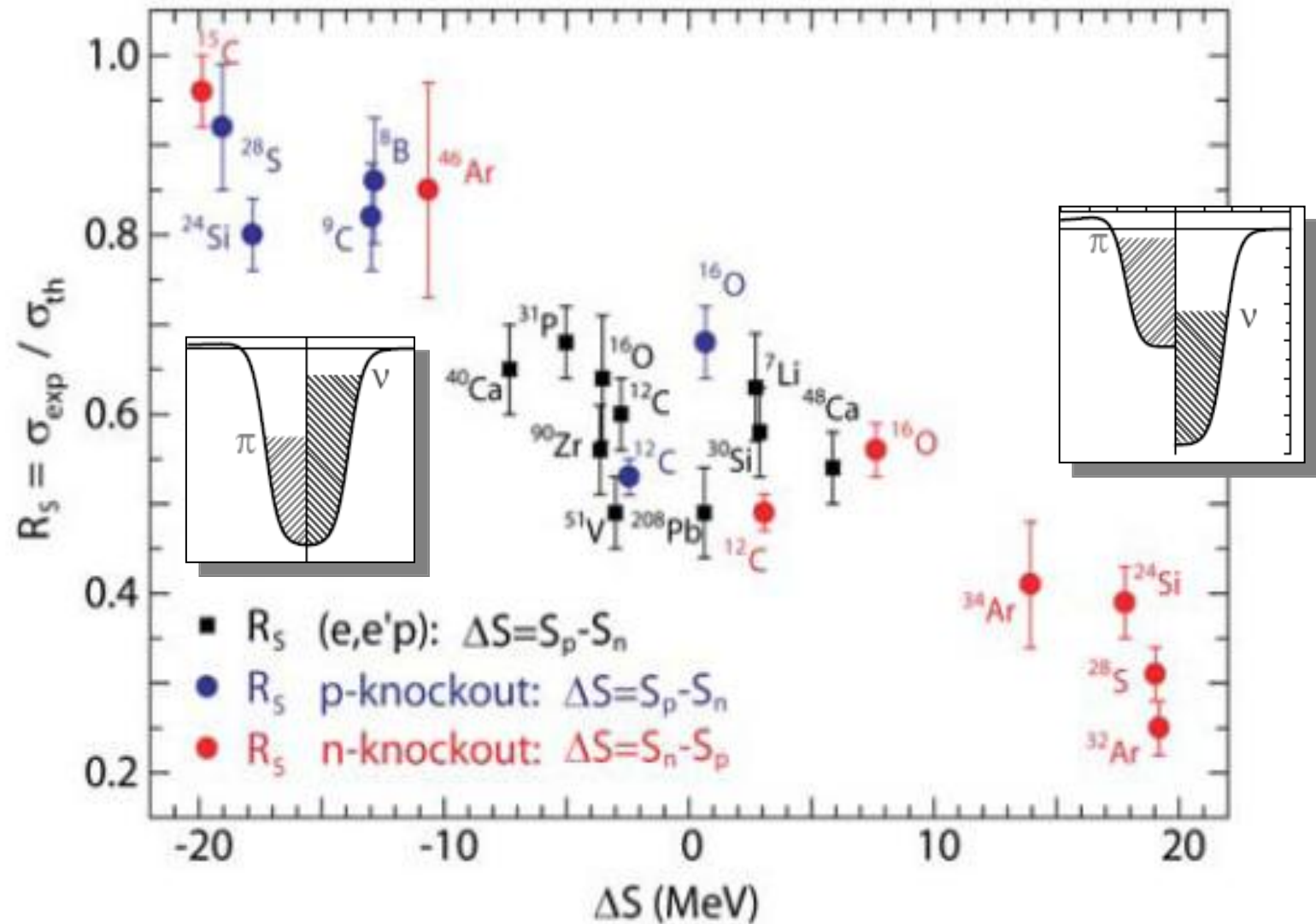
# Our Present Knowledge of Proton Behaviour in Symmetric Nuclei

- $80 \pm 5\%$  single particles moving in average potential
  - 60-70% independent single particle in a shell model potential
  - 10-20% shell model long range interactions
- $20 \pm 5\%$  two-nucleon short-range and tensor correlations:



# Correlations in Asymmetric Nuclei

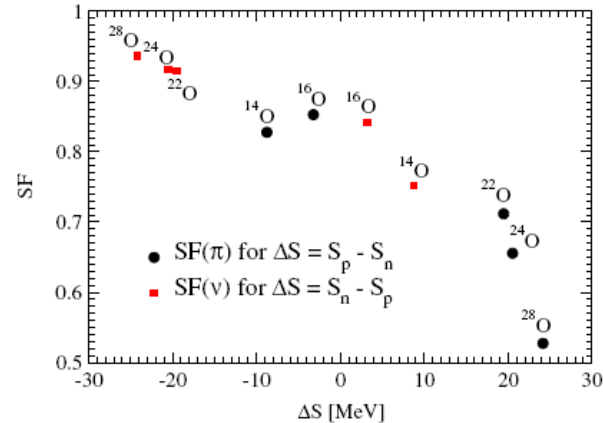
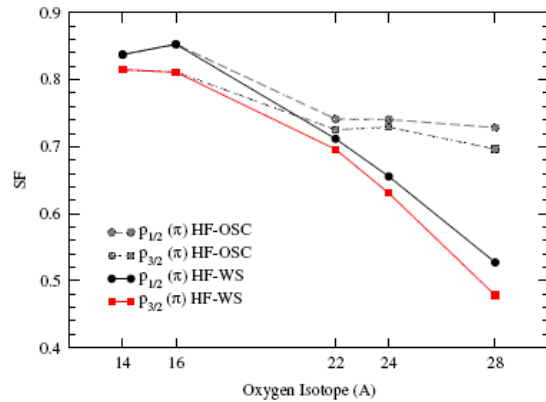
## 1n Removal Reactions





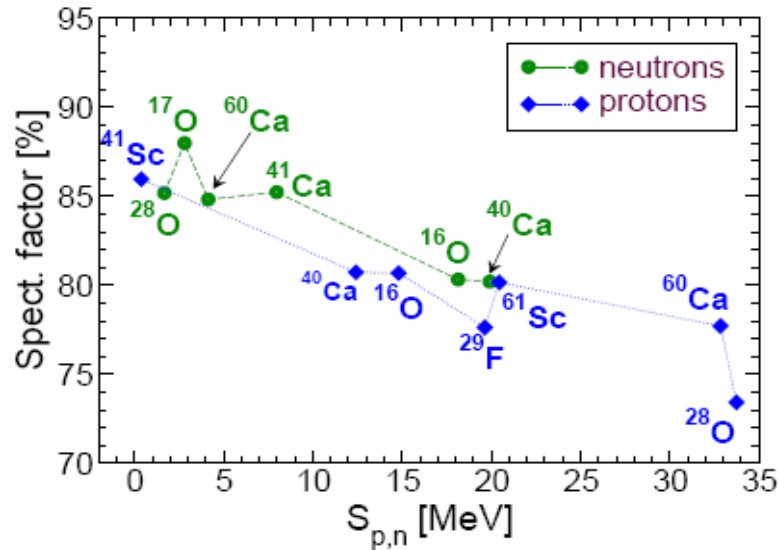
# Quenching of Spectroscopic Factors for Proton Removal in Oxygen Isotopes

Ø. Jensen,<sup>1</sup> G. Hagen,<sup>2,3</sup> M. Hjorth-Jensen,<sup>1</sup> B. Alex Brown,<sup>4,5</sup> and A. Gade<sup>4,5</sup>



Coupled-cluster calculation N<sup>3</sup>LO

including coupling to scattering states above the neutron separation threshold

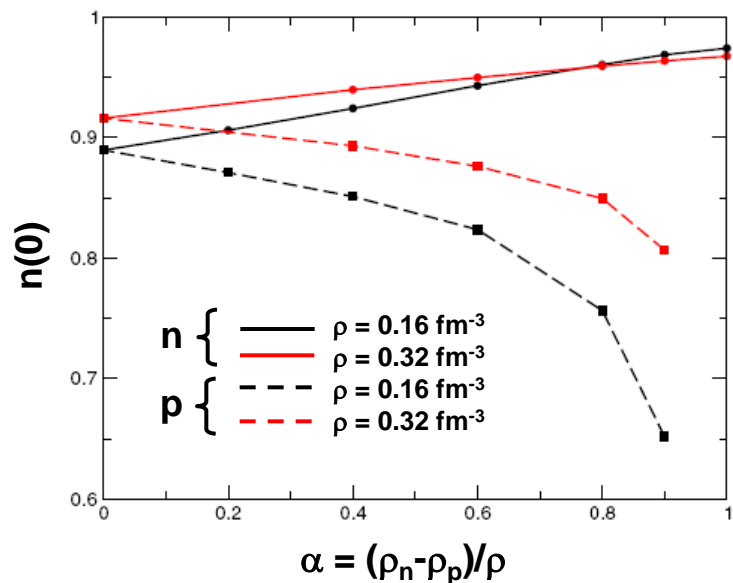
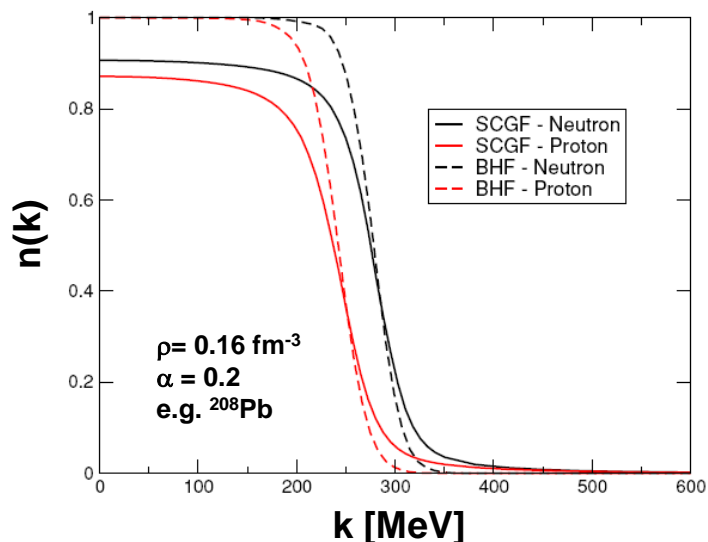


C. Barbieri et al.,  
arXiv:0901.1920v1 (2009).

SCGF method using chiral N3LO force

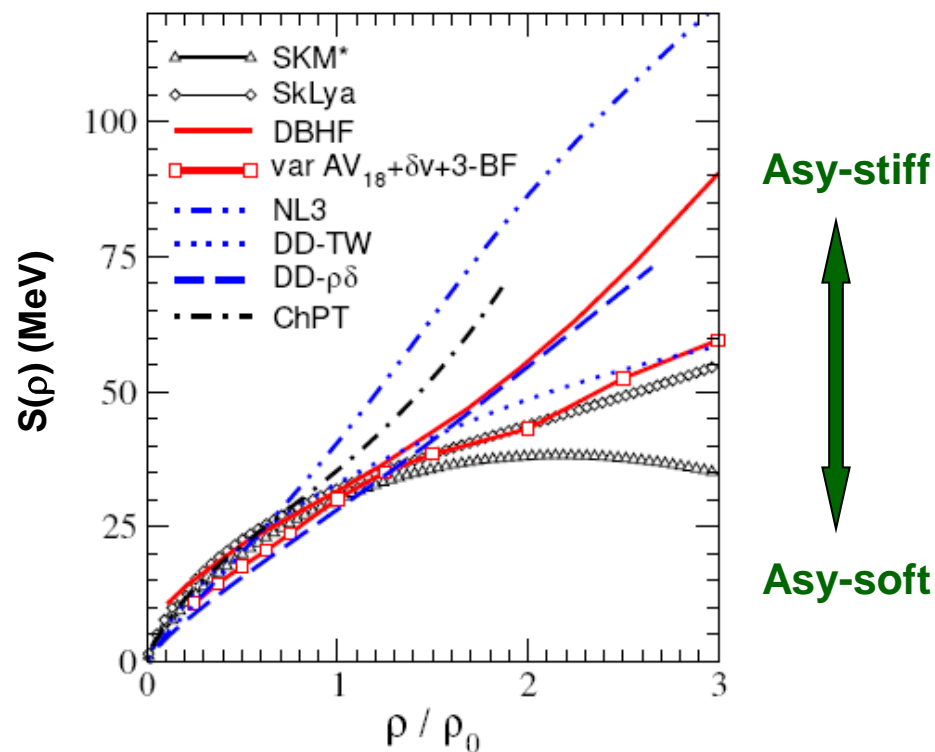
# SRC in Isospin Asymmetric Matter

Brueckner-Hartree Fock (BHF)  
Self-Consistent Green's Function (SCGF)



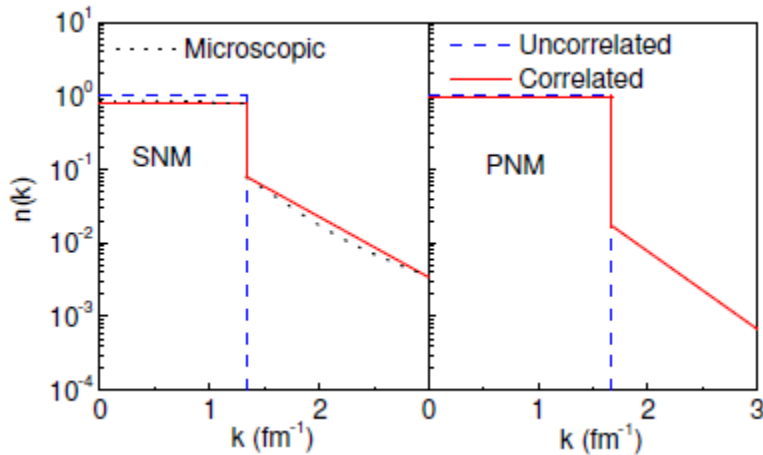
T. Frick et al. PRC 71 (2005) 014313.

$$E/A(\rho, \delta) = E/A(\rho, 0) + \delta^2 S(\rho)$$



Dependence of correlations on density, isospin asymmetry etc. is vital to understand asymmetric matter: EOS, neutron stars etc.

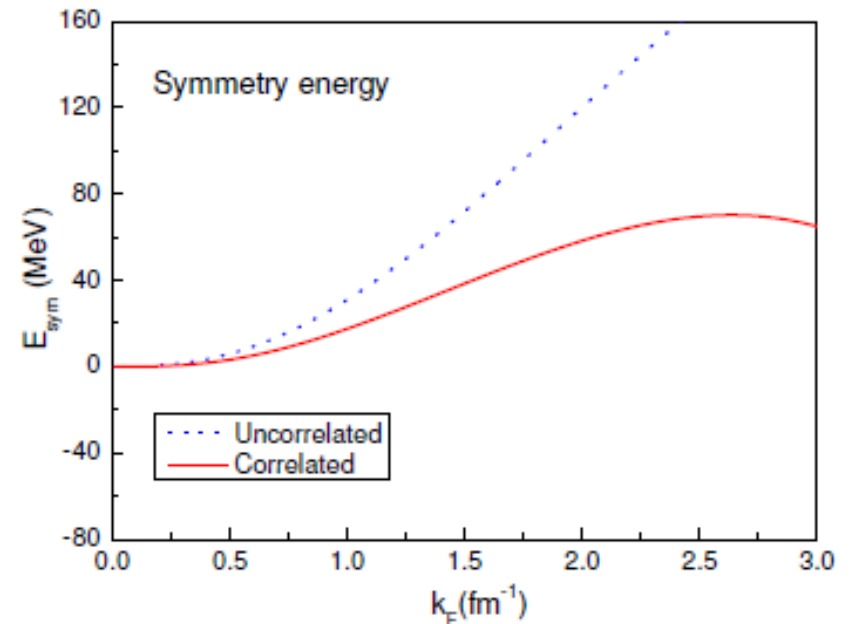
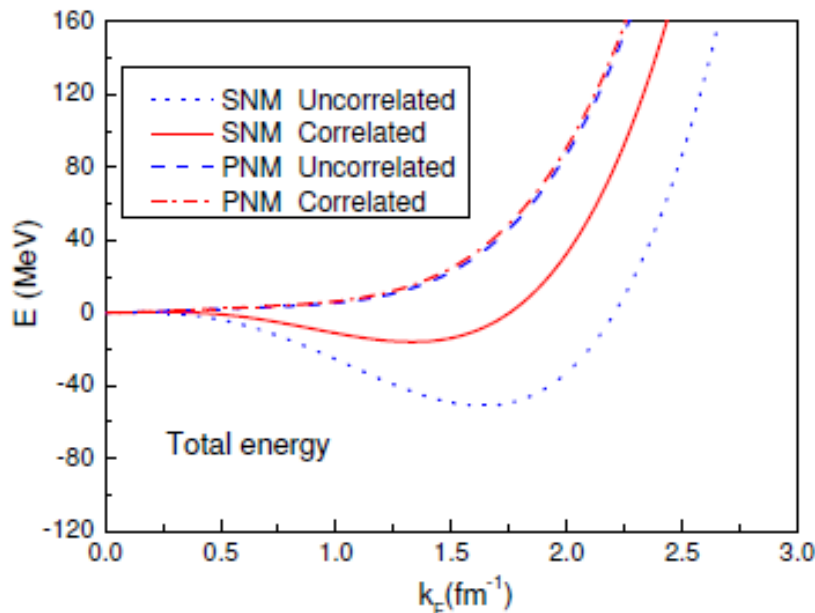
# Effect of Isospin Dependence of SRC on Nucleonic EOS



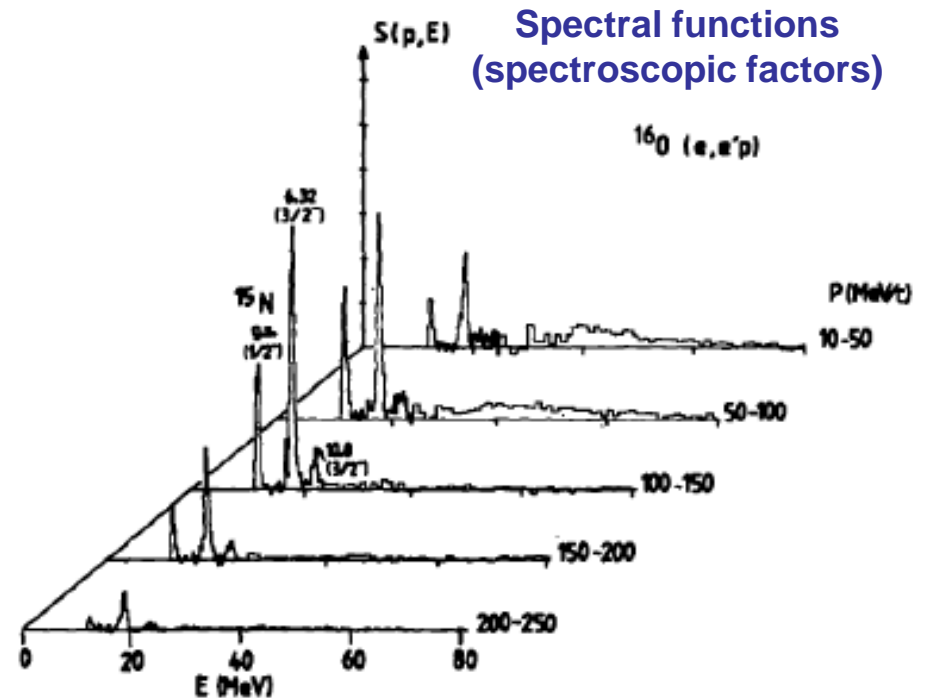
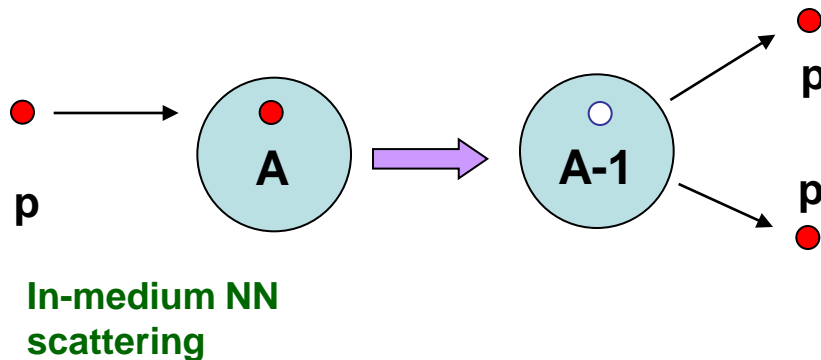
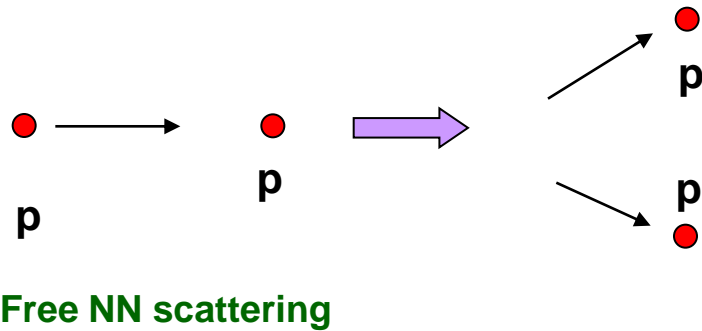
- Constrained to match measured isospin dependence of SRC
- Softening of symmetry energy

C. Xu and B.-A. Li, arXiv:1104.2075v1

A. Carbone and A. Rios, arXiv.1111.0797v2



# Probing Nucleon-Nucleon Correlations Experimentally



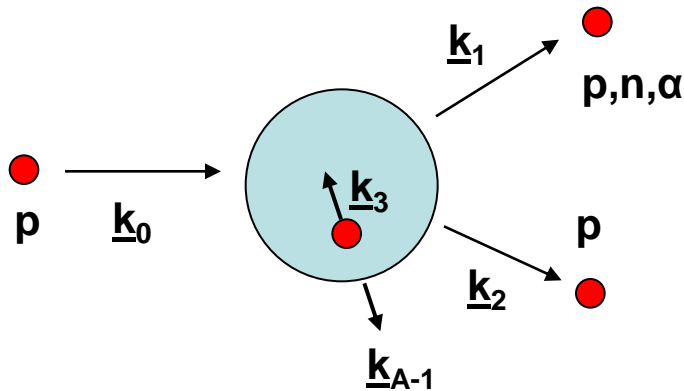
QFS most direct probe of the properties of a nucleon inside the nuclear medium:

- validity of mean field/single particle concepts
- role of correlations, e.g. LRC, SRC, Tensor
- in-medium nucleon-nucleon interaction

# Quasifree Scattering Reaction: Normal Kinematics

High energy protons,  $E_p = 100\text{-}1000\text{ MeV}$

- simplify reaction mechanism: impulse approximation
- minimise final state interactions: spectator nucleons



Measure  $k_1$  and  $k_2$ .  
 $k_{A-1}$  not measured directly.

Nuclear recoil momentum :

$$k_{A-1} = k_0 - k_1 - k_2 = -k_3$$

Separation energy of knocked-out nucleon

$$E_s = E_0 - E_1 - E_2 - \frac{k_{A-1}^2}{2(A-1)}$$

Distortion of the incoming and outgoing nucleon wavefunctions (from final state interactions, multiple scattering):

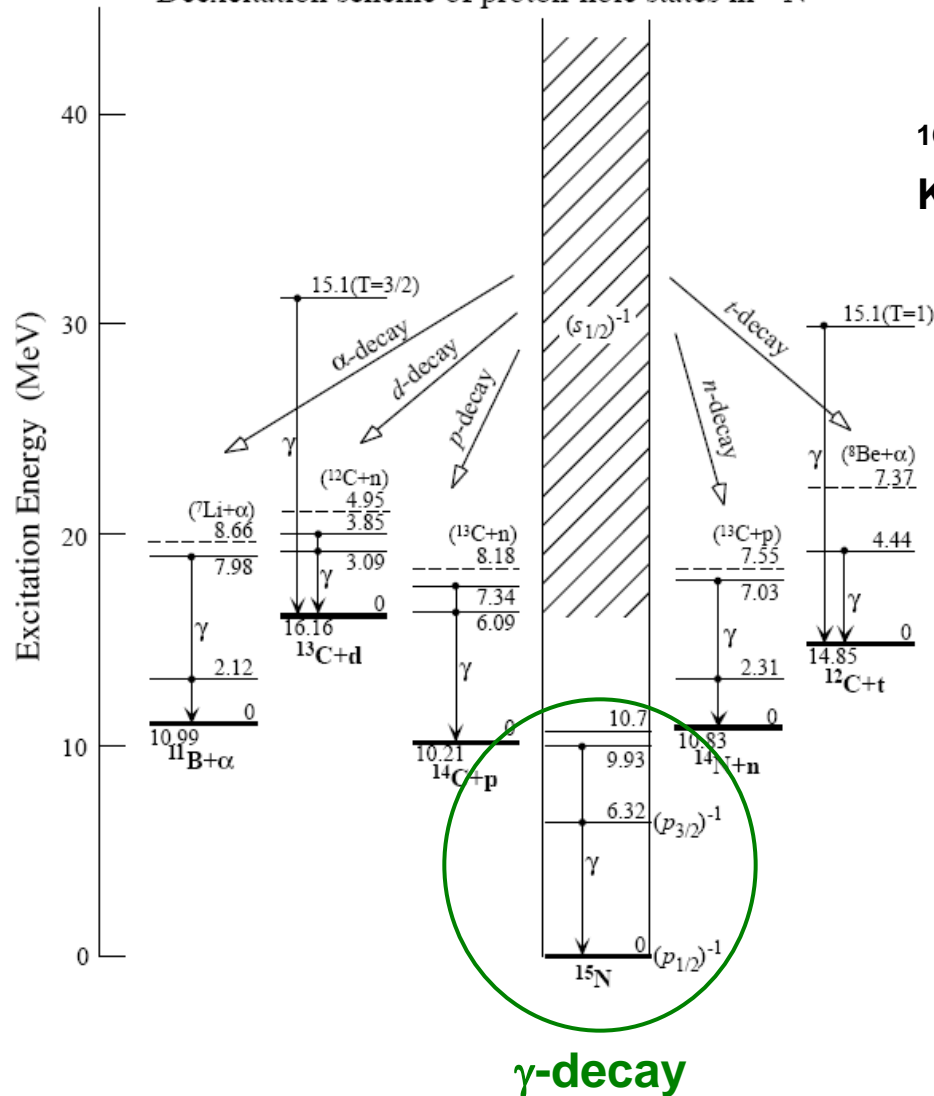
**Distorted Wave Impulse Approximation**

$$\frac{d^3\sigma}{d\Omega_1 d\Omega_2 dE} = \underbrace{S_3}_{\text{spectroscopic factor}} \underbrace{F_k \frac{d\sigma_{pp}}{d\Omega}}_{\text{free n-n cross-section}} \underbrace{G(\vec{k}_3)}_{\text{distorted momentum distribution}}$$

spectroscopic factor      free n-n cross-section      distorted momentum distribution

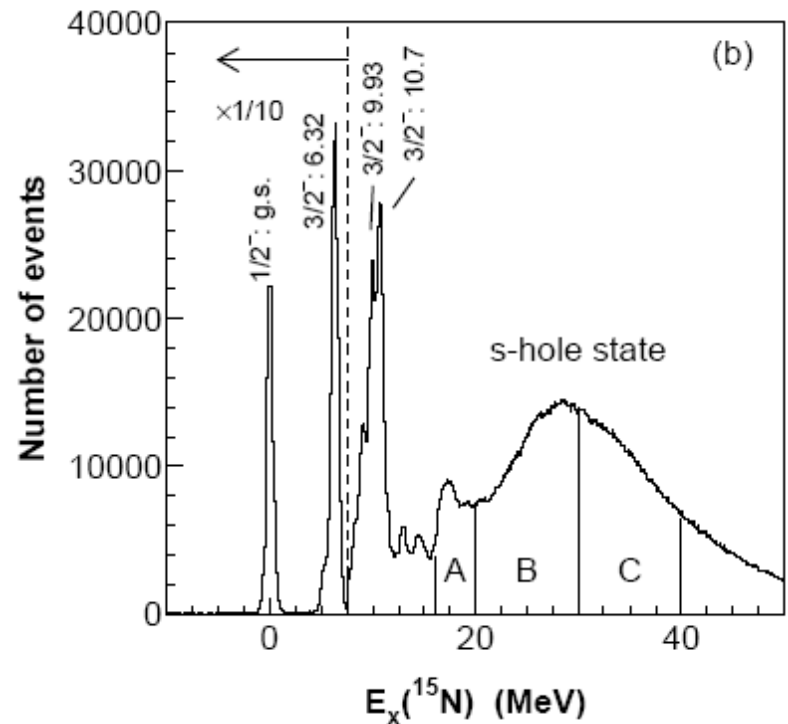
# States Populated in Quasifree Hadronic Scattering

Deexcitation scheme of proton-hole states in  $^{15}\text{N}$

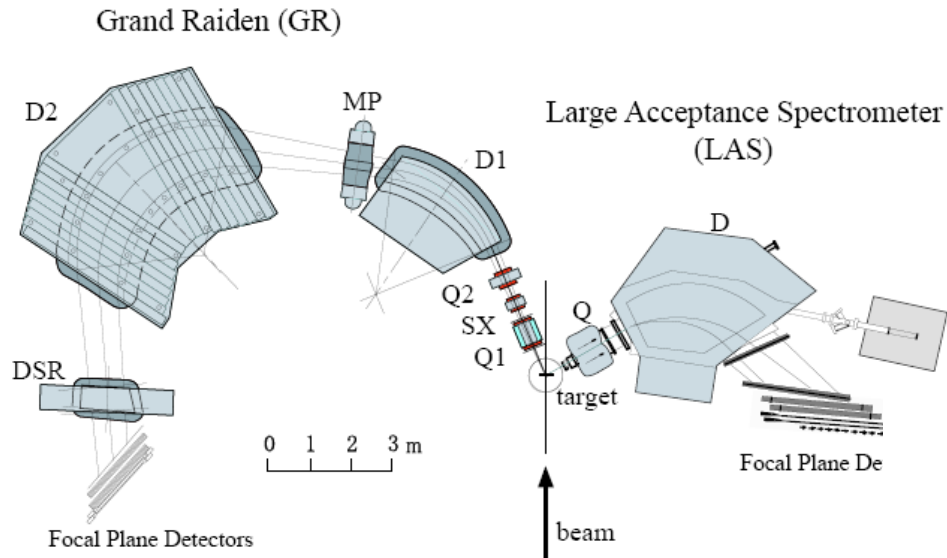


$^{16}\text{O}(p,2p)^{15}\text{N}$ ,  $E_{\text{beam}} = 392 \text{ AMeV}$

K. Kobayashi et al., arXiv:nucl-ex/0604006



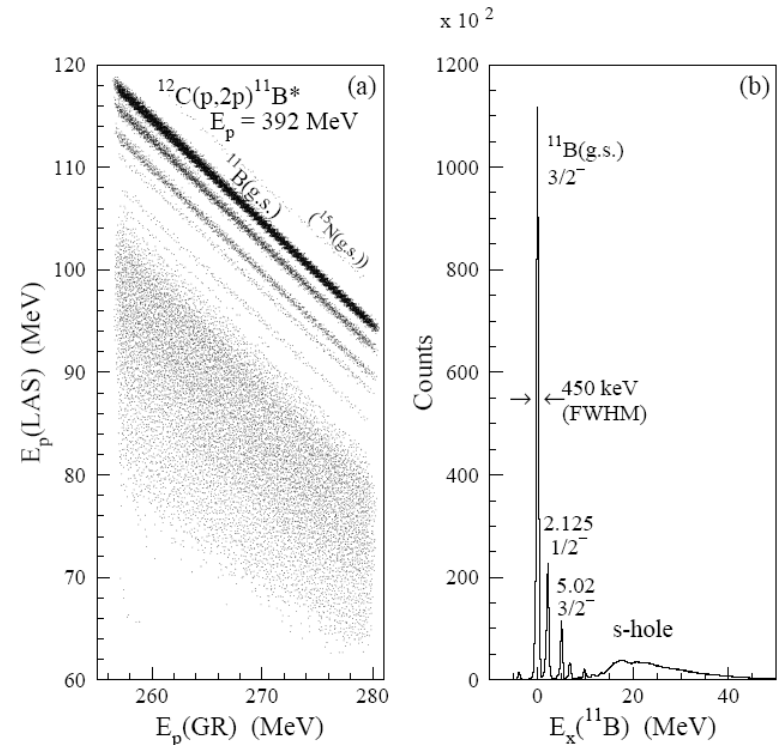
# Recent Experiment in Normal Kinematics: $^{12}\text{C}(p,2p)^{11}\text{B}$



## Study of deep-hole states ( $s_{1/2}$ )

M. Yosoi et al., Phys. Lett. B 551, 255 (2003).  
M. Yosoi, PhD Thesis, 2003, Kyoto University

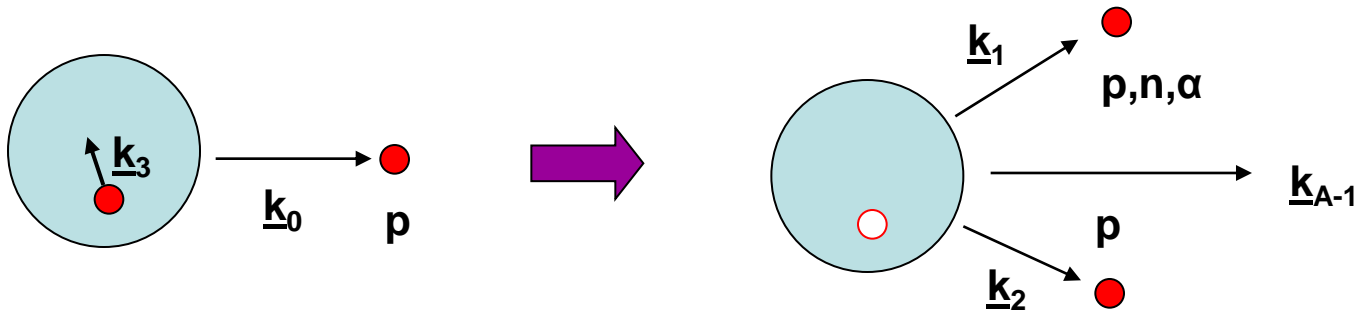
RCNP, Osaka  
 $E_p = 392 \text{ MeV}$   
Two spectrometer measurement  
Energy resolution (FWHM)  $\approx 450 \text{ keV}$



# Quasifree Scattering Reaction: Inverse Kinematics

High energy heavy ion beams,  $E = 100\text{-}1000 \text{ A.MeV}$

- simplify reaction mechanism: impulse approximation
- minimise final state interactions: spectator nucleons



Can now measure momentum distribution  $k_{A-1}$  in **two** ways:

- **directly**
- **indirectly** by measuring  $k_1$  and  $k_2$  as in normal kinematics

**Better understanding of  
final state interactions  
-see next slide**

In inverse kinematics,  $k_{A-1}$  is related to momentum of struck nucleon  $k_3$  by :

$$k_3 = \frac{A-1}{A} k_A - k_{A-1}$$

Hence, by only measuring  $k_{A-1}$  we can obtain:

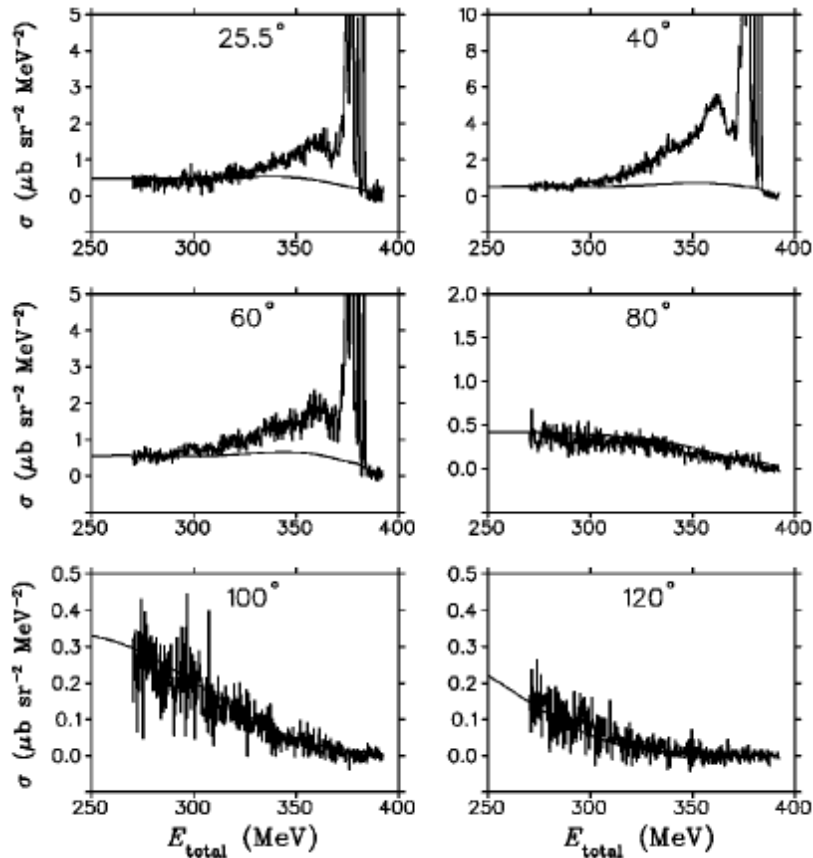
- l-value from momentum distribution of core
- energy of core states can be obtained with  $\gamma$ -rays

**c.f. one-nucleon removal reactions with light-ion targets**

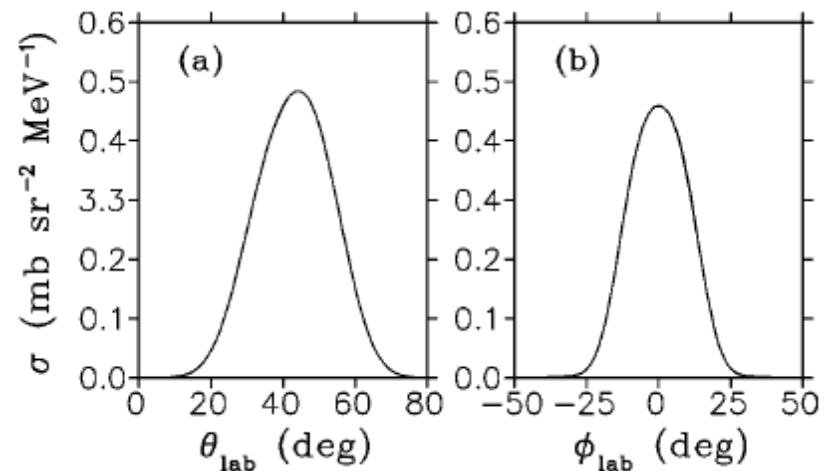


# Advantages of Inverse Kinematics : Rescattering Contributions

$^{40}\text{Ca}(p,p'p'') E_p = 392 \text{ MeV}$



DWIA calculations



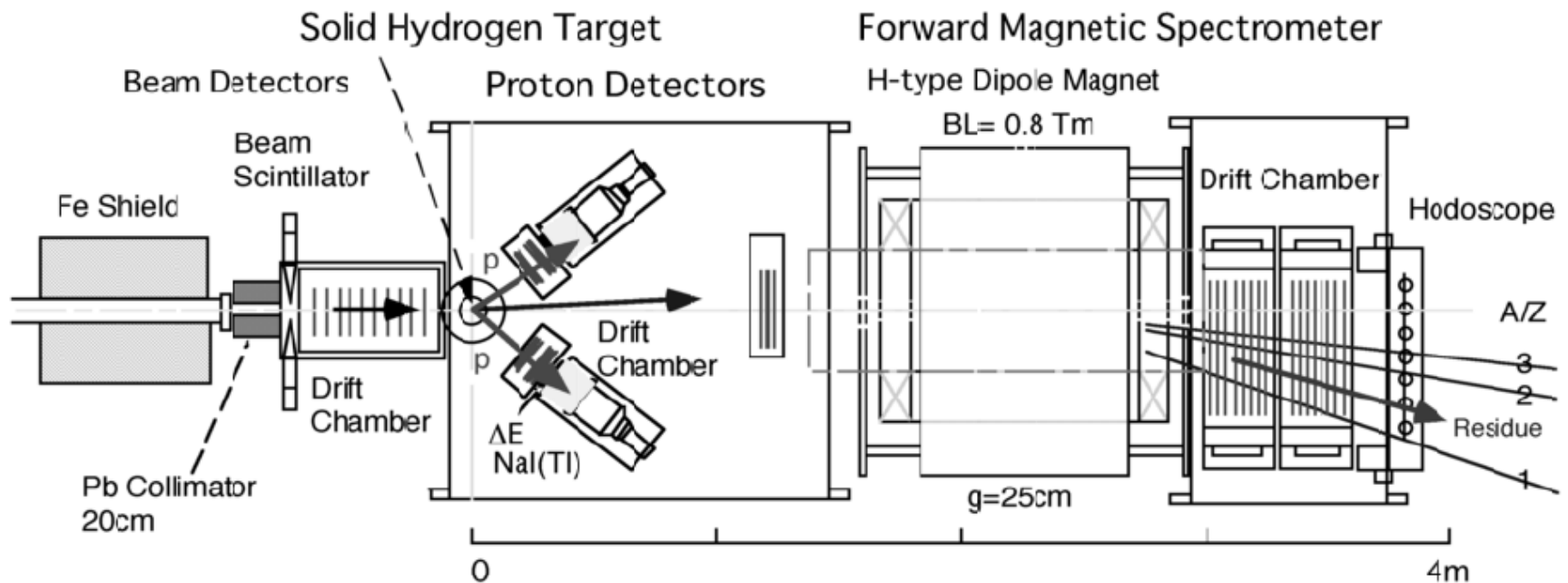
In-plane

Out-of-plane

Two spectrometer measurement  
LAS + Grand Raiden at RCNP, Osaka

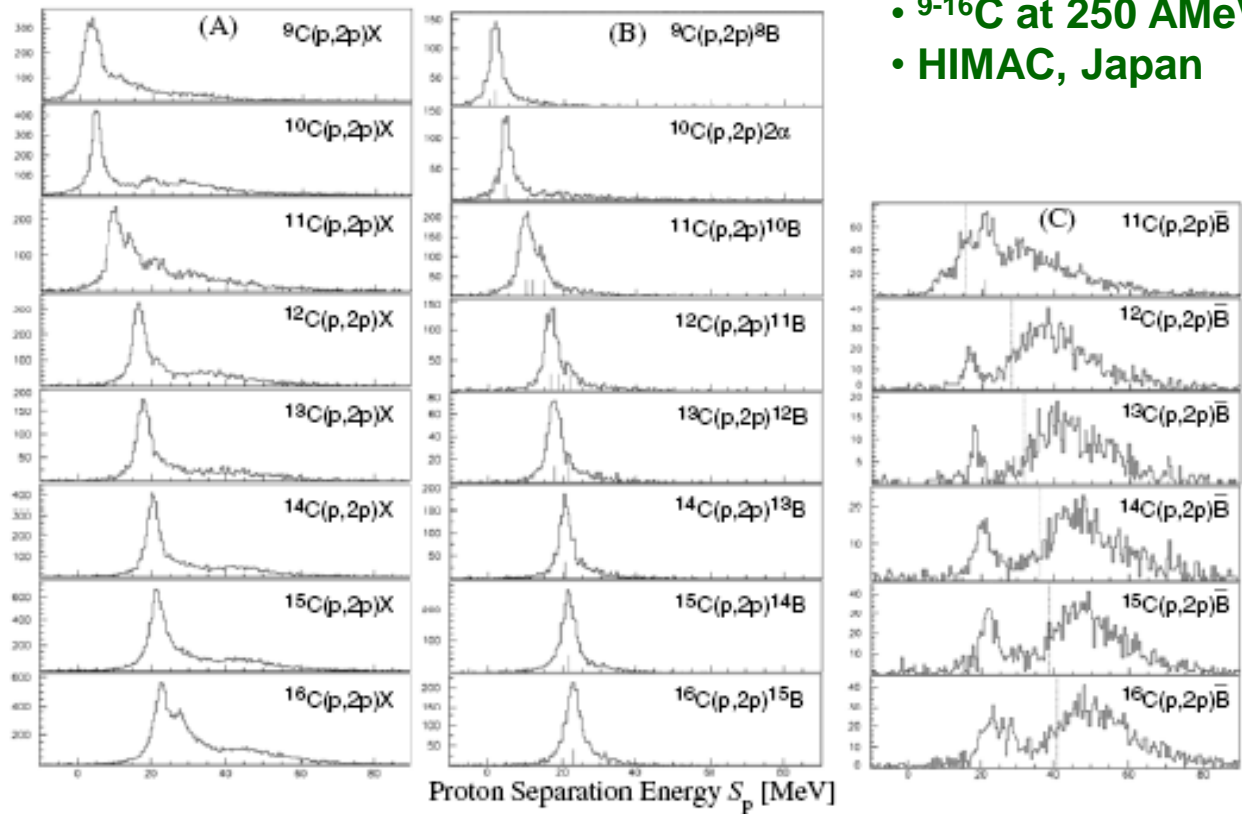
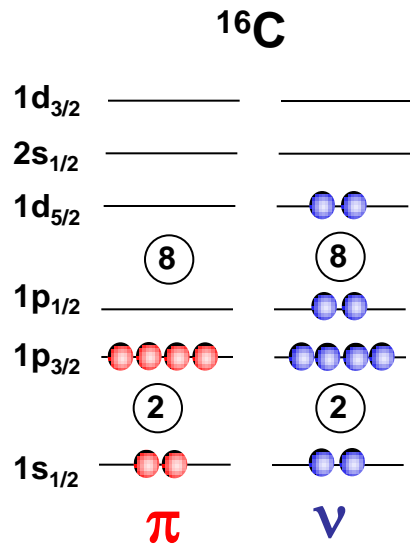
A.A. Cowley et al., Phys. Rev. C 57 (1998) 3185.

# Experiments at HIMAC: $^{9-16}\text{C}(p,2p) @ 250 \text{ AMeV}$

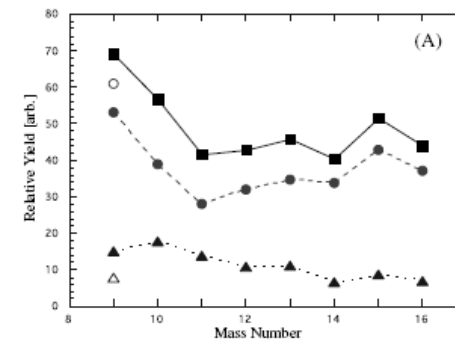
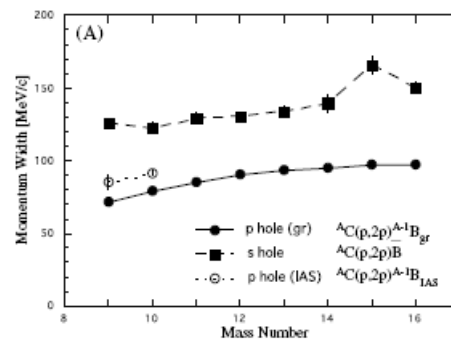
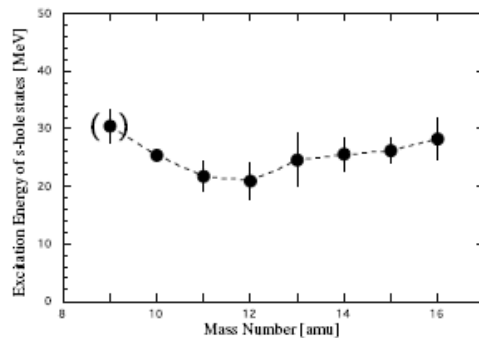


T. Kobayashi et al.

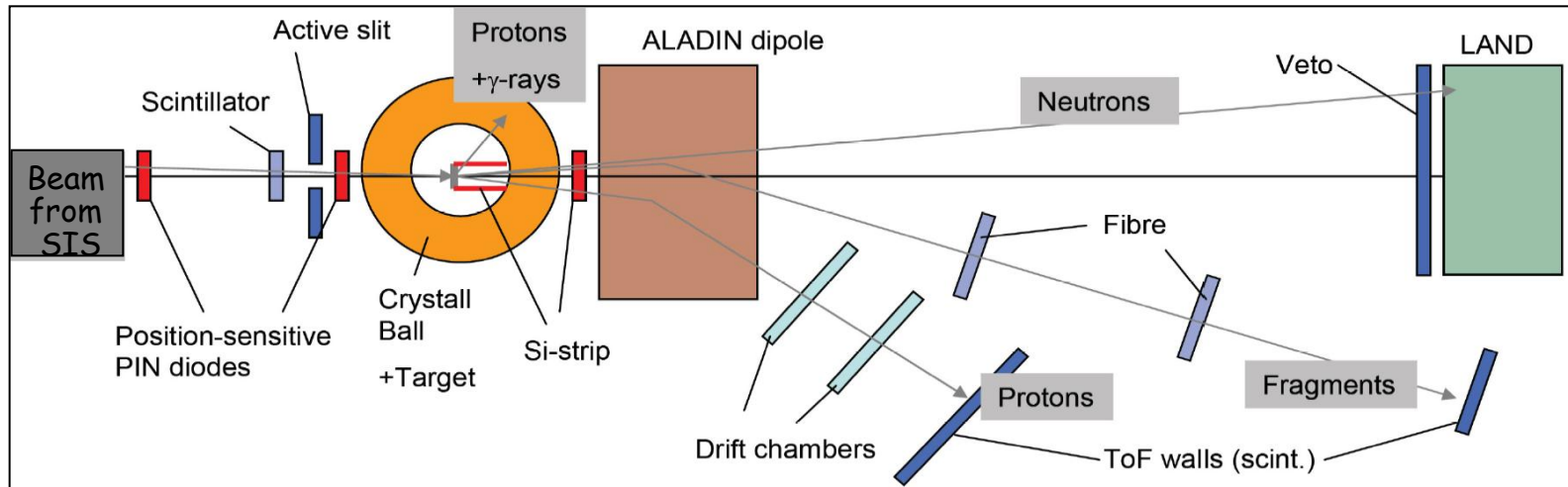
# Spectroscopy of Valence and Deeply Bound Nucleons



- $^9\text{-}^{16}\text{C}$  at 250 AMeV
- HIMAC, Japan



# Experiments at GSI: LAND/R3B



- **kinematical complete measurement of:**
  - (p,pn), (p,2p), (p,pd), (p,α), .... reactions
- **redundant experimental information:**
  - kinematical reconstruction from proton momenta
  - plus gamma rays, invariant mass, recoil momentum
- **sensitivity not limited to surface:**
  - spectral functions
  - knockout from deeply bound states
  - cluster knockout reactions

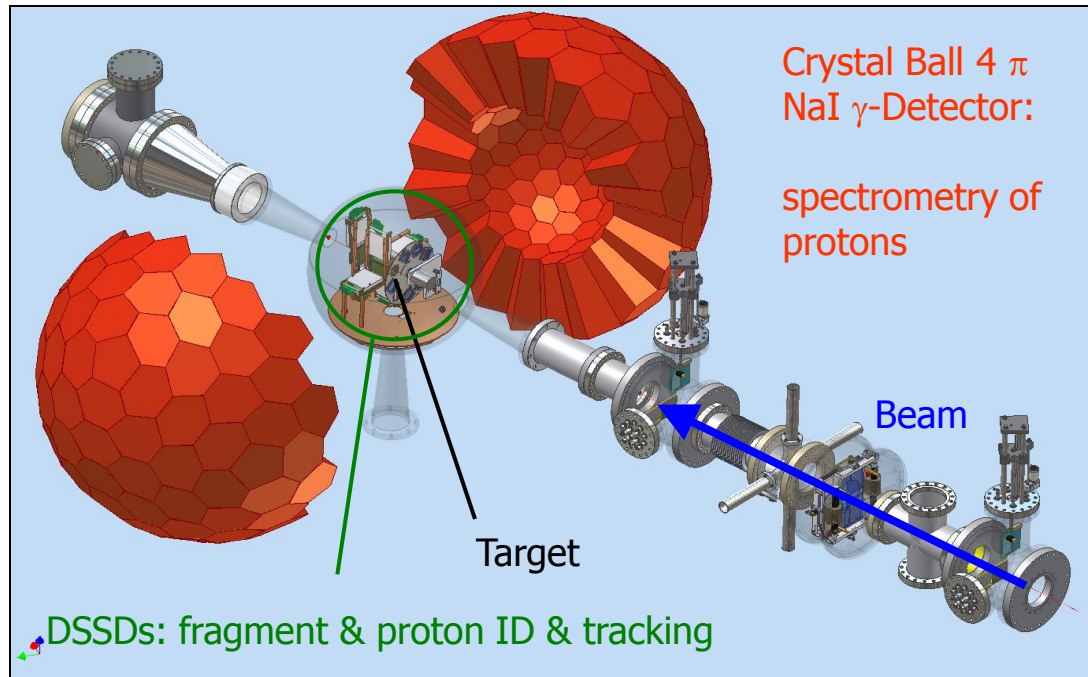
**Experiments so far:**

- $^{12}\text{C}$
- $^{17}\text{Ne}$
- O isotopic chain

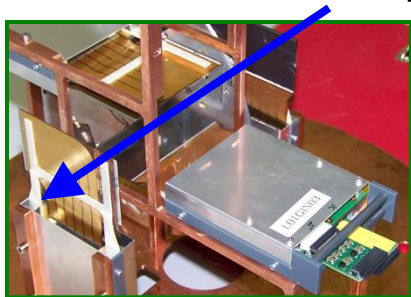
**All use C/CH<sub>2</sub> targets**

# Target Recoil Detector for QFS Experiments

LAND setup: Detectors around the target



New: DSSDs for proton tracking



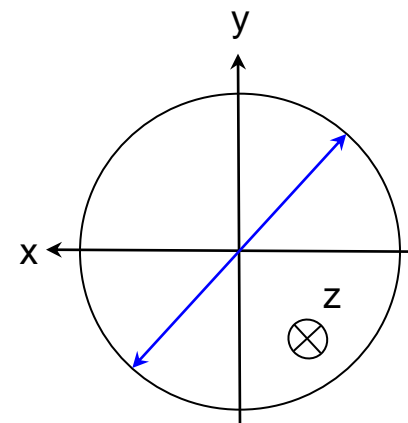
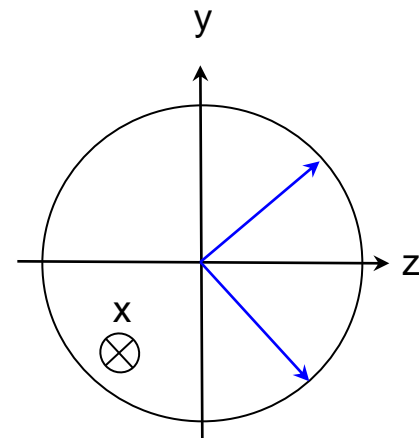
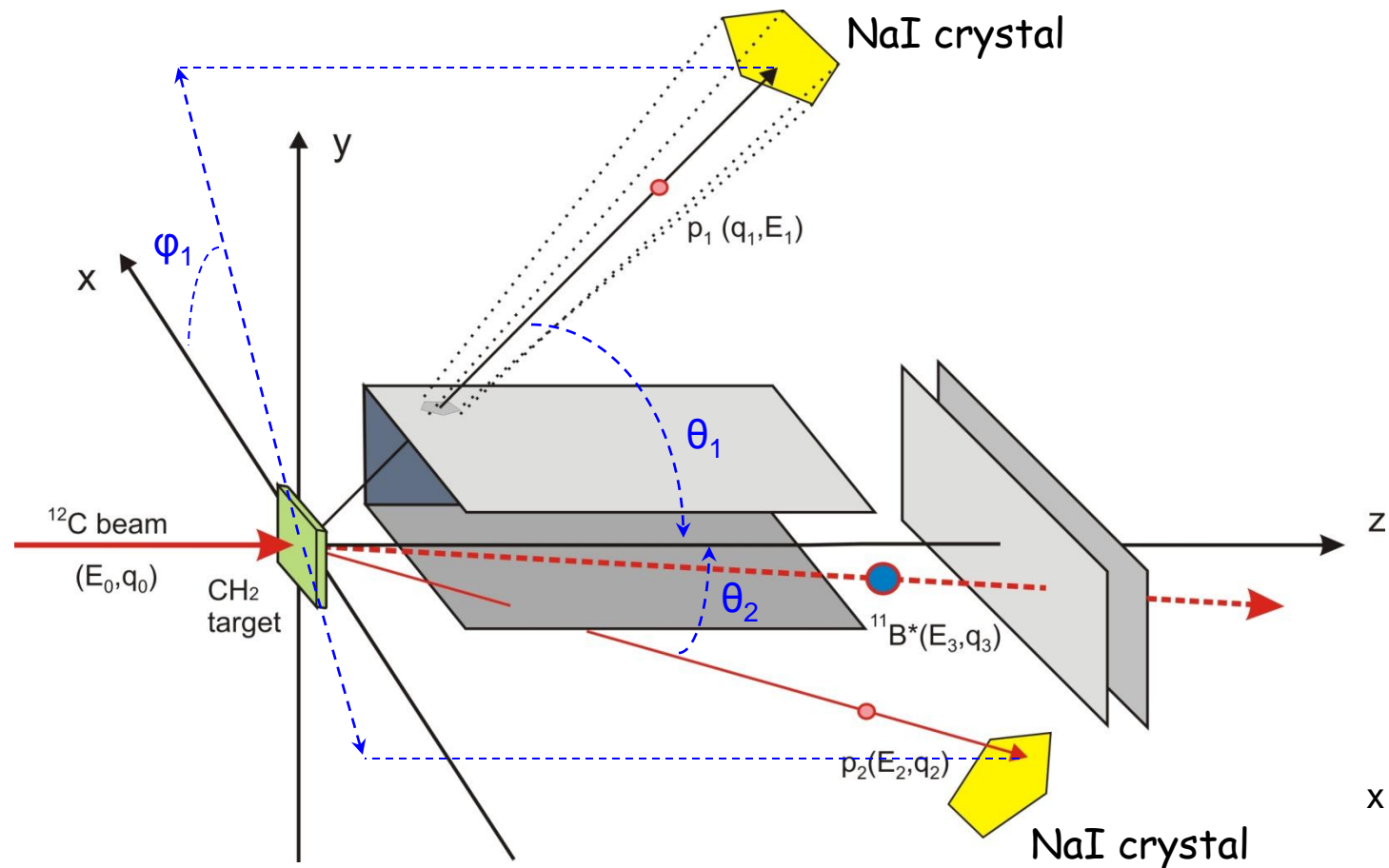
- 4 box detectors for proton tracking
- polar angle coverage  $\approx 15^\circ \leq \theta \leq 80^\circ$
- resolution:  $\Delta x \sim 100 \mu\text{m}$ ;  $\Delta E \sim 50 \text{ keV}$
- range:  $100 \text{ keV} < E < 14 \text{ MeV}$
- 2 in-beam detectors for tracking & ID of fragments and protons

New: Crystal Ball for proton spectrometry

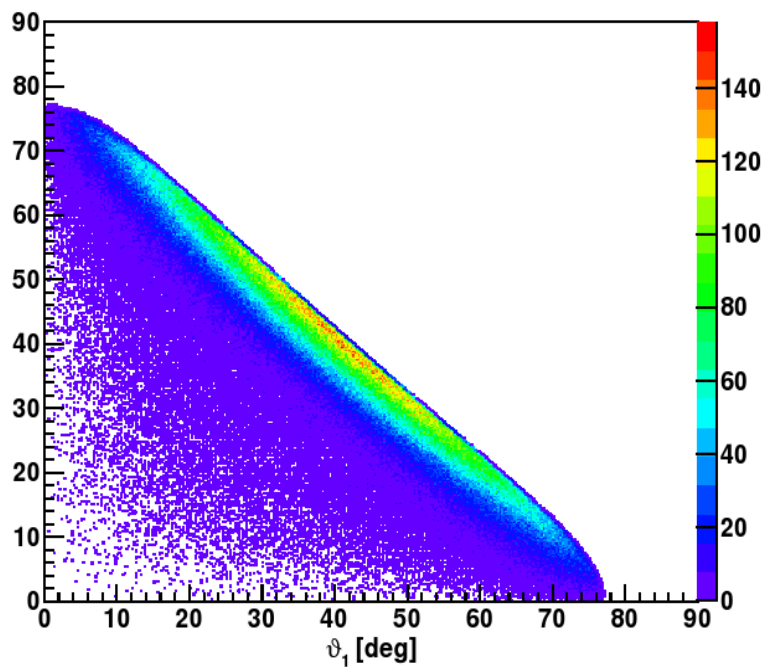
- $4\pi$  gamma detector (\*1980 - ...)
- 162 NaI(Tl) crystals of 20 cm length
- New: Measure energy of recoil protons with additional readout of the forward 64 crystals ( $\sim 2\pi$ ) !



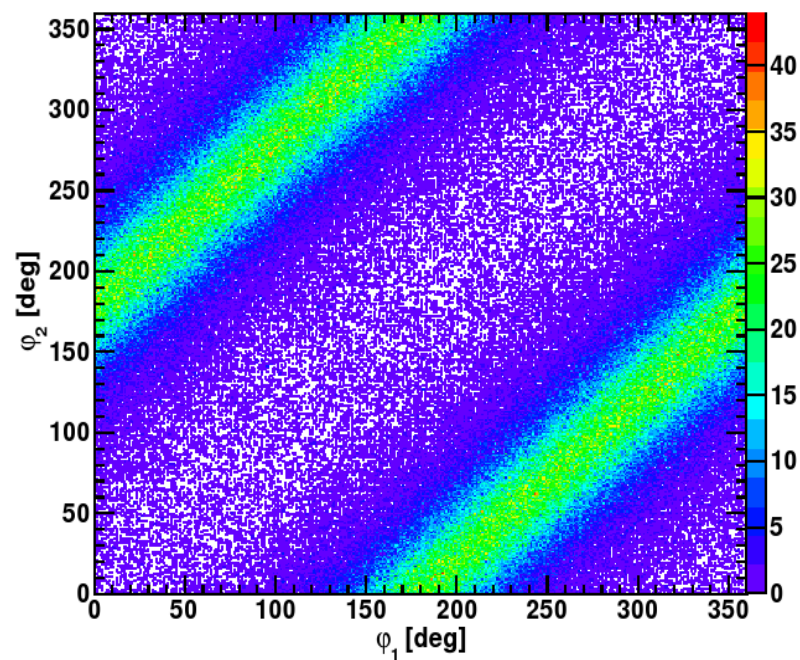
# Angular Correlations of Two Protons from (p,2p) Reaction



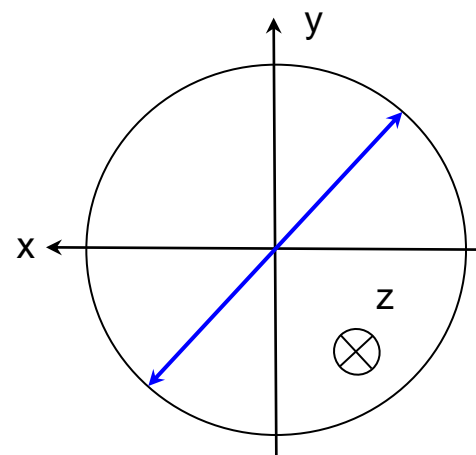
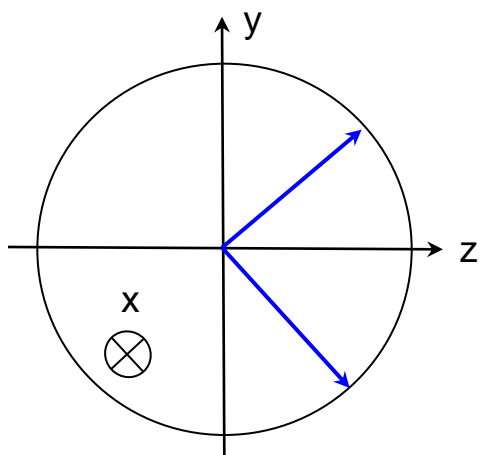


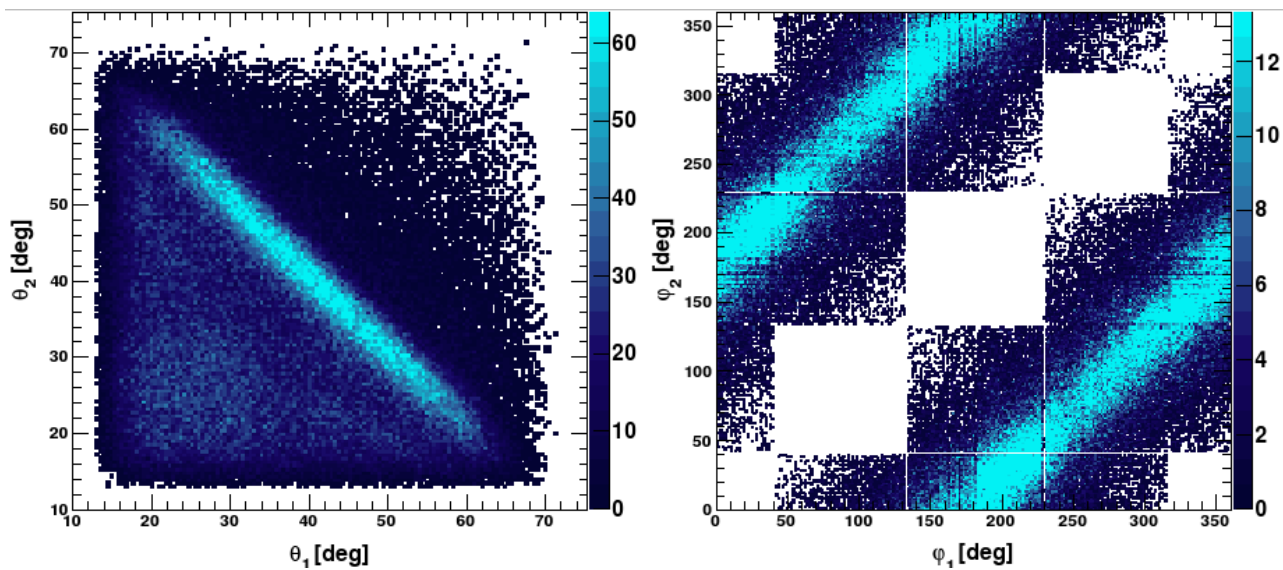


(a) Correlation of zenith angles

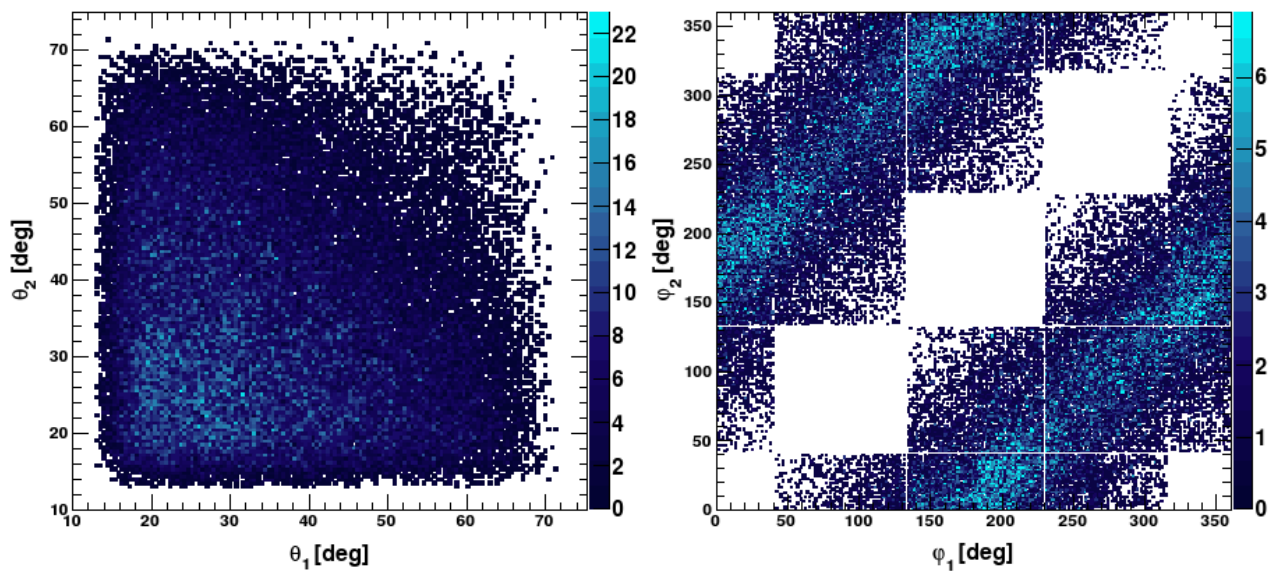


(b) Correlation of azimuth angles



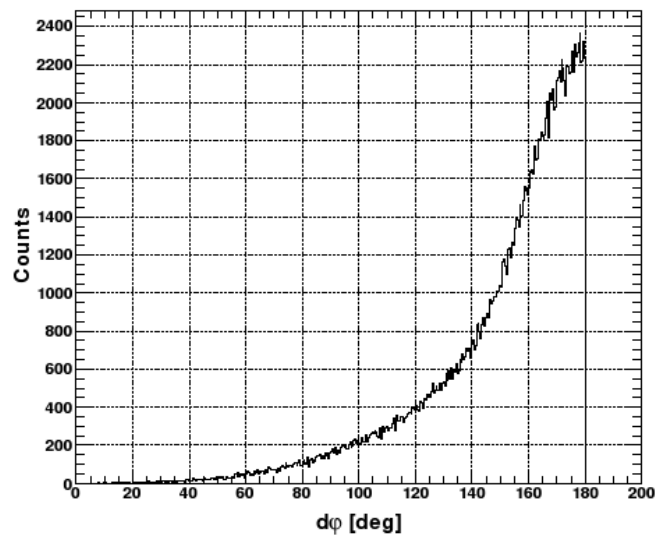
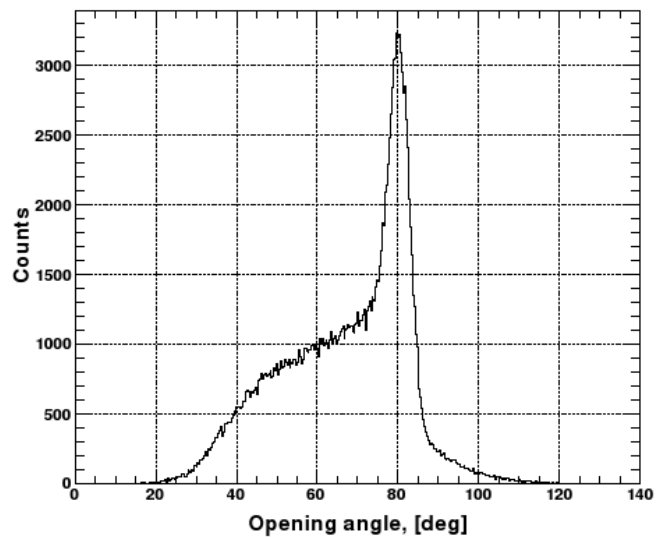


CH2 target

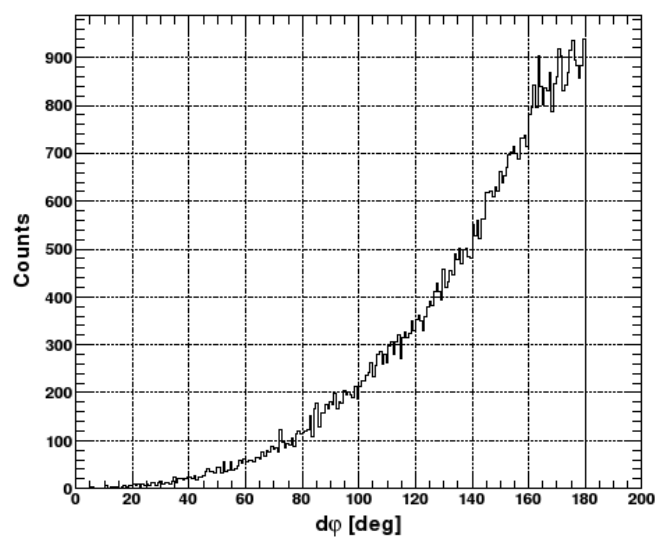
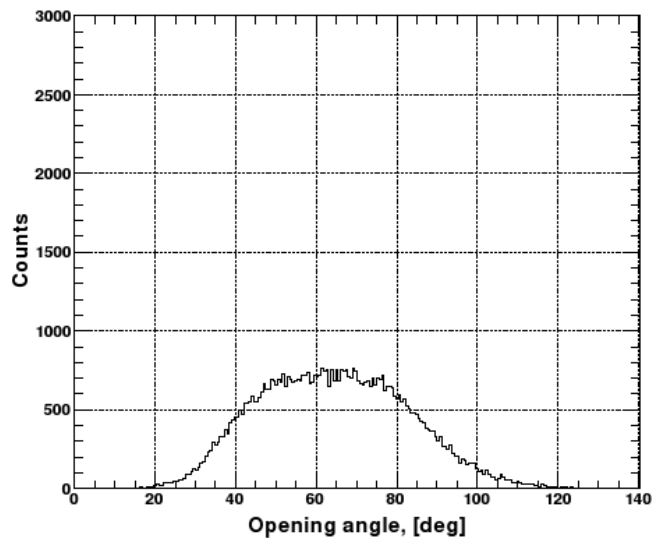


Carbon target



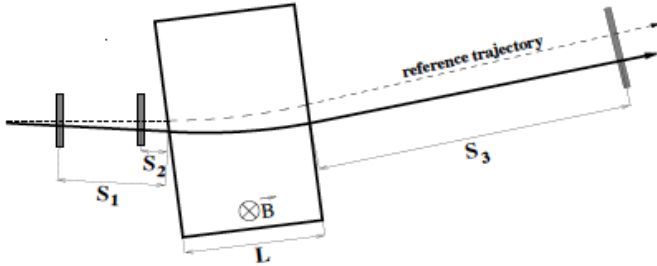
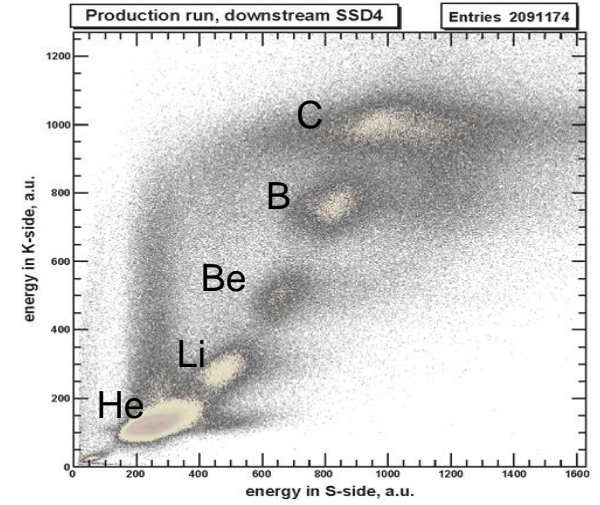
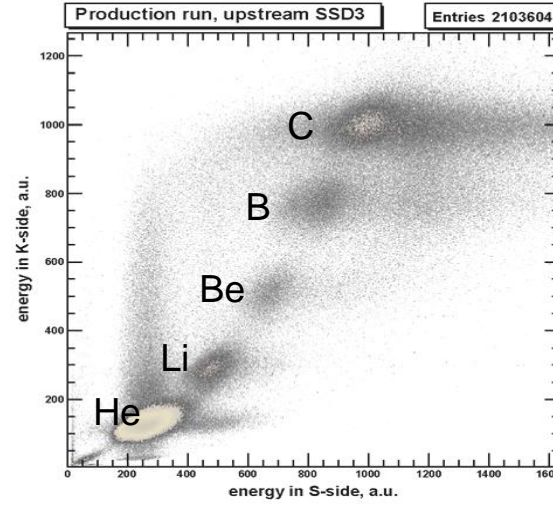
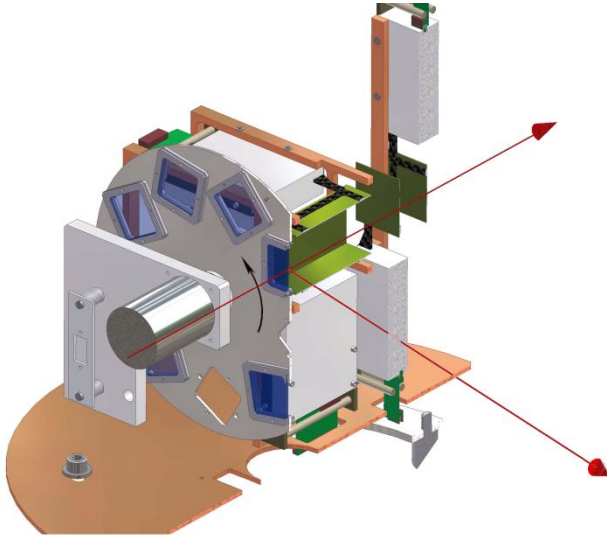


CH2 target



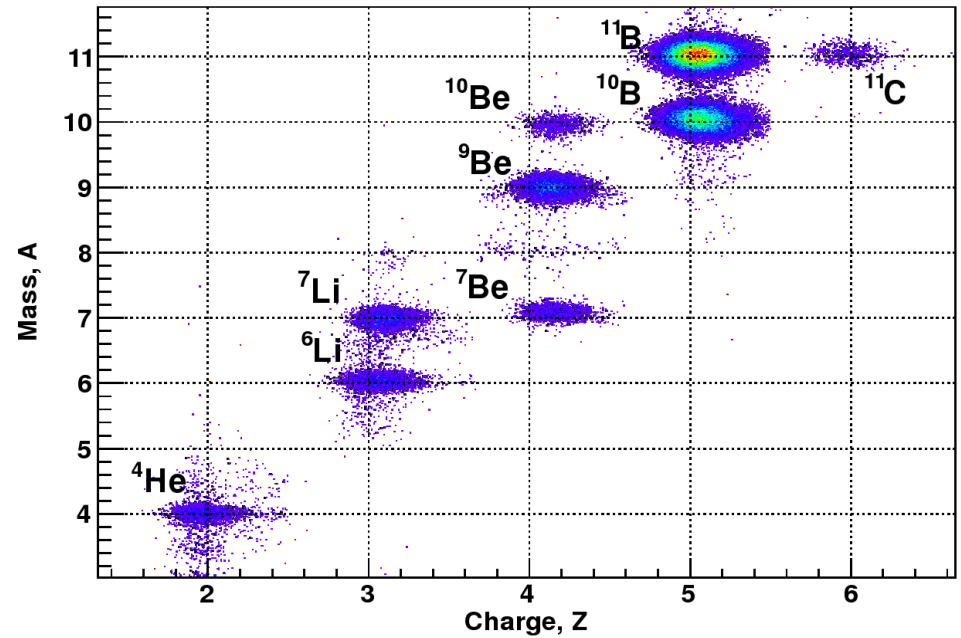
Carbon target

# Charge identification in two in-beam DSSDs



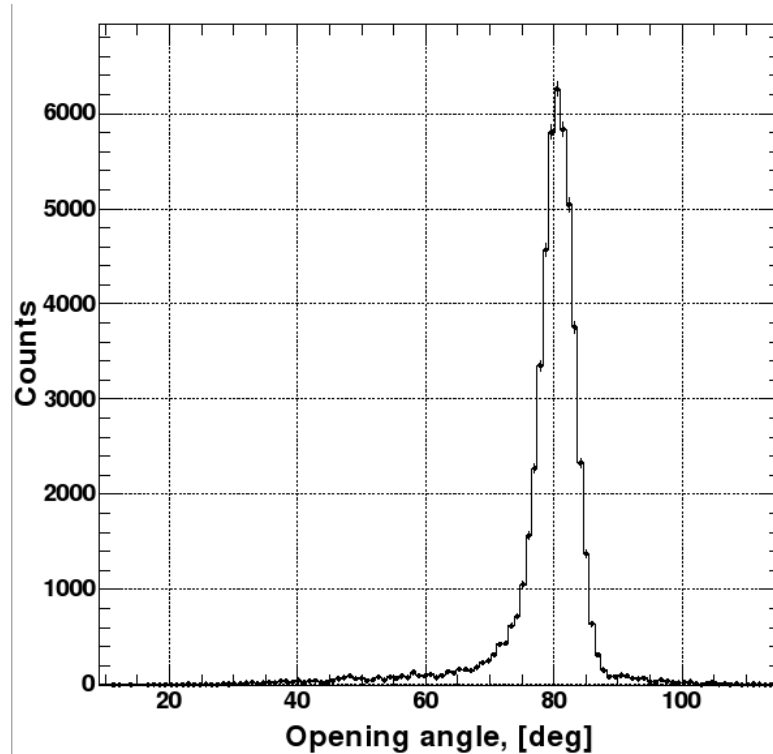
$$(B\rho)_0 = \frac{m_u c}{e} \frac{A_0}{Z_0} \beta_0 \gamma_0 = 3.10716 \frac{A_0}{Z_0} \beta_0 \gamma_0$$

$$\frac{d(B\rho)}{(B\rho)_0} = \frac{1}{c_{13}} \left( x_3 - a_{13} x_1 - b_{13} \frac{x_2 - x_1}{S_1 - S_2} \right)$$



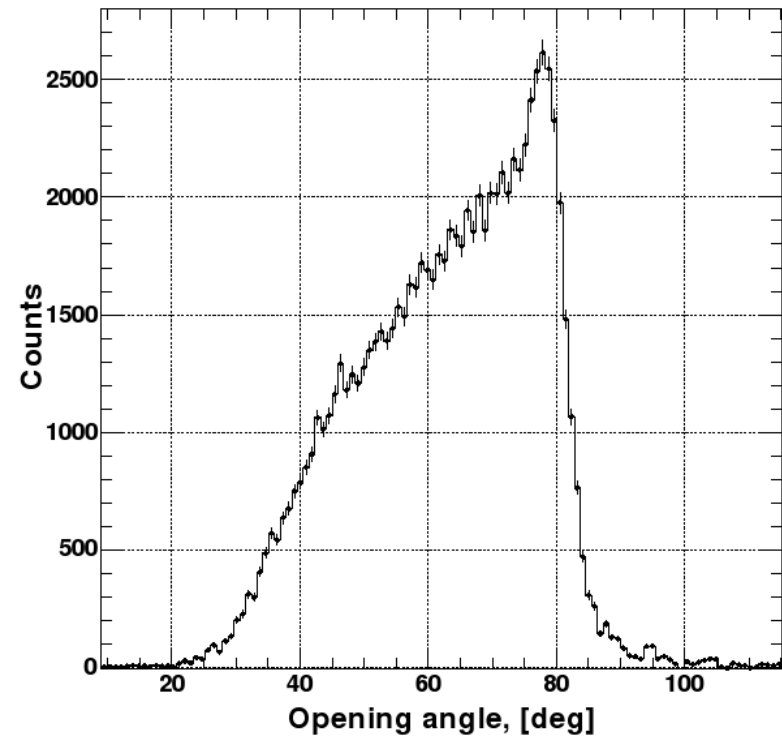
# Hydrogen target (BG subtracted)

$^{12}\text{C}(\text{p},2\text{p})^{11}\text{B}$



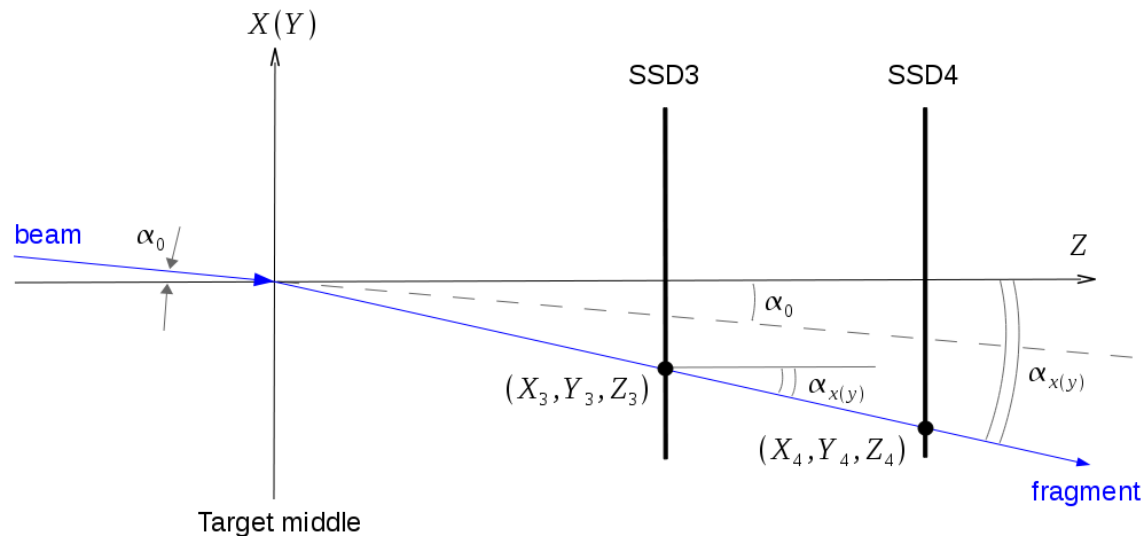
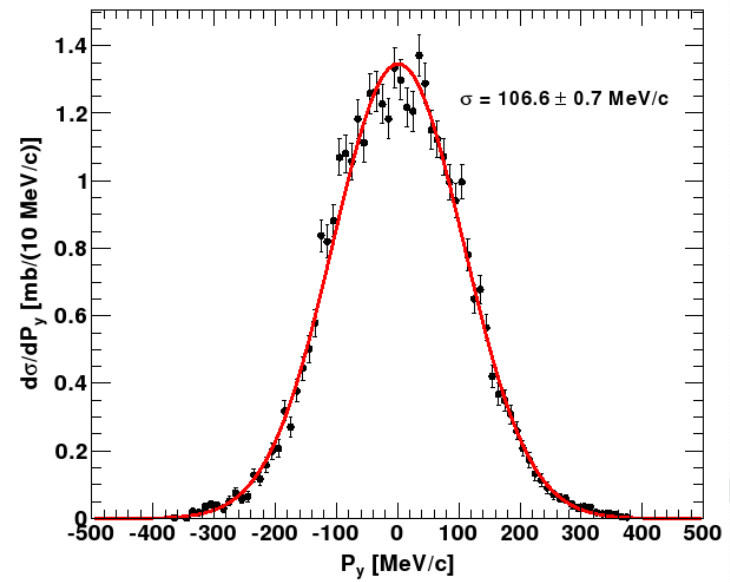
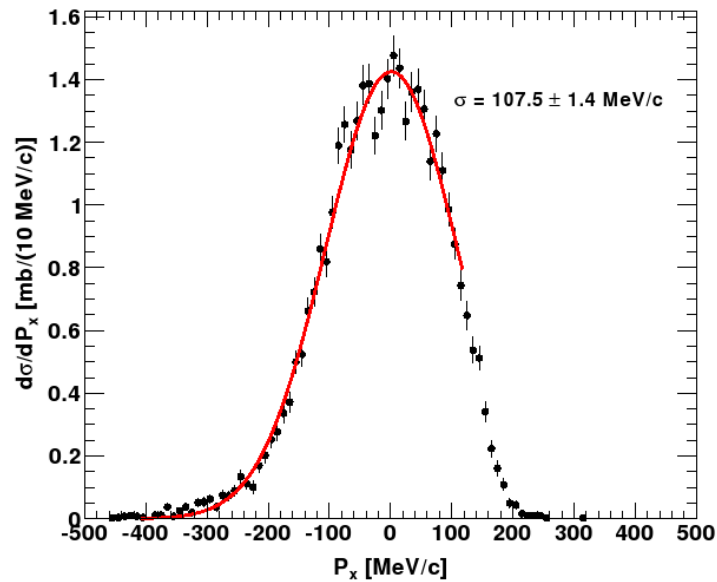
**p-shell**

$^{12}\text{C}(\text{p},2\text{p})\text{X}$



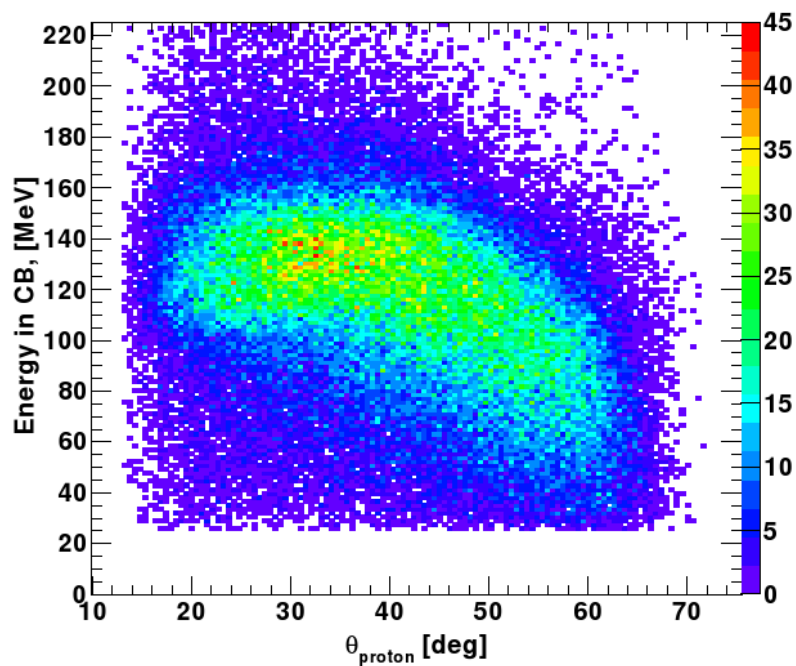
**s-shell**

## Recoil Momentum (p-shell knockout)

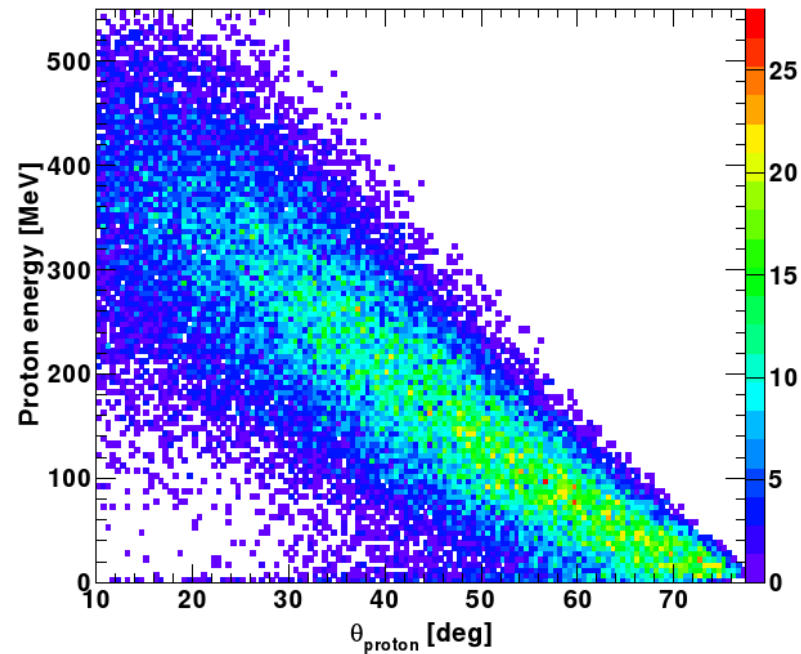


# Energy Measurements of QFS protons

Experiment

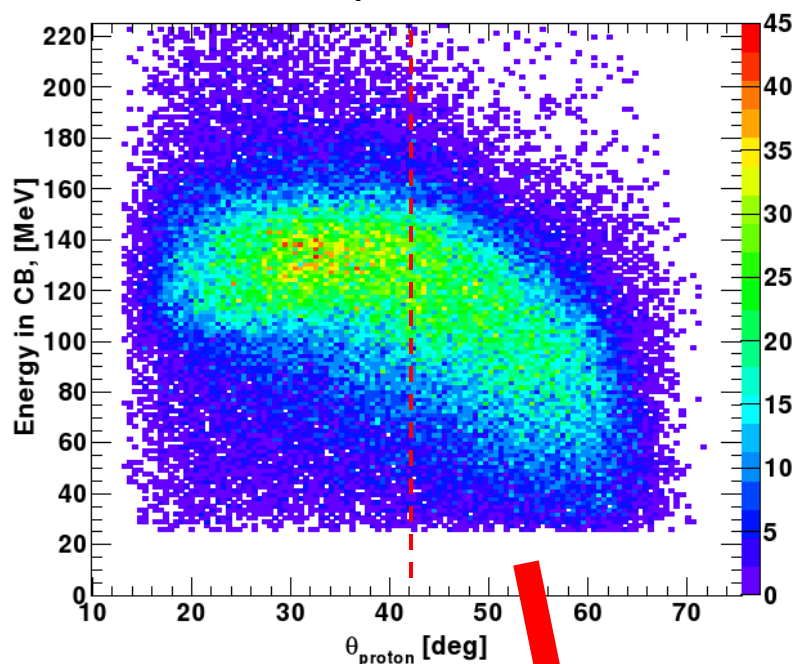


Simulation

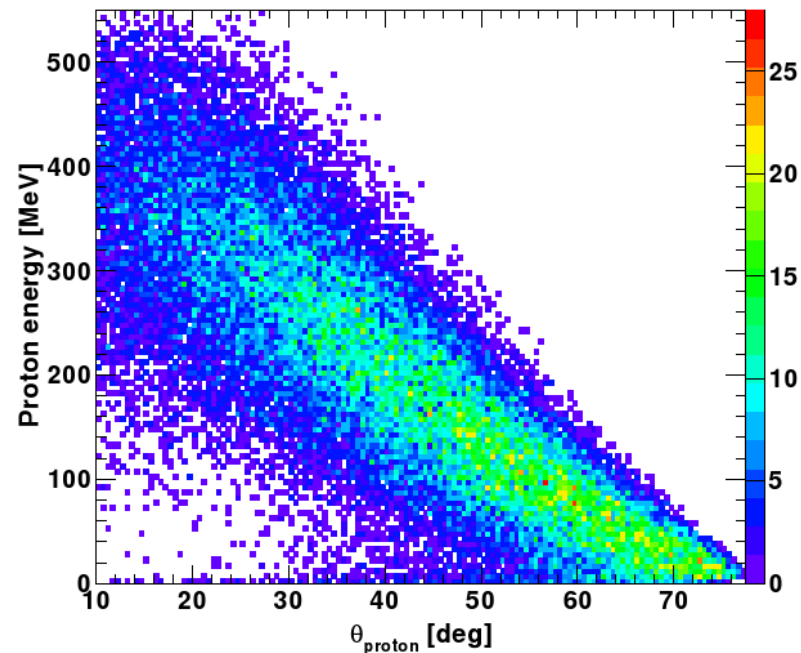


# Energy Measurements of QFS protons

Experiment



Simulation

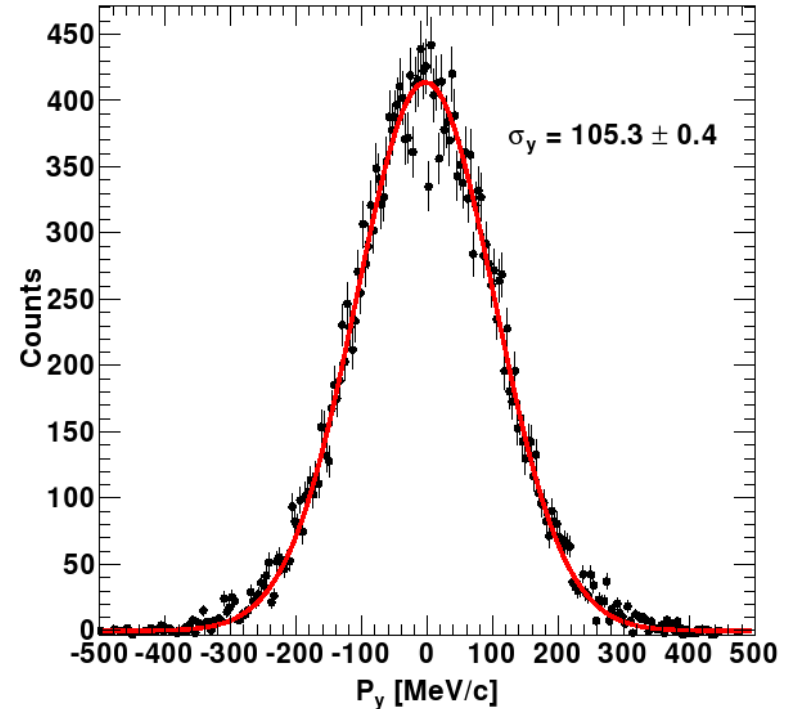
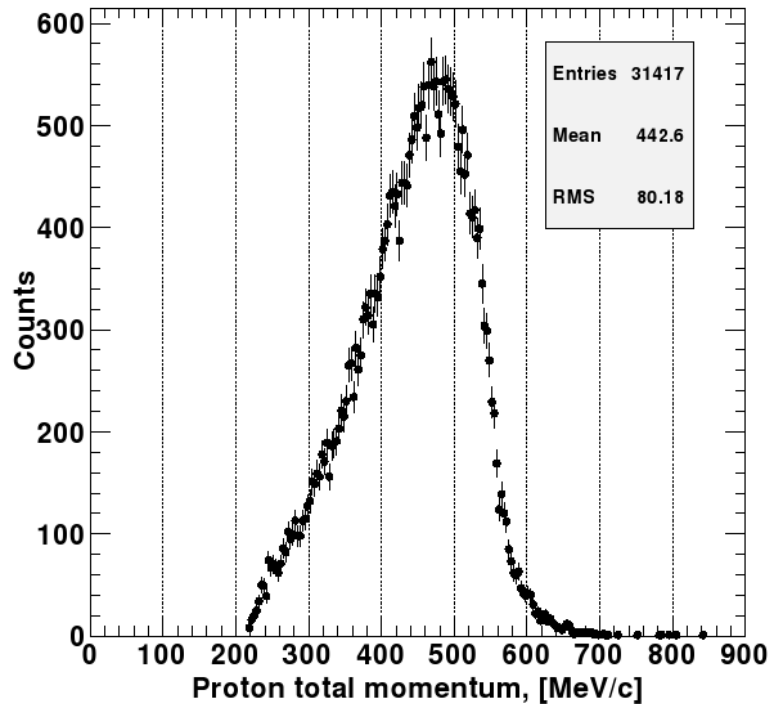


$$Q = \frac{1}{c} \sqrt{E_k(E_k + 2m_p c^2)} \quad \rightarrow \quad \text{total momentum of a proton}$$

$$P_{x,y} = Q_k \times \sin\theta_k \sin(\varphi_k - \varphi_i) \quad \rightarrow \quad \text{transverse component of internal momentum}$$

*L. Chulkov et al. Nucl.Phys. A759, 43, (2005)*

# Internal Momentum Measurements via QFS protons

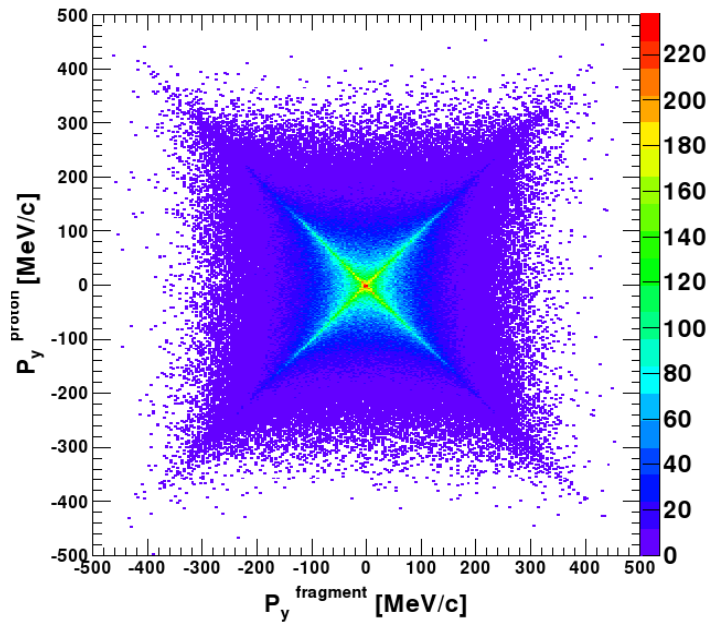


$$Q = \frac{1}{c} \sqrt{E_k(E_k + 2m_p c^2)} \quad \rightarrow \quad \text{total momentum of a proton}$$

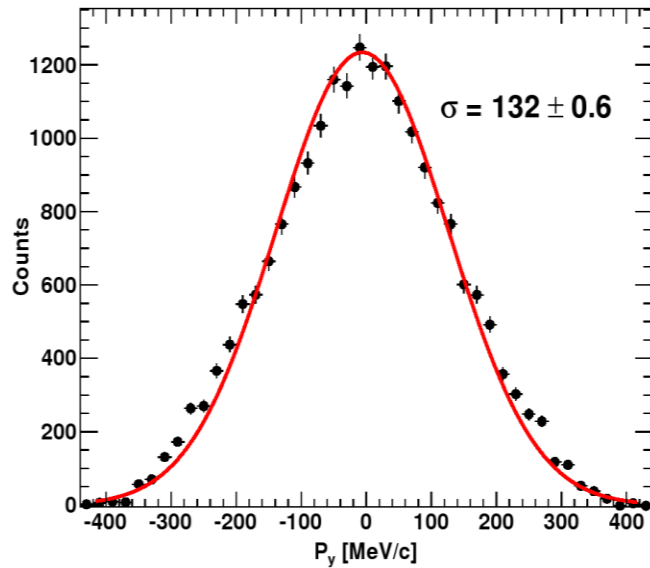
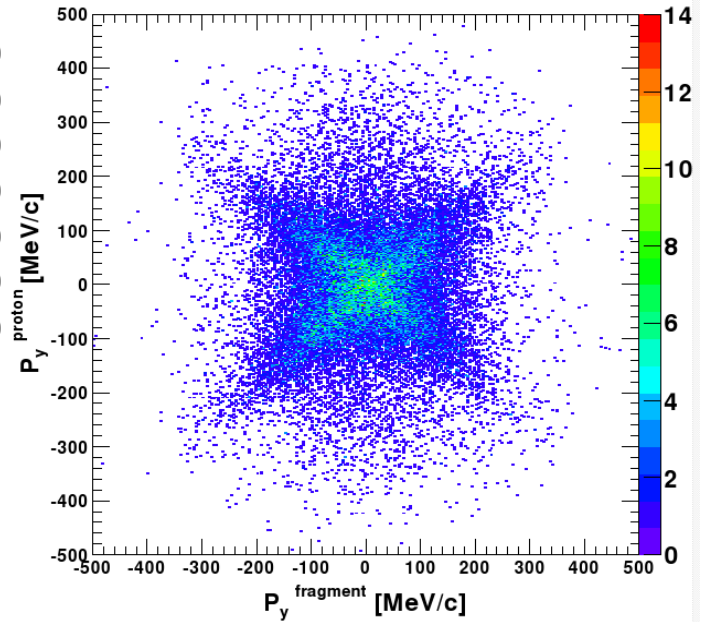
$$P_{x,y} = Q_k \times \sin\theta_k \sin(\varphi_k - \varphi_i) \quad \rightarrow \quad \text{transverse component of internal momentum}$$

*L. Chulkov et al. Nucl.Phys. A759, 43, (2005)*

## Simulation



## Experiment (p-shell)



← Internal momentum distribution  
of protons in s-shell

26% increased comparing to  
p-shell knock-out



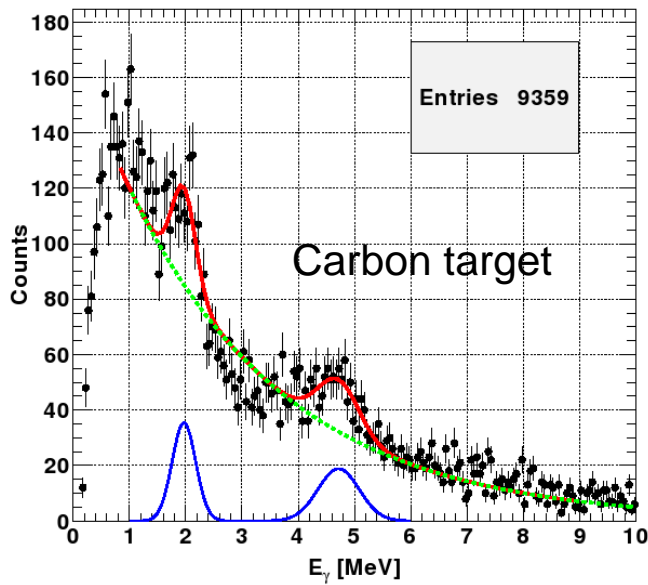
<div> <div>Target</div> <div>Reaction</div> </div>	$CH_2$	Carbon	Hydrogen
$^{12}\text{C}(p, 2p)X$	$89.2 \pm 2.2$	$23.6 \pm 1.0$	$32.8 \pm 1.2$
$^{12}\text{C}(p, 2p)^{11}\text{B}$	$47.3 \pm 1.6$	$11.1 \pm 0.7$	$18.1 \pm 0.9$
p-removal	$82.7 \pm 7.7$	$45.9 \pm 4.4$	$18.4 \pm 2.7$
pn-removal	$48.1 \pm 5.3$	$30.7 \pm 2.3$	$8.7 \pm 1.7$
Inelastic breakup	$2.64 \pm 0.97$	$0.96 \pm 0.65$	$0.84 \pm 0.59$

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$16 \pm 4$  mb  
 integral (p,2p) c.s. for p-shell  
*Nuclear Physics* 18 (1960) 46---64,

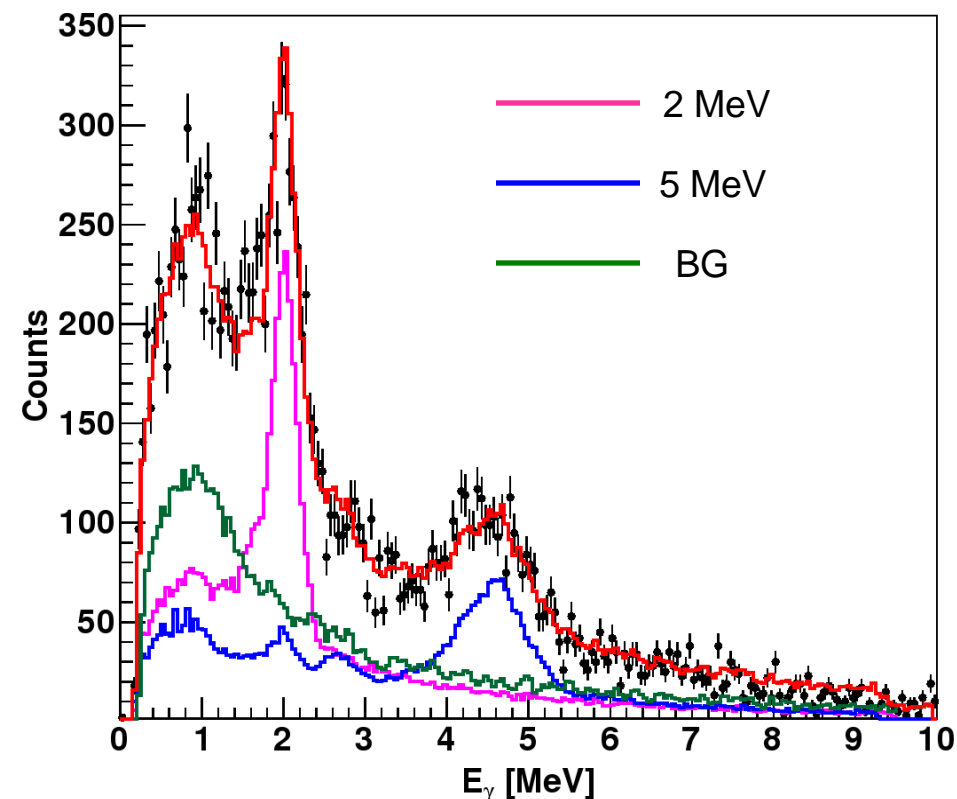
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14.7 mb (45%)  
to unbound  
states (s-shell)



Energy level diagram for  $^{11}\text{B}$  showing levels from 0 to 110 keV. The diagram includes levels for  $3/2^+$ ,  $5/2^+$ ,  $1/2^+$ ,  $3/2^-$ ,  $5/2^-$ , and  $1/2^-$  states. Transitions are labeled with energy values and multipolarities. The ground state is  $3/2^-$  with  $T=1/2$ . The diagram also shows the  $\alpha$  decay of  $^{11}\text{B}$  to  $^7\text{Li}$ .

Energy (keV)	Spin-Parity	Transition(s) from $3/2^-$ (Ground State)	Transition Energy (keV)	Multipolarity
0	$3/2^-$ (T=1/2)	-	-	-
2124.693	$1/2^-$	$100 \rightarrow$	2124.693	$M1$
4444.89	$5/2^-$	$100 \rightarrow$	4444.89	$M1+E2$
5020.31	$3/2^-$	$85.6 \rightarrow$	5019.08	$M1$
6791.80	$1/2^+$	$28.5 \rightarrow$	6763.21	$M1+E2$
7285.51	$5/2^+$	$67.5 \rightarrow$	7218.00	$M1$
7977.84	$3/2^+$	$87.0 \rightarrow$	7890.85	$E1$
9876	$3/2^+$	$46.2 \rightarrow$	9829.74	$E1$



BG subtracted gamma-spectrum:

2 MeV: 17% ( $3.1 \pm 0.2$  mb)

5 MeV: 12% ( $2.2 \pm 0.1$  mb)

G.S : 71% ( $12.9 \pm 0.8$  mb)

Comparison with relative spectroscopic factors

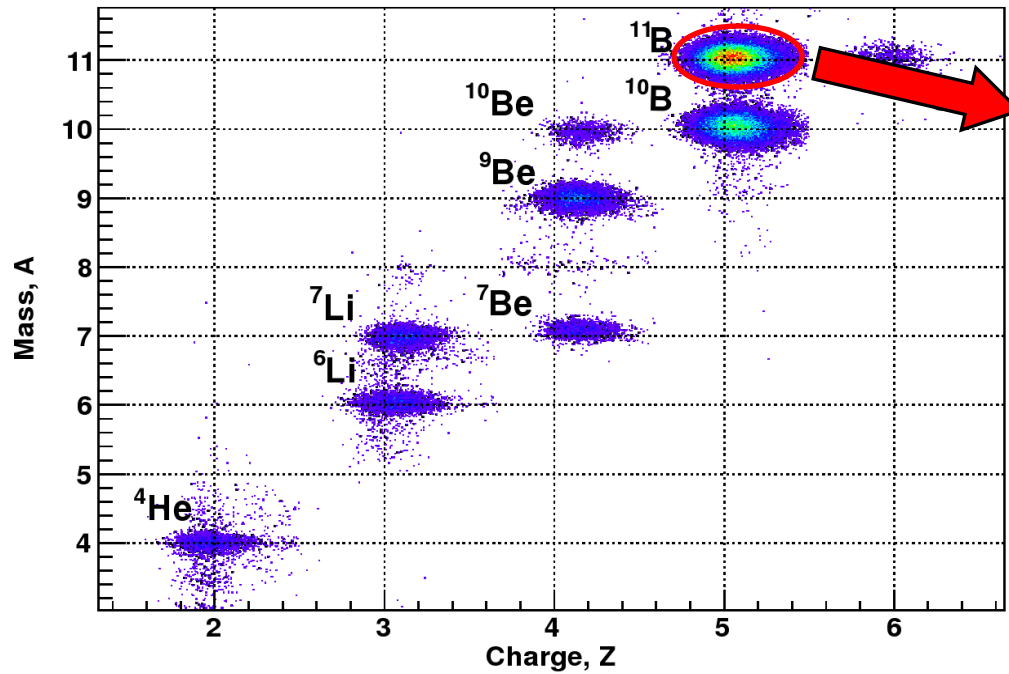


	present exp.	(p,2p) <sup>2</sup> @ 100MeV	(e,e'p) <sup>1</sup>	(d, <sup>3</sup> He) <sup>1</sup>	Cohen-Kurath <sup>1</sup>
G.S	0.71	0.76	0.79	0.75	0.71
2 MeV	0.17	0.12	0.12	0.17	0.19
5 MeV	0.12	0.12	0.09	0.08	0.10

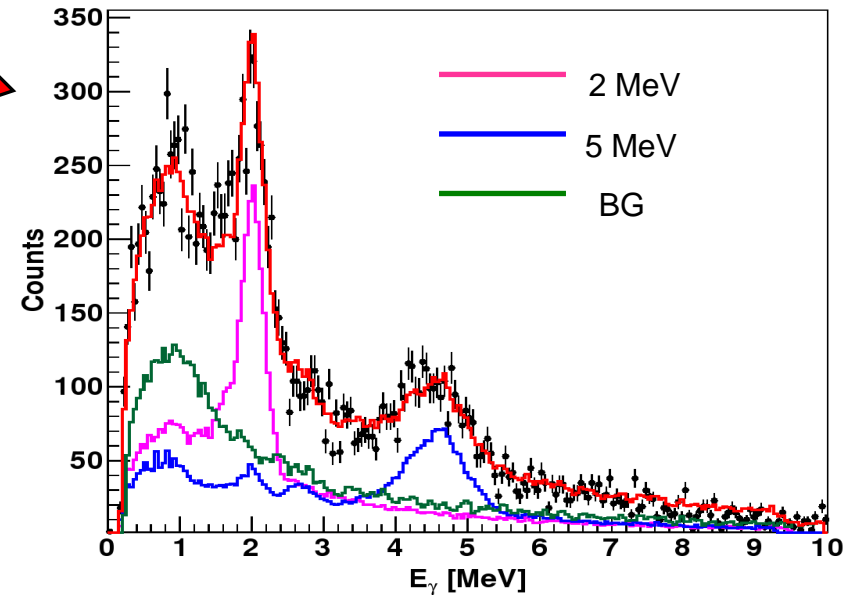
<sup>1</sup>Aust. J. Phys., 1979, 32, 323-34

<sup>2</sup>Nuclear Physics A480 (1988) 547-572

# Reconstruction of excitation energy in $^{11}\text{B}$

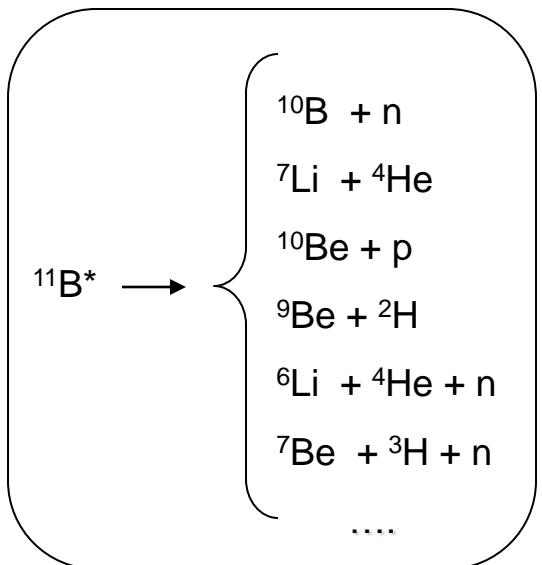


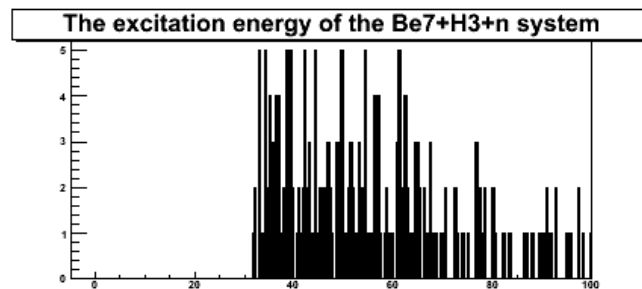
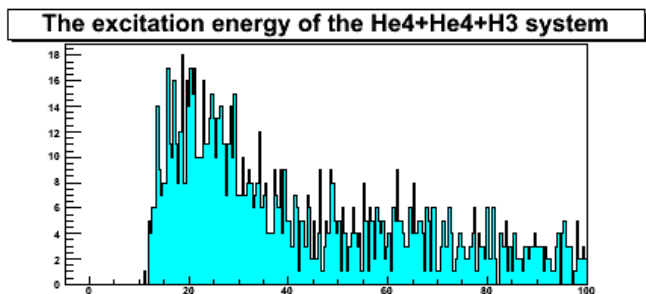
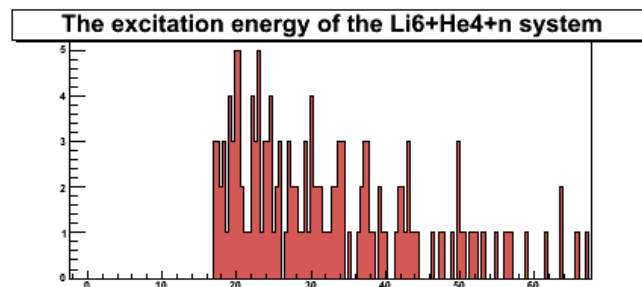
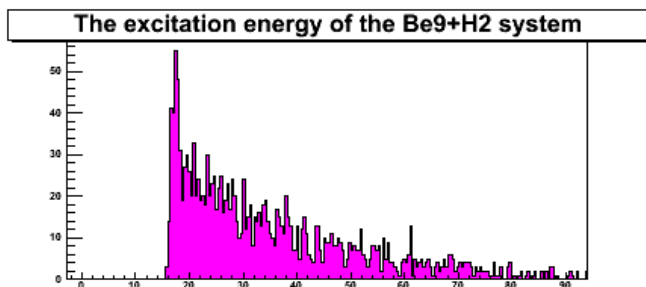
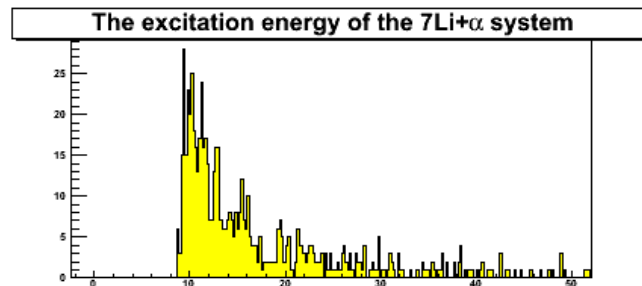
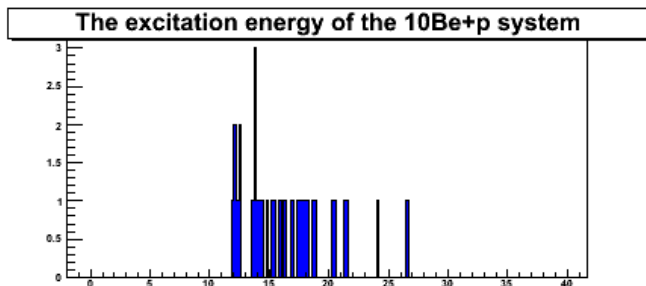
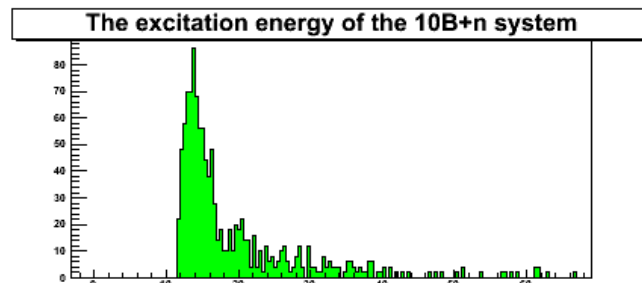
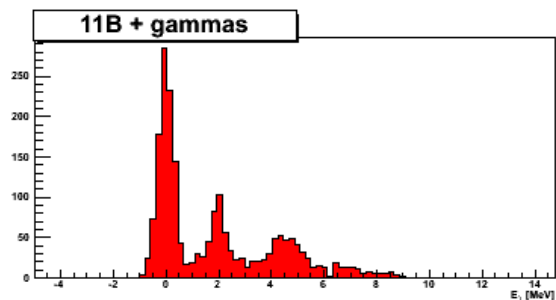
## Gamma spectrometry

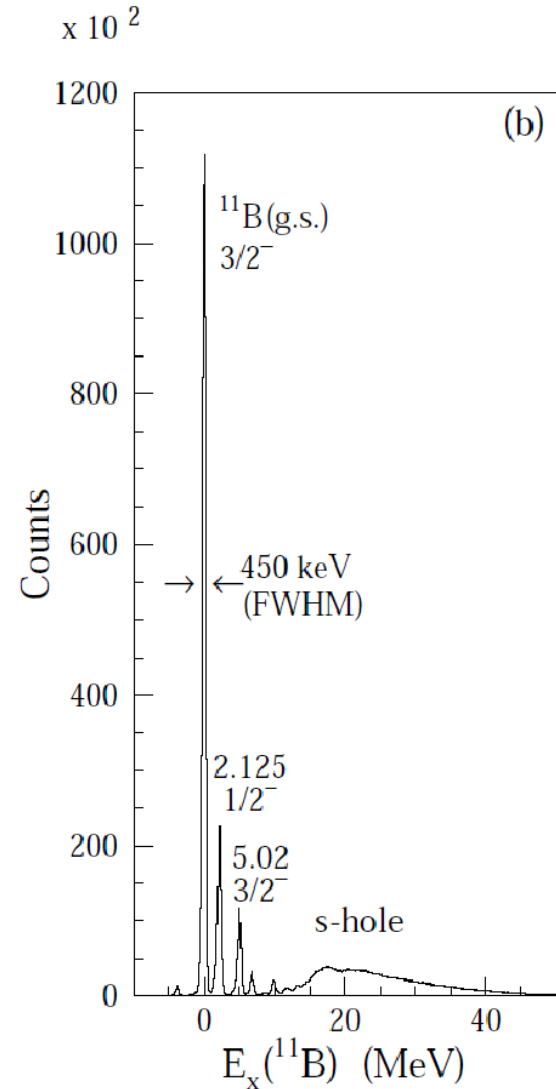
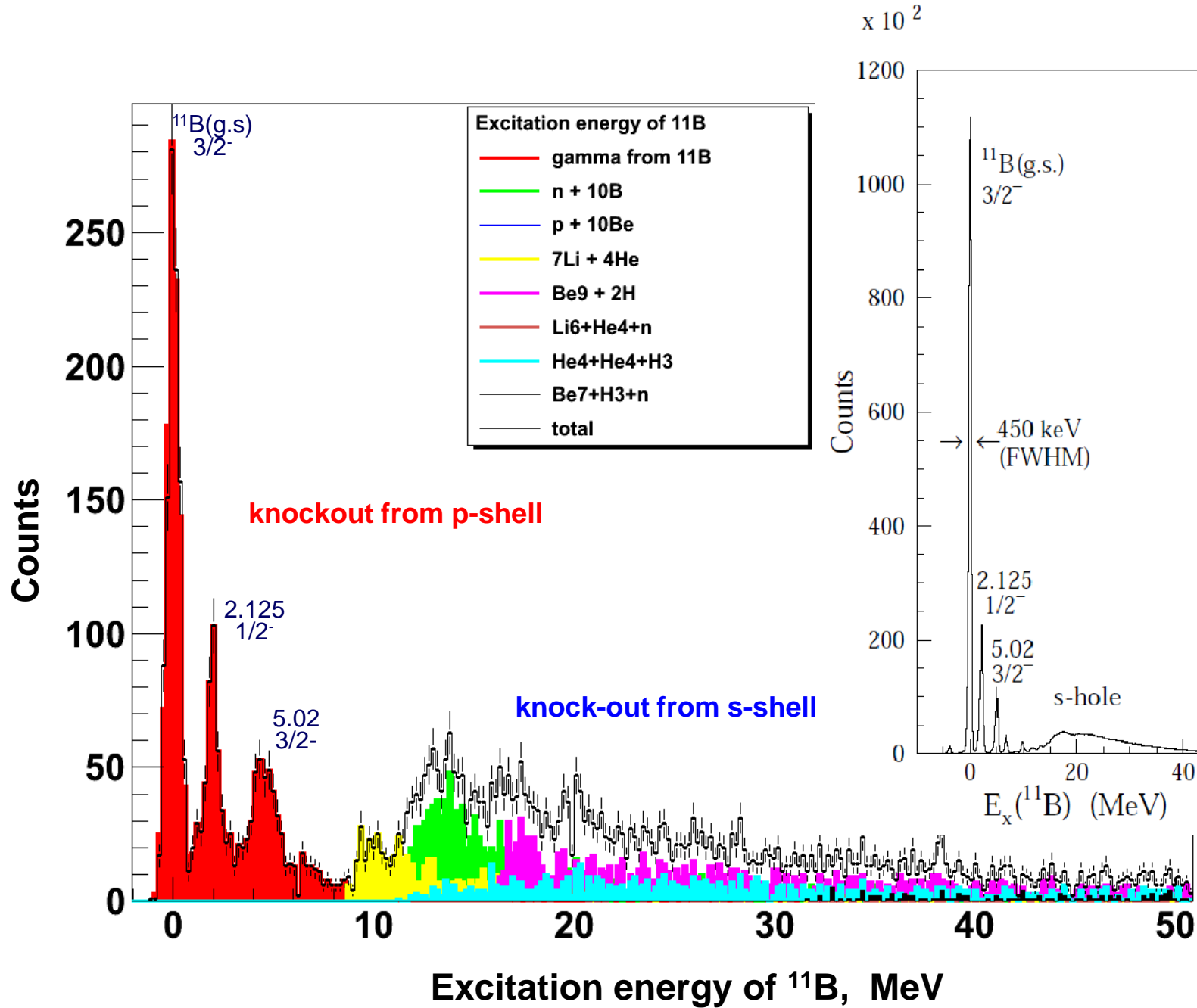


Invariant mass method for breakup channels  
(s-shell knock-out)

$$E^* = \sqrt{\sum_i m_i^2 + \sum_{i \neq j} \gamma_i \gamma_j m_i m_j (1 - \beta_i \beta_j \cos \vartheta_{ij})} + E_\gamma - m_{proj}$$

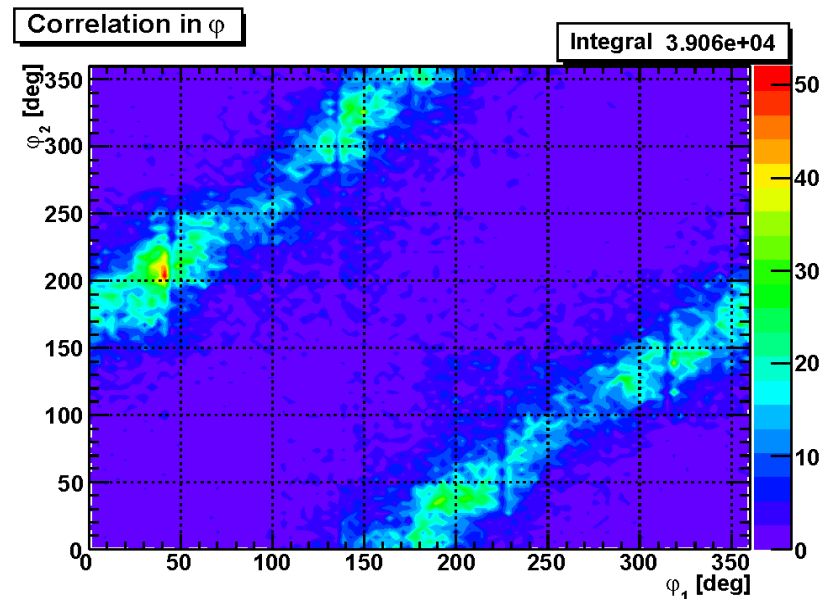
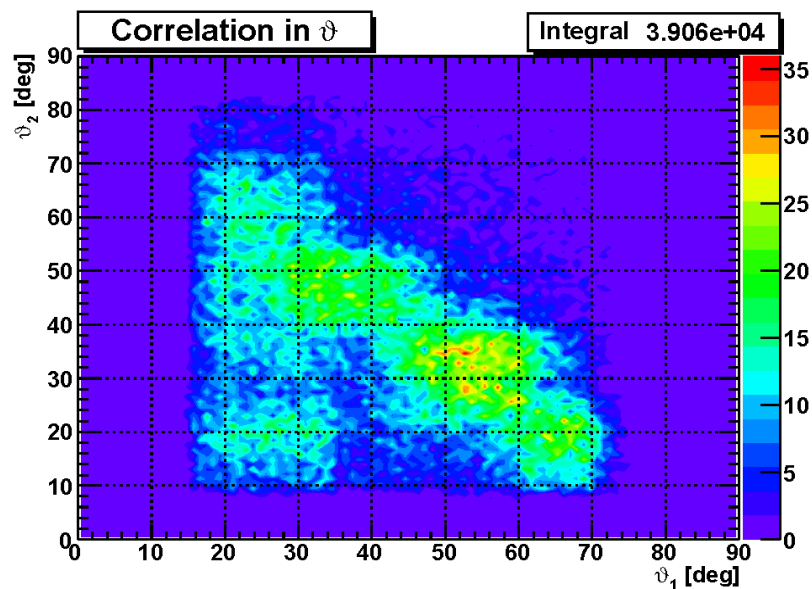
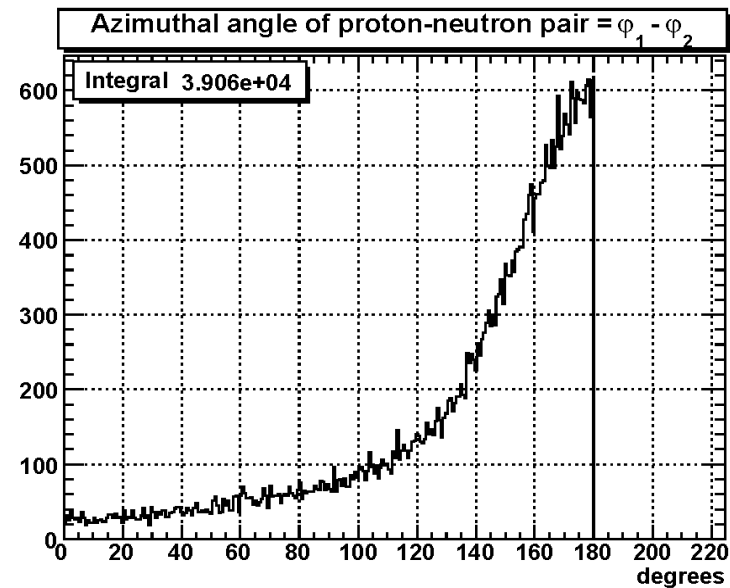
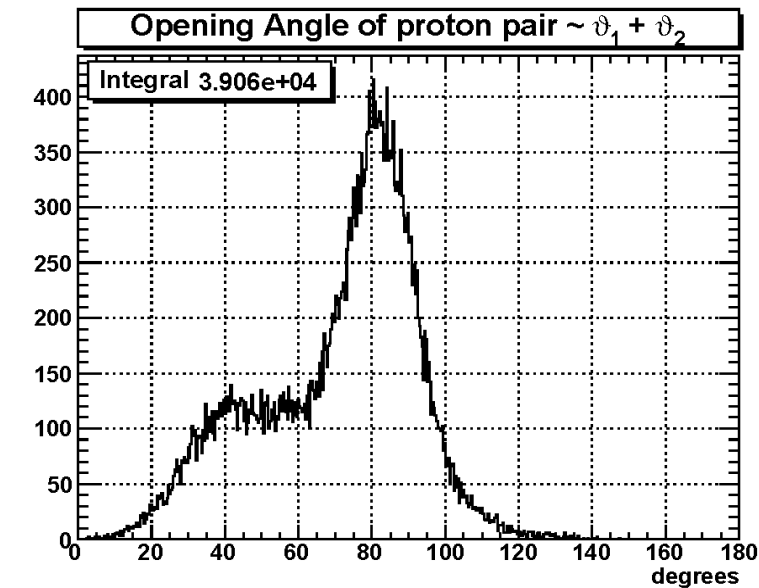






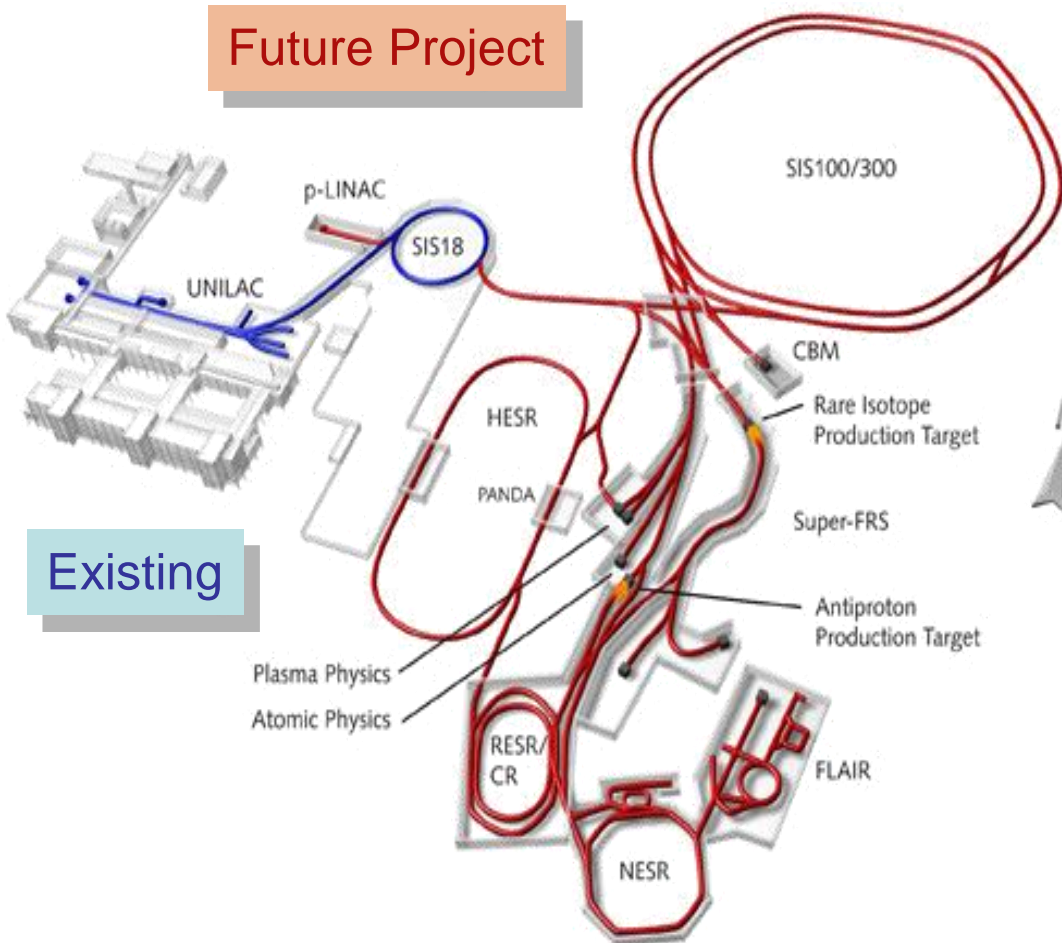


# Angular Distributions of p-n pair from $^{12}\text{C}(\text{p,pn})^{11}\text{C}$ Reaction



# FAIR: Facility for Antiproton and Ion Research

## Future Project



## Existing

## Key Technical Features

- Cooled beams
- Rapidly cycling superconducting magnets

## Primary Beams

- $10^{12}/s$ ; 1.5-2 GeV/u;  $^{238}\text{U}^{28+}$
- Factor 100-1000 over present in intensity
- $2(4) \times 10^{13}/s$  30 GeV protons
- $10^{10}/s$   $^{238}\text{U}^{73+}$  up to 35 GeV/u
- up to 90 GeV protons

## Secondary Beams

- Broad range of radioactive beams up to 1.5 - 2 GeV/u; up to factor 10 000 in intensity over present
- Antiprotons 3 - 30 GeV

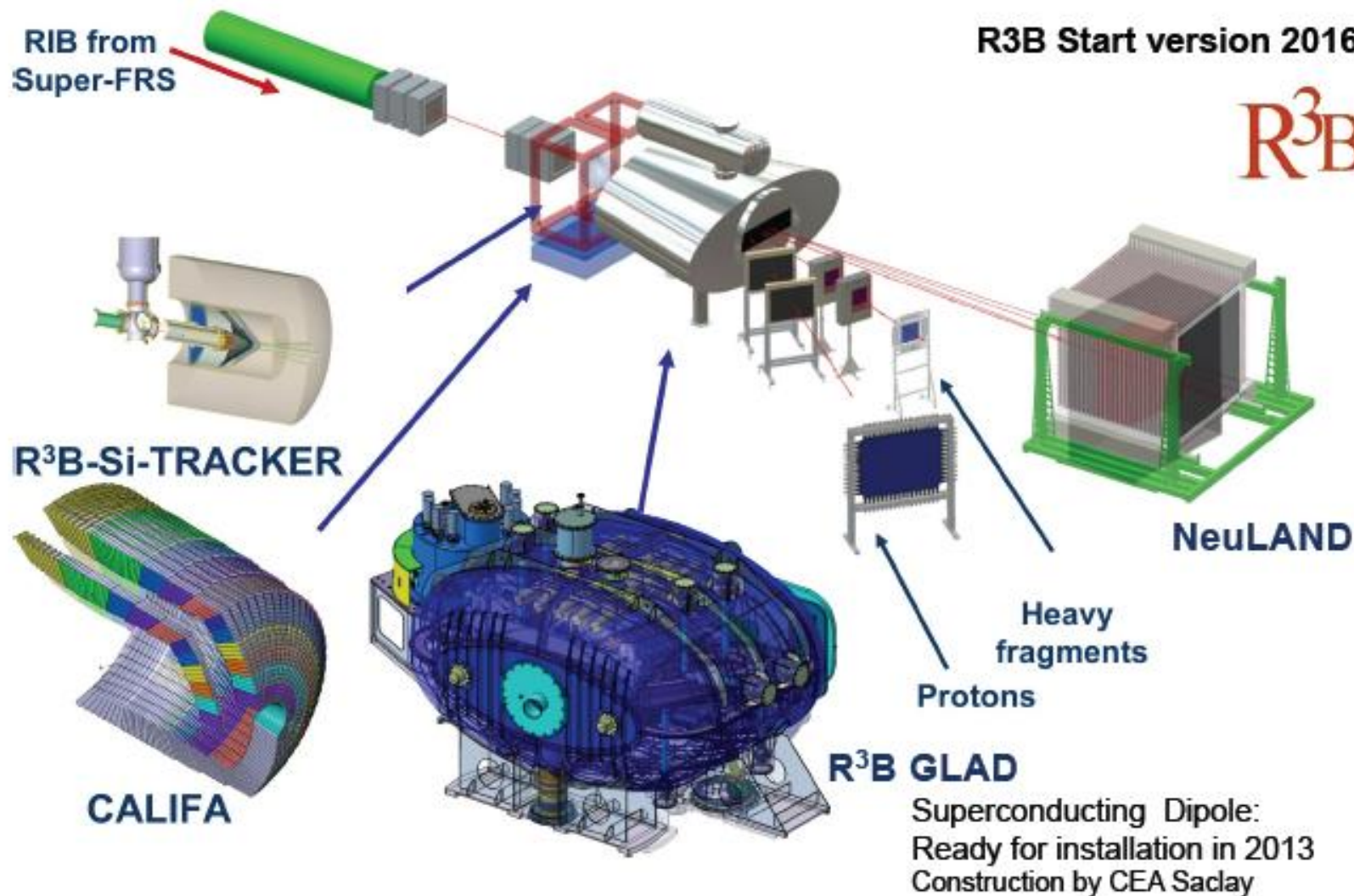
## Storage and Cooler Rings

- Radioactive beams
- e – A collider
- $10^{11}$  stored and cooled 0.8 - 14.5 GeV antiprotons

# Reactions with Relativistic Radioactive Beams

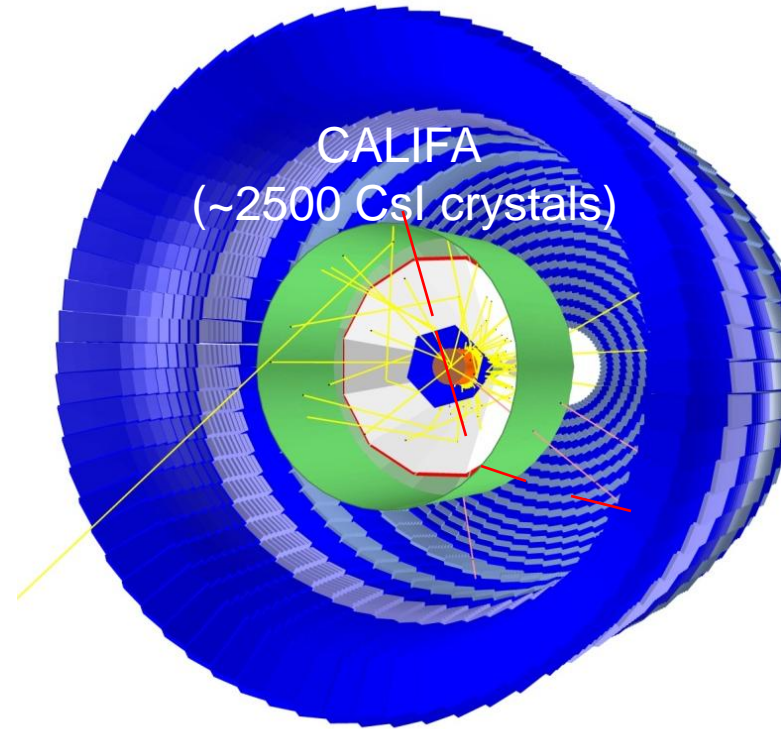
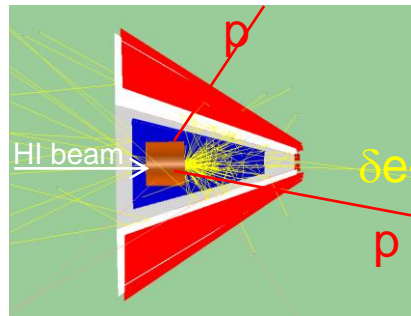
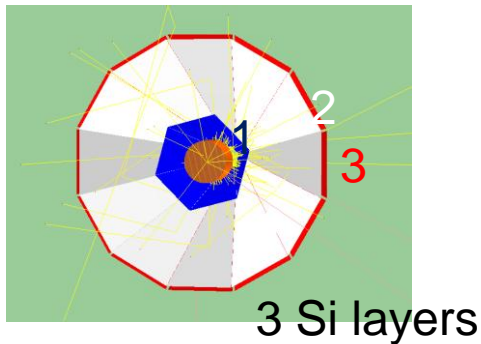
R3B Start version 2016

R<sup>3</sup>B



# Si Tracker for R3B

- Target recoil detector for typical (p,2p) reactions:
  - Si tracker (UK)
  - Calorimeter CALIFA (Spain led collaboration)
  - LH2 target (France and UK)



- Designed to detect target recoil particles from reactions of RIBs with LH2 target
  - e.g. protons with energies from 50 – 500 MeV

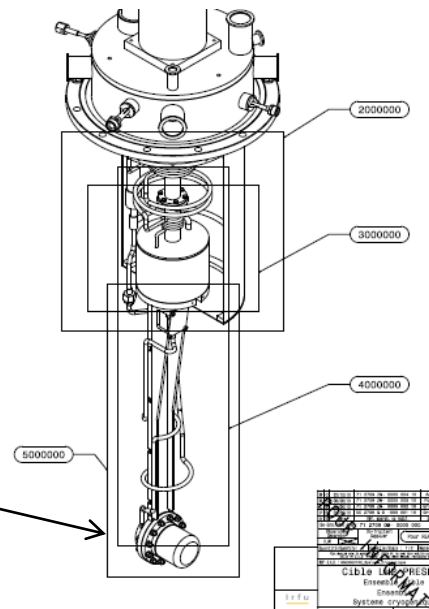
LH2:

Ø 70 mm

Thickness < 61mm

Mylar envelope:

150 -250 µm

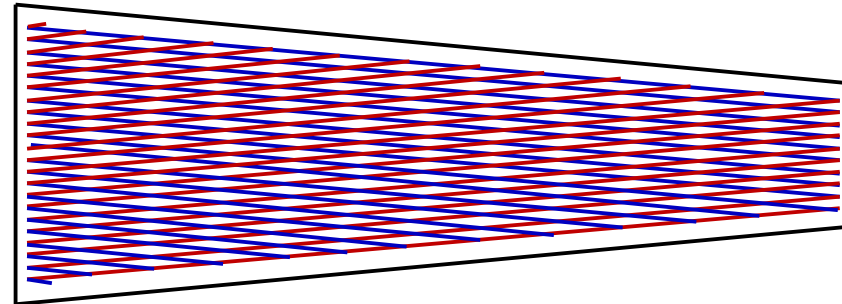




# Si Tracker for R3B

- Provide particle tracking and identification
- Prototype build with double sided stereo angle Si micro strip detector.
- 50 um pitch strips
- Total channels for complete array: ~120k channels (using Si micro-strip)
- ASIC readout (912 ASICs, with 128 channels each)
- inner layer
  - reduce material as much as possible, thickness  $\leq 100\mu\text{m}$ .
  - Evaluating both MAPS and Si micro-strip options
- Two outer layers:
  - 300um thick
- All layers: ~100 um position resolution

Blue P side strips  
Red N side strips  
(Representation only)



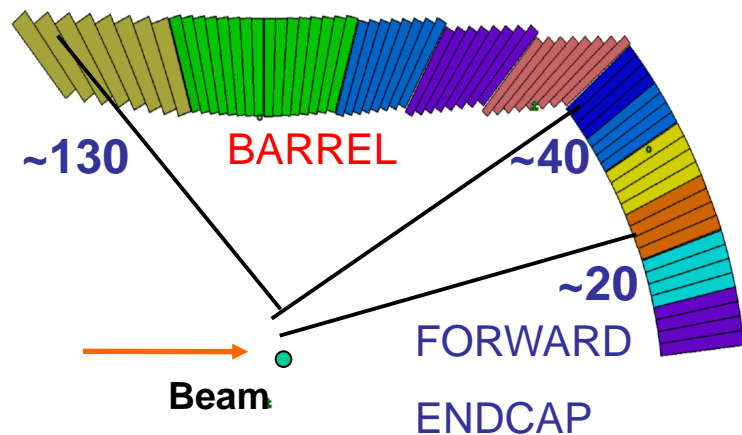
Each silicon detector is double sided with P and N side strips forming a STEREO angle detector arrangement



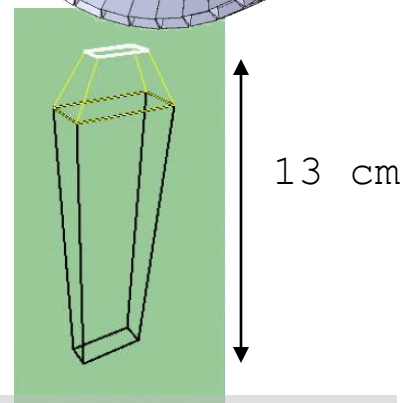
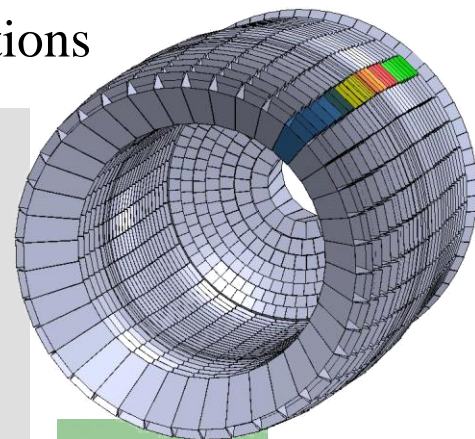
Ladder on which Si detectors and ASICs will be mounted

# Calorimeter - CALIFA

General design of the detector based on kinematical considerations

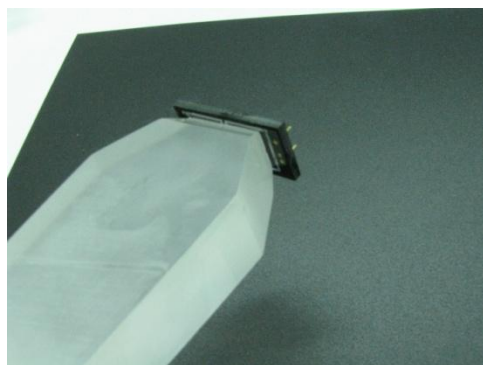


“Egg” shape  
Highly segmented  
Thick detection volume  
Scintillation based  
performant photo-sensors

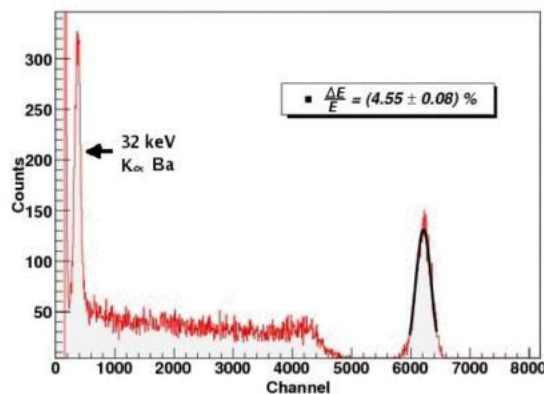


Crystal and photosensors

Barrel  $\rightarrow$  CsI+APD



1 cm<sup>3</sup> and 662 keV  $\gamma$

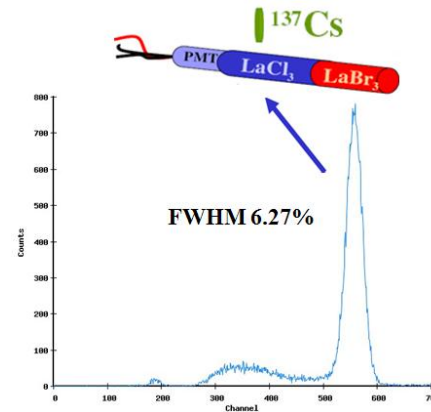
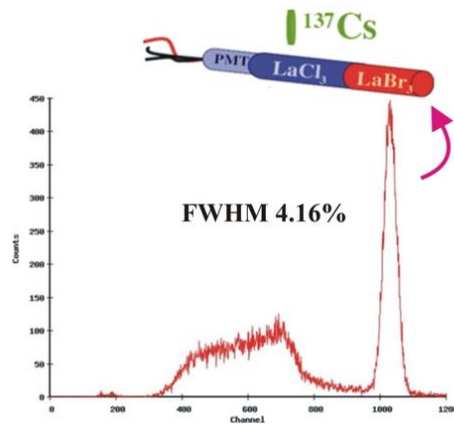


Real shape, 1 MeV  $\gamma$

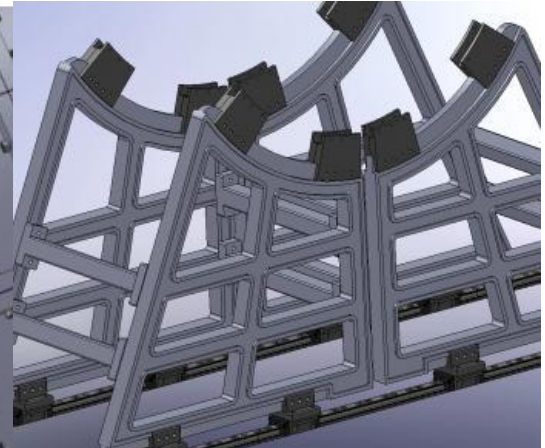
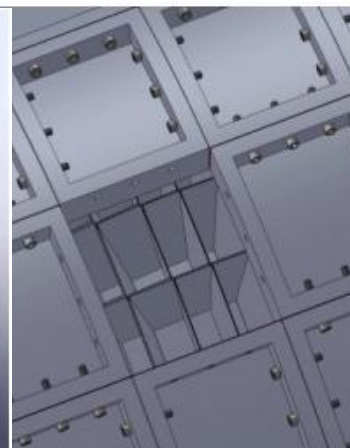
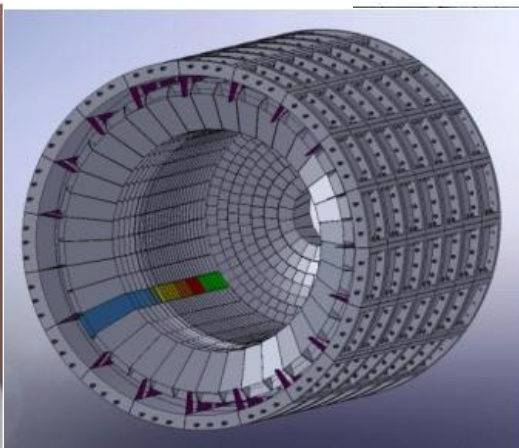
$\rightarrow \Delta E/E \sim 5 \%$

# Calorimeter - CALIFA

Forward Endcap → Phoswich solution is being investigated



Engineering design and Mechanical structure → based on carbon fiber



# Target Recoil Detector for High-Momentum Transfer Region ?

- If we use full RIB energy available at FAIR (1-1.5 AGeV),  $E_p < 1$  GeV
- E-dE techniques alone will not work (punchthrough, secondary reaction losses in scintillator, etc.)
- Possible concept based on tracking in magnetic field

## HERMES recoil detector - 1T solenoid field

### Silicon & Fiber Tracker:

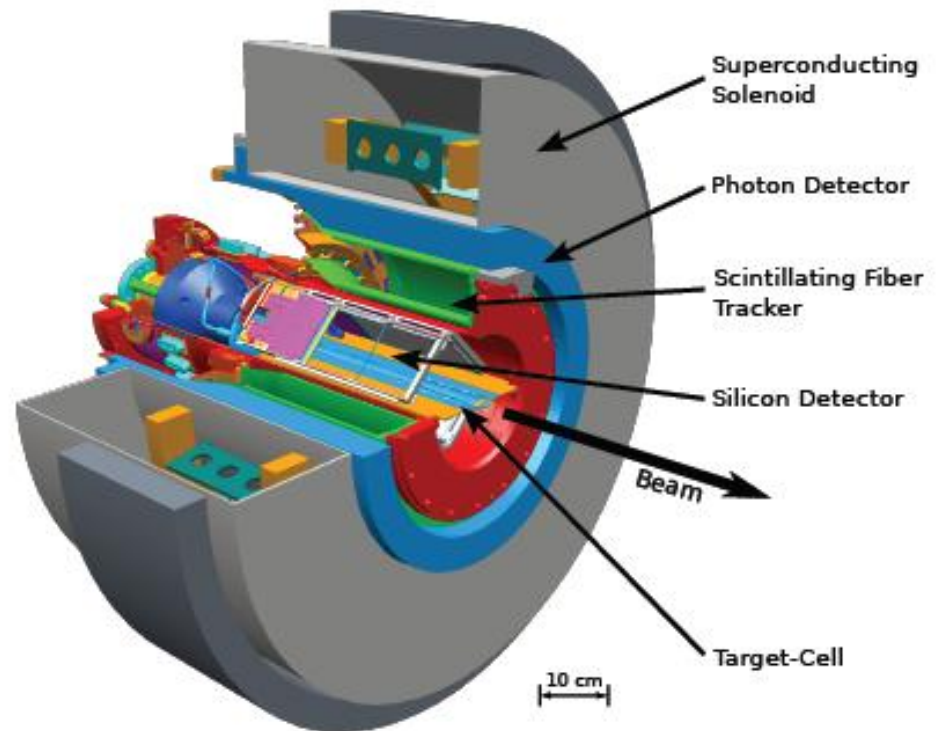
$$p_p \in [135, 1200] \text{ MeV}/c$$

p/ $\pi$  PID for  $p < 650$  MeV/c

### Photon Detector:

p/ $\pi$  PID for  $p > 600$  MeV/c

$\pi^0$  background suppression





# Summary

- QFS a powerful and unique tool to explore correlations and in-medium nucleon properties in asymmetric nuclei
- Both valence and deeply bound nucleons can be studied
- Strong synergy with studies of nuclear matter and neutron stars
- R3B at GSI/FAIR is ideally suited for such studies with beam energies up to 1000 AMeV +
- First experiments with simple target recoil detector in Cave C:
  - Ongoing analysis of  $^{17}\text{Ne}$  and  $^{12}\text{C}$  (p,2p) at 400 AMeV
  - New experiment approved to study complete O isotopic chain in 2010
- New target recoil detector being designed/constructed to significantly enhance capabilities for QFS studies at R3B
- Development of programme to study QFS at high momentum transfer at FAIR
- NOTE: (p,2p) measurements with multi (1-30) GeV protons beams on symmetric nuclei will also be possible at FAIR, e.g. PANDA, CBM