

# Low temperature and timing properties of SIPMs

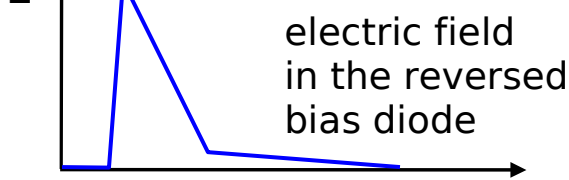
G.Collazuol  
INFN Padova

## Overview

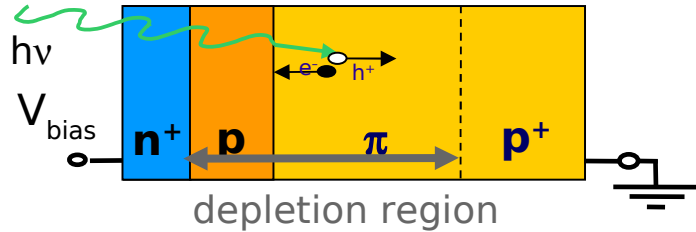
- Introduction
- Low T measurements & discussion
- Timing measurements & discussion
- Conclusions

# Introduction: building block of a SiPM → GM-APD

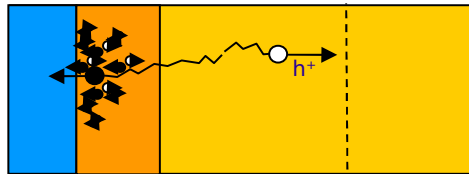
Diode reverse-biased above  $V_{breakdown}$



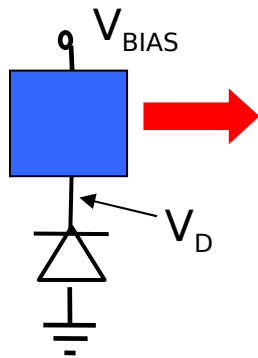
- $t=0$ : carrier initiates the avalanche



- $0 < t < t_1$ : avalanche spreading



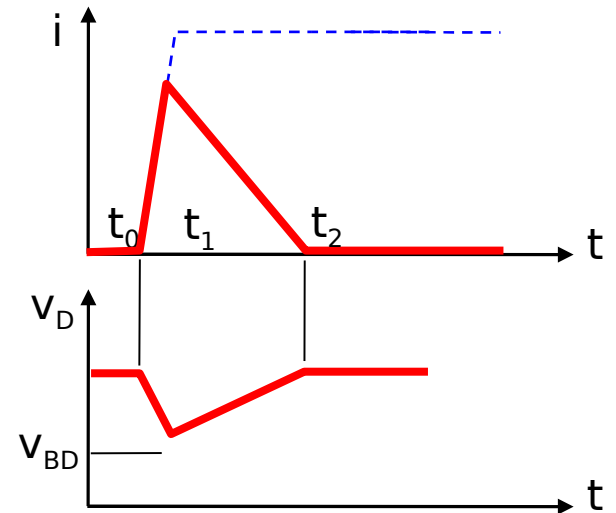
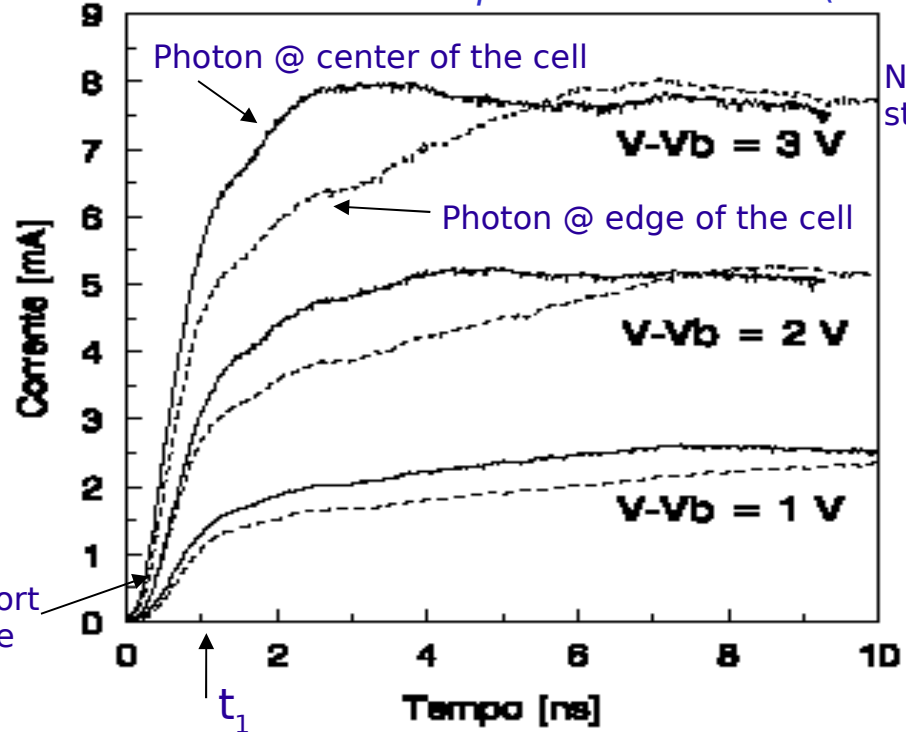
- $t_1 < t$ : self-sustaining current (limited by series R)



To detect another photon need a **quenching mechanism**. Two solutions:

- large resistance: **passive quenching**
- analog circuit: **active quenching**

*A. Spinelli Ph.D thesis (1996)*



# Operation principle of a GM-APD

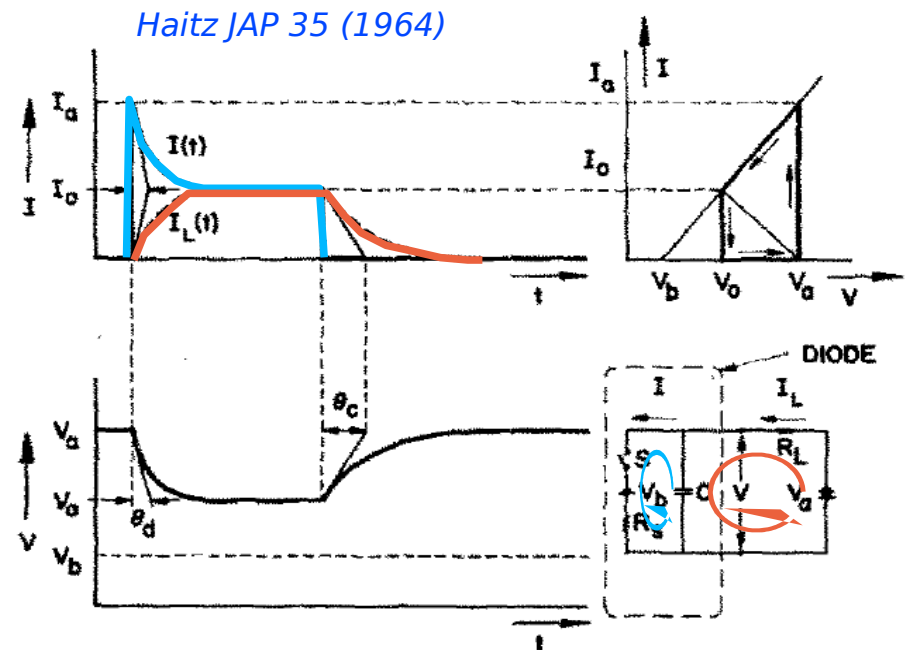
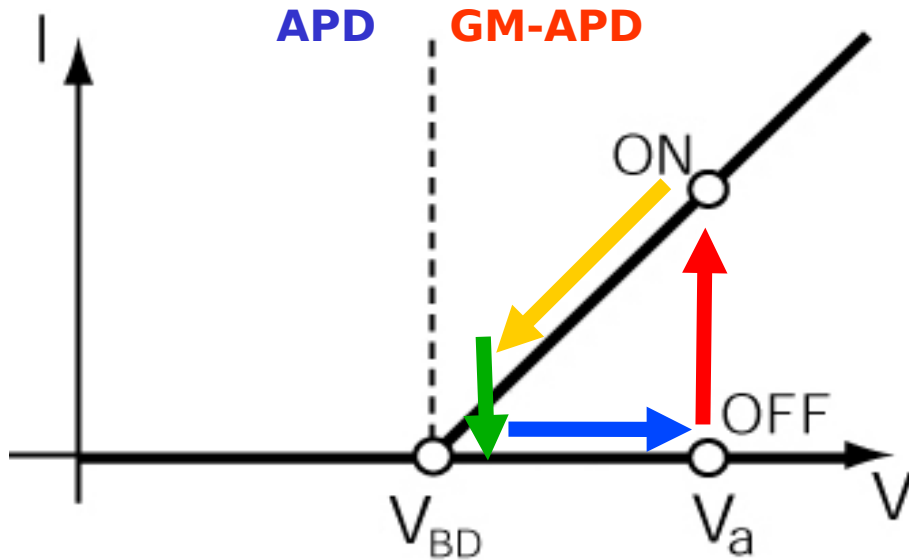


FIG. 3. Shape of current pulse for  $\theta_d \ll \tau_{r1}(I_0)$ .

**OFF condition:** avalanche quenched, switch open, capacitance charged until no current flowing from  $V_{BD}$  to  $V_{BIAS}$  with time constant  $R_q \times C_d = \tau_{Quenching}$  ( $\rightarrow$  recovery time)

$P_{01}$  = turn-on probability  
probability that a carrier traversing the high-field region triggers the avalanche

$P_{10}$  = turn-off probability  
probability that the number of carriers traversing the high-field region fluctuates to 0

**ON condition:** avalanche triggered, switch closed  $C_D$  discharges to  $V_{BD}$  with a time constant  $R_S \times C_D = \tau_{discharge}$ , at the same time the external current asymptotic grows to  $(V_{BIAS} - V_{bd}) / (R_q + R_s)$

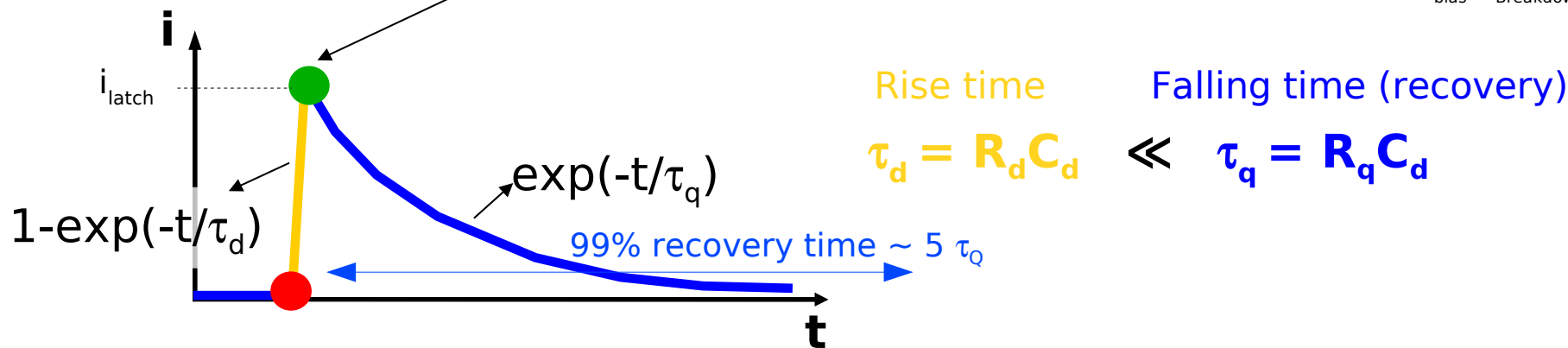
# Signal shape, Gain and Recovery time

Fast Capacitor (cell) discharge and slow recharge (roughly speaking)

If  $R_q$  is high enough the internal current decreases at a level such that statistical fluctuations quench the avalanche: need  $i_{latch} \sim \Delta V / (R_q + R_d) \sim 10 \mu A$

With usual  $R_q$  values turn-off time is very short  $O(1ns)$

"Overvoltage"  
 $\Delta V \equiv (V_{bias} - V_{Breakdown})$



Recovery time:

increases at low  $T$  due to polysilicon  $R_q$  while  $C_d$  is independent of  $T$

also rise time expected to be  $T$  dependent (silicon  $R_d$  vs  $T$ )

Gain  $\sim C_d \Delta V \rightarrow$  independent of  $T$

at fixed Over-Voltage ( $\Delta V$ )



# SiPM equivalent circuit (detailed model)

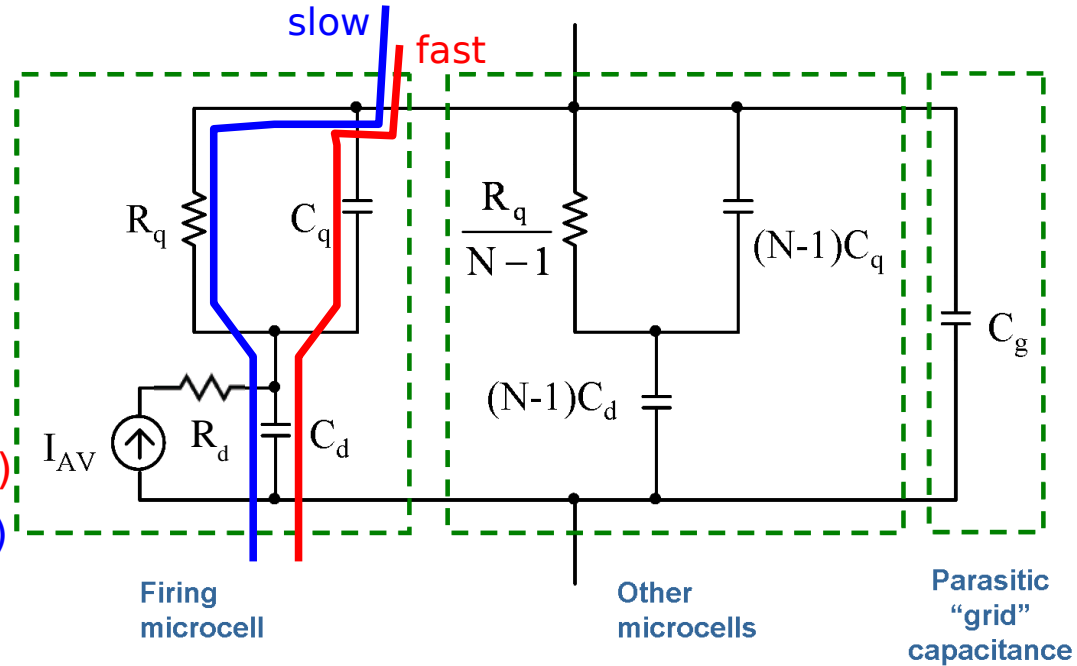
Single cell model  $\rightarrow (R_d || C_d) + (R_q || C_q)$

SiPM + load  $\rightarrow (||Z_{cell}) || C_{grid} + Z_{load}$

Signal = **slow** pulse ( $\tau_{d (rise)}, \tau_{q-slow (fall)}$ ) +  
+ **fast** pulse ( $\tau_{d (rise)}, \tau_{q-fast (fall)}$ )

- $\tau_{d (rise)} \sim R_d (C_q + C_d)$
- $\tau_{q-fast (fall)} = R_{load} C_{tot}$  (fast; parasitic spike)
- $\tau_{q-slow (fall)} = R_q (C_q + C_d)$  (slow; cell recovery)

*F.Corsi, et al. NIM A572 (2007)*



$\rightarrow$  Rise time degraded by parasitic inductance

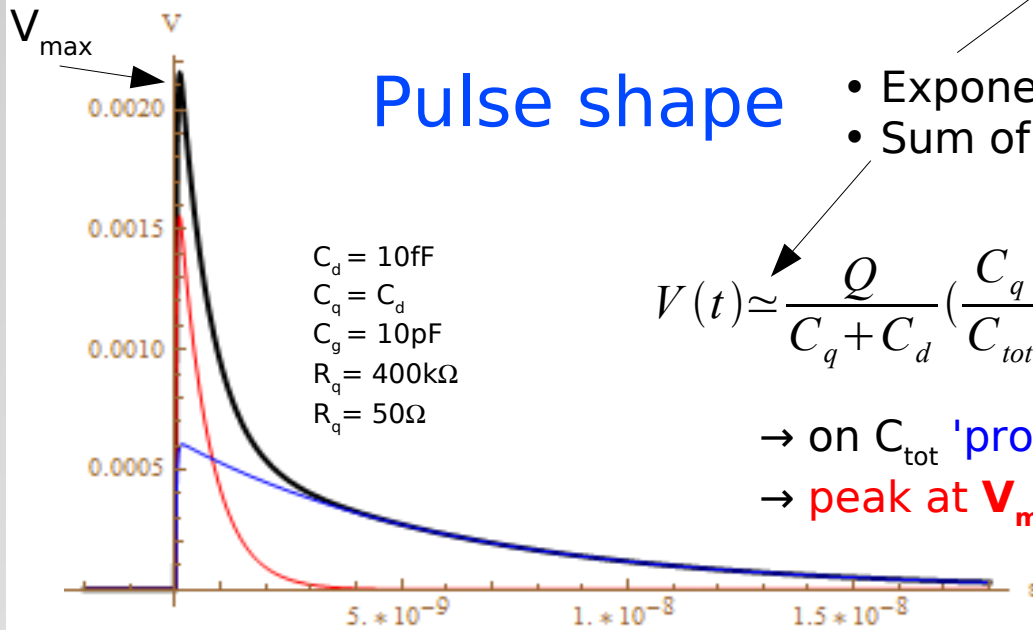
## Pulse shape

- Exponential rise
- Sum of two exponential fall

$$V(t) \simeq \frac{Q}{C_q + C_d} \left( \frac{C_q}{C_{tot}} e^{\frac{-t}{\tau_{FAST}}} + \frac{R_{load}}{R_q} \frac{C_d}{C_q + C_d} e^{\frac{-t}{\tau_{SLOW}}} \right)$$

$\rightarrow$  on  $C_{tot}$  'prompt' charge  $Q_{fast} = Q \frac{C_q}{(C_q + C_d)}$

$\rightarrow$  peak at  $V_{max} \sim Q_{fast} / C_{tot}$  is independent of  $R_{load}$



# Pulse shape: dependence on Temperature

Single cell model  $\rightarrow (R_d || C_d) + (R_q || C_q)$

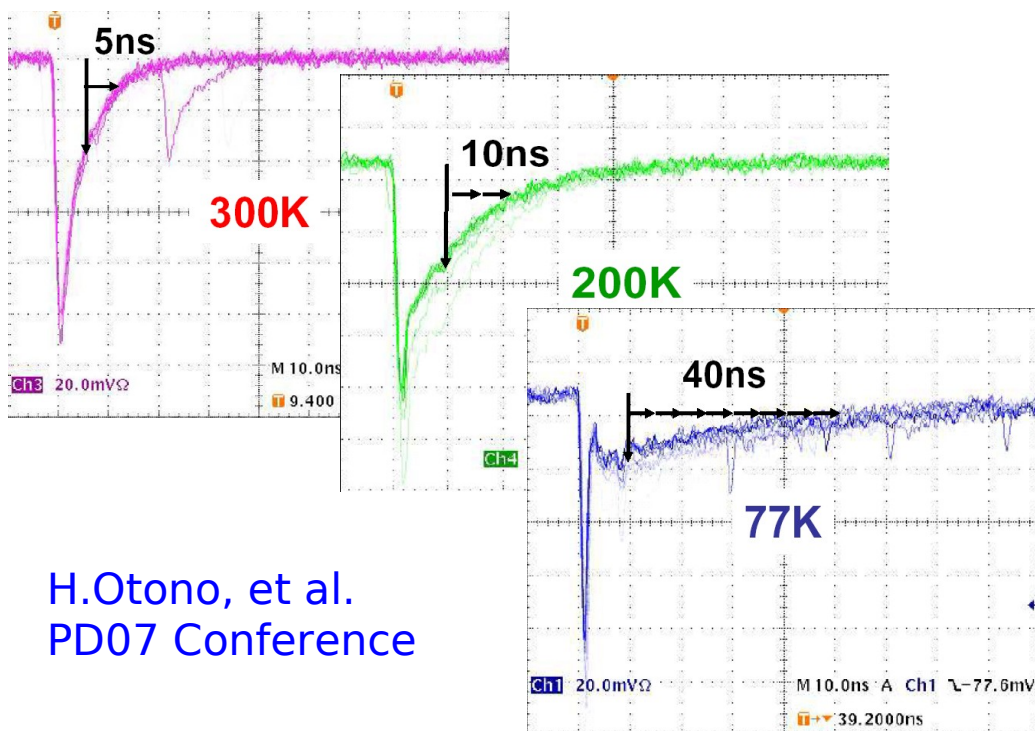
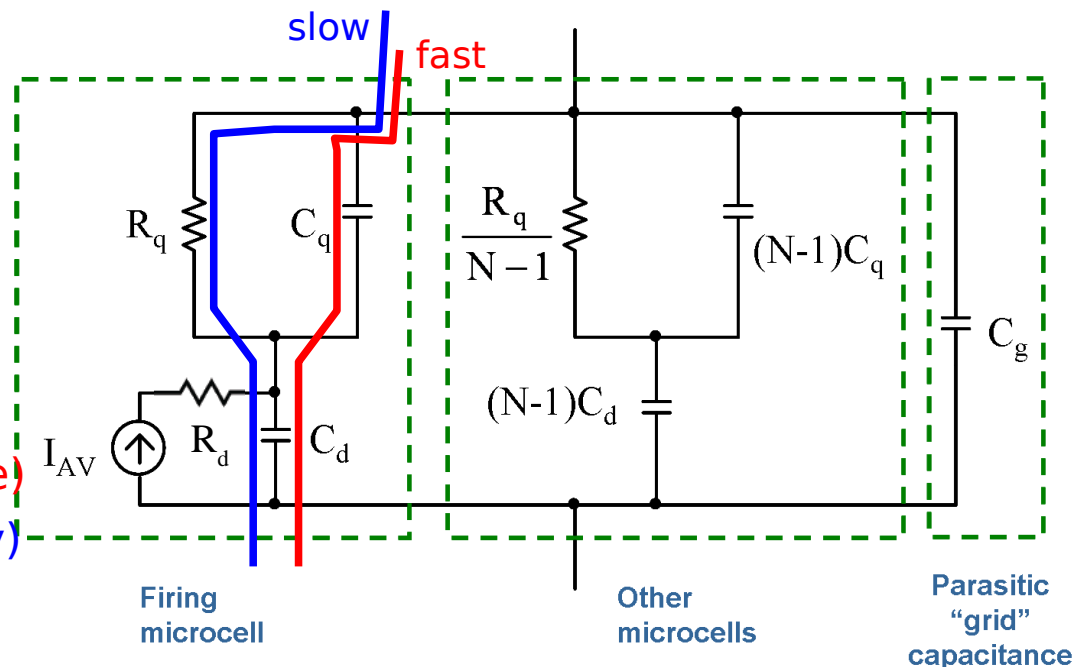
SiPM + load  $\rightarrow (||Z_{cell}) || C_{grid} + Z_{load}$

Signal = **slow** pulse ( $\tau_{d \text{ (rise)}}, \tau_{q \text{-slow (fall)}}$ ) +  
 + **fast** pulse ( $\tau_{d \text{ (rise)}}, \tau_{q \text{-fast (fall)}}$ )

- $\tau_{d \text{ (rise)}} \sim R_d (C_q + C_d)$

- $\tau_{q \text{-fast (fall)}} = R_{load} C_{tot}$  (fast; parasitic spike)

- $\tau_{q \text{-slow (fall)}} = R_q (C_q + C_d)$  (slow; cell recovery)



H.Otono, et al.  
 PD07 Conference

## Pulse shape:

The two current components show different behavior with Temperature

$\rightarrow$  fast component is independent of T because stray  $C_q$  couple with external  $R_{load}$  (no dependence on T) while  $R_q$  is strongly dependent on T

$\leftarrow$  (we used low light level, BW filters against noise and AC coupling  $\rightarrow$  difficult to disentangle the two components)

# Overview - SiPM properties at low T

Complete characterization of FBK SiPM in the temperature range  $50\text{K} < T < 320\text{K}$

- 1) junction characteristics: forward and reverse (breakdown)
- 2) gain, dark current, after-pulses, cross-talk
- 3) photon detection efficiency (PDE)

*G.C. et al NIM A628 (2011) 389*

→ Improved SiPM performances at low temperature (w/ respect to T room):

- 1) lower dark noise by several orders of magnitude
- 2) after-pulsing probability constant down to  $\sim 100\text{K}$  (then blow up)
- 3) PDE variations up to  $\pm 50\%$  (depending on  $\lambda$ ) down to  $\sim 100\text{K}$
- 4) better timing resolution
- 5) better  $V_{\text{breakdown}}$  stability against variations of T

→ SiPM is an excellent alternative to PMT at low T

...even more than at room temperature !!!



**Vacuum vessel ( $P < 10^{-3}$  mbar)**

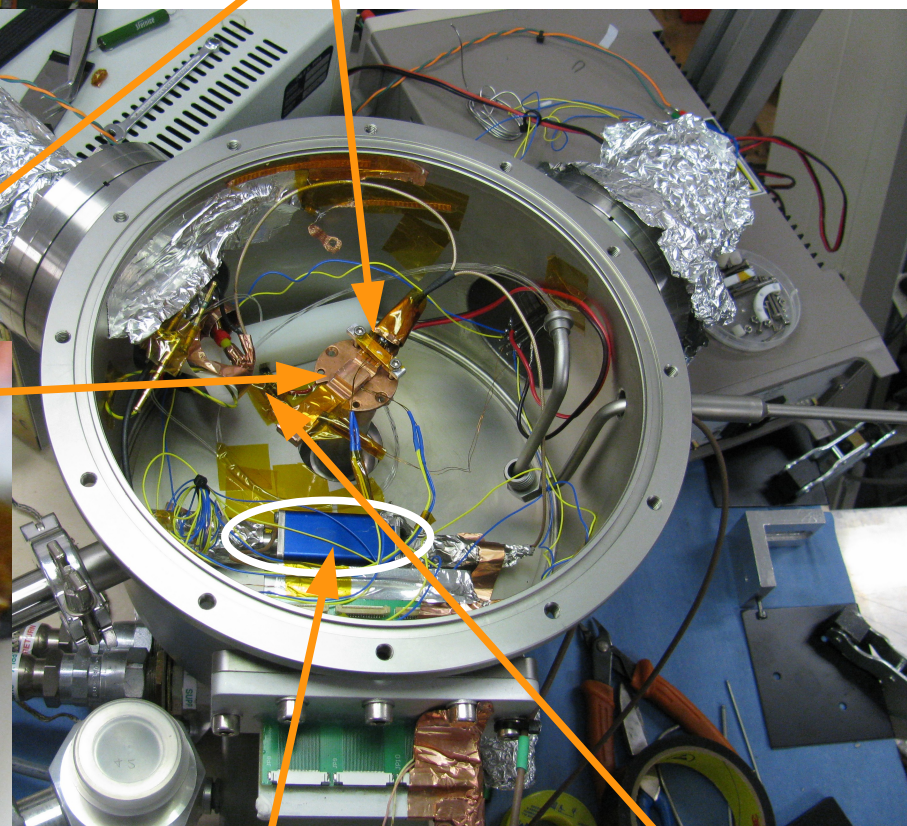
# Experimental Setup



**Halogen Lamp / Pulsed Laser**

**Monochromator (200-900nm) and neutral filters**

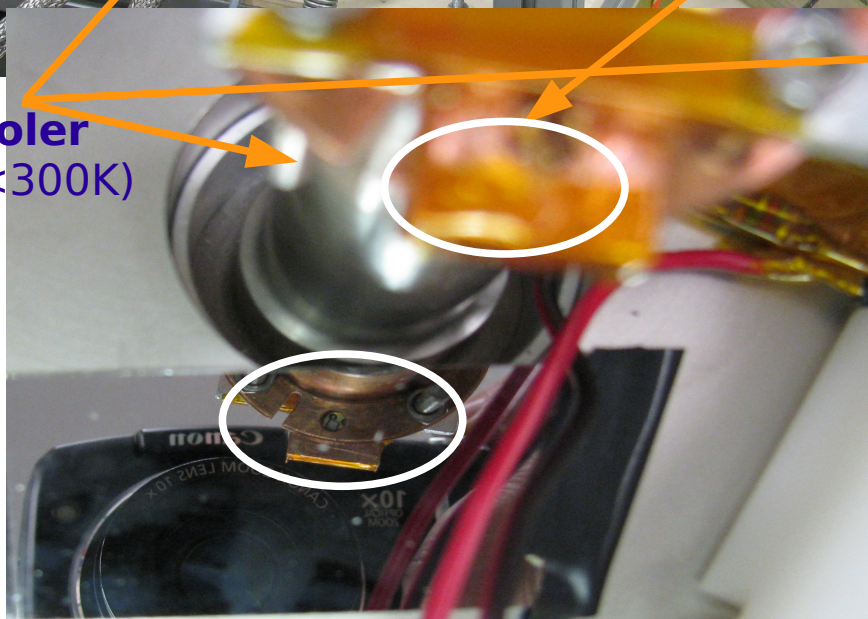
**Quartz fibers to Calibrated Photodiode (outside) and to SiPM (inside vessel)**



**Amplifier**

**UV LED (380nm) + fibers to SiPM**

**Cryo-cooler ( $50K < T < 300K$ )**





# Experimental setup

## Temperature control/measurement

- Close cycle, two stages, He cryo-cooler and heating with low R resistor
- Vacuum with  $P < 10^{-3}$  mbar
- thermal contact (critical) with cryo-cooler head: SiPM within a copper rod + kapton (electrical insulation)
- T measurement with 3 pt100 probes
- Measurements on SiPM carried after thermalization, ie all probes at the same T
- check junction T with forward characteristic

## Light sources

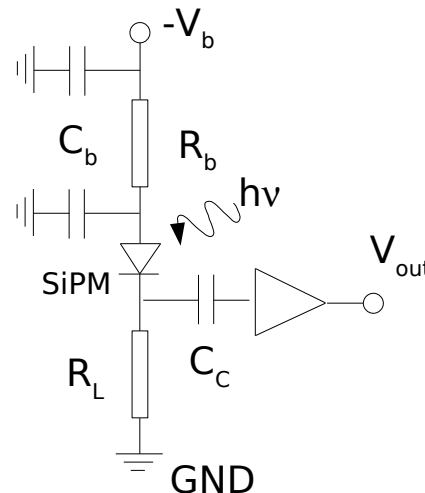
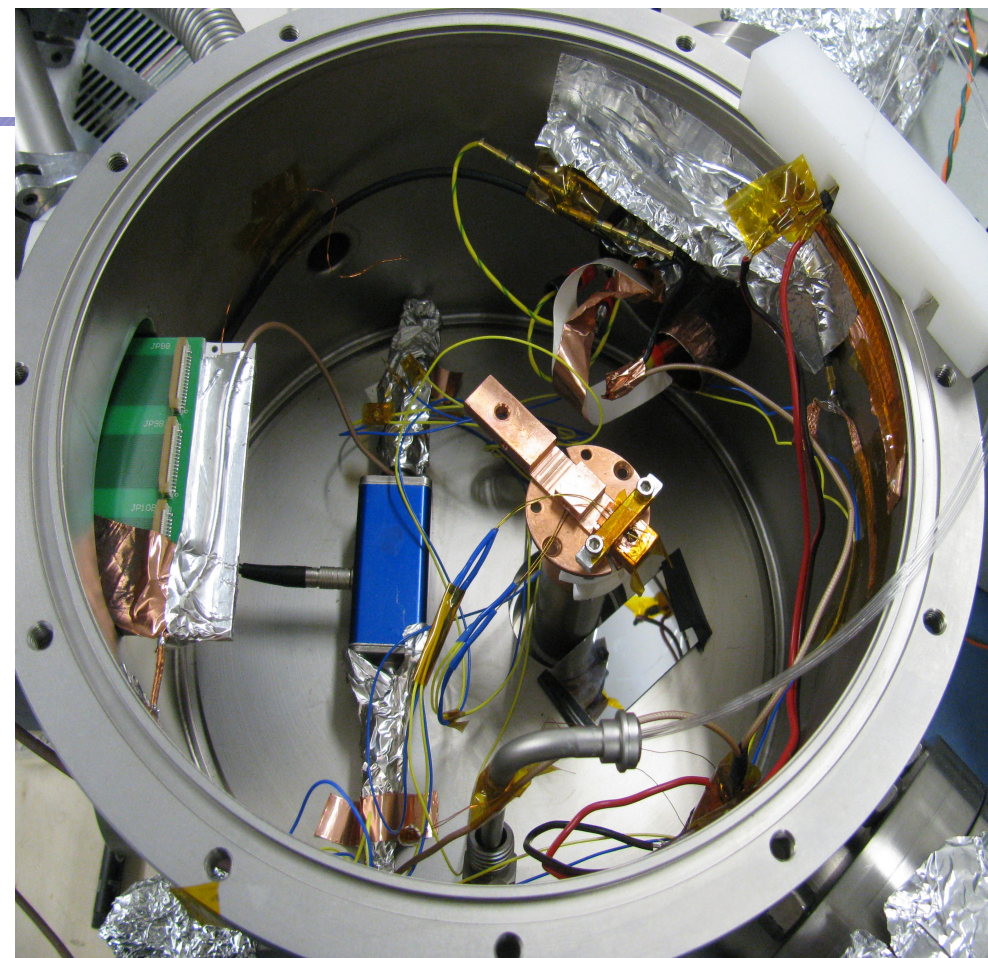
- CW: halogen lamp and UV LED ( $\lambda \sim 380\text{nm}$ )
- Pulsed: laser (30ps rms,  $\lambda \sim 405\text{nm}$ )

## $V_{\text{bias}}$ and current measurements

- Keytley 2148  
Voltage/Current source/meter

## Pulse/Waveform sampling

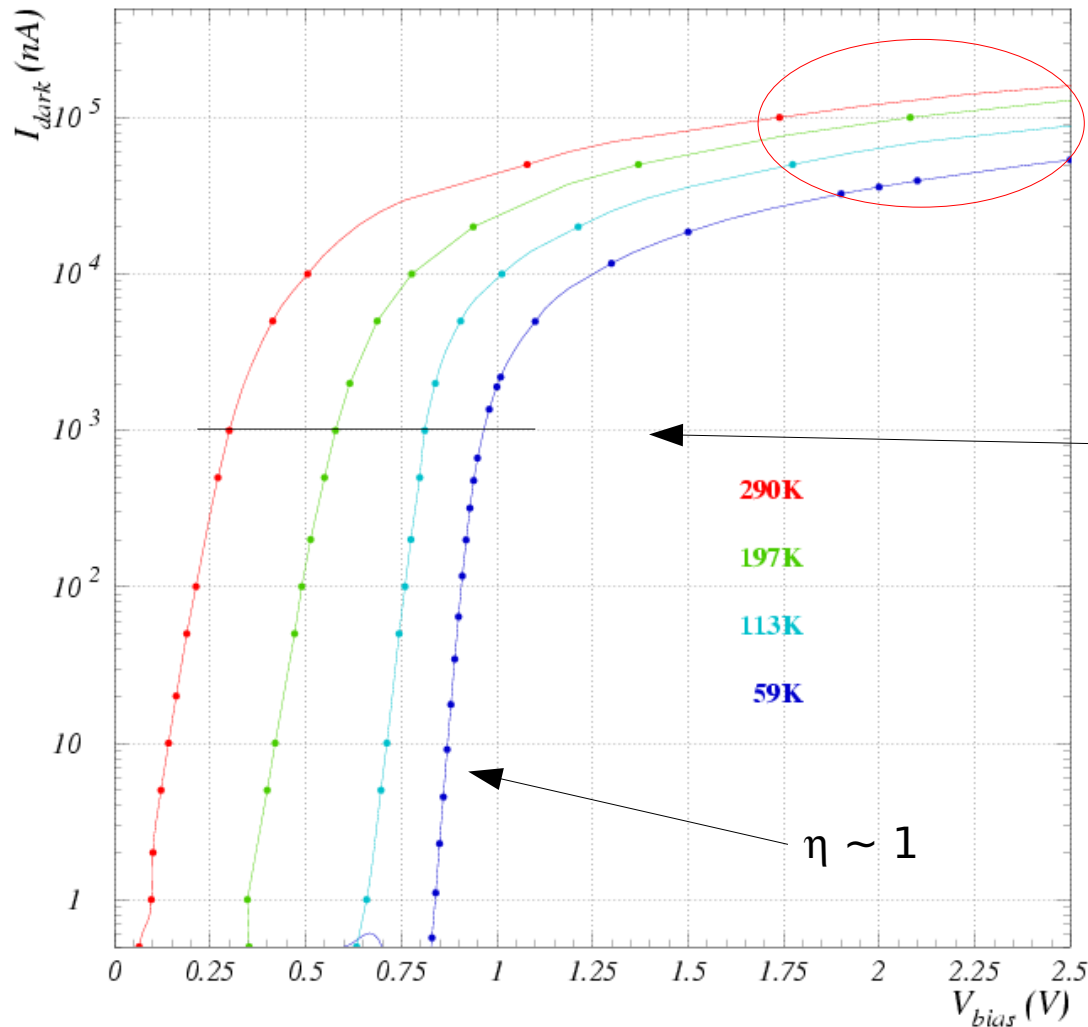
- Care against HF noise  
→ feedthroughs !!!
- Amplifier Photonique/CPTA  
(gain  $\sim 30$ , BW  $\sim 300\text{MHz}$ )
- Lecroy o.scope, 1GHz, 20GS/s



## SiPM samples

- FBK SiPM (2008) -  $1\text{mm}^2$   
( $V_{\text{br}} \sim 33\text{V}$ , fill factor  $\sim 20\%$ )
- n-on-p shallow junction
  - $4\mu\text{m}$  fully depleted region (active volume)
  - no protective epoxy (epoxy cracks avoided)

# I-V measurements: forward bias



③ **Ohmic** behavior at high current

Linear fit  $\rightarrow R_{\text{series}} \sim R_q / N_{\text{cells}}$

② **Voltage drop** ( $V_d$ ) decreases linearly with  $T$  decreasing (e.g. at  $1\mu\text{A}$ )

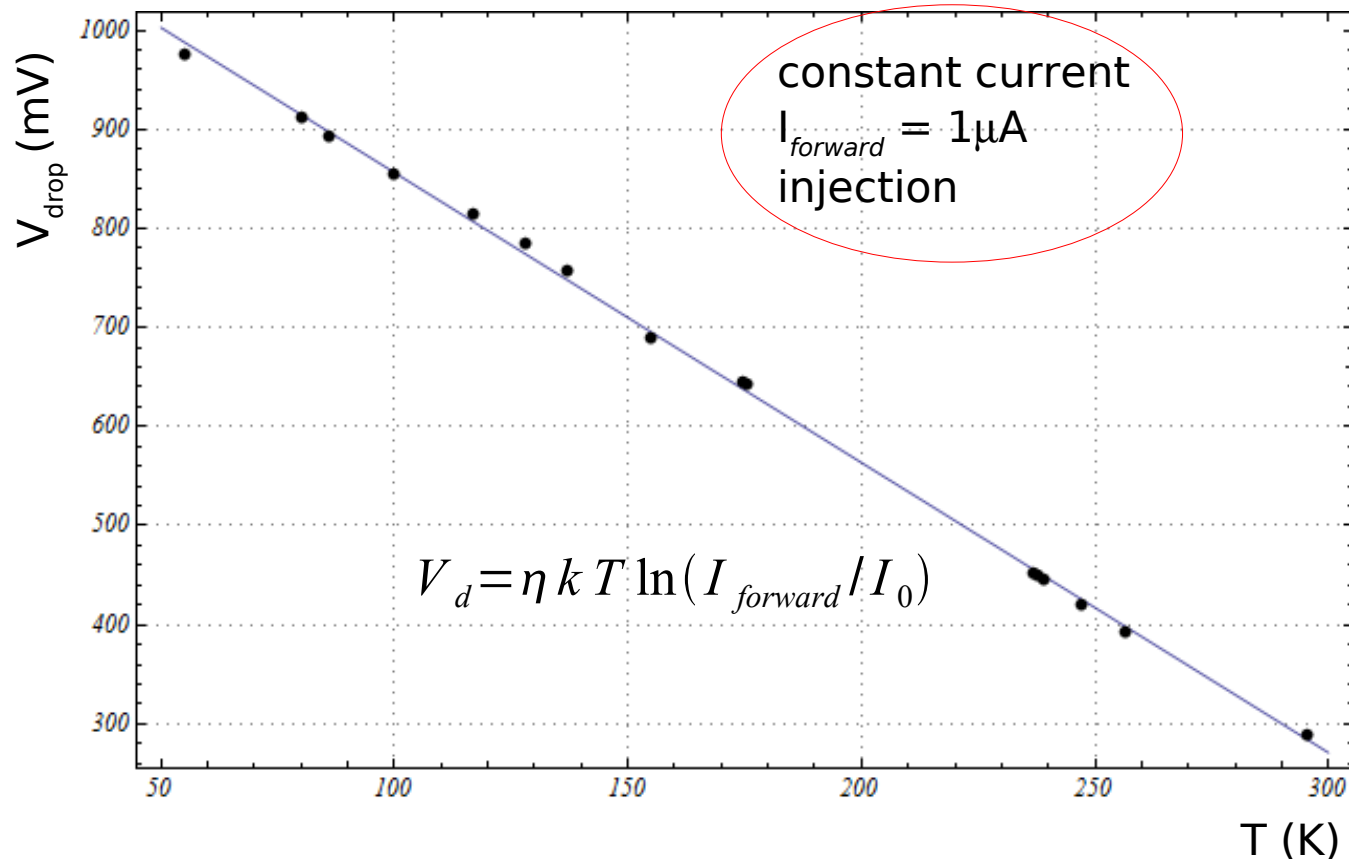
① **Forward current**  $J_F \sim \exp\left(V_d \frac{q}{\eta k T}\right)$

Diffusion dominating:  $\eta \rightarrow 1$

Recombination dominating:  $\eta \rightarrow 2$

# I-V measurements: forward bias

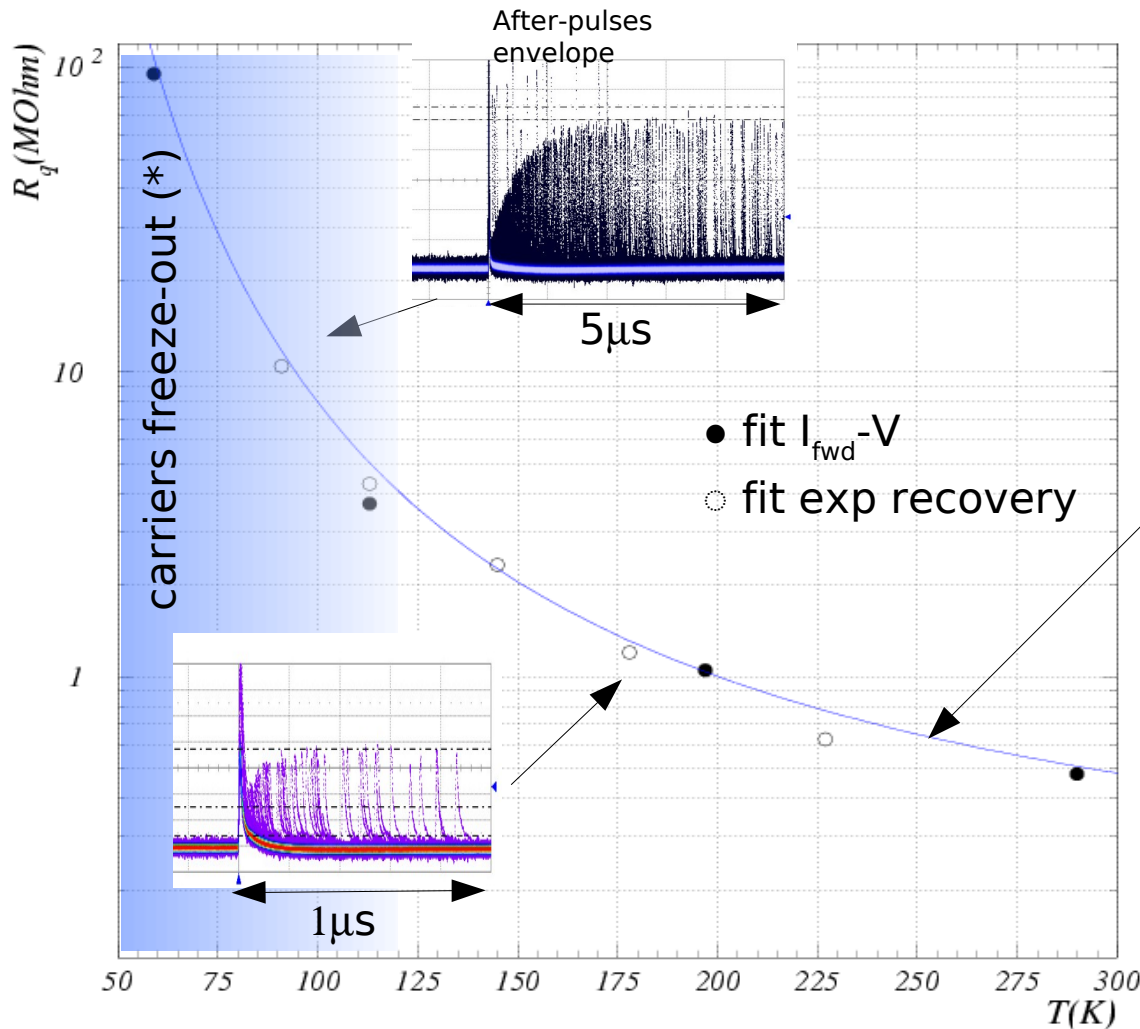
Voltage drop at fixed forward current → precise **measurement of junction T...**  
... otherwise not trivially measured !



- linear dependence with slope  $dV_{\text{drop}}/dT|_{1\mu\text{A}} \sim 3\text{mV/K}$
- precise **calibration**/probe of junction Temperature

# Series Resistance vs T

- 1) Fit at high V of forward characteristic → **measurement of series resistance  $R_s$**
- 2) Exponential recovery time (afterpulses envelope) → **measurement of  $R_s$**

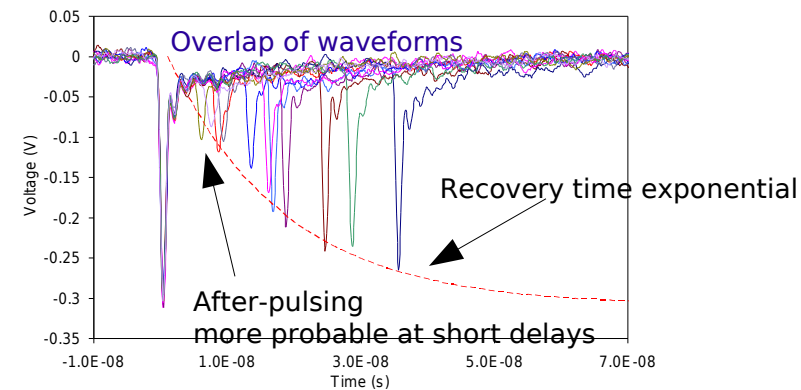


Measurements (1) and (2) consistent → **dominant effect from quenching resistor  $R_q$**   
 (→ R bulk gives smaller effect)

Empirical fit:

$$R_q(T) \sim 0.13 (1 + 300/T e^{300/T}) M \Omega$$

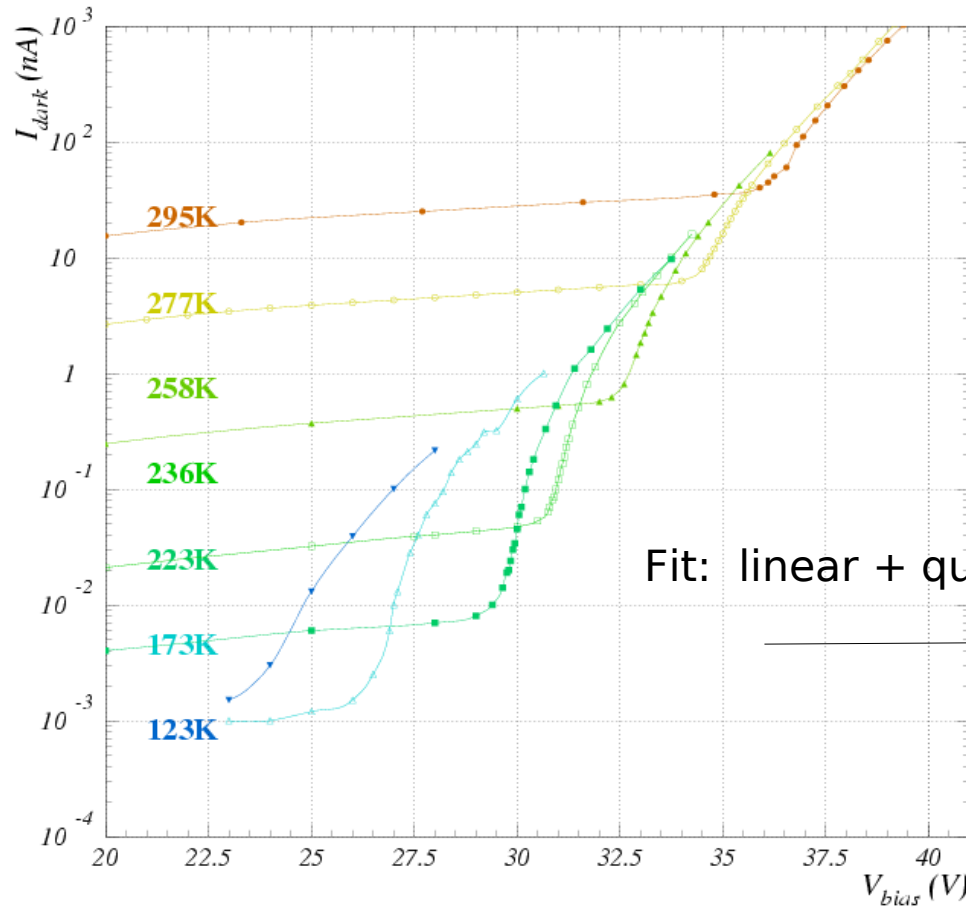
Afterpulses envelope



(\*) carrier losses at very low T due to ionized impurities acting as shallow traps

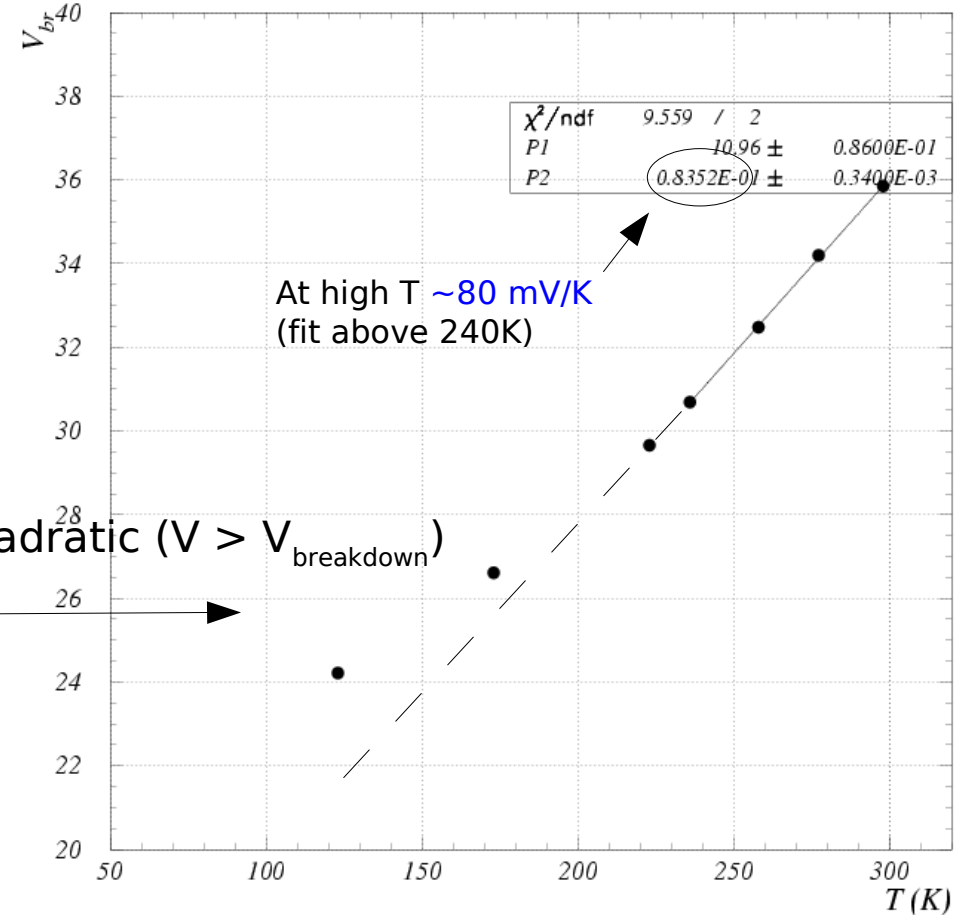


# I-V measurements: reverse bias



Fit: linear + quadratic ( $V > V_{breakdown}$ )

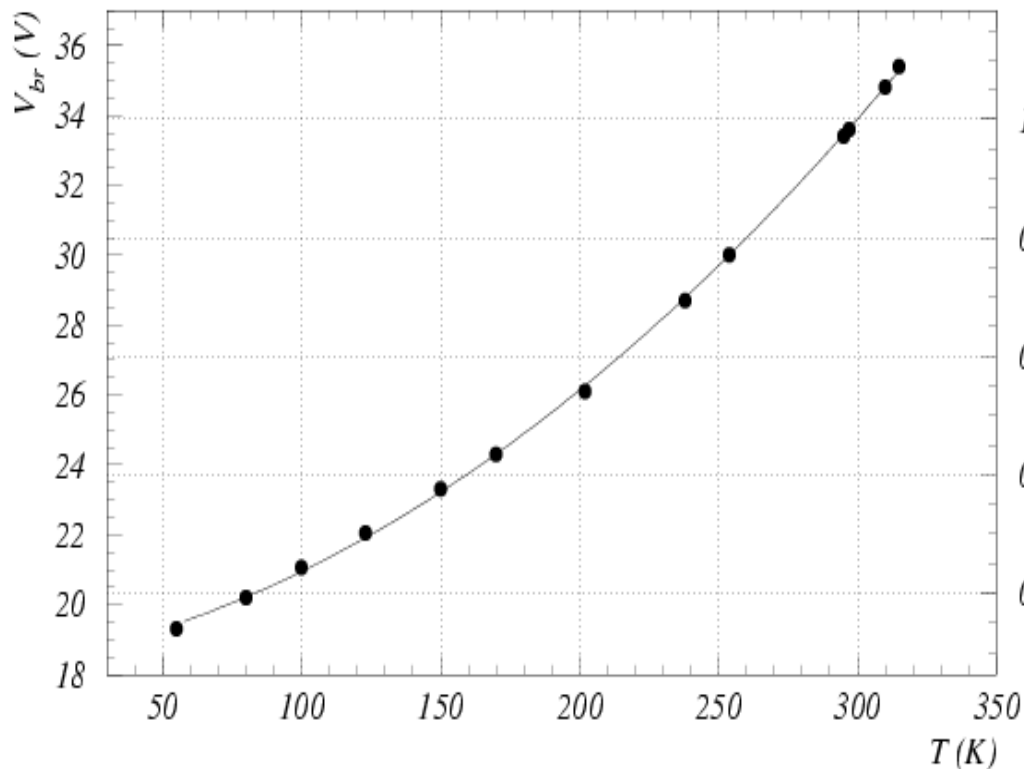
## $V_{breakdown}$ vs T



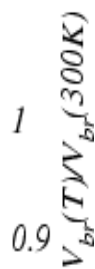
Avalanche breakdown voltage decreases due to larger carriers mobility at low T  $\rightarrow$  larger ionization rate (at constant electric E field)

# V breakdown vs T

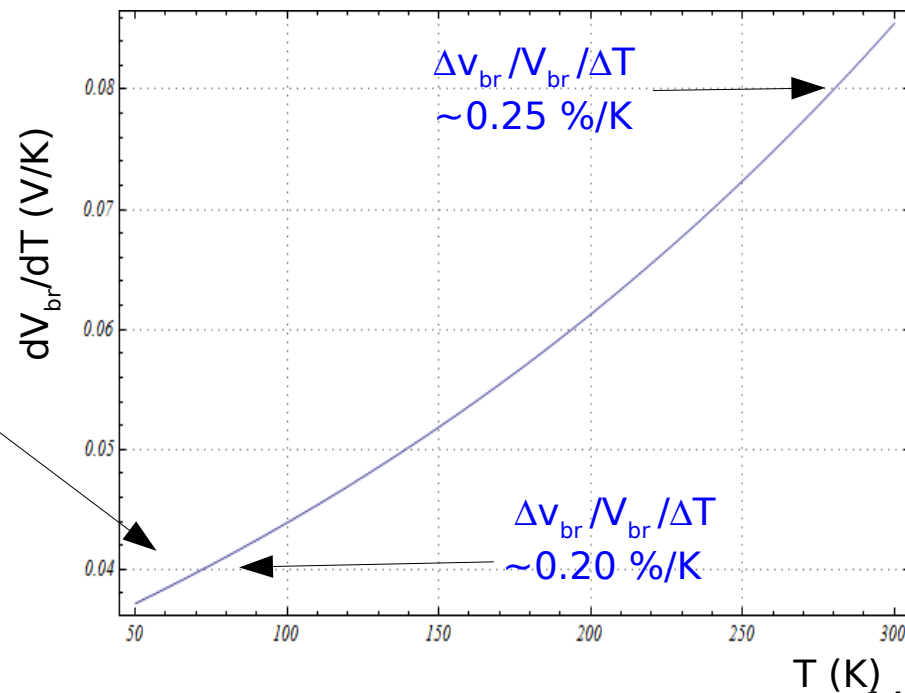
Breakdown Voltage



Consistent with Breakdown simulations for abrupt junctions with p-region doping at a level of  $\sim 10^{17} \text{ cm}^{-3}$



Temperature coefficient

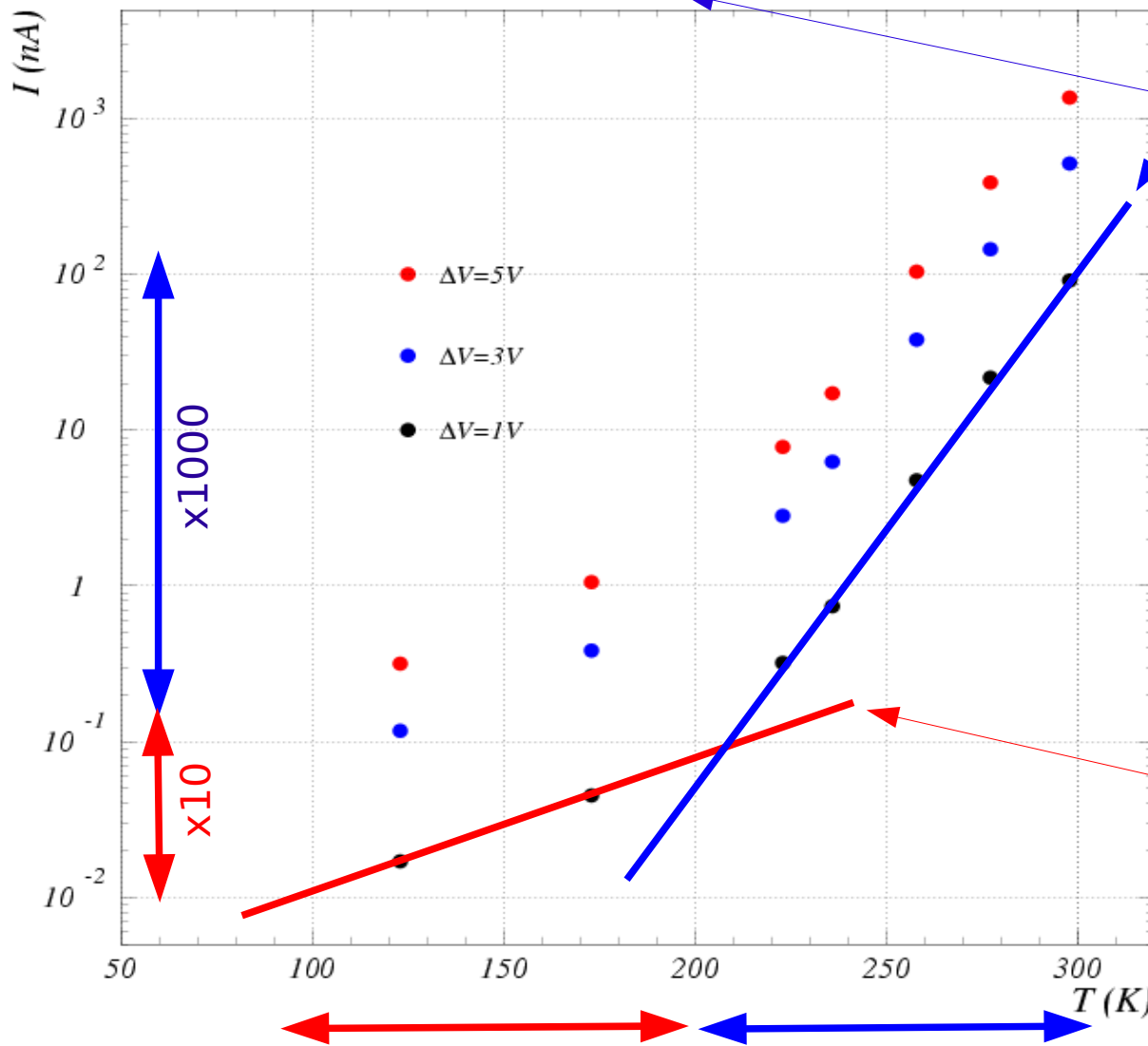


better stability at low T

# Dark current vs T (constant $\Delta V$ )

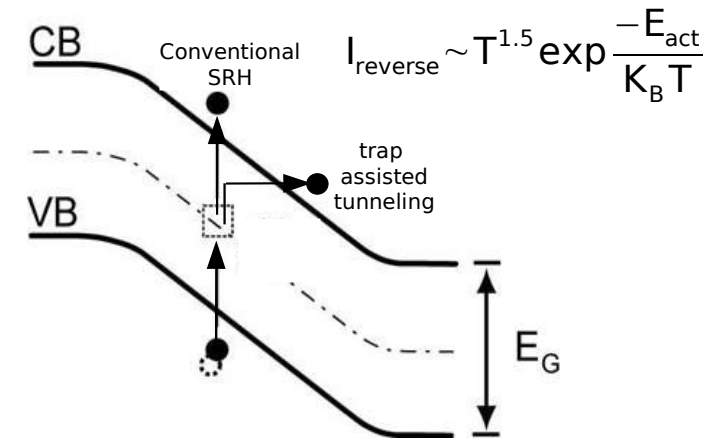
Thermal noise mainly due to G-R in the High E Field region

## Main noise mechanisms

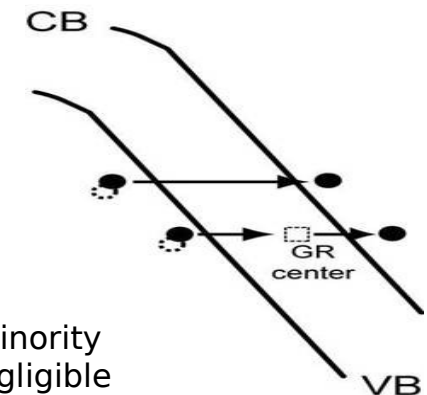


Tunnel noise dominating for  $T < 200\text{K}$  (FBK devices)

1) Generation/Recombination SRH noise (enhanced by trap assisted tunneling)

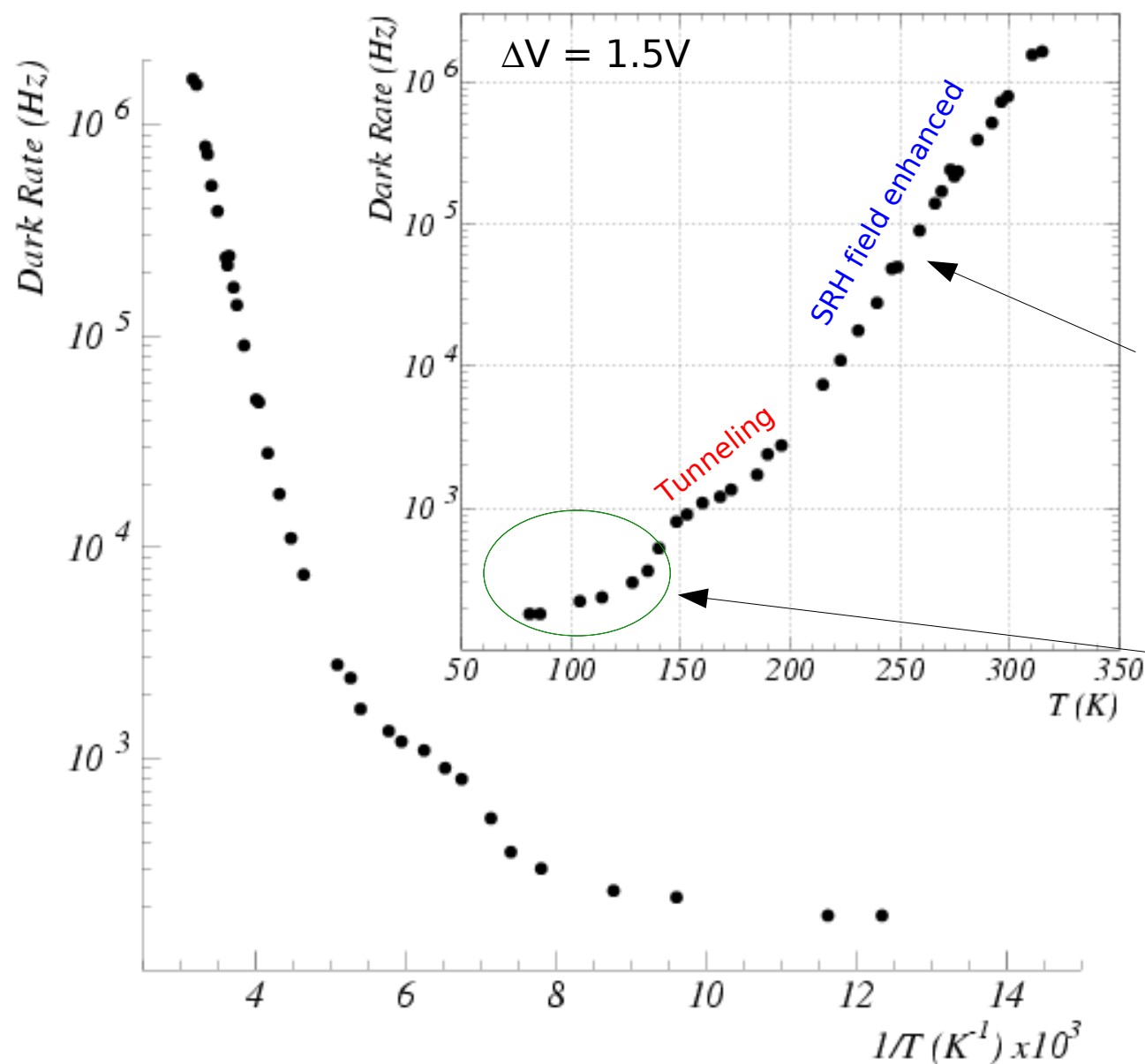


2) Band-to-band Tunneling noise (strong dependence on the Electric field profile)



(\*) noise due to minority carriers diffusion: negligible

# Dark count rate vs T (constant $\Delta V$ )



Measurement of **counting rate of  $\geq 1$ p.e.** at fixed  $\Delta V=1.5V$  ( $\rightarrow$  constant gain)

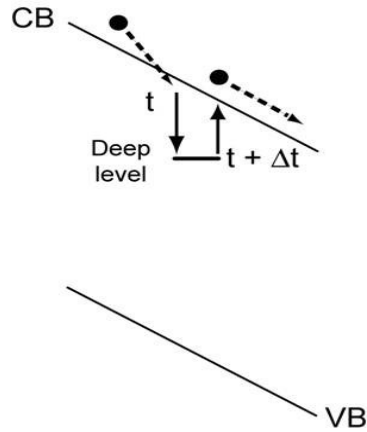
$$DCR \sim T^{1.5} \exp \frac{-E_{act}}{K_B T}$$

Activation energy  $E_{act} \sim 0.36eV$

Additional structure ???  
Under investigation

# After-Pulsing (AP)

## Carrier trapping and delayed release



$$P_{\text{afterpulsing}}(t) = P_c \cdot \frac{\exp(-t/\tau)}{\tau} \cdot P_{\text{trigg}} \propto \Delta V^2 \quad \sim \text{Few \% level at 300K}$$

avalanche triggering probability  $\propto \Delta V(t)$

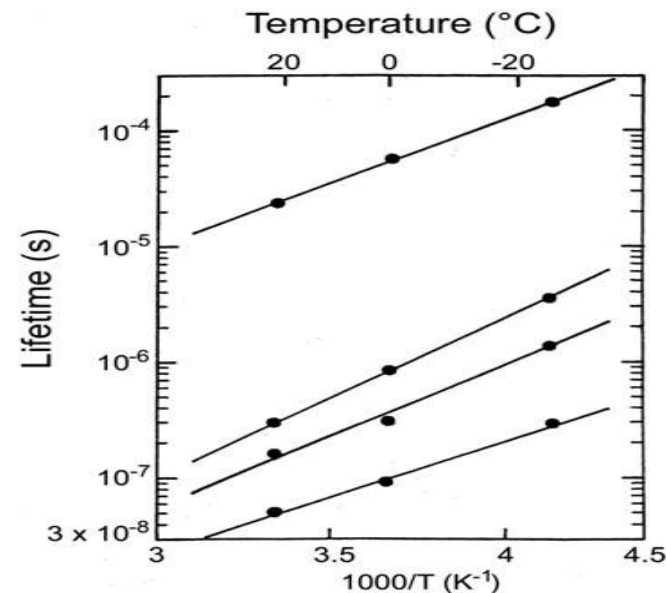
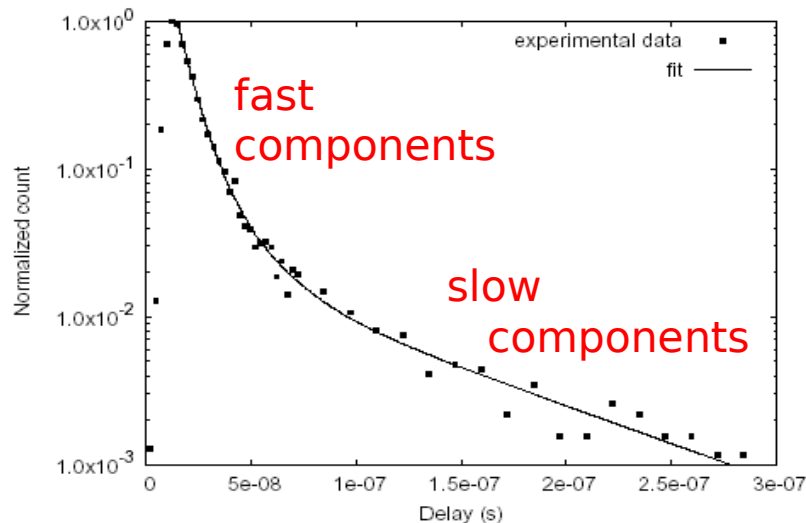
$\tau$  : trap lifetime depends on trap level position

quadratic dependence on  $\Delta V$

$P_c$  : trap capture probability

$\propto$  carrier flux (current) during avalanche  $\propto \Delta V$

$\propto N$  traps



S.Cova, A.Lacaita,  
G.Ripamonti, IEEE EDL (1991)

Fig. 10. Spectrum of the delay time from the primary pulse to the after-pulse.

# After-Pulses vs T (constant $\Delta V$ )

Measurement by waveform analysis:

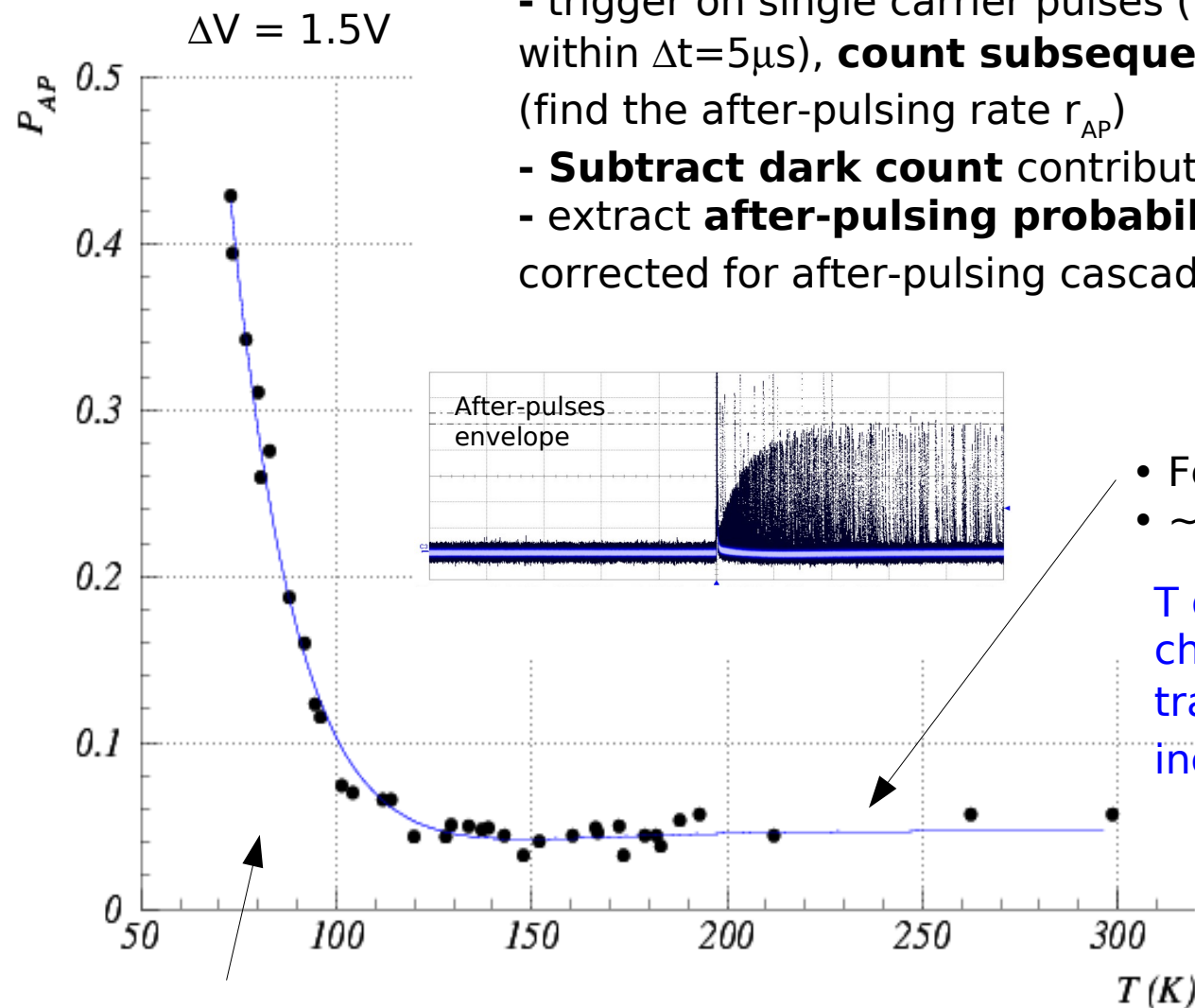
- trigger on single carrier pulses (with no preceding pulses within  $\Delta t=5\mu s$ ), **count subsequent pulses** within  $\Delta t=5\mu s$  (find the after-pulsing rate  $r_{AP}$ )

- **Subtract dark count** contribution

- extract **after-pulsing probability**  $P_{AP}$

corrected for after-pulsing cascade

$$P_{AP} = \frac{r_{AP}}{1 + r_{AP}}$$



- Few % at room T
- ~constant down to ~120K

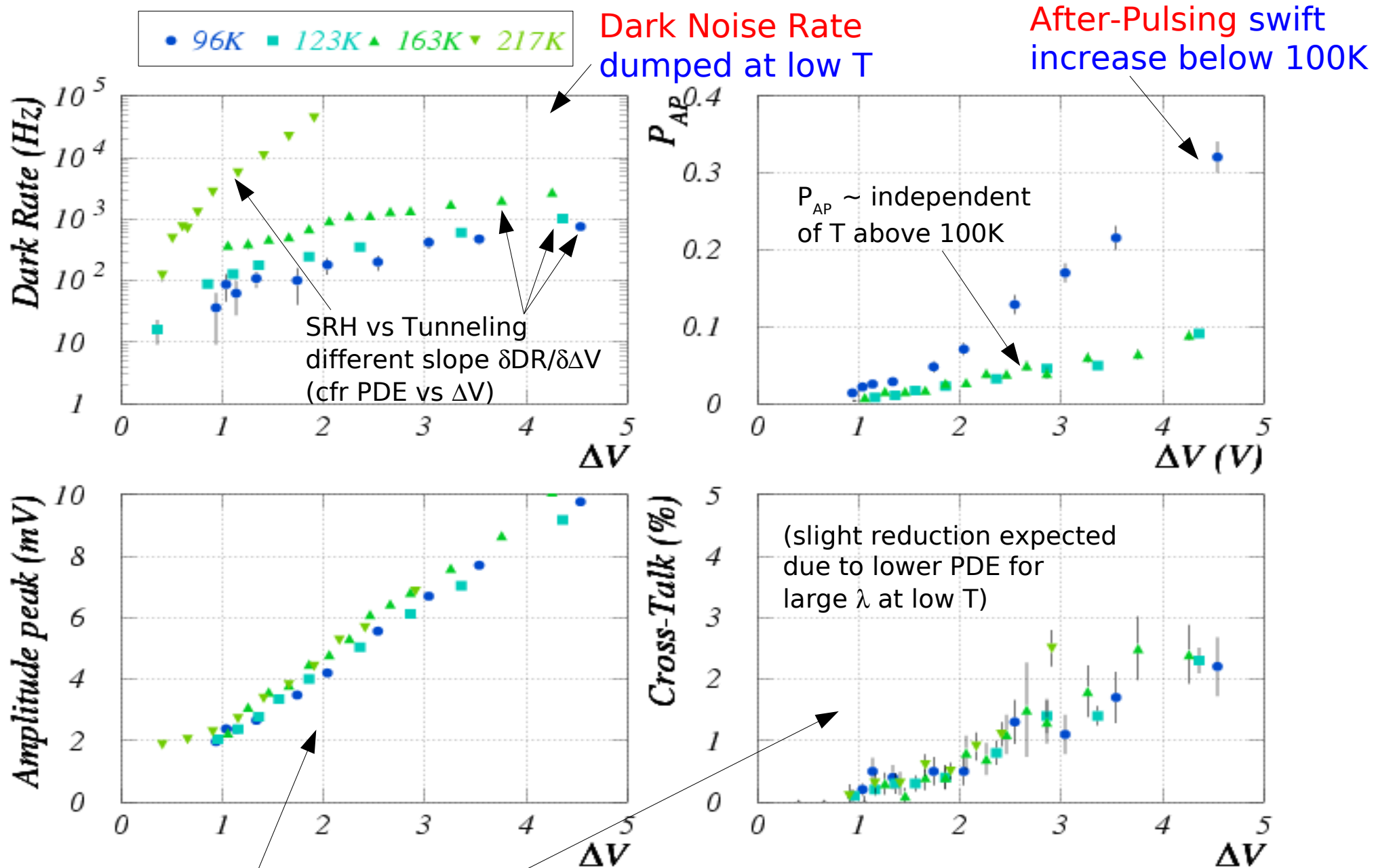
T decreasing: increase of characteristic time constants of traps ( $\tau_{traps}$ ) is compensated by increasing cell recovery time ( $R_q$ )

- several % below 100K

T < 100K: additional trapping centers activated? possibly related to carrier freeze-out (under investigation)

→ On-going work:  
analysis of life-time evolution vs T  
of the various traps (at least 3 found)

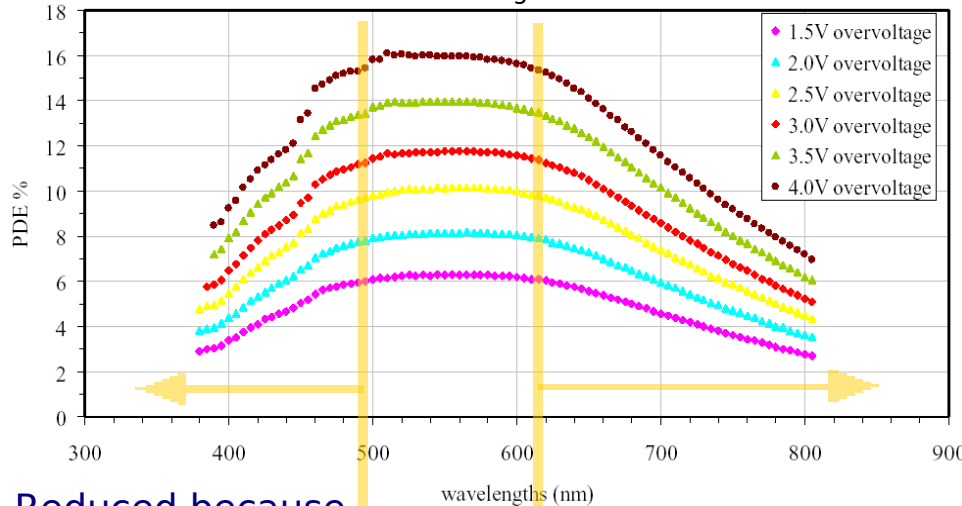
# DR, AP, Gain, X-talk vs $\Delta V$ (constant T)



Gain and Cross-Talk are independent of T

# Photo-Detection Efficiency (PDE) vs $\Delta V$ and $\lambda$

SiPM with  $\epsilon_{\text{geom}} \sim 22\%$



Reduced because avalanche triggered by holes (and ARC)

Reduced because low QE

PDE dependence on  $\lambda$   
(at different  $\Delta V$ ) - room T

PDE =

$\epsilon_{\text{geom}}$  (fraction of active area)

X

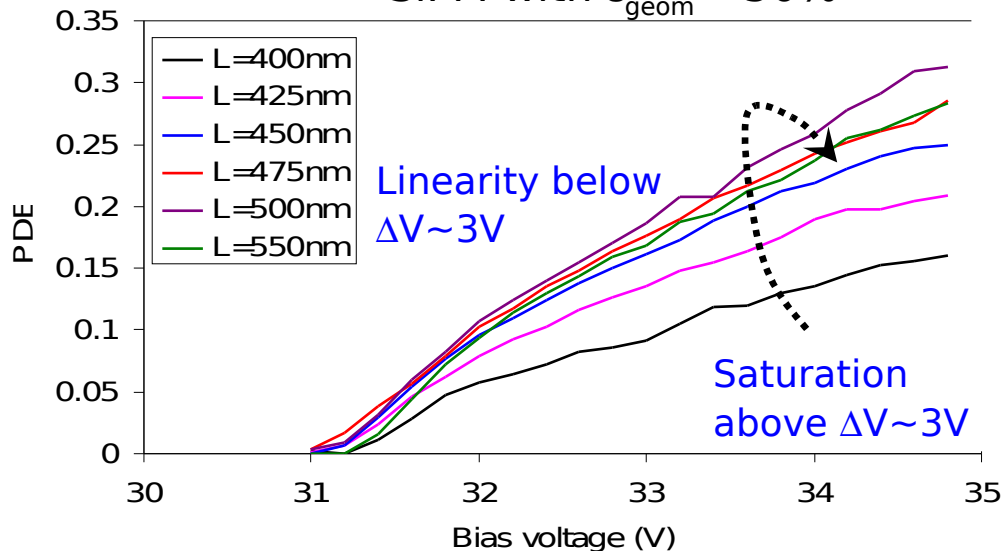
QE (efficiency of photo-conversion)

X

$P_{\text{trigg}}$  (avalanche triggering probability)

Expected to be T dependent

SiPM with  $\epsilon_{\text{geom}} \sim 50\%$



PDE dependence on  $\Delta V$   
(at different  $\lambda$ ) - room T

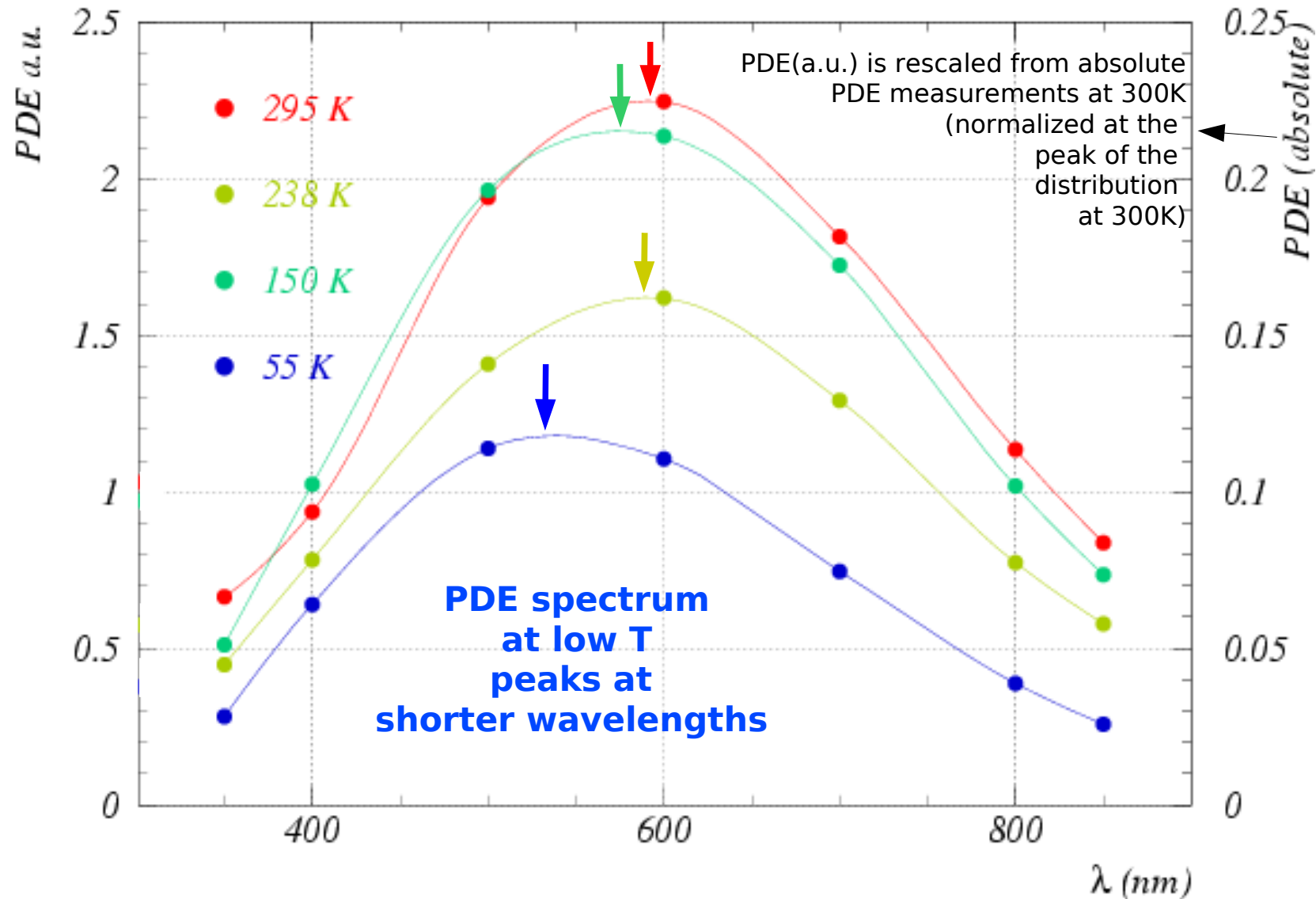


# PDE vs $\lambda$ (constant $\Delta V=2V$ ) - halogen lamp (CW)

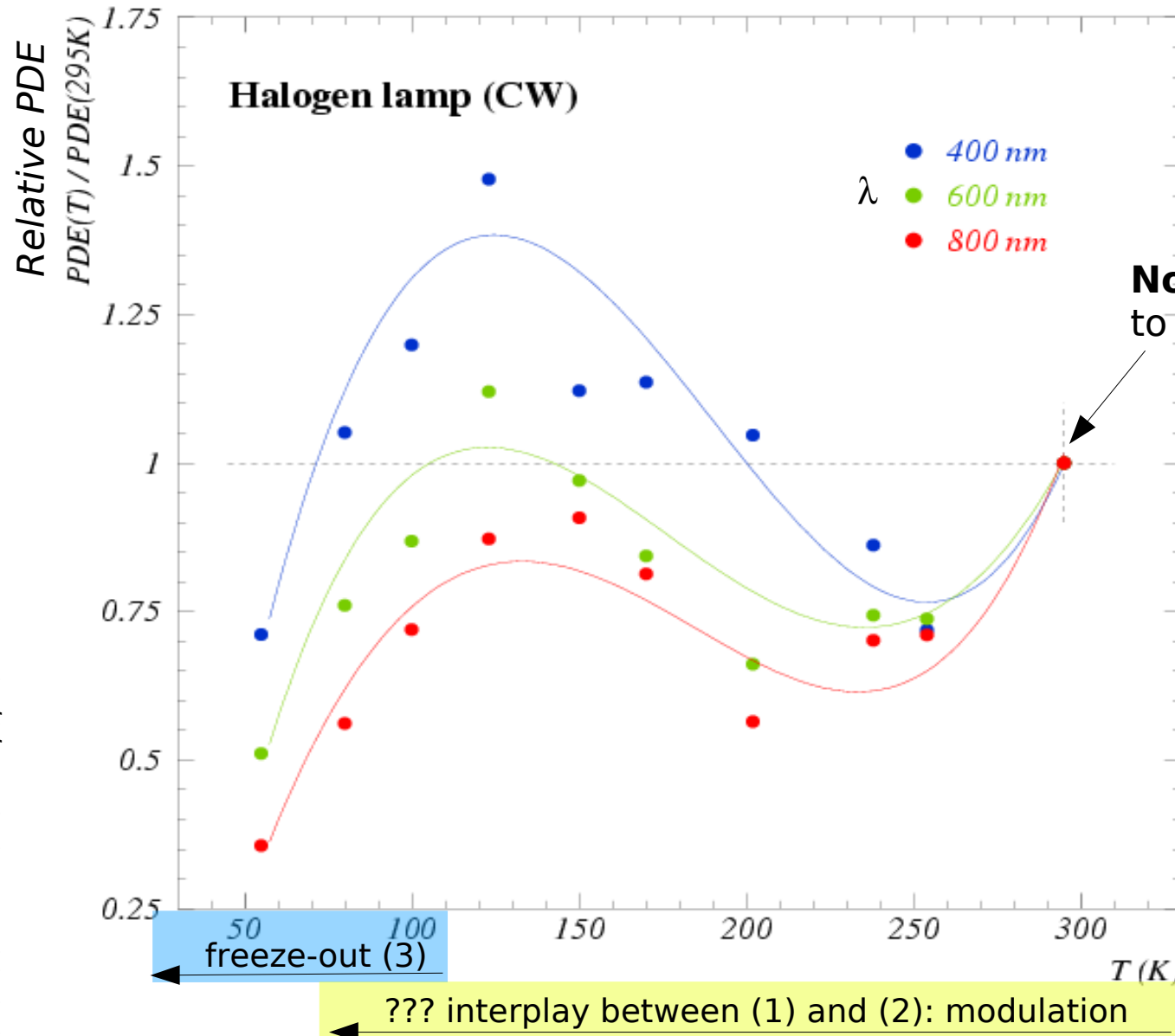
- Measure  $\rightarrow$
- $I_{sipm} / G$  = current drawn by SiPM / SiPM gain
  - $I_{photons}$  = rate of photons by calibrated photo-diode

$\rightarrow$  Find:  $PDE = I_{sipm} / G / I_{photons}$

which differs from absolute PDE but for a common factor due to different photon acceptance of SiPM wrt calibrated diode (different light paths)



# PDE vs T (constant $\Delta V=2V$ ) - halogen lamp (CW)



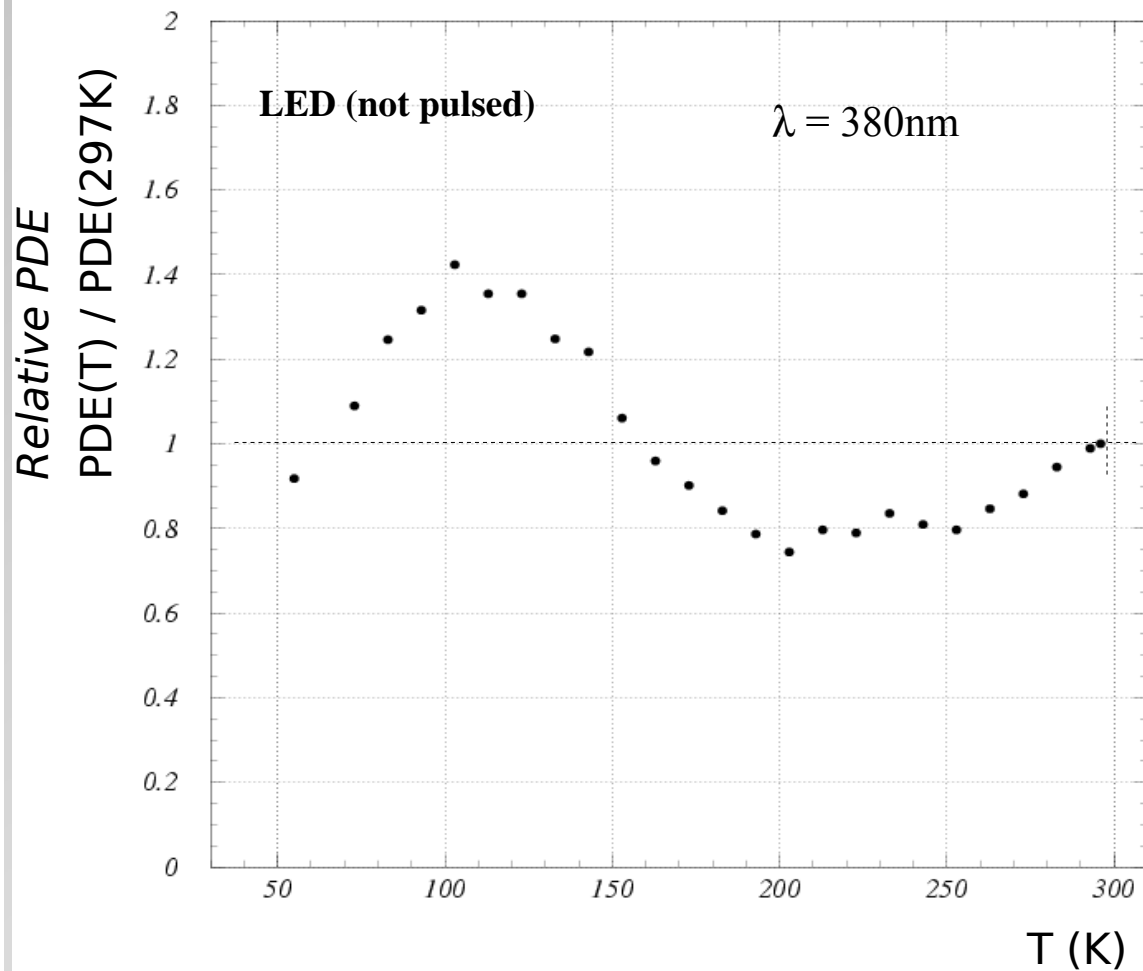
$$PDE = I_{sipa} / G / I_{photons}$$

When T decreases we expect:

- 1) silicon  $E_{gap}$  increasing  
 → larger attenuation length  
 → lower QE (for larger  $\lambda$ )
- 2) mobility increasing  
 → larger impact ionization  
 → larger trigg. avalanche  $P_{01}$
- 3) carriers freeze-out  
 onset below 120K  
 → loss of carriers

# PDE vs T ( $\Delta V=2V$ ) - LED and Laser

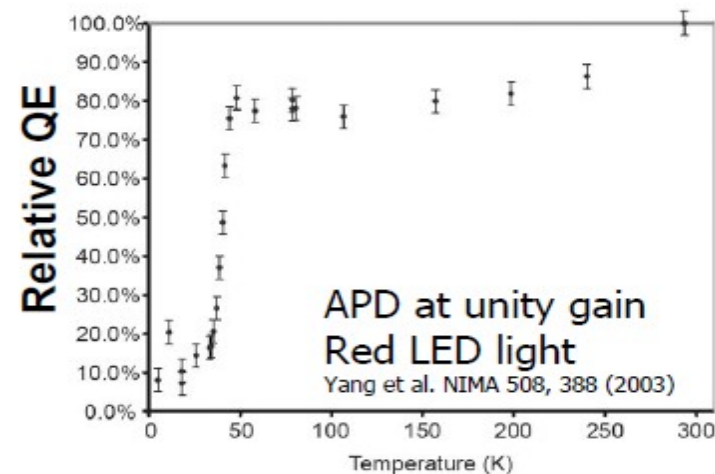
PDE dependence on T at constant gain:  
similar results with LED (cont. light - 380nm)  
and Laser (pulsed light - 405nm)



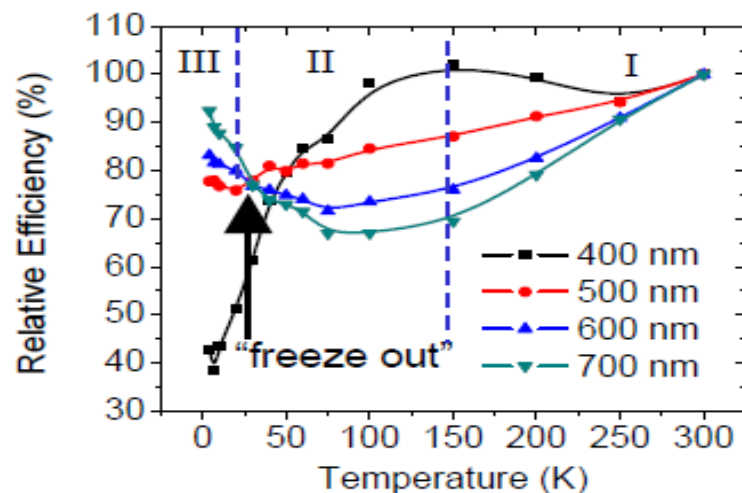
$$PDE(T) \equiv I_{SiPM}(T) / I_{LED}$$

Normalization with PDE at T=297K

Some common features  
with APDs (proportional mode)



APD at  $400\text{nm} < \lambda < 700\text{nm}$   
Johnson et al, IEEE NSS 2009

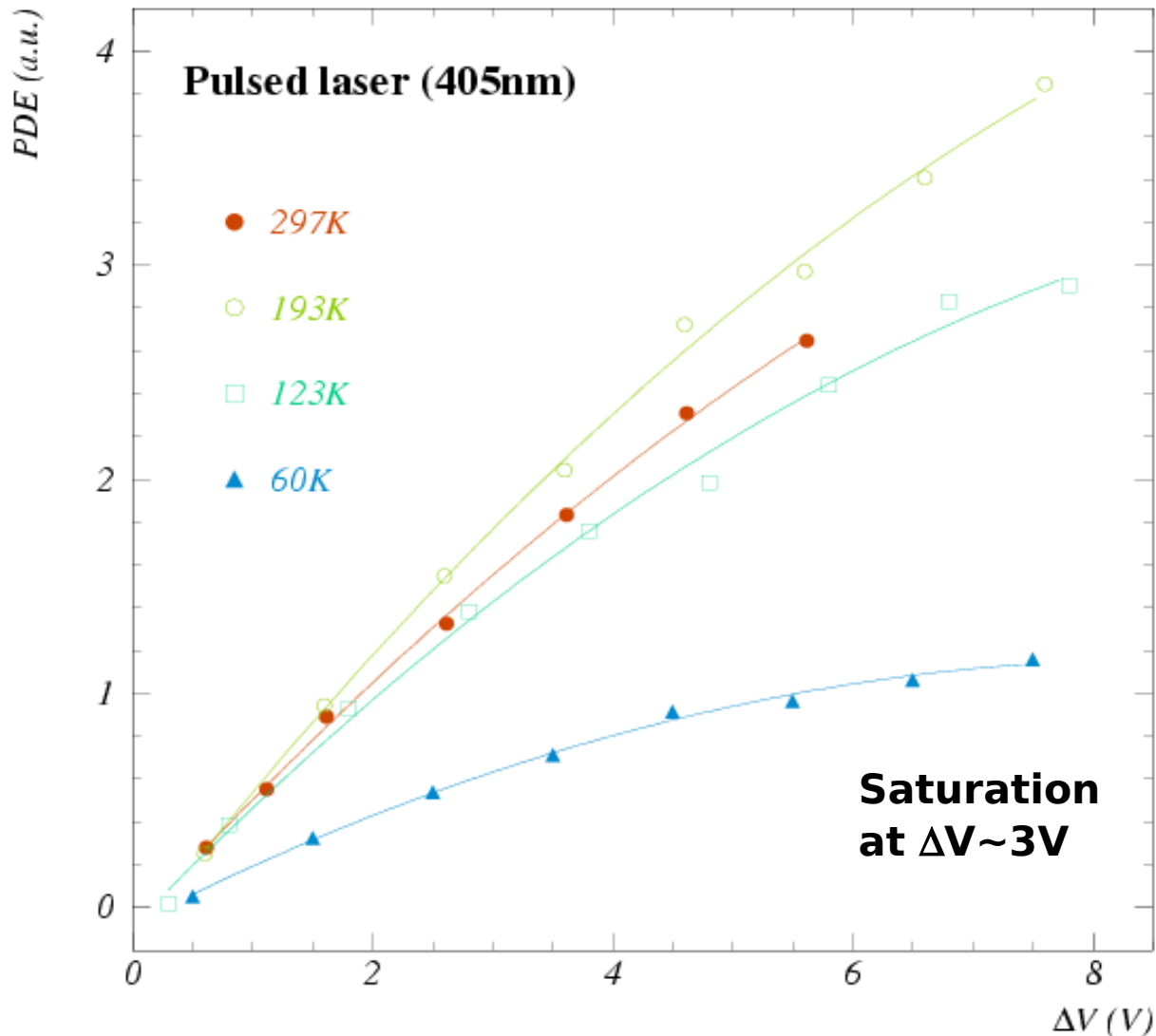


Additional effects in APD  
(depletion region depends on T, ...)

# PDE vs $\Delta V$ (constant T) - pulsed laser (405nm)

Measure  $\rightarrow$

- $I_{pe}$  = average number of photo-el. in coincidence with laser trigger x trigger rate
- $I_{photons}$  = average rate of photons measured by calibrated photo-diode



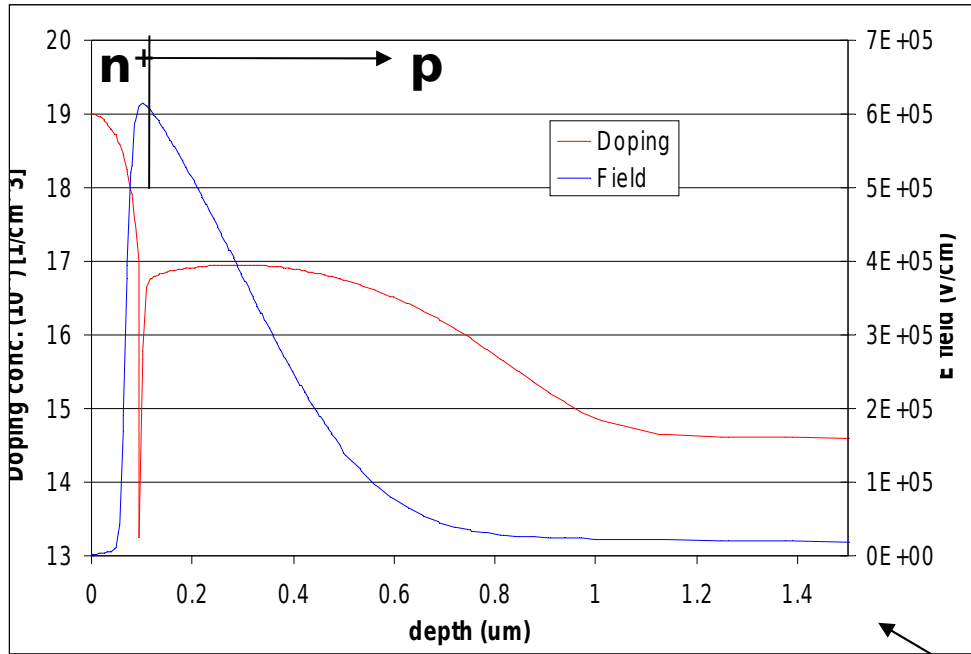
$\rightarrow$  Find:  $PDE = I_{pe} / I_{photons}$

which differs from absolute PDE but for a common factor due to different photon acceptance of SiPM wrt calibrated diode (different light paths)

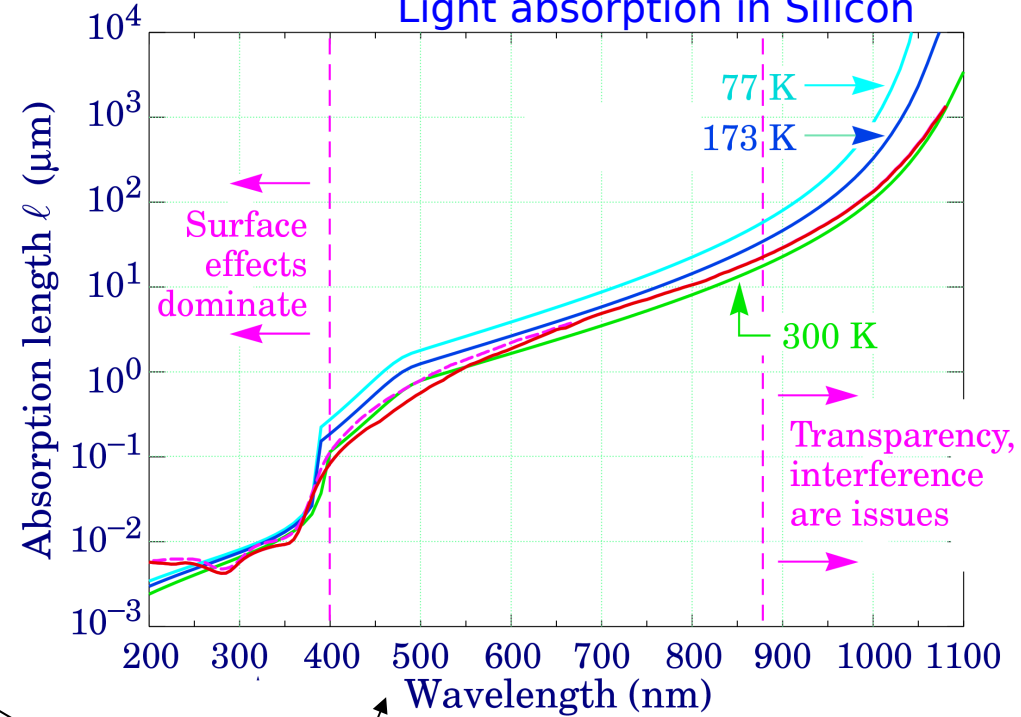
**Saturation starts earlier at low T**

# Understanding PDE vs T

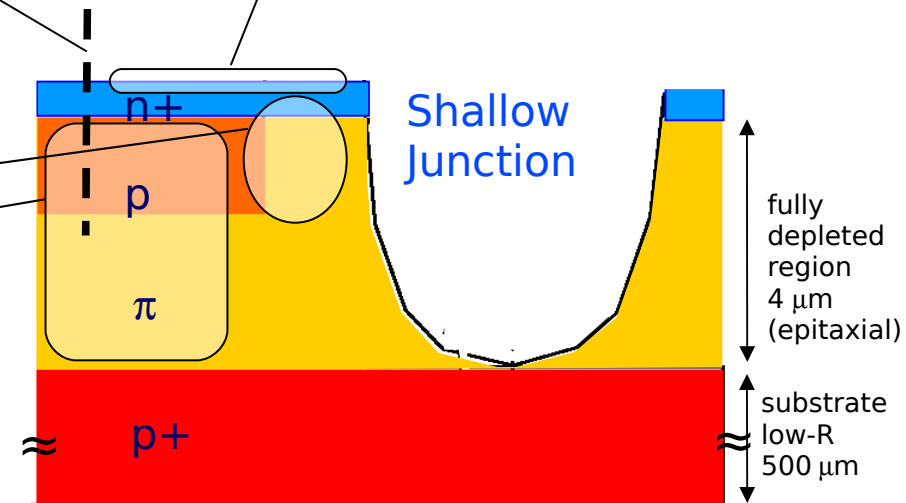
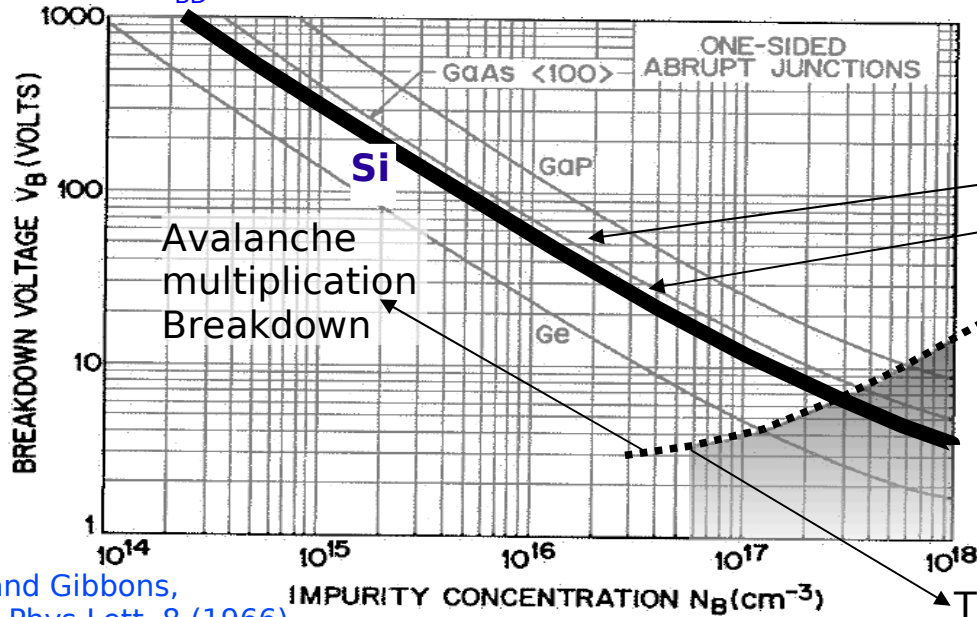
Doping and Field profiles (IRST)



Light absorption in Silicon



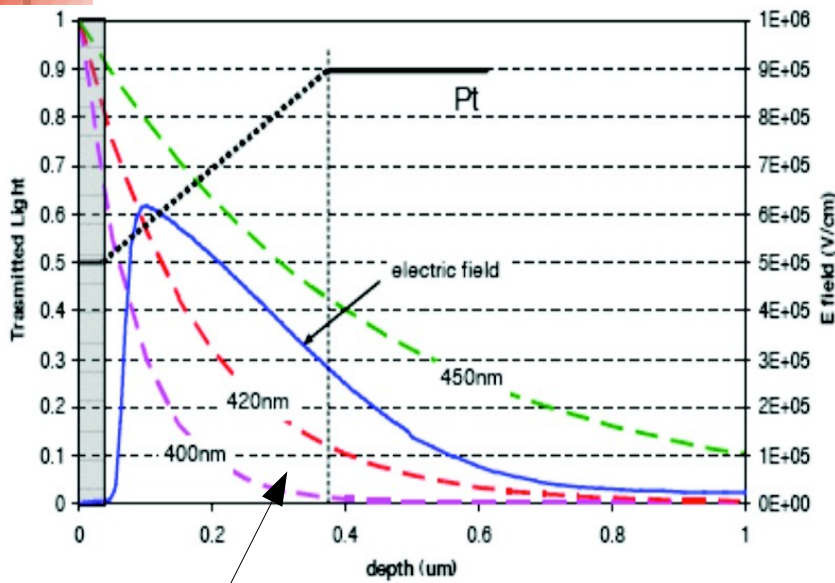
$V_{BD}$  versus doping concentration



Tunneling effect Breakdown

# Understanding PDE vs T: 1D model

Preliminary results



## Breakdown voltage vs T

**Avalanche triggering probability** for electrons and holes ( $P_{trigger,e}$ ,  $P_{trigger,h}$ ) (using differential equations method after Oldham et al, IEEE TNS 19 (1972) 1056)

**E field profile +**

**+ impact ionization**

calculate

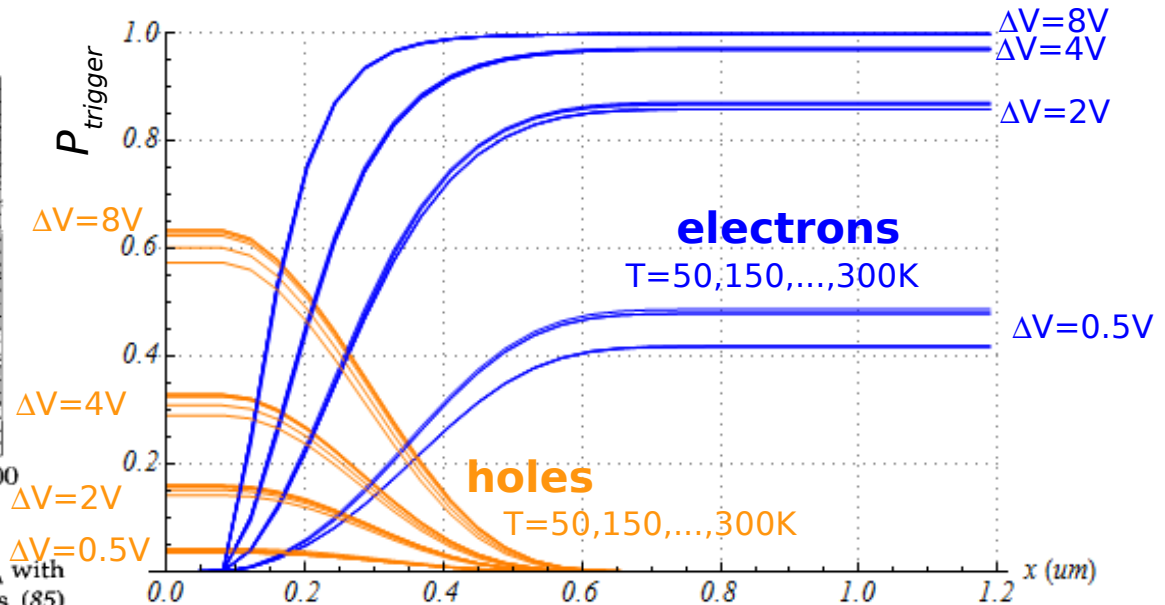
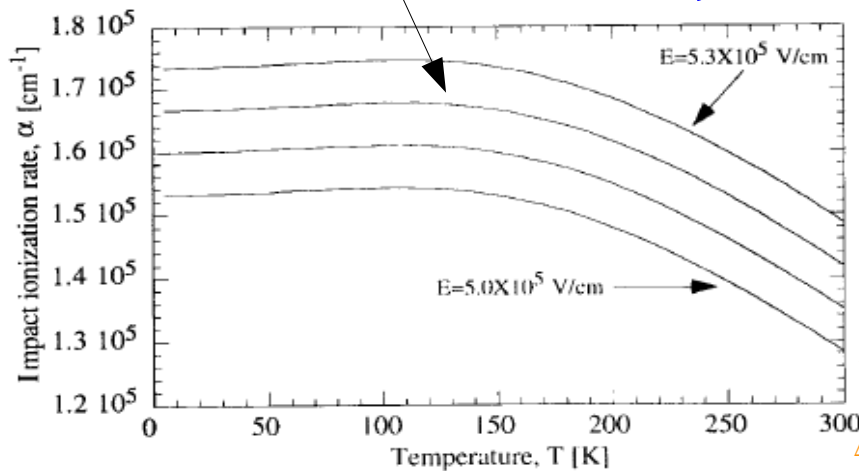


FIGURE 1.43. The impact ionization rate  $\alpha$  as a function of temperature  $T_A$  with the electric field  $E$  as a parameter calculated from Okuto and Crowell's (85) model.



# Understanding PDE vs T: 1D model

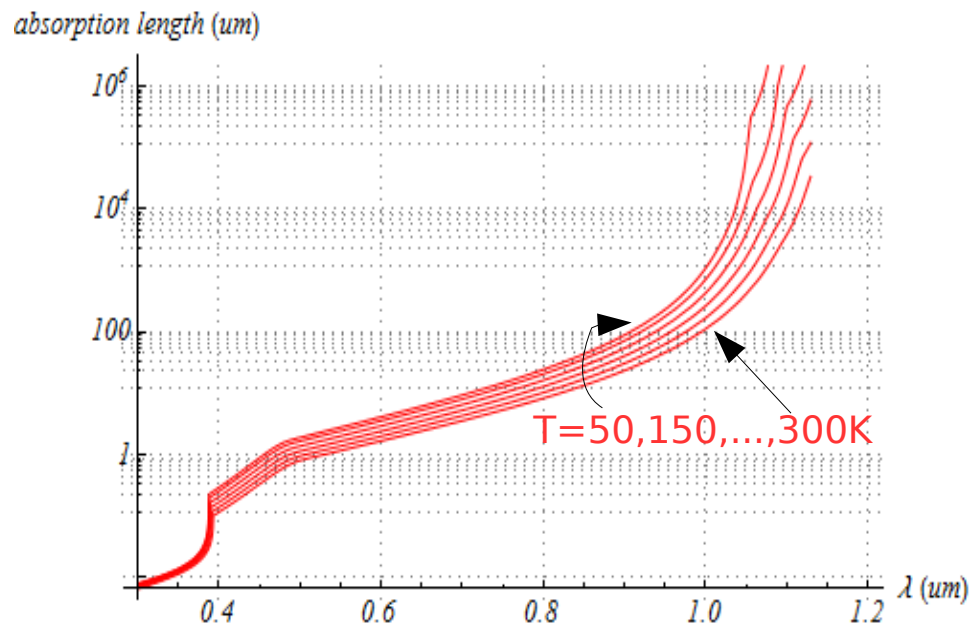
Preliminary results

avalanche triggering probability +  
+ light absorption length in Si ( $1/\alpha$ )

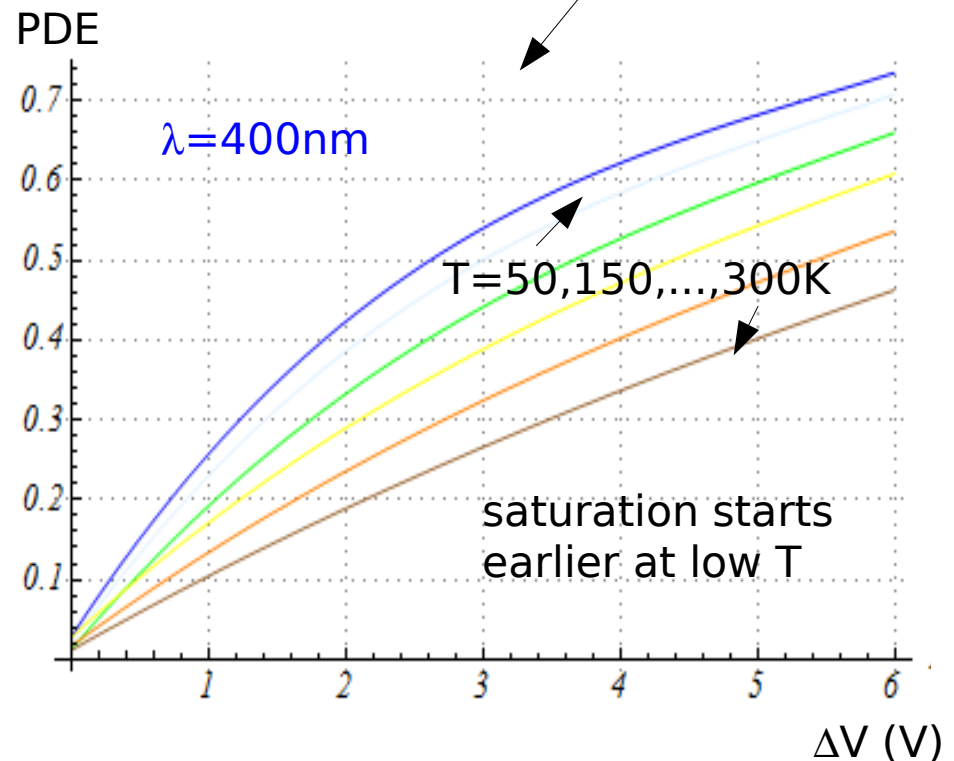
calculate



**PDE as a function of ( $\lambda, T, \Delta V$ )**  
obtained by the convolution of  
 $P_{\text{trigg}}(x)$  and  $\alpha \exp(-\alpha x)$   
(integrated over the depletion layer)

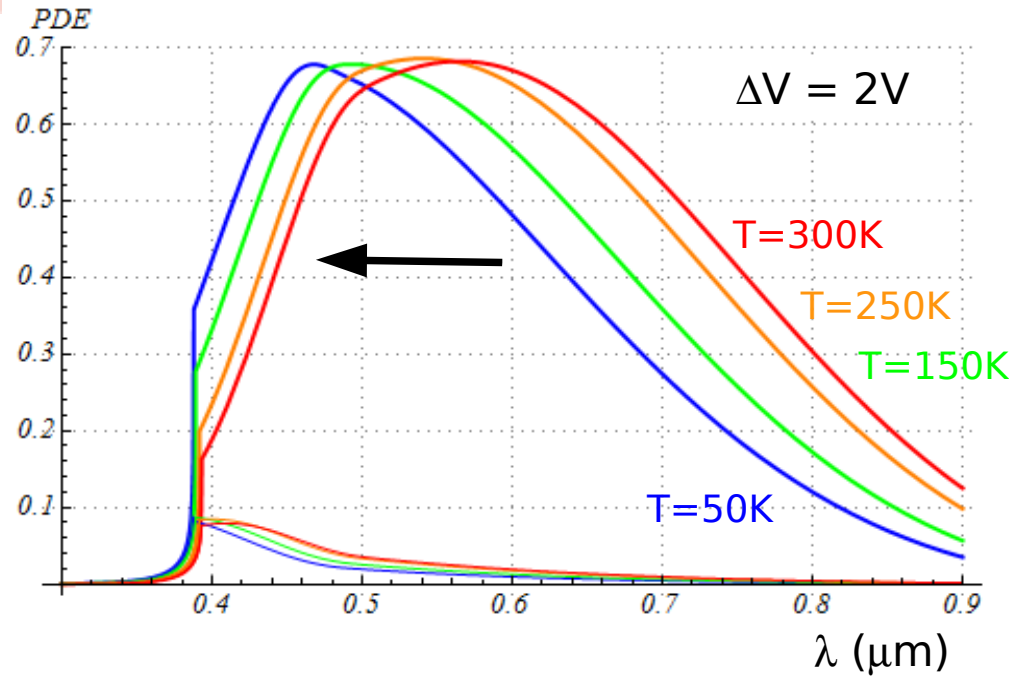


Rajkanan et al, Solid State Ele 22 (1979) 793  
Accounting  $E_{\text{gap}}$  variations with T, etc...



# Understanding PDE vs T: 1D model

Preliminary results

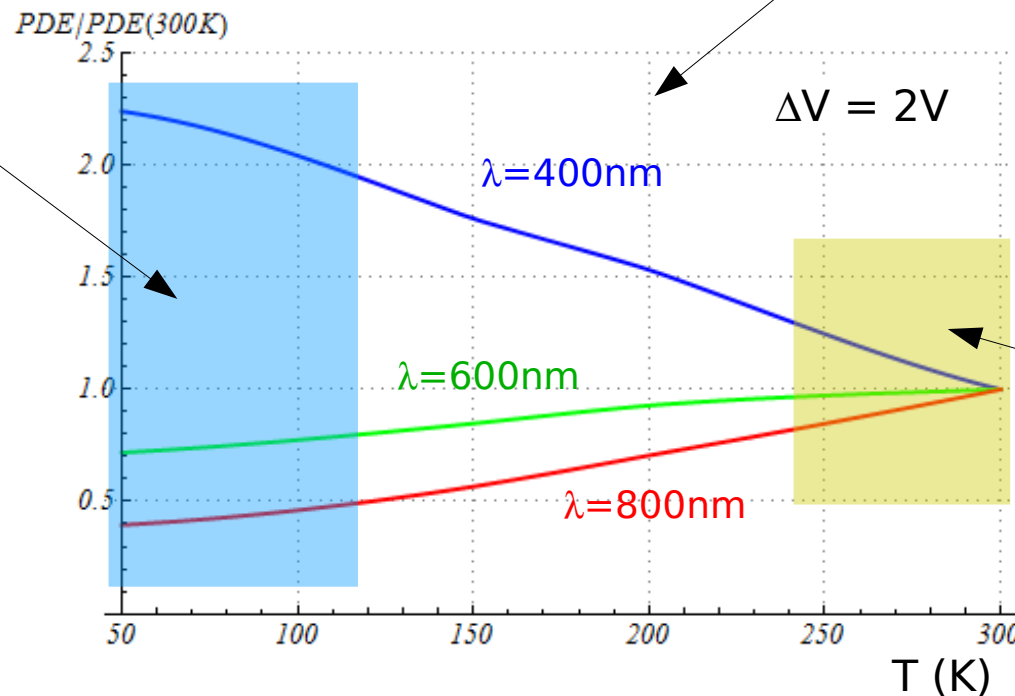


1) main contribution to PDE from electrons  $\rightarrow$  PDE distribution shifted toward short  $\lambda$  at low T because of larger absorption length (photo-generation deeper into depletion layer  $\rightarrow$  gain for shorter  $\lambda$ , loss for longer  $\lambda$ )

(see also PDE vs T)

2) tunneling effects not (yet) included in the model (enhancement of PDE, interplay with band gap variations with T)

3) freeze-out not (yet) included in the model



4) something else is missing: need to explain PDE decreasing with T for  $250\text{K} < T < 300\text{K}$

**to be understood !**



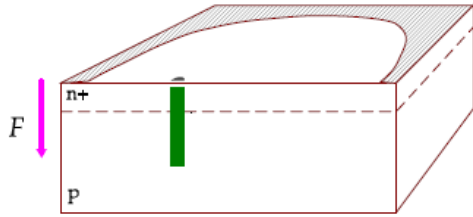
# Overview - SiPM timing properties

- **Intrinsic timing**: discussion of intrinsic timing properties based on measurements of **single photon** timing resolution

G.C. et al NIMA 581 (2007) 461

- A few comments about **Signal shape**, **Front-End** and **Read-Out Electronics** aiming at timing applications in **low light intensity** conditions

# GM-APD timing: avalanche development



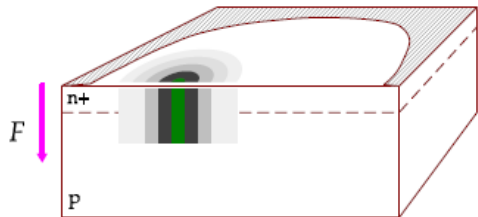
## Longitudinal multiplication

Duration ~ few ps  
Internal current up to ~ few  $\mu\text{A}$

(1) Avalanche "seed": free-carrier concentration rises exponentially by **"longitudinal" multiplication**

(2) E field locally lowered until  $E_{\text{max}}$  reaches breakdown value

Multiplication is self-sustaining  
Avalanche current steady until new multiplication triggered in near region



## Transverse multiplication

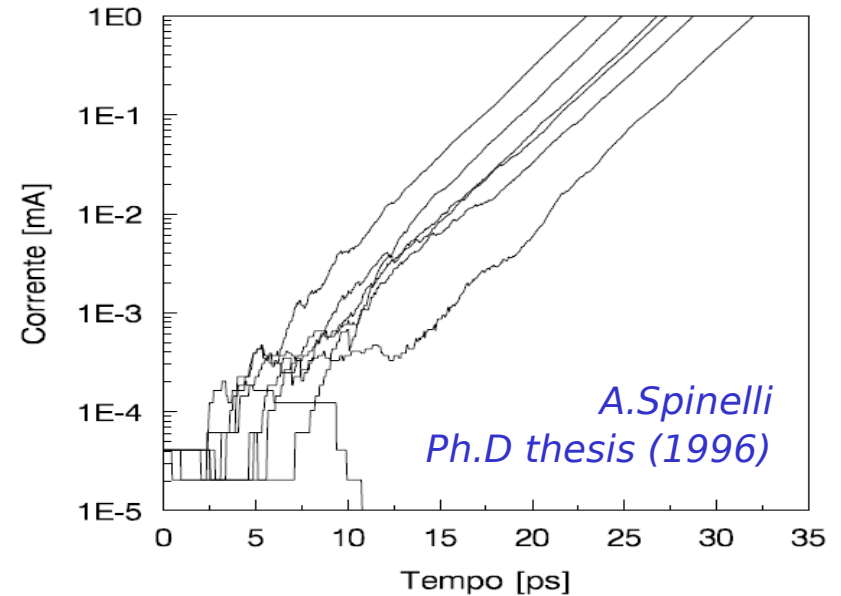
Duration ~ few 100 ps  
Internal current up to ~ few  $10\mu\text{A}$

(3) **Avalanche spreads "transversally"** over the junction

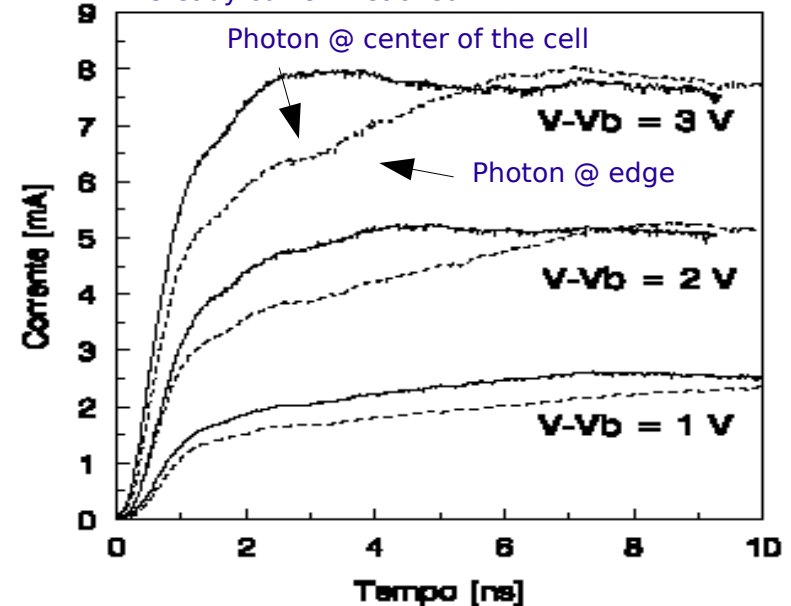
(diffusion speed ~ some  $10\mu\text{m/ns}$  enhanced by multiplication)

(4) **Passive quenching mechanism** effective only after transverse **avalanche size ~  $10\mu\text{m}$**

(Otherwise avalanche spreads over the whole active depletion volume  $\rightarrow$  avalanche current reaches a final saturation steady state value)



Simulation w/o quenching:  
 $\rightarrow$  steady current reached

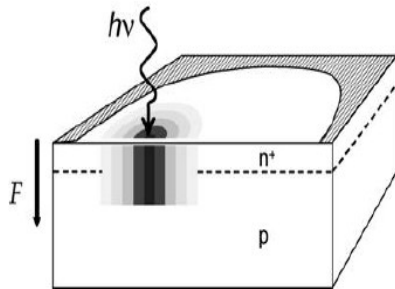


# GM-APD timing: fast and slow components

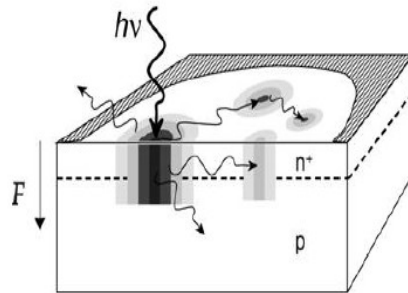
## 1) Fast component: gaussian with time scale $O(100\text{ps})$

Statistical fluctuations in the avalanche:

- **Longitudinal** build-up (minor contribution)
- **Transversal** propagation (main contribution):
  - via Multiplication assisted diffusion (dominating in few  $\mu\text{m}$  thin devices)  
A.Lacaita et al. APL and El.Lett. 1990
  - via Photon assisted propagation (dominating in thick devices -  $O(100\mu\text{m})$ )  
PP.Webb, R.J. McIntyre RCA Eng. 1982  
A.Lacaita et al. APL 1992



Multiplication assisted diffusion



Photon assisted propagation

- **Fluctuations** due to impact ionization statistics
- Jitter at minimum  $\rightarrow O(10\text{ps})$  (very low threshold  $\rightarrow$  not easy)
- additional **Fluctuations** due to longitudinal position of photo-generation due to finite drift time in low E field region (even at saturated velocity)
- **Fluctuations** due to large variance of the transverse diffusion speed
- Jitter  $\rightarrow O(100\text{ps})$  (usually threshold set high)
- dependence of avalanche build-up rate on transverse impact position ( $\rightarrow$  cell size)

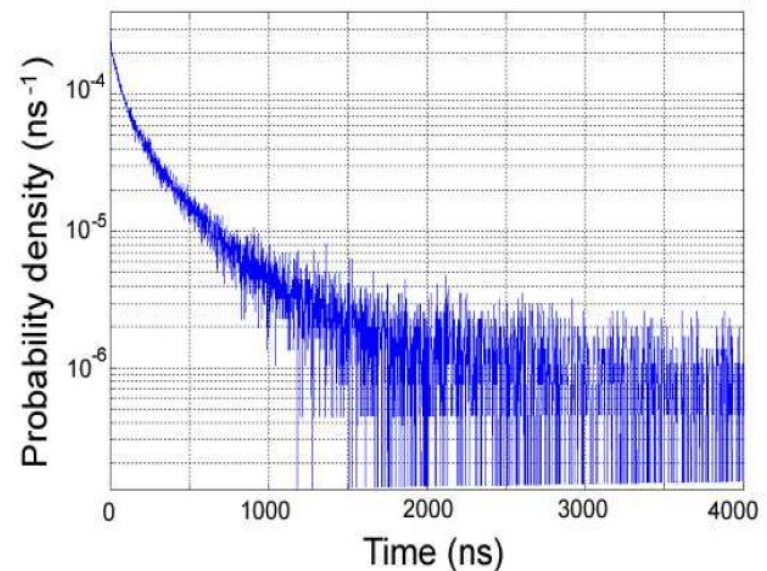
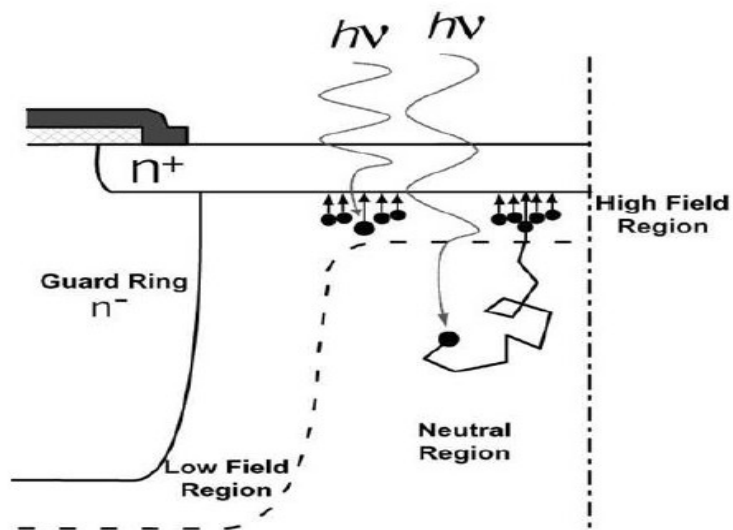
Higher over-voltage  $\rightarrow$  improved time resolution

# GM-APD timing: fast and slow components

## 2) Slow component: minor non-gaussian tails with time scale $O(\text{ns})$

Carriers photo-generated in the neutral regions beneath the junction and reaching the electric field region by diffusion

G.Ripamonti, S.Cova Sol.State Electronics (1985)



tail lifetime:  $\tau \sim L^2 / \pi^2 D$

$L$  = effective neutral layer thickness

$D$  = diffusion coefficient

S.Cova et al. NIST Workshop on SPD (2003)

Shorter wavelengths  $\rightarrow$  higher resolution (reduced tails)

# Experimental Setup

## Pump Laser

Millenia V (Spectra-physics)  
solid state CW visible laser

pump laser

## Crystal for Second Harmonic Generation (SHG)

conversion  $800\text{ nm} \rightarrow 400\text{ nm}$   
efficiency at % level

Ti:sapphire laser

SHG

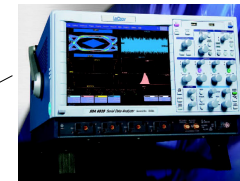
## Filters

blue + neutral  
for rejecting IR light  
and tune intensity

## Dark box

SiPM + amplifier

Low noise LV suppliers



## LeCroy SDA 6020

Analog bandwidth: 6GHz  
Sampling rate: 20GS/s  
Vertical resolution: 8 bits

(Acknowledgments:  
E.Marcon, LeCroy)

External trigger from  
Ti:sapphire laser  
signal

## Mode-locked Ti:sapphire Laser

Tsunami (Spectra-physics)  
femtosecond pulsed laser

wavelength: tuned at  $800 \pm 15\text{ nm}$   
pulse width:  $\sim 60\text{ fs}$  FWHM  
pulse period:  $\sim 12\text{ ns}$   
pulse timing jitter  $< 100\text{ fs}$

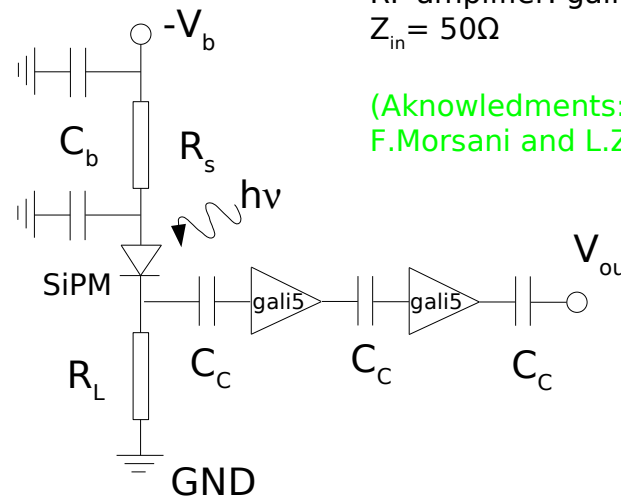
## Electronics

$I \rightarrow V$  conversion via  $R_L$  ( $500\Omega$ )  
Two stage voltage amplification (= x50)  
based on high-bandwidth low-noise  
RF amplifier: gali-5 (MiniCircuit)  
 $Z_{in} = 50\Omega$

(Acknowledgments:  
F.Morsani and L.Zaccarelli, INFN-Pisa)

## Data taking conditions:

- different  $V_{bias}$
- both at  $800\text{ nm}$  and  $400\text{ nm}$
- with different light intensities  
(counting rates  
in the range  $10 \div 20\text{ Mhz}$   
ie  $15 \div 30\text{ KHz}$  per single cell)



# Waveform analysis: method

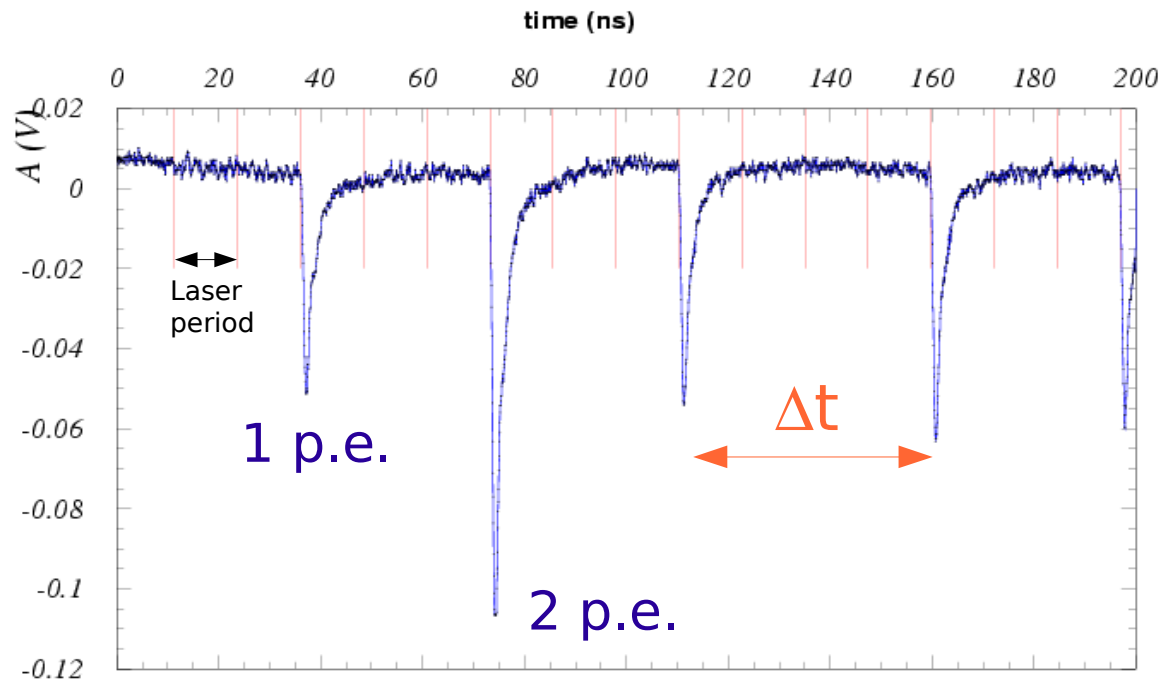
## (1) Selection of candidate peaks:

- single photon peaks
- proper signal shape
- **low instantaneous intensity**  
(no activity before/after within 50ns)
- **low noise** during the previous 10 ns  
(typical noise  $\sim 1\text{mV rms}$ )

## (2) Peak reconstruction

- **optimum time reconstruction**
- amplitude and width (baseline shift correction)

## (3) Time difference $\Delta t$ between consecutive peaks

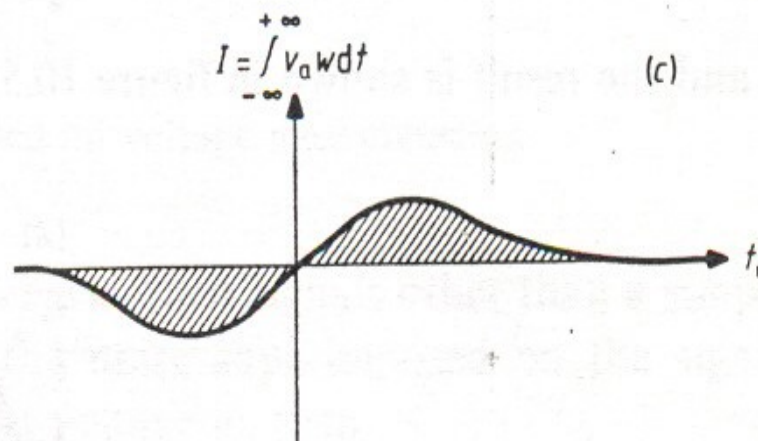
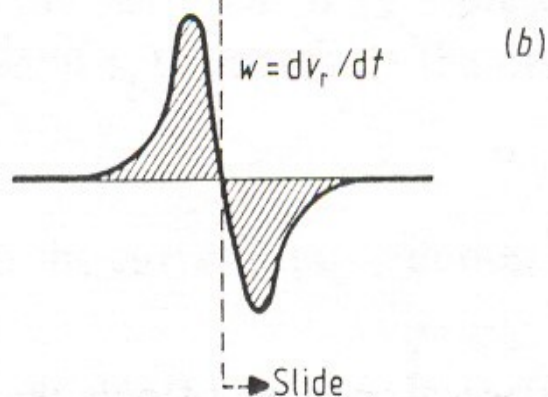
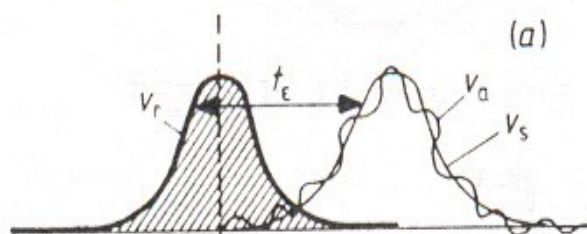


NOTE: good timing properties even up to  $10\text{MHz/mm}^2$  photon rates

# Waveform analysis: optimum timing filter

Different methods to reconstruct the time of a peak:

- ✗ parabolic fit to find the peak maximum
- ✗ average of time samples weighted by the waveform derivative
- ✓ digital filter: weighting by the derivative of a reference signal  
→ best against noise (signal shape known)



Digital filter method to minimize N/S  
for timing measurements:  
solve the following equation on  $t_0$  :

$$\int V_a(t) \frac{\partial V_r(t-t_0)}{\partial t} dt = 0$$

$V_a$  = measured signal  
(includes noise)  
 $V_r$  = reference signal  
 $t_0$  = reference time



# Single Photon Timing Resolution (SPTR)

Analysis of the distributions of the  $t$  difference between successive peaks (modulo the laser period  $T_{\text{laser}} = 12.367\text{ns}$ )

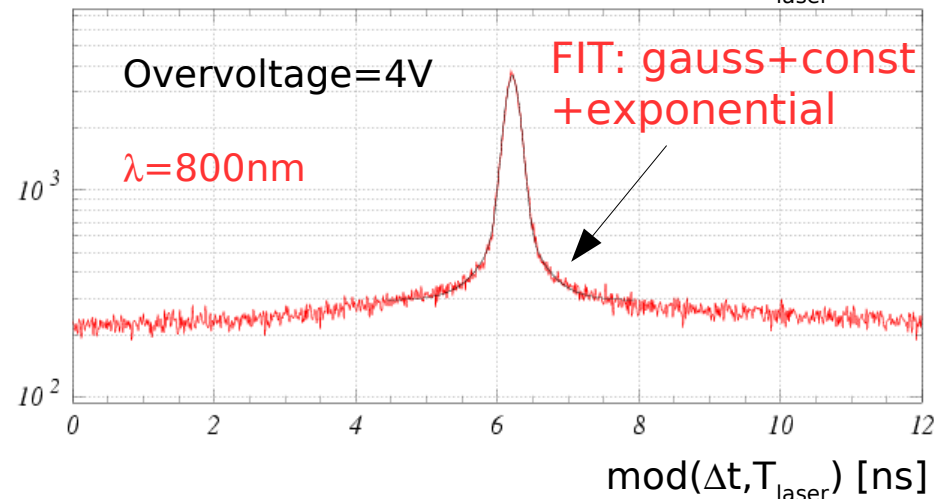
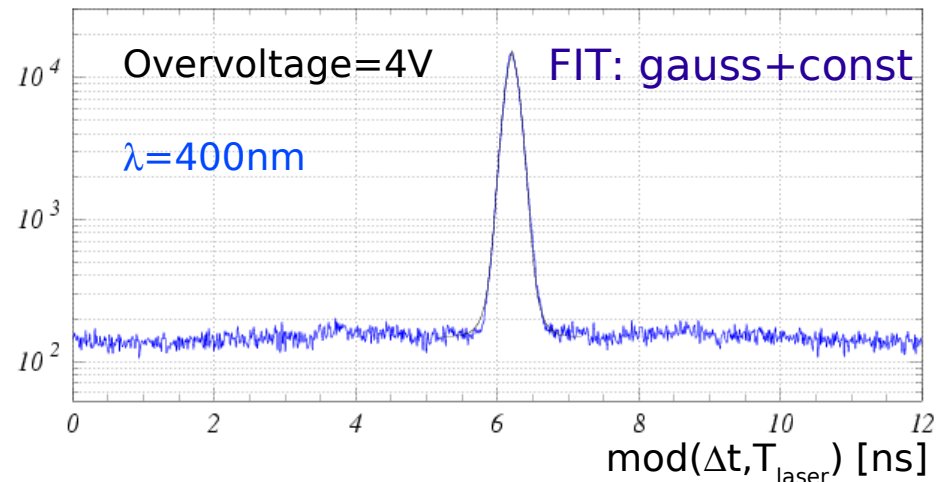
Data at  $\lambda = 400\text{nm}$   
fit gives reasonable  $\chi^2$  with gaussian ( $\sigma_t^{\text{fit}}$ ) + constant term (dark noise contribution)

The detector resolution is obtained by  $\sigma_t^{\text{fit}}/\sqrt{2}$

Data at  $\lambda = 800\text{nm}$   
fit gives reasonable  $\chi^2$  with an additional exponential term  $\exp(-\Delta t/\tau)$

- $\tau \sim 0.2 \div 0.8\text{ns}$  in rough agreement with diffusion tail lifetime:  $\tau \sim L^2 / \pi^2 D$  if  $L$  is taken to be the diffusion length
- Contribution from the tails  $\sim 10 \div 30\%$  of the resolution function area

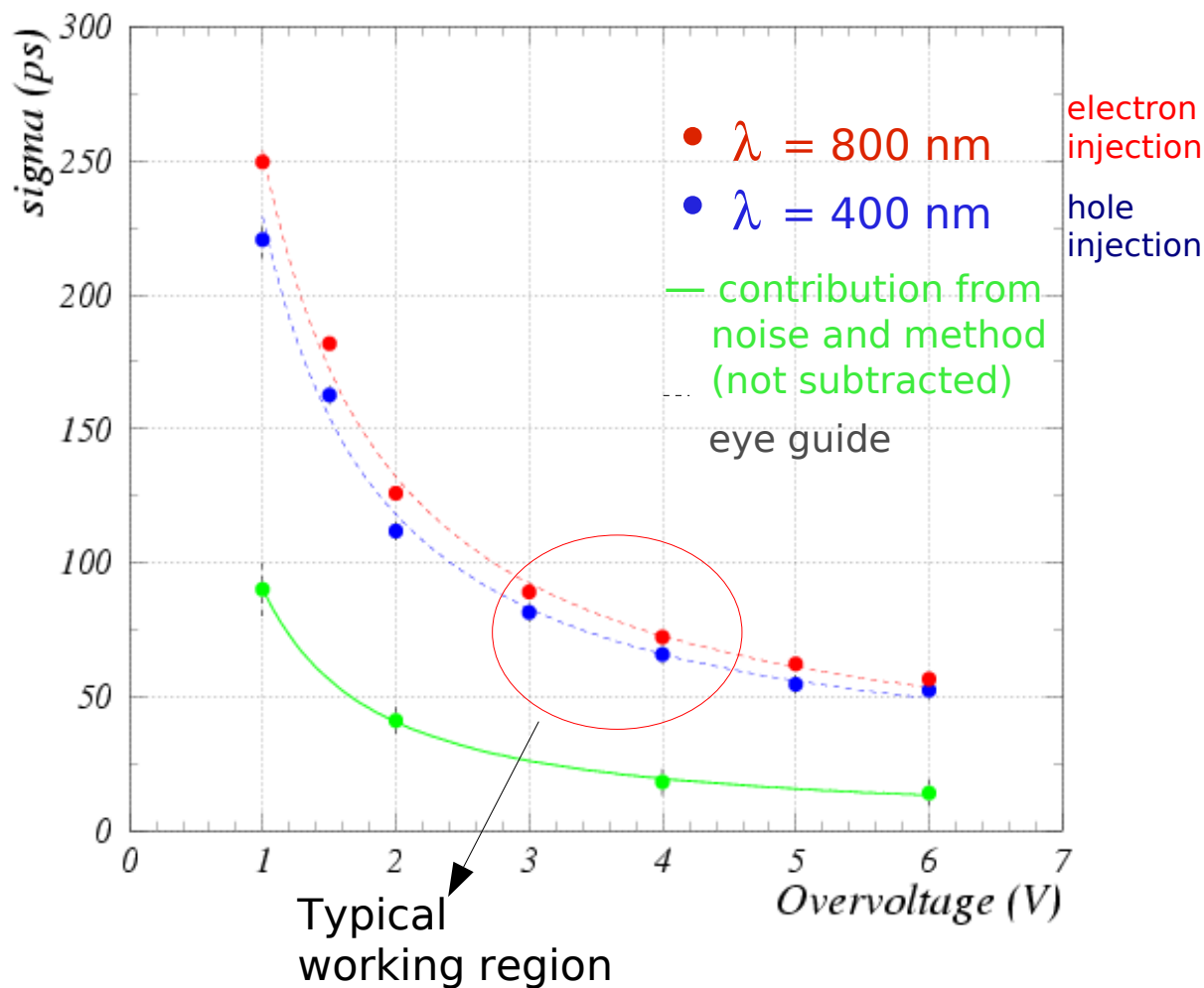
Gaussian + Tails (long  $\lambda$ )  
rms  $\sim 50\text{-}100\text{ ps}$   $\sim \exp(-t / O(\text{ns}))$   
contrib. several % for long wavelengths



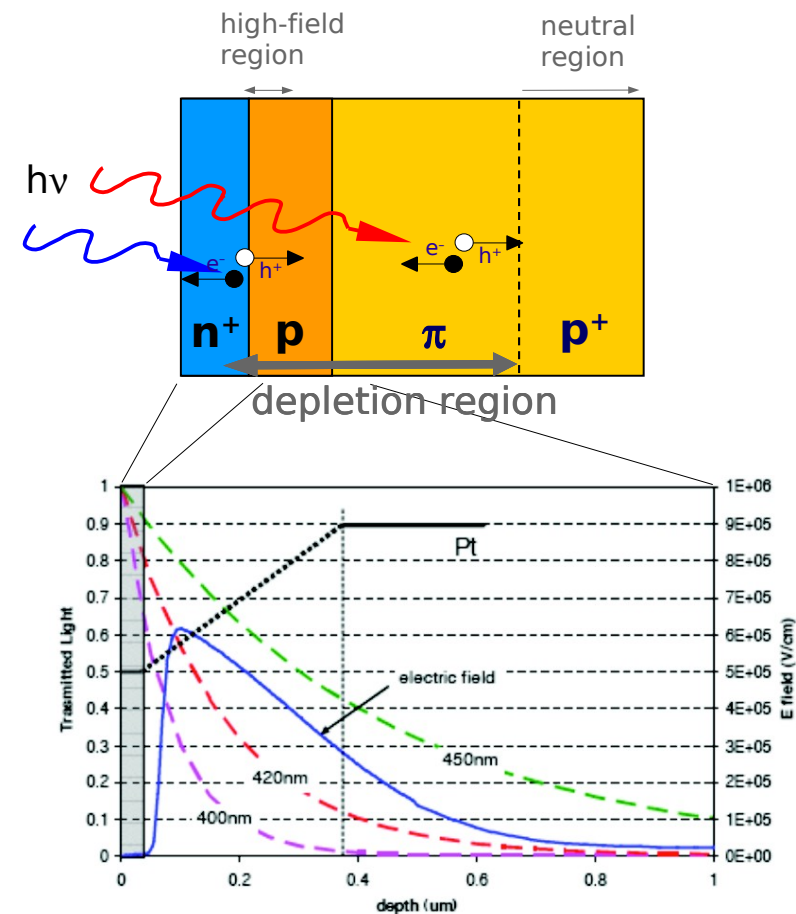
Distributions of the difference in time between successive peaks (modulo the measured laser period  $T_{\text{laser}} = 12.367\text{ns}$ )



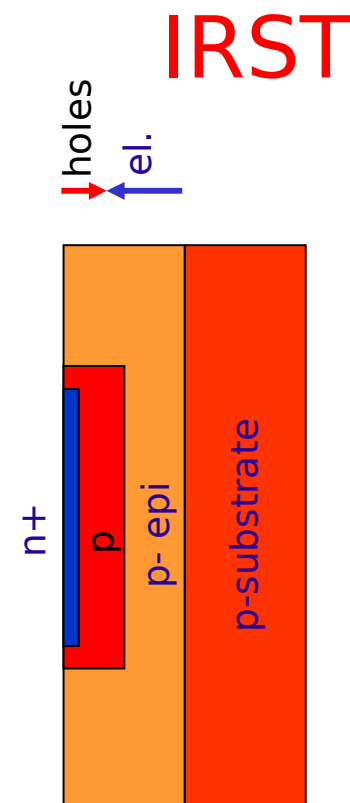
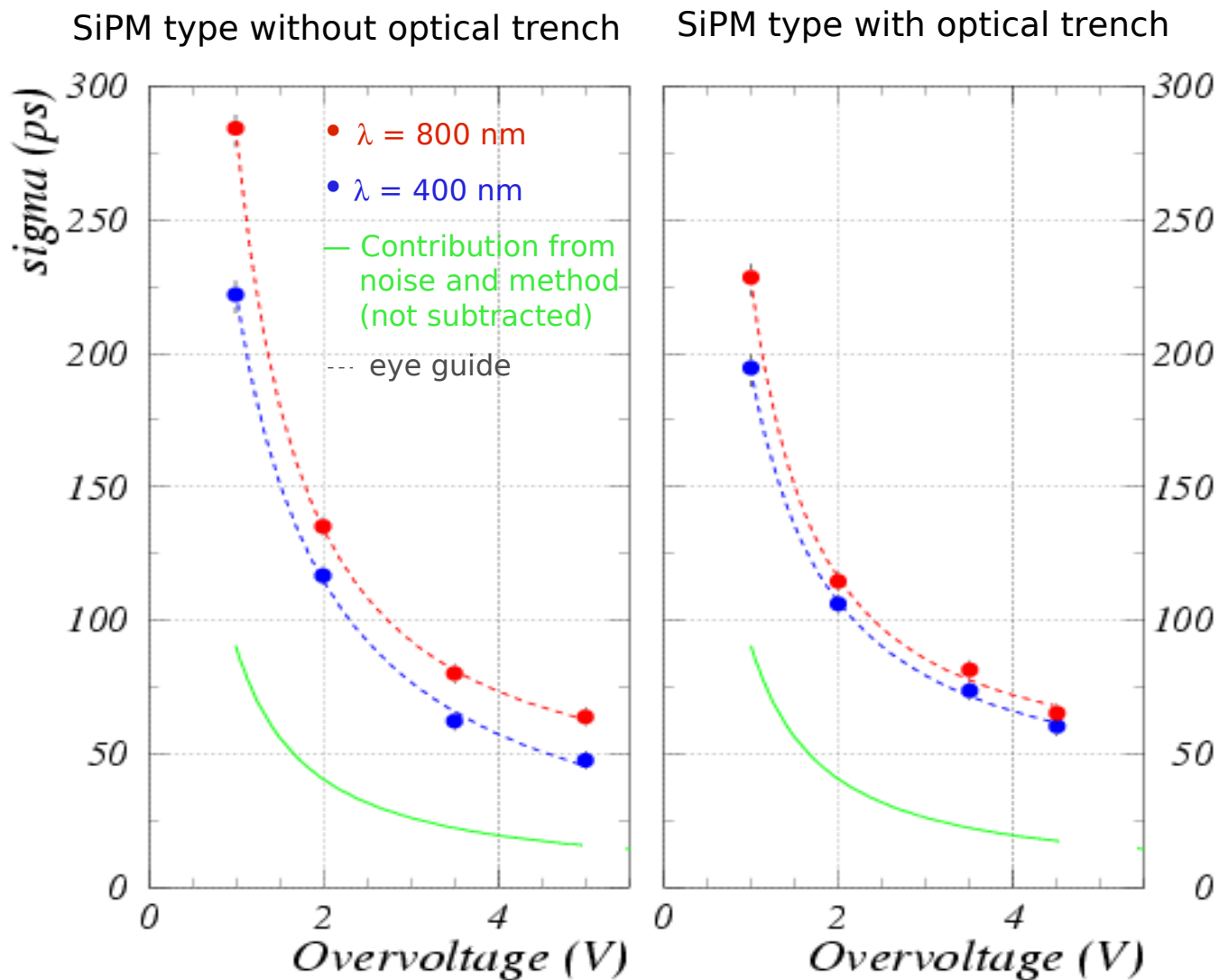
# IRST - single photon timing res. (SPTR)



Better resolution for short wavelengths: carriers generated next to the high E field region

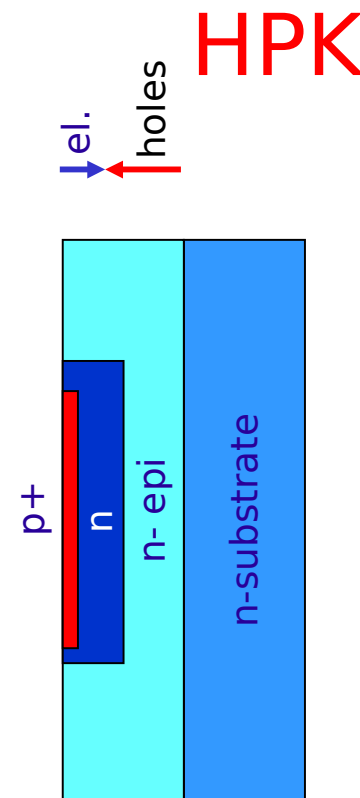
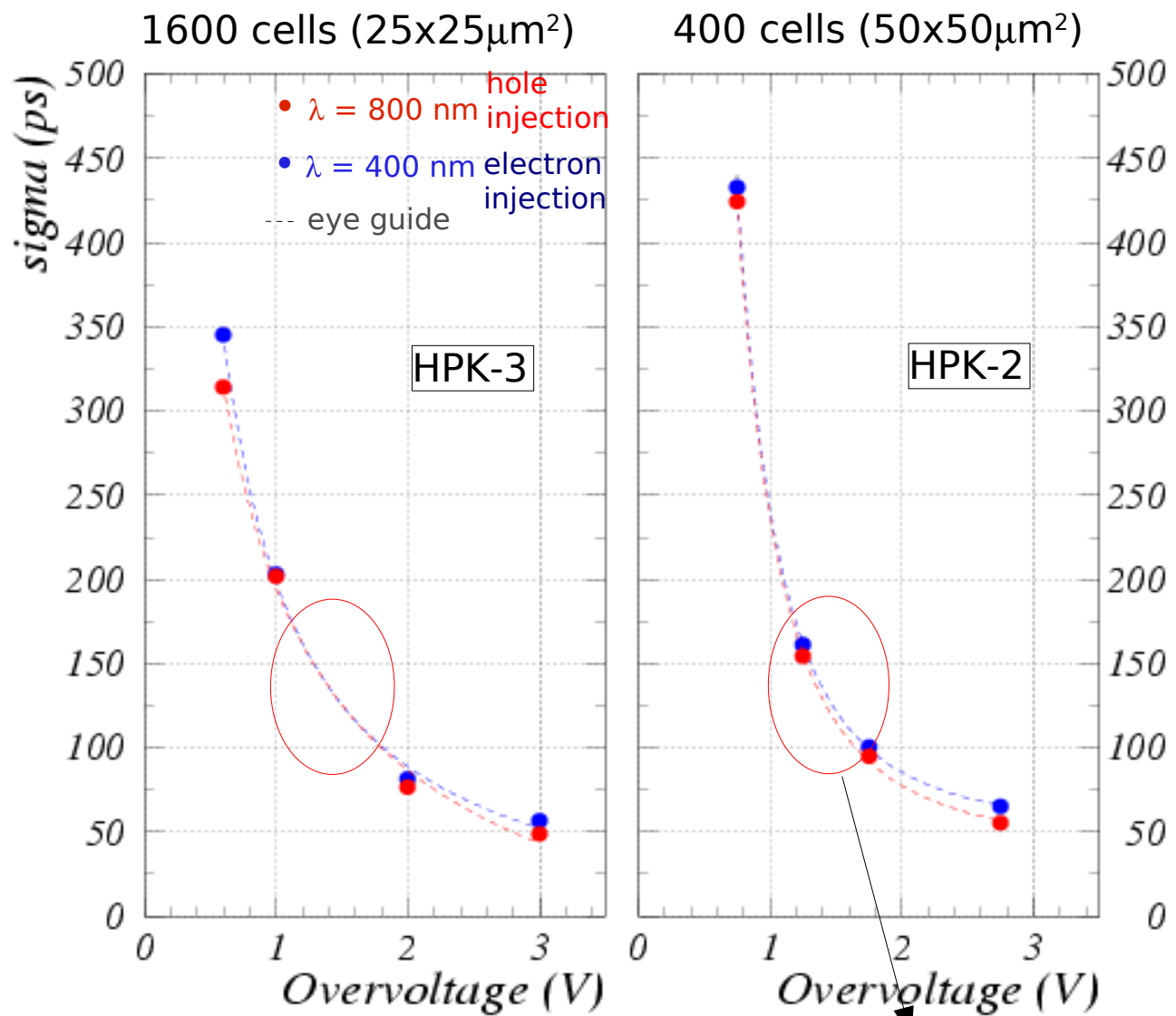


# IRST devices - shallow junction



Results in fair agreement for devices with the same structure

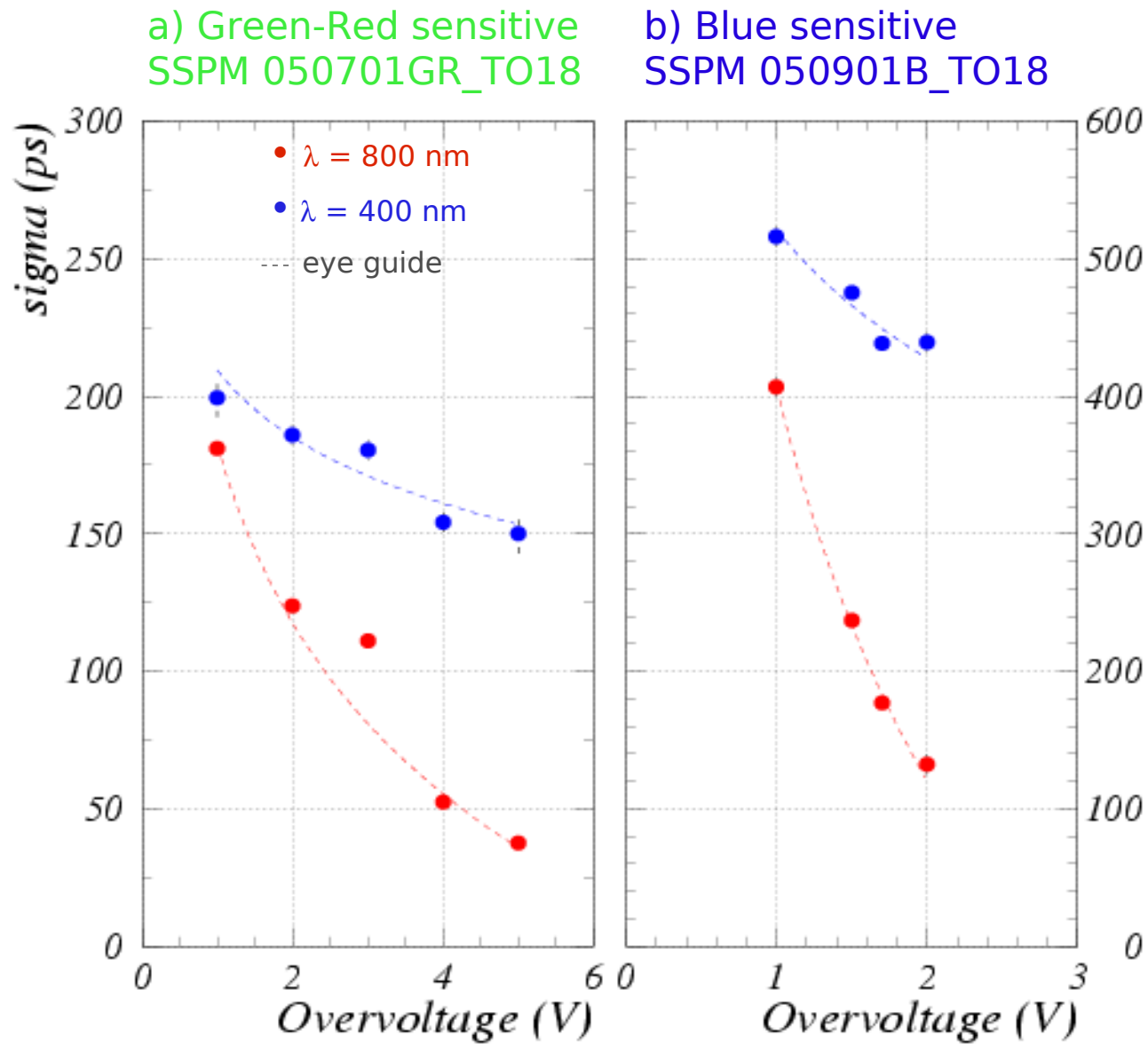
# Hamamatsu - shallow junction



G.Collazuol et al (unpublished)

Suggested  
Operating range

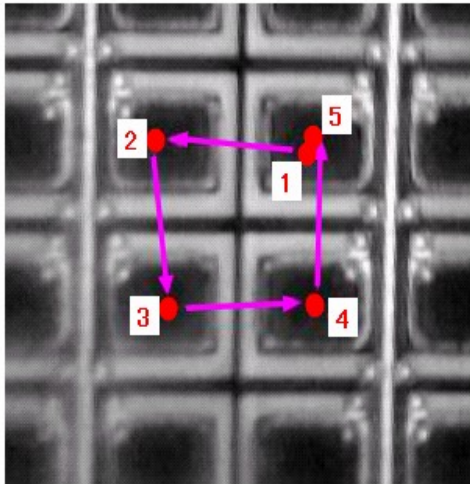
# CPTA/Photonique - deeper structures



Two different structures:  
a) thick n<sup>+</sup>/p  
b) p<sup>+</sup>/n deep junction

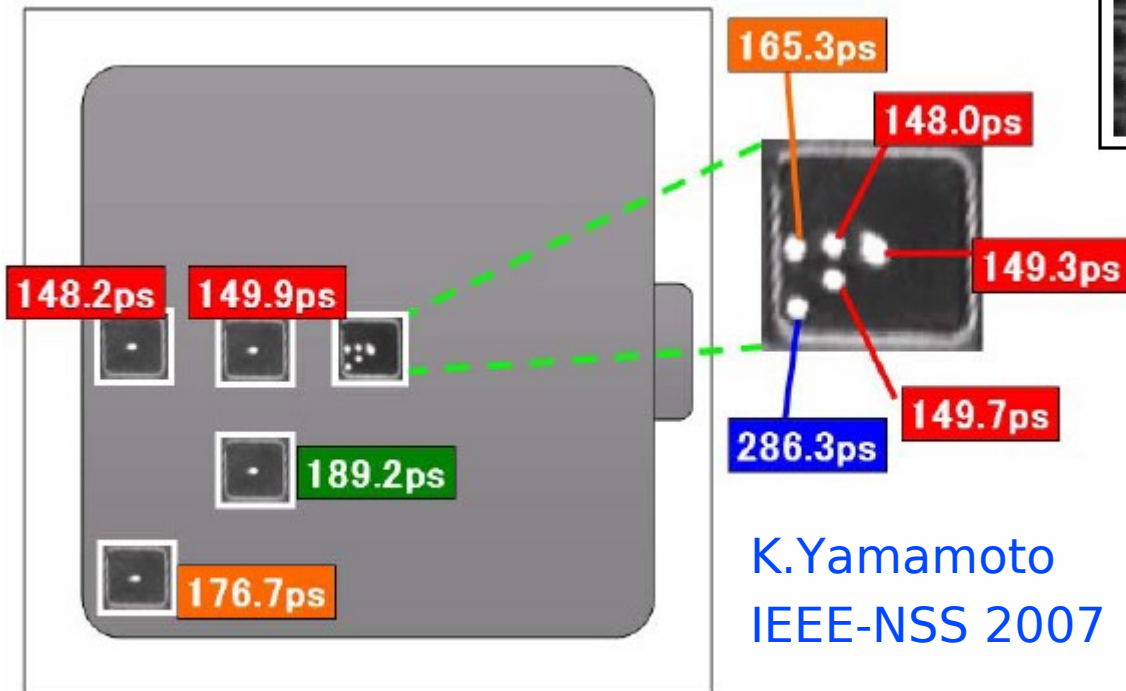
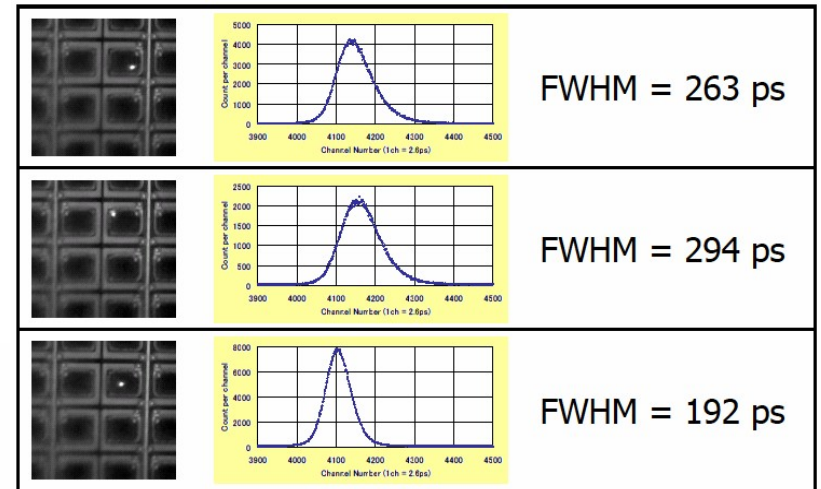
G.Collazuol et al (unpublished)

# SPTR: position dependence



	FWHM (ps)	FWTM (ps)
1	199	393
2	197	389
3	209	409
4	201	393
5	195	383

K.Yamamoto PD07



K.Yamamoto  
IEEE-NSS 2007

Lower jitter if photo-conversion at the center of the cell

Due to higher  $V_{bd}$  at edges  
→ cfr PDE vs position

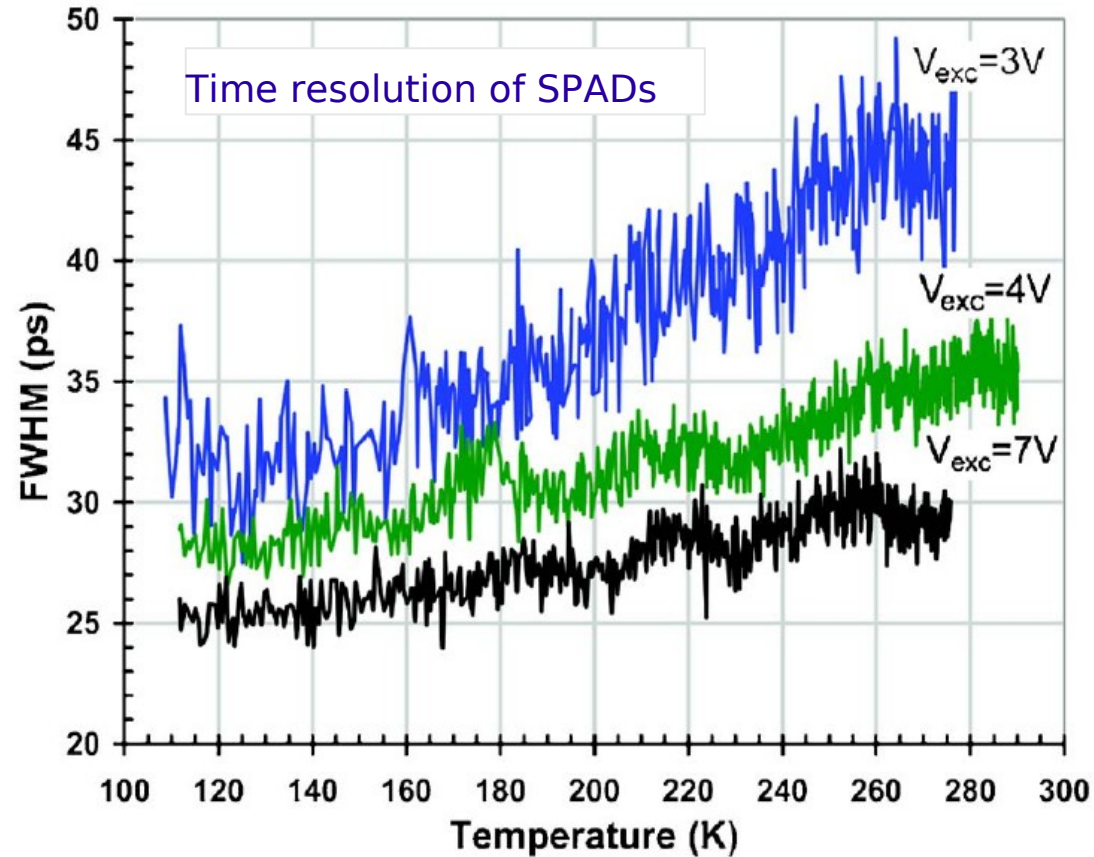
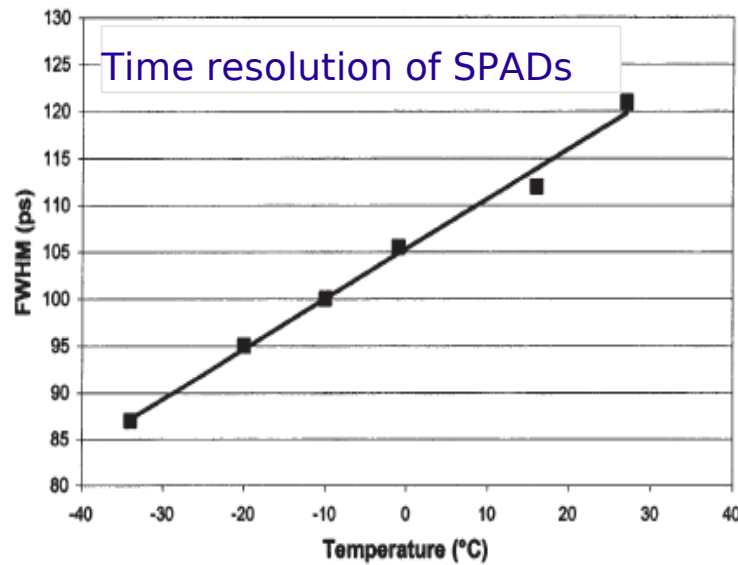
Data include the system jitter (common offset, not subtracted)

# SPTR: timing at low T

## Timing: better at low T

Lower jitter at low T due to higher mobility

(Over-voltage fixed)



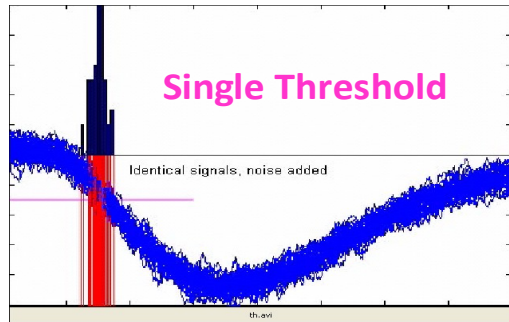
I.Rech et al, Rev.Sci.Instr. 78 (2007)

Fig. 11. FWHM of the SPAD response as a function of the temperature for a 20  $\mu\text{m}$  diameter SPAD at 10 V overvoltage.

S.Cova et al, IEEE TED (2003)



# Timing properties → fast timing devices



## Timing by (single) threshold:

→ time spread proportional to  $\sim 1/\text{rise-time and noise}$

$$\sigma_{time} = \frac{\sigma_{amplitude}}{\frac{df(t)}{dt}}$$

## Timing with optimum filtering:

→ best resolution with  $f'(t)$  weighting function

$$\sigma_{time}^2 = \frac{\sigma_{amplitude}^2}{\int dt \left[ \frac{df(t)}{dt} \right]^2}$$

## Pulse sampling and Waveform analysis:

Sample, digitize, fit the (known) waveform  
→ get time and amplitude

$$\sigma_{time}^2 = \frac{\sigma_{amplitude}^2}{N_{samples} \int dt \left[ \frac{df(t)}{dt} \right]^2}$$

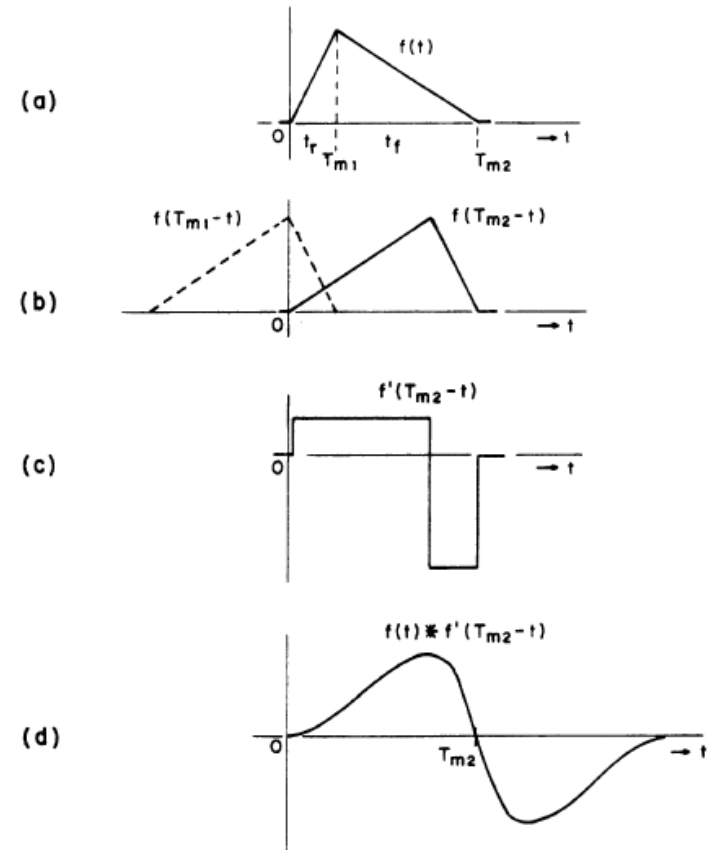


Fig. 7. Optimum filter for timing in presence of white noise (method of derivation).

- (a) signal waveform
- (b) optimum filter for amplitude measurements.
- (c) optimum filter for timing - derivative of (b).
- (d) output waveform.

V.Radeka IEEE TNS 21 (1974)



# SiPM equivalent circuit (detailed model)

Single cell model  $\rightarrow (R_d || C_d) + (R_q || C_q)$

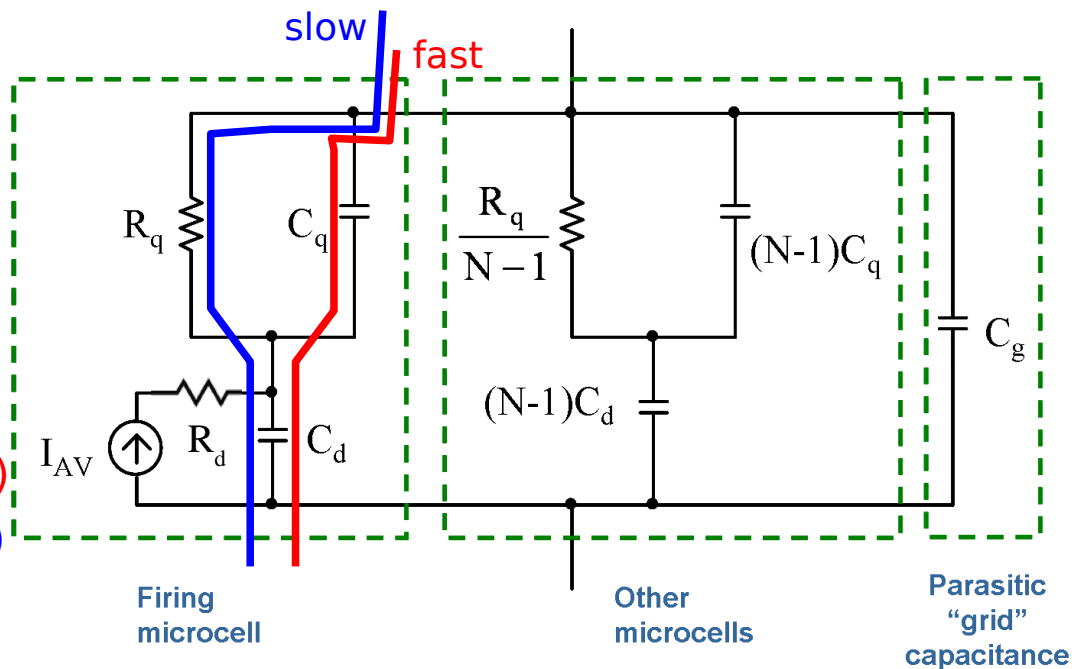
SiPM + load  $\rightarrow (||Z_{cell}) || C_{grid} + Z_{load}$

Signal = **slow** pulse ( $\tau_{d \text{ (rise)}}, \tau_{q \text{-slow (fall)}}$ ) +  
+ **fast** pulse ( $\tau_{d \text{ (rise)}}, \tau_{q \text{-fast (fall)}}$ )

- $\tau_{d \text{ (rise)}} \sim R_d (C_q + C_d)$

- $\tau_{q \text{-fast (fall)}} = R_{load} C_{tot}$  (fast; parasitic spike)

- $\tau_{q \text{-slow (fall)}} = R_q (C_q + C_d)$  (slow; cell recovery)

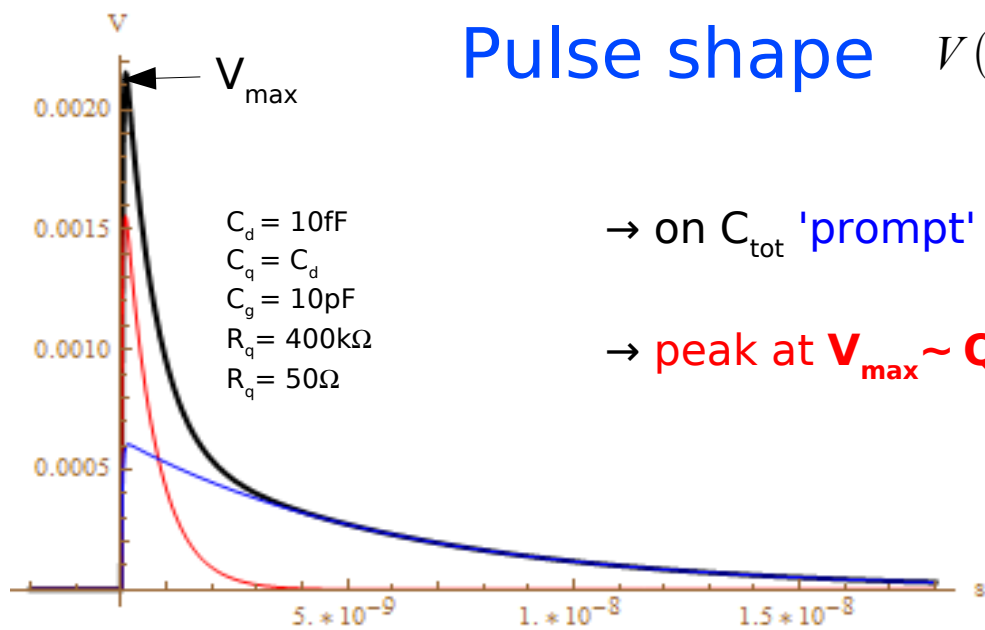


Pulse shape

$$V(t) \simeq \frac{Q}{C_q + C_d} \left( \frac{C_q}{C_{tot}} e^{-\frac{t}{\tau_{FAST}}} + \frac{R_{load}}{R_q} \frac{C_d}{C_q + C_d} e^{-\frac{t}{\tau_{SLOW}}} \right)$$

$\rightarrow$  on  $C_{tot}$  'prompt' charge  $Q_{fast} = Q \frac{C_q}{(C_q + C_d)}$

$\rightarrow$  peak at  $V_{max} \sim Q_{fast} / C_{tot}$  is independent of  $R_{load}$



# Optimizing signal shape for timing

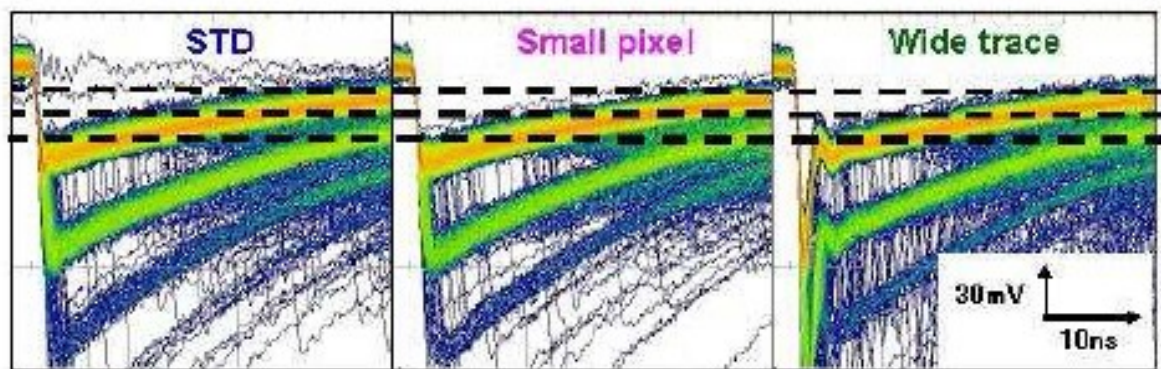
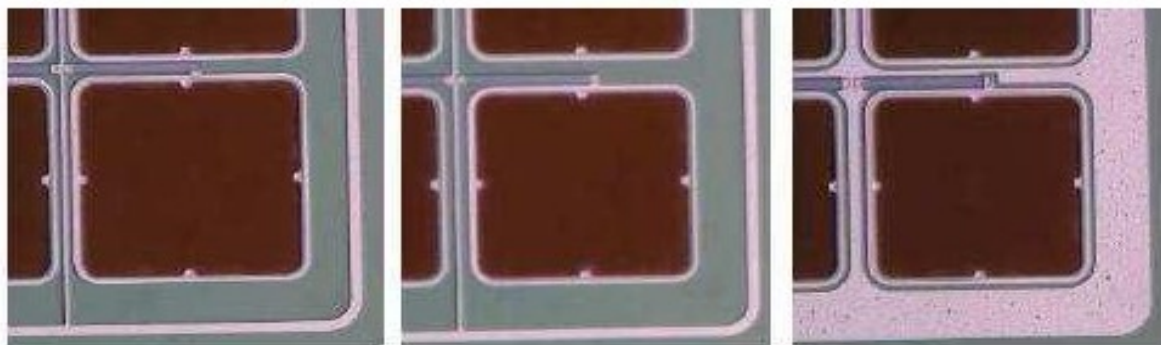
Single cell model  $\rightarrow (R_d || C_d) + (R_q || C_q)$

SiPM + load  $\rightarrow (||Z_{cell}) || C_{grid} + Z_{load}$

Signal = **slow** pulse ( $\tau_{d \text{ (rise)}}, \tau_{q\text{-slow} \text{ (fall)}}$ ) +  
+ **fast** pulse ( $\tau_{d \text{ (rise)}}, \tau_{q\text{-fast} \text{ (fall)}}$ )

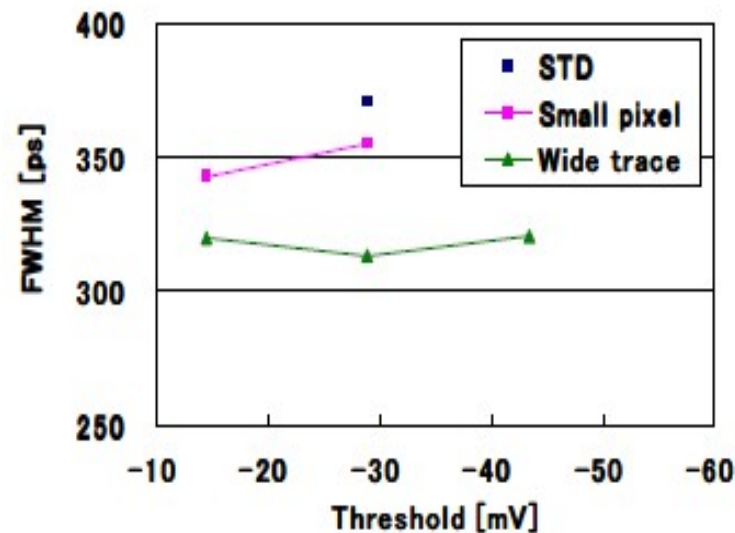
- $\tau_{d \text{ (rise)}} \sim R_d (C_q + C_d)$
- $\tau_{q\text{-fast} \text{ (fall)}} = R_{load} C_{tot}$  (fast; parasitic spike)
- $\tau_{q\text{-slow} \text{ (fall)}} = R_q (C_q + C_d)$  (slow; cell recovery)

High  $C_q$  improves timing performances



Yamamura et.al. at PD09

1mm $\square$ 100um (GAIN=2.4E+06, 25 $^{\circ}$ C)  
Timing resolution of 1p.e. vs threshold



# ASICs for SiPM signal readout (QDC/TDC)

W.Kucewicz "Review of ASIC developments for SiPM signal readout" - talk at CERN 11-2-2011

Chip Name	Measured quantity	Application	Input configuration	Technology
FLC_SiPM	Pulse charge	ILC Analog HCAL	Current input	CMOS 0,8 $\mu\text{m}$
MAROC	Pulse charge, trigger	ATLAS luminometer	Current input	SiGe 0,35 $\mu\text{m}$
SPIROC	Pulse charge, trigger, time	ILC HCAL	Current input	SiGe 0,35 $\mu\text{m}$
NINO	Trigger, pulse width	ALICE TOF	Differential input	CMOS 0,25 $\mu\text{m}$
PETA	Pulse charge, trigger, time	PET	Differential input	CMOS 0,18 $\mu\text{m}$
BASIC	Pulse height, trigger	PET	Current input	CMOS 0,35 $\mu\text{m}$
SPIDER (VATA64-HDR16)	Pulse height, trigger, time	SPIDER RICH	Current input	
RAPSODI	Pulse height, trigger	SNOOPER	Current input	CMOS 0,35 $\mu\text{m}$

# ASICs for SiPM signal readout (QDC/TDC)

W.Kucewicz - CERN 11-2-2011

Chip Name	# of channels	Digital output	Power supply	Area [sqr mm]	Dynamic range	Input resistance	Timing jitter	Year
FLC_SiPM	18	n	5V (0,2W)	10			-	2004
MAROC2	64	y	5 V	16	80 pC	50 $\Omega$		2006
SPIROC	36	y	5 V	32				2007
NINO	8	n	(0,24W)	8	2000 pe	20 $\Omega$	260 ps	2004
PETA	40	y	(1,2W)	25	8 bit		50 ps	2008
BASIC	32	y	3,3 V	7	70 pC	17 $\Omega$	~120 ps	2009
SPIDER (VATA64-HDR16)	64	n		15	12 pC			2009
RAPSODI	2	y	3,3 V (0,2W)	9	100 pC	20 $\Omega$	-	2008

- Only a few of the suitable for low light intensity
- None is optimized for timing performances

# ASICs for waveform sampling

Best performances for timing with [Waveform Sampling](#)  
 → allowing proper processing of the peculiar SiPM signal  
 (handling fast/slow trailing front, after-pulses, cross-talk, ...)

	Hawaii	Varner		Saclay/Orsay	Delagnes/	Breton		PSI	S.Ritt	This proposal
	Blab1	Lab1-2	Lab 3	Hamac	Matacq	Sam	Planned	DRS3	DRS4	
Sampling	100 MHz-6 GHz		20 MHz-3.7GHz	40 MHz	0.7-2.5 GHz	0.7-2.5 GHz	10 GHz	10 MHz-5 GHz	5 GHz	10-20 GHz
Bandwidth (3db)	300 MHz		900 MHz	50 MHz	200-300 MHz	300 MHz	650 MHz	450 MHz	950MHz	> 1.5 GHz
Channels		1	8	9	8	1	2	12 6 2 1	8 4 2 1	4 16
Triggered mode	Yes		Common stop		Yes			Common stop	Common stop	Channel trigger
Resolution	10 bit			13.3 bit	13.4 bit	11.6 bit		11.6 bit	11.5 bit	8-10-bit
Samples	128 rows of 512	256	256	144	2520	256	2048	1024-12288	1024-8192	256
Clock			33 MHz	40 MHz	100 MHz				fsamp/2048	20-40 MHz
Max latency	560 us	2.2ms	50us							
Input Buffers	Yes			Yes	Yes	Yes	No	No	No	No
Differential inputs	No	No	No	Yes	Yes	Yes		Yes	Yes	Yes
Input impedance	50 Ohms	50 Ohms	50 Ohms Ext	10 MOhm/3pF	50 Ohms				11pF	50 Ohms
Readout clock	500 MHz			5 MHz	5 MHz	16 MHz		33 MHz	33MHz	500 MHz
Locked delays	Ext DAC	Ext DAC	Ext DAC			Yes		Ext PLL	Int PLL	Int PLL
On-chip ADC	12-b +500MHz TDC			No		No		No	No	Yes
R/W simultaneous	Yes			Yes		No		No	Yes	No
Power/ch	15mW/1.6W			36 mW	250-500 mW	150 mW		2-8mW	7.2mW at 2GS/s	
Dynamic range	1mV/1V			0.26mV/2.75V	175 uV-2V	0.65mV-2 V		0.35mV/1.1V	.35mV/1V	1V
Xtalk	Inter-rows 0.1%		10%			0.30%		< 0.5%		
Sampling jitter			4.5ps			25ps			6ps	?
Power supplies	-tbd/+2.5	-tbd/2.5V	-tbd/2.5V	-1.7/3.3V				2.5V	2.5V	1.2V
Process	TSMC .25	TSMC .25	TSMC .25	HP/DMILL .8	AMS .8	AMS .35	AMS .18	UMC .25	UMC .25	IBM .13
Chip area	5.25 mm2	10 mm2	2.5mm2	19.8mm2	30mm2			25mm2		1mm2/ch
Temp coeff	0.2%/°C		0.2%/°C					5e-5/°C	25ppm/°C	
Cost/channel	500\$/40	10\$/2k							10-15\$	

Table by J.F.Genat "A 20 GS/s sampling ASIC in 130nm CMOS technology" - TWEPP 2010



# Conclusions

- **Breakdown V** decreases non linearly with T, as expected  
→ better stability against T variations than at T room
- **Dark rate** reduced by several orders of magnitude  
→ tunneling mechanism(s) below ~200K
- **After-pulsing** at % level down to 100K; blow up below 100K
- **PDE** vs T: modulation up to  $\pm 50\%$  wrt T room  
→ PDE decr. as T 300K  $\rightarrow$  250K, incr. as T 250K  $\rightarrow$  120K, then freeze-out
- **PDE** vs  $\lambda$ : PDE peaks at lower  $\lambda$  as T decreases
- **Cross-talk and Gain** (detector capacity) are independent of T (at fixed  $\Delta V$ )
- **Timing** resolution improves at low T

## Properties at low T

SiPMs behave very well at low T, even better than at room T

In the range **100K < T < 200K SiPM perform optimally;**

→ excellent **alternatives to PMTs in cryogenic applications** (eg Noble liquids)

→ Optimization for low T (quenching R, ...)

## Timing Properties

- Intrinsically **ultra-fast** devices:  
time to breakdown and jitter < 100ps
- Not negligible **non-gaussian tails** (ns) for longer wavelengths
- Smaller jitter for blue light than red (depends on the structure)
- Peculiar **signal shape**  
→ device optimization for timing  
→ waveform sampling superior to CFT/ADC/TDC readout

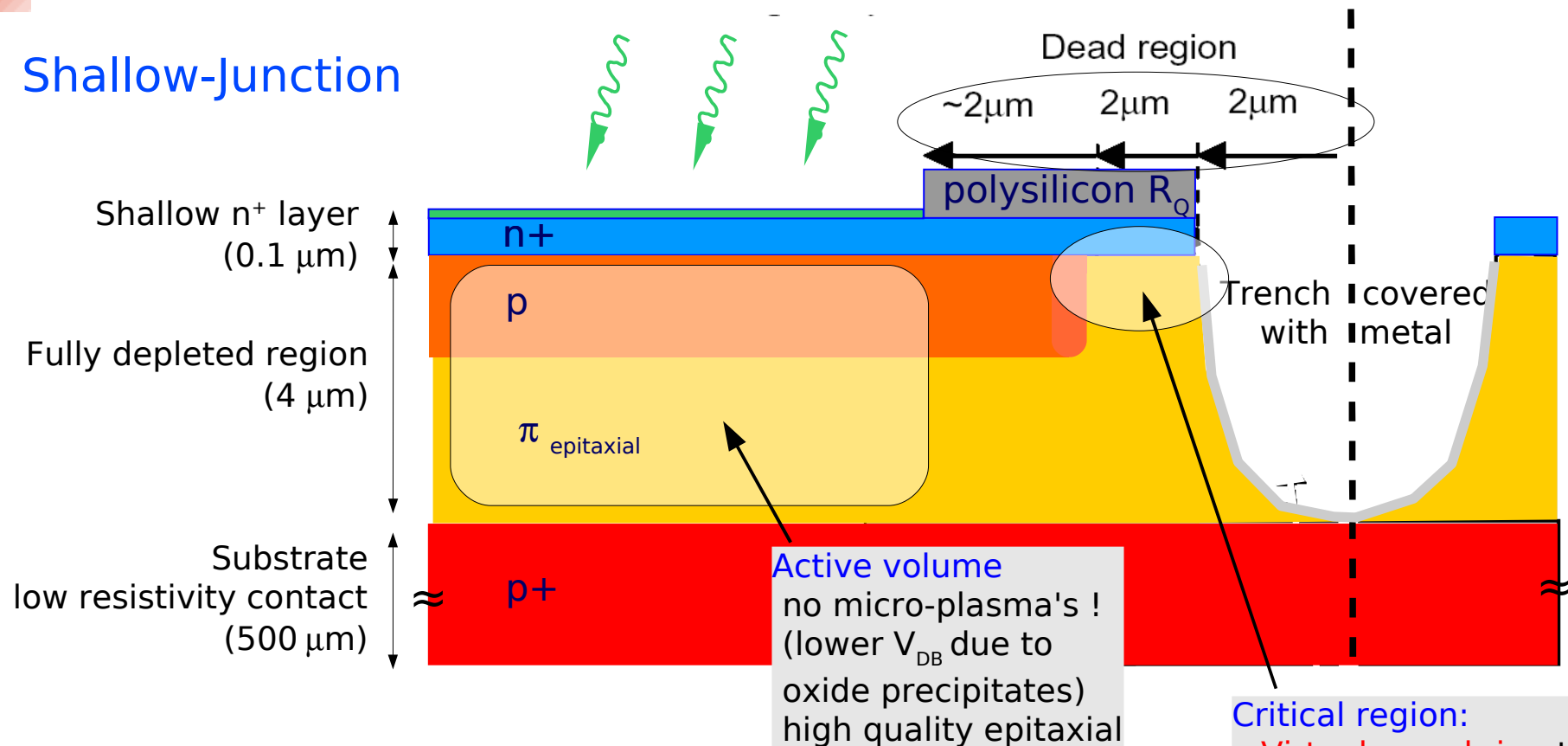


# Additional material



# Zoom of the cell: SiPM technology at IRST

## Shallow-Junction



## Optimization for the blue light (420nm)

- $n^+$  on  $p$  abrupt junction structure
- Anti-reflective coating (ARC) optimized for  $\lambda \sim 420\text{nm}$
- Very thin (100nm)  $n^+$  layer: "low" doping  $n^+$  layer  
→ minimize Auger and SHR recombination
- Thin high-field region: "high" doping  $p$  layer (limited by tunneling breakdown)  
→ fixes  $V_{BD}$  junction well below  $V_{BD}$  at edge
- $R_q$  by doped polysilicon
- Trenches for optical insulation (low cross-talk)
- Fill factor: 20% - 80%

C.Piemonte NIM A 568 (2006) 224



Low T

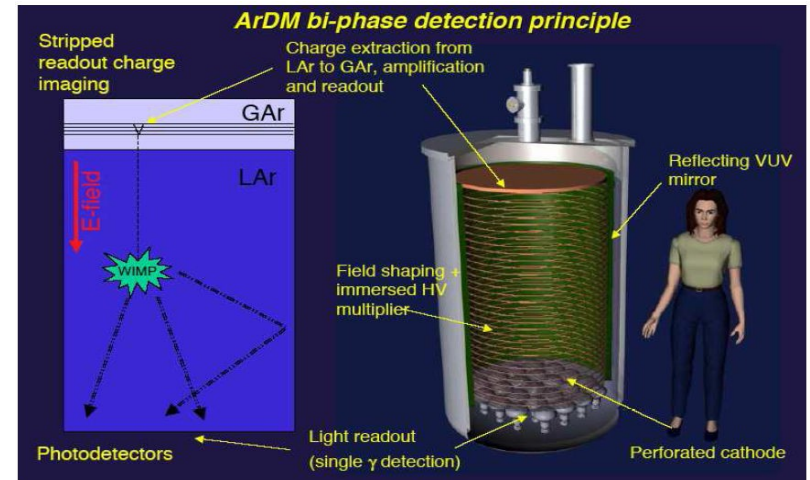
# Applications w/ SiPM in cryogenic environments

Secondary scintillation from noble liquids generated by thick GEM (THGEM) for applications in neutrino physics, dark matter searches and PET

ArDM: Two-phase Ar detector using THGEM for DM search  
[A.Rubbia et al., J. Phys. Conf. Ser. 39(2006)129]

!!! Need recording both ionization and scintillation with a threshold of  $\leq 10\text{keV}$  (200 electrons)

A.Buzulutskov et al.  
Vienna Conference VCI 2010 and  
arXiv:1005.5216v1



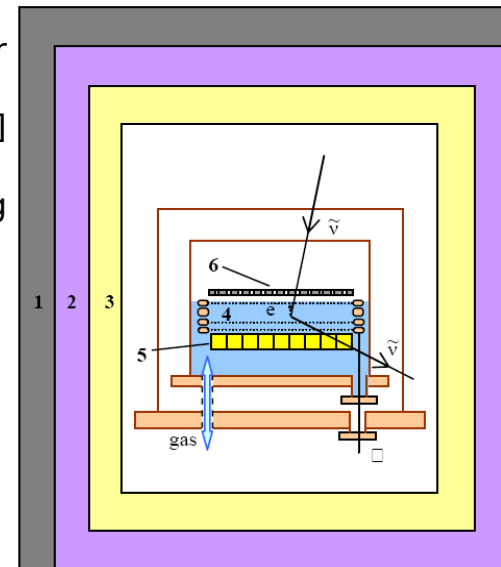
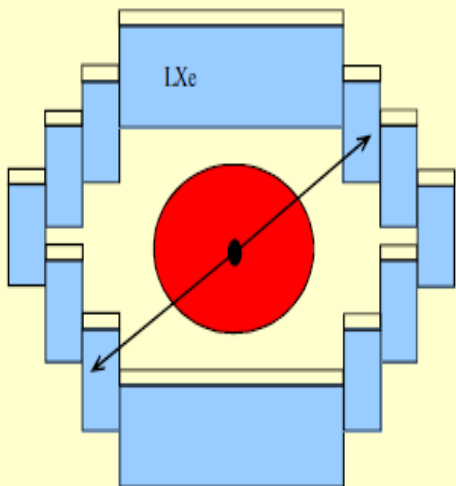
NIR emission spectrum of pure Ar (due to Ar I atomic lines) from avalanche scintillations at 750 Torr, gain  $\sim 30$ , yield  $\sim 1\text{ph/e}$ . [M.M.Fraga et al. IEEE Trans.Nucl.Sci. 47(2000)933]

Two-phase Ar and Xe detectors using GEM/THGEM for coherent neutrino-nucleus scattering  
[ITEP & Budker INP: Akimov et al. JINST 4 (2009) P06010]

!!! Need single electron counting

GEM-based two-phase Xe avalanche detector for PET:  
3D liquid TPC recording 511 keV  $\gamma$ -rays  
→ obtain superior ( $\sim 1\text{mm}$ ) spatial resolution.  
[Budker INP: CRDF grant RP1-2550 (2003)]

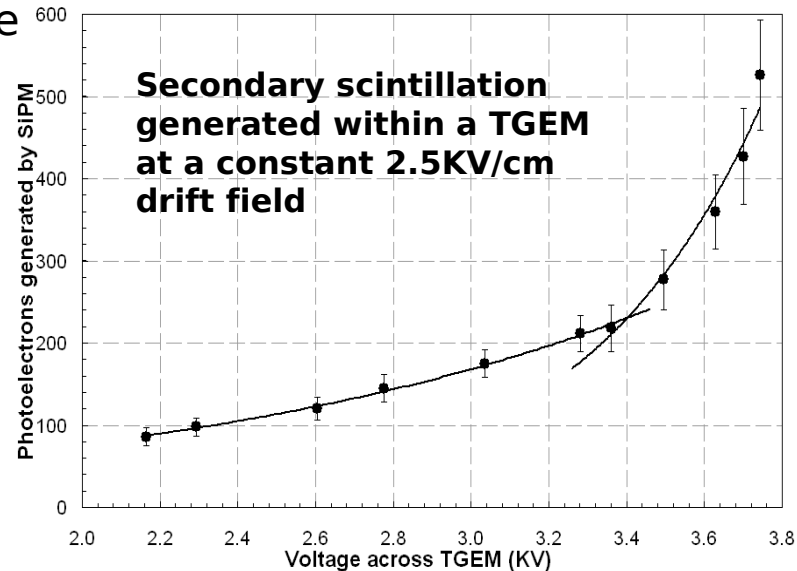
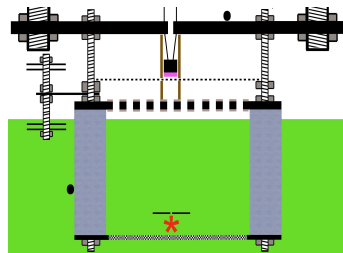
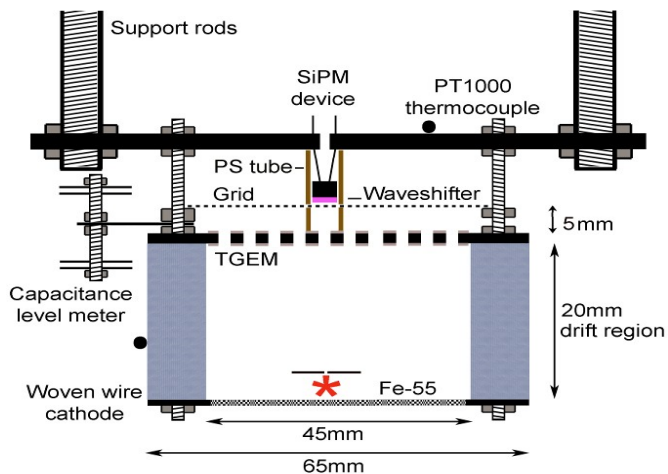
Need for Xe detector with 3D readout of both ionization and scintillation with a threshold of  $> 100\text{ keV}$  (2000 electrons)



# Applications w/ SiPM in cryogenic environments

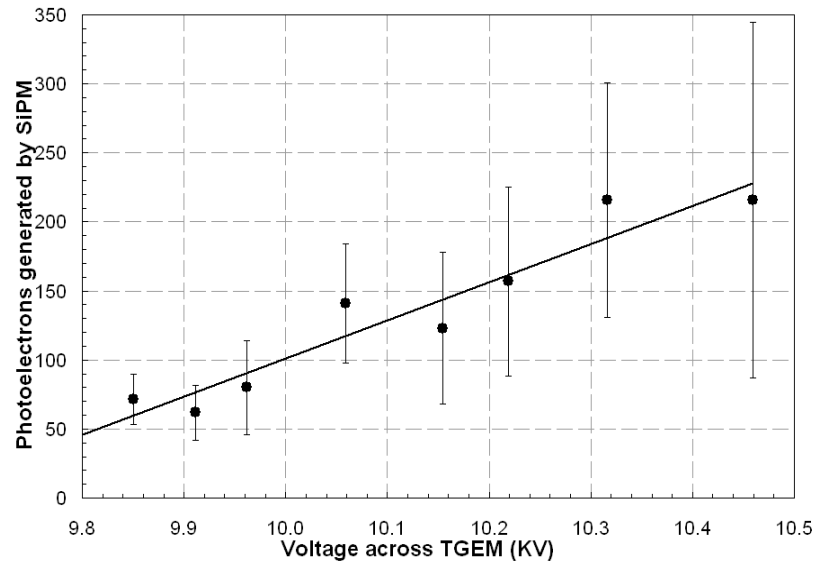
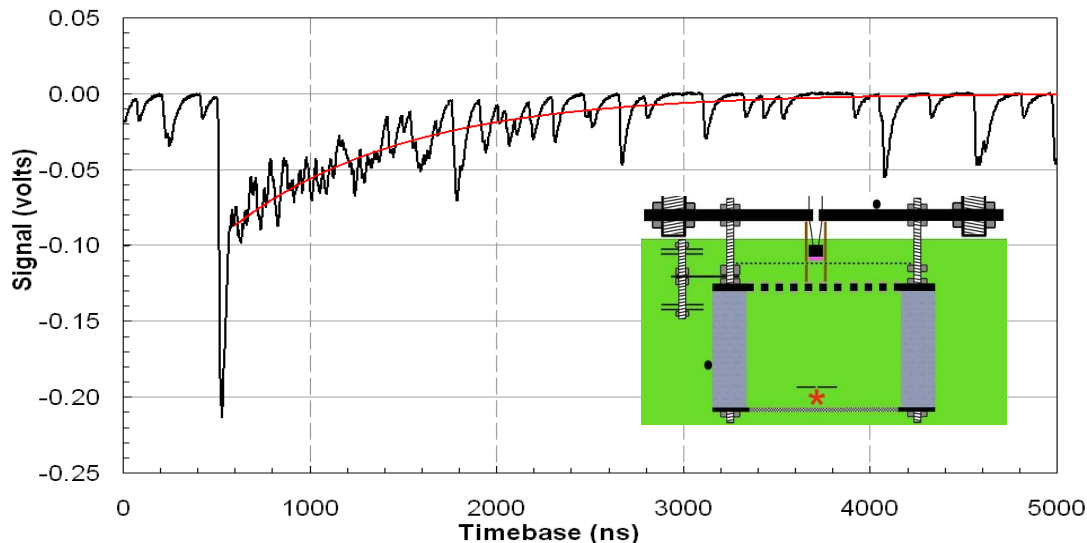
P.K.Lightfoot, et al.  
 J. Phys.: Conf. Ser. 179 (2009) 012014

## Electroluminescence from the cold gas phase of a double phase Ar system



see talk by N.McConkey at this conference !!!

## Electroluminescence from LAr



128nm VUV light produced within the TGEM holes was then incident on an immersed SiPM device coated in the wavershifter tetraphenyl butadiene (TPB), the emission spectrum peaked at 460nm in the high quantum efficiency region of the device

# Silicon properties at low T: higher mobility

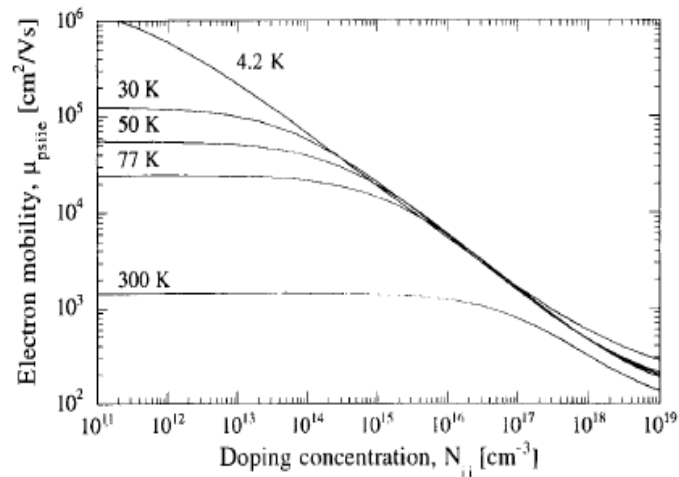


FIGURE 1.16. Calculated electron mobility due to phonon and ionized impurity scattering mechanisms. The five plots correspond to  $T = 300, 77, 50, 30,$  and  $4.2$  K.

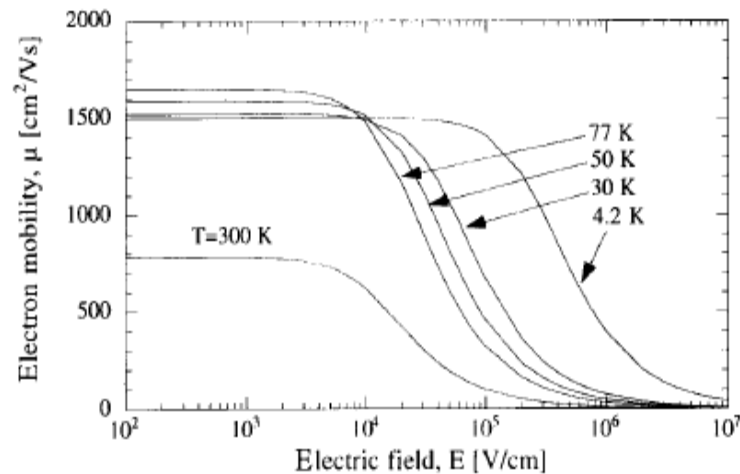


FIGURE 1.17. Calculated electron mobility, due to phonon, ionized impurities, and velocity saturation effects, as a function of the electric field for five temperatures;  $N_{ii} = 10^{17} \text{ cm}^{-3}$ .

# Silicon prop't's at low T: carriers freeze-out

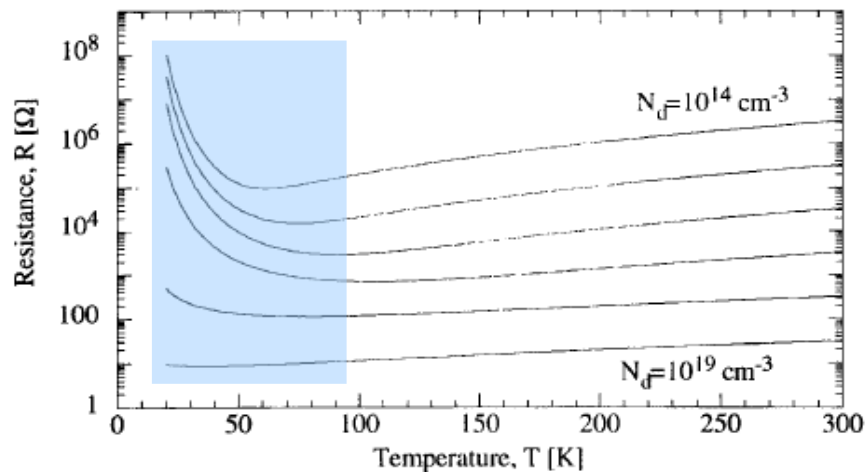


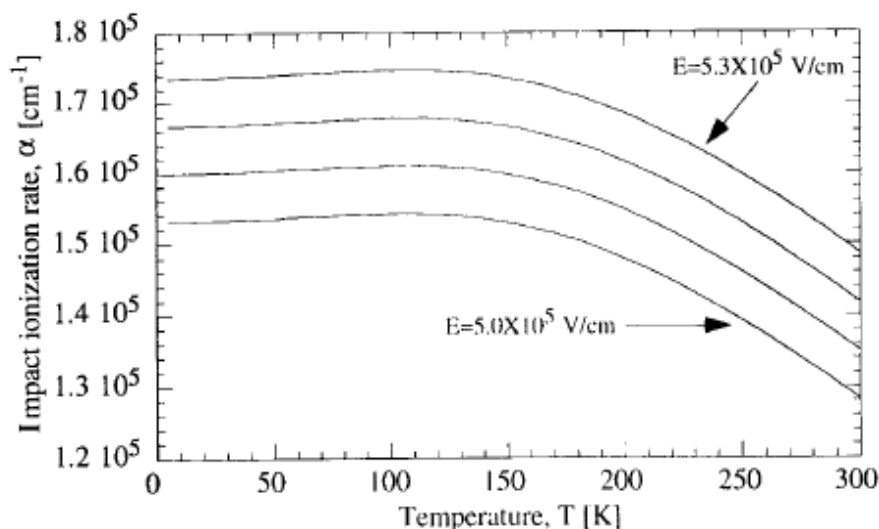
FIGURE 1.14. Calculated electrical resistance of a silicon slab of  $(W/L) = 20/50 \mu\text{m}$  and depth of  $1 \mu\text{m}$  for different doping concentration levels.

For  $T < 100$  K, the ionized impurities act as shallow traps (provided the impurity doping concentration below of  $10^{18}$  atoms/cm<sup>2</sup>) and carriers begin to occupy these shallow levels.

For  $T < 30$  K, practically no carriers remain in the bands

Plots from Guterrez, Dean, Claeys - "Low Temperature Electronics: Physics, Devices, Circuits and Applications", Academic Press 2001

# Silicon propt's at low T: impact ionization



For  $T < 77\text{K}$  no data are available  $\rightarrow$  modeling is quite difficult...

FIGURE 1.43. The impact ionization rate  $\alpha$  as a function of temperature  $T_A$  with the electric field  $E$  as a parameter calculated from Okuto and Crowell's (85) model.

# Silicon propt's at low T: absorption length

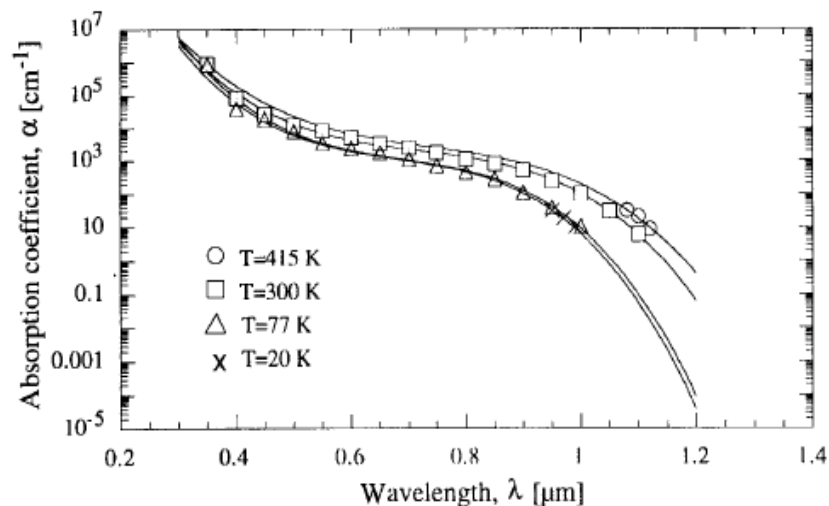


FIGURE 1.53. Experimental (symbols) and fitted (lines) absorption coefficient  $\alpha$  of silicon at  $T = 415, 300, 77,$  and  $20\text{ K}$  [replotted from Rajkanan *et al.* (109)].

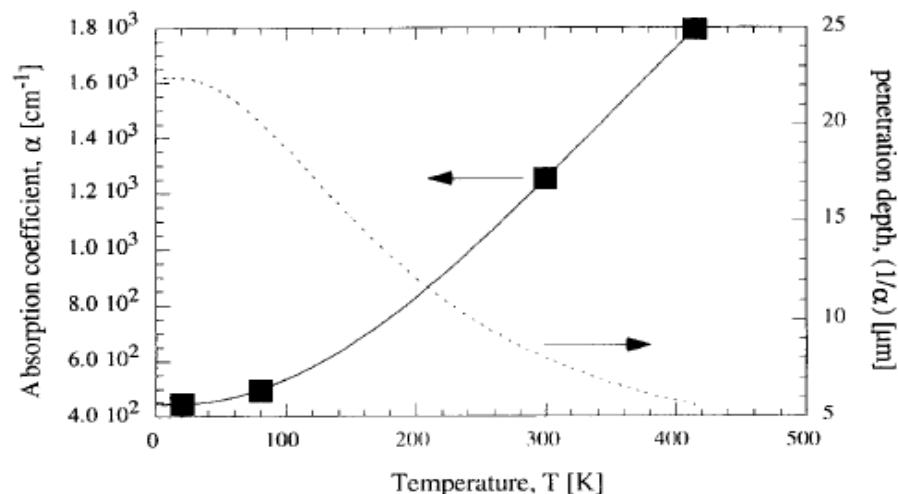


FIGURE 1.54. Measured absorption coefficient  $\alpha$  (■) (101) and fitted  $\alpha$  (solid line) versus temperature  $T$ . On the right axis the fitted penetration depth ( $1/\alpha$ ) is also shown.

# Avalanche breakdown vs T

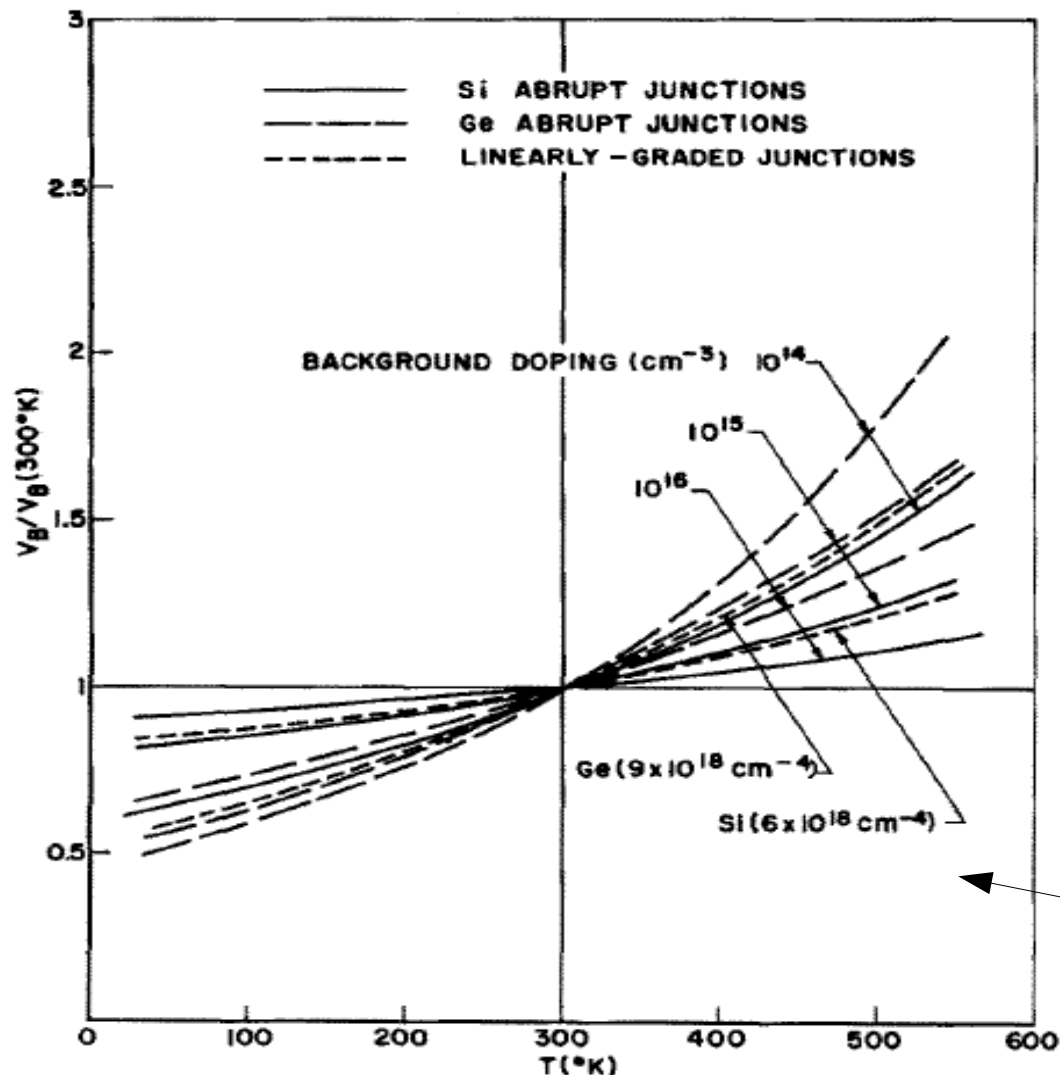


Fig. 4. Breakdown voltage vs temperature for Si and Ge  $p$ - $n$  junctions.  $V_B(300^\circ\text{K})$  is 2000, 330, and 60 V for Si and 950, 150, and 25 V for Ge for dopings of  $10^{14}$ ,  $10^{15}$ , and  $10^{16}\text{ cm}^{-3}$  respectively. The linear-graded junctions have  $V_B(300^\circ\text{K})$  the same as those for doping of  $10^{15}\text{ cm}^{-3}$ .

Avalanche breakdown  $V$  is expected to show a **non linear dependence on T** (depending of the junction type and doping concentration)

Breakdown  $V$  decreasing with  $T$  due to increasing mobility

NOTE: in freeze-out regime Zener (tunnel) breakdown could be relevant.  $\rightarrow$  negative Temperature coefficient (increasing with decreasing  $T$ )

Crowell and Sze

More recent model by Crowell and Okuto after Shockley, Wolff, Baraff, Sze and Ridley.



# p-n junction characteristics: forward bias

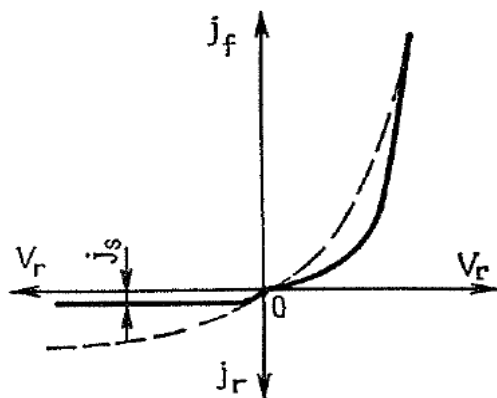
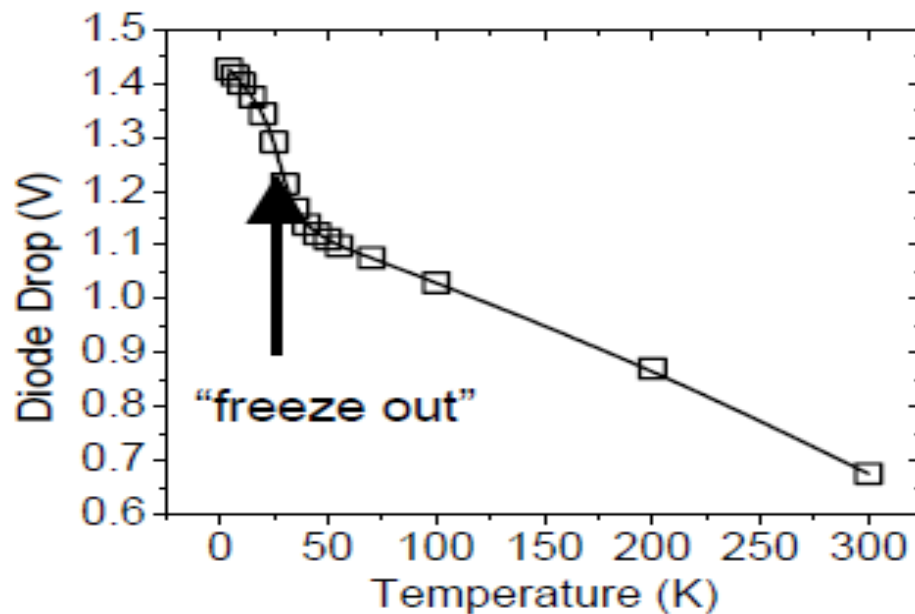
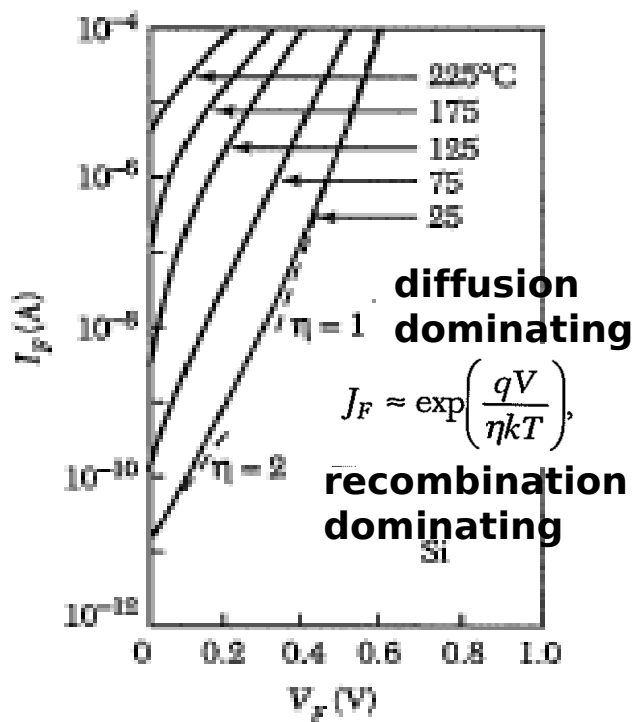
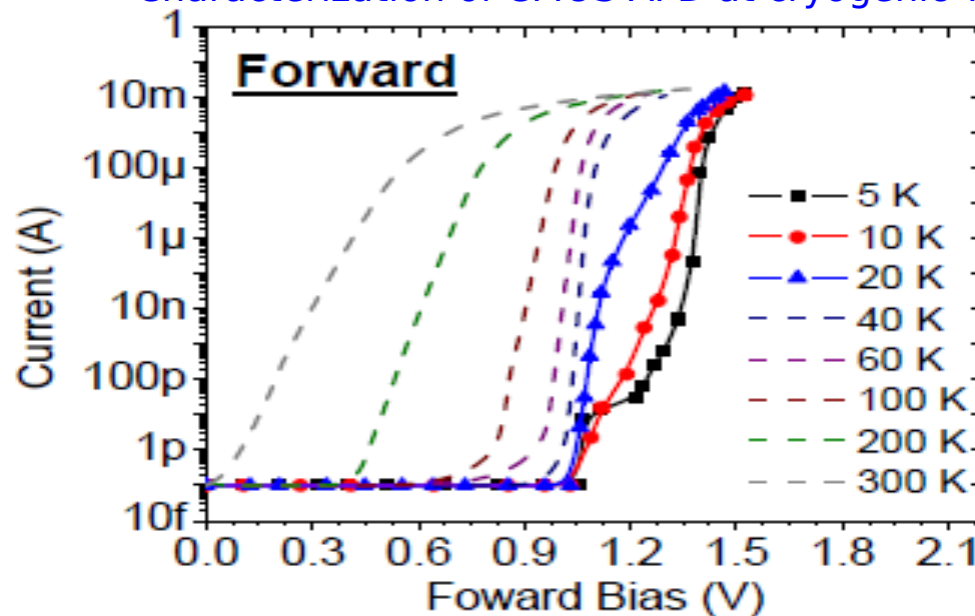


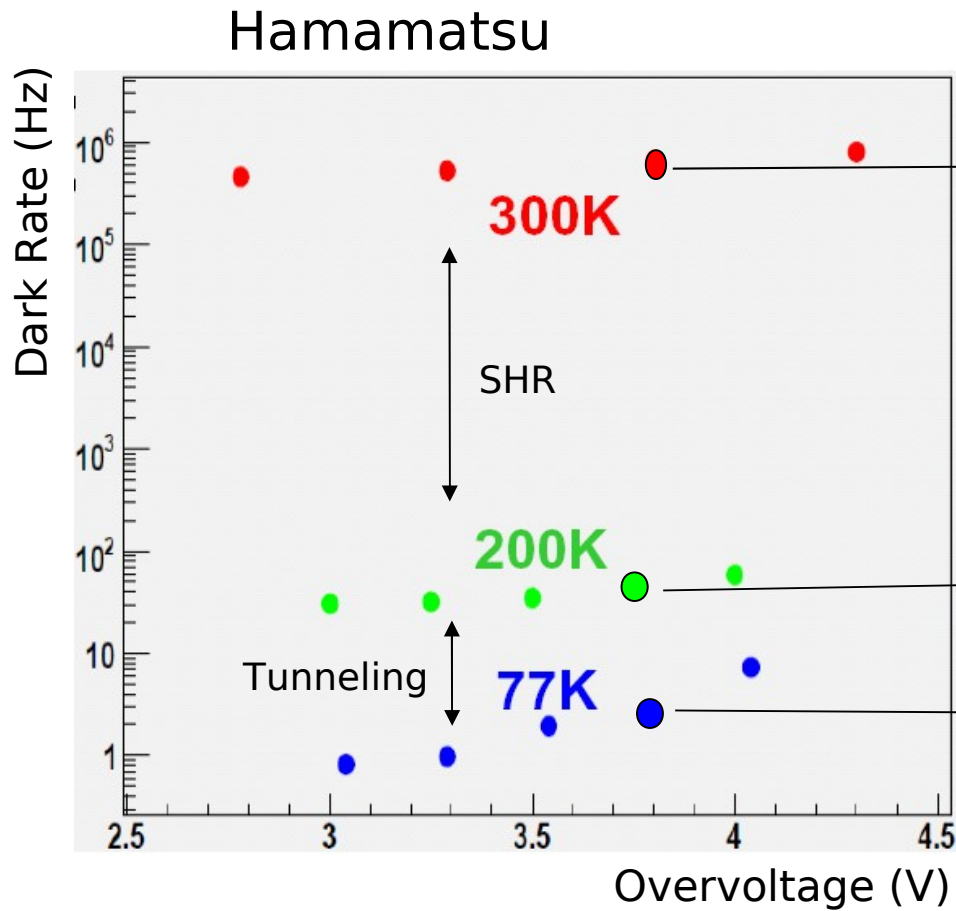
Fig. 8.16. The current-voltage characteristic of a *pn* junction

E.Johnson (RMD) at IEEE 2009  
 "Characterization of CMOS APD at cryogenic T"

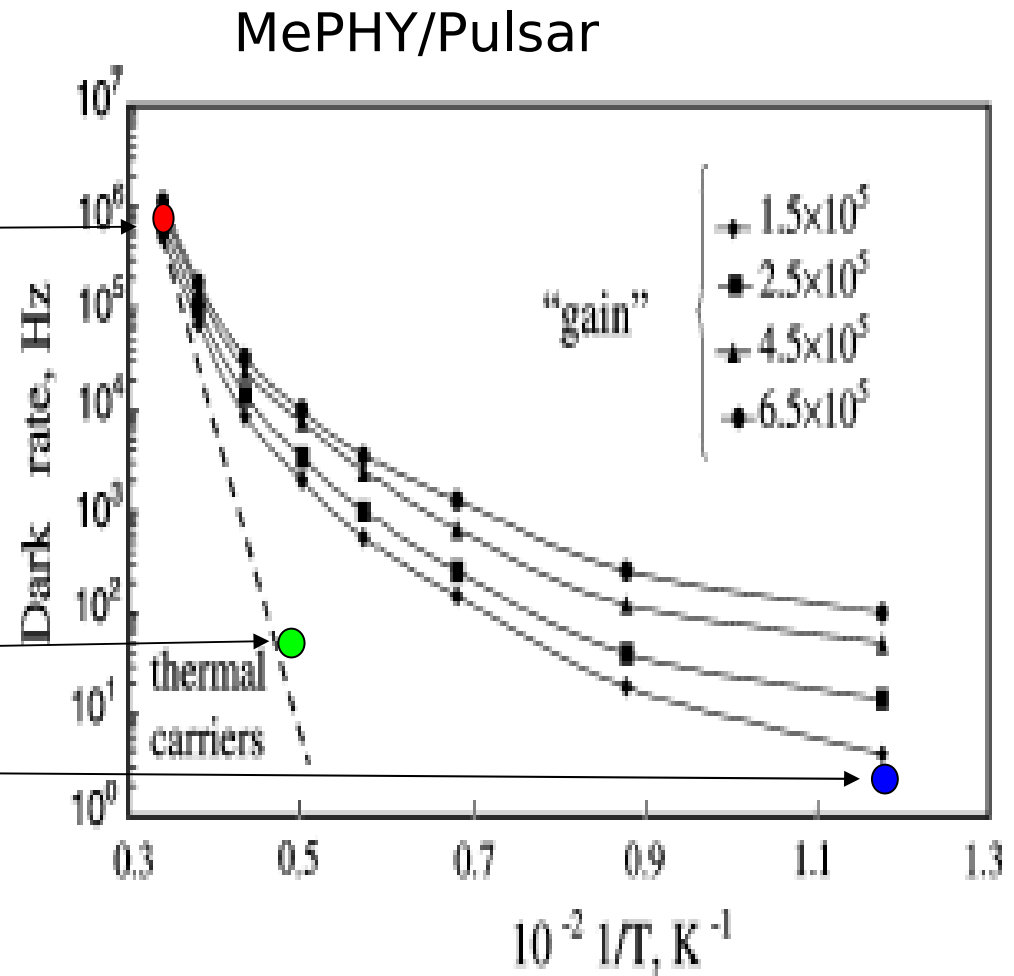


Sze - "Semiconductor devices"

# Dark Rate



H.Otono - PD07



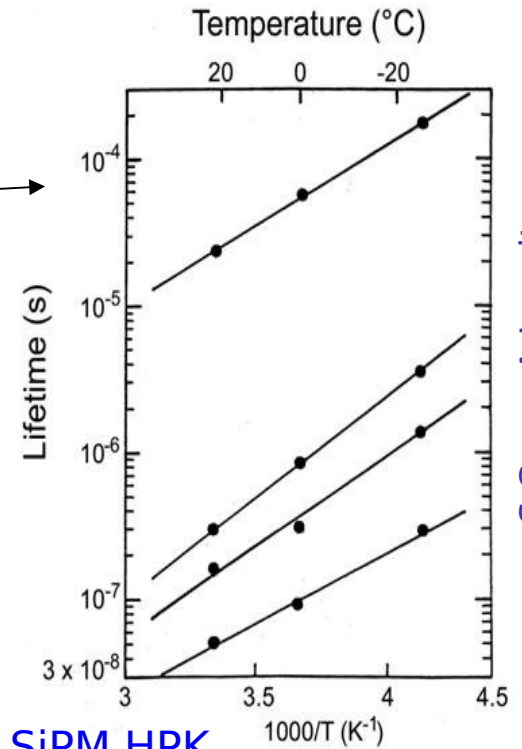
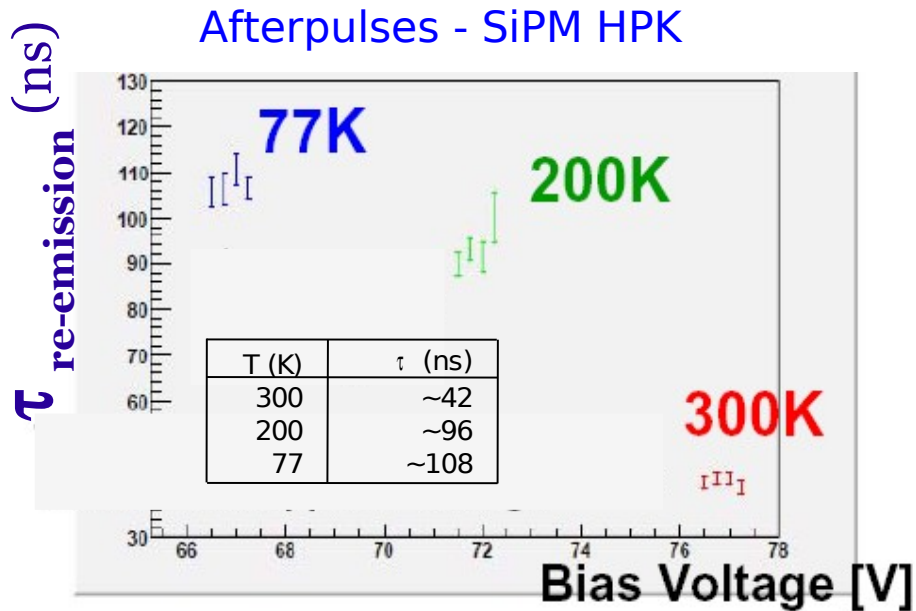
Dolgoshein et al, NIM A 442 (2000)

Electric field engineering and silicon quality make huge differences in dark noise as a function of T

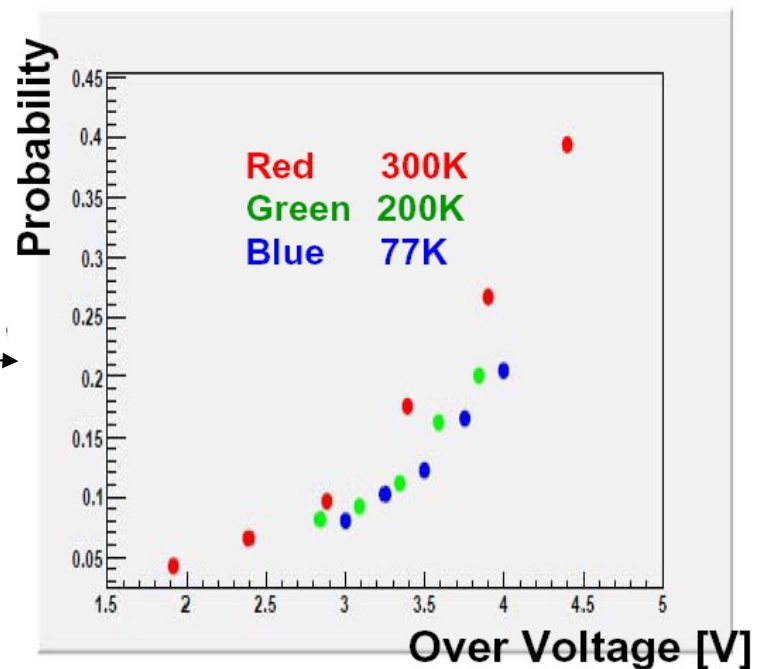
# T dependence: after-pulse, cross-talk

**After-pulses:** increases at low T

Trap lifetime decreases as T increases



Crosstalk - SiPM HPK



**Crosstalk:** decreases at low T

Observed slight reduction at low T

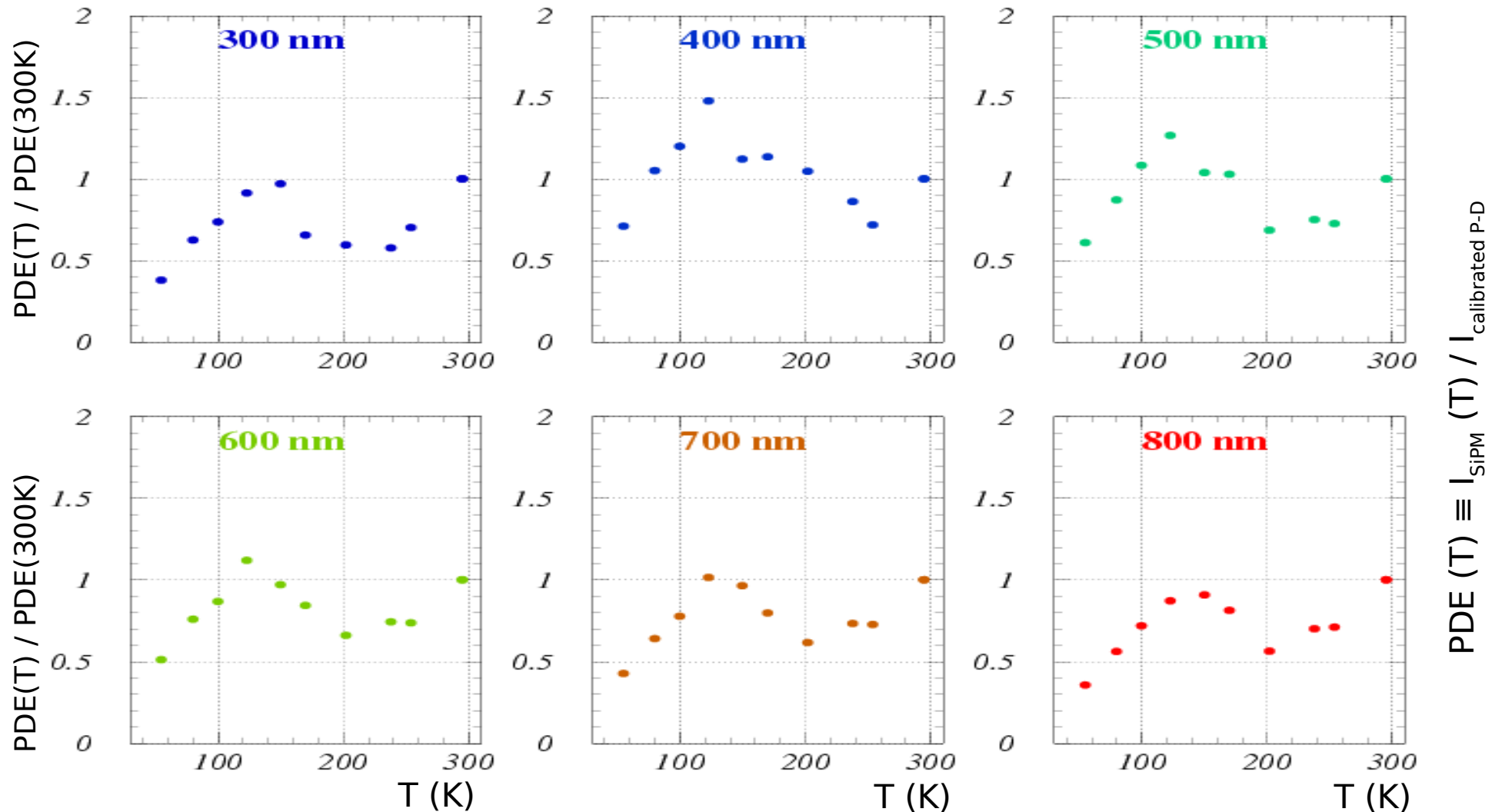
(I guess: due to lower PDE for long wavelength photons which dominate the carrier luminescence spectrum)

H.Otono - PD07

S.Cova, A.Lacaita,  
G.Ripamonti, IEEE EDL (1991)

# PDE at various $\lambda$ - T scan ( $\Delta V = 2V$ )

PDE dependence on T at fixed gain. Normalization with calibrated photo-diode current and with PDE at T=300K (double ratio)



$$PDE(T) \equiv I_{SiPM}(T) / I_{calibrated P-D}$$

- **shape** similar at different  $\lambda$   $\rightarrow$  **related to properties of multiplication /recombination**
- **lower efficiency** at low T for longer  $\lambda$   $\rightarrow$  **due to absorption length  $\sim 1/T$  (with constant depletion width)**

# PDE (SPAD/APD devices)

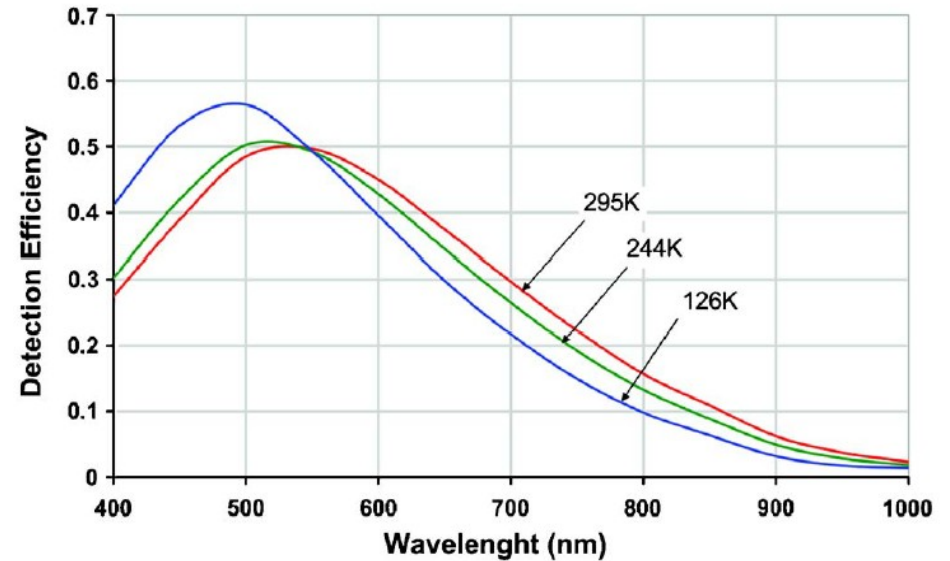
## PDE dependence on T (Over-voltage fixed)

Combination of various effects:

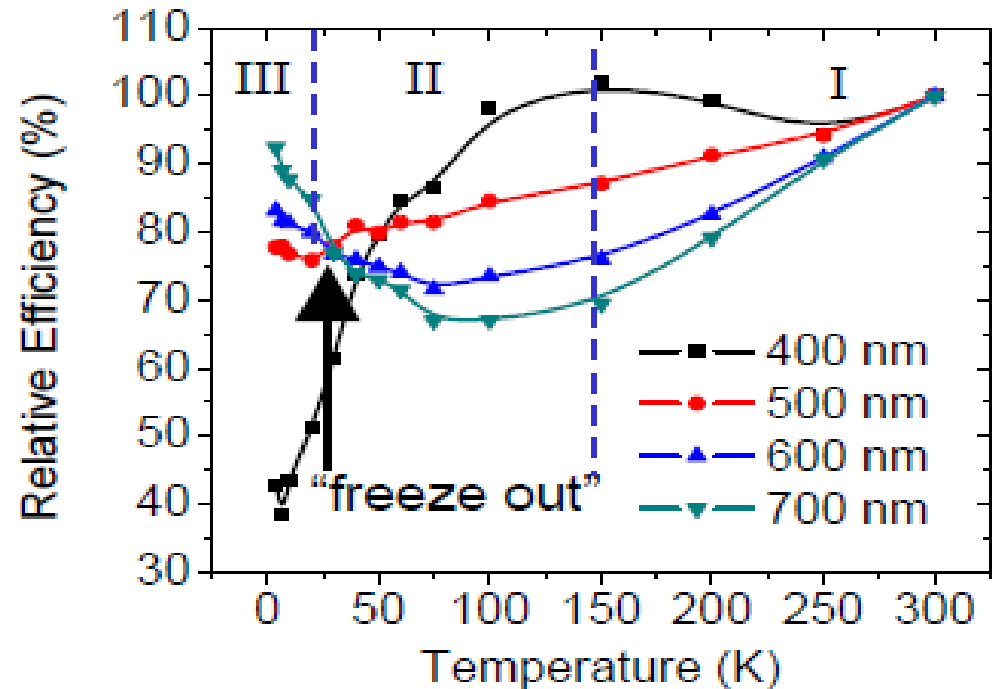
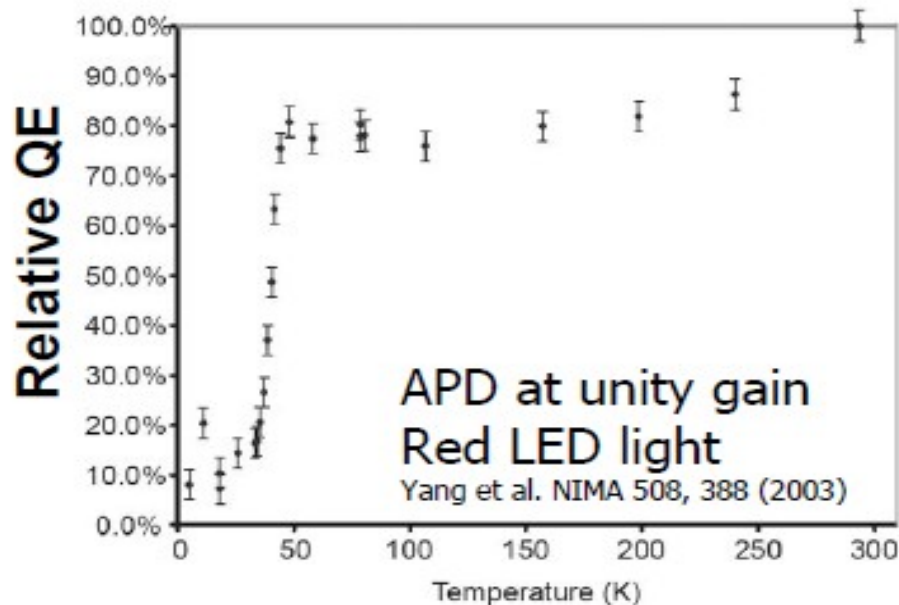
- $P_{01}$  increases at low T because of increased impact ionization
- Optical attenuation length increased (Energy gap increases) at low T
- Depletion region widening in APDs, but not in SiPM which are fully depleted

Similar effect expected also for SiPM

SPAD: Cova et al, Rev.Sci.Instr. 7 (2007)



APD: Johnson et al (RMD) IEEE 2009





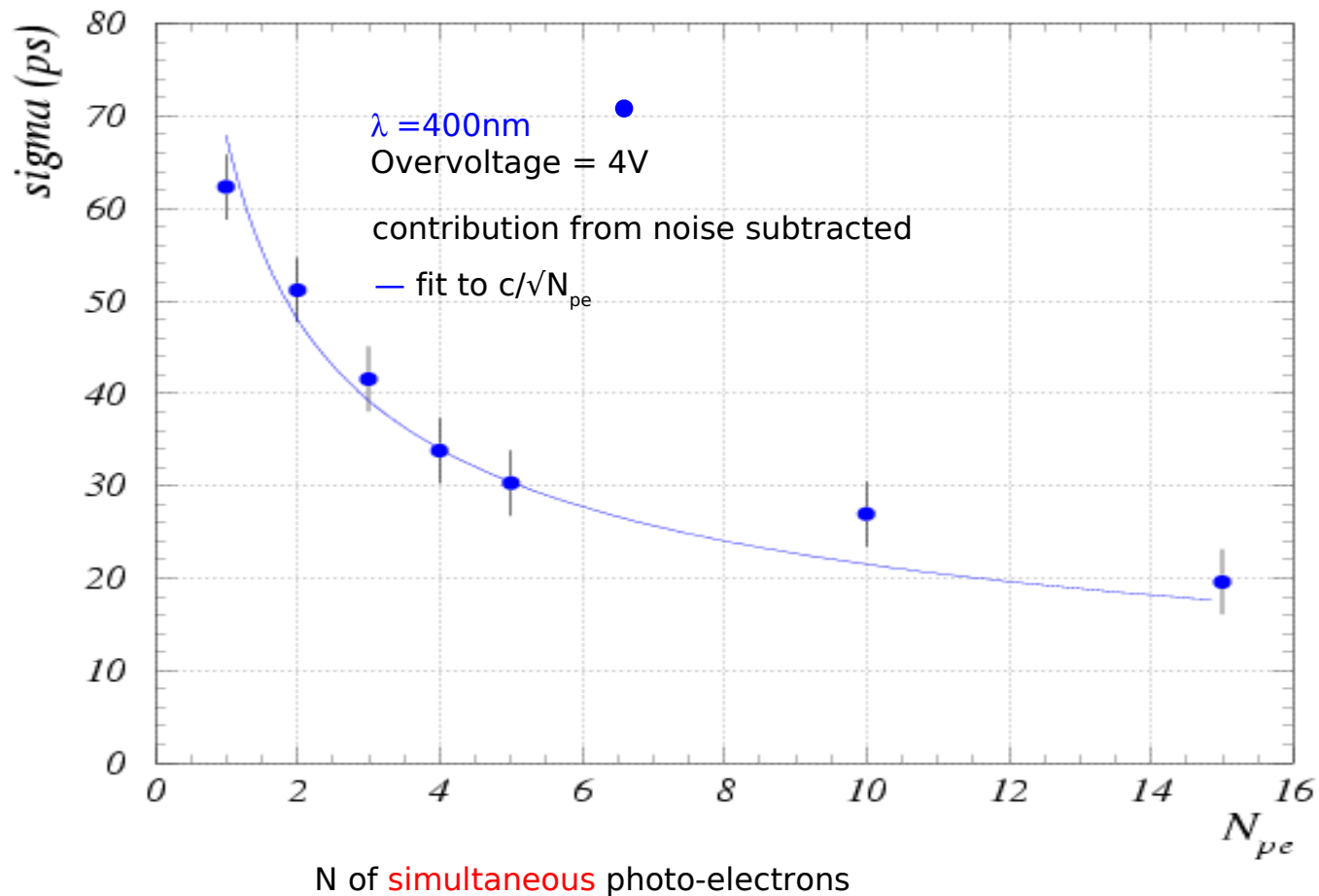
# Timing



# Many photons (simultaneous)

Dependence of SiPM timing on the  
number of simultaneous photons

Poisson statistics:  $\sigma_t \propto 1/\sqrt{N_{pe}}$

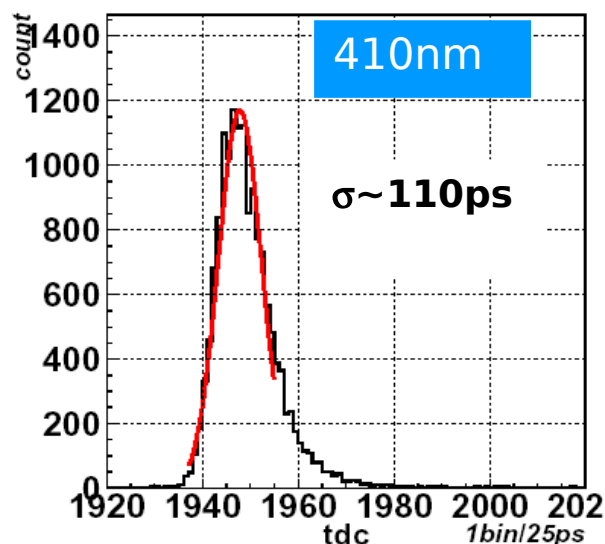
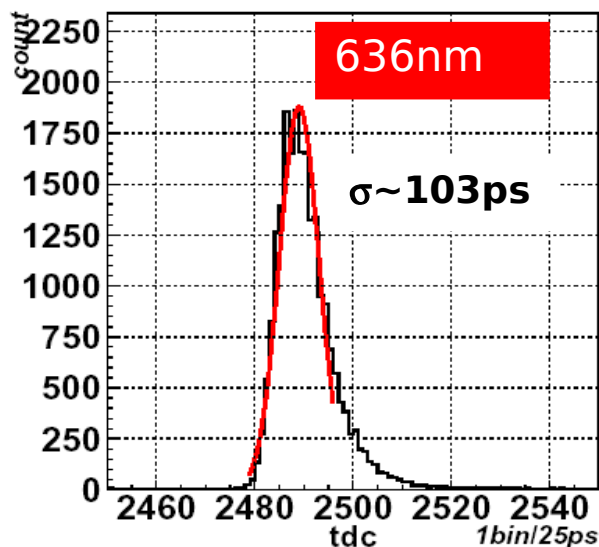


# SPTR: HPK/CPTA comparison

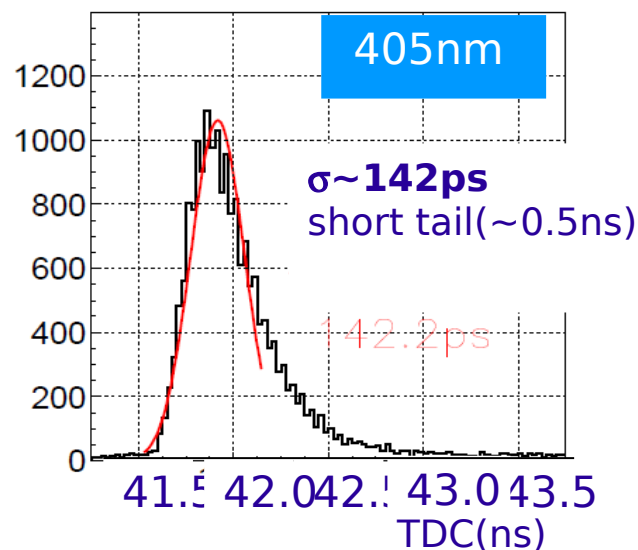
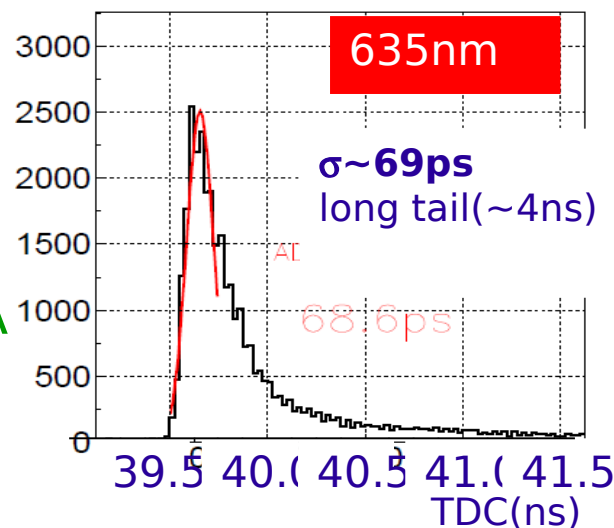
T.Iijima - PD07

Nagoya and Lubiana groups

SiPM - HPK  
(MPPC)



SiPM - CPTA  
(MRS-APD)



Method: CFD + TDC + Time walk corrections

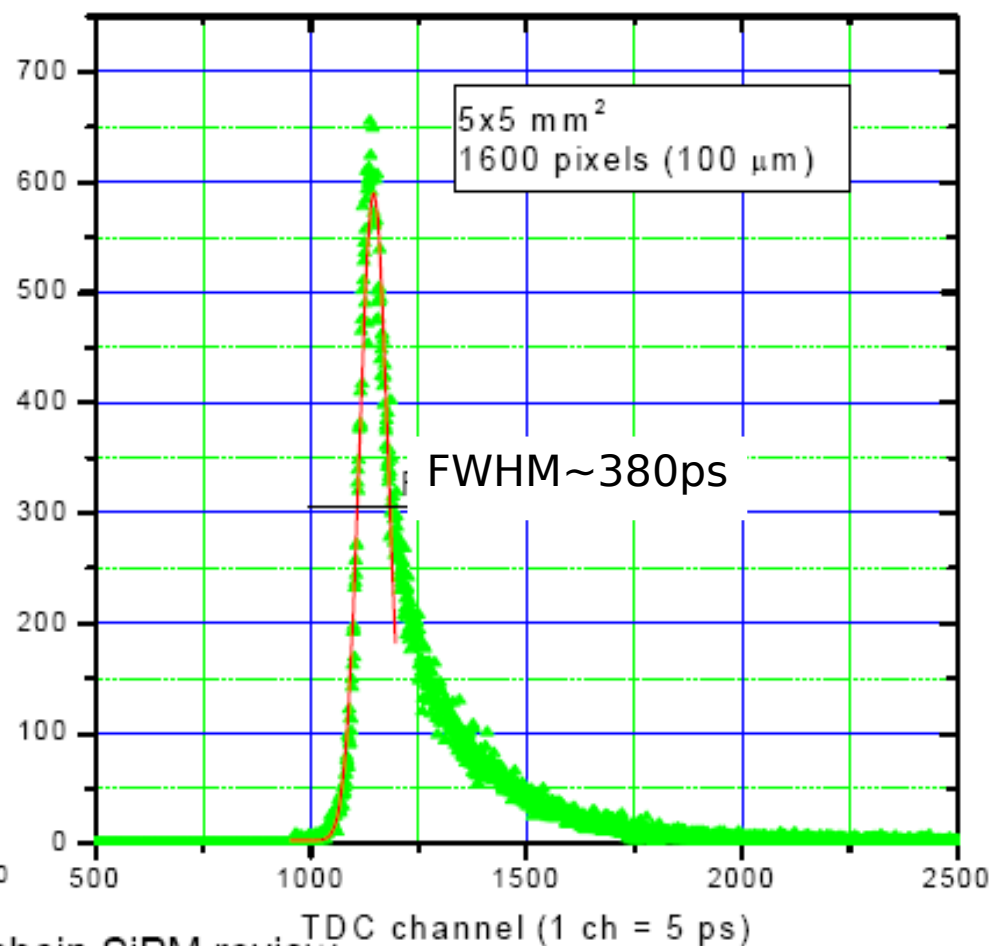
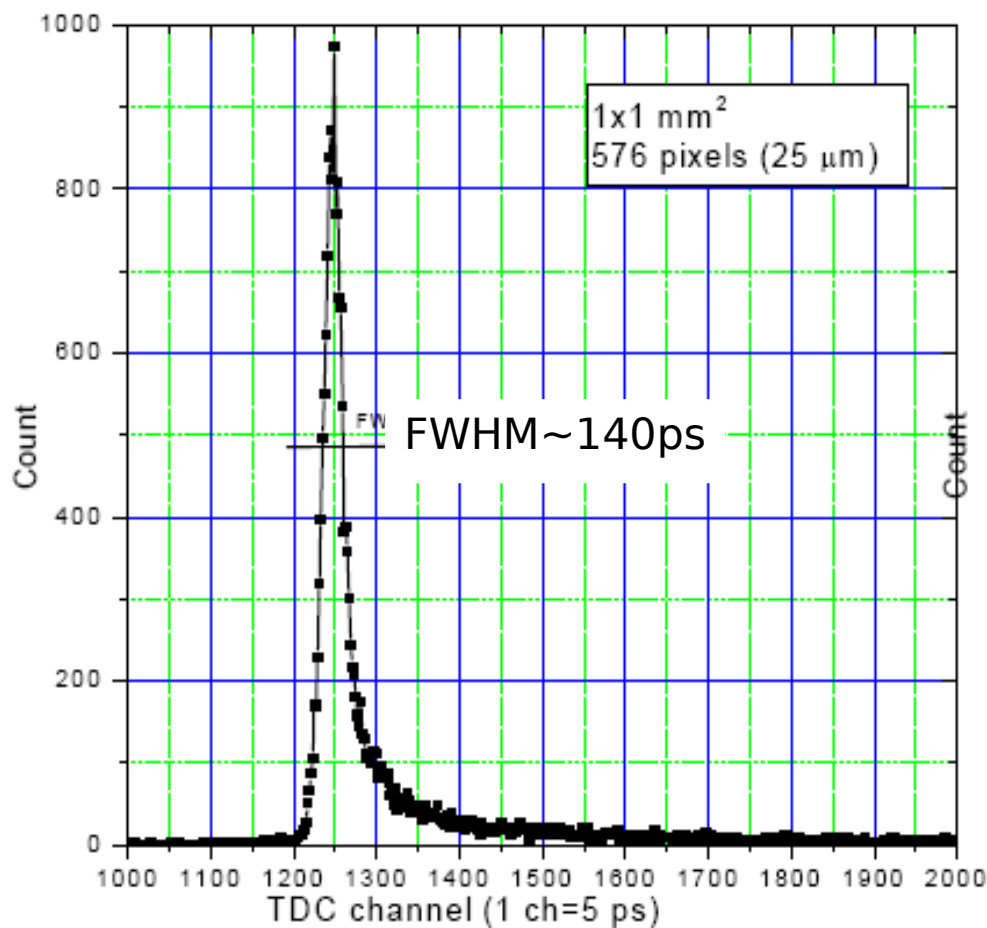
Compatible with DASIPM measurements

# SPTR: cell and sipm size dependence

B.Dolgoshein - LIGHT07

SiPM - MePhi/Pulsar:  
576 cells ( $25 \times 25 \mu\text{m}^2$ )  
Area =  $1 \times 1 \text{ mm}^2$

SiPM - MePhi/Pulsar:  
1600 cells ( $100 \times 100 \mu\text{m}^2$ )  
Area =  $5 \times 5 \text{ mm}^2$



B.Dolgoshein, SiPM review

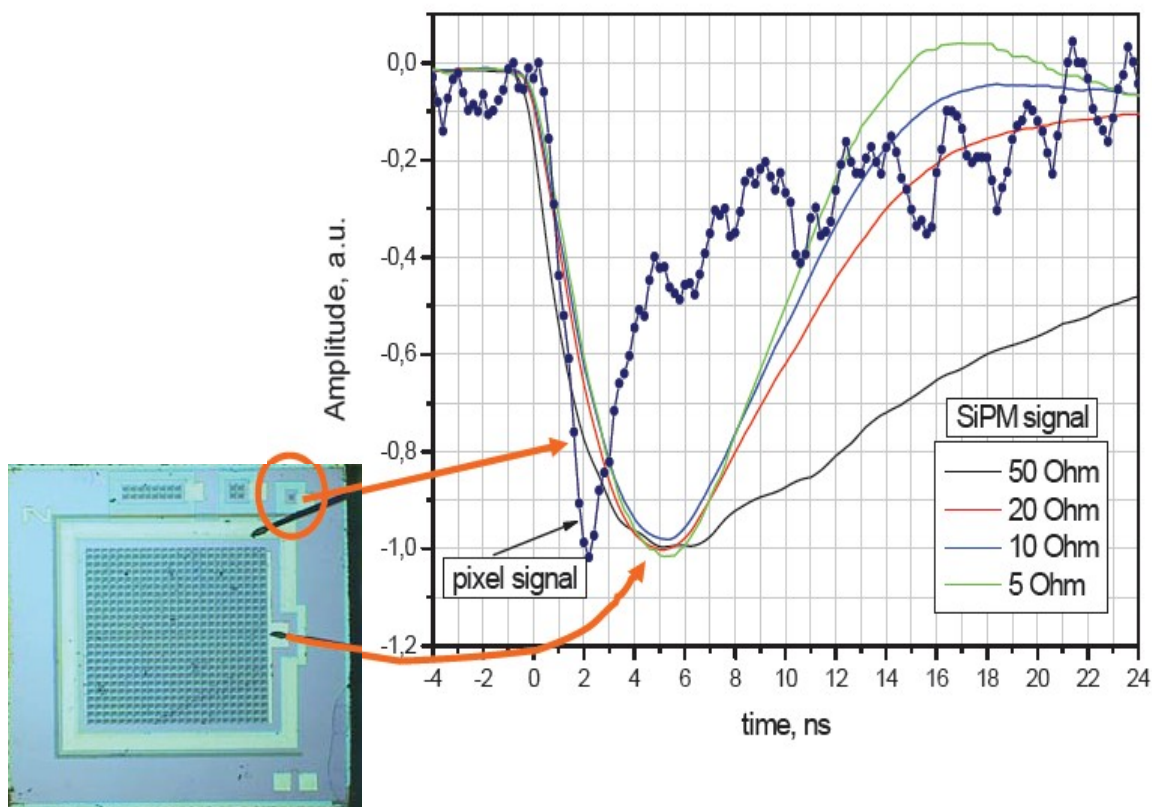
# SiPM signal: effect of $C_{tot}$ and $Z_{load}$

SiPM - MePhi/Pulsar:

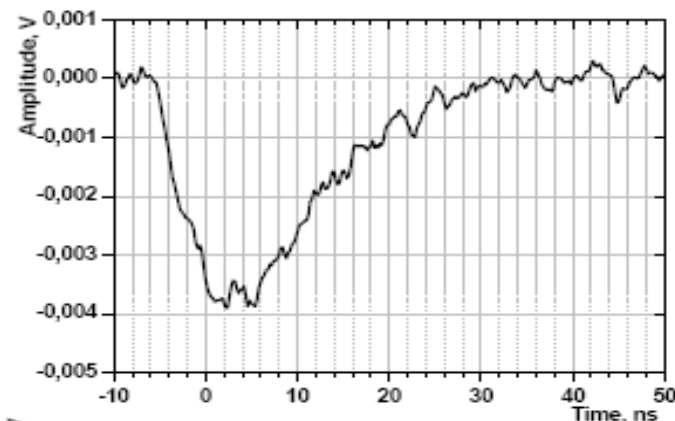
1600 cells ( $100 \times 100 \mu\text{m}^2$ )

Area =  $5 \times 5 \text{ mm}^2$

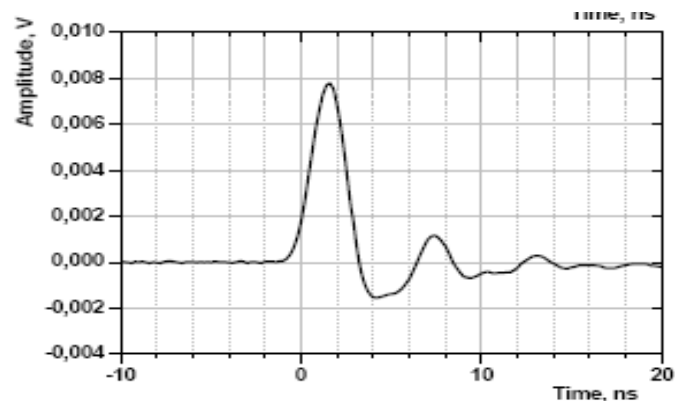
$C_{tot} \sim 160 \text{ pF}$



$Z_{in} \sim 50 \Omega$   
FWHM  $\sim 15 \text{ ns}$



$Z_{in} \sim 7 \Omega$  + shaper  
FWHM  $\sim 2.5 \text{ ns}$



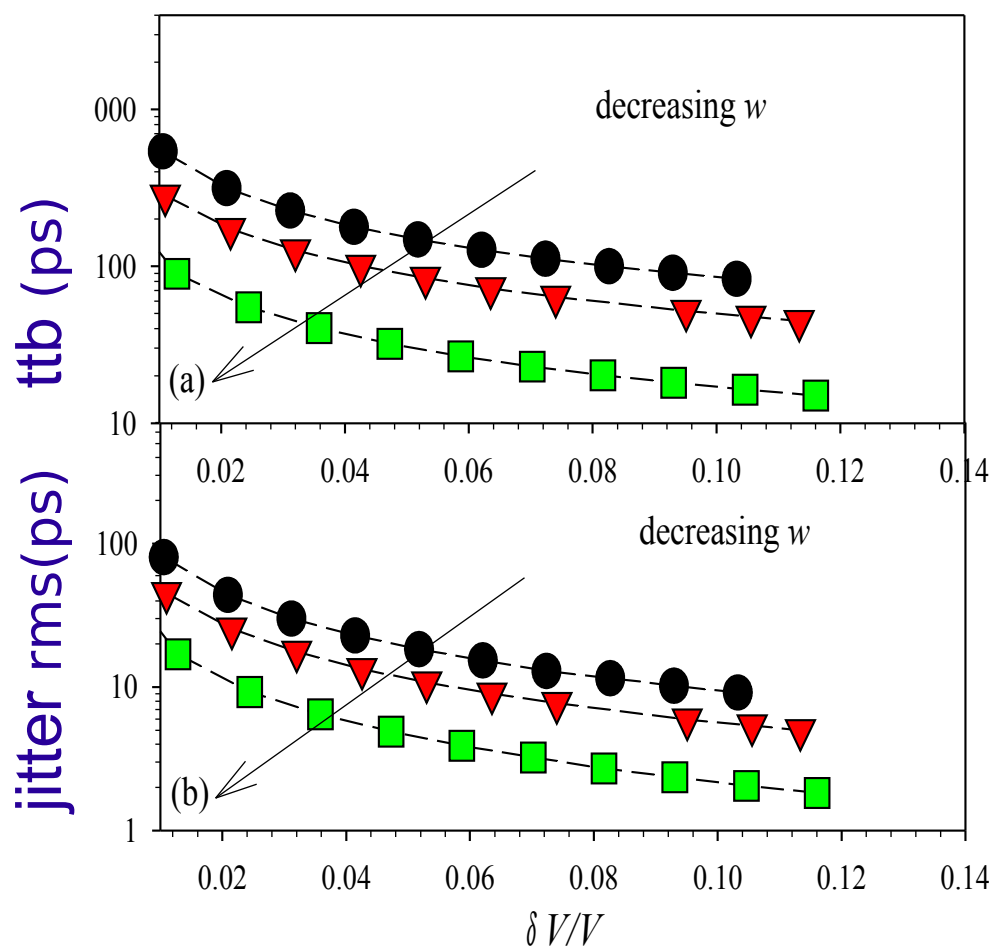
Trans-impedance amplifier

B.Dolgoshein and E.Popova  
LIGHT07

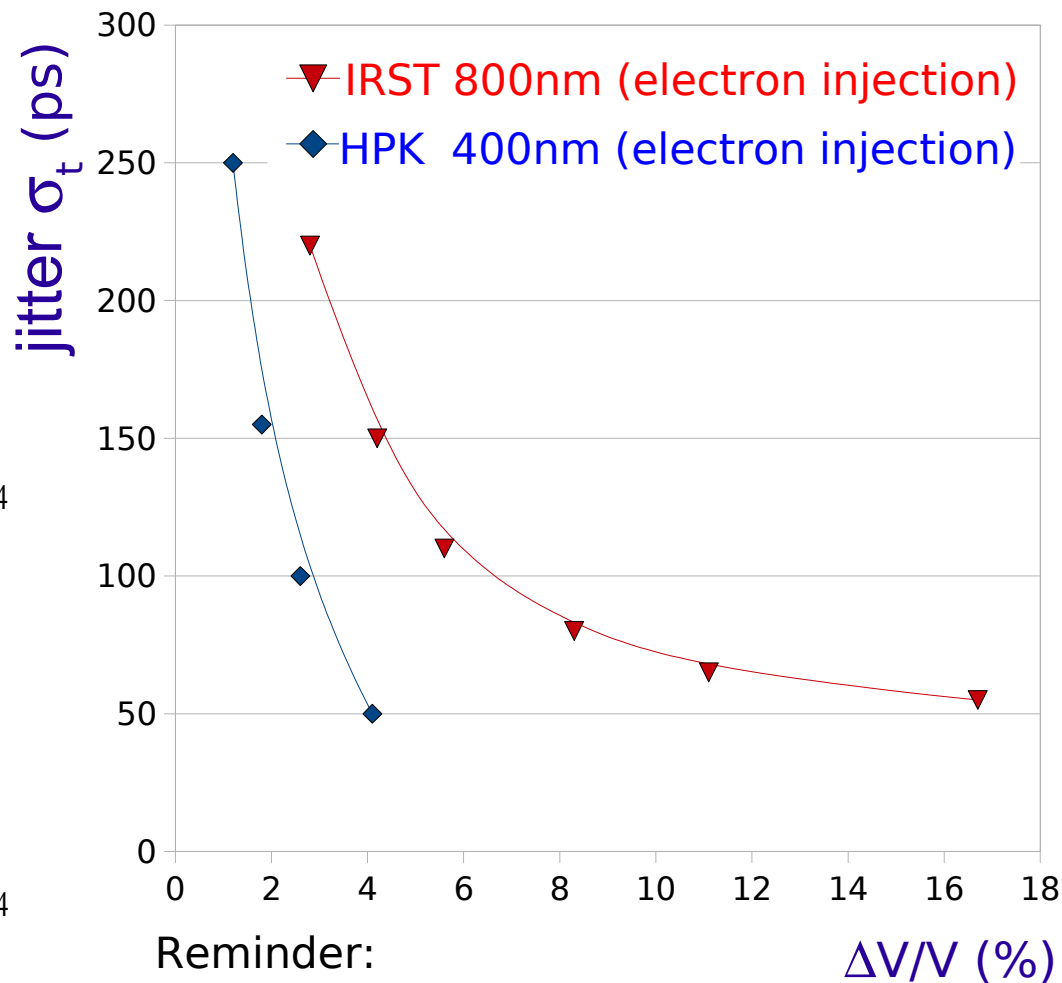
# RPL model vs data: comparison ... not yet

Example of RPL simulation of pure electron injection in Si SPAD

Courtesy of C.H.Tan



DATA  
(DASIPM)



Reminder:

IRST structure is n on p

HPK structure is p on n

# PDE



# Photo-detection efficiency (PDE)

$$PDE = N_{\text{pulses}} / N_{\text{photons}} = QE \cdot P_{01} \cdot \epsilon_{\text{geom}}$$

## Carrier Photo-generation

(QE = probability for a photon to generate a carrier that reaches the high field region)

\*

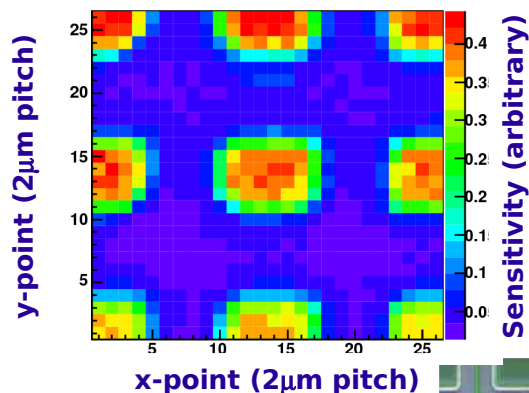
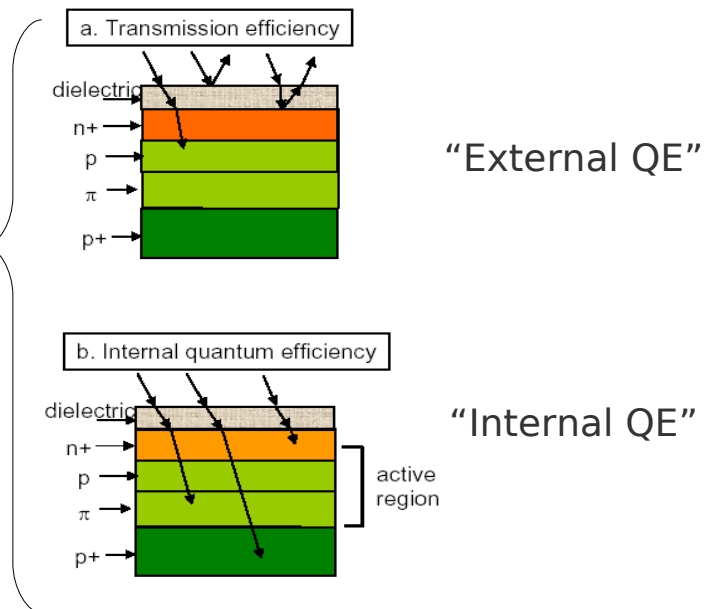
## Avalanche triggering

( $P_{01}$  = probability for a carrier traversing the high-field to generate the avalanche)

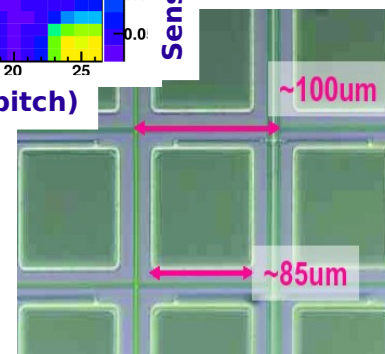
\*

## Geometrical fill factor

( $\epsilon$  = fraction of dead area due to structures between the cells, eg. guard rings, trenches)



Hamamatsu SiPM close up



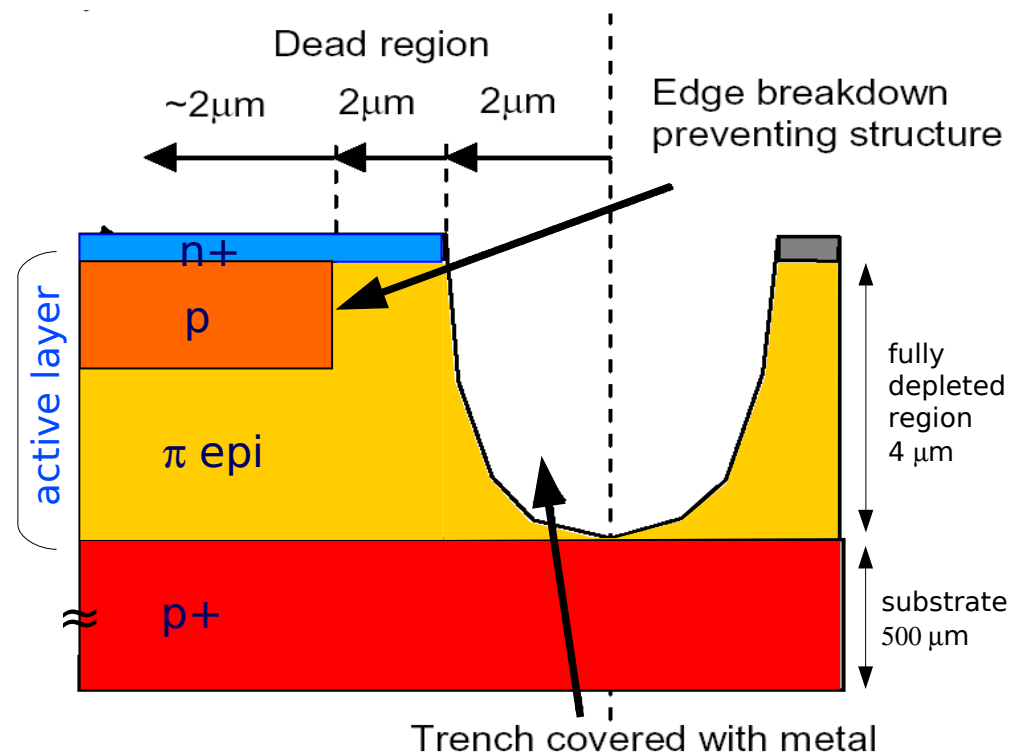
# QE: Efficiency of a single cell

Two factors in QE:

- (1) transmittance of the entrance window (dielectric on top of silicon surface)
- (2) probability of a photon inside to generate a e-h pair in the active layer (internal quantum efficiency)

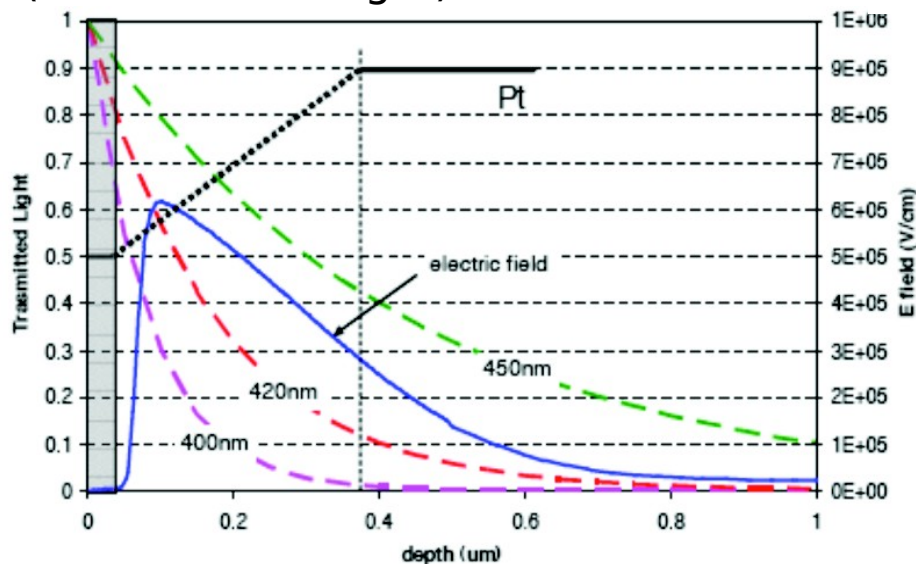
Only the depleted region is fully active to efficiently photo-generate because of high recombination probability in the un-depleted regions.

Only a small layer ( $\lambda_{\text{diffusion}} \sim \sqrt{D\tau_{\text{recomb}}}$ ) at the edge of un-depleted regions contributes to the photo-generation (critical for UV light)



## QE optimization

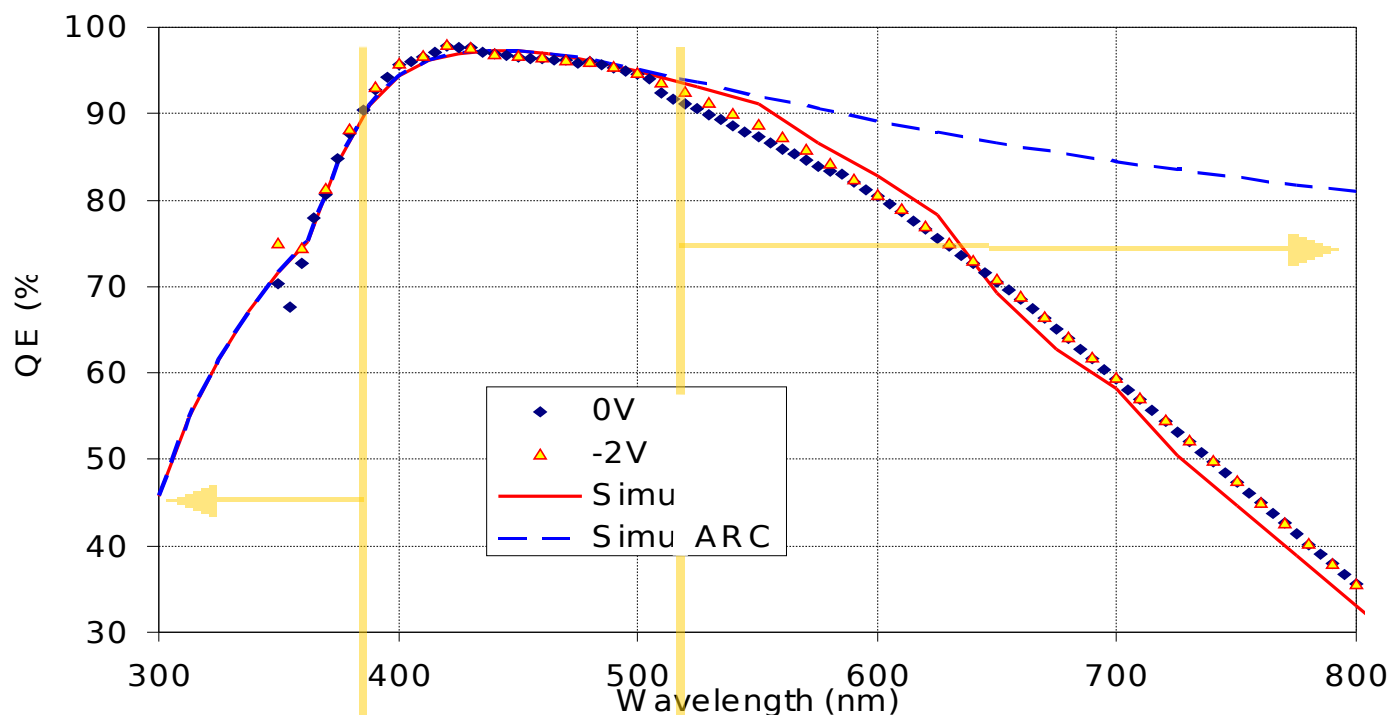
- Anti-reflective coating (ARC)
- Shallow junctions for short  $\lambda$
- Thick epi layers for long  $\lambda$



# QE: Efficiency of a single cell

Direct access to **internal QE** and **transmittance through ARC** by measuring photo-voltaic regime ( $V_{\text{bias}} \sim 0 \text{ V}$ )

the photon detection efficiency of a diode with the same  $n^+/p$  junction structure and same ARC

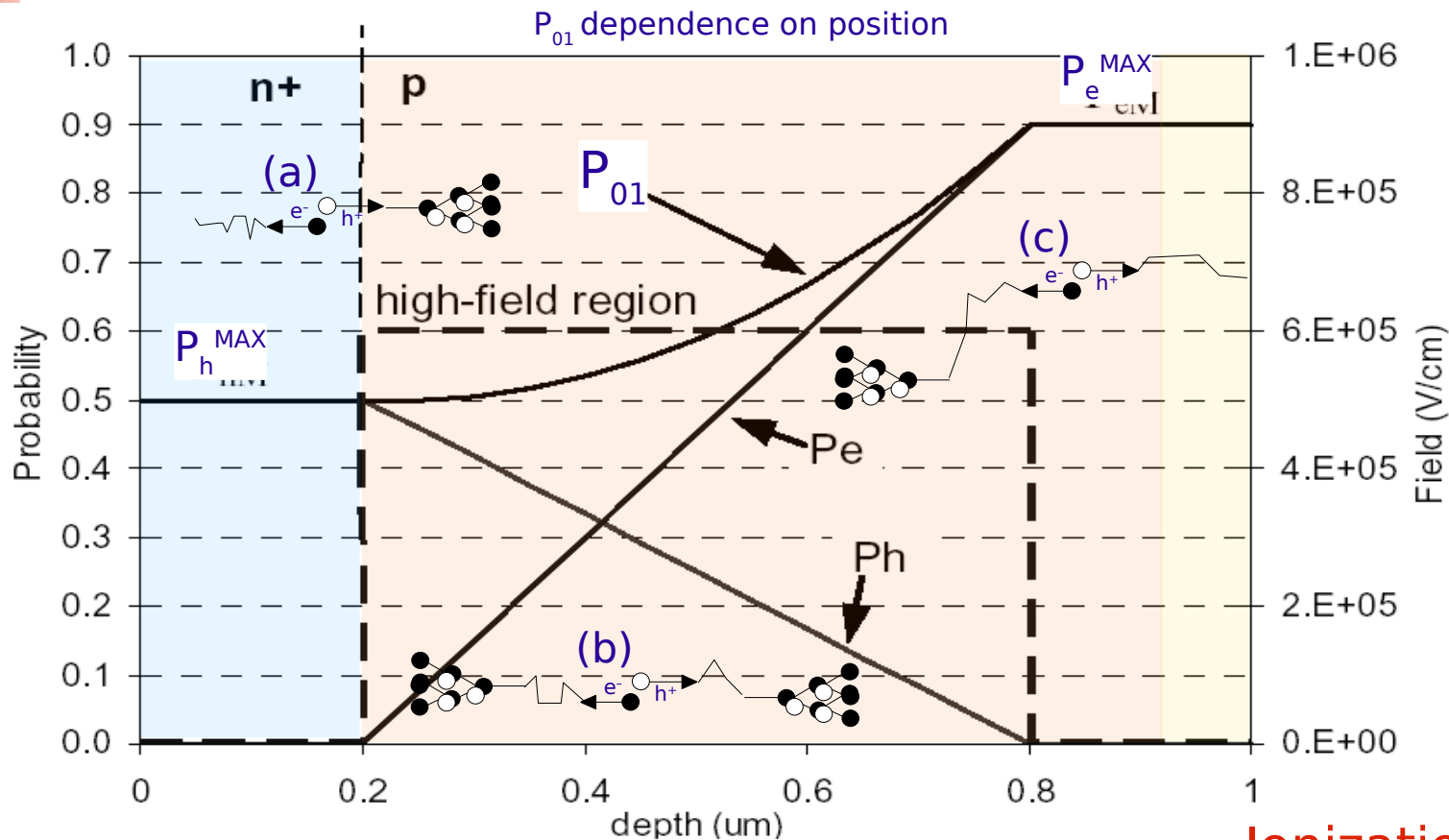


Reduced by  
ARC Transmittance

Reduced by the  
small  $\pi$  layer thickness

# Avalanche trigger probability ( $P_{01}$ )

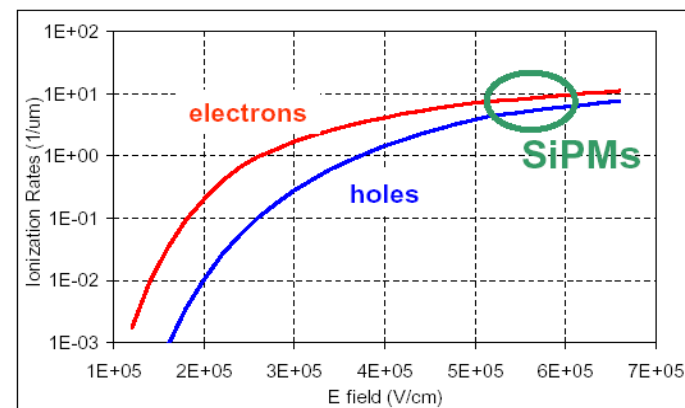
C.Piemonte  
NIM A 568  
(2006) 224



- Example with constant high-field:
- (a) only holes may trigger the avalanche
  - (b) both electrons and holes may trigger (but in a fraction of the high-field region)
  - (c) only electrons may trigger

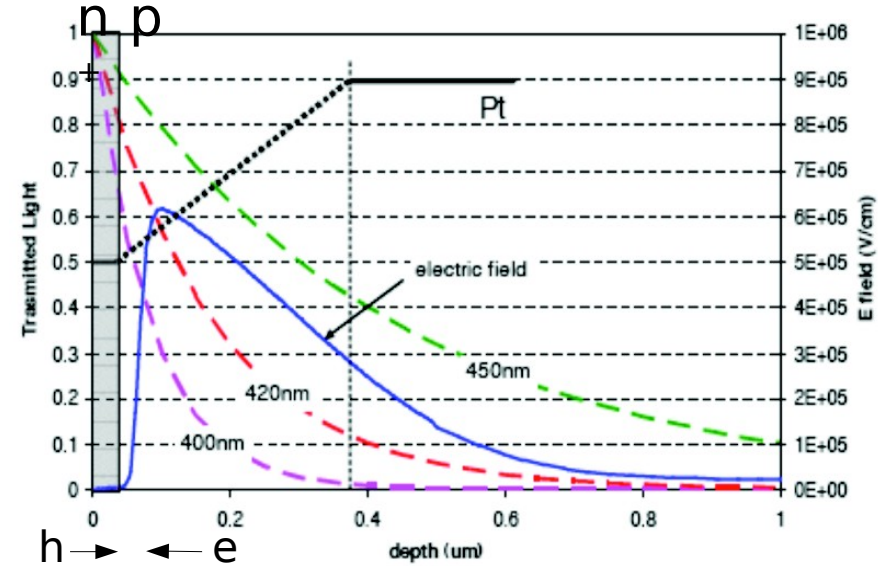
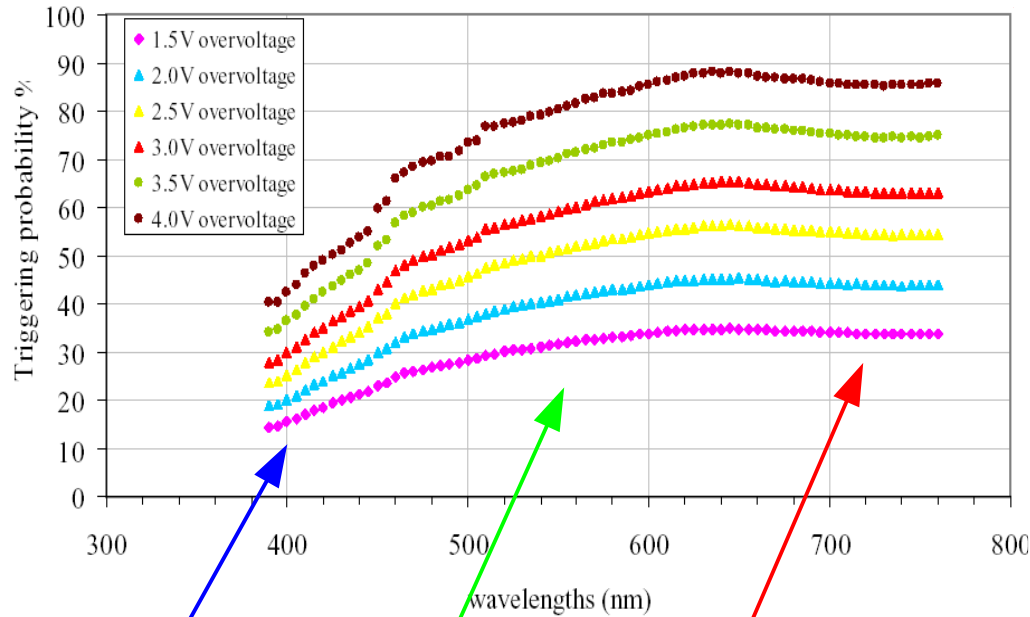
- high over-voltage
  - photo-generation in the p-side of the junction
- $P_{01}$  optimization ←

## Ionization rate in Silicon



# Avalanche trigger probability ( $P_{01}$ )

$$P_{01} = \text{PDE} / \text{QE} / \epsilon_{\text{geom.}}$$



Only  $e^-$  cross the high E field region and trigger the avalanche

Both  $h^+$  and  $e^-$  might trigger the avalanche (but cross only a fraction of high field region)

Only  $h^+$  cross the high E field trigger the avalanche

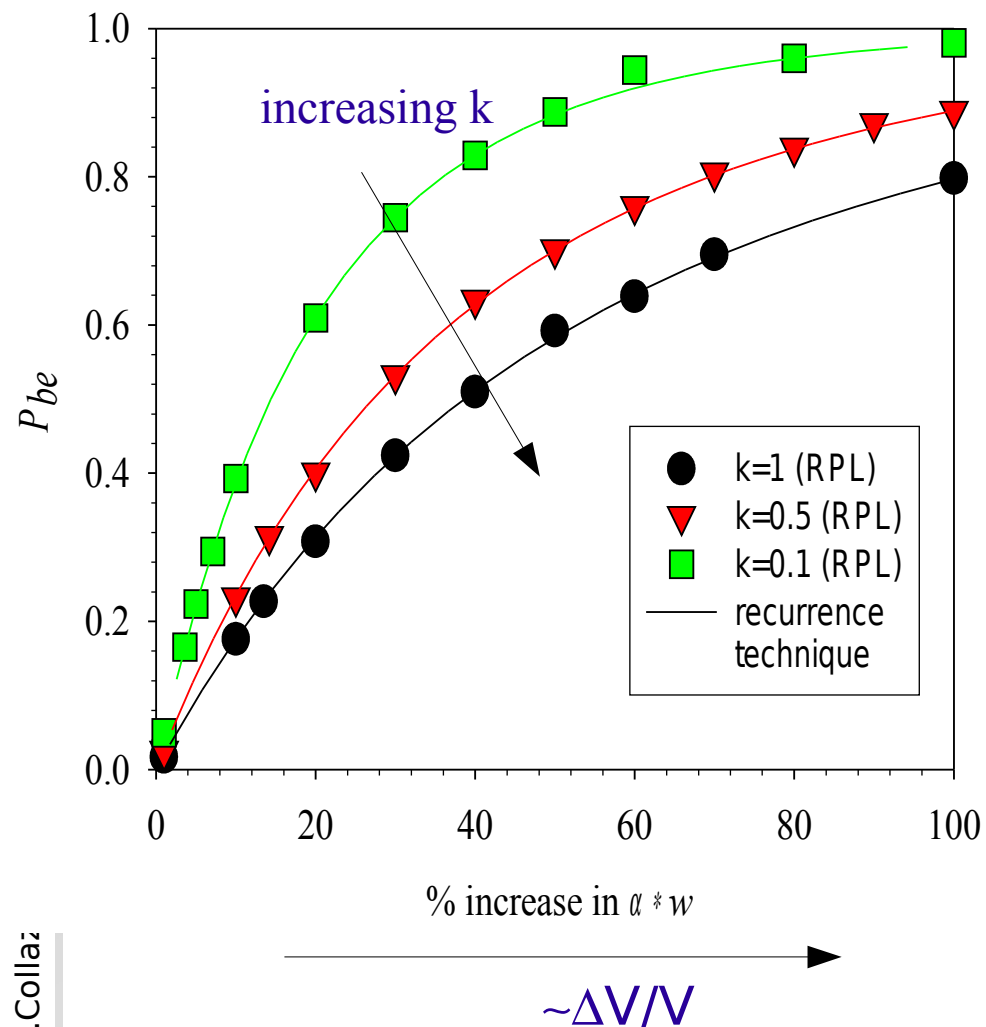
# PDE vs $\Delta V$

“Statistics of Avalanche Current Buildup Time in Single-Photon Avalanche diodes”

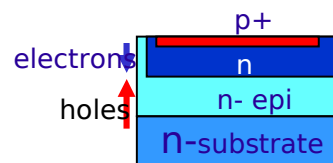
C.H.Tan, J.S.Ng, G.J.Rees, J.P.R.David (Sheffield U.)

IEEE J.Quantum Electronics 13 (4) (2007) 906

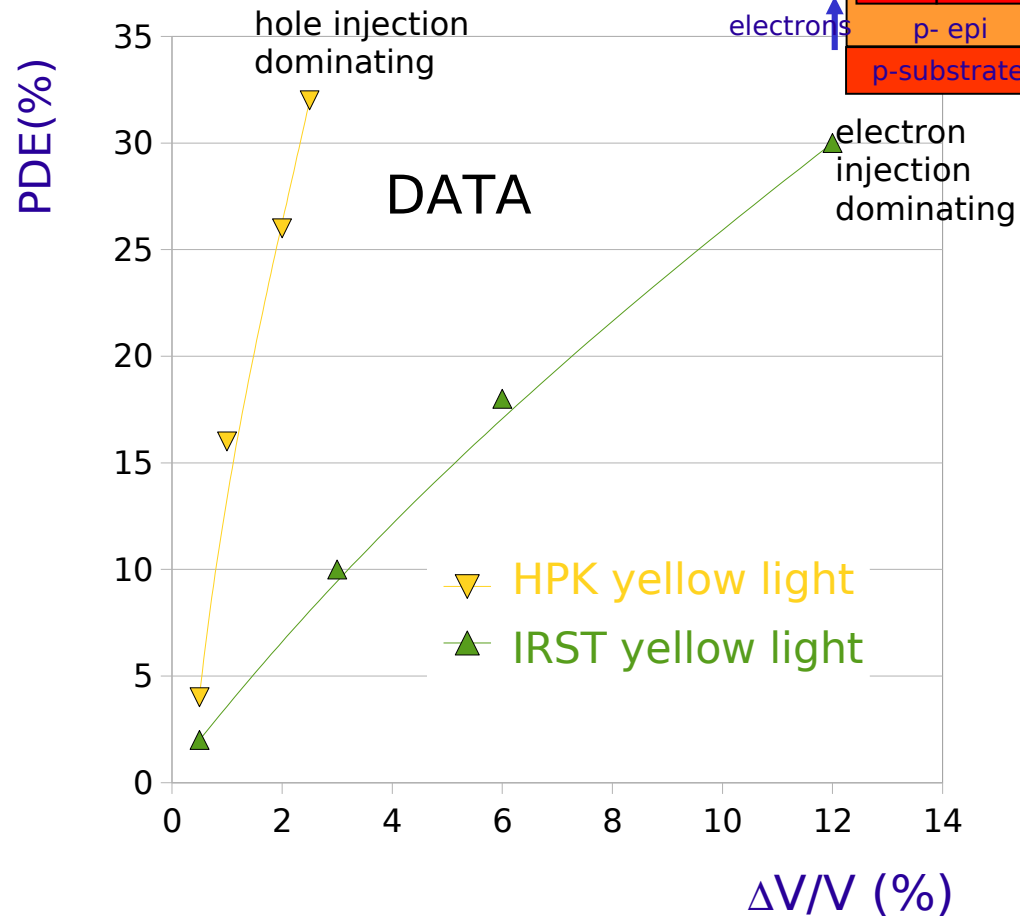
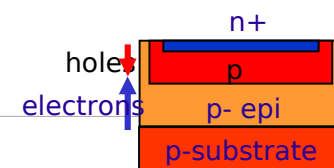
RPL model Courtesy of C.H.Tan



p-on-n structure



n-on-p structure





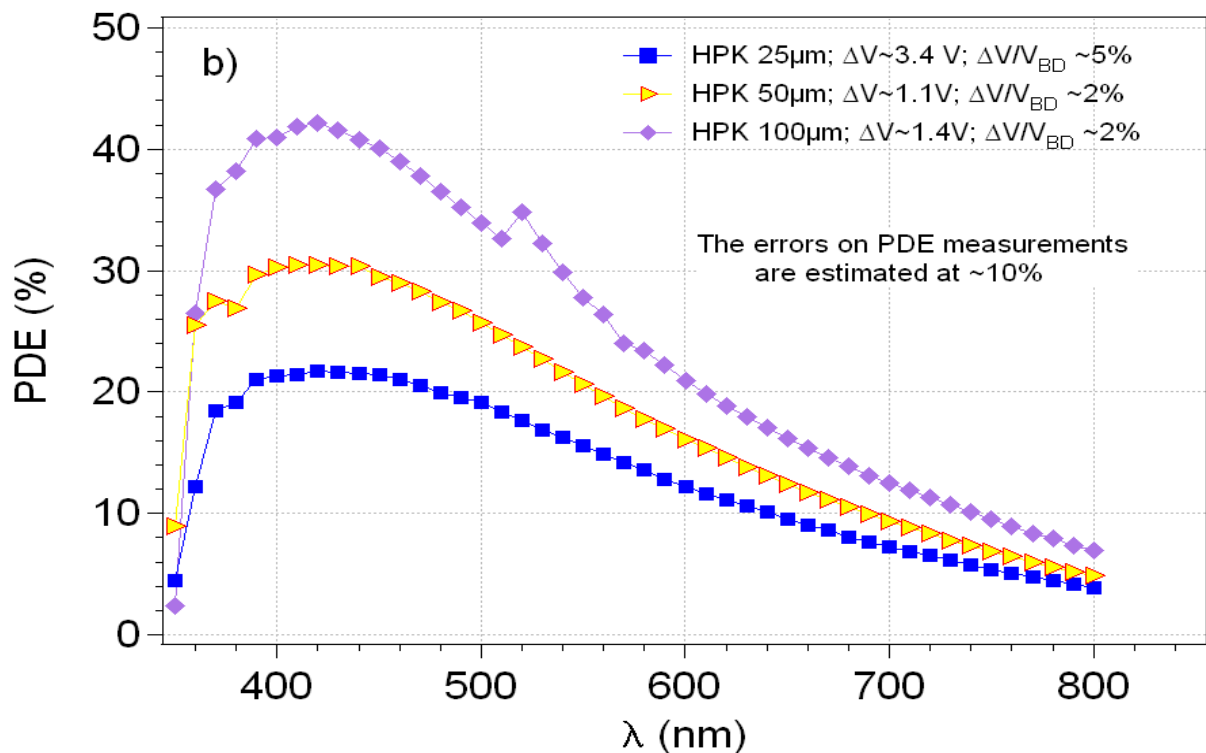
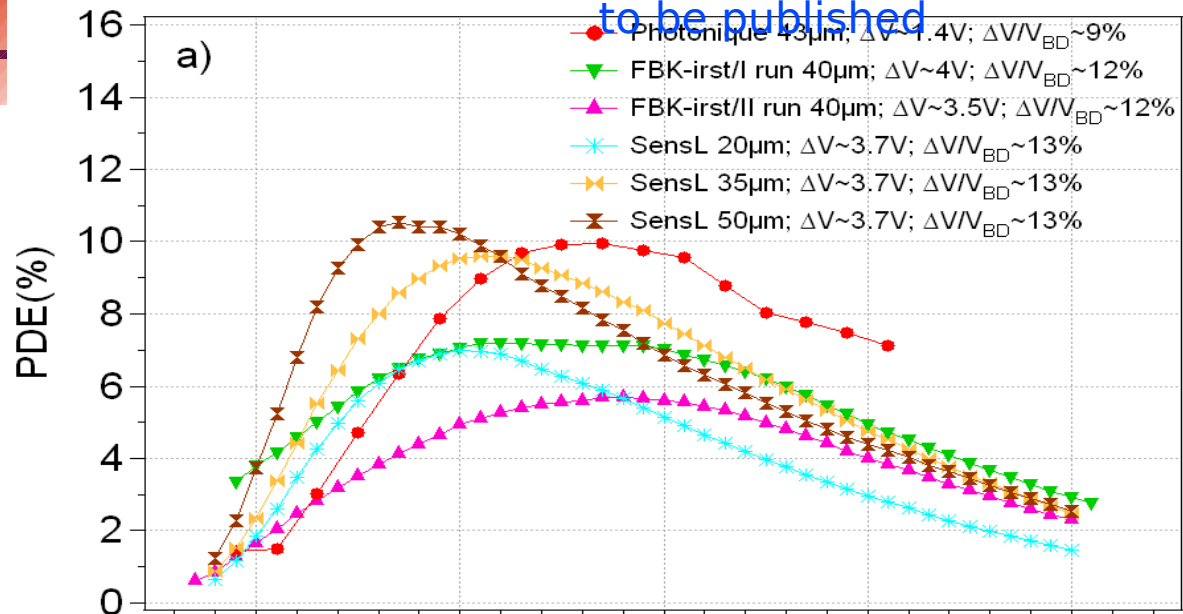
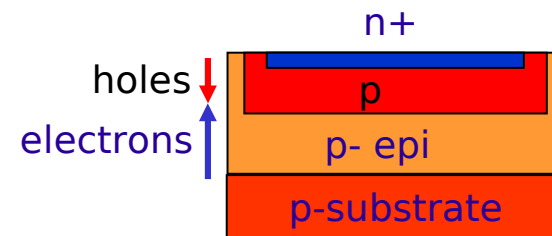
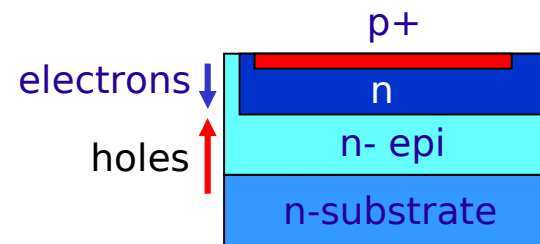


Fig. 5a) The PDE vs.  $\lambda$  of the Photonique, FBK-irst and SensL devices and b) HPK

### n-on-p structures



### p-on-n structure



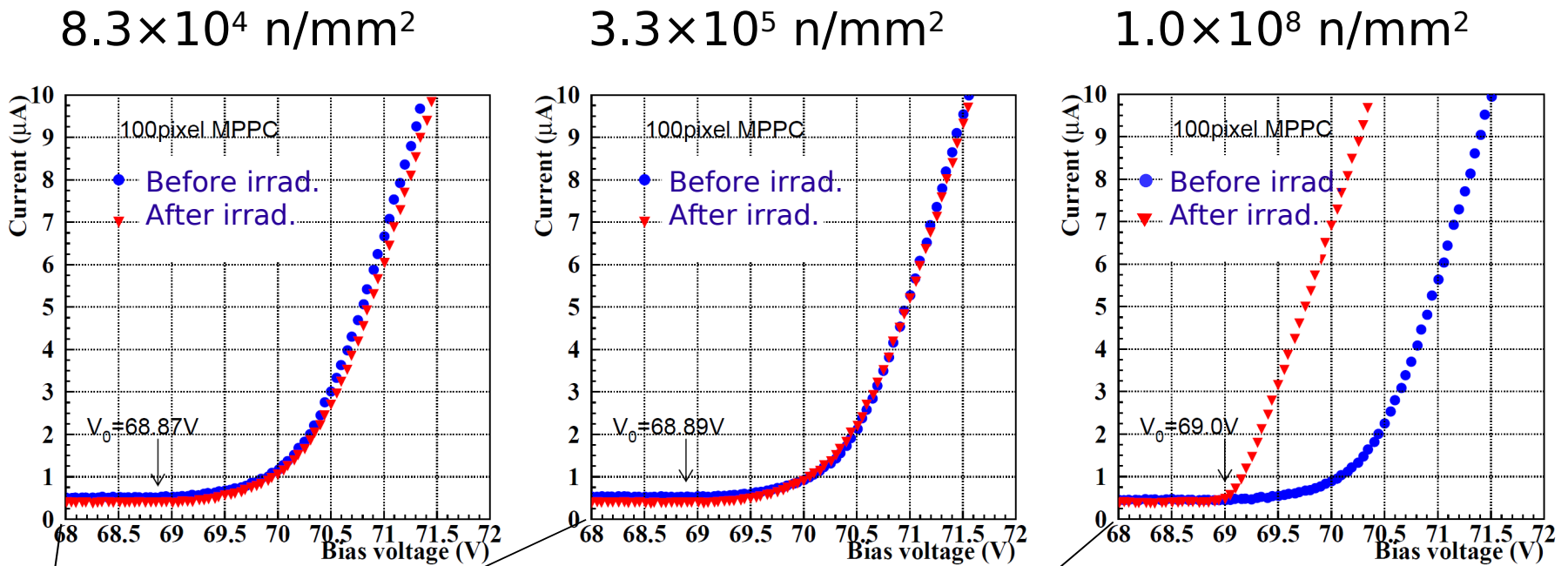
Note:

- 1) geometrical fill factor included
- 2) PDE in HPK catalog is 20%-30% more than the real PDE due to after-pulses and cross-talk

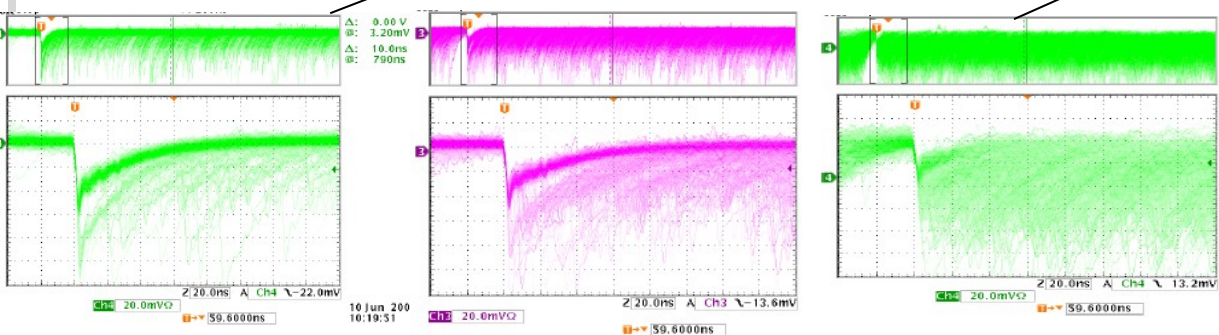
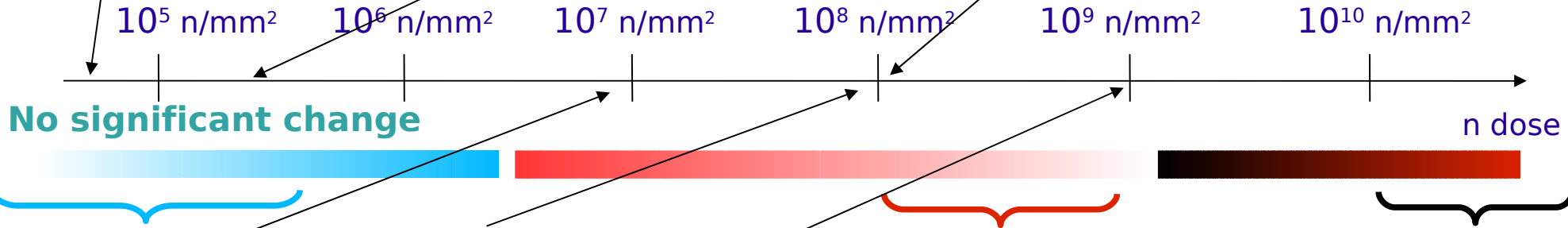


# Radiation Hardness

# Radiation damage: neutrons (0.1 -1 MeV)



T. Matsumura - PD07



I-V drastically change. No signal  
 Signal pulse is still there,  
 but continuous pulse height.  
 (No photon-counting capability)

Nakamura at NDIP08