



# *EMMI Program, GSI Darmstadt 2012*

## *“Precision Measurements of Ground-State Properties for Nuclear Structure Studies”*

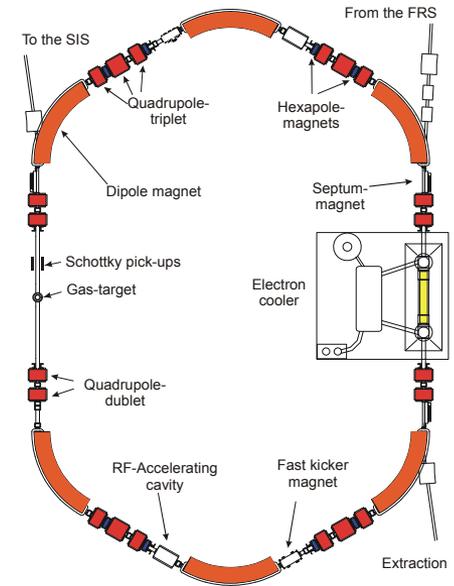
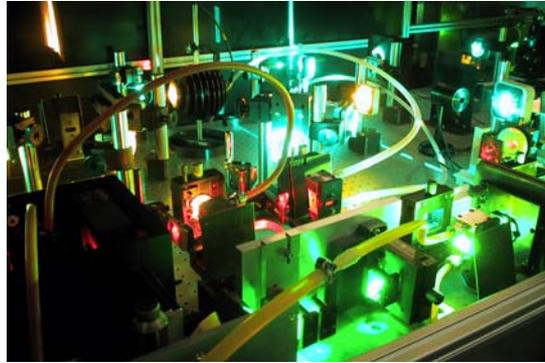


Klaus Blaum  
May 02, 2012





# Outline



● Introduction and motivation

● Principle of laser spectroscopy and mass spectrometry

● Recent results

● Summary and outlook



# Nuclear ground state properties

## What do we learn?

### Charge Radii

nuclear structure: nuclear charge distribution, deformation

### Spins, Moments

microscopic nuclear structure: wave functions, coupling of nucleons, configuration mixing, shell structure

macroscopic nuclear structure: deformation

### Masses

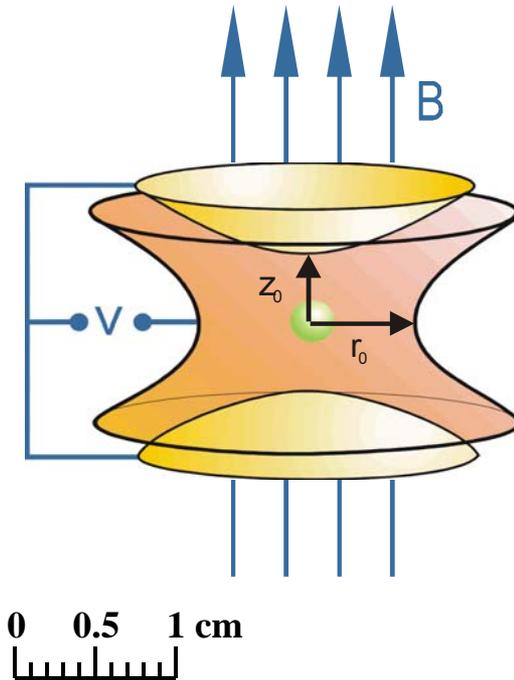
nuclear binding energy

basic test of nuclear models

nuclear structure: shell closures, pairing, onset of deformation, drip lines, halos

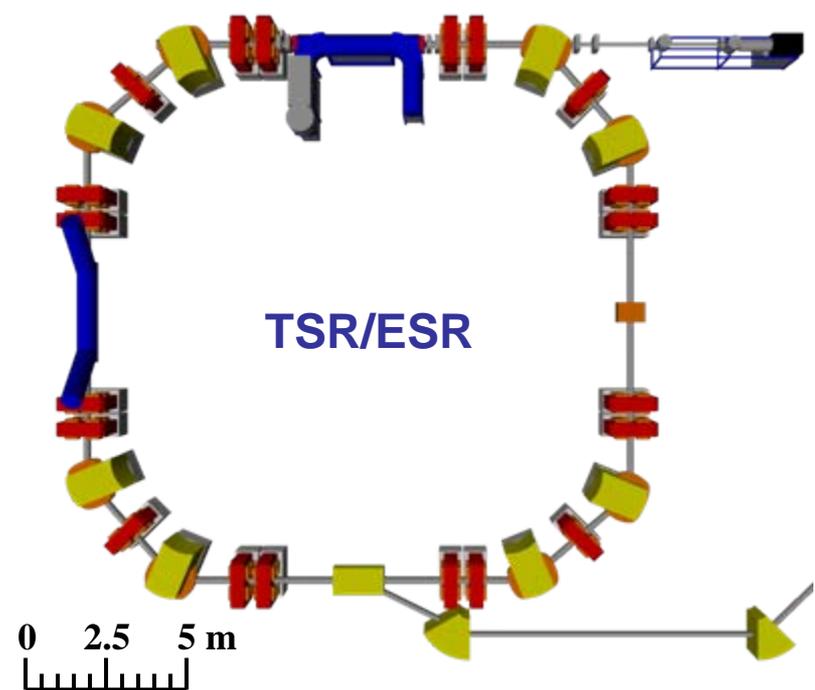
# Storage and cooling techniques

Penning trap



particles at nearly rest in space

Storage ring



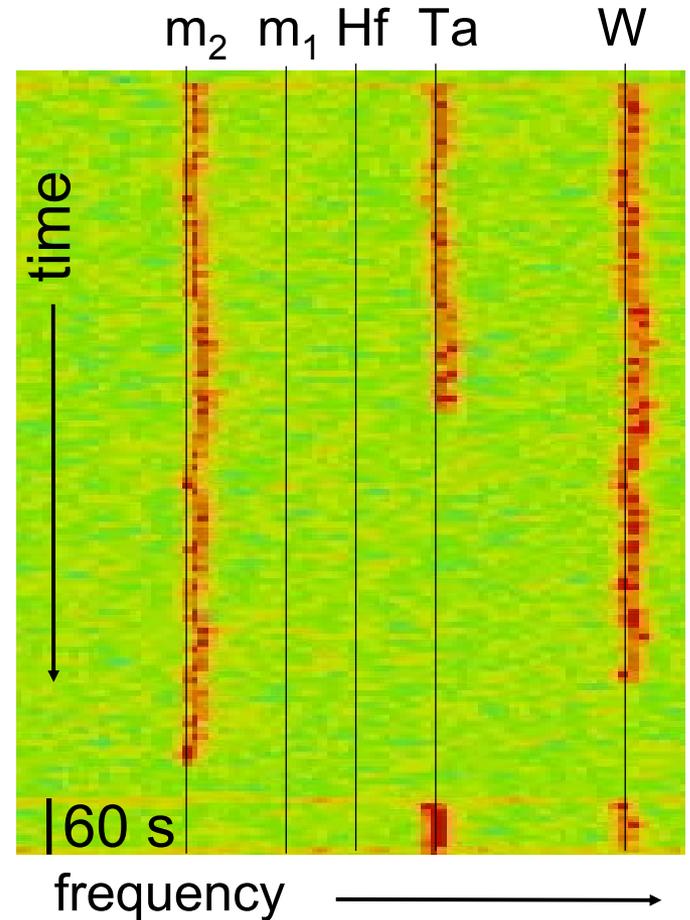
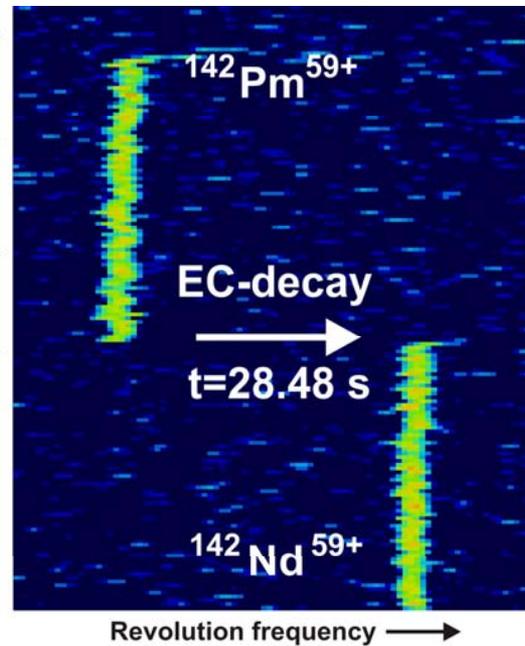
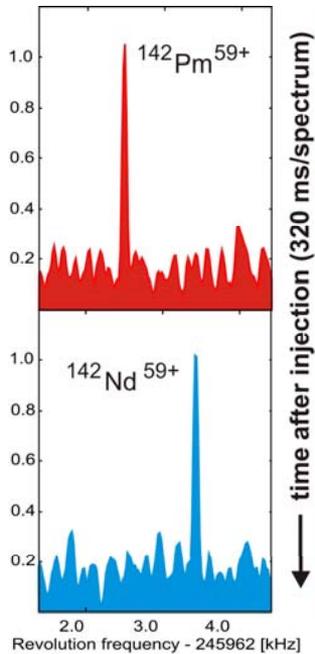
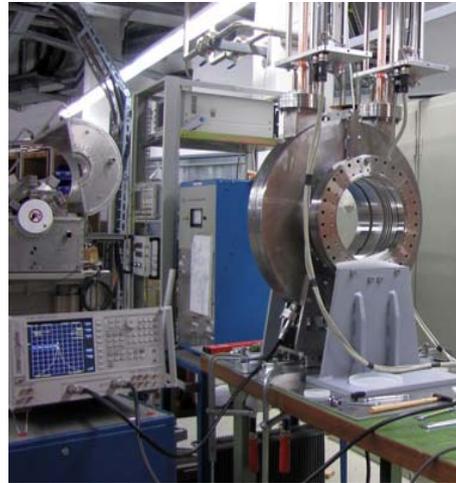
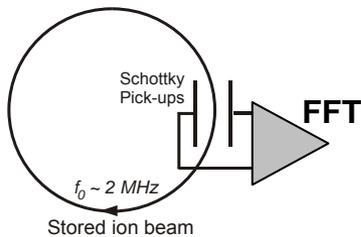
relativistic particles

- \* ion cooling
- \* single-ion sensitivity
- \* long storage times
- \* high accuracy



# Single ion sensitivity

Schottky detection in a storage ring

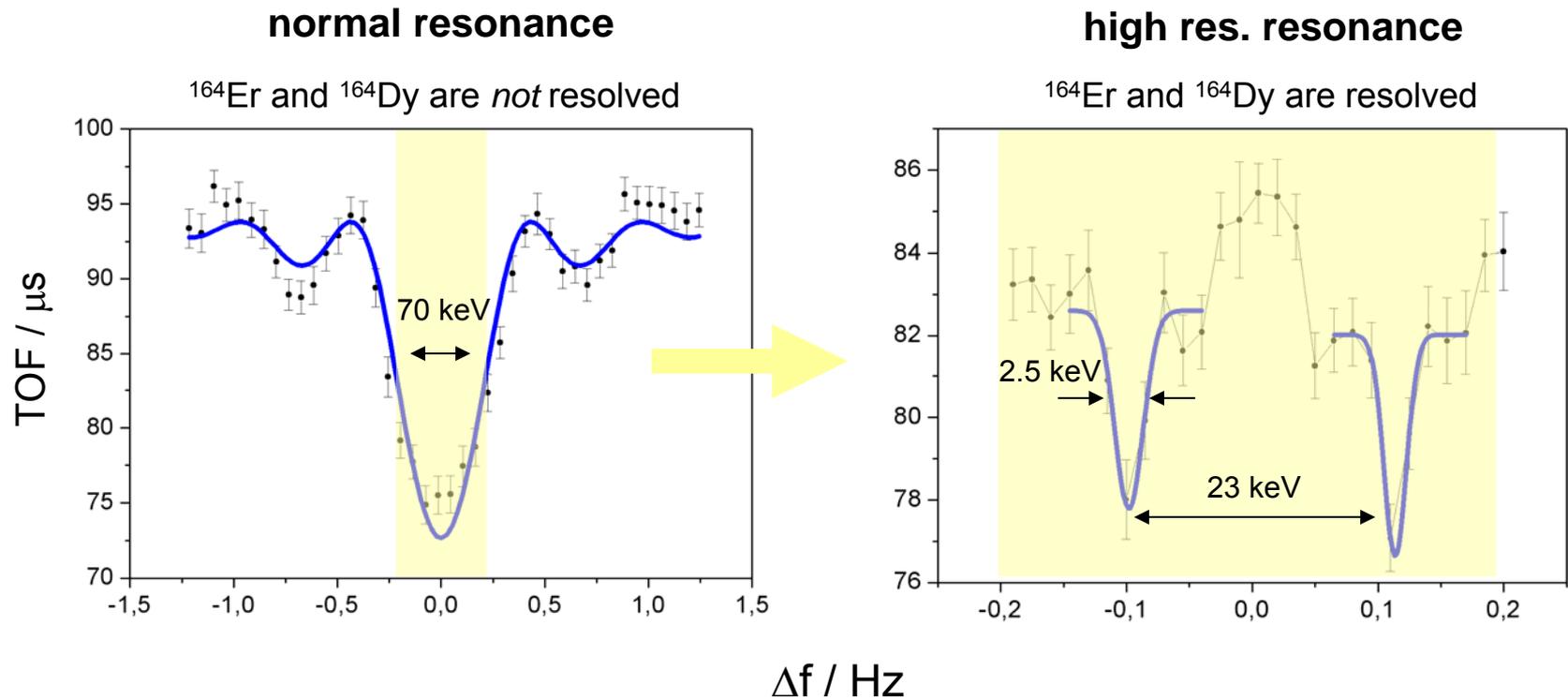


Discovery of new isotopes and isomers.

Hf: Phys. Rev. Lett. 105 (2010) 172501



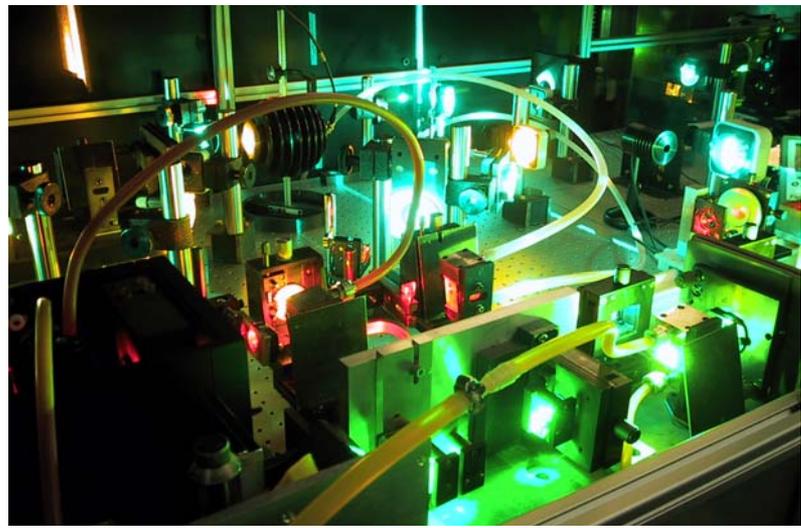
# Ultra-high resolving power



**A resolving power of  $10^8$  has been demonstrated in a Penning trap.**



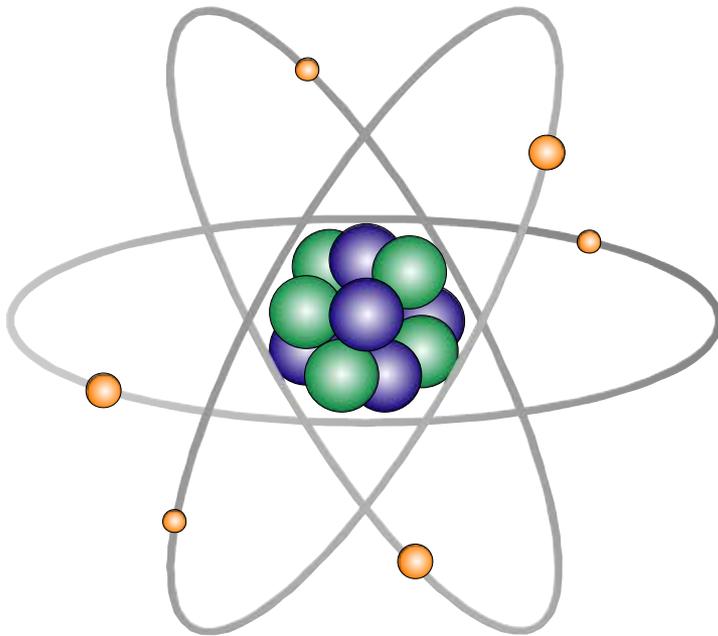
# High-precision Penning trap and laser experiments



**Determination of atomic and nuclear ground state properties:  
masses, binding energies,  $g$ -factors, nuclear moments, radii**

# Applications of precision masses

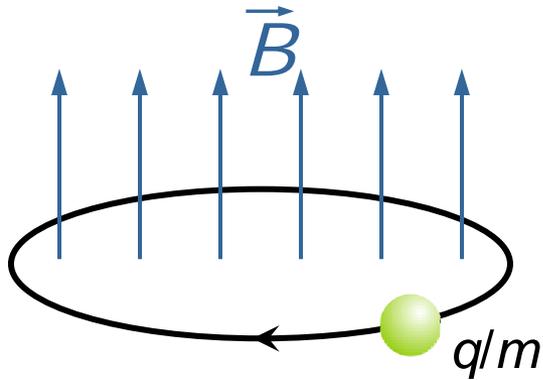
High-accuracy mass measurements allow one to determine the atomic and nuclear binding energies reflecting all forces in the atom/nucleus.



$$= N \cdot \text{green sphere} + Z \cdot \text{purple sphere} + Z \cdot \text{orange sphere} - \text{binding energy}$$

$$M_{\text{Atom}} = N \cdot m_{\text{neutron}} + Z \cdot m_{\text{proton}} + Z \cdot m_{\text{electron}} - (B_{\text{atom}} + B_{\text{nucleus}})/c^2$$

# Principle of Penning trap mass spectrometry

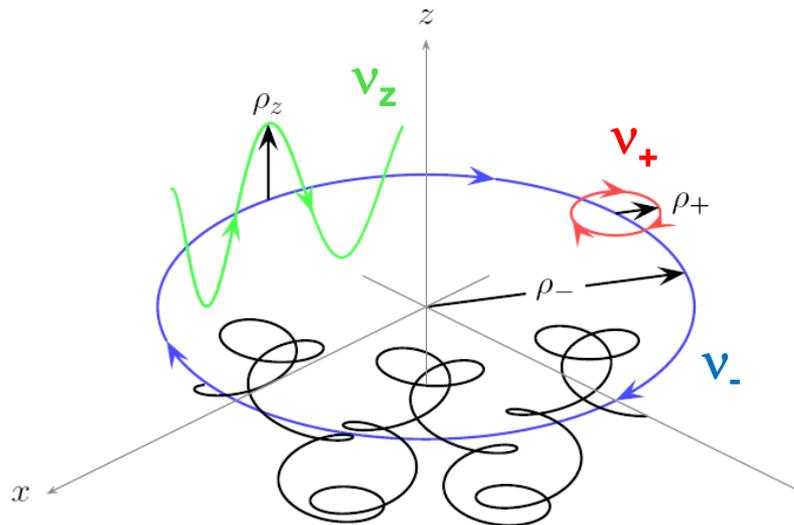
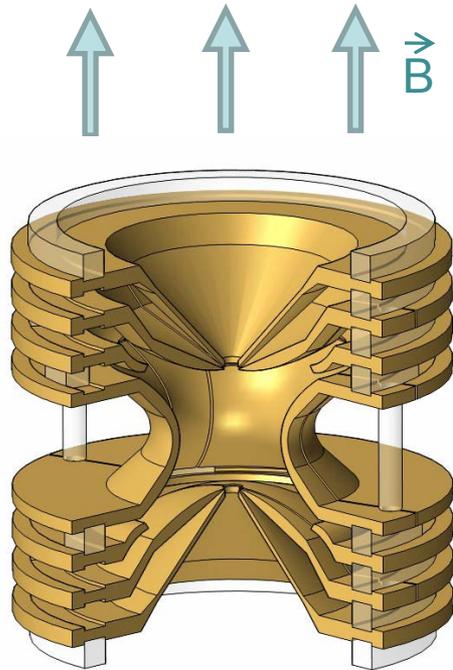


Cyclotron frequency:

$$f_c = \frac{1}{2\pi} \cdot \frac{q}{m} \cdot B$$

## PENNING trap

- Strong homogen. magnetic field
- Weak electric 3D quadrupole field



Typical freq.

$$q = e$$

$$m = 100 \text{ u}$$

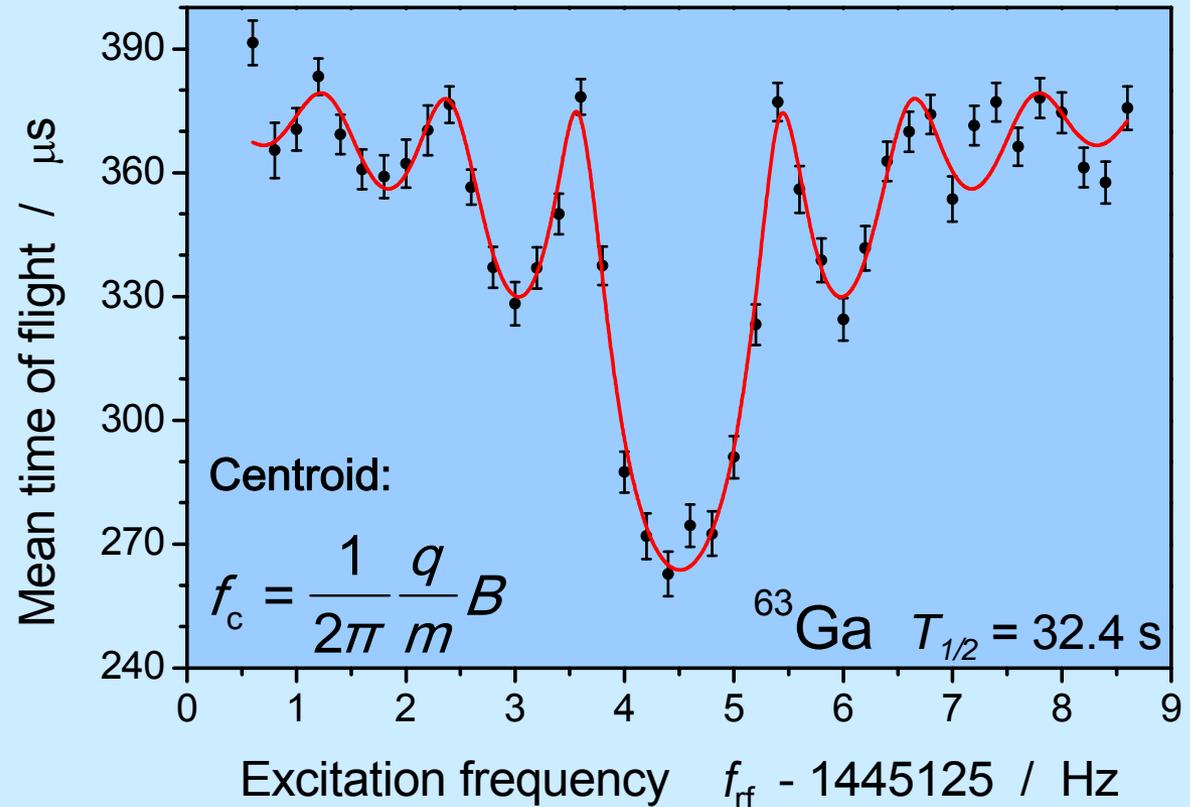
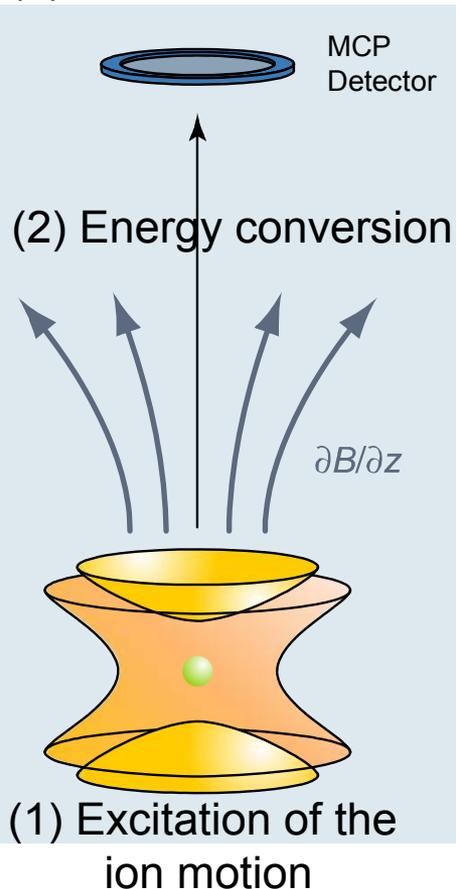
$$B = 6 \text{ T}$$

$$\Rightarrow f_- \approx 1 \text{ kHz}$$

$$f_+ \approx 1 \text{ MHz}$$

# TOF cyclotron resonance detection

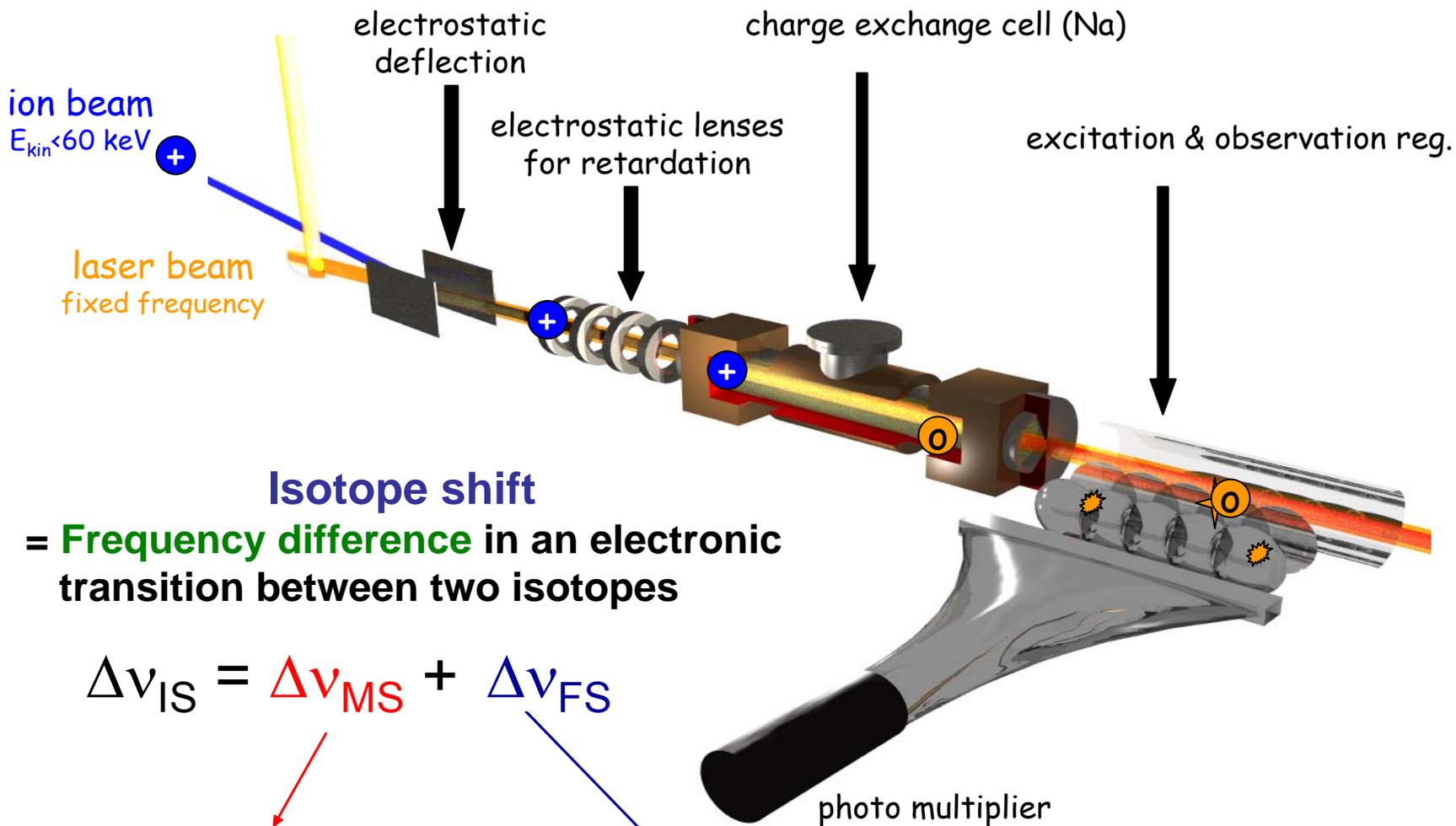
## (3) TOF measurement



Determine atomic mass from frequency ratio  
with a well-known “reference mass”.

$$\frac{f_{c,\text{ref}}}{f_c} = \frac{m - m_e}{m_{\text{ref}} - m_e}$$

# Principle of collinear laser spectroscopy



## Isotope shift

= Frequency difference in an electronic transition between two isotopes

$$\Delta\nu_{IS} = \Delta\nu_{MS} + \Delta\nu_{FS}$$

Mass Effect

$$\Delta\nu_{MS} \sim (A-A')/AA'$$

$$\frac{2\pi Z}{3}$$

$$|\psi(0)|^2 \delta\langle r^2 \rangle \text{ Field Shift}$$



# TRIGA-SPEC: TRIGA-LASER + TRIGA-TRAP

project start @ TRIGA: 01/08  
start off-line data taking: 05/09

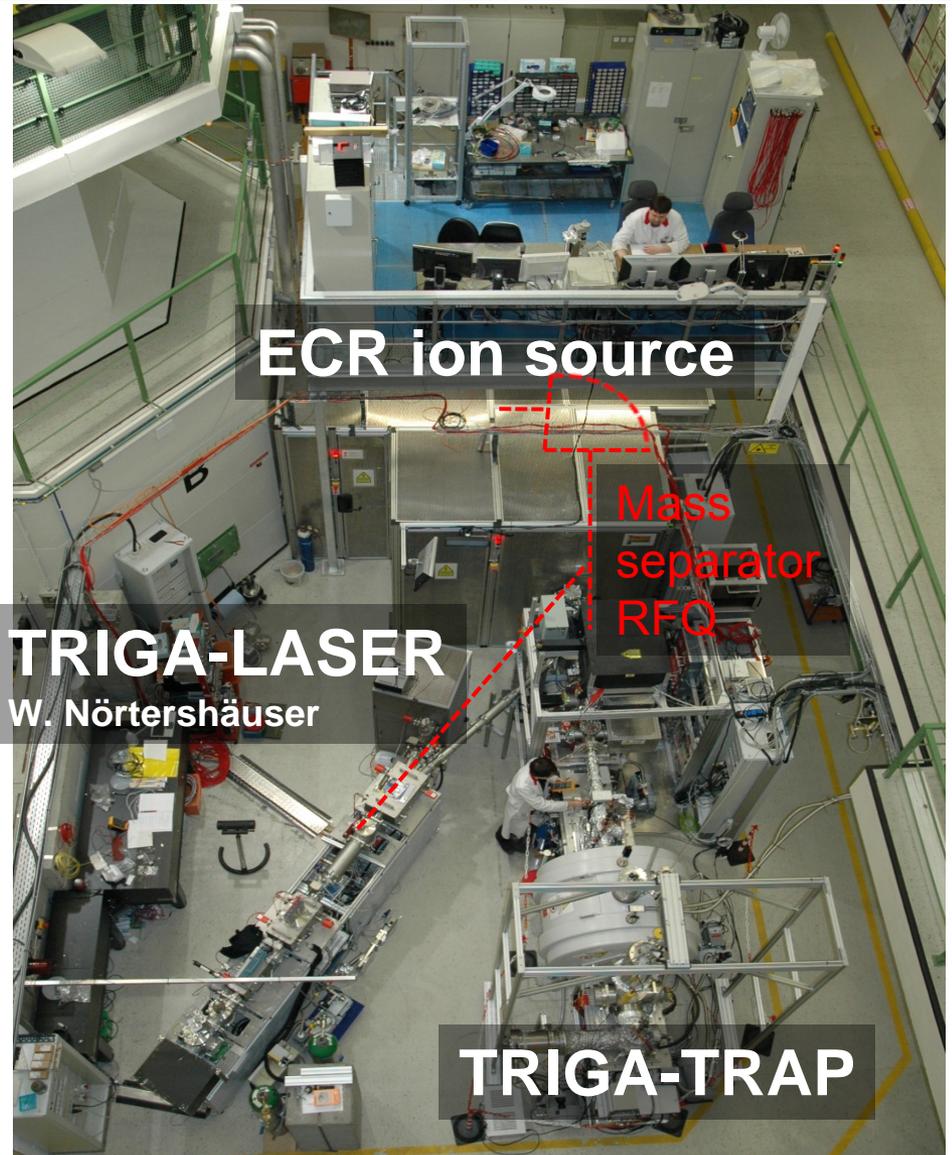


TRIGA Mainz

G. Hampel  
K. Eberhardt  
N. Trautmann

steady 100 kW,  
pulsed 250 MW,  
neutron flux  $1.8 \times 10^{11}$  / cm<sup>2</sup>s

Nucl. Instrum. Meth. A 594, 162 (2008)





# Nuclear structure studies

Only Penning trap mass measurements!

Stability  
of SHE

Isospin Symmetry  
Pairing

Exotic decays  
Fundamental  
Interactions

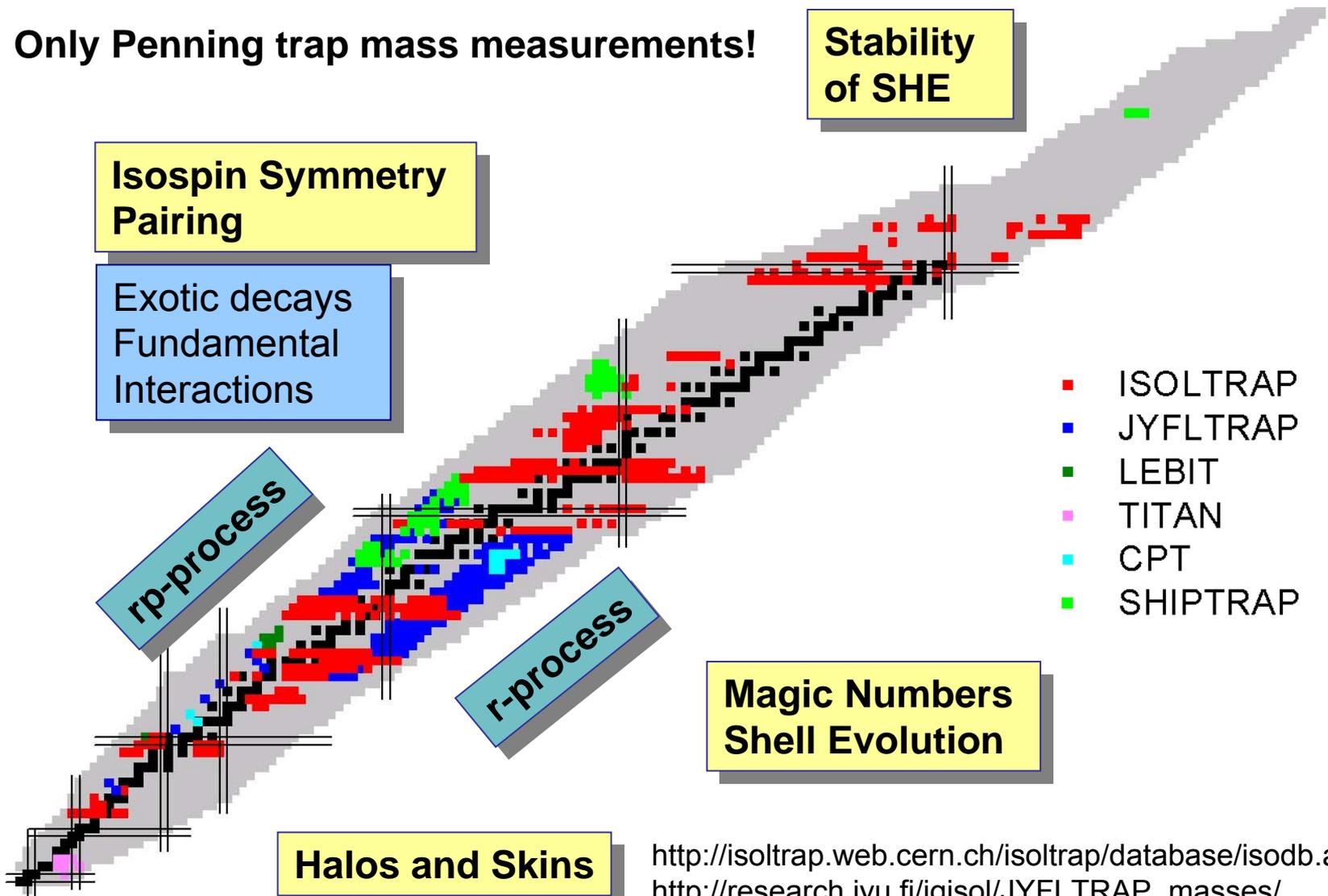
rp-process

r-process

Magic Numbers  
Shell Evolution

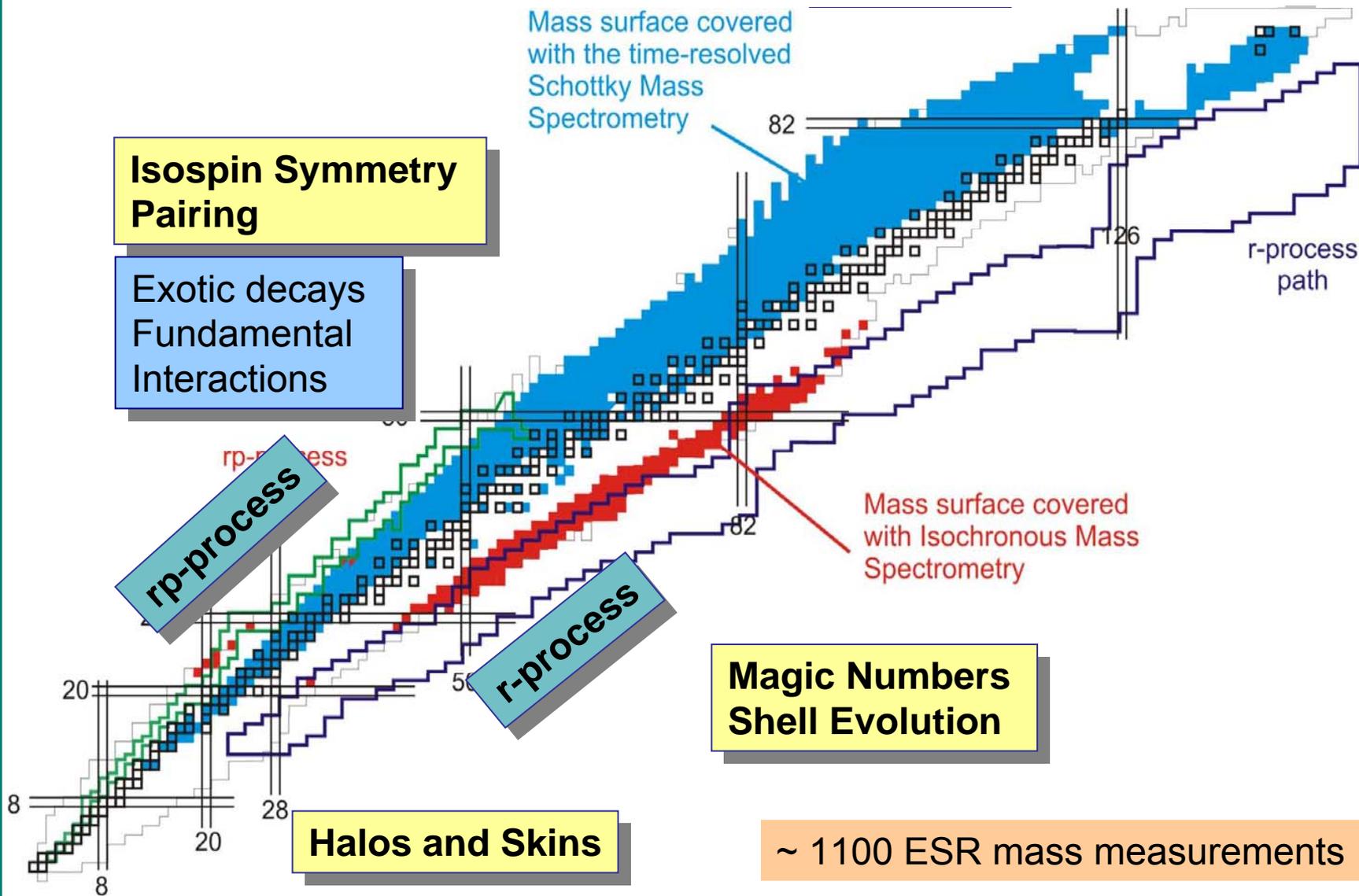
Halos and Skins

- ISOLTRAP
- JYFLTRAP
- LEBIT
- TITAN
- CPT
- SHIPTRAP



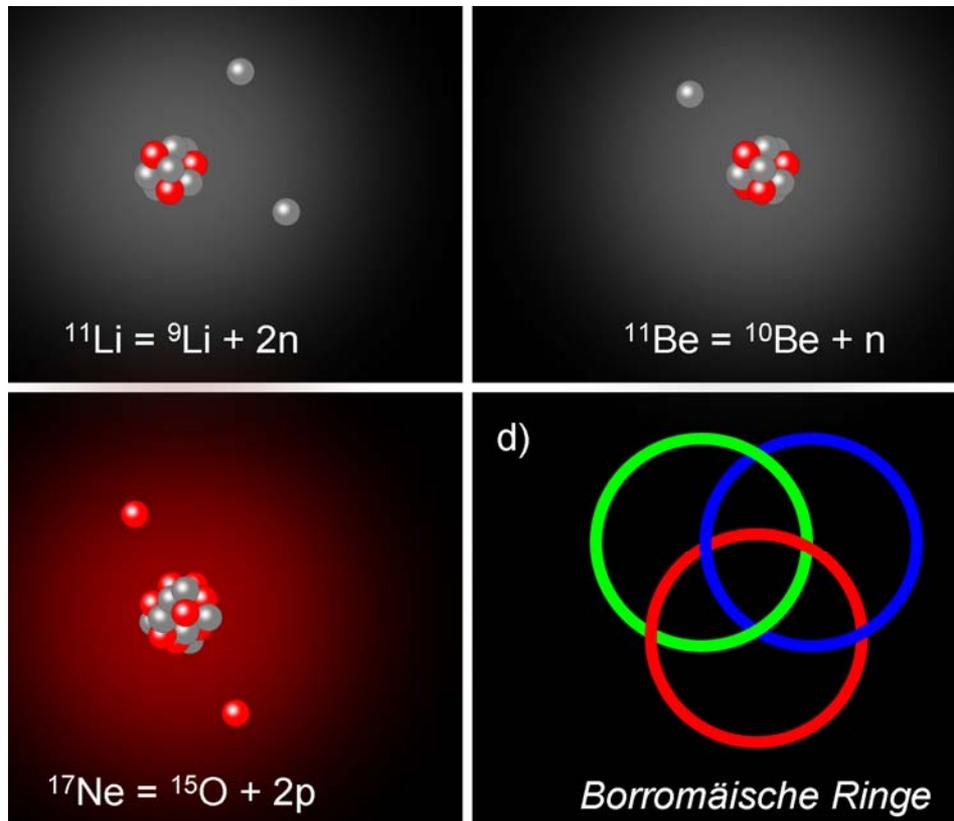
<http://isoltrap.web.cern.ch/isoltrap/database/isodb.asp>  
[http://research.jyu.fi/igisol/JYFLTRAP\\_masses/](http://research.jyu.fi/igisol/JYFLTRAP_masses/)

# Nuclear structure studies



# Investigation of nuclear halos

... via nuclear mass (binding energy) and charge radii measurements!



$^{6,8}\text{He}$

P. Mueller *et al.*, PRL 99, 252501 (2007)  
V.L. Ryjkov *et al.*, PRL 101, 012501 (2008)

$^{9,11}\text{Li}$ :

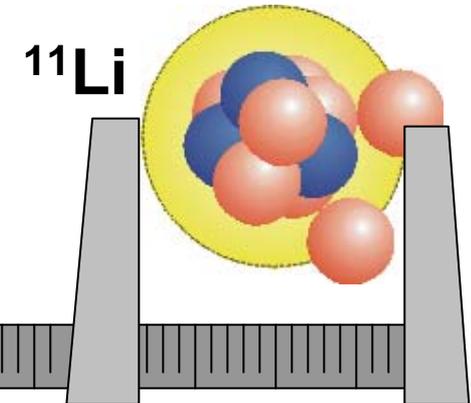
R. Neugart *et al.*, PRL 101, 132502 (2008)  
M. Smith *et al.*, PRL 101, 202501 (2008)

$^{11}\text{Be}$ :

W. Nörtershäuser *et al.*, PRL102, 062503 (2009)  
R. Ringle *et al.*, PLB 675, 170 (2009)

$^{17}\text{Ne}$ :

W. Geithner *et al.*, PRL102, 252502 (2008)

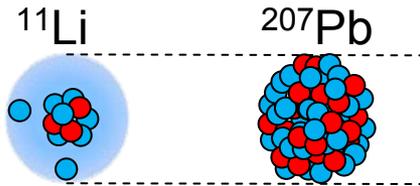


Argonne, GANIL, GSI, ISOLDE, TRIUMF

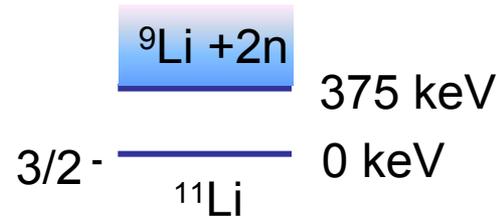
# Beryllium: nuclear charge radii

## characteristic properties of nuclear halos

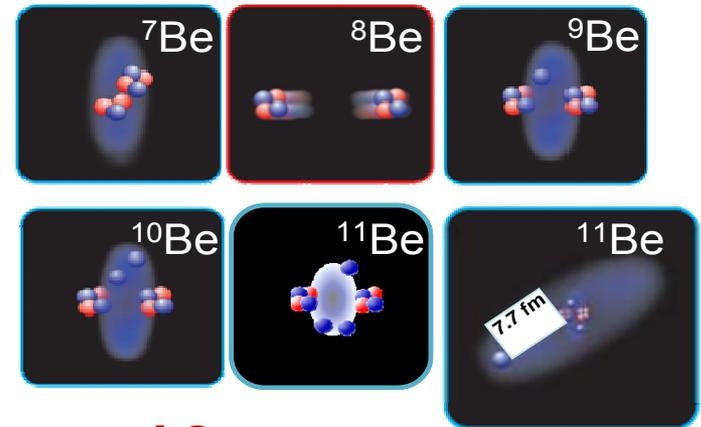
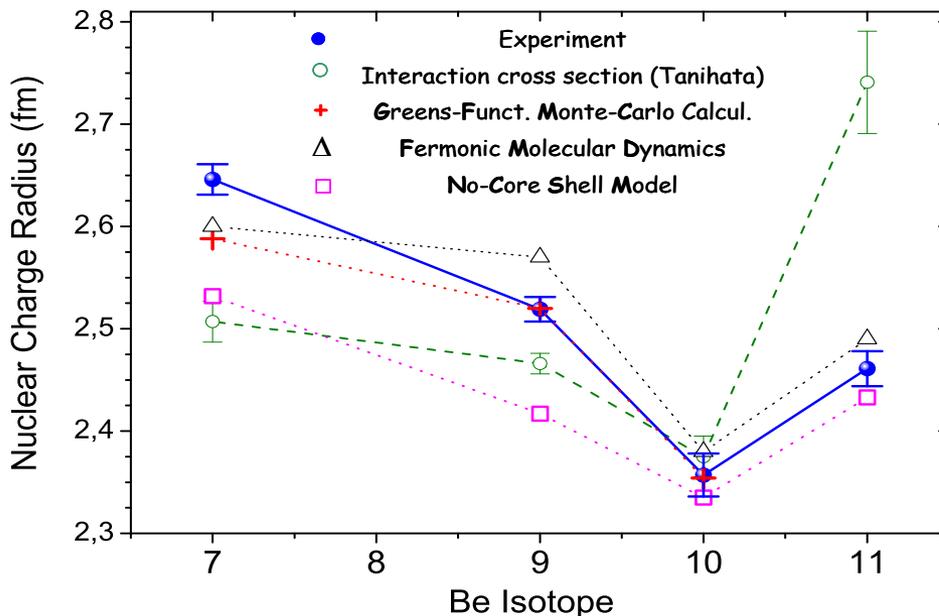
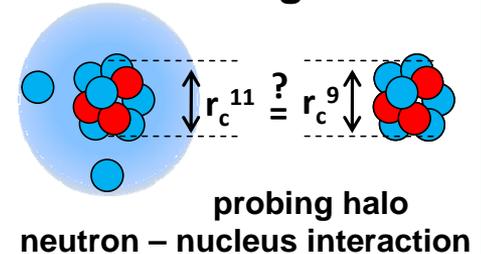
large matter radius



weakly bound



increased charge radius

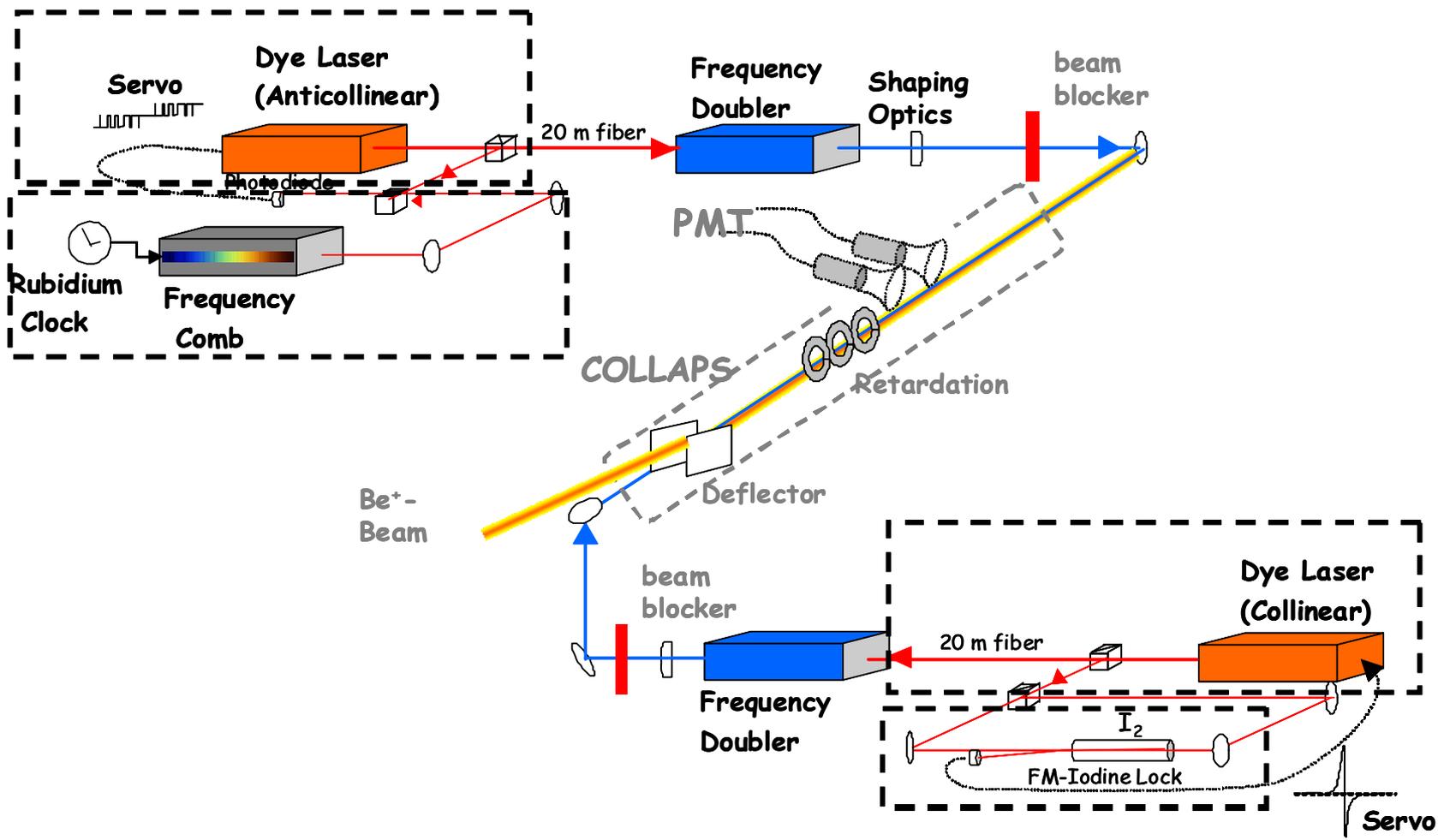


# 12Be

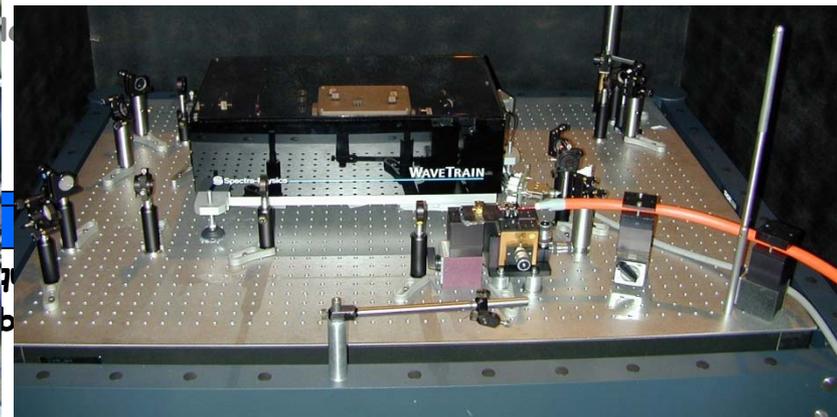
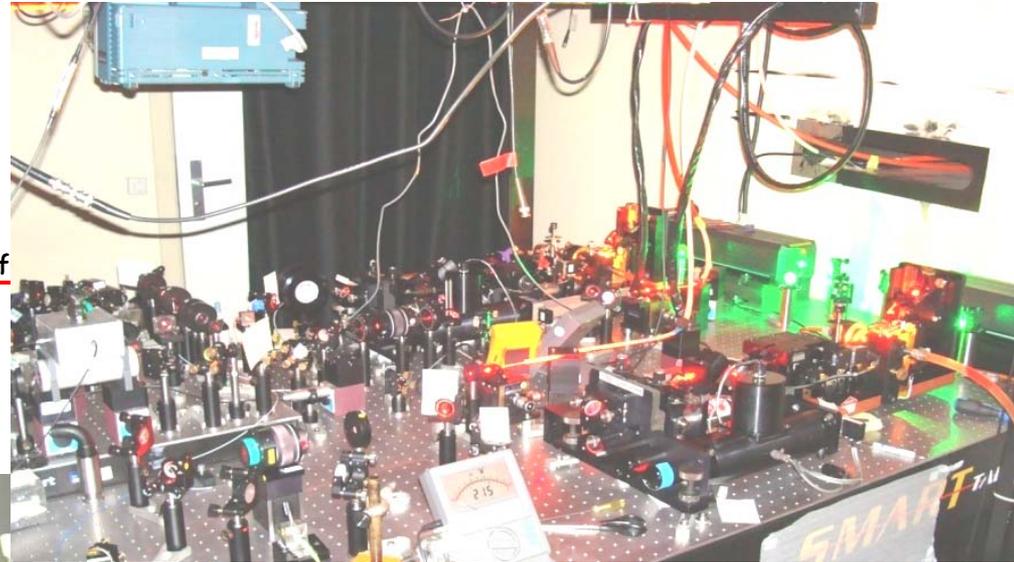
<sup>11</sup>Be: Phys. Rev. Lett. 102, 062503 (2009)

„Size“ and structure determination of the neutron halos in <sup>11,12</sup>Be

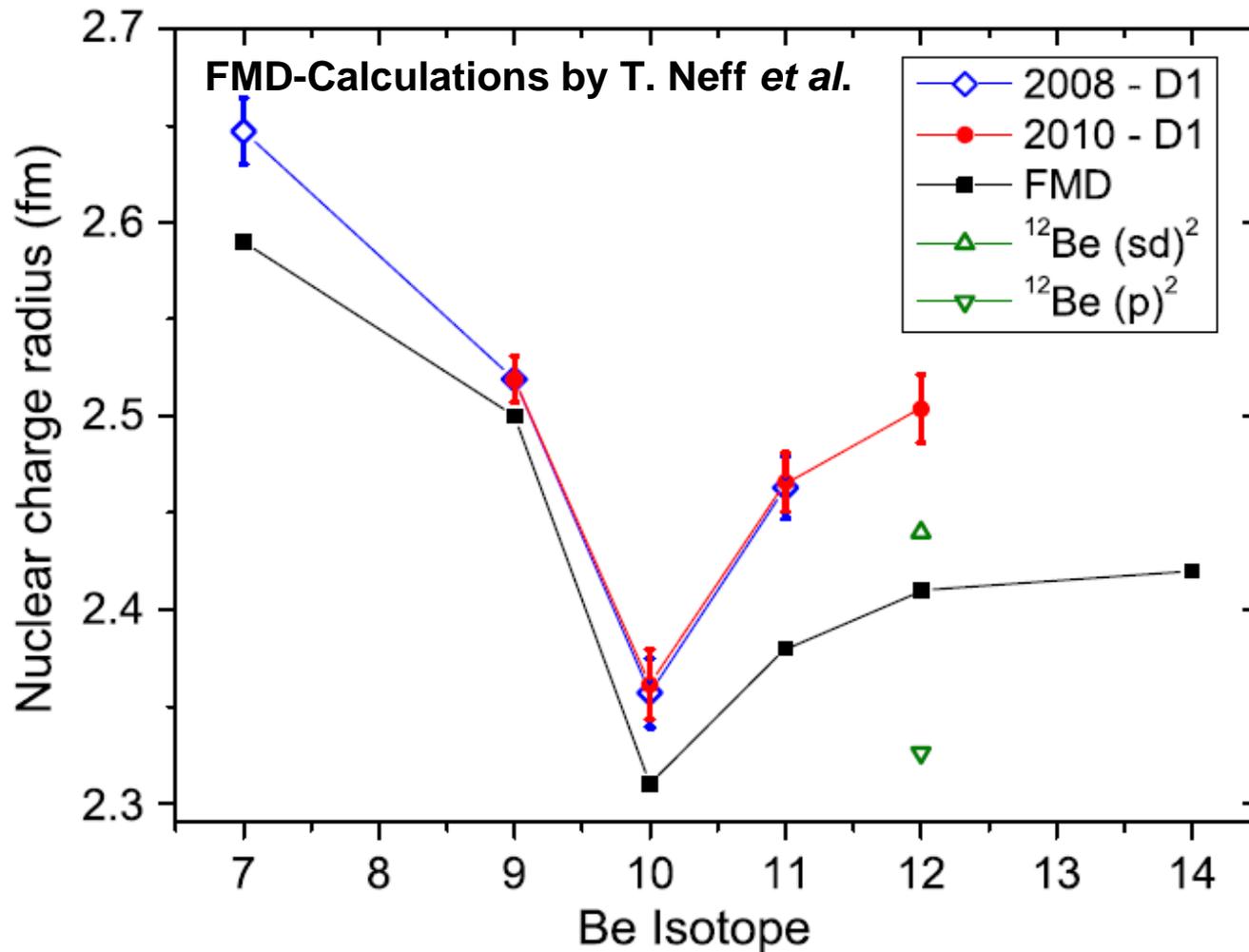
# Be spectroscopy – laser system



# Be spectroscopy – laser system



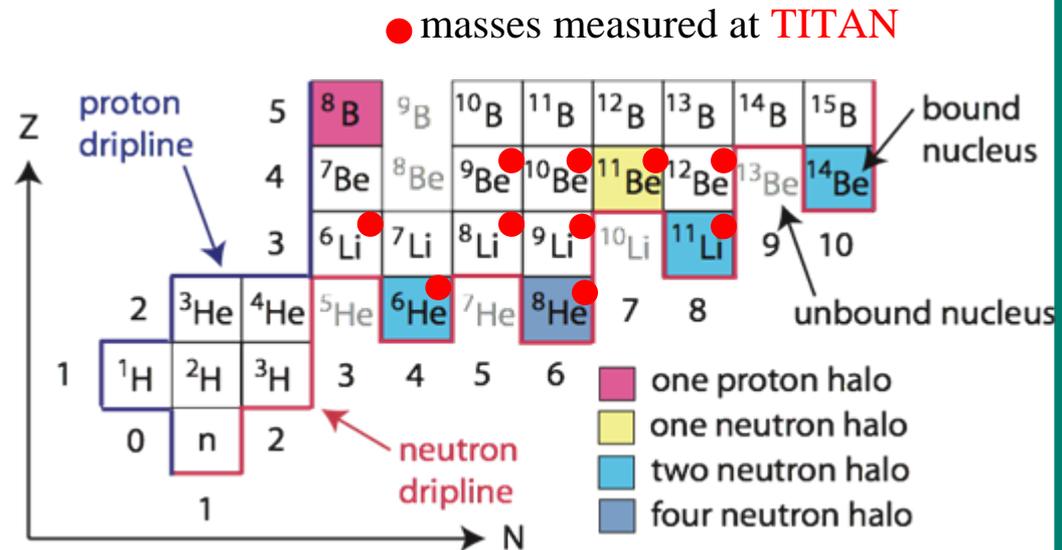
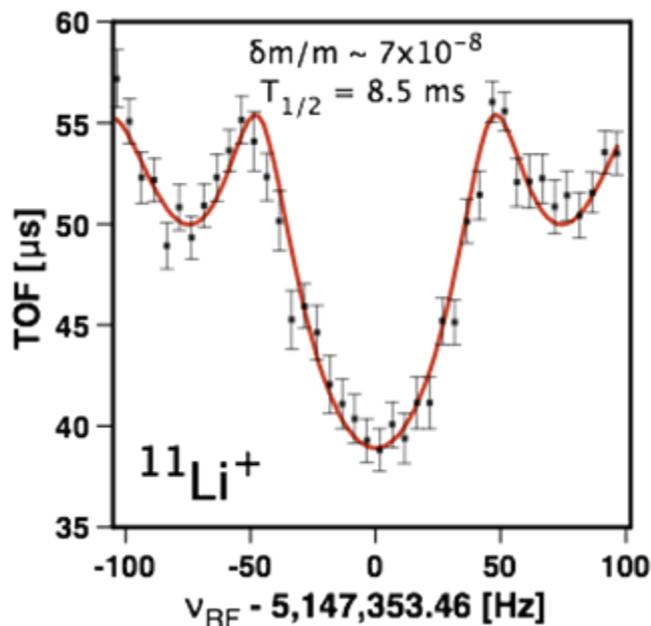
# Beryllium: Nuclear Charge Radii



# Halo mass measurements

## Motivations:

- 1) guide nuclear theory and refine our understanding of the nucleus
- 2) mass is the **major** contribution to the charge radius error



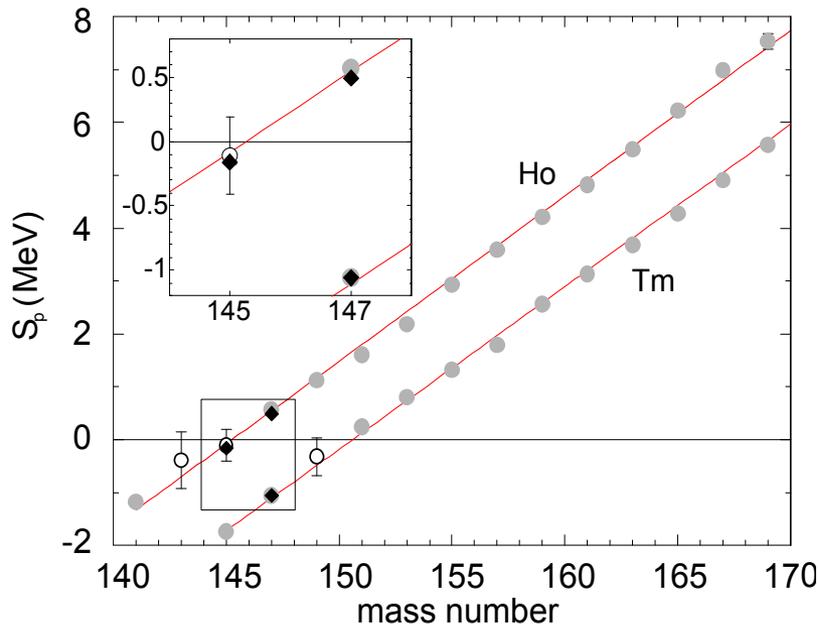
Ab-initio methods points to the need of 3-body interactions in order to explain both the binding energy and charge radius of halo nuclei.

TITAN (TRIUMF)

e.g. V.L. Ryjkov *et al.*, PRL 101, 012501 (2008), M. Smith *et al.*, PRL 101, 202501 (2008)

# Nuclear structure studies

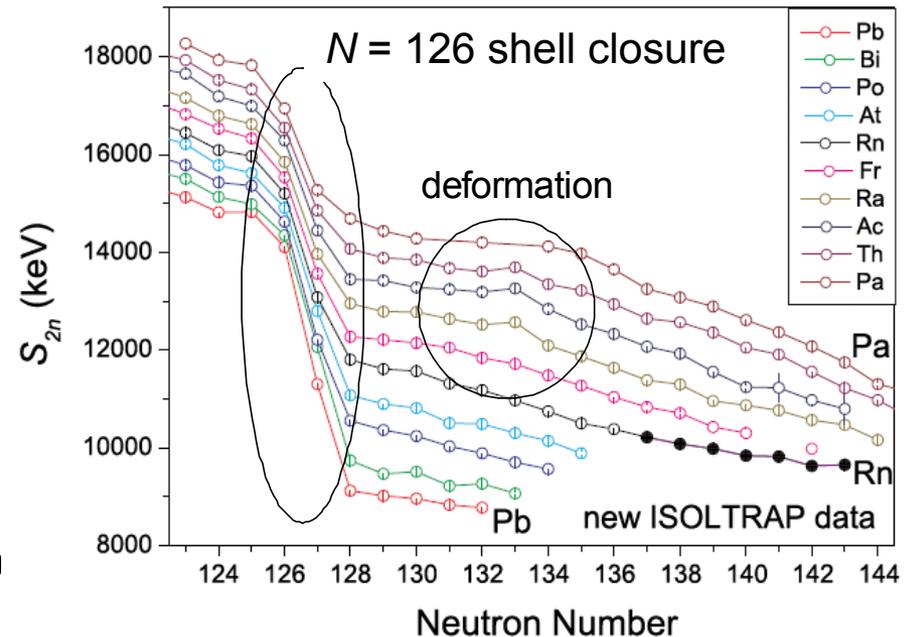
$$S_p = B(Z, N) - B(Z-1, N)$$



SHIPTRAP: First direct mass measurement beyond the proton dripline.

C. Rauth *et al.*, Phys. Rev. Lett. 100, 012501 (2008)  
 M. Dworschak *et al.*, Phys. Rev. Lett. 100, 072501 (2008)  
 W. Geithner *et al.*, Phys. Rev. Lett. 101, 252502 (2008)

$$S_{2n} = B(Z, N) - B(Z, N-2)$$

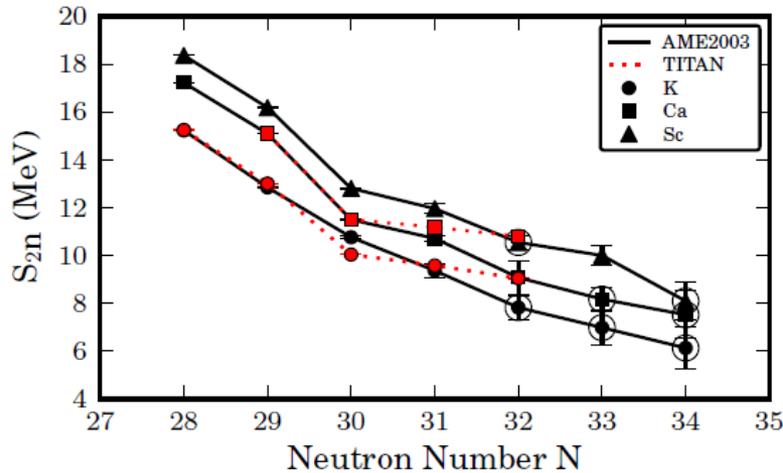


CPT/ISOLTRAP/JYFLTRAP/LEBIT/TITAN: Investigation of shell closures, halos, ...

B. Cakirli *et al.*, Phys. Rev. Lett. 102, 082501 (2009)  
 D. Neidherr *et al.*, Phys. Rev. Lett. 102, 112501 (2009)  
 S. Naimi *et al.*, Phys. Rev. Lett. 105, 032502 (2010)

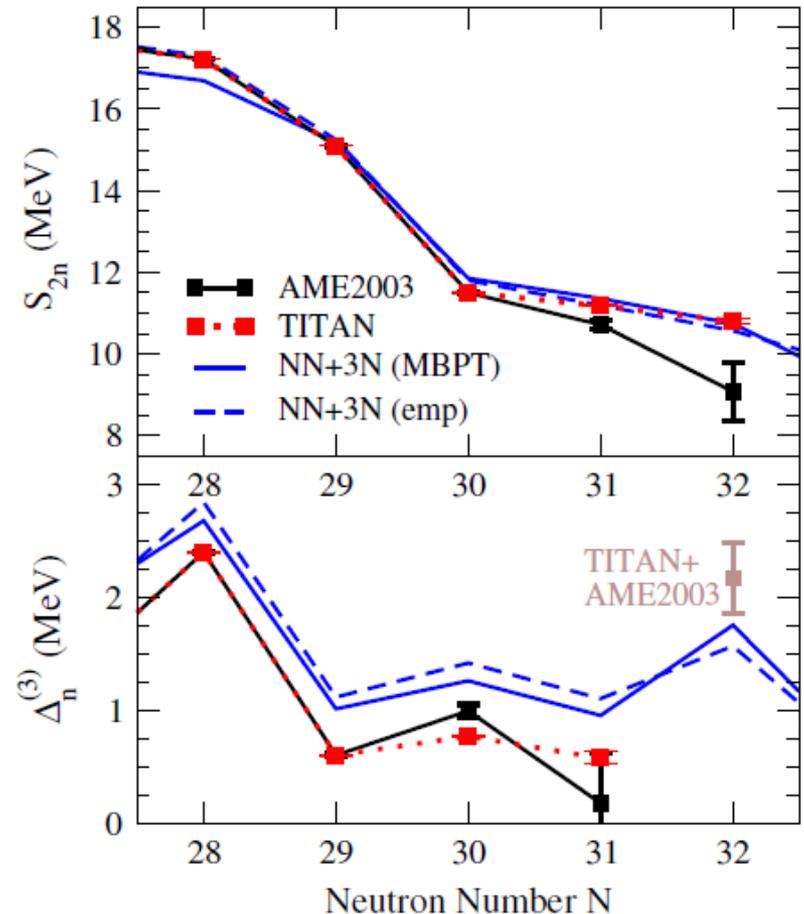
# Nuclear masses and 3N-forces

## New neutron-rich Ca and K masses.



$^{52}\text{Ca}$  is more bound by 1.74 MeV.

Calculations including three-nucleon (3N) forces by A. Schwenk *et al.*

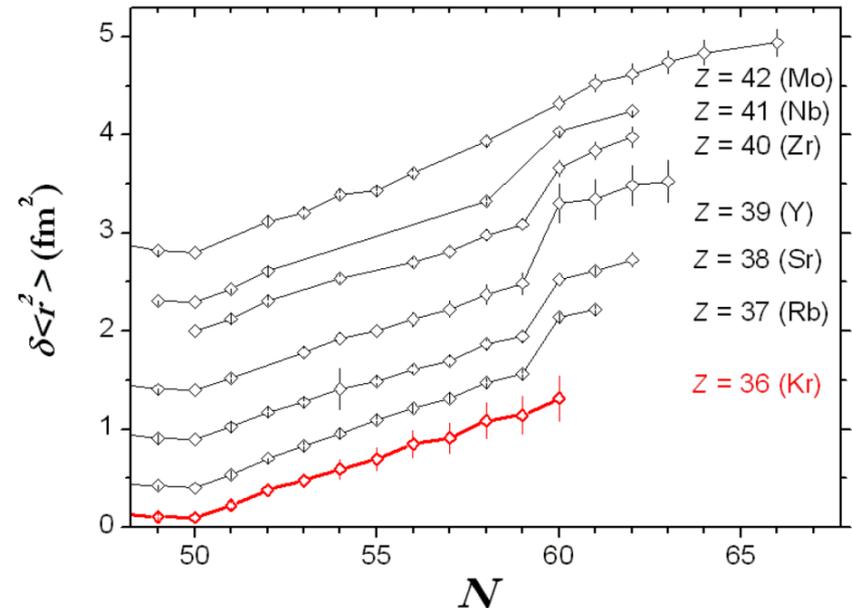
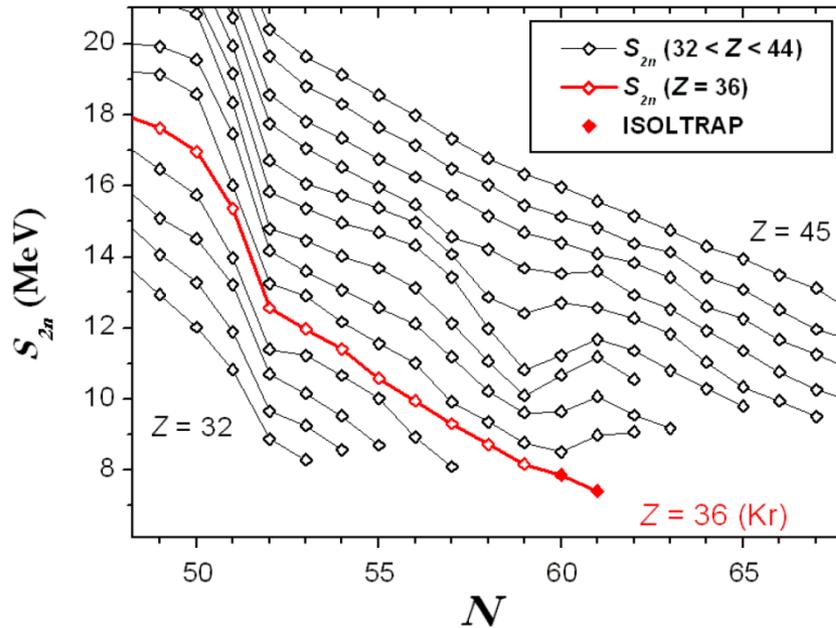


TITAN (TRIUMF)

A.T. Gallant *et al.*, ArXiv 1204.1987v1 (2012).

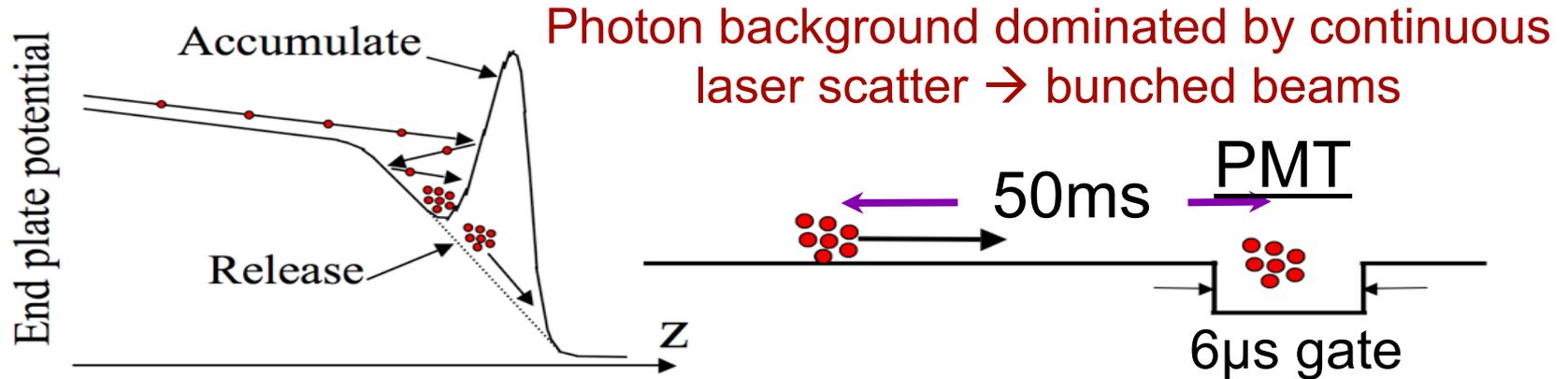


# Quantum phase transition

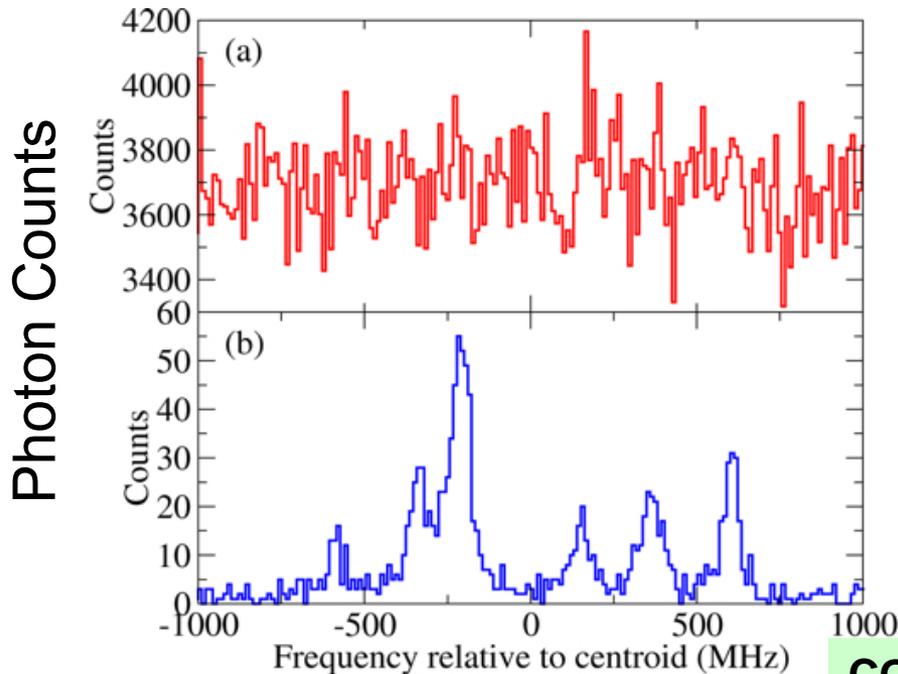


- End of phase transition region reached: critical-point boundary
- Supported by charge radii measurements

# Laser spectroscopy with ISCOOL



Idea: A. Nieminen *et al.*, PRL 88 (2002)



← Ungated

← Gated (64 $\mu$ s - 70 $\mu$ s)

Background suppression

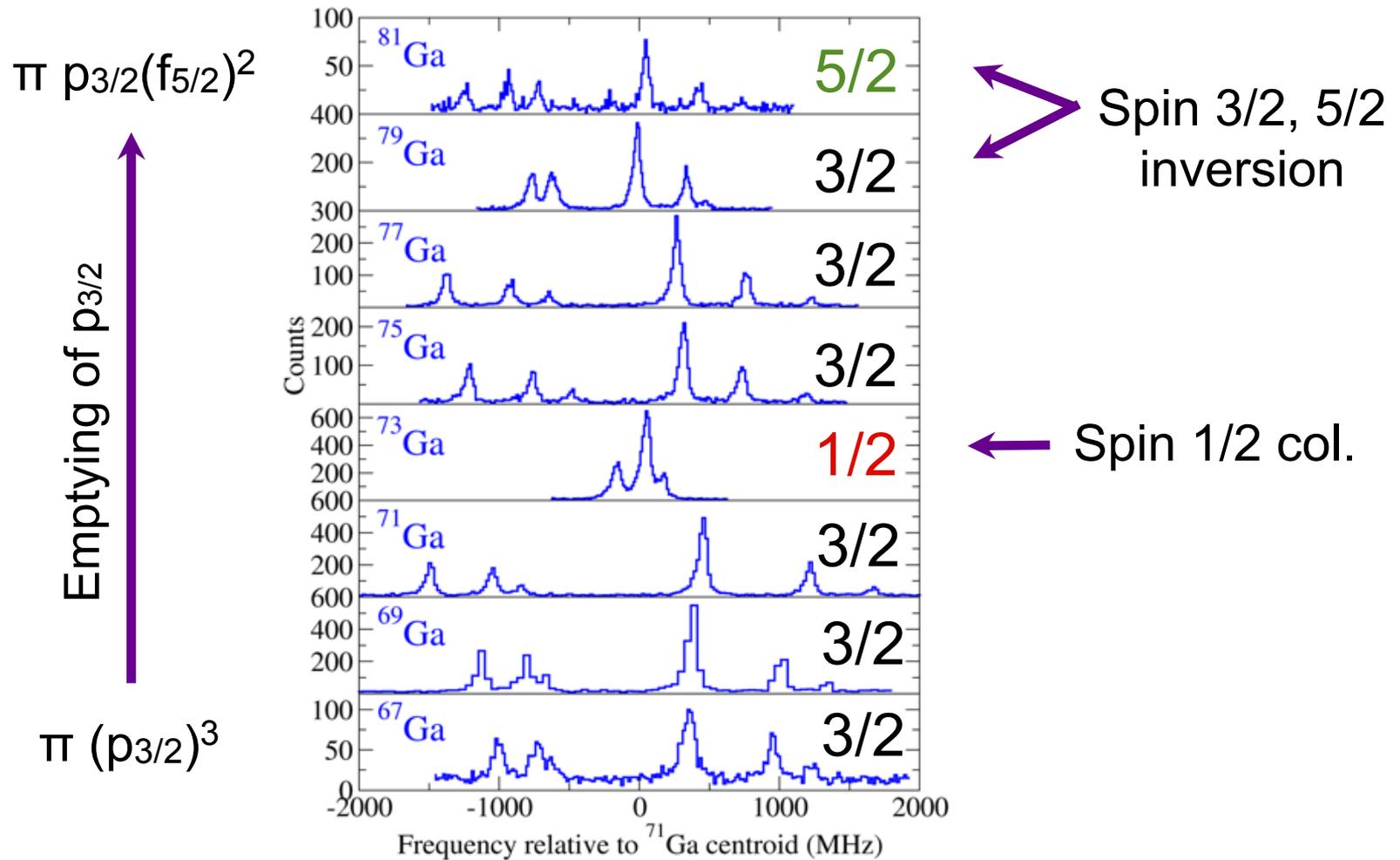
$$50\text{ms} / 6\mu\text{s} = \sim 10^4$$

COLLAPS (ISOLDE)

IGISOL (Jyväskylä)



# Isotope shifts in Cu and Ga



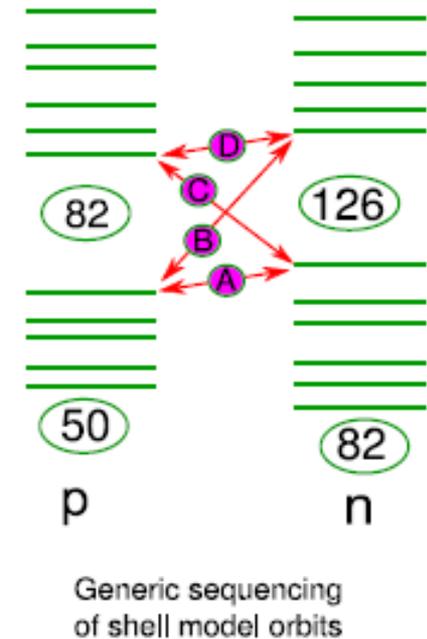
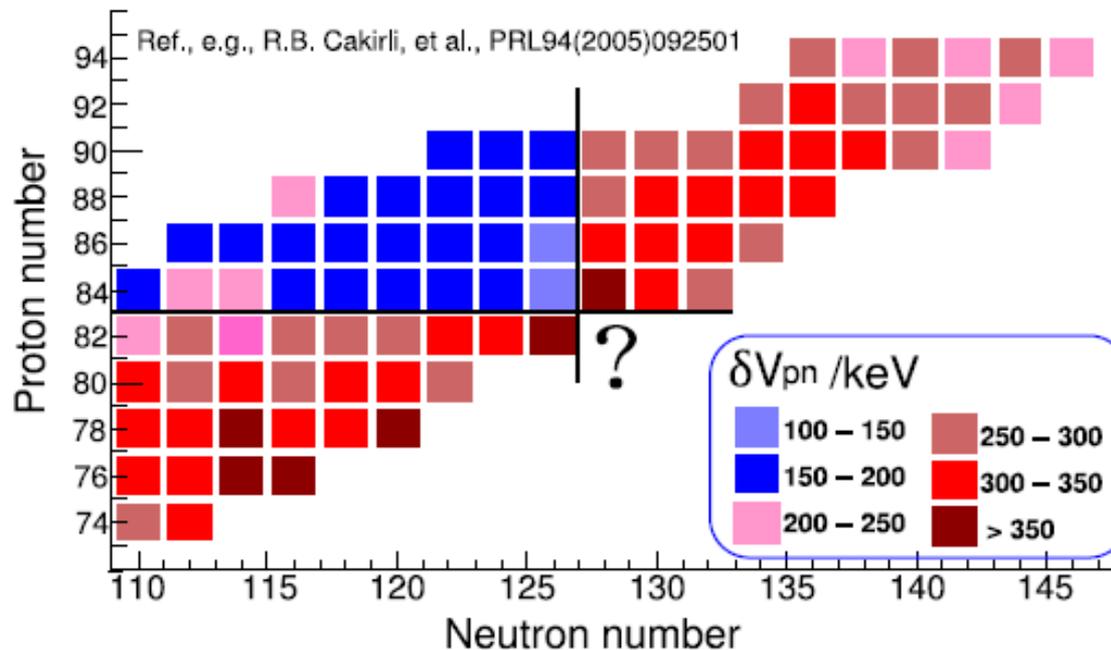
**Sudden nuclear structure changes between  $N=40$  and  $N=50$**

$^{71,73,75}\text{Cu}$ : Phys. Rev. Lett. 103, 142501 (2009);

$^{67-81}\text{Ga}$ : Phys. Rev. Lett. 104, 252502 (2010)



# Experimental proton-neutron interaction



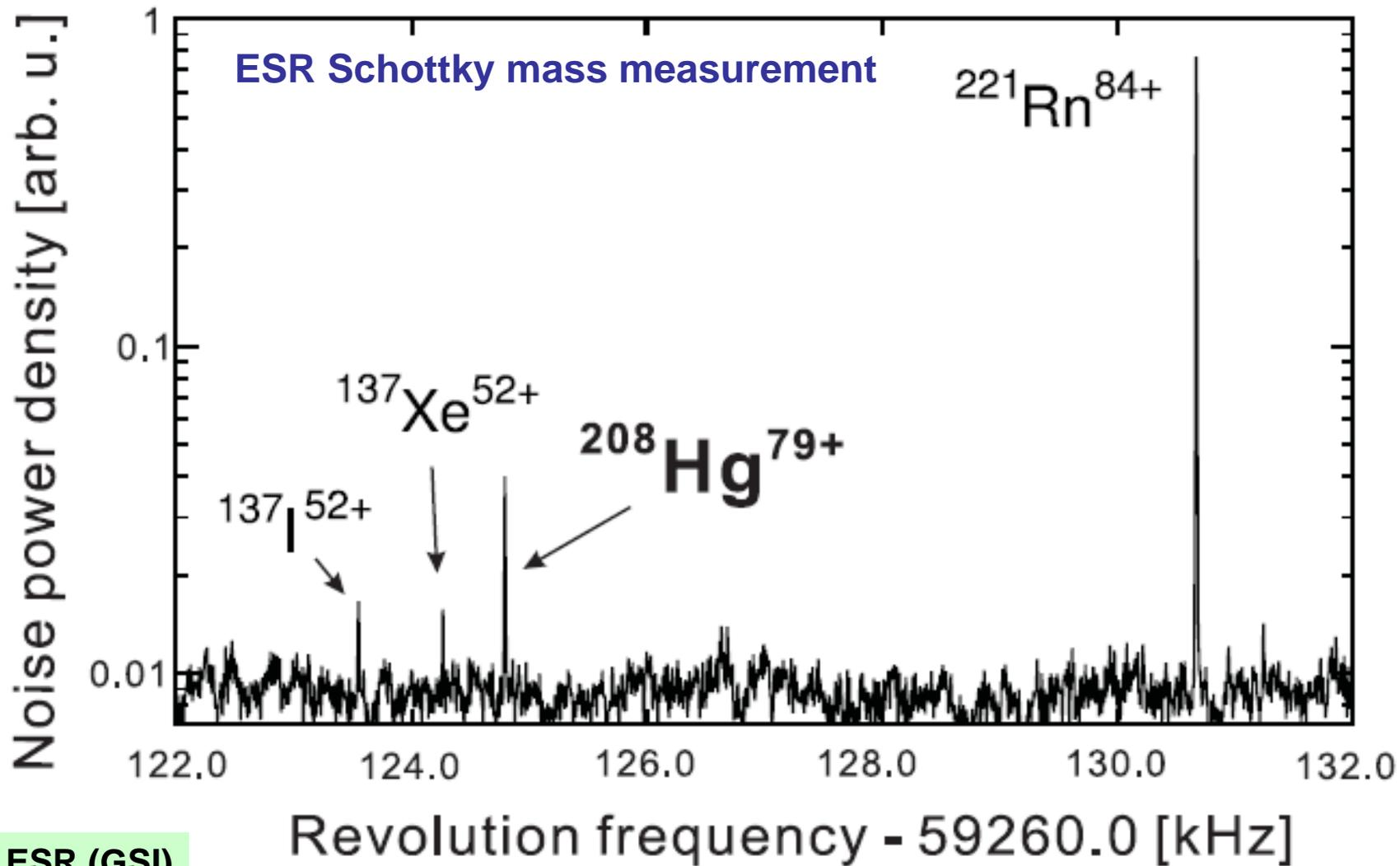
For even-even nuclei

$$\delta V_{pn}(Z, N) = \frac{1}{4} [\{B(Z, N) - B(Z, N-2)\} - \{B(Z-2, N) - B(Z-2, N-2)\}]$$

**p-n interactions are sensitive to the spatial overlaps of the proton and neutron wave functions**



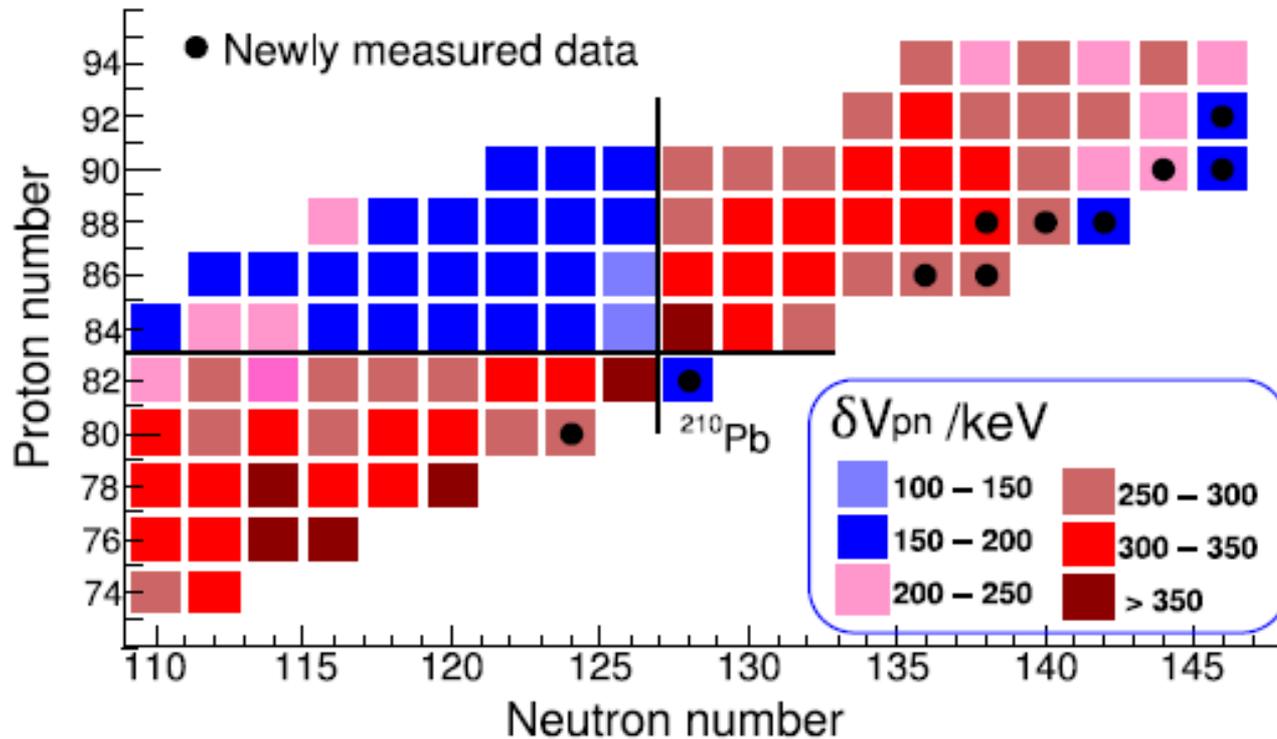
# Experimental proton-neutron interaction



ESR (GSI)



# Masses reveal the p-n interaction strength

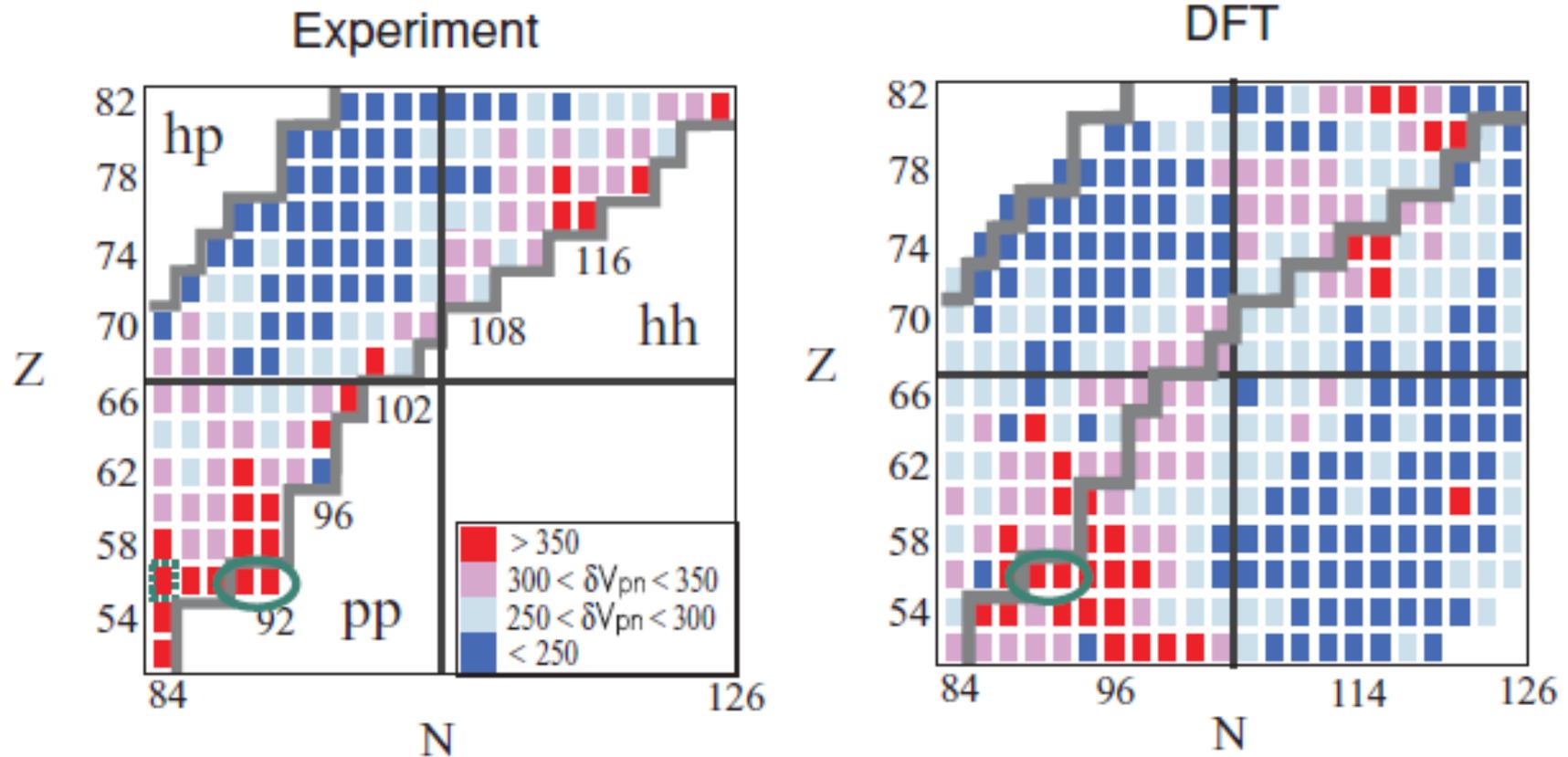


For even-even nuclei

$$\delta V_{pn}(Z, N) = \frac{1}{4} [\{B(Z, N) - B(Z, N-2)\} - \{B(Z-2, N) - B(Z-2, N-2)\}]$$



# Experiment – Theory (DFT)



Excellent agreement on a few 10 keV level!

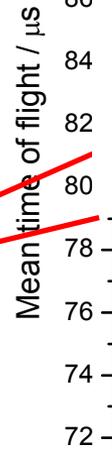
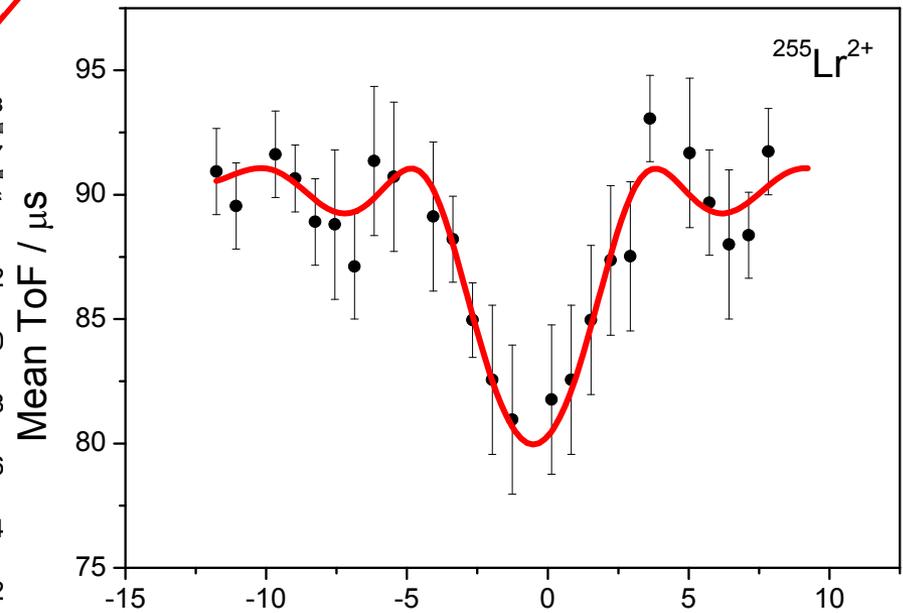
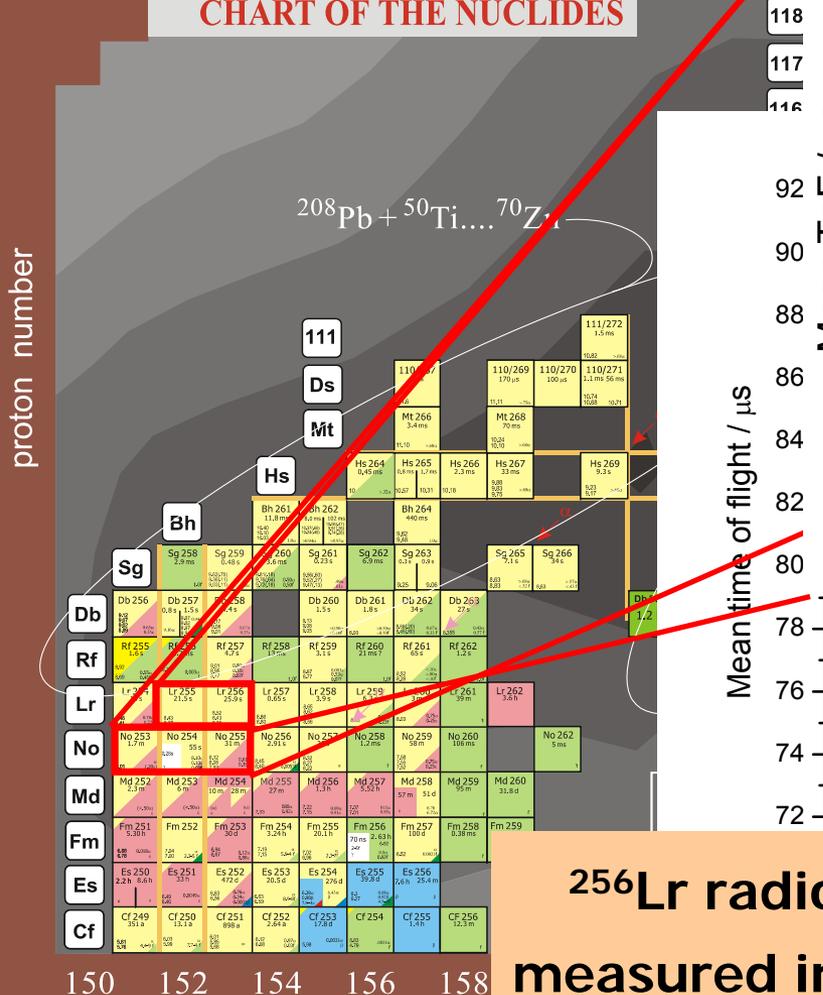
ISOLTRAP (ISOLDE)

D. Neidherr *et al.*, PRC 80, 044323 (2009)  
M. Stoitsov *et al.*, PRL 98, 132502 (2007)

# Direct mass measurements on No and Lr

M. Block et al., Nature 463, 785 (2010)  
 M. Dworschak et al., PRC 81, 064312 (2010)

## CHART OF THE NUCLIDES



$^{256}\text{Lr}$  radionuclide with lowest yield ever  
 measured in a Penning trap (2 ions/minute)



# Summary

***Atomic physics techniques are an ideal tool for the precise determination of nuclear ground state properties for nuclear structure studies!***

- Tools: lasers, Penning traps and storage rings
- Observables: charge radii, masses, moments, spins
- Nuclear structure:
  - Halos and skins
  - Magic numbers and shell evolution
  - Pairing, onset of deformation
  - Stability of superheavy elements

# Thanks

**Thanks a lot for the invitation  
and your attention!**

**Email:** [klaus.blaum@mpi-hd.mpg.de](mailto:klaus.blaum@mpi-hd.mpg.de)

**WWW:** [www.mpi-hd.mpg.de/blaum/](http://www.mpi-hd.mpg.de/blaum/)